

# Coarse-grained ionomer melts under an external electric field

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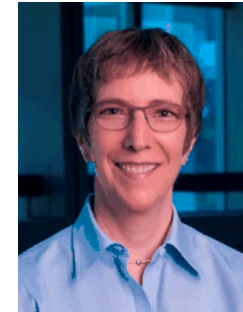
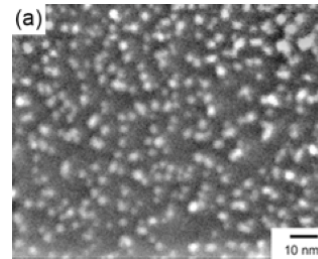
APS March Meeting  
March 5, 2014

# Ionomers

Polymers with small fraction of charged groups

- ion-ion interactions + low dielectric polymer

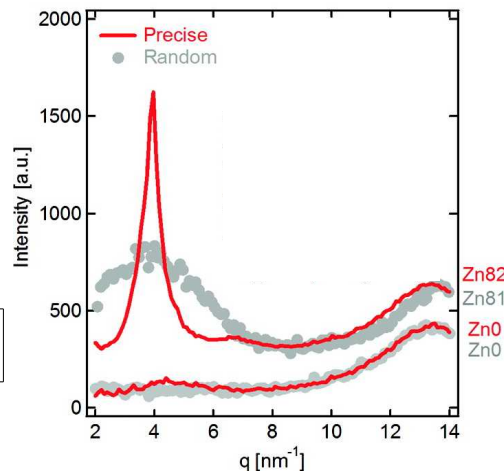
→ ionic aggregates



Karen Winey, Penn

*Precise* ionomers:

Synthesize by acyclic diene metathesis (ADMET)



- What do the aggregates look like?
- What is the dependence on polymer architecture?
- How does this affect ion dynamics?

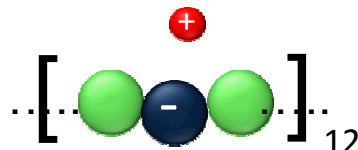
Ken Wagener, U Florida

# Coarse-grained MD simulations

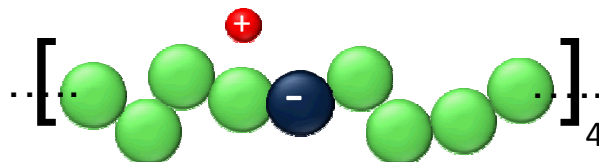
charged groups in the backbone:

“ionene”

$N_{bb} = 3$

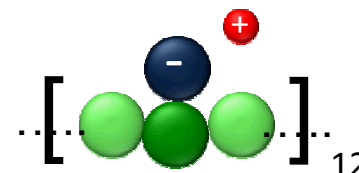


$N_{bb} = 9$

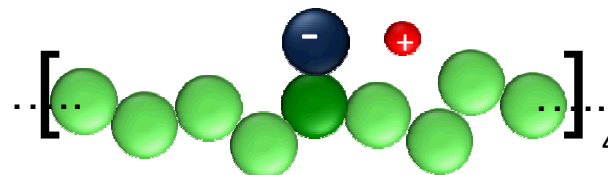


charged groups pendant to the backbone:

“pendant”



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repulsive LJ interactions

+ FENE bonds

+ coulomb interactions:  $U(r) = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon r}$

+ Langevin thermostat

Simulation details:

800 polymers

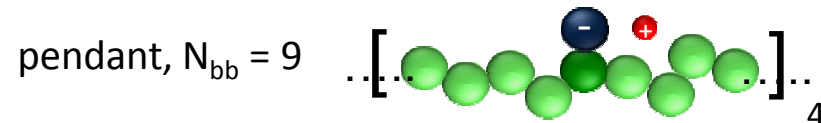
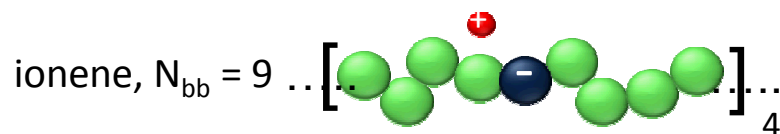
100% neutralization

