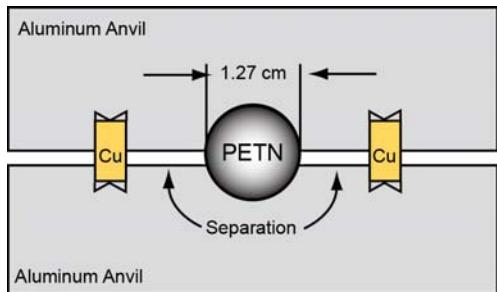


MODELING PETN IGNITION

Michael L. Hobbs

Sandia National Laboratories
Albuquerque, New Mexico

ODTX

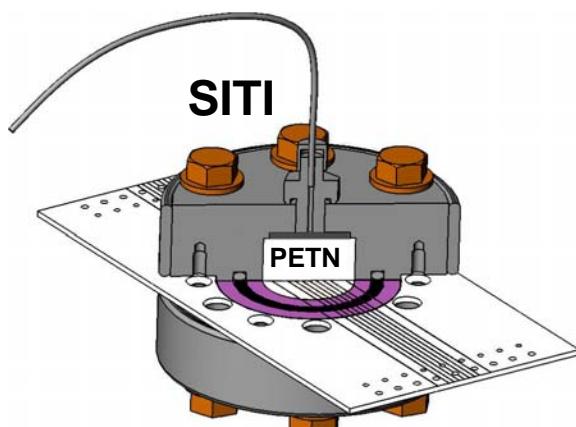


1.8 grams in ~1 cc

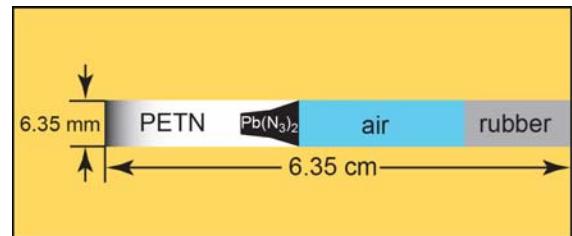
21.7 grams in ~13 cc

0.5 grams in ~0.7 cc

SITI

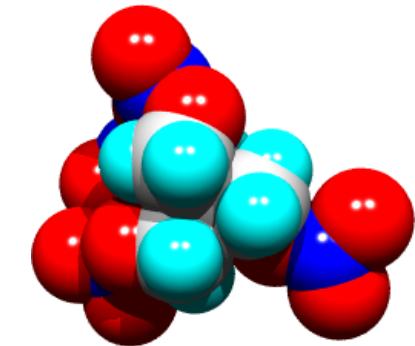


Detonator



Why study PETN ignition?

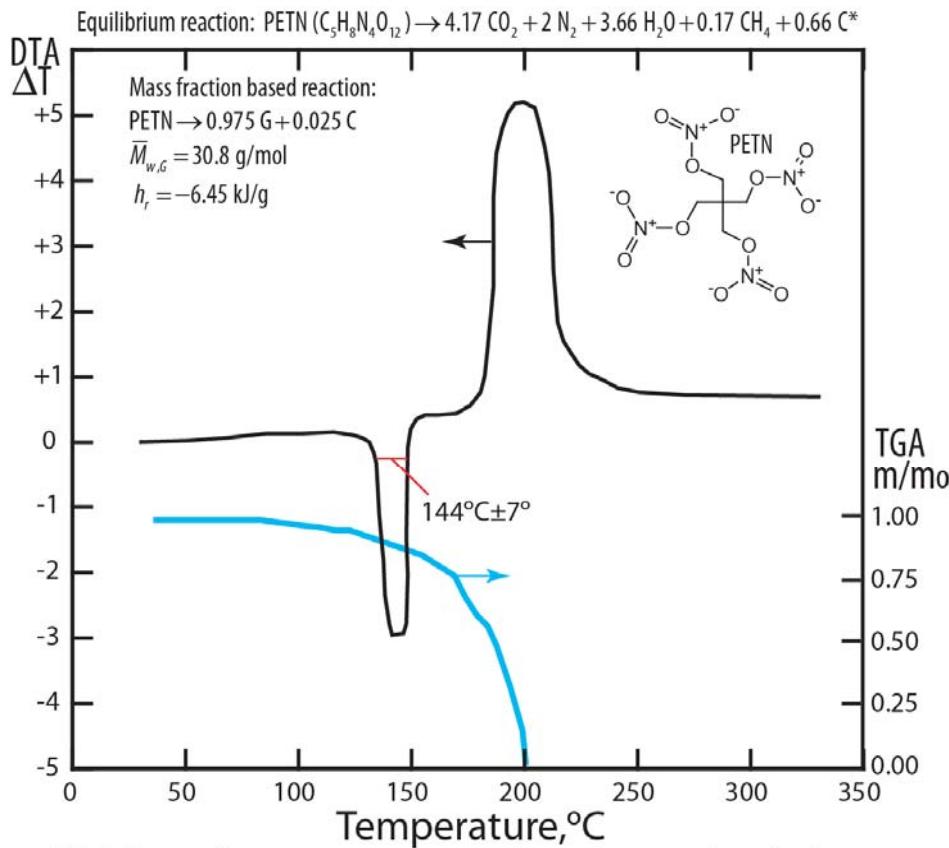
- Used extensively in military and civilian applications
- Used in numerous explosives
 - LX-02 (73.5% PETN, 17.6% butyl rubber, 6.9% acetyltributyl citrate, 2% Cab-O-Sil)
 - LX-08 (63.7% PETN, 34.3% Sylgard, 2% Cab-O-Sil)
 - LX-16 (98% PETN, 4% FPC 461)
 - Pentolite (50% PETN, 50% TNT)
 - PEP-3 (86% PETN, 14% plasticizing oil)
 - PTX-2 (43.2%RDX, 28% PETN, 28.8% TNT)
 - Semtex 1A (87% PETN, dye, antioxidants, plasticizer, binder)
 - Semtex 10 (82% PETN, dye, etc.)
- Standard booster and bursting charge
 - Small caliber ammunition
 - Detonators
 - Explosive core of detonation cord
- Explosive chosen by Richard Reid (shoe bomber)



YouTube video of 20 g of PETN cutting down tree



Some observations



*G, C, $M_{w,G}$, and h_r represent gaseous reaction products, condensed carbon, average gas product molecular weight, and reaction enthalpy, respectively.

A) Semtex 1A (87% PETN with dye, antioxidant, plasticizer, and binder)



Does not slump as melting occurs, gases ignite in air.

