



# REACTIVE NANO-FILMS OF AL AND PT

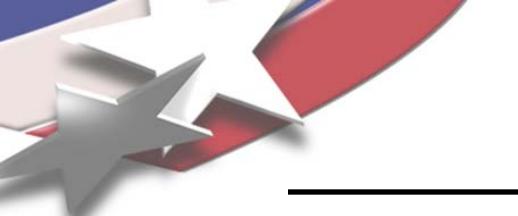
**8<sup>TH</sup> World Congress on Computational Mechanics (WCCM8)**

**5<sup>th</sup> European Congress on Computational Methods in Applied Sciences and Engineering (ECCOMAS 2008)**

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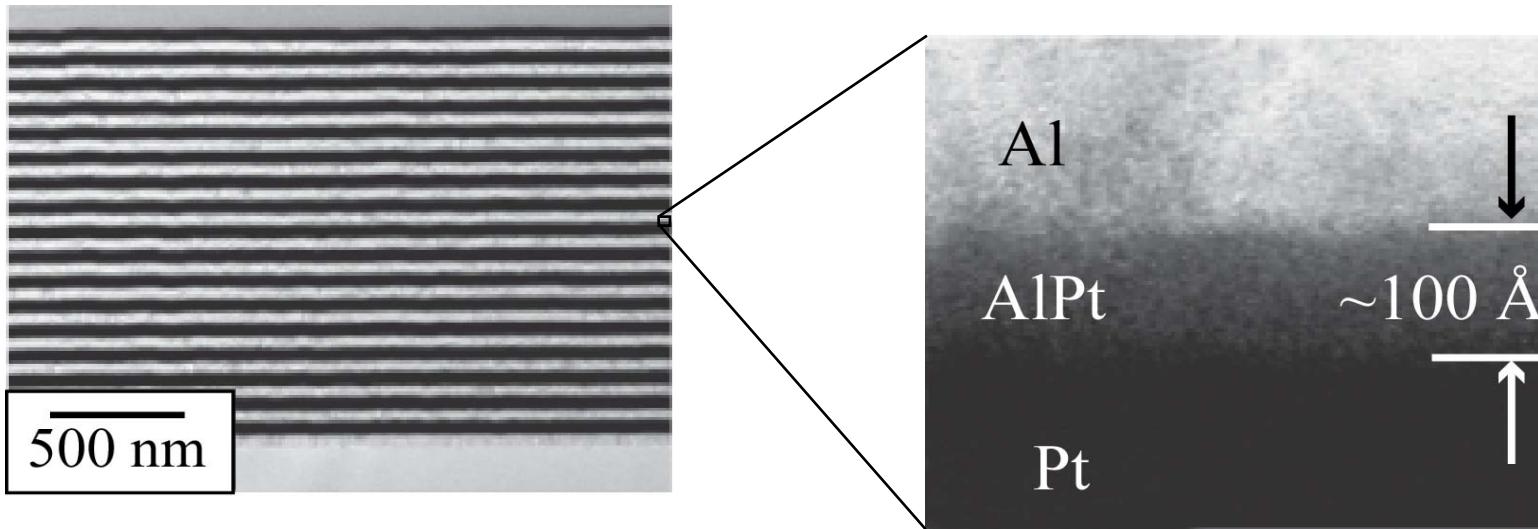
\*Sandia is a multiprogram laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the United States Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.



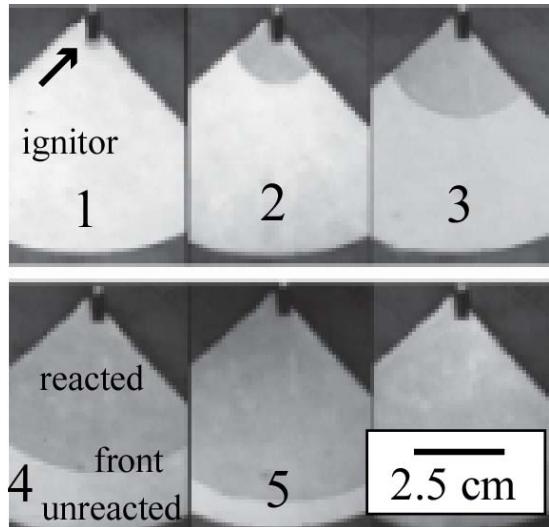
# Soldering or Brazing of Microelectronics

