



# Ionic Aggregation and Dynamics in Ionomers: Insights from Molecular Simulation

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GRC on Colloidal, Macromolecular &  
Polyelectrolyte Solutions

February 20, 2014



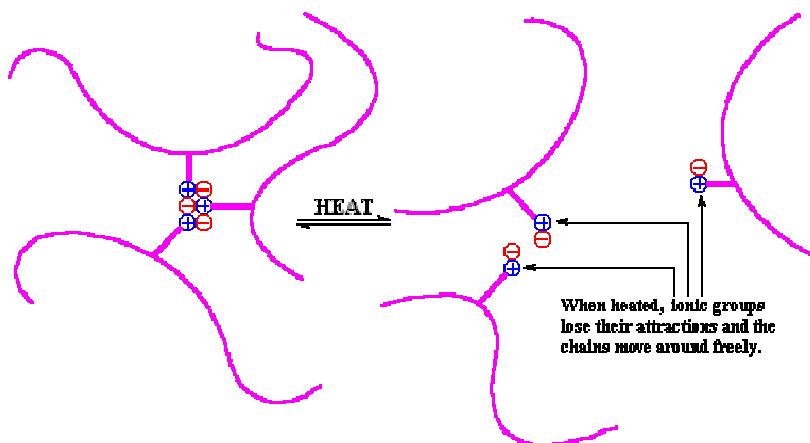
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# Ionomers

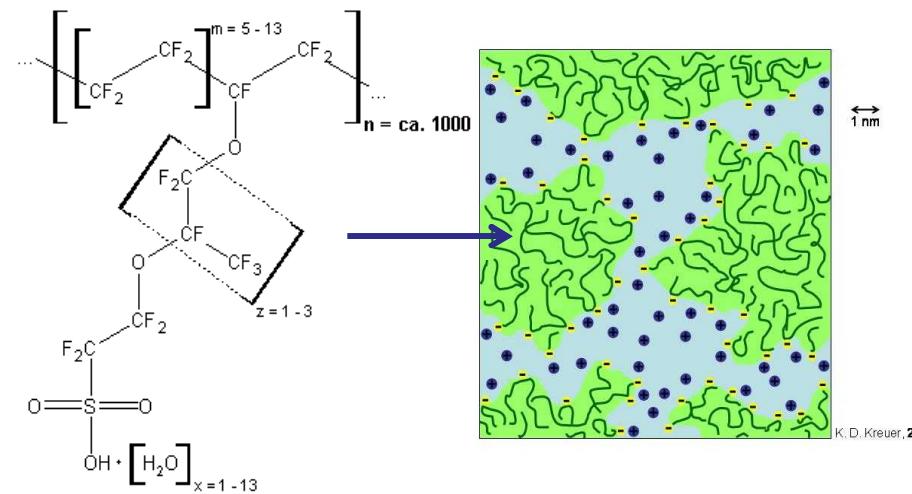
## thermoplastic elastomers



- low T: ionic aggregates behave like crosslinks
  - material is elastic
  - high strength
- high T: ionic aggregates break up
  - material flows (is a liquid)

## ion-selective membranes typically in water

- water purification
- fuel cells



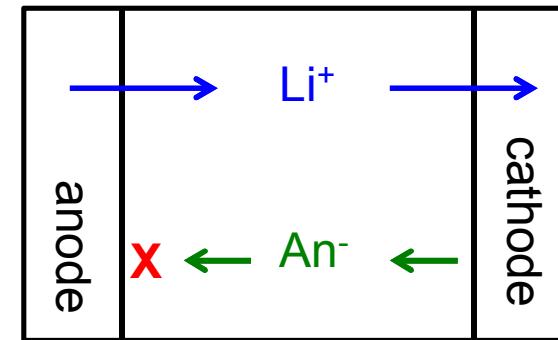
# Possible Application: Batteries

Issues with current electrolytes in Li-ion batteries:

- organic solvents
- PEO + lithium salts + solvent
  - need containment
  - flammable!



- solvent free PEO + salt
- conductivity dominated by anions
- salt concentration at electrodes
- extra heating



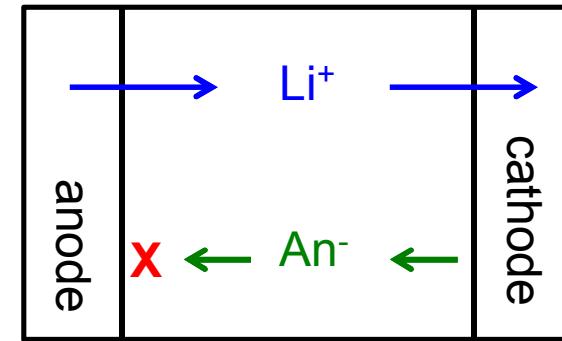
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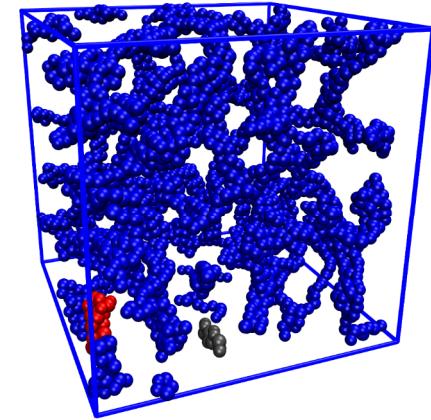
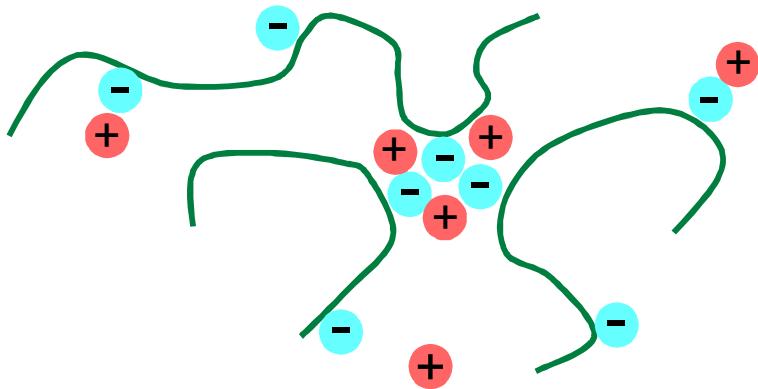


ionomers as next generation electrolytes?

- safer: no solvent
- serve as electrolyte & separator
- less packaging
- improved electrochemical stability
- higher efficiency: single ion conductors

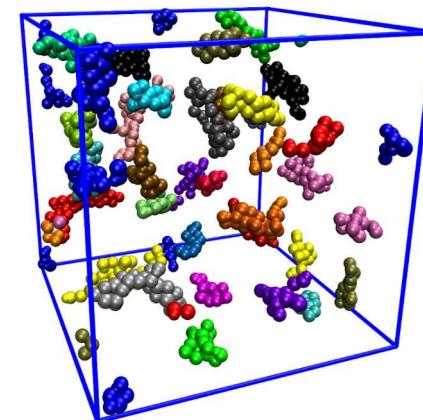
# Ionomers: Polymers + Ions

often form ionic aggregates



- electrostatic forces favor aggregates
- polymer entropy limits size

do aggregates lead to low conductivity?



# Current Ionomer Conductivities



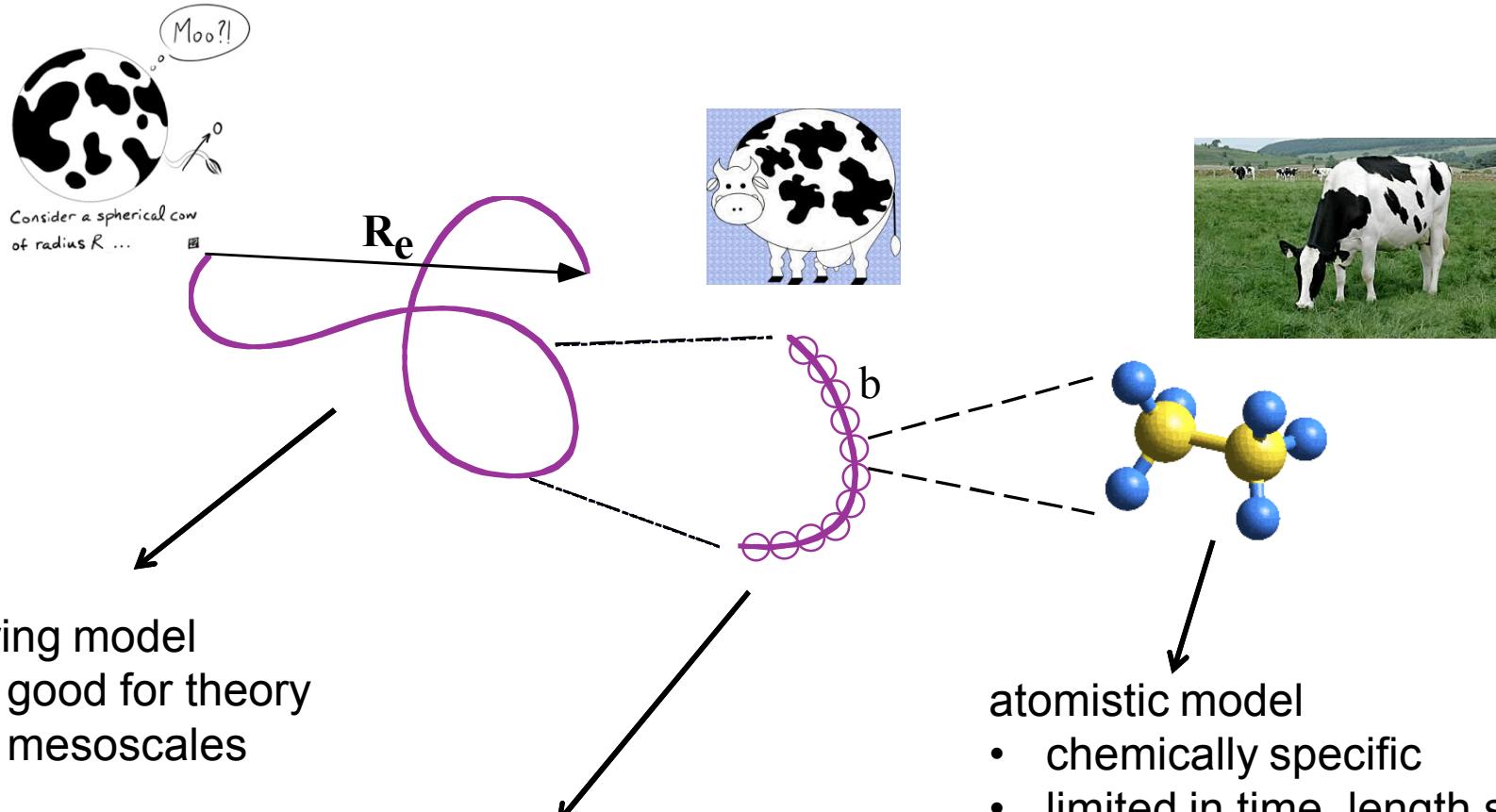
- conductivity too low
  - needed for Li-ion batteries:  $\geq 10^{-4}$  S/cm at room temp.
  - Li salt + solvent:  $\approx 10^{-2}$  S/cm
  - gel polyelectrolytes: 1-3  $10^{-3}$  S/cm
  - ionomers: often  $< 10^{-5}$  S/cm
- why?
  - few mobile ions (ion pairs instead)
  - often get ionic aggregates

Need for electrochemical apps:

- relation between molecular architecture & morphology
- effects of morphology on ion transport
- understanding of ion transport mechanisms

Simulations can help!

