
Modeling of Epileptic Seizures using Tensor Analysis

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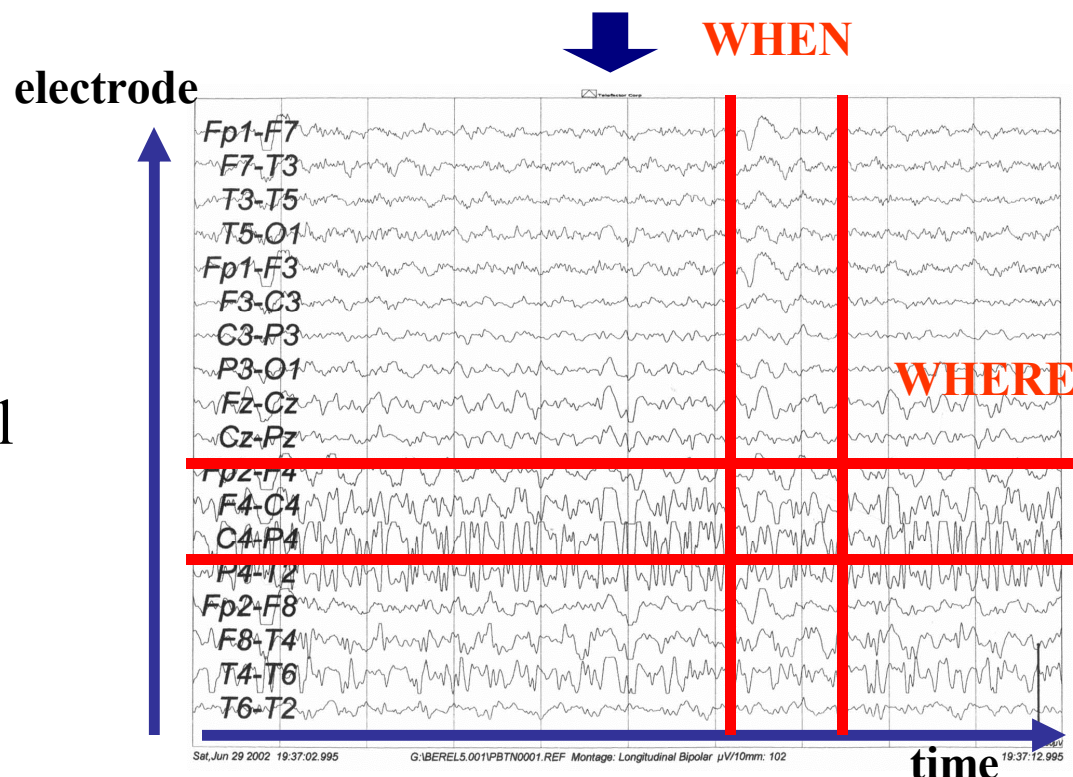


Sandia National Laboratories



Problem Definition

- **Epilepsy:** neurological disorder characterized by recurrent, abrupt seizures.
- WHO: over 50 million people!
- Diagnosis techniques
 - Physical and neurological exams
 - Neuroimaging
 - Video-EEG monitoring



Problem Definition (Cont.)

Motivation:

- Visual analysis is time-consuming
>> saving manpower
- Visual analysis is subjective and error-prone
>> objective/robust analysis

Goal: Developing mathematical models that can capture a seizure structure automatically.

- Seizure recognition **(when)**
- Seizure localization **(where)**



Overview

- **Part I: Tensor Basics**
- **Part II: Epileptic Seizure Recognition**
 - Related Work (e.g., feature extraction from epileptic EEG)
 - Methodology:
 - Construction of a third-order **Epilepsy Feature Tensor**
 - Seizure recognition using Multilinear PLS
- **Part III: Discussions**
 - Future Research Directions
 - Other studies on epileptic EEG signals

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Why tensors?

Two-way data

Higher-order data

- **Social networks:**

<user, keyword>

<user, keyword, time>

- **Text mining:**

<document, term>

< document, term, author>

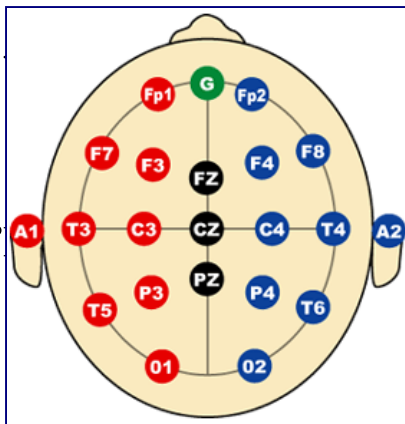
- **Face recognition:**

<person, pixel>

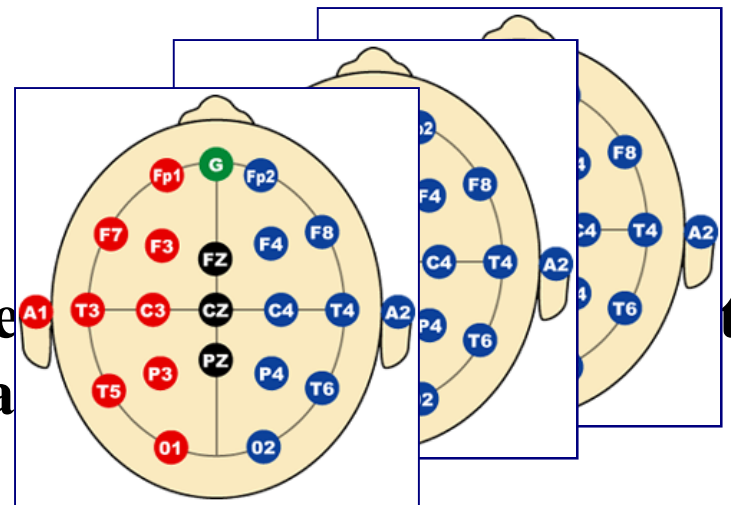
< person, pixel, viewpoint>

- **Neuroscience:**

Matr



ough to represent
the data from a



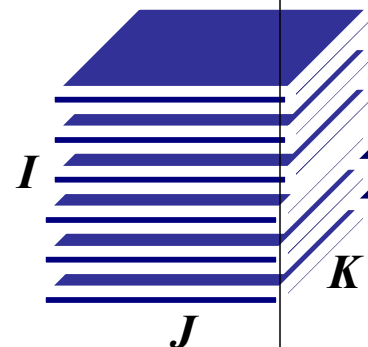
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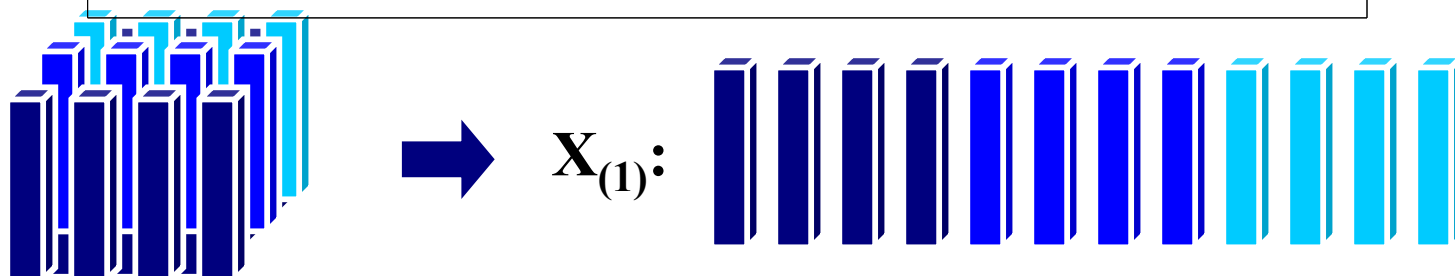
What is a tensor?

