

Determination of Plasma Temperature, Density, and Uniformity in Iron Opacity Experiments at Conditions Approaching the Base of the Solar Convection Zone

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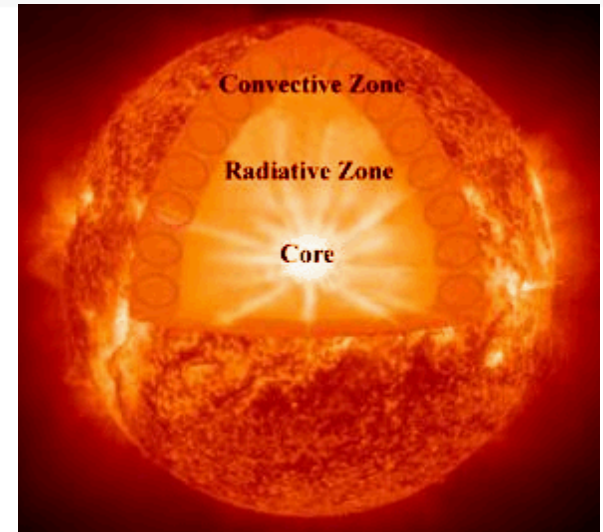
²*University of Nevada, Reno, Nevada 89557, USA*

³*Prism Computational Sciences, Madison, Wisconsin 53703, USA*



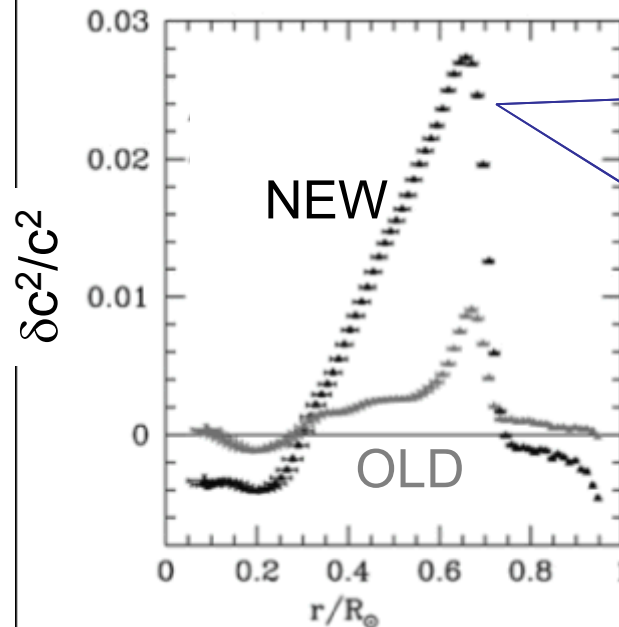
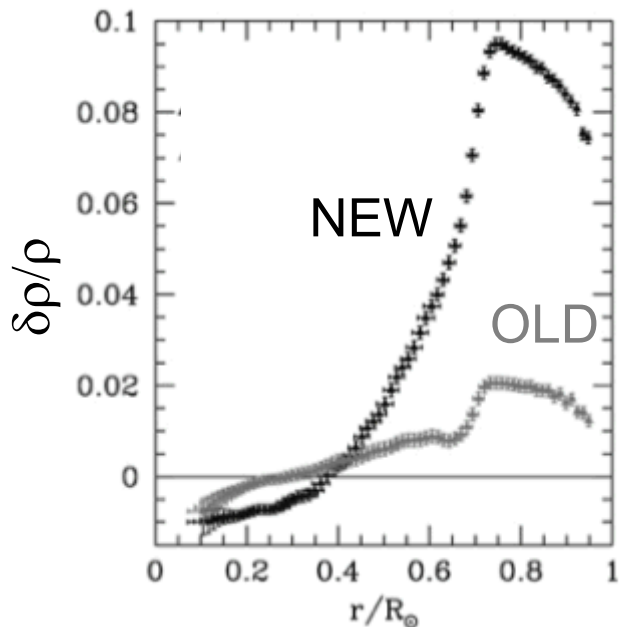
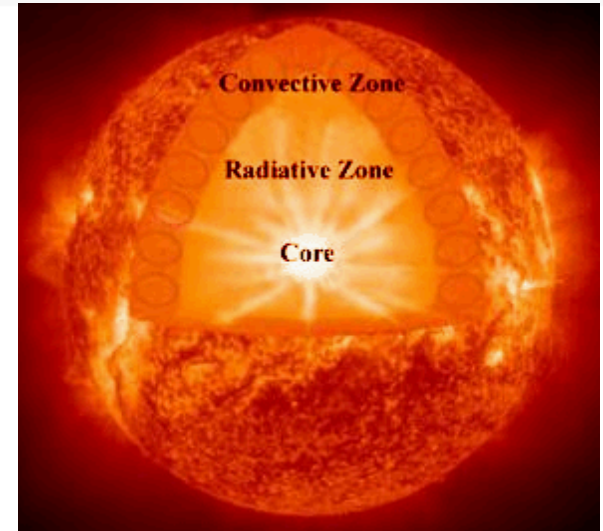
Two ways to study the solar structure

- Standard solar model (simulation)
 - Hydrostatic model
 - Inputs
 - Abundance
 - Nuclear reaction rate
 - Opacity
 - Diffusion rate
 - EOS
- Helioseismology (measurements)
 - Seismic study of acoustic pressure oscillation
 - From space-resolved solar pulsation



After solar abundance revision, simulation disagrees measurements

- In 2005, Asplund improved solar abundance by including
 - NLTE effects
 - 3D convection effects
- Reduces abundances of metals (=elements heavier than He)

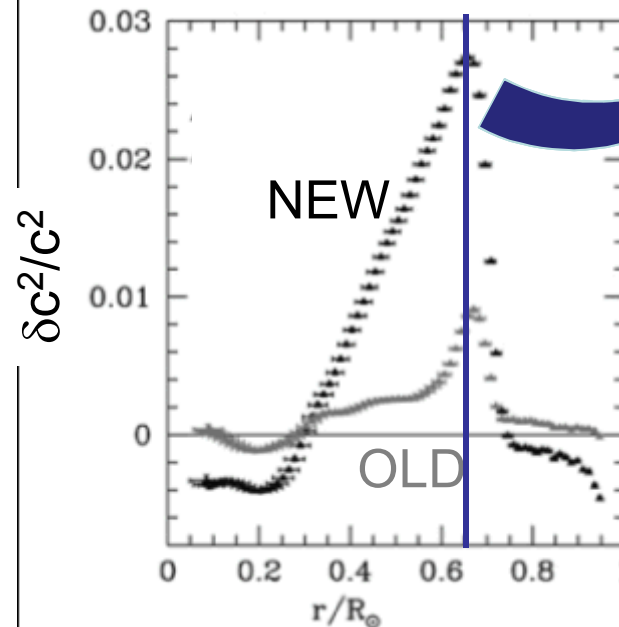
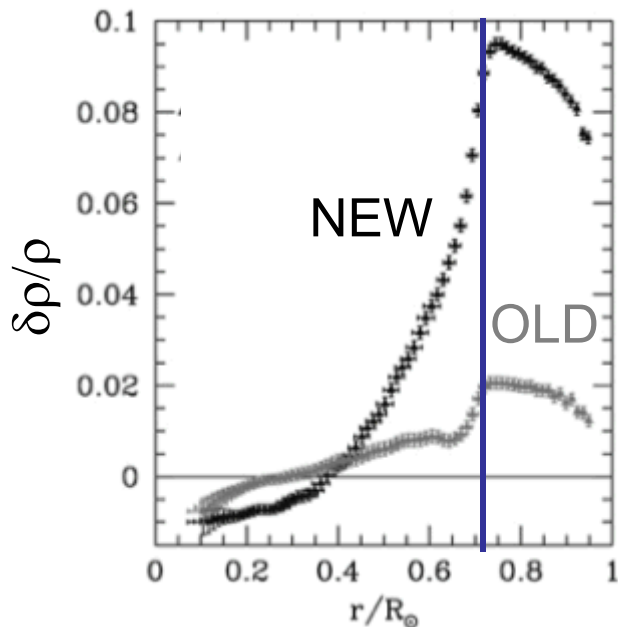
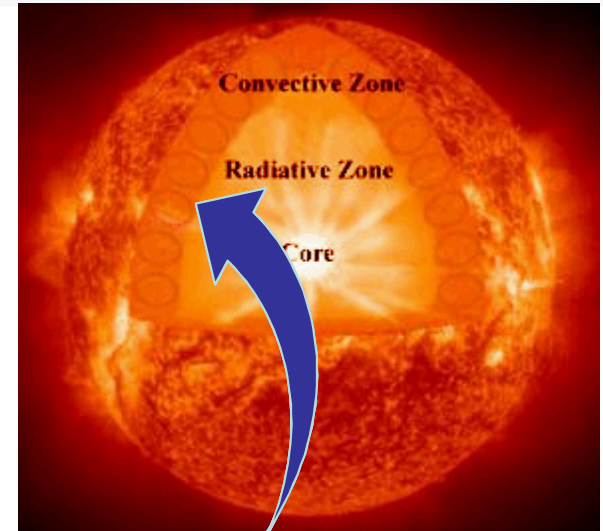


New abundance increases the discrepancies w/ Helioseismology



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Discrepancy in convection zone (CZ) base location became larger too !!



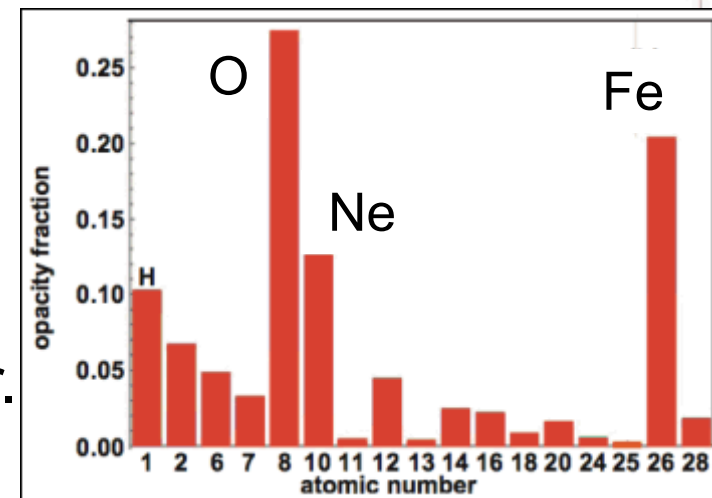
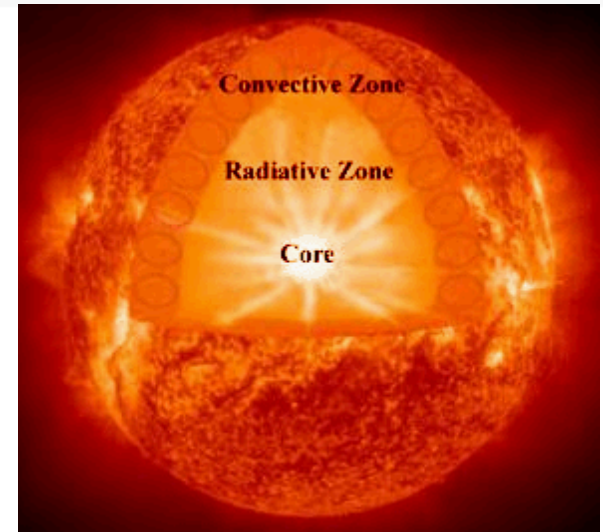
New model does not have enough opacity around CZ base

“The base of the convection zone occurs at a point where opacity is just small enough to allow the entire heat flux to be transported by radiation.”
(Basu Phys. Rep. 2008)

What happens when heavy element abundance is lowered?

- Total opacity decreased
- CZ base location moves outward

Maybe input opacity should be higher.
Fe opacity is most likely suspect.



Opacity is important input for HED plasma simulation

- Opacity = determines how energy is transferred by radiation
- Applications
 - Standard solar model
 - Inertial confinement fusion
 - Z-pinch



Opacity is difficult

- Theory becomes difficult when
 - Atomic number (Z) increases
 - # of bound electrons increase
 - Measurement becomes difficult at high T
 - Self-emission becomes stronger
- ➔ Modeled opacity is challenging but used without being benchmarked for
- mid-/high-Z (Fe: 26)
 - Large # of bound electrons (Fe at CZB: ~9-10)
 - High temperature (Fe at CZB: ~190 eV)

Let's benchmark modeled Fe opacity at CZB condition ($T_e=190$ eV, $n_e=1 \times 10^{23} \text{cm}^{-3}$)



Three requirements for reliable opacity experiments

- Steps

- Make Fe plasma to uniform conditions to CZB
- Provide a backlighter to transmission
- Compute the Fe opacity and compare with data → need to know the exact condition

A little animation to show how each step is done helps

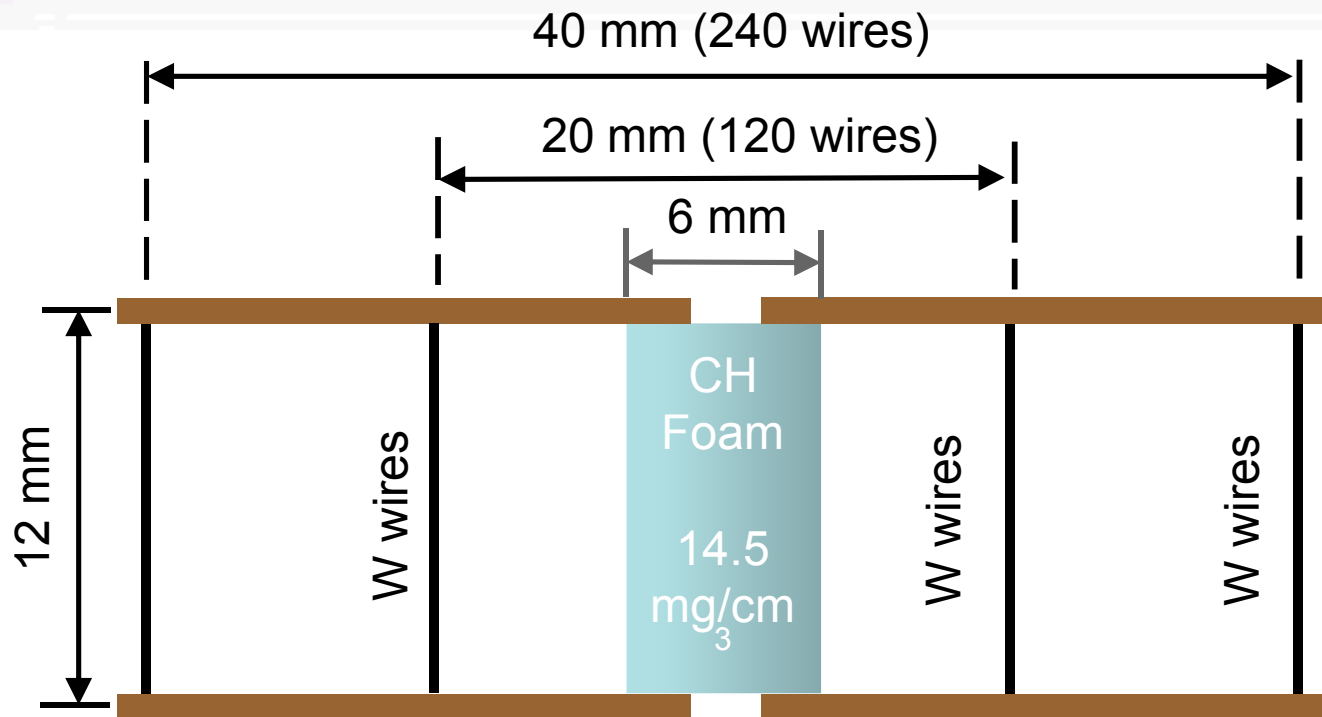
- Requirements

1. Strong and smooth backlighter
2. Sample uniformity
3. Independent T_e and n_e measurement

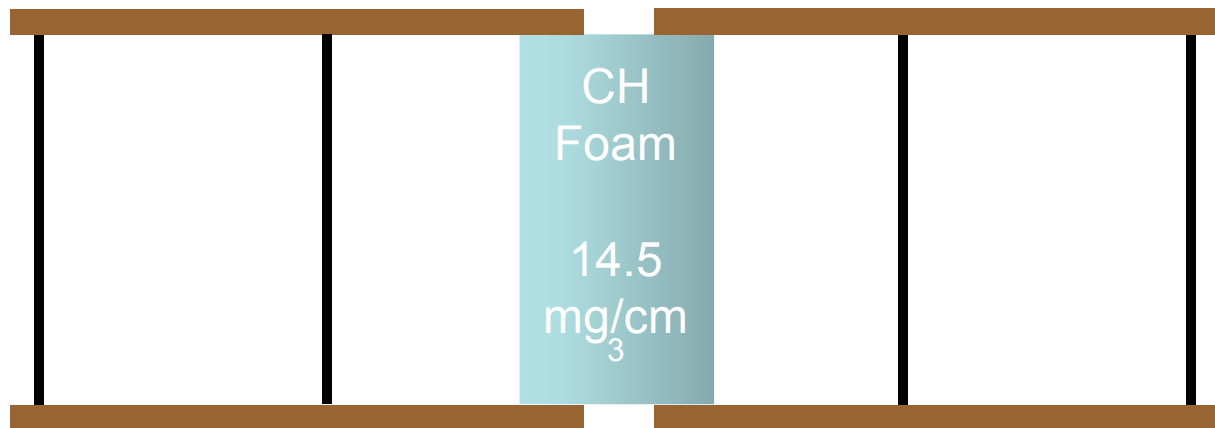
Z-pinch dynamic hohlraum satisfies these



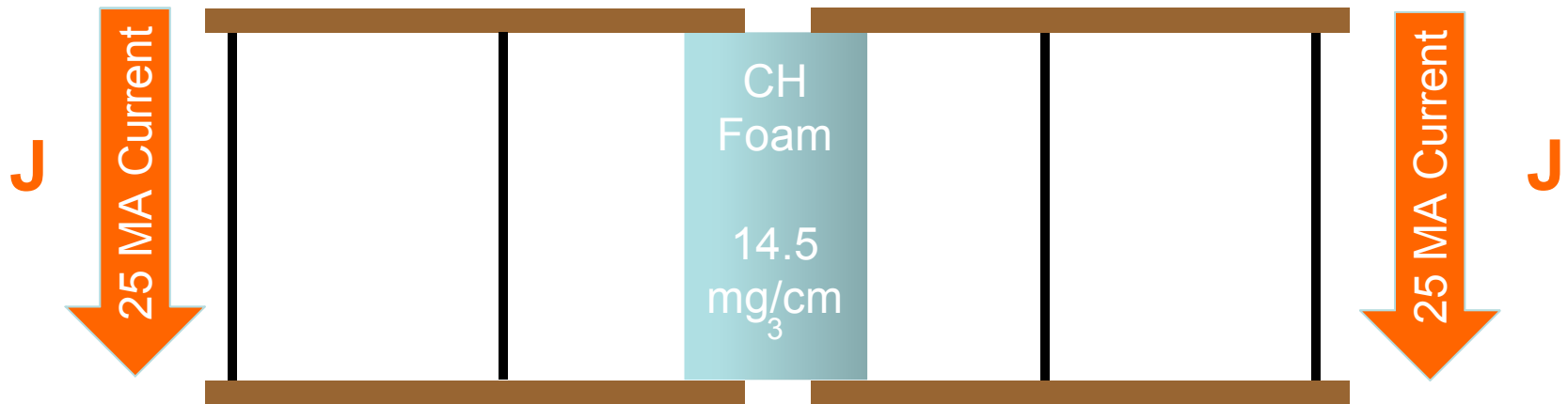
Z Pinch Dynamic Hohlraum



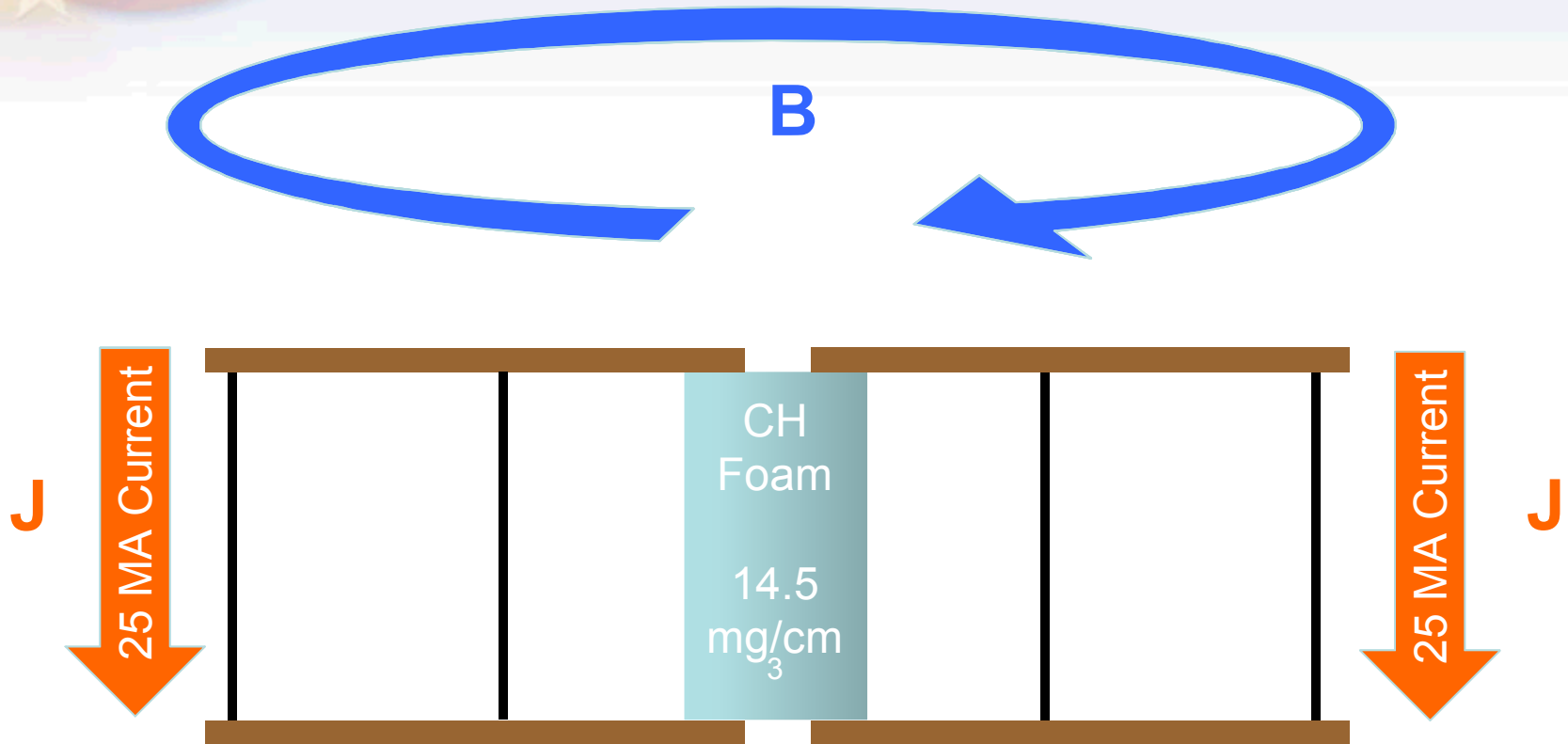
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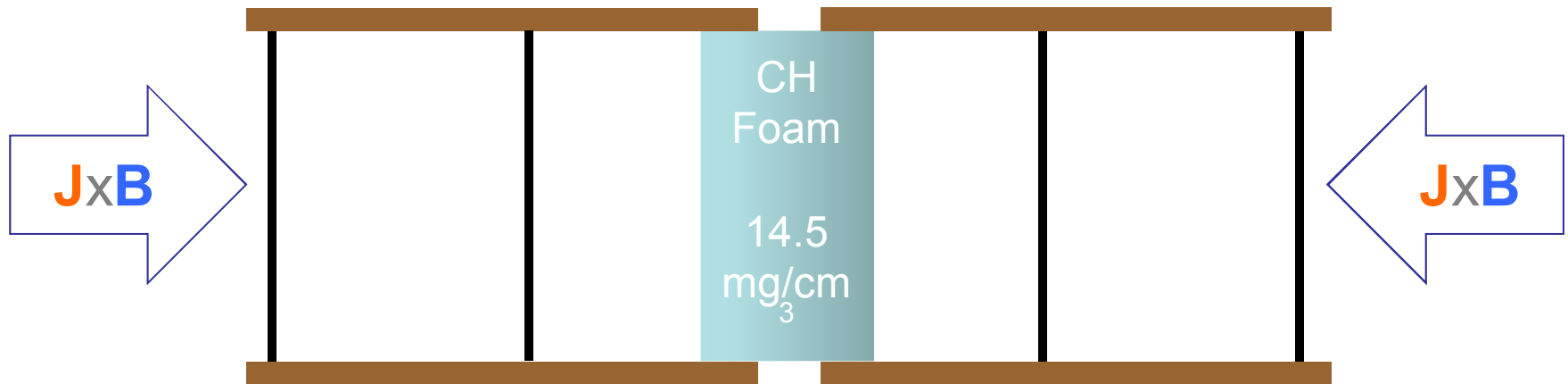
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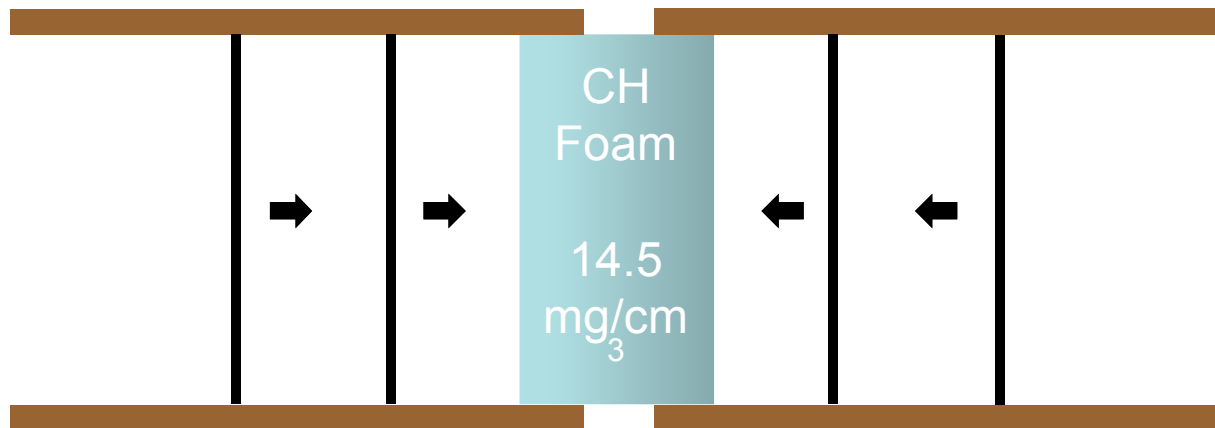
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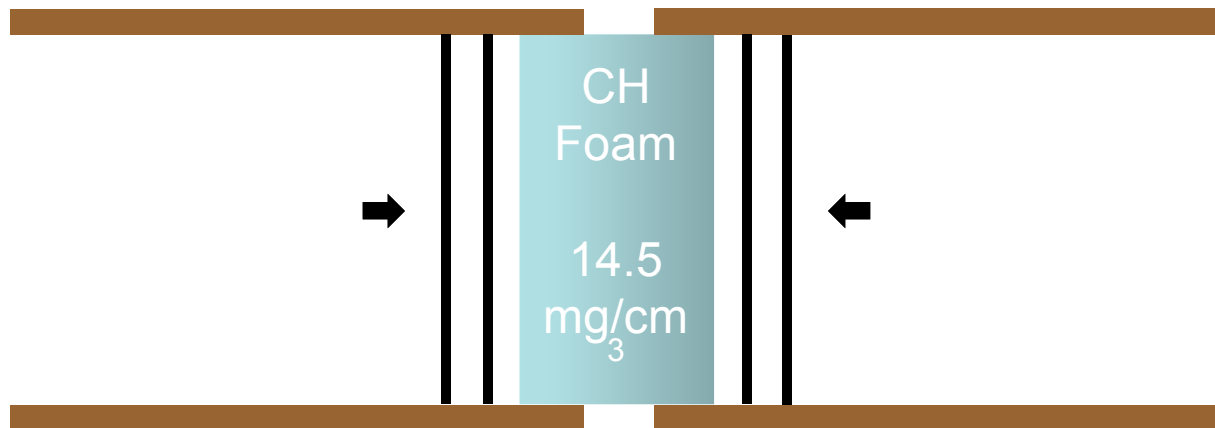
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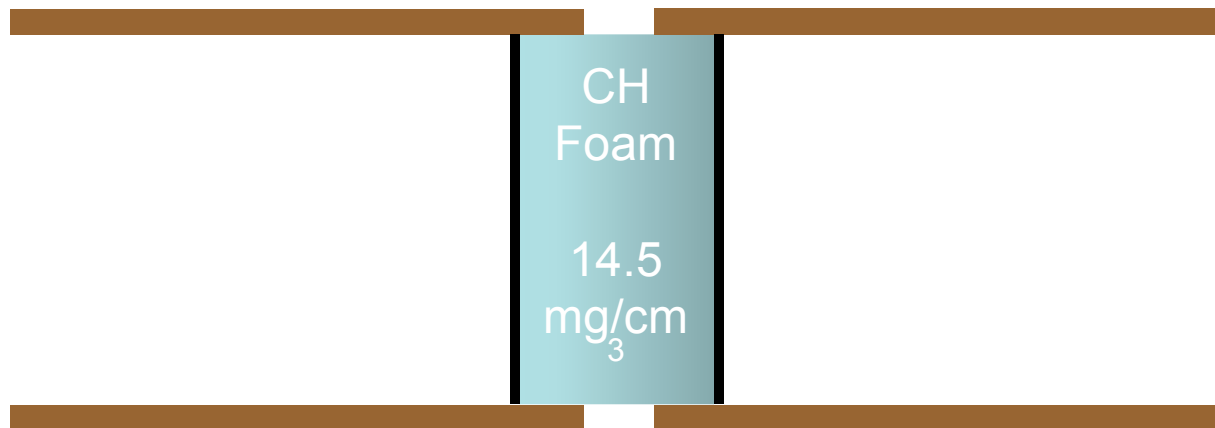
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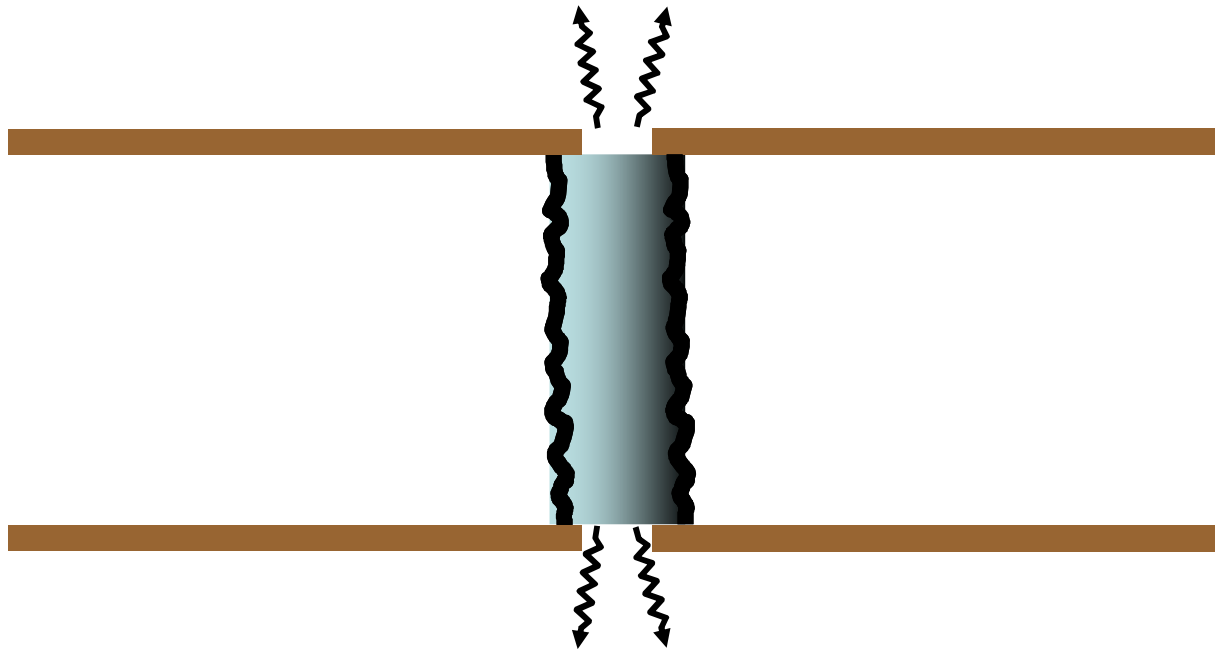
Z Pinch Dynamic Hohlräum



