

# Self-assembly of Model Microtubules: Shape, Chirality and Twist

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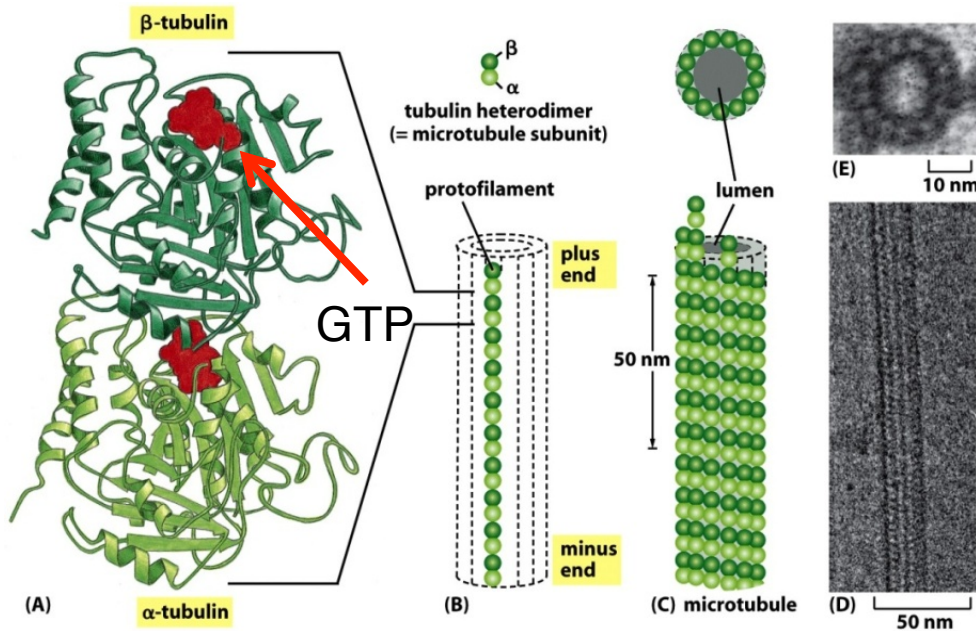
Shengfeng Cheng → Virginia Tech

**Funding: Basic Energy Sciences**



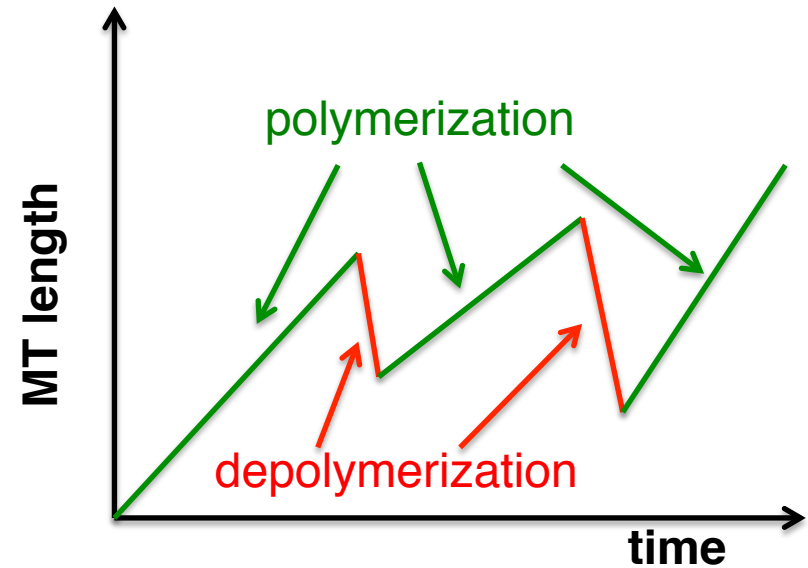
# Microtubules

tubulin to microtubules



Alberts et al., *Molecular Biology of the Cell* (2008)

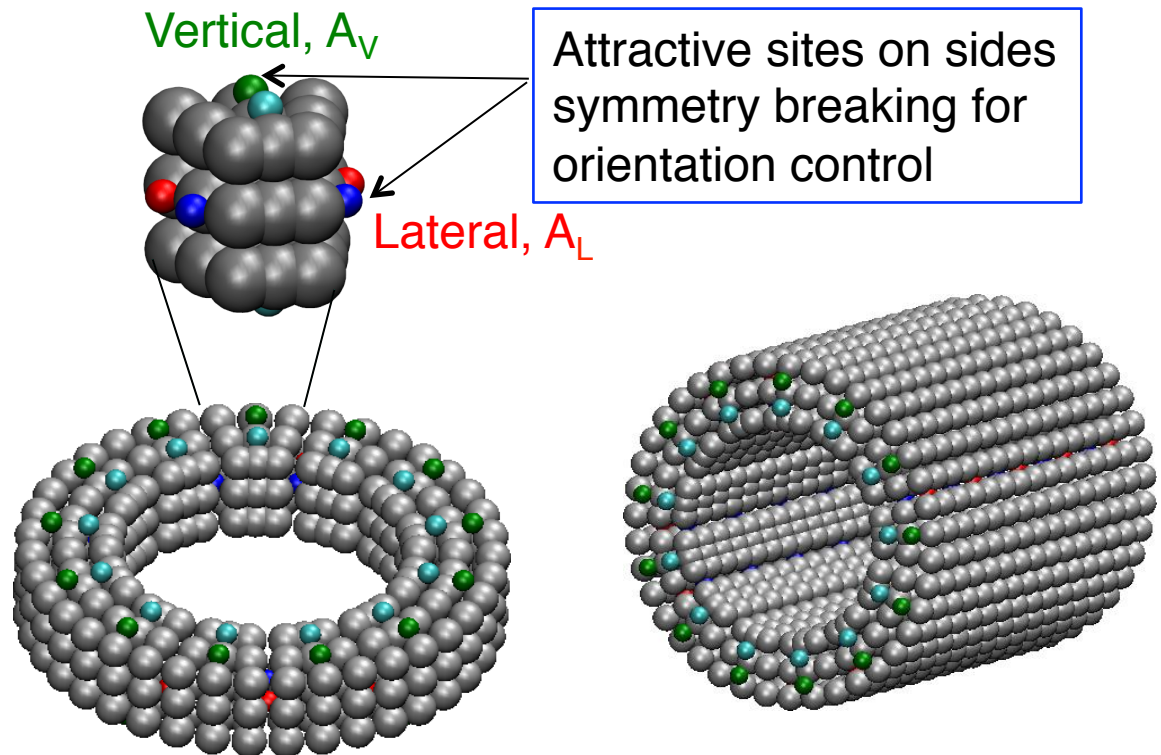
- chiral, tubular polymer
- 24 nm diameter
- most have 13 protofilaments
- very, very stiff
- dynamic growth & depolymerization
- track from motor proteins



