

# **Performance of Mesoscale Modeling Methods for Predicting Rheological Properties of charged Polystyrene/Water Suspensions**

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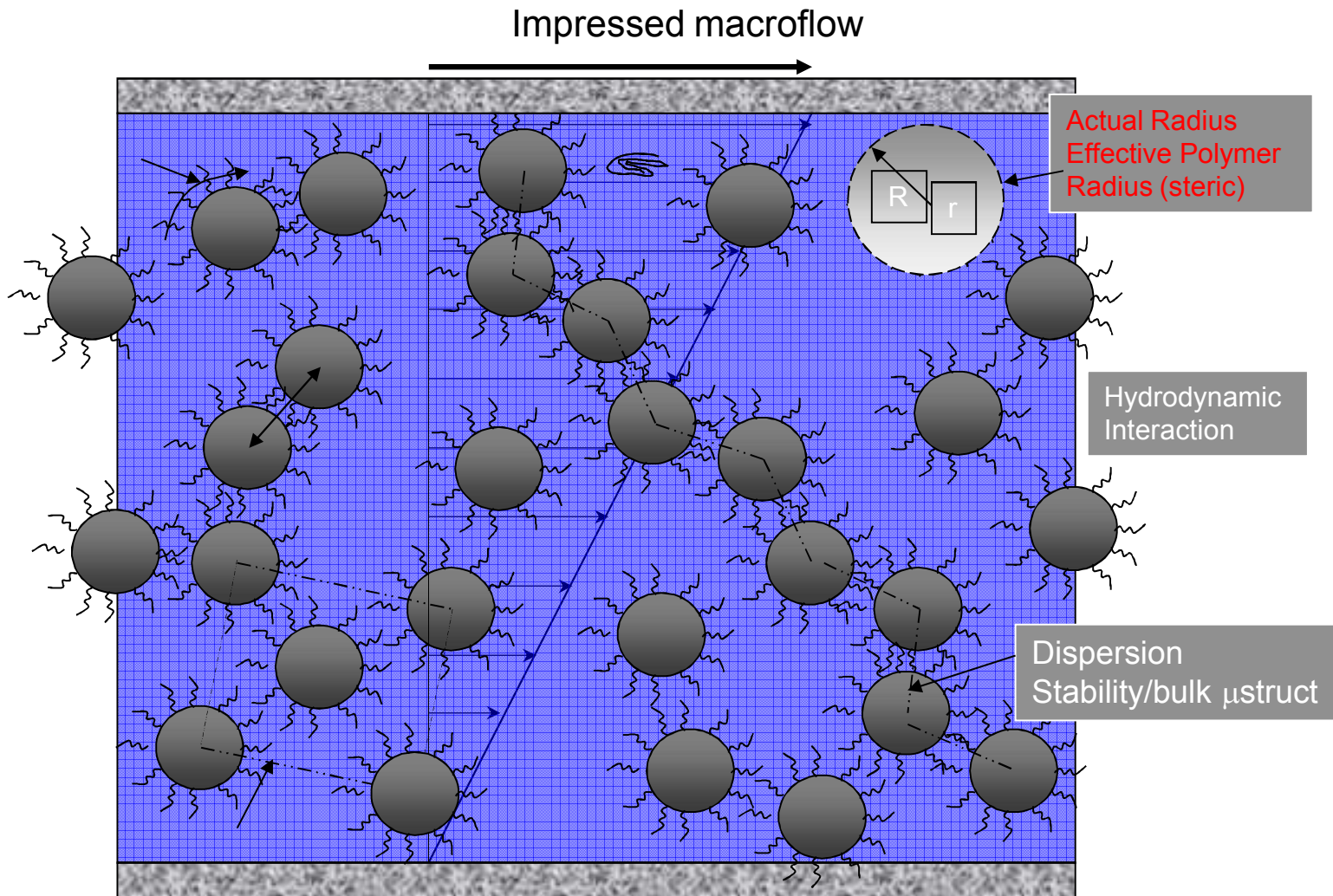


# Outline

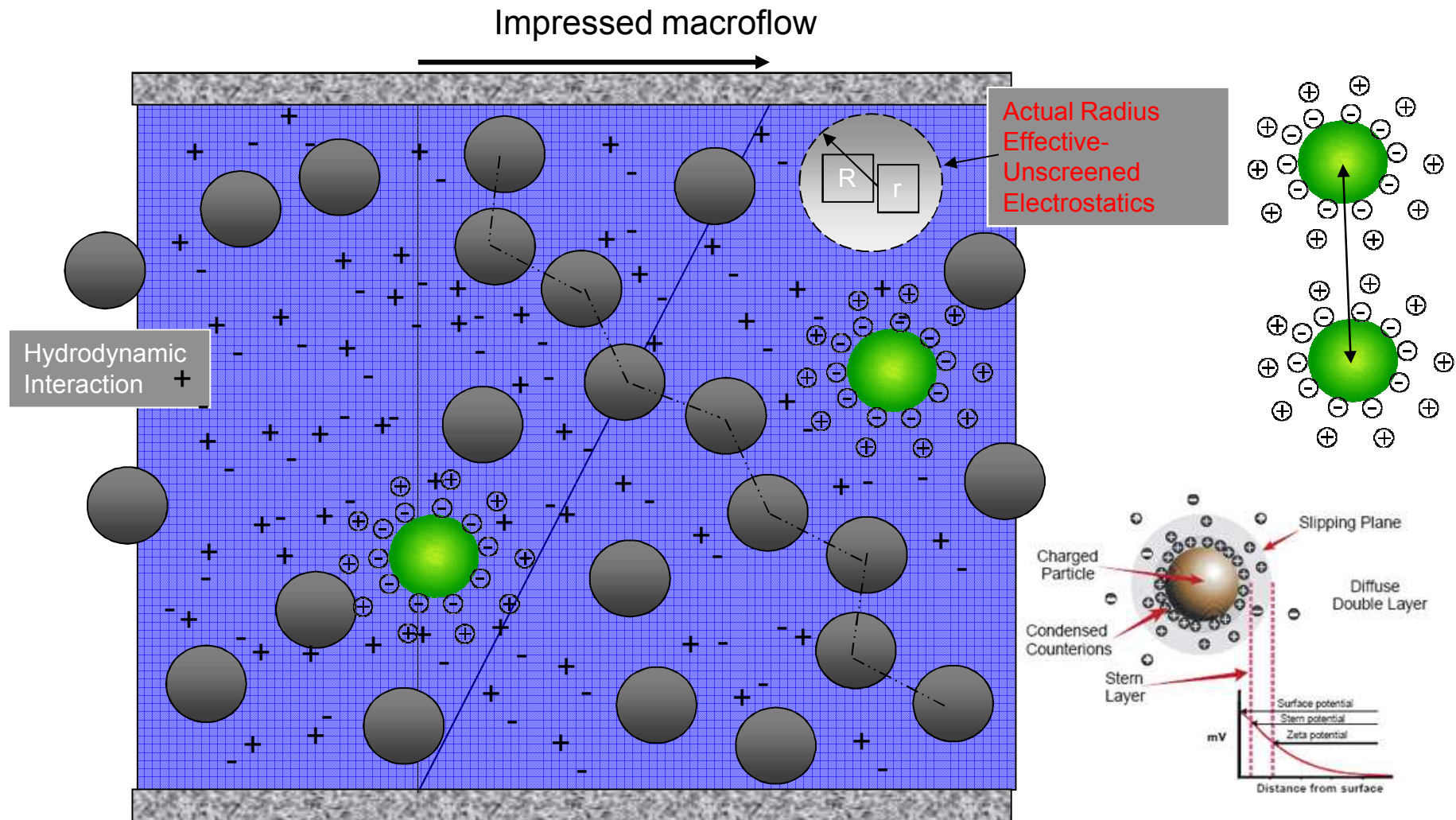
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- Meso-scale Modeling Methods for Nanoparticle Suspension Flows
  - SRD, DPD, FLD, FEM for solvent*
  - DEM with LAMMPS code for particles ([www.lammps.sandia.gov](http://www.lammps.sandia.gov))*
- Sample preparation and Rheological Testing
  - Charged polystyrene in water. 950 nm*
  - Shear rheology (steady and oscillatory)*
- Equilibrium structure properties, diffusivities, shear viscosity
  - Methods cross compare (performance and agreement)*
- Validation results
- Conclusions and Outlook

