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# Precision Volume Measurements: Challenges to Reducing Uncertainties

**Steven M. Thornberg, Adriane N. Irwin, Rachael D. Boyd,  
Michael I. White, James M. Hochrein, Jason R. Brown**

**Materials Reliability Department  
Sandia National Laboratories  
Albuquerque, NM 87185**



# **Accurate volume determination is extremely important in many disciplines**

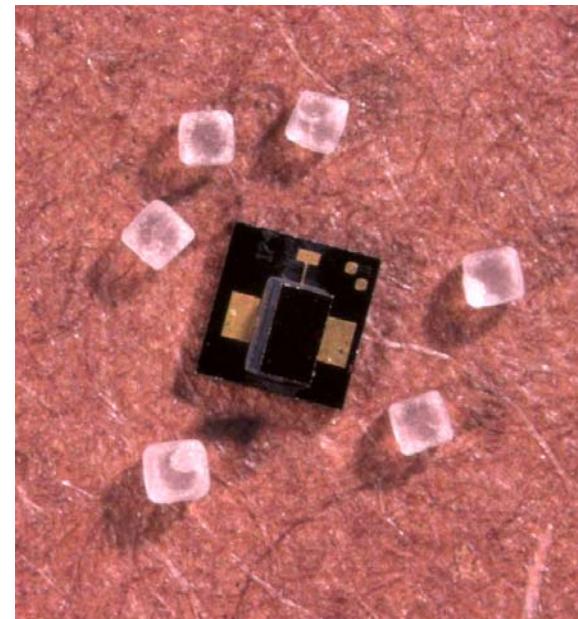
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$$P\ V = n\ R\ T$$

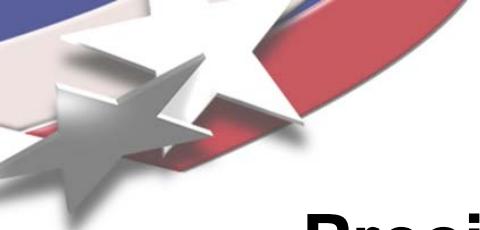
**The ideal gas law is used in many, many applications**

- Semiconductor industry
- Aerospace
- Defense
- Automobile
- Energy

**In this talk, we will focus on the measurement of VOLUME.**



***30 nanoliter MEMS device surrounded by grains of table salt.***



# Precision gas volume measurements

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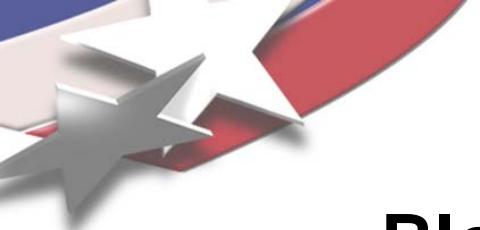
## Selected previous methods

- Gravimetric: liquid filled (even mercury filled)
- Volume expansion – still need a standard
- Pressure rise with calibrated leaks

## Need a method for determining volumes...

- Of complex manifolds
- Without exposing the manifold or part to a liquid
- That minimizes impact of outgassing and virtual leaks

