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# **Dual-Permeability Modeling and Evaluation of Drift-Shadow Experiments**

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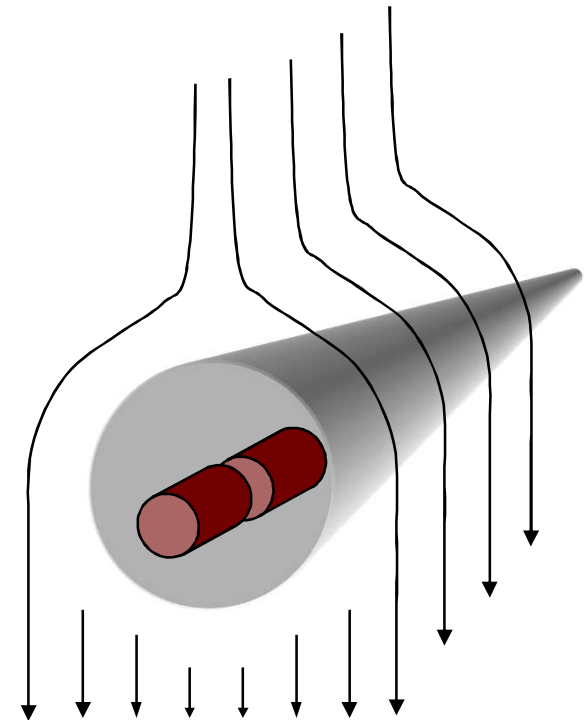


# Overview

- **Background and Objectives**
- **Experimental Summary**
- **Modeling Approach & Results**
- **Conclusions**

# Background and Objectives

- Capillary diversion around tunnel may cause “drift shadow” effect
- Previous models evaluated drift-shadow effect
  - Philip et al. (1989)
    - Analytical Solution
  - Houseworth et al. (2003)
    - Dual-permeability model
  - No comparisons to data
- Simulate drift-shadow tests (Altman et al., 2008) with dual-permeability models