# Mesoscale Models of Suspension Dynamics



# Mesoscale Models of Suspension Structure/Dynamics- Charged Systems





# Overview of Nanoparticle Flow Project

## Colloidal (Nano) Particle Mechanics

### Methodology (Algorithms, Platforms, Requirements)

- N-body Newton-equation solver (translation/rotation)
- N-body Equilibrium Solver (long time)
- Distributed/parallel or of suitable performance
- Interface to add any effective pair-wise potentials
- LAMMPS or similar, expandable platform
- LAMMPS infrastructure changes (Particle Layers)
- Capable of handling massive contact/aspherics
- 10000 Particles, 3D.

### Long, Intermediate Range Interaction Models

- Effective potential development
- Solvent effects (solvation, brownian)
- Particle temperature (thermostat)
- Polymer brush effects (potentials)- attributes
- Coarse graining with aggregates
- ...

### Colloidal Contact Models

- Minorly aspherical
- Composite Particle structures
- Generally aspherical
- Elastic/Hertzian
- Viscoelastic

Active effort

Eliminated per requirements

## Flow Solver

### Algorithms, Platforms, Requirements

- High performance (parallel, or whatever)
  - ARIA, Goma, other
- Multiphase flow approach (effective Darcy Law, ...)
- Numerically stable at contact/near contact (stress singularities)
- FEM/FDM
  - ARIA, Goma (Explicit, SemImplicit, body-fitted grid/imbedded)
- Stokasian Dyn. (Specialized)
- BEM (Specialized)
- SRD (Pe of colloid part  $O(1)$ . Too expensive otherwise.
- DPD (limited Performance Depletion forces)
- LB (depletion forces)
- FLD - Frame-invariant pair-drag model

### Subgrid Models (contact/near contact)

- Dominate viscous modes
- Effect of polymer graft
- Effect of surface roughness
- Aspherical

## Coupled Multiphase Solver

### Methodology

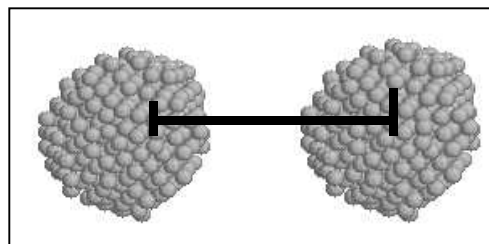
- CDFEM/DLM/Distributed volumetric source (Glowinski)
- Body fitted grids: remeshing and remapping as needed)
- Hybrid scheme: Imbedded interfaces + one-level adaptivity to capture surface
- Intrinsic: BEM, Stokasian Dynamic
- Implicit Solvent
- Explicit coarse-grained solvent/colloid collision

### Platform

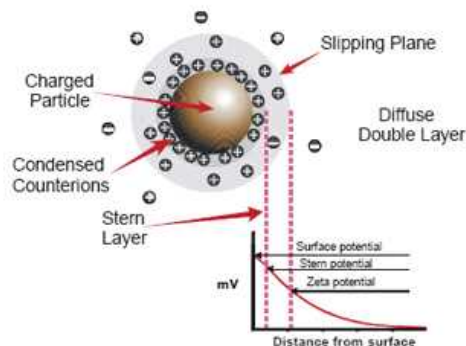
- LAMMPS
- ARIA
- Home grown

# About Coarse Graining - What is needed?

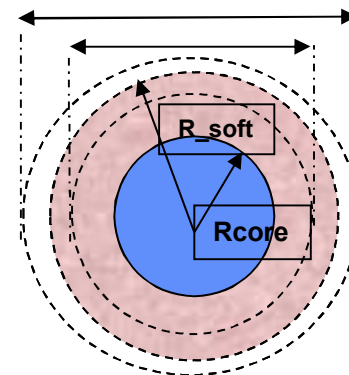
## Particle



e.g. Integration to Hamaker's equation and DLVO



electrostatic  
Structural  
representation

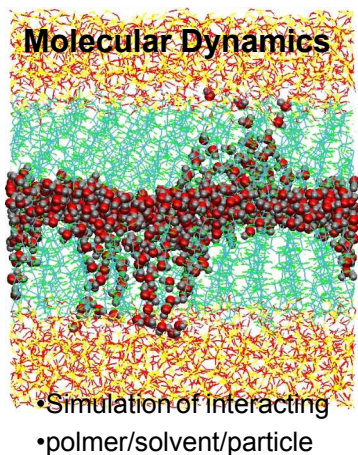


- Computational standoffs
- Polymer layer parameters
- **Screening layer thickness**
- Structural constants (polymer and hard sphere)

## Solvent

Blobs->SRD/DPD  
Dual particle approach

Continuum



QuickTime™ and a  
YUV422 codec decompressor  
are needed to see this picture.