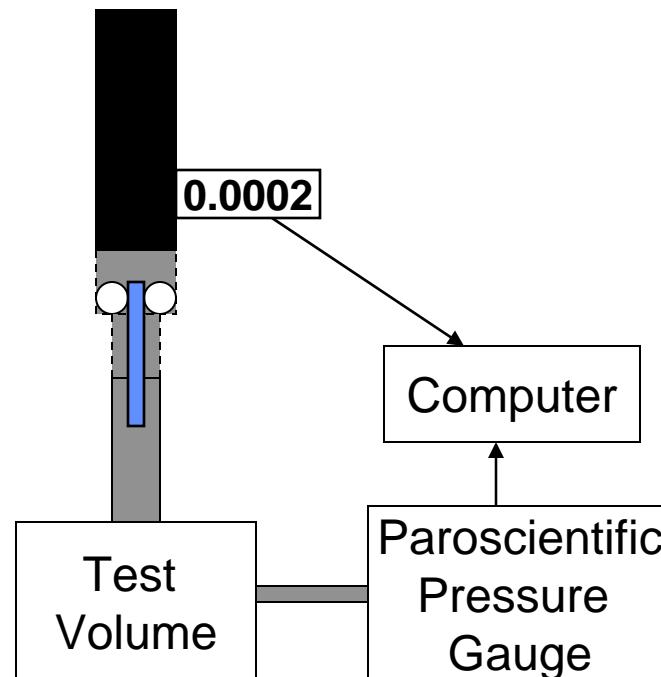




# Block diagram of the experiment

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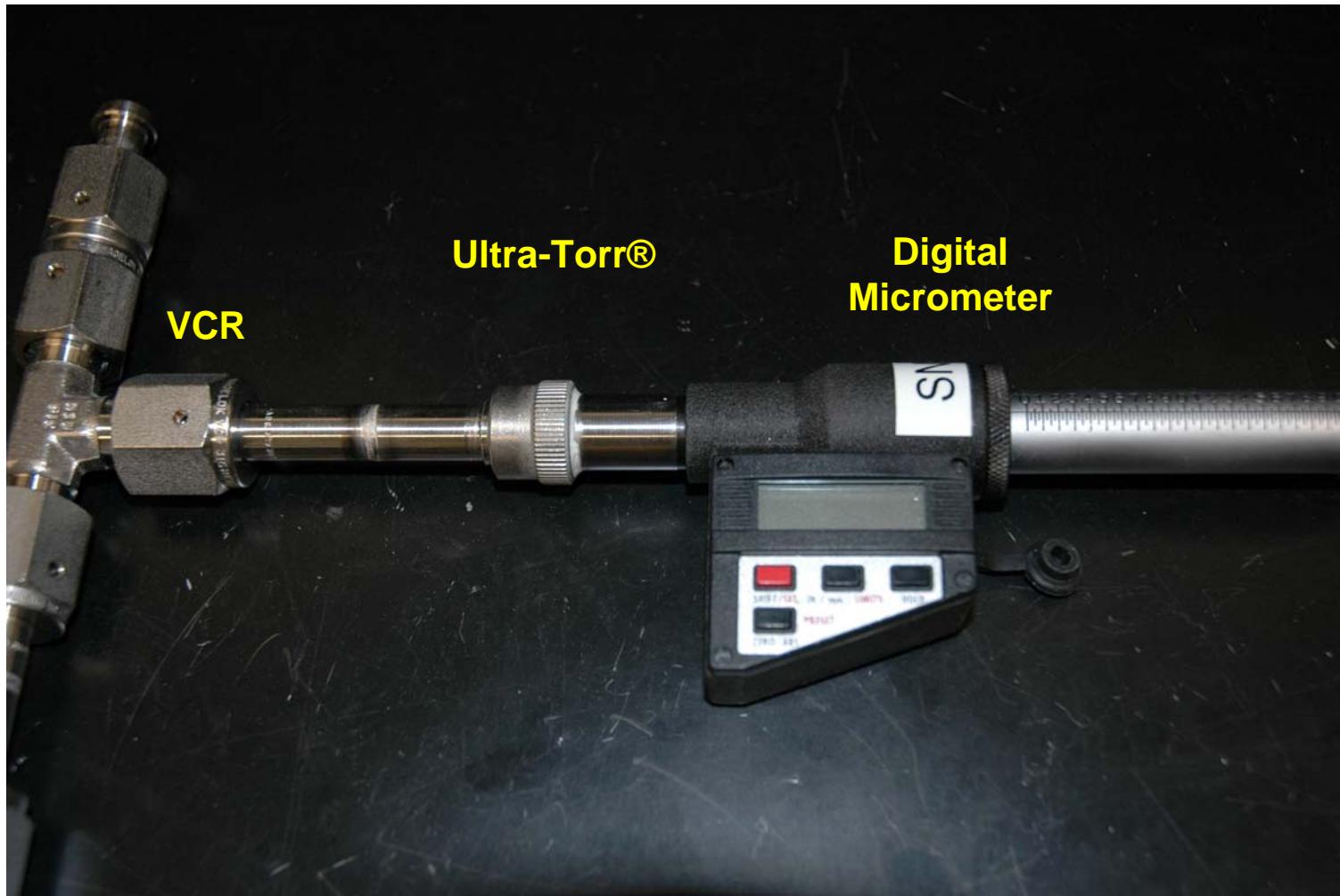
The experiment involves moving a piston (shown in blue) in or out of the test volume a known distance and recording the induced pressure change.