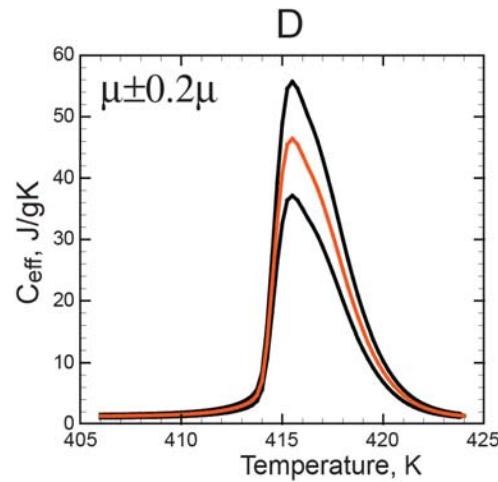
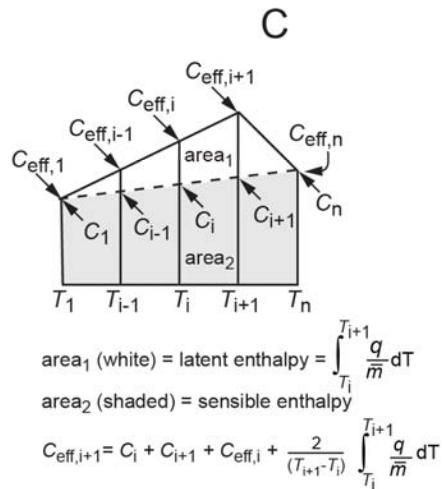
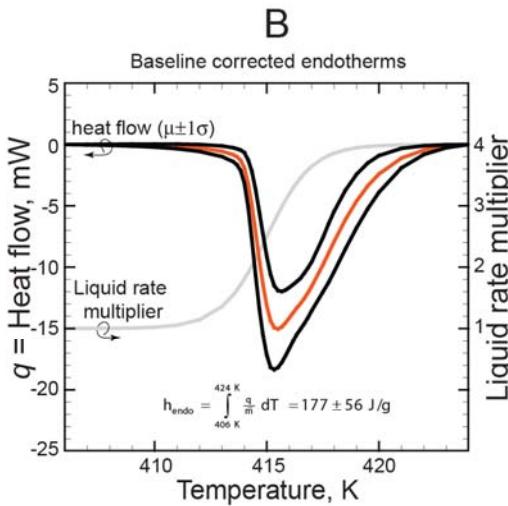
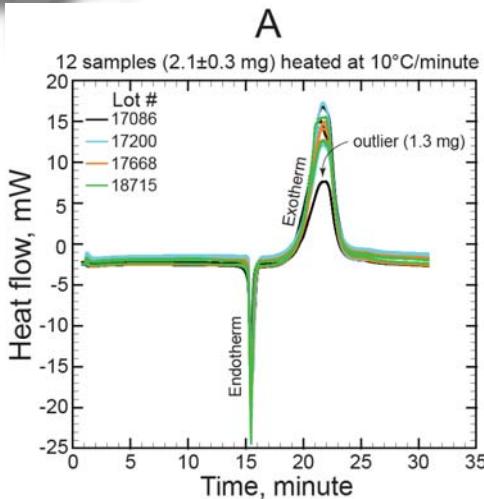
B) Semtex 10 (82% PETN with dye, antioxidant, plasticizer, and binder)



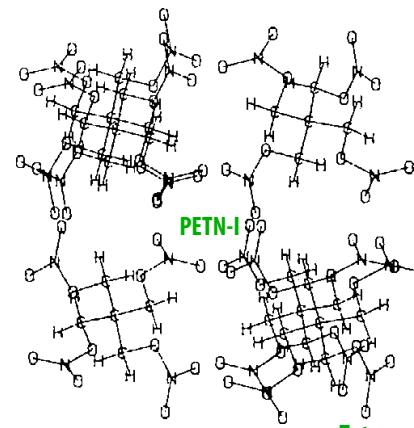
Decomposes and ignites before melting completes.

Violence increases with fast, confined decomposition

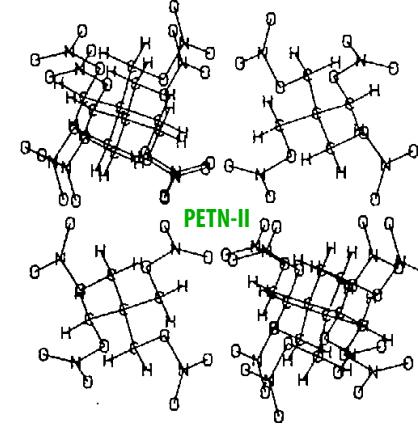
Endotherms modeled using effective capacitance



2 polymorphs



Tetragonal (1.778 g/cc)



Orthorhombic (1.716 g/cc)

*Cady, HH; Larson, AC, *Acta Crystallographica B*(31), 1864 (1975)

Overlapping endotherms associated with solid-to-solid (PETN-I to PETN-II) polymorphic phase change, sublimation of PETN, and the solid-to-liquid phase transition (i.e. melting).

PETN ignition model

Gas continuity (integral)

$$\frac{dM_g}{dt} = \int_{\Lambda} r \rho_c^o (1 - \phi^o) d\Lambda + \dot{m}_i - \dot{m}_o \quad (1)$$

Gas momentum (low Mach)

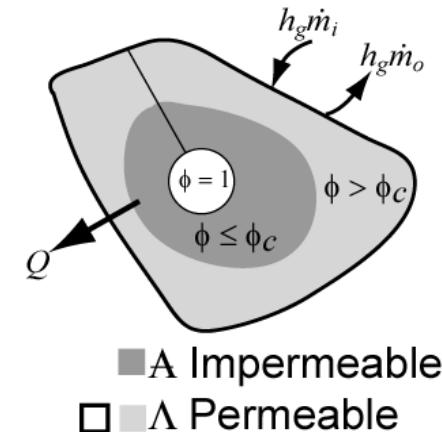
$$P(x, y, z, t) = P(t) = M_g / \int_{\Lambda} \frac{M_{wg}}{RT} d\Lambda \quad (2)$$

Energy (integral: bulk elements)