bulk dielectric constant = 4

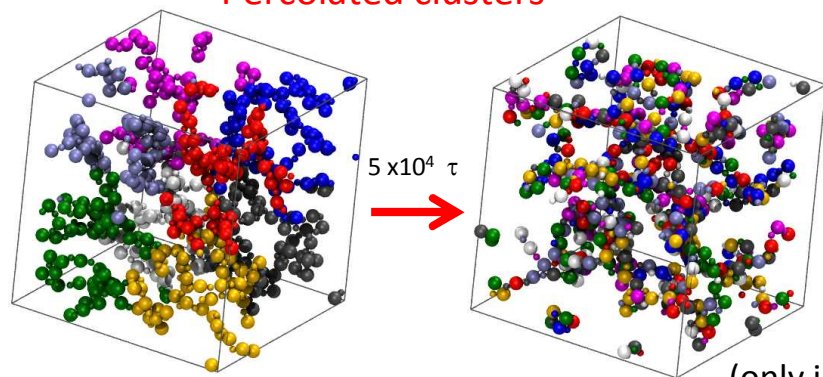
counterion size =  $0.5\sigma$

Bjerrum length =  $35.7\sigma$

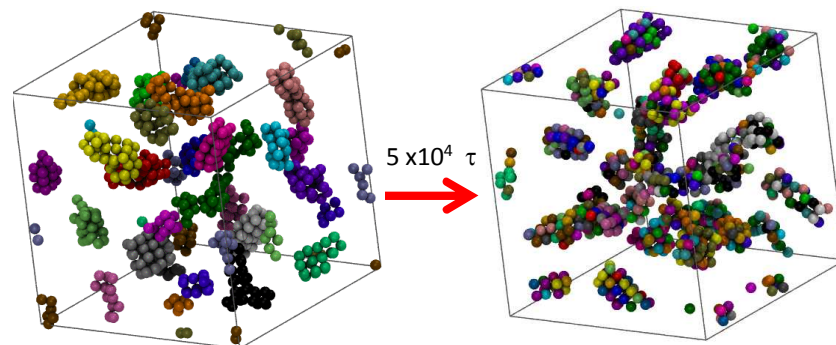
# Aggregate structure and dynamics



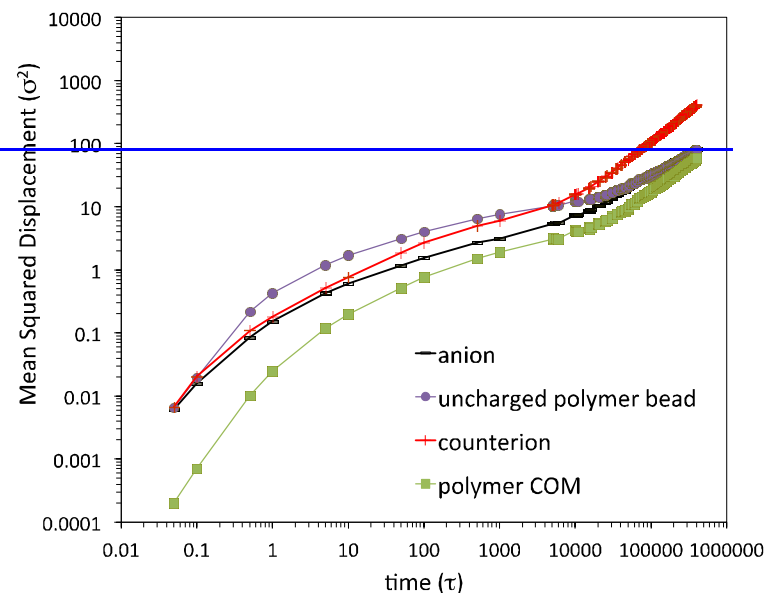
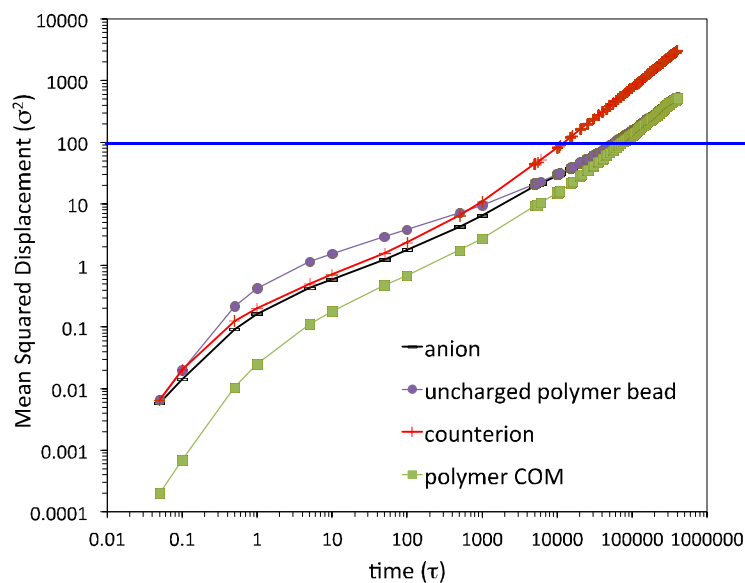
Percolated clusters



