

# Towards Formal Analysis of Device Authentication in Ubiquitous Computing

**Abstract**—Authentication between mobile devices in ubiquitous computing environments is a challenging problem. Indeed, without pre-shared knowledge, we will show that device authentication between previously unknown devices in this environment is not possible using a single broadcast channel alone. To address this problem, various techniques have been proposed, many using side-channels (or location limited channels) to transmit additional information. When discussing such protocols, however, an important topic is proving them correct, which requires analysis using some formal method such as BAN logic. However, this technique is not fully capable of analyzing many ubiquitous computing protocols, mainly because BAN logic does not consider the additional capabilities afforded by mobile devices when sending and receiving out-of-band information. We propose extensions to BAN logic that address these capabilities, enabling the careful analysis of mobile device authentication protocols. Furthermore, we demonstrate our extensions using two existing device authentication protocols.

**Keywords**-mobile communication, wireless LAN, protocols

## I. INTRODUCTION

The field of ubiquitous computing has shown tremendous growth over the past several years, both in the sophistication and capabilities of devices, and in the variety of applications to which devices are being applied. Many people rely on *mobile devices*, such as smart phones, personal digital assistants (PDAs), tablets, and laptop computers to stay in touch with friends, family, co-workers, and other important contacts.

One core component of ubiquitous computing is communication with other devices. However, communication in this paradigm usually occurs using radio frequency (RF) transmission, which can be overheard by other devices. In some cases, this is not a problem, but often the communication between two devices is expected to be private. Consider a credit-card transaction between a smart-phone and a movie-ticket kiosk; the consumer's credit card information should be protected from eavesdropping. The most common method for protecting information sent via unsecured channels such as RF is encryption. However, this raises additional issues. First, devices in ubiquitous computing are usually constrained in both power and computational capabilities, making some encryption techniques either too expensive in terms of power consumption, or undesirable in terms of time. Fortunately, advances in device hardware have addressed this concern very well. Second, in order to encrypt information, both the sender and receiver must agree on the method of encryption, as well as key information. While this is a relatively simple operation between two machines operating

in a wired, trusted environment, accomplishing key establishment between devices in untrusted environments presents several challenges. The greatest of these challenges is *device authentication*, which means ensuring that only the intended devices are those actually communicating. Put another way, it is ruling out the possibility that an unknown device, or “man-in-the-middle,” is present and intercepting data between the devices. This challenge is especially difficult because devices in ubiquitous computing are not assumed to possess a priori knowledge of each other.

Several solutions have appeared to date, proposing authenticated information exchange between mobile devices using an array of methods other than the standard broadcast channel. These are sometimes called *out-of-band*, *side-channels* or *location-limited channels* (LLCs), and include audio, visual, infrared, ultrasound, and even laser transmission. While not necessarily providing confidentiality, they allow the receiver of the device to physically verify the source of the transmission. Using the authenticated information received, secure key establishment can occur.

In standard computing environments, authentication protocols are subject to rigorous performance analysis and verification. One tool for doing this is known as BAN Logic [1]. This work presents a logic of *belief*, which is basically the process of coupling assumptions about current states with a simple set of steps and reasoning, to arrive at a conclusion regarding the soundness of an authentication protocol. It has been used extensively to identify flaws in new and existing security protocols, and is often employed by authors to prove new proposals sound.

However, applying such formal analysis to device authentication protocols in mobile computing has not been studied to date. Questions arise such as: can the device authentication protocols that use location-limited channels be shown correct using protocol analysis techniques such as BAN logic? More importantly, are location-limited channels a necessary component of device authentication between mobile devices in ubiquitous computing?

In this paper, we seek to answer these questions. Specifically, we show that device authentication between previously unknown devices in ubiquitous computing is not possible using only a single broadcast channel for communication. Next, we attempt a formal analysis of device authentication protocols that use LLCs. However, as originally proposed, BAN logic is insufficient to address the characteristics of such protocols, so we propose two extensions to BAN logic to support them. To demonstrate our extension, we show the

analysis of a basic bi-directional location-limited channel device authentication protocol. Then, we analyze a more complicated, asymmetric device authentication protocol between two mobile devices.

The remainder of this paper is organized as follows. Section II discusses background material and related works. Section III considers device authentication using a single broadcast channel only, while Section IV extends BAN logic to support analysis of device authentication protocols. Section V demonstrates the use of these extensions, and Section VI concludes the paper with a discussion of future work.

## II. BACKGROUND

Mobile computing environments generally do not assume the presence of a trusted authority (TA) to provide verified authentication information, such as public keys. Therefore, to authenticate public keys, another solution is necessary, and several approaches have been developed to address this problem. Solutions requiring some sort of additional knowledge, passed between users either in the form of a password or via some other communication channel besides the standard channel make up the bulk of the work on this subject.

