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# Precision Volume Measurements: Challenges to Reducing Uncertainties

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**Accurate volume determination is extremely important in many disciplines**

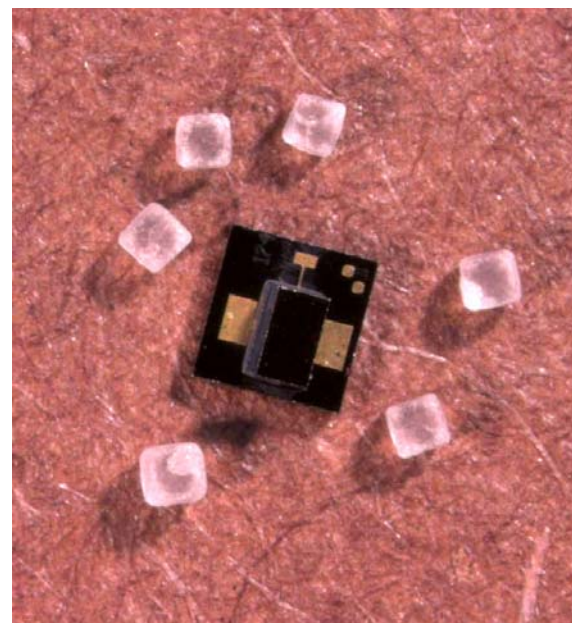
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$$P V = n R T$$

**The ideal gas law is used in many, many applications**

- Semiconductor industry
- Aerospace
- Defense
- Automobile
- Energy

**In this talk, we will focus on the measurement of VOLUME.**



***30 nanoliter MEMS device surrounded by grains of table salt.***

# Precision gas volume measurements

## Selected previous methods

- Gravimetric: liquid filled (even mercury filled)
- Volume expansion – still need a standard
- Pressure rise with calibrated leaks

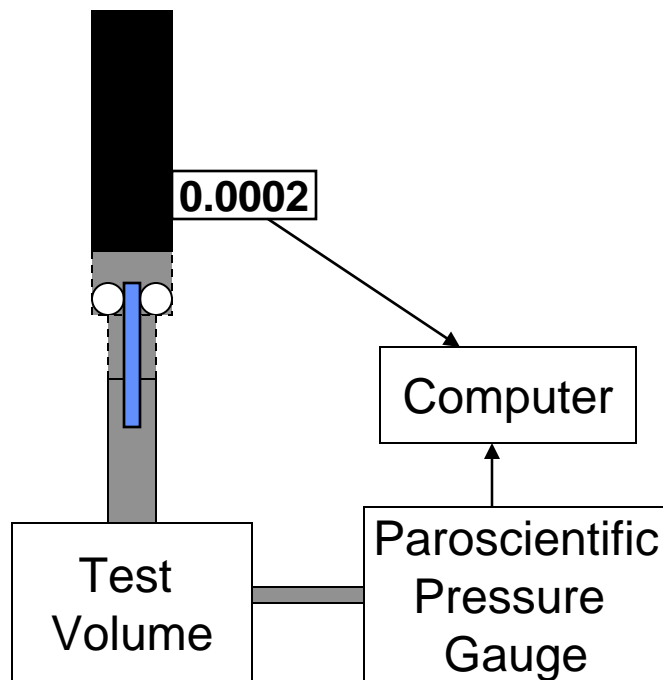
## Need a method for determining volumes...

- Of complex manifolds
- Without exposing the manifold or part to a liquid
- That minimizes impact of outgassing and virtual leaks