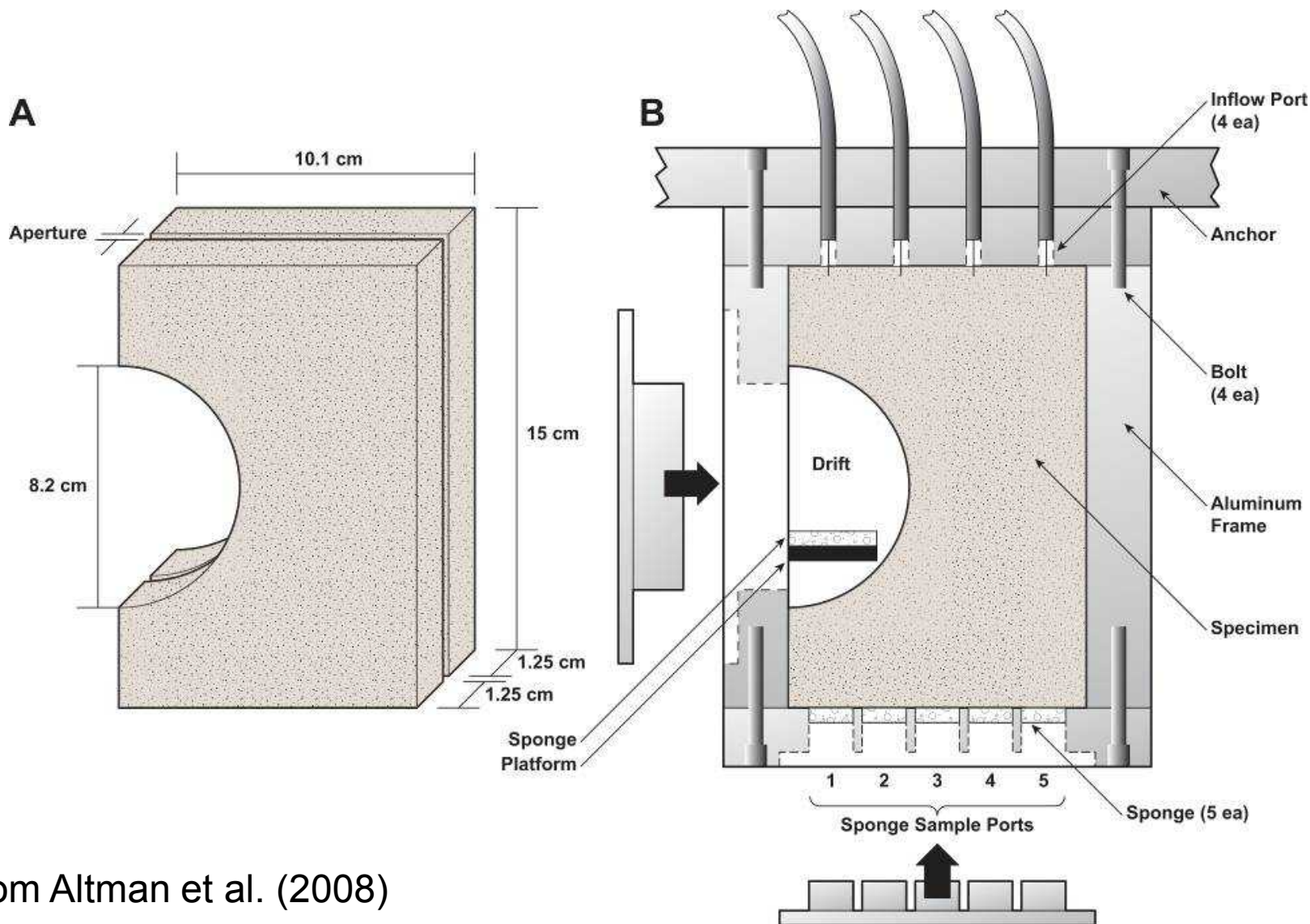




# Overview

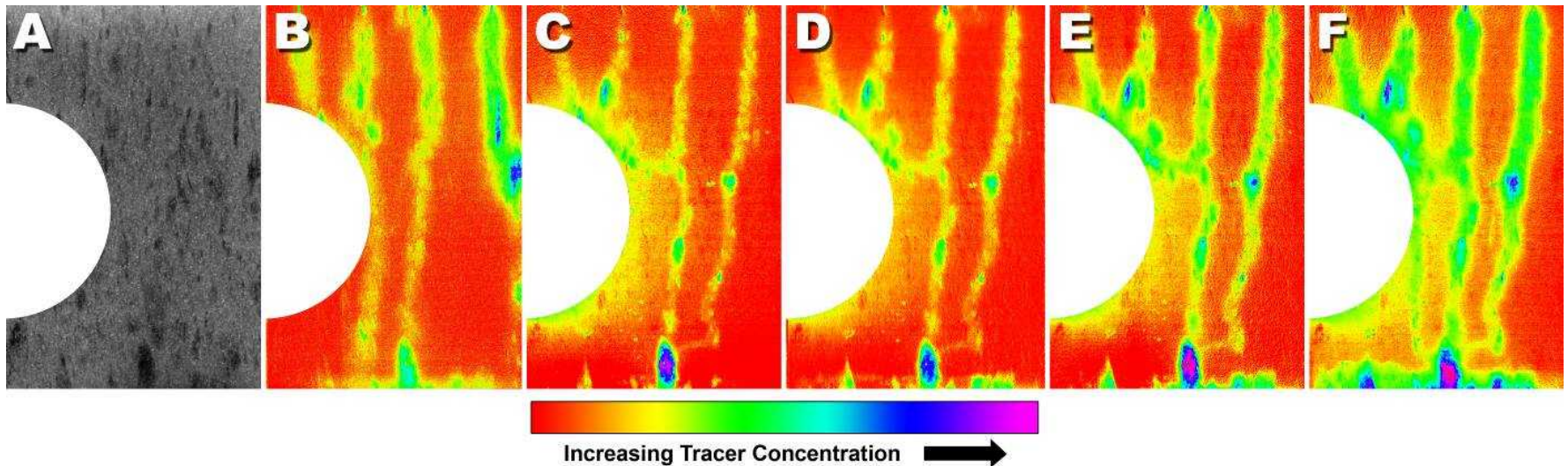
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# Experimental Design



from Altman et al. (2008)

# X-Ray Imaging Results



X-ray absorption images of the 500-micron aperture test cell taken (A) before and (B) 5 h after the start of experiment at 0.01 ml/min and (C) 1, (D) 2, (E) 3, and (F) 5 h after start of experiment with 0.23 ml/min flow rate. Image of cell without tracer (A) shows porous pumice fragments as darker areas. From Altman et al. (2008).



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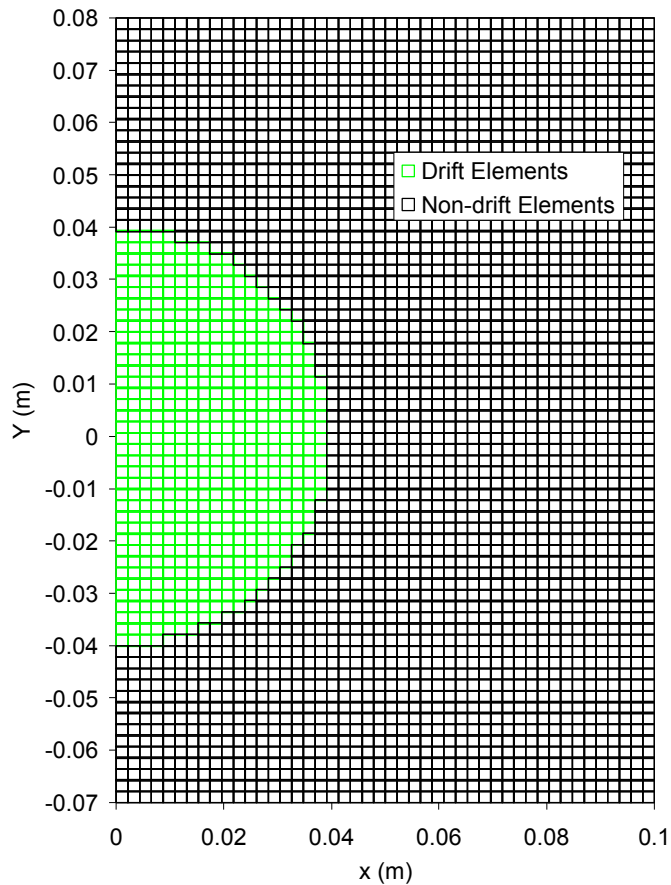


# Computational Domain

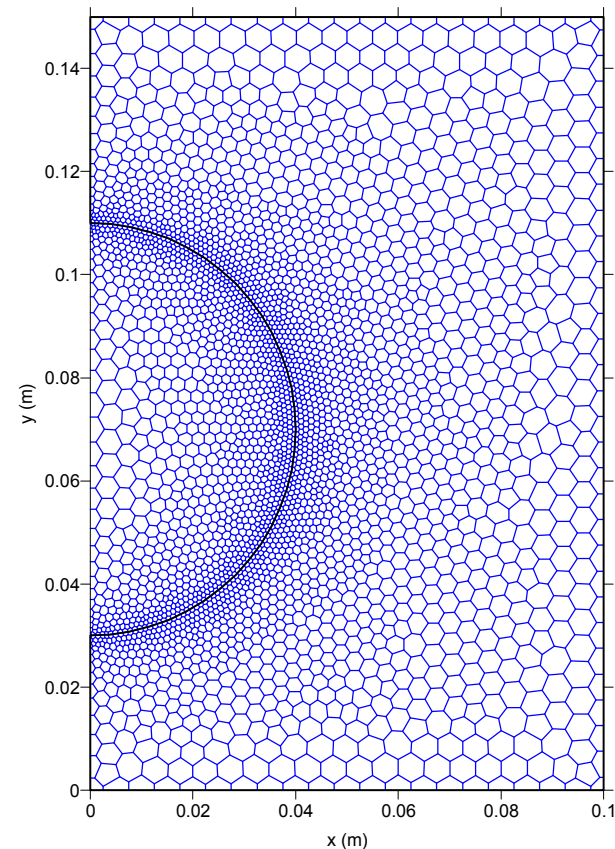
## Dual-Permeability Model

Fracture and Matrix Continua Simulated

Structured Orthogonal Mesh



Unstructured Voronoi Mesh





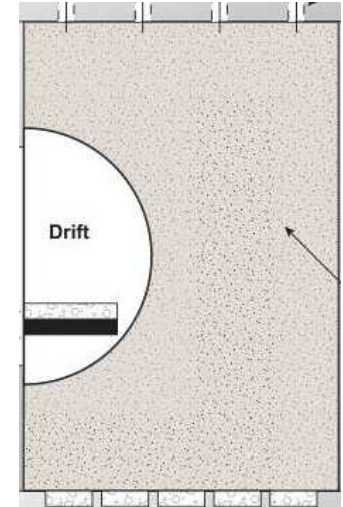


# Model Parameters

- **Matrix properties taken from Flint (2003) and Altman et al. (2006)**
  - Porosity, permeability, van Genuchten  $\alpha$  and  $n$
- **Fracture properties calculated as a function of fracture aperture**