(Rapid, localized heating minimizes damage)

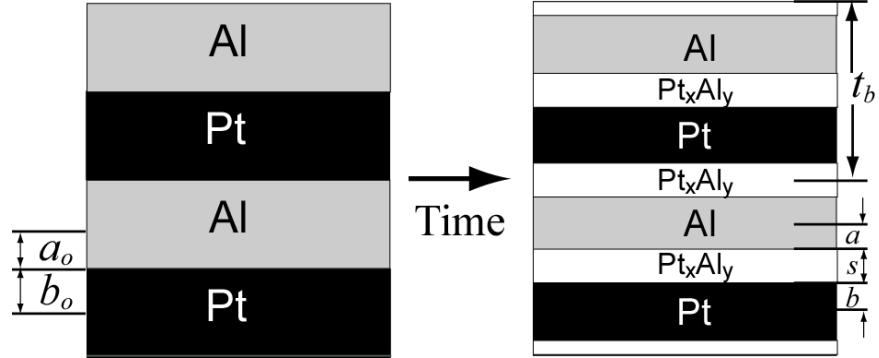
## Cross section



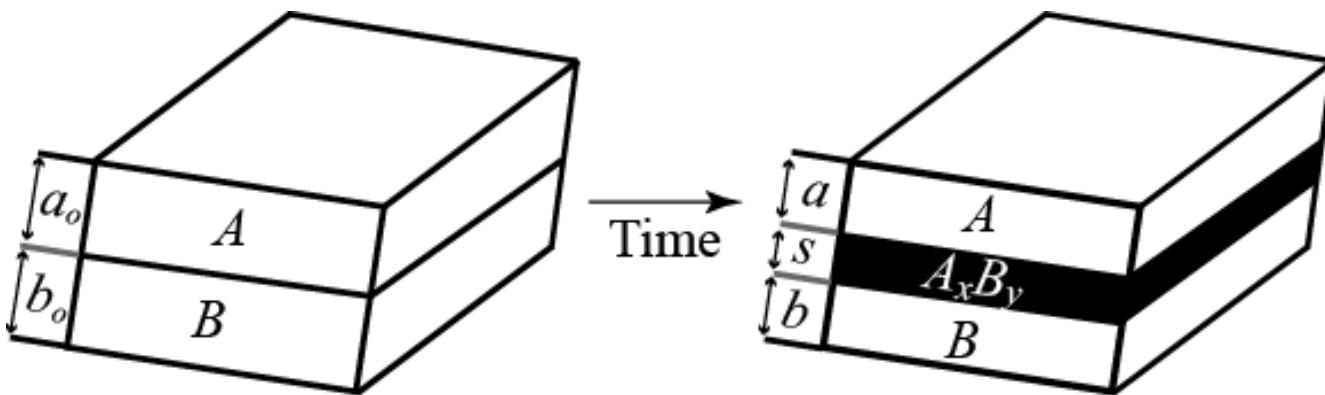
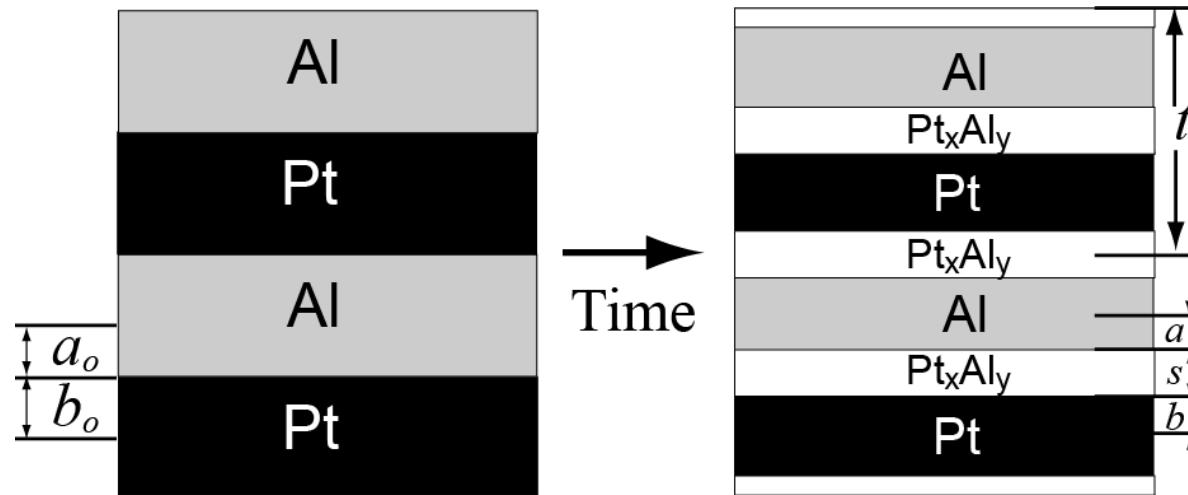
## Plan view