- W plasma collide with CH foam, and generates radiative shock
- Radiation is trapped inside W plasma due to high W opacity



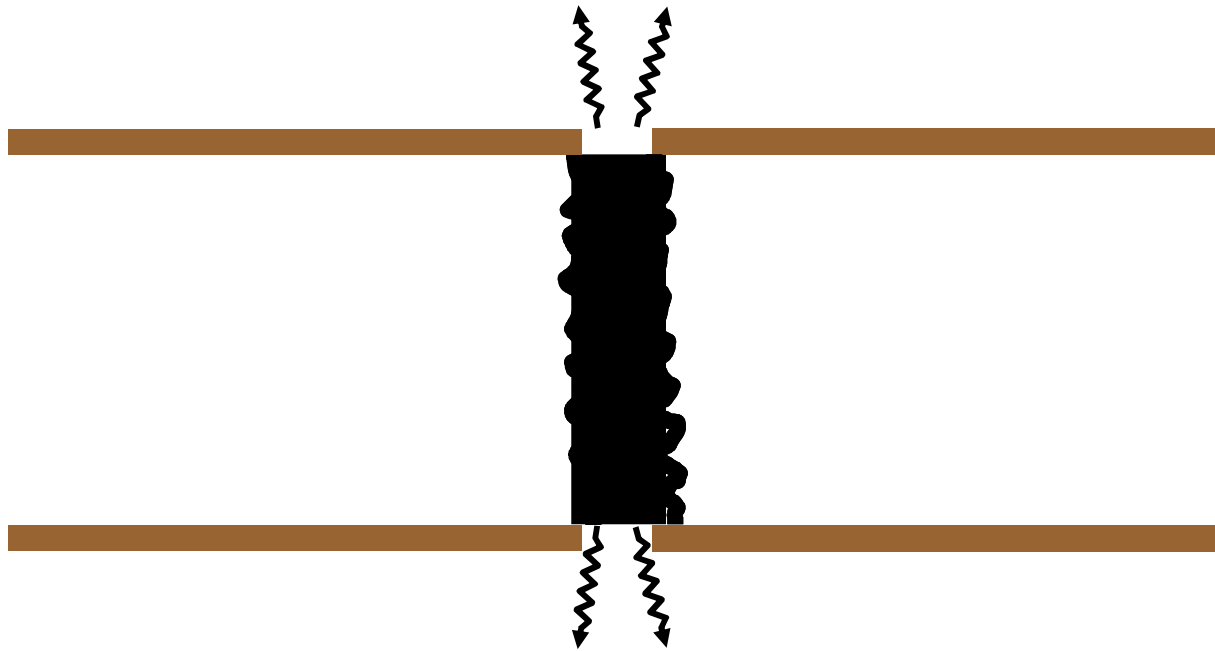
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- As W plasma implodes further, radiation temperature increases
- Some radiation are leaked from the top/bottom wholes



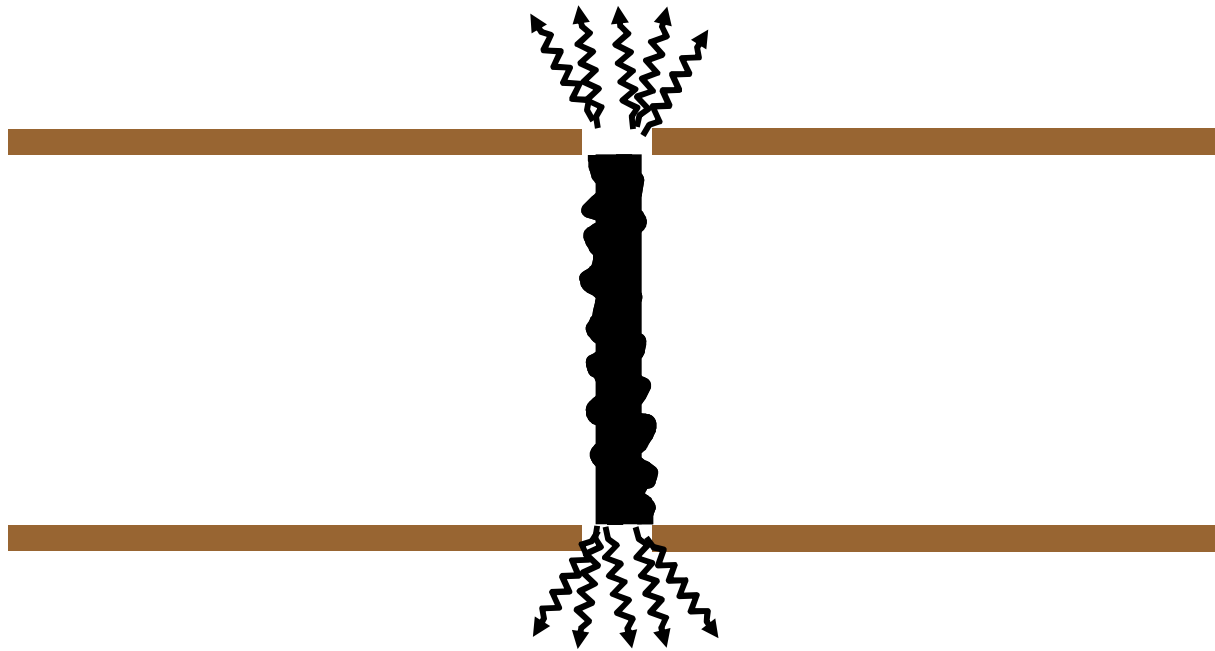
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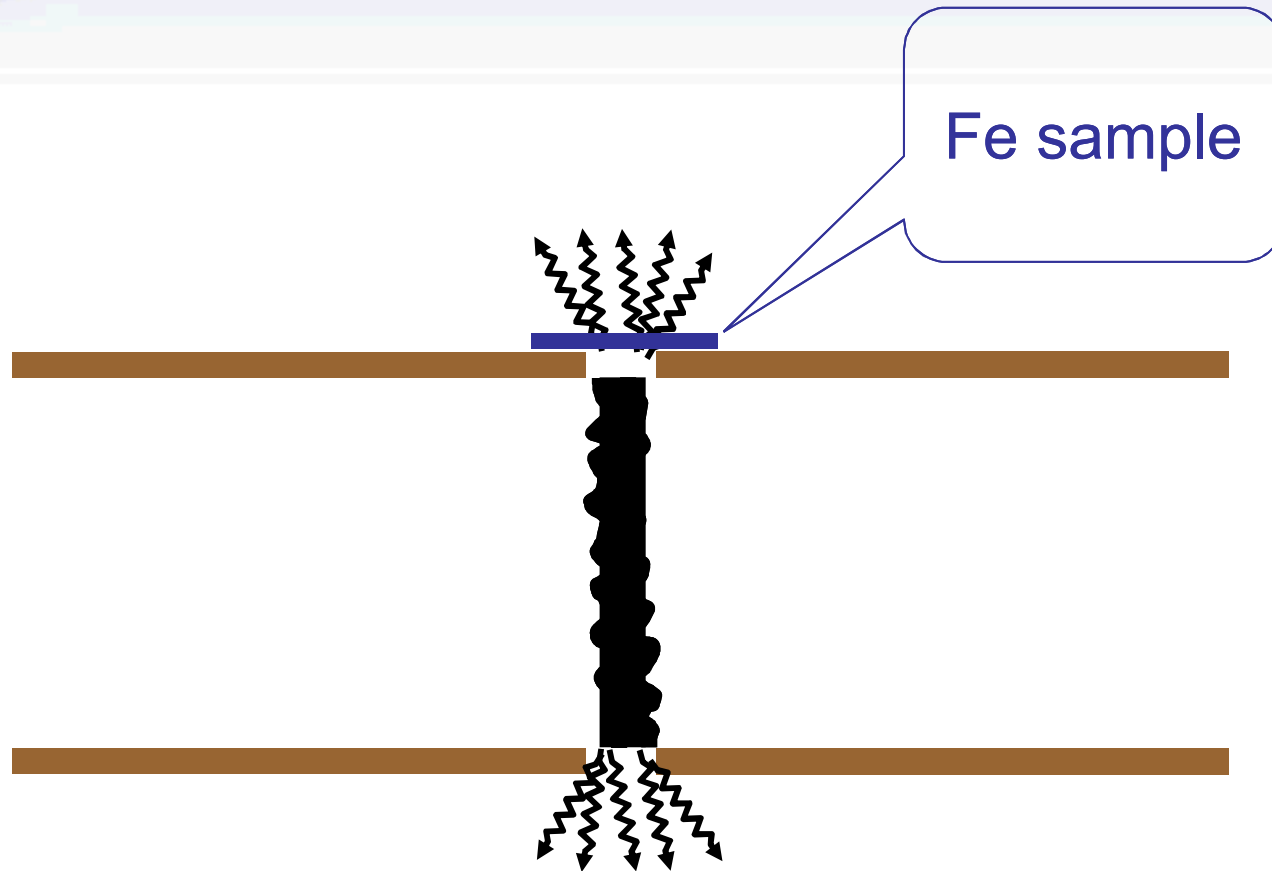
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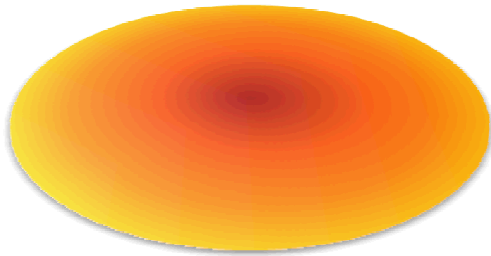
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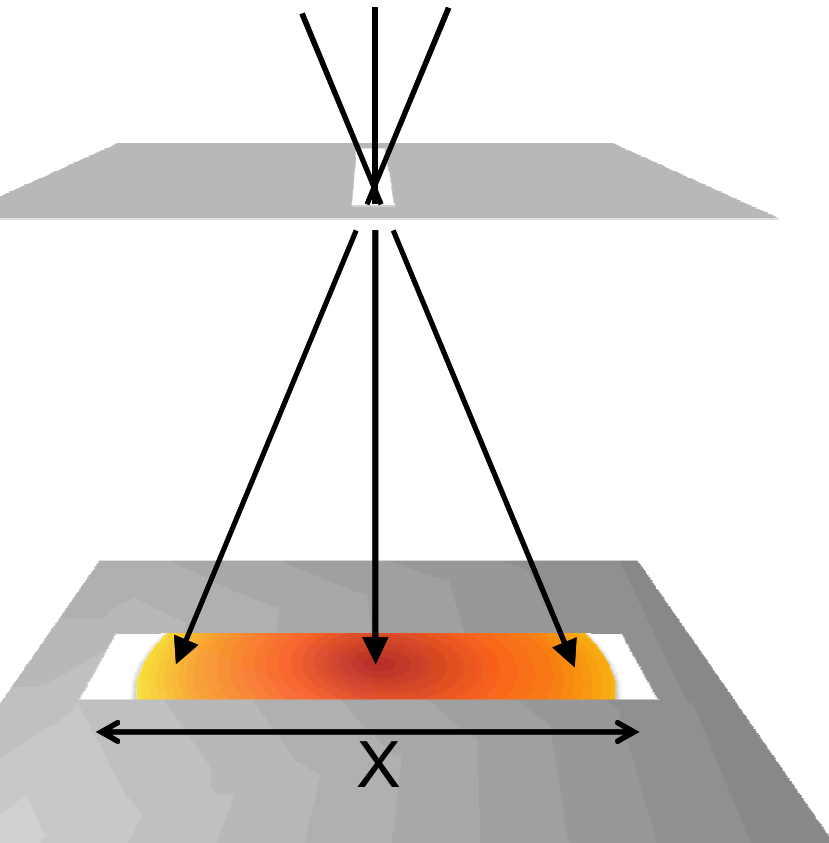
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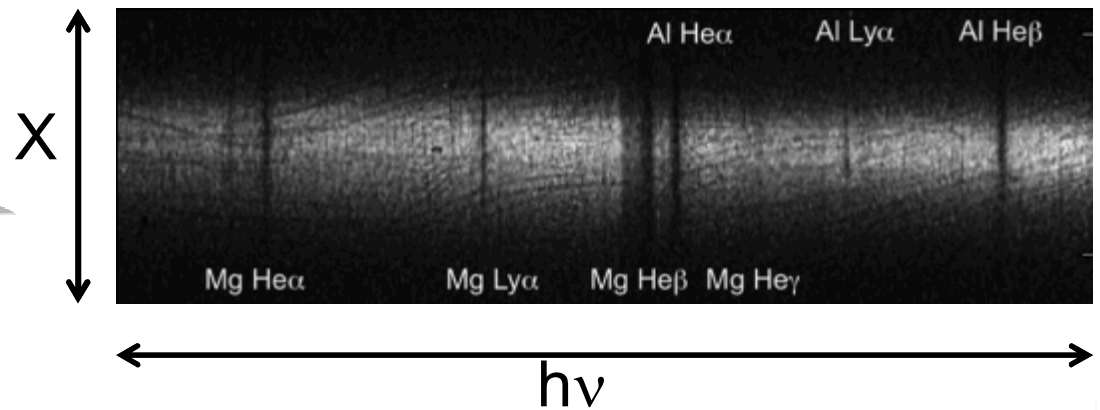
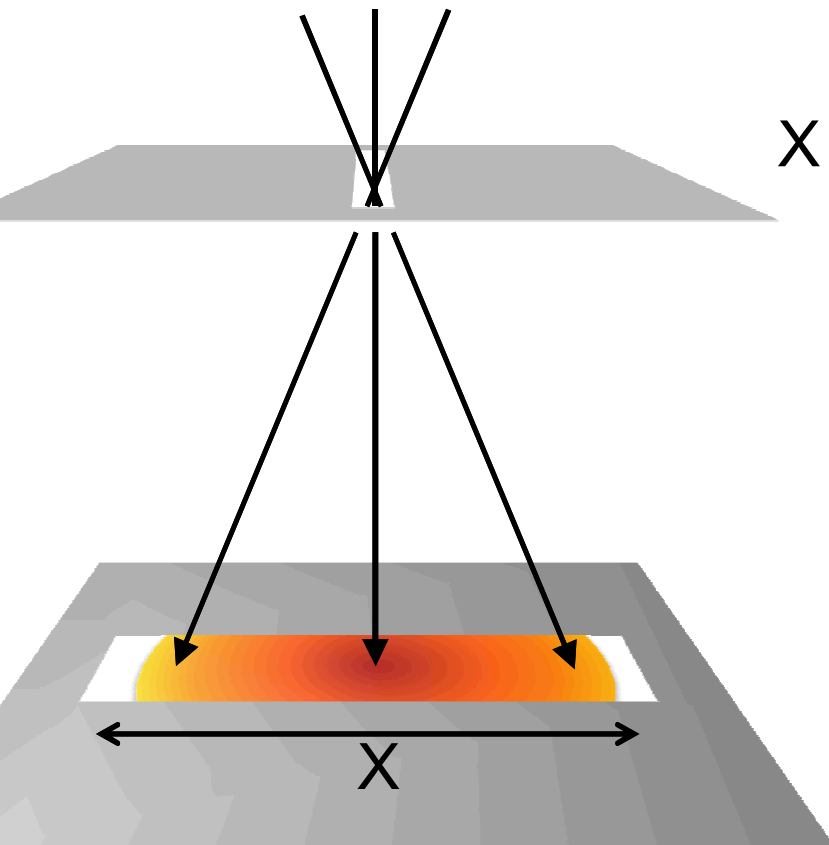
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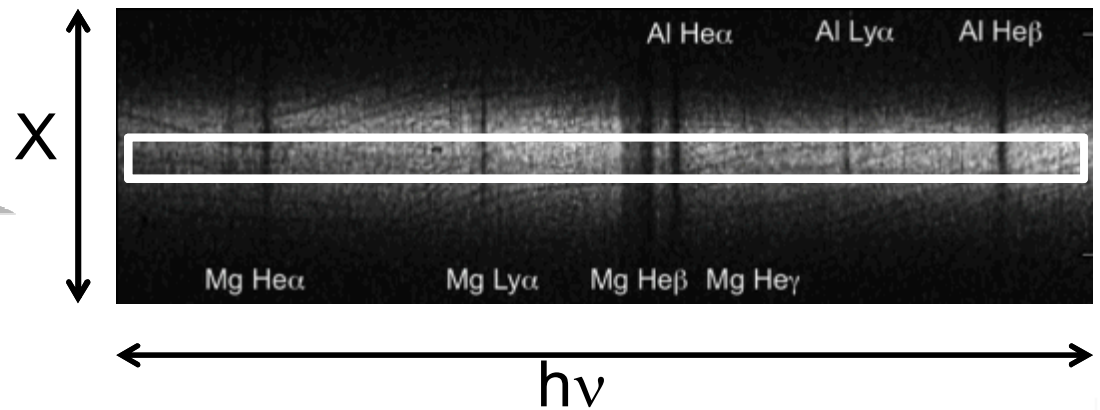
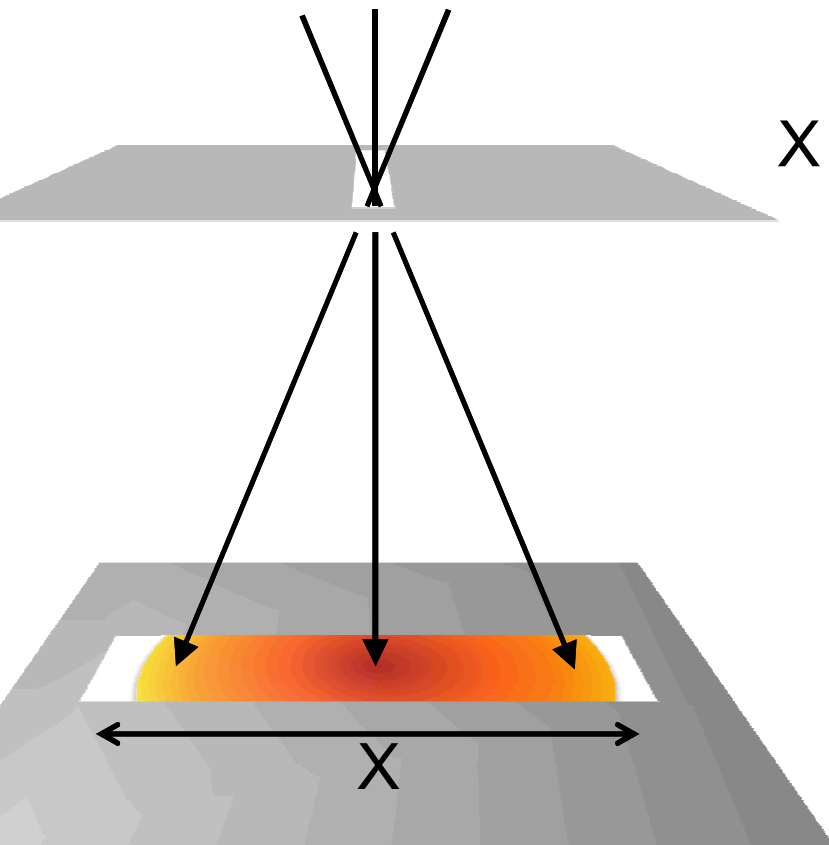
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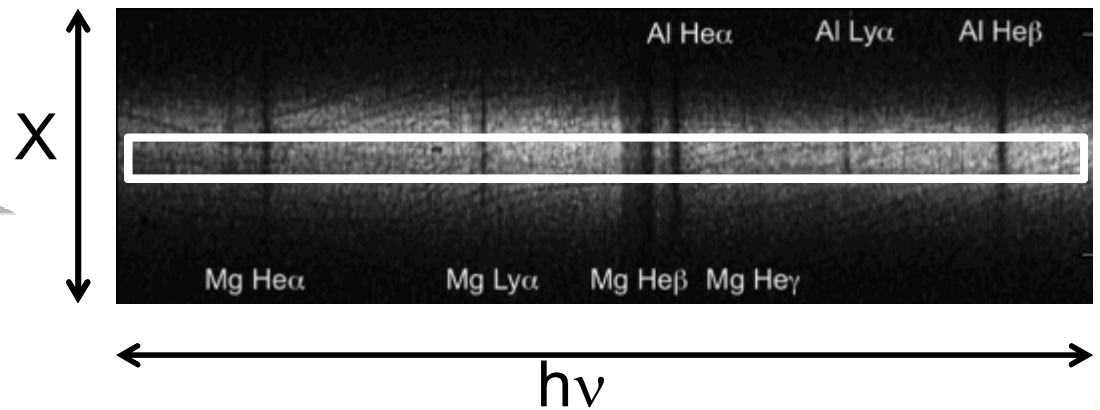
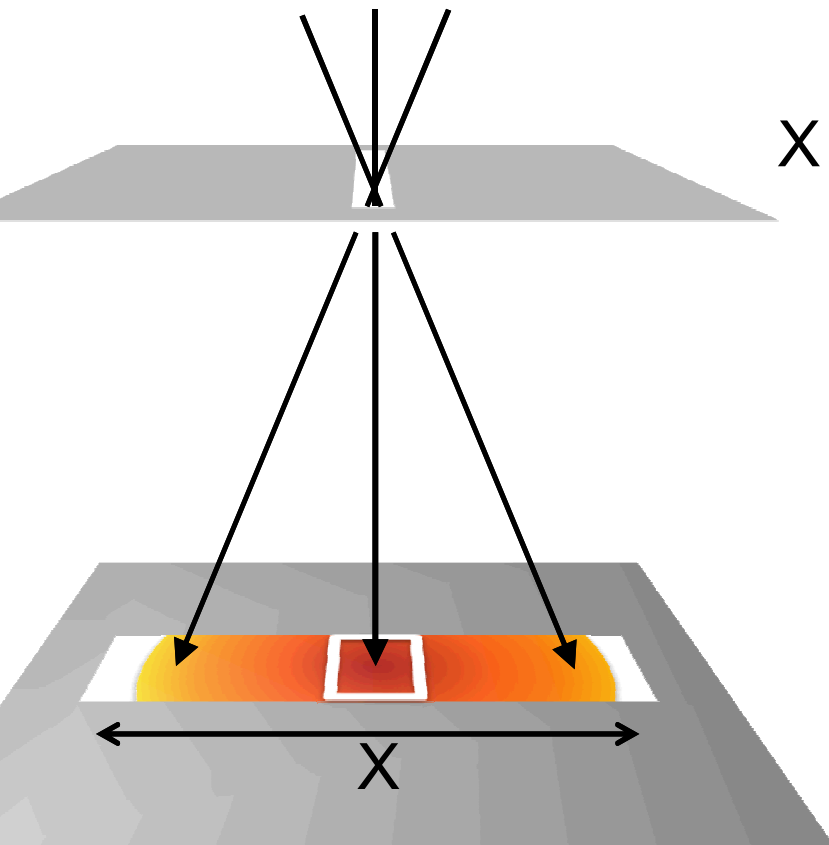
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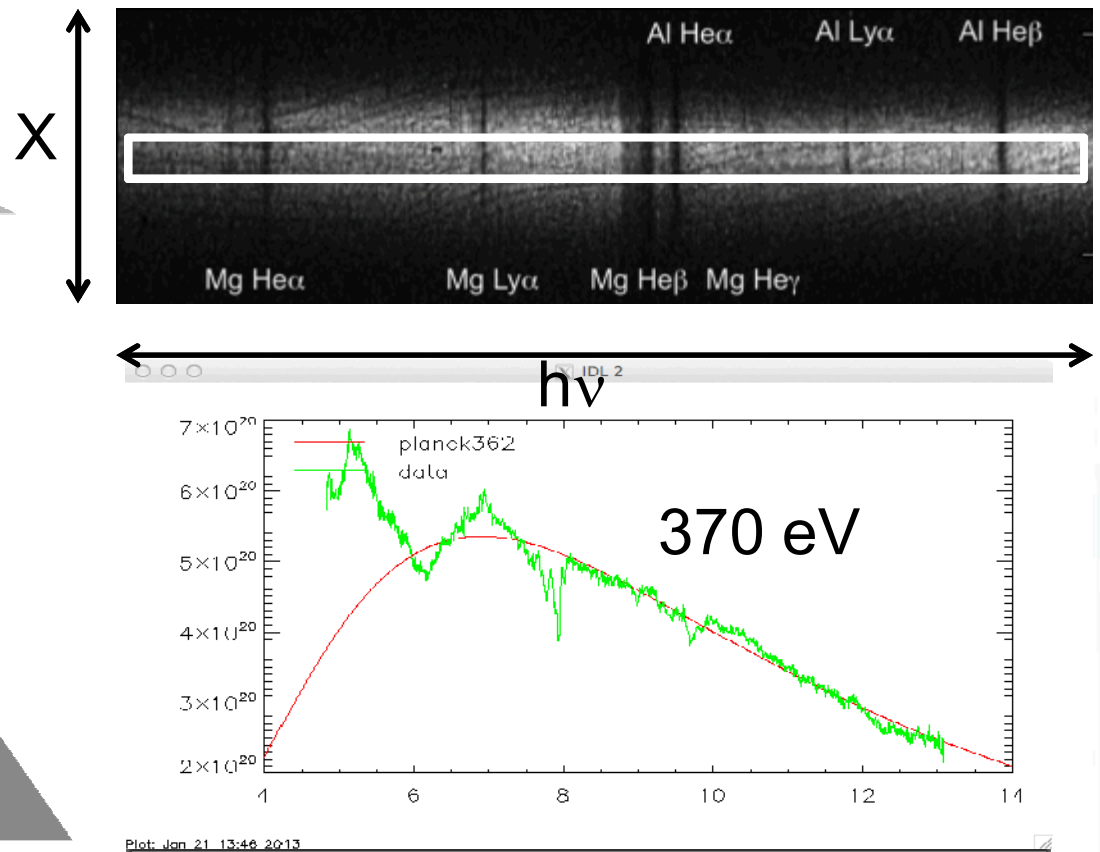
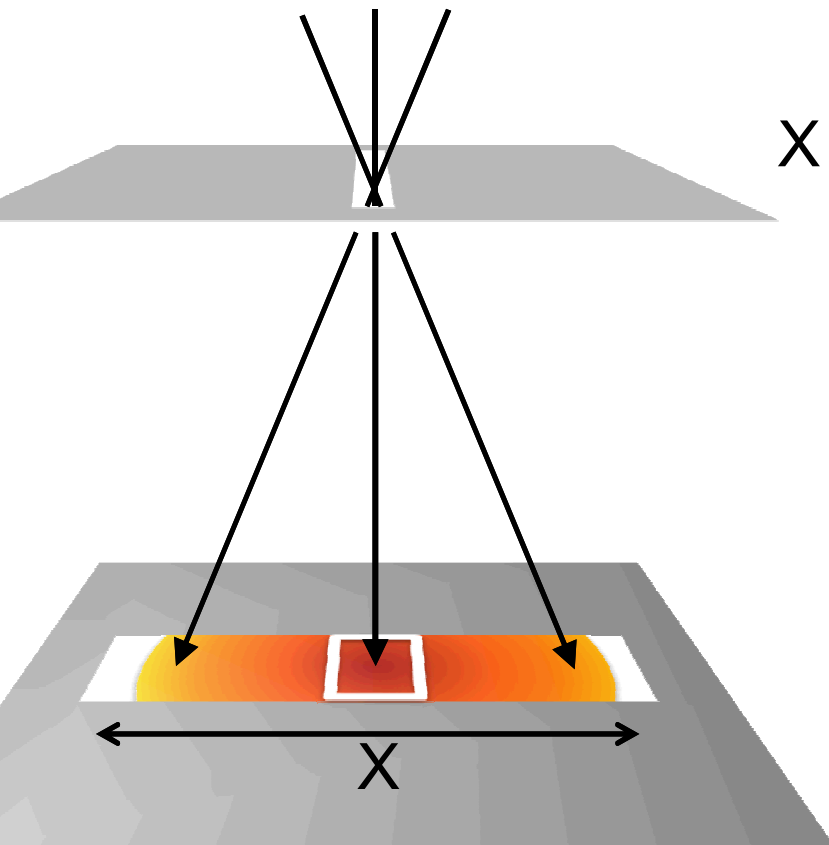
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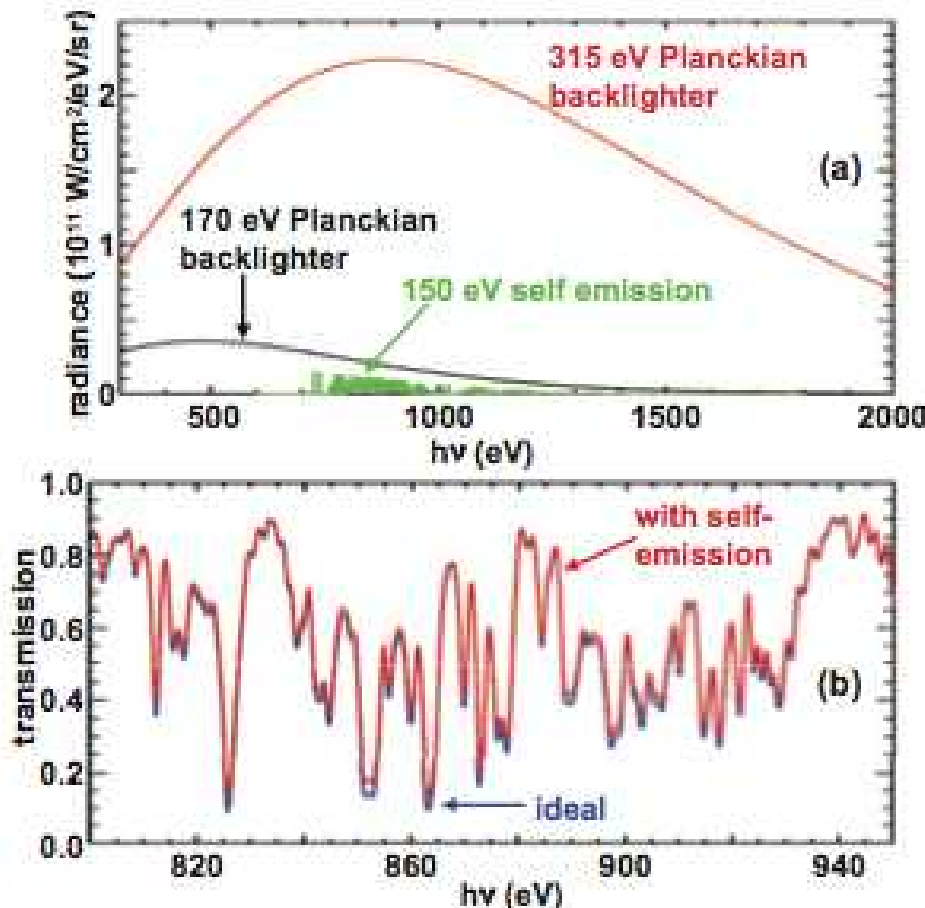
ZPDH supports three requirements