Not percolated: discrete compact clusters



(only ions shown)



# How strong a field should we add?

$$E^* = \frac{kT}{q\sigma} = 1$$

Adds force  $F_x = qE_x$  to each ion  $\longrightarrow F = 1/kT\sigma$

Compare with electrostatic force between two ions at contact:

$$\frac{F}{kT\sigma} = -\frac{q_i q_j}{r^2} \frac{\ell_B}{\sigma} \quad \begin{array}{l} \ell_B/\sigma = 35.7 \\ r = 0.75\sigma \end{array}$$

$$F = -63/kT\sigma$$

Rough estimate for  $E^* = 1$  in real units:

$$\sigma = 0.4\text{nm}, \quad T = 298\text{K}, \quad E = 0.8\text{V/nm}$$

# Visualizing field effects on clusters

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pendants,  $N_{bb} = 9$

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$E = 0$

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→  
after  $1.5 \times 10^4 \tau$

$E = 1.0$

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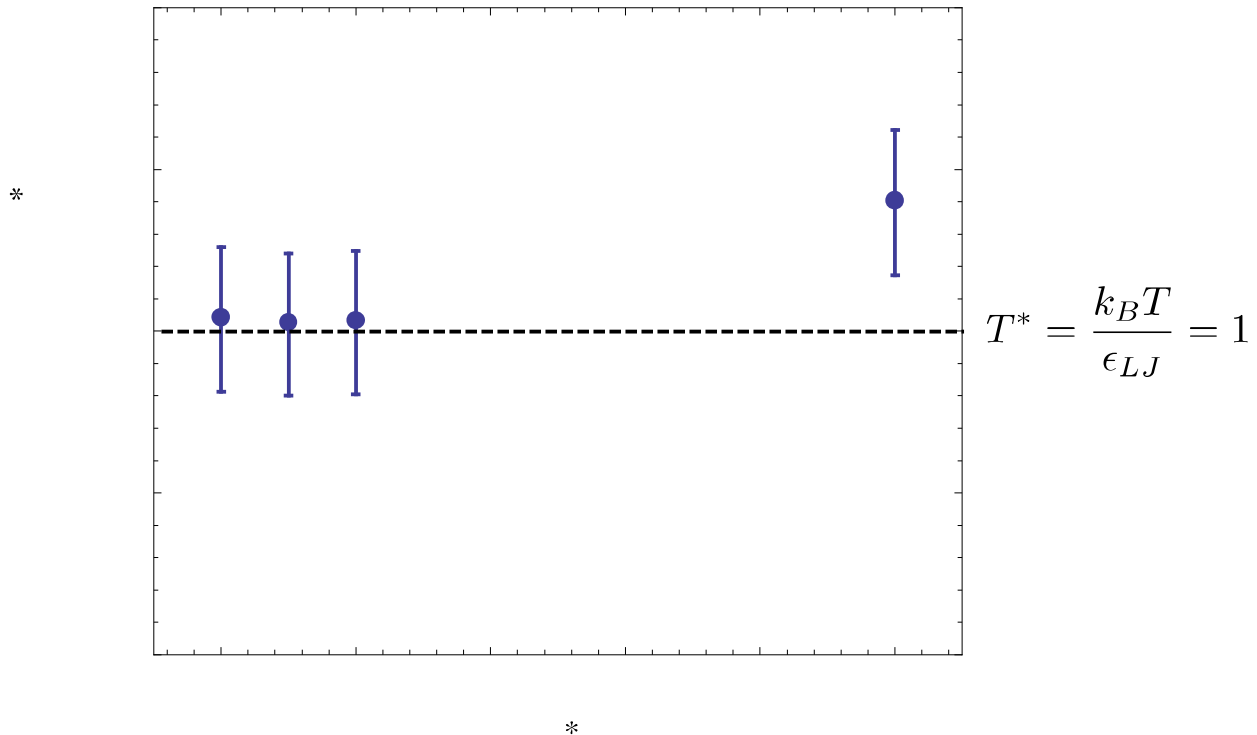
$E = 5.0$