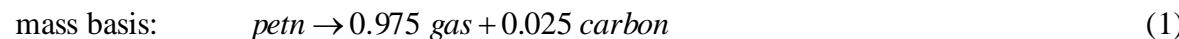
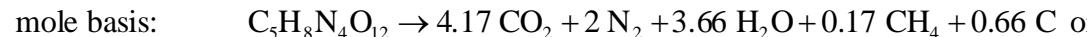
$$\frac{dV_b \rho_g C_g T_b}{dt} = - \int_S h (T_b - T) dS + \dot{m}_i h_i - \dot{m}_o h_o \quad (3)$$

Energy (field: material blocks)

$$\rho_b C_b \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + \rho_b h_r r \quad (4)$$



Mechanism



Reaction Rate

$$r = \frac{d}{dt}(\text{petn}) = \xi A \exp\left[-(E + z\sigma_E)/RT\right] \text{petn}, \text{ where petn}_o = 1 \quad (2)$$

Distribution parameter

$$1 - \text{petn} = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp\left(\frac{-z^2}{2}\right) dz \quad \text{or} \quad z = \text{norminv}(1 - \text{petn}) \quad (3)$$

Gas volume fraction

$$\phi = 1 - \left[S_f (1 - \phi^o) \rho_c^o / \rho_c \right] \text{ where } S_f = \text{petn} + \text{carbon} \quad (4)$$

Bulk density

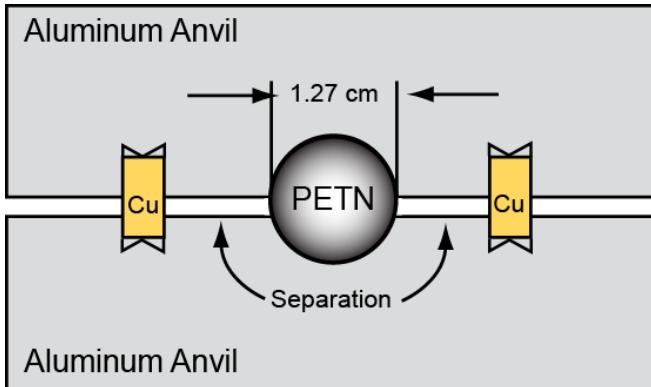
$$\rho_b = \phi \rho_g + (1 - \phi) \rho_c \quad (5)$$

Thermal conductivity

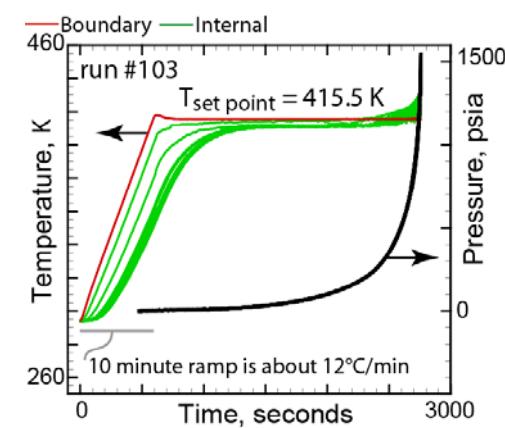
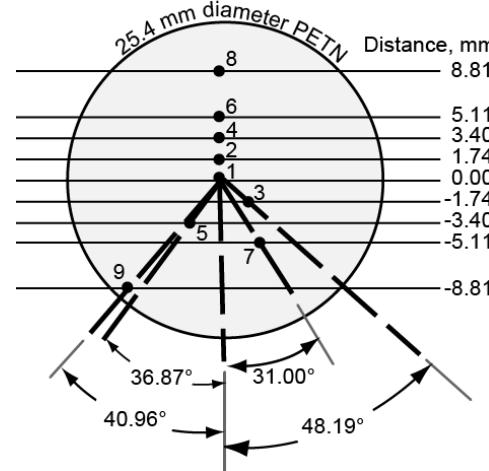
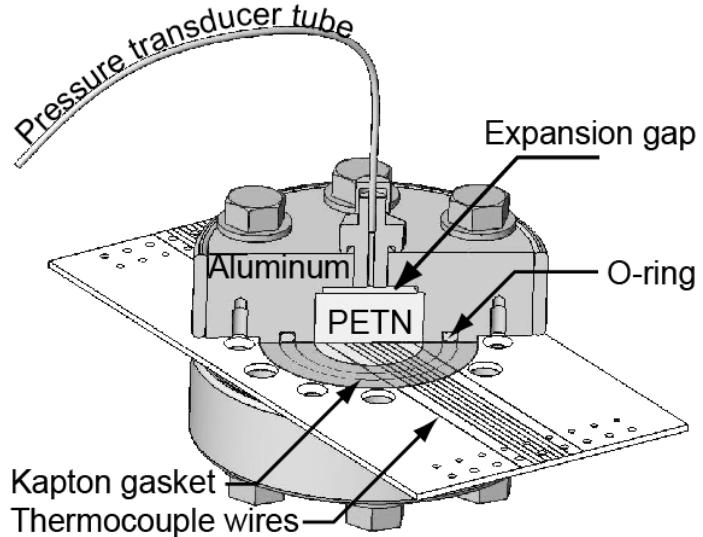
$$k = \phi k_g + \frac{2}{3} (1 - \phi) k_c + \frac{16\sigma T^3}{3[\phi\alpha_g + (1 - \phi)\alpha_c]} \quad (6)$$

Validation experiments

ODTX



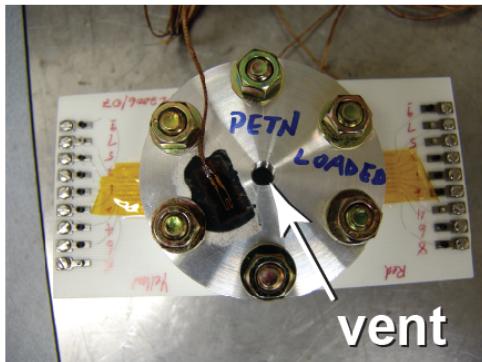
SITI



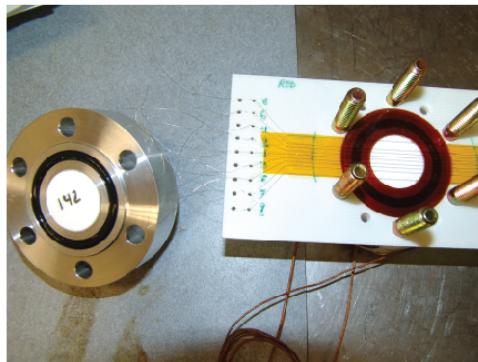


Violence prediction is of interest

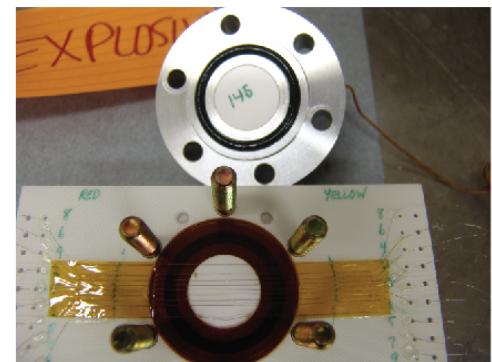
Run #102
(unconfined powder)