# Monomer Model

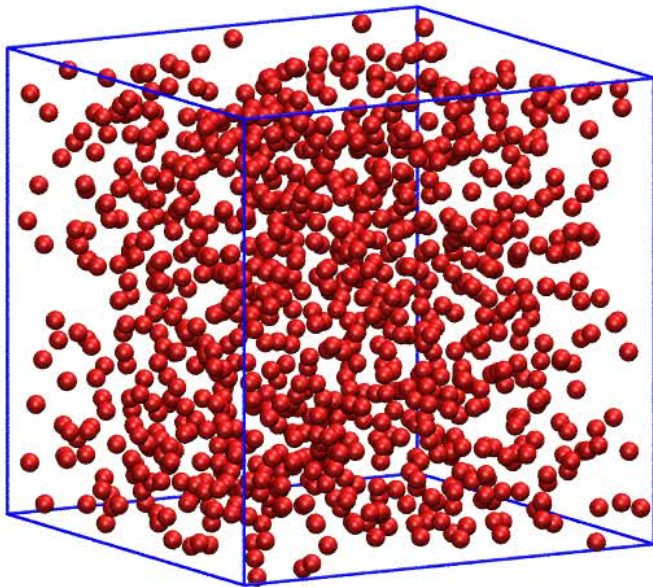
## Wedge monomer

- shape designed to produce rings that stack into cylinders
  - 13 wedges/ring
  - gray particles define shape
- gray particles interact purely repulsively
- attraction only between sites of same 'color'
- implicit good solvent

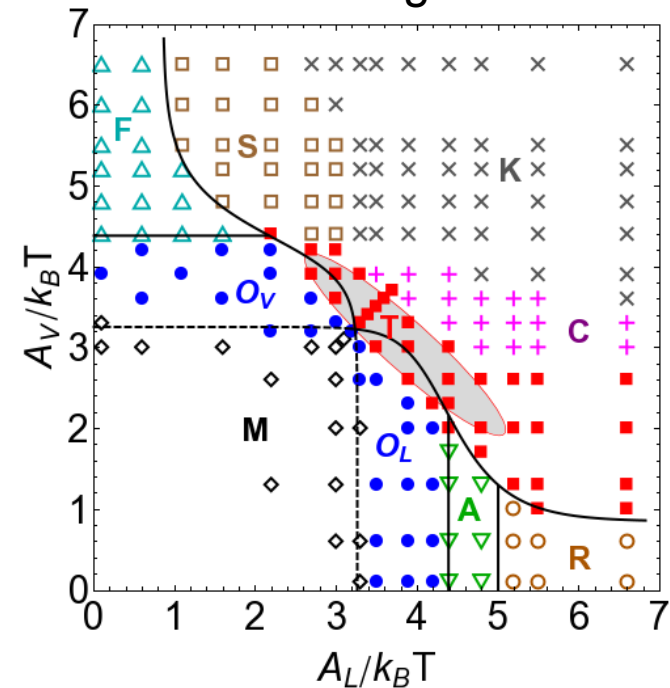


# MD Simulations

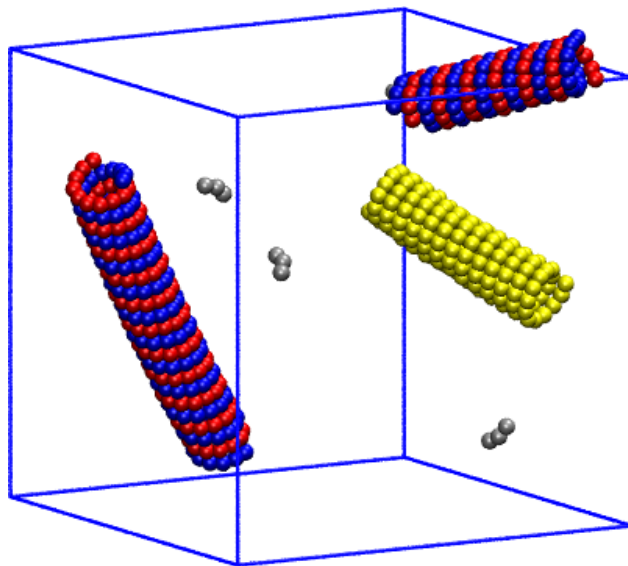
- monomer is a rigid body
- standard NVT MD,  $\sim 1$  billion time steps
- 1000 **achiral** wedge monomers
- Starting state: with  $A_L = 4.2$  kT and  $A_V = 3.0$  kT
- Wedge shown as single sphere
- **Monomers to tubules**



