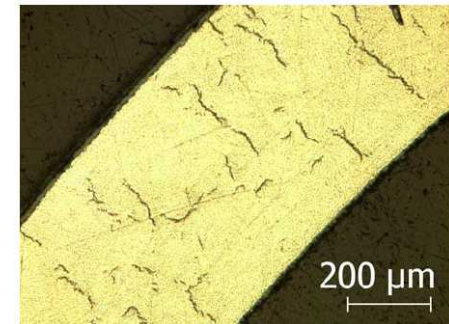


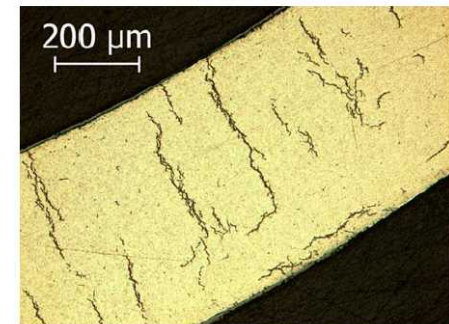
# Simulation of Hydride Formation in Zr-Based Cladding during Dry Storage

SAND2014-0657C

**Veena Tikare**  
**Sandia National Laboratories**  
**Albuquerque, NM**



(a) 50% RHCF



**Billone et al, ANL, 2013**

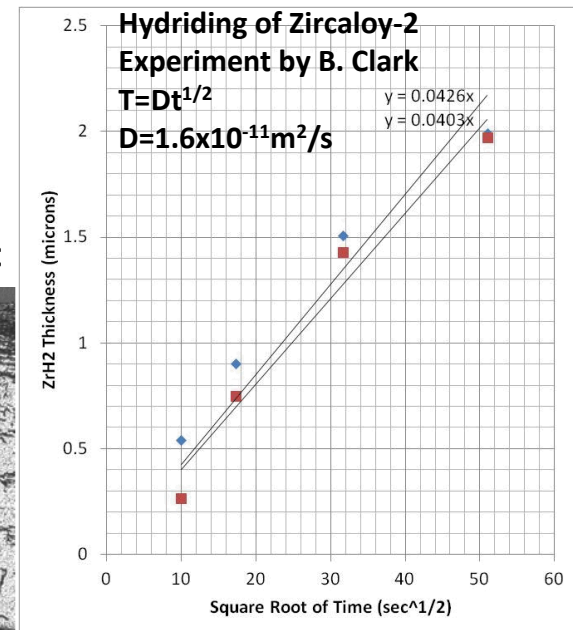
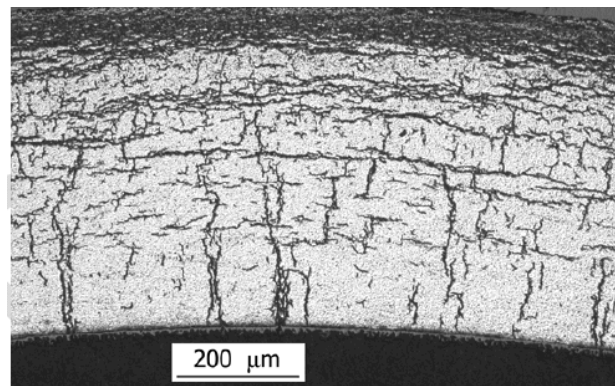
Sandia is a multiprogram laboratory operated by Sandia Corporation,  
a Lockheed Martin Company, for the United States Department of Energy  
under the Contract DE-AC04-94AL-85000.

# ZrH<sub>2</sub> Formation during Dry Storage May Limit the Lifetime of Used Nuclear Fuel Cladding

Hydride formation in Zr-based cladding is known to degrade clad reliability during dry storage

- The drying cycle dissolves the ZrH<sub>2</sub>.
- During dry storage as the clad temperature decreases, the ZrH<sub>2</sub> precipitates on grain boundaries, dislocation loops and, possibly, other defects.
- ZrH<sub>2</sub> forms perpendicular to the tensile stress
- Its morphology appears to be needle-like lathes
- B. Clark's experiments indicate the ZrH<sub>2</sub> growth is diffusion controlled
- Microstructure, stress, composition, H pick-up, temperature are known to control ZrH<sub>2</sub> formation & morphology.

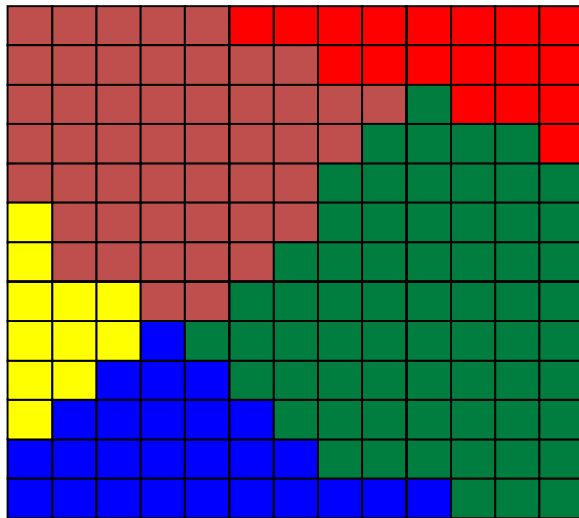
Zirlo 720 wppmH 140 MPa hoop stress 400 °C



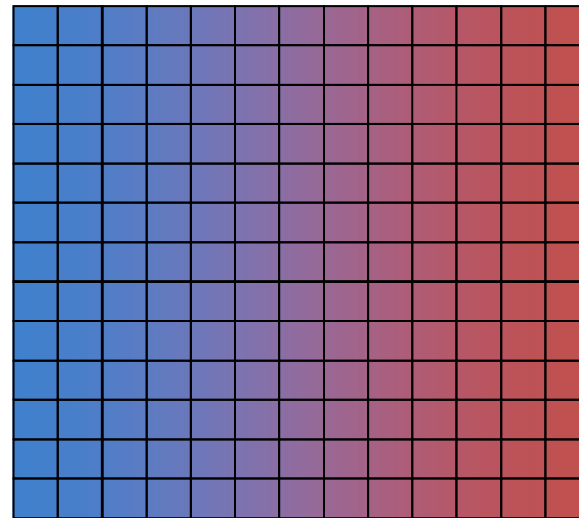
# Representation of Microstructure and Composition Hybrid Model

- Potts kMC digitizes represents microstructure using spins  $q_i$
- Phase field represents composition with field variable  $C_i$ 
  - Both are on the same grid