# Modeling (Simulating) Polymers



## string model

- good for theory
- mesoscales

## coarse-grained model

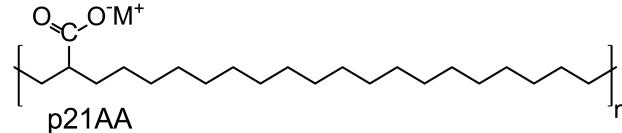
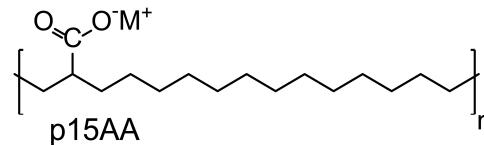
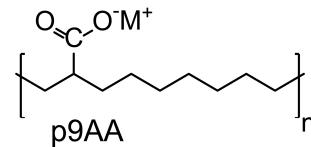
- used a lot in simulations
- intermediate length, time scales

## atomistic model

- chemically specific
- limited in time, length scales

# Precise Ionomers

# Acyclic Diene Metathesis (ADMET) Precise Copolymer



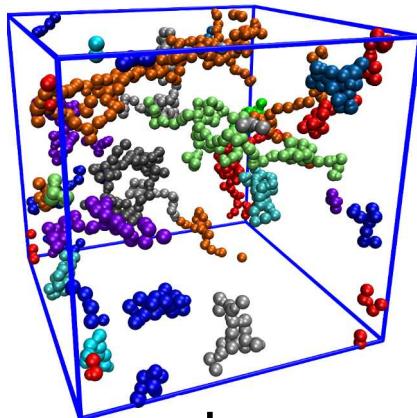
## precise polymers:

- acid group every 9, 15, 21 carbons
- swap H for  $Zn^{2+}$ ,  $Li^+$ ,  $Na^+$ ,  $Cs^+$
- nomenclature: pxAA-y%M

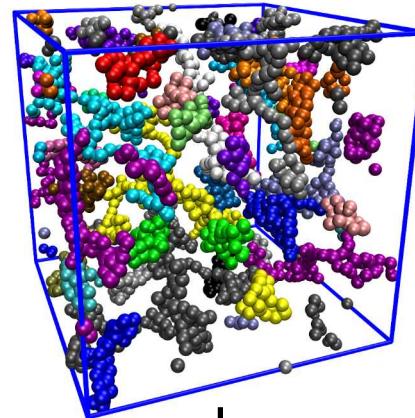
# Morphology: Li-neutralized pAA

coloring by cluster

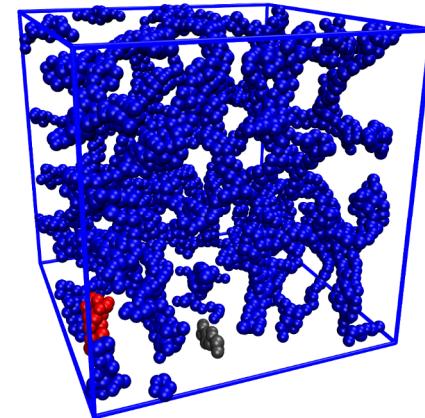
p9AA-10%Li



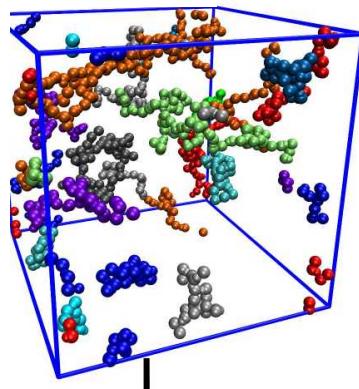
p9AA-43%Li



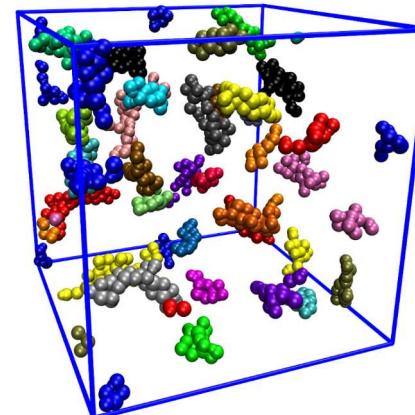
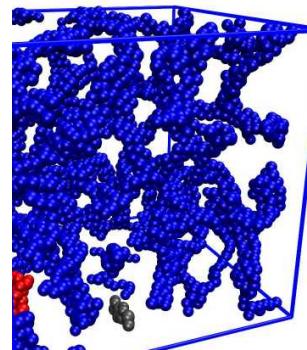
p9AA-100%Li



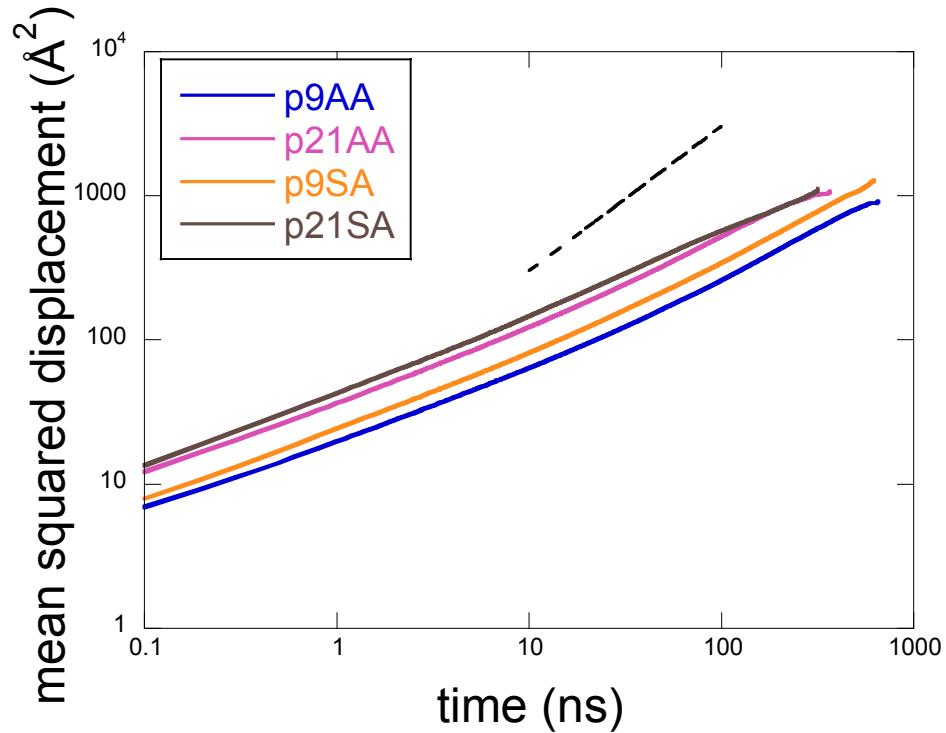
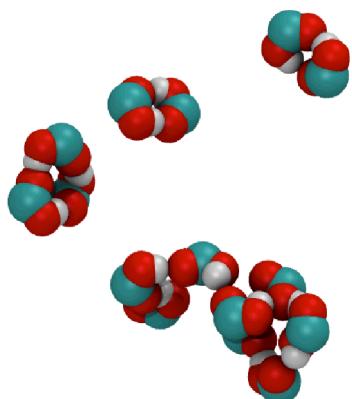
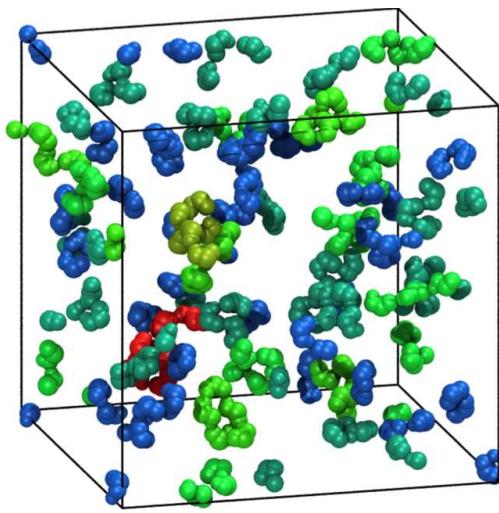
p21AA-43%Li



c. p9AA-100%Li  
FP



# Dynamics in Acid Copolymers



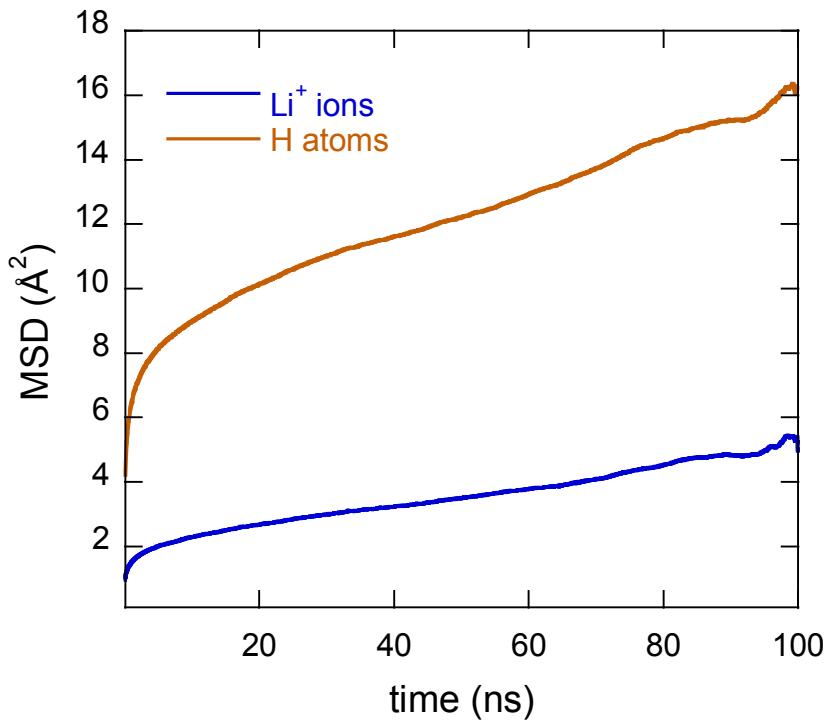
- H's move about 31 Å during simulation
- not yet diffusive

$$\langle r^2 \rangle = Dt$$

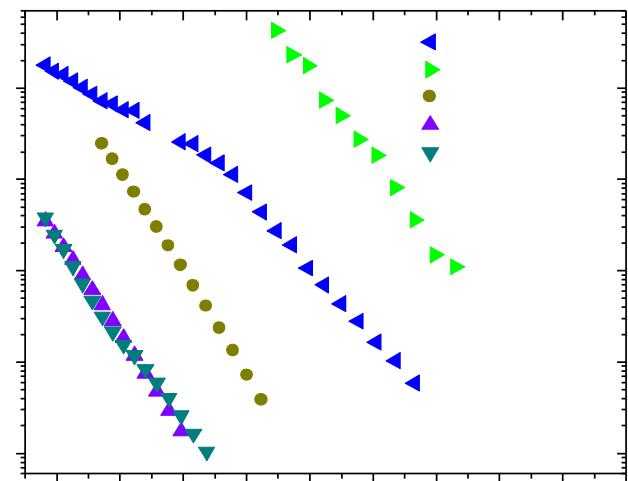
# Dynamics in ionomers

p9AA-43%Li

last 100 ns of 500 ns simulation  
very slow!

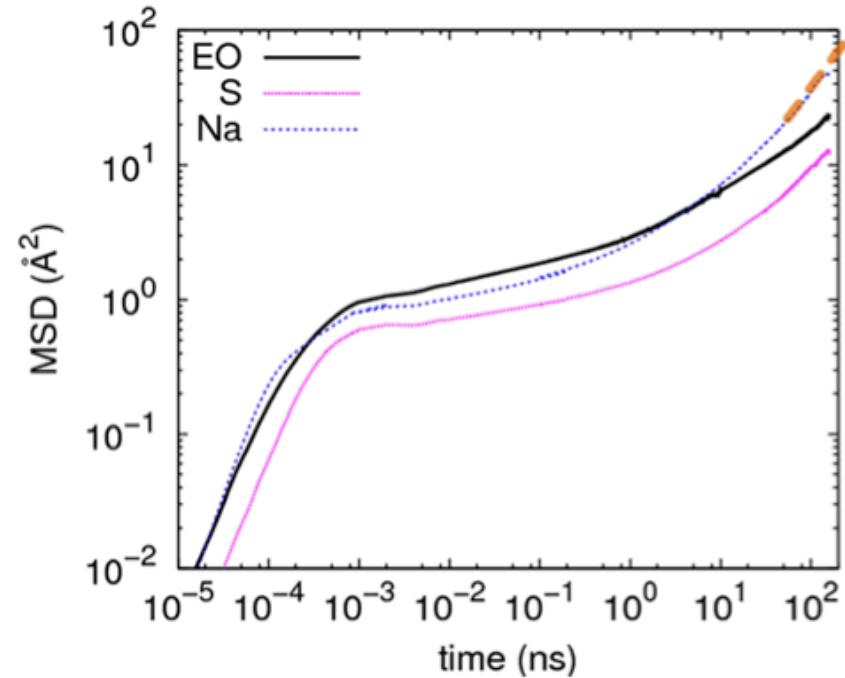
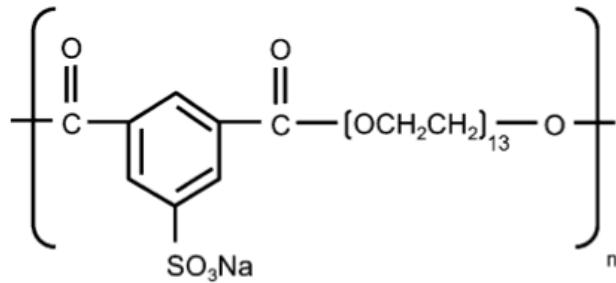


conductivity by DRS



J. Runt, H. Choi, et al.

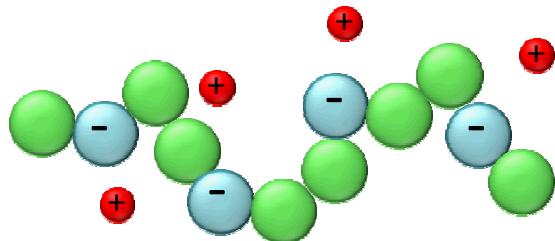
# A Faster Ionomer



Lin, K.-J. & Maranas, J. K. *Macromolecules* **45**, 6230–6240 (2012).

# Coarse-Grained Simulations

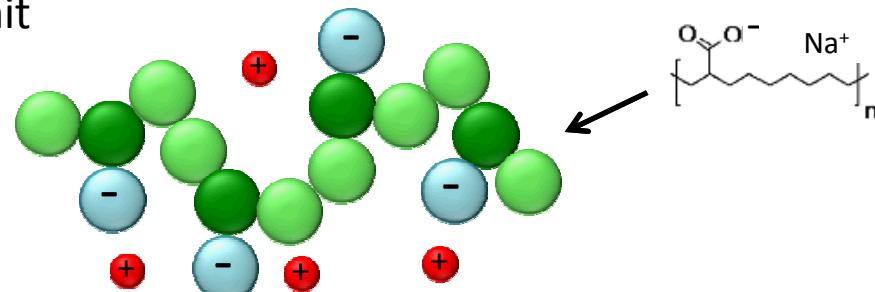
Ions in the polymer backbone:  
“ionenes”



backbone beads  
per repeat unit

$$N_{bb} = 3$$

Ions pendant to the backbone:  
“pendants”



$$N_{bb} = 3, 5, 7, 9 (11)$$

800 polymers

100% neutralization

bulk dielectric constant = 4

counterion size =  $\frac{1}{2}\sigma$

Bjerrum length =  $35.7\sigma$

$10^8$  time steps

$$\ell_B = \frac{e^2}{4\pi\epsilon_0\epsilon_r kT} = 35.7\sigma$$

$$R_g \approx 3.1 - 3.3\sigma$$

# Ionomer MD Simulations



repulsive LJ interactions + FENE springs ...