Clusters visibly align in  
high fields

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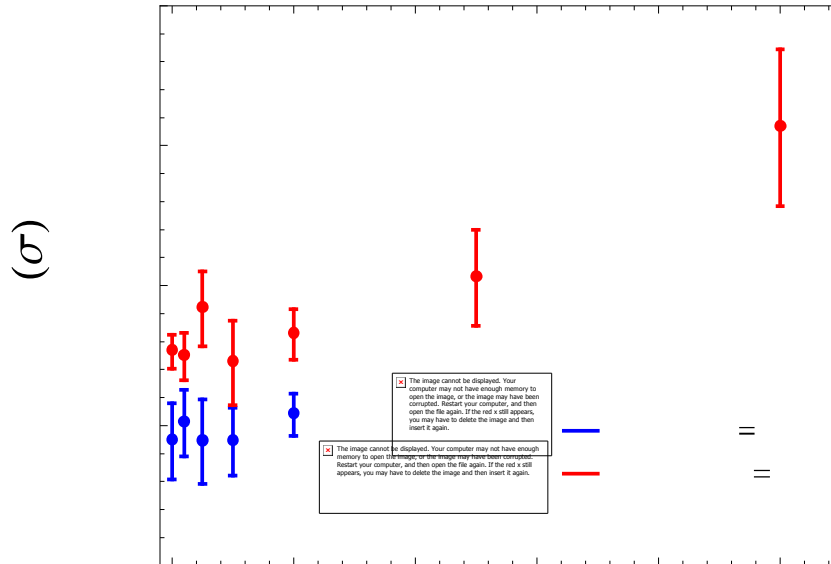
# Check Field Strengths

Turn off thermostat in field direction:

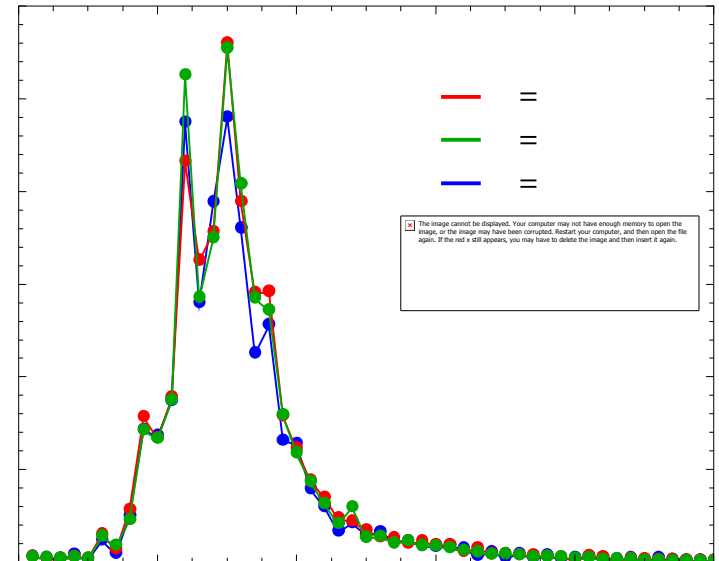


# Field effects on structure

## Polymer size



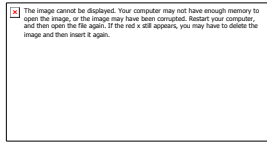
## Cluster size distribution



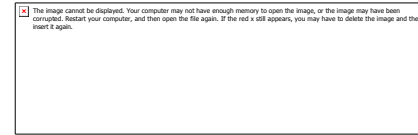
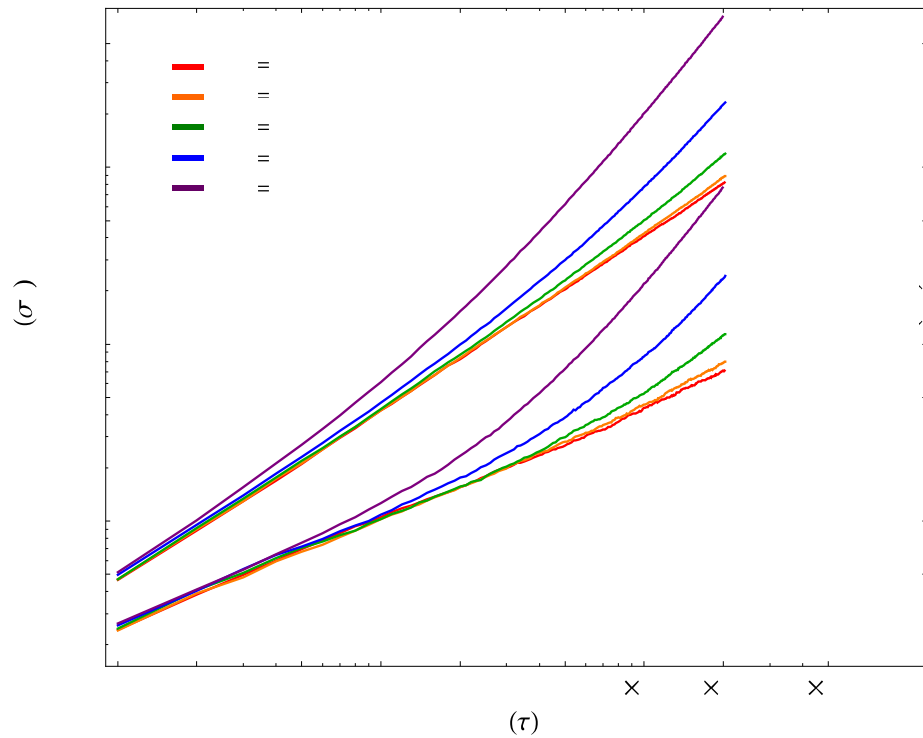
no effect on structure for  $E \leq 1$