Microstructure



Composition



# Equation of State (Thermodynamics)

## Hybrid Model

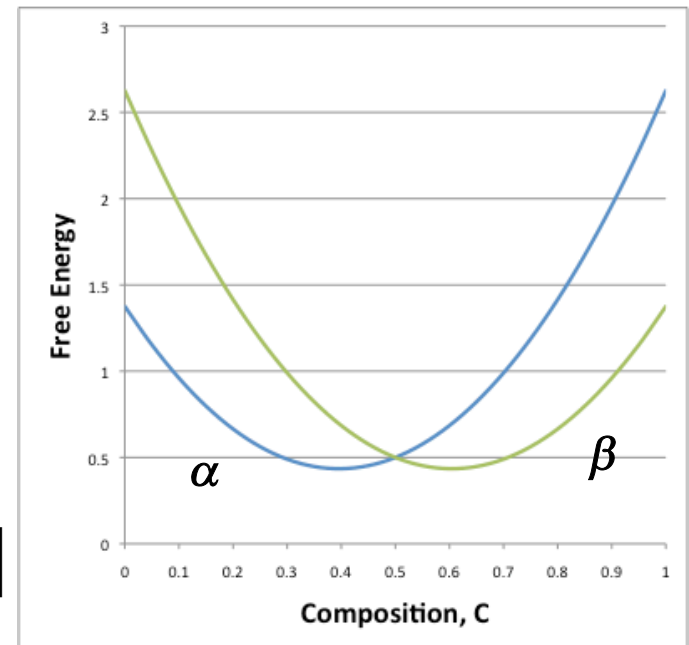
- EOS is a function of volume free energy and interfacial energies.

$$E_{hyb} = \sum_{i=1}^N \left( \underbrace{E_v(q_i, C)}_{\text{Volume free energy}} + \underbrace{\frac{1}{2} \sum_{j=1}^n J(q_i, q_j)}_{\text{Interfacial free energy}} \right) + E_{dC}$$

$$E_{dC} = \int 2\kappa_C (\nabla C)^2 dV$$

An example of  $E_v$

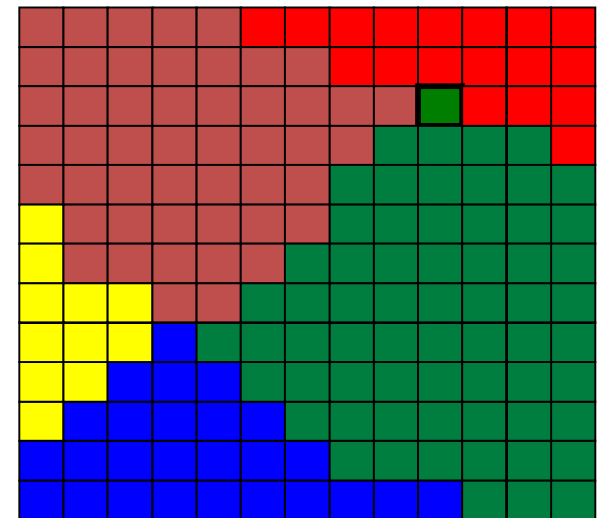
$$E_v = a \left[ (C - C_1)^2 + (C_2 - C)^2 \right] + b \left[ (C - C_3)q_\alpha + (C_4 - C)q_\beta \right]$$



# Representation of Microstructure and Composition

## kMC

- Potts kMC digitizes space into discrete 'bits' of material
  - An ensemble of particles populate the lattice
  - Each color can represent a membership in a phase and / or feature (i.e. grain)
  - Each color can also represent composition, but true gradients in composition would require huge simulations



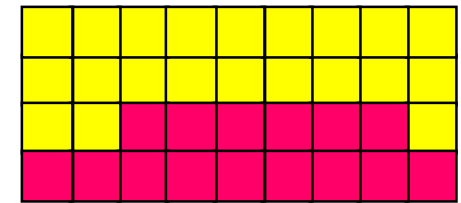
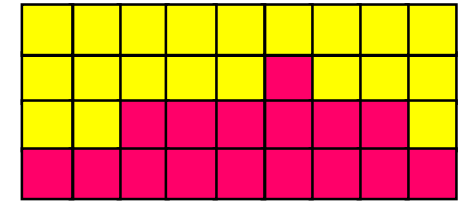
# Kinetic of Evolution Hybrid Model

- Microstructure is evolved in the same manner as Potts in response to local free energy using  $E_{hyb}$ 
  - Metropolis algorithm
- Composition evolved as a phase field parameter.

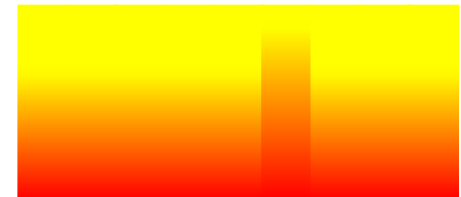
$$\frac{\partial C}{\partial t} = -M_c \left( \nabla^2 \frac{\partial E_v}{\partial C} - \kappa_c \nabla^4 C \right)$$