+ Coulomb interactions

$$U(r) = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon r} \quad \epsilon = 4$$

+ temperature

NVT ensemble: Langevin thermostat

$$f_i = -m_i \Gamma \nu_i + W_i(t)$$

noise  $W$  sets temperature

- 800 chains of 35-36 beads
- 4-12 charges per chain
- 1 cation per charged bead (anion)

- equilibrate for  $10^7$  timesteps
- collect averages for  $4 \times 10^7$
- 1M CPU-hours  $\approx$  325 days on 128 cores

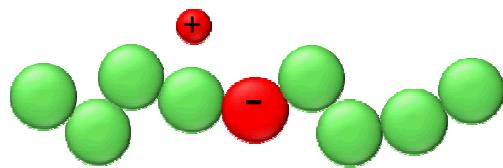
LAMMPS: open source MD code from Sandia  
<http://lammps.sandia.gov/>



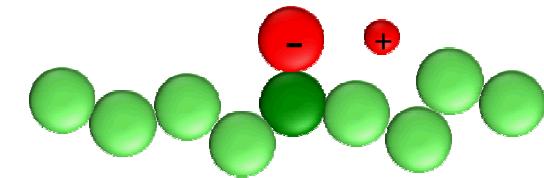
2,816 nodes / 22,528 cores



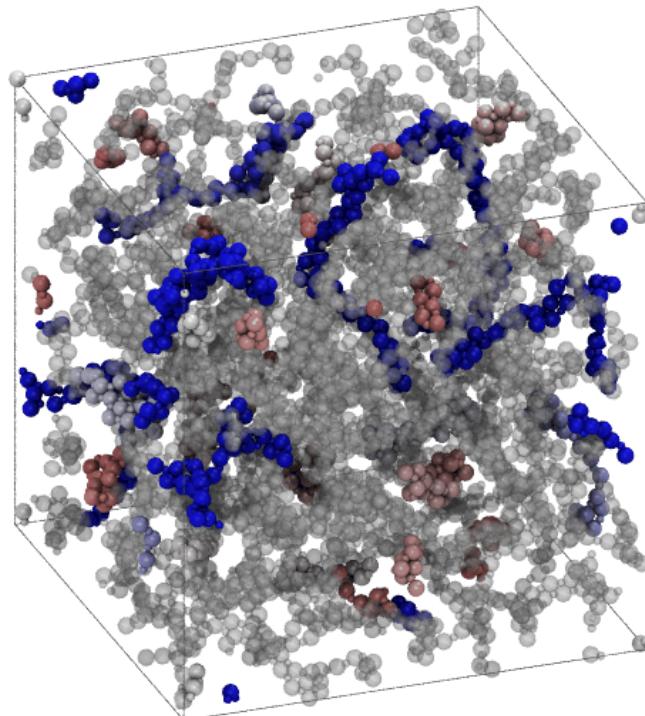
# Aggregate Morphology: Architecture Matters



Ionenes: percolated



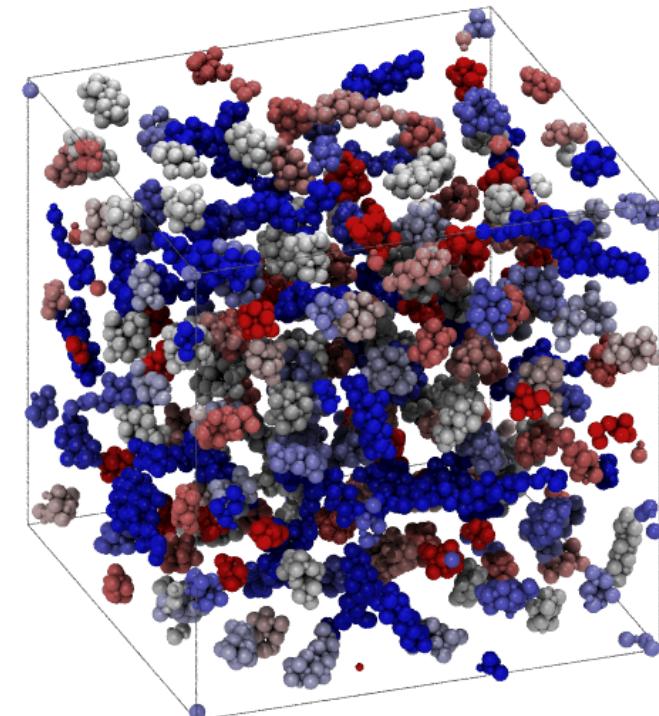
Pendants: not percolated



$$N_{bb} = 9$$

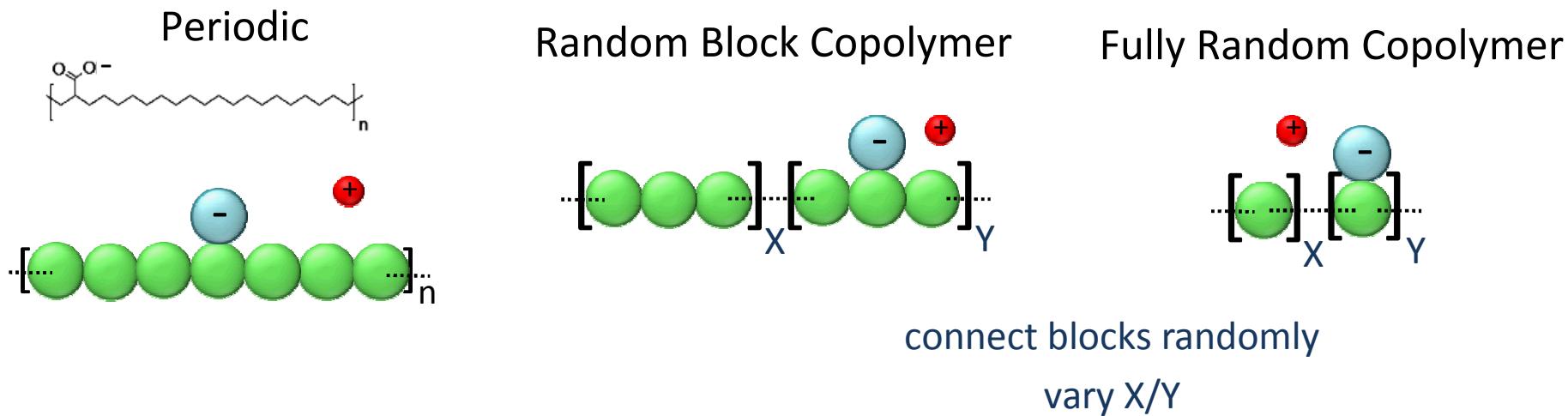
$$\epsilon_r = 4$$

Small clusters  Large clusters  
Only charged beads shown



# Randomly Spaced Ionomer Model

- random block
  - mimic ROMP
- fully random
  - mimics typical random polymerization