1) *Location-Limited Channels*: In one of the first works on the subject, the “Resurrecting Duckling” protocol [2] is proposed, which uses physical touch between a mobile device and a desired target to transmit authentication information. Building on this concept, one of the most widely referenced techniques for verifying key establishment is proposed by [3] and introduces three components: *location-limited channels*, *demonstrative identification*, and *pre-authentication*. Location-limited channels (LLC) are a means of communication between two devices with the property that the operators of the devices have control over which devices are communicating. Unlike radio frequency (RF), where the sending and receiving devices are not easily identifiable, LLCs could include non-RF communication. Demonstrative identification describes the process by which the sending device is authenticated simply by sending information via the LLC. For instance, a kiosk showing a video display of a two-dimensional barcode can be verified as the source of the data simply by looking at it - it demonstrates that the information being shown originated from that device. Although this seems rather simple and intuitive, it plays a key role in key establishment protocols between mobile devices. Pre-authentication is the process of identifying the devices to communicate, and exchanging information over the LLC between them. Using that information, key establishment can occur.

A protocol for device authentication using these two concepts, shown in Table I using a protocol trace developed in [4], has served as the basis for most of the later work on the subject [3]. Using this protocol and an LLC, devices

#	Ch	Alice	Bob
1	LL	$\rightarrow Addr_{Alice}, H\{K_{Alice}\}$	
2	LL	$\leftarrow Addr_{Bob}, H\{K_{Bob}\}$	
3	RF	$\leftarrow$ Key exchange protocol	$\rightarrow$

Table I  
BASIC PROTOCOL FOR EXCHANGING KEYING INFORMATION VIA A LOCATION-LIMITED CHANNEL (CH: COMMUNICATION CHANNEL, RF: RADIO FREQUENCY, LL: LOCATION-LIMITED)

exchange information - specifically, the network addresses of the devices and the hash values of the devices’ public keys. Then, using the network addresses exchanged, the devices establish communication over the normal channel and request the others’ public key. The key received is hashed and compared to the value received via the LLC. If the values match, then the public key is authenticated.

2) *Building on Location-Limited Channels*: Many works build upon the foundations established by [3]. Approaches based on visual channels are proposed in [5]–[10], audio transmission [11]–[15], infrared [3], ultrasound [16], and facial recognition [17] or other biometric identification techniques such as grip pattern analysis [18]. While most of these approaches use two-way LLC transmission (as seen in Table I), some of them achieve device authentication using only one LLC transmission [4], [10], [15].

3) *Device Authentication Without a Side-Channel*: One approach to device authentication appears to use no additional side-channel [19]. This solution is based on a technique called *distance bounding* [20], in which the distance between devices is known, or can at least be bounded to within the transmission range of both devices. We believe this technique violates the constraints of true ad-hoc authentication in mobile computing by placing the constraint of close physical proximity on mobile devices for the entire duration of the device authentication protocol. Furthermore, the transmission range of devices and absence of an active attacker, employing jamming techniques for instance, is very difficult to ascertain. Therefore, we do not consider this solution an answer to the problem of device authentication in ubiquitous computing using a single broadcast channel only.

### A. BAN Logic Basics

We can turn to formal methods as a tool in evaluating the soundness of proposed authentication protocols. An approach to formalizing the logic associated with authentication, called “BAN Logic,” is presented in [1]. This work presented a logic of *belief*, which is basically the process of coupling assumptions about current states with a simple set of steps and reasoning, to arrive at a conclusion regarding the soundness of an authentication protocol. It has been used extensively to identify flaws in new and existing security protocols, and is often employed by authors to prove new

proposals sound.

BAN logic is not without limitation, however. Various issues have been identified with the original BAN Logic [21]–[23]. Specifically, these works point out that BAN Logic can be used to show an authentication protocol secure, when in fact it is insecure. While the creators of BAN logic refute at least one of these claims [24], others have shown that often the issue is a result of ambiguous assumptions [25], [26], which should be more carefully specified. Additional approaches have been published to clarify the original protocol by developing a semantic model for BAN logic [27], and other approaches have been proposed to extend BAN logic’s capabilities, as well as address some of the concerns [25], [28]. A fourth approach was proposed by [29] that combined the approaches of previous works to generate a unified logic. These subsequent approaches often add additional components or logic to allow more complex protocols to be correctly analyzed. However, the original BAN logic continues to be used by authors to prove authentication protocols, generally due to the simplicity of the approach [30].

