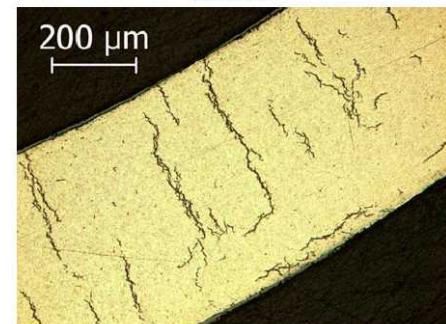
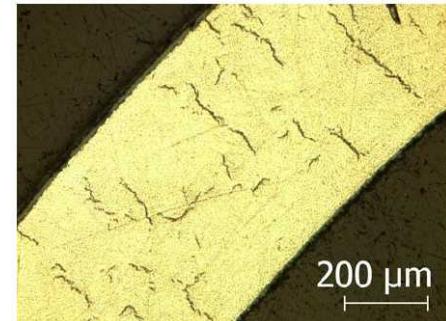


Simulation of Hydride Formation in Zr-Based Clad during Dry Storage

Veena Tikare
Sandia National Laboratories
Albuquerque, NM



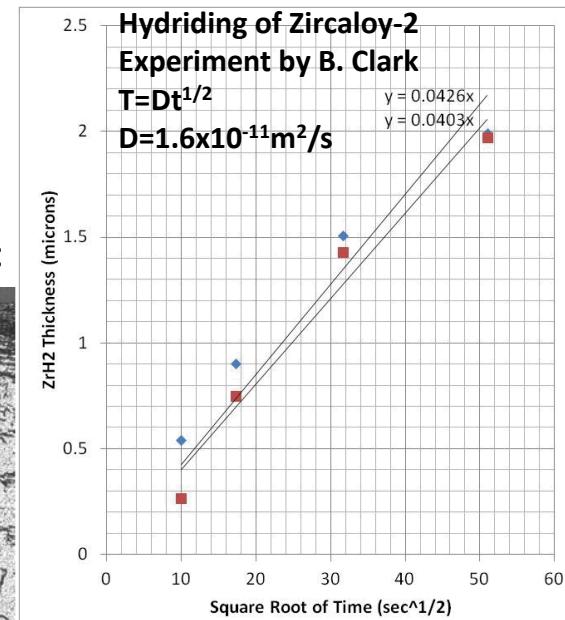
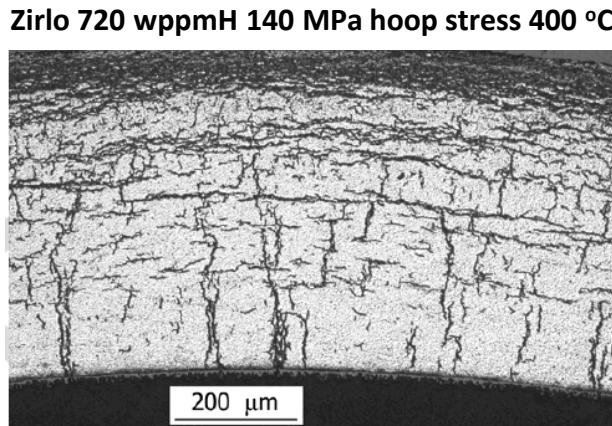
Billone et al, ANL, 2013

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ZrH₂ Formation during Dry Storage May Limit the Lifetime of Used Nuclear Fuel Cladding

Hydride formation in Zr-based cladding is known to degrade clad reliability during dry storage

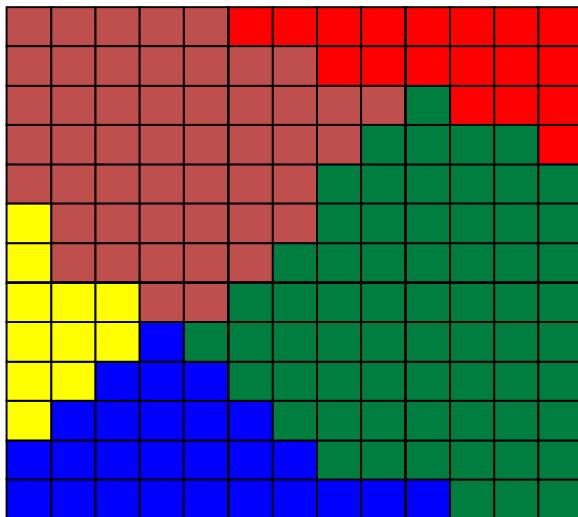
- The drying cycle dissolves the ZrH₂.
- During dry storage as the clad temperature decreases, the ZrH₂ precipitates on grain boundaries, dislocation loops and, possibly, other defects.
- ZrH₂ forms perpendicular to the tensile stress
- It morphology appears to be needle-like lathes
- B. Clark's experiments indicate the ZrH₂ growth is diffusion controlled
- Microstructure, stress, composition, H pick-up, temperature are known to Control ZrH₂ formation & morphology.



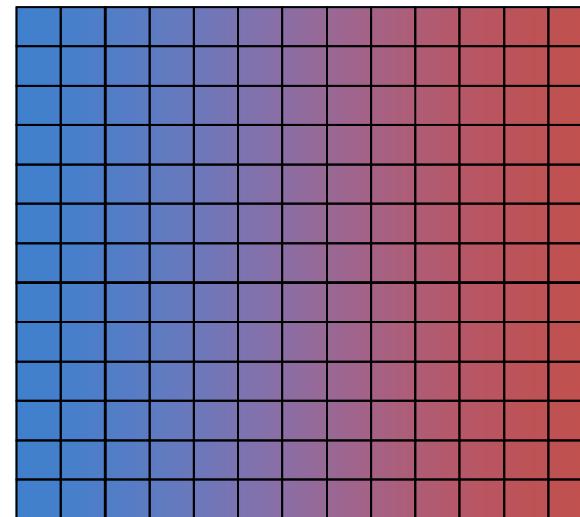
Representation of Microstructure and Composition Hybrid Model

- Potts kMC digitizes represents microstructure using spins q_i
- Phase field represents composition with field variable C_i
 - Both are on the same grid

Microstructure



Composition



Equation of State (Thermodynamics)

Hybrid Model

- EOS is a function of volume free energy and interfacial energies.