Run #103
(confined pressed solid)

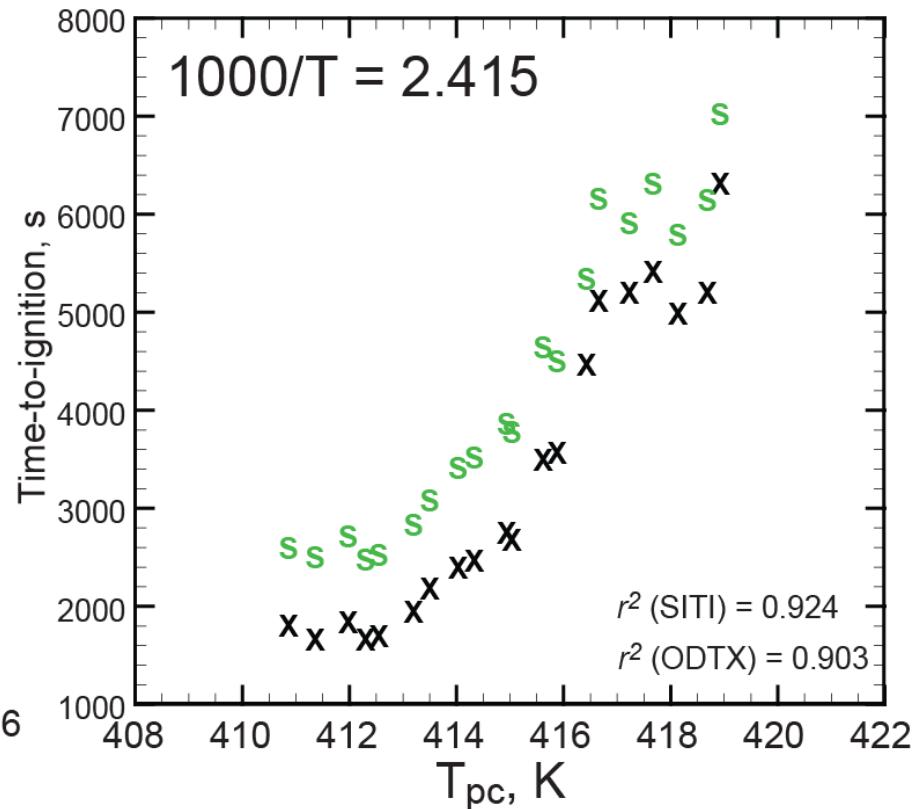
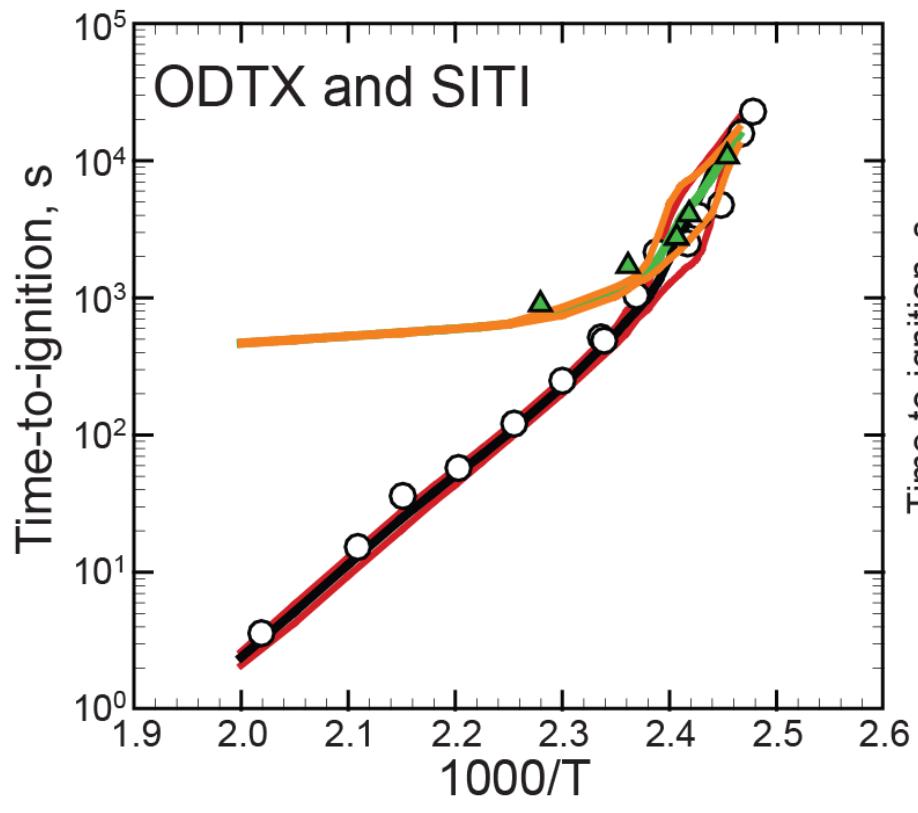


Run #105
(confined pressed solid)