## Schematic

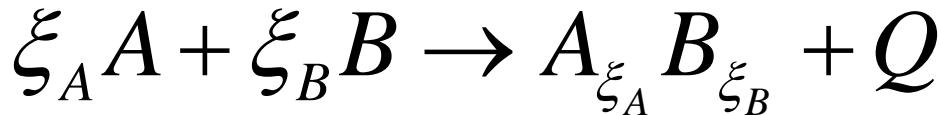
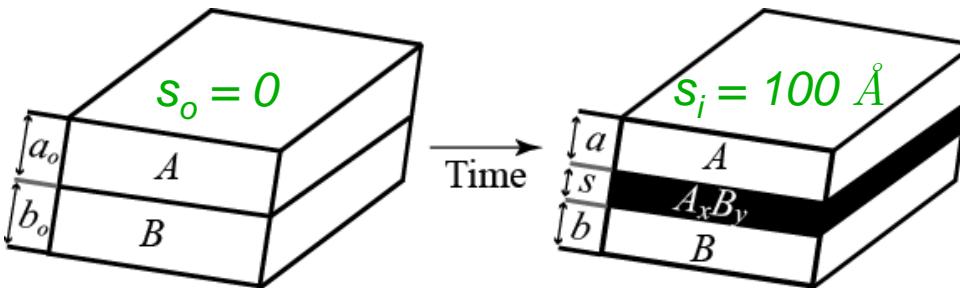


# Two bilayers of Al and Pt



$$t_b = 2(a + b + s)$$

# 1D diffusion controlled growth reaction with zero strain assumption\*



ODE's

$$\frac{da}{dt} = -\frac{D}{s}$$

$$\frac{db}{dt} = -\frac{b_o}{a_o} \frac{D}{s}$$

$$\frac{ds}{dt} = -\frac{D}{s} \left( 1 + \frac{b_o}{a_o} \right)$$

$$\frac{dF}{dt} = -\frac{D}{a_o s}$$

Auxiliary Eqns.