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Motion JPEG OpenDML decompressor  
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# Framework + Methods Implemented and Tested

www.lammps.sandia.gov

## LAMMPS - DEM Solver

“COLLOID” Package for Pairwise Potentials  
(e.g. DLVO)



## EXTERNAL HYDRODYNAMICS SOLVERS

**MEZZO (ARIA)** - Incompressible  
Finite element flow solver

- Coupled with LAMMPS through  
overset grid CDFEM.
- Advantages: [completely general](#).
- Disadvantages: performance?

## LAMMPS PACKAGES FOR COARSE- GRAINED EXPLICIT HYDRODYNAMICS

**DPD** - Dissipative Particle Dynamics

- Explicit Solvent “particles”. Molecular dynamics  
framework. Solvent potentials.
- Advantages: no grid. [Full HI](#),
- Disadvantages: relatively more expensive.  
[Difficult to map to real system](#) (coarse grained)

**SRD** - Stochastic Rotation Dynamics

- Explicit Solvent “particles”. Molecular dynamics  
framework
- Advantages: [Full HI](#). [Highly scalable](#). [Intrinsic  
Brownian](#).
- Disadvantages: [Difficult to map to real system](#)

## LAMMPS PACKAGES FOR IMPLICIT HYDRODYNAMICS

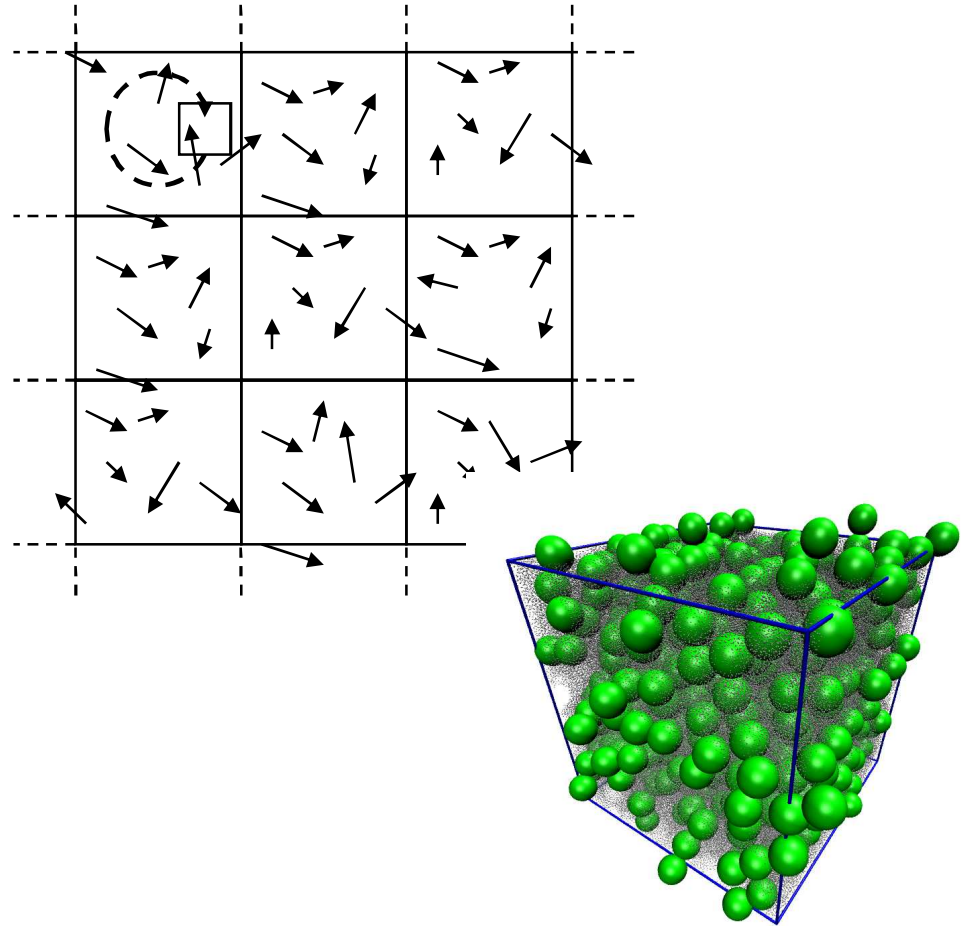
**SD** - Stokesian Dynamics with FLD  
simplification

- Ball-Melrose pair-drag models and  
FLD. Implicit, explicit integrator.  
Hydro through pairwise interactions  
and Long-range isotropic tensor
- Advantages: [Scalable](#).
- Disadvantages: spherical, needs  
tuning

# SRD - Stochastic Rotation Dynamics

## MPCD - Multi-Particle Collision Dynamics

- SRD is a point particle based fluid (mass, velocity), wherein the fluid interacts through collision operations
- Conserves linear momentum
- Produces fluctuating hydrodynamic behavior
- Computational efficient
  - No pair wise potential
  - SRD rotation does not limit time step
  - $10^3$  improvement over explicit Lennard-Jones solvent



*390 nm charged polystyrene  
In water being sheared (500 colloids+  
400000 srd particles)*

A. Malevanets, R. Kapral, J. Chem. Phys. **110**, 8605 (1999)

A. Malevanets, R. Kapral, J. Chem. Phys. **112**, 7260 (2000)





# DPD - Dissipative Particle Dynamics

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- Approach similar to Non-equilibrium Molecular Dynamics
  - Apply driving force
  - Measure response
- For suspension viscosity use Couette flow
  - Apply known shear rate
  - Measure system stresses
- Use Lees-Edwards BC and DPD thermostat
- Two types of particles
  - Solid (larger)
  - Fluid (smaller)
- Interaction forces
  - Solid-solid
    - DLVO theory for colloids
  - Solid-fluid
    - Standard DPD forces from literature
    - Currently working on highly viscous fluid
  - Fluid-fluid interactions
    - Standard from literature (Groot-Warren)

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TIFF (Uncompressed) decompressor  
are needed to see this picture.

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J. M. V. A. Koelman and P. J. Hoogerbrugge, *N*Dynamics Simulations of hard-sphere suspensions under steady shear, *Europhys. Lett.*, **21**, 363-368 (1993).

R. D. Groot and P. B. Warren, *N*Dissipative particle dynamics: Bridging the gap between atomistic and mesoscopic simulation, *J. Chem. Phys.* 107, 4423-4435 (1997).