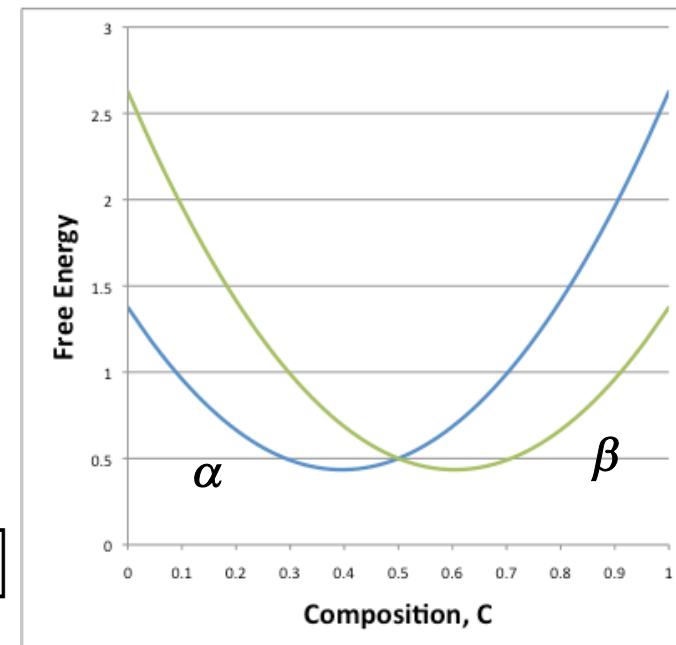
$$E_{hyb} = \sum_{i=1}^N \left(E_v(q_i, C) + \frac{1}{2} \sum_{j=1}^n J(q_i, q_j) \right) + E_{dC}$$

Volume free energy Interfacial free energy

$$E_{dC} = \int 2\kappa_C (\nabla C)^2 dV$$

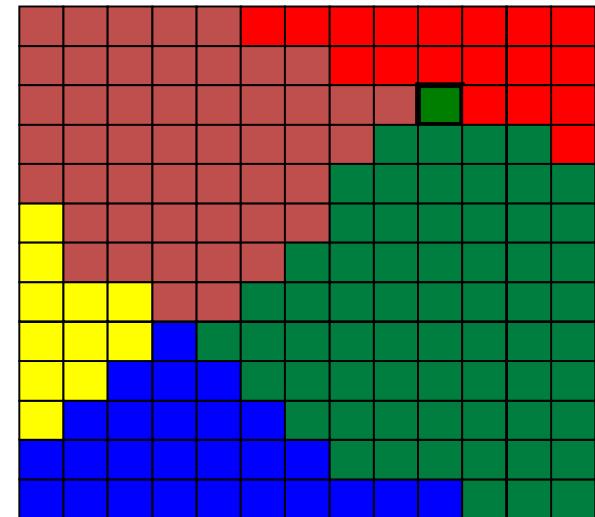
An example of E_v

$$E_v = a \left[(C - C_1)^2 + (C_2 - C)^2 \right] + b \left[(C - C_3)q_\alpha + (C_4 - C)q_\beta \right]$$



Representation of Microstructure and Composition kMC

- **Potts kMC digitizes space into discrete ‘bits’ of material**
 - An ensemble of particles populate the lattice
 - Each color can represent a membership in a phase and / or feature (i.e. grain)
 - Each color can also represent composition, but true gradients in composition would require huge simulations

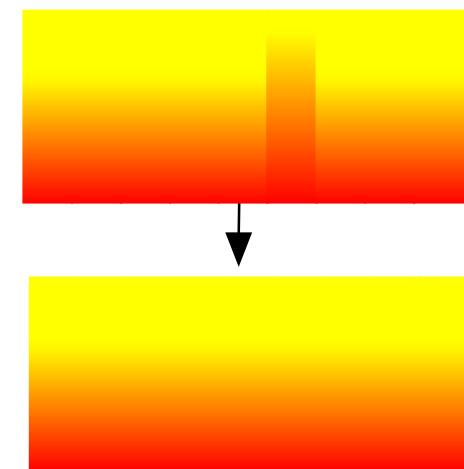
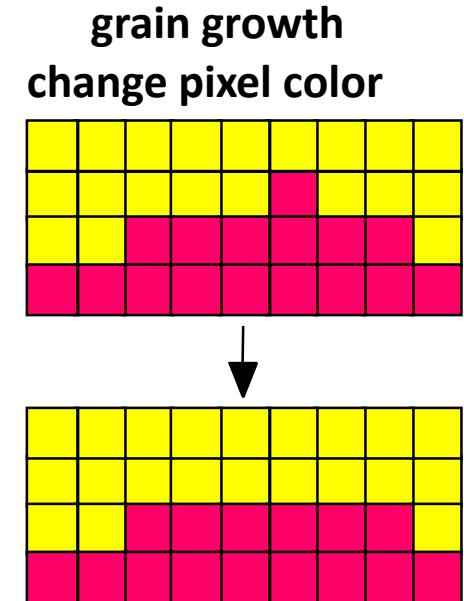


Kinetic of Evolution Hybrid Model

- Microstructure is evolved in the same manner as Potts in response to local free energy using E_{hyb}
 - Metropolis algorithm
- Composition evolved as a phase field parameter.

$$\frac{\partial C}{\partial t} = -M_c \left(\nabla^2 \frac{\partial E_v}{\partial C} - \kappa_c \nabla^4 C \right)$$

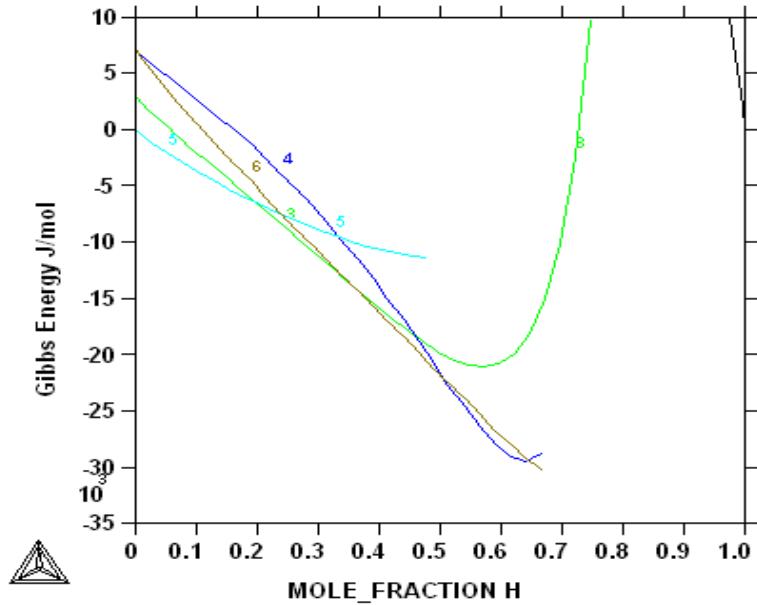
- Where E_v is from the hybrid Free Energy



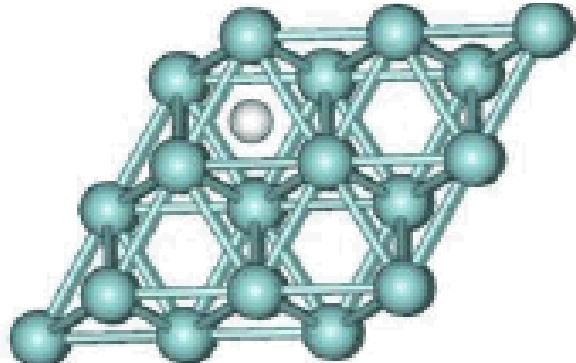
Phase Equilibrium Calculations for Zr and $ZrH_{1.5}$