$$D = D_o \exp(-\frac{E}{RT})$$

$$a = \frac{a_o + b_o - s}{1 - \frac{\rho_A M_B \xi_B}{\rho_B M_A \xi_A}}$$

$$b = a \frac{\rho_A}{\rho_B} \frac{M_B}{M_A} \frac{\xi_B}{\xi_A}$$

$$\rho_{AB} = \frac{a_o \rho_A + b_o \rho_B}{a_o + b_o}$$

Algorithm

Choose  $a_o$ , calculate  $b_o$

Choose  $s_i$ , calculate  $a_i$ ,  $b_i$ , and  $F_i$

Solve ODE's for  $s$  and  $F$

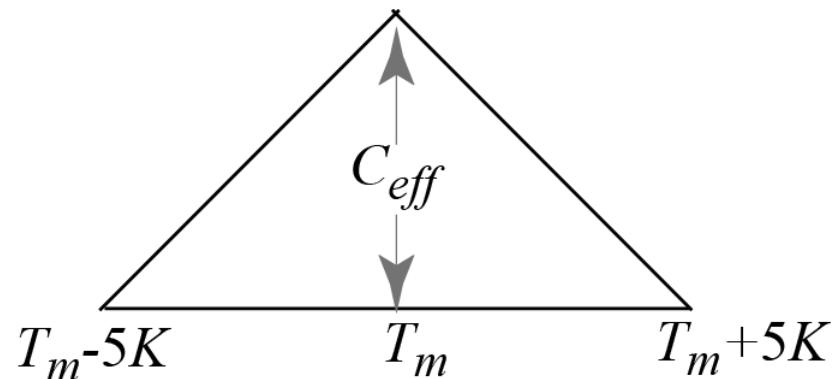
Energy Equation

$$\rho c \frac{\partial T}{\partial t} \nabla \cdot (k \nabla T) = -Q \rho \frac{dF}{dt}$$

\*Hardt AP and Phung PV, "Propagation of gasless reactions in solids—I. Analytical study of exothermic intermetallic reaction rates," *Combustion and Flame*, **21**, pp. 77-89, 1973.

# Parameters

Thermophysical Properties				
Property	Description	Al	Pt	AlPt
$c, \text{J/kgK}$	Specific Heat	894-900	133	226
$c_{\text{eff}}, \text{J/kgK}$	Effective $c$ at $T_m$	$h_{\text{fus}}/\circ \text{T}$	$h_{\text{fus}}/\circ \text{T}$	$h_{\text{fus}}/\circ \text{T}$
$\circ \text{T}, \text{K}$	half of mush zone	4-6	4-6	4-6
$h_f, \text{J/kg}$	Formation enthalpy	0	0	-901,000
$h_{\text{fus}}, \text{J/kg}^b$	Latent enthalpy	397,000	114,000	48,300; 100,000
$k, \text{W/mK}$	Thermal conductivity	213-261	71.6	158
$M_w, \text{kg/kgmol}$	Molecular weight	27.0	195	222
$\circ, \text{kg/m}^3$	Density	2700	21500	11600
$T_m, \text{K}$	Melting point	934	2040	934, 2040



## Diffusion model parameters

Property	Description	AlPt
$s_0, \text{m}$	Initial thickness of reacted layer	$1 \times 10^{-8}$
$D_0, \text{m}^2/\text{s}$	Initial diffusion coefficient	$1 \times 10^{-7}$
$E, \text{J/kgmol}$	Activation energy	$4.1868 \times 10^7$

$$\text{Area} = \frac{1}{2}(\text{Base} \times \text{Height})$$

$$h_{\text{fus}} = \frac{1}{2}(10 \text{ K} \times C_{T_{mp}})$$

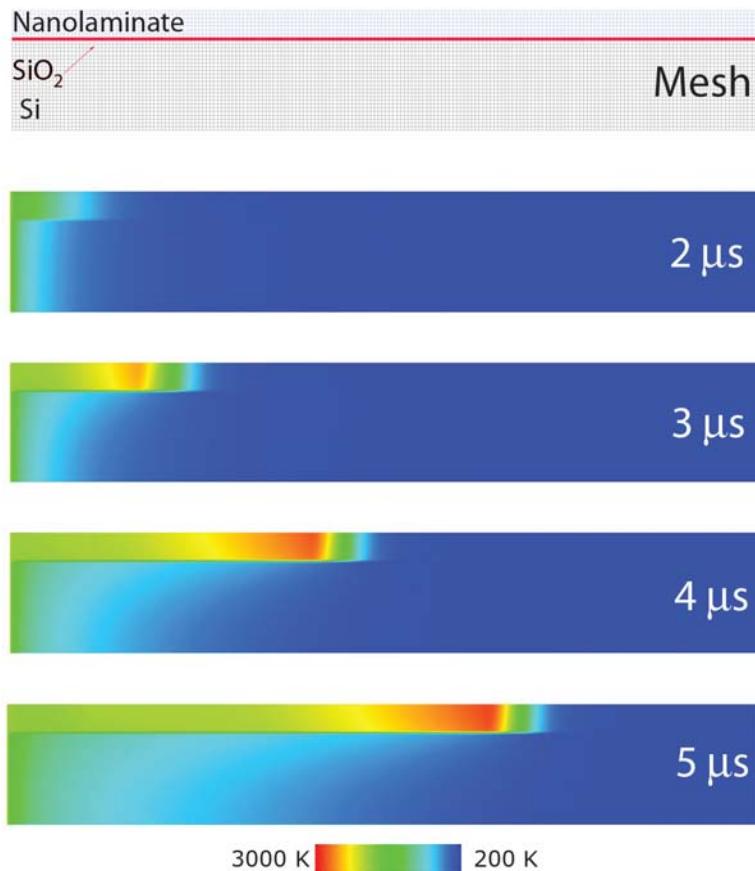
$$C_{T_{mp}} = 5 \times h_{\text{fus}}$$

## Two Phase Changes (Al, Pt)\*

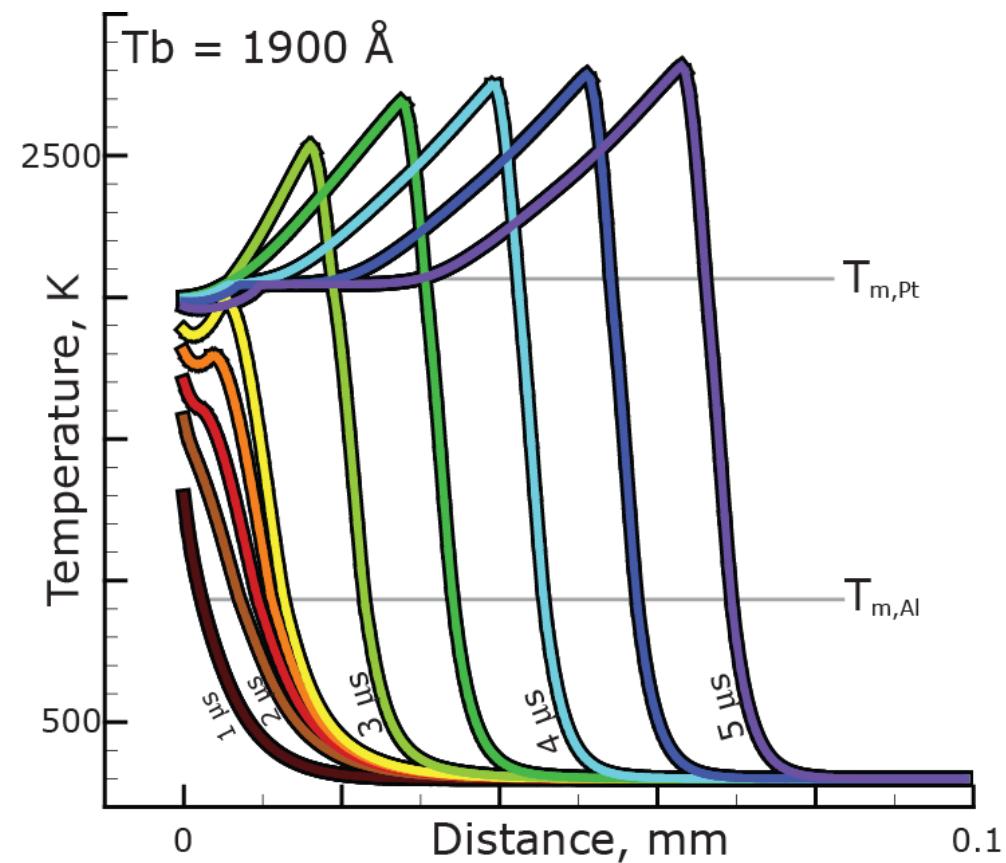
\*Effective capacitance method: Yao, L.S. and Prusa, J., Melting and freezing, *Advances in Heat Transfer*, 5<sup>th</sup> Edition, John Wiley & Sons, New York, 2002.