# Model Boundary Conditions

- Lateral and top boundaries were no-flow
- Elements located within the drift specified as seepage boundaries (zero capillary pressure)
- Bottom boundary specified as gravity drainage flow (no capillary-pressure gradient)
- Simulated water injection rates and fracture apertures were varied

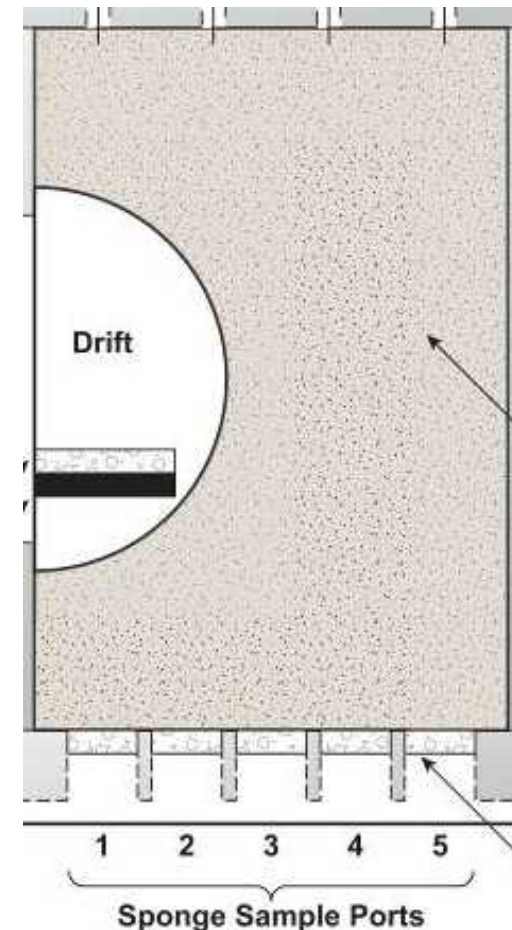
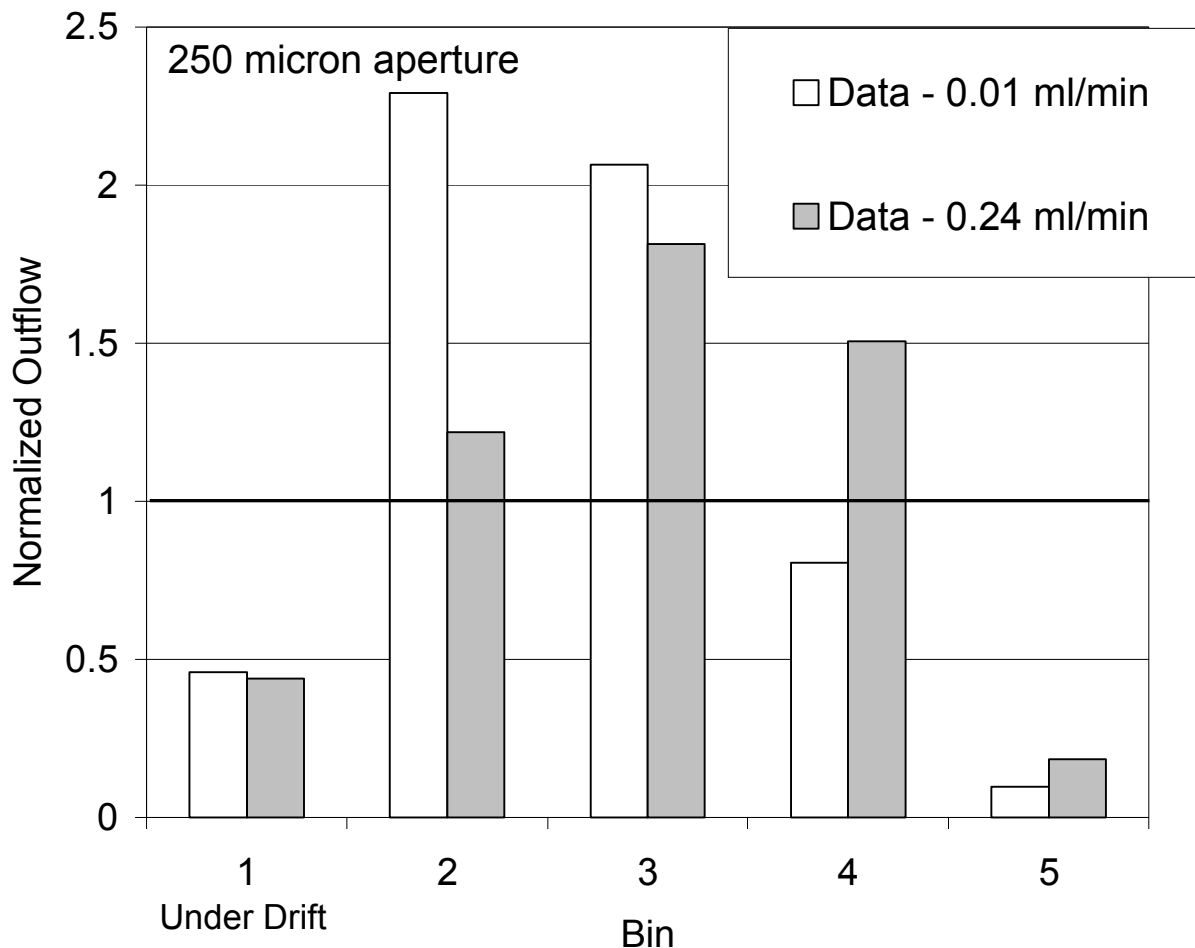


| Aperture<br>(microns) | Low Injection Rate<br>per Port (mL/min) | High Injection Rate<br>per Port (mL/min) |
|-----------------------|-----------------------------------------|------------------------------------------|
| 100                   | 0.01                                    | 0.12                                     |
| 250                   | 0.01                                    | 0.24                                     |
| 500                   | 0.01                                    | 0.23                                     |