1. Strong and smooth backlighter
 - 370 eV Planckian



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 - 370 eV Planckian



315 eV Planckian is already much brighter than Fe self-emission



ZPDH supports three requirements

1. Strong and smooth backlighter
 - 370 eV Planckian
2. Sample uniformity
 - Volumetric heating by ZPDH radiation
 - Large sample size (1-4mm)
 - Long duration (3ns)



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3. Independent condition measurement
 - Mix Mg into Fe sample
 - Infer temperature and density from Mg K-shell absorption spectroscopy



ZPDH supports three requirements

1. Strong and smooth backlighter

- 370 eV Planckian

Focus of the talk

2. Sample uniformity

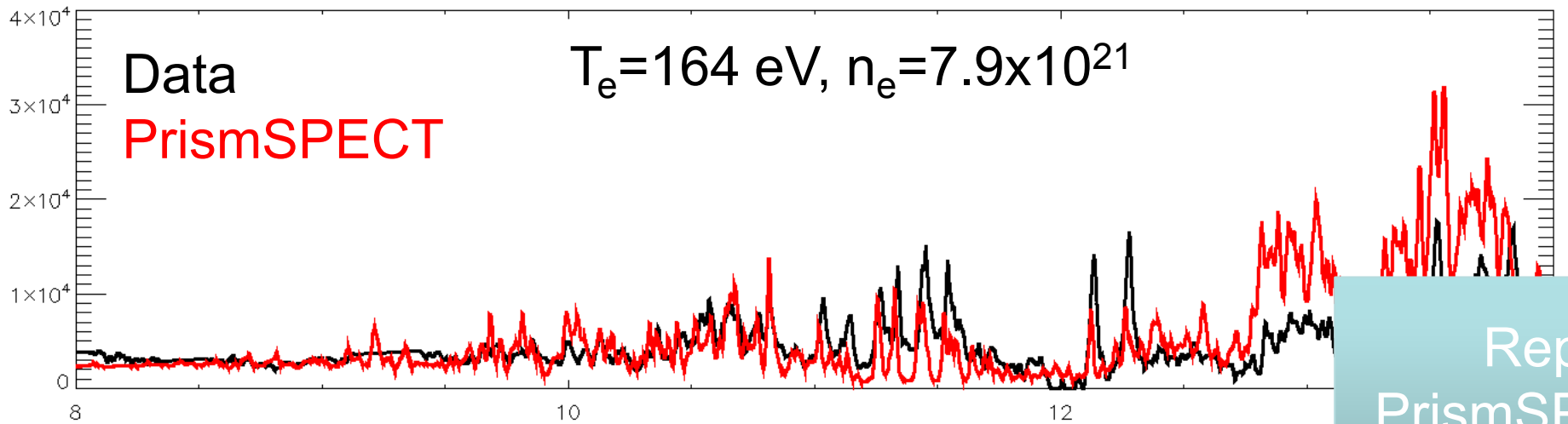
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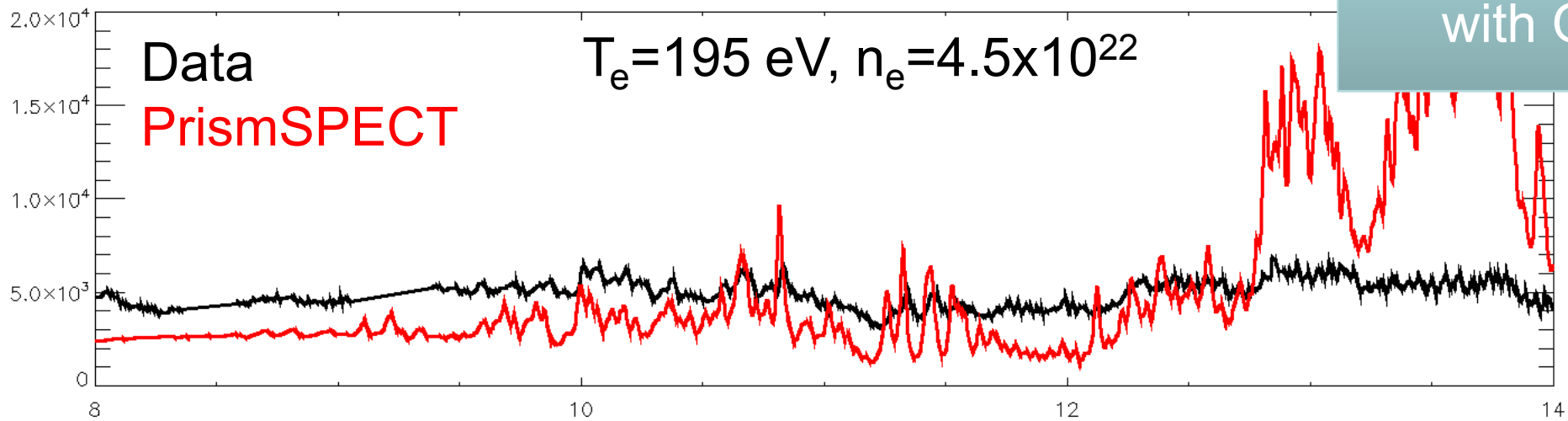
- Mix Mg into Fe sample
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Preliminary results show the opacity that astrophysicists use are lower than data



Rep
PrismSP
with O



Impacts of the project

Goal: experimentally validate the modeled Fe opacity at CZ base condition ($T_e=190$ eV, $n_e=9 \times 10^{22}$ e/cc)

- Impact:
 - Astrophysics
 - High energy density physics (HEDP)
 - Atomic physics
 - SNL



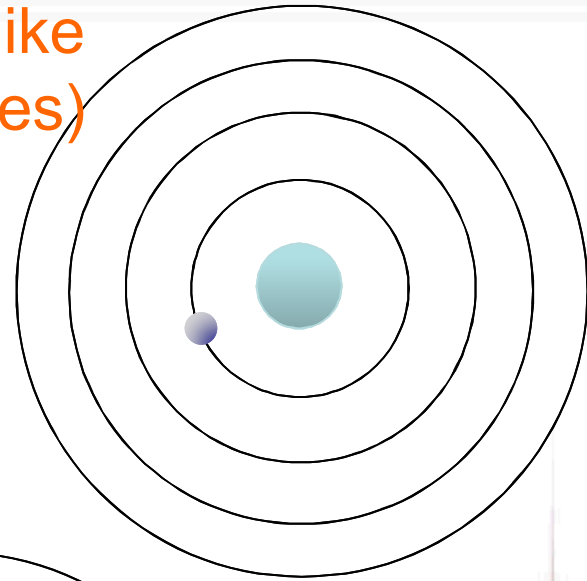
Mg K-shell line spectroscopy



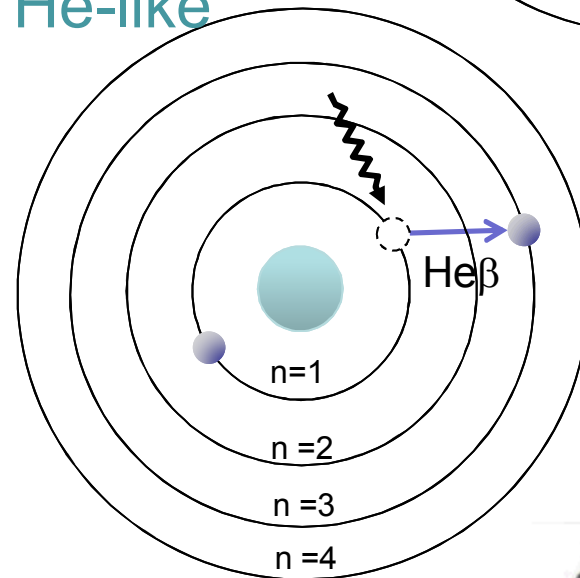
Fe plasma condition is inferred from Mg K-shell transmission spectra

- Mg is mixed into Fe
- Mg are ionized into He-like Mg
 - # of bound electrons = 2
 - $Z = 12$
 - K-shell spectra

H-like
(Ly series)



He-like

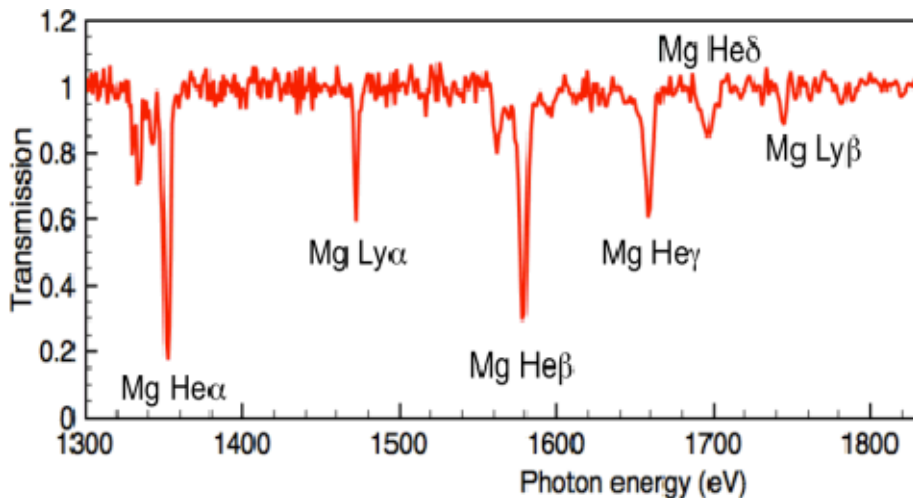


Transitions

$\alpha: n=1 \rightarrow 2$

$\beta: n=1 \rightarrow 3$

$\gamma: n=1 \rightarrow 4$



Measured transmission depends on optical depths: $T_v = \exp(-\tau_v)$

Optical depths:

$$\tau_v = \frac{\pi e^2}{mc} f_{lu} \cdot \{N_{Mg} \Delta x\} \cdot \Phi_v \cdot p_l$$

f_{lu} = oscillator strengths

$\{N_{Mg} \Delta x\}$ = areal density of Mg

Φ_v = line shape

p_l = fractional population of the lower state



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Line ratio is sensitive to electron temperature

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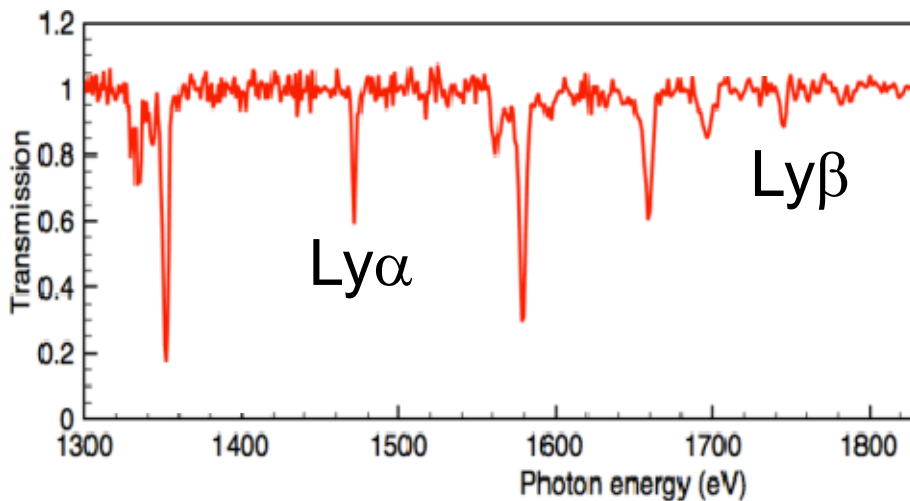


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$\text{Ly}\alpha, \beta \dots$ Proportional to $p_{H\text{-like},g}$



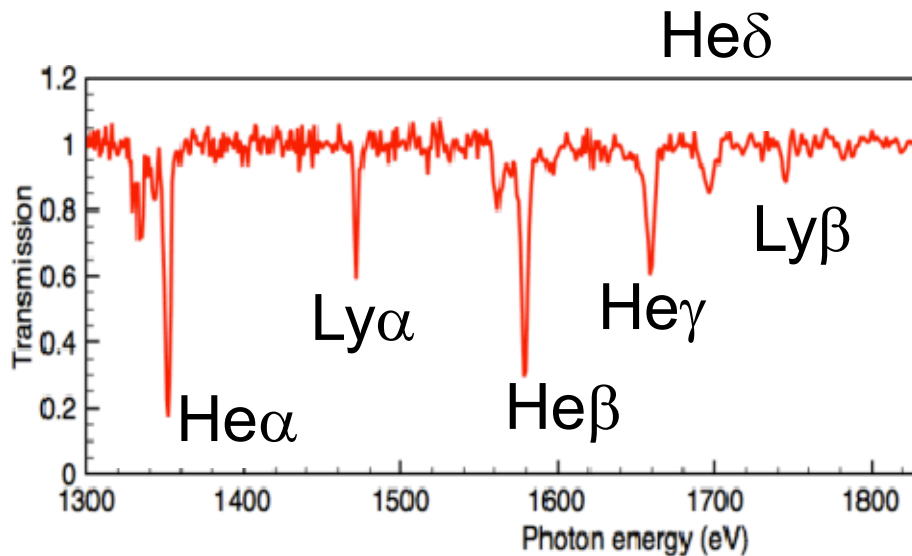
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Optical depths:

$$\tau_{\nu} = \frac{\pi e^2}{mc} f_{lu} \cdot \{N_{Mg} \Delta x\} \cdot \Phi_{\nu} \cdot p_l$$

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$\text{He}\alpha, \beta, \gamma, \delta \dots$ Proportional to $P_{\text{He-like},g}$



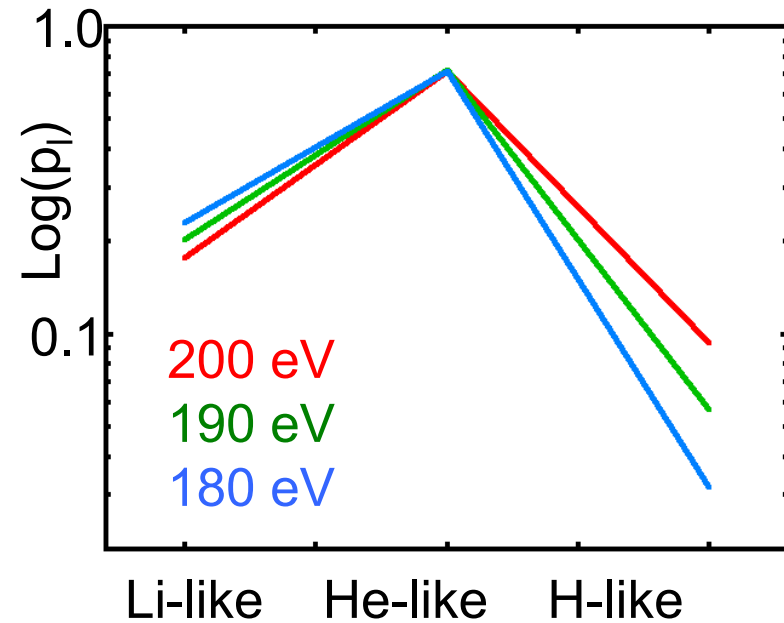
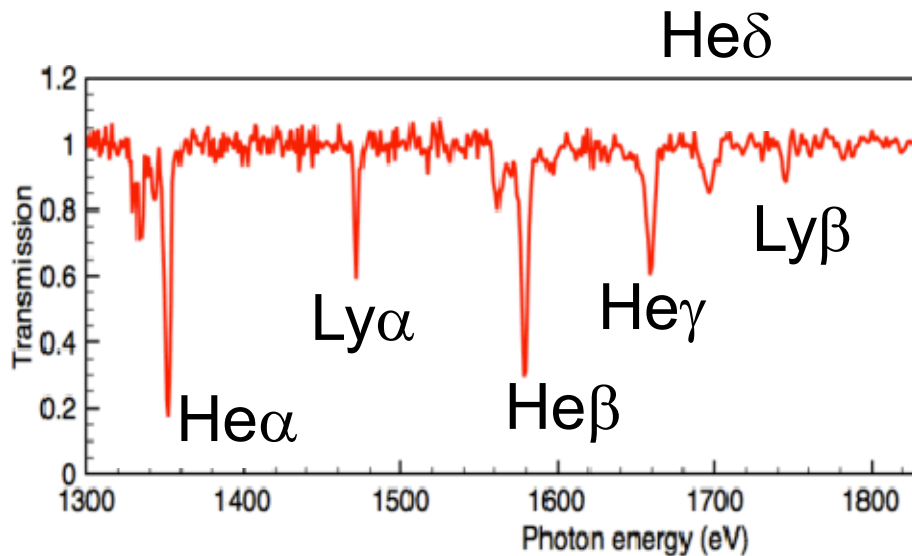
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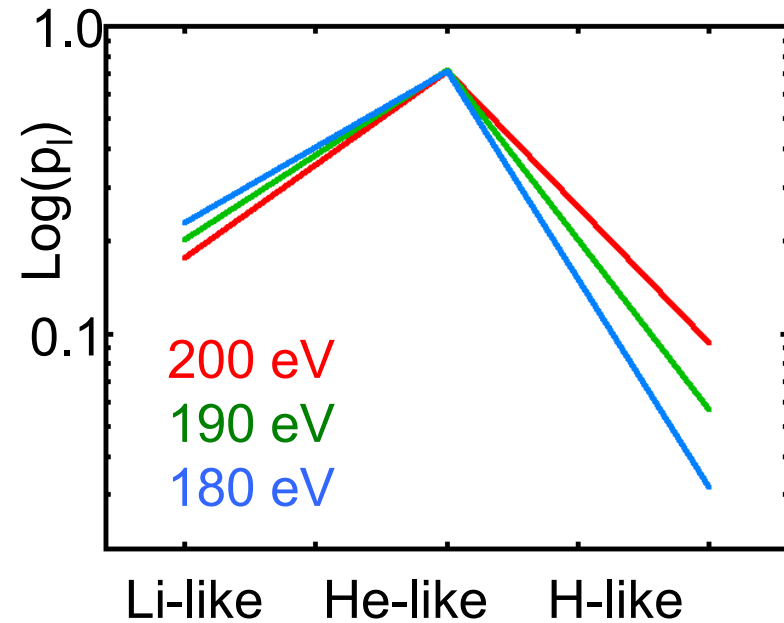
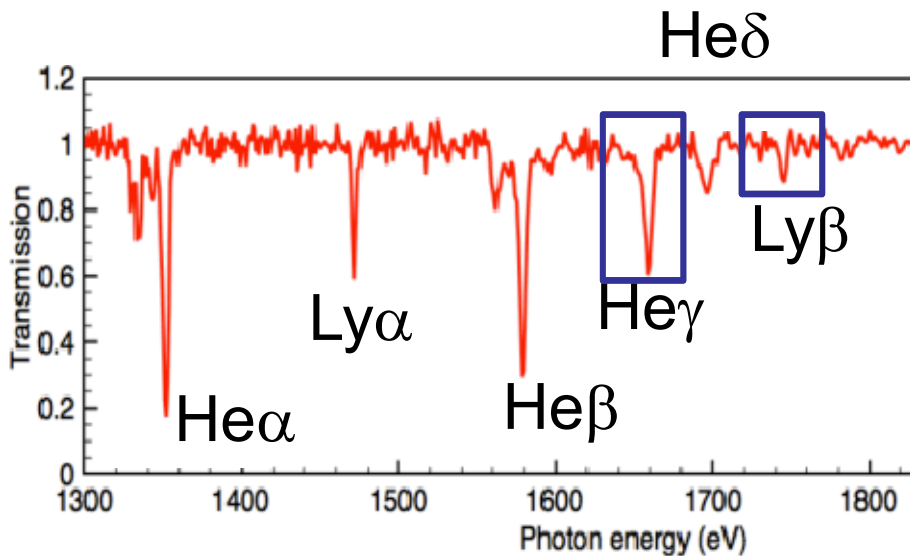
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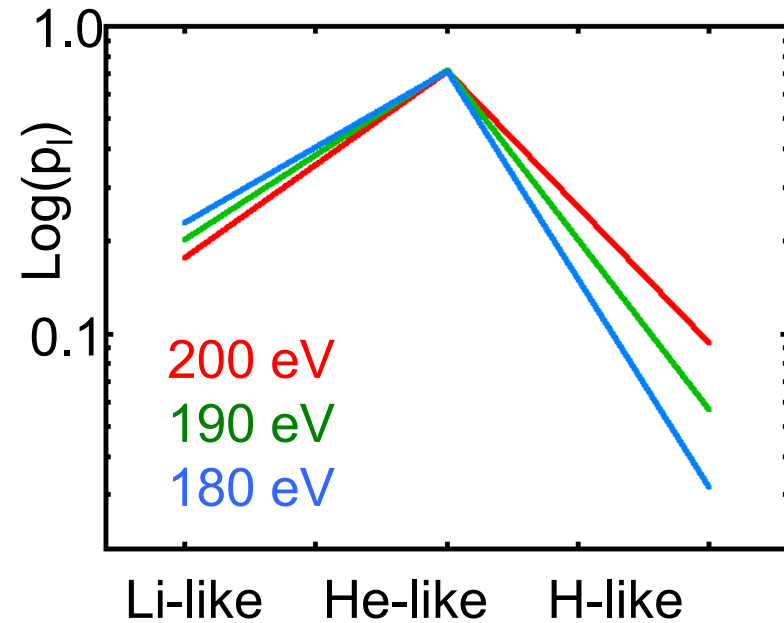
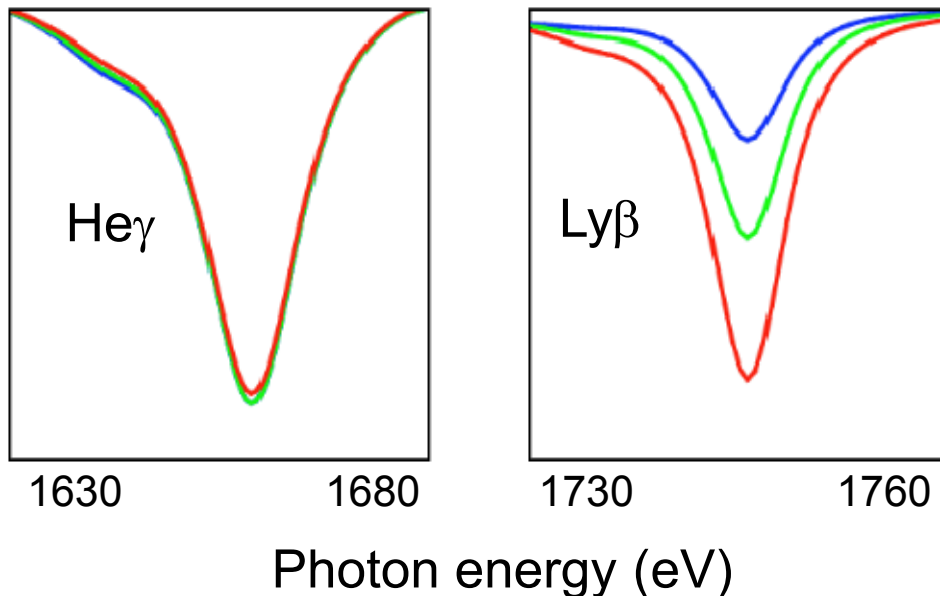
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Optical depths:

$$\tau_v = \frac{\pi e^2}{mc} f_{lu} \cdot \{N_{Mg} \Delta x\} \cdot \Phi_v \cdot p_l$$