# Micrometer assembly

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# Theory - derivation of equation

- Assume isothermal
- Simple equation
- We bypass the direct solution for  $V_1$  in favor of the least-squares compatible form.

$$P_1 V_1 = P_2 V_2$$

$$P_1 V_1 = P_2 (V_1 + dV)$$

$$V_1 = \left( \frac{P_2}{P_1 - P_2} \right) dV$$

$V_1$  in favor squares form.

$dV = V_1 \frac{P_1}{P_2} - V_1$

Slope

Intercept



# What are the contributors to the measured volume uncertainty?

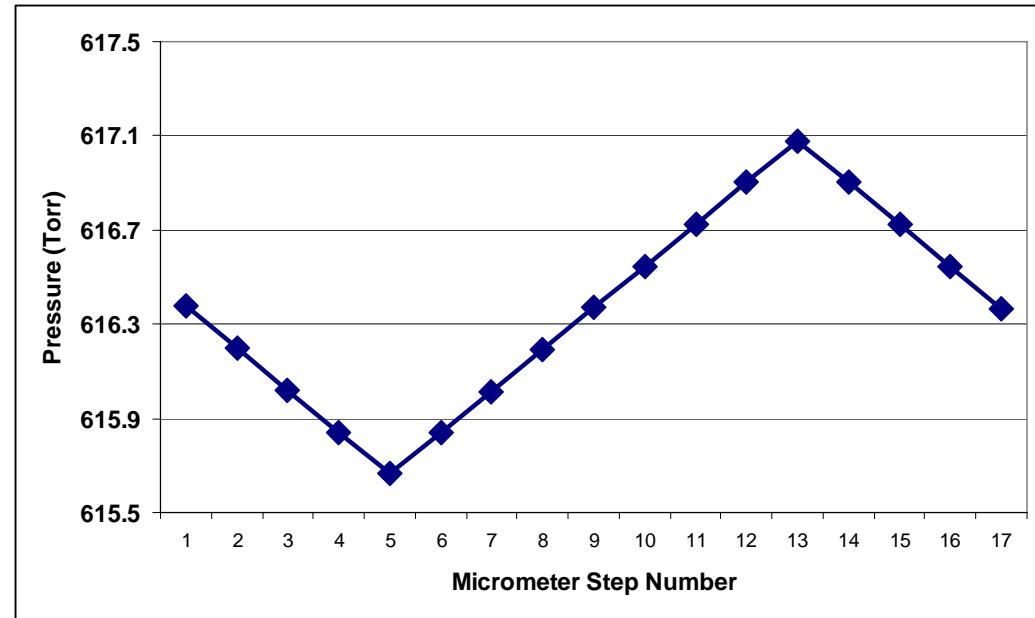
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$$dV = V_1 \frac{\frac{P_1}{P_2} - 1}{\frac{P_1}{P_2}} V_1$$

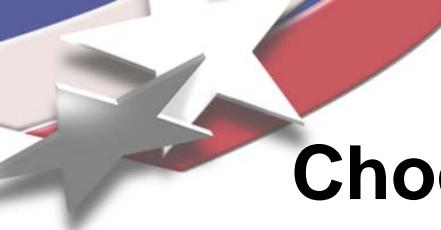
- $dV$ 
  - Linear linear movement (largest contributor to uncertainty)
  - Piston diameter as a function of displacement
- $P_1$  – measured using a Paroscientific pressure gauge
- $P_2$  – measured using the same Paroscientific pressure gauge as  $P_1$
- Temperature – measures taken to create an isothermal environment (i.e.,  $T_2/T_1 = 1$ )