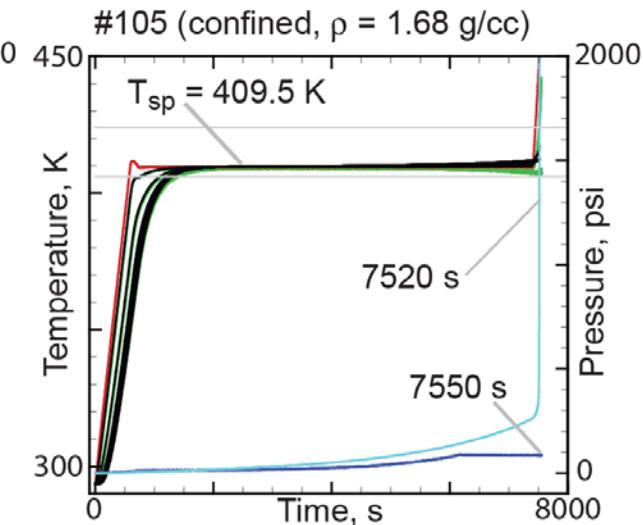
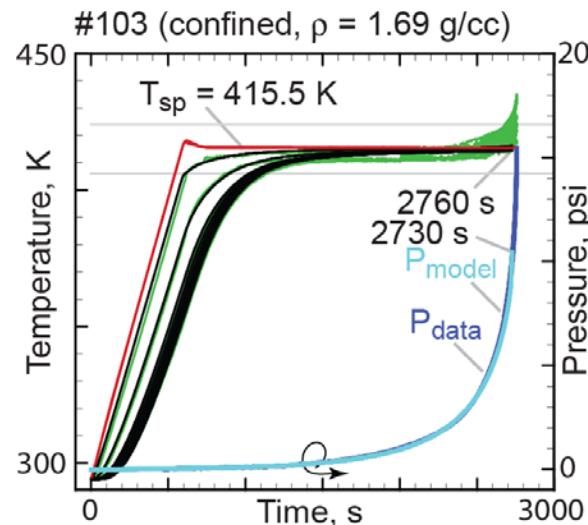
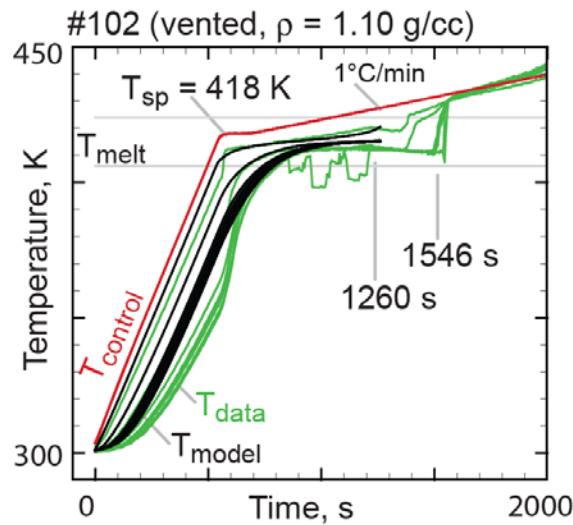
*Does it go **pop**, **bang**, or **kablooey**?*

Model predicts ignition time



Uncertainty calculated with 20 LHS samples

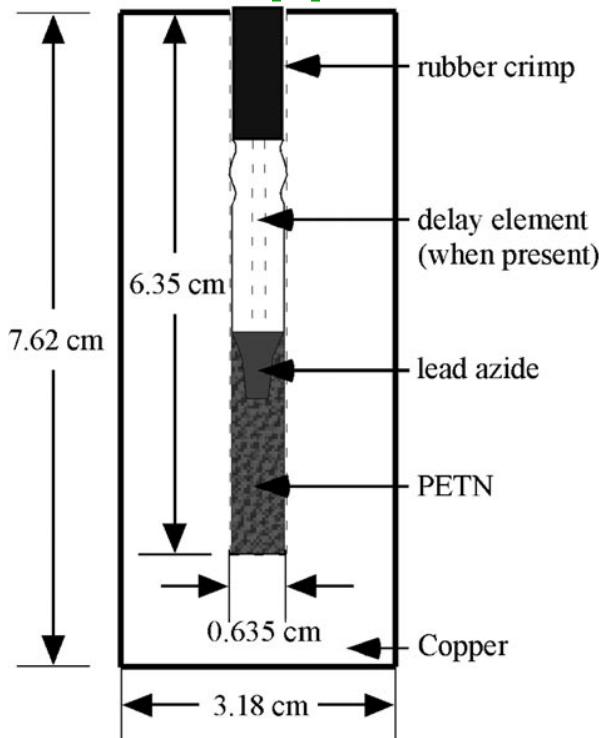
Model predicts temperatures/pressures



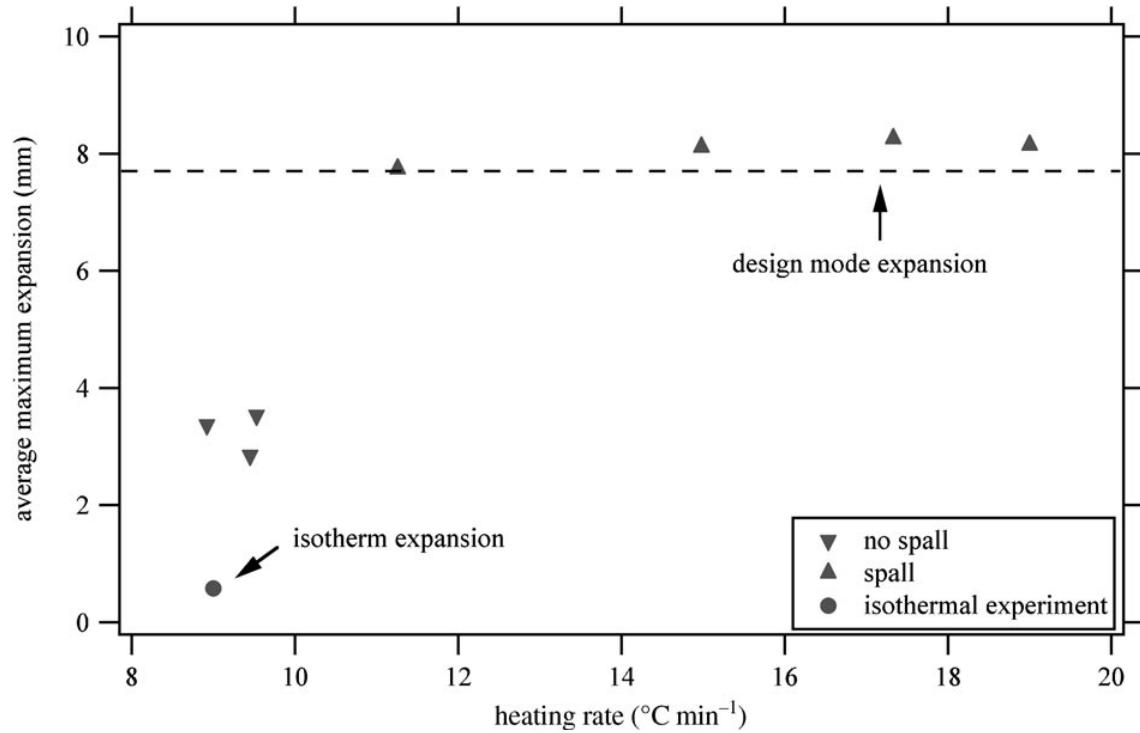
Model does not calculate violence

Does ignition guarantee failure?