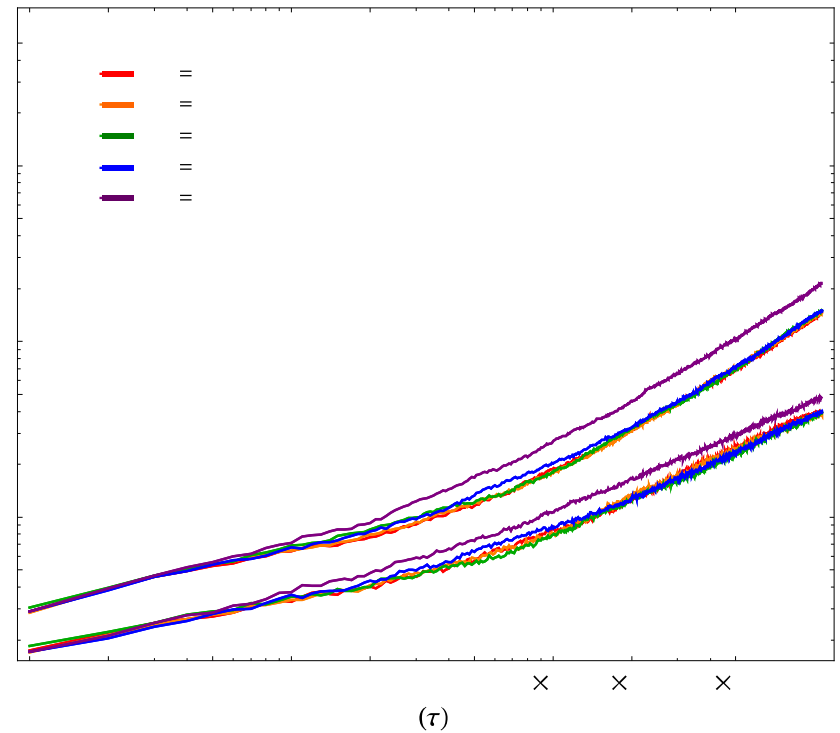
# Field effects on dynamics: MSDs



ionene,  $N_{bb} = 3$   
(highest fraction of percolated ions)



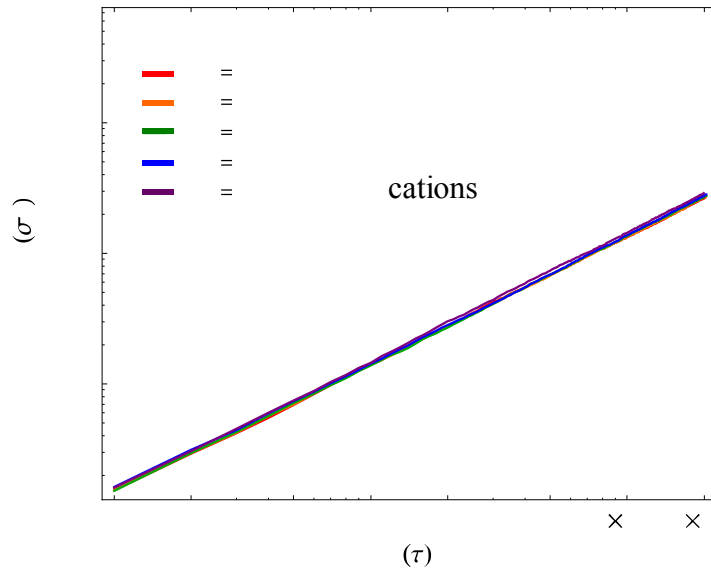
pendant,  $N_{bb} = 9$   
(discrete ionic aggregates)