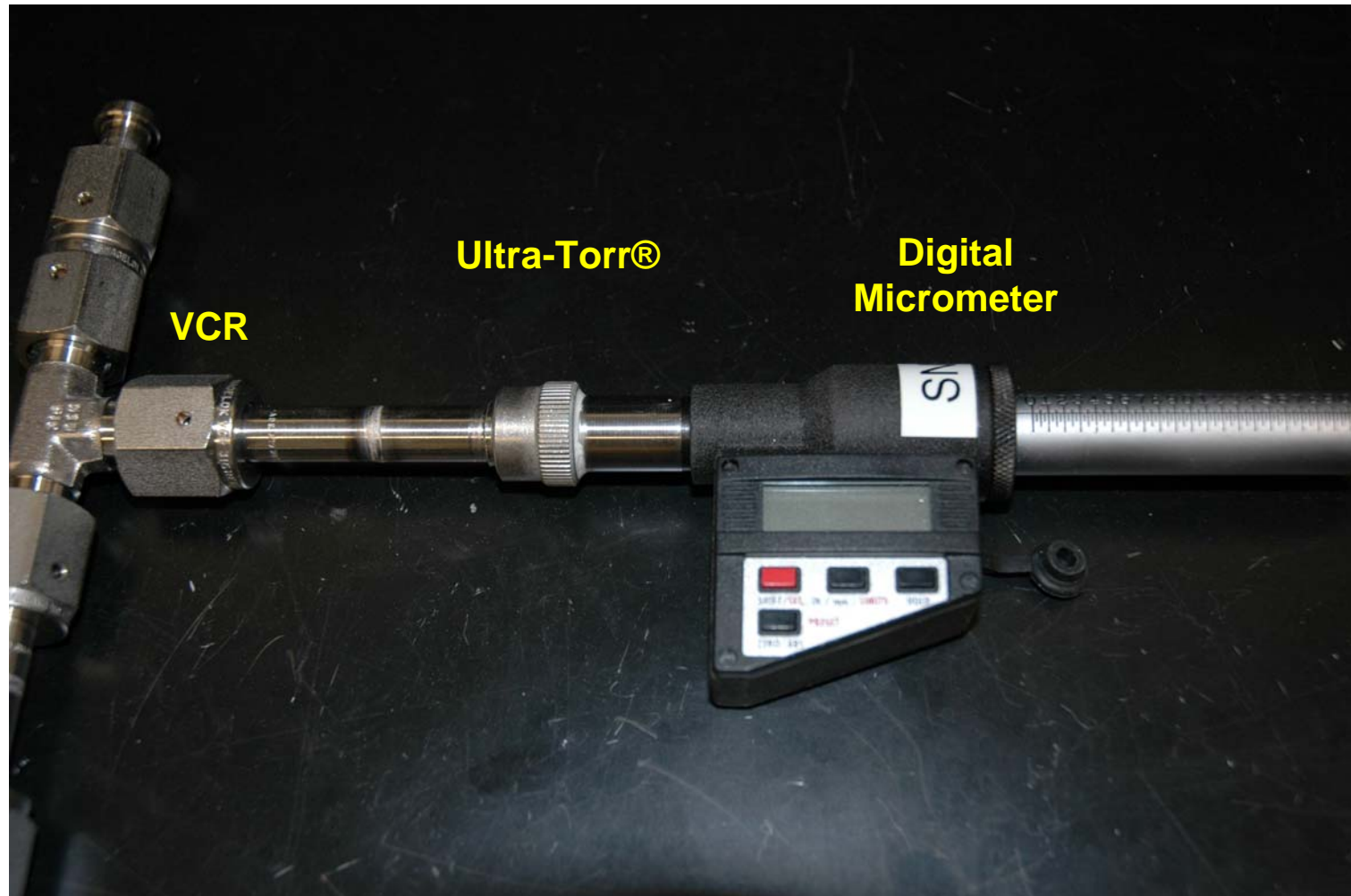


# Block diagram of the experiment

The experiment involves moving a piston (shown in blue) in or out of the test volume a known distance and recording the induced pressure change.