- Where  $E_v$  is from the hybrid Free Energy

grain growth  
change pixel color



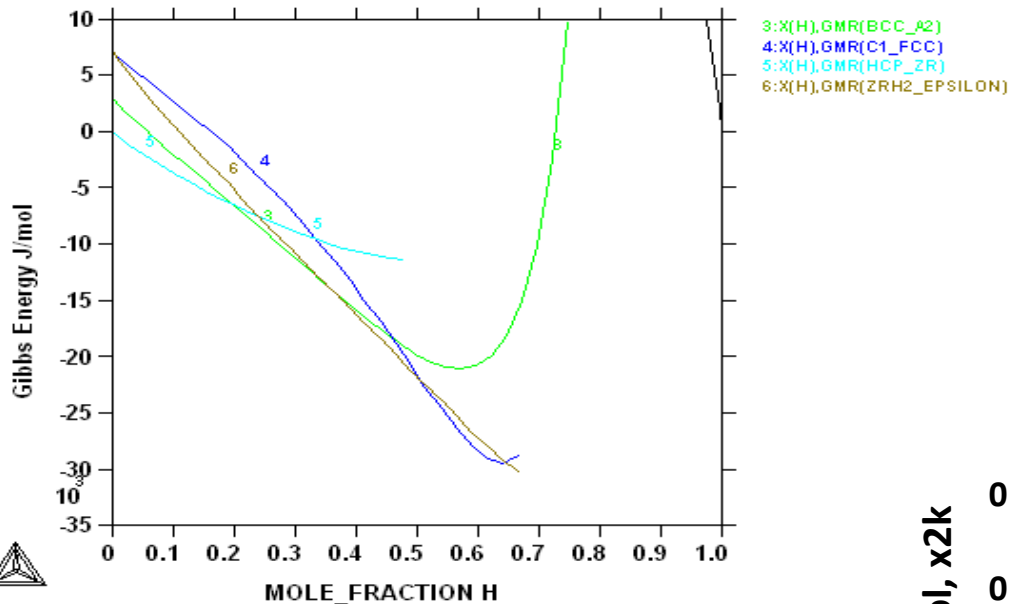
Composition change  
by diffusion



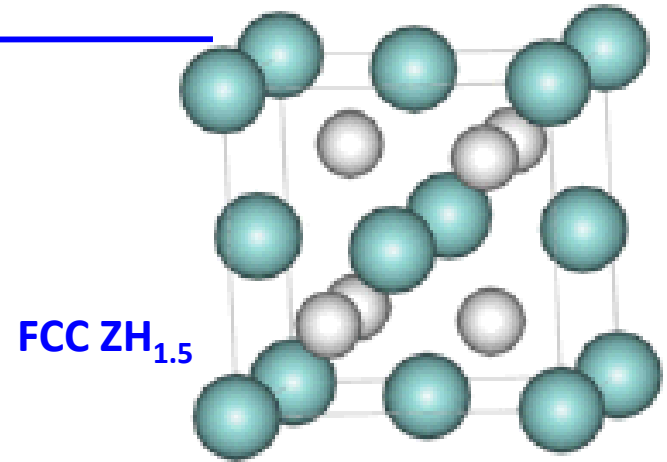
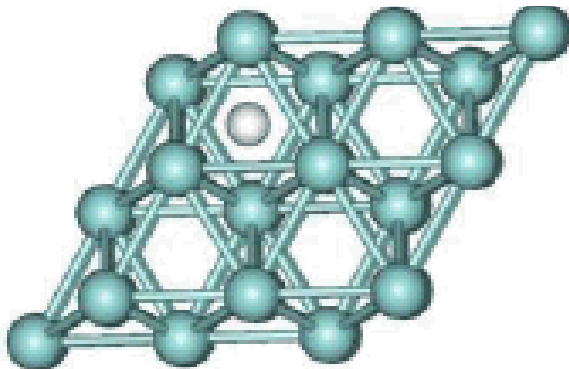
# Phase Equilibrium Calculations for Zr and $\text{ZrH}_{1.5}$

M. Glazoff, INL

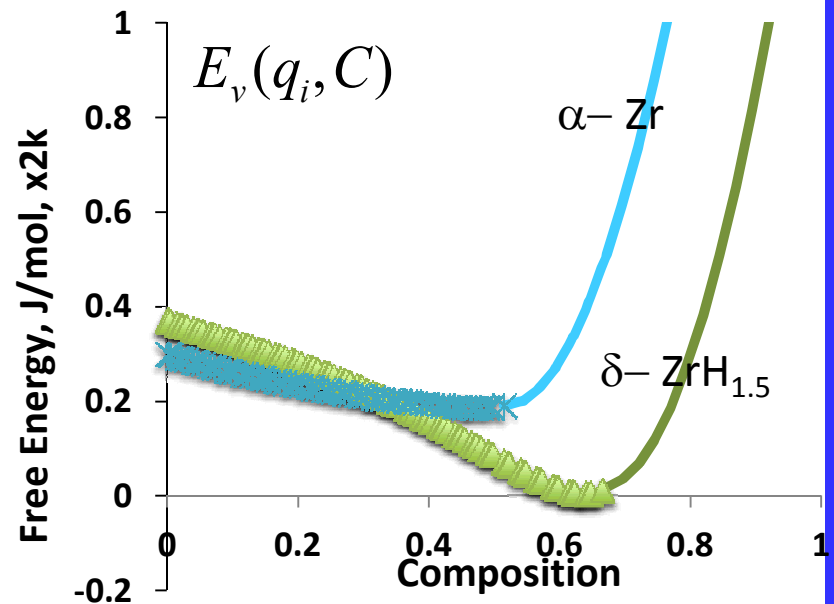
DATABASE:TCBIN  
P=1E5, N=1, T=573;



HCP Zr



FCC  $\text{ZrH}_{1.5}$



Jan, 2014



Sandia National Laboratories

# Morphology of $\text{ZrH}_{1.5}$ Precipitates

## $\text{ZrH}_{1.5}$ Precipitates

- Intragranular
- needle-like lathes
- Cubic (FCC)
- specific crystallographic orientation with HCP Zr
- Growth is by nucleation and diffusion-controlled growth



Hydride Precipitates orient on  $(111)_\delta // (0001)_\alpha$ ;  $[1\bar{1}0]_\delta // [11\bar{2}0]_\alpha$   
 $(111)_\delta // (10\bar{1}0)_\alpha$ ;  $[1\bar{1}0]_\delta // [11\bar{2}0]_\alpha$

Bradbrook et al, JNM 1972



# Hybrid Potts-Phase Field Model

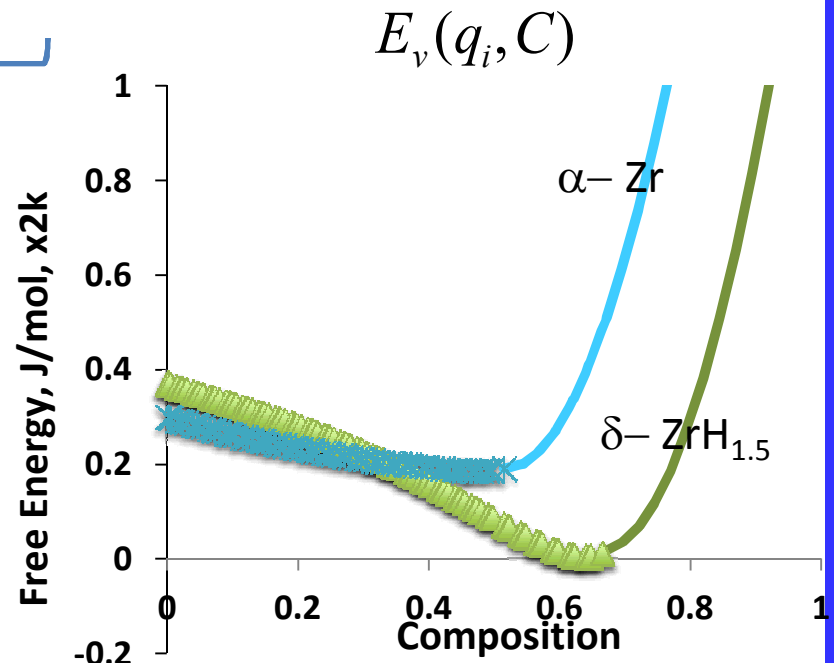
## Equation of State (Thermodynamics)

- Combines elements of Potts and phase-field models to treat microstructure and composition evolution.
- EOS is a hybrid of volume free and interfacial energies obtained from both models.

$$E_{hyb} = \underbrace{\sum_{i=1}^N \left( E_v(q_i, C) \right)}_{\text{Volume free energy}} + \underbrace{\frac{1}{2} \sum_{j=1}^n J(q_i, q_j)}_{\text{Interfacial free energy}} + E_{dC}$$

- $E_v(q_i, C)$  is obtained from Thermo Cal
- $E_{dC} = \int 2\kappa_C (\nabla C)^2 dV$