M. Glazoff, INL

DATABASE:TCBIN
P=1E5, N=1, T=573;

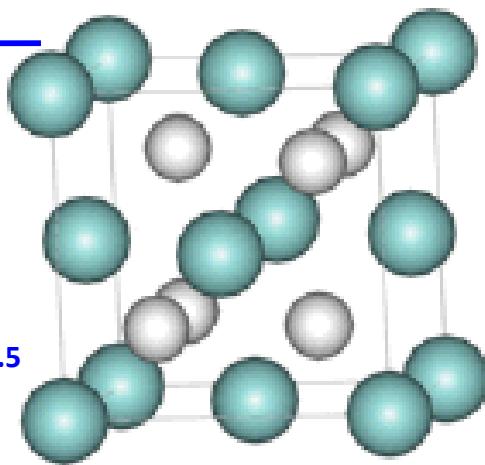


HCP Zr

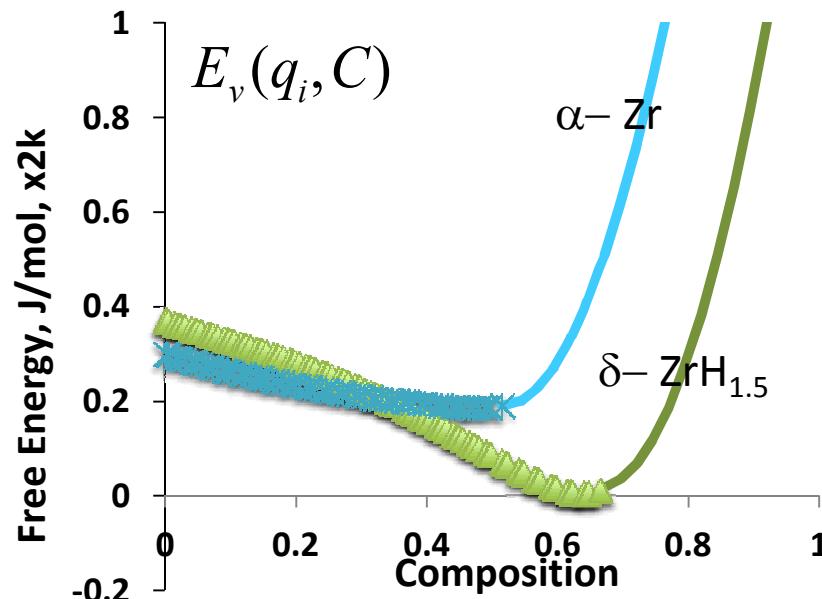


Jan, 2014

3:X(H),GMR(BCC_A2)
4:X(H),GMR(C1_FCC)
5:X(H),GMR(HCP_ZR)
6:X(H),GMR(ZRH2_EPSILON)



FCC $ZrH_{1.5}$



Sandia National Laboratories

Morphology of ZrH_{1.5} Precipitates

ZrH_{1.5} Precipitates

- Intragranular
- needle-like lathes
- Cubic (FCC)
- specific crystallographic orientation with HCP Zr
- Growth is by nucleation and diffusion-controlled growth



Hydride Precipitates orient on $(111)_\delta // (0001)_\alpha$; $[1\bar{1}0]_\delta // [11\bar{2}0]_\alpha$
 $(111)_\delta // (10\bar{1}0)_\alpha$; $[1\bar{1}0]_\delta // [11\bar{2}0]_\alpha$

Bradbrook et al, JNM 1972

Hybrid Potts-Phase Field Model

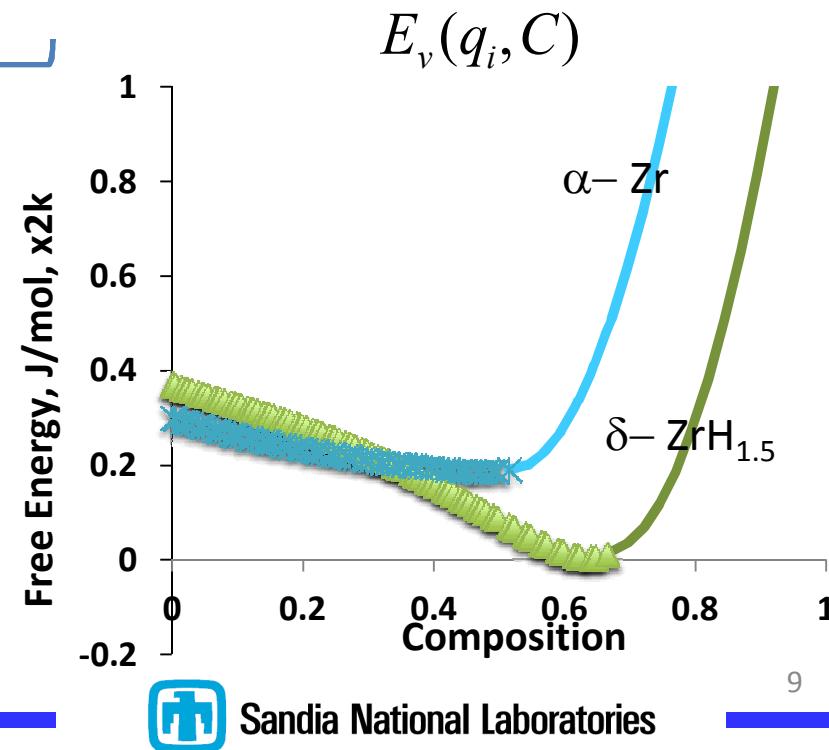
Equation of State (Thermodynamics)

- Combines elements of Potts and phase-field models to treat microstructure and composition evolution.
- EOS is a hybrid of volume free and interfacial energies obtained from both models.

$$E_{hyb} = \sum_{i=1}^N \left(\underbrace{E_v(q_i, C)}_{\text{Volume free energy}} + \underbrace{\frac{1}{2} \sum_{j=1}^n J(q_i, q_j)}_{\text{Interfacial free energy}} \right) + E_{dC}$$

- $E_v(q_i, C)$ is obtained from Thermo Cal
- $E_{dC} = \int 2\kappa_C (\nabla C)^2 dV$