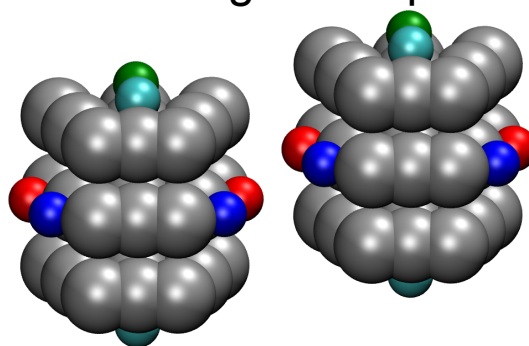
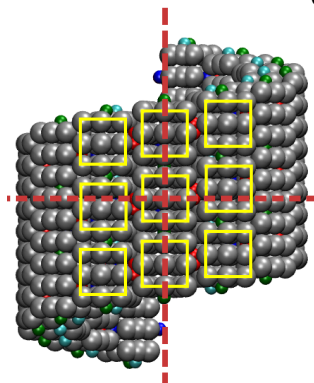
vary lateral  $A_L$  and vertical  $A_V$  interaction strengths



# Helical Tubules?



Shouldn't **mismatch** between attractive sites make the energy be much higher for pitch  $> 0$ ?

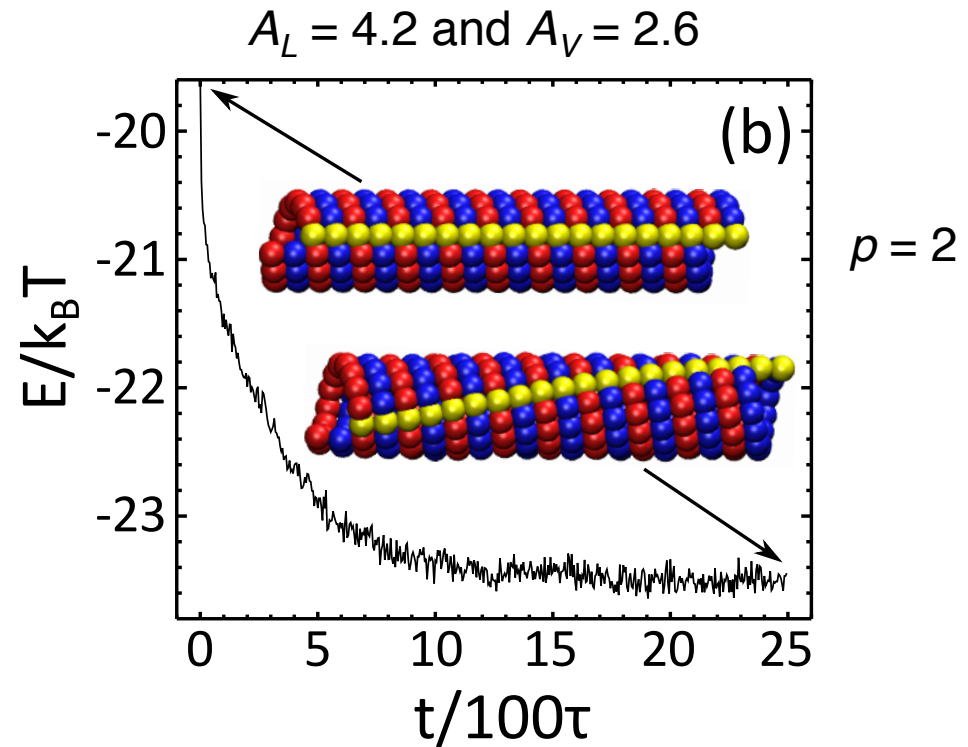


**chirality = 0**



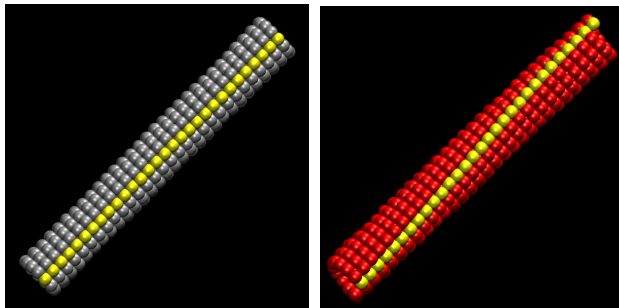
# Twist & Energy

- Build tubule with pitch  $p$
- Do MD
- Calculate energy distribution
  
- Energy drops
- Tubule twists



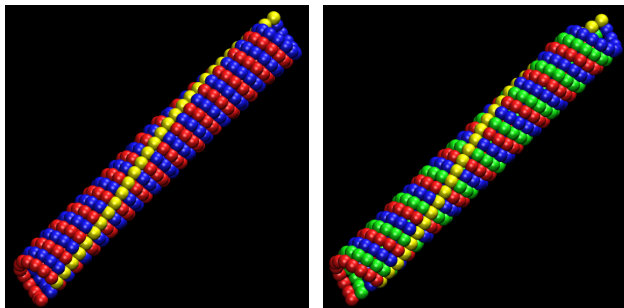
# Twist & Energy

- Number of protofilaments ( $N$ )
- Pitch of helix ( $p$ )
- $N_p$



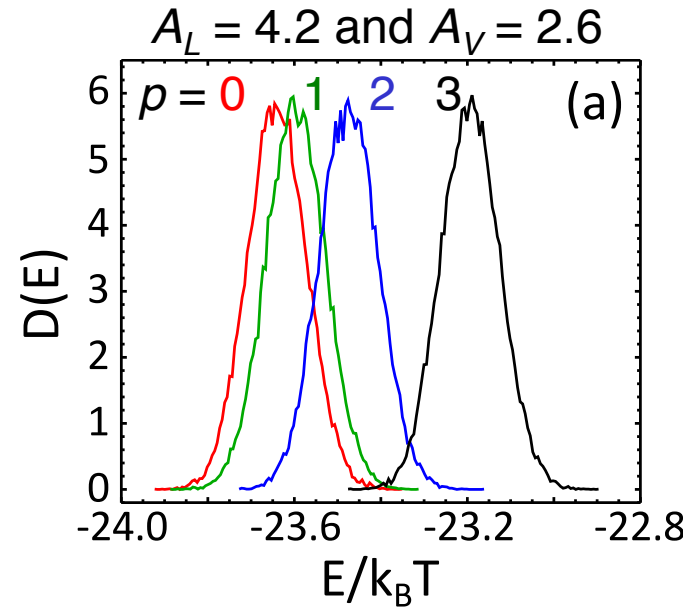
13\_0

13\_1



13\_2

13\_3

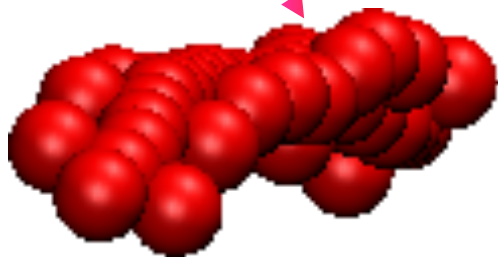
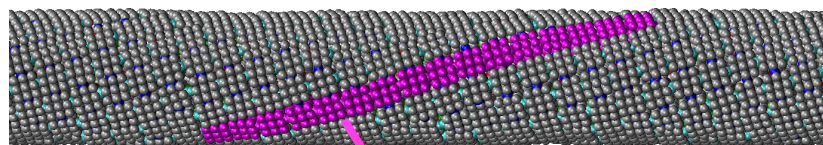