Ly α , β ... Proportional to $p_{H-like,g}$

He α , β , γ , δ ... Proportional to $p_{He-like,g}$

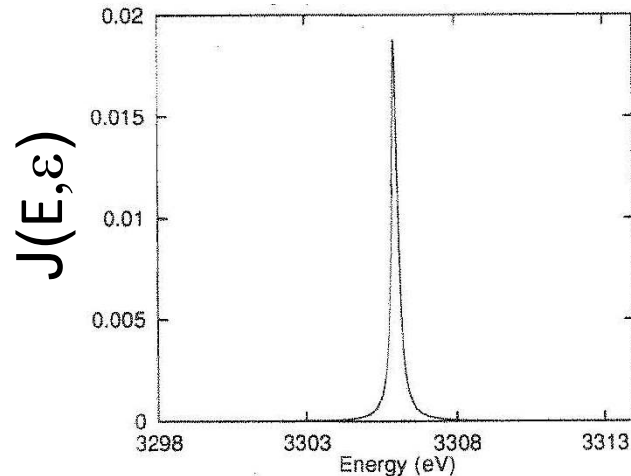
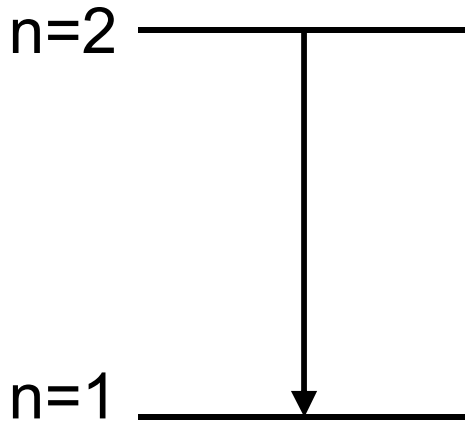


Line shape Φ_ν is sensitive to electron density, n_e

Optical depths:

$$\tau_\nu = \frac{\pi e^2}{mc} f_{lu} \cdot \{N_{Mg} \Delta x\} \cdot \Phi_\nu \cdot p_l$$

- Line shape is dominated by the Stark broadening

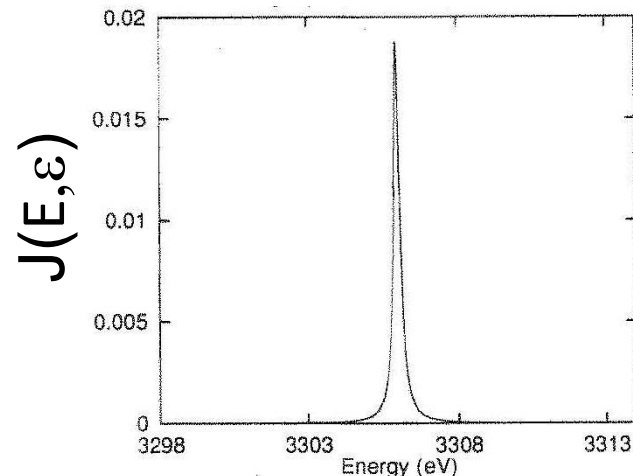
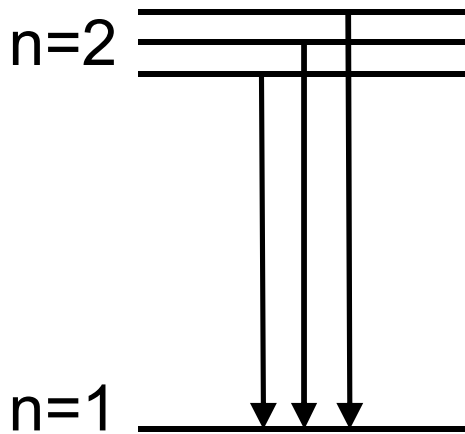


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- Line shape is dominated by the Stark broadening
 - External field, ε , splits the energy levels

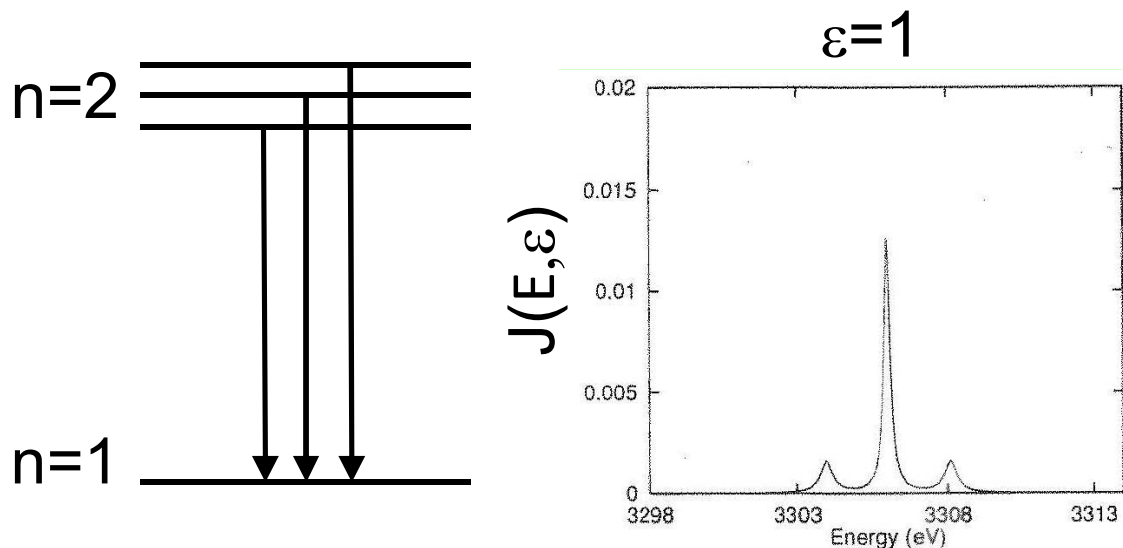


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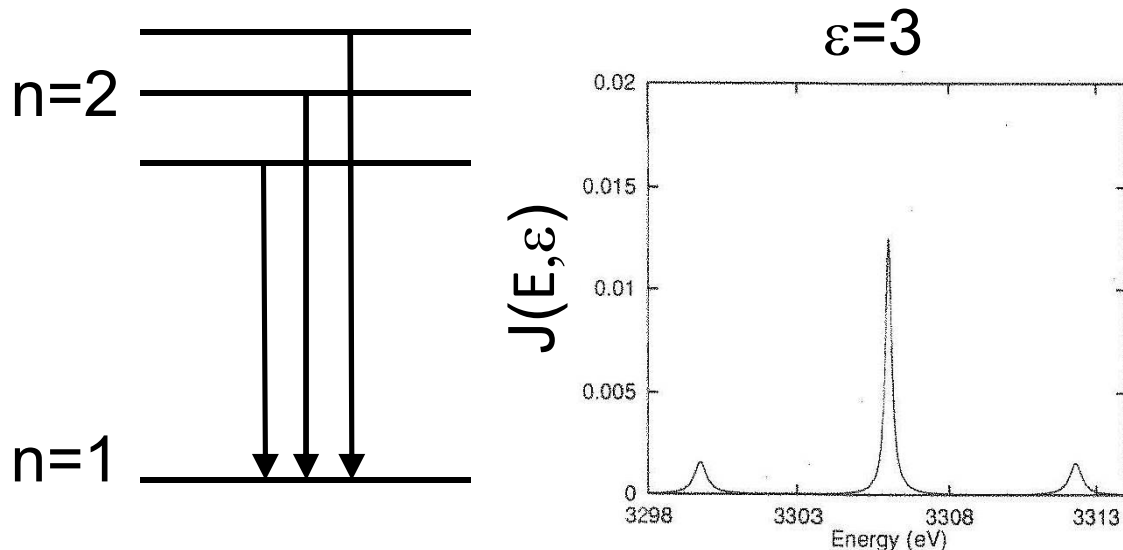


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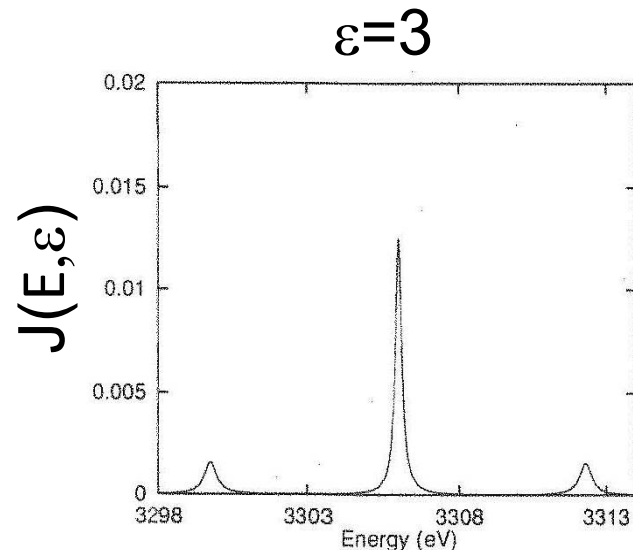
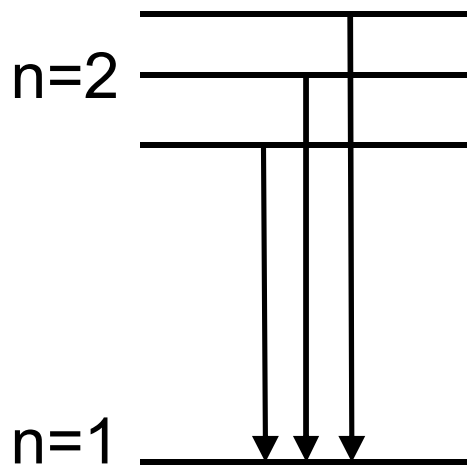


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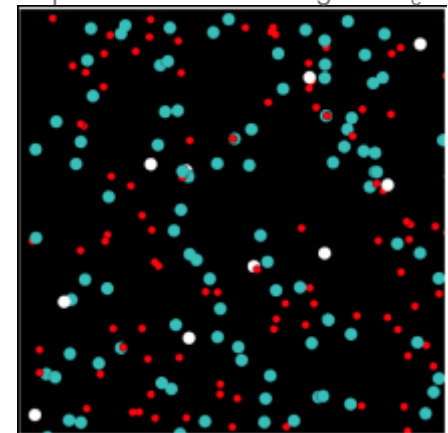
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- Line shape is dominated by the Stark broadening
 - External field, ε , splits the energy levels
 - Each radiator sees different ε



Snapshot of microscopic particle motion for a given n_e



S. Ferri RPHDM2012

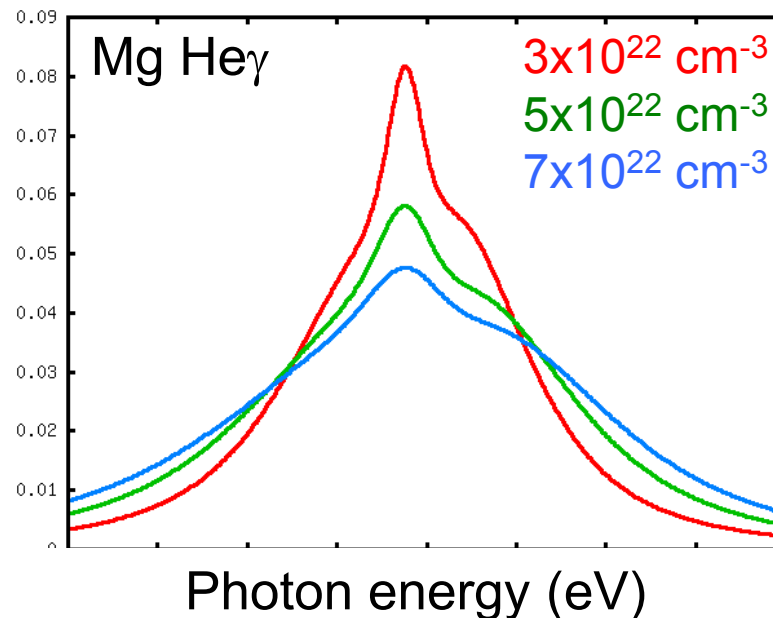


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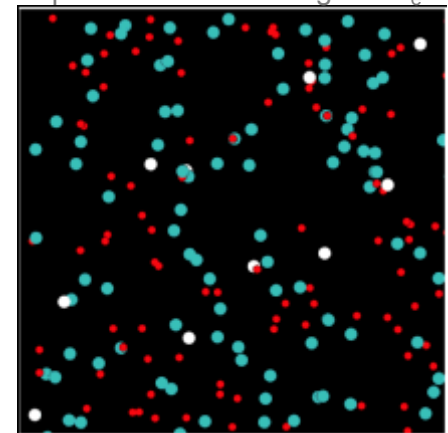
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- Line shape is dominated by the Stark broadening
 - External field, ε , splits the energy levels
 - Each radiator sees different ε
 - Net effect is broadening



Snapshot of microscopic particle motion for a given n_e



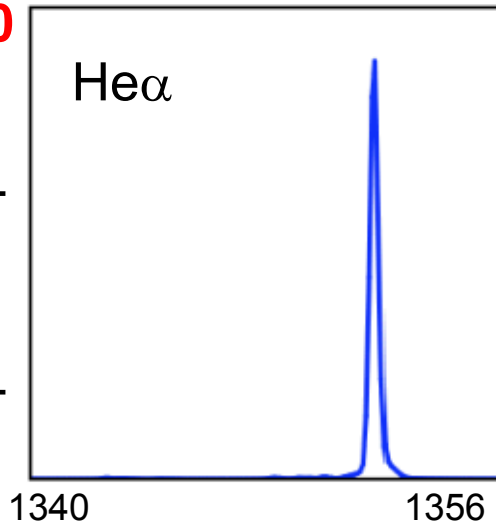
S. Ferri RPHDM2012



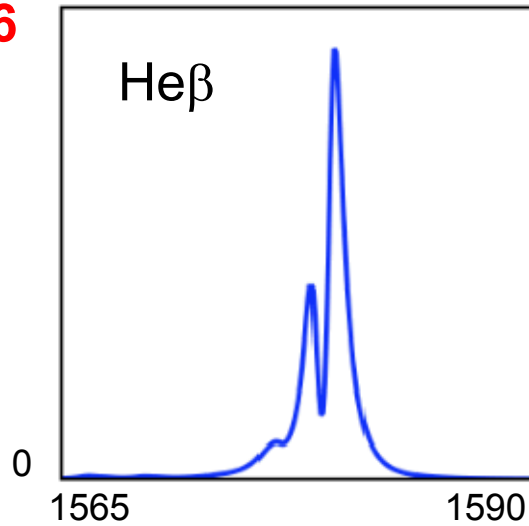
Which lines should we fit?

150

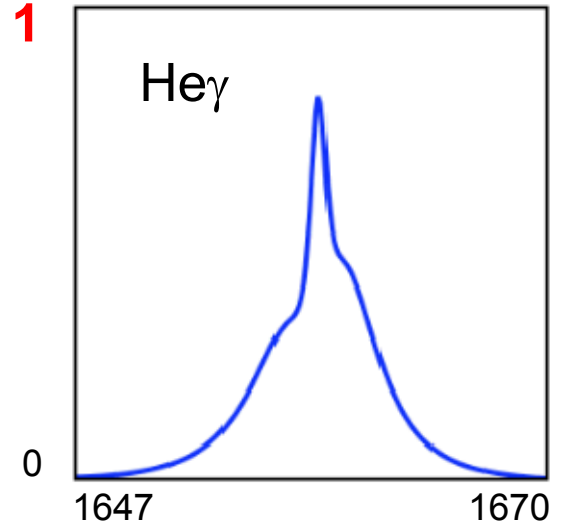
o Optical depths



6



1

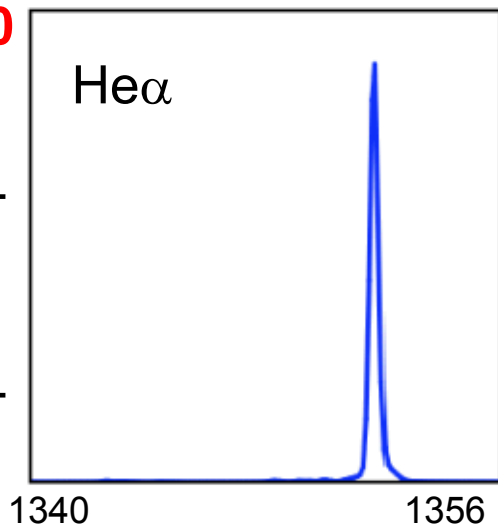


Which lines should we fit?

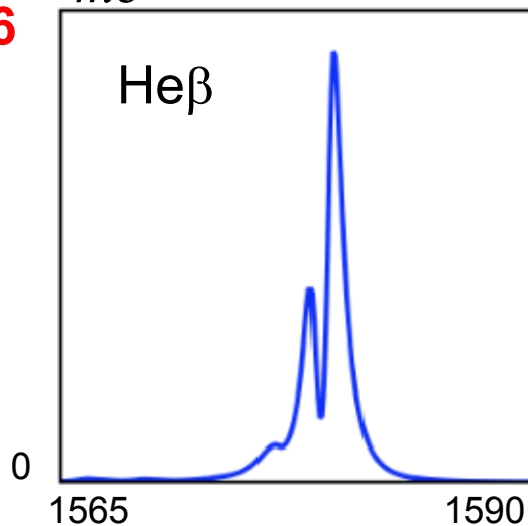
$$\tau_v = \frac{\pi e^2}{mc} f_{lu} \cdot \{N_{Mg} \Delta x\} \cdot \Phi_v \cdot p_l$$

150

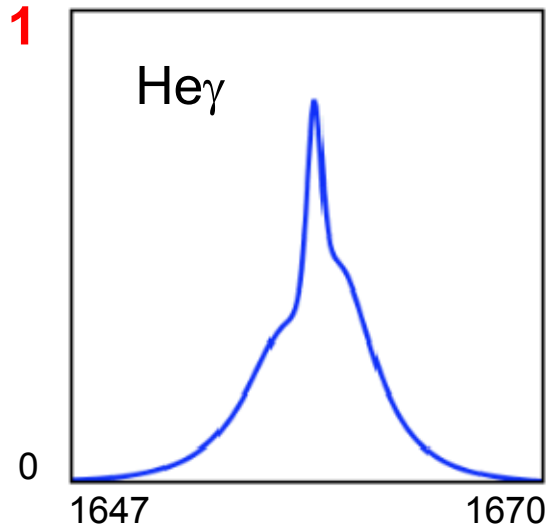
Optical depths



6



1

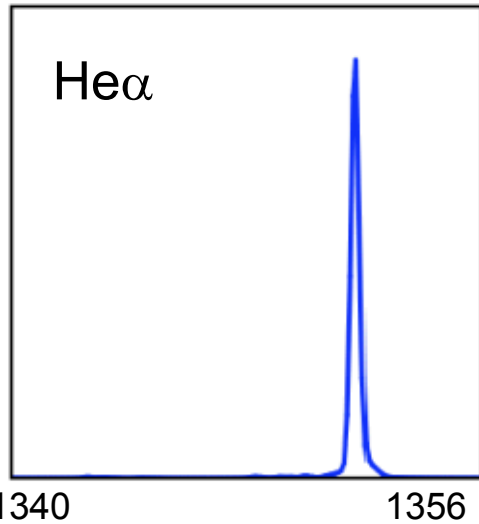


Which lines should we fit?

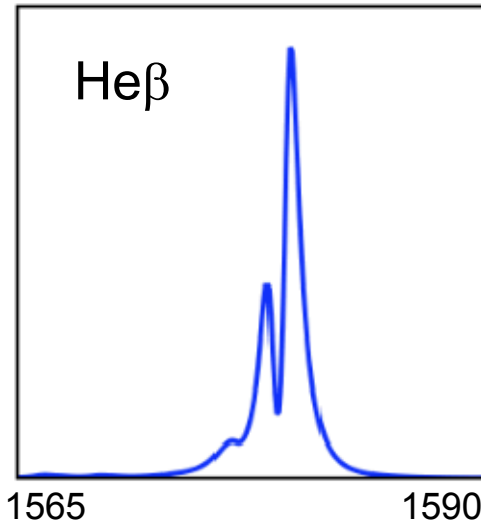
$$\tau_v = \frac{\pi e^2}{mc} f_{lu} \cdot \{N_{Mg} \Delta x\} \cdot \Phi_v \cdot p_l$$

150

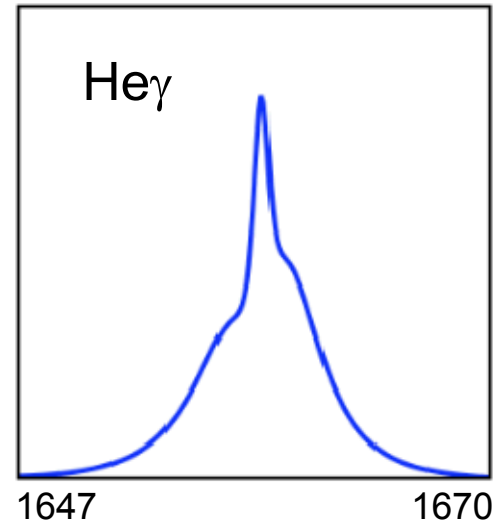
Optical depths



6

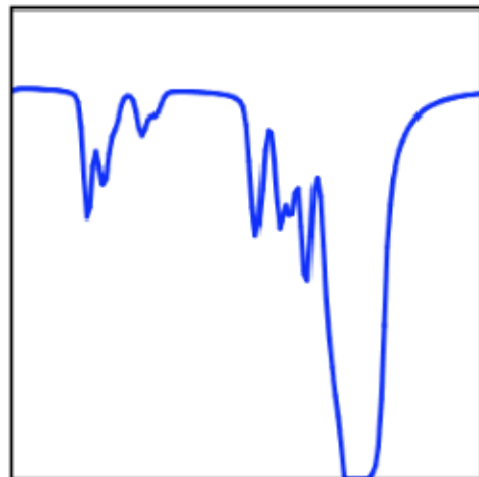


1

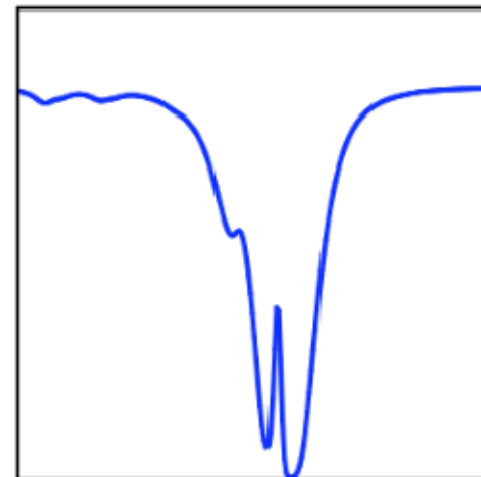


1.2

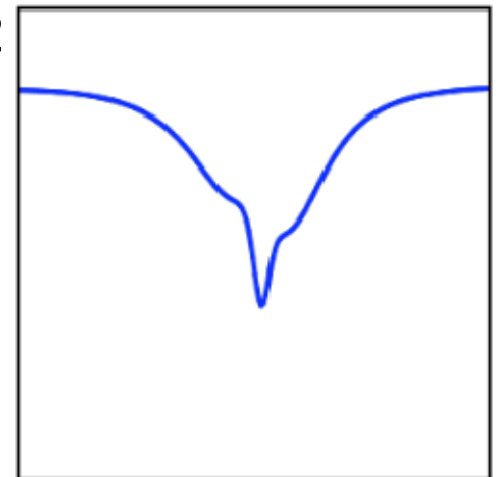
Transmission



1.2



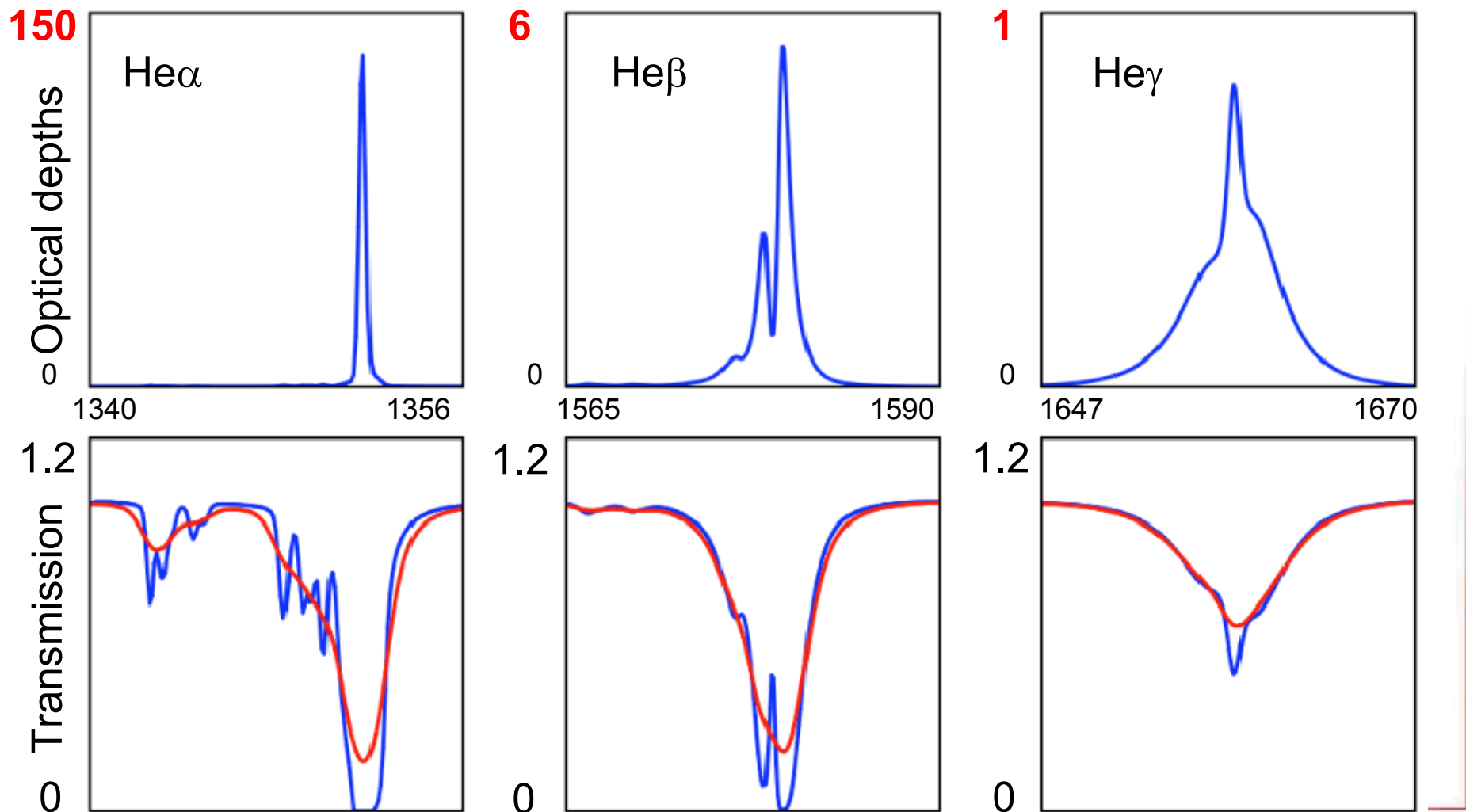
1.2



$$T_v = \exp(-\tau_v)$$



Which lines should we fit?

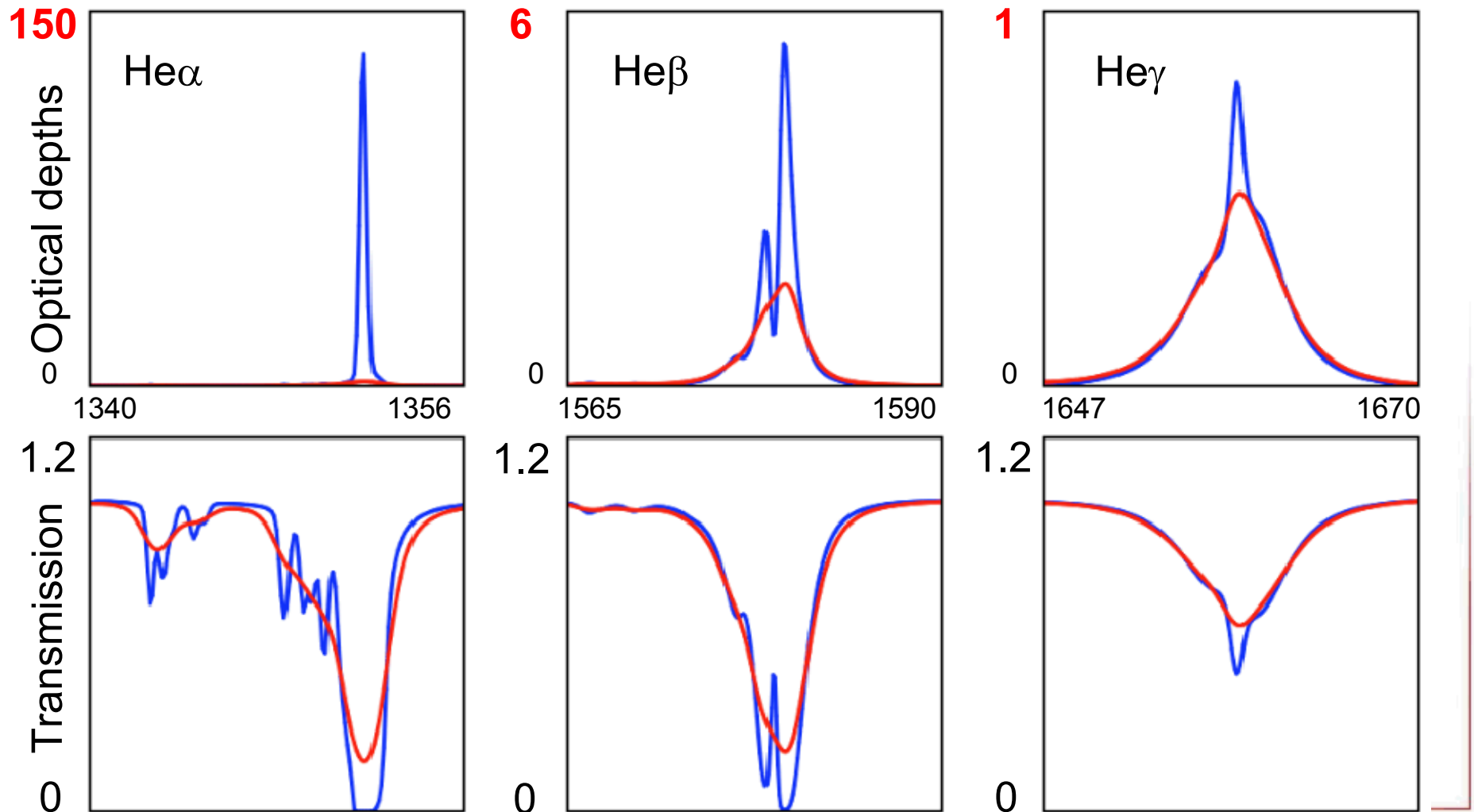


With the instrumental broadening



Which lines should we fit?