# Micrometer assembly





# Theory - derivation of equation

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- Assume isothermal
- Simple equation
- We bypass the direct solution for  $V_1$  in favor of the least-squares compatible form.

$$P_1 V_1 = P_2 V_2$$

$$P_1 V_1 = P_2 (V_1 + dV)$$

$$V_1 = \left( \frac{P_2}{P_1 - P_2} \right) dV$$

$$dV = V_1 \frac{P_1}{P_2} - V_1$$

Slope  $\nearrow$  Intercept  $\nwarrow$



# What are the contributors to the measured volume uncertainty?

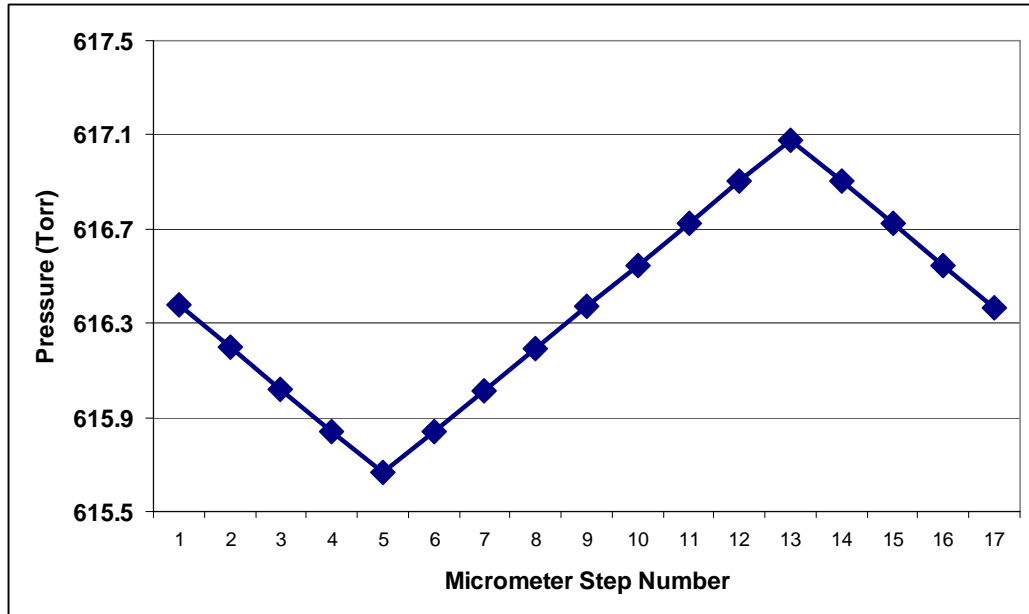
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$$dV = V_1 \frac{P_1}{P_2} - V_1$$

- $dV$ 
  - Linear linear movement (largest contributor to uncertainty)
  - Piston diameter as a function of displacement
- $P_1$  – measured using a Paroscientific pressure gauge
- $P_2$  – measured using the same Paroscientific pressure gauge as  $P_1$
- Temperature – measures taken to create an isothermal environment (i.e.,  $T_2/T_1 = 1$ )