# FLD - Fast Lubrication Dynamics

*Higdon, Kumar et al. UIUC*

## Hydrodynamic Interaction

**PME Stokesian Dynamics**  $O(N \log N)$

$$R = (I - \mathcal{R})^{-1} R_{1B} + R_{lub}$$

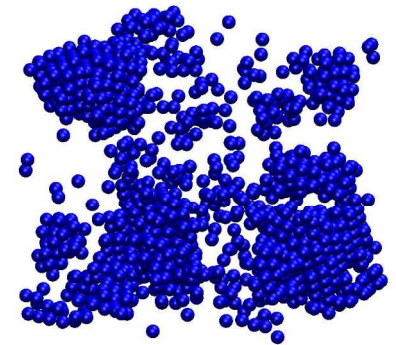
**Fast Lubrication Dynamics**  $O(N)$

$$R = R_0 + R_\delta$$

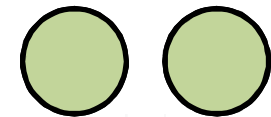
**Isotropic Constant**

$$\delta \text{ FLD} \sim 1/\delta$$

$$\delta\text{-log}\delta \text{ FLD} \sim 1/\delta + \ln(1/\delta)$$



690 nm charged polystyrene  
In water being sheared into phase  
separation



$\delta$

Wednesday, 21 October, 10:10 AM. Paper Number - SC32

Session Suspensions and Colloids. A. Kumar and J. Higdon

Charge effects on microstructure, rheology and order-disorder transitions for sheared colloidal crystals and suspensions



# CDFEM and Fluctuating Hydro and Colloidal Dynamics with Sierra/Mezzo

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- Coupled Aria and LAMMPS in Mezzo

Monodisperse spheres

$$\rho_f = 0.6$$

$$k_B T = 1.0$$

$$\nu = 1.67$$

- Can do 3D, no problem
- Parallel, no problem
- Currently
  - Quasi-static fluid (creeping Stokes) - novel velocity/pressure decoupling solver
  - Explicit time integration of colloid dynamics

$$\mathbf{v}^{n+1} = \mathbf{v}^n + \frac{\Delta t}{m} (\mathbf{R} \mathbf{v}^n + \sum \mathbf{f}^n)$$

$$\left( \frac{\Delta \mathbf{x}}{\Delta t} \right)^{n+1} = \mathbf{R}^{-1} \sum \mathbf{f}^n$$

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# Validation Tests, Experimental Program

- **System Characteristics**

Bangs Labs. Nominally 950 nm monodisperse. Required 0.003M SDS surfactant for stability. Zeta potentials measured with Malvern Zetasizer ZS (Light-scattering velocimetry)

Salt Concentration	$\kappa$	$\Psi_Z$	$\Psi_0$
1e-4 M	$3.25e7 \text{ m}^{-1}$	112.4 mV	114 mV
1e-3 M	$1.03e8 \text{ m}^{-1}$	116.6 mV	118mV
1e-2 M	$3.25e8 \text{ m}^{-1}$	124.2 mV	125 mV

$$\sigma = \sqrt{\epsilon\epsilon_0 kT} \sinh\left(\frac{e\Psi_0}{2KT}\right) c_{i0}^{1/2} \quad \sigma = \frac{2\epsilon\epsilon_0 \kappa KT}{e} \left[ \sinh\left(\frac{e\Psi_d}{2KT}\right) + \frac{2}{\kappa a} \tanh\left(\frac{e\Psi_d}{2KT}\right) \right] \quad \frac{1}{\kappa} = \sqrt{\frac{\epsilon\epsilon_0 kT}{1000e^2 N_{Av} c_{i0}}}$$

- **Particle Diffusivities**

BASF: Measurements forthcoming.

- **Dynamic Tests**

- Shear/Oscillatory. RFS Rheometer (TA Instruments).
- Viscosity is reproducible, though data is very scattered at low shear rates (No indication of settling or aggregation)
- Preshear at steady shear rate  $10 \text{ s}^{-1}$  for 300 seconds.
- Run a shear rate step test for 60s each at  $1 \text{ s}^{-1}$ ,  $10 \text{ s}^{-1}$ ,  $100 \text{ s}^{-1}$ , and  $10 \text{ s}^{-1}$
- Run a shear rate step test for 60s each at  $100 \text{ s}^{-1}$ ,  $200 \text{ s}^{-1}$ ,  $300 \text{ s}^{-1}$ , and  $500 \text{ s}^{-1}$ .



# Viscosity Measurements

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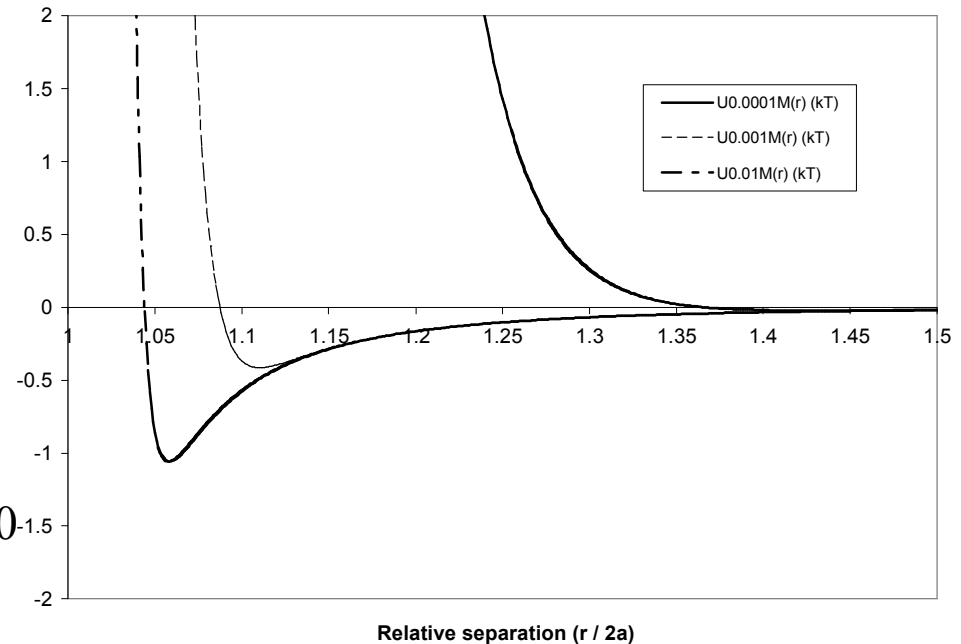
40 vol %

