

Atomistic Potentials for Palladium-Silver Hydrides

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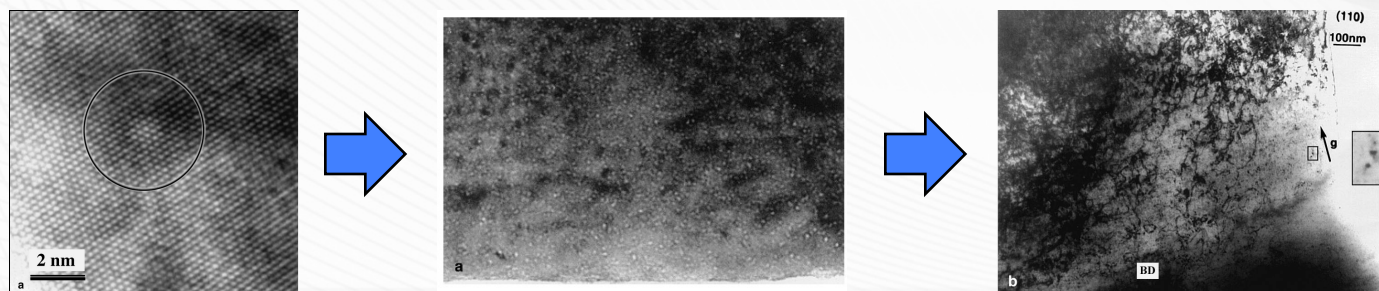
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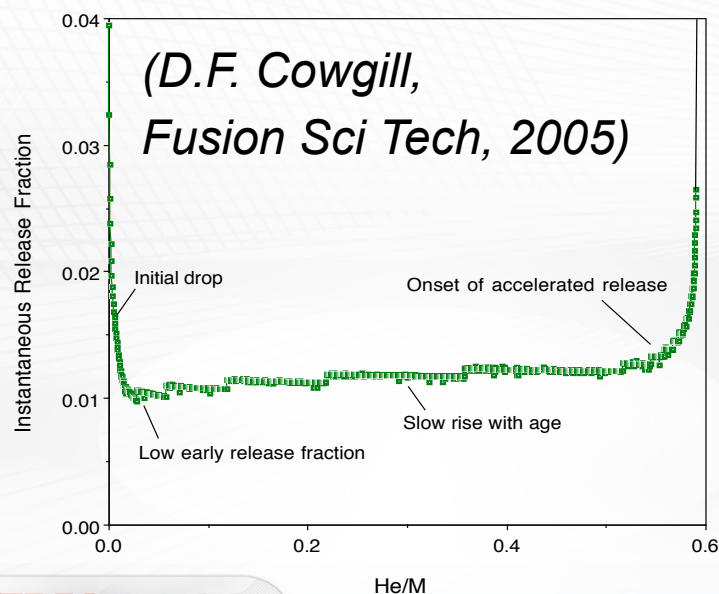
How do hydrogen and hydrogen-isotope storage materials fail?

- Hydrogen (H) and hydrogen-isotopes (D,T) in metals produce a variety of defect-mediated behaviors that can result in deformation, failure and fracture, e.g. H embrittlement (HE), H enhanced localized plasticity (HELP).
- Decay of tritium produces helium (He) atoms that cluster and form bubbles.
- For He in palladium (Pd), He gas is released from the metal at an accelerated rate at some critical concentration of He/Pd.
- Experiments reveal dislocation loops and other defects in these aged samples

Determining the cause of accelerated release of helium gas



(S. Thiébaut et al, *J Nucl Mater*, 2000)



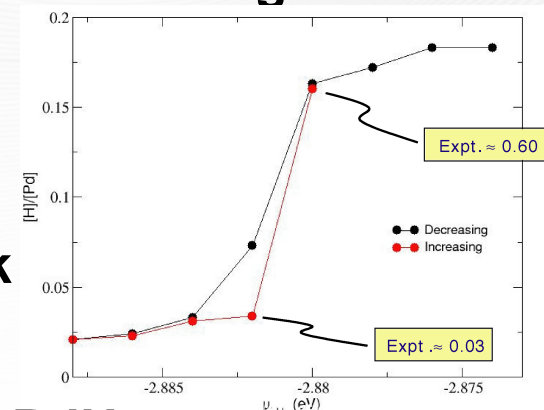
Our focus:

Identify physical mechanisms leading to accelerated release of He gas

We simulate and examine the material defects that originate from having He bubbles in a metal lattice using atomistic modeling methods.

Potentials in the scientific literature

- Embedded Atom Method (EAM) model by Daw and Baskes (*Phys Rev Lett*, 1983; *Phys Rev B*, 1984)
 - Accurate for dilute amounts of H and reasonable for PdH alloy.
 - Incorrectly predicts tetrahedral site occupation for high H concentrations.
 - Displays only a very small miscibility gap:
- Multi-body potential by Zhong, Li and Tománek (*Phys Rev B*, 1991, 1992)
 - Accurate for dilute amounts of H in Pd and PdH.
 - Agreement on properties of H-covered Pd surfaces.
 - Incorrectly predicts tetrahedral site occupation for high H concentrations.
 - Displays no miscibility gap.