# Typical pressure step cycle for a single volume measurement

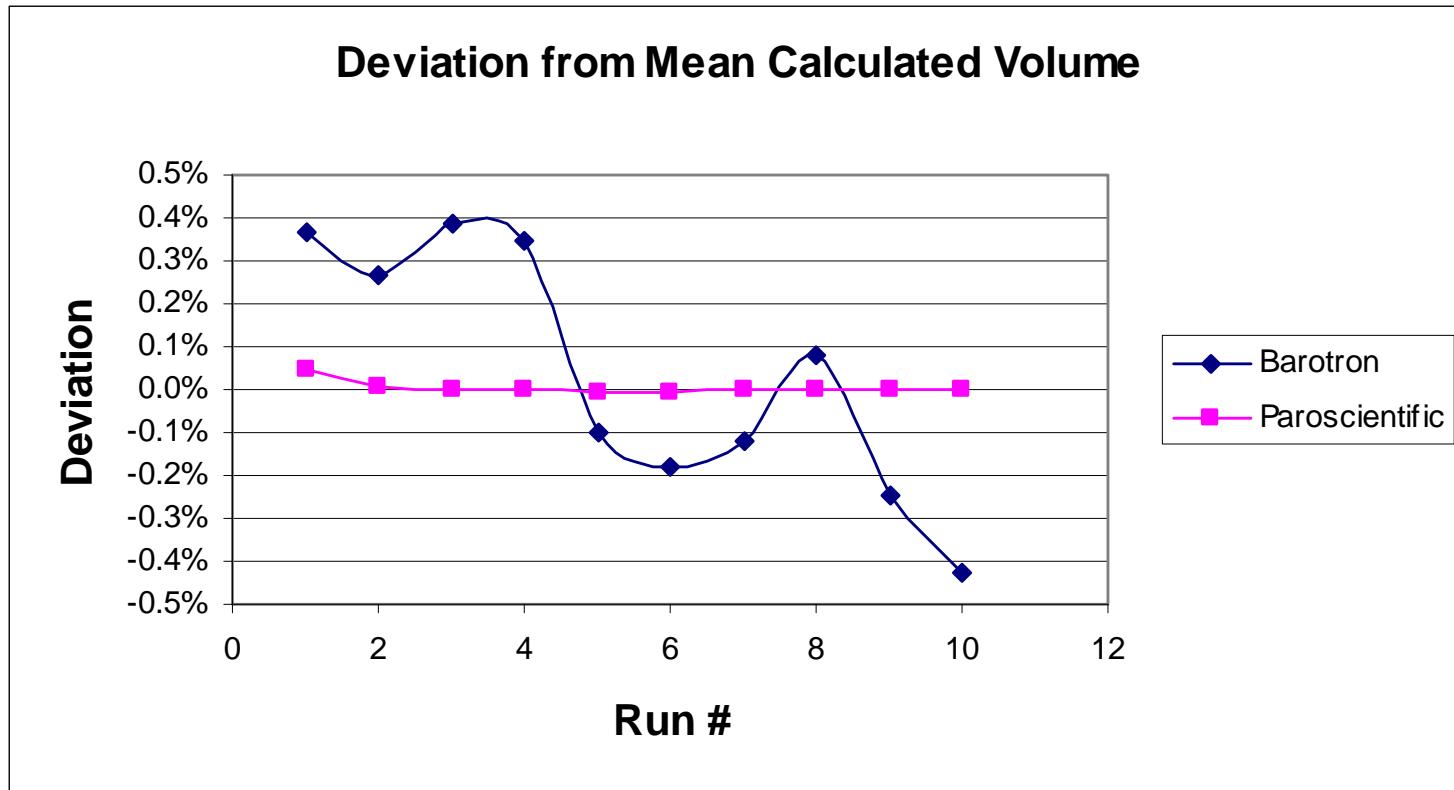
- The delta volume is induced by moving the micrometer and the pressures at each step are recorded.
- These data are amenable to least squares analysis.