Detonator in copper



Expansion of copper



*J.M. Zucker, P. Dickson, V.E. Sanders, *Propellants Explos. Pyrotech.*, **34**, 142 (2009).

Can violence be correlated to conditions at the onset of ignition with Damköhler (group IV) number, DaV, or something similar?

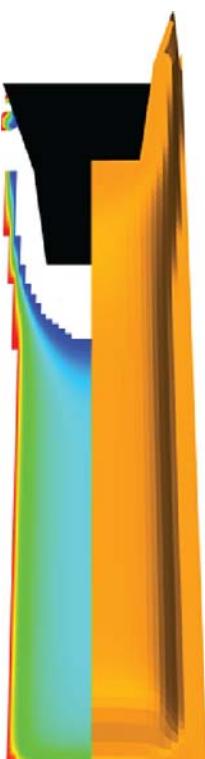
$$D_{a,c} = D_a \text{IV}^* = \frac{\text{reaction time scale}}{\text{conduction time scale}} = \frac{\rho_b h_r r}{\nabla \cdot (k \nabla T)} = \frac{h_r r}{C_b \frac{\partial T}{\partial t} - h_r r}$$

$$D_{a,s} = \frac{\text{reaction time scale}}{\text{storage time scale}} = \frac{h_r r}{C_b \frac{\partial T}{\partial t}}$$

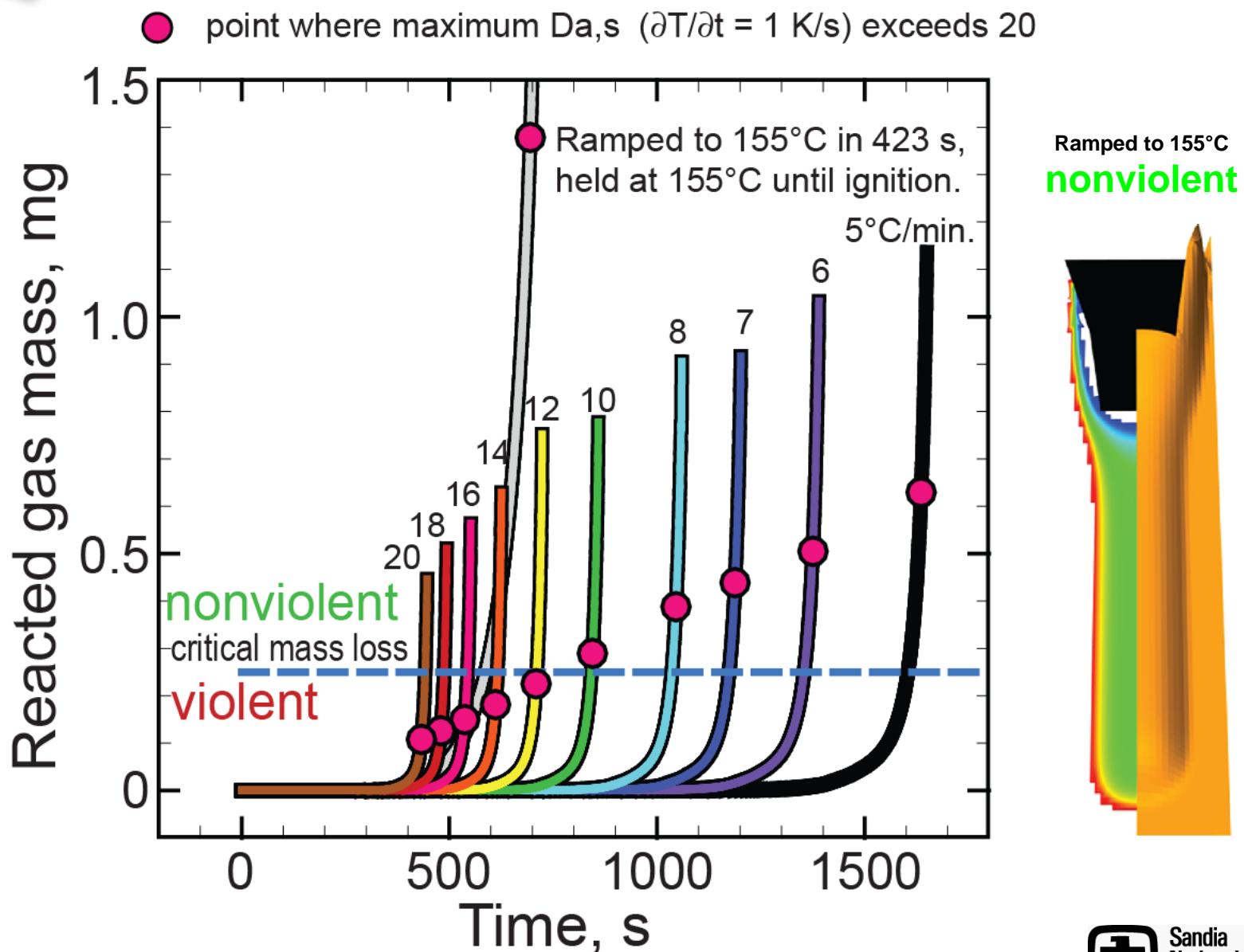
*derived from $\rho_b C_b \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + \rho_b h_r r$