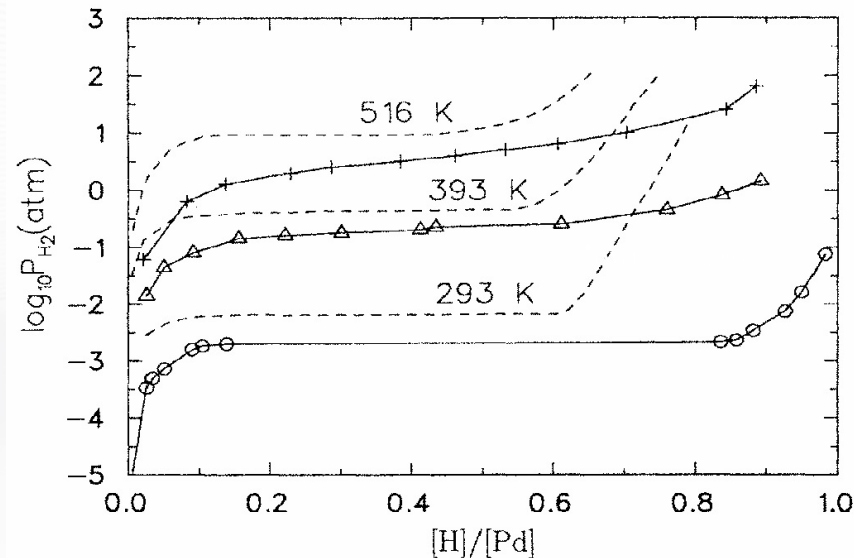


Potentials in the scientific literature

- EAM by Wolf, Lee *et al.* (*Phys Rev B*, 1992, 1993; *Phys Rev Lett*, 1994)
 - Displays qualitatively correct miscibility gap:
 - BUT, functions and parameters for Pd-H and H-H interactions are not in publications! (or anywhere, trust me)

... so, we decided to build our own potential to capture miscibility gap.

Later, developed an interest in exploring Pd-Ag-T alloys to determine if alloying impacts He bubble/gas retention.



Pd-H EAM Model

Start with Pd-Pd interaction by Foiles and Hoyt (*SAND2001-0661*)...

- **Total energy**
$$E = \sum_{i=1}^N F_i(\rho_i) + \frac{1}{2} \sum_{i=1}^N \sum_{\substack{j=1 \\ j \neq i}}^N \phi(r_{ij}), \quad \rho_i = \sum_{\substack{j=1 \\ j \neq i}}^N \rho^a(r_{ij})$$
- **Pd potential functions known**
- **H embedding energy**
$$F(\rho) = A \cdot \rho \cdot \ln(\rho) + B \cdot \rho$$
- **H electron density**
$$\rho^a(r) = C \cdot \exp(-\delta \cdot r)$$
- **H-H and Pd-H pair energy**

$$\phi(r) = \beta \cdot D \cdot \exp[-\alpha \cdot (r - r_0)] - \alpha \cdot D \cdot \exp[-\beta \cdot (r - r_0)]$$

Model problems, and solutions...

- For elemental system, invariances relating the pair potential, atomic charge density and embedding energy functions introduce non-uniqueness:

$$F(\rho) + k_1 \cdot \rho, \quad \phi(r) - 2k_1 \cdot \rho^a(r) \quad F\left(\frac{\rho}{k_2}\right), \quad k_2 \cdot \rho^a(r)$$

Solutions: $k_1 = -F'(\rho_0)$ $\rho_{low} < \rho_{0,i} < \rho_{high}, \quad i = 1, 2, \dots$

- For Pd-H system, properties of selected Pd-H phases do not uniquely determine H properties

Solution: Include H phase in the fitting of potential parameters

Whenever possible, use analytic functions of composition

- **OC PdH_x structure**: a fully occupied fcc Pd sublattice, and a partially occupied fcc H sublattice at the Pd octahedral interstitial sites. The occupancy probability for the H sublattice is x .
- **TE PdH_x structure**: a fully occupied fcc Pd sublattice, and two partially occupied fcc H sublattices at the Pd tetrahedral interstitial sites. The occupancy probability for the H sublattice is $x/2$.
- Analytical energy as a function of composition can be derived assuming atom distribution is perfectly random.