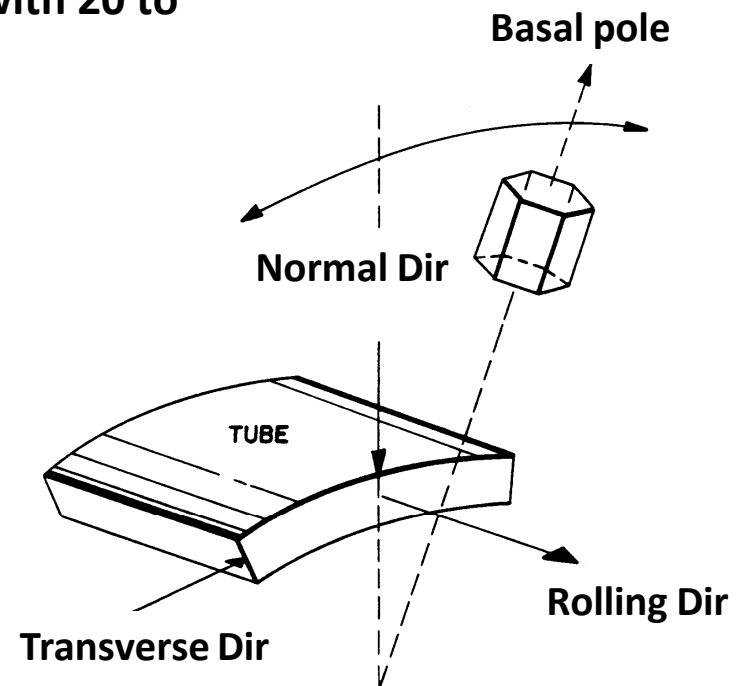
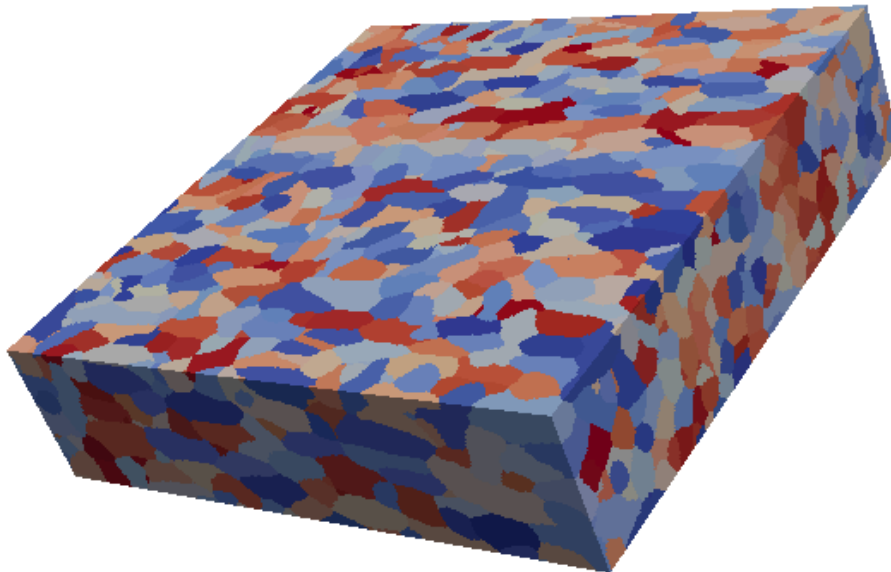
M. Glazov, INL, 2013



# Zircaloy-4 and other Zr-based claddings are known to have texture

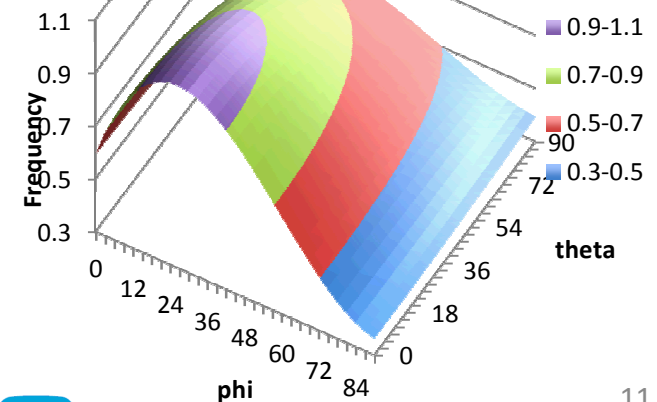
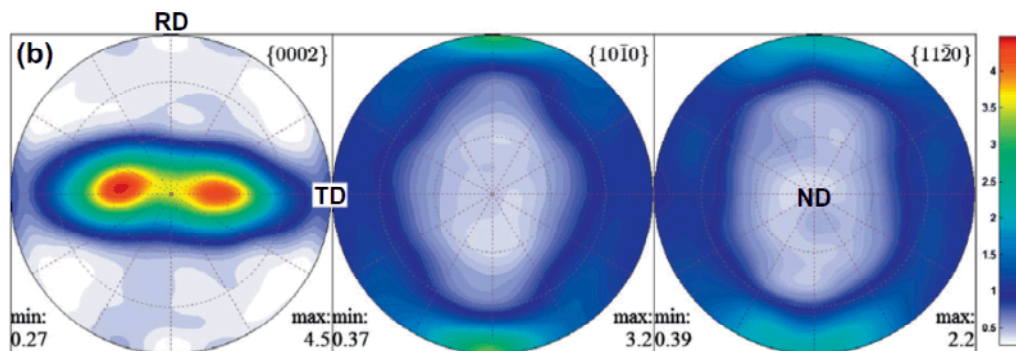
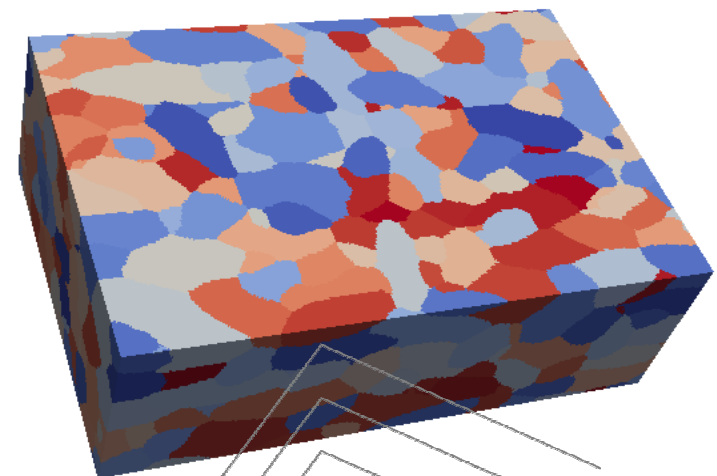
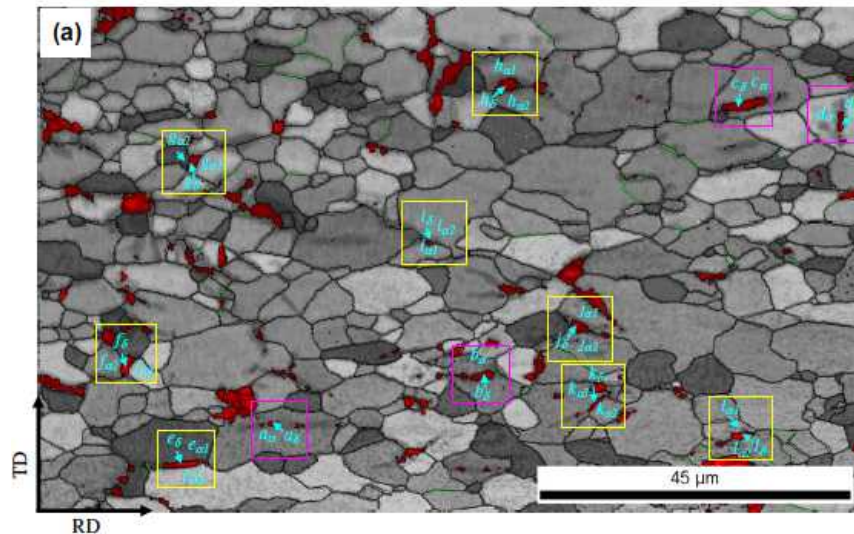
Pilgering process imparts texture