$$dV = V_1 \frac{P_1 - P_2}{P_2} - V_1$$
$$y = m x + b$$

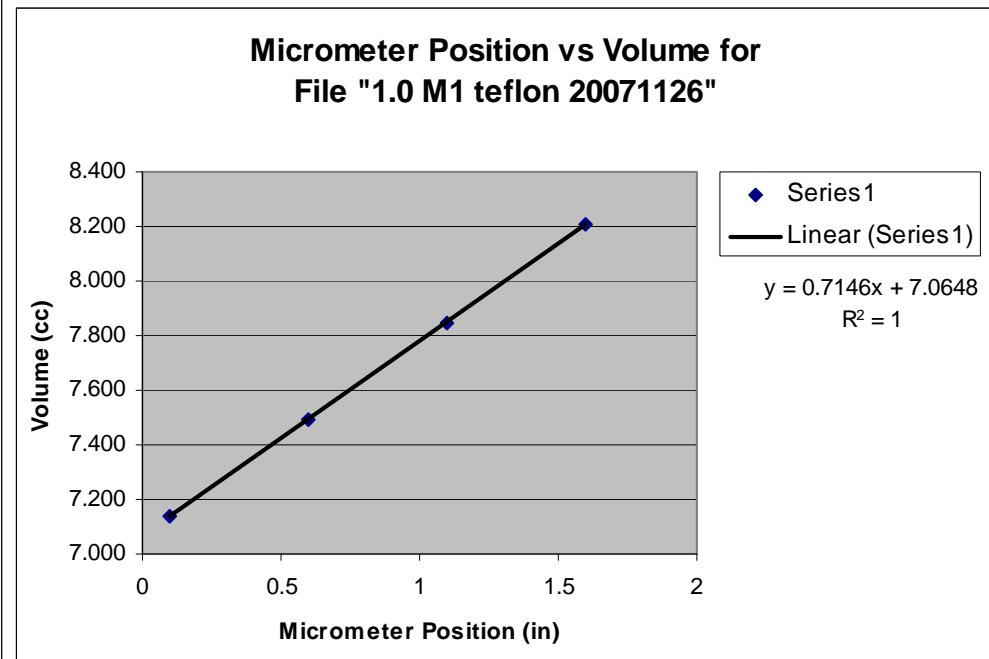
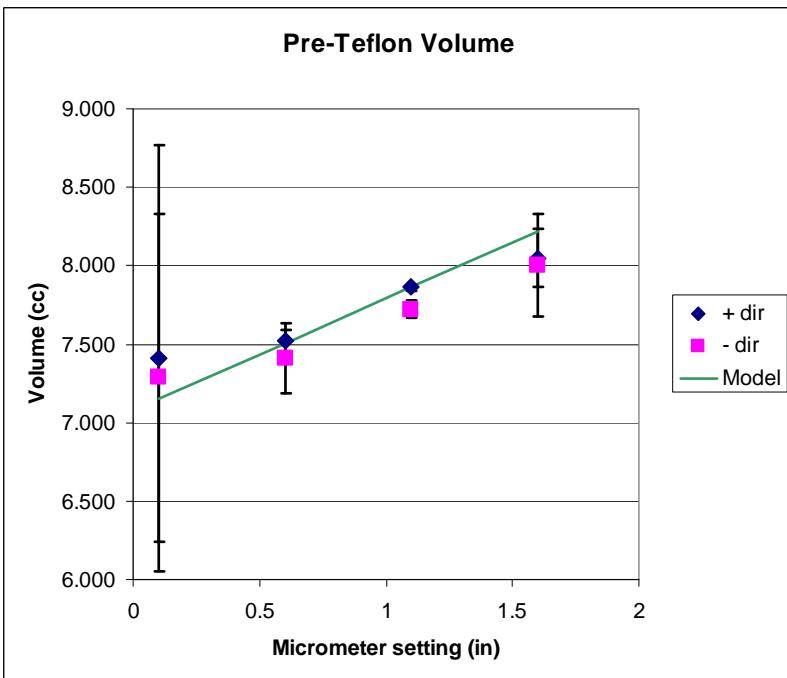


# Choosing the correct pressure gauge for the application



These data are for a nominal 50 cc volume. The superior performance of the Paroscientific pressure gauge for this application is clearly seen.

# Sealing to micrometer shaft is challenging



- Implementation of a Teflon o-ring seal instead of the standard butyl o-ring in the Ultra-Torr® fitting improved repeatability tremendously and eliminated hysteresis.