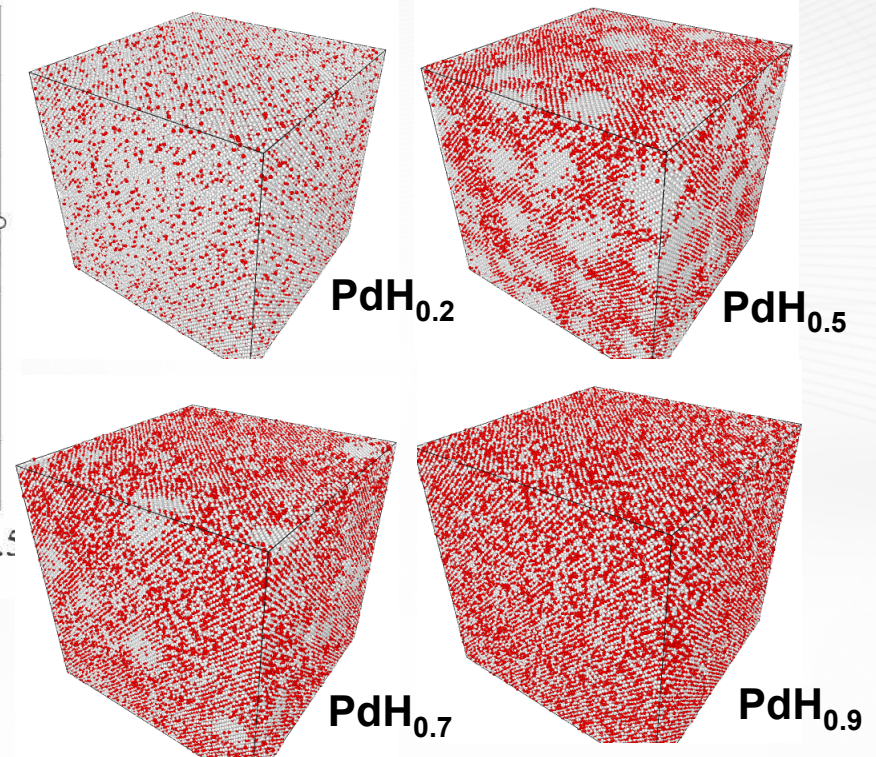
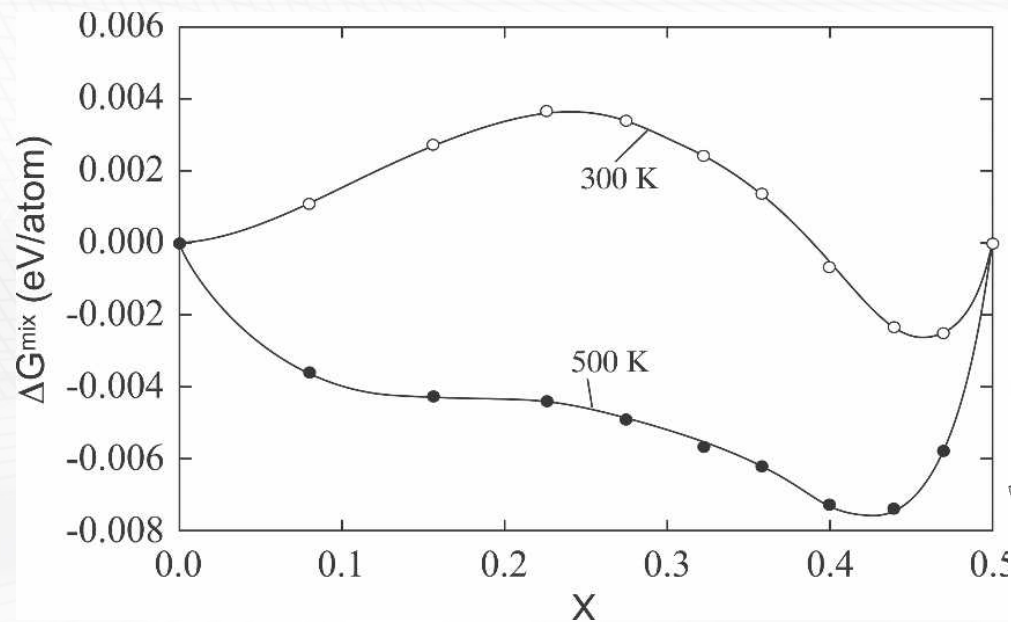
fitEAM Mathematica program

- **Mathematica used for its symbolic computation, automated derivation, graphic analysis capabilities, and built-in optimization routines**
- **Conversion of input Pd potential**
- **Derivation of analytical expressions for cohesive energy, pressure, bulk modulus, other elastic constants.**
- **Optimization under constraints using four routines: conjugate gradient, simulated annealing, differential evolution and Nelder Mead methods**
- **Fitting data includes ab initio estimates of cohesive energy, lattice constant and bulk modulus for various H-compositions. Also, experimental data for elastic constants from Schwarz et al.**
- **Characterization: heat of mixing, Gibbs free energy of mixing, elastic constants**

Success: new potential exhibits

(a) miscibility gap

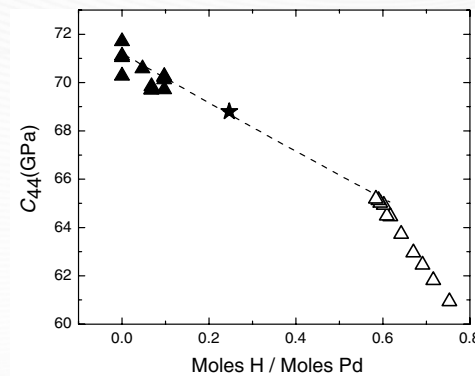
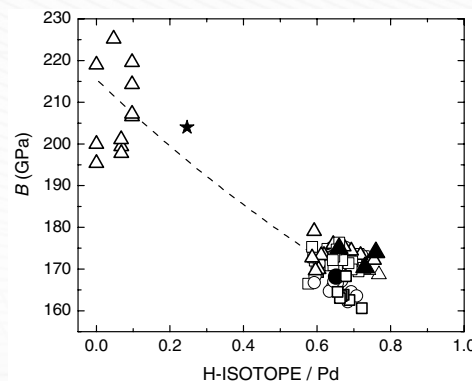
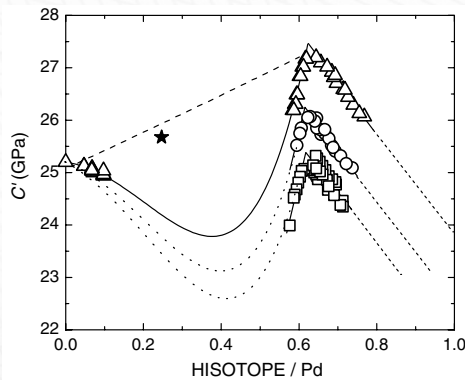
- Miscibility gap exists, cause phase separation into H-rich and H-poor regions (annealed at 300 K for 14,000,000 timesteps)
 - In experiments, α phase = $\text{PdH}_{0.03}$ and β phase = $\text{PdH}_{0.6}$
 - With the potential, α phase $\approx \text{PdH}_{0.00}$ and β phase $\approx \text{PdH}_{0.85}$