- Grain shape, elongated  $\sim 2\times$  in rolling direction
- Crystallographic, basal plane parallel to ND with 20 to  $40^\circ$  rotation around TD



## Generated a Digital Zr-4 Microstructure

**from information available in the literature on grain and crystallographic texture**



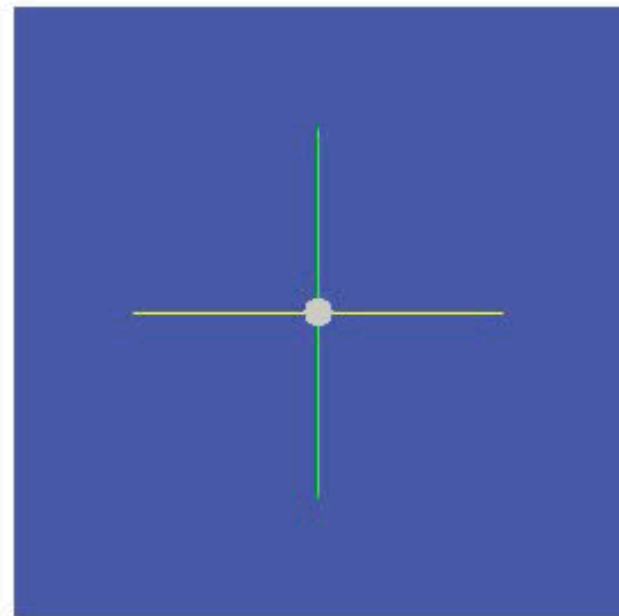
# Nucleation and growth of hydride precipitates is simulated by diffusion-controlled kinetics

## Model:

- Nucleation sites are designated in the single crystal at random locations
- Nucleation rate is constant
- Energetic bias is given to growth direction of the lathes

Precipitate nucleation and growth

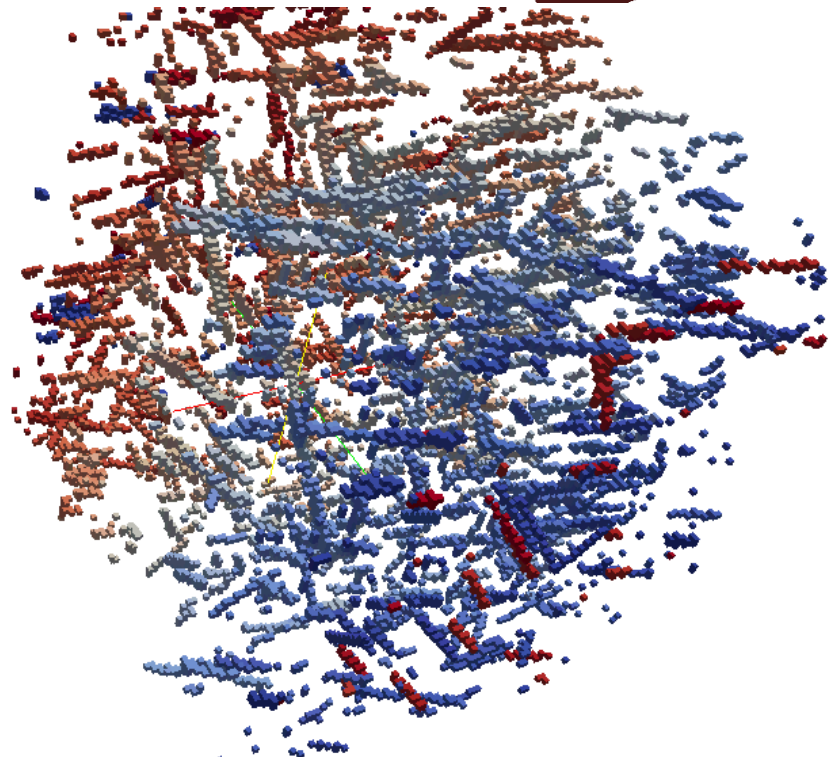
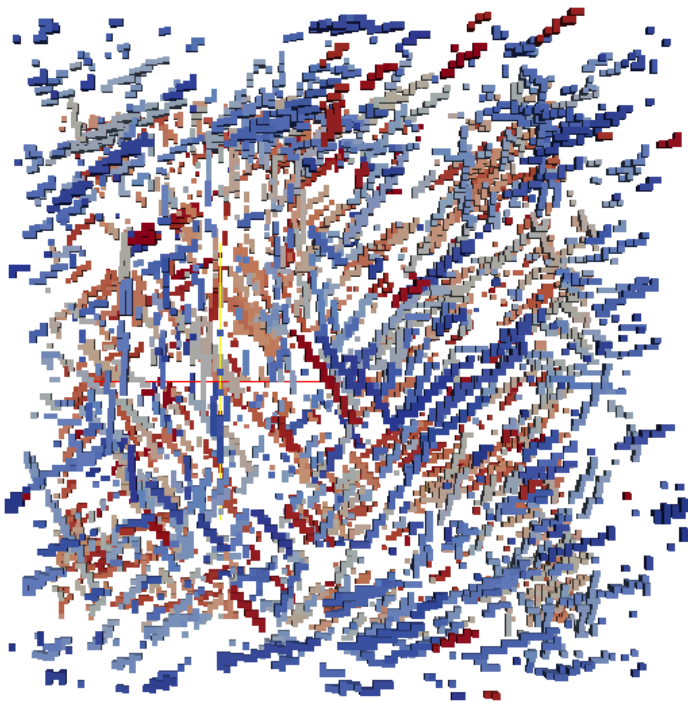
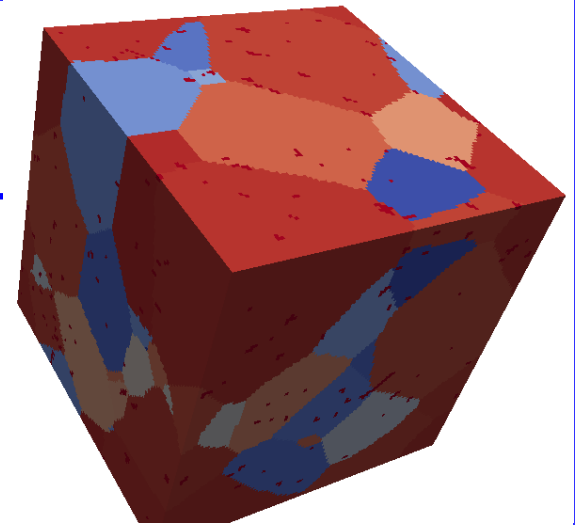
compositional evolution



# ZrH<sub>1.5</sub> Precipitation Polycrystalline Zr

## Model:

- Nucleation at random locations and nucleation rate is constant
- Energetic bias is given to growth direction of the lathes **with the orientation of the grain**