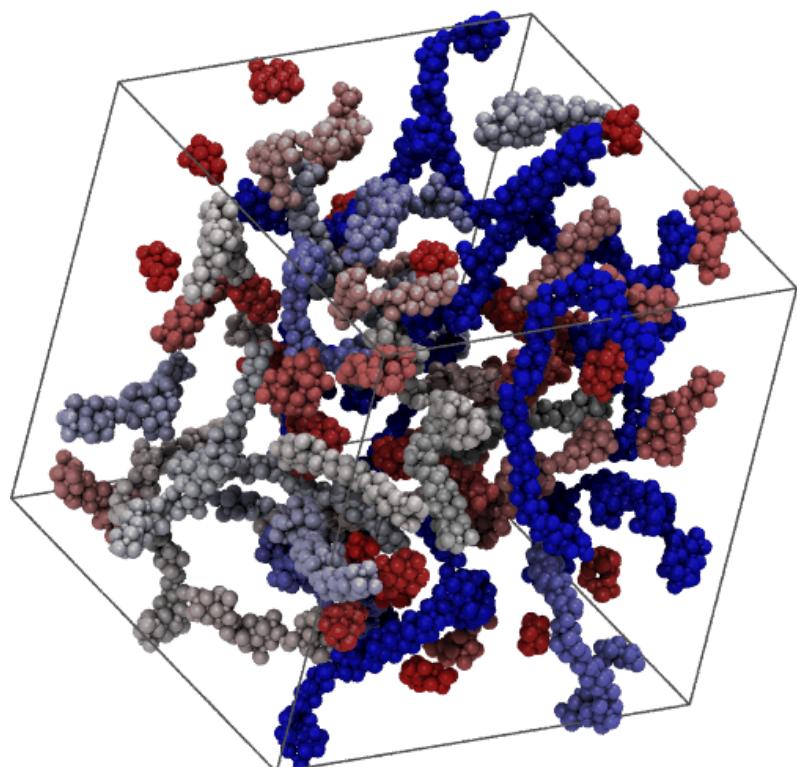


$N_{bb}$  = Number of **backbone beads** per charged bead

# Aggregate Morphology: Random vs. Periodic

**Random Block Copolymer  
Pendants:** stringy, large clusters

Mean cluster size 87

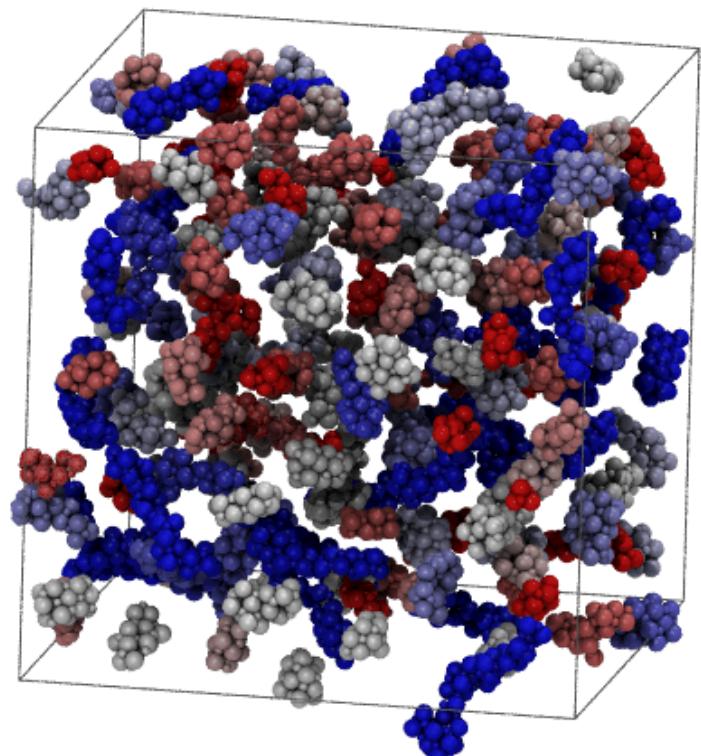


$$\begin{aligned}\varepsilon_r &= 4 \\ N_{bb} &= 9\end{aligned}$$

Small clusters

**Periodic Pendants:**  
narrow cluster size distribution

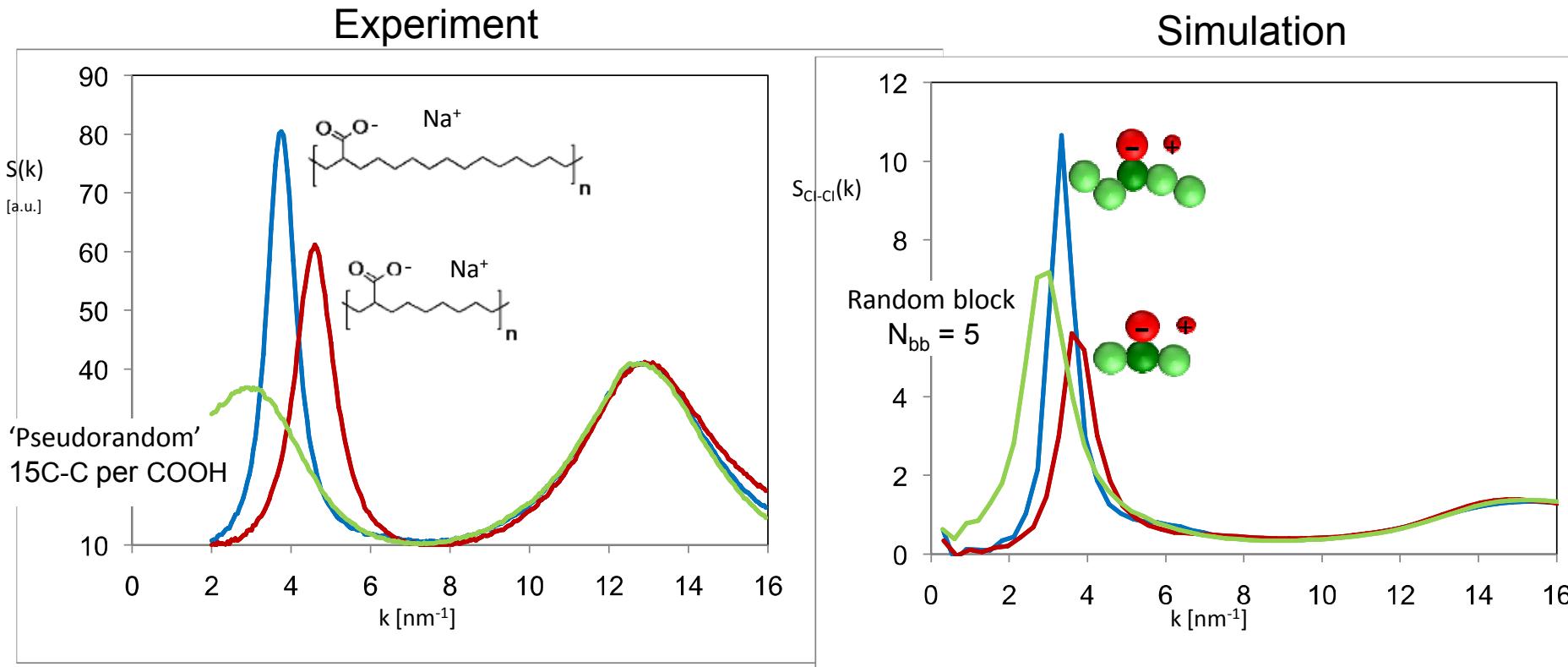
Mean cluster size 31



Large clusters

# CG MD: Comparison to X-ray Scattering

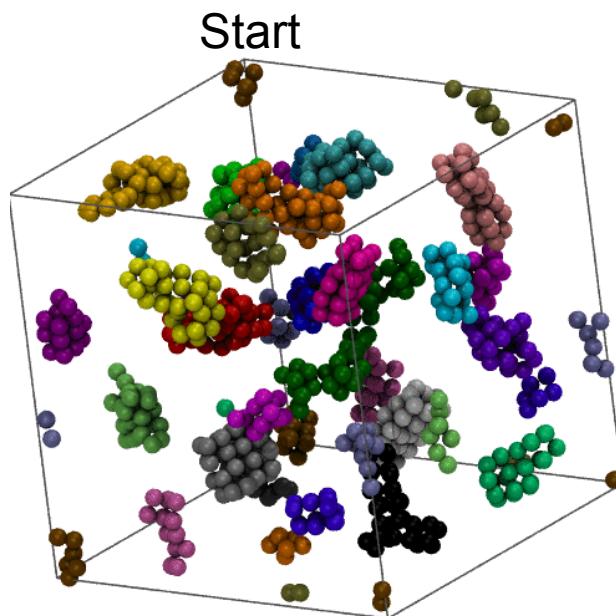
- Experimental/Simulation Agreement
  - Peak location similar
  - Increasing spacing moves peak to left
  - Random spacing moves and broadens peak



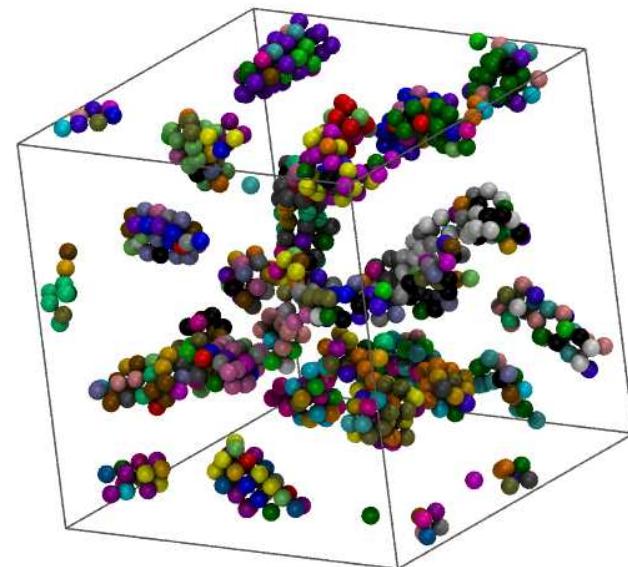
# Cluster Dynamics

Is there any?

Color distinct clusters by  
different color



Finish ( $10^7$  steps later)

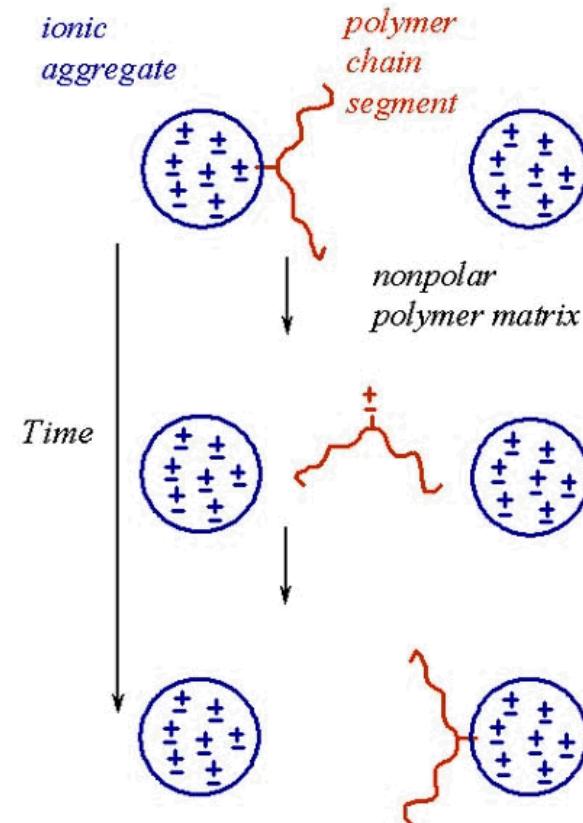


*Ions move.*

# Historical View of Dynamics

- requires traversing low dielectric polymer matrix
- large activation energy barrier
- ion **pairs** “hop” between aggregates

this is SLOW

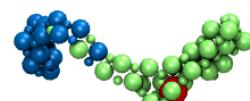
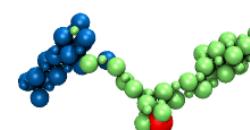
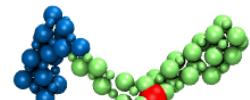
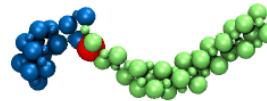
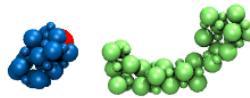


<http://www.princeton.edu/cbe/people/faculty/register/group/research/ionomers/ionomer-melt-rheology-and/>

# Ion Trajectories

periodic pendants  $N_{bb}=9$

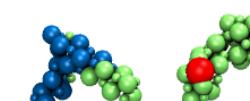
2 separate clusters  
Follow one **counterion**



Clusters have collided

Ion has moved to other cluster.  
**NEVER** separated from a cluster.

ions move by cluster  
rearrangement/collision



Clusters reform with ion moved

# Energies and Cluster Dynamics

$+$  – pair energy (contact) is  $48 \text{ kT}$ .

pairs are not likely to separate.

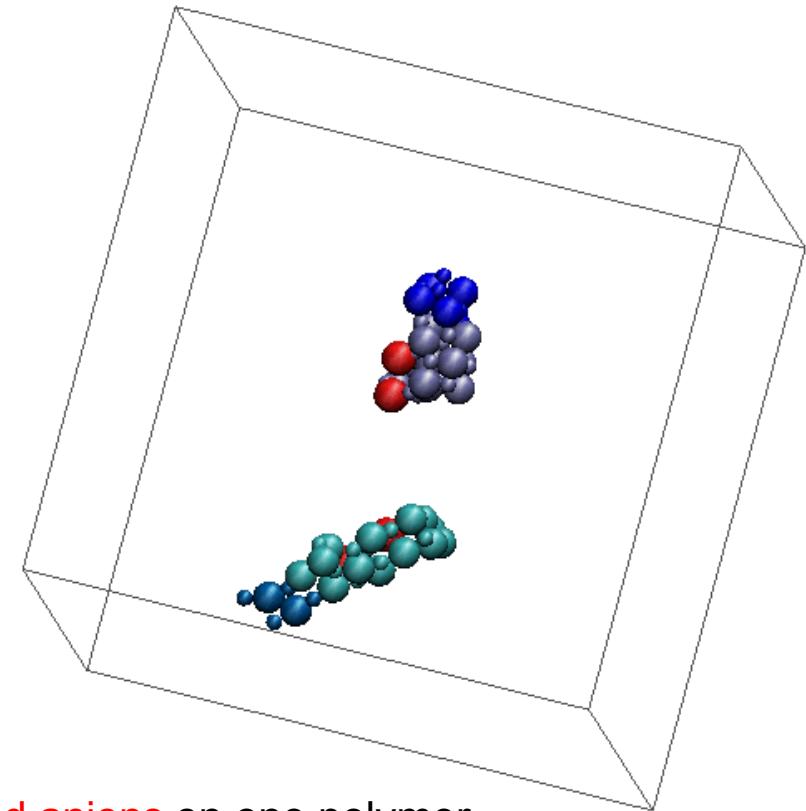
energy to split a cluster is much less  
ideal, 2D crystallite has a separation energy of  
only  $20 \text{ kT}$ :



simulations show clusters are flexible (they're liquids after all) and the energies will be less than these crystallite calculations.

ions move a lot within a cluster

Pendant (discrete clusters)



Red anions on one polymer.

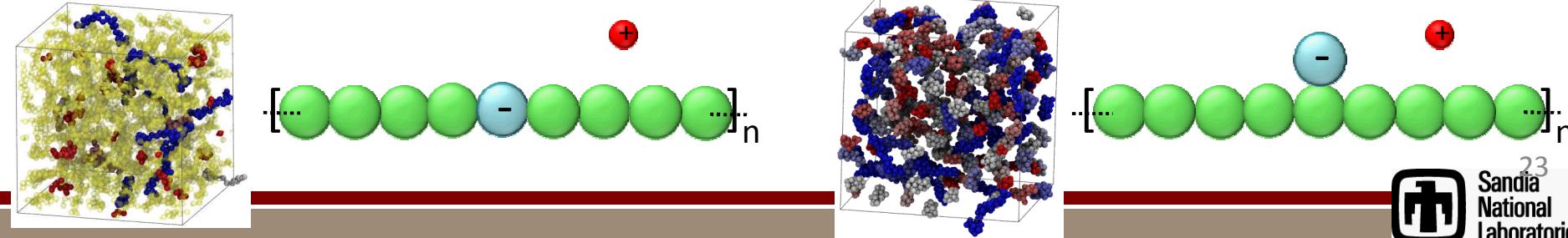
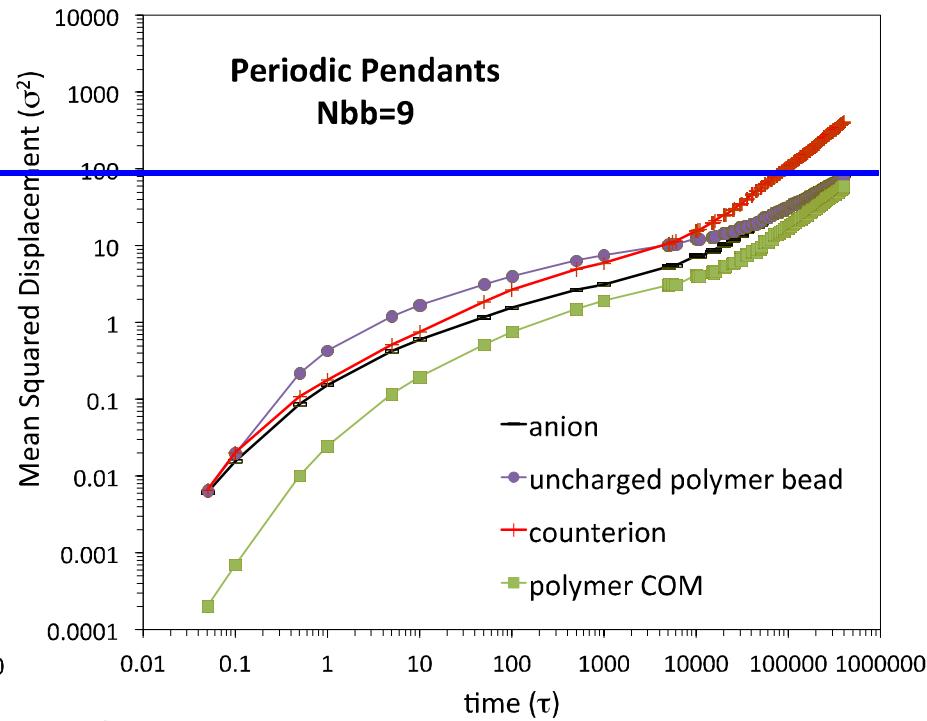
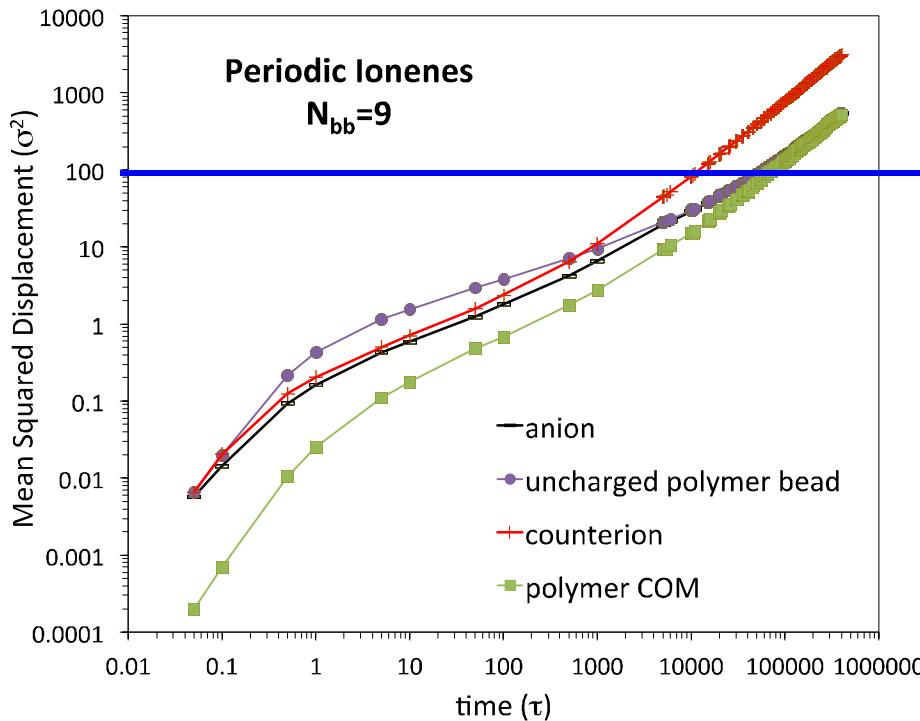
Blue ions initially within  $3\sigma$  of red anions.