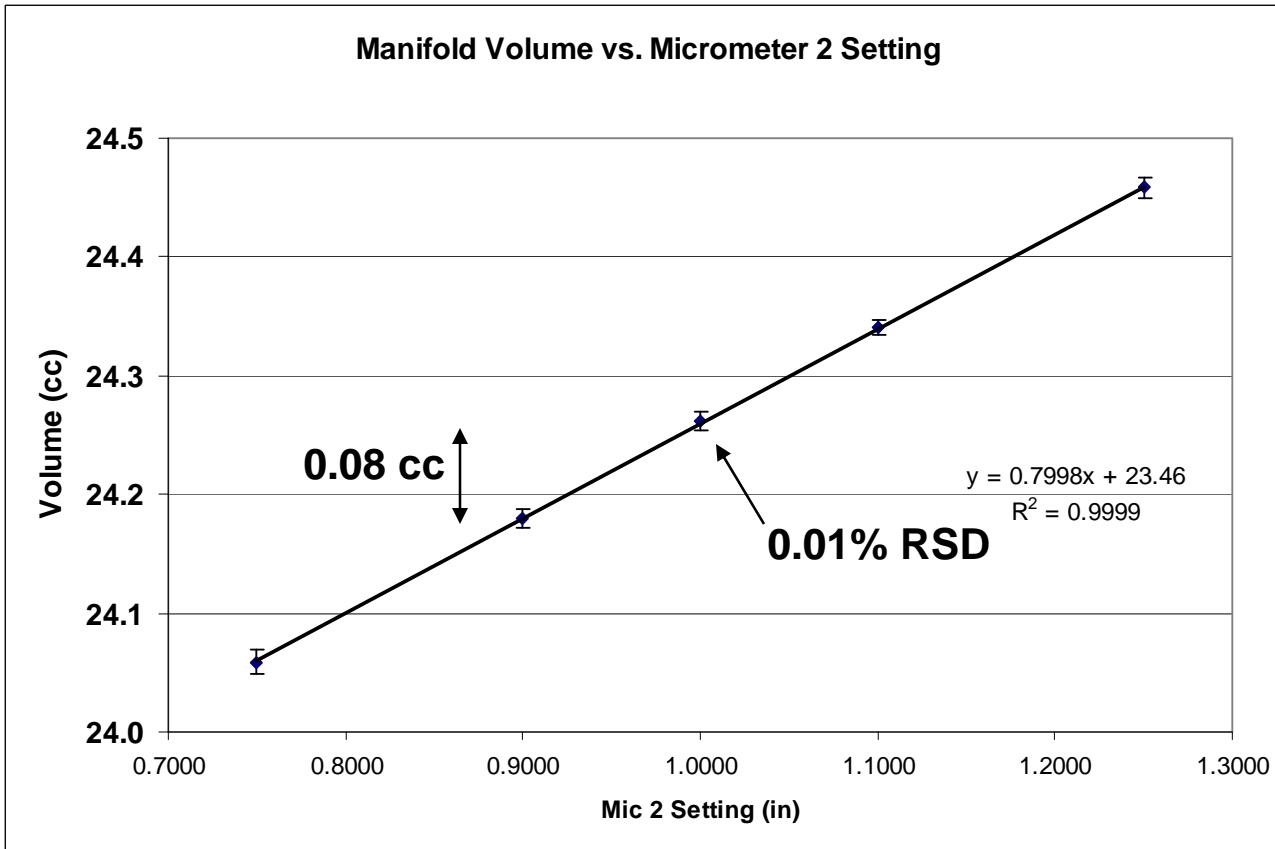
# Improving Temperature Stability: “The Marble Sarcophagus”

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- A marble “sarcophagus” (4 inch thick walls) was constructed as a thermal ballast.
- Temperature drifts are now less than 0.01°C/hour with drifts during typical 1-2 minute measurement cycles much less
- Provides stability without the mess of water baths