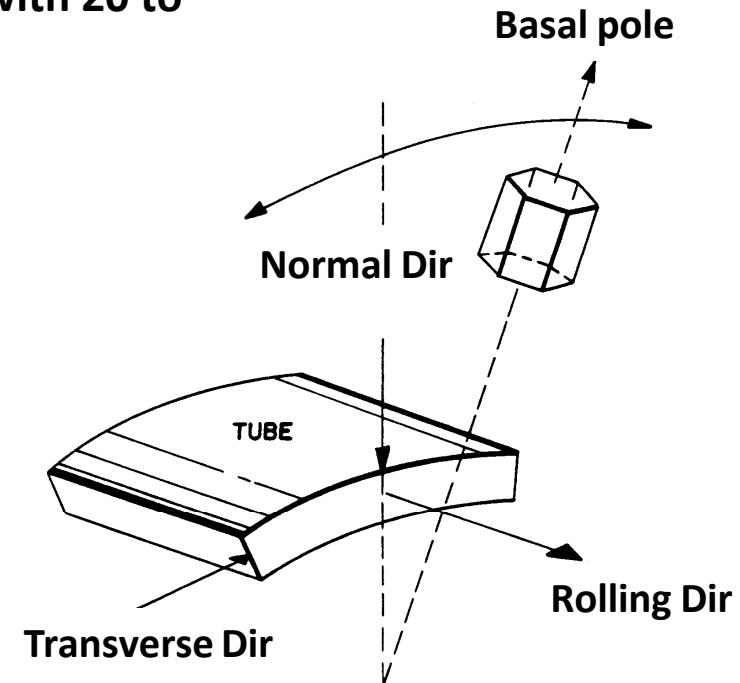
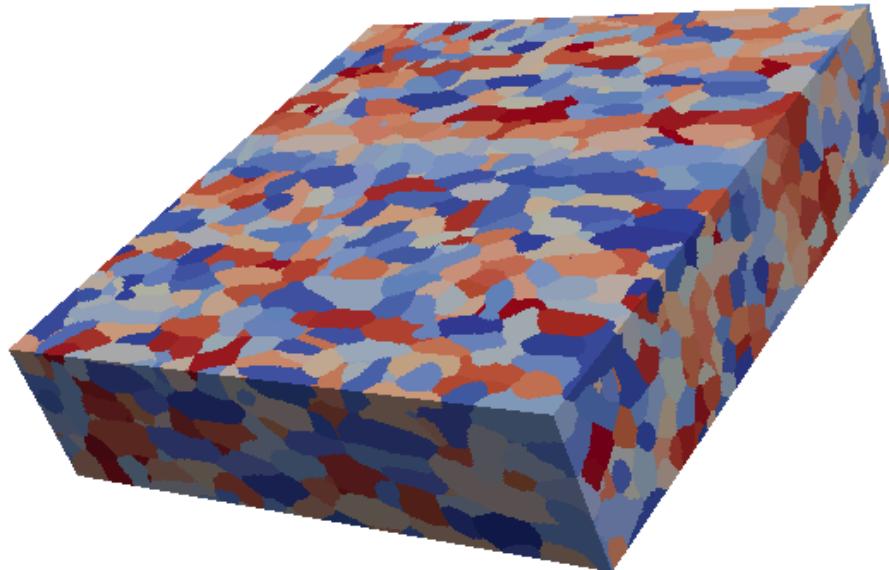
M. Glazov, INL, 2013



Zircaloy-4 and other Zr-based claddings are known to have texture

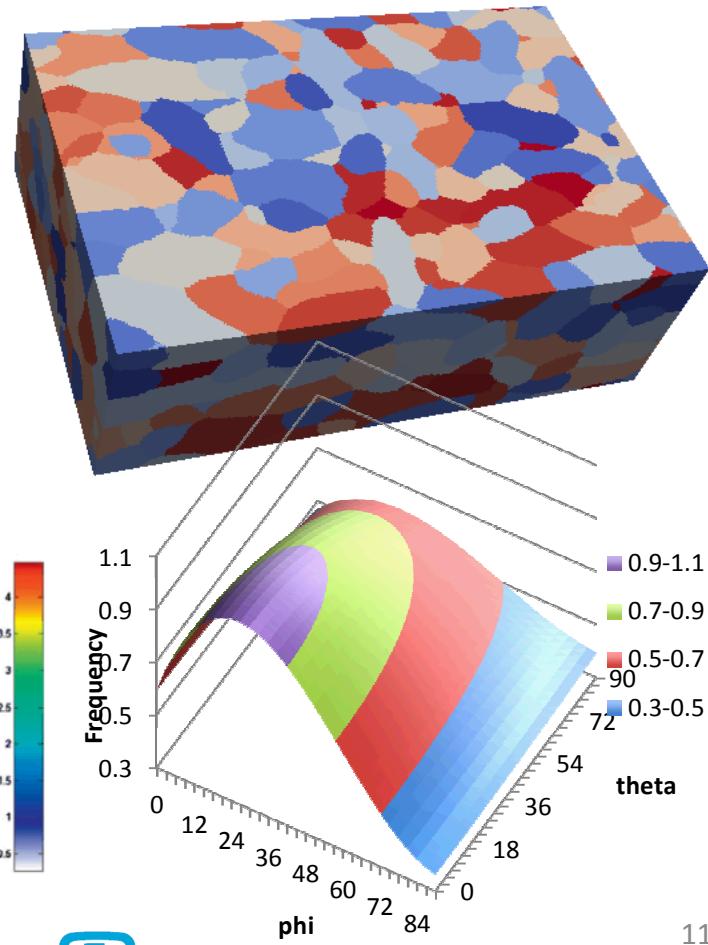
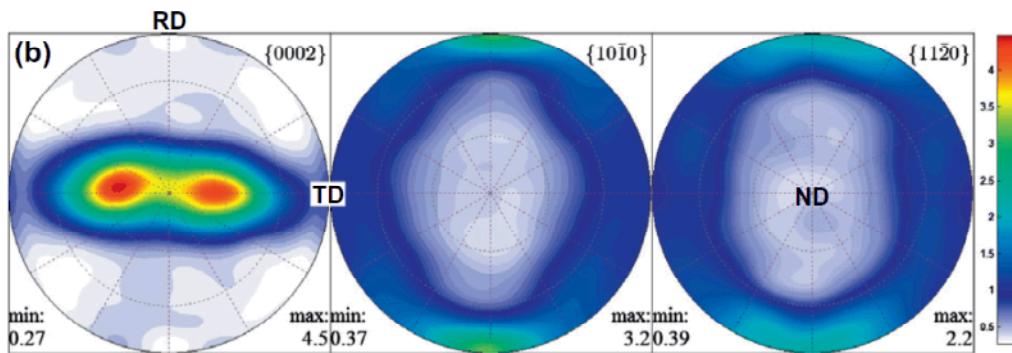
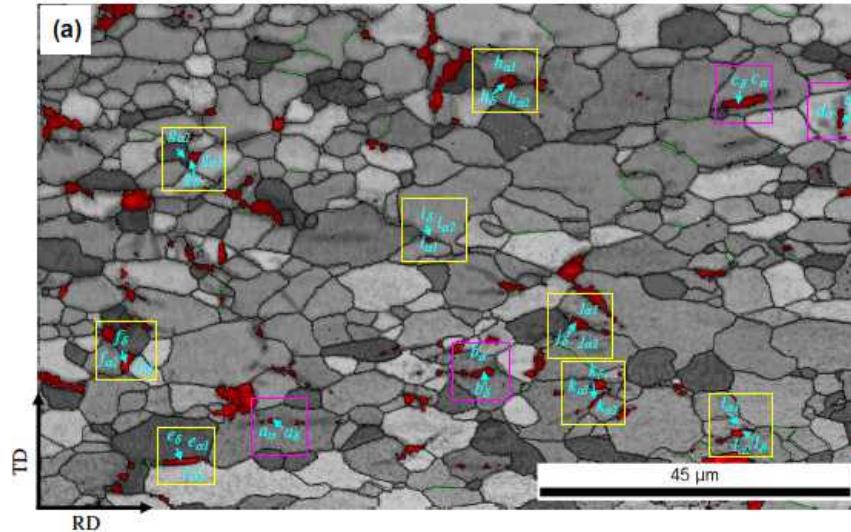
Pilgering process imparts texture