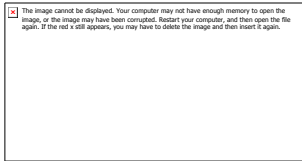
# Directional MSDs and the conductivity



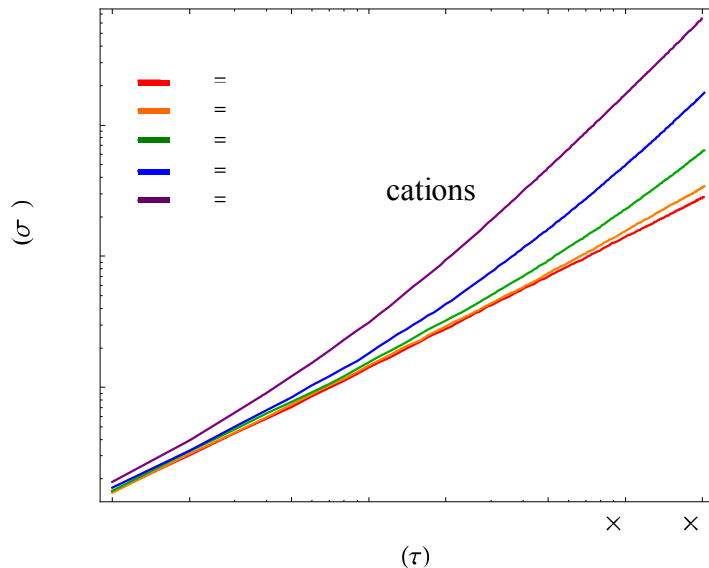
*perpendicular to field*



# Directional MSDs and the conductivity



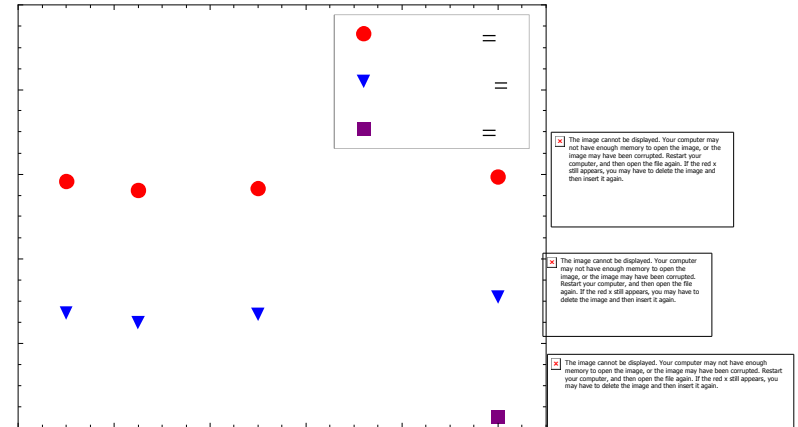
*in field direction*



drift velocity:  $\langle x_E^2(t) \rangle - \langle x_0^2(t) \rangle = \langle v_x^2 \rangle t^2$

ion mobility:  $\mu_i = \langle v_{x,i} \rangle / E$

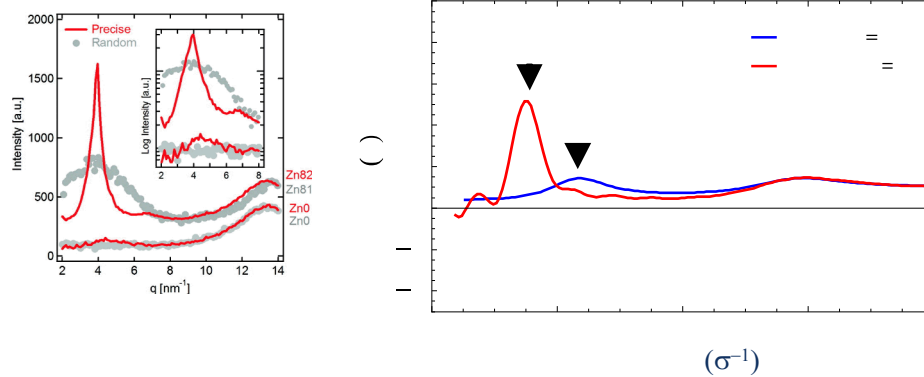
conductivity:  $\lambda = \rho e (\mu_+ - \mu_-)$