# Typical pressure step cycle for a single volume measurement

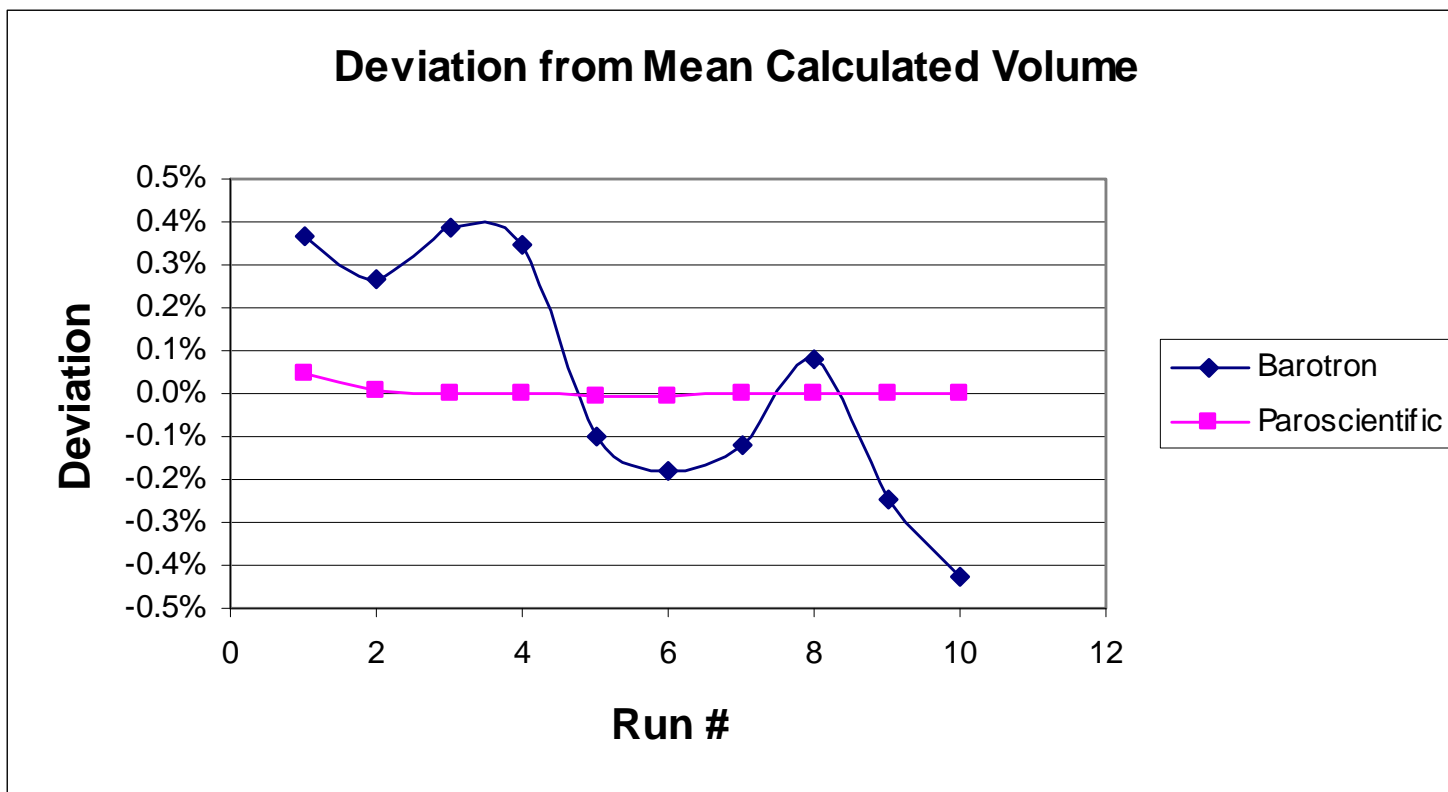
- The delta volume is induced by moving the micrometer and the pressures at each step are recorded.
- These data are amenable to least squares analysis.