30 vol %

20 vol %

# Target Physical Parameters and Simulation Parameters

- Particle diameter – 950 nm
- Particle density – 1050 kg/m<sup>3</sup>
- Surface potential – 0.112-0.124 V
- Solvent viscosity – 0.001 Pa-sec
- Solvent density – 1000 kg/m<sup>3</sup>
- Temperature – 298 K
- Hamaker constant – 1.37E-20 J
- Nominal Particle volume fraction – 0.30



$$U_{vdw, att}(r) = -\frac{A_{cc}}{6} \left[ \frac{2a^2}{r^2 - 4a^2} + \frac{2a^2}{r^2} + \ln \left( \frac{r^2 - 4a^2}{r^2} \right) \right]$$

$$U_{vdw, rep}(r) = \frac{A_{cc}}{37800} \frac{\sigma^6}{r} \left[ \frac{r^2 - 14ar + 54a^2}{(r - 2a)^7} + \frac{r^2 + 4ar + 54a^2}{(r + 2a)^7} - 2 \frac{r^2 - 30a^2}{r^7} \right]$$

$$U_{el}(r) = \frac{64\pi kT \rho_{NaCl}(\infty) a \psi_0^2}{\kappa^2} e^{-\kappa(r-2a)}$$



# Target Colloidal Dispersion Properties for V&V

- Equilibrium Structure Properties

Pair distribution function, Coordination number, Cluster size distribution, Nearest neighbor distance, System energy per colloid, Cell density distribution, Order parameter

- Particle Mobility - Short-time and long-time diffusivity

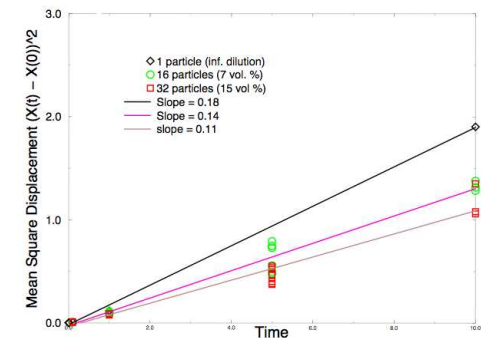
Measure mean-square displacement

- Shear viscosity (steady)

TriClinic Deforming Box,  
Muller-Plathe for bulk shear

- $G'$ ,  $G''$

Triclinic deforming box - FLD only

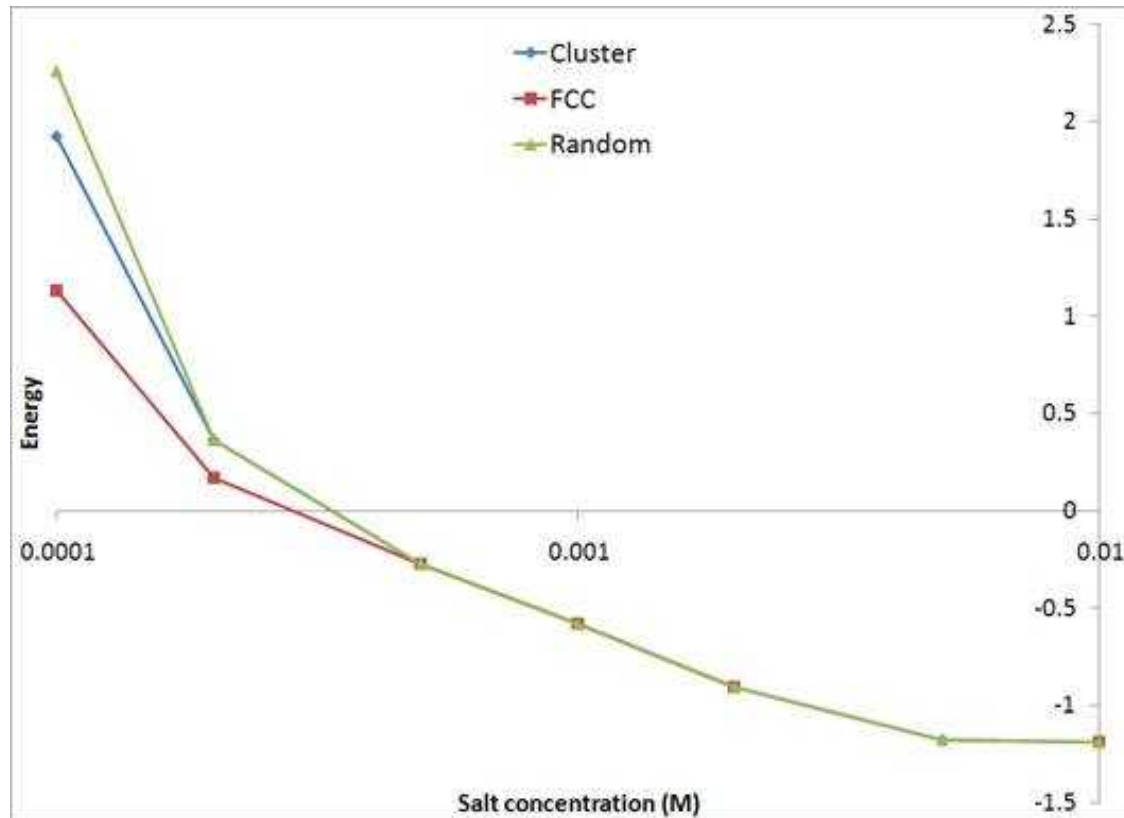


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# Equilibration

- Monte Carlo Simulations - System Energy per Colloid. Volume Fraction 0.3



**Under  $5 \times 10^{-4}$  M salt concentration, the systems can arrest at a local equilibrium.**

# Simulation Parameters

•Method	$\mu$	$\rho$	$U[r]$	T	No. Colloids	$\square$ Pe/Cld*
•FLD	0.001 Pa-s	1000 kg/m <sup>3</sup>	As Shown	298K	256-1370	196/3
•FEM	0.001 Pa-s	1000 kg/m <sup>3</sup>	As Shown	298K	256-??	196/3
•SRD	1e-8 Pa-s	1000 kg/m <sup>3</sup>	A=1.4e-25 J	2.8e-3K	256	196/2.9
•DPD	<0.001 Pa-s	1000 kg/m <sup>3</sup>	As Shown	298K	216	196**/2.9

$$m_i \frac{d^2 \underline{r}_i}{dt^2} = \underline{F}_i^H + \underline{F}_i^B + \sum_j \underline{F}_{ij}^P$$

$$Pe = \frac{\text{Colloid Advection time}}{\text{Colloid diffusion time}} = \frac{8\mu \dot{\gamma} a^3}{kT}$$

$$Cld = \frac{\text{Colloidal Forces}}{\text{Hydrodynamic forces}} = \frac{A_{cc}}{kT}$$