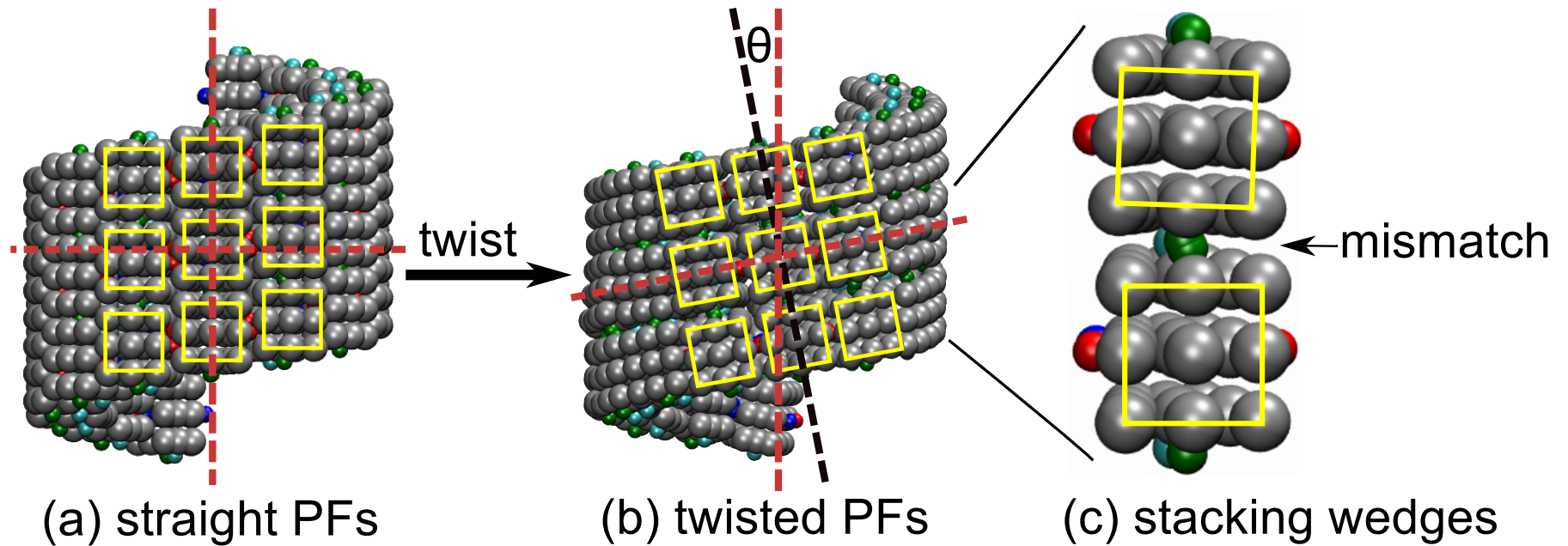


Overlap of  $D(E) \Rightarrow$  coexistence of different pitches

Why do  $p=0$  & 1 overlap?  
Why don't  $p=0$  and 3 overlap?



# Twist & Alignment



Twist:

Rotation about radial axis aligns lateral binding sites

Rotation about vertical axis misaligns vertical sites

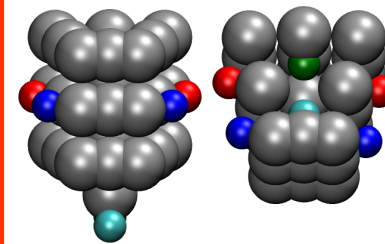
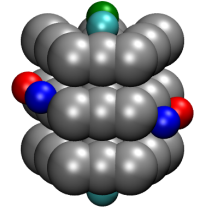


# Tubule Pitch

- How control pitch?
  - chiral monomer
  - reduce variation in pitch
- Twist misaligns vertical placement
  - increase  $A_v$  ?
  - lock & key

## Chirality $c$

Shift positions of lateral site up/down to produce chirality



## Lock & Key $LK$

Push central column down



# Modifying Monomer

Make vertical mismatch expensive

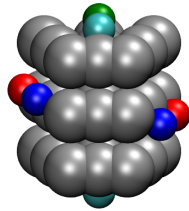
$A_V > A_L$  better?