*Constructs:* We must first cover several basic components of BAN logic, including its constructs and postulates. The constructs are represented as follows [1]:

- $A \equiv X$ : ***A believes X.***  $A$  may act as though  $X$  is true.
- $A \triangleleft X$ : ***A sees X.***  $A$  has received a message containing  $X$ .
- $A \sim X$ : ***A said X.***  $A$  once said  $X$ , though when  $X$  was said is unknown.
- $A \Rightarrow X$  : ***A controls X (A has jurisdiction over X).***  $A$  is an authority on  $X$  and should be trusted to provide a correct  $X$ .
- $\sharp(X)$  : ***X is fresh.***  $X$  has not been sent in any previous message during the current protocol run.  $X$  is typically a *nonce*.
- $A \xleftarrow{K} B$  :  $K$  is a shared key  $A$  and  $B$  may use to communicate
- $\xrightarrow{K} A$  :  $K$  is the public key of  $A$ , with a matching secret key  $K^{-1}$  that remains secret to  $A$  or any principal trusted by  $A$ .
- $A \xrightleftharpoons{X} B$  :  $X$  is a *secret* formula, such as a password, known only to  $A$  and  $B$ .
- $\{X\}_K$  : The formula  $X$  encrypted under  $K$ .
- $\langle X \rangle_Y$  :  $X$  combined with formula  $Y$ . Usually,  $Y$  is a secret, and its presence proves the identity of whoever utters  $\langle X \rangle_Y$ .

*Postulates:* The postulates which manipulate these constructs are as follows:

*Message-Meaning Rule* If  $A$  believes  $K$  is the shared key with  $B$ , and  $A$  sees  $X$  encrypted under  $K$ , then  $A$  believes  $B$  once said  $X$ :

$$\frac{A \text{ believes } A \xleftarrow{K} B, A \text{ sees } \{X\}_K}{A \text{ believes } B \text{ said } X}$$

Or, written using the construct notation (as all future postulates will be):

$$\frac{A \equiv A \xleftarrow{K} B, A \triangleleft \{X\}_K}{A \equiv B \sim X}$$

For public key cryptography, the postulate is similar:

$$\frac{A \equiv \xrightarrow{K} B, A \triangleleft \{X\}_{K^{-1}}}{A \equiv B \sim X}$$

For instances where the key is simply a shared secret, such as a password, the postulate is:

$$\frac{A \equiv A \xleftarrow{Y} B, A \triangleleft \langle X \rangle_Y}{A \equiv B \sim X}$$

*Nonce-Verification Rule* This rule checks to see if the message was sent recently, that is, the sender still believes in the message. If  $A$  believes  $X$  is fresh, and  $A$  believes  $B$  once said  $X$ , then  $A$  believes  $B$  believes  $X$ .

$$\frac{A \equiv \sharp(X), A \equiv B \sim X}{A \equiv B \equiv X}$$

*Jurisdiction Rule* If  $A$  believes that  $B$  has jurisdiction over  $X$ , and  $A$  believes  $B$  believes  $X$ , then  $A$  trusts  $B$  on the truth of  $X$ , thus  $A$  believes  $X$ :

$$\frac{A \equiv B \Rightarrow X, A \equiv B \equiv X}{A \equiv X}$$

### III. USING BAN LOGIC TO ANALYZE AUTHENTICATION IN MOBILE COMPUTING

First, we must establish the conditions by which the problem of device authentication in mobile computing is bound. We assume the only channel of communication is a wireless broadcast channel (RF), available to all devices, including those of an attacker. We assume no a priori knowledge exists between the two devices wishing to communicate securely. Furthermore, we assume the existence of an active attacker, who is able to intercept and modify the contents of RF transmissions between our two devices - this is commonly referred to as the “man in the middle.”

We will use BAN logic to analyze a basic question of authentication protocols for mobile computing: is authentication possible without the use of a side-channel (LLC, human interaction, etc.)? In considering this question, we make the following claim: *If* a protocol exists that allows device authentication without use of LLCs (i.e. using RF communication only), *then* it can be verified to be correct using BAN logic.

It is important to note that we assume both parties participating in the authentication protocol are trustworthy. That is, neither device knowingly provides incorrect information. This is consistent with [1], which does not deal with authentication of untrustworthy principals, stating “We focus on the beliefs of trustworthy parties involved in the protocols

and on the evolution of these beliefs as a consequence of communication.” Other security protocol analysis works also make this assumption [31]–[34].

### A. Analyzing Authentication in Mobile Computing

Let us consider the following definitions regarding our environment and goals:

**Definition 1.** *A device authentication protocol is a procedure for identifying the identity of another device on a network.*

**Definition 2.** *Ad-hoc computing environments exhibit the following characteristics:*

- *No pre-shared, or a priori, knowledge exists between devices*
- *Device location is not fixed, nor is device proximity assumed*
- *Only a broadcast method of communication is used for normal data transfer*

We must establish these definitions for several reasons. First, it is important to be very clear about our definition of “ad-hoc computing,” as interpretations have been proposed which differ from ours [19]. Next, we must remove any ambiguity regarding the meaning of “device authentication” protocols. It is essential that we be clear about these definitions in order to proceed with the following proposition regarding device authentication in ad-hoc computing:

**Proposition III.1.** *Key-based device authentication between two previously unknown mobile devices in an ad-hoc computing environment is not possible using only a single broadcast communication channel.*

*Proof:* We will prove this proposition by contradiction. To do so, we will assume that there *is* a protocol for device authentication between two previously unknown devices in an ad-hoc environment that does *not* use additional information, such as that provided by a demonstrative side-channel, and attempt to prove this assumption correct.