- A tensor is a higher-order generalization of a matrix.

Example: A third-order tensor $\underline{X} \in \mathbb{R}^{I \times J \times K}$



- Matricization (unfolding/flattening)
 - rearranging a tensor as a matrix.
 - The mode-n matricization of a higher-order dataset, e.g., \underline{X} , denoted by $X_{(n)}$ unfolds the data in the n^{th} mode.



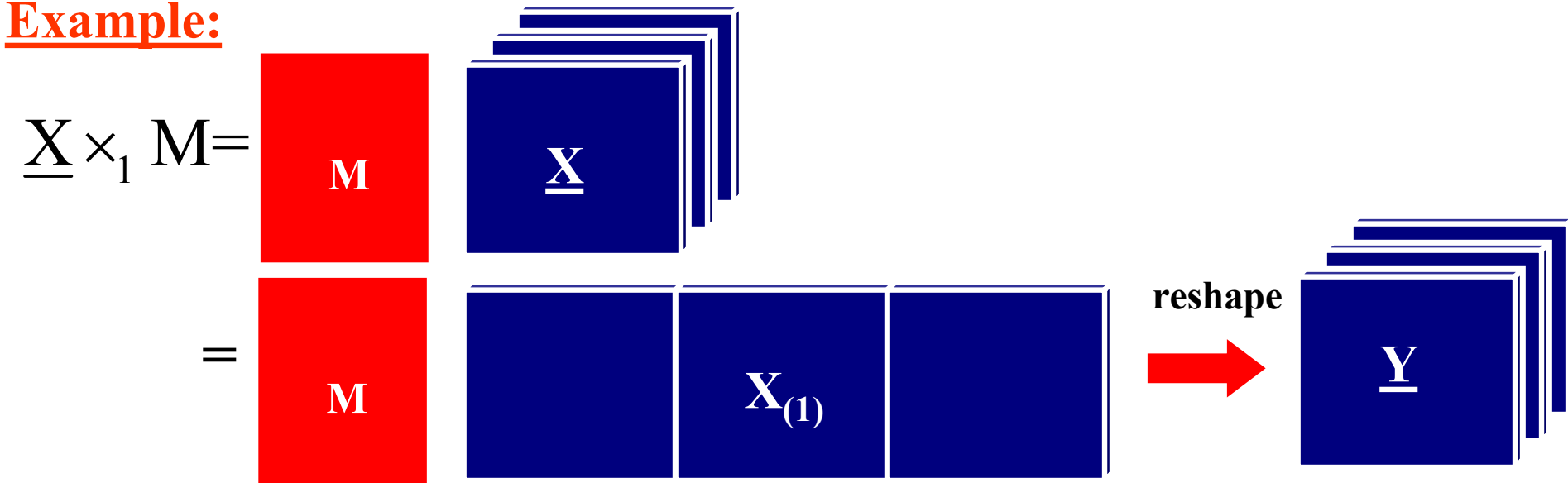
Tensor times a matrix

- The mode- n product of a tensor $\underline{X} \in \mathbb{R}^{I_1 \times I_2 \times \dots \times I_n \times \dots \times I_N}$ with a matrix $M \in \mathbb{R}^{P \times I_n}$ is denoted by

$$\underline{Y} = \underline{X} \times_n M$$

where $\underline{Y} \in \mathbb{R}^{I_1 \times I_2 \times \dots \times I_{n-1} \times P \times I_{n+1} \times \dots \times I_N}$

Example:



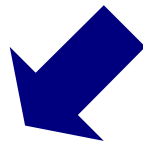


Overview

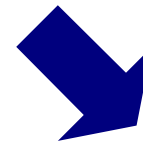
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Related Work

Common Approach: Divide an EEG recording into time epochs and extract features that can distinguish between seizures and other brain dynamics.