\*Based on 100 s<sup>-1</sup>, 298K

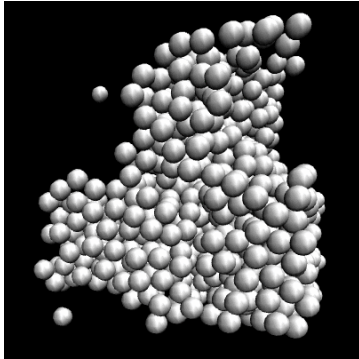
\*\*Achieved by adjusting the effective shear rate

# Sample Results (SRD)

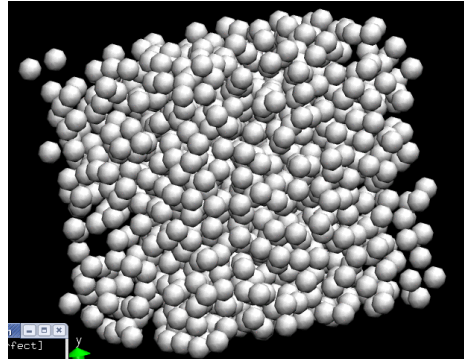
Shear-Rate  $85 \text{ s}^{-1}$

- Volume fraction 0.30; Surface potential 33 mV and 300 mV;

•30 mV

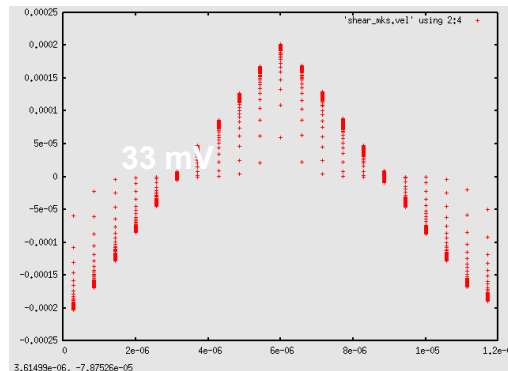
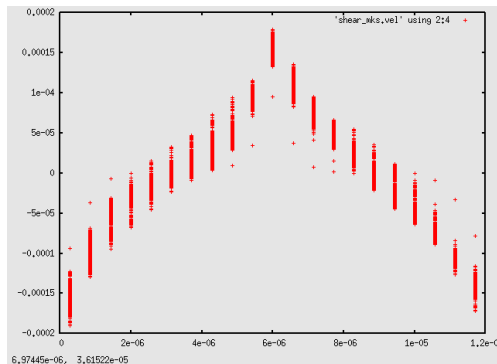