Other ions which temporarily come within  $3\sigma$  are transparent.

5000  $\tau$  X million time steps

# Mean Squared Displacements

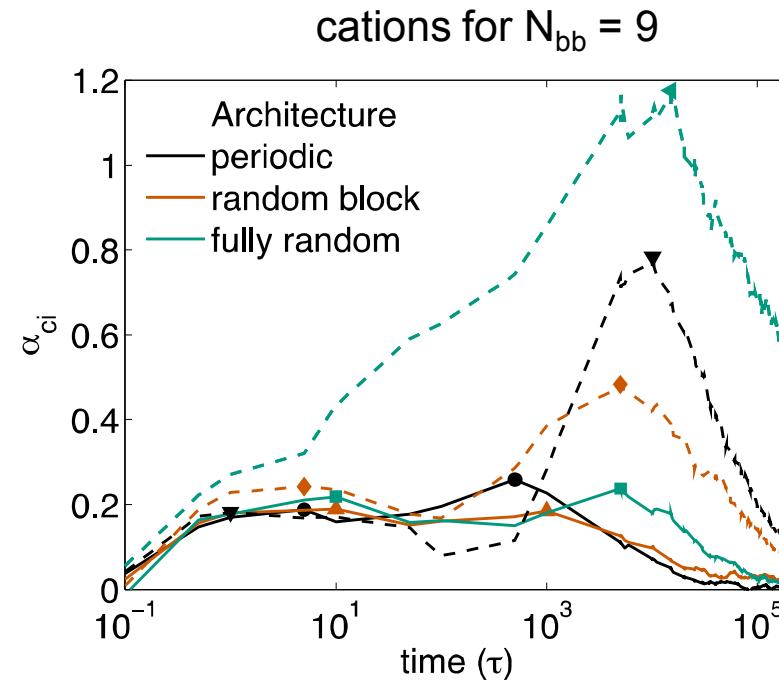
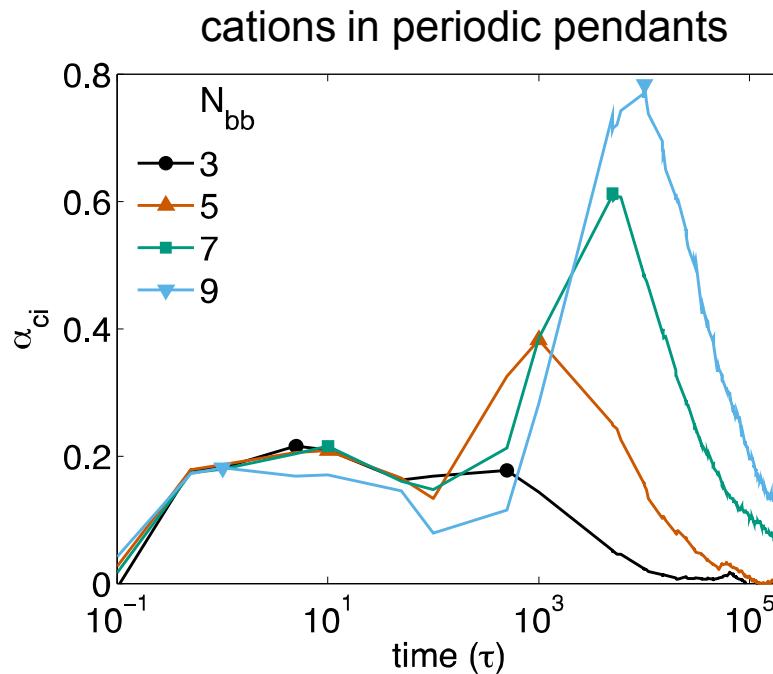
- Ionenes, pendants similar at short times
- Pendants slower but qualitatively similar at long times



# Ion Dynamics

non-Gaussian parameter

$$\alpha(t) = \frac{3 \langle (r(t))^4 \rangle}{5 \langle (r(t))^2 \rangle^2} - 1$$

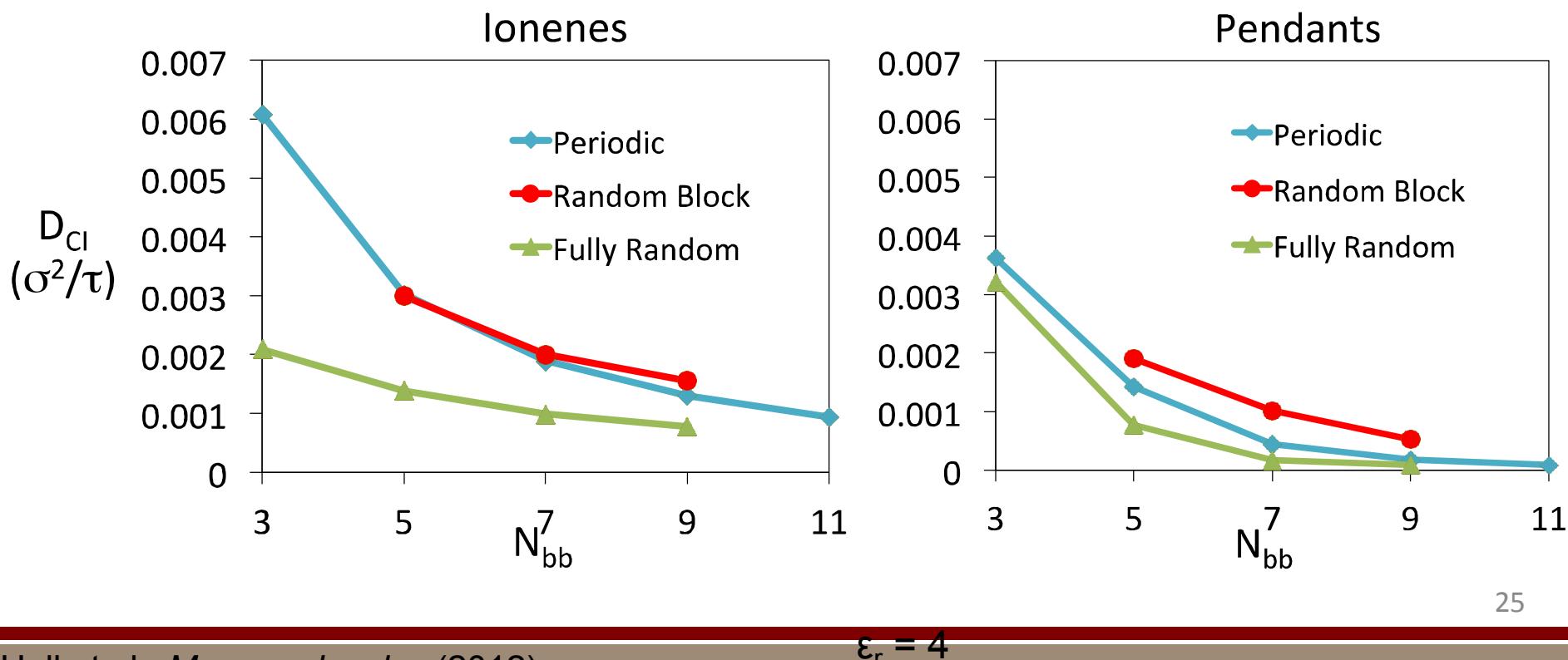


indicative of 2 time scales:

- local motion in clusters
- slower rearrangement between clusters

# Counterion Diffusion Constants

- Ionenes conduct better than pendants
- Greater concentration of ions increases diffusion
- Blocky random copolymerization increases diffusion



# Static Electric Field

add force  $F_x = qE_x$  to each ion

how strong a field should we add?

electrostatic force

$$\frac{F}{kT\sigma} = -\frac{q_i q_j}{r^2} \frac{\ell_B}{\sigma}$$

LJ units:  $|q| = 1$ ,  $kT = 1$ ,  $\sigma = 1$ ;  $\ell_B/\sigma = 35.7$

at contact,  $r = 0.75\sigma$ :  $F = -63/kT\sigma$

for field

$$E^* = \frac{kT}{q\sigma} = 1 \quad F = 1/kT\sigma$$

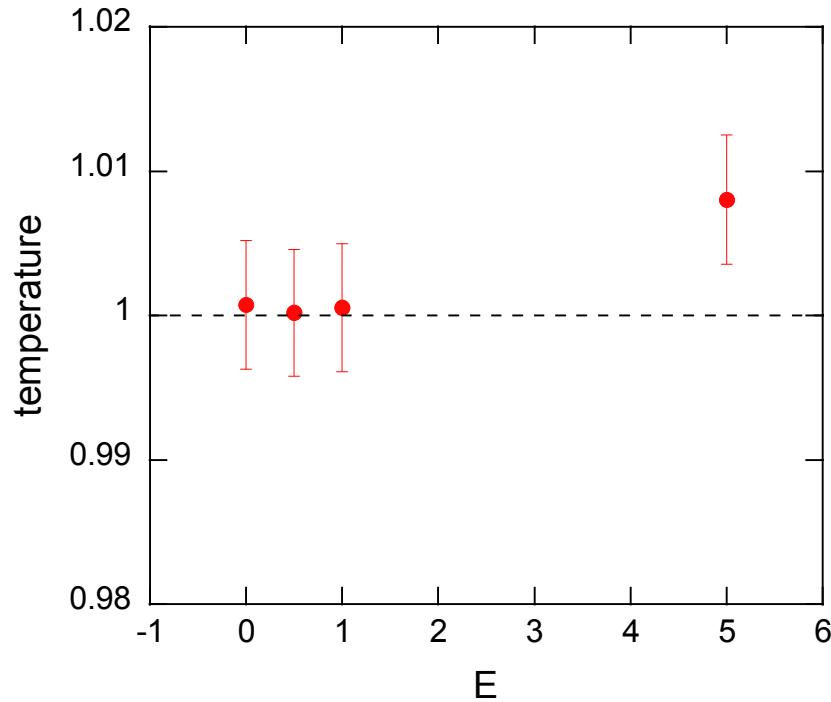
rough estimate in real units:

$\sigma = 0.4$  nm,  $T = 298$ K,  $E = 0.8$  V/nm =  $8 \times 10^6$  V/cm

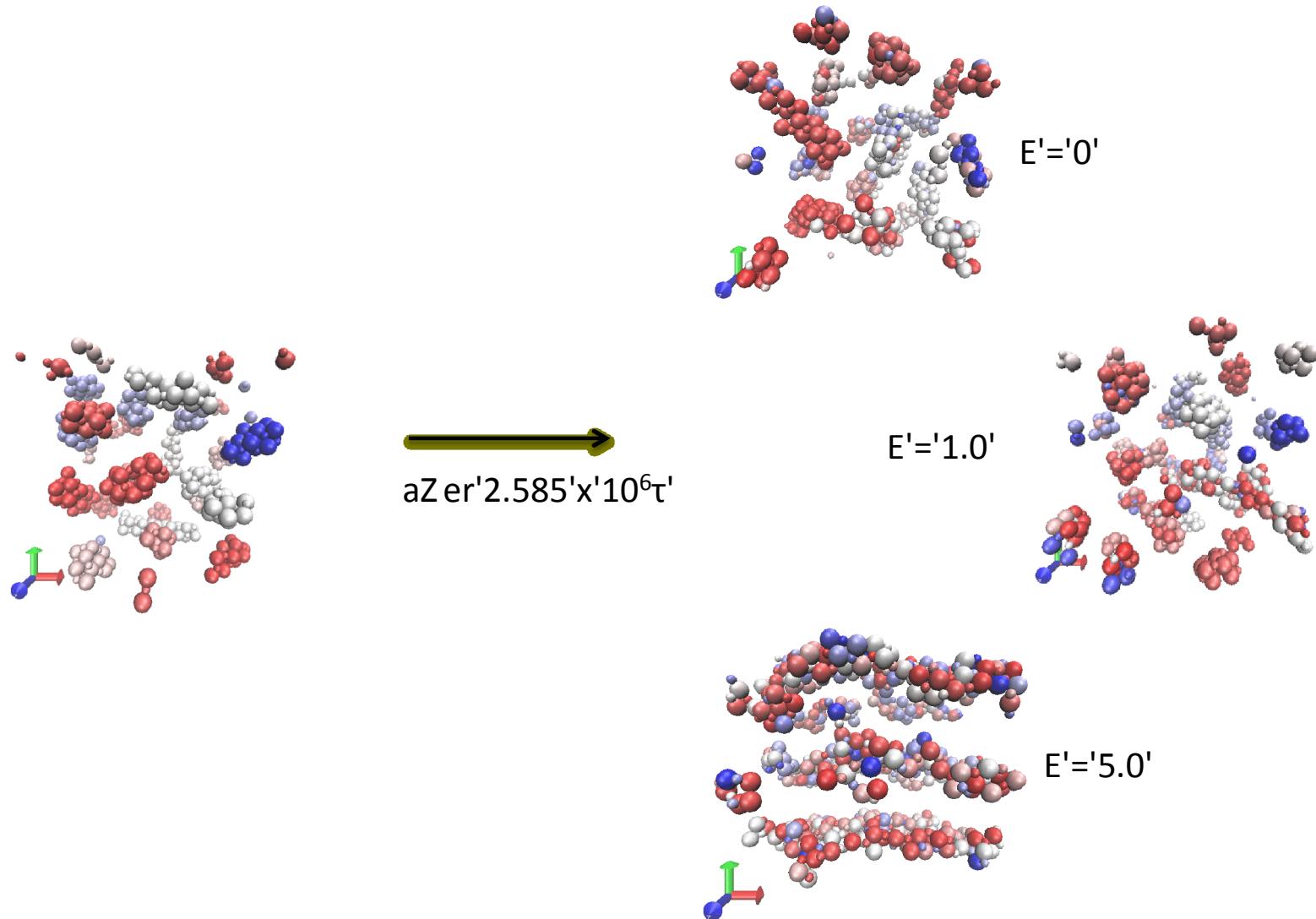
# Check Field Strengths

turn off thermostat in field direction

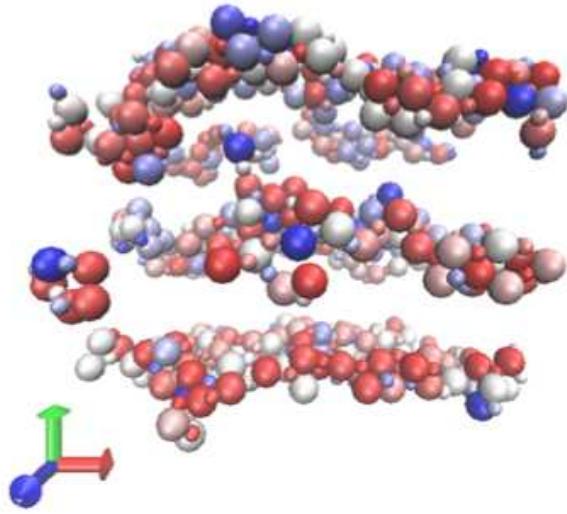
set  $T^* = \frac{k_B T}{\epsilon_{LJ}} = 1$



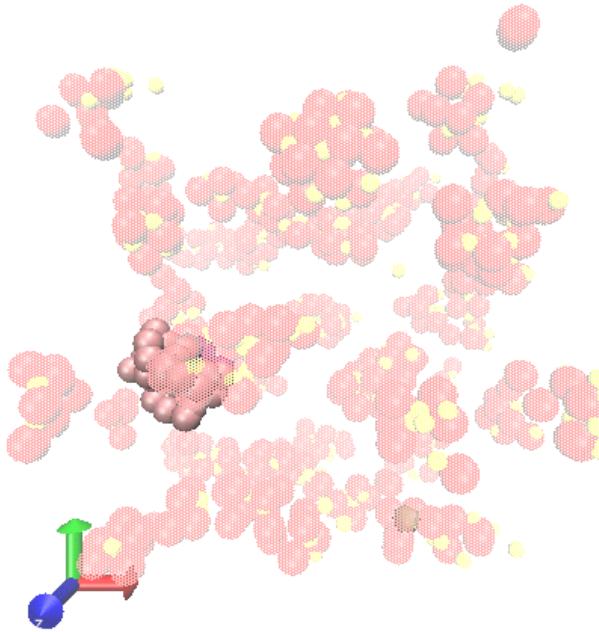
# Effects on Clusters



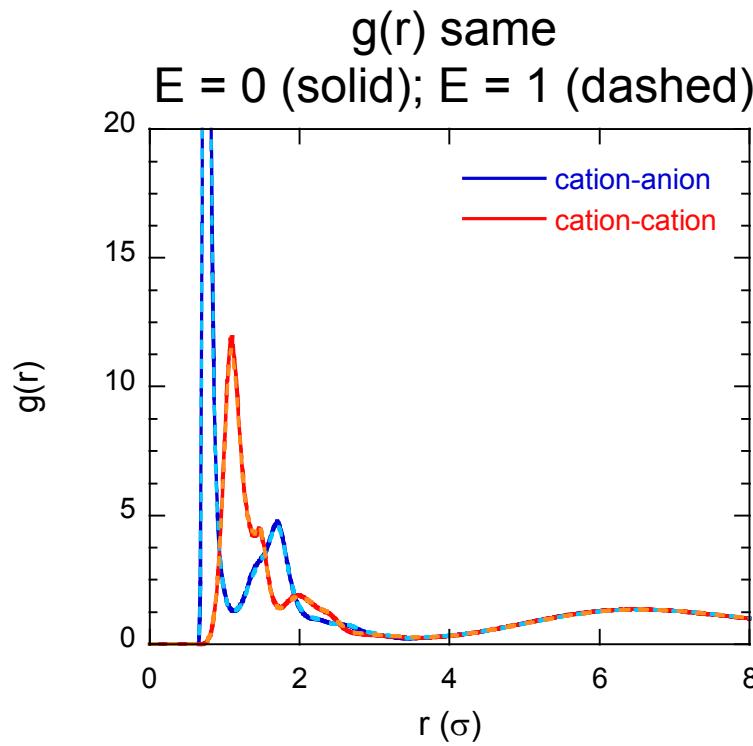
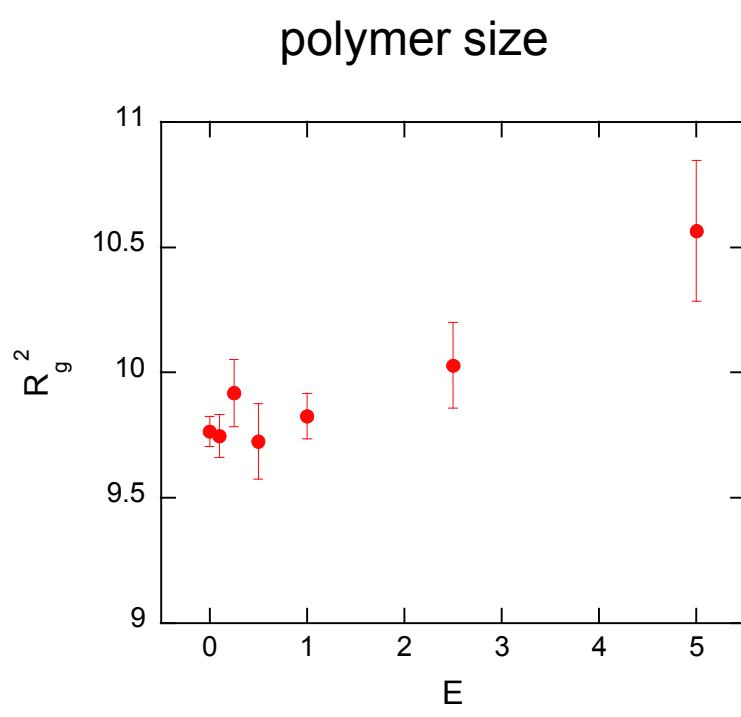
# Aggregates Align in High Fields



$E = 5.0$



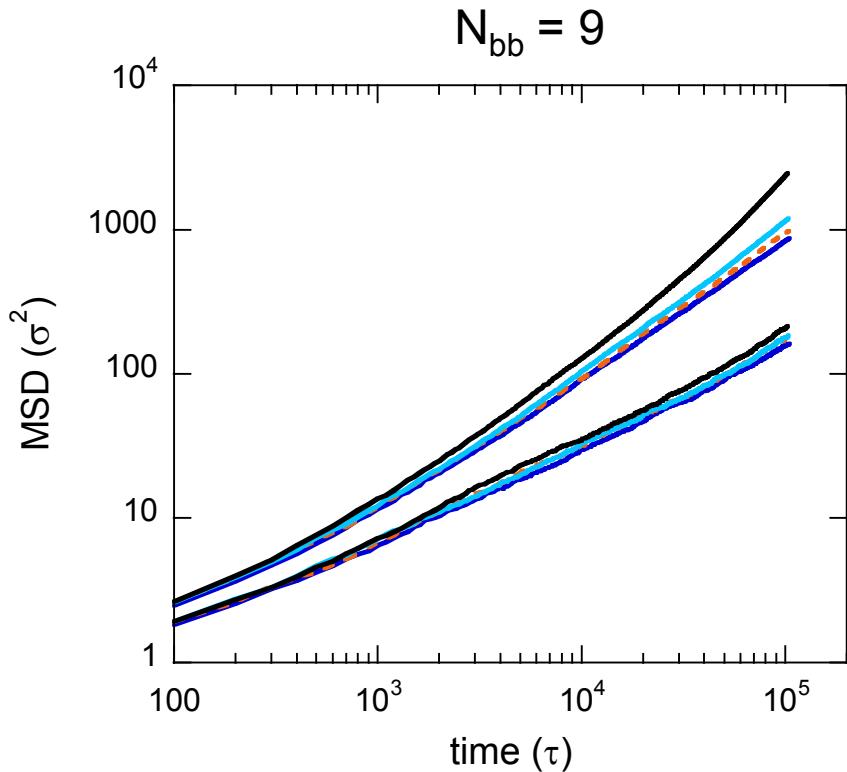
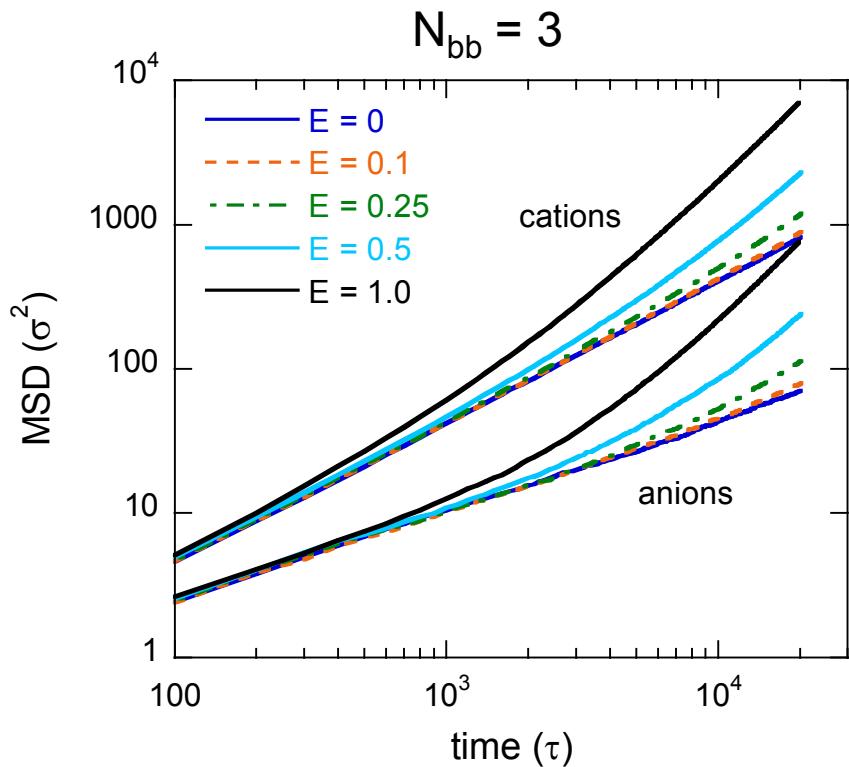
# Effect of Field on Structure