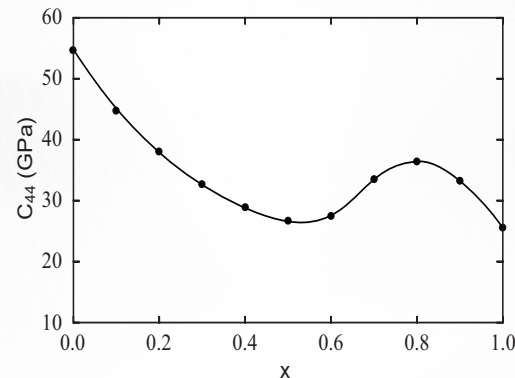
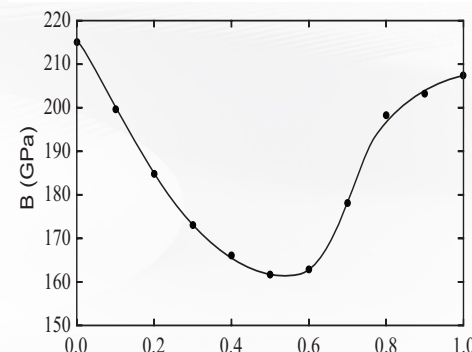
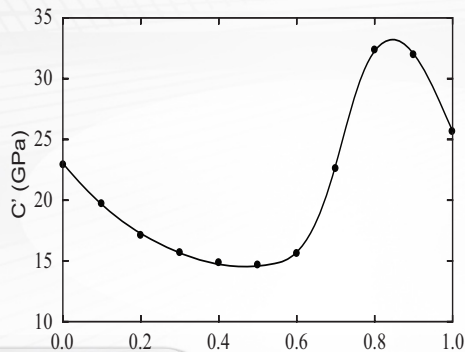
Elastic constants

(weakly used for potential fitting)

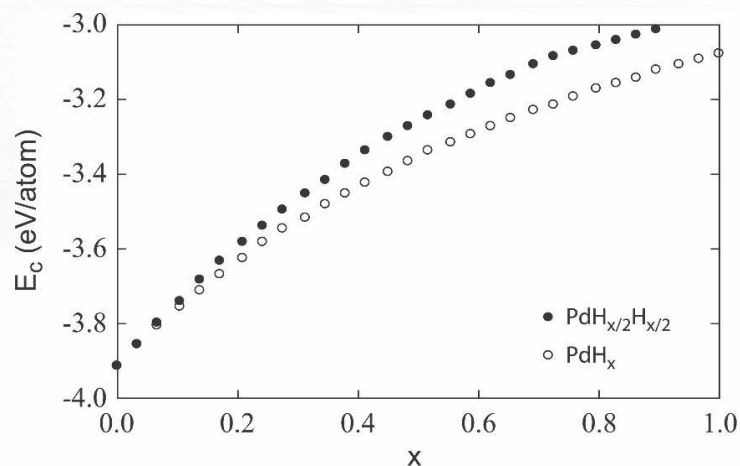
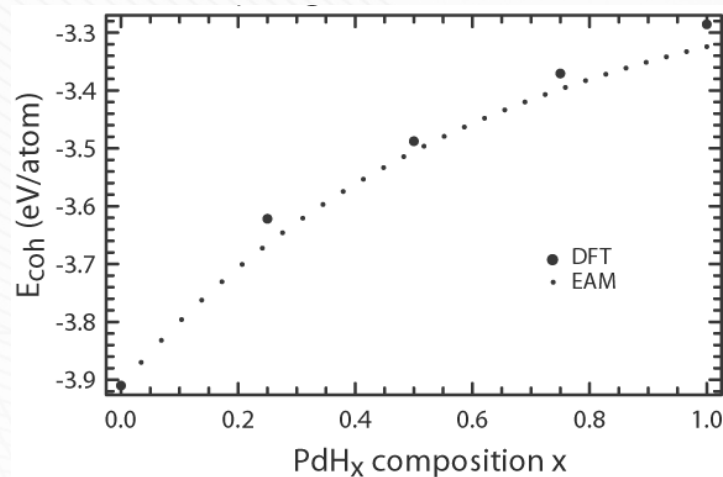
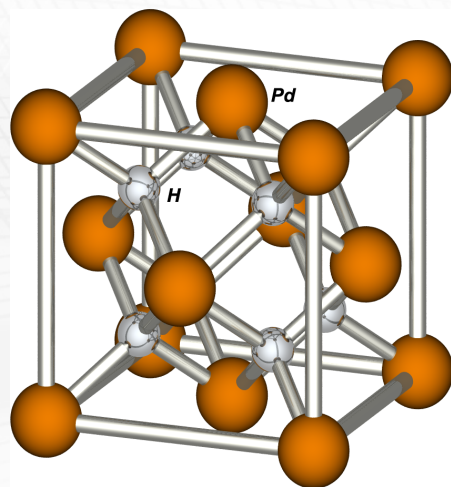
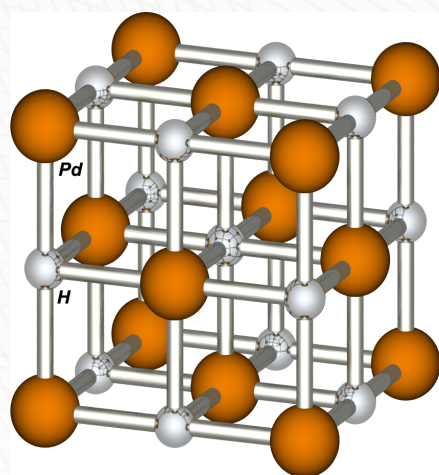
- Good qualitative agreement for C' ($= (C_{11} - C_{12})/2$).
- $B_\alpha \sim B_\beta$ and essentially flat for $0.82 \leq x \leq 1$.
- C_{44} shows a decreasing trend for $0.82 \leq x \leq 1$. Also, a line connecting the α and β regimes has a lower slope than for the high concentration region.