$A_V = 6.3$

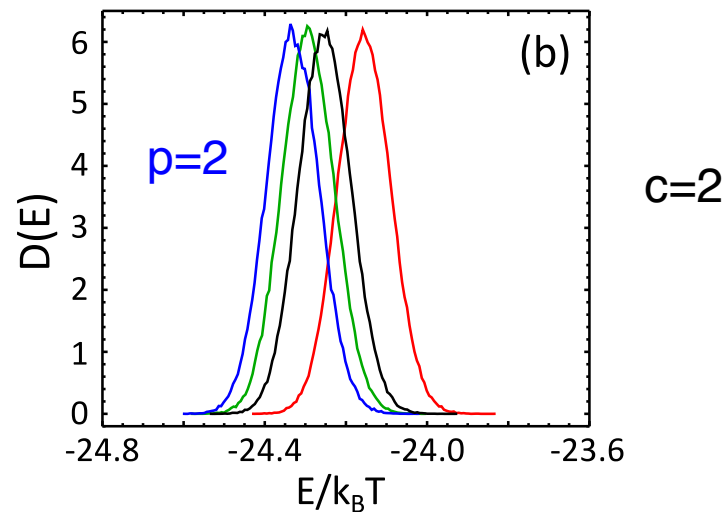
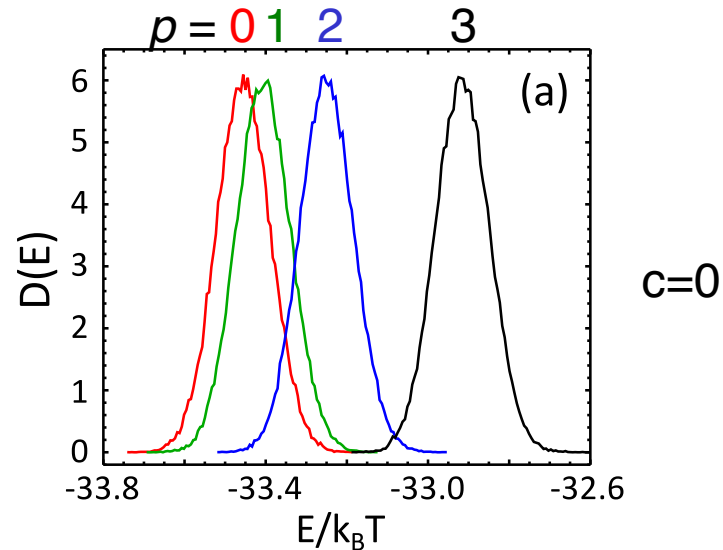
$A_L = 3.0$

but kinetically trapped

**Chirality**  $c \rightarrow$   
tubule pitch  $p$



Chirality does shift  
pitch values.



# Energy distribution

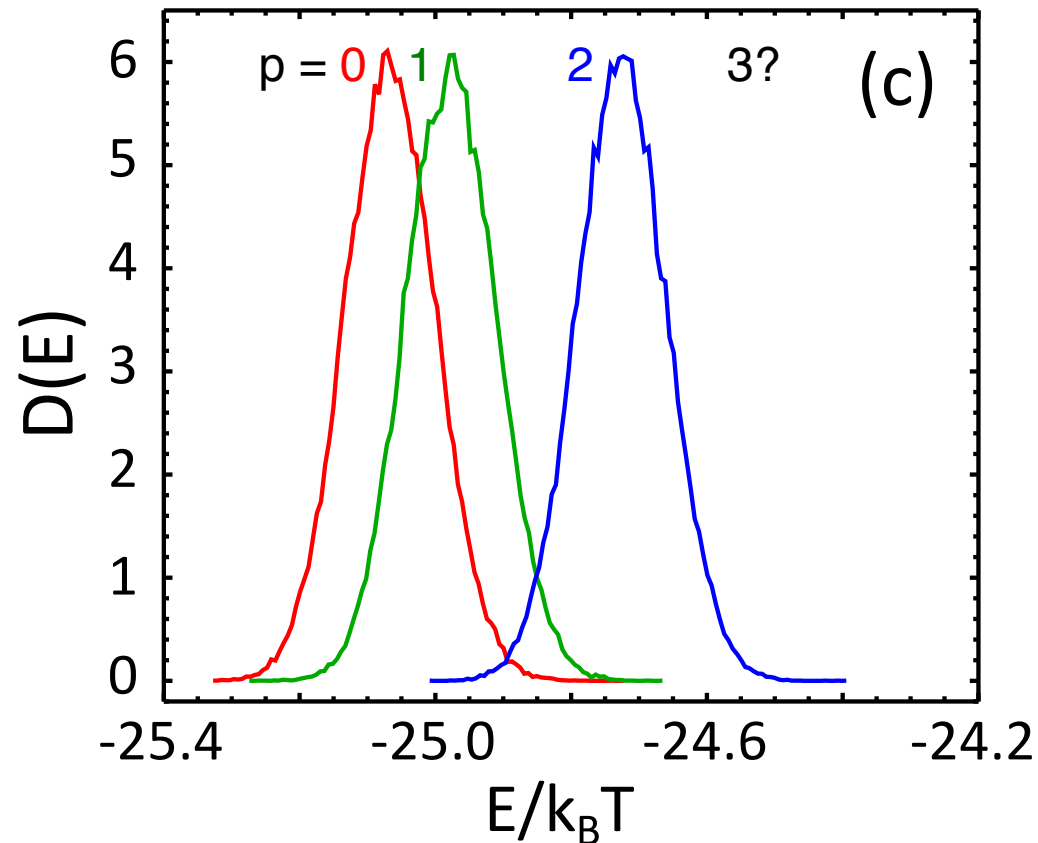
Lock & Key  
(must increase  $A_V$  to  
insert key)

$$A_V = 6.3$$

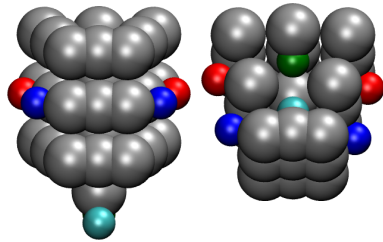
$$A_L = 3.0$$

$$c=0$$

See increased  
separation of  $D(E)$   
and disappearance of  
 $p=3$ .