With the instrumental broadening

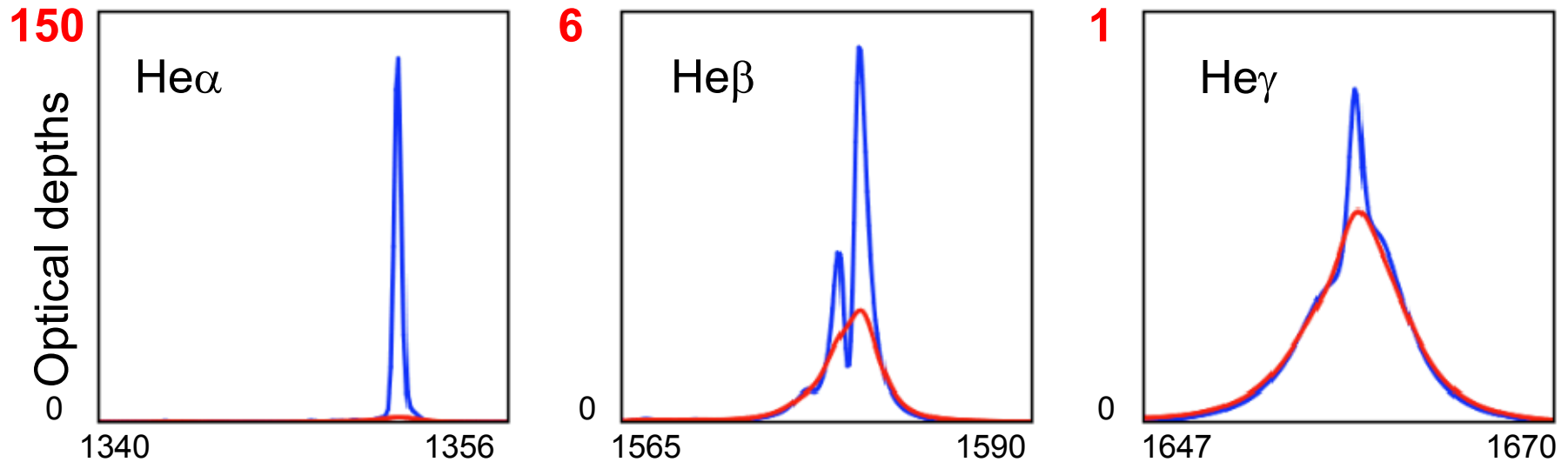


With the instrumental broadening



Which lines should we fit?

With the instrumental broadening



- Measuring optical depths
 - Less than 1 ... reliable
 - Less than 3 ... challenging
 - Precise measurement
 - Precise knowledge of instrumental broadening
 - Larger than 3 ... impossible
- We should fit weaker lines





Table based flexible spectral model
And optimization



Extract emissivity and opacity database

- Use a collisional radiative model to compute fractional emissivity and opacity for a range of Te and ne
 - PrismSPECT¹ is used
 - LTE
 - ATBASE 6.1 for atomic data
 - Continuum lowering by occupation probability
 - Detailed Stark line shape calculation by MERL²+APEX³

$$\varepsilon_{\nu}^{frac} = \frac{1}{4\pi} p_u A_{ul} E_{\nu} \Phi_{\nu} \longrightarrow I_{\nu}^{opt.thin} = \varepsilon_{\nu}^{frac} (N_a \Delta x)$$

$$\kappa_{\nu}^{frac} = \frac{1}{4\pi} p_l B_{lu} E_{\nu} \Phi_{\nu} \longrightarrow T_{\nu}^{pure} = \exp\{-\kappa_{\nu}^{frac} (N_a \Delta x)\}$$

- Compute ε_{ν}^{frac} and κ_{ν}^{frac} databases for Al, Mg, and Fe

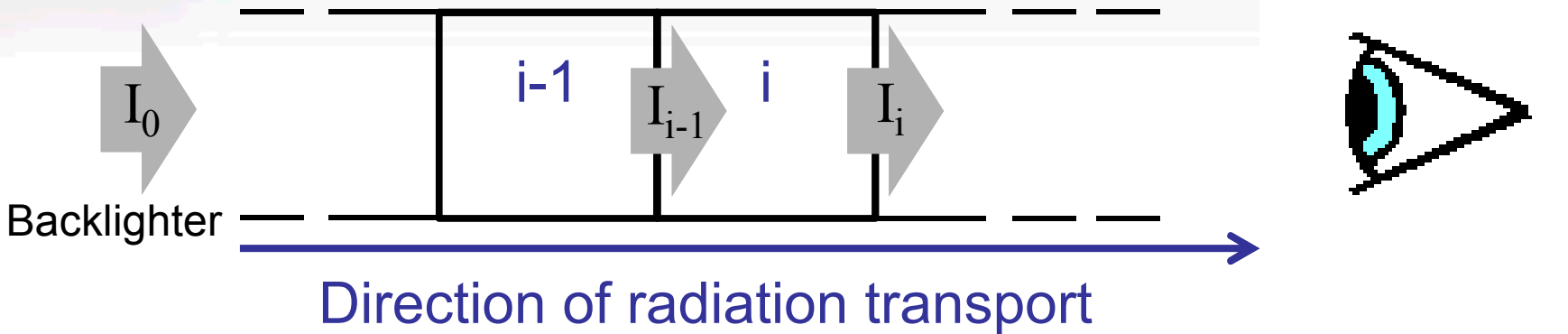
¹ J.J. MacFarlane, I.E. Golovkin, et al, High Energ Dens Phys **3**, 181 (2007).

² R.C. Mancini, D.P. Kilcrease, et al, Computer Physics Communications **63**, 314 (1991).

³ C. Iglesias, H. DeWitt, et. al., Phys. Rev. A **31**, 1698 (1985).



Database + Radiation transport



$$I_{v,i} = \underbrace{I_{v,i-1} T_{v,i}}_{\text{Attenuation of } I_{v,i-1}} + \underbrace{\frac{\epsilon_{v,i}^{frac}}{\kappa_{v,i}^{frac}} (1 - T_{v,i})}_{\text{Self-emission in cell } i}}$$

where

$$\epsilon_{v,i}^{frac} = \epsilon_v^{frac}(T_{e,i}, n_{e,i})$$

$$\kappa_{v,i}^{frac} = \kappa_v^{frac}(T_{e,i}, n_{e,i})$$

$$I_v^{observed} = \sum_{i=1}^N \left\{ I_{v,i-1} T_{v,i} + \frac{\epsilon_{v,i}^{frac}}{\kappa_{v,i}^{frac}} (1 - T_{v,i}) \right\}$$

- Mixture
- Gradient
- Instrumental broadening
- Detailed line shapes
- Direct dependence on Ne
- Optimization



Optimization algorithms

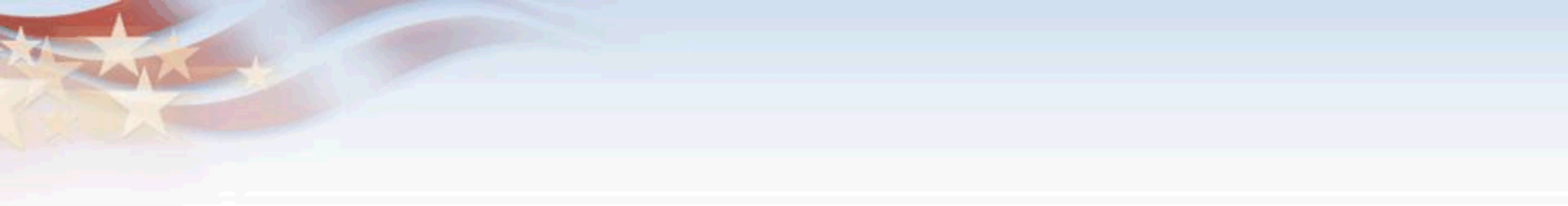
1. Genetic algorithms

- Inspired by evolutionary biology
- Search is unbiased
- Search by population
- Uniqueness check by changing random seed
- Quickly find good solution

2. Levenberg-Marquardt

- Non-linear least squares minimization
- Quick convergence from good solution





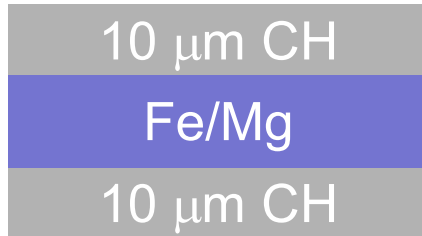
Condition analysis



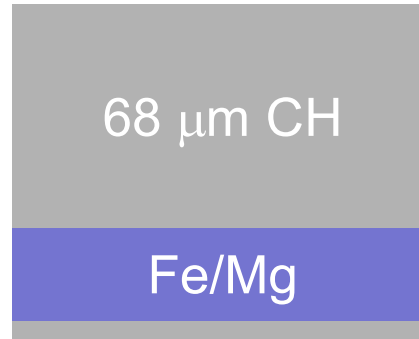
Density controlled by CH tamper thickness

Uniformity measured by Mg and Al dopants

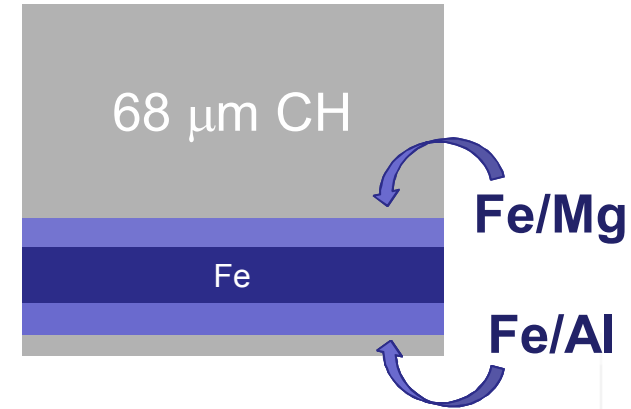
Low density



High density



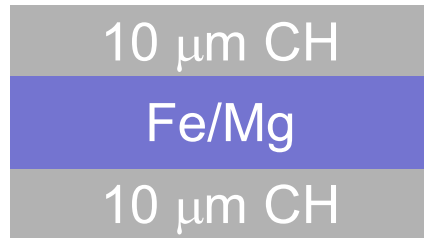
Uniformity



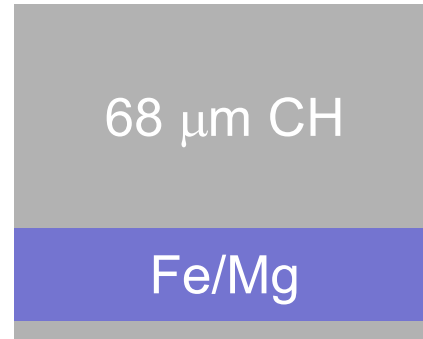
Density controlled by CH tamper thickness

Uniformity measured by Mg and Al dopants

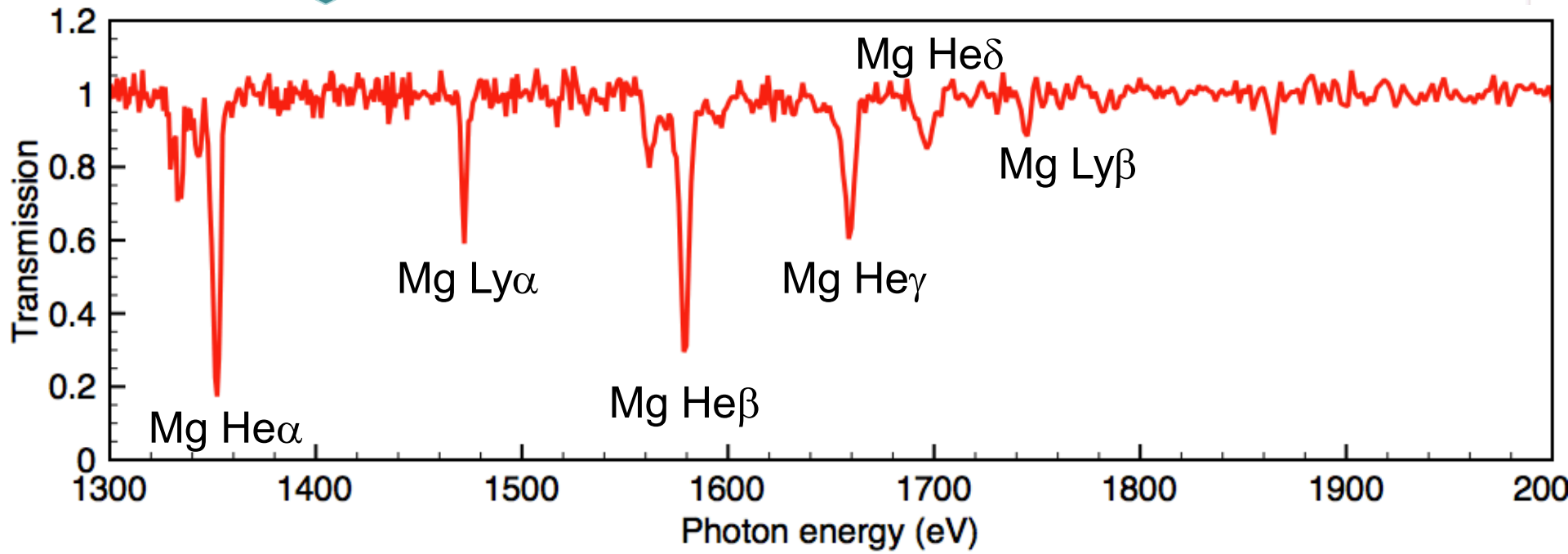
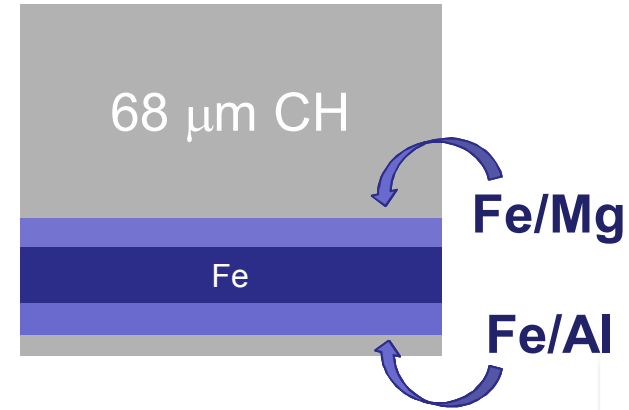
Low density



High density



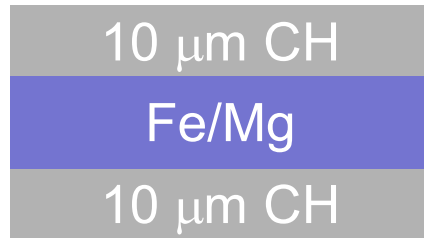
Uniformity



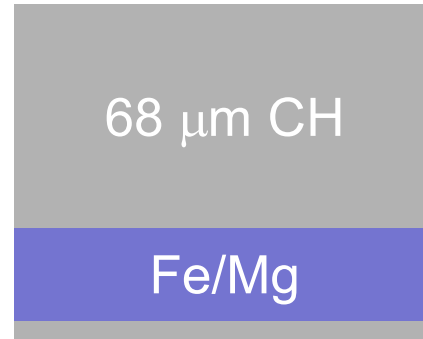
Density controlled by CH tamper thickness

Uniformity measured by Mg and Al dopants

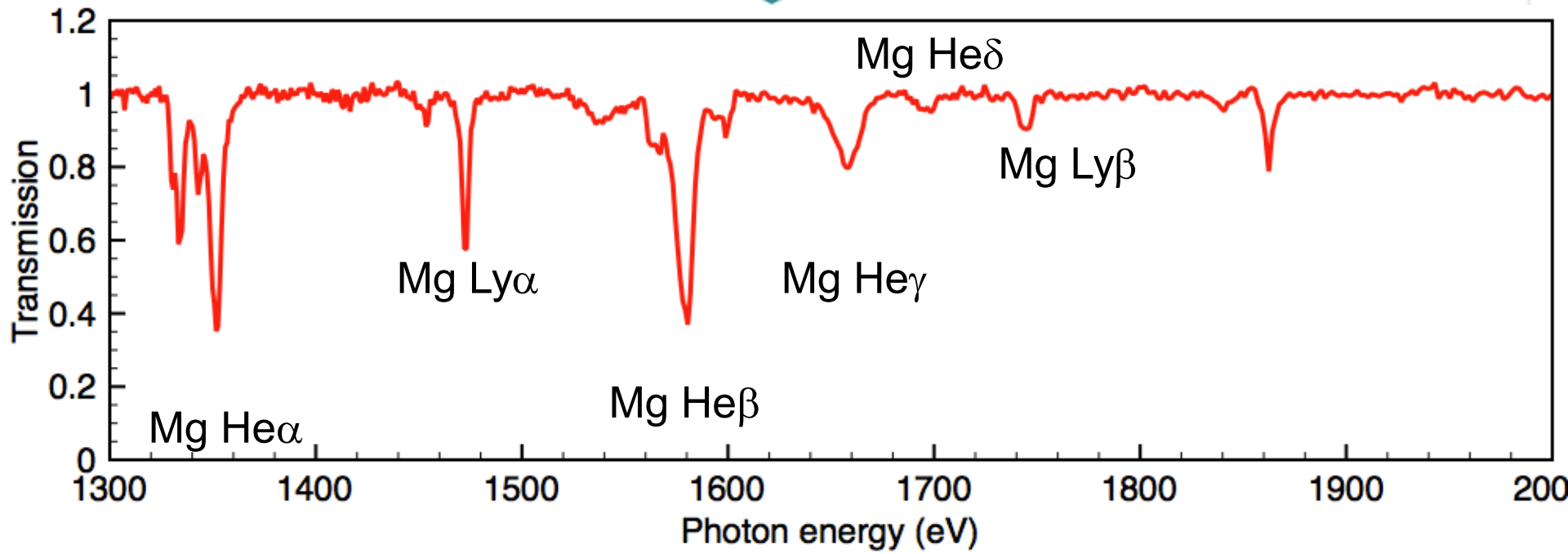
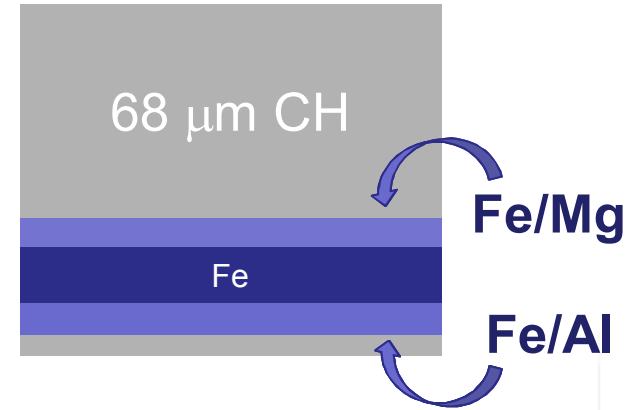
Low density



High density



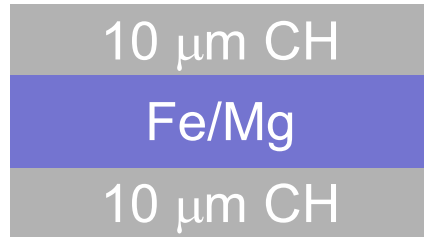
Uniformity



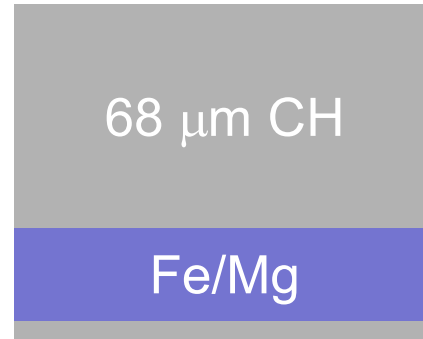
Density controlled by CH tamper thickness

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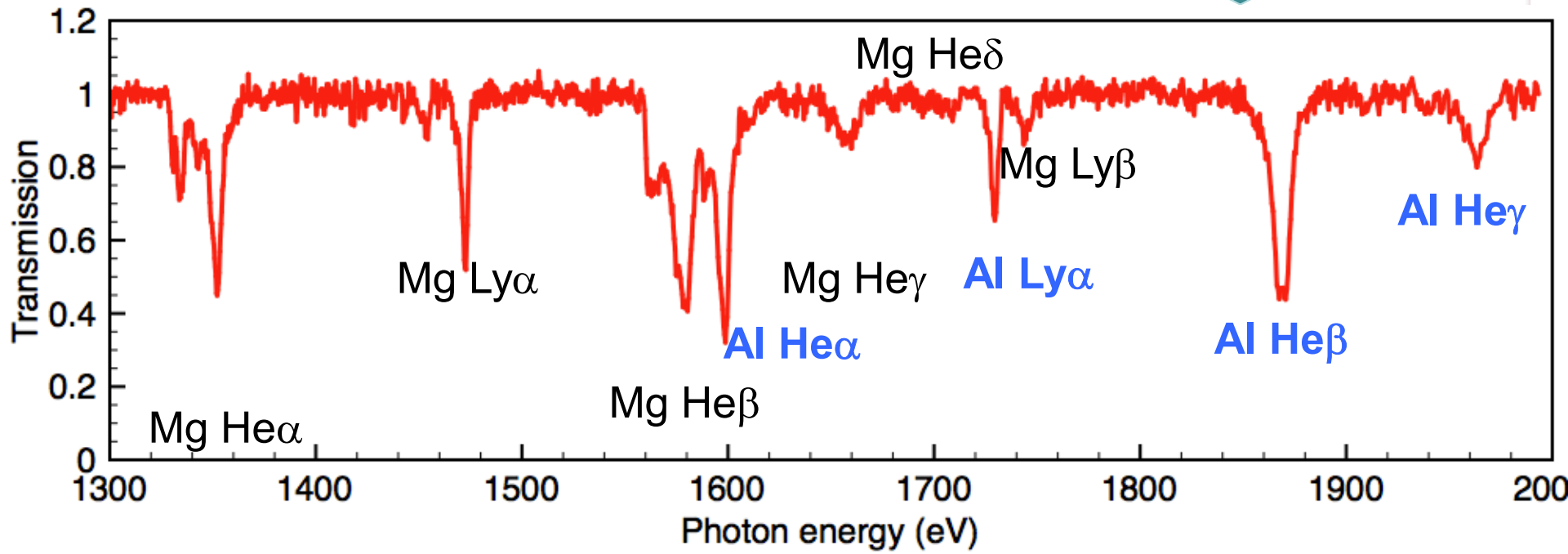
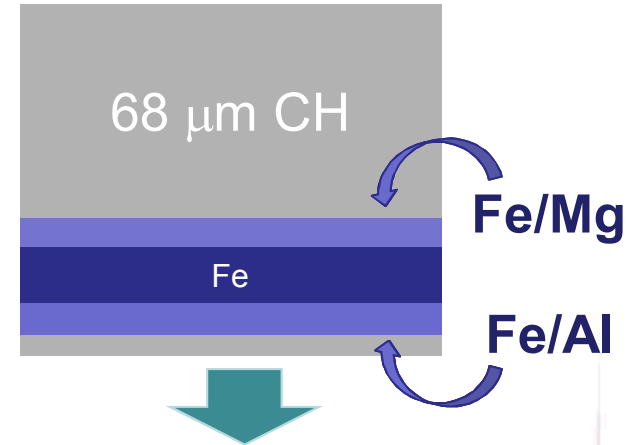
Low density



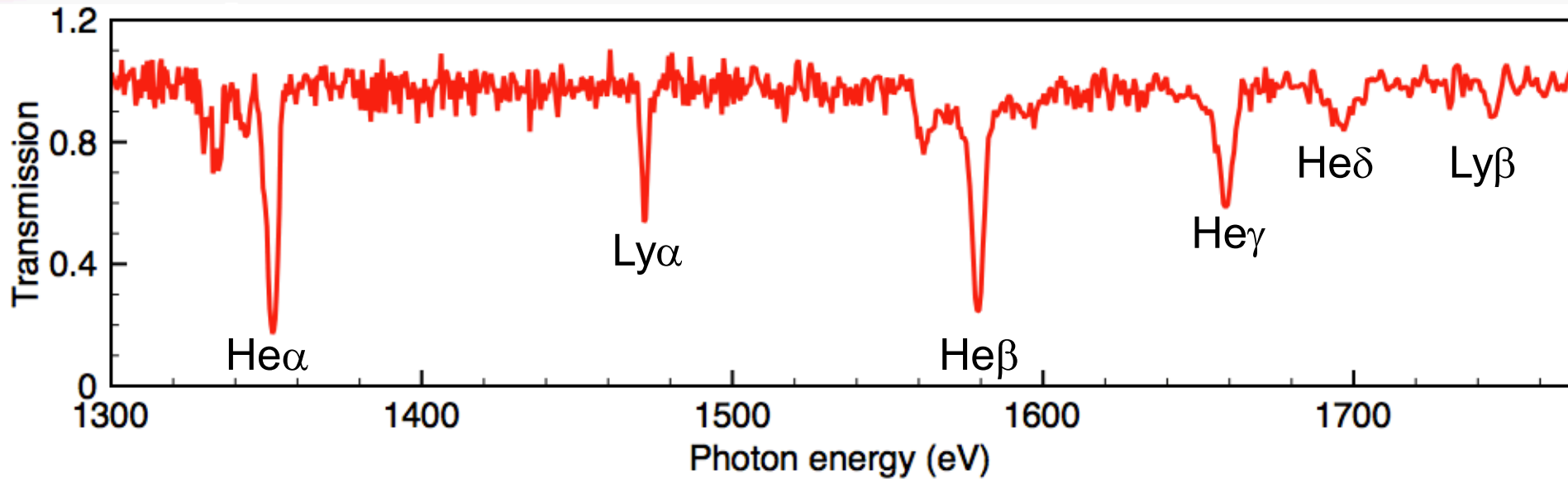
High density



Uniformity



Analysis of low density data gives
 $T_e = 164 \text{ eV}$ and $n_e = 7.91 \times 10^{21} \text{ cm}^{-3}$