Let us first establish the goals of device authentication. The goals of authentication, according to [1], can vary, but generally consist of a shared session key between two entities, that is:

$$\begin{aligned} A \equiv A &\xleftrightarrow{K} B \\ B \equiv A &\xleftrightarrow{K} B \end{aligned}$$

Because we assume no a priori knowledge between devices, the shared key  $A \xleftrightarrow{K} B$  must be established via the authentication protocol between  $A$  and  $B$ , it cannot be assumed to exist beforehand. There are two possible cases for authentication protocols that are key-based: those that use symmetric keys and those that use asymmetric keys.

*Case 1: Symmetric Keys.:* Device authentication protocols using symmetric keys, by the very definition of symmetric keys, assume that information is already shared between both devices - specifically a shared symmetric key. It is trivial to show, because this violates the constraints we have established for key-based device authentication in mobile computing, that this family of protocols is not possible.

*Case 2: Asymmetric Keys.:* For device authentication protocols utilizing asymmetric keys, it is required that each device *know* the public key of the other device. Doing so requires that each device, at some point during the mutual device authentication protocol, *receives* the public key of the other device. To put it formally, at some point, the following must occur:

$$\begin{aligned} A \rightarrow B : &\xrightarrow{K_A} A \\ B \rightarrow A : &\xrightarrow{K_B} B \end{aligned}$$

However, simply receiving a public key does not assure a device that it is the authentic public key of the intended target device. Therefore, the goal in this protocol is more stringent, specifically, it is assurance the public key of the sending device is authentic, or to put it formally:

$$\begin{aligned} A \equiv &\xrightarrow{K_b} B \\ B \equiv &\xleftarrow{K_a} A \end{aligned}$$

Note that both components are required for mutual device authentication to occur. We will therefore begin with an analysis of the first component,  $A \equiv \xrightarrow{K_b} B$ .

*Case 2.1: Authenticating B to A.:* Typically, when proving a protocol using BAN logic, assumptions are established first. We assume the following for our hypothetical device authentication algorithm:

$$\begin{aligned} A \equiv &\xrightarrow{K_a} A & B \equiv &\xrightarrow{K_b} B \\ A \equiv A &\xrightarrow{K_a} A & B \equiv B &\xrightarrow{K_b} B \\ A \equiv B &\xrightarrow{K_b} B & B \equiv A &\xrightarrow{K_a} A \\ A \equiv \#(\xrightarrow{K_a} A) & & B \equiv \#(\xrightarrow{K_b} B) & \\ A \equiv \#(\xrightarrow{K_b} B) & & B \equiv \#(\xrightarrow{K_a} A) & \\ \neg(A \equiv \xrightarrow{K_b} B) & & \neg(B \equiv \xrightarrow{K_a} A) & \end{aligned}$$

Most of these assumptions are obvious. However, the assumptions in the last row require a brief explanation. Normally, we only state what we assume to be true, rather than what we assume is *not* true. However, in this case, these statements of negation are necessary because of the ad-hoc computing environment. It is not enough to omit the assumption that we believe a specific public key belongs another device, we must explicitly state that we do *not* believe a specific public key belongs to another device, because an ad-hoc environment explicitly excludes this type of prior knowledge.

Working backwards from our goal, by the jurisdiction rule, we see that for  $A \equiv \xrightarrow{K_b} B$  to be true, we must establish  $A \equiv B \Rightarrow \xrightarrow{K_b} B$  and  $A \equiv B \equiv \xrightarrow{K_b} B$ . We assume  $A \equiv B \Rightarrow \xrightarrow{K_b} B$ , that is,  $B$  has control of its own public key. To establish the second part of this rule,  $A \equiv B \equiv \xrightarrow{K_b} B$ , we must establish  $A \equiv \sharp(\xrightarrow{K_b} B)$  and  $A \equiv B \succ \xrightarrow{K_b} B$ .

Considering our assumptions, we see that only  $A \equiv \sharp(\xrightarrow{K_b} B)$  is shown. To establish  $A \equiv B \equiv \xrightarrow{K_b} B$ , we would need to show that  $A \equiv B \succ \xrightarrow{K_b} B$ . This is achieved either by assumption (which we do not have) or by the message-meaning rule, which stipulates  $A \equiv \xrightarrow{K_b} B$  and  $A \triangleleft \{X\}_{K_b^{-1}}$  must be true for  $A \equiv B \succ \xrightarrow{K_b} B$ . However, this contradicts our assumption  $\neg(A \equiv \xrightarrow{K_b} B)$ , and therefore, Case 2.1 is not possible.