# Model Results & Comparisons

## Distribution of Normalized Outflow

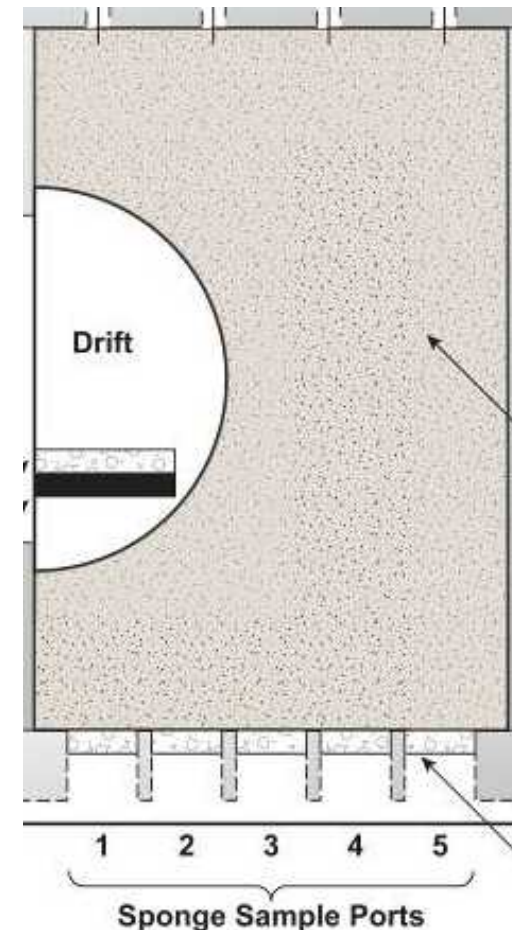
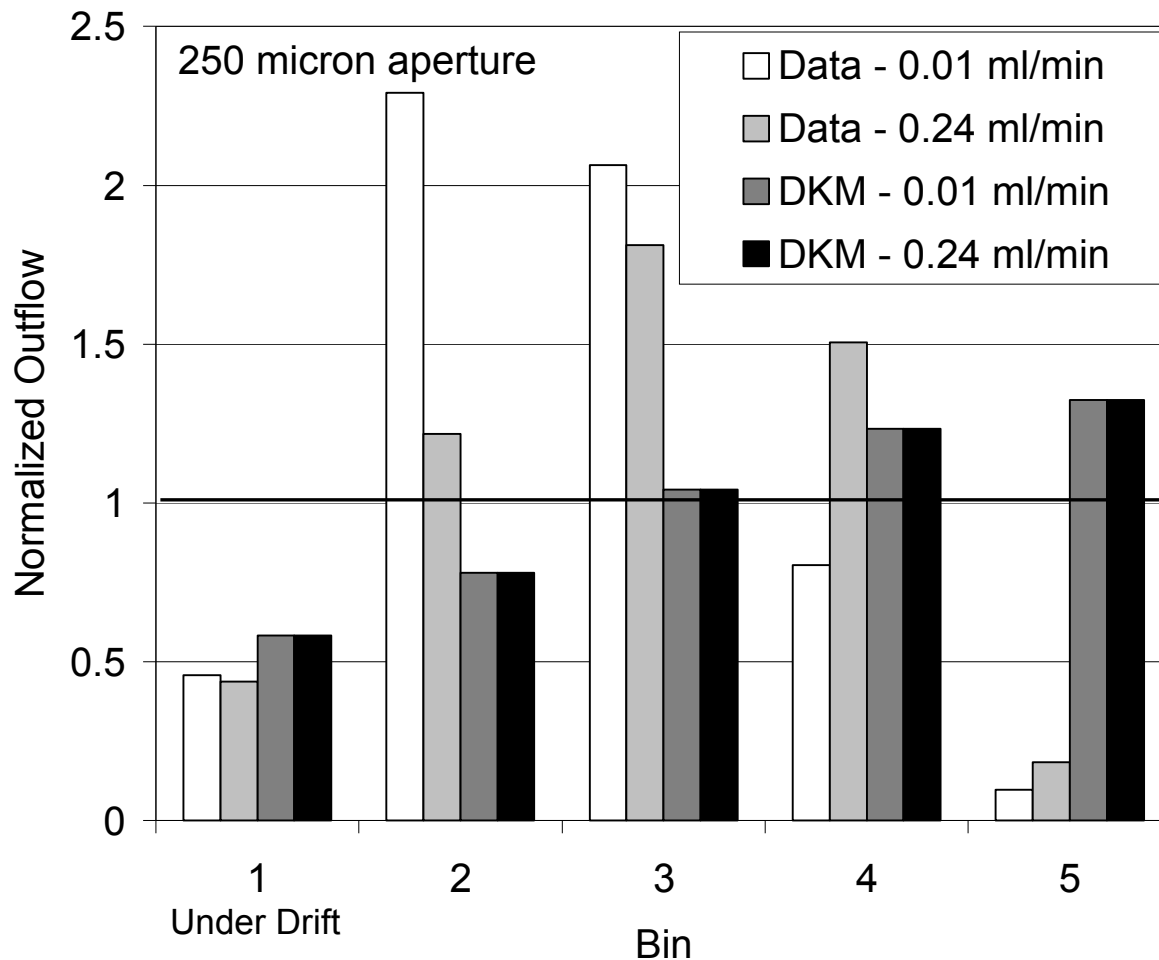
Less than ~1% of flow observed to enter drift during test