Cookoff violence correlated with extent of reaction

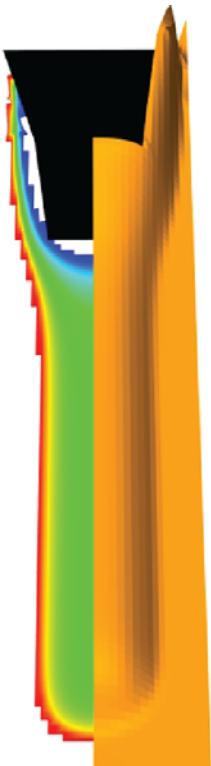
20°C/min
violent



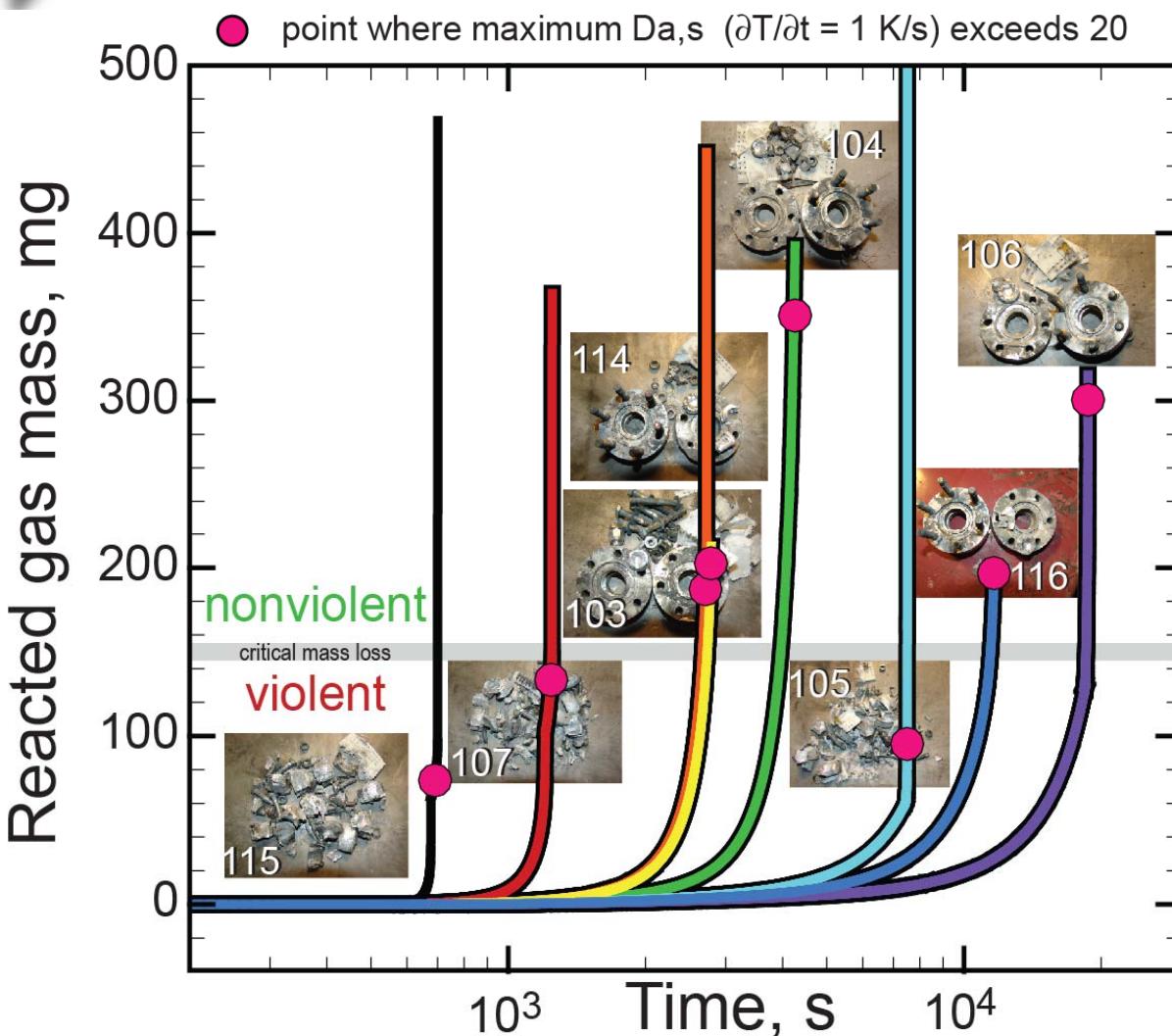
Temp., K
413 417



Ramped to 155°C
nonviolent



SITI cookoff violence correlated with extent of reaction at onset of ignition





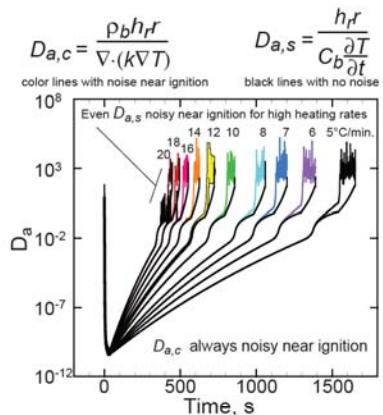
Summary and Conclusions

- 1-step, 1st-order, distributed activation energy, pressure dependent, thermodynamic phase change, effective thermal conductivity, low Mach pressure model with decomposition products in equilibrium.
- Model fits ignition times from three experiments: SNL's SITI experiment, LLNL's ODTX experiment, LANL's detonator experiments. Predicts time, location, pressure, but not violence. Cookoff violence correlated with state of material at onset of ignition determined using storage Damköhler number.
- Need to know the thermophysical properties such as thermal conductivity, phase change temperature, phase change enthalpy, reaction enthalpy, reaction products, specific heat, bulk density, volumetric expansion coefficient, and phase density.
- Model form applicable to many explosives (e.g. HMX, RDX, TNT, PETN, TATB, etc.).
- Need to confirm cookoff violence correlations with experiments.

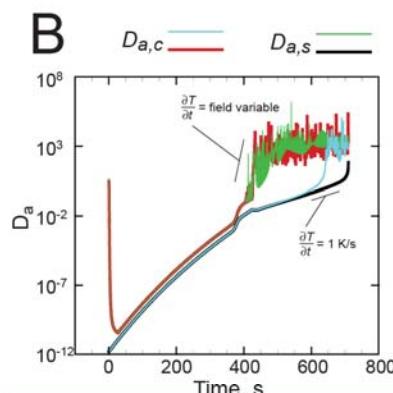
Simulations correlate violence with...

Extent of reaction

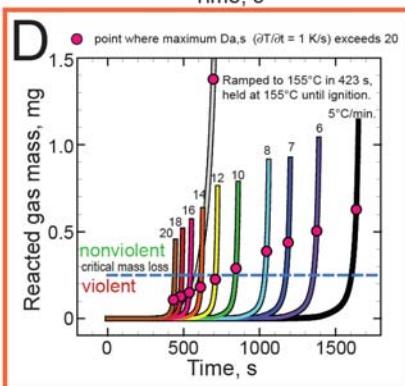
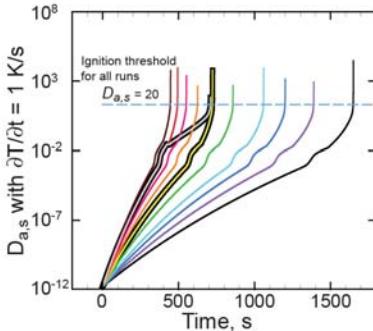
A