(R. Schwarz
et al, Acta
Mater, 2005)



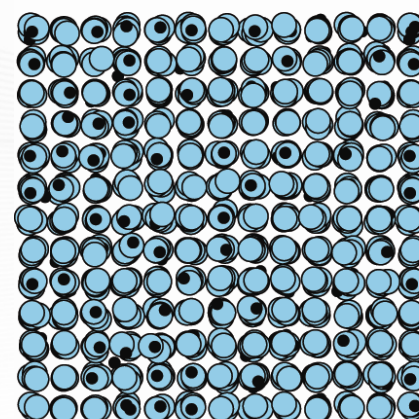
Octahedral site preferred at all H concentrations



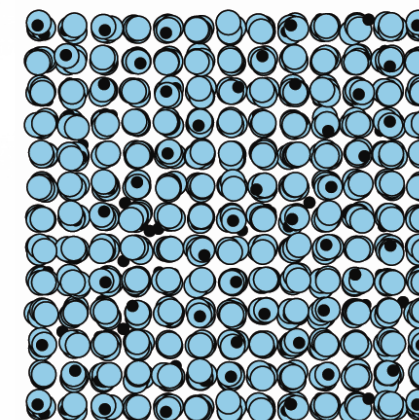
$PdH_{0.784}$ after 8 ps MD annealing at 300 K

● Pd ● H

octahedral initial H sites



tetrahedral initial H sites

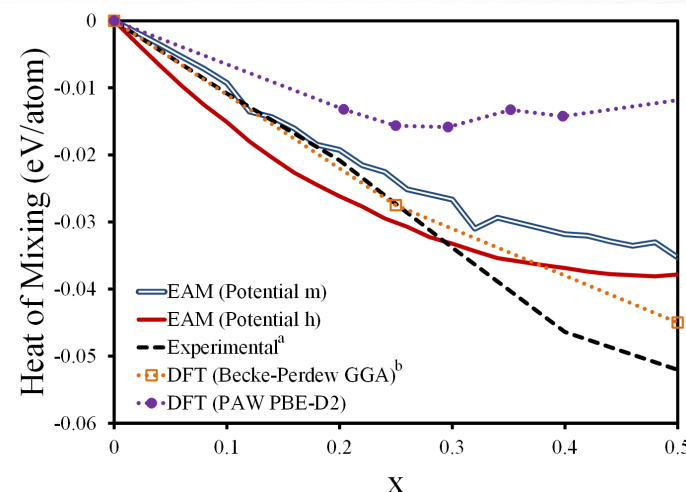
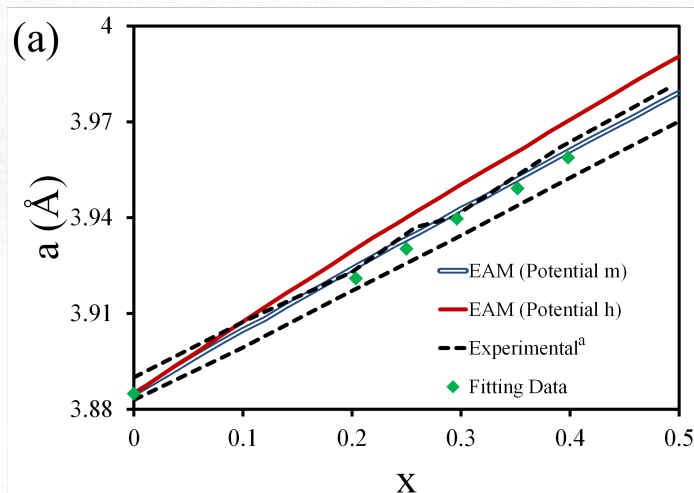