# Model Results & Comparisons

## Distribution of Normalized Outflow

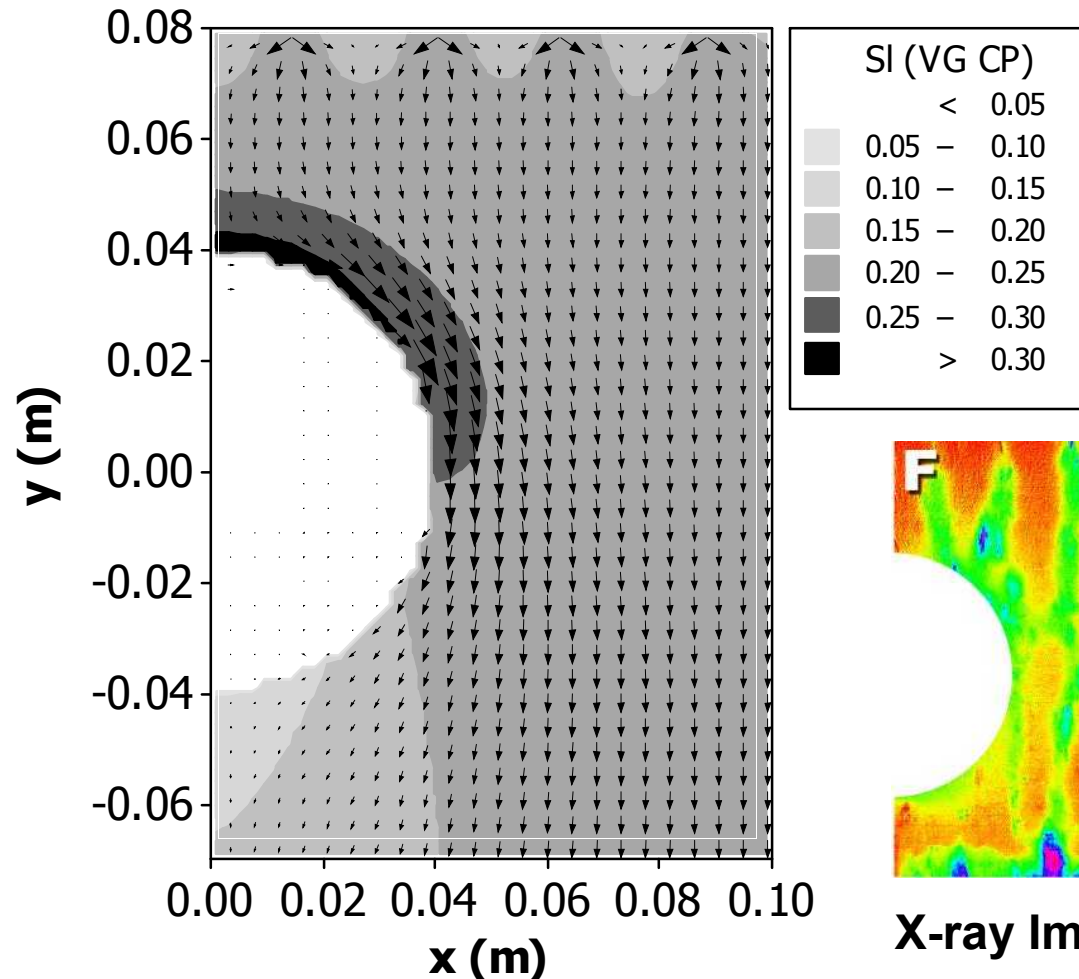
Less than ~1% of flow observed to enter drift during test



# Simulated Fracture Saturation

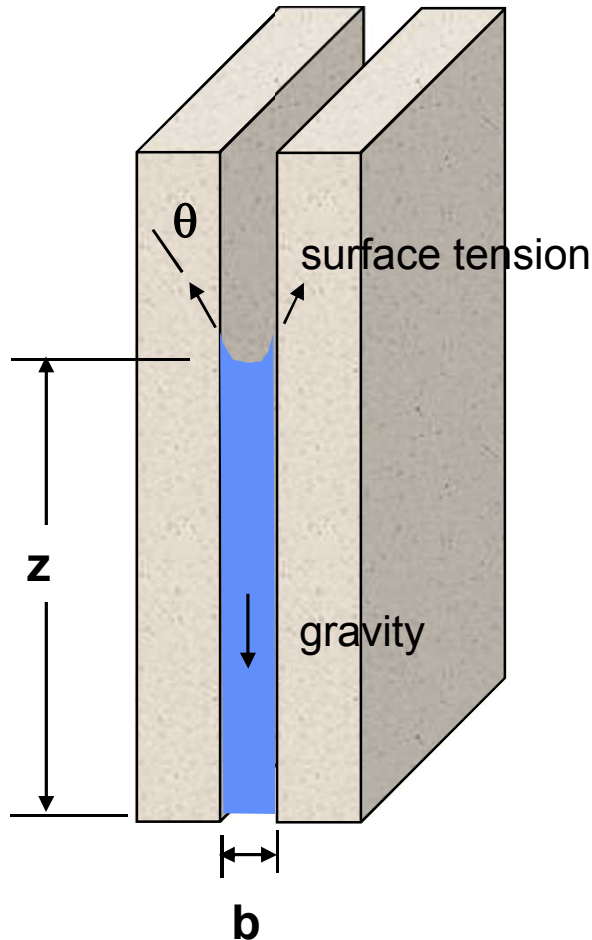
500 micron aperture, 0.23 ml/min

- van Genuchten capillary pressure curves with unbounded maximum pressure ( $1e10$  Pa)
- Distribution of flow within the fracture is too uniform (no fingers)