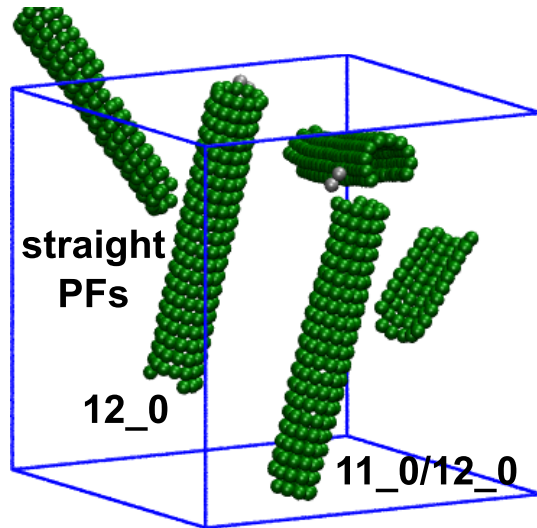
# Lock & Key, Chiral Assembly



Need stronger vertical interaction, but cannot increase  $A_v$

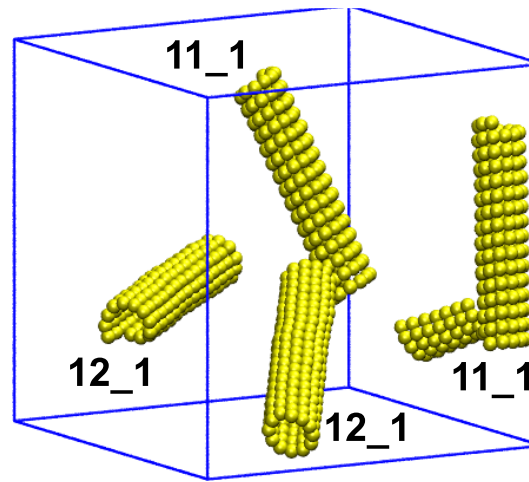
Introduce lock & key

It works!



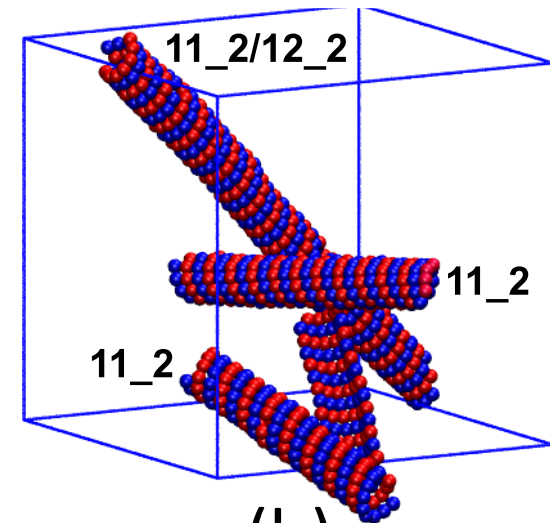
(f)

$c=0$   
 $p=0$



(g)

$c=1$   
 $p=1$



(h)

$c=2$   
 $p=2$



# Summary

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- Model system forms tubules
- Have now introduced chiral and lock-and-key in monomer
- Twist allows multiple tubule pitch values
- Can control pitch better than should be able to
- Need strong vertical interaction to limit pitch values
  - true in microtubules
- Find a range of pitch and protofilament number in assembly simulations
  - true in microtubules

## Future

- mechanics
- model development
  - two state monomer (GTP/GDP)
  - dimer (Why is microtubule monomer a dimer?)
    - need for  $p=3$ ?
  - charges (repulsion, attraction, longer range)
  - adjust wedge geometry to obtain  $N = 13$  on average
  - explicit solvent (number of particles  $\rightarrow \sim 1$  Sagan)



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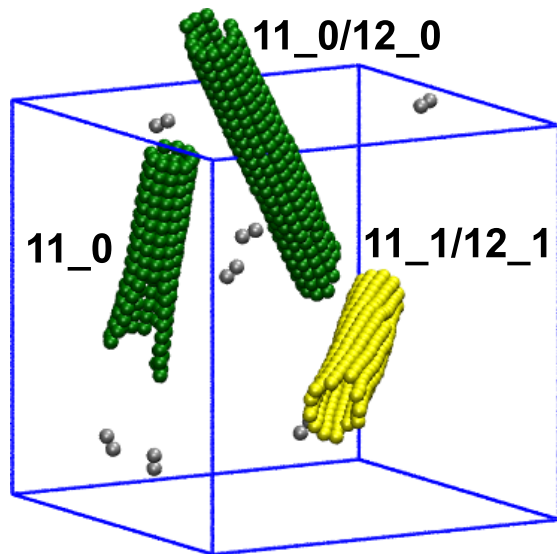
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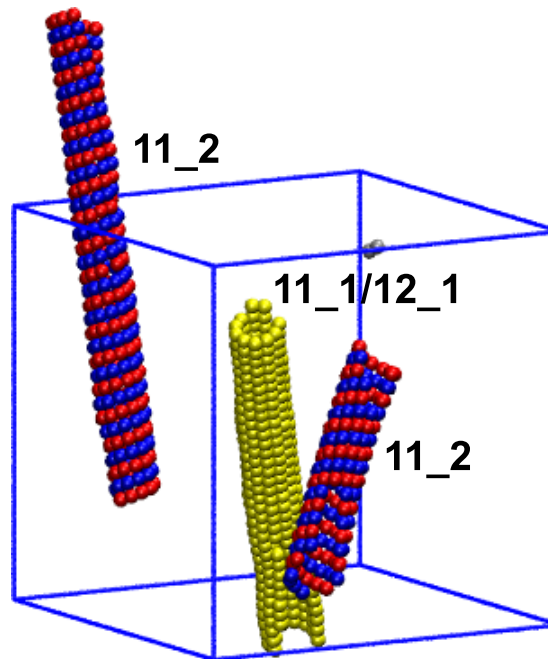
# Self-Assembly with Chiral Monomers