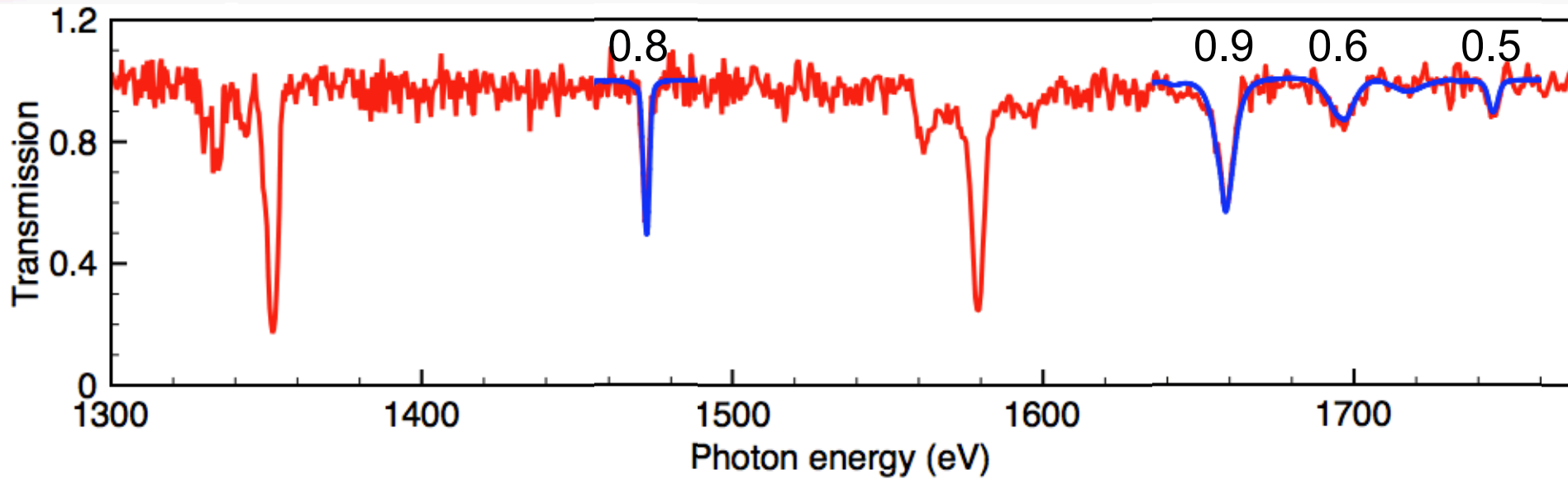
10 μm CH

Fe/Mg

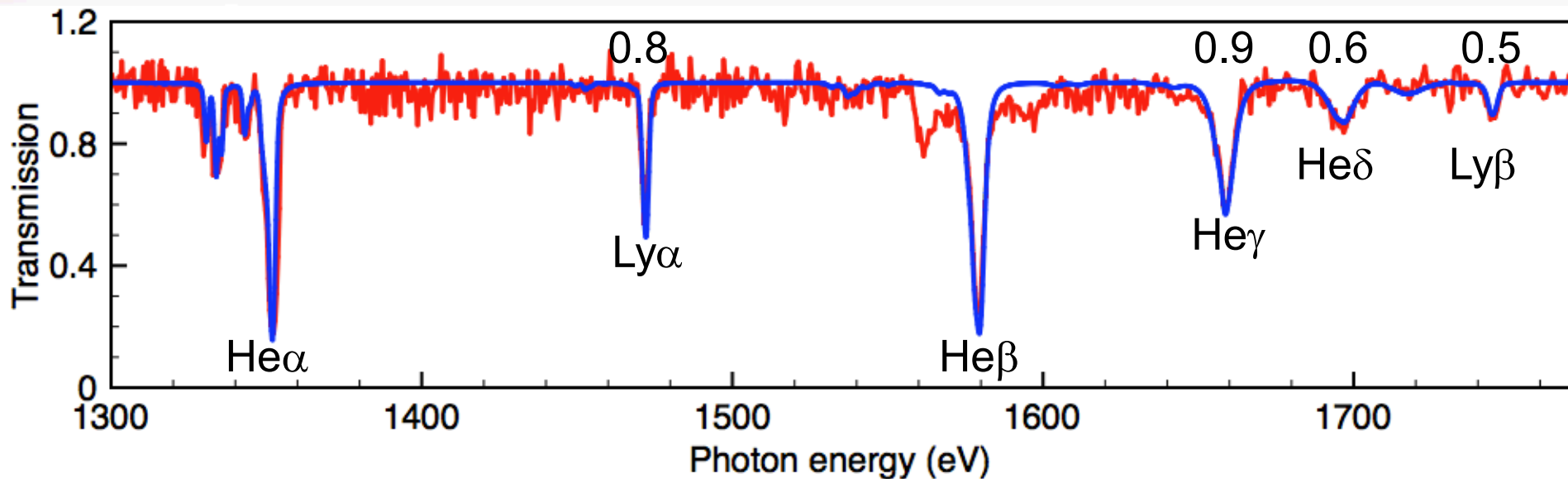
10 μm CH



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Analysis of low density data gives $T_e=164$ eV and $n_e=7.91 \times 10^{21} \text{ cm}^{-3}$



- Fitted lines: Mg He γ and Ly β

- $\diamond T_e=164 \pm 5$ eV

- $\diamond n_e=(7.91 \pm 1.92) \times 10^{21} \text{ cm}^{-3}$

- $\diamond \rho L=(3.30 \pm 0.35) \times 10^{-5} \text{ g/cm}^2$

- Model shows good agreement to all the lines

- \rightarrow Atomic data used is consistent with the data

- Inferred areal density agrees to Rutherford Back Scattering (RBS) measurements

- Measured areal density: $3.01 \times 10^{-5} \text{ g/cm}^2$

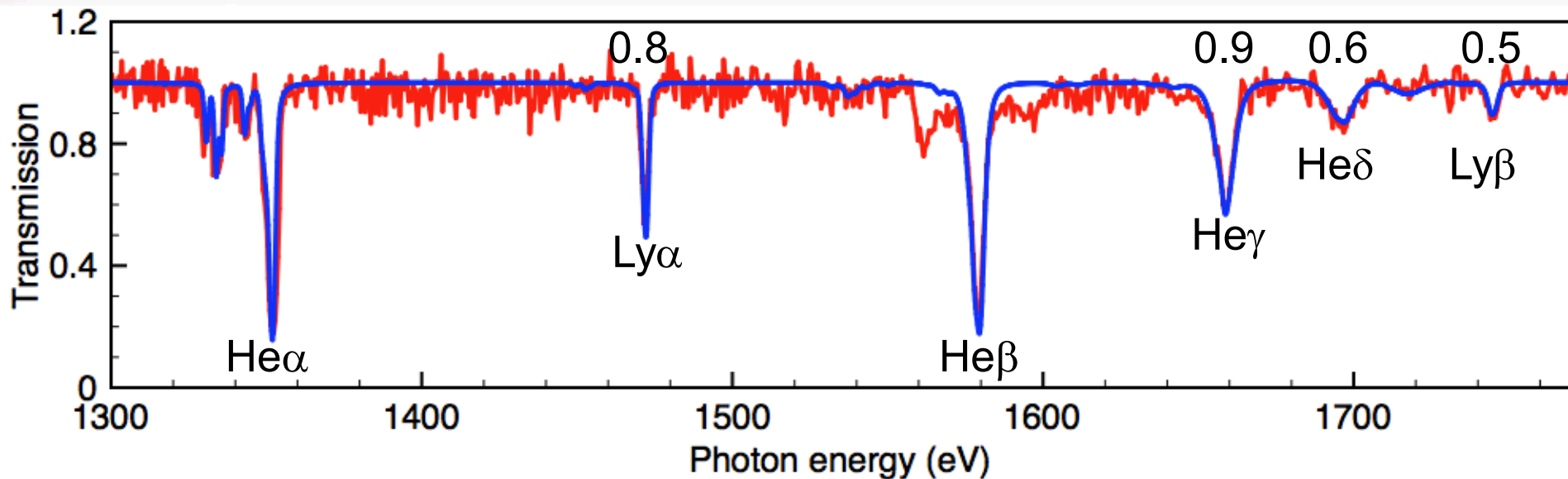
10 μm CH

Fe/Mg

10 μm CH



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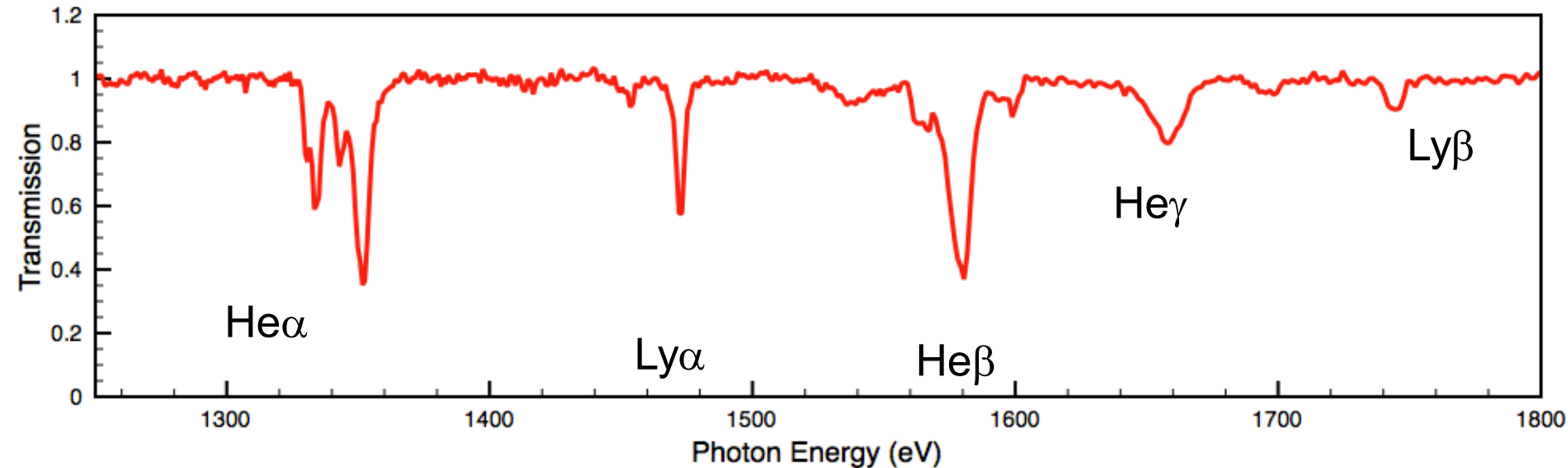
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10 μm CH
Fe/Mg
10 μm CH

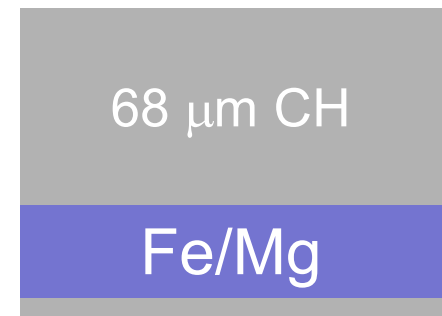


Analysis of high density data gives $T_e = 195 \text{ eV}$ and $n_e = 4.06 \times 10^{22} \text{ cm}^{-3}$

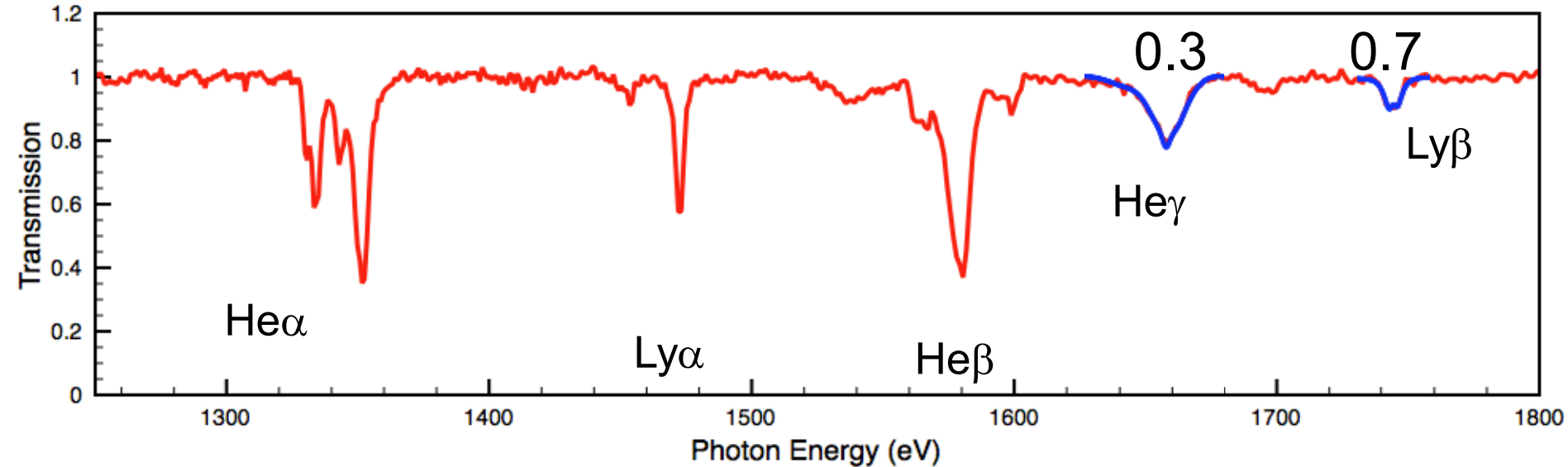


- Fitted lines: Mg He γ and Ly β
 - ✧ $T_e = 195 \pm 3 \text{ eV}$
 - ✧ $n_e = (4.06 \pm 0.62) \times 10^{22} \text{ cm}^{-3}$
 - ✧ $\rho L = (4.88 \pm 0.58) \times 10^{-5} \text{ g/cm}^2$

- Inferred areal density agrees to RBS measurements
 - Measured areal density: $5.00 \times 10^{-5} \text{ g/cm}^2$

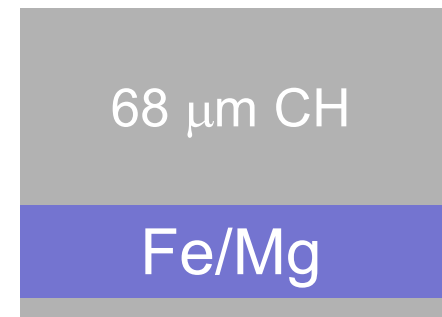


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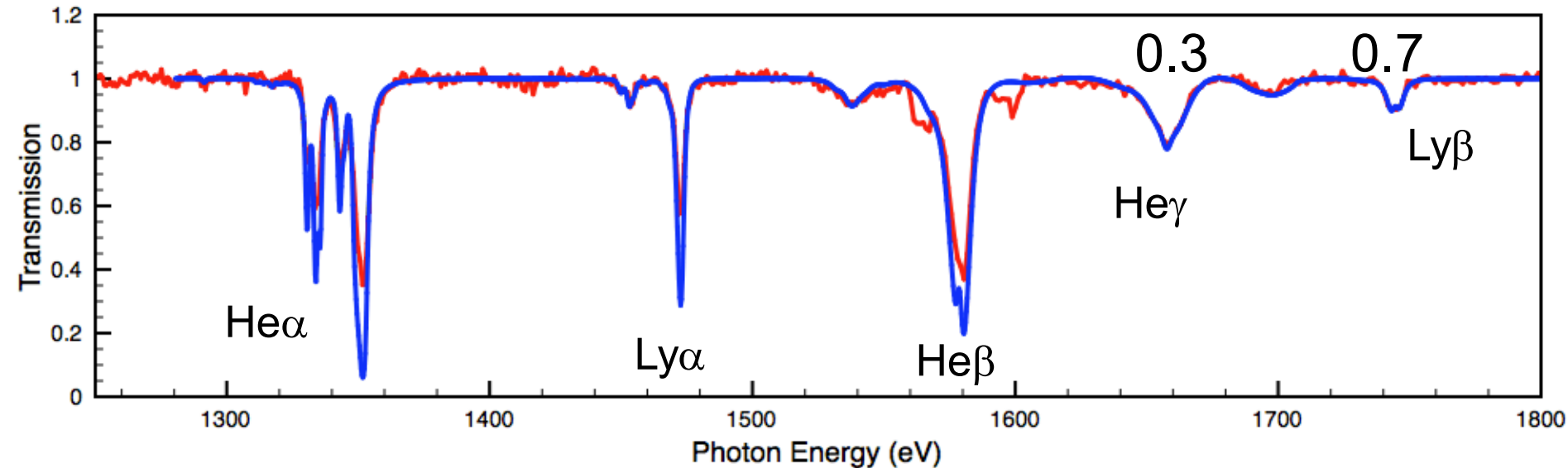


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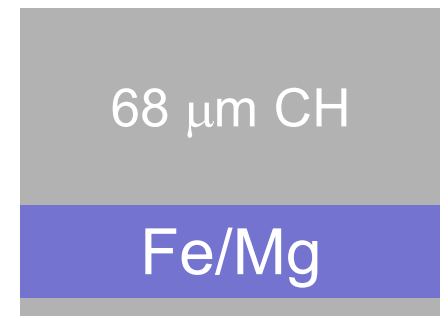


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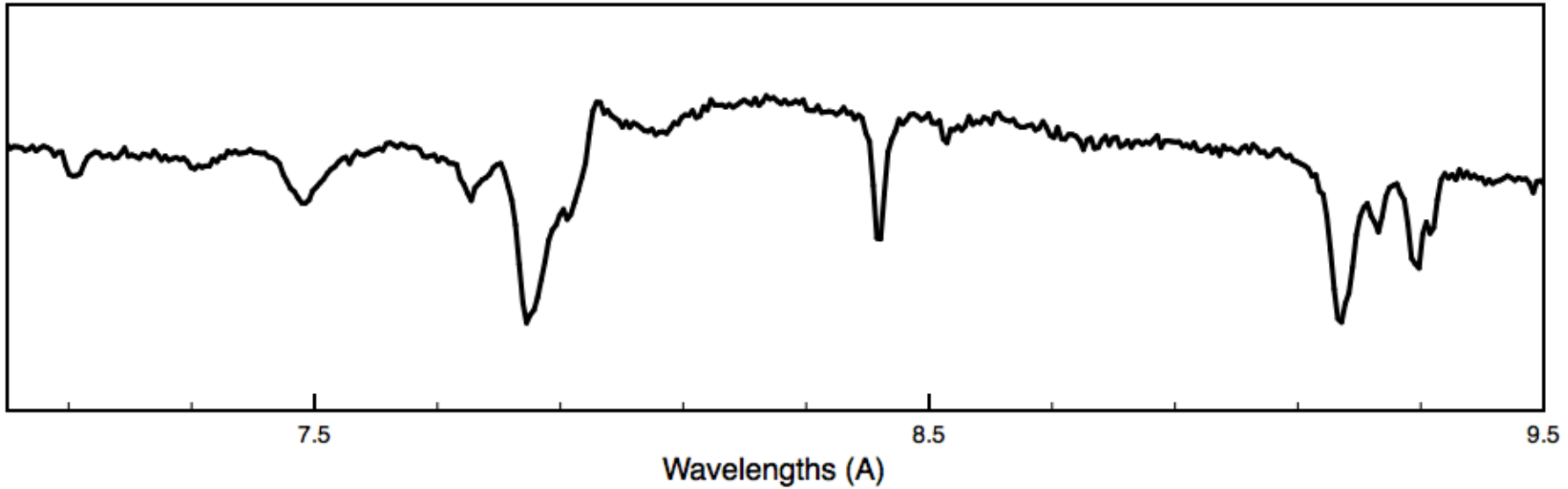


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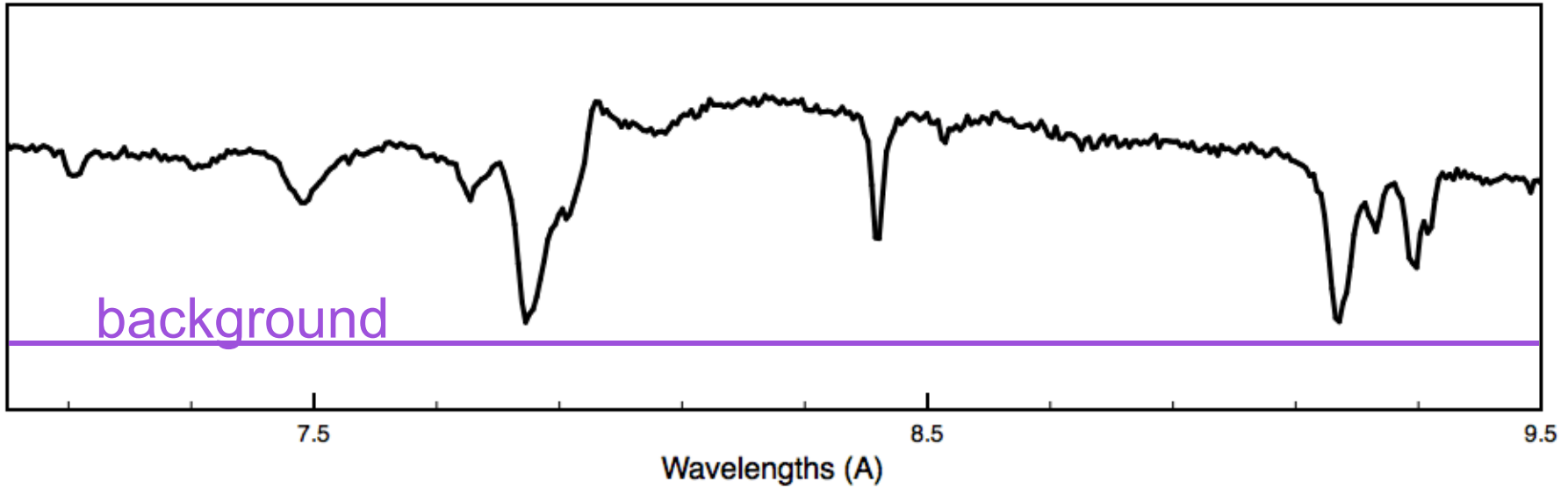
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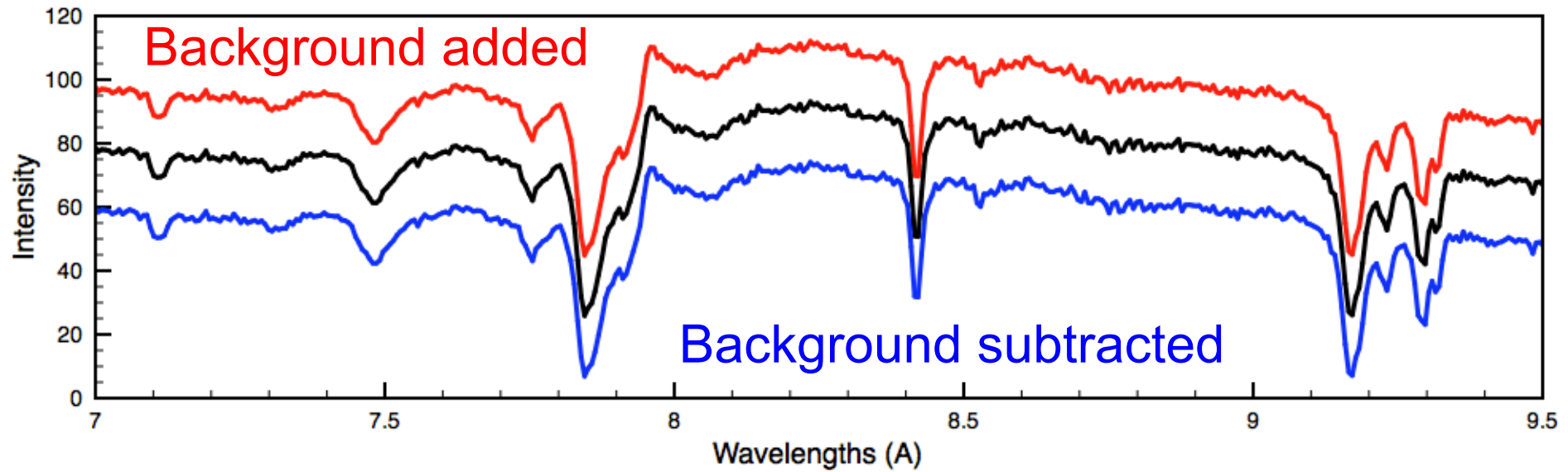
How does the additional background change the analysis results?



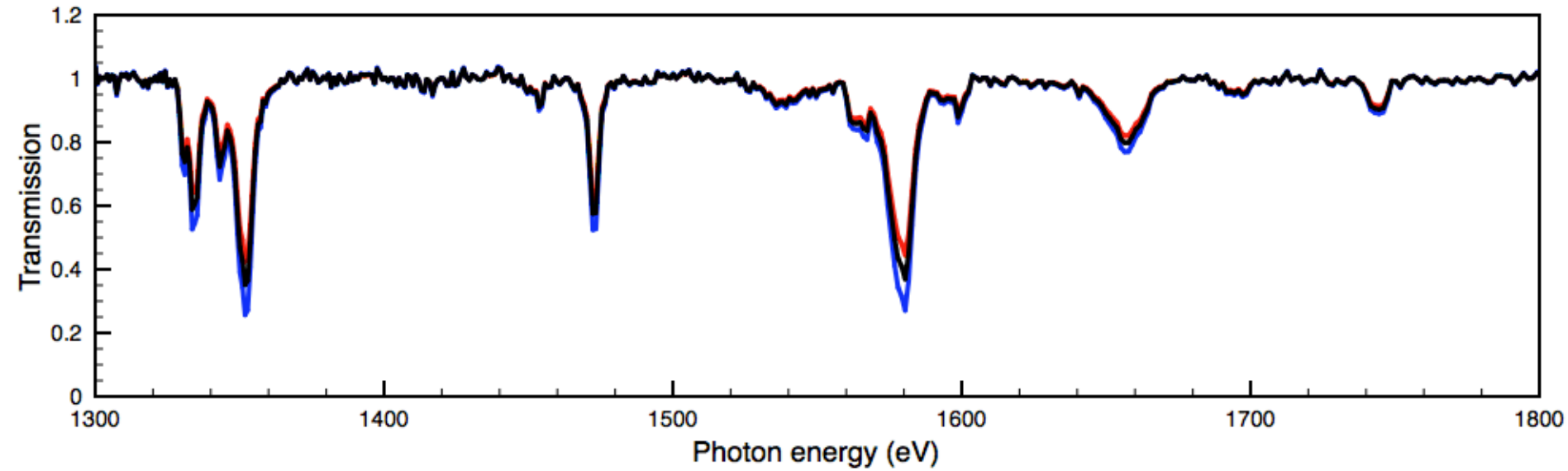
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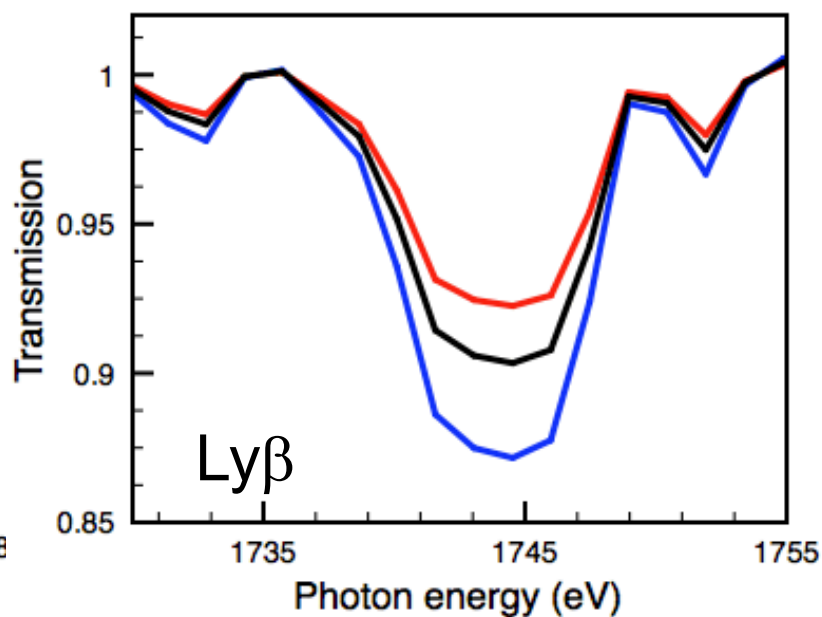
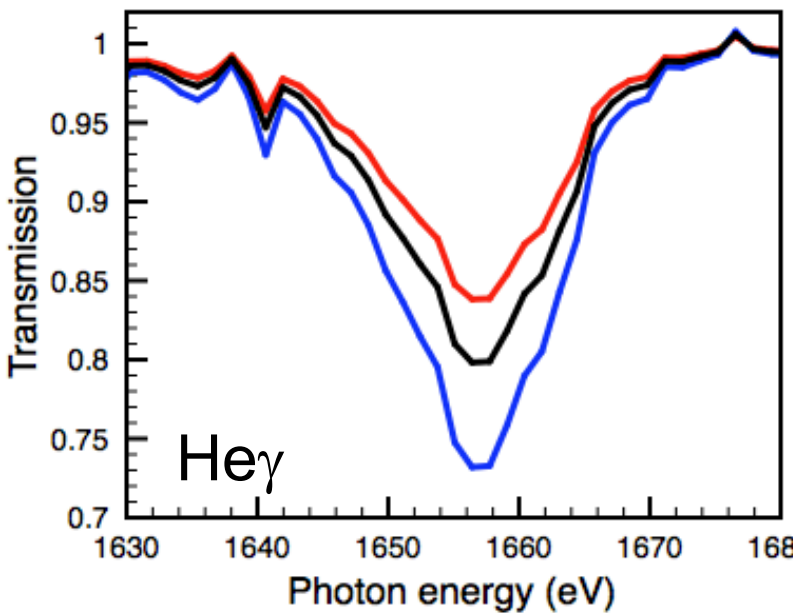
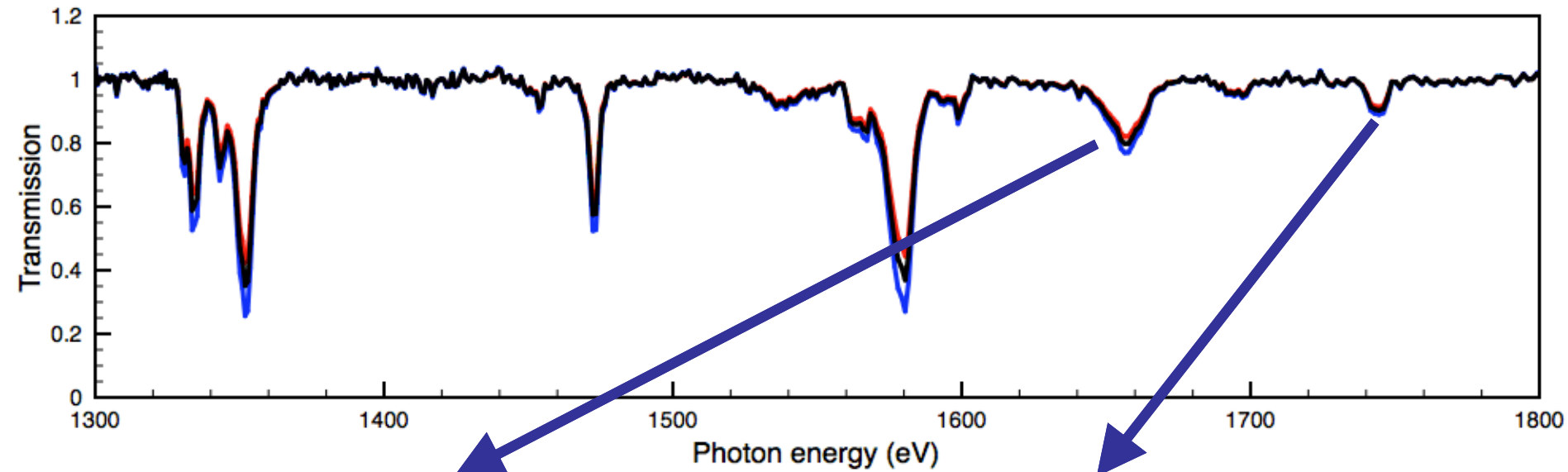
How does the additional background change the analysis results?