Analysis of the performance of multiple features on **single channel** EEG data



Analysis of the performance of a **single feature** on multi-channel EEG data

Time Epochs
 $i=1,2,\dots,I$



Features
 $j=1,2,\dots,J$

Time Epochs
 $i=1,2,\dots,I$

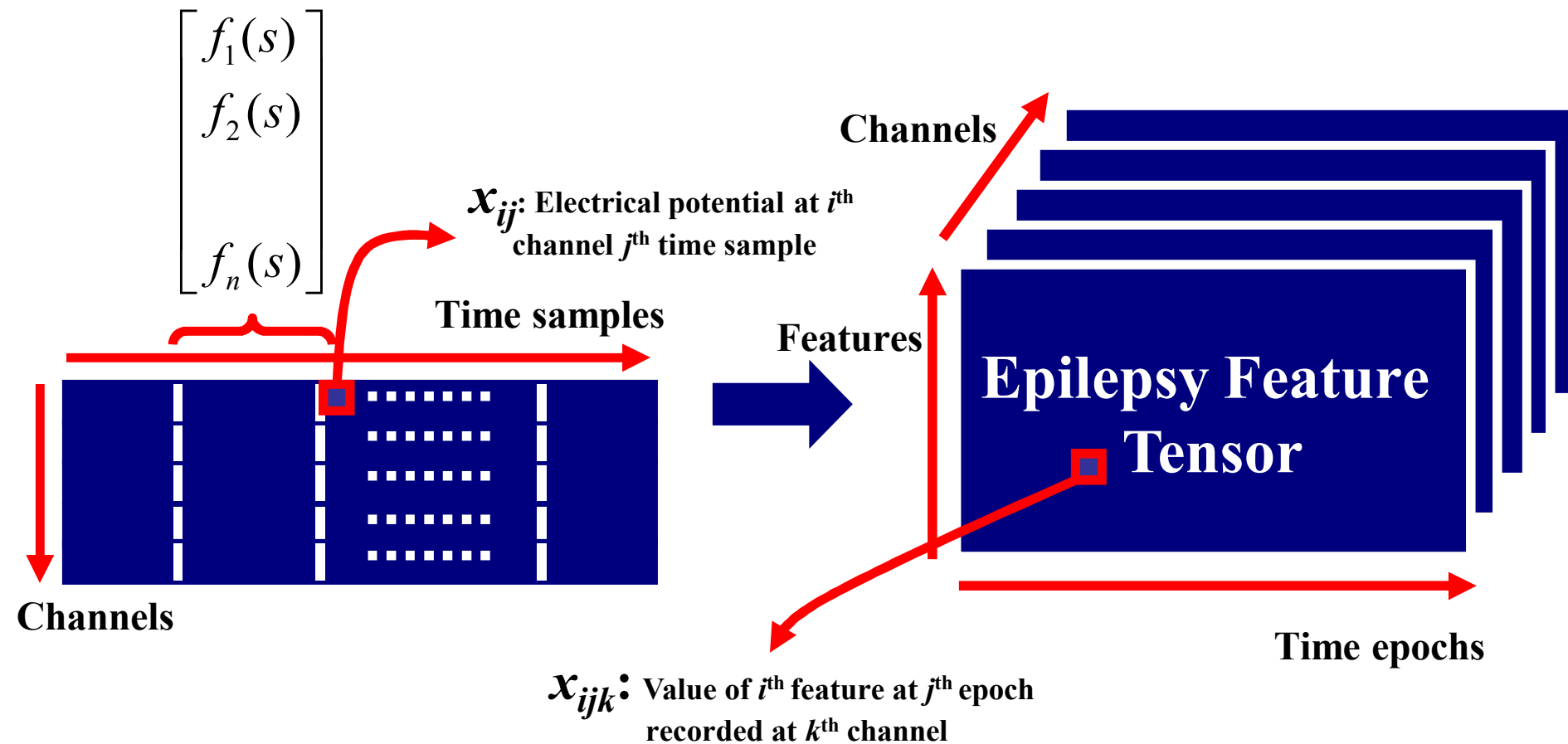


Channels
 $k=1,2,\dots,K$

Our Approach: Analysis of **multiple features** from different domains on **multi-channel** EEG data

STEP1: Epilepsy Feature Tensor

- Construction of an Epilepsy Feature Tensor from multi-channel EEG





Features from Multiple Domains



Time domain

Let $s = \{s(1), s(2), \dots, s(N)\}$ be the time sequence for a particular epoch of length N .

- Activity: $f_1(s) = \sigma_s^2$
- Mobility: $f_2(s) = \frac{\sigma_{s'}}{\sigma_s}$
- Complexity

$$f_3(s) = \frac{(\sigma_{s''} / \sigma_{s'})}{(\sigma_{s'} / \sigma_s)}$$

- Mean Absolute Slope: $f_4(s)$

Frequency domain

Take the first difference and then compute the Fourier coefficients to construct the amplitude spectrum

- Median Frequency: $f_5(s)$

Compute the energy spread across different EEG bands, i.e., δ (0.5-3.5Hz), θ (3.5-7.5Hz), α (7.5-12.5Hz), β (12.5-30Hz) and γ (>30Hz)

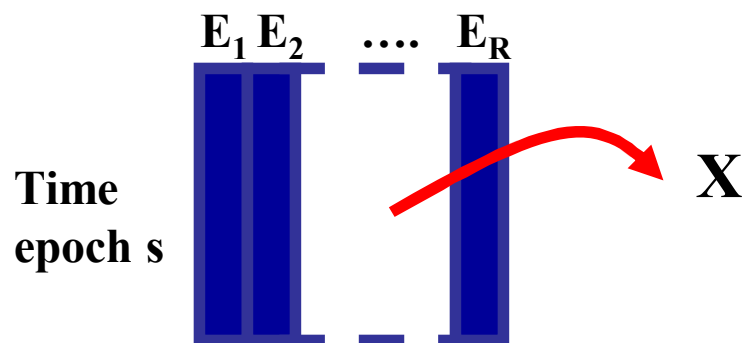
- Spectral Entropy: $f_6(s)$
- Relative Energy in each freq. band:

$$f_7(s) - f_{10}(s)$$



More features

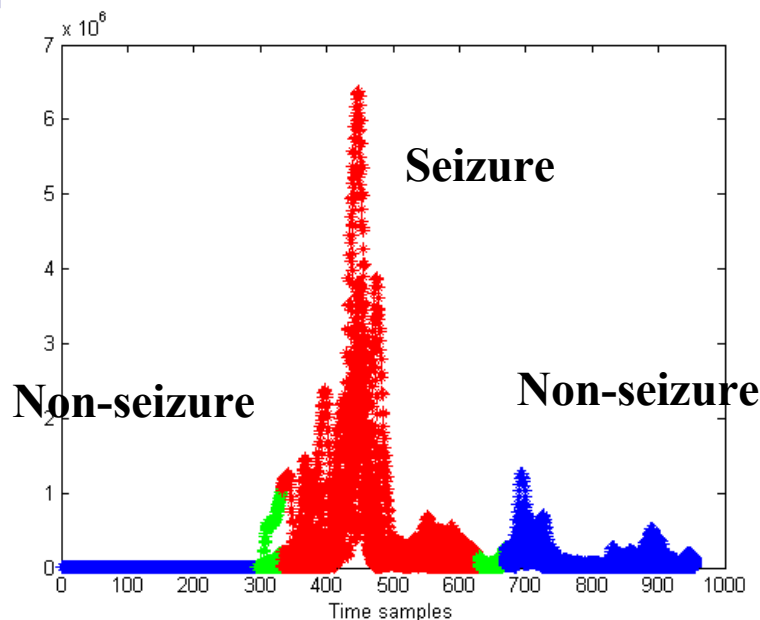
- To quantify the synchronization among channels, especially among neighboring channels as the seizure starts.



$$f_{11}(s, i) = \sum_{j \in NEIGH_i} |(X^T X)_{ij}|$$

where $NEIGH_i$ contains the neighbors of electrode i .

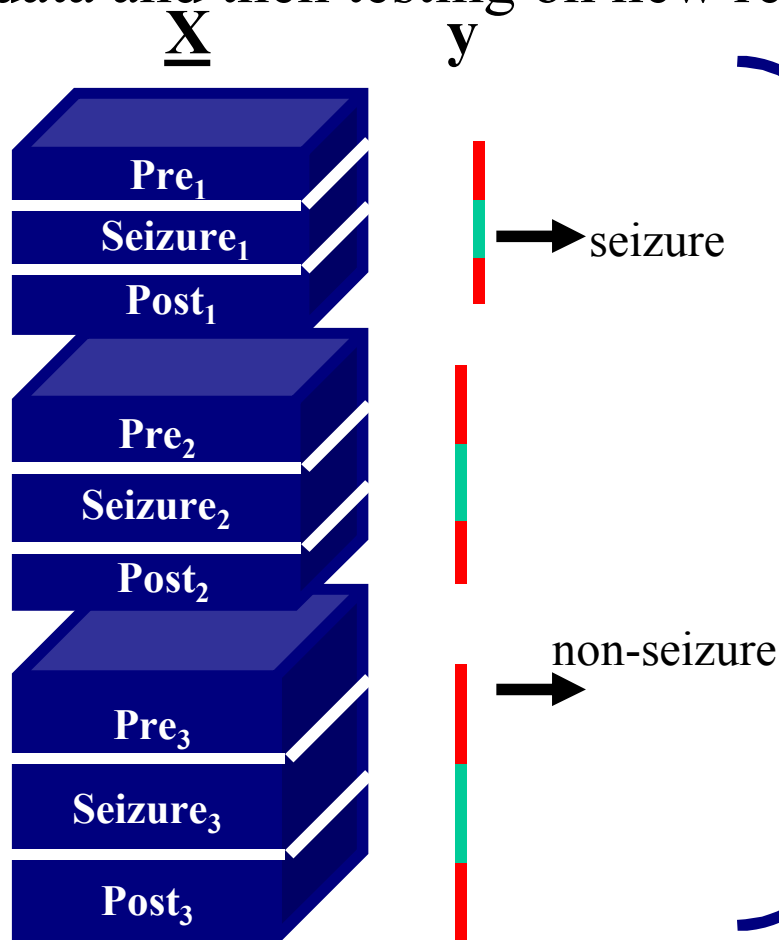
Example:





STEP2: Seizure Recognition

- Building a mathematical model based on Multilinear PLS on available data and then testing on new recordings



Training Set

- Build a model based on N-PLS using the training set \underline{X} and the labels y .