$$dV = V_1 \frac{P_1}{P_2} - V_1$$
$$y = mx + b$$

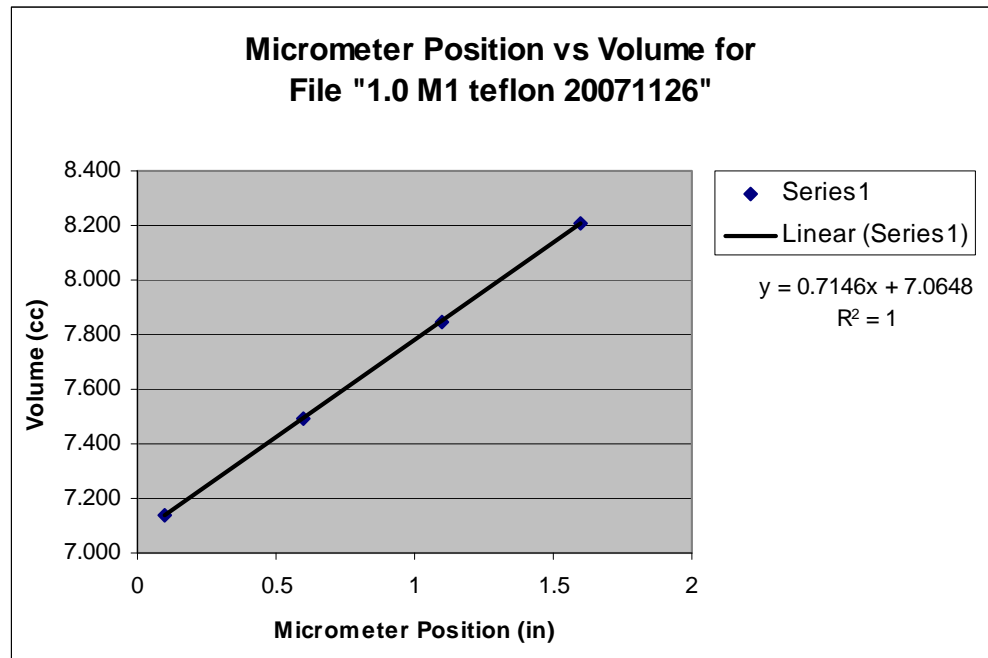
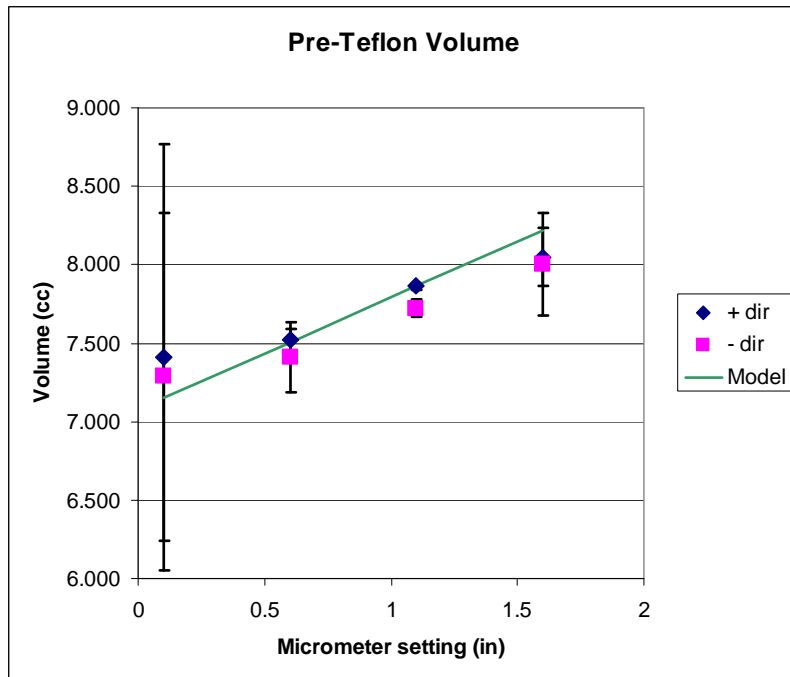


# Choosing the correct pressure gauge for the application



These data are for a nominal 50 cc volume. The superior performance of the Paroscientific pressure gauge for this application is clearly seen.

# Sealing to micrometer shaft is challenging



- Implementation of a Teflon o-ring seal instead of the standard butyl o-ring in the Ultra-Torr® fitting improved repeatability tremendously and eliminated hysteresis.