Pd-Ag-H potential development

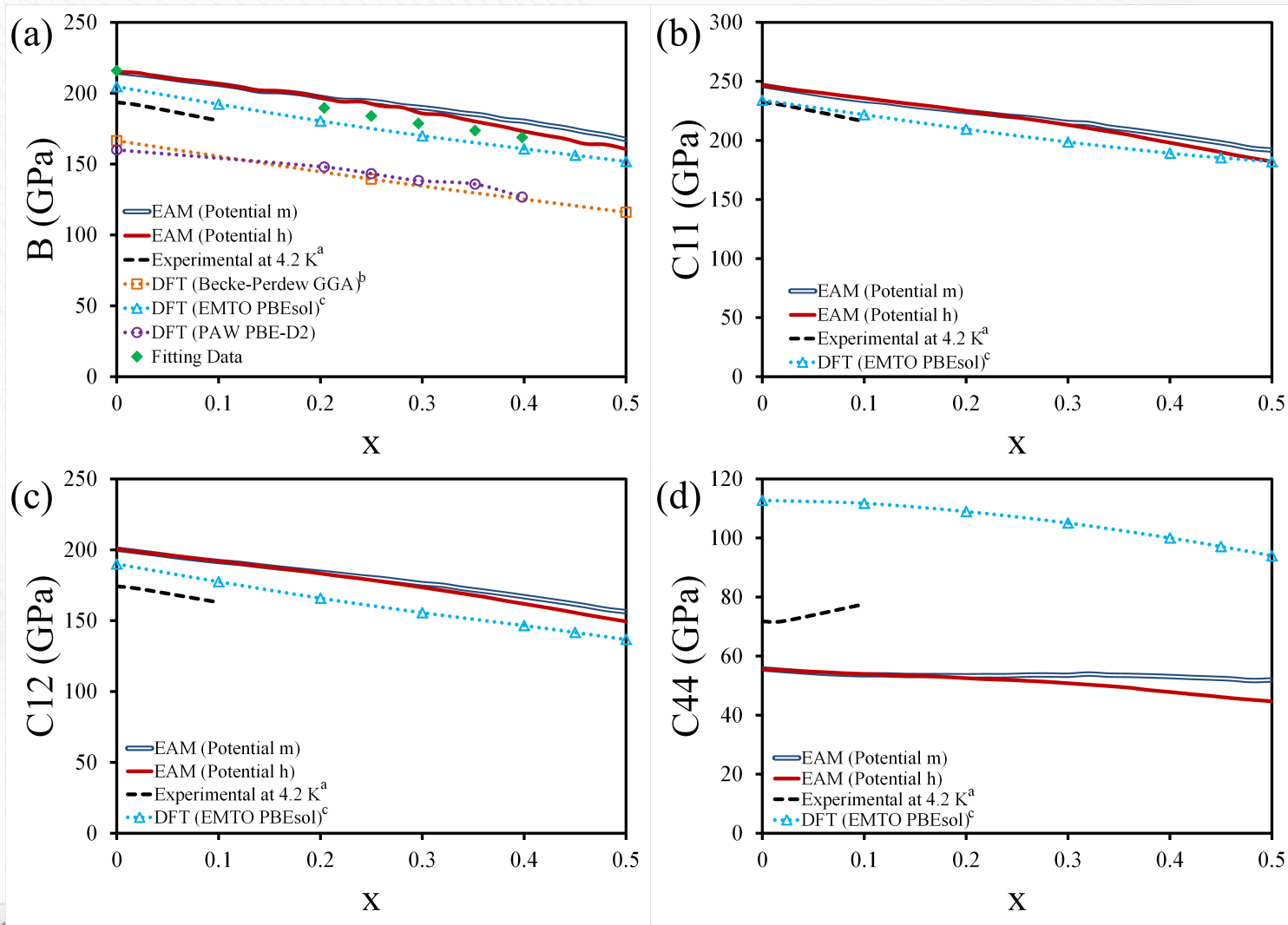
- Alloying palladium with another metal alters properties
 - Tensile and shear strengths (loop-punching and fracture pressures)
 - Maximum H concentrations (rate of He/M formation)
 - Miscibility gap (single or multiphase material)
- $\text{Pd}_x\text{Ag}_{1-x}$ alloys: not many experimental measurements on bulk properties
- Palladium and silver are completely solid soluble (no intermediate compounds, phase separations)
- Solubility of H into Ag is negligible
- H preferentially occupy interstitial sites near Pd.
Experiments on Pd-Au hydrides show an increase in occupied tetrahedral sites with increasing Au concentration
- Adding Ag reduces the miscibility gap, which disappears around 25-30% Ag

Modeling the Pd-Ag interaction

- Start with EAM potential by Williams *et al* (MSMSE, 2006) for Ag
- Pd-Ag interactions fitted using two different functional models (Morse-style (m) and Hybrid (h) of Pd-Pd and Ag-Ag)
- Fitting parameters determined such that properties of the potentials match with lattice parameter, a , and bulk modulus, B , obtained from DFT, and heat of mixing reported experimentally
- Smooth change in properties and favorable mixing results in solid solution