# Volume measurements using “marble sarcophagus” have high precision

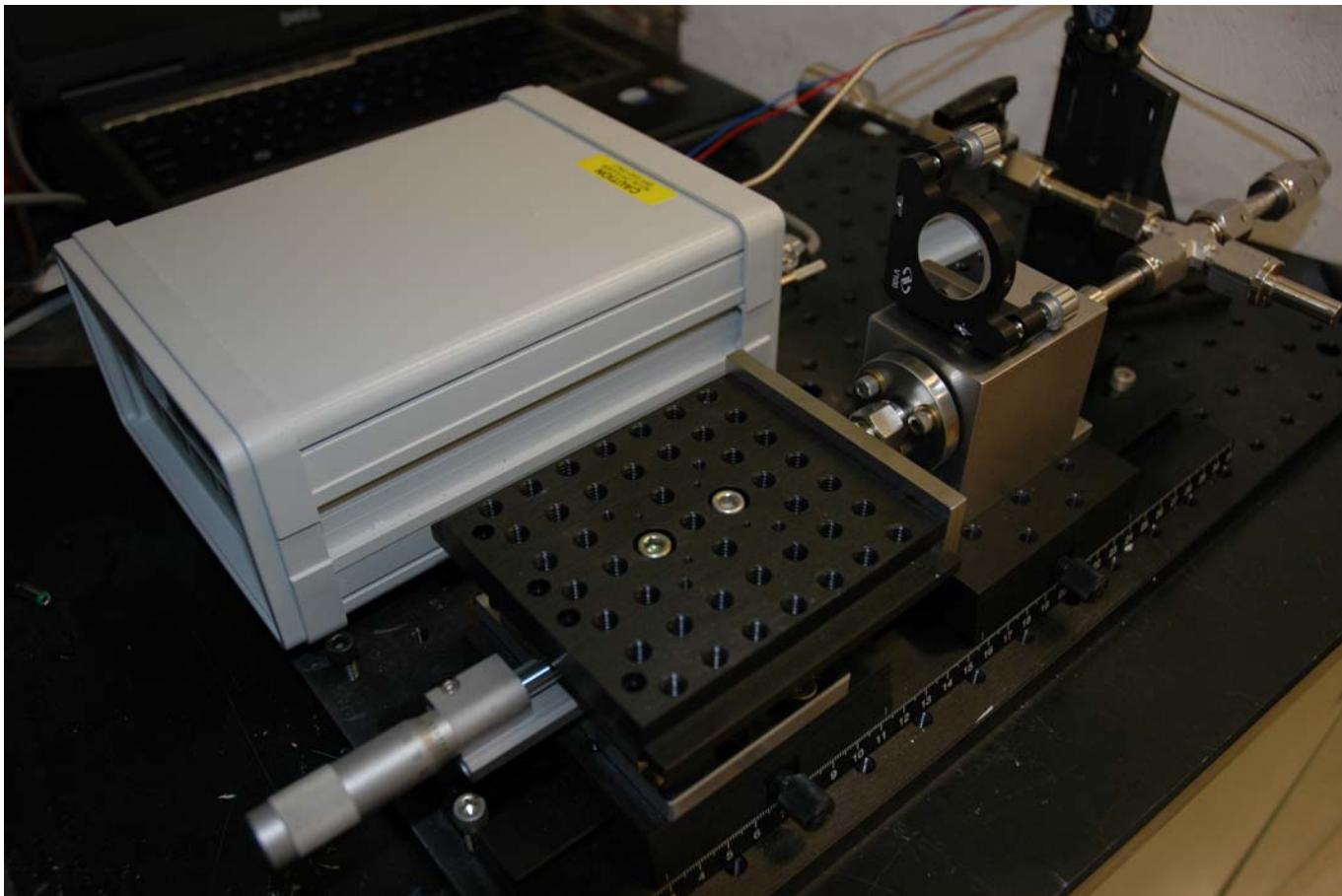


- Error bars are 3-sigma values for five replicate measurements at each point. Micrometer 2 was used to provide a known change in volume in the manifold.