$A_V=3.9, A_L=3.0$



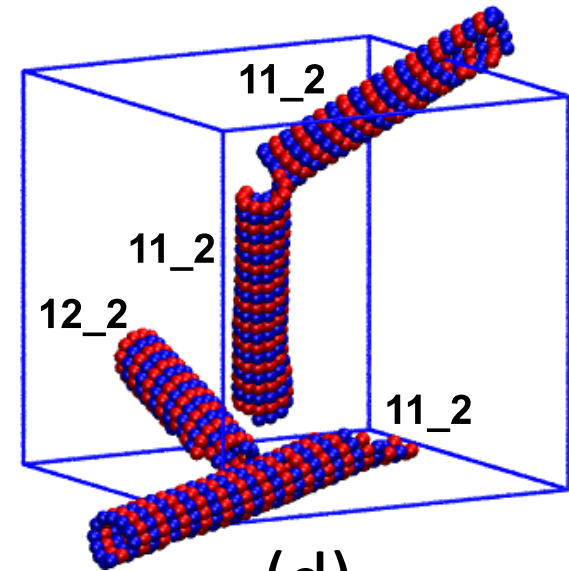
(b)

$c=0$   
 $p=0,1$



(c)

$c=1$   
 $p=1,2$



(d)

$c=2$   
 $p=2!$



# Microtubules

monomer is  $\alpha$ - $\beta$  tubulin

13 monomers per turn

24 nm diameter

polymerization/depolymerization

protofilaments  $\rightarrow$  sheets  $\rightarrow$  tubules

catastrophe

polarity

binding involves GTP/GDP

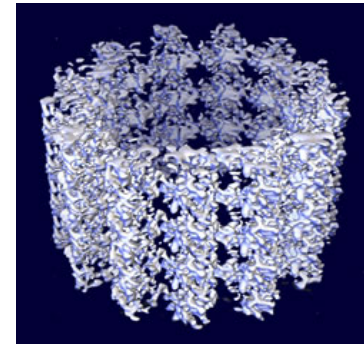
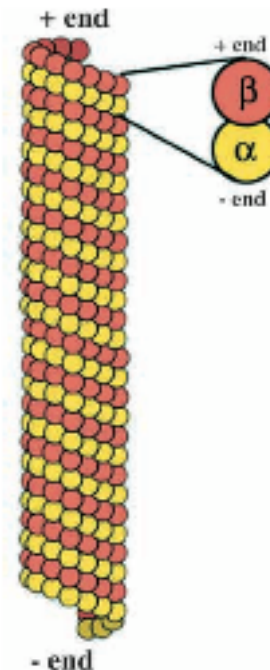
motor proteins walk on MT

tubulin polymers

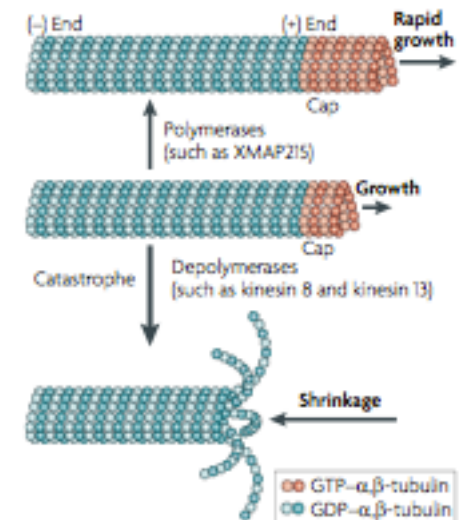
straight: protofilaments, GTP bound

curved: depolymerizing protofilaments/GDP bound

**Microtubules are an example of hierarchically assembled structure with many interesting features.**



GTP cap



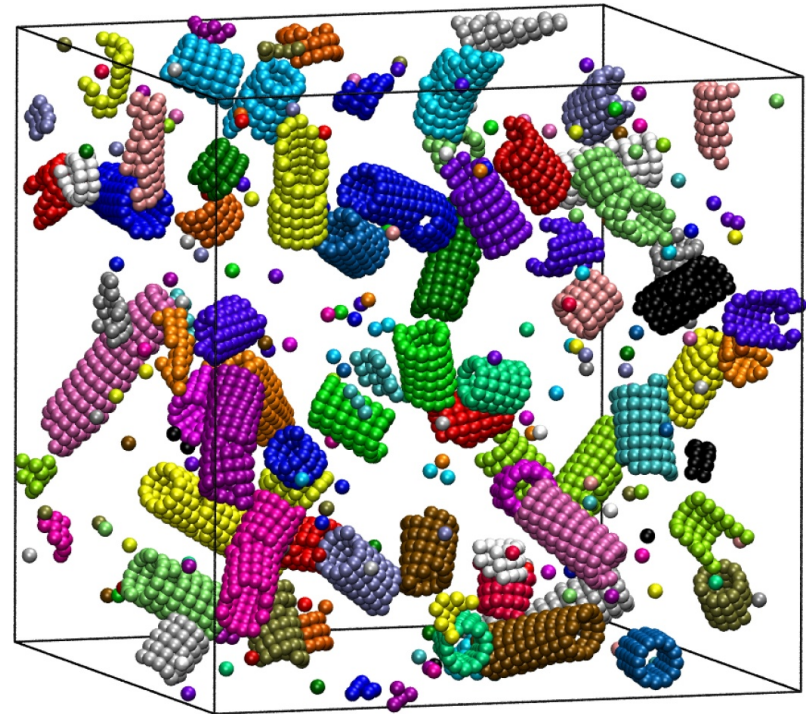
# What are the factors that control assembly?