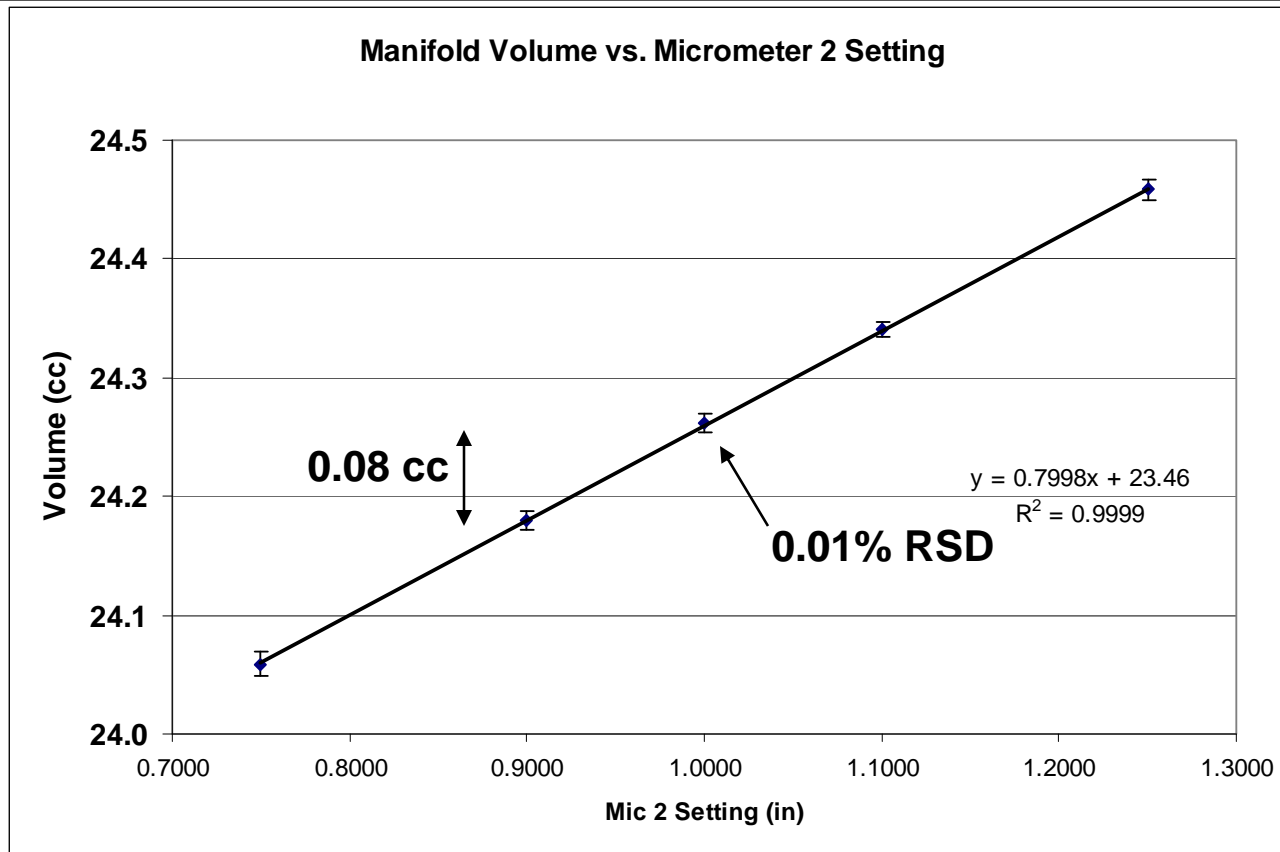
# Improving Temperature Stability: “The Marble Sarcophagus”