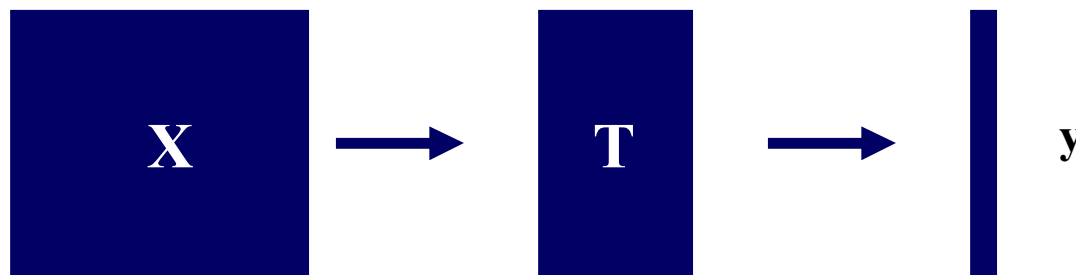
Test Set

- Predict the labels of new recordings.





Partial Least Squares (PLS)



Let $X \in \mathbb{R}^{I \times J}$ and $y \in \mathbb{R}^I$ be the independent and dependent (response) variables, respectively

- Map X to a low-dimensional space and regress onto y

$$y = Tb + e$$

- Determine the columns of $T \in \mathbb{R}^{I \times K}$ (where $K < J$), such that

$$\max_w \text{cov}(Xw, y)$$

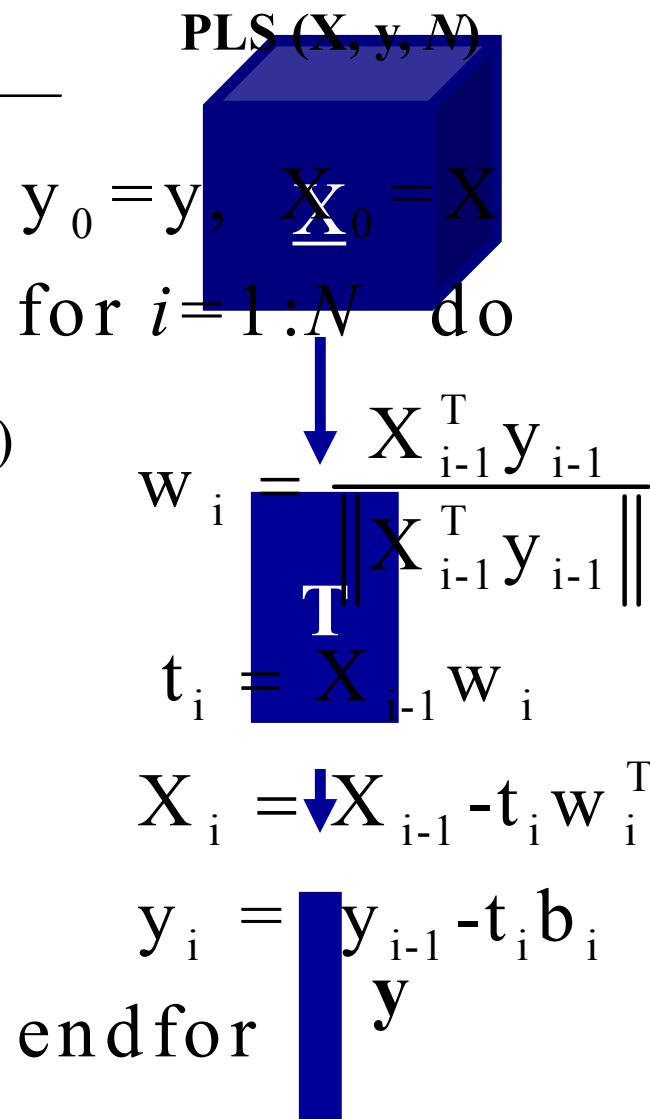
where $\mathbf{t} = X\mathbf{w}$ is a column of matrix \mathbf{T} .



Multilinear PLS (N-PLS) (by Bro'96)

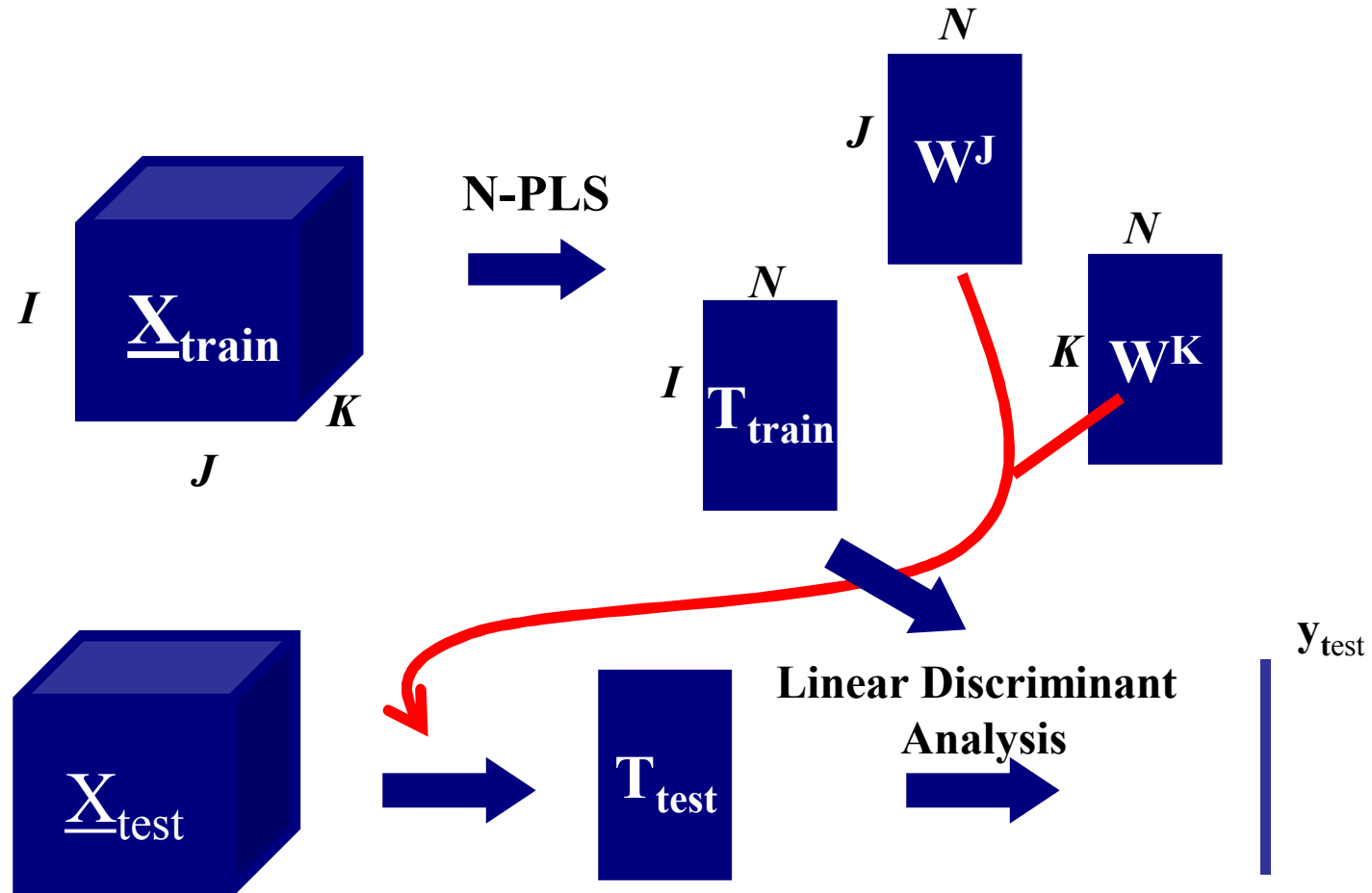
Multilinear PLS (X, y, N)

