



## Pulse shaping techniques with nested wire arrays

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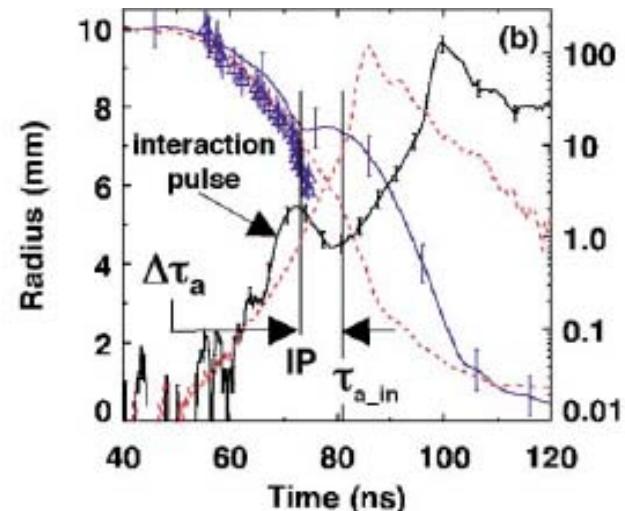
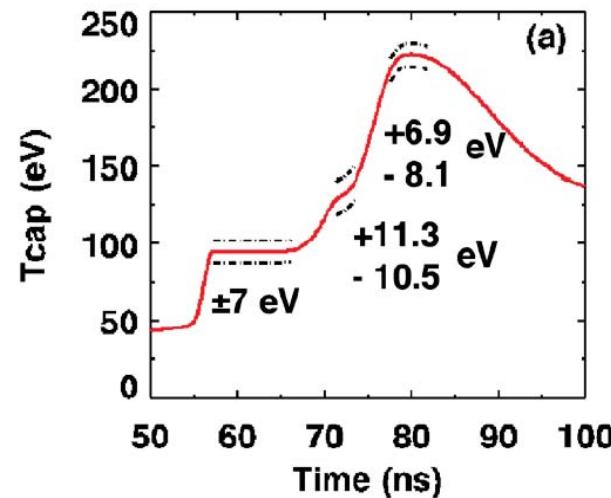
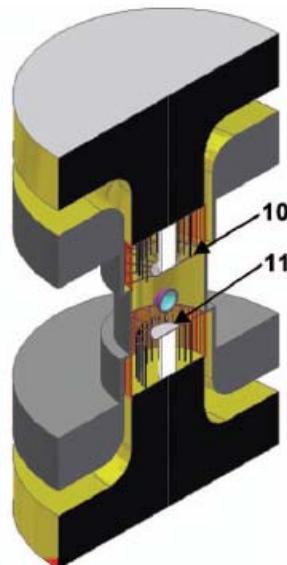
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## Pulse shaping is vital to z-pinch ICF concepts



- Three or more controlled x-ray pulses are required in order to heat a fusion capsule
- One suitable pre-pulse is observed as the imploding outer array of two nested arrays interacts with the inner array, however detailed physical mechanism of the interaction pulse is not fully understood
- Necessary to broaden main pulse (and interaction pulse)
  - nested arrays on Z are *too good* at temporal compression
- Gaining energy in the main pulse useful for both ICF and RES

Images reproduced from  
M.E. Cuneo et al. Phys Plas 13 056318, 2006



# This talk will use MAGPIE data to help understand / interpret Z data

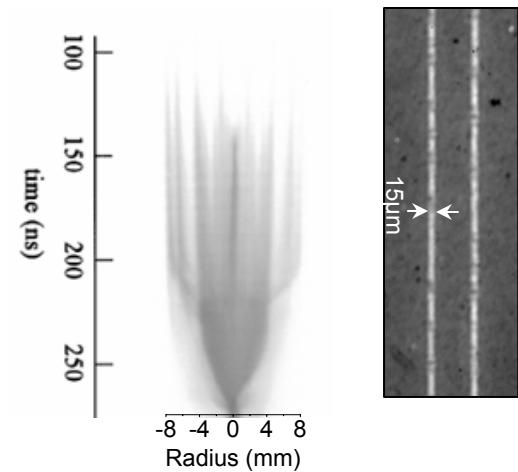
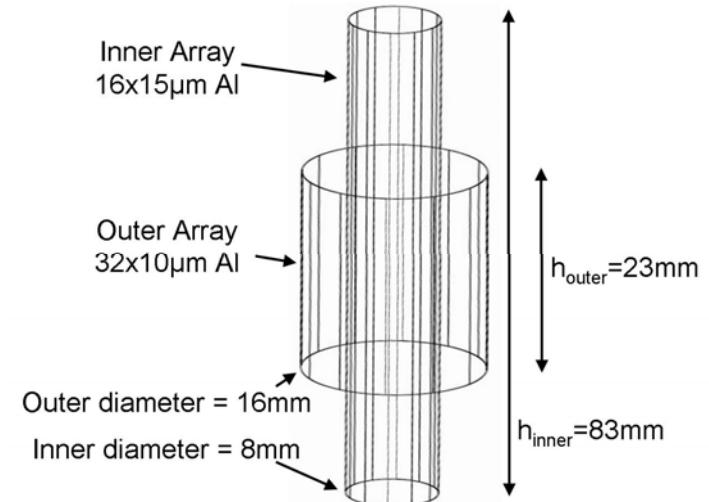
## Aims:

- Understand our present pulse shaping capability
  - New understanding of mechanism possibly responsible for interaction pulse
- New tools in the pulse-shaping toolbox
  - Look at what conical nested can bring to pulse shaping
- Measures that might increase efficiency of arrays
  - Discuss planned experiments to study elimination of cathode bubble
  - Possible applications to RES, Vacuum & Dynamic Hohlraum

1MA experiments can be used to understand 20MA experiments if careful consideration given to getting appropriate setup and being aware of differences

## Nested wire arrays on MAGPIE use high inductance inner to suppress current through the inner array to be similar to Z

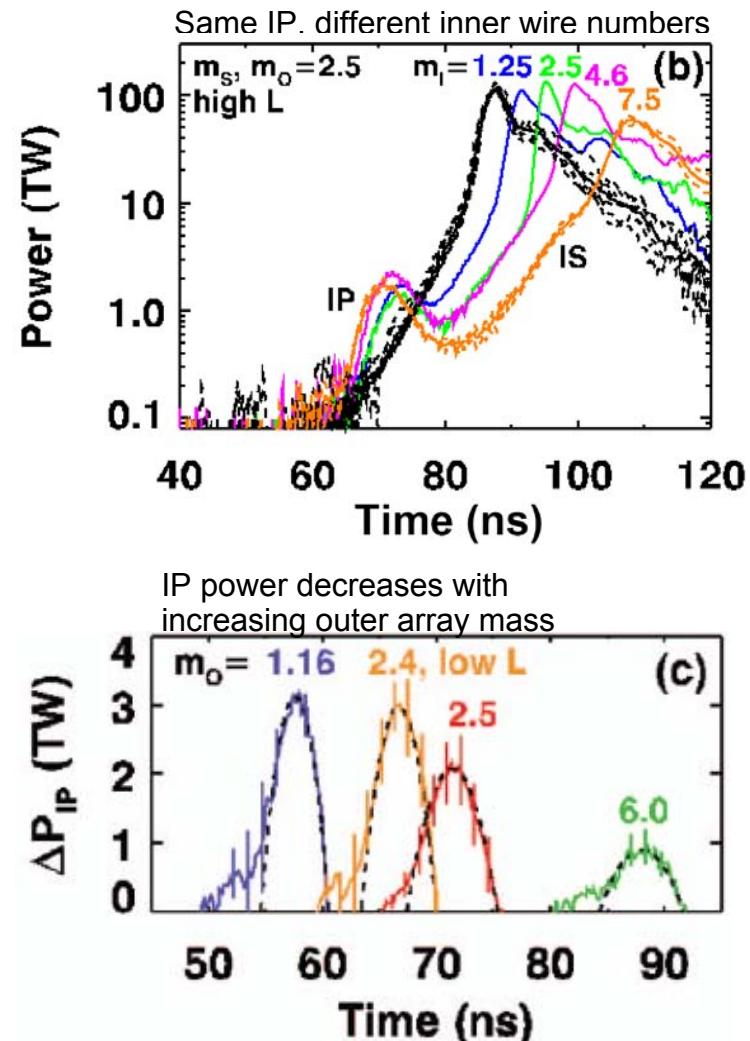
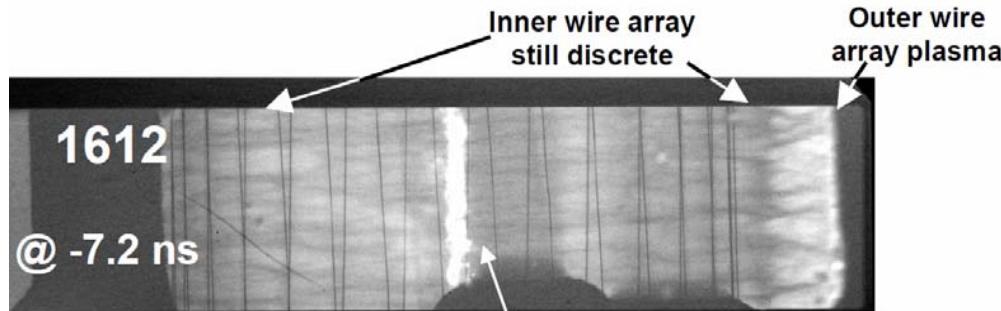
- High wire number in outer at 20MA leads to  
Inductive contrast:  $L_{\text{outer}} \ll L_{\text{inner}}$   
e.g. Cuneo et al PRL 94, 225003 (2005)
- High wire number not possible at  $\sim 1\text{MA}$
- Array design can give same inductive contrast  
(by lengthening inner)  
Lebedev et al. PRL 84, 1708 (2000)
- Negligible inner current confirmed by
  - Radial optical streak
  - X-pinch radiography
  - B-dot probes
- Present experiments use
  - Outer array 16-32 x 10 $\mu\text{m}$  Al 5056 at 16mm
  - Inner array 16 wire Al, W or CH at 8mm





## Interaction pulse on Z is critical for pulse shaping, but remains a puzzle

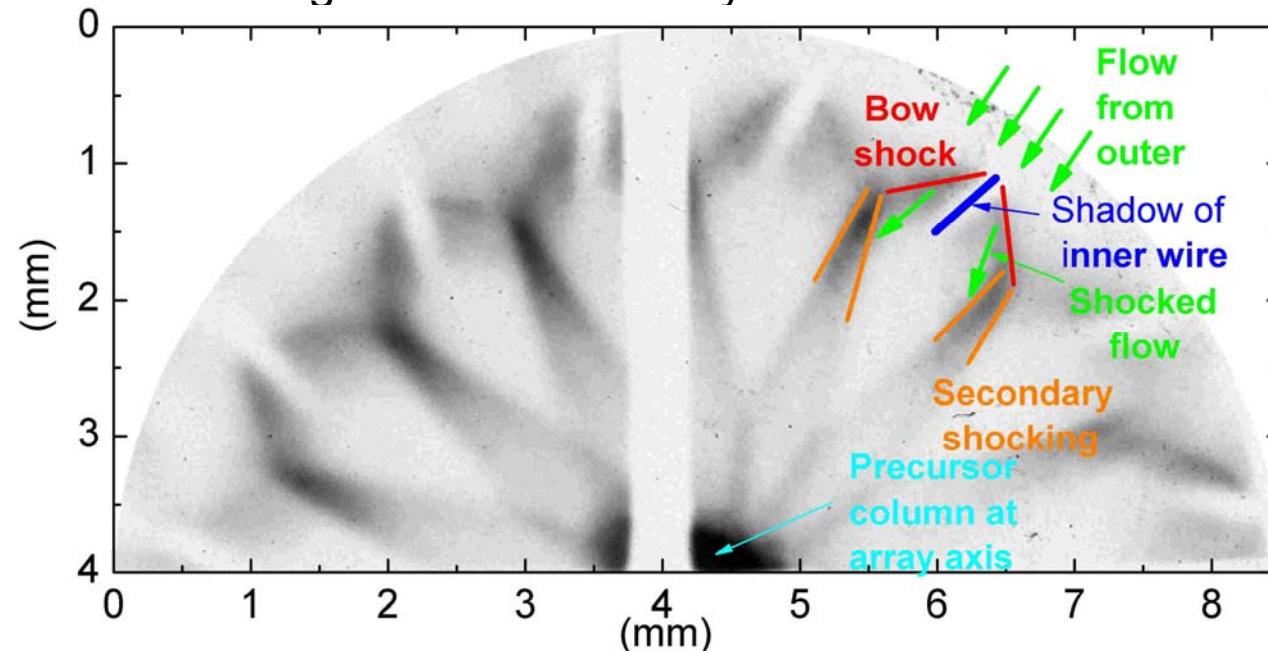
- Interaction energy measured is less than that predicted from hydrodynamic collision of outer and inner shells
- Nested arrays on Z now recognized to operate in a transparent mode
- Partial transparency cannot explain same power for different inner wire numbers
- Alternative models (e.g. ohmic heating, possibly by flux compression), do not recreate dependency on outer array mass, or explain small cores prior to interaction



Plots reproduced from  
M.E. Cuneo *et al.* Phys Plas 13, 056318, 2006

## Ablation streams from outer array are supersonic and will shock on the inner array

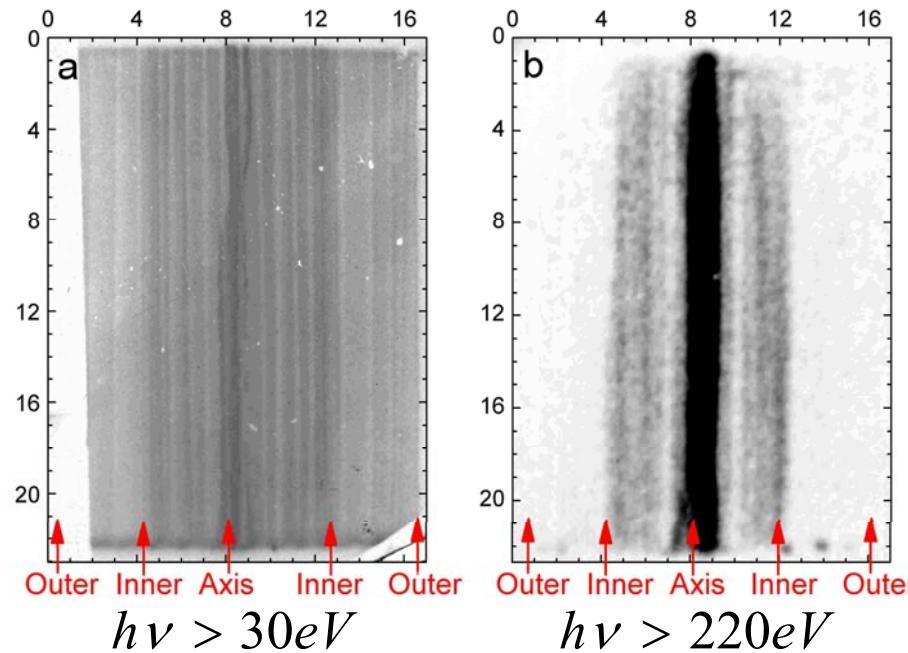
- Precursor plasma flows from outer array are supersonic at position of inner array:
  - MAGPIE (from spectra):  $T_e \sim 40\text{eV}$ ,  $Z \sim 6$     $c_s \sim 3\text{cm}/\mu\text{s}$     $M \sim 5$
  - Z (from MHD):  $T_e \sim 25\text{eV}$ ,  $Z \sim 11$     $c_s \sim 1.3\text{cm}/\mu\text{s}$     $M > 11$
- At reaching the inner array the precursor flow will be shocked
  - end-on XUV image inside inner array on MAGPIE



- Define angle  $\beta$  as angle between initial precursor flow and shock

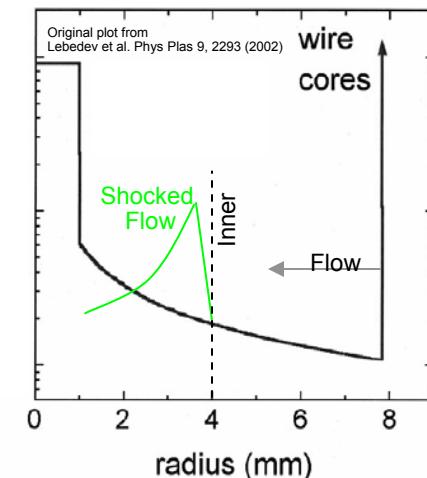
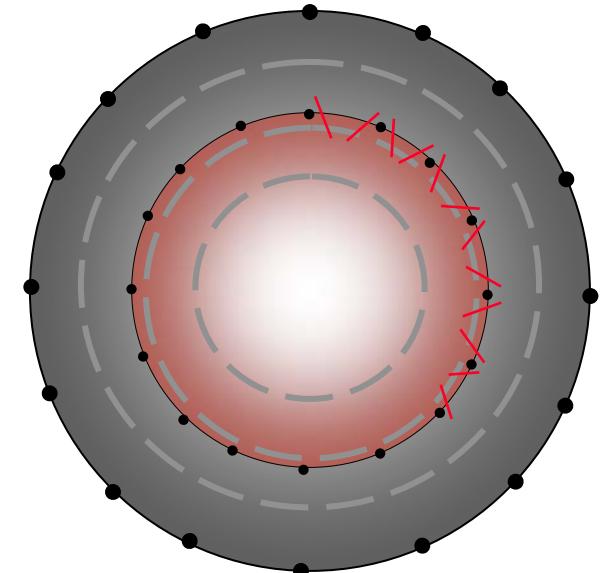
# Shock will perturb plasma conditions in streams as they pass inner

- Perpendicular component of stream velocity will be reduced across shock
 
$$\frac{v_{\perp sh}}{v_{\perp abl}} = \frac{1}{\eta} = \frac{M_{\perp}^2(\gamma - 1) + 2}{M_{\perp}^2(\gamma + 1)} \sim 0.14$$
- Density will be increased by the compression ratio  $\eta$
- Temperature of streams will also be increased
- Temperature and/or density jumps inferred from side-on emission imaging during ablation process
  - Definite change in plasma conditions near inner array, despite ‘transparency’ :



## Perturbing the pre-fill will effect the snowplow

- For single array snowplow of pre-fill by implosion results in emission
- Power radiated by snowplow emission is
  - $P_{SP} \propto \rho(r,t) (v_{piston} - v_{prefill})^3$
- Comparing nested with single,  $\rho$  and  $v_{prefill}$  both altered by jump conditions
- Modifications act to enhance snowplow emission.
- Can adapt a snowplow model to incorporate these jumps



# Snowplow model for perturbed system predicts enhanced emission above that of a single array

Variable	MAGPIE
$v_{abl}(cm/\mu s)$ [1, 2]	15 (Ablation velocity)
$c_s(cm/\mu s)$ [2-4]	3 (Sound speed)
$\beta$ (end-on image)	39° (Shock angle)
$\gamma$ [5]	1.1 (Adiabatic index)
$M_{\perp} = \frac{v_a \sin(\beta)}{c_s}$	3.4 (Mach numb perp)
$\eta = \frac{v_{abl}}{v_{sh}}$	7.7 (Compression)

[1] S. V. Lebedev et al., *Plas. Phys. Contr. Fus.* 47, A91 (2005).

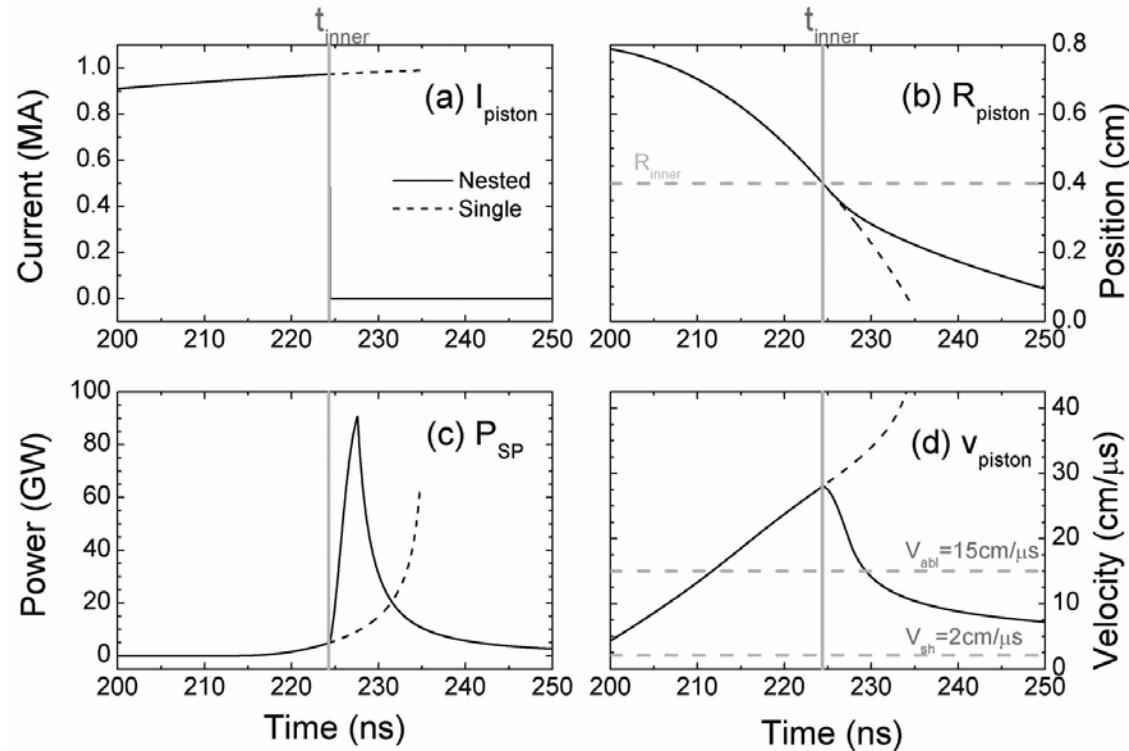
[3] S. V. Lebedev et al., *Laser Particle Beams* 19, 355 (2001).

[4] J. P. Chittenden et al., *Phys. Plasmas* 8, 675 (2001).

[5] R. P. Drake, *High Energy Density Physics* (Springer, 2006).

## Model setup

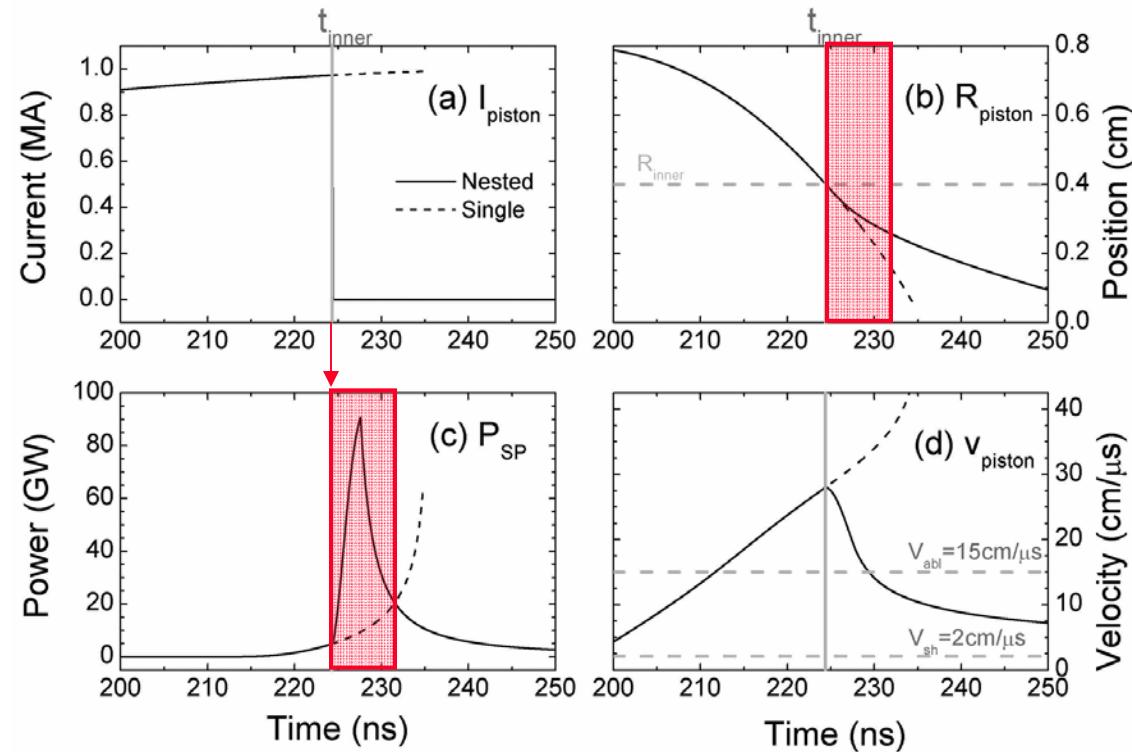
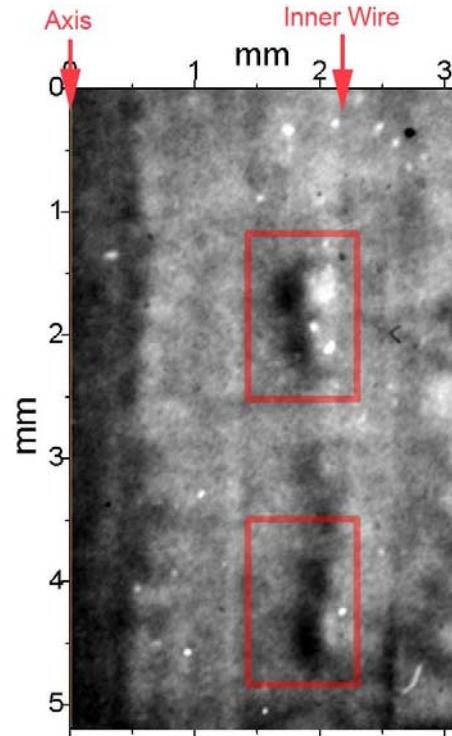
- Ablation model for fill
- Jump conditions at inner
- Snowplow model for implosion trajectory



## Results of model

- Snowplow model shows excess emission despite current being switched out of piston prior to experiencing perturbed density
- Excess emission is AFTER piston passes inner wires (in shocked region)
- Experiments show that piston slows below ablation velocity, despite 100% transparency
- Averaging emission over total MAGPIE array smoothes out interaction pulse due to azimuthal and axial non-uniformities

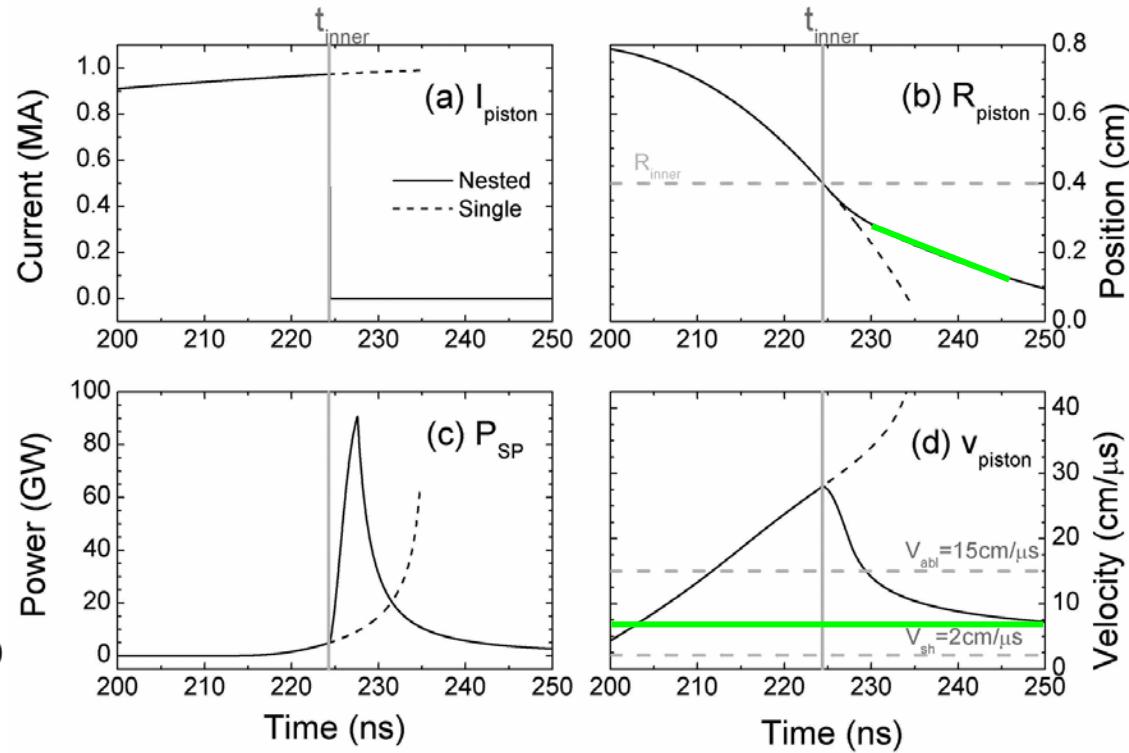
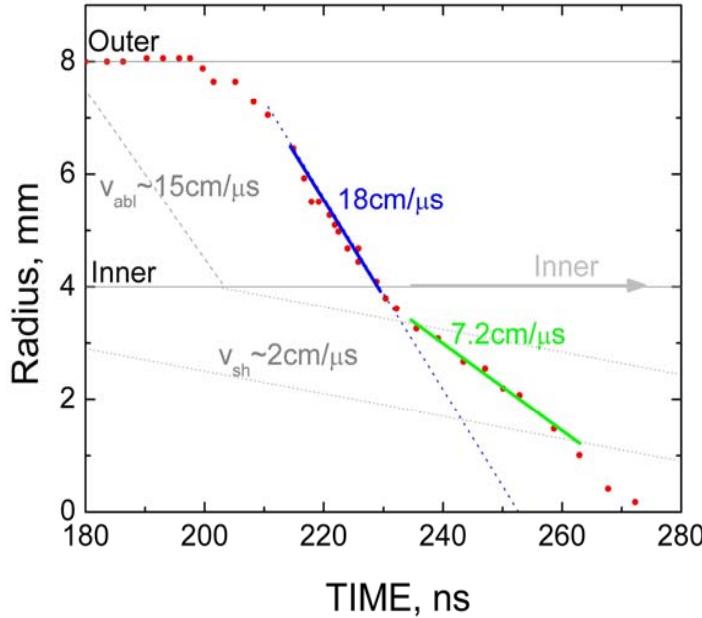
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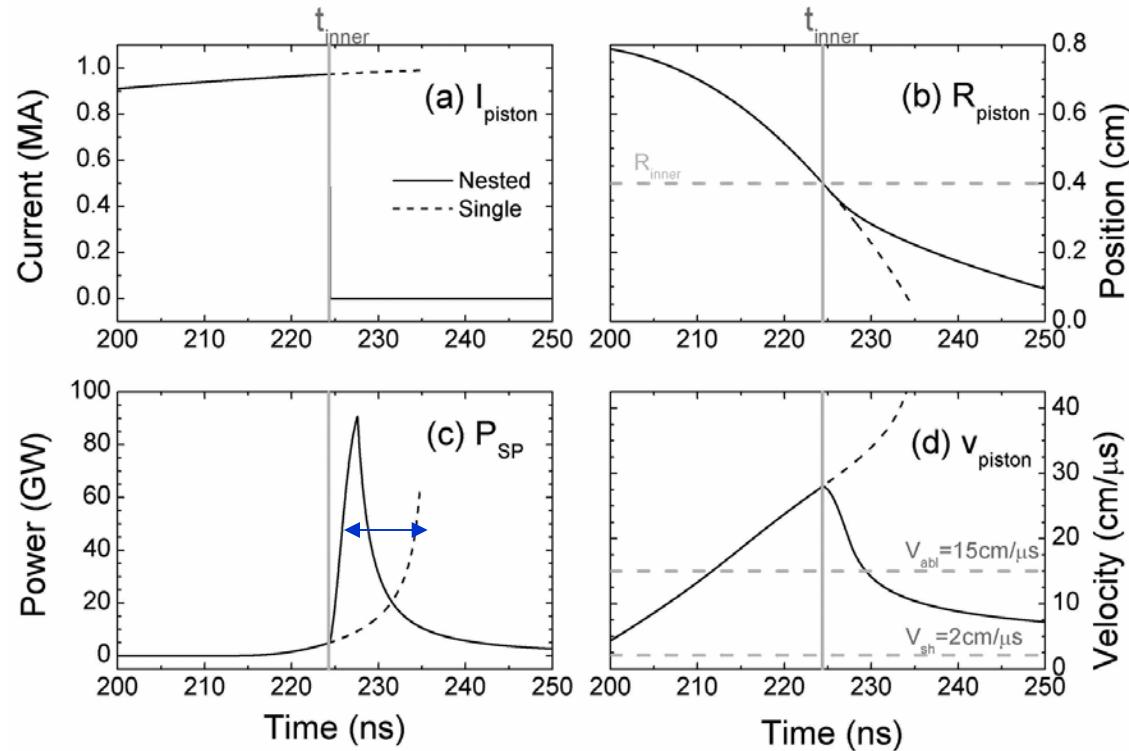
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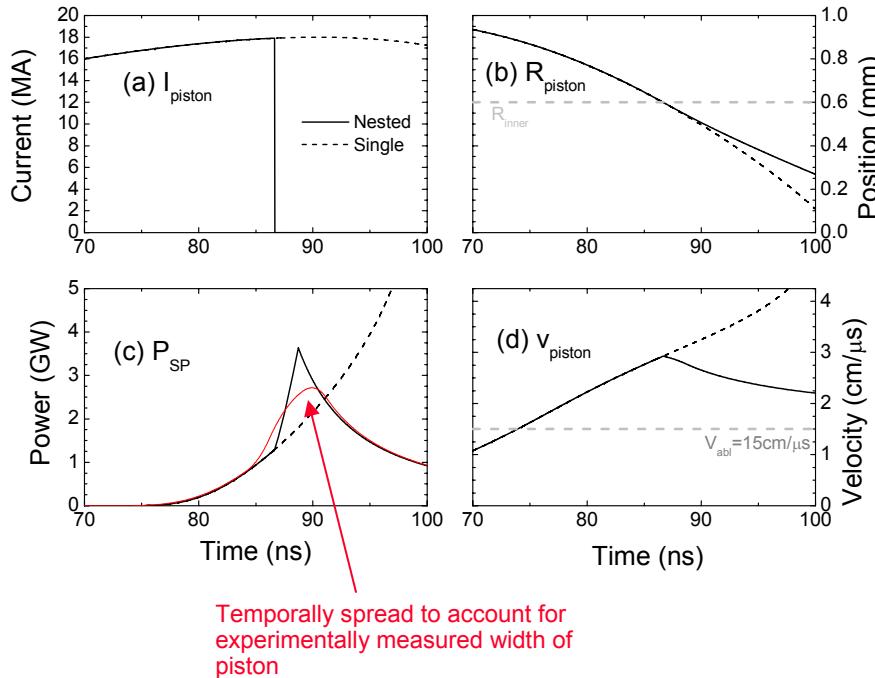
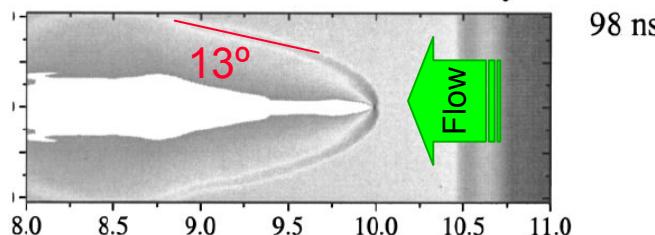
# Applying similar model to a (more uniform) Z implosion allows a comparison of powers

Variable	MAGPIE Z-6mg	
$v_{abl}(cm/\mu s)$ [1, 2]	15	15
$c_s(cm/\mu s)$ [2–4]	3	1.3
$\beta$ (end-on image)	$39^\circ$	$\rightarrow 5^\circ$
$\gamma$ [5]	1.1	1.1
$M_\perp = \frac{v_a \sin(\beta)}{c_s}$	3.4	1.25
$\eta = \frac{v_{abl}}{v_{sh}}$	7.7	1.5

Shock angle smaller in sims of Z than measured on MAGPIE

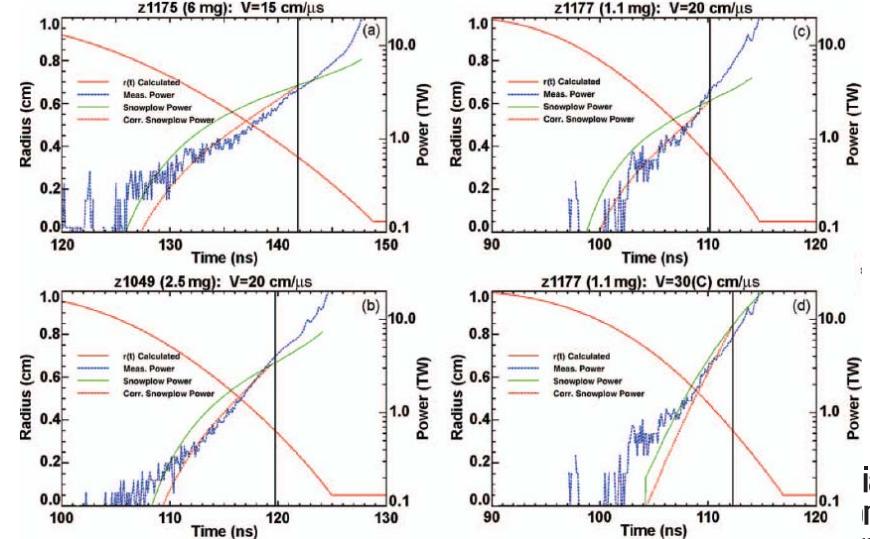
Chittenden *et al.* Phys Plas 8, 675 (2001)

Plasma stream from outer array



Snowplow for 6mg outer on Z gives good fit for  $v_{abl}$

Sinars *et al.* Phys Plas 13, 042704 (2006)





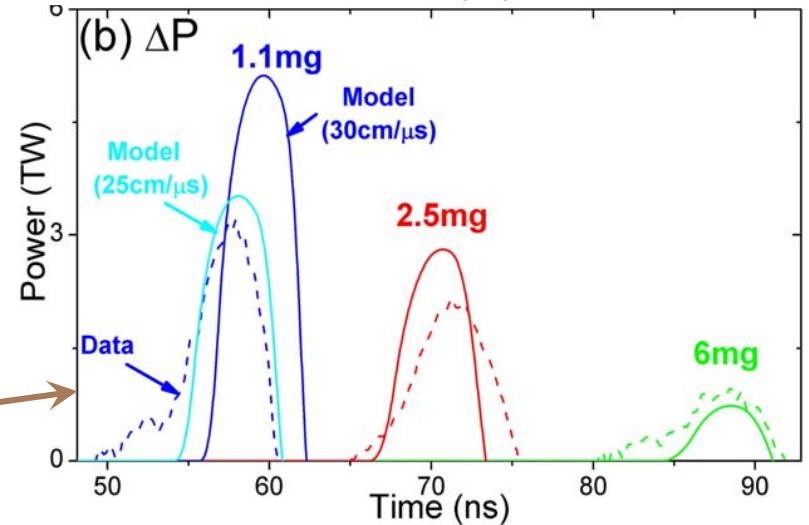
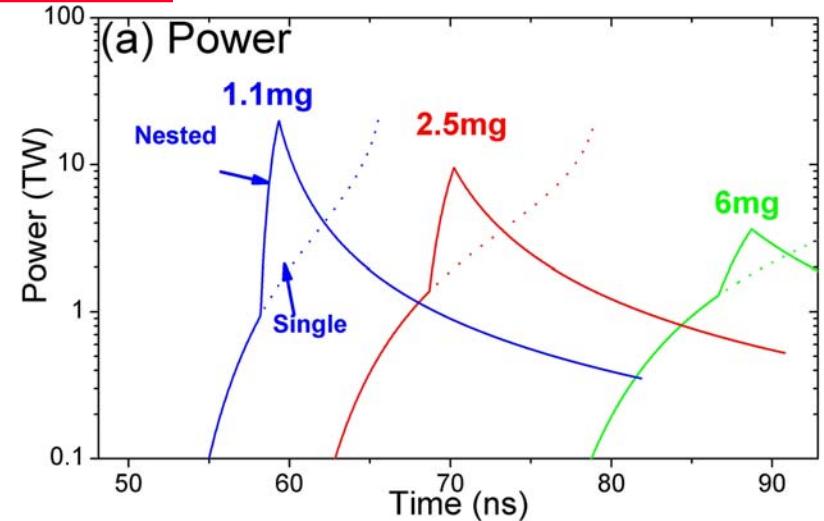
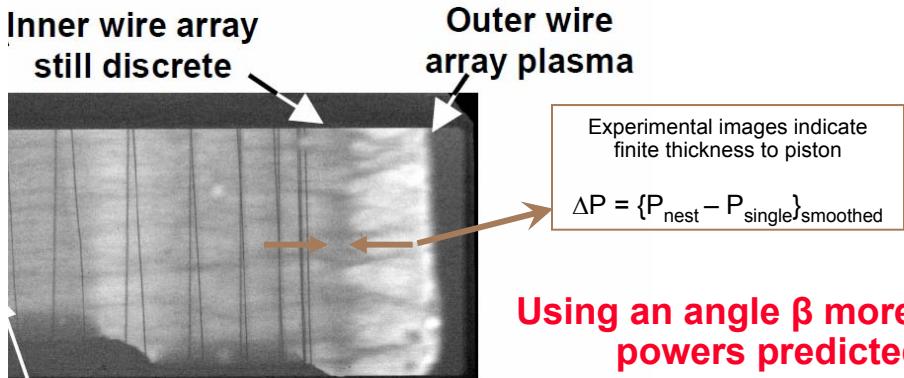
# Snowplow model recreates interaction pulse for Z outer array mass scan

Variable	MAGPIE	Z-6mg	Z-2.5mg	Z-1.1mg	Z-1.1mg
$v_{abl}(cm/\mu s)$ [1, 2]	15	15	20	30	25
$c_s(cm/\mu s)$ [2-4]	3	1.3	1.3	1.3	1.3
$\beta$ (end-on image)	39°	5°	5°	5°	5°
$\gamma$ [5]	1.1	1.1	1.1	1.1	1.1
$M_{\perp} = \frac{v_a \sin(\beta)}{c_s}$	3.4	1.25	1.66	2.5	2.0
$\eta = \frac{v_{abl}}{v_{sh}}$	7.7	1.5	2.5	5.0	3.7
$E_{Sp}(kJ)$	-	3.0	12.4	22.5	15.3
$E_{Exp}(kJ)$ [6]	-	5.2	12.1	15.0	15.0
$P_{Sp}(TW)$	-	0.7	2.8	5.1	3.5
$P_{Exp}(TW)$ [6]	-	1.2	2.2	3.2	3.2

Variable ablation velocity  
Sinars et al. Phys Plas 13, 042704 (2006)

?

- [1] S. V. Lebedev et al., Plas. Phys. Contr. Fus. 47, A91 (2005).
- [2] D. B. Sinars et al., Phys. Plasmas 13, 042704 (2006).
- [3] S. V. Lebedev et al., Laser Particle Beams 19, 355 (2001).
- [4] J. P. Chittenden et al., Phys. Plasmas 8, 675 (2001).
- [5] R. P. Drake, High Energy Density Physics (Springer, 2006).
- [6] M. E. Cuneo et al., Phys. Plasmas 13, 056318 (2006).

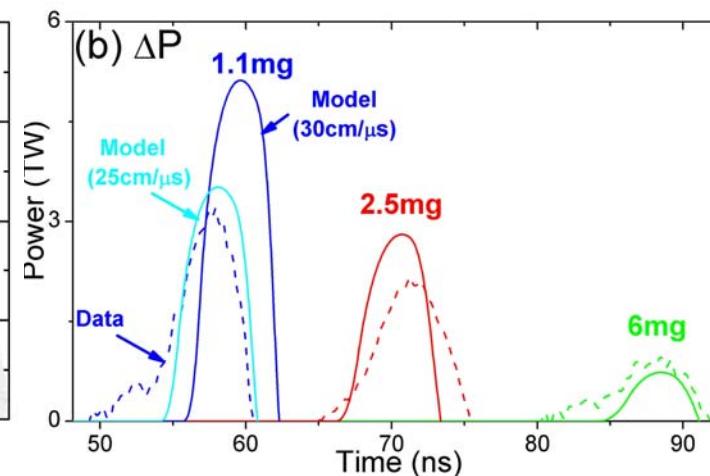
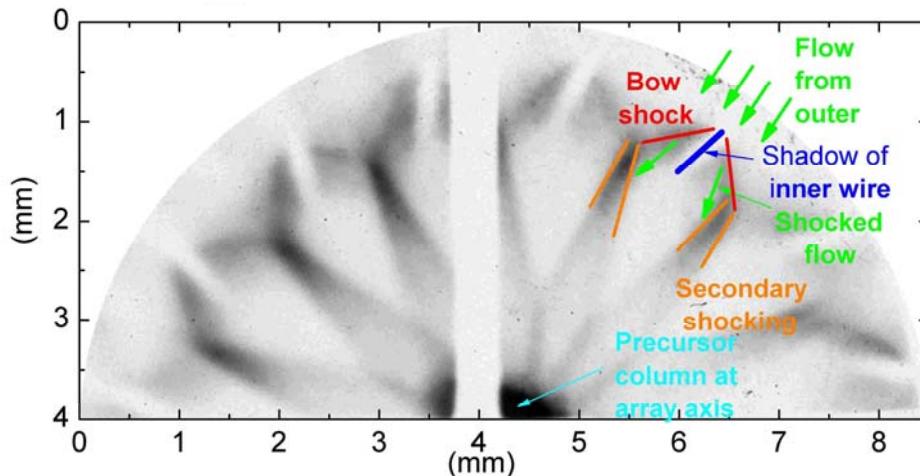


Using an angle  $\beta$  more like MAGPIE or MHD would increase powers predicted, but reduce mass dependence



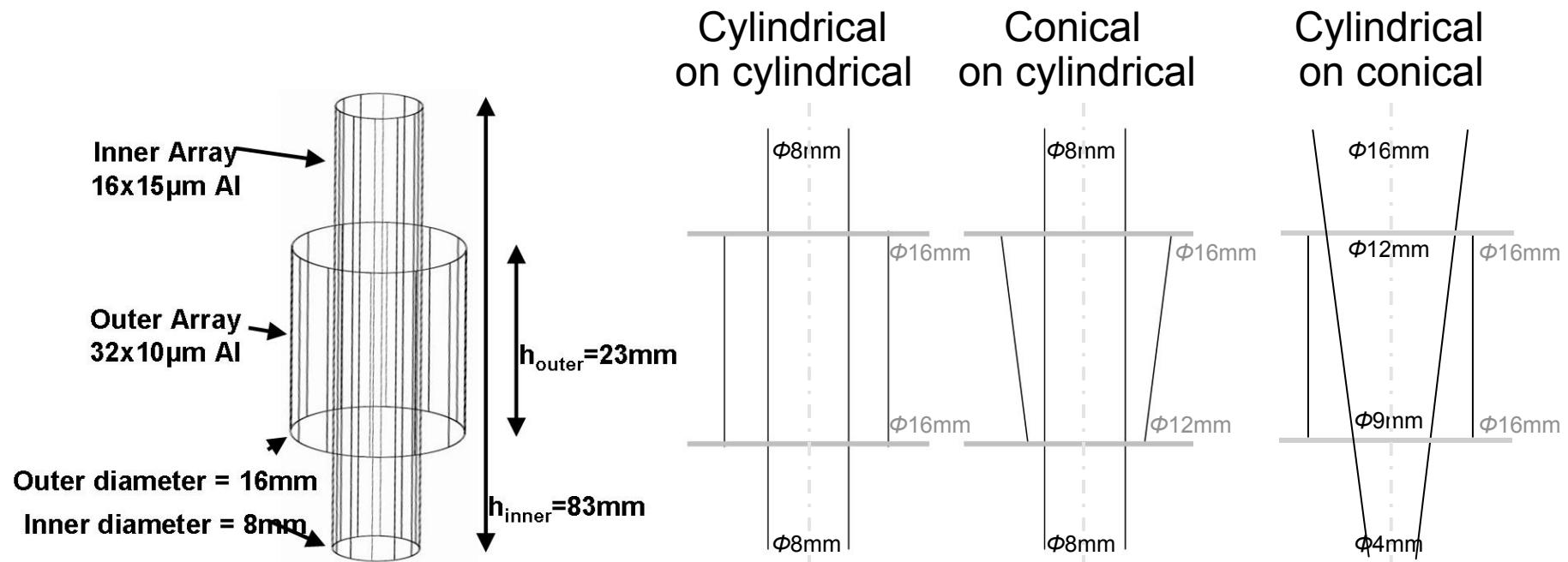
## Part 1 Summary : Perturbed snowplow can lead to observed Interaction Pulse

- Inner array shocks precursor plasma streams on MAGPIE
- Shock will alter  $\rho$ ,  $T$ ,  $v$  of the streams
- This jump is likely to alter the snowplow emission as the outer array implodes
- For Z conditions this change in snowplow radiation can be comparable to the observed interaction pulse
- Able to recreate correct outer mass dependency
- Future plans include analytics, simulations and experiments to better determine correct angle  $\beta$  for W arrays on Z



## Part 2: Conical nested

- One suggested technique to lengthen the main pulse from nested arrays is to seed a zipper using conical arrays  
c.f. zipper observed in gas puff experiments
- Two modified setups tested on both MAGPIE and Z



# Use of a conical outer array will alter mass ablation rate

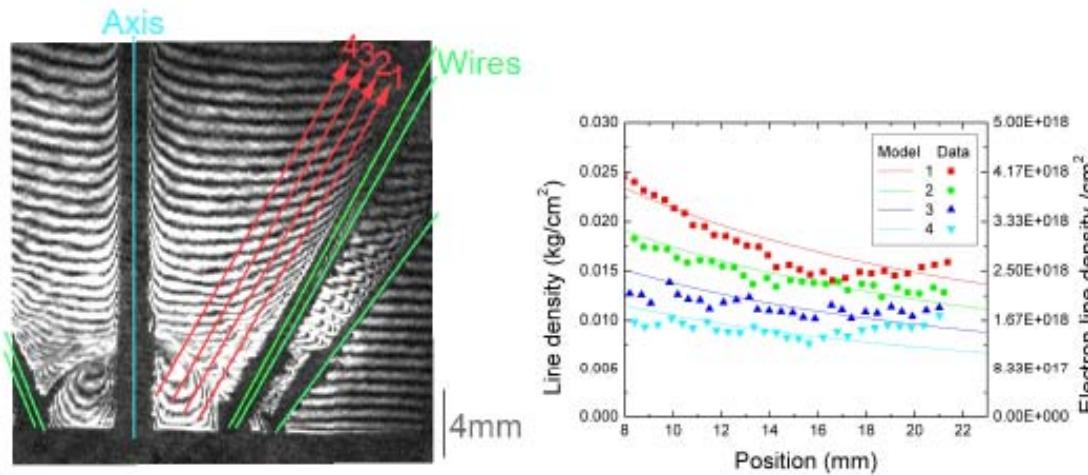
- With conical outer array the global field strength is varied along the length of the wire

$$B(z, t) = \frac{\mu_0 I(t)}{2\pi R(z)} = \frac{\mu_0 I(t)}{2\pi(R_0 + z \tan(\alpha))}$$

- Variation in global field alters mass ablation (due to fixed  $v_{abl}$ )

$$\dot{m} = \frac{\mu_0 I(t)}{2\pi V_{abl}(R_0 + z \tan(\alpha))}$$

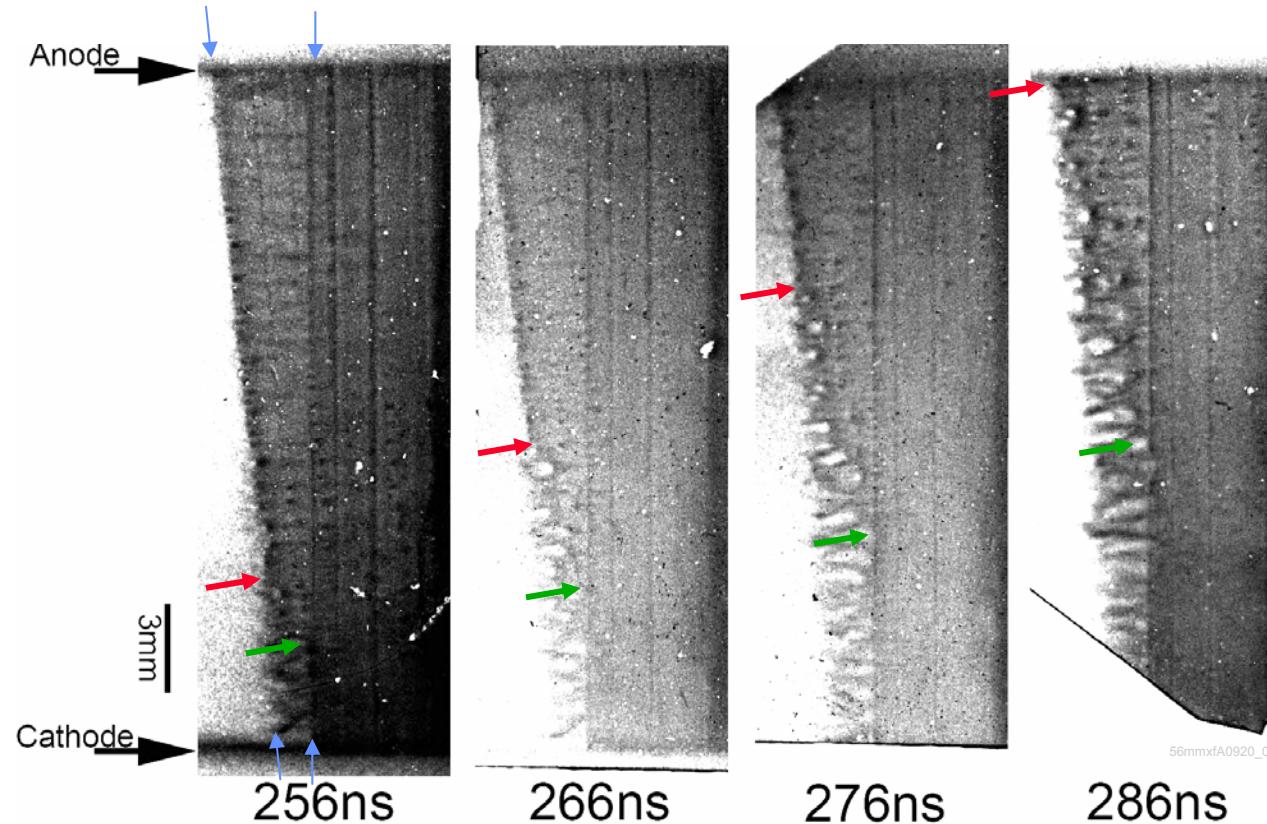
- Mass density profiles in single conical arrays are consistent ( $v_{abl} \sim 15 \text{ cm}/\mu\text{s}$ )



- Time of mass depletion (for single or nested) is expected to be a function of axial position

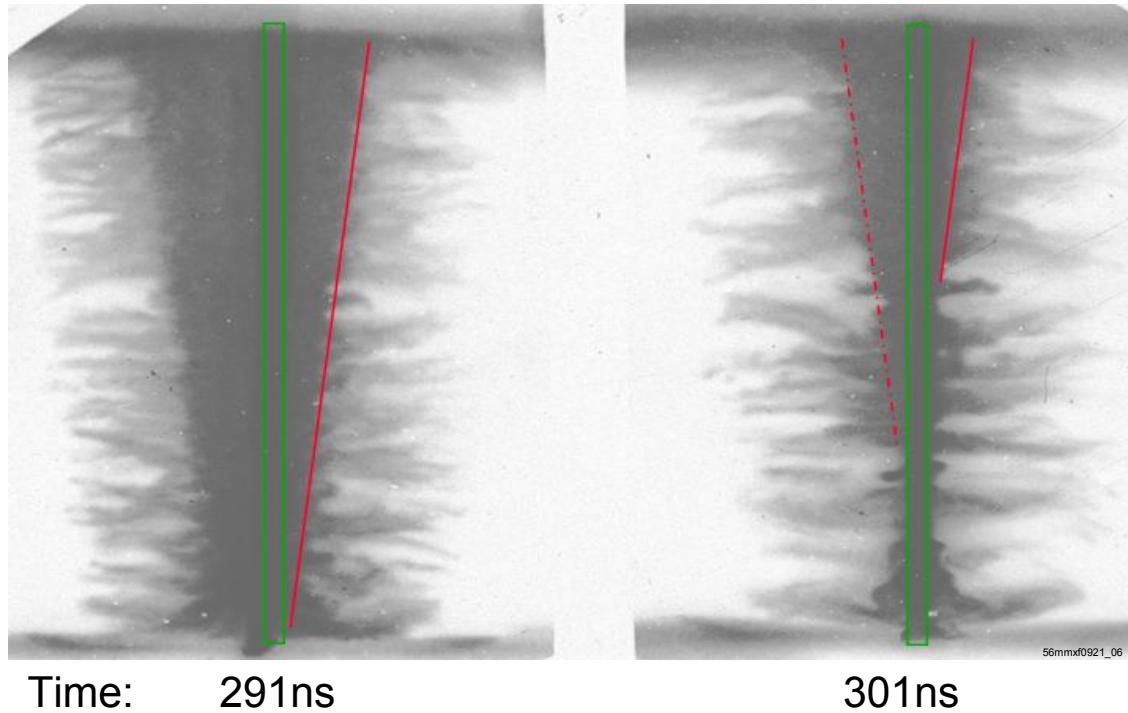
# A conical outer array can be used to seed an axial zipper

- Nested conical data agrees with predicted delay in time of wire breakage



- Also see that zipper of implosion gives an axial dependence time of interaction with the inner array

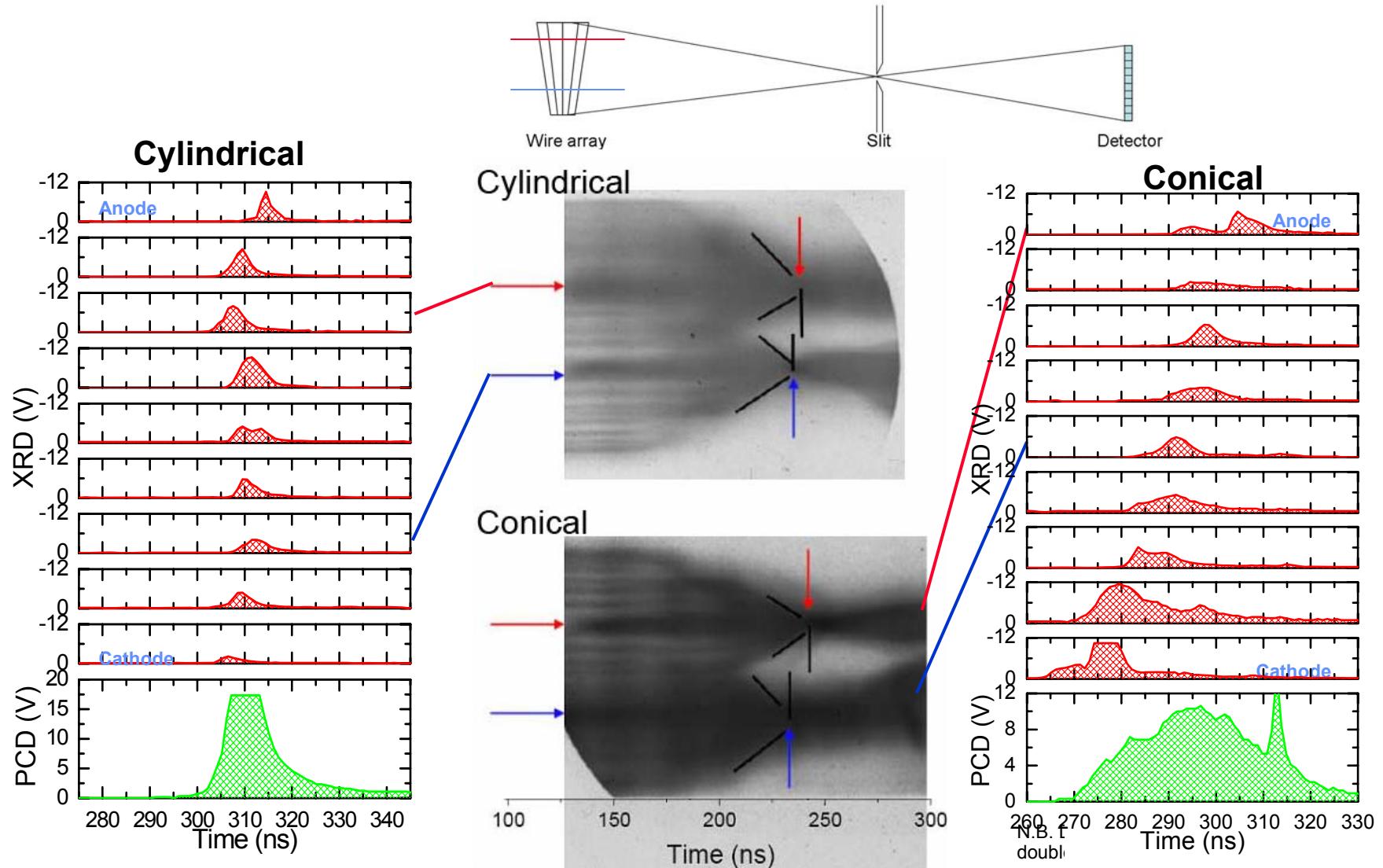
**Axial zipper survives through the interaction, leading to a zippered implosion of inner**



- Data indicates zipper velocity  $\sim 139\text{cm}/\mu\text{s}$
- Estimated zipper over this time frame indicates zipper along full axis  $\Delta t_{\text{zip}} \sim 16.5\text{ns}$
- On MAGPIE, left-right asymmetry also present due to concentricity issue,
  - will effect pulse, but temporal effect is less ( $\Delta t_{\text{L-R}} \sim 7\text{ns}$ )

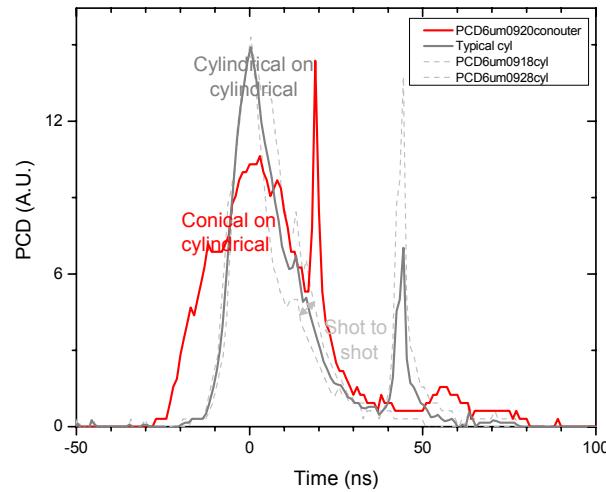
# Seeded zipper translates into a zippered stagnation, and elongated x-ray pulse

- Twin radial optical streak and zipper array each indicate conical outer zippers stagnation
- Axial dependence of stagnation time leads to pulse lengthening





# Comparison of conical and cylindrical outers indicates success at widening main pulse



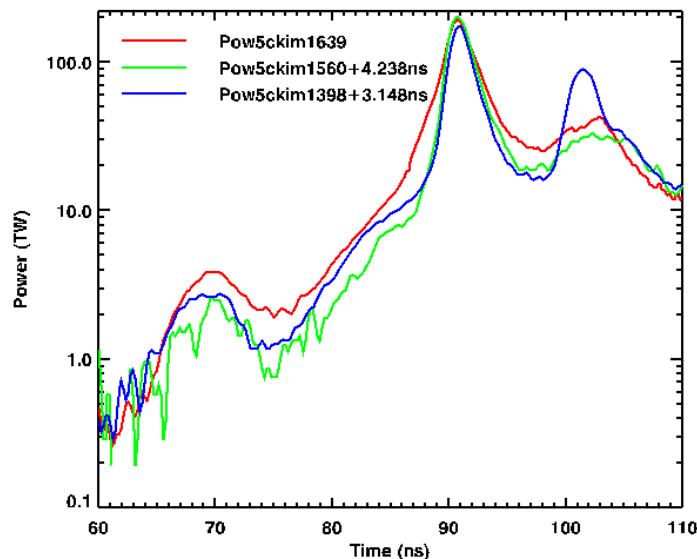
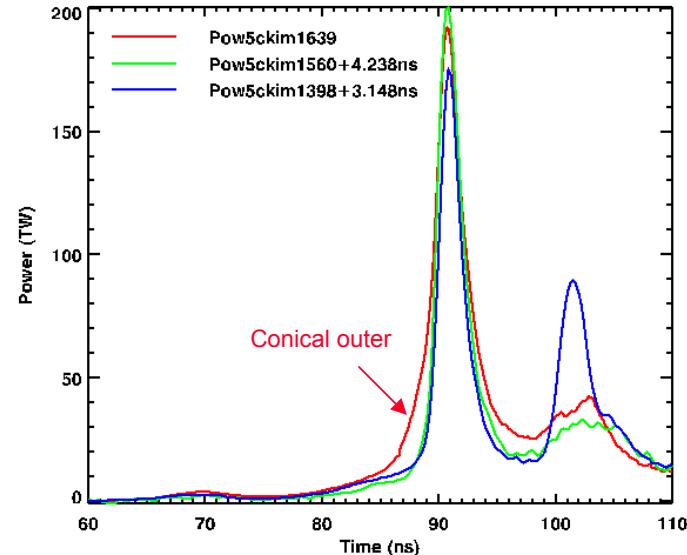
## For conical outer on MAGPIE:

- See a longer rise in x-ray pulse
- Peak power down, but total energy similar
  - (possibly 25% higher for conical outer)

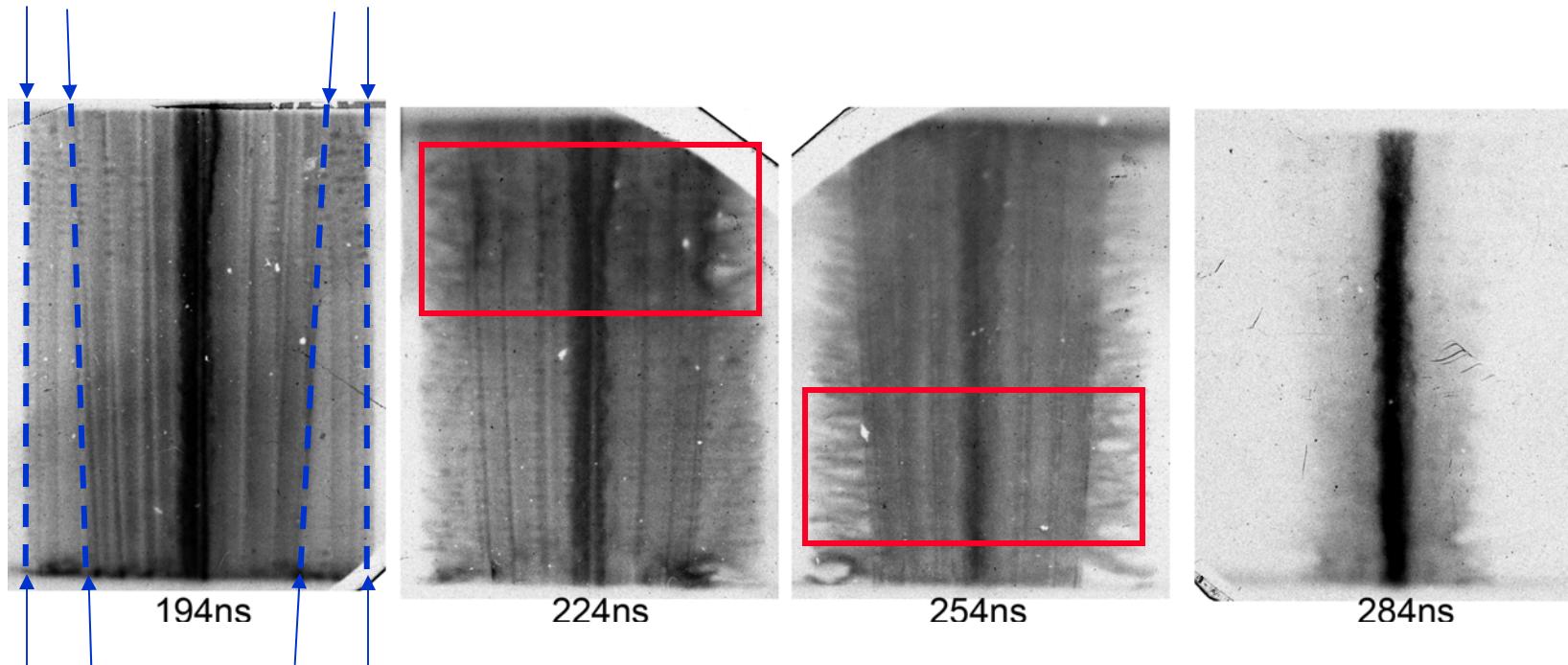
## For conical outer on Z:

(Z1639, Cuneo et al., 22mm Cathode, 20m anode, 12mm inner)

- Increased foot pulse power by 45% because of increase in outer velocity
- Increase first step by zippering implosion onto foam
  - power by a factor of ~4.6
  - energy by ~4.2
- Increase energy in the first step from 25 kJ to 104 kJ
- Energy radiated after the first step is unchanged
- Conical outer increases energy radiated in the main peak 22%

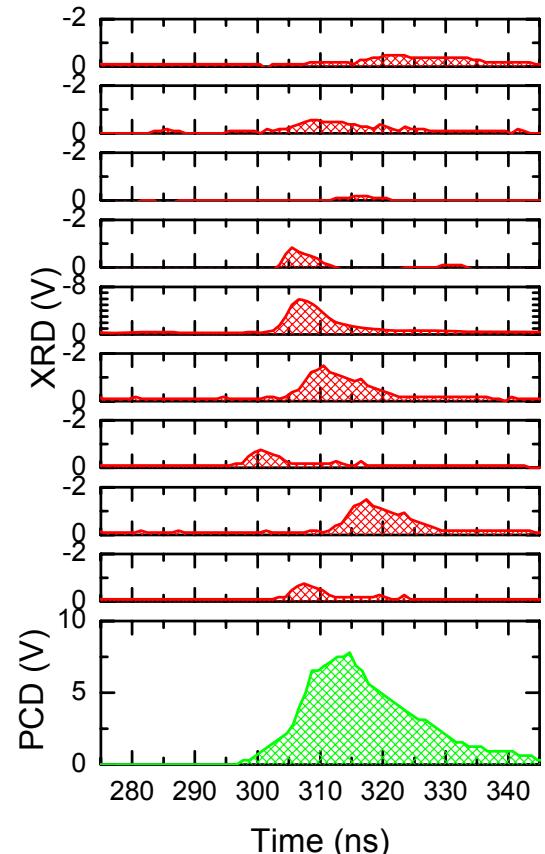
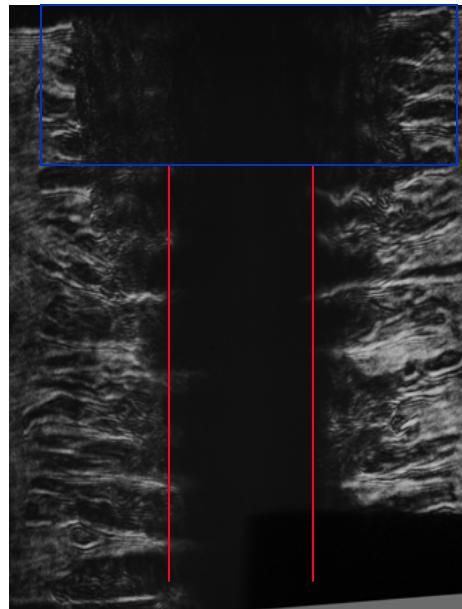
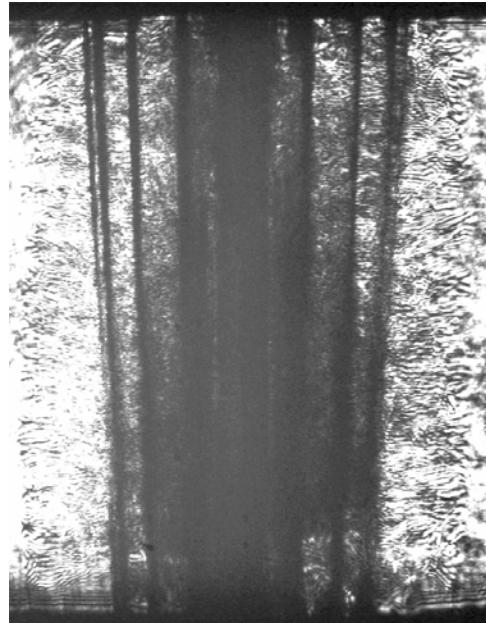


## Inclining inner leads to change of time of flight of outer to inner, and alters timing of Interaction



- Cylindrical wire arrays show variation in time of inner collision with inner array diameter
- Conical inner shows that time of interaction varies with  $z$
- Power pulse will be lengthened
- Zipper less significant after inner ablation

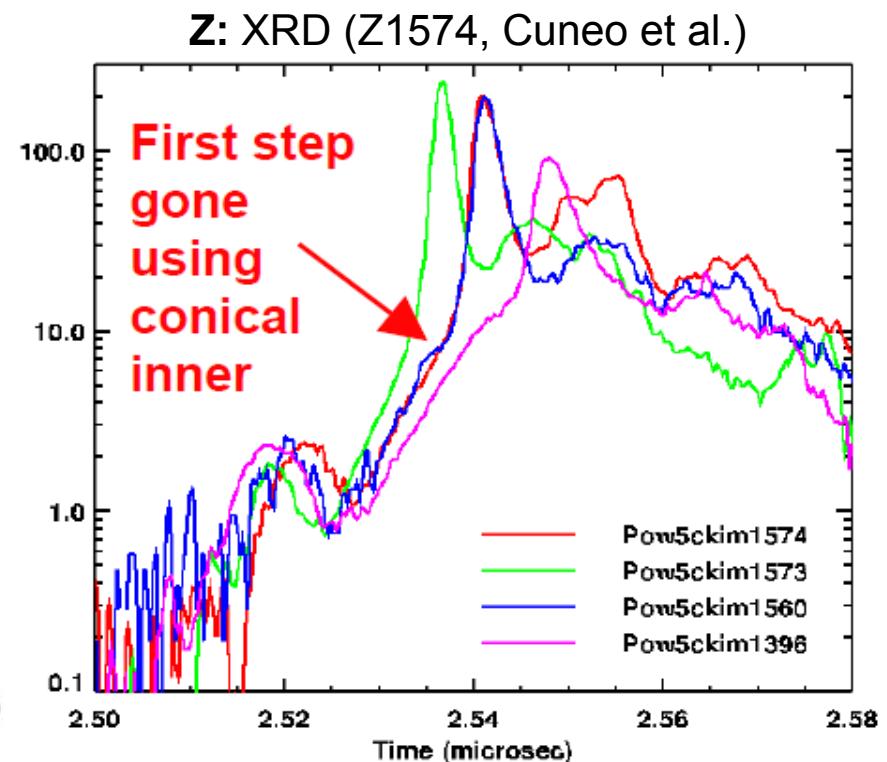
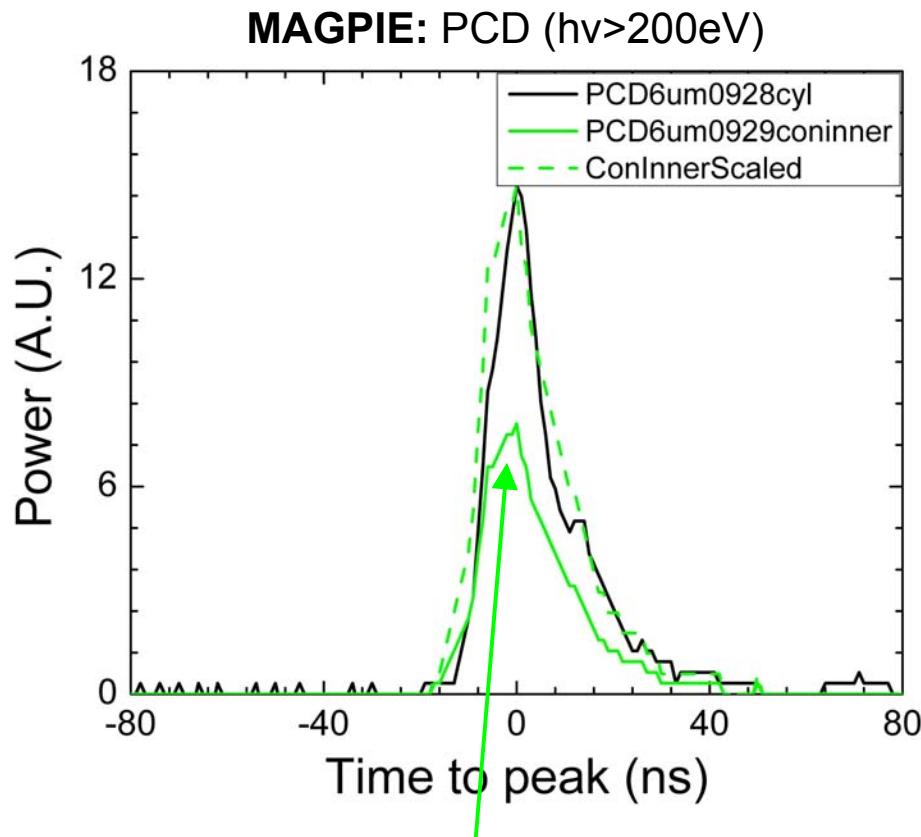
## Nested array with conical inner does not globally zipper stagnation on MAGPIE, but would alter Interaction Pulse



- Laser imaging after interaction indicates no substantial zipper
- Zipper array confirms no zipper in stagnation
- Laser imaging does show top section does not participate in implosion



## Conical inner has some effects, but does not alter width of main pulse on MAGPIE or Z

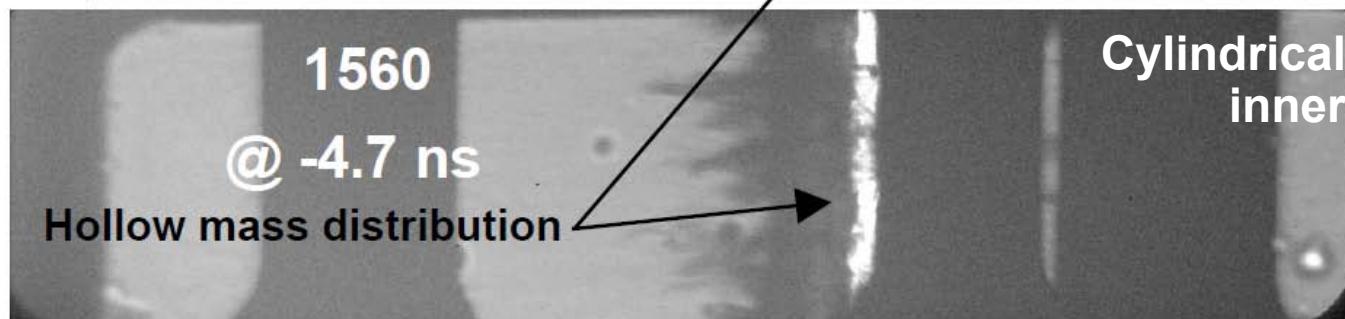
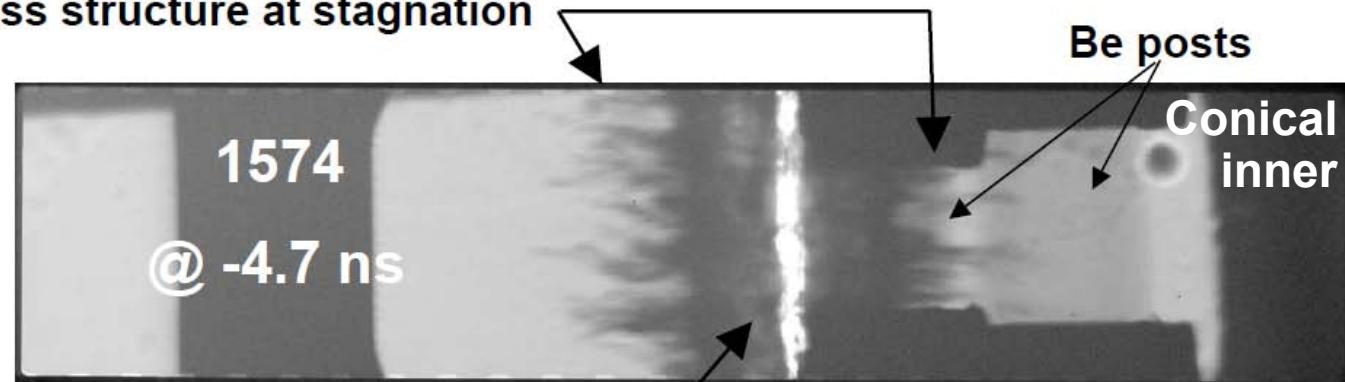


MAGPIE power lower than cylindrical  
due to part of array not participating in implosion

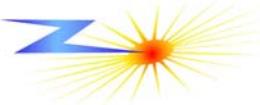


## Radiography on Z indicates no zipper present after interaction

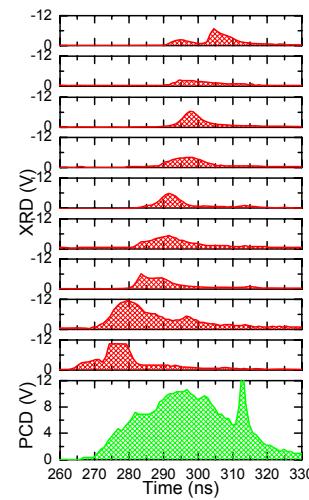
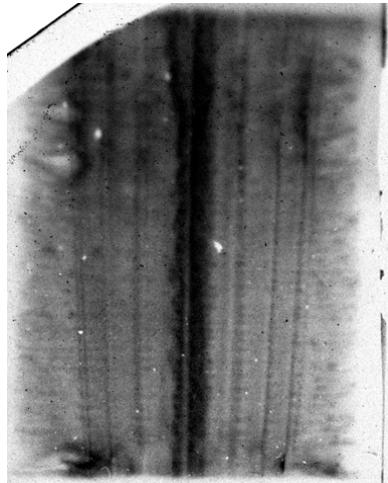
3D mass structure at stagnation



- For Z see no evidence of change to the mass distribution post-interaction



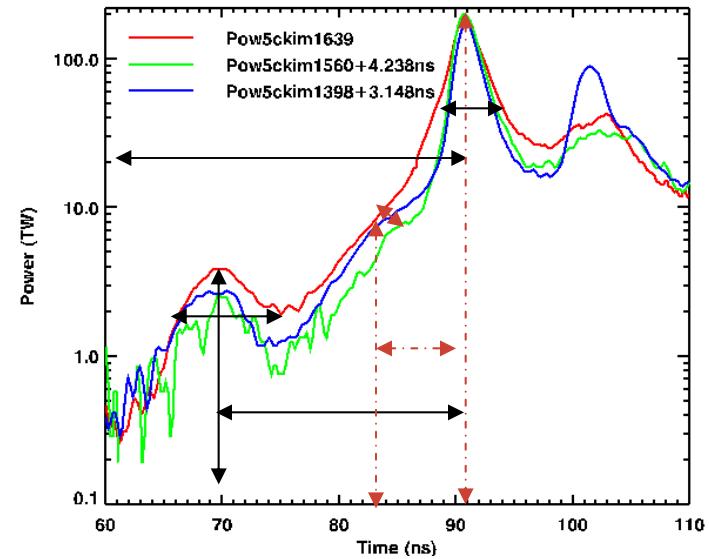
## Part 2 Summary: What can we now control



- Conical inner can control
  - Time scale of interaction
- Conical outer can control
  - Time scale of interaction (MAGPIE)
  - Time scale of main stagnation
- Need a more quantitative comparison

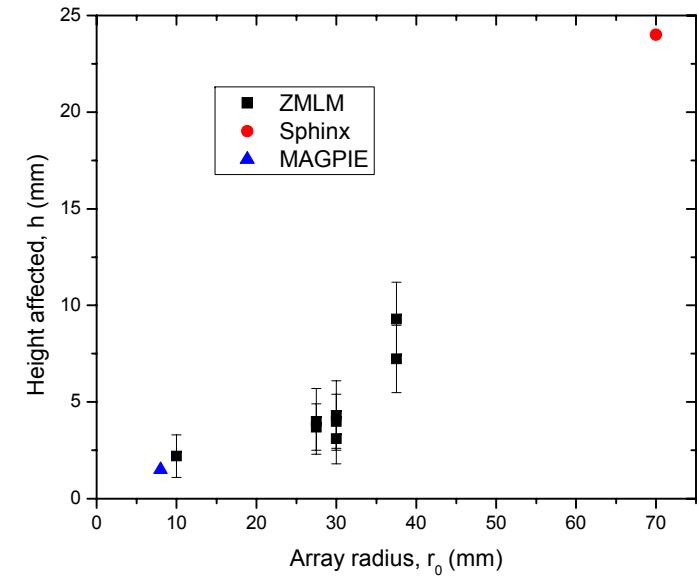
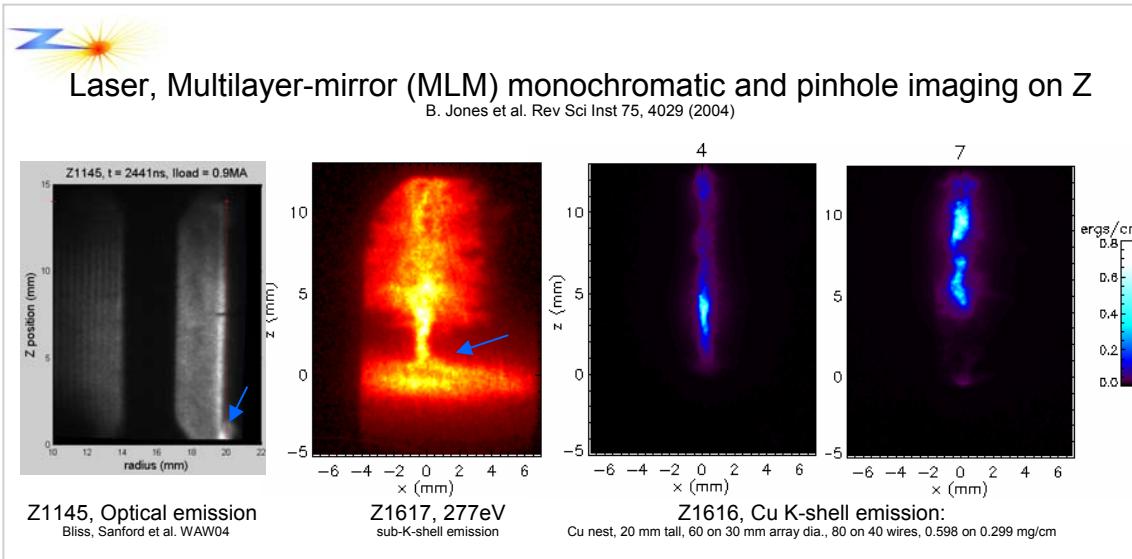
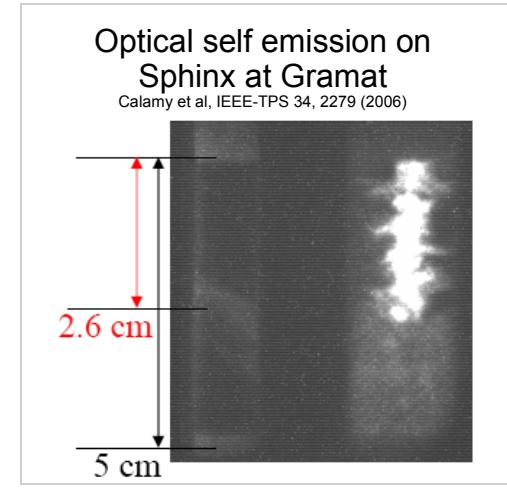
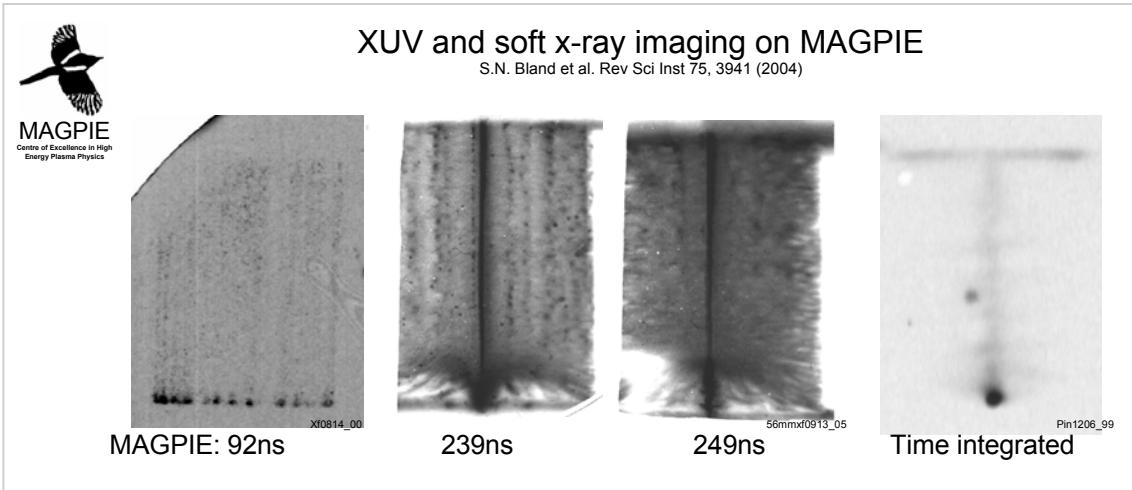
Combine with previous data (Cuneo et al.), now have control of:

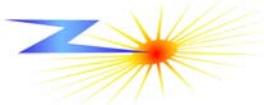
- Time of peak (Outer mass, inner mass, outer diameter)
- Interaction to peak (inner diameter and mass)
- Pulse length of stagnation (outer angle)
- Pulse length of interaction (relative angle between outer and inner – needs verification)
- Understanding of interaction may lead to control of amplitude and length (need more experiments)



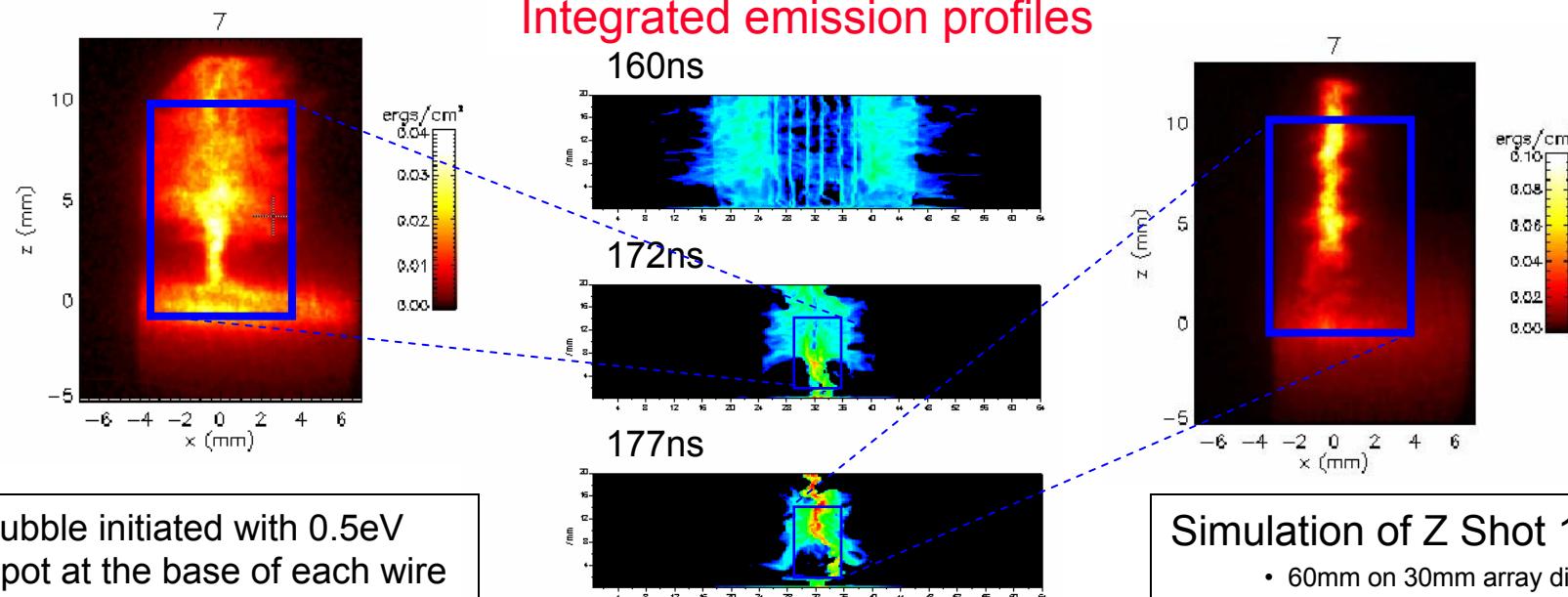


# End effects impact arrays at all current levels





## Simulations can reproduce effect and show possible mitigation with step

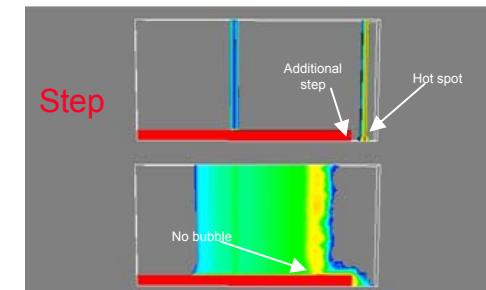
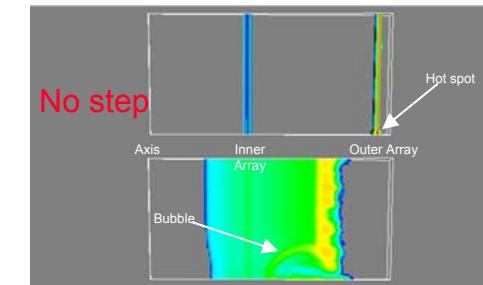
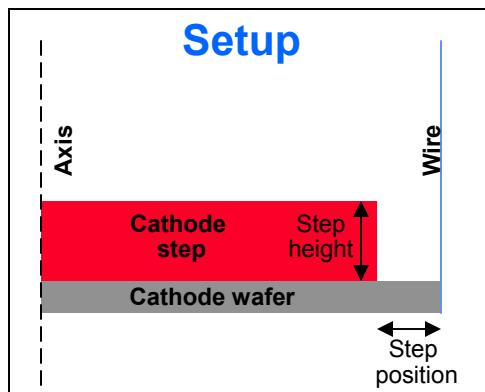


Bubble initiated with 0.5eV hotspot at the base of each wire

Simulation of Z Shot 1617

- 60mm on 30mm array diameters
- 80 on 40 copper wires

## Presence of step on cathode step changes dynamics

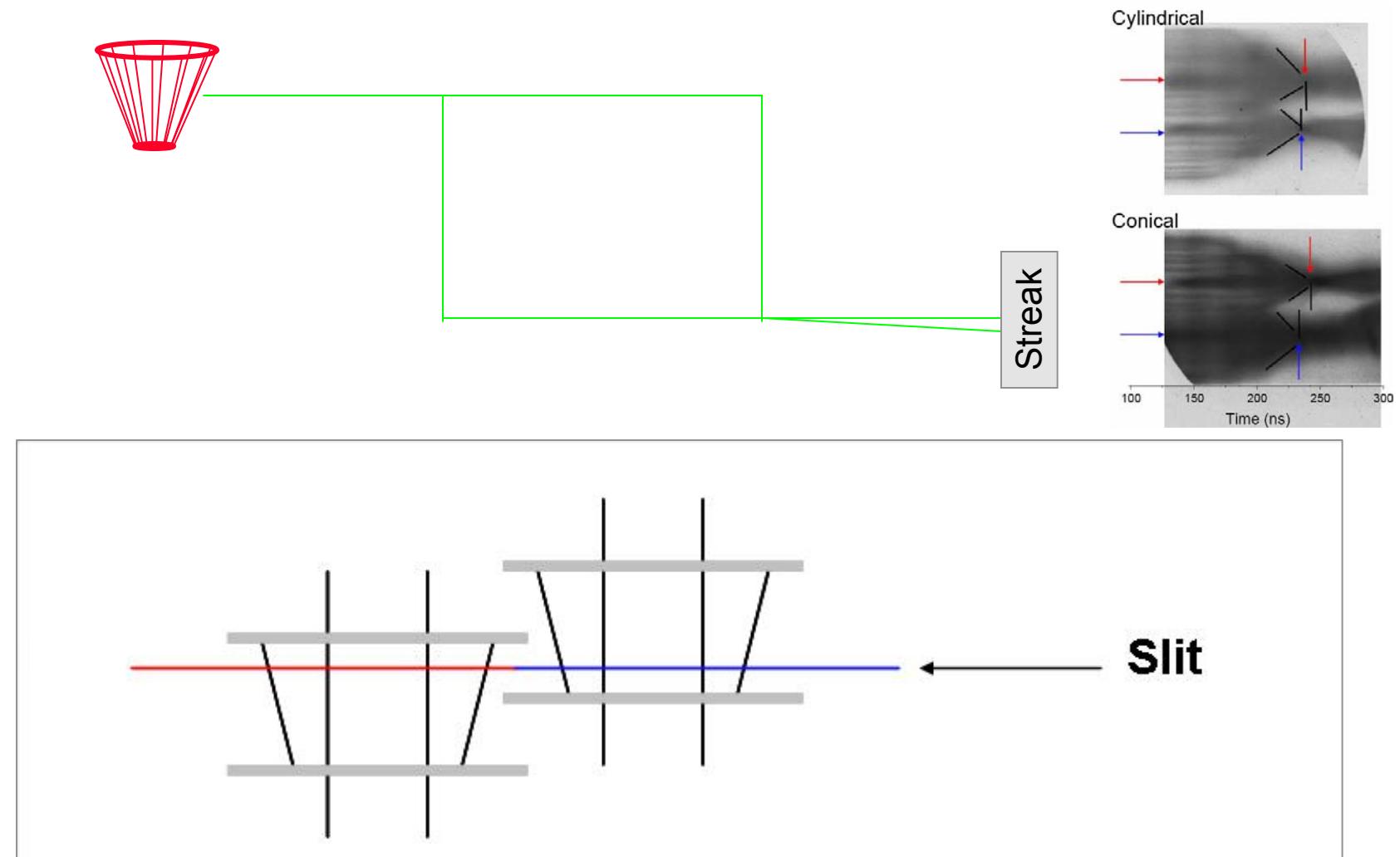


# Simulations by C. Jennings using Gorgon 3D resistive MHD code

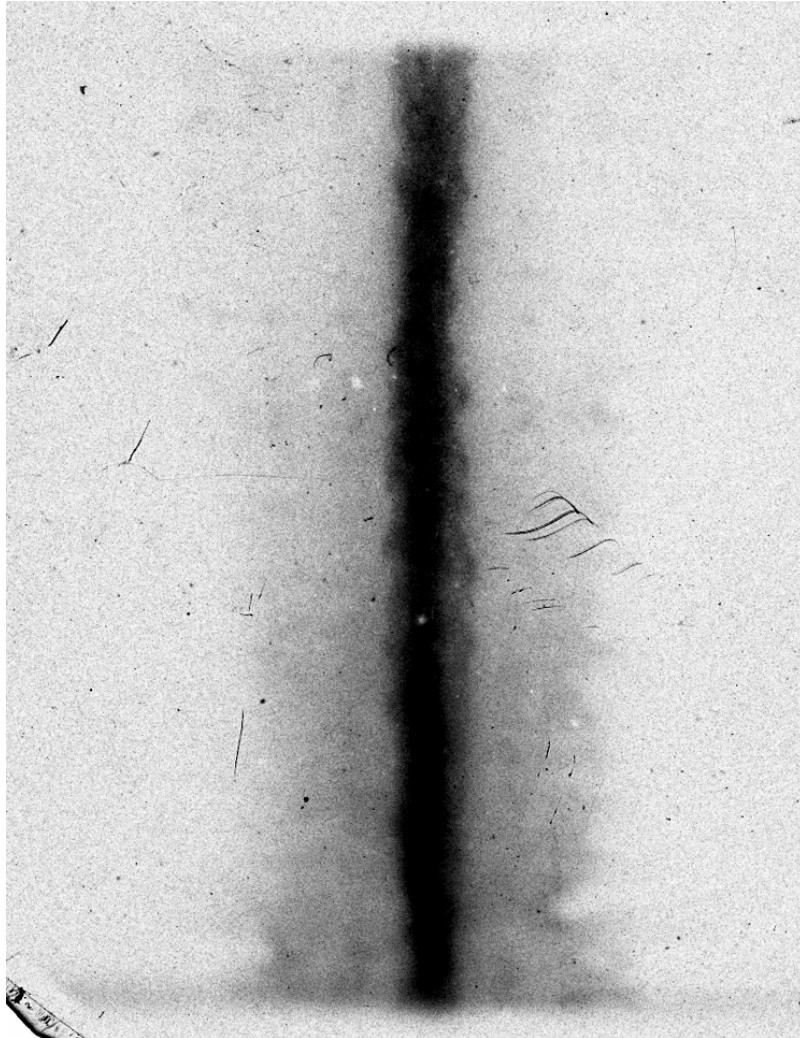
## Experiments to test idea planned for Saturn in May-June

# Backup

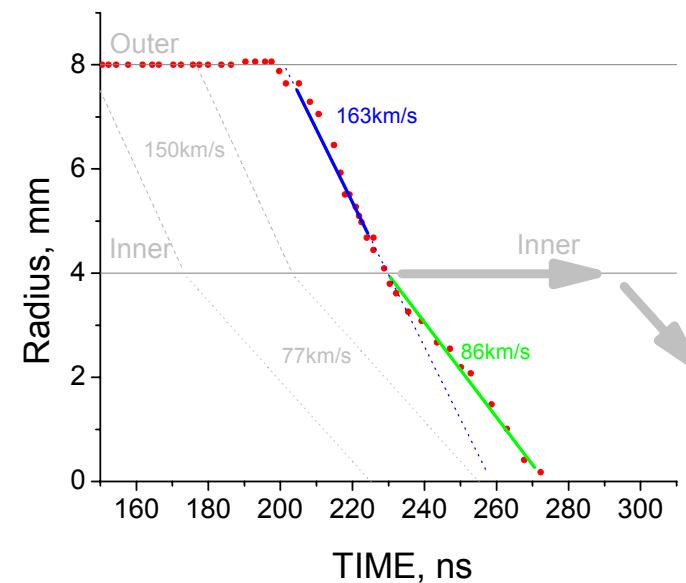
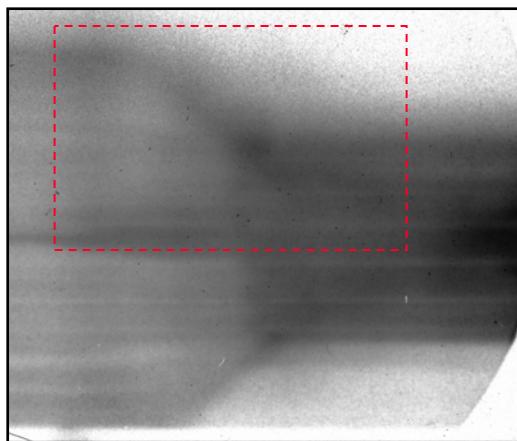
# Streak setup for dual image



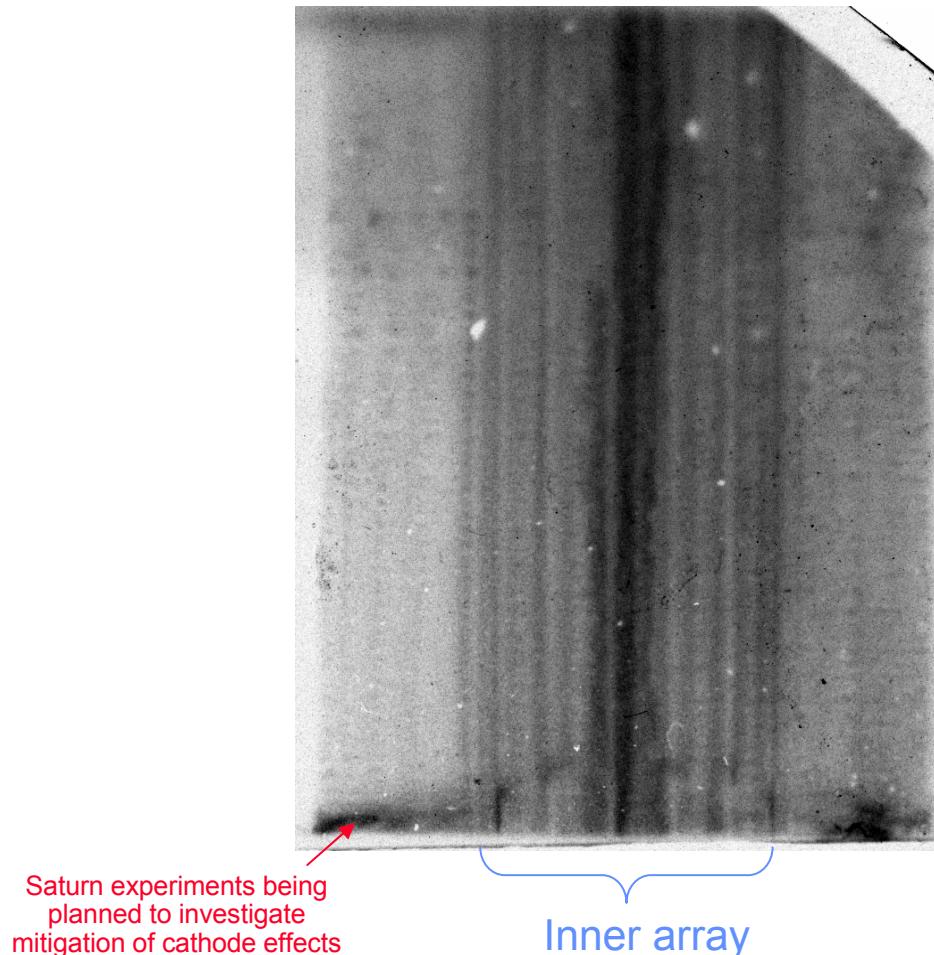
## XUV images can be overlaid to show evolution



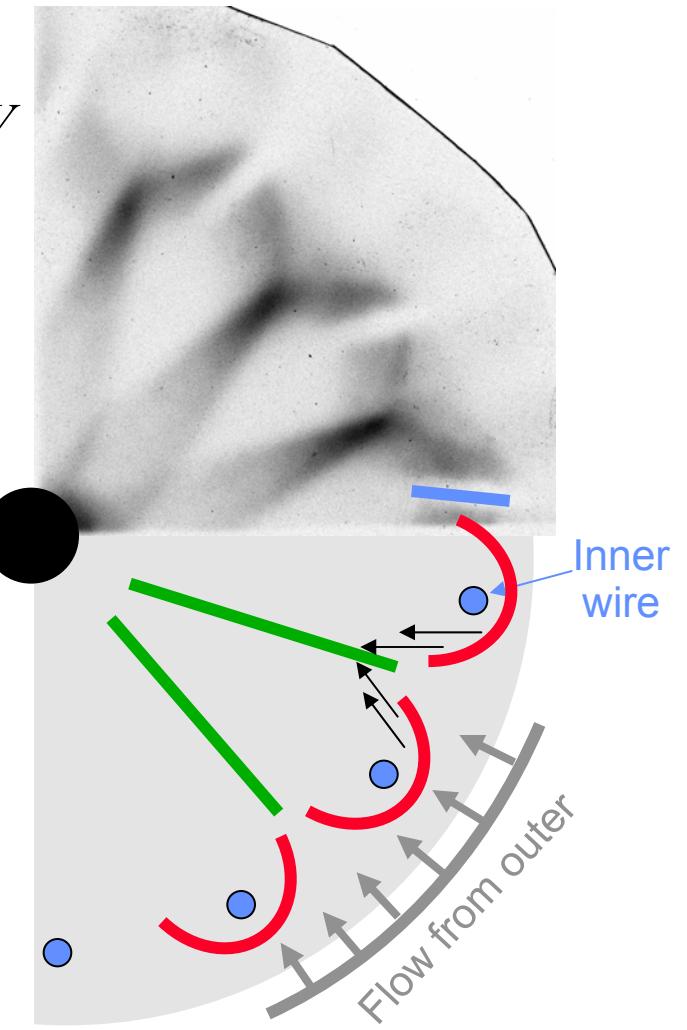
# Streak shows evolution after interaction



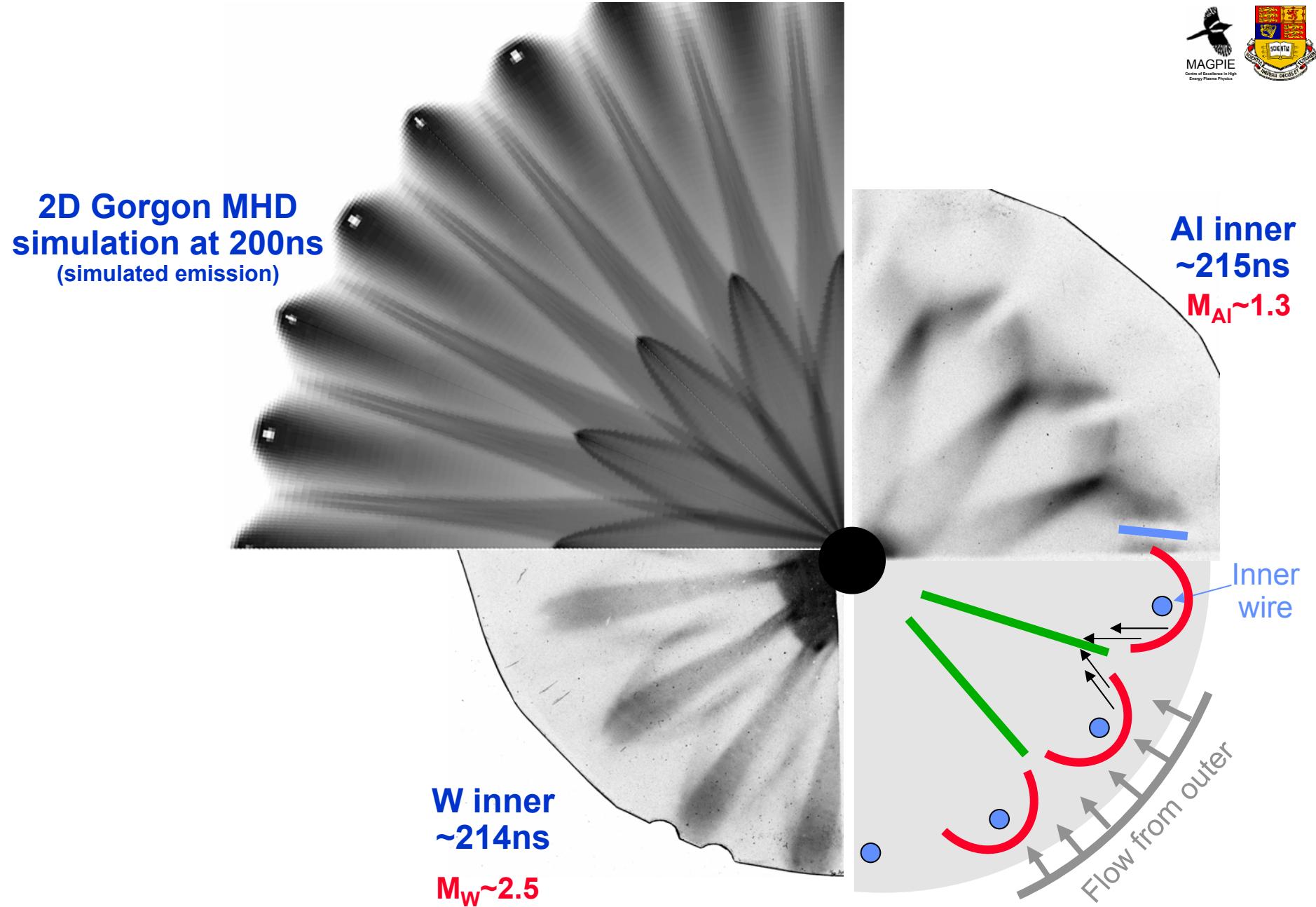
# Precursor plasma streams are shocked as they pass the inner array



Al inner  
 $\sim 215\text{ns}$   
 $h\nu > 30\text{eV}$



- Ablated streams perturbed by presence of inner forming bow shocks
- Shock leads to increased emission at position of inner (shock heating and change in density distribution)



# Shock jump in precursor streams

- For MAGPIE conditions estimate  $M \sim 1.3$ ,  $\gamma \sim 1.3$

- Estimate jump conditions:

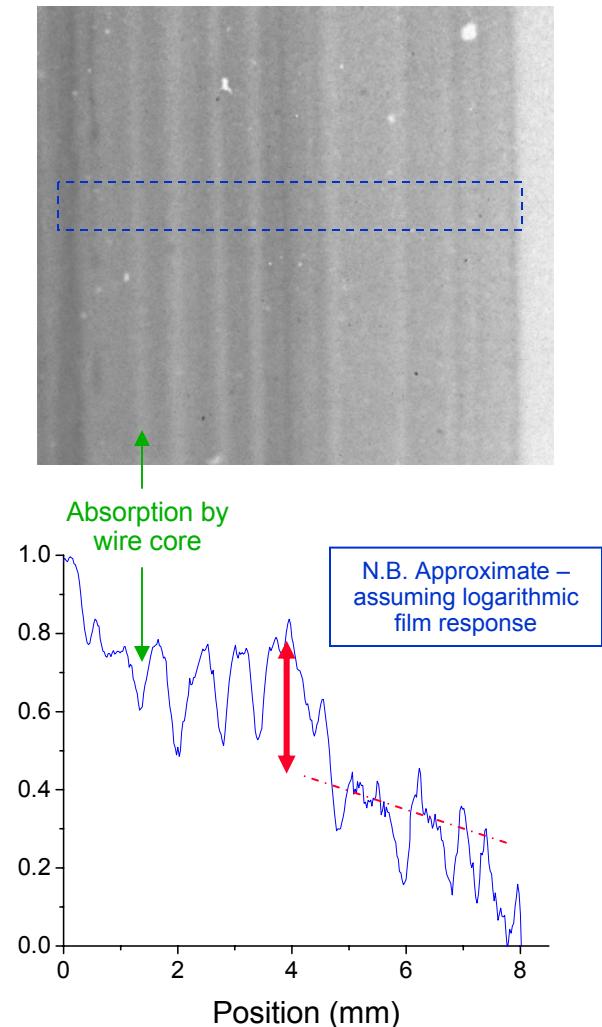
$$\frac{T_1}{T_0} = 1 + \frac{2(\gamma - 1)}{(\gamma + 1)^2} \frac{M_{\perp 0}^2 - 1}{M_{\perp 0}^2} [\gamma \cdot M_{\perp 0}^2 + 1] \sim 1.1$$

$$\frac{\rho_1}{\rho_0} = \frac{(\gamma + 1)M_{\perp 0}^2}{(\gamma - 1)M_{\perp 0}^2 + 2} \sim 1.5$$

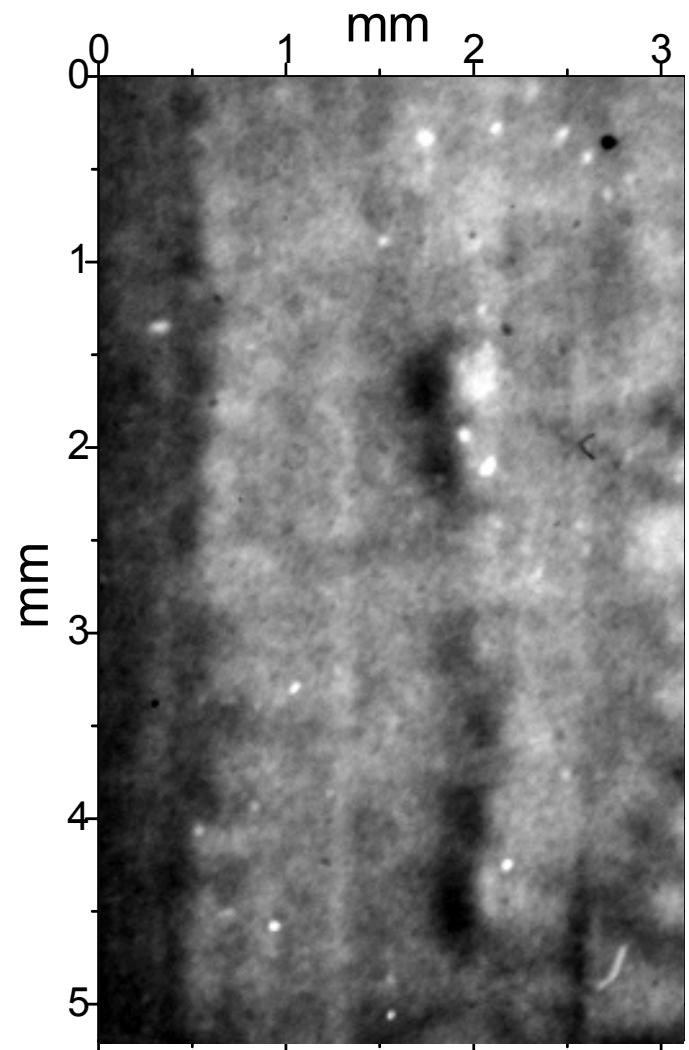
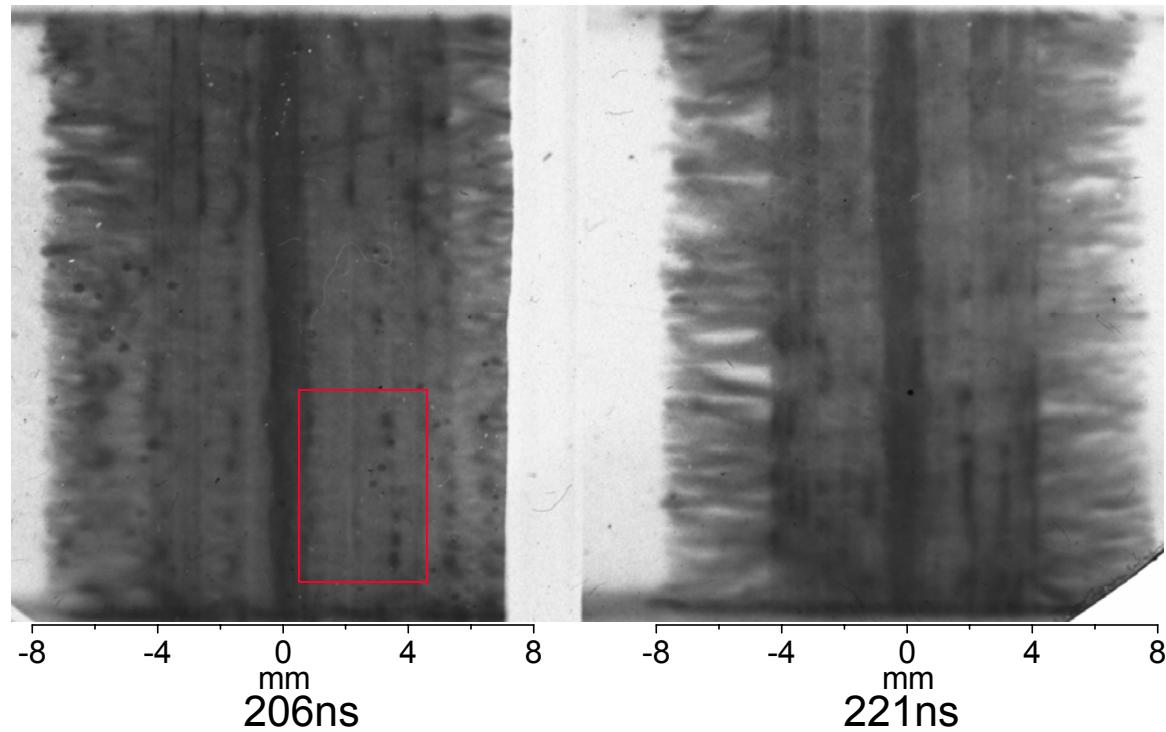
- From these, can estimate change in emission from incoming flows, e.g. assuming recombination emission:

$$\frac{P_1}{P_0} = \frac{\rho_1^2 / \sqrt{T_1}}{\rho_0^2 / \sqrt{T_0}} \sim 2.2$$

- Lineout of image is consistent (no Abel inversion...)
- Shock setup should be steady state before imploding outer reaches it



## Interaction: Bubbles emit as they pass inner

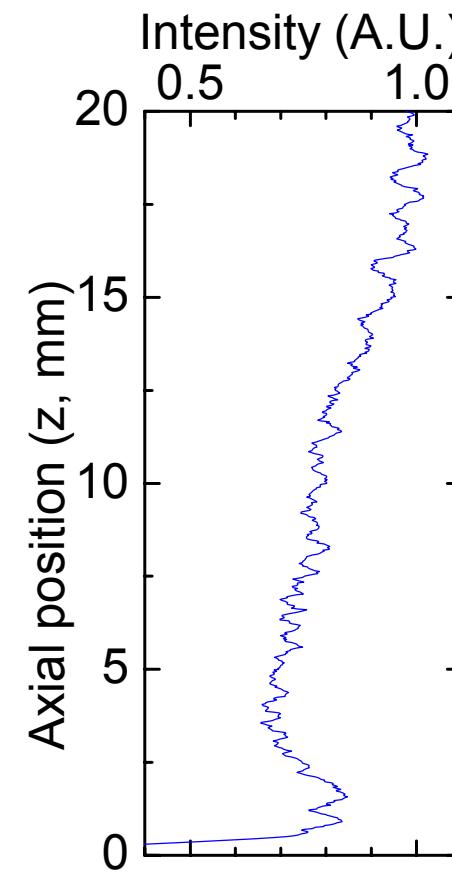
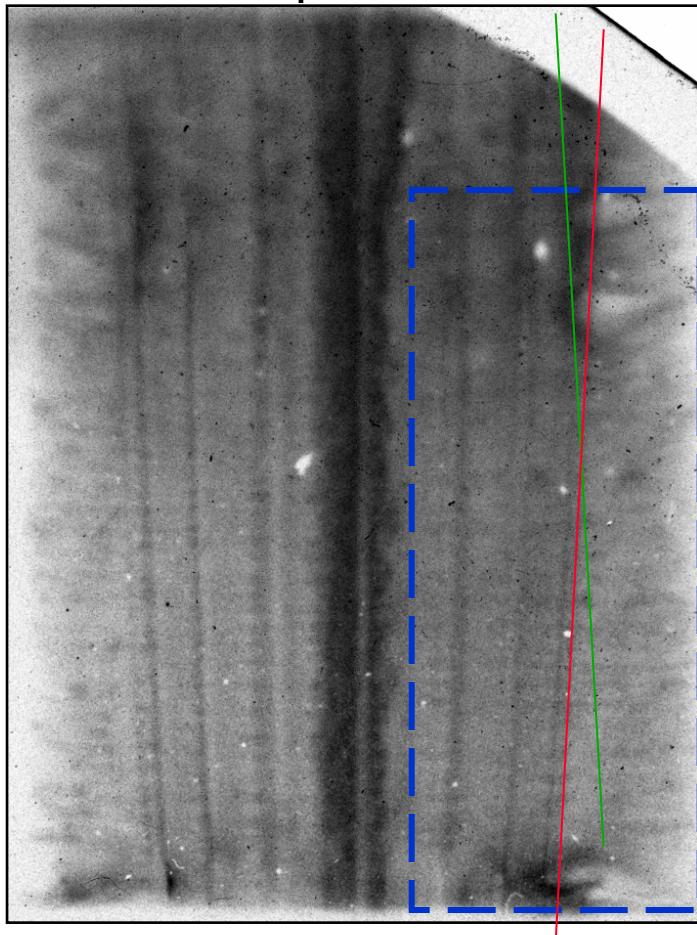


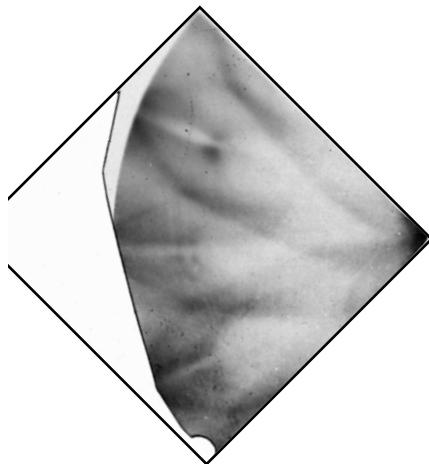
On MAGPIE see enhanced emission from imploding bubbles as they reach the inner array

Detailed image demonstrates this emission increases inside the inner wires

## Conical inner isolates snowplow from interaction

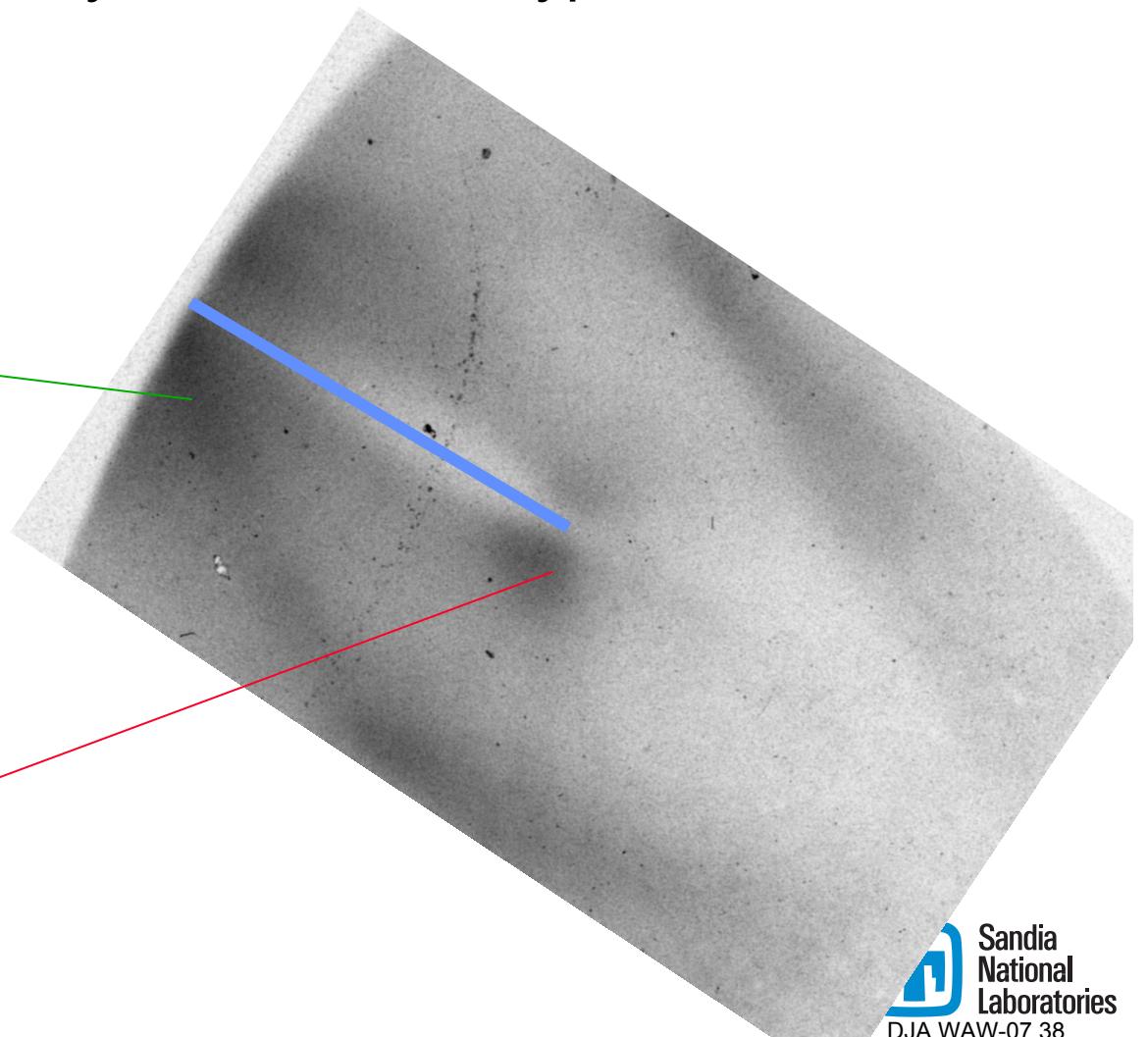
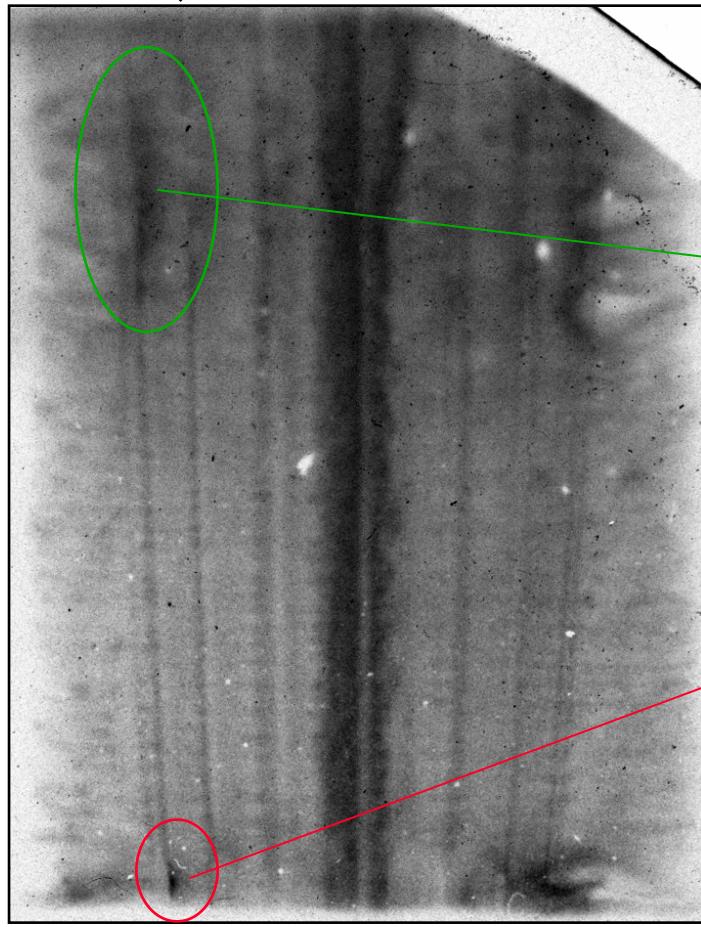
- Setup designed such that snowplow is constant along axis, however interaction time changes
- See emission from bubbles interacting with inner near for larger inner radius positions, but not at smaller inner radius



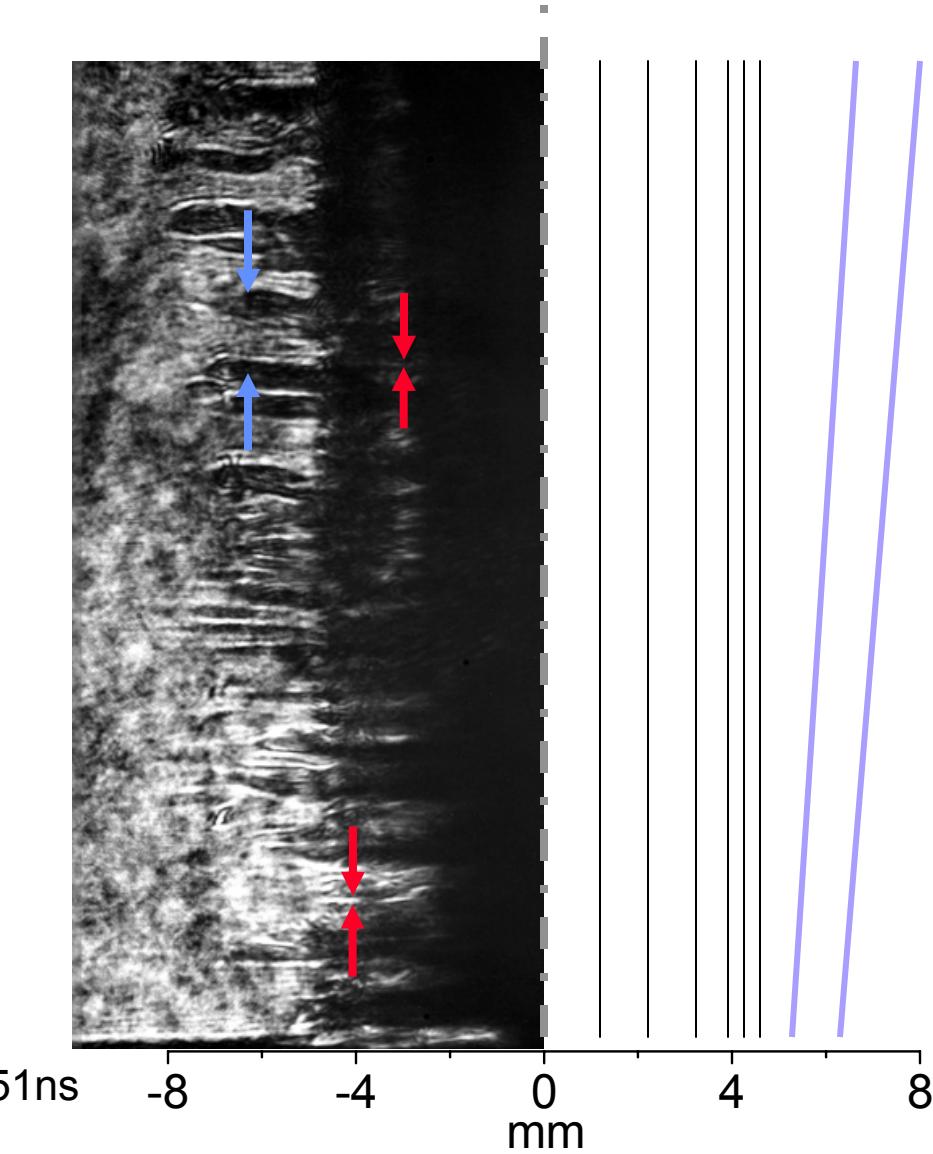


## End-on probing shows interaction

- See interaction emission surrounds wire, possibly in bow-shock type structure

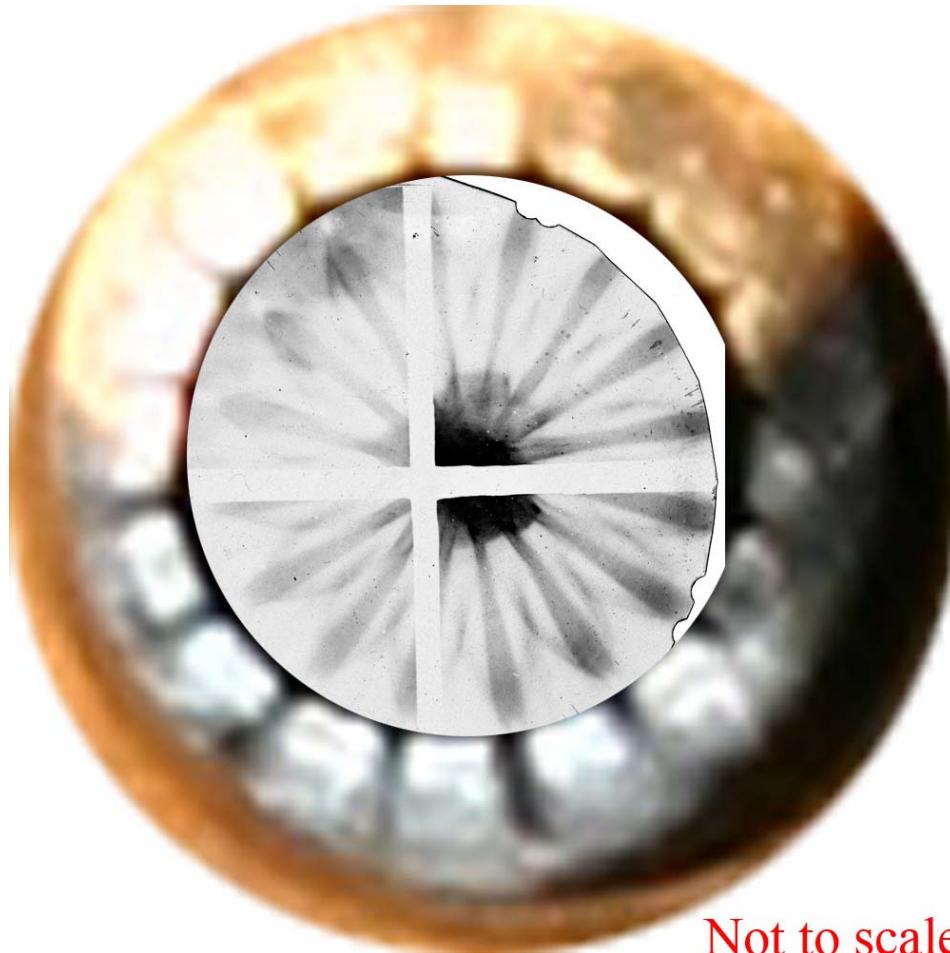


# Interaction with inner resets implosion wavelength

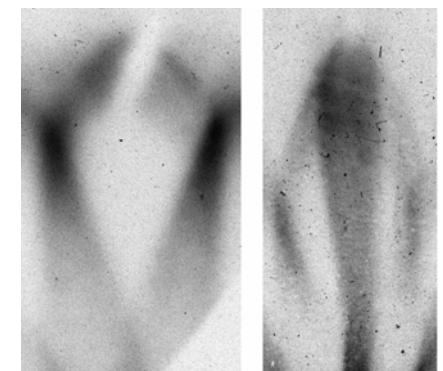


- Conical outer onto cylindrical inner shows change in wavelength is different before and after interaction with inner
- Interaction resets wavelength to sub-mm natural mode

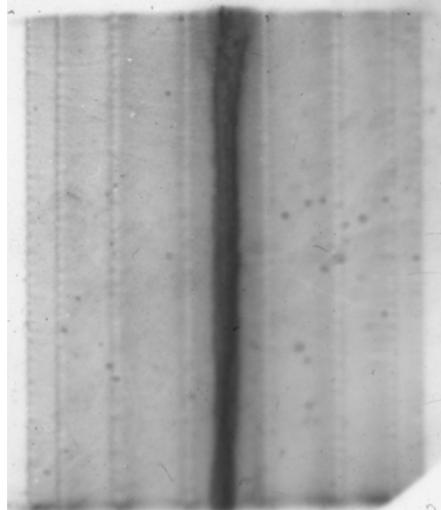
## End-on orientation



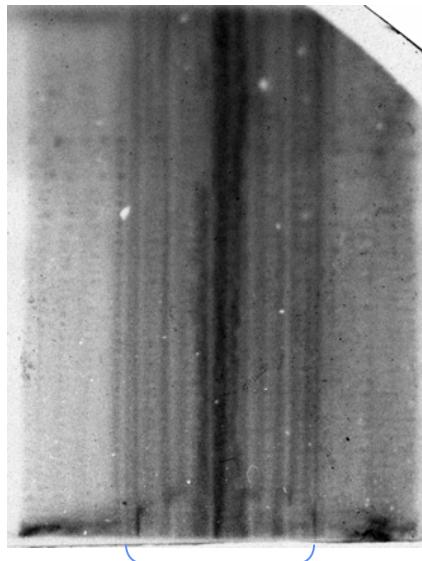
Not to scale



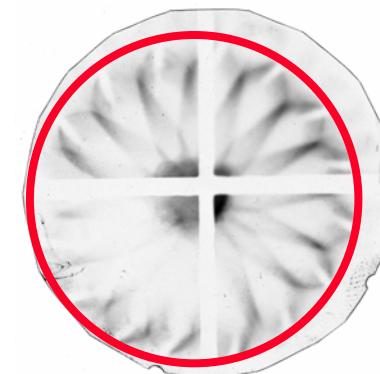
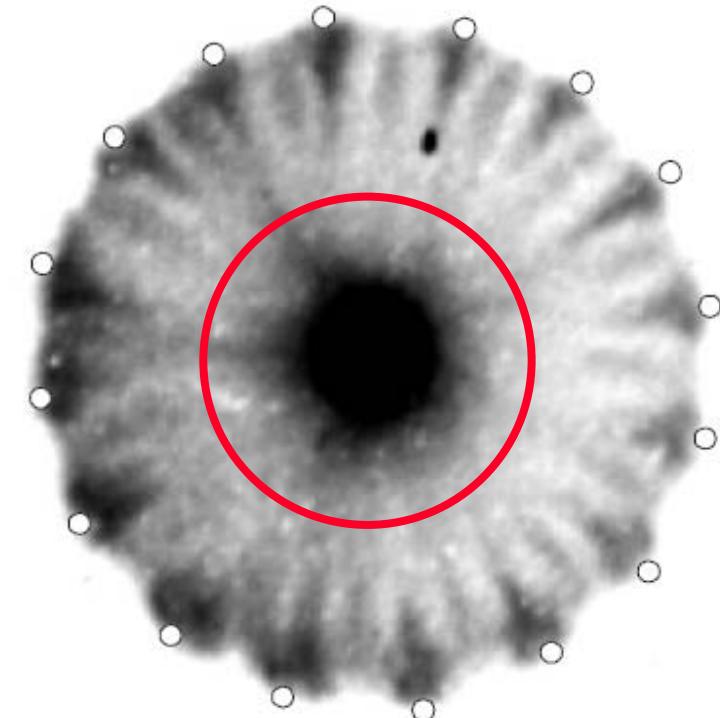
## Single/nested side-on and end-on



Single array  
(16 Al wires)

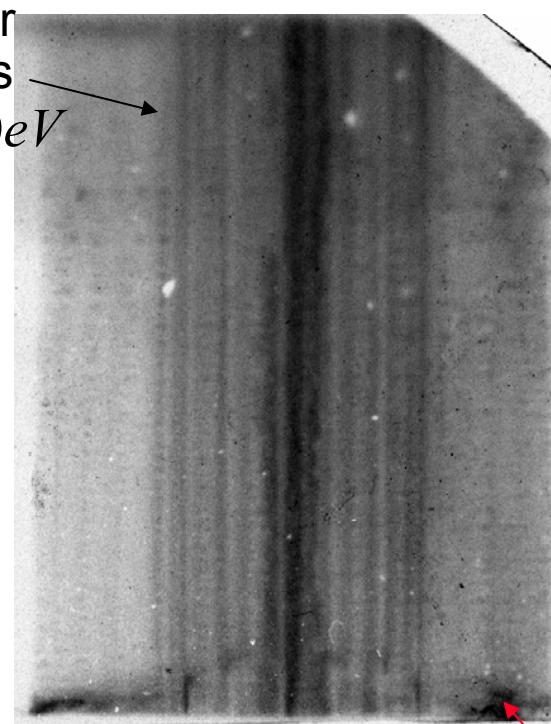
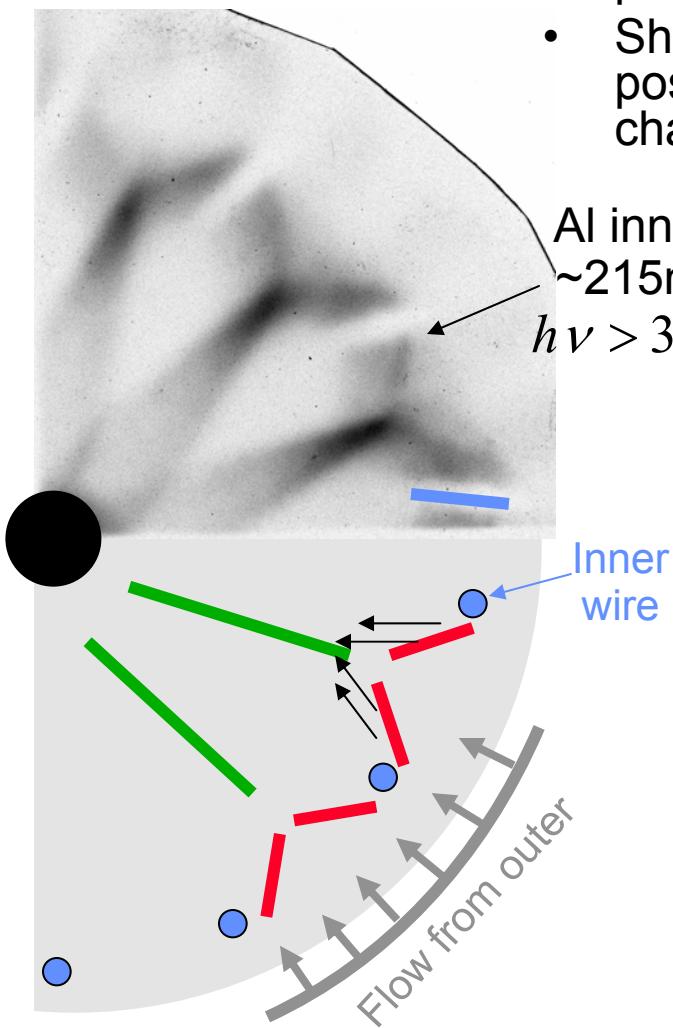


Nested array  
(32 Al onto 16 Al)



# Precursor plasma streams are shocked as they pass the inner array

- Ablated streams perturbed by presence of inner forming bow shocks
- Shock leads to increased emission at position of inner (shock heating and change in density distribution)



See APS poster GP1.00097  
by C.A. Jennings et al.

W inner, at 214ns