# Capillarity in a Smooth Fracture Plane

↑ Surface tension = ↓ liquid weight



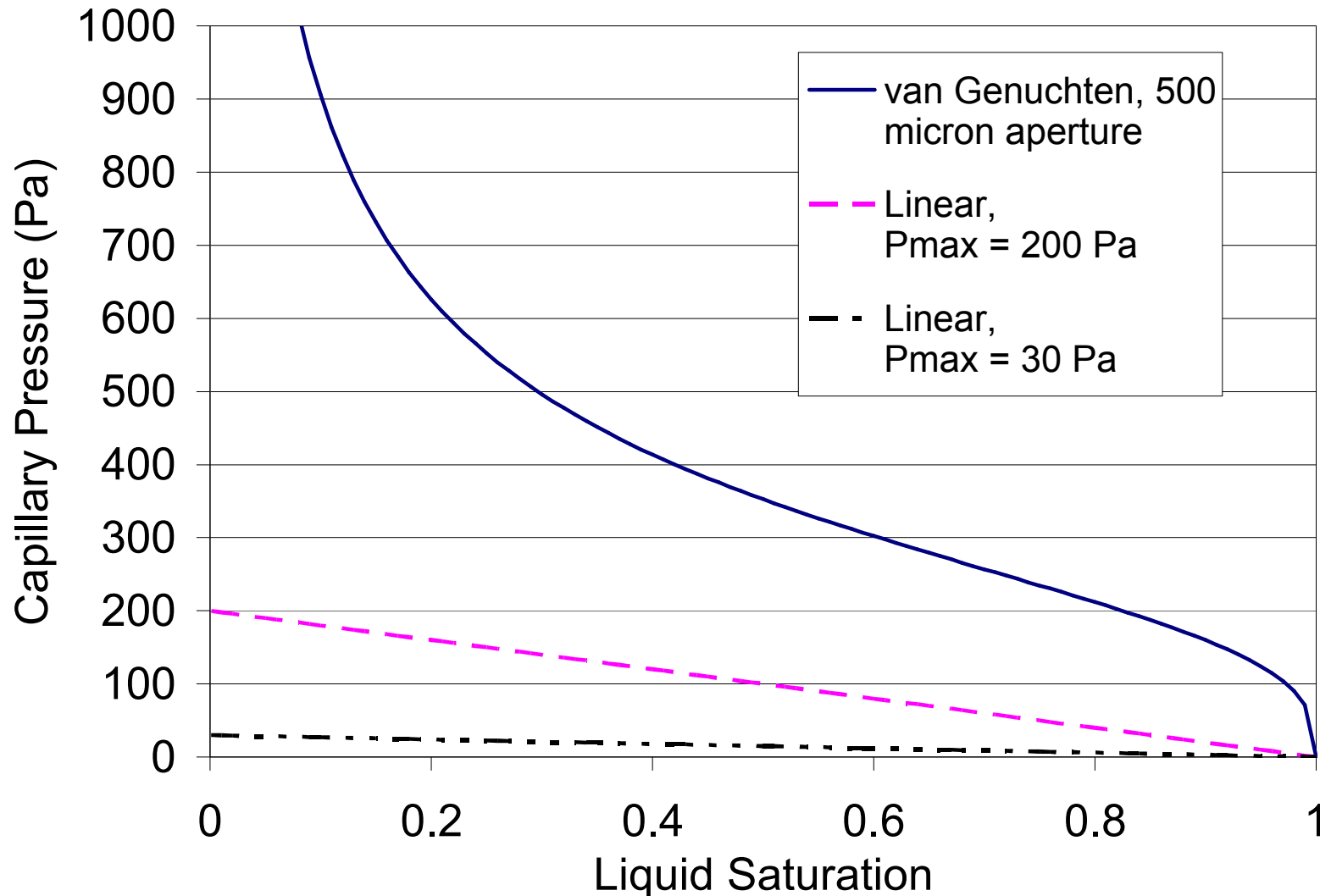
$$z = \frac{2\sigma \cos \theta}{\rho g b}$$

or

$$P_{cap} = \rho g z = \frac{2\sigma \cos \theta}{b}$$

| $b$ (microns) | $P_{cap}$ (Pa) |
|---------------|----------------|
| 100           | 1440           |
| 250           | 578            |
| 500           | 288            |

# Capillary Pressure Curves

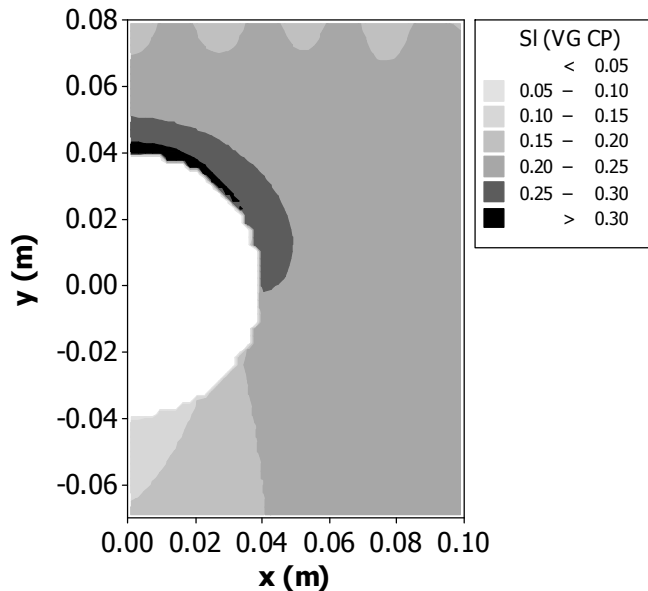




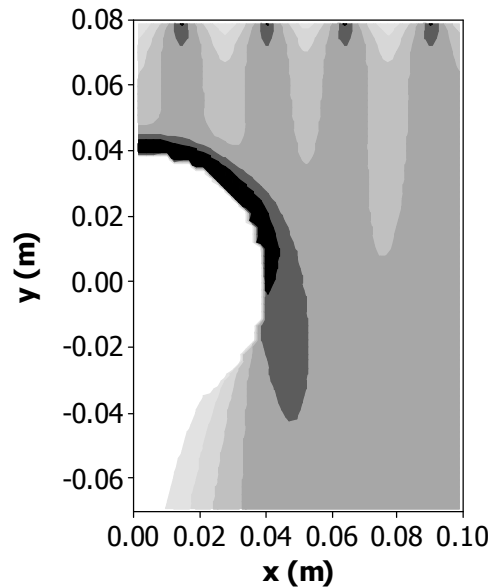


# Impact of Fracture Capillary Pressure

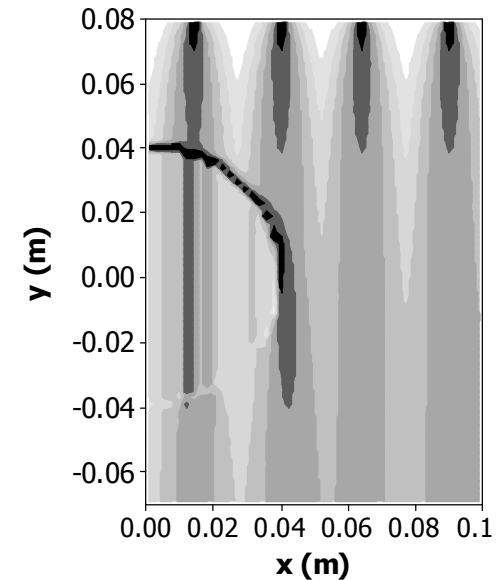
**van Genuchten  
( $P_{\text{max}} = 1\text{e}10 \text{ Pa}$ )**