*Case 2.2: Authenticating A to B.:* By symmetry, Case 2.2 is also not possible.

*Final Steps.:* By analyzing the necessary steps for key-based device authentication protocols between two previously unknown mobile devices, we have demonstrated that such protocols under the constraints of ad-hoc computing are not possible using only a single broadcast communication channel. Because our example is representative of any key-based device authentication protocol operating under the constraints of ad-hoc computing, and we have shown that such an protocol is not possible, we have successfully proven our proposition. ■

In essence, what BAN logic tells us about the constraints of ad-hoc computing is that it is necessary to have some sort of basis to believe a message was sent from a particular device. Because we use a broadcast method of communication, we cannot make any statements about the origin of a particular message simply because we suppose it came from a specific device, or the message claims to have originated from a specific device. To *prove* that a message originated from a specific device, BAN logic tells us that the message must have been encrypted (or otherwise encoded) using a key (or secret) that  $A$  believes is either shared with  $B$ , or belongs to  $B$ . There is no other way, using the BAN logic constructs and postulates we specified, to form a belief about the origin of a message.

#### IV. AN ADDITIONAL COMPONENT TO BAN LOGIC FOR MOBILE COMPUTING

If we cannot achieve device authentication using only a single broadcast channel, suppose data  $X$  is transmitted from  $B$  to  $A$  using a side-channel, or LLC. This allows the users of each device to identify the other device, establishing the origin of the data received (*demonstrative identification* [3].) This additional information exchanged supplies the conditions necessary to establish our goals. While the data can also be seen by an attacker, an attacker is not able to modify the data transmitted. The receiving device

knows with certainty the information was said by the sending device.

Doing so allows us to conclude the following:

$$\begin{array}{c} A \triangleleft X \\ A \equiv B \succ X \end{array}$$

The last statement is of particular importance. Under the message-meaning rule and normal communication, to establish  $A \equiv B \succ X$  would require us to establish  $A \equiv \xrightarrow{K_b} B$  and  $A \triangleleft \{X\}_{K_b^{-1}}$ . However, since we are using another method which allows  $A$  to verify the origin of  $X$ , we can establish  $A \equiv B \succ X$  without using the message-meaning rule.

This is an extension to BAN logic afforded by the properties of LLCs, and to assist in our proofs of device authentication protocols, we will denote this extension using the following construct:

$$A \xleftarrow{X} B : A \text{ receives } X \text{ from } B \text{ via a channel by which} \\ A \text{ can verify the origin of } X \text{ is } B.$$

The following postulate will also be added:

*Side-Channel-Communication (SCC) Rule* If  $A$  receives  $X$  from  $B$  via a side-channel, then  $A$  sees  $X$ , and  $A$  is entitled to believe  $B$  said  $X$ :

$$\frac{A \xleftarrow{X} B}{A \triangleleft X, A \equiv B \succ X}$$

#### A. Handling Hash Functions

The device authentication protocol we seek to prove correct involves the transmission of hash values via the side-channel. However, this raises serious issues; specifically, how do we treat hash values with respect to the constructs and postulates of BAN Logic? The authors of BAN logic, in an extended technical report [35], propose a postulate for handling a hash function  $H$ , as follows:

$$\frac{A \equiv B \succ H(X), A \triangleleft X}{A \equiv B \succ X}$$

However, it is clear from their work that  $H(X)$  refers to signed hashes, not an arbitrary hash function, as the authors state, “If  $H$  is an arbitrary function, nothing convinces one that when  $A$  has uttered  $H(m)$  he must have also uttered  $m$ . In fact,  $A$  may never have seen  $m$ .”

How then are we to deal with the use of arbitrary hash functions in our protocols? According to [35] we cannot assume that because  $B$  said  $H(X)$ ,  $B$  also said  $X$ . However, we can deduce the following: if  $A$  believes  $H(X)$ , and sees some message  $Y$  (not necessarily from  $B$ ), and confirms that  $H(Y)$  equals  $H(X)$ , then  $A$  can reasonably assume that  $Y$  equals  $X$ , and can say that  $A$  sees  $X$ <sup>1</sup>. However, what we

<sup>1</sup>Although we recognize that collisions exist in hash functions, we assume the use of strong cryptographic hash functions for this step. Assuming an attacker is unable to produce a collision (i.e. generate  $Y \neq X$  such that  $H(Y) = H(X)$ ) in this case is similar to assuming an attacker is unable to decrypt encrypted messages in other BAN logic postulates

really need to determine is: did  $B$  say  $X$ ?

To help with this determination, we must first reveal an implicit assumption within the constructs of BAN logic, specifically, the notion of *uniqueness*. In all postulates involving a key  $K$ , it is assumed  $K$  is unique. For instance, we assume  $\overset{K}{\leftrightarrow} A \neq \overset{K}{\leftrightarrow} B$ . In other words, without the assurance that  $K$  is unique, the message-meaning rule would not be true, if it were possible that  $\overset{K}{\leftrightarrow} A = \overset{K}{\leftrightarrow} B$ . Uniqueness of keys is a safe assumption to make in the case of sufficiently large cryptographic keys, and for secret data that is generated prior to protocol execution.

However, in the case of hash values, it is not safe to say that all values generated are unique. Virtually any cryptographic hash function will generate an infinite number of collisions for an infinite input set. Additionally, two entities hashing the same value, using the same hash function, will return identical hashes. Consider the case where  $A$  generates the hash value of the word “cat,” and  $B$  also generates the value of the word “cat”. If they both use the same hashing function, they will both return the same value, and it will be impossible to determine which entity performed the hash. This is the problem stated by [35] above.

However, if we make a stronger assumption about the value being hashed, that is, that the  $X$  which is used to generate  $H(X)$  is unique, then we can also assume that  $H(X)$  is unique<sup>2</sup>. We will use this belief in comparing values and their hashes during our communication protocol. We can say that if we have a hash value  $H(X)$ , and we receive another value  $Y$ , that we may determine  $Y = X$  if we can show  $H(Y) = H(X)$ , as long as we believe  $X$  is unique.

Combining the notion of uniqueness with the BAN logic construct of jurisdiction, we may conclude the following. If  $A$  believes  $B$  is an authority on  $X$ , and  $A$  believes  $X$  is unique, then  $A$  may believe  $B$  created  $X$ . More importantly,  $A$  may conclude that no other entity could have independently created  $X$ . So, once  $A$  establishes that it sees  $X$  (realizing that  $A$  has no foreknowledge of the value of  $X$ , so it is still incumbent on the protocol to establish the value of  $X$ , as well as its origin in  $B$ ),  $A$  may conclude that at some point in time,  $X$  was said by  $B$ .

To show that we consider a value to be unique, we propose the following additional construct:

$\dagger(X)$ :  $X$  is considered to be sufficiently unique that two entities independently generating the same  $X$  is considered computationally unlikely.

The applications of this construct extend beyond hash functions. For instance, uniqueness could be used to describe newly generated symmetric or asymmetric keys. If  $A$  and  $B$  independently generate  $K_A$  and  $K_B$ , they should be unique.

<sup>2</sup>This is not absolutely true. As stated previously, hash functions generate infinite numbers of collisions. We assume a sufficiently complex hash function is used, making the chance of a collision computationally unlikely (i.e. using SHA256 results in a collision probability of 1 in  $10^{153}$ ).

Now we can address the question of establishing which entity *said*  $X$ , based on our beliefs about  $X$  and  $H(X)$ . We do this by adding some constraints to the hashing postulate proposed by [35], making it correct for arbitrary hash functions. Our proposed addition is as follows:

*Hash Analysis Rule* If  $A$  believes  $B$  controls  $X$ , and if  $A$  believes  $X$  is unique, and if  $A$  believes  $B$  said  $H(X)$ , and  $A$  sees  $X$ , then  $A$  believes that  $B$  said  $X$ .<sup>3</sup>

$$\frac{A \equiv B \Rightarrow X, A \equiv \dagger(X), A \equiv B \sim H(X), A \triangleleft X}{A \equiv B \sim X}$$

Next, we consider why each component in this rule is necessary:

$A \equiv B \Rightarrow X$ :  $A$  has to believe  $B$  controls the value  $X$ , in our case,  $B$ 's public key.

$A \equiv \dagger(X)$ : As mentioned above, for this to hold,  $X$  cannot be independently generated anywhere else (within computational allowances); combined with the previous component, this means  $A$  believes only  $B$  created  $X$ .

$A \equiv B \sim H(X)$ : This is necessary to verify  $A \triangleleft X$ . Otherwise,  $A$  has no way to know whether or not the message it sees is actually  $X$ . Despite the assumptions above,  $A$  does not initially know the value of  $X$ , but  $A$  does know the value of  $H(X)$ .

$A \triangleleft X$ : This is actually determined using another component in the same rule.  $A$  cannot know it has seen  $X$  until it compares  $H(X)$  to the value contained in  $A \equiv B \sim H(X)$ .

## V. APPLICATION

We will demonstrate the application of the SCC and Hash Analysis Rules by applying them to the formal analysis of two device authentication protocols. The first is a basic bi-directional protocol based on [3]. The second is a uni-directional protocol requiring only one LLC transmission [15].

*1) Proving the Basic Device Authentication Protocol Secure*: The basic mobile device key authentication protocol is shown in Table II. The first step in analyzing this protocol is to *idealize* the protocol, that is, to change it into a form more easily analyzed by the logic. (See [1] for more details on this process.) The idealized form of our protocol is as follows:

*Message 1* :  $A \rightarrow B : H(\overset{K_A}{\leftrightarrow} A)$

<sup>3</sup>For simplicity we assume the following trivial rule:

$$\frac{B \Rightarrow X}{B \Rightarrow H(X)}$$

#	Ch	Alice	Bob
1	LL		$\neg Addr_A, H(K_A) \rightarrow$
2	LL		$\leftarrow Addr_B, H(K_B) -$
3	RF		$\neg K_A \rightarrow$
4	RF		$\leftarrow K_B -$
5		Calc $H(K_B) \#4$	Calc $H(K_A) \#3$
6		$H(K_B) \#4 \stackrel{?}{=} H(K_B) \#2$	$H(K_A) \#3 \stackrel{?}{=} H(K_A) \#1$

Table II  
SIMPLE PROTOCOL FOR AUTHENTICATING PUBLIC KEYS VIA A LOCATION-LIMITED CHANNEL

Message 2 :  $B \rightarrow A : H(\xrightarrow{K_B} B)$

Message 3 :  $A \rightarrow B : \xrightarrow{K_A} A$

Message 4 :  $B \rightarrow A : \xrightarrow{K_B} B$

The assumptions we make are as follows:

$$\begin{array}{ll}
 A \equiv \xrightarrow{K_A} A & B \equiv \xrightarrow{K_B} B \\
 A \equiv A \xrightarrow{K_A} A & B \equiv B \xrightarrow{K_B} B \\
 A \equiv \sharp(\xrightarrow{K_B} B) & B \equiv \sharp(\xrightarrow{K_A} A) \\
 A \equiv \sharp(H(\xrightarrow{K_B} B)) & B \equiv \sharp(H(\xrightarrow{K_A} A)) \\
 A \equiv B \xrightarrow{K_B} B & B \equiv A \xrightarrow{K_A} A \\
 A \equiv B \xrightarrow{H(\xrightarrow{K_B} B)} & B \equiv A \xrightarrow{H(\xrightarrow{K_A} A)} \\
 A \equiv \dagger(\xrightarrow{K_B}) & B \equiv \dagger(\xrightarrow{K_A})
 \end{array}$$

Why is  $\sharp(\xrightarrow{K_A} A)$ ,  $\sharp(H(\xrightarrow{K_A} A))$ ,  $\sharp(\xrightarrow{K_B} B)$ ,  $\sharp(H(\xrightarrow{K_B} B))$  assumed in this protocol? This may seem to be a poor assumption to make. The notion of *freshness* is BAN logic is meant to assure that the messages being exchanged are recently generated (during the current run of the protocol), and not being replayed by an attacker. It could be argued that the properties of side-channels prevent a replay attack of the data transmitted ( $A$  knows that the information came immediately from  $B$ , therefore, it is fresh). We use this reasoning in our assumptions above. However, a more complete notion of freshness would be assured if some nonce were included in the side-channel data, or if the side-channel data were generated uniquely for each instance of communication [9]. This would assure the sending device,  $B$ , that subsequent protocol messages from  $A$  were, in fact, fresh.

Note that both  $A$  and  $B$  trust the other on the correctness of their respective public keys. This is a staple of BAN logic, we assume our counterpart is trustworthy, that is, it has not been compromised to provide incorrect information. We do not, however, assume that anything purported to be received by  $A$  from  $B$  is actually from  $B$ ; deciding that is the purpose of the message-meaning rule.

The main steps of our proof are as follows:

$B$  receives message 1. The SCC rule yields that:

$$B \triangleleft H(\xrightarrow{K_A} A), B \equiv A \succsim H(\xrightarrow{K_A} A)$$

Likewise, receiving message 2 yields for  $A$ :

$$A \triangleleft H(\xrightarrow{K_B} B), A \equiv B \succsim H(\xrightarrow{K_B} B)$$

Since we have the assumptions

$$\begin{aligned}
 A \equiv \sharp(H(\xrightarrow{K_B} B)) \text{ and} \\
 B \equiv \sharp(H(\xrightarrow{K_A} A))
 \end{aligned}$$

We can apply the nonce-verification rule to get

$$\begin{aligned}
 A \equiv B \equiv H(\xrightarrow{K_B} B) \text{ and} \\
 B \equiv A \equiv H(\xrightarrow{K_A} A)
 \end{aligned}$$

Recall we also assume

$$\begin{aligned}
 A \equiv B \xrightarrow{H(\xrightarrow{K_B} B)} \text{ and} \\
 B \equiv A \xrightarrow{H(\xrightarrow{K_A} A)}
 \end{aligned}$$

Next, we apply the jurisdiction rule to get

$$\begin{aligned}
 A \equiv H(\xrightarrow{K_B} B) \text{ and} \\
 B \equiv H(\xrightarrow{K_A} A)
 \end{aligned}$$

Next, we consider messages 3 and 4, where we find  $A$  and  $B$  receive messages purporting to be  $K_B$  and  $K_A$ , respectively. However, since these messages do not come from known sources, we will call them  $Y$  and  $Z$  for now.