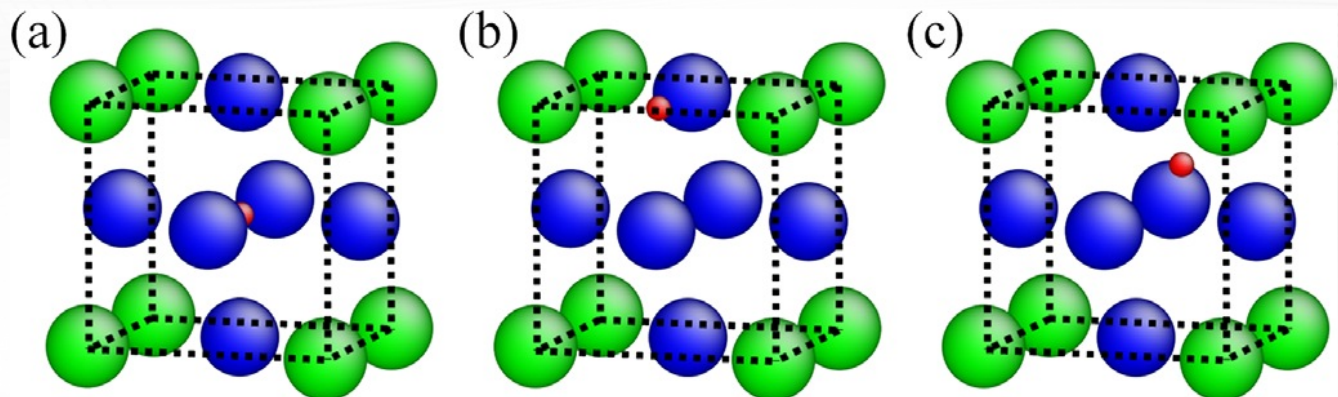


Pd-Ag elastic constants



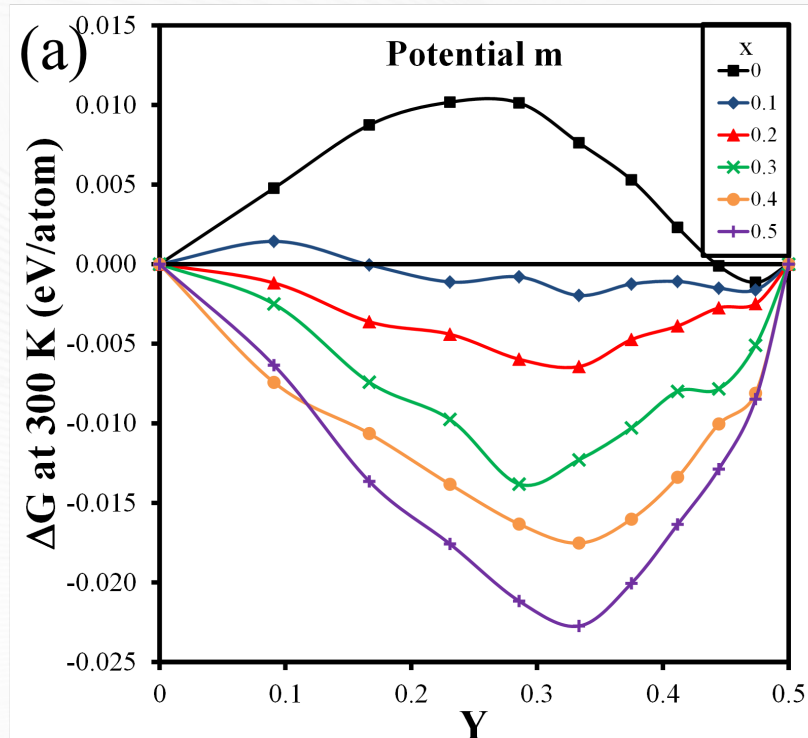
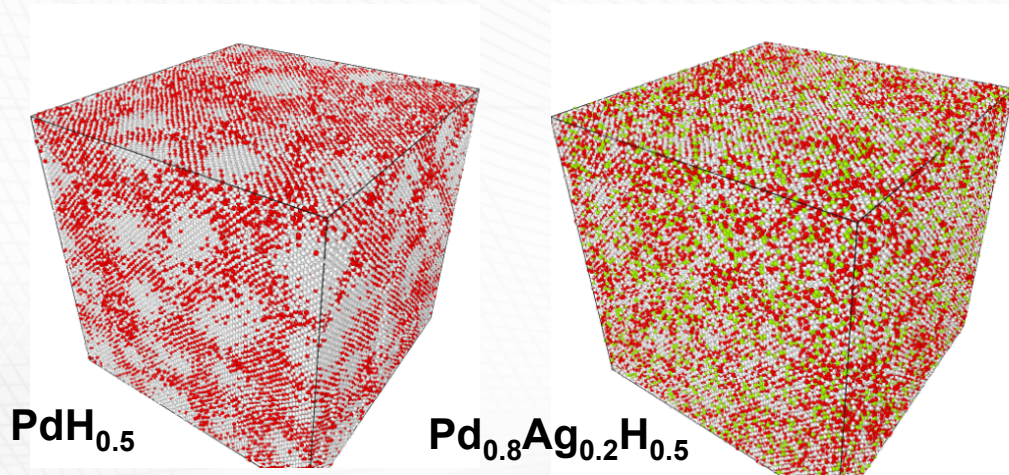
Modeling the Ag-H interaction