# Temperature profiles leading to ignition

## 2D Axisymmetric Temperature

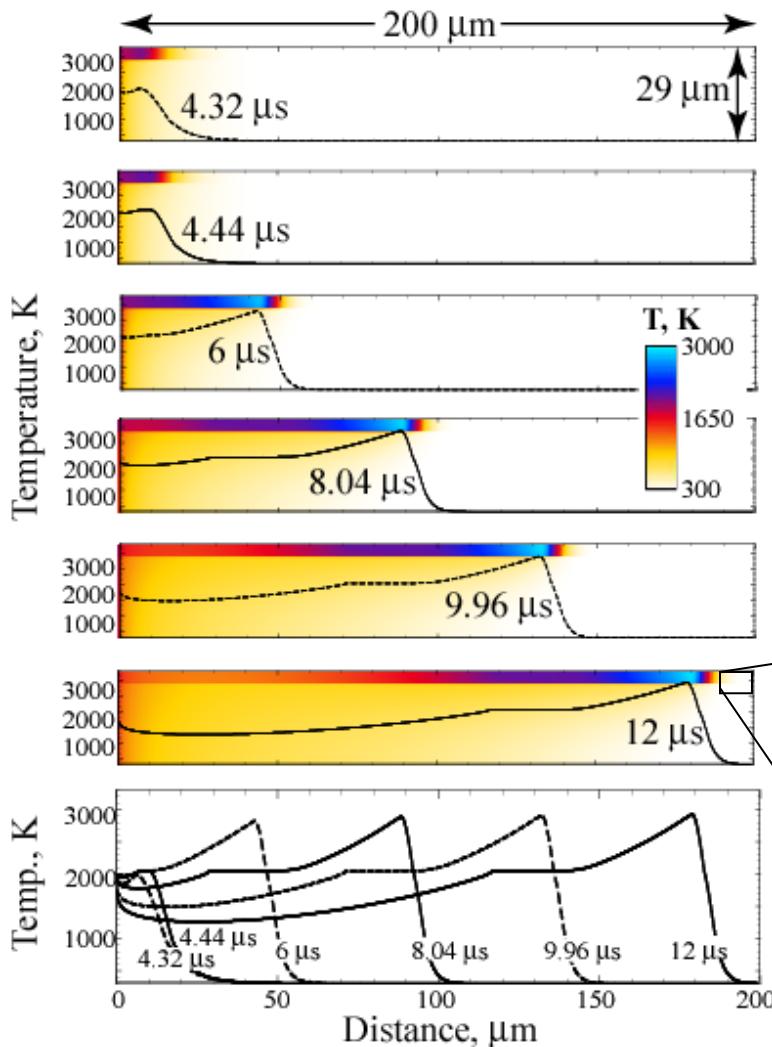


## Temperature on top of nanolaminate

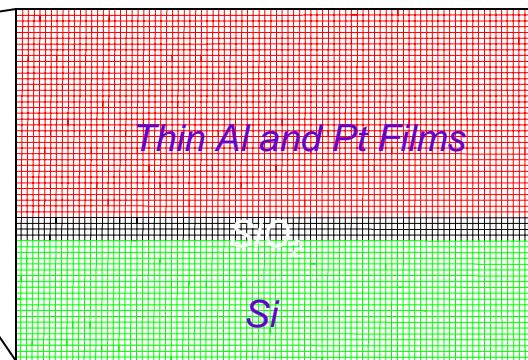


*Reaction energy sufficient to melt both layers*

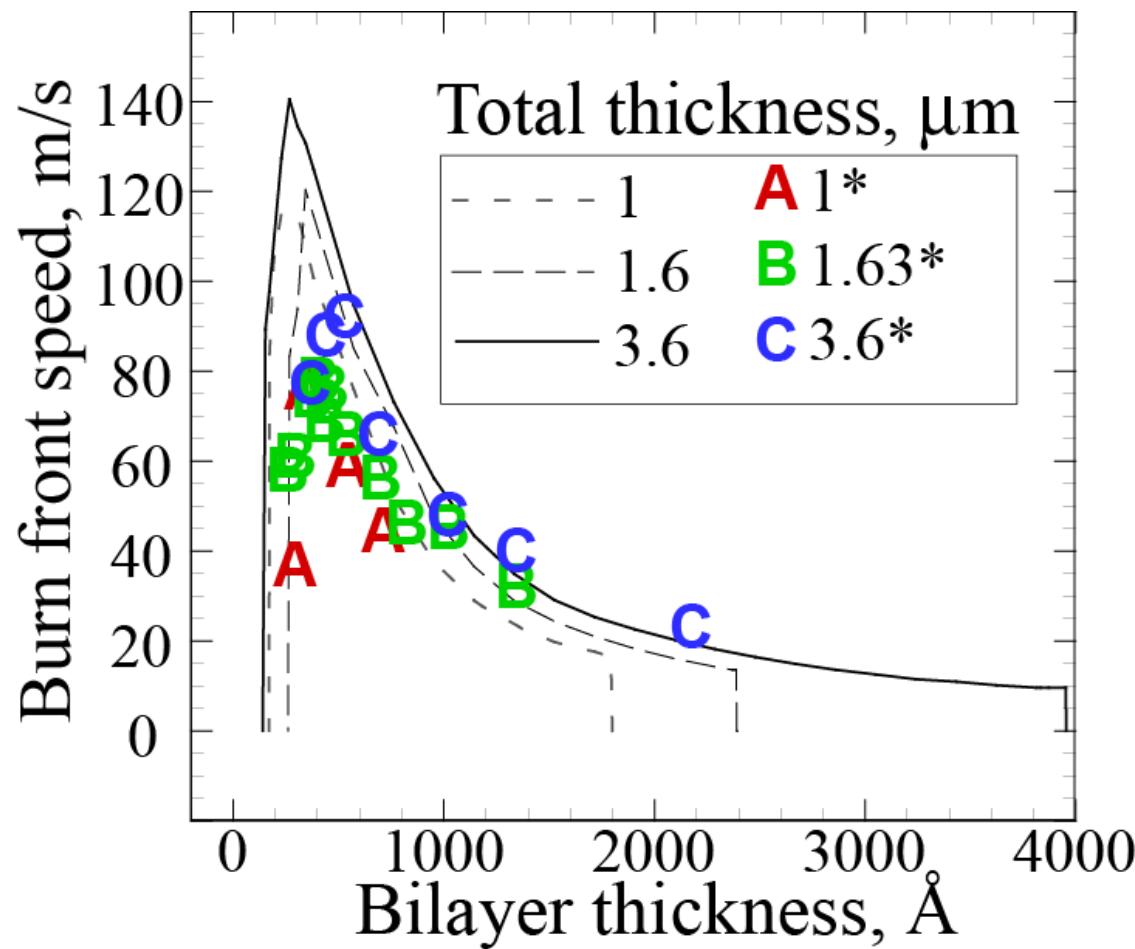
# 2D axisymmetric mesh (580,000 elements)



- Elements are  $0.1 \times 0.1 \mu\text{m}$
- Fixed time step,  $4 \times 10^{-10} \text{ s}$
- Ignition occurs  $\sim 10 \mu\text{m}$  from electric match
- Al melt in front of wave
- Solidification of AlPt should occur at 1830 K



# Front Velocity Variations with Bilayer Thickness



\*Adams DP, Rodriguez MA, Tigges CP, and Kotula PG, "Self-propagating, high-temperature combustion synthesis of rhombohedral AlPt thin films," *J. Mater. Res.*, Vol. 21(12), pp. 3168-3179 (2006).



# Summary and Conclusions

- The diffusion-limited model of Hardt and Phung has been used with a simple phase-change model to simulate the self-sustained, high temperature front propagation of Al/Pt nanolaminates on silicon substrates using a 2D axisymmetric finite element code.
- Results were within experimental uncertainty for nanolaminate thicknesses ranging from 1 to 3.6  $\mu\text{m}$
- Despite success, deficiencies should be addressed
  - Temperature dependent thermophysical properties
  - Solidification of mixed material
  - Strain due to thermal expansion
  - Adaptive mesh refinement
  - Stiff numerics