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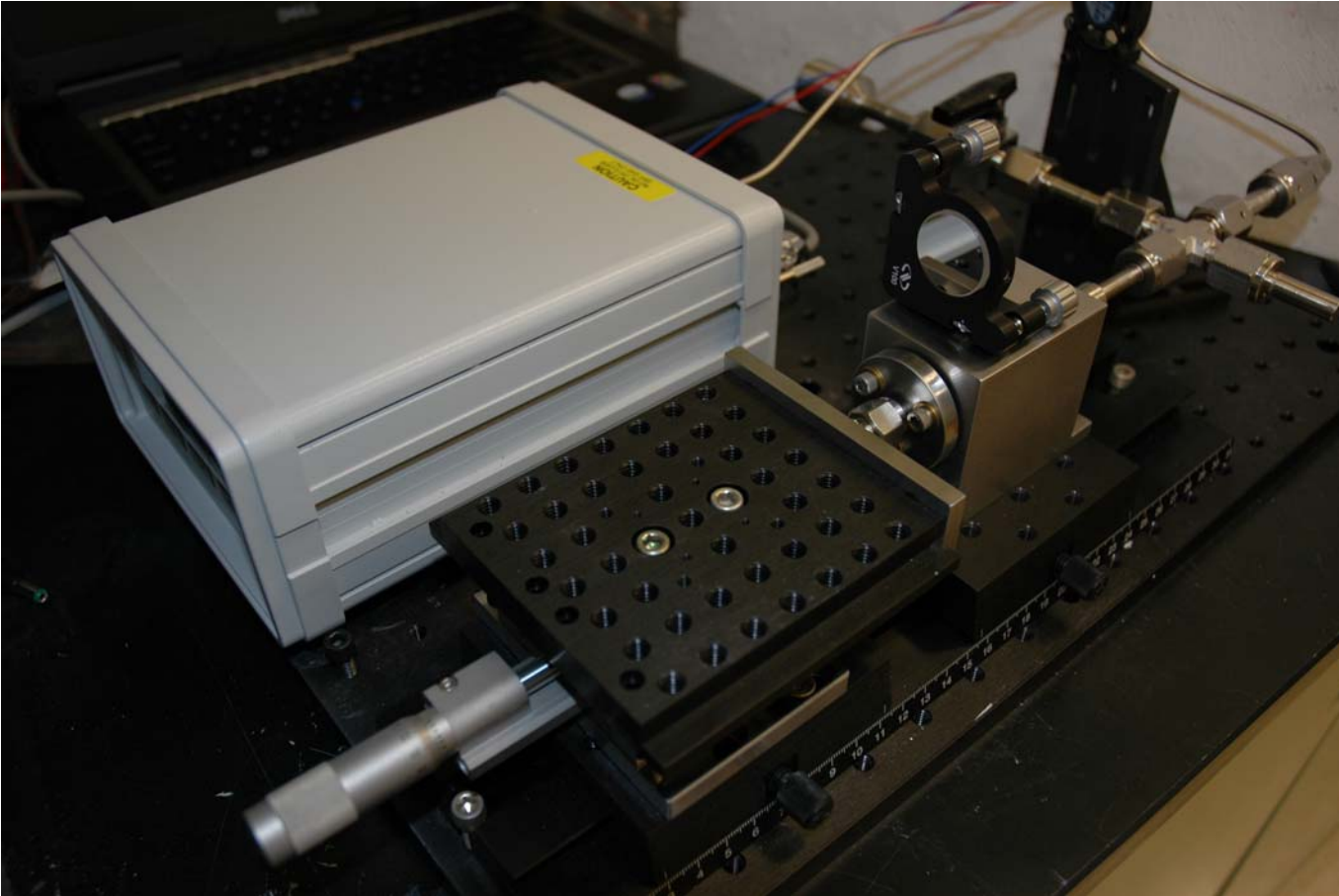
- A marble “sarcophagus” (4 inch thick walls) was constructed as a thermal ballast.
- Temperature drifts are now less than  $0.01^{\circ}\text{C}/\text{hour}$  with drifts during typical 1-2 minute measurement cycles much less
- Provides stability without the mess of water baths