•300 mV



•300 mV, Electrolyte concentration 0.0001 M

•Electrolyte concentration 0.1 M

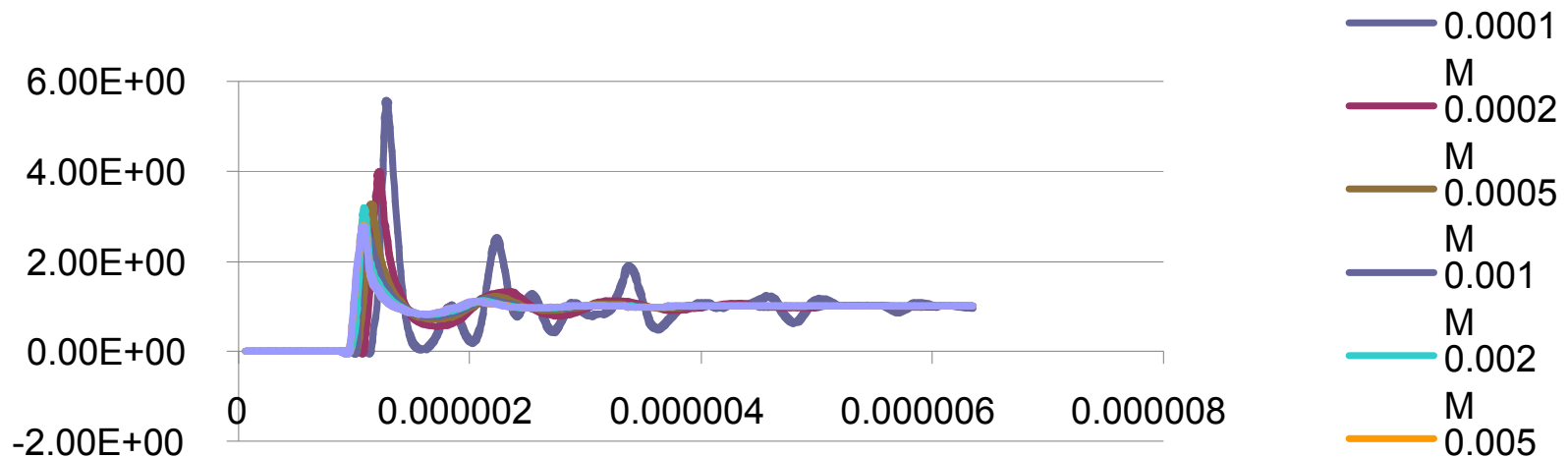


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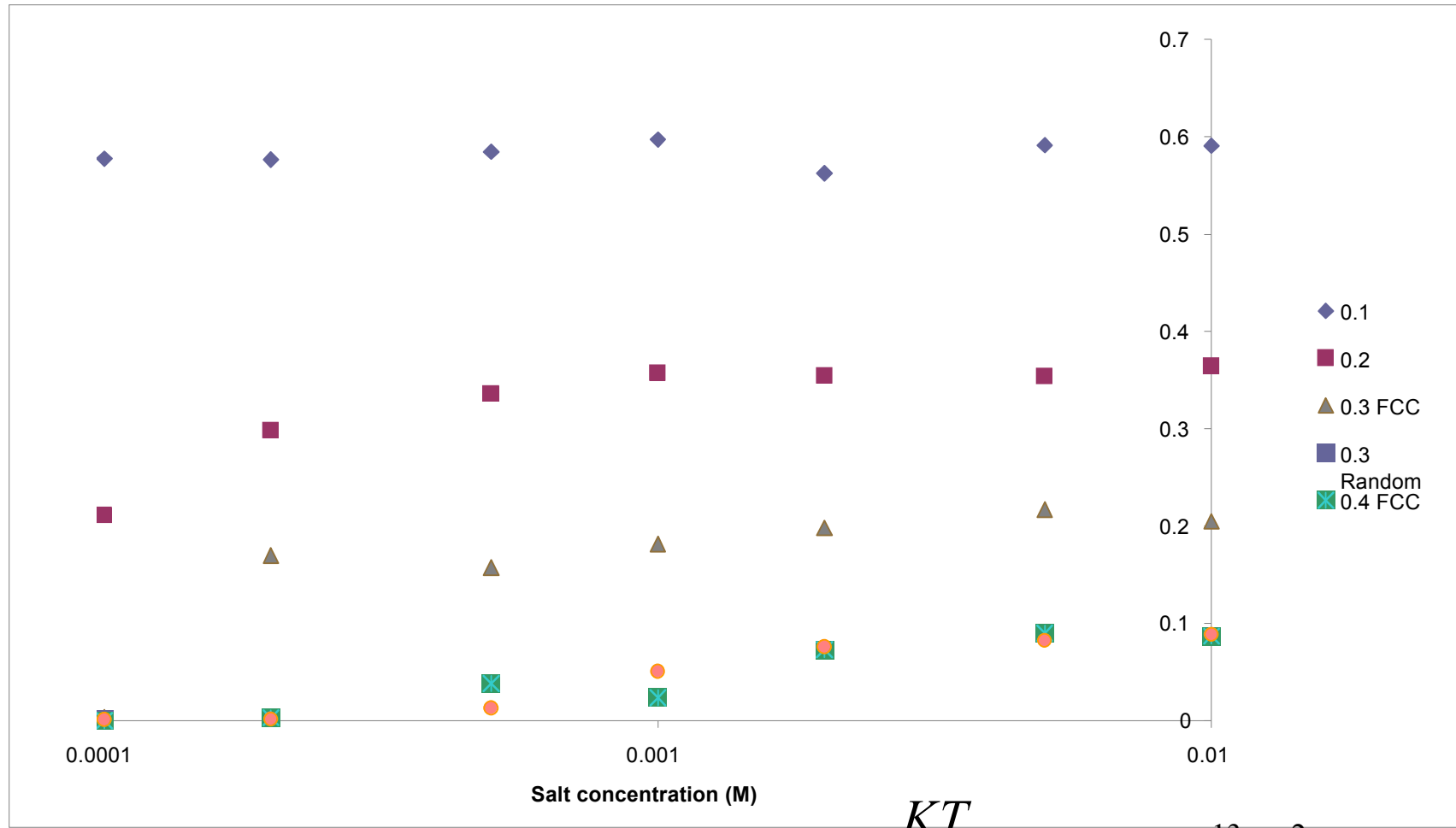
•Velocity Profile - MP Method