What features are necessary in the monomer?

The monomer is going to be a nanoparticle or a macromolecule (e.g. dendrimer) with large surface area.

- How do monomer shape and structure influence polymer structure (i.e. tubule).
- Where are interaction sites placed?
- How strong should they be?

Proteins as monomers possess a complex set of interactions.



# Artificial Microtubules (?)

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Can we generalize microtubules? Can we make synthetic variations?  
What do we need to know about the monomer building block?

complex surfaces → set of interactions → complex systems  
shape change (GDP/GTP binding) [energy driven system]

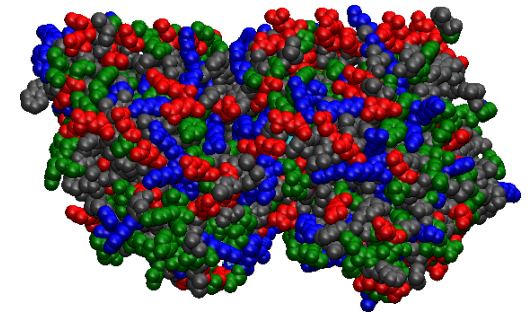
Very complex. Let's start 'simple.'

**How assemble tubular polymer?**  
(focus on geometry first)

**What features are necessary in the monomer?**

- How do monomer shape and structure influence polymer structure (i.e. tubule).
- Where are interaction sites placed?
- How strong should they be?

tubulin dimer



acidic, basic, polar, nonpolar

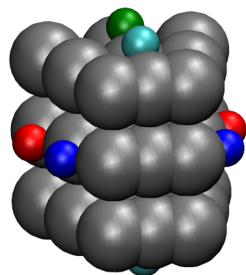


# Theoretical Structure Diagram

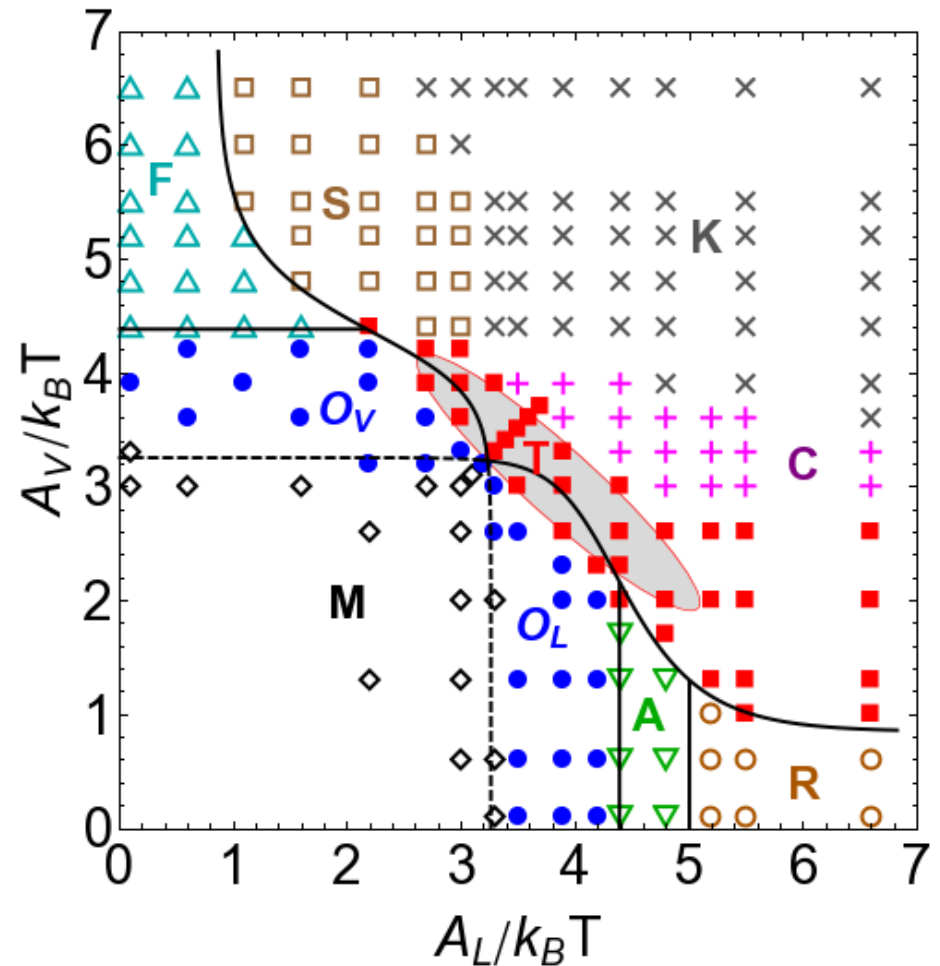
Each wedge is represented by a sphere.  
Color represents cluster size.

- M) no assembly
- O) oligomers
- F) filaments
- A) arcs
- R) rings
- S) sheets
- K) kinetically trapped (gunk)
- C) clusters
- T) Tubes

vertical,  $A_v$



Lateral,  $A_L$



Soft Matter, 2012