no effect for  $E \leq 1$

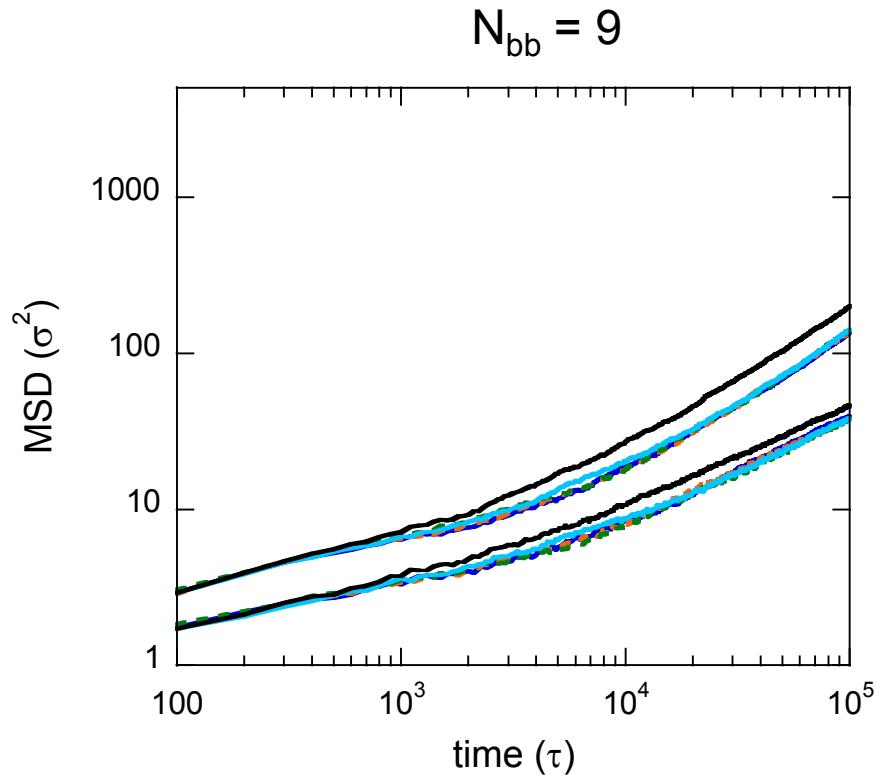
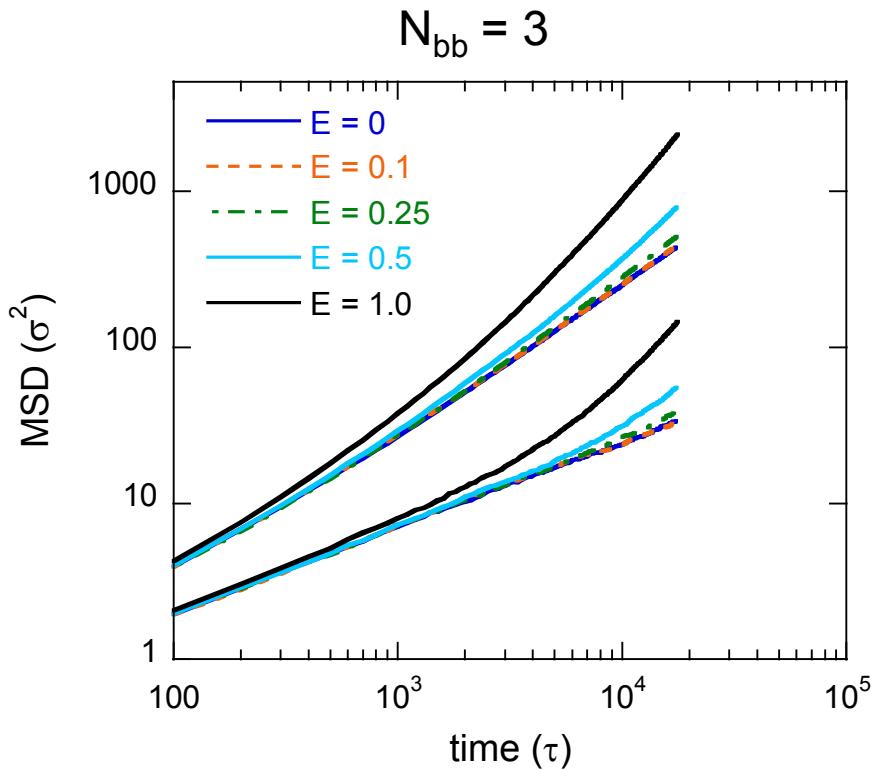
# Mean-Squared Displacements

ionenes



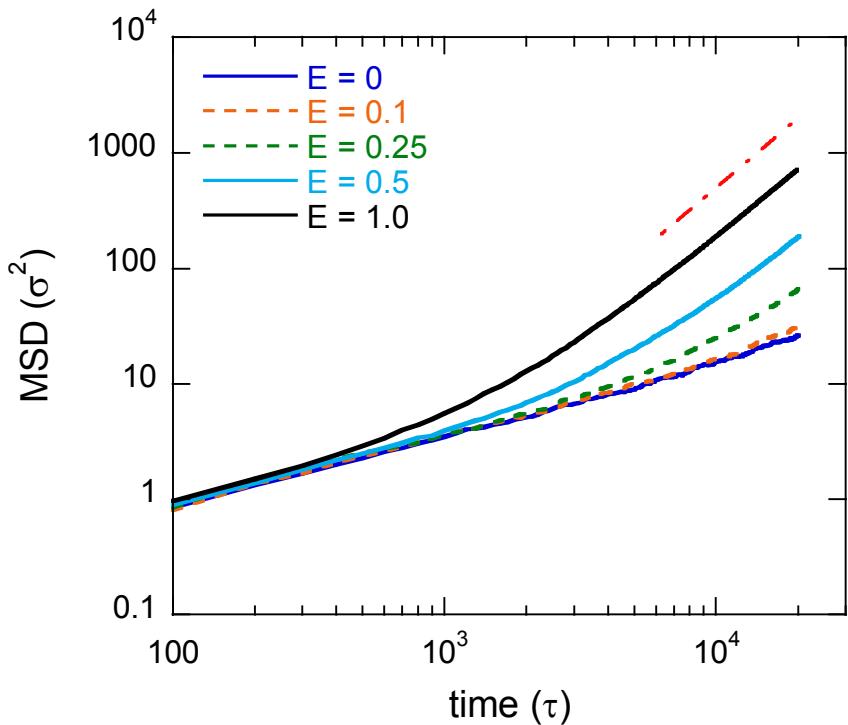
# Mean-Squared Displacements

pendants

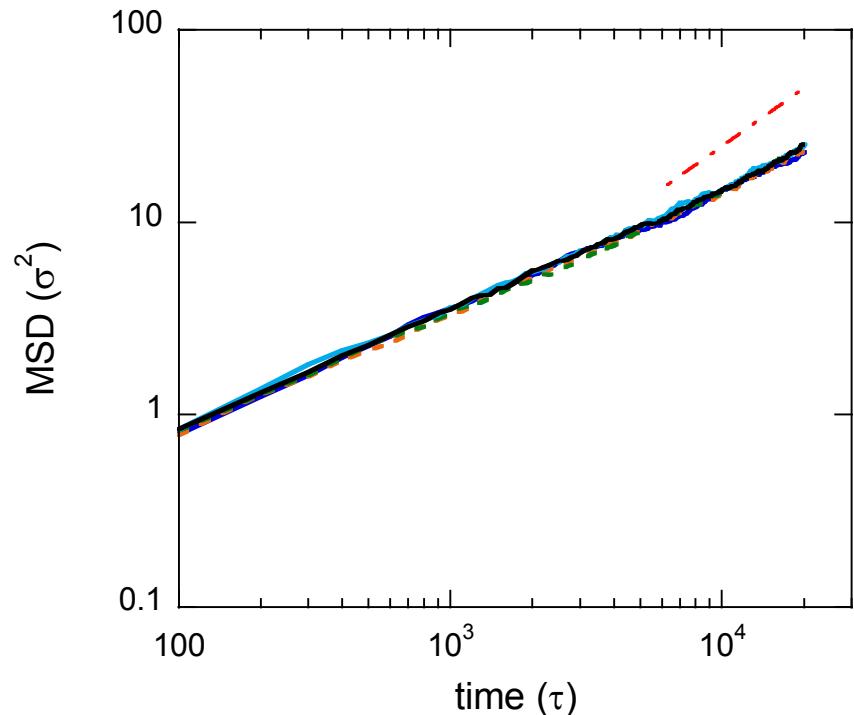


# Directional MSDs

in field direction



perpendicular to field

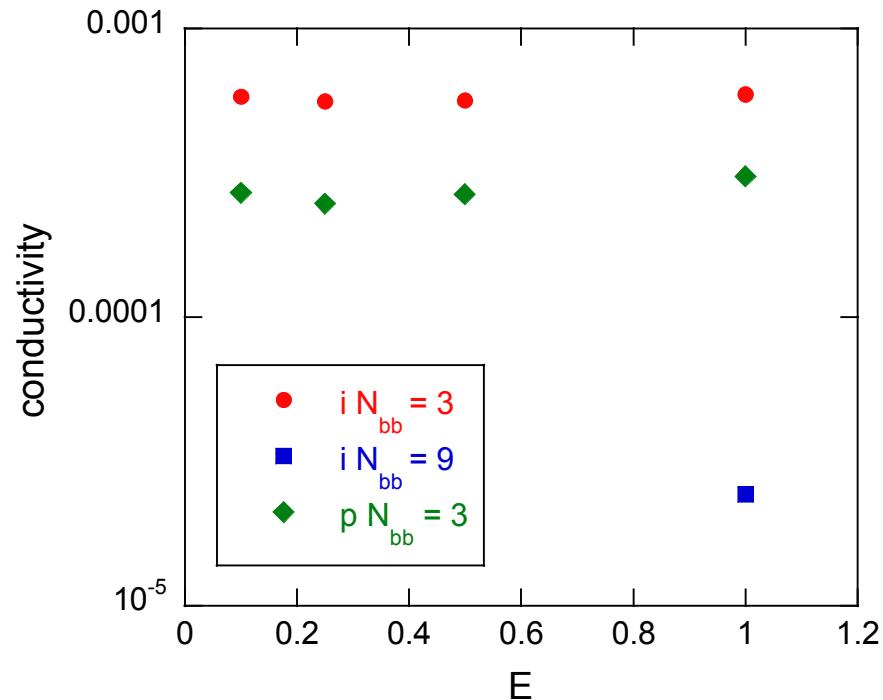
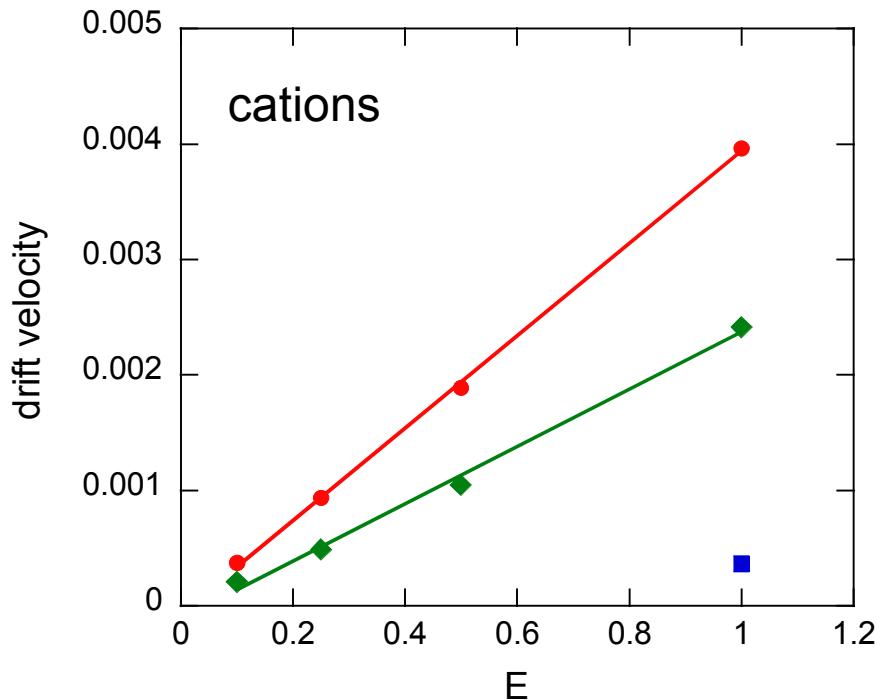


drift velocity:  $\langle x_E^2(t) \rangle - \langle x_0^2(t) \rangle = \langle v_x^2 \rangle t^2$

# Conductivity

ion mobility:  $\mu_i = \langle v_{x,i} \rangle / E$

conductivity:  $\lambda = \rho e(\mu_+ - \mu_-)$



# Nernst-Einstein

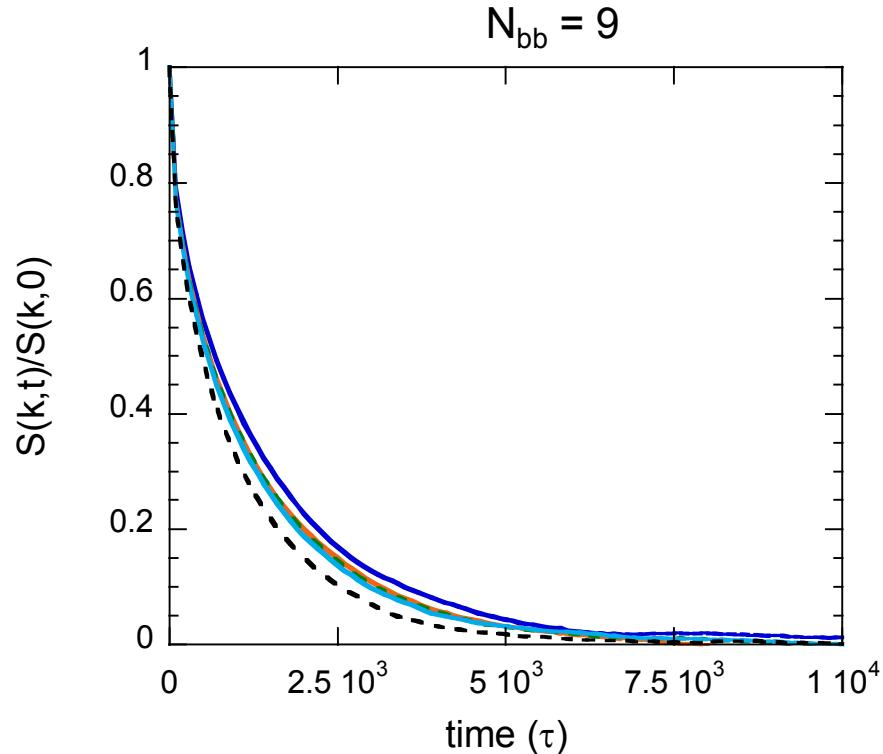
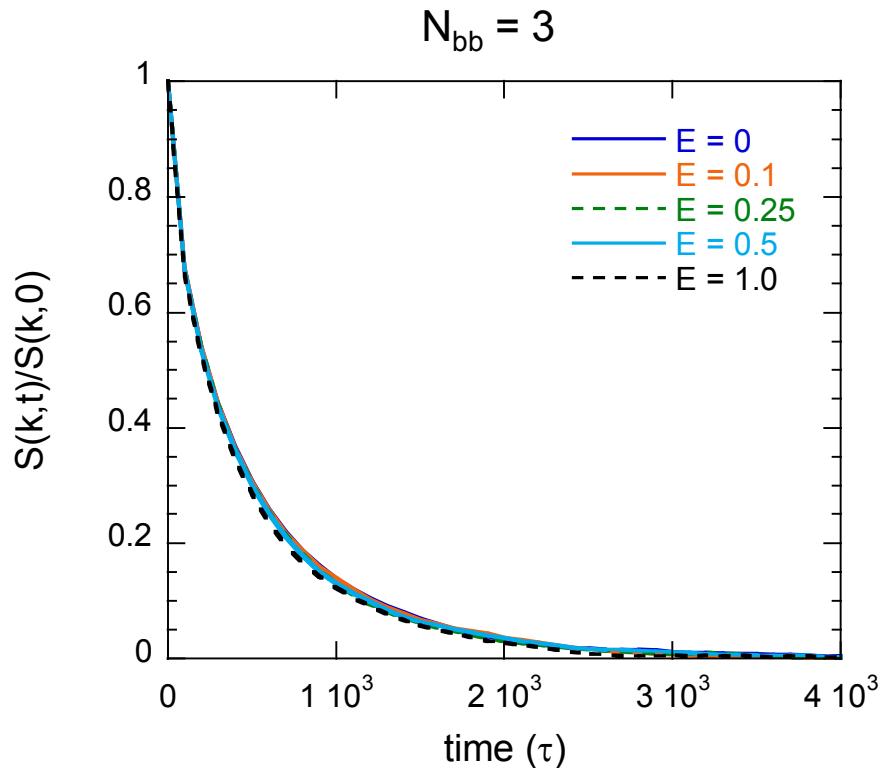
if ions are uncorrelated:  $\lambda^{NE} = \frac{e^2 \rho}{kT} (D_+ + D_-)$