# Future Enhancement - Interferometer

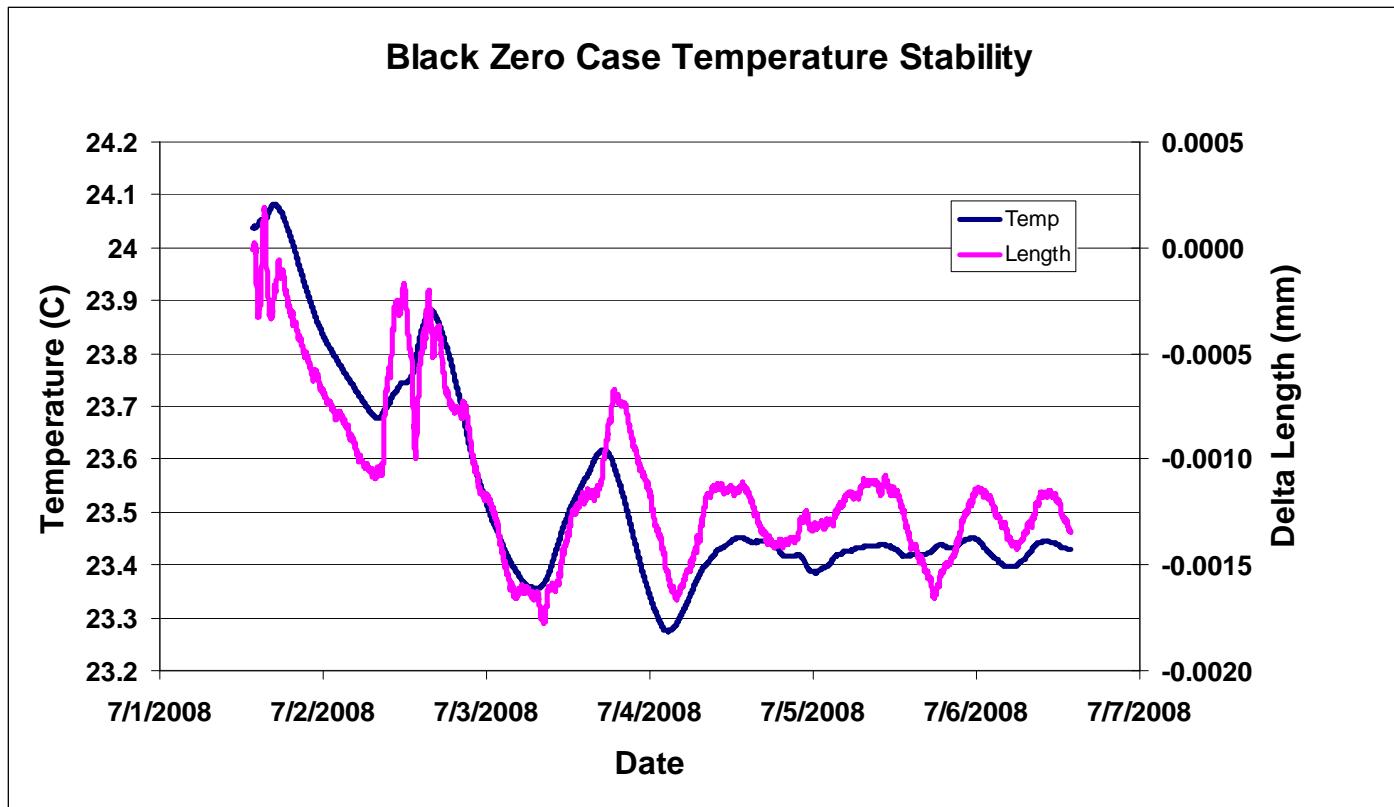
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**The piston linear movement will be measured with a laser interferometer to reduce that uncertainty orders of magnitude.**



# Impact of temperature drift on interferometer length measurement



- Maximum change is 18 ppm/ $^{\circ}\text{C}$  so for a stable environment ( $\pm 0.002^{\circ}\text{C}$ ) the impact of temperature will be minimal on the length measurement.



# Better tools will enable reduced uncertainties for piston position

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	Resolution (inches)	% of 0.025 inch movement
Vernier micrometer	0.001	4.0%
Digital micrometer	0.00005	0.2%
Laser interferometer	> 0.000001	< 0.04%



# Conclusion

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- The measurement repeatability has been greatly improved by:
  - Moving to a least-squares compatible form of the volume equation
  - Choosing a precise, stable pressure gauge
  - Using a Teflon o-ring to seal to the piston
  - Increasing the thermal mass around the calibration system to dampen temperature fluctuations
- Repeatability of volume measurements to better than 0.01% RSD for 5 measurements is readily attainable.
- The future enhancement of adding the laser interferometer will greatly reduce the linear movement error.