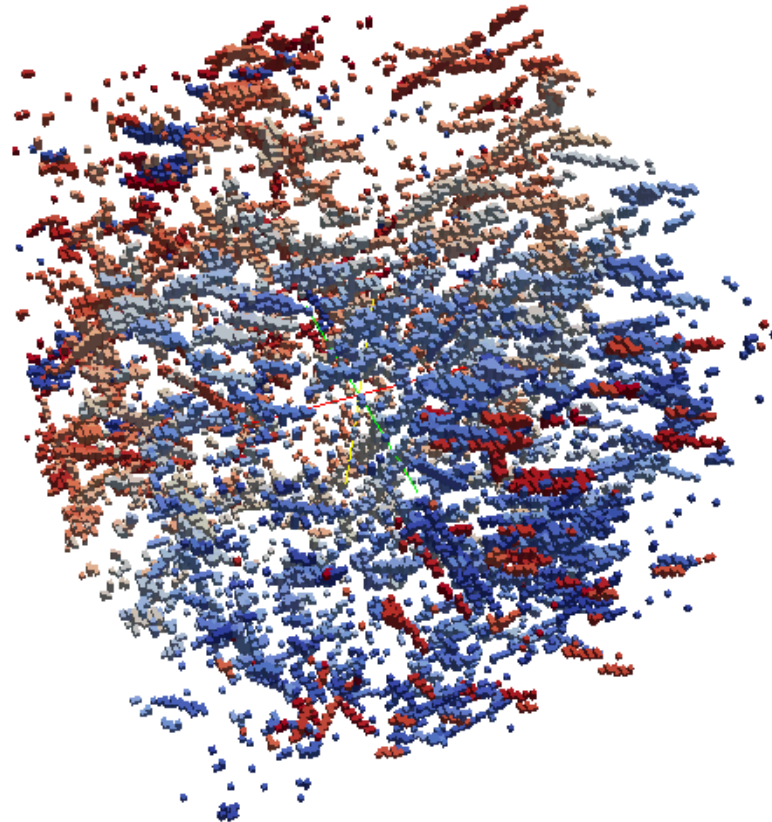
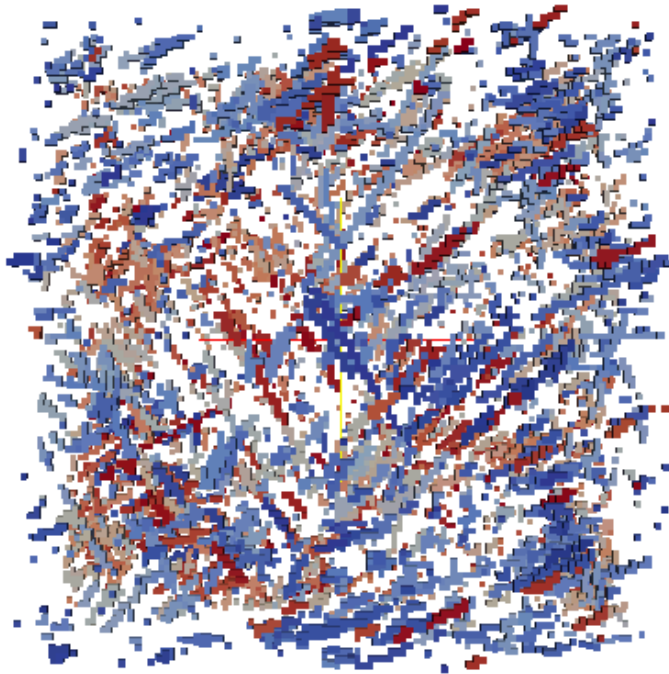
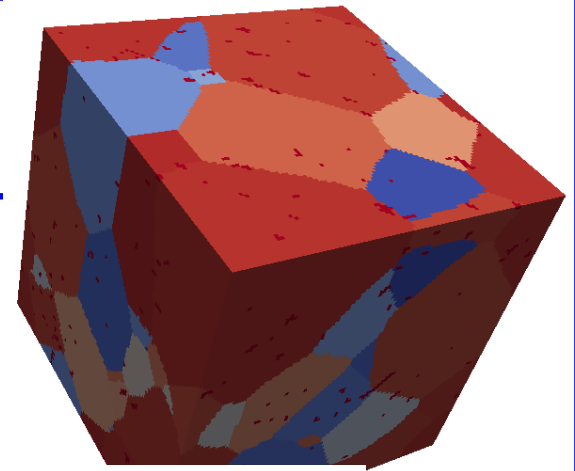




# ZrH<sub>1.5</sub> Precipitation Uniaxial Stress

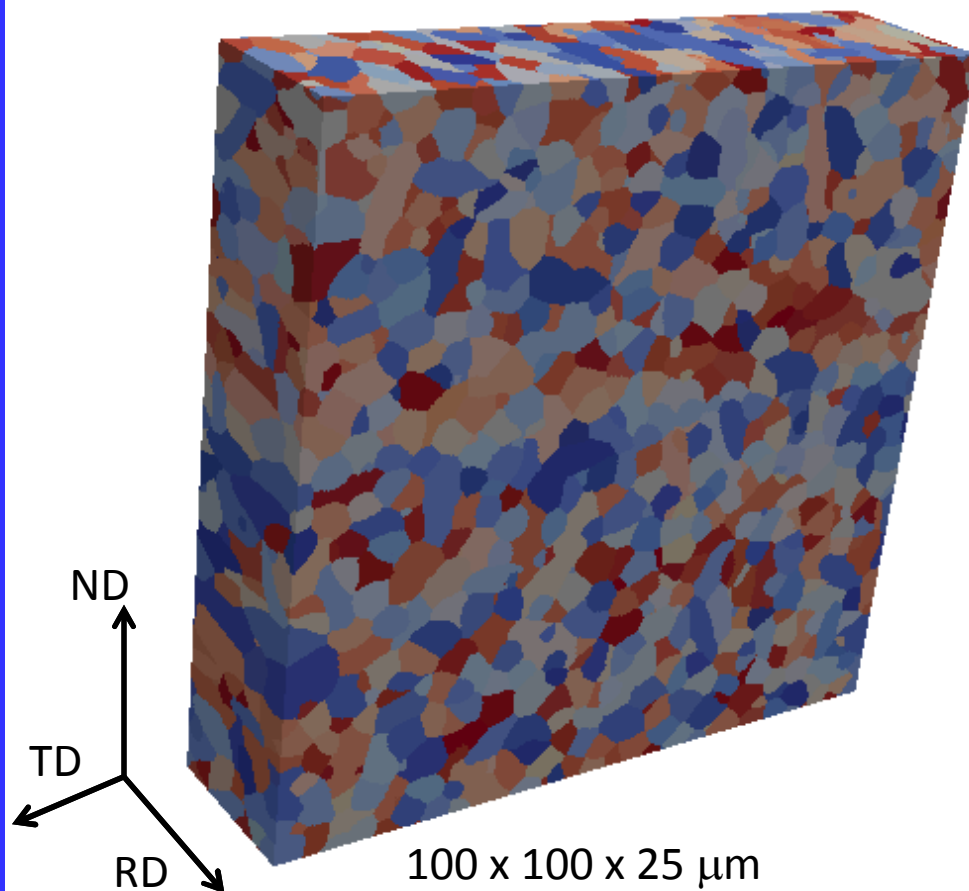
## Model:

- Same microstructure
- Energetic bias is given to growth direction of the lathes **with the orientation of the grain and stress direction.**



# Nucleation and growth of hydride precipitates

## Initial microstructure

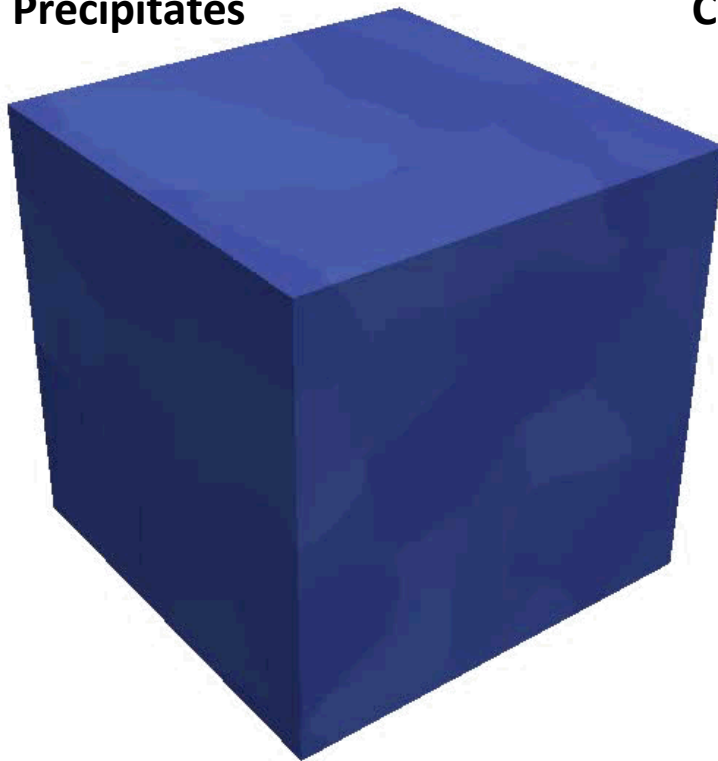


## Simulation:

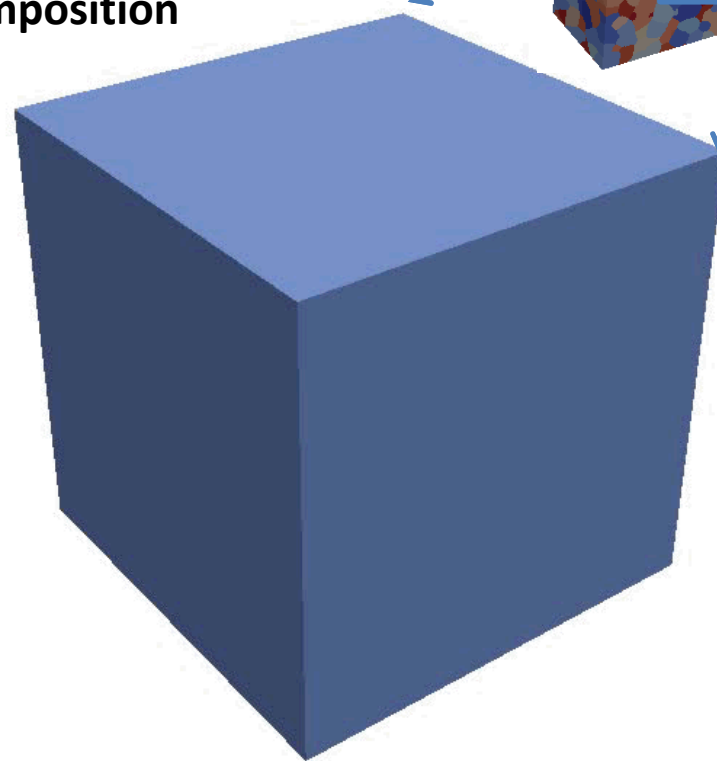
- Microstructure as shown
- Basal plane alignment with RD
- 1000 ppm H
- Zr-H thermo
- Nucleation and growth of precipitates
- Diffusion controlled kinetics

# Nucleation and growth of hydride precipitates

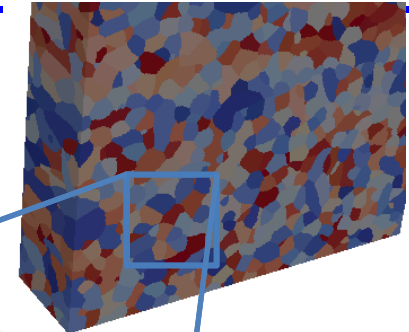
**Precipitates**



**Composition**



10 x 10 x 10  $\mu\text{m}$



Comp  
0.530905  
0.4  
0.2  
0  
-0.001834



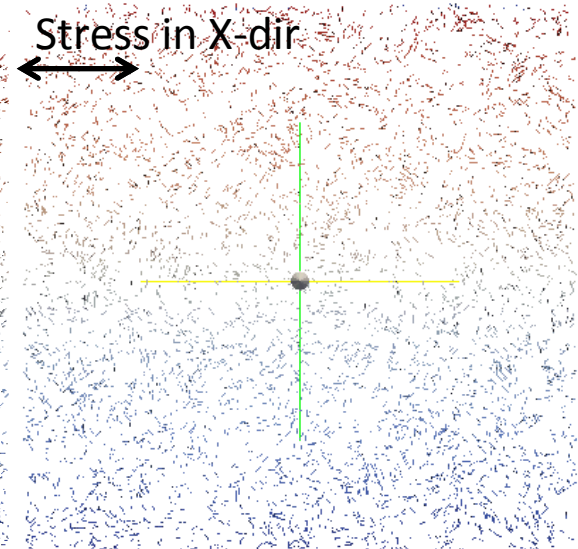
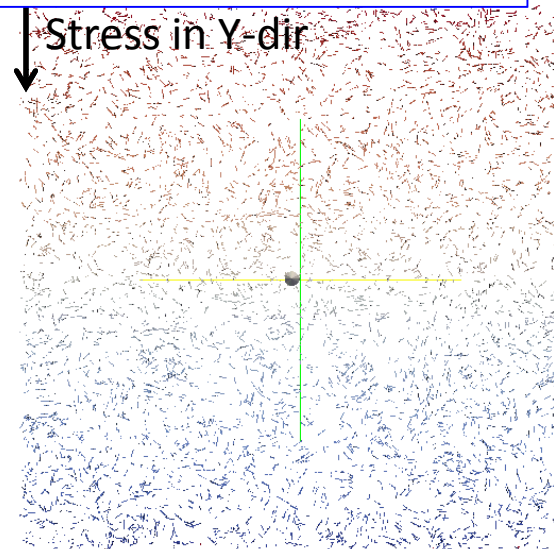
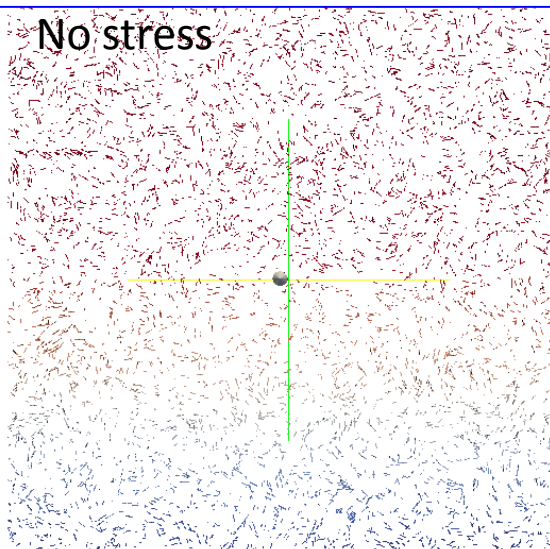
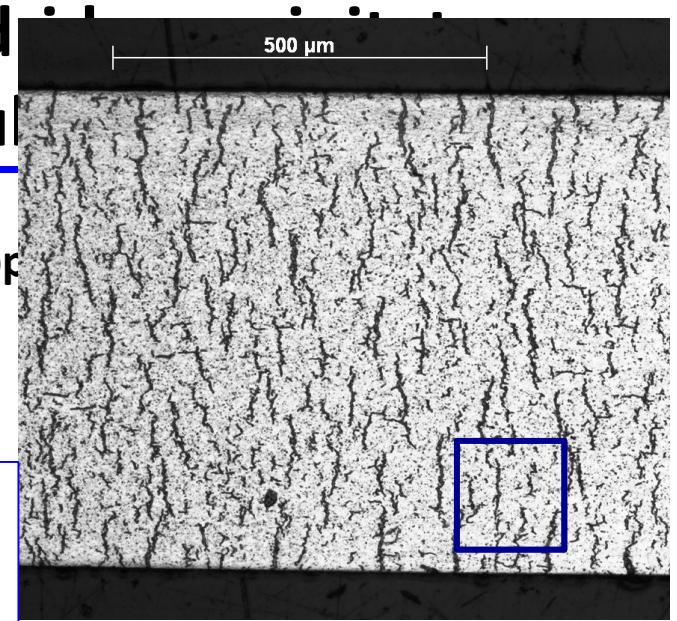
# Nucleation and growth of hydrides