1. $y_0 = y, X_0 = X_{(1)}$
2. for $i = 1$ to N do
3. $z = y_{i-1}^T X_{i-1}$
4. $Z = USV^T$, where $Z(m, n) = z(m + J(n - 1))$
5. $w^J = U(:, 1), w^K = V(:, 1)$
 $W^J(:, i) = w^J, W^K(:, i) = w^K$
6. $T(:, i) = X_{i-1}(w^K \otimes w^J)$
7. $X_i = X_{i-1} - T(:, i)(w^K \otimes w^J)^T$
8. $b_i = (T^T T)^{-1} T^T y_{i-1} = T^+ y_{i-1}$
9. $y_i = y_{i-1} - T b_i$
10. endfor



To predict y_{test} :

Combine N-PLS and LDA



Feature Selection:

Generalization of VIP to 3-way

- **Goal:** Eliminate the features that are not very relevant with the classification of non-seizure and seizure epochs.

- **Approach:**

Use the loadings to determine which variables are important
(Variable Importance in Projection (VIP) (Word et al.'93))

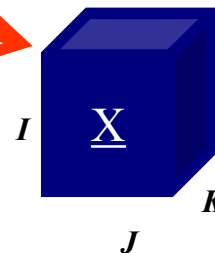
$$VIP_j = \sqrt{J \times \frac{\sum_{k=1}^N b_k^2 t_k^T t_k \left(\frac{w_{jk}}{\|w_k\|} \right)^2}{\sum_{k=1}^N b_k^2 t_k^T t_k}}$$

2-way

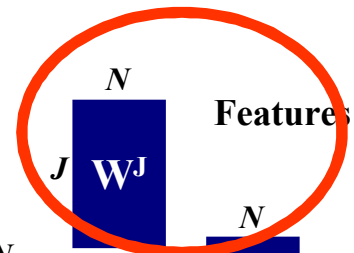
$$\mathbf{X} = \mathbf{T}\mathbf{W}^T + \mathbf{E}$$

$$\mathbf{y} = \mathbf{T}\mathbf{b} + \mathbf{e}$$

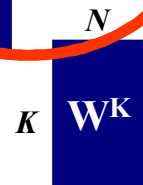
3-way



NPLS



Features



Channels

Multi-channel
EEG

Multi-channel
EEG

Multi-channel
EEG

Feature Extraction and Epilepsy Feature Tensor construction

Pre1

S1

Post1

Pre2

S2

Post2

Pre3

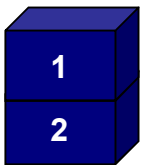
S3

Post3

Form training and test datasets

Feature Selection

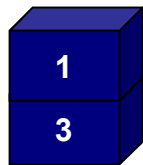
Training



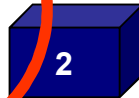
Test



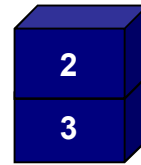
Training



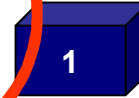
Test



Training



Test



Cross
Validation

Use NPLS+LDA to predict the labels of test recordings

Performance evaluation

DATA (Patient-Specific Seizure Recognition)

- Collected in the epilepsy monitoring unit of
 - Yeditepe University Hospital (Istanbul, Turkey)
 - Albany Medical College (NY, USA)
- 32 seizures from 9 patients with different seizure origins (at least 3 seizures/patient)
- Seven Features: Activity, Complexity, Mobility, Mean Absolute Slope, Spatial Information, Spectral Entropy, Median Frequency.
- Preprocessing:
 - Filter at 50Hz/60Hz
 - Scaling within features mode

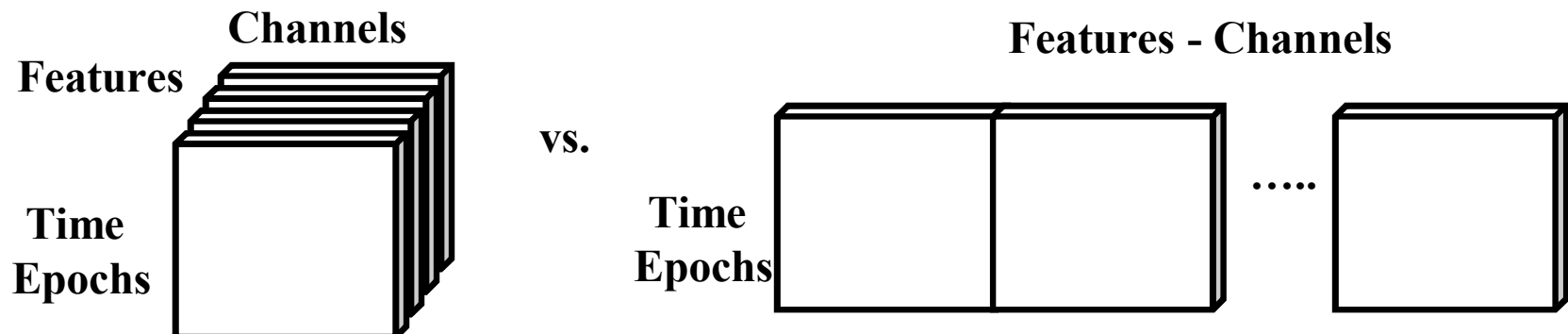
Patient Id	Seizure Id	Size of an Epilepsy Feature Tensor
1	1	302 x 7 x 18
	2	386 x 7 x 18
	3	320 x 7 x 18
	4	398 x 7 x 18
	5	444 x 7 x 18
2	1	878 x 7 x 18
	2	866 x 7 x 18
	3	902 x 7 x 18
	4	986 x 7 x 18
	5	998 x 7 x 18
3	1	790 x 7 x 18
	2	746 x 7 x 18
	3	1034 x 7 x 18
4	1	1174 x 7 x 18
	2	1346 x 7 x 18
	3	1170 x 7 x 18
⋮		