if ions are uncorrelated:  $\lambda^{NE} = \frac{e^2 \rho}{kT} (D_+ + D_-)$

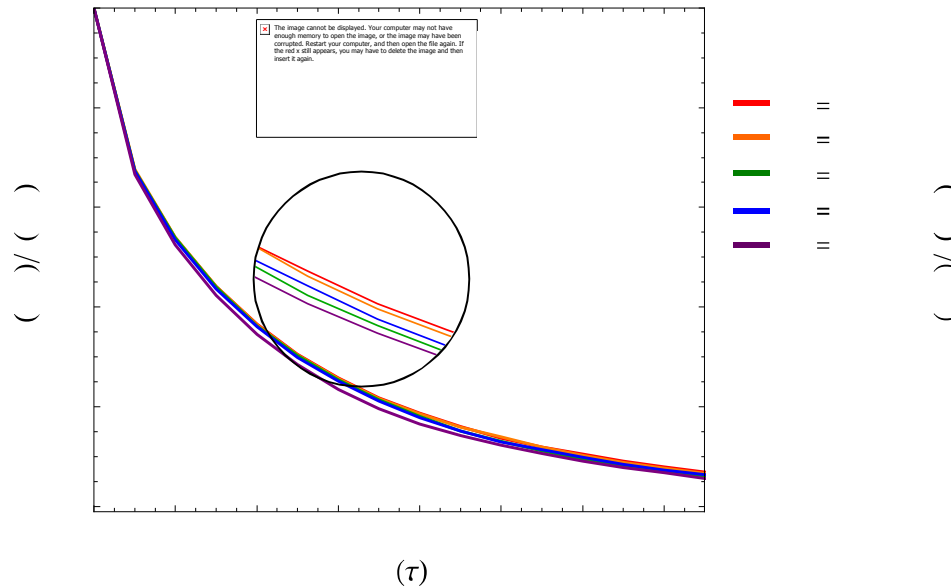
system	$\alpha = \lambda / \lambda^{NE}$
ionene N = 3	0.36
ionene N = 9	0.18
pendant N = 3	0.36

# Time-dependent structure factor

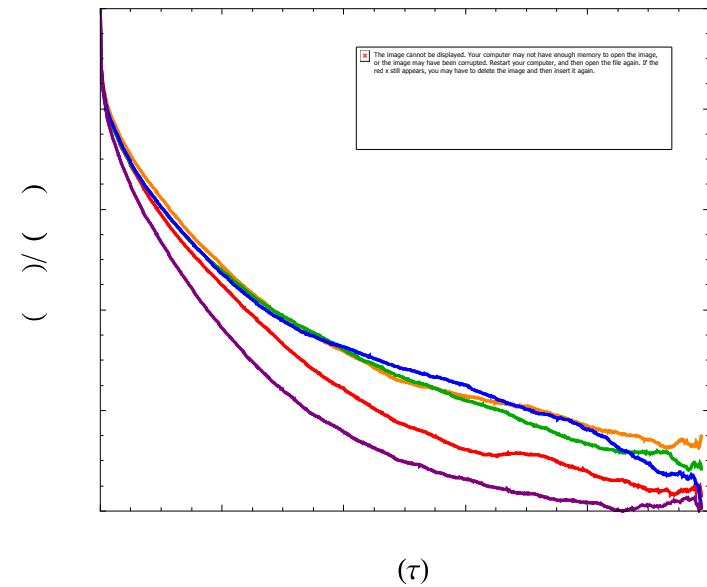


$$S(k, t) = 4\pi\rho \int_0^\infty \frac{\sin(kr)}{kr} r^2 (g(r, t) - 1) dr$$

ionene,  $N_{bb} = 3$   
(highest fraction of percolated ions)



pendant,  $N_{bb} = 9$   
(discrete ionic aggregates)



# Conclusions and future work

Conductivity is highest for ionene systems, concentration-dependent  
Ions are correlated

Field speeds up dynamics and decorrelation clusters for percolated case  
Moderate fields slows down decorrelation of discrete, isolated clusters

Analyze cluster trajectories to better understand field effect on dynamics.

## Acknowledgements



Lisa Hall (now at OSU)



Mark Stevens



Amalie Frischknecht

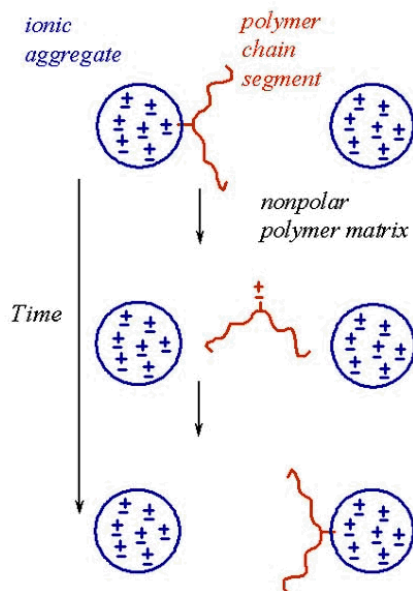
Harry S. Truman Fellowship  
“Ionomers” LDRD team