| system        | $\lambda$            | $\lambda^{NE}$       | $\alpha = \lambda/\lambda^{NE}$ |
|---------------|----------------------|----------------------|---------------------------------|
| ionene N = 3  | $5.7 \times 10^{-4}$ | $1.6 \times 10^{-3}$ | 0.36                            |
| ionene N = 9  | $2.4 \times 10^{-5}$ | $1.3 \times 10^{-4}$ | 0.18                            |
| pendant N = 3 | $2.7 \times 10^{-4}$ | $7.5 \times 10^{-4}$ | 0.36                            |

# Time-Dependent Structure Factors

ionenes

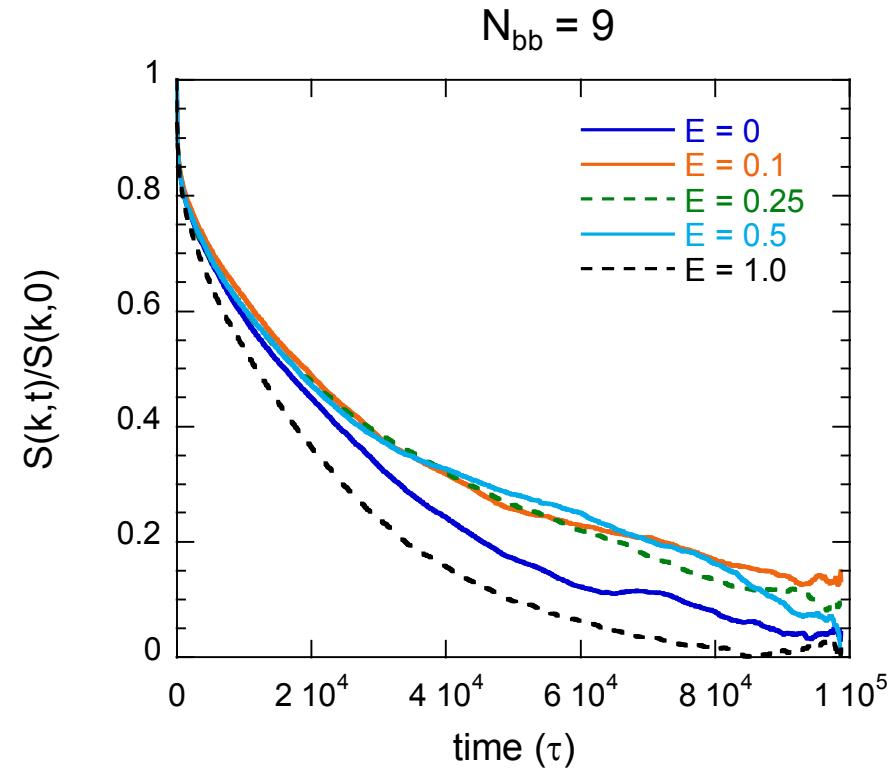
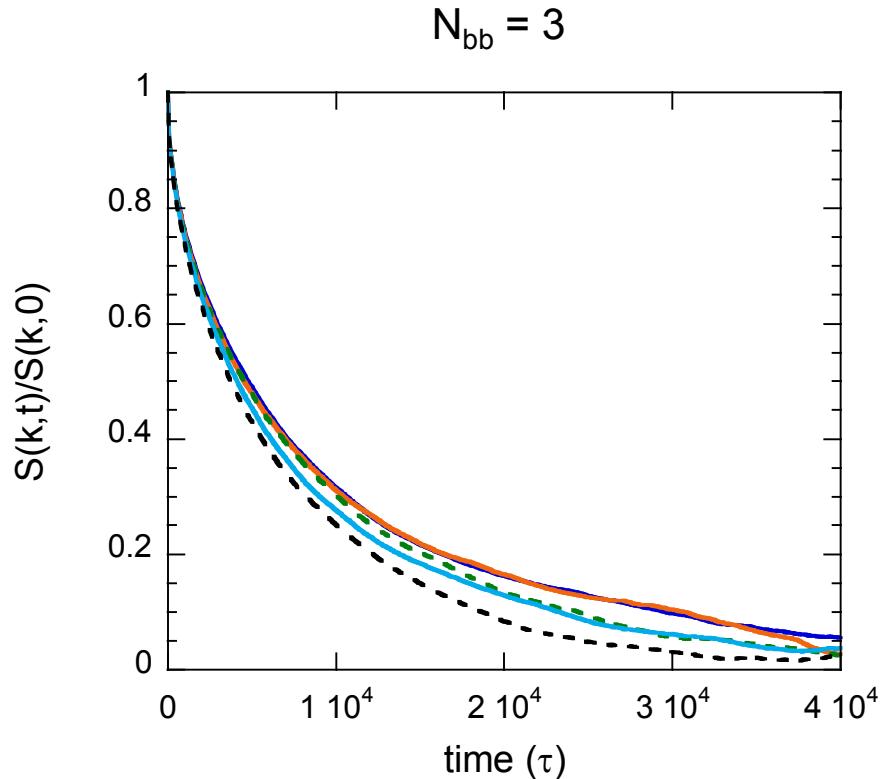
decay at the ionomer peak



field speeds up decorrelation of clusters

# Time-Dependent Structure Factors

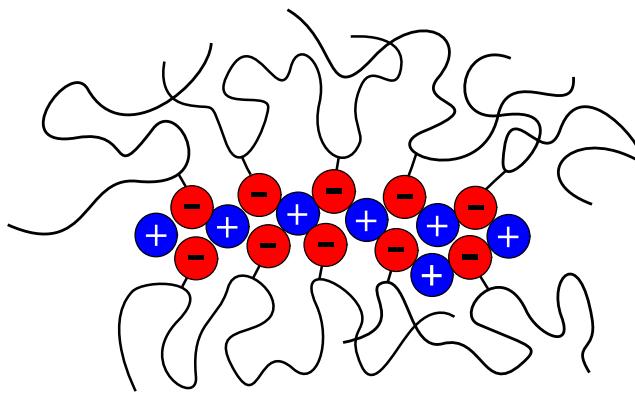
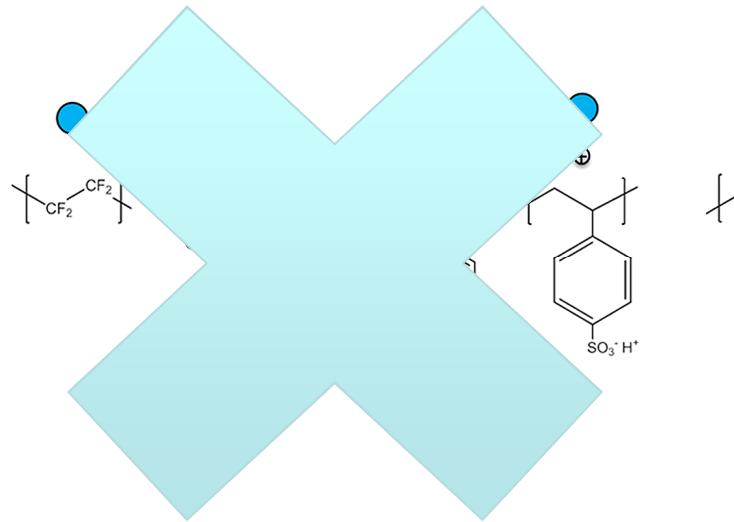
pendants



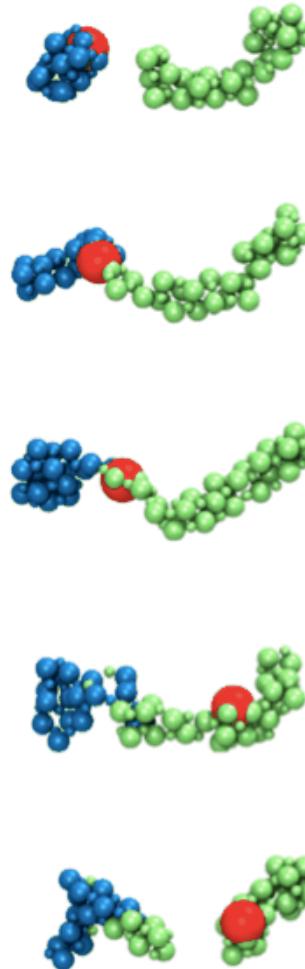
field slows down motion!  
why?

# The New Picture

stringy morphologies



ion motion by cluster rearrangement



# Conclusions

- aggregates have many shapes
- molecular architecture important
  - isolated aggregates for pendants or large spacing
  - percolation for ionenes or short spacing
- ion motion by cluster rearrangement
- ions diffuse faster in percolated morphologies
- ion motion is correlated

coarse-grained

Hall, et al., *Phys Rev Lett* **106**, 127801 (2011);  
*J. Am Chem. Soc.* **134**, 574 (2012);  
*Macromolecules*, **45**, 8097 (2012)

atomistic

Alam et al., *Materials* **5**, 1508 (2012)  
Bolintineanu et al., *ACS Macro Lett.* **2**, 206 (2013);  
Bolintineanu et al., *Macromolecules* **46**, 5381 (2013);  
Lueth et al., *J Chem Phys* **140**, 054902 (2014)

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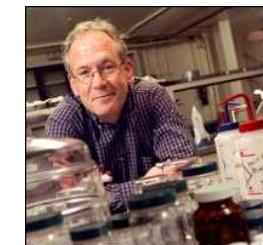
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University of Pennsylvania



Jim Runt, Penn State



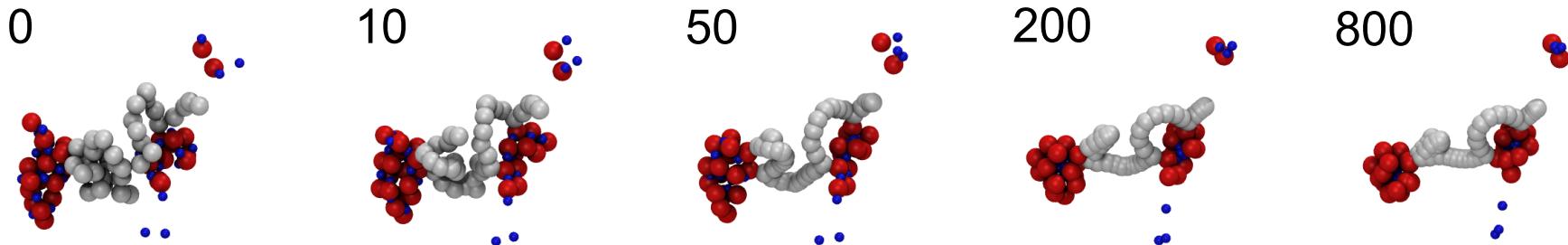
The “ionomers” LDRD team  
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CINT  
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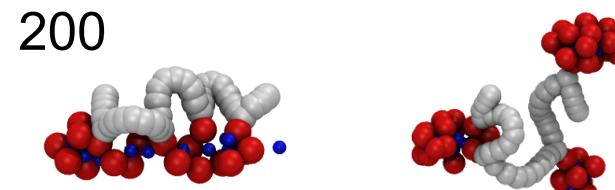
# Average Local Structure

one polymer (white, red anions) and nearby ions (red anions, blue counterions)  
 $N_{bb}=9$ , frames are 1000 steps apart

periodic pendant, frames averaged:



other periodic pendant  
examples



periodic ionene, frames averaged:

