

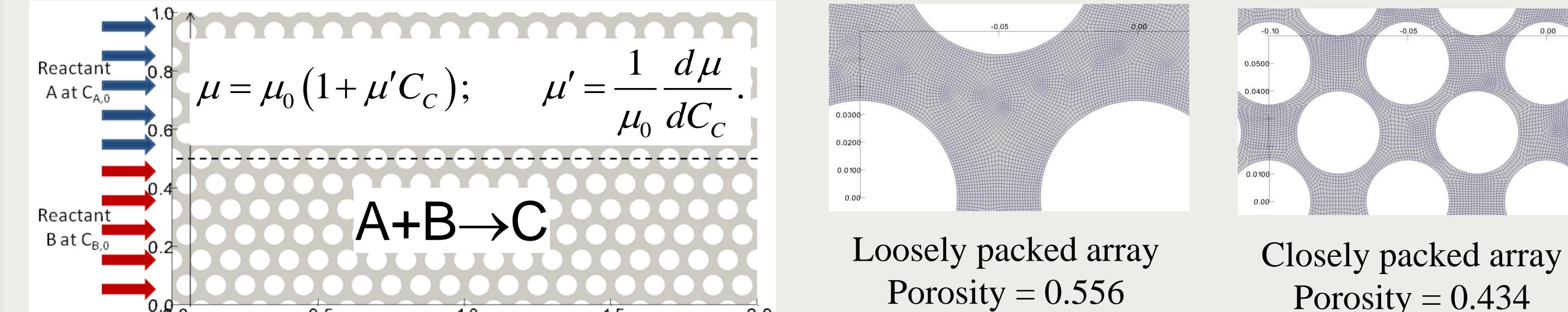
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## Overview

- Mixing-induced reacting flows in porous media can be used to develop subsurface flow for enhanced subsurface natural resource recovery and carbon sequestration
- In this work, we examine the case of reaction products that change the viscosity of the fluid to evaluate :
  - the impact of viscosity variations on mixing efficiency in porous media
- Computationally powerful & highly parallelized pore-scale model implemented in the SIERRA/ARIA finite element CFD code is used to examine:
  - flow in porous media with chemical reaction dependent viscosity

## Pore Scale Modeling

- Mixing-induced chemical reactions can alter fluid properties (viscosity and density), mixing efficiency, and shear rate for engineered solutions



$\mu$  is the viscosity of the solvent. Thickening ( $\mu' > 0$ ) and thinning ( $\mu' < 0$ ) viscosity with product concentration ( $C_c$ ) by bimolecular reaction

### Incompressible Navier-Stokes equation: Velocity ( $u$ ) at pore scale

#### Multicomponent Reactive Transport at pore scale

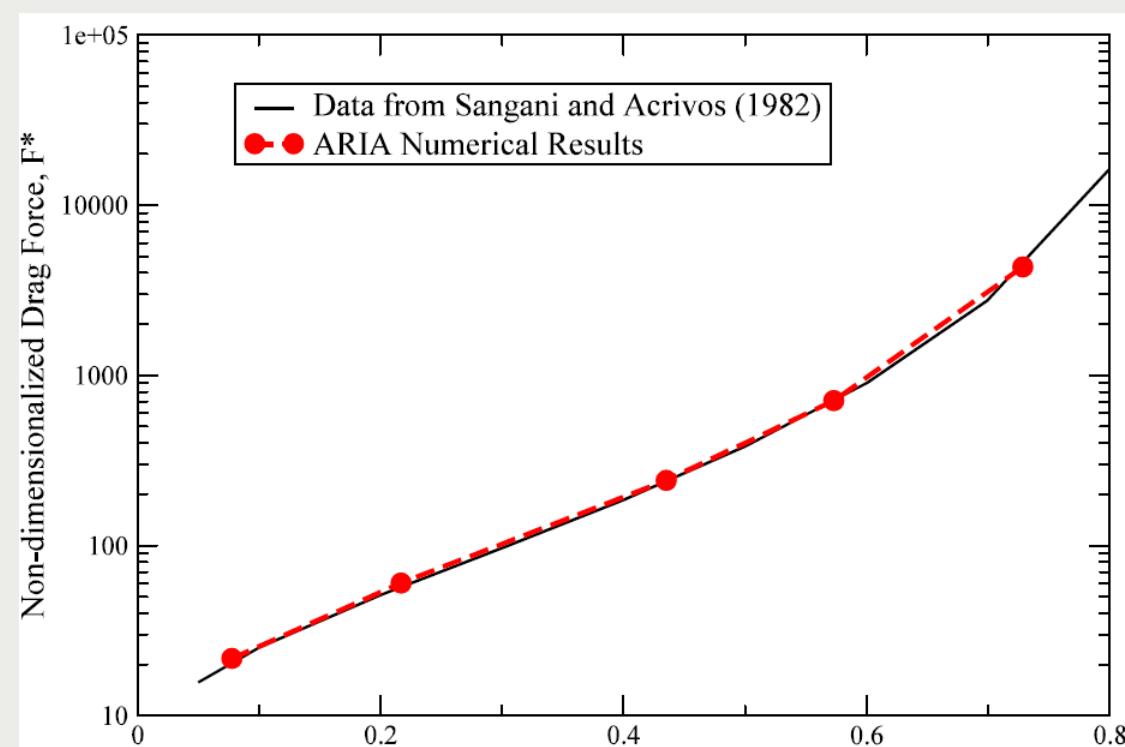
$$\begin{aligned} \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) C_A &= D_A \nabla^2 C_A - k C_A C_B \\ \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) C_B &= D_B \nabla^2 C_B - k C_A C_B \\ \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) C_C &= D_C \nabla^2 C_C + k C_A C_B \end{aligned} \quad \Rightarrow \quad \begin{aligned} \frac{\partial}{\partial t} + P e \mathbf{u} \cdot \nabla \right) C_A &= \delta_A \nabla^2 C_A - D_a c_A c_B \\ \frac{\partial}{\partial t} + P e \mathbf{u} \cdot \nabla \right) C_B &= \delta_B \nabla^2 C_B - D_a c_A c_B \\ \frac{\partial}{\partial t} + P e \mathbf{u} \cdot \nabla \right) C_C &= \nabla^2 c_C + D_a c_A c_B \end{aligned}$$

$$P e = \frac{U l}{D_C} \quad D_a = \frac{k c_{A,0} l^2}{D_C} \quad \delta_A = D_A / D_C \quad \delta_B = D_B / D_C$$

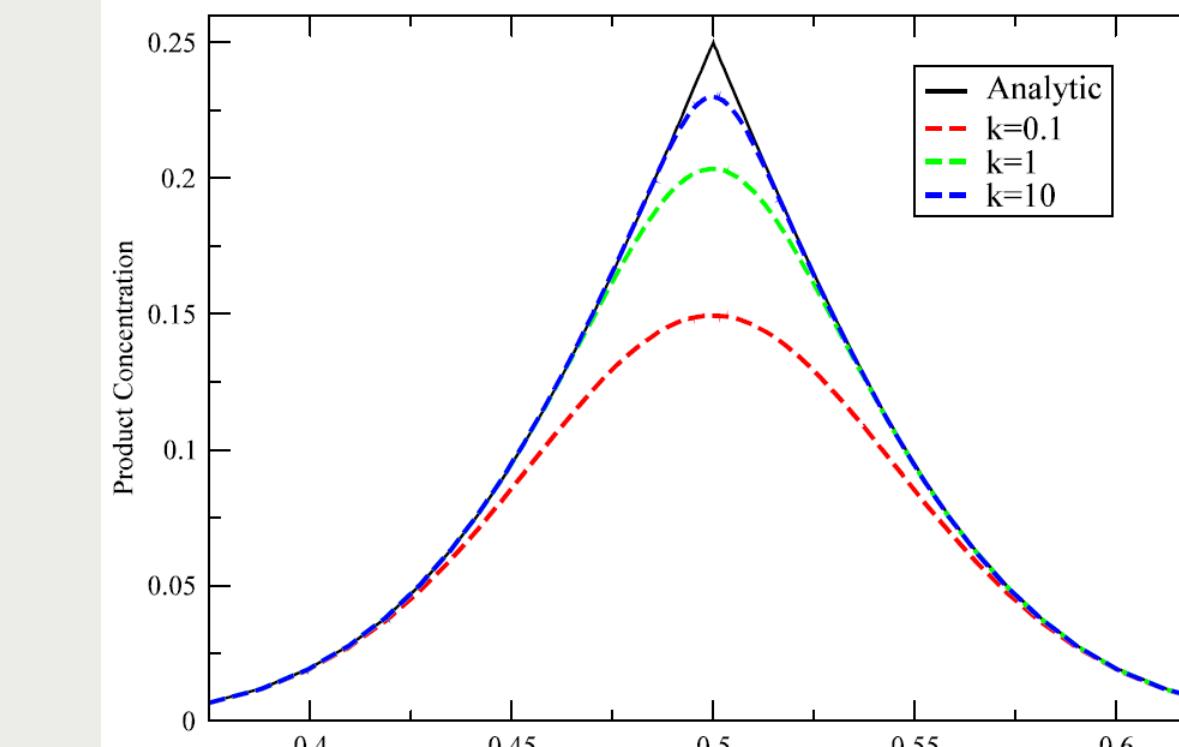
#### Fluid Viscosity Update

$$\bar{\mu} = \mu / \mu_0 = 1 + \bar{\mu}' c_c \quad \bar{\mu}' = \frac{C_{A,0}}{\mu_0} \frac{d\mu}{dC_c}$$

#### Drag force on an array of cylinders



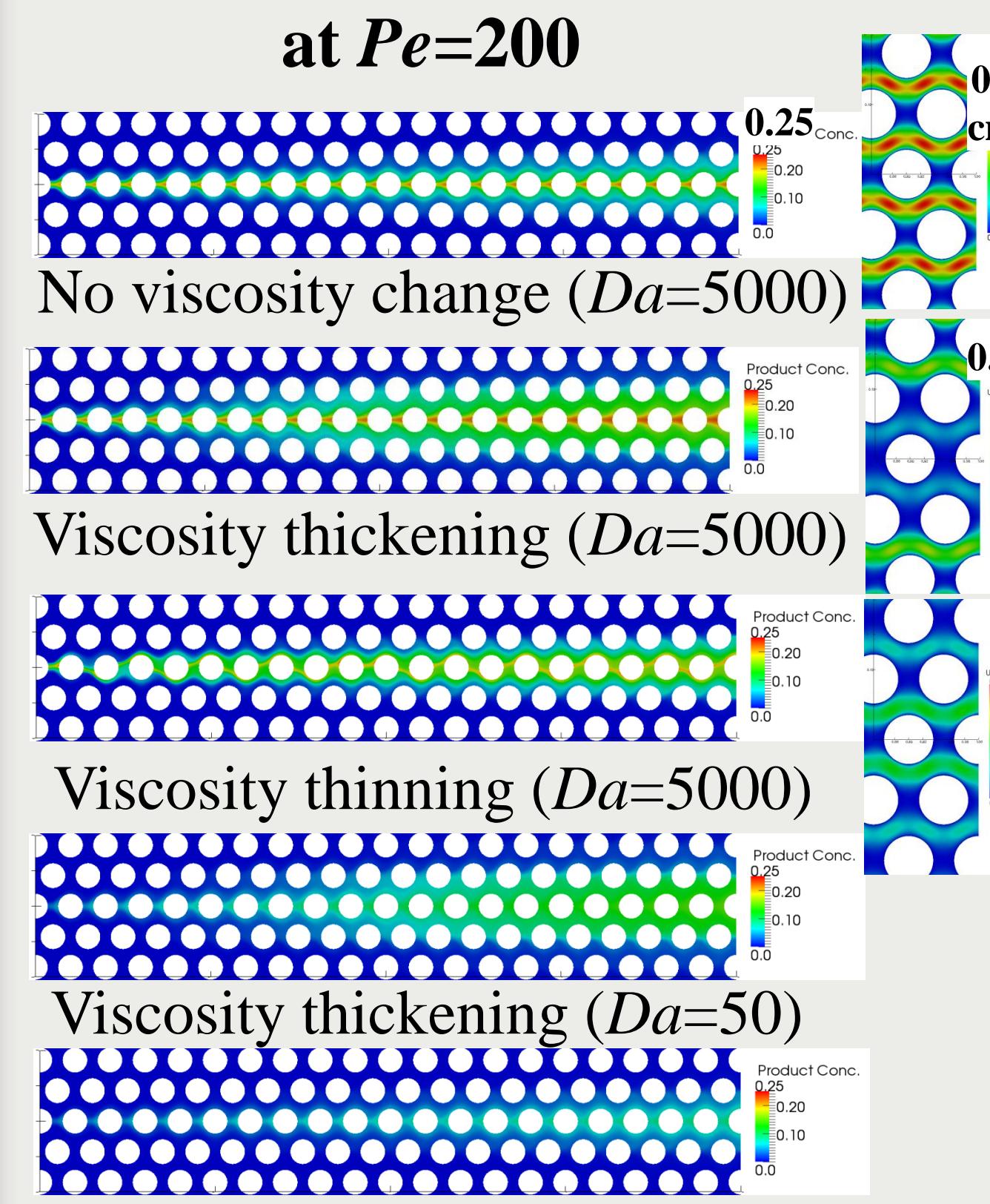
#### Reaction along a transverse mixing zone with constant viscosity



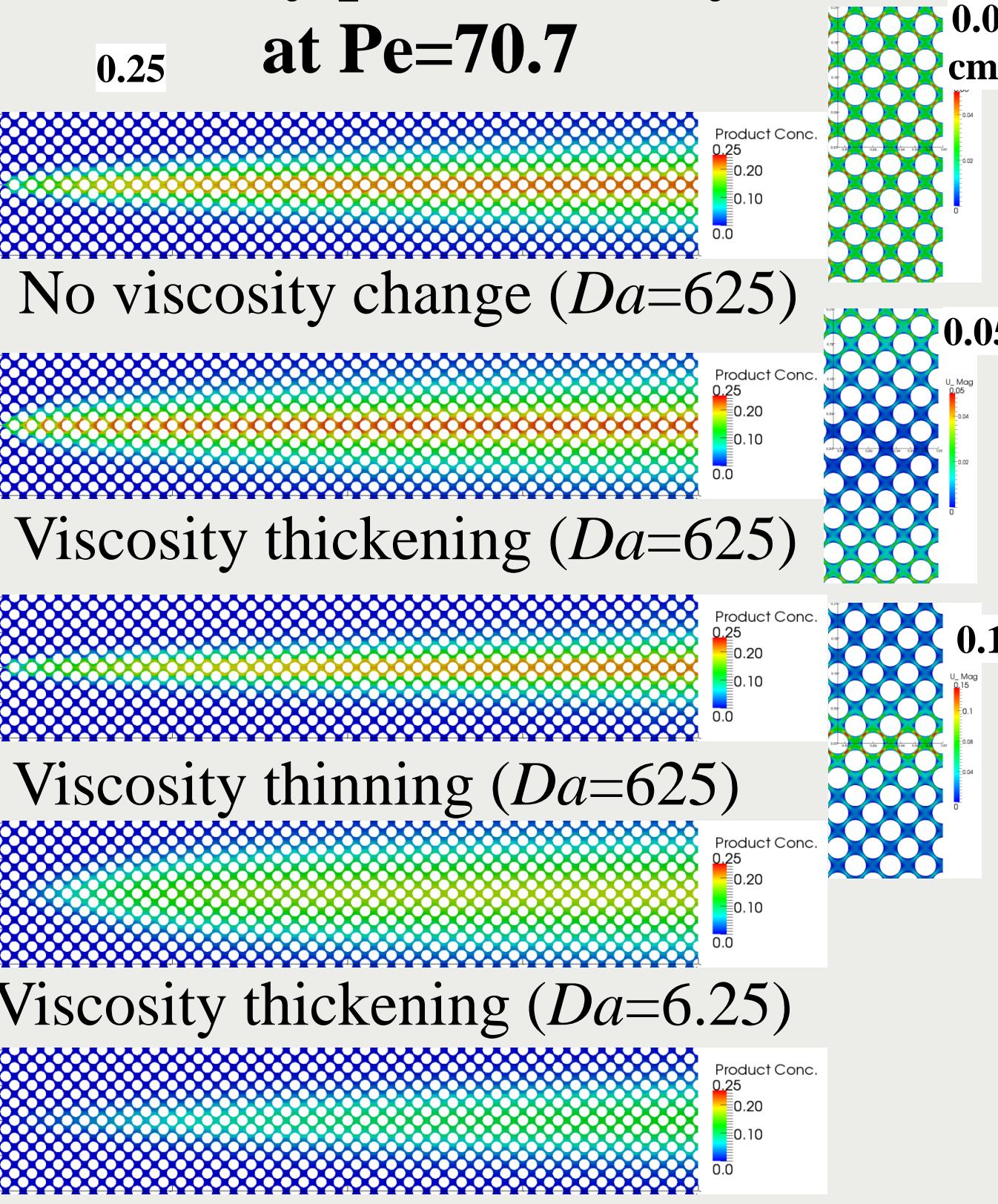
## Pore Scale Modeling Results

### Product concentration and flow velocity change

#### Loosely packed array at $Pe=200$

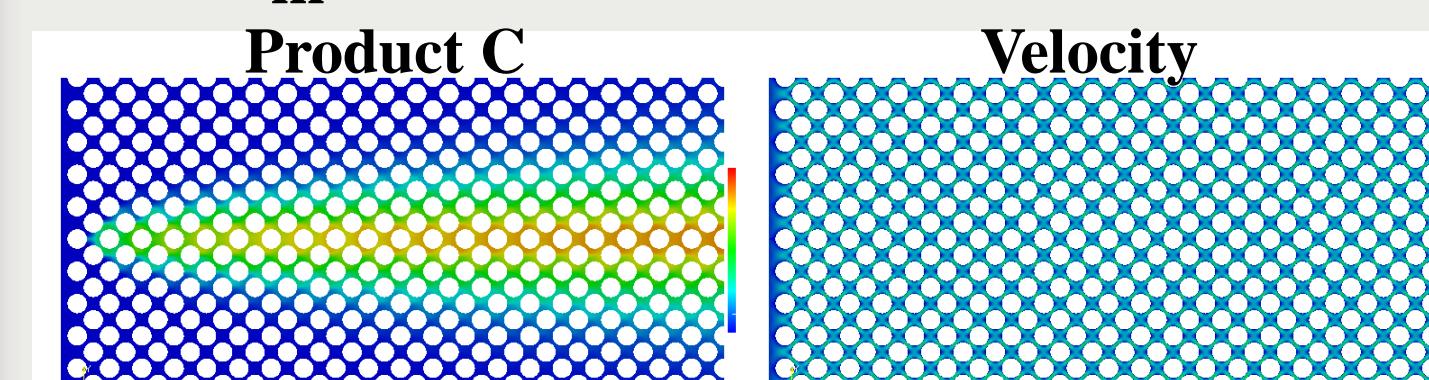


#### Closely packed array at $Pe=70.7$

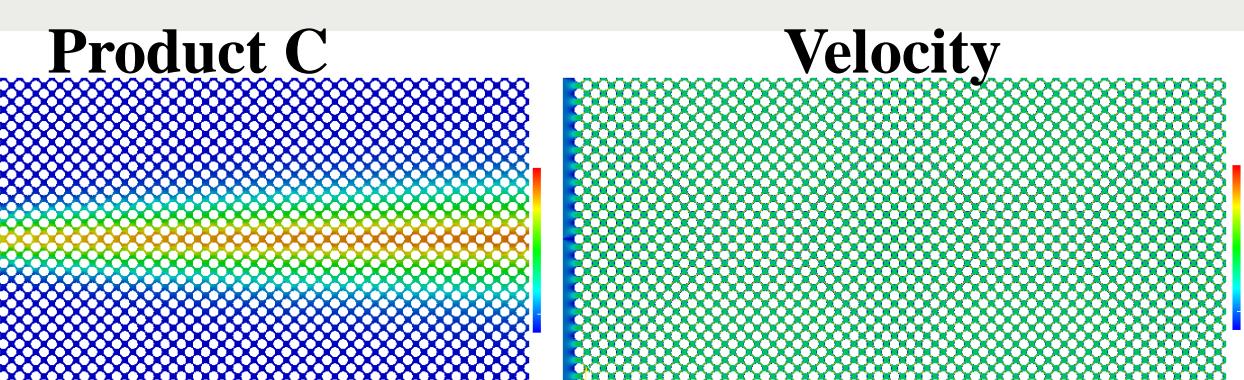


$Pe=7$  &  $Da=62.5$

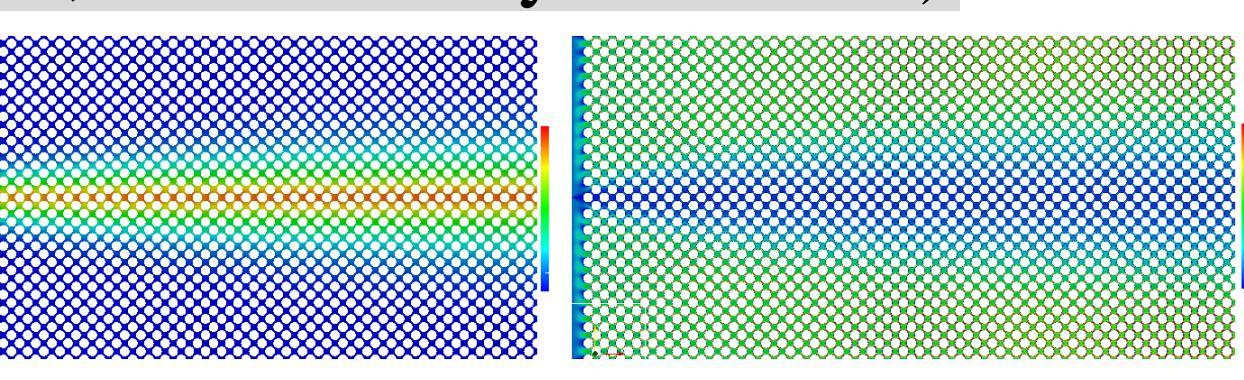
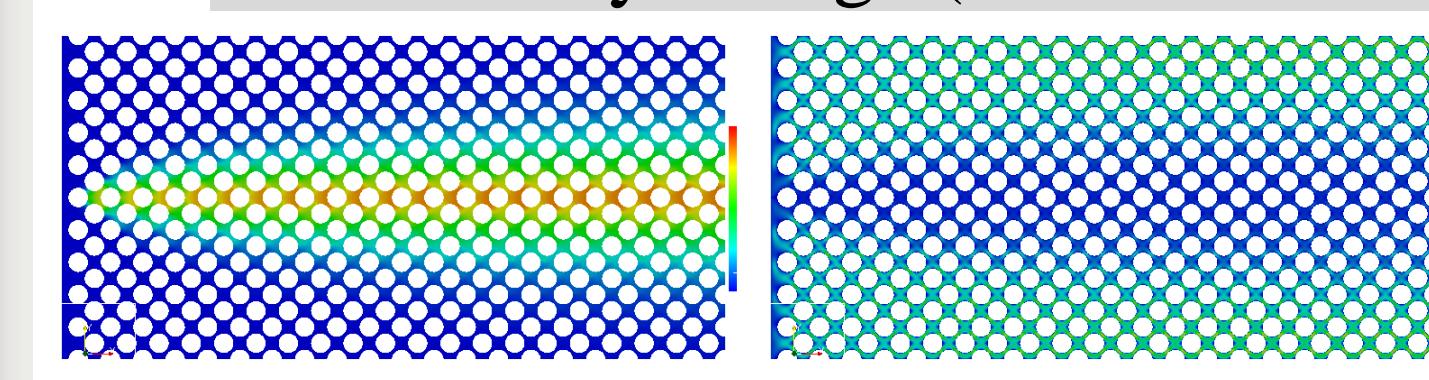
$U_{in}=0.01\text{cm/s}$  &  $k=2.5\text{s}^{-1}$



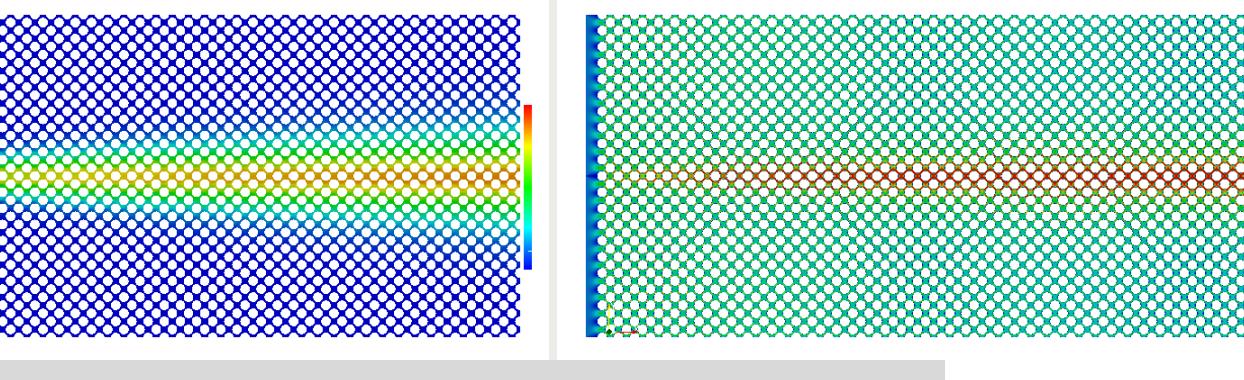
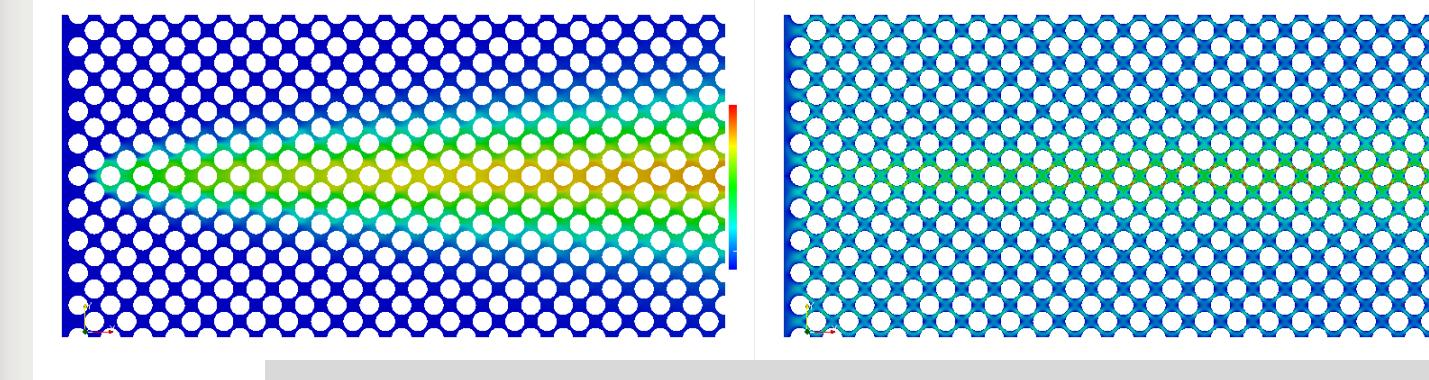
$U_{in}=0.02\text{cm/s}$  &  $k=10\text{s}^{-1}$



No viscosity change (Max. Product C=0.25; Max velocity=0.15cm/s)



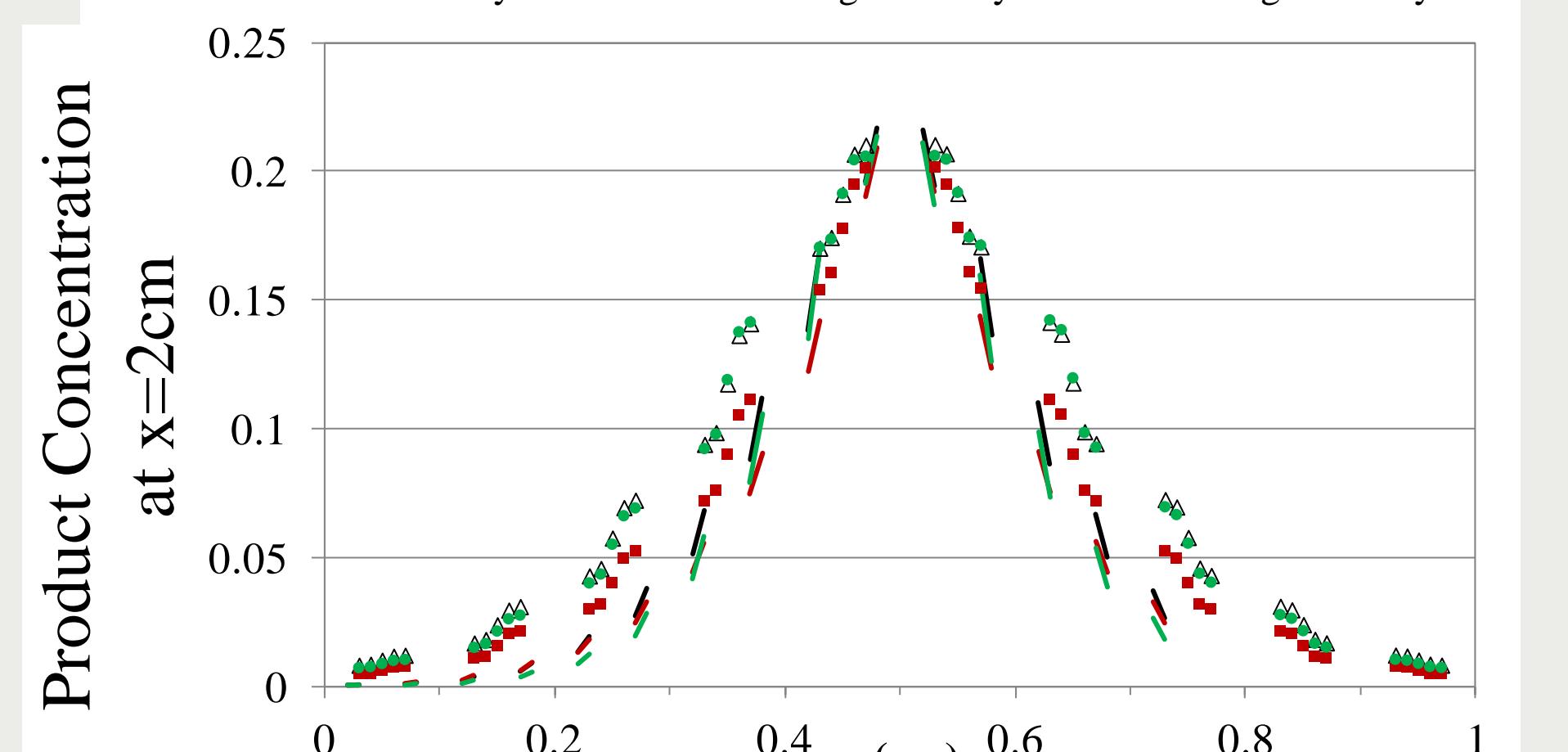
Viscosity thickening (Max. Product C=0.25; Max velocity=0.15cm/s)



Viscosity thinning (Max. Product C=0.25; Max velocity=0.15cm/s)

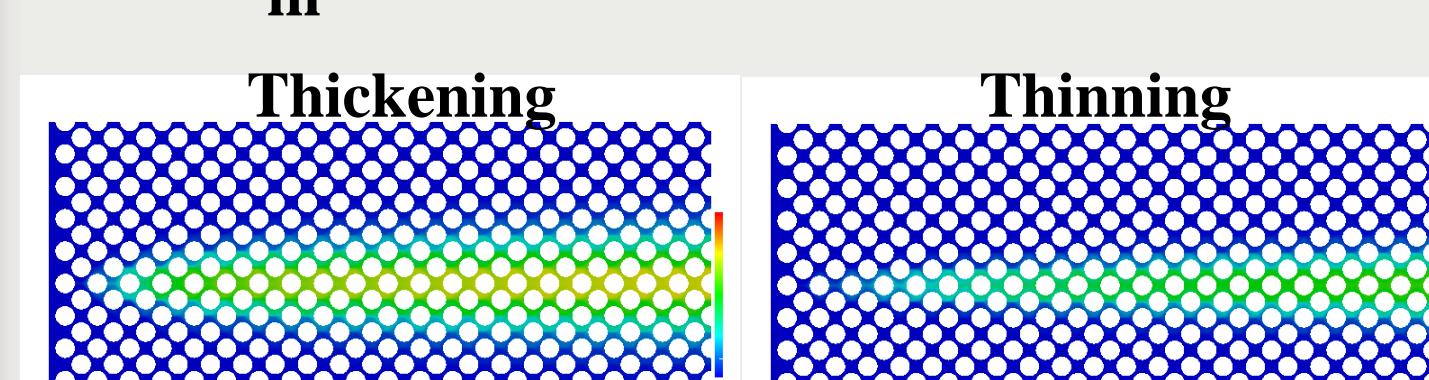
Symbol: loosely packed array △: Constant Viscosity Line: closely packed array —: Constant Viscosity

— Thickening Viscosity — Thickening Viscosity ● Thinning Viscosity ● Thinning Viscosity

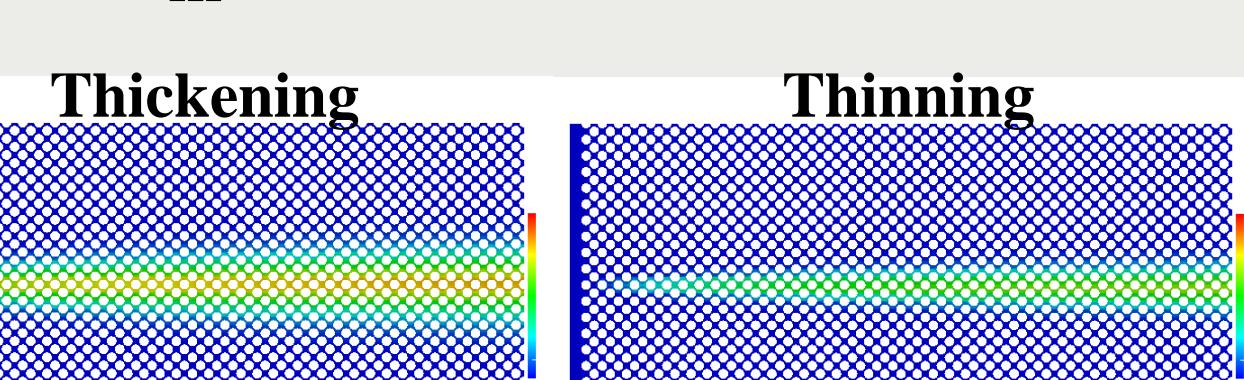


$Pe=70$  &  $Da=62.5$

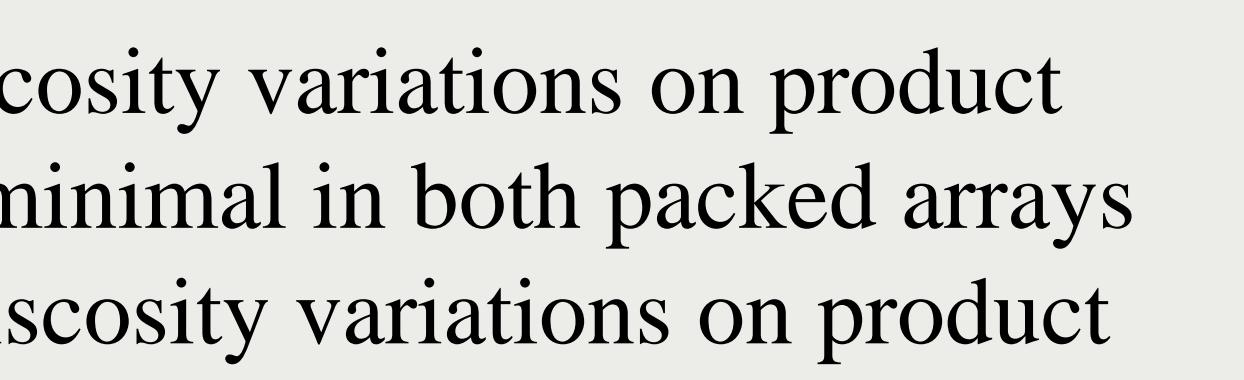
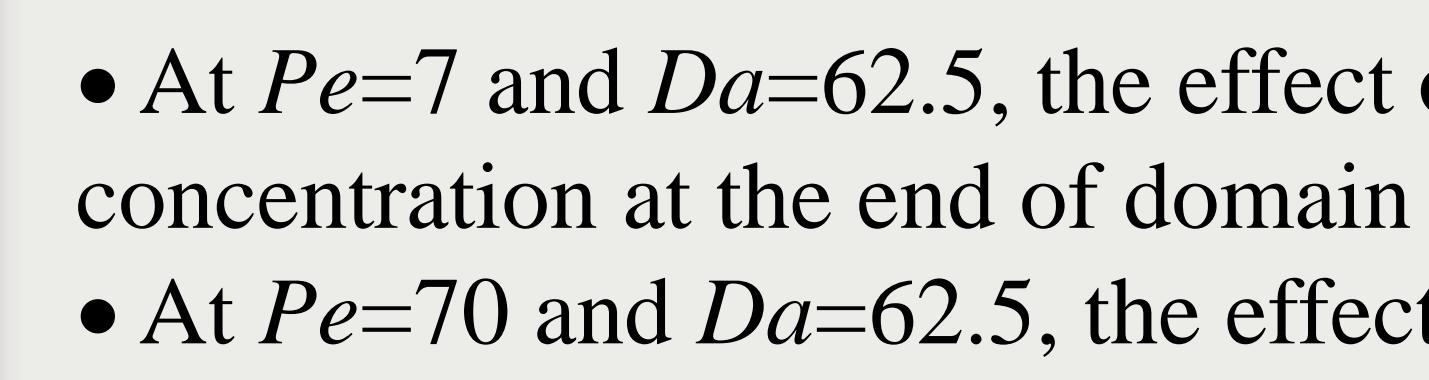
$U_{in}=0.01\text{cm/s}$  &  $k=0.25\text{s}^{-1}$



$U_{in}=0.02\text{cm/s}$  &  $k=1\text{s}^{-1}$



Thickening



Thinning

• At  $Pe=7$  and  $Da=62.5$ , the effect of viscosity variations on product concentration at the end of domain was minimal in both packed arrays

• At  $Pe=70$  and  $Da=62.5$ , the effect of viscosity variations on product concentration is significant in both packed arrays

• This comparison shows that at a moderate  $Da$  (62.5) a case with the lower  $Pe$  has more significant dependence of the overall reaction rate on  $Pe$ . A range of  $Da$  and  $Pe$  values need to be tested.

• Pore scale model with high performance computing capability will be used to test experimental results with emulsion-stabilizing nanoparticles in order to find optimal delivery of engineered solutions under a variety of pore-geometry conditions

References: • Davison, S. M., H. Yoon, and M. J. Martinez, 2012, Pore scale analysis of the impact of mixing-induced reaction on viscosity variations, *Advances in Water Resources*, 38, 70-80.