B



C



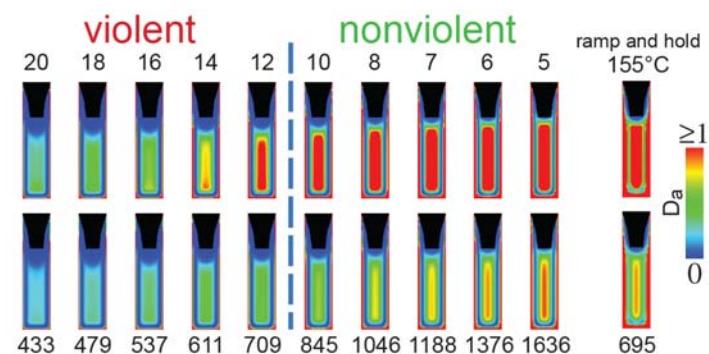
Damköhler numbers

rate, °C/min.

$$Da_c = \frac{\rho_b h_f r}{\nabla \cdot (k \nabla T)}$$

$$Da_s = \frac{h_f r}{C_b \frac{\partial T}{\partial t}}$$

time (s) when
 Da_s^{\max} exceeds 20



violent

20°C/min

solid

$\xi = 1$

$\xi = 1.5$

$\xi = 4$

nonviolent

5°C/min

ramp and hold

155°C

417

413

*Elevated surface is proportional to liquid reaction rate multiplier, ξ .

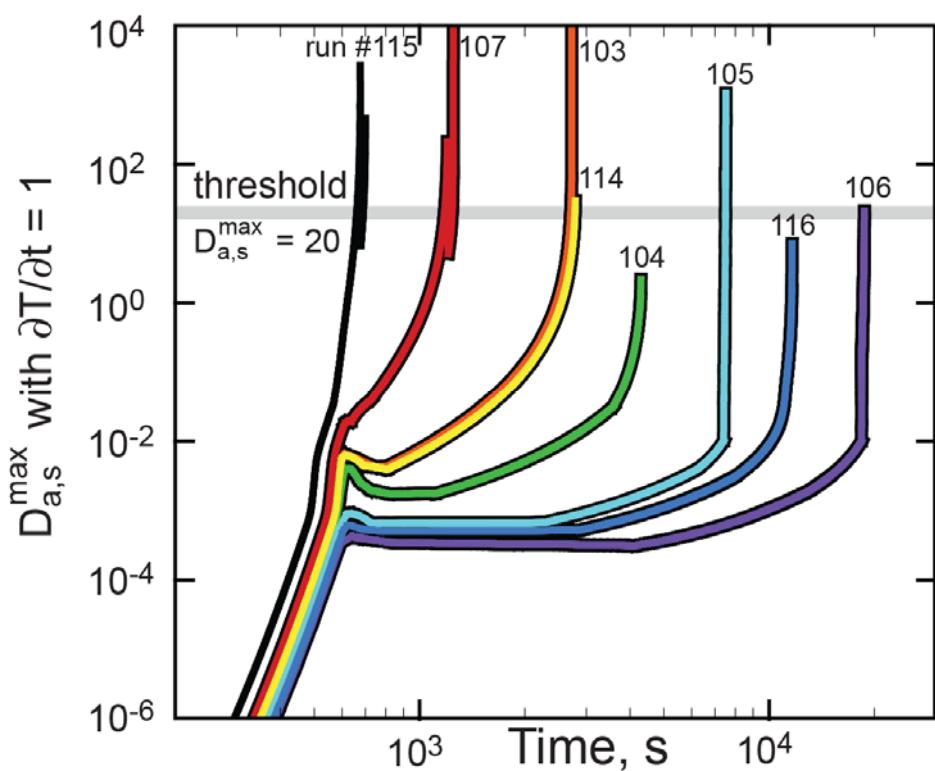
†Limit fringes are invisible (i.e. white).

Think liquid formation and hot spots!

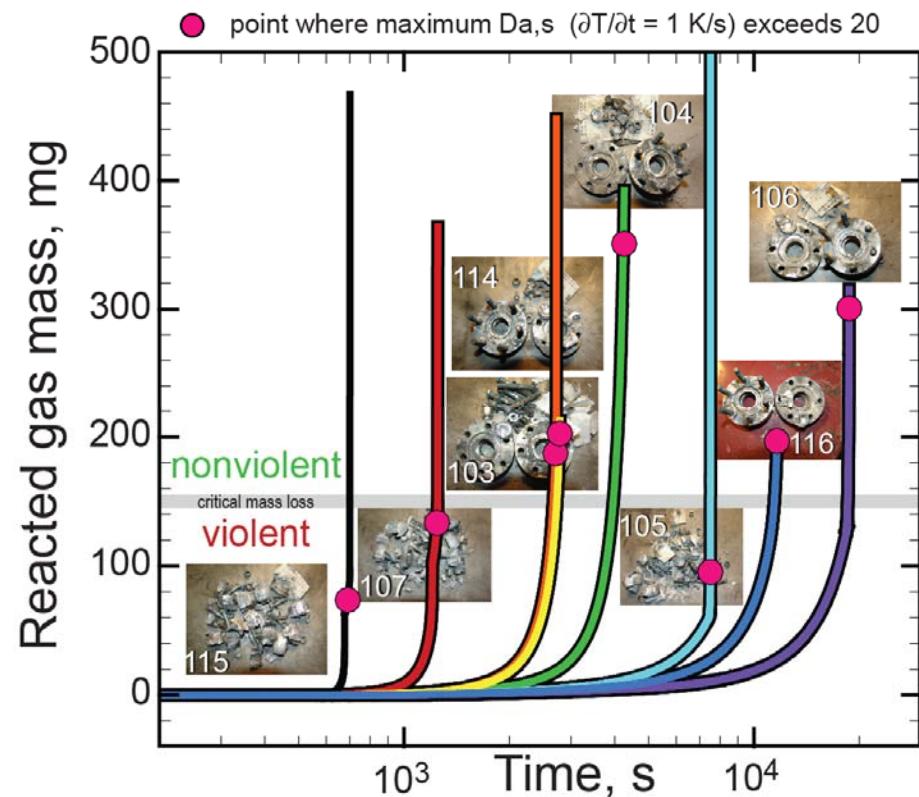
Detonators attained *full output* when the extent of reaction was small and were *duds* when the extent of reaction was large at the onset of ignition.

SITI violence correlated with extent of reaction at onset of ignition

Onset of ignition
when $D_{a,s}^{\max}$ exceeds 20



Violence correlated with
extent of reaction at ignition



Run #105 intentionally ignited after 2 hours.