Performance Evaluation

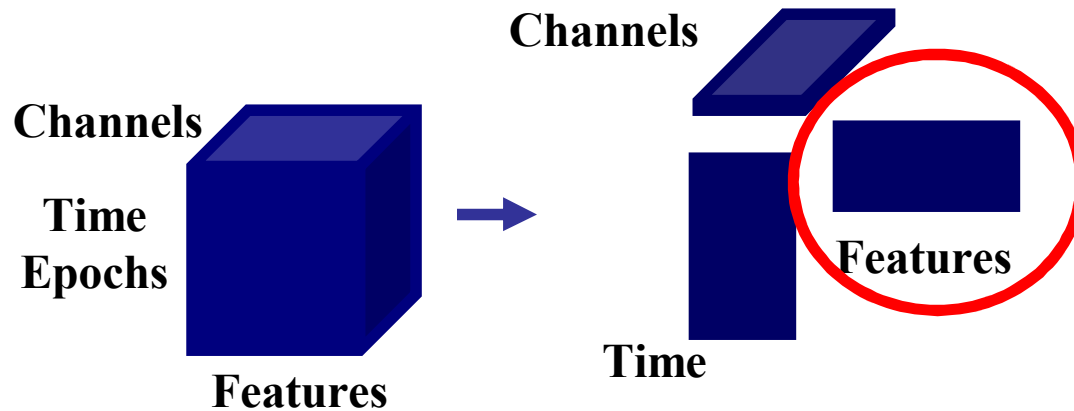
- **G-means:** $\sqrt{Sensitivity \times Specificity}$

	NPLS+LDA	NPLS+LDA (FS)
Patient1	85.3%	86.6%
Patient2	97.6%	96.7%
Patient3	91.3%	91.1%
Patient4	75.0%	77.3%
Patient5	28.6%	83.1%
Patient6	72.3%	89.3%
Patient7	97.0%	92.1%
Patient8	86.0%	78.4%
Patient9	84.5%	77.4%

- **Three-way vs. Two-way:**



Features



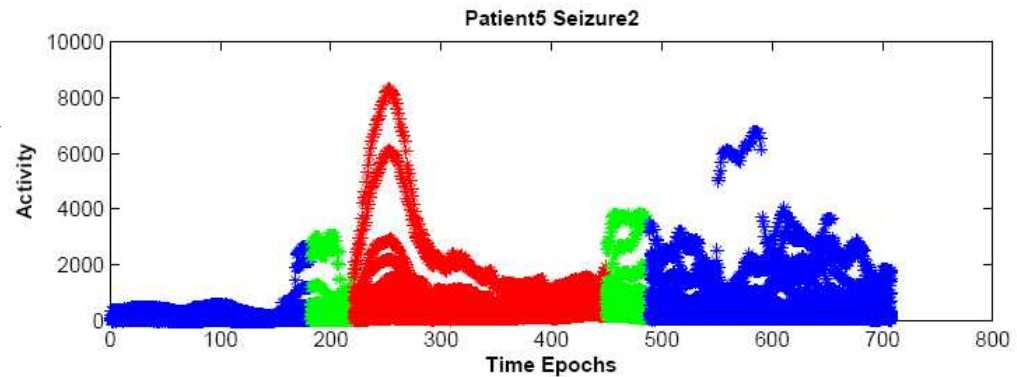
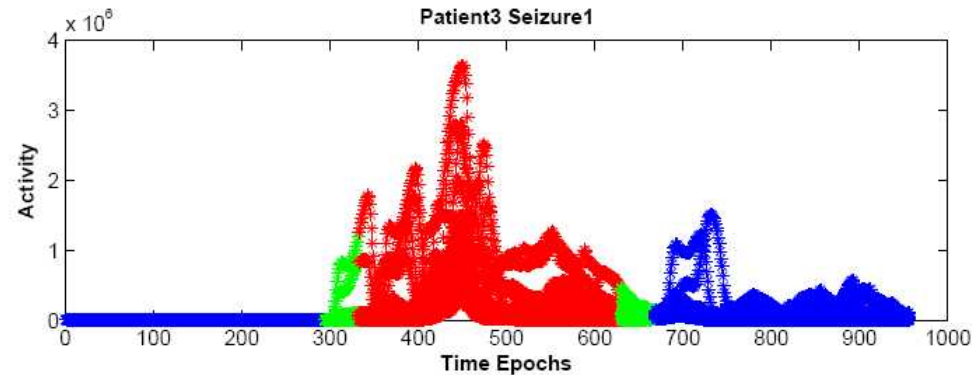
PID	Activity	Mobility	Complexity	Mean Abs. Slope	Spatial Info	Median Freq.	Spectral Entropy
1	✓	✓	✓	✓	✓	×	✓
2	✓	✓	✓	✓	✓	×	✓
3	✓	✓	✓	×	✓	×	✓
4	✓	✓	✓	×	✓	×	✓
5	✓	✓	✓	×	×	×	✓
6	✓	✓	✓	×	✓	×	×
7	✓	✓	✓	✓	✓	×	✓
8	✓	✓	✓	✓	✓	×	×
9	✓	✓	×	×	✓	×	×



DATA (Patient Non-Specific Seizure Recognition)

- Collected in the epilepsy monitoring unit of
 - Yeditepe University Hospital (Istanbul, Turkey)
 - Albany Medical College (NY, USA)
- 26 seizures from 9 patients (left or right temporal)
- Eleven Features: Activity, Complexity, Mobility, Mean Absolute Slope, Spatial Information, Spectral Entropy, Median Frequency, **Relative Energy**.
- Preprocessing:
 - Filter at 50Hz/60Hz
 - Scaling within features mode
 - **Log transform**

Patient Seizure Size of an Epilepsy



■
■
■

Performance Evaluation

- **G-means:** $\sqrt{Sensitivity \times Specificity}$

Patient ID	NPLS+LDA (v1)	NPLS+LDA (v2)	NPLS+LDA (v1+heuristic)
1	87.7%	81.4%	89.0%
2	88.8%	87.0%	90.2%
3	83.7%	88.1%	85.2%
4	41.9%	84.7%	39.8%
5	95.6%	94.9%	96.9%
6	95.6%	92.6%	95.6%
7	94.5%	88.1%	95.6%
8	69.6%	71.1%	69.3%
9	68.1%	72.8%	68.6%
MEAN	80.6%	84.5%	81.1%