How does the additional background change the analysis results?



How does the additional background change the analysis results?



How does the additional background change the analysis results?

	T_e [eV]	n_e [10^{22} e/cc]	ρL [10^{-5} g/cm ²]
BG added	195	4.2	3.9
ORIGINAL	195±3	4.1±0.6	4.9±0.6
BG subtracted	194	4.0	6.6

- Analysis of T_e and n_e using $Ly\beta$ and $He\gamma$ lines are quite robust against background
- Inferred areal density changes due to background
- Areal density values measured prior to the experiment are closest to the one inferred from the original data (i.e. 5.00×10^{-5} g/cm²)



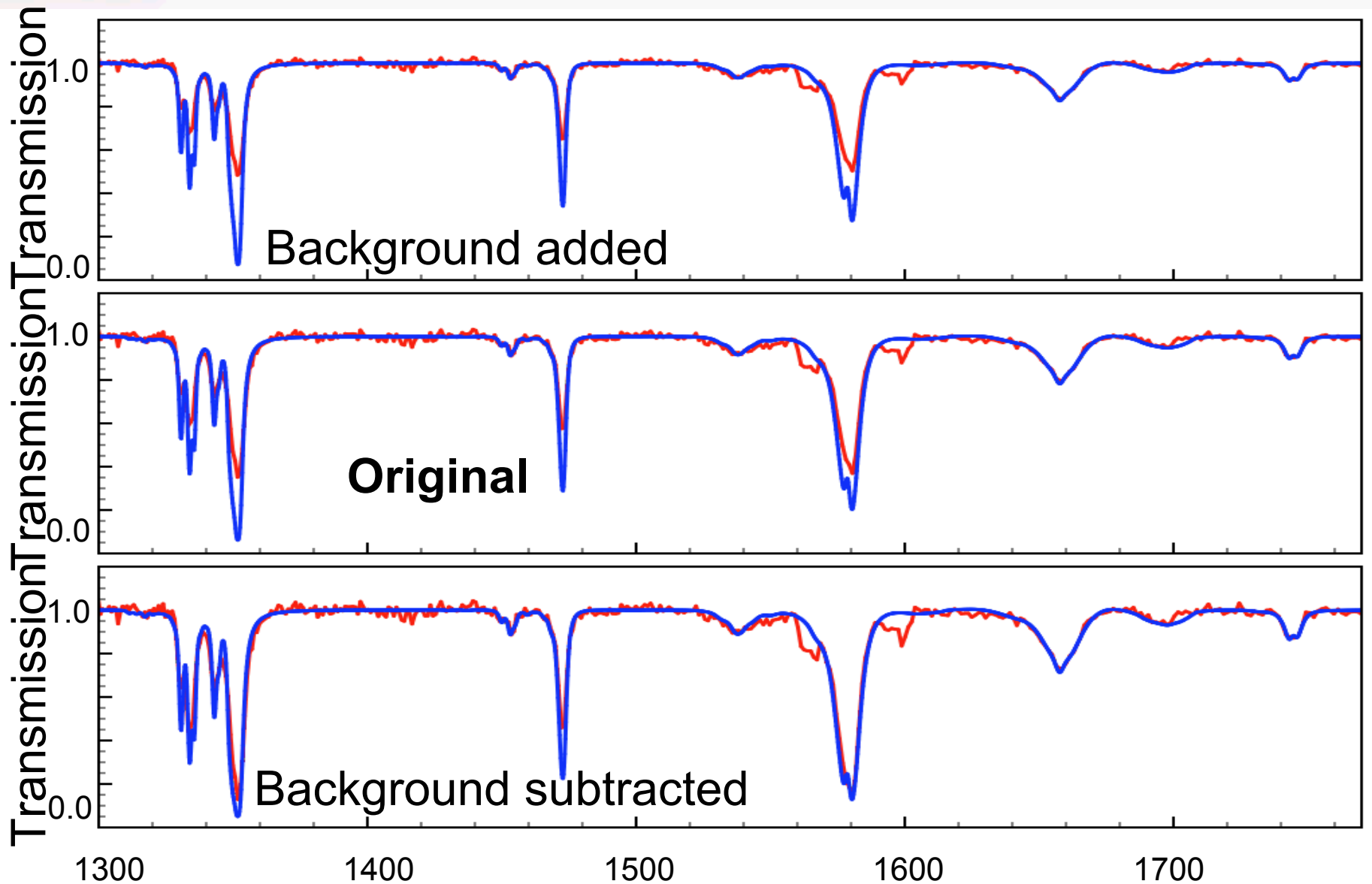
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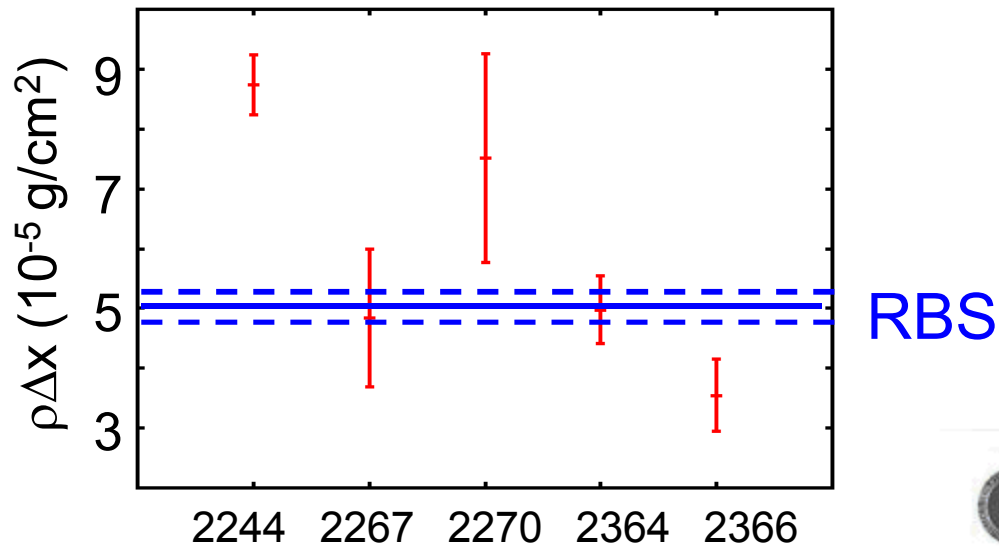
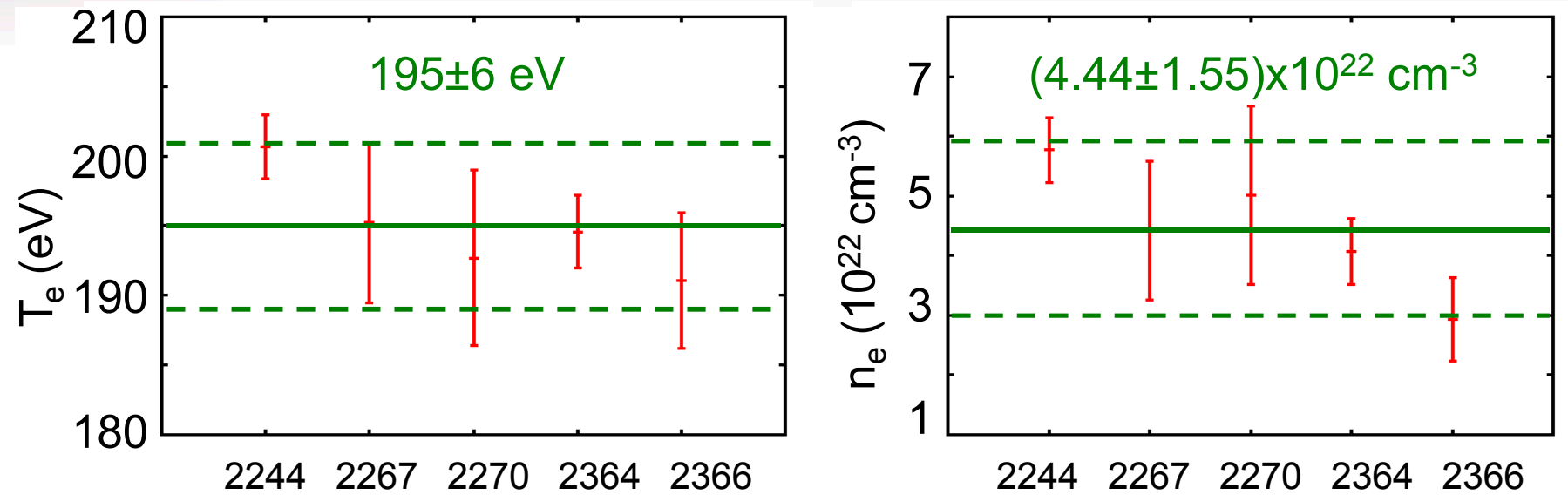
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How does the additional background change the analysis results?

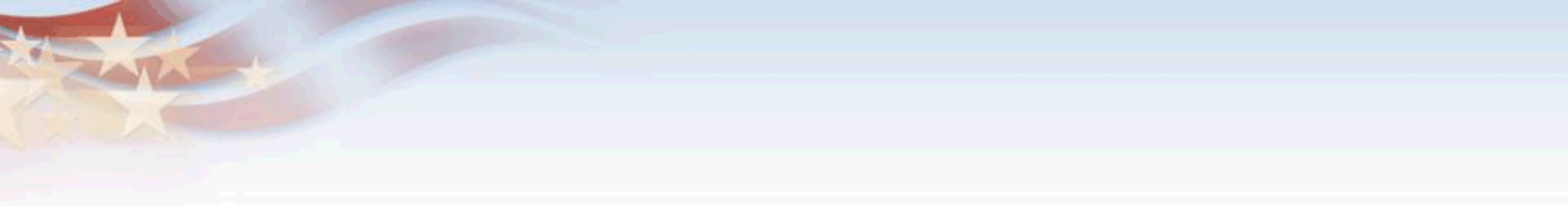


Condition reproducibility on high density data is $T_e = \pm 3\%$ and $n_e = \pm 33\%$



RBS



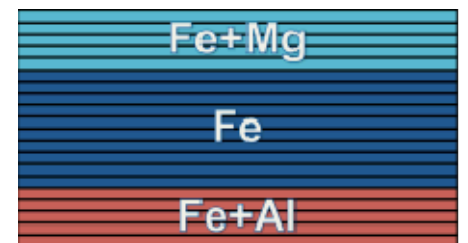
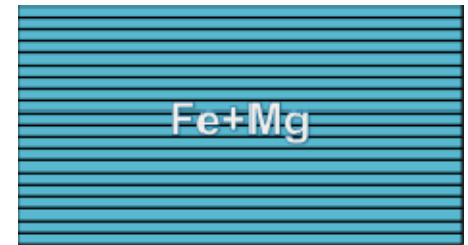


Uniformity analysis



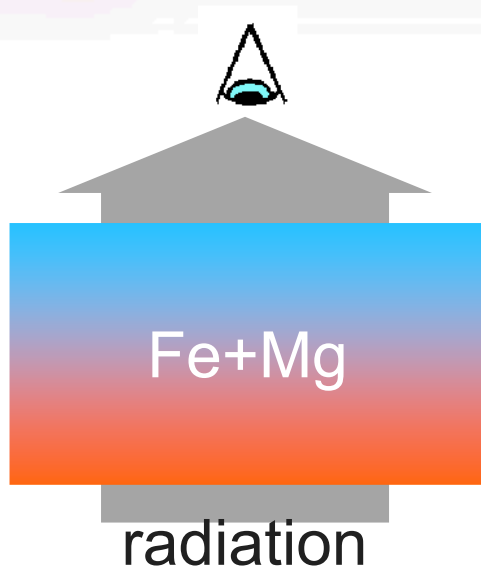
We can model gradient. ...but, does it work?

- Too many constraints will end up in non-unique solution
- Questions
 1. How does χ^2 deteriorates due to non-uniformity?
 2. How does the gradient model work on Fe+Mg sample?
 3. How does the gradient model work on Fe+Mg+Al sample?



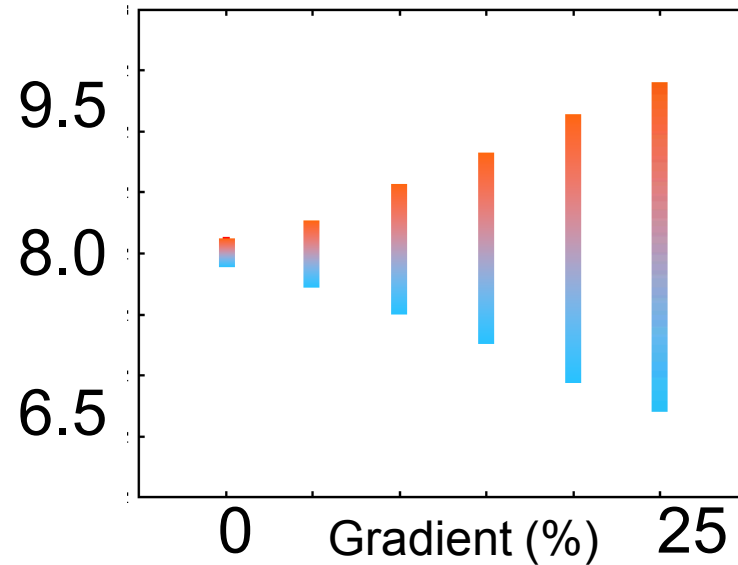
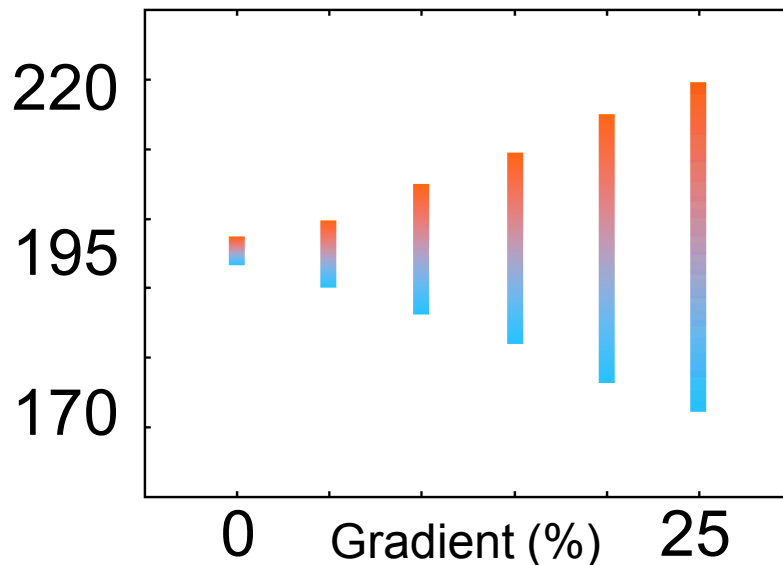
Can be studied synthetically!

How does χ^2 deteriorates due to non-uniformity?

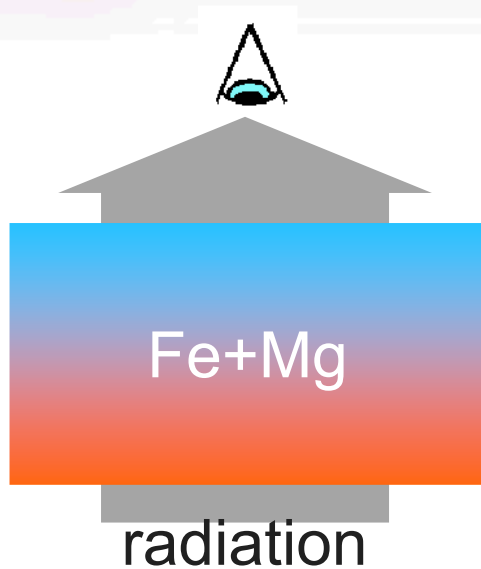


For 0% - 25 % gradient

1. Compute synthetic spectrum
2. Add some noise
3. Analyze the spectrum with uniform model

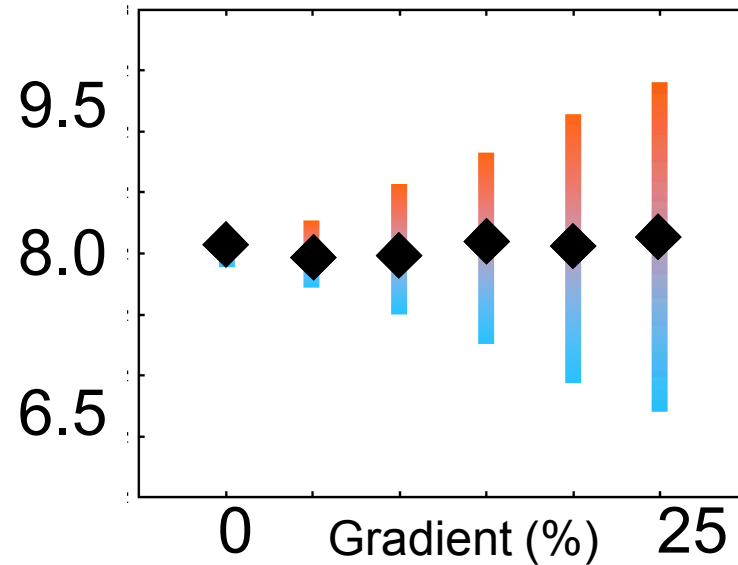
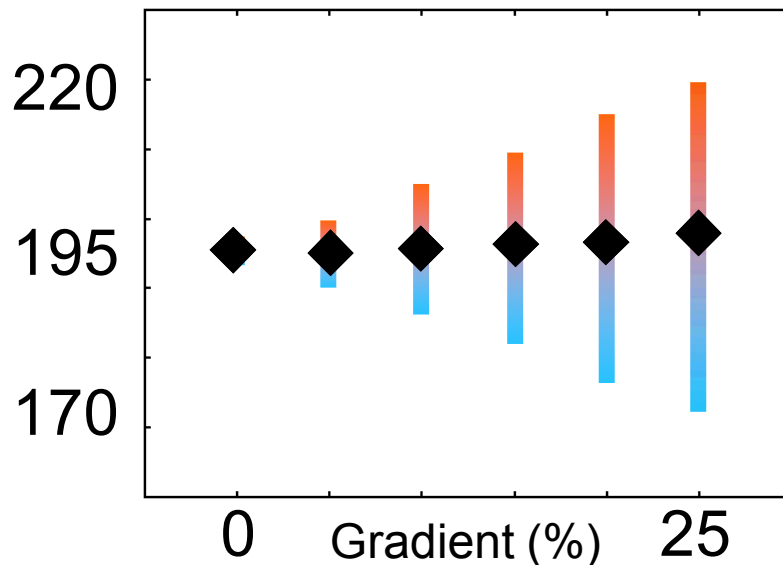


How does χ^2 deteriorates due to non-uniformity?



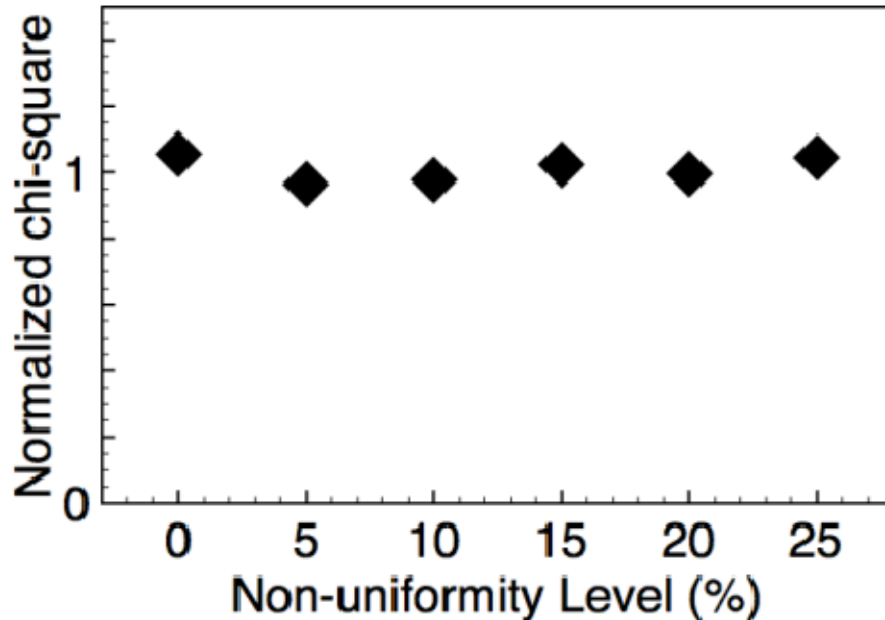
For 0% - 25 % gradient

1. Compute synthetic spectrum
2. Add some noise
3. Analyze the spectrum with uniform model

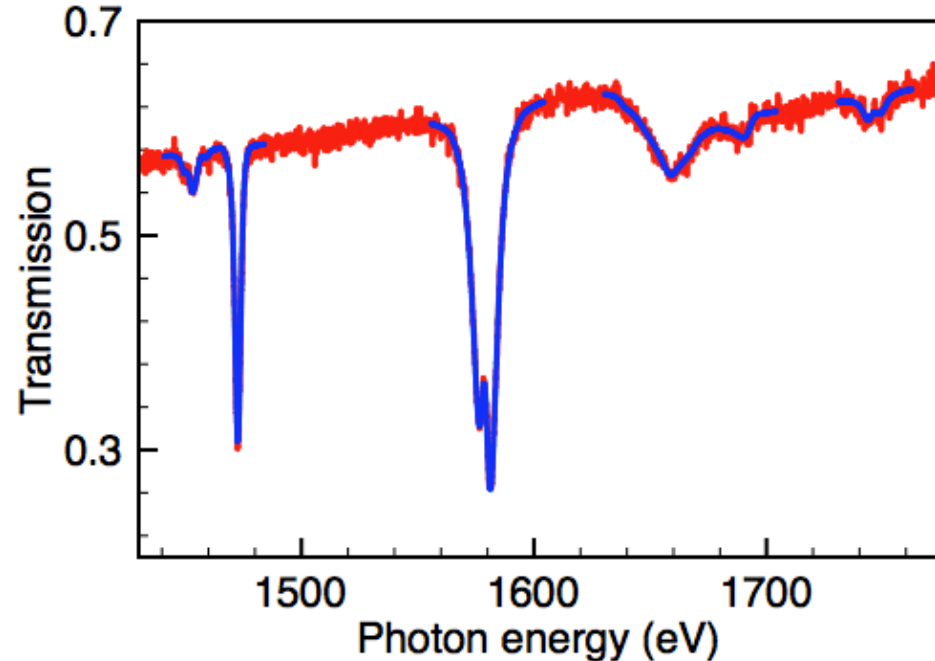


How does χ^2 deteriorates due to non-uniformity?

χ^2



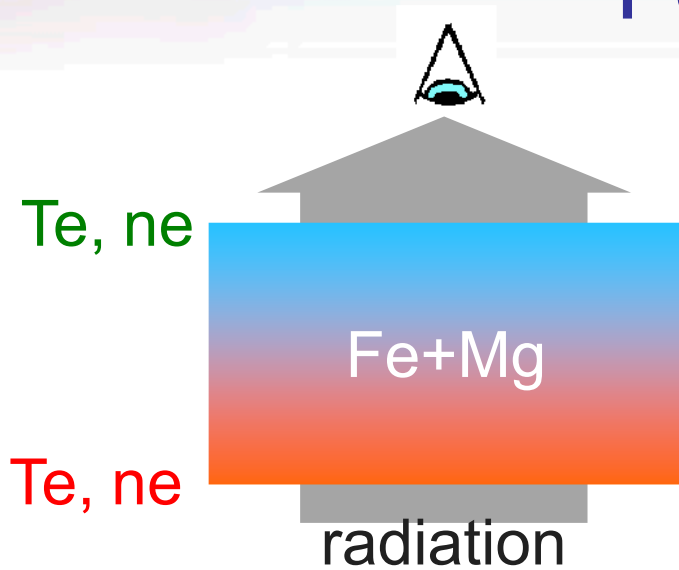
Fits for 25% non-uniformity



- Uniform model with the sample average can provide good fits even if there is a non-uniformity



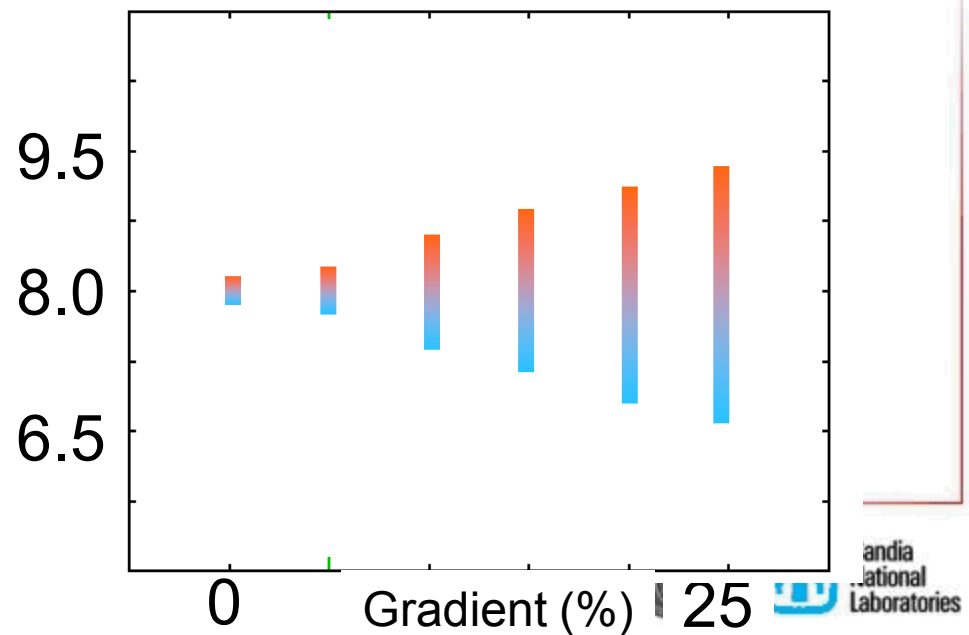
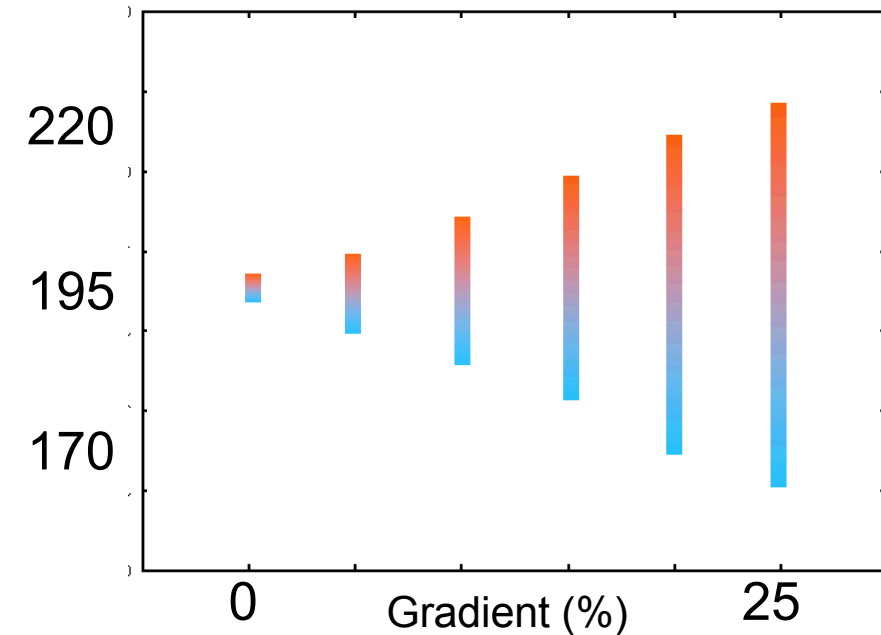
How does the gradient model work for Fe+Mg sample?