- Grain shape, elongated $\sim 2x$ in rolling direction
- Crystallographic, basal plane parallel to ND with 20 to 40° rotation around TD



Generated a Digital Zr-4 Microstructure

from information available in the literature on grain and crystallographic texture



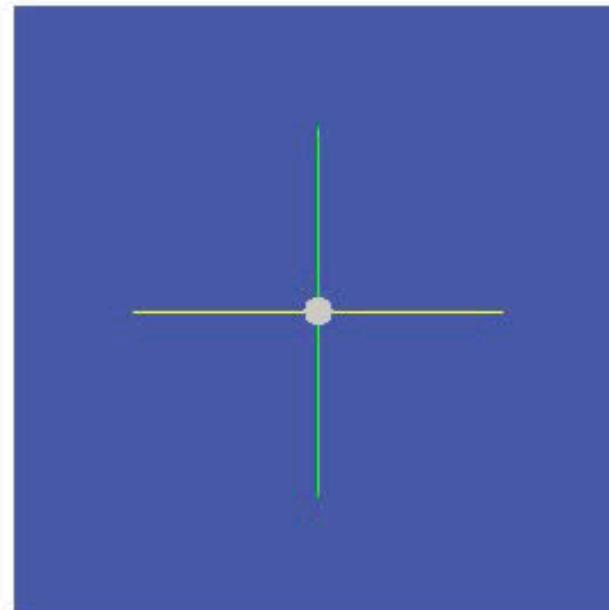
Nucleation and growth of hydride precipitates is simulated by diffusion-controlled kinetics

Model:

- Nucleation sites are designated in the single crystal at random locations
- Nucleation rate is constant
- Energetic bias is given to growth direction of the lathes

Precipitate nucleation and growth

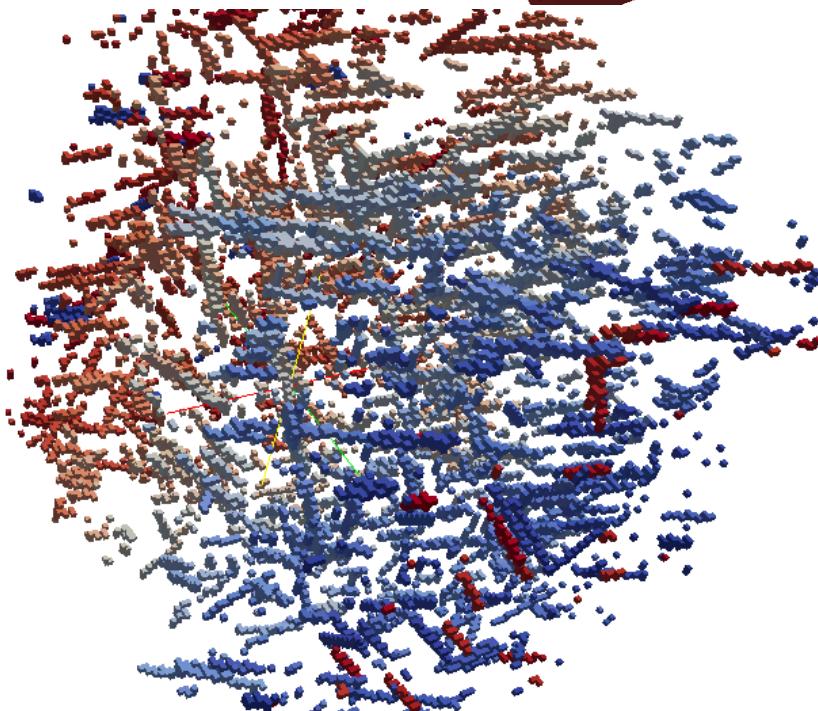
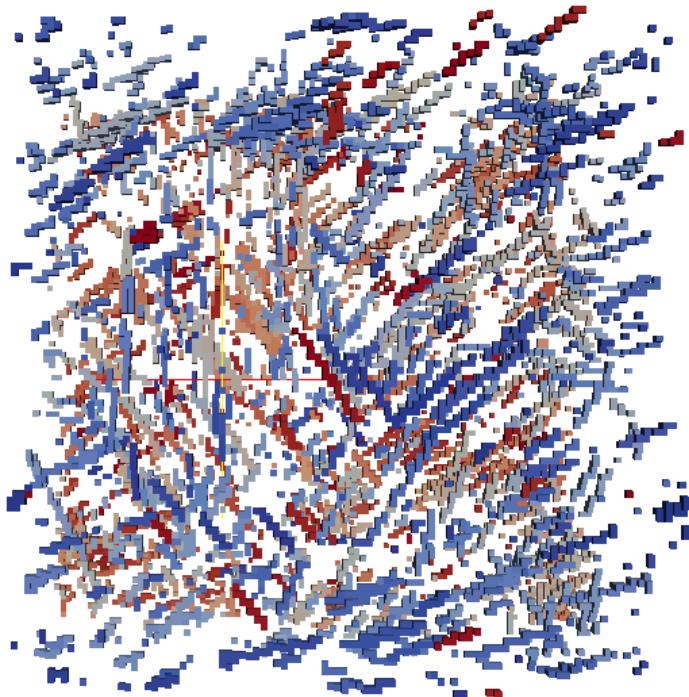
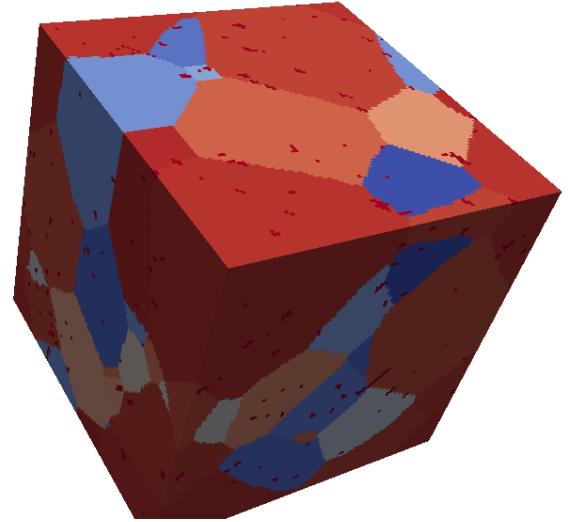
compositional evolution



ZrH_{1.5} Precipitation Polycrystalline Zr

Model:

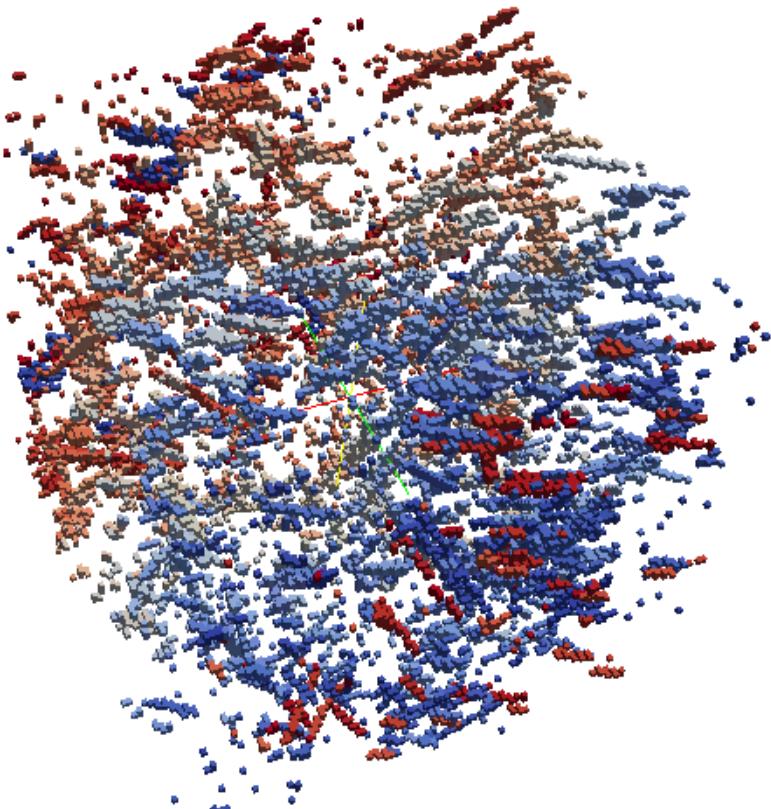
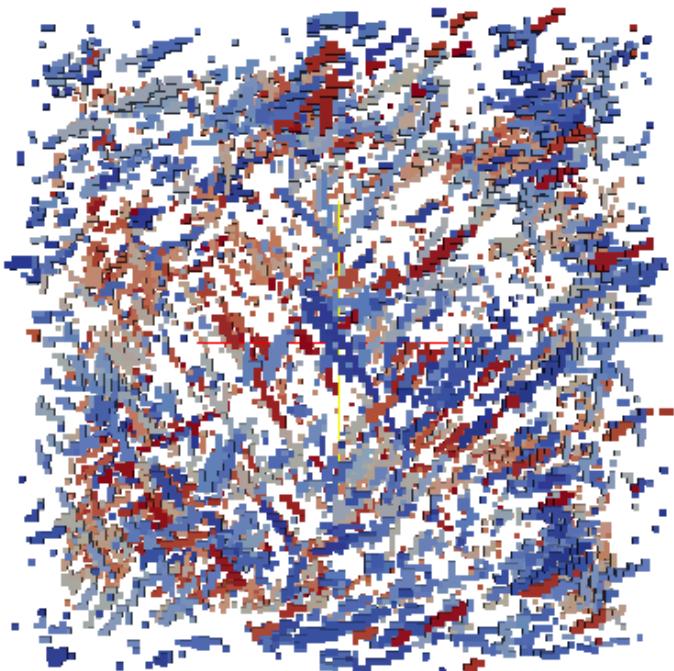
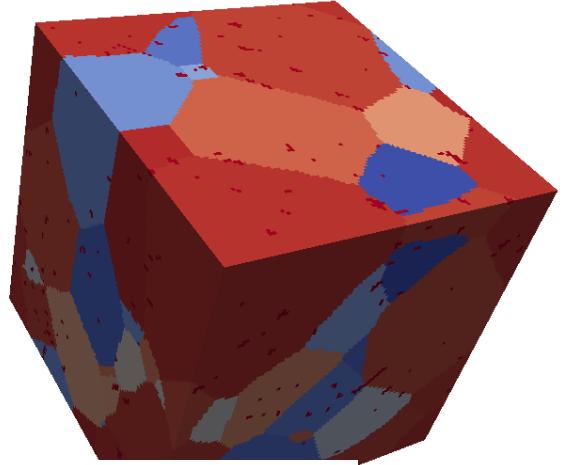
- Nucleation at random locations and nucleation rate is constant
- Energetic bias is given to growth direction of the lathes **with the orientation of the grain**



ZrH_{1.5} Precipitation Uniaxial Stress

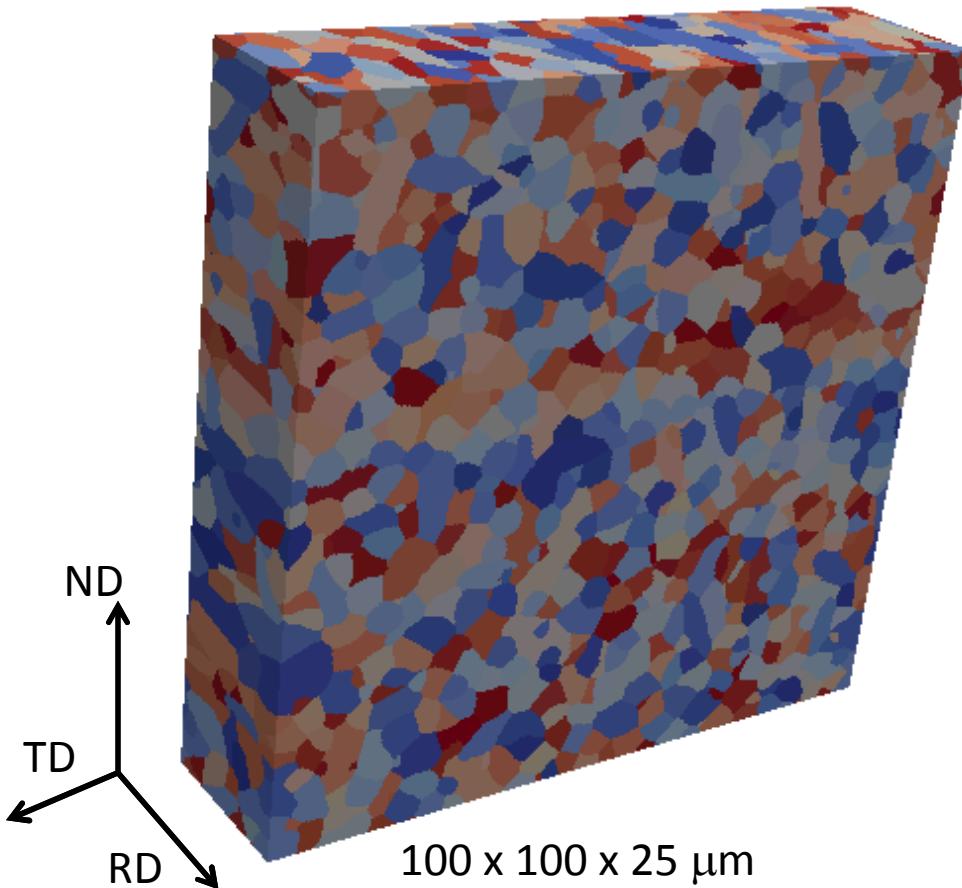
Model:

- Same microstructure
- Energetic bias is given to growth direction of the lathes **with the orientation of the grain and stress direction.**



Nucleation and growth of hydride precipitates

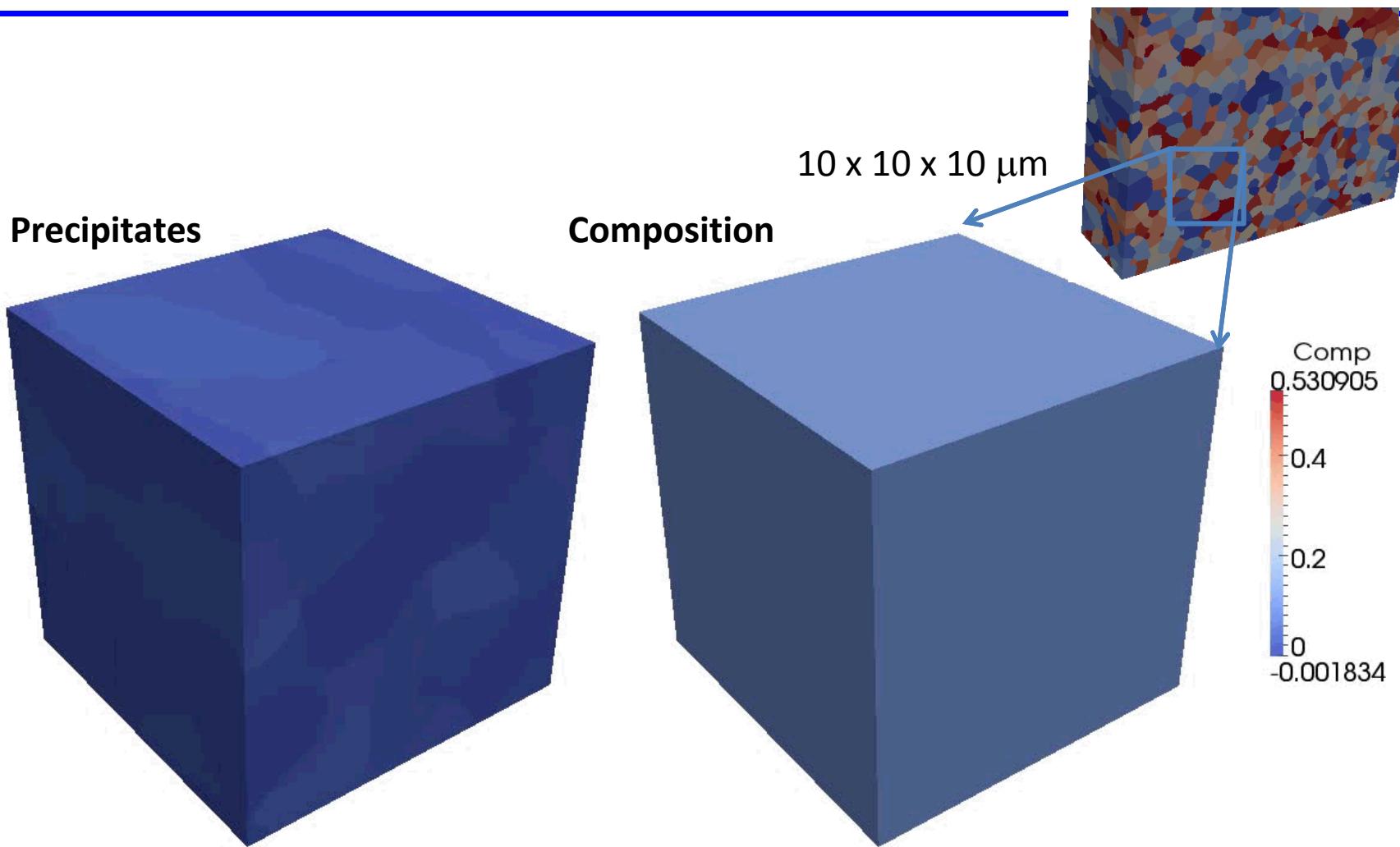
Initial microstructure



Simulation:

- Microstructure as shown
- Basal plane alignment with RD
- 1000 ppm H
- Zr-H thermo
- Nucleation and growth of precipitates
- Diffusion controlled kinetics

Nucleation and growth of hydride precipitates



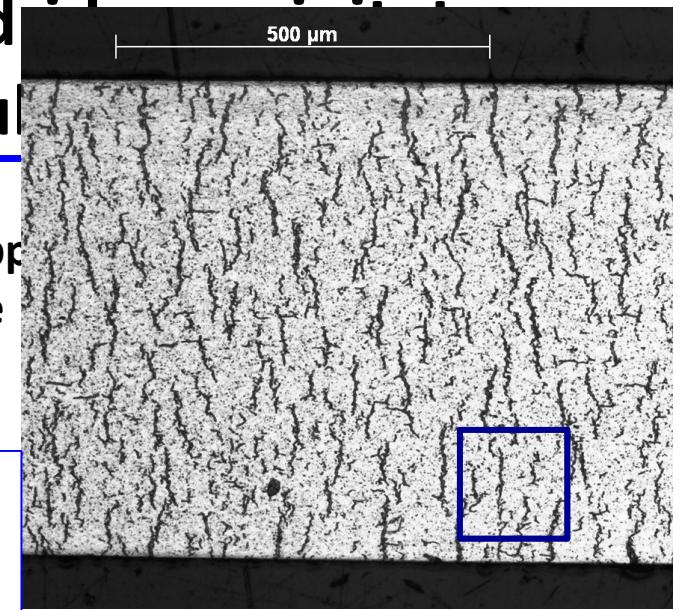
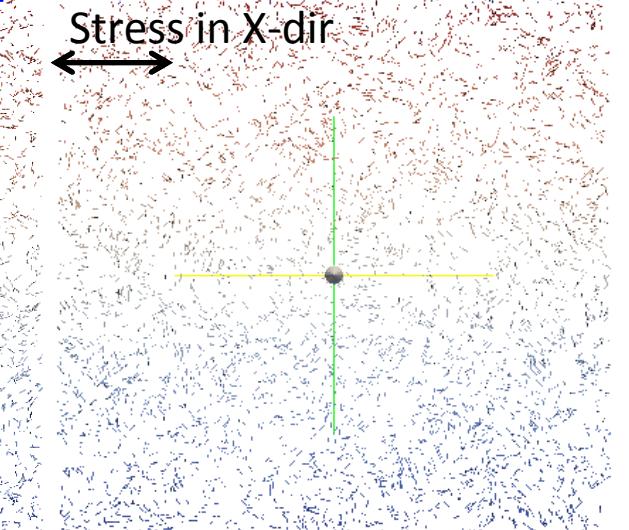
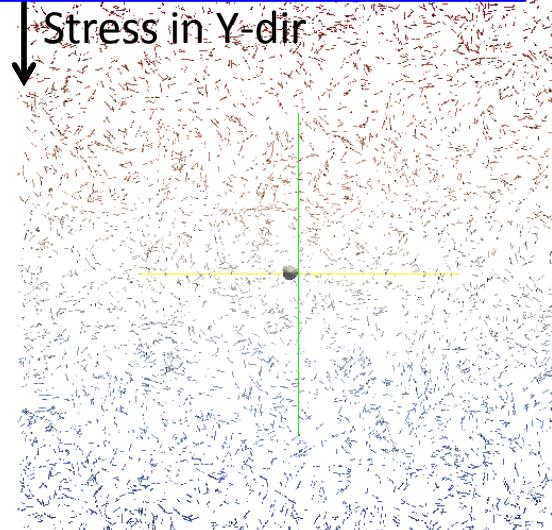
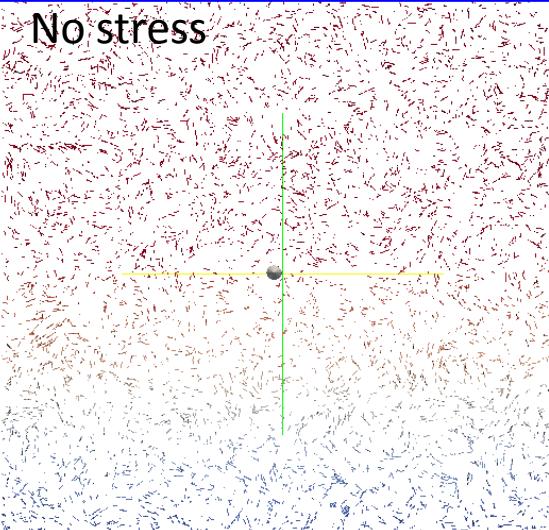
Nucleation and growth of hydrides