**Linear  
( $P_{\text{max}} = 200 \text{ Pa}$ )**



**Linear  
( $P_{\text{max}} = 30 \text{ Pa}$ )**

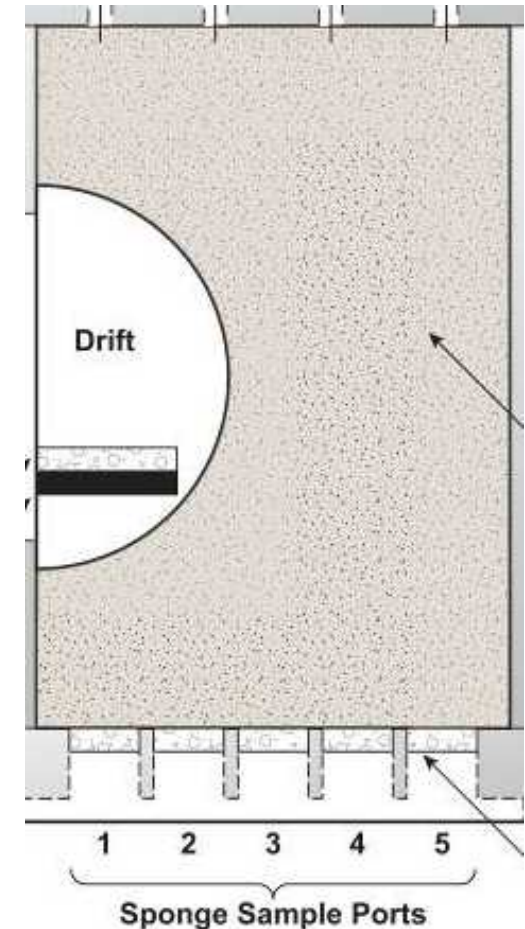
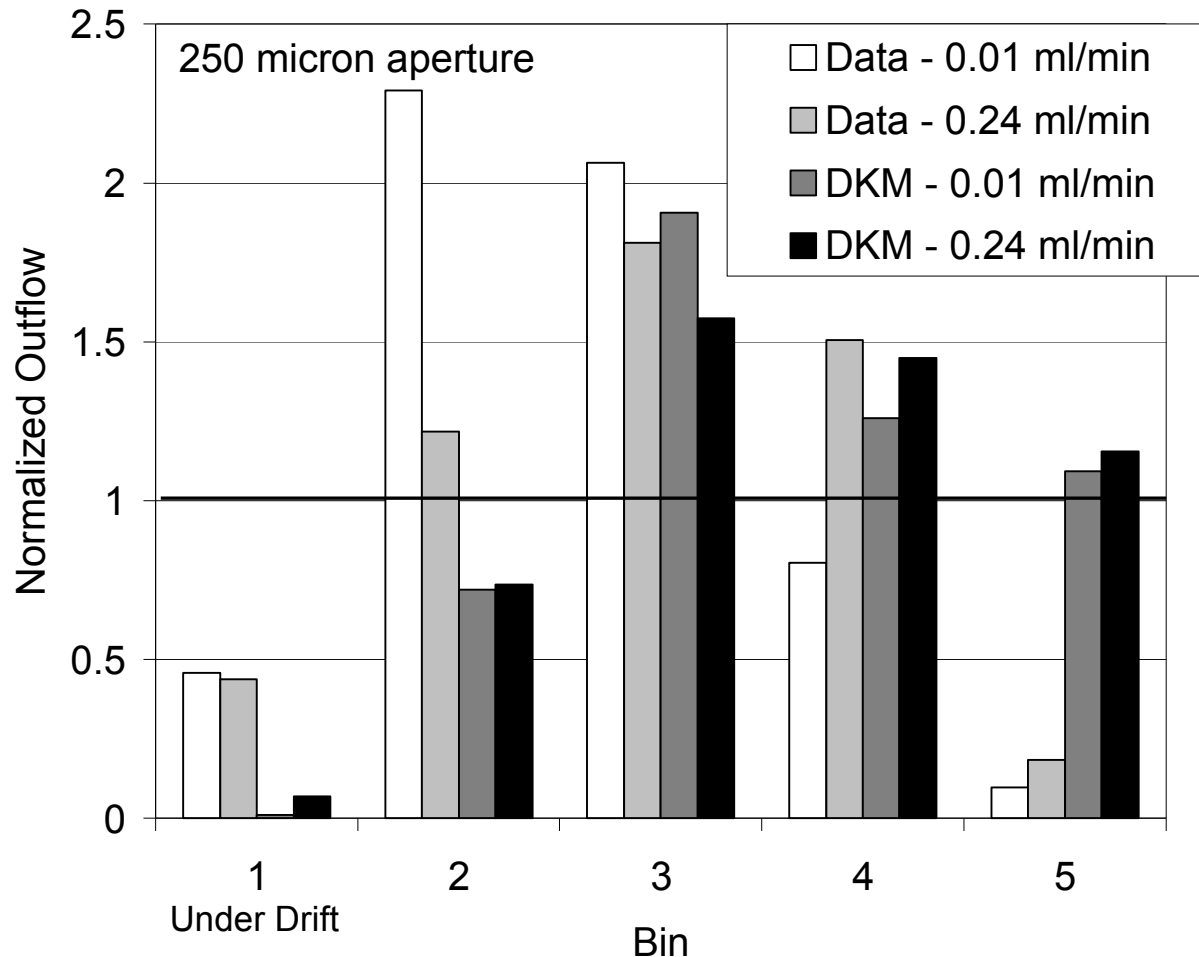


**500 micron aperture and 0.23 ml/min flow rate**

# Model Results & Comparisons

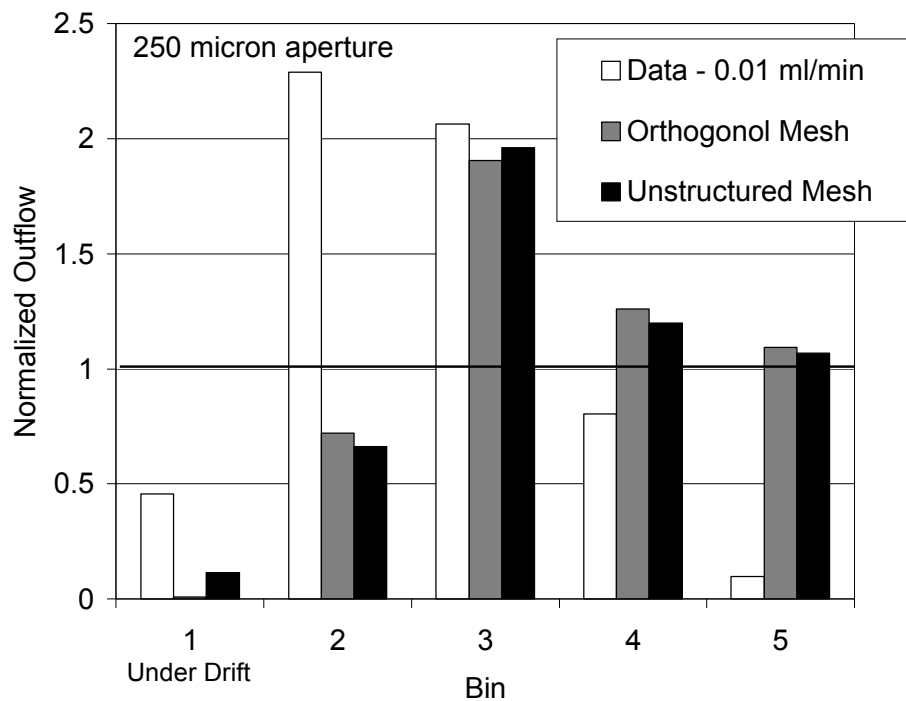
## Distribution of Normalized Outflow with Reduced Capillary Pressure (Linear, $P_{\max} = 200$ Pa)