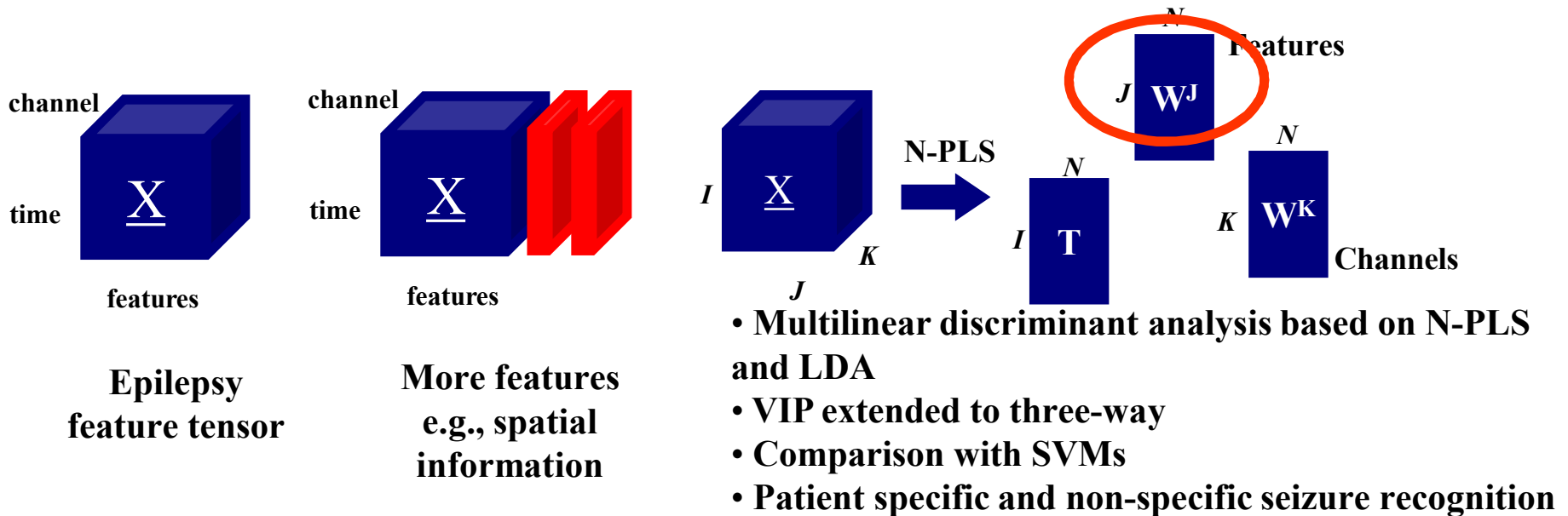
Results

- Average performance of patient-specific seizure recognition over 9 patients (32 seizures) is **85.8%**.
 - better performance using feature selection
 - performance comparable with SVMs and easier interpretation
 - feature selection may improve the understanding of epileptic seizures
- Average performance of patient non-specific seizure recognition over 9 patients (26 seizures) is **80.6%**.
 - heuristics to handle false-positives may improve the performance.



Summary

- Epileptic Seizure Recognition:**





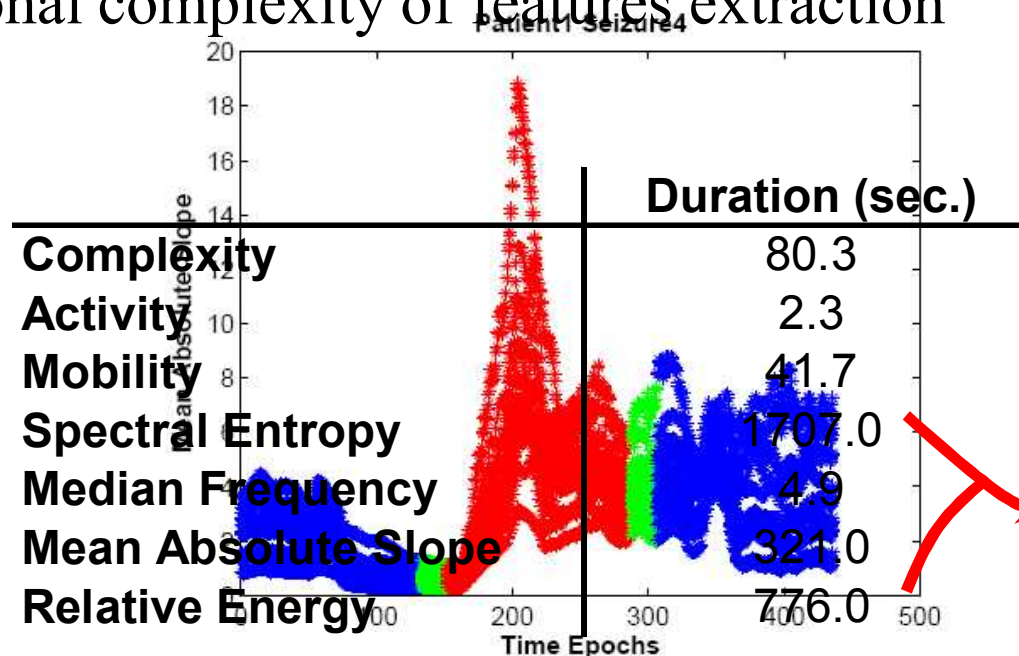
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Epilepsy Feature Tensor Construction

- Features can distinguish between pre-seizure and post-seizure.
- Computational complexity of features extraction

Example:

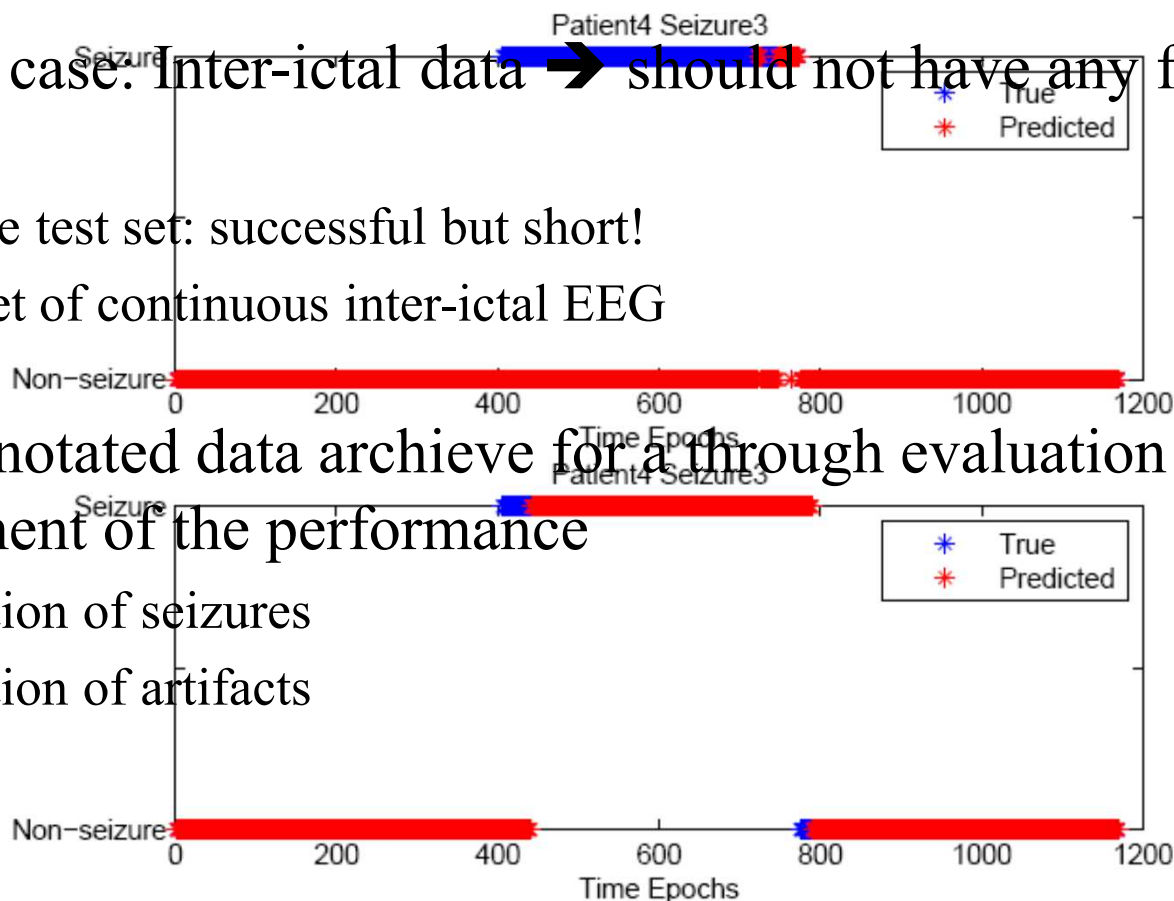


$O(n \log n) / \text{scale}$

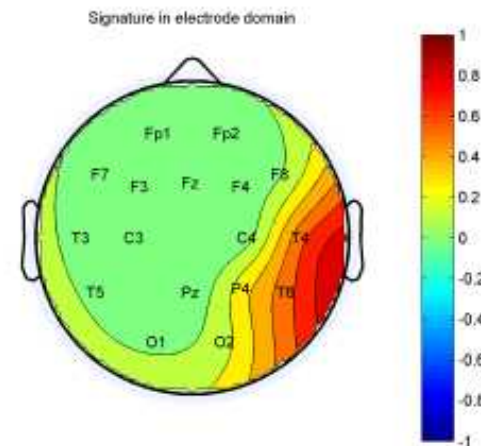
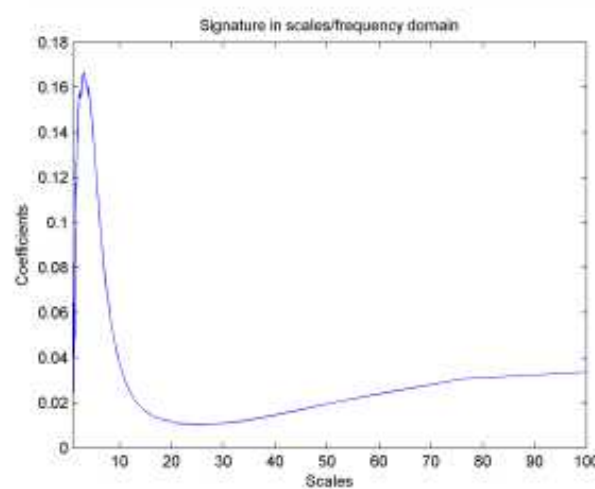
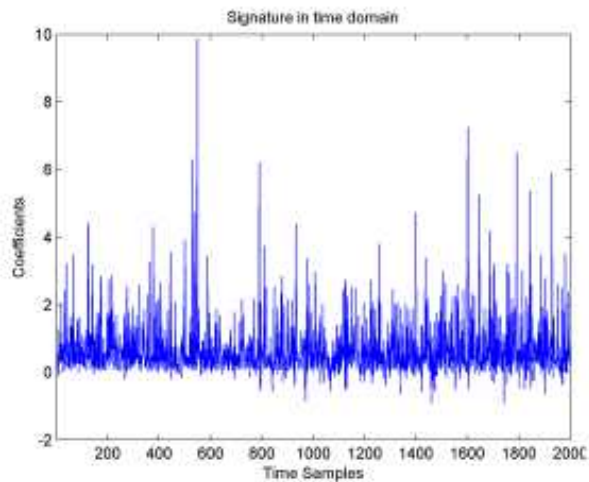
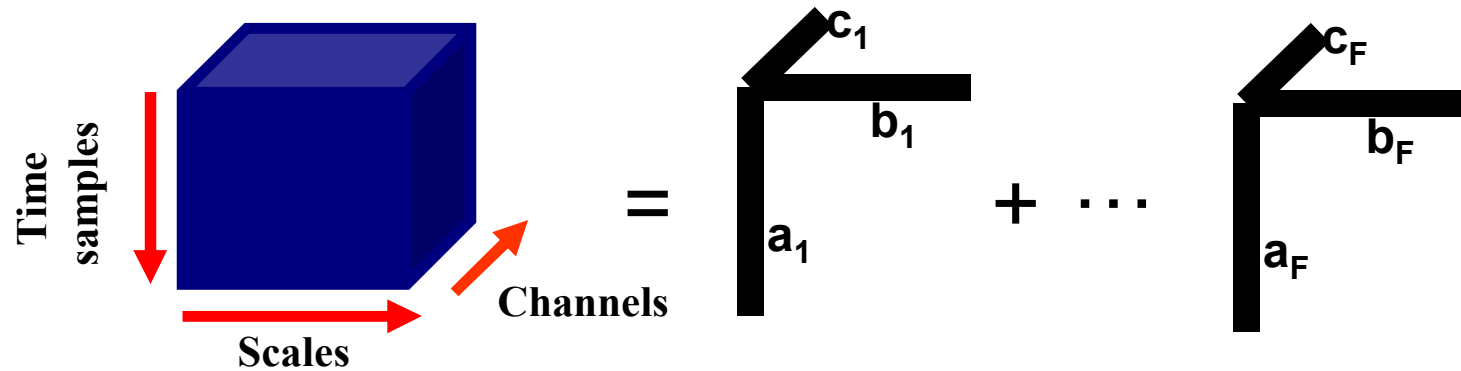


Seizure Recognition

- Log transform to handle inter-patient variation not enough!
- Good test case: Inter-ictal data → should not have any false positives!
 - 4-minute test set: successful but short!
 - Large set of continuous inter-ictal EEG
- Larger annotated data archive for a thorough evaluation and improvement of the performance
 - Annotation of seizures
 - Annotation of artifacts



Epilepsy Focus Localization





Thank you!

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MATLAB scripts: www.cs.rpi.edu/~acare/Epilepsy