# Cross-Comparison: Equilibrium Structure Properties

**$\phi = 0.3$ , random IC**



# Cross-Comparison: Diffusivities

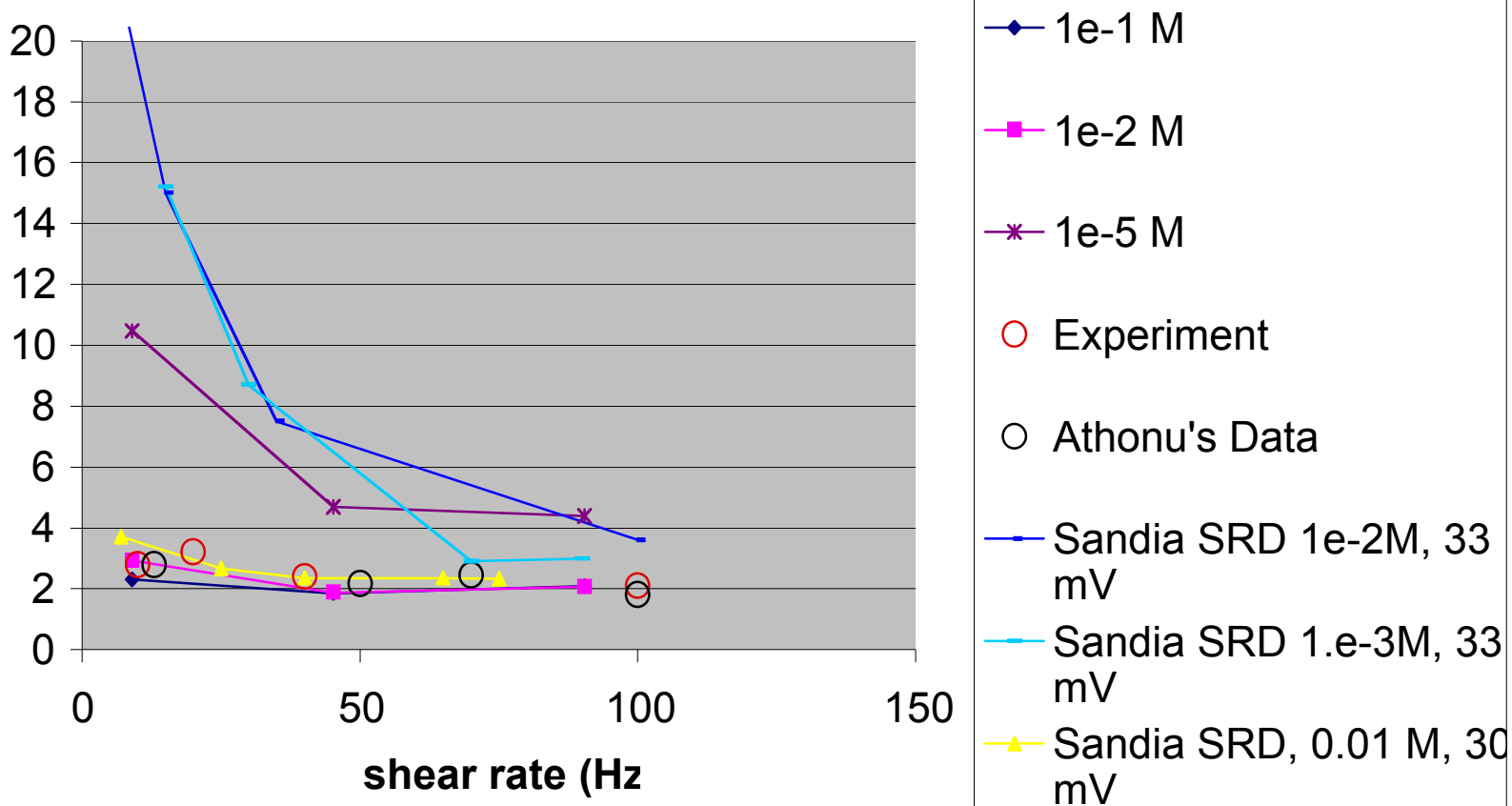


$$D_0 = \frac{KT}{6\pi\mu a} = 4.6 \times 10^{-13} m^2/s$$



## Cross Comparison for Rheology. Experimental comparison

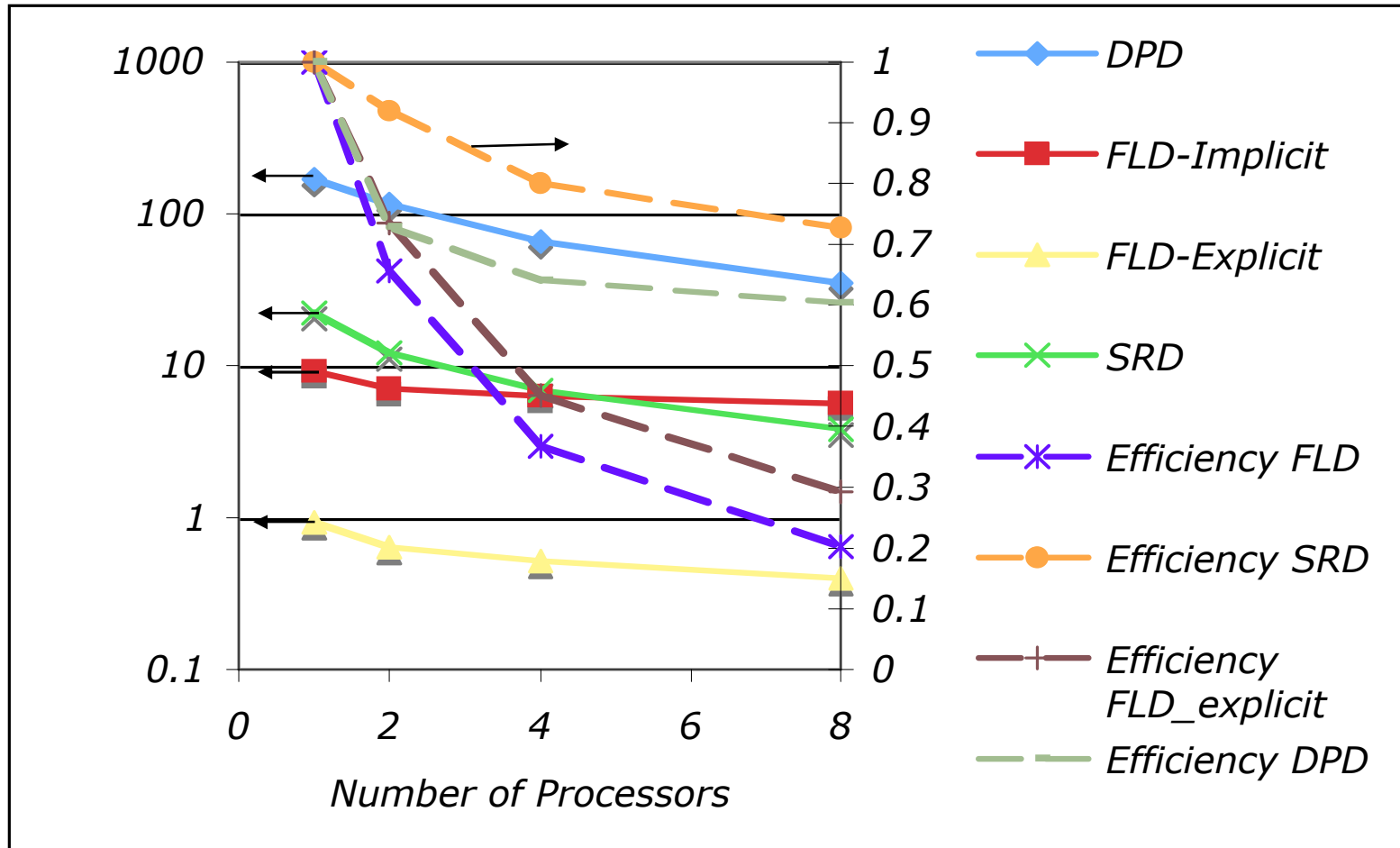
### 30% PS Suspensio



# Performance Comparison

0.3 Vol. % PS in Water, 0.001M NaCL, ~220-256 Colloids

- Time reported for 1000 time steps for equilibration/diffusion measurement run. Timings on 8000-node T-Bird Machine: Dual 3.6 GHz Intel EM64T Processors.





# Performance Comparison - The Real Story

0.3 Vol. % PS in Water, 0.001M NaCL, ~220-256 Colloids

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- Parallel Performance of FLD-Implicit:

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are needed to see this picture.

- Wall-Clock Time to Integrate to 1 s real time (4 Proc):

<u>FLD</u>	<u>FLD expl</u>	<u>SRD</u>	<u>DPD</u>
124 s	49,961s (13.8 hrs)	69,000 s (~19 hrs) ~2 hrs on 32 proc	~300 hrs

- So why not simply go with implicit FLD? Accuracy and Stokes...



# Retrospective and Outlook

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Implemented/Developed and demonstrated four solver-methods for dynamics of meso-scale simulations of colloidal suspensions -- *Our work is aimed at the nanoparticle scale.*

Presented verification and validation results (cross-compare and comparisons with experimental test data)

- Radial distribution functions compare well across all methods, verifying potentials
- Diffusivities predicted by FLD and SRD agree at 0.2 and 0.3 volume fraction. DPD-predicted diffusivities suspect at all volume fractions.
- Viscosity at moderate shear rates ( $1\text{-}100\text{ s}^{-1}$ ) predicted well vs. volume fraction.

SRD shows the best parallel scalability. FLD-Impl the most cost-effective despite its limitations.

Considering the overall criteria of “Better, faster”:

- Winner: Give to FLD\_impl for overall efficiency.
- Loser: Give to DPD for lack of efficiency and accuracy.

SDS confounding our validation effort and in some sense spoiling it. Suspected that a coating is influencing the effecting Hamaker constant and influencing the effective potential.

DPD is just too compute-intensive for this class of problem to be practical, notwithstanding its issues with accuracy. Reasons are primarily time-step limitations, and inefficient solvent representation.



# Acknowledgements

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- Chris Brotherton, Sandia
- Roger Bonnecaze, UT Austin
- Nanoparticle Flow Consortium (NPFC)