# Aggregate dynamics

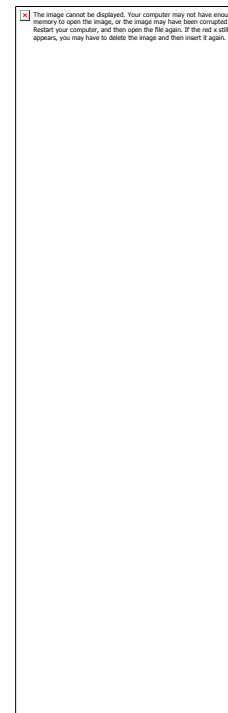
historical view

vs.

simulation view



ion **pairs** “hop” between aggregates



ions move by cluster merging, rearranging, and breaking

# Field effects on structure

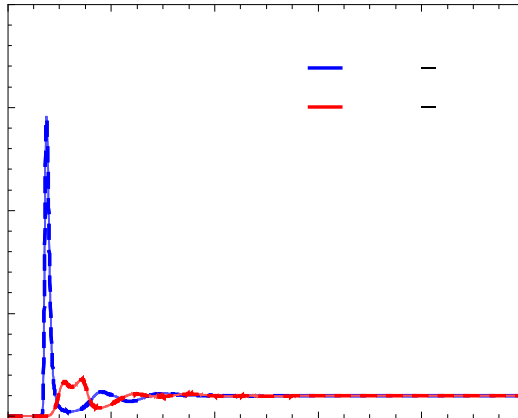
## Pair correlation function

ionene,  $N_{bb} = 3$   
(highest fraction of  
percolated aggregates)

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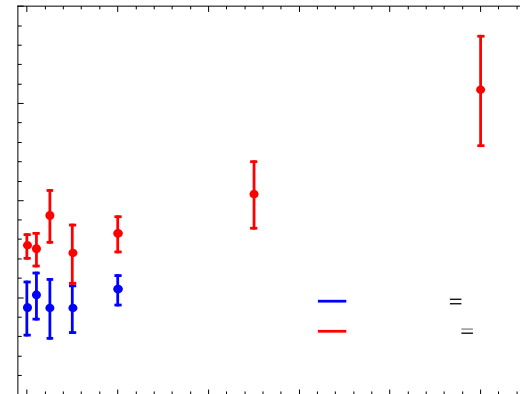
( )

$E = 0$  (solid)  
 $E = 1.0$  (dashed)



## Polymer size

(b)

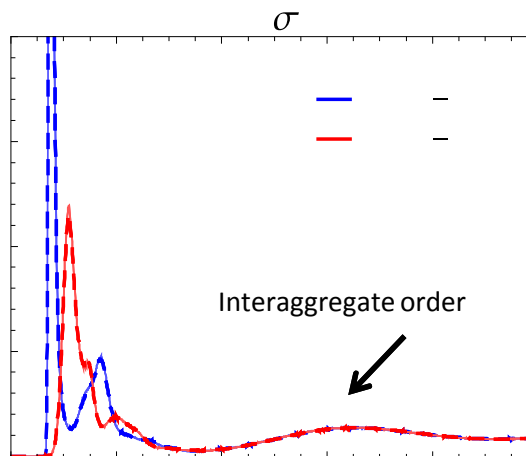


pendant,  $N_{bb} = 9$   
(discrete aggregates)

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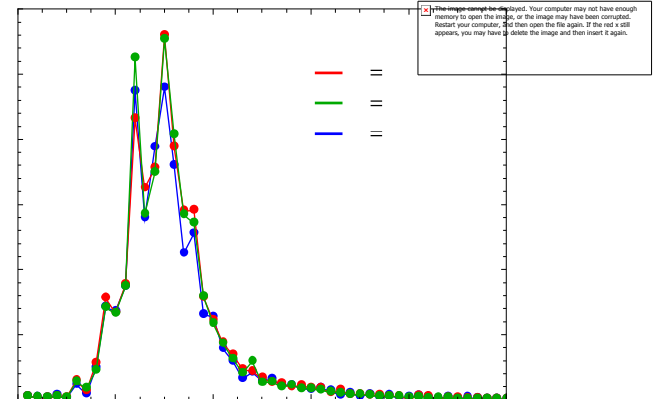
( )

$E = 0$  (solid)  
 $E = 1.0$  (dashed)



$\sigma$

## Cluster distribution for pendant $N_{bb} = 9$



no effect on structure for  $E \leq 1$