Simulation results

Precipitates align themselves perpendicular to the applied stress

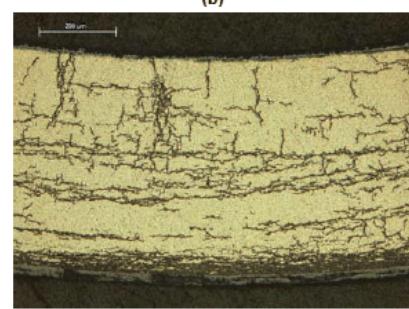
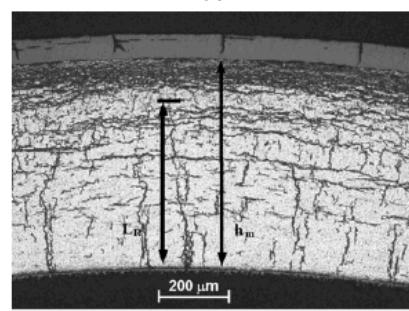
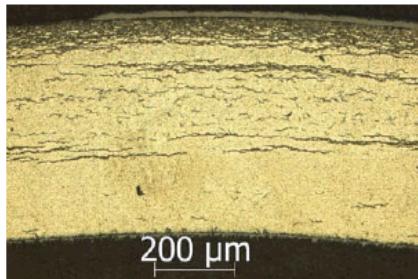
- No stress, alignment is \sim random along basal plane
- Stress along Y-dir, alignment is perpendicular
- Stress along Z-dir, alignment is *less* perpendicular

However, simulated precipitates are uniformly distributed, individual precipitations do not re-align sufficiently to explain observed behavior

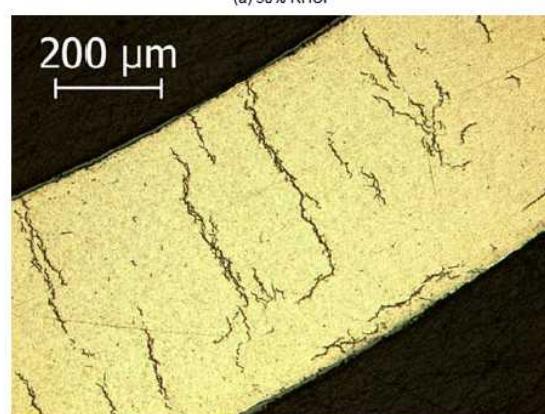
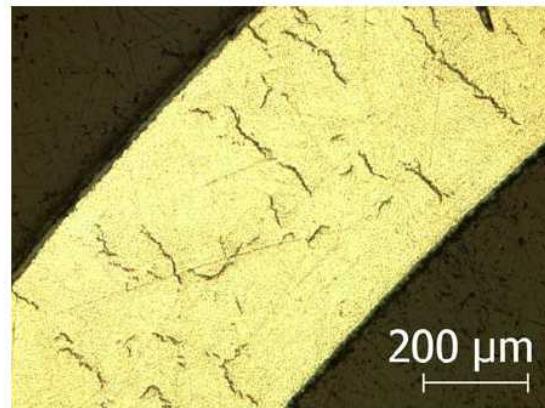


All Zr-based claddings show long-range cooperative formation (Billone et al, ANL UFD report, 2013)

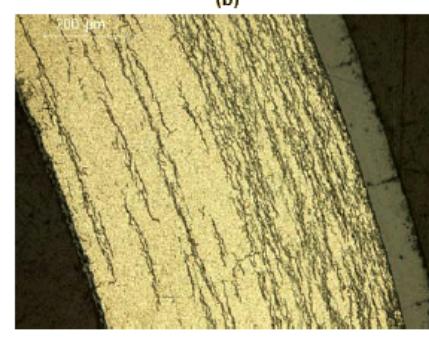
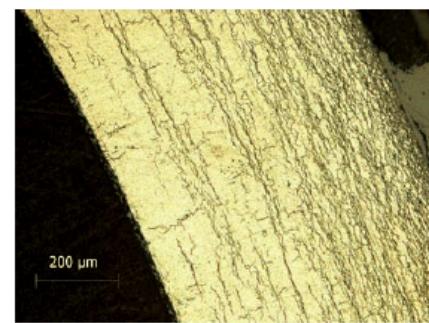
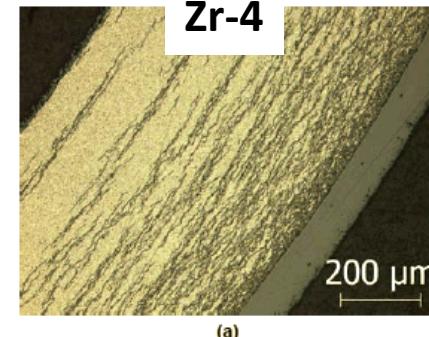
Zirlo™



M5™



Zr-4



Conclusions

- **Hydride precipitate re-orientation cannot be simulated by the re-orientation of individual precipitates**
 - There must be cooperative nucleation and growth of individual precipitates that leads to re-orientation as observed by optical microscopy.