# Volume measurements using “marble sarcophagus” have high precision



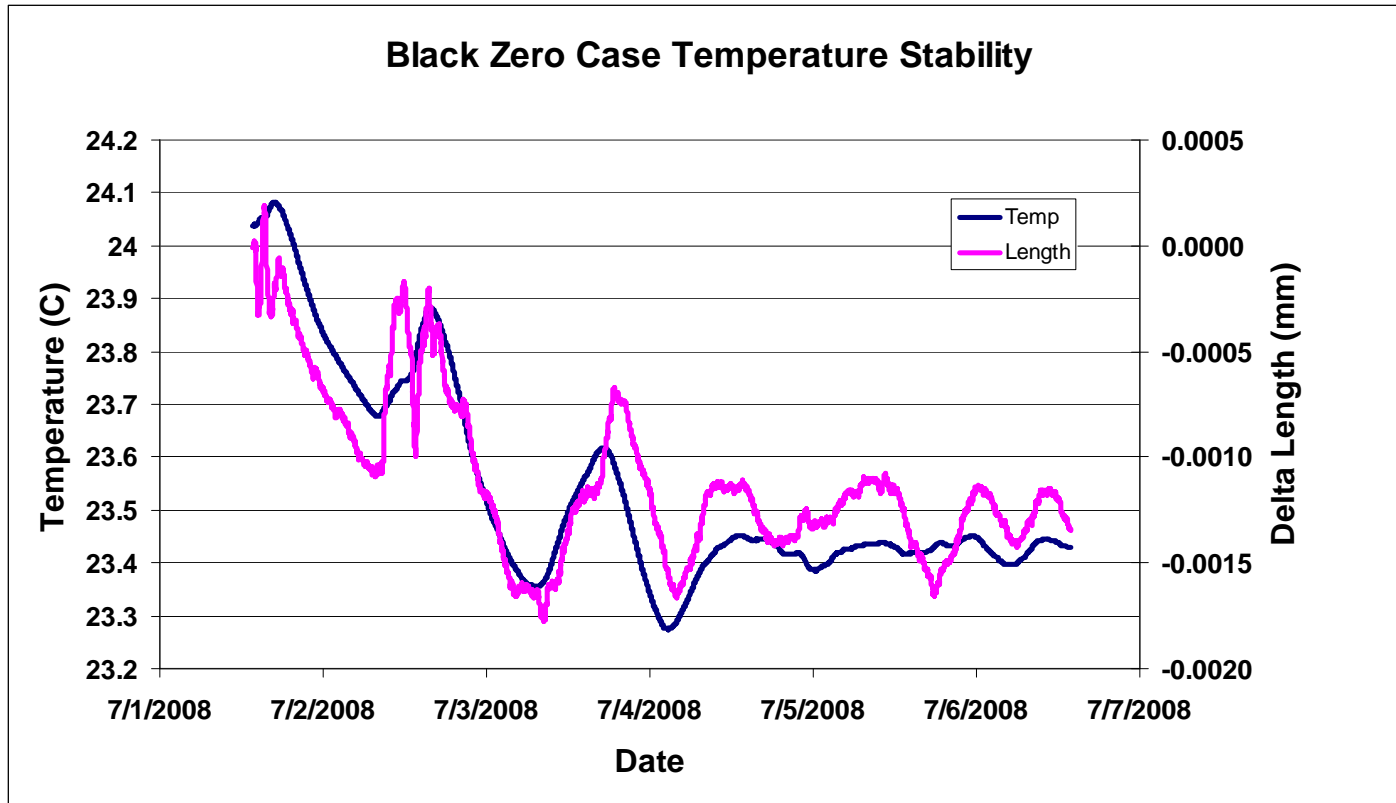
- Error bars are 3-sigma values for five replicate measurements at each point. Micrometer 2 was used to provide a known change in volume in the manifold.

# Future Enhancement - Interferometer



**The piston linear movement will be measured with a laser interferometer to reduce that uncertainty orders of magnitude.**

# Impact of temperature drift on interferometer length measurement



- Maximum change is 18 ppm/°C so for a stable environment ( $\pm 0.002^\circ\text{C}$ ) the impact of temperature will be minimal on the length measurement.



## **Better tools will enable reduced uncertainties for piston position**

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	<b>Resolution (inches)</b>	<b>% of 0.025 inch movement</b>
<b>Vernier micrometer</b>	<b>0.001</b>	<b>4.0%</b>
<b>Digital micrometer</b>	<b>0.00005</b>	<b>0.2%</b>
<b>Laser interferometer</b>	<b>&gt; 0.000001</b>	<b>&lt; 0.04%</b>



# Conclusion

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- The measurement repeatability has been greatly improved by:
  - Moving to a least-squares compatible form of the volume equation
  - Choosing a precise, stable pressure gauge
  - Using a Teflon o-ring to seal to the piston
  - Increasing the thermal mass around the calibration system to dampen temperature fluctuations
- Repeatability of volume measurements to better than 0.01% RSD for 5 measurements is readily attainable.
- The future enhancement of adding the laser interferometer will greatly reduce the linear movement error.