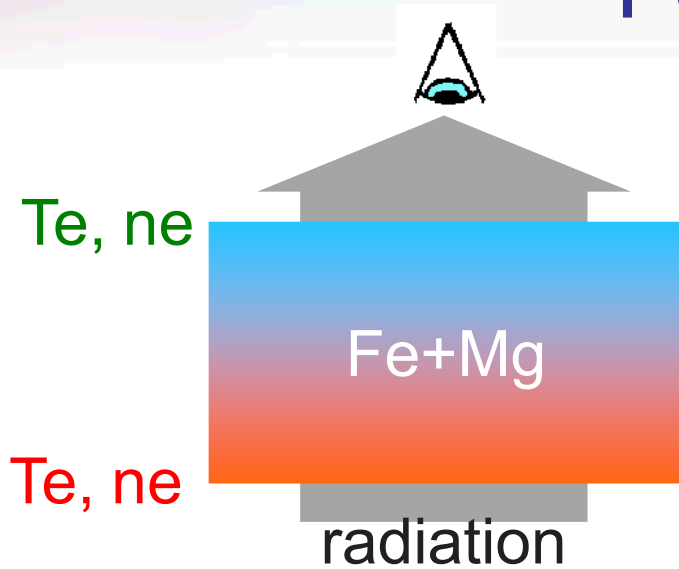
Gradient model calculation

1. For given condition on both sides, compute linear gradient
2. Numerically integrate radiation transport for mixture of Fe and Mg

PGALM+Gradient model finds (Te, ne) and (Te, ne) that optimize the fits



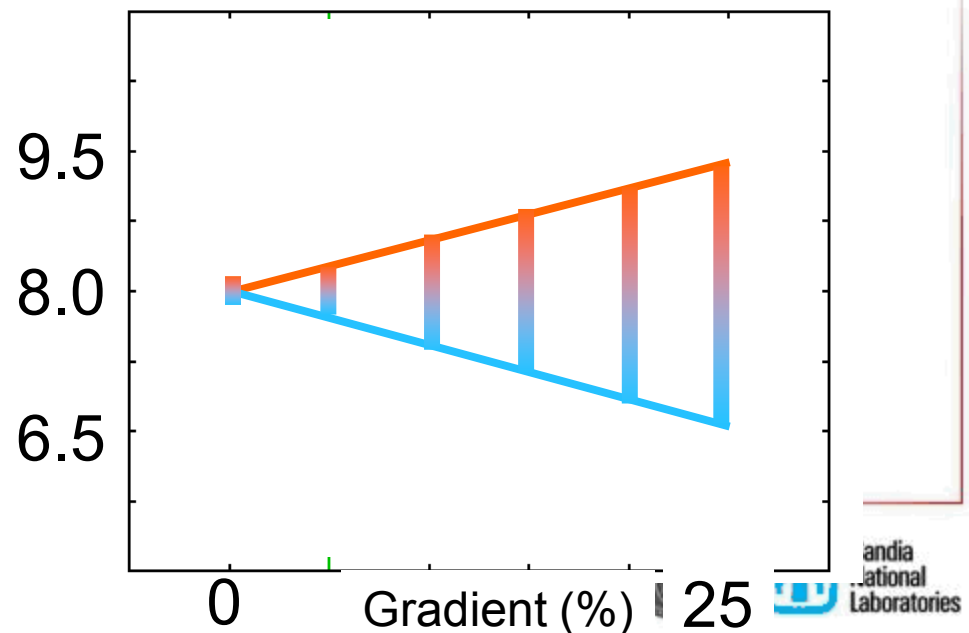
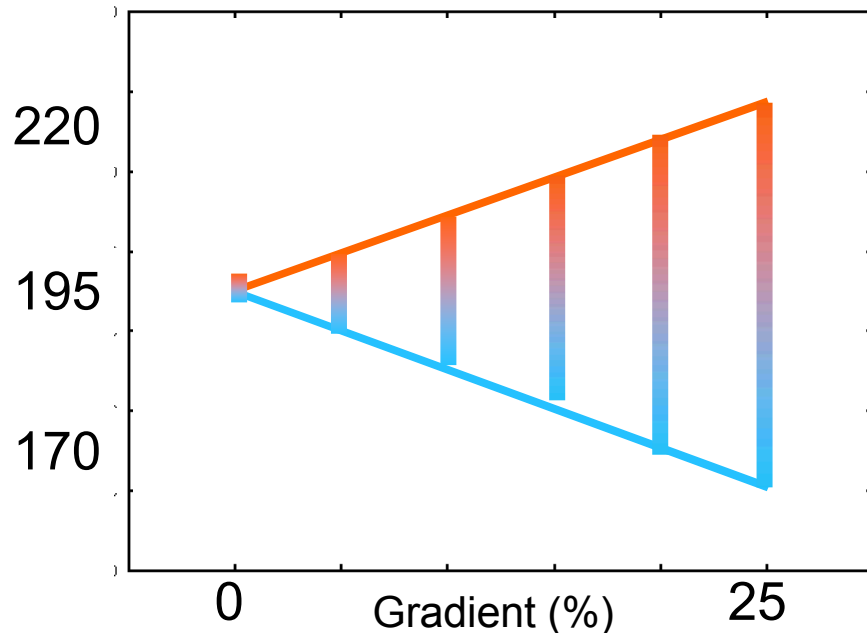
How does the gradient model work for Fe+Mg sample?



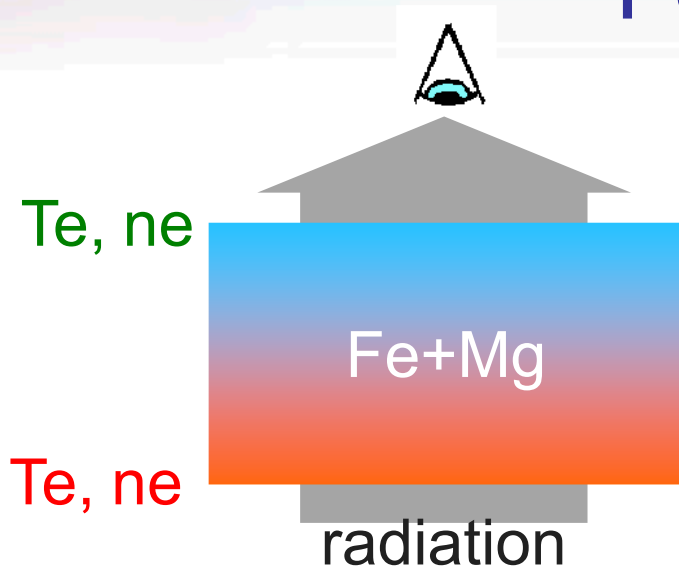
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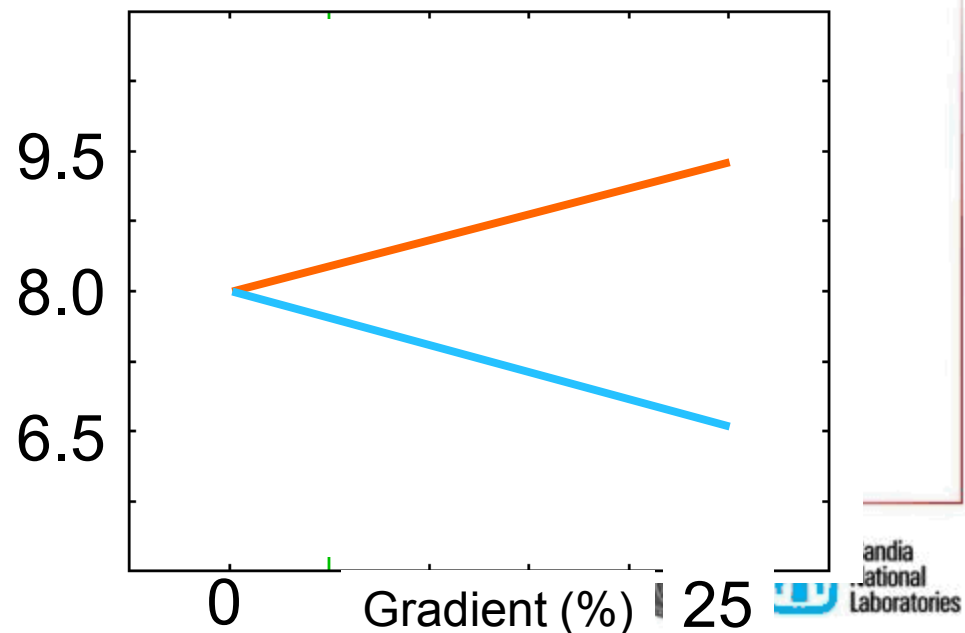
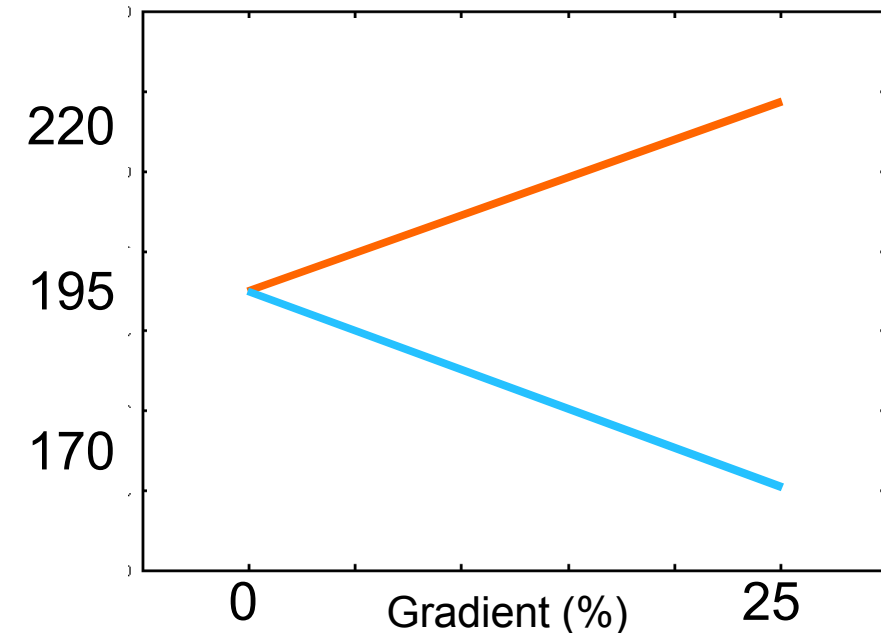
How does the gradient model work for Fe+Mg sample?



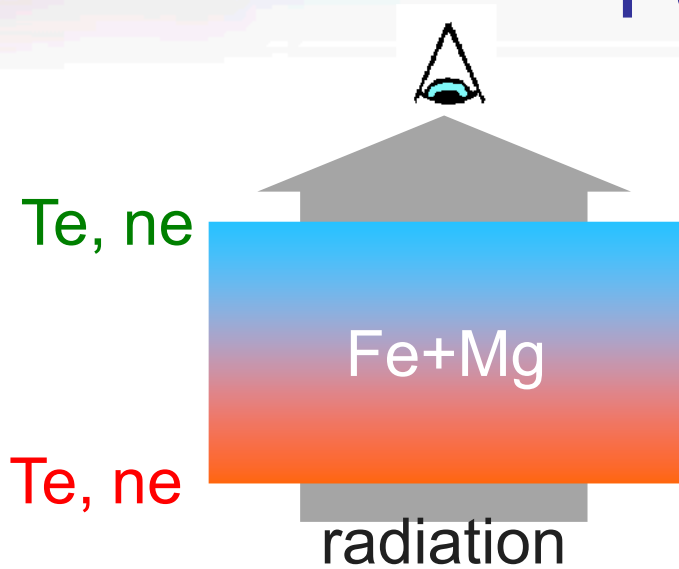
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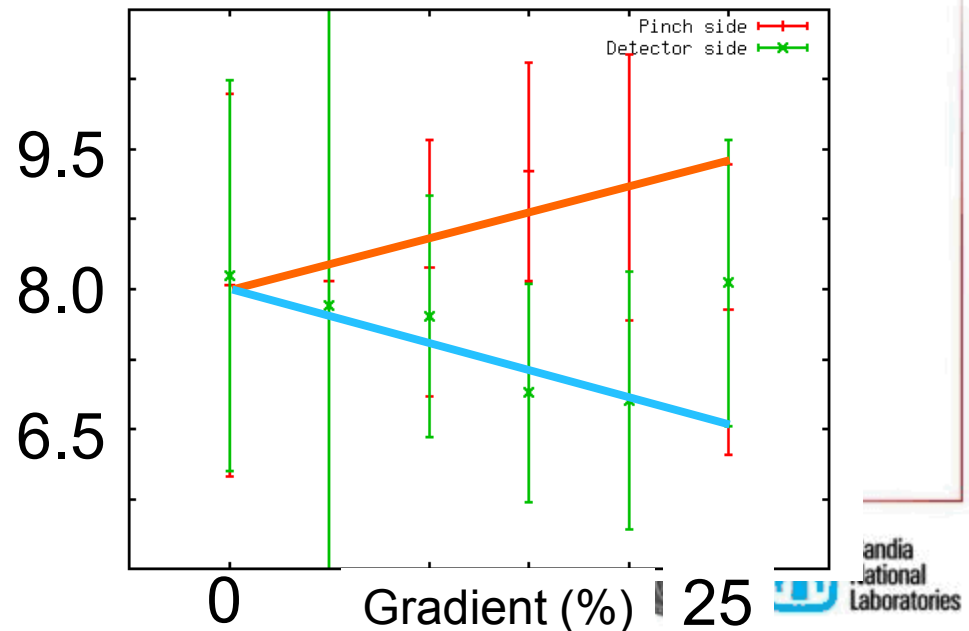
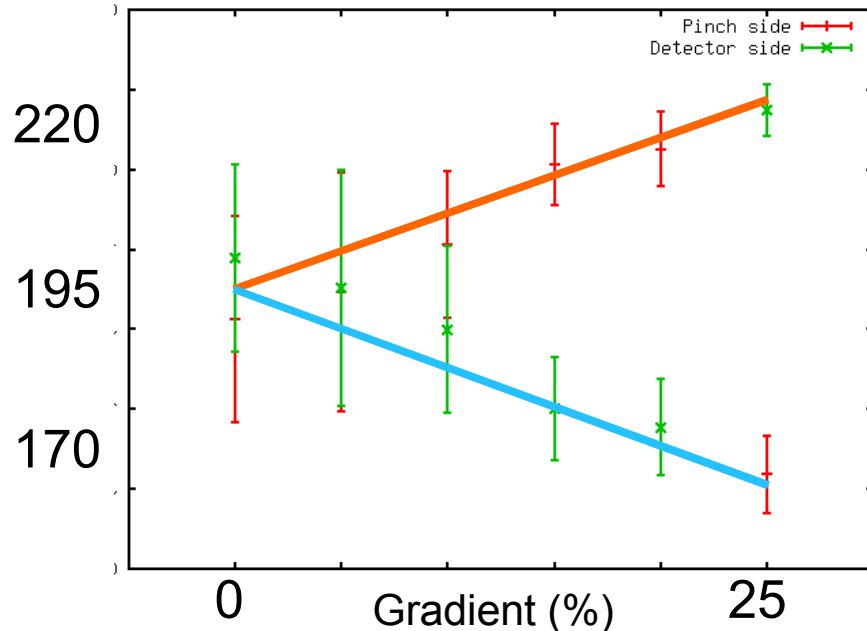
How does the gradient model work for Fe+Mg sample?



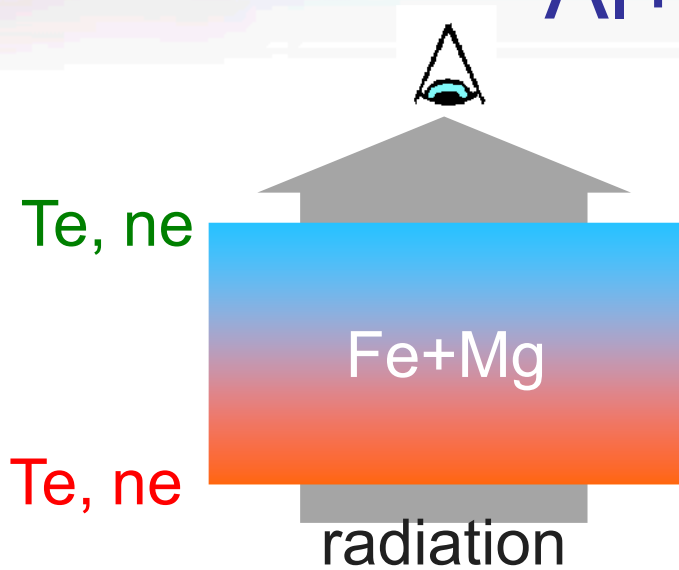
Gradient model calculation

1. For given condition on both sides, compute linear gradient
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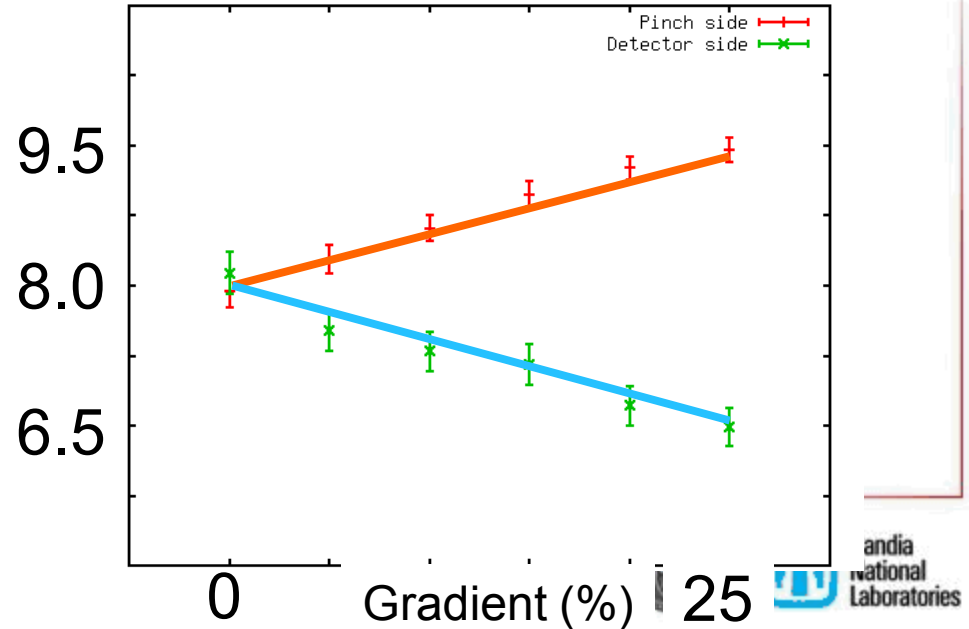
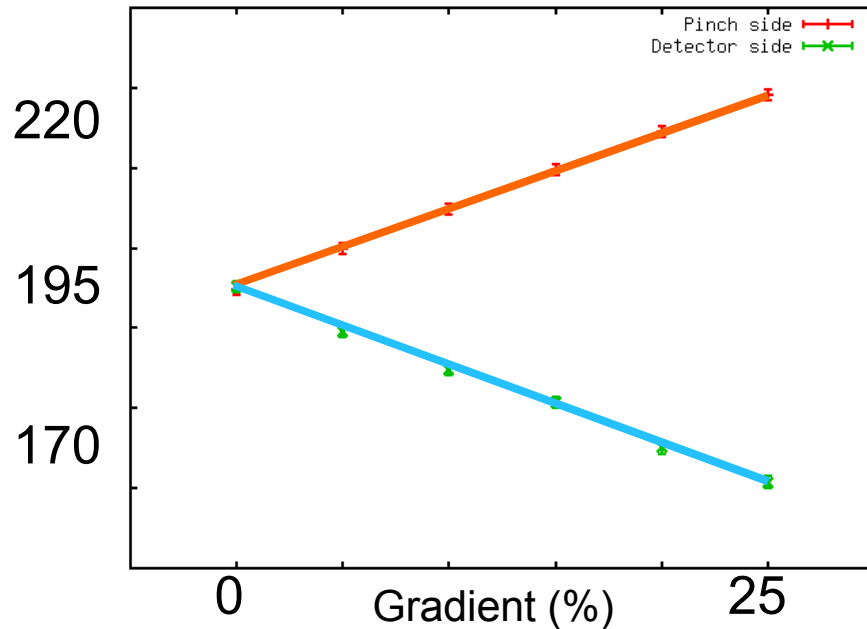
How does the gradient model work for Al+Fe+Mg sample?



Gradient model calculation

1. For given condition on both sides, compute linear gradient
2. Numerically integrate radiation transport for mixture of Al+Fe+Mg

PGALM+Gradient model finds (Te, ne) and (Te, ne) that optimize the fits

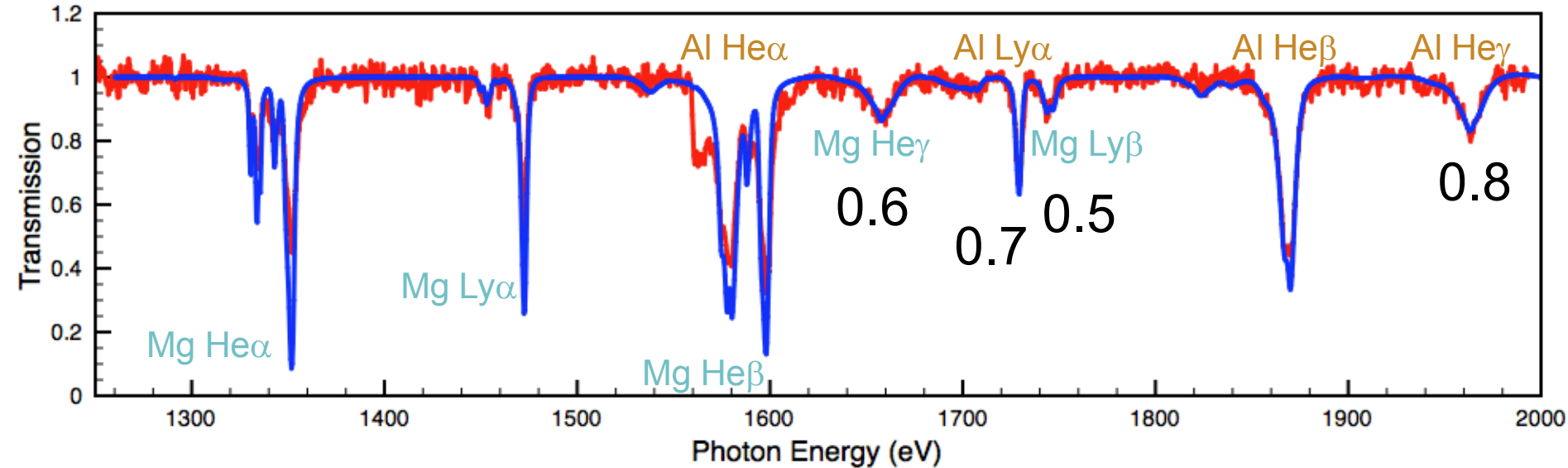


Summary of synthetic study on non-uniformity analysis

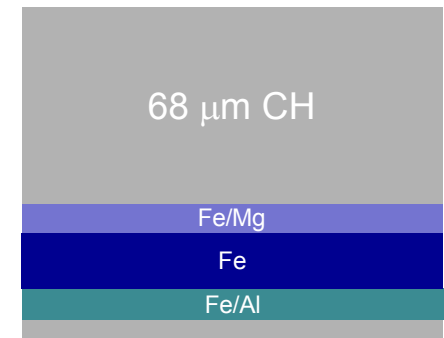
- Uniform model can fit data through non-uniform condition with average conditions
- Gradient model on Fe+Mg sample
 - Average density is reliable
 - Te gradient could be extracted when gradient is larger than 10%, but fails to find gradient direction
- Gradient model on Al+Fe+Mg sample
 - Find gradient very precisely



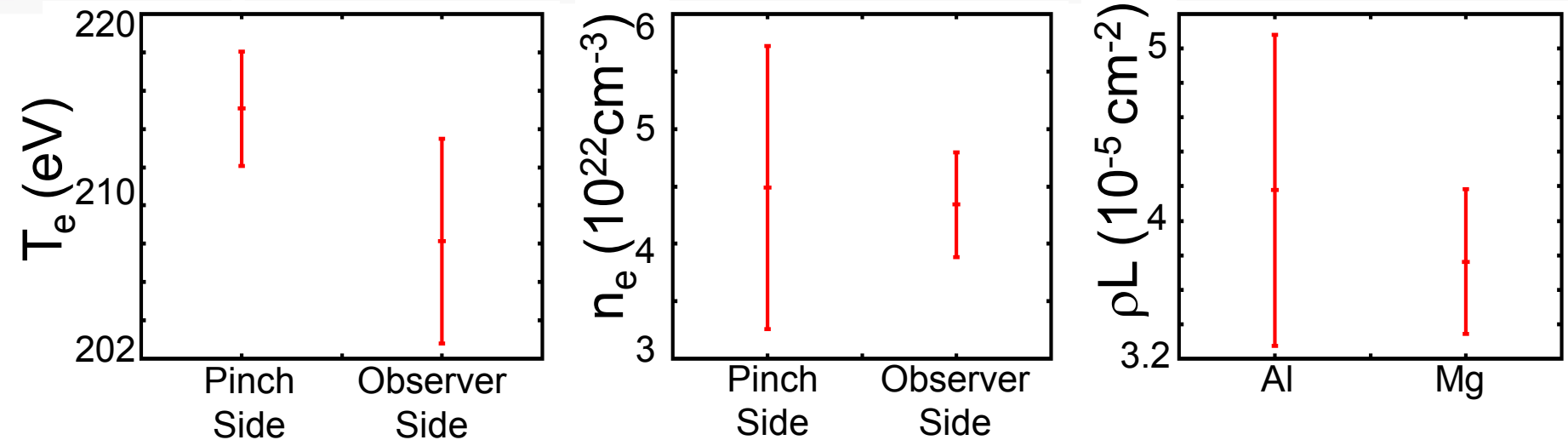
Direct uniformity measurement confirmed there is no gradient within the experimental uncertainties



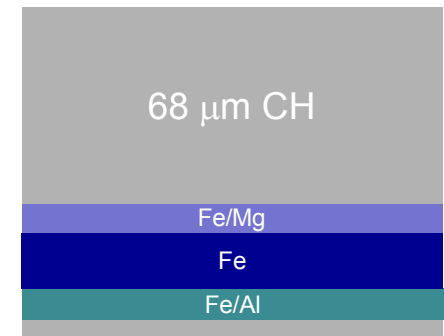
- Al Ly α and He γ and Mg Ly β and He γ are simultaneously fit.
- Weaker lines are fit very well
- All stronger lines are heavily saturated



Direct uniformity measurement confirmed there is no gradient within the experimental uncertainties



	T_e	n_e (10^{22} cm^{-3})	rL ($10^{-5} \text{ g/cm}^{-2}$)
Pinch side	215±3	4.49±1.23	3.78±0.90
Obs. side	208±5	4.34±0.46	3.36±0.42

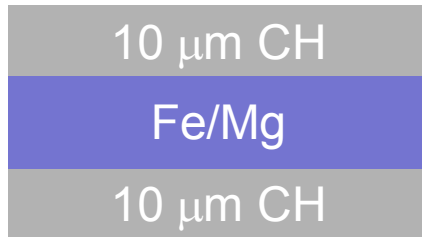


- Temperature turned out to be somewhat higher than other thick target cases
- Inferred areal densities are about 80% of RBS measurement (81% for Mg, 79% for Al)



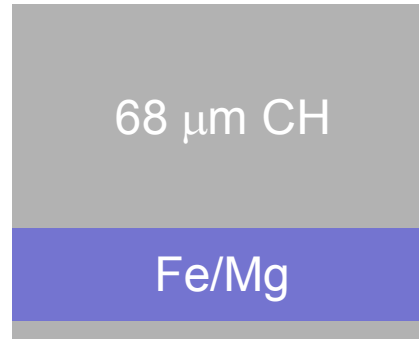
Summary and future work

Sample1: Low density



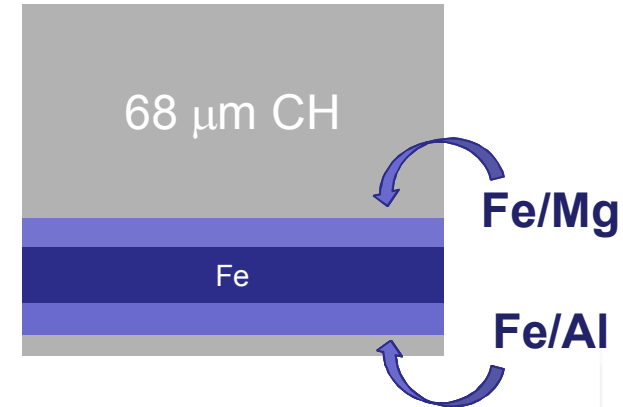
- $T_e = 164 \pm 5$ eV
- $n_e = (7.91 \pm 1.92) \times 10^{21}$

Sample2: High density



- $T_e = 195 \pm 6$ eV
- $n_e = (4.44 \pm 1.55) \times 10^{22}$

Sample3: Uniformity



- =====Mg=====
- $T_e = 208 \pm 5$ eV
 - $n_e = (4.34 \pm 0.46) \times 10^{22}$

- ===== Al =====
- $T_e = 215 \pm 3$ eV
 - $n_e = (4.49 \pm 1.23) \times 10^{22}$

- We inferred T_e and n_e by fitting weaker lines
- This method is insensitive to possible additional background
- Future work:
 - Iron opacity modeling with the inferred conditions
 - Investigate possible background



Conclusions