Less than ~1% of flow observed to enter drift during test

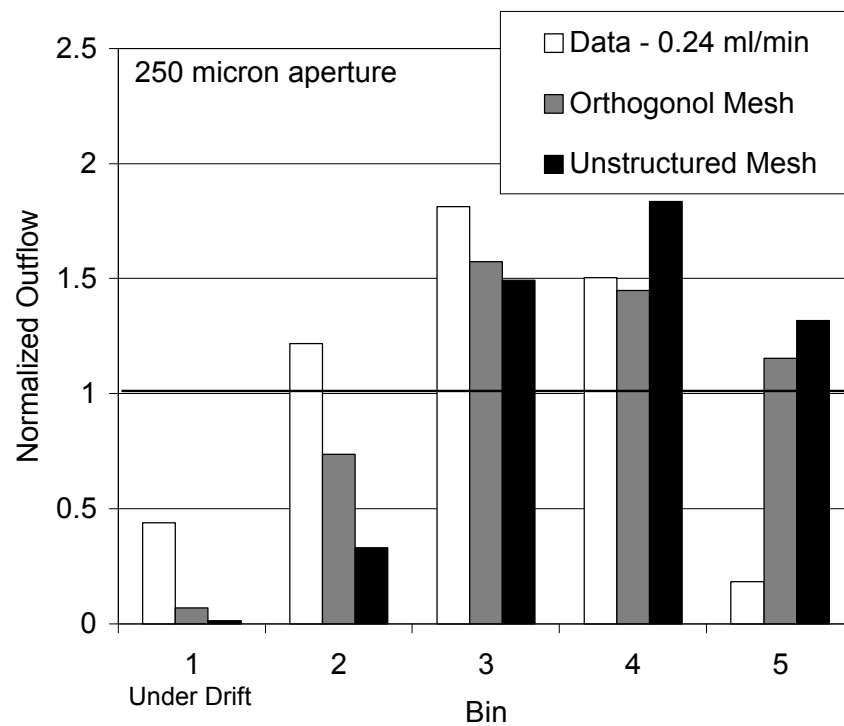


# Impact of Mesh

0.01 ml/min



0.24 ml/min





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# Conclusions

- **Capillary diversion and drift shadow can be modeled by existing dual-permeability models**
- **Distribution of flux beneath the drift depends on magnitude of fracture capillary pressure**
  - **van Genuchten curves with unbounded capillary pressures yielded more uniform fluxes**
  - **Linear curves with reduced maximum capillary pressures yielded better matches to data**
- **Orthogonal and unstructured meshes yielded similar results**



# Backup Slides

# Image Analysis

Digitize X-Ray  
Film



Grey-Level  
Adjust Film



From digitized film know light intensity ( $I$ ) at each pixel

From image of  
Dry Sample

$I_{d\ i,j}$

From image of  
Saturated Sample

$I_{s\ i,j}$

From images of  
samples taken during  
the experiment

$I(t)_{i,j}$

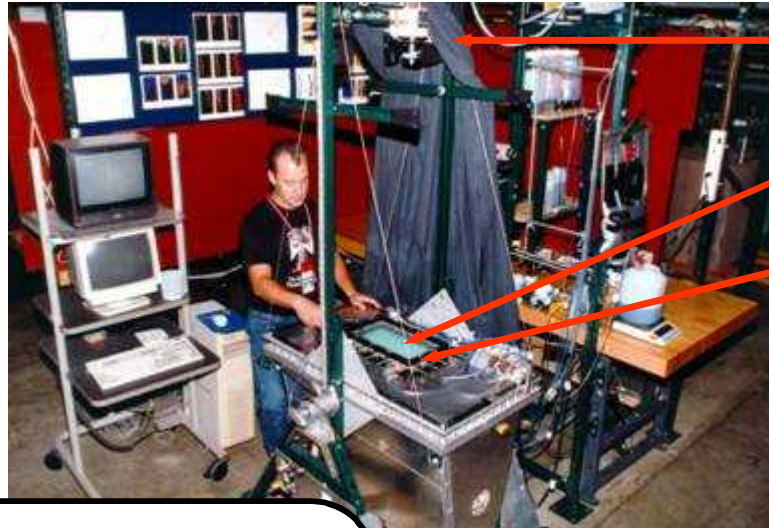
Calculate  
Porosity  
 $C/Co(t)$

Pixel Size = 0.3 mm x 0.3 mm

Tidwell, V. C., and R. J. Glass Jr., WRR, 1994.

Tidwell, et al., *Journal of Contaminant Hydrology*, 2000.

Altman, et al., *Journal of Contaminant Hydrology*, 2004.



CCD Camera

Controlled  
Light Source

X-Ray Film





# X-Ray Imaging Formulation

$$\phi_{i,j} = \frac{\ln(I_s) - \ln(I_d)}{E[\ln(I_s) - \ln(I_d)]} \phi_{bulk}$$

$$\frac{C}{C_o}(t) = \frac{\ln(I(t)) - \ln(I_d)}{\ln(I_s) - \ln(I_d)}$$

$$\frac{M}{M_o}(t) = \frac{\sum_{i=1}^N \left( \frac{C}{C_o}(t) \right)_i \phi_i}{\sum_{i=1}^N \phi_i}$$

Tidwell, V. C., and R. J. Glass Jr., WRR, 1994.

Tidwell, et al., *Journal of Contaminant Hydrology*, 2000.

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