## Simulation results

Precipitates align themselves perpendicular to the applied stress

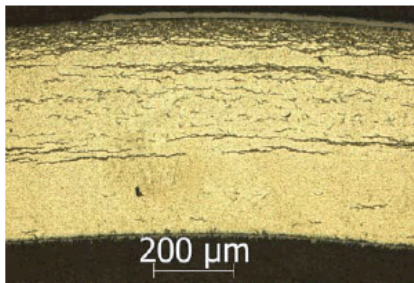
- No stress, alignment is ~random along basal plane
- Stress along Y-dir, alignment is perpendicular
- Stress along Z-dir, alignment is *less perpendicular*

However, simulated precipitates are uniformly distributed, individual precipitations do not re-align sufficiently to explain observed behavior

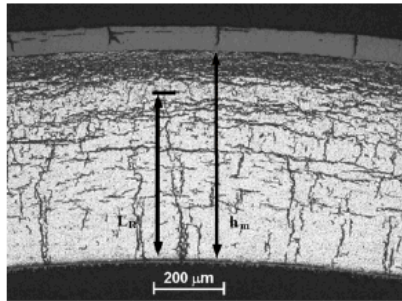


# All Zr-based claddings show long-range cooperative formation (Billone et al, ANL UFD report, 2013)

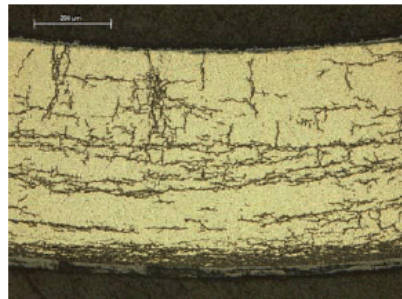
Zirlo™



(a)

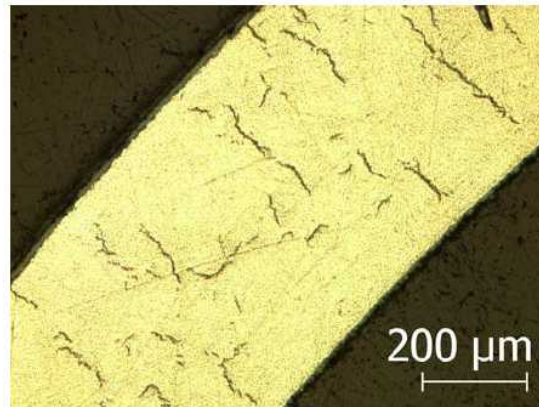


(b)

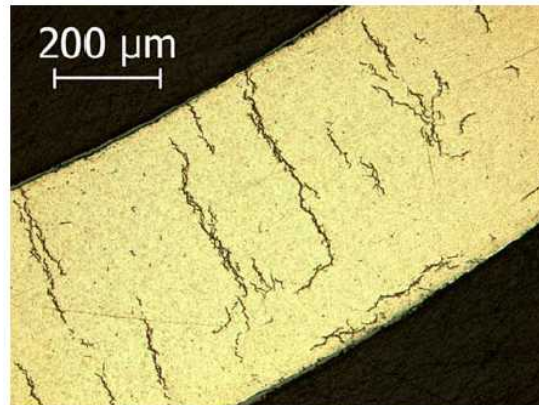


(c)

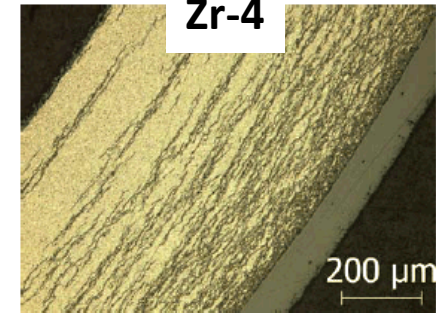
M5™



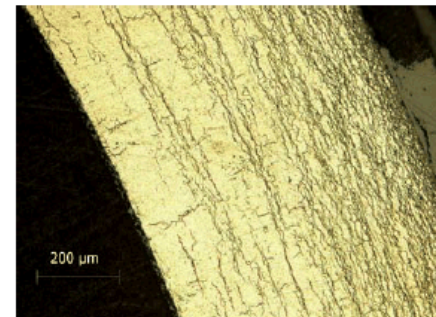
(a) 50% RHCF



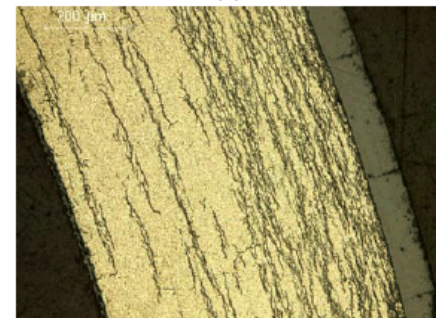
Zr-4



(a)



(b)



(c)



## Conclusions

- **Hydride precipitate re-orientation cannot be simulated by the re-orientation of individual precipitates**
  - There must be cooperative nucleation and growth of individual precipitates that leads to re-orientation as observed by optical microscopy.