- Fitting to a broad range of compositions and bulk properties failed to capture the correct behaviors
 - Averaged system values good, but locally poor and crystallographically unstable
- Ideal Pd_3Ag systems with H added to both octahedral and tetrahedral sites
 - DFT to obtain relaxed structure and relative energy of that structure
 - Fit parameters such that EAM potential matches the DFT results



Addition of Ag removes miscibility gap

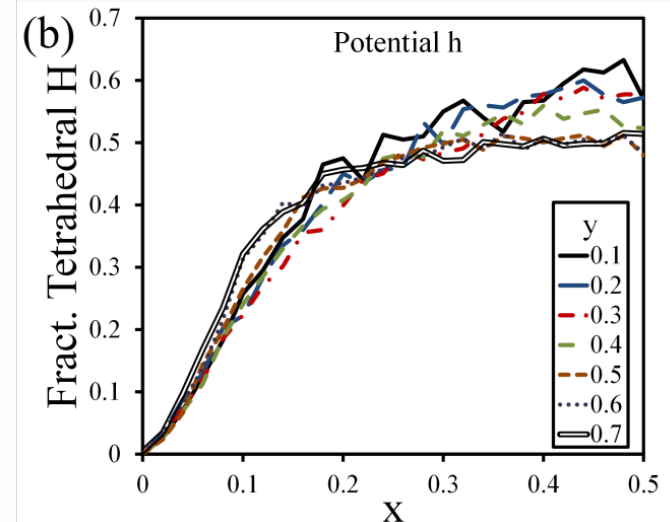
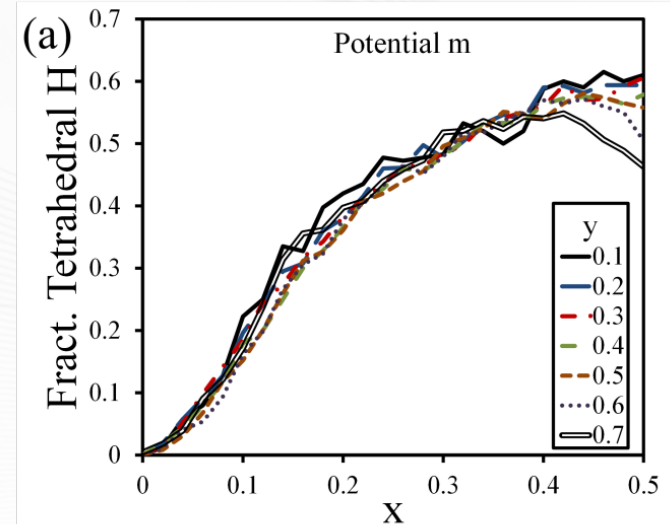
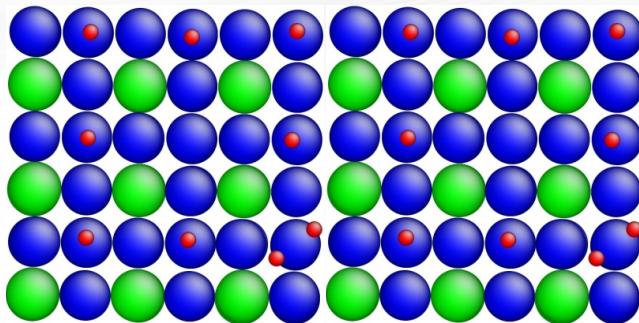
- Loss of miscibility gap noticed between 10% and 20% Ag.
- Experiments show this occurs in real systems at 25% Ag.



Examination of Gibbs free energy indicates that Morse-style (Pd-Ag) pair function may better represent the loss of the miscibility gap with increasing Ag content.

H interstitial occupancy depends on proximity to Pd atoms

- Occupancy of H in tetrahedral interstitial sites increases as %Ag increases, similar to neutron diffraction data for Pd-Au-D by Nanu *et al.* (*Acta Mater.*, 2008).
- H prefers sites near Pd atoms over Ag atoms; Increasing Ag limits favorable H octahedral interstitial sites
- H in tetrahedral sites increases with increasing Ag (like as seen for PdAuH)



Concluding remarks

- Improvement of potential requires additional measurements:
 - Elastic properties of Pd-Ag and Pd-Ag-H alloys
 - Neutron diffraction of Pd-Ag-H would provide a definitive answer on the hydrogen interstitial site occupancy
 - Additional ab initio calculations to investigate long-range interactions between Ag and H, vibrational entropy, and the energy and structure of defects in the hydrides.
 - Ab initio estimates of ideal tensile and shear strengths
- Publications:
 - Pd-H: Zhou *et al*, *J Mater Res*, 23(3), 704-718, 2008
 - Pd-Ag-H: Hale *et al*, *MSMSE*, 21, 045005, 2013
- Simulations performed with Sandia's LAMMPS code (<http://lammps.sandia.gov>).
- Questions? For further info: jzimmer@sandia.gov