$$\begin{aligned}
 A \triangleleft Y \text{ and} \\
 B \triangleleft Z
 \end{aligned}$$

We use our hash analysis reasoning to check that  $H(Y)$  equals  $H(K_B)$  and  $H(Z)$  equals  $H(K_A)$ . (This is step 5 and 6 in the protocol listed in Table II.) Because they match, we now assume

$$\begin{aligned}
 A \triangleleft \xrightarrow{K_B} B \text{ and} \\
 B \triangleleft \xrightarrow{K_A} A
 \end{aligned}$$

Next, we recall our assumptions

$$\begin{aligned}
 A \equiv B \xrightarrow{K_B} B \text{ and} \\
 B \equiv A \xrightarrow{K_A} A \text{ and} \\
 A \equiv \dagger(\xrightarrow{K_B}) \text{ and} \\
 B \equiv \dagger(\xrightarrow{K_A})
 \end{aligned}$$

We couple those assumptions with the previously determined statements and apply them to our Hash Analysis Rule to achieve

$$A \equiv B \succsim \xrightarrow{K_B} B \text{ and}$$

Table III  
UBI SOUND KEY ESTABLISHMENT PROTOCOL [15] (RF: RADIO FREQUENCY CHANNEL, LL: LOCATION-LIMITED CHANNEL, PB: MANUAL USER INTERACTION (PUSH-BUTTON))

#	Ch	Alice	Bob
1		Chooses $g^a$	
2	RF		$-g^a \rightarrow$
3			Chooses $g^b$
4			Chooses random $R_b$
5			$H_b = H(g^a g^b R_b)$
6	RF		$\leftarrow H_b -$
7	LL		$\leftarrow R_b -$
8	RF		$\leftarrow g^b -$
9		$H'_b = H(g^a g^b R_b)$	
10		Verifies $H_b = H'_b$	
11	PB		$-verify \rightarrow$

$$B \equiv A \sim \xrightarrow{K_A} A$$

Using the assumptions

$$\begin{aligned} A \equiv \sharp(\xrightarrow{K_B} B) \text{ and} \\ B \equiv \sharp(\xrightarrow{K_A} A) \end{aligned}$$

We can apply the nonce-verification rule to get

$$\begin{aligned} A \equiv B \equiv \xrightarrow{K_B} B \text{ and} \\ B \equiv A \equiv \xrightarrow{K_A} A \end{aligned}$$

Next, we apply the jurisdiction rule to get

$$\begin{aligned} A \equiv \xrightarrow{K_B} B \text{ and} \\ B \equiv \xrightarrow{K_A} A \end{aligned}$$

Which is the goal of our protocol.

#### A. One-way LLC for device authentication

In [15], a simplified the key establishment protocol, based on [4], is presented. This protocol is shown in Table III. The simplified protocol begins with both Alice and Bob selecting new public keys,  $g^a$  and  $g^b$ . Alice sends her public key,  $g^a$ , to Bob using the unsecured wireless channel. Bob then chooses a random number,  $R_b$ , of sufficient size to prevent guessing by Marvin, the adversary. Next, Bob calculates a hash value,  $H_b$ , as the concatenation of  $g^a$ ,  $g^b$ , and  $R_b$ , and sends  $H_b$  to Alice using the unsecured channel.

The next step involves the LLC.  $R_b$  is encoded and transmitted over this channel, followed by Bob's public key,  $g^b$ , which is sent over the unsecured wireless channel. After receiving  $g^b$ , Alice has all the information she needs to calculate  $H'_b = H(g^a|g^b|R_b)$ , and verify that  $H_b = H'_b$ . Because Alice can verify that  $R_b$  came from Bob, using the demonstrative identification [3] of the LLC, she can verify that  $H_b$  was also generated by Bob. Assuming that an adversary has not compromised Bob's device, this confirms to Alice that the information she received from Bob is authentic, verifying his device, his public key  $g^b$ , and allowing key establishment to commence.

How does Bob establish that he is communicating with Alice, though? This question is addressed in [4], and the answer is reasoned as follows. Bob does not receive any communication from Alice via an LLC, which may lead to the conclusion that Bob cannot demonstratively identify Alice's device. While this would be true for completely automated devices, we have the advantage of user interaction to complete the protocol. When Alice verifies she is communicating with Bob, she implicitly verifies to Bob that  $H_b$  is correct. Because  $H_b$  contains  $g^a$ , Alice's verification to Bob also confirms to Bob that he has used the correct values in calculating  $H_b$ , and those values can be trusted to establish a secure channel. Even if Bob were a kiosk device, he could receive confirmation from Alice via a push-button device, which only Alice would be able to press. ([4] points out that it would take an extremely sophisticated attacker to develop a button-pushing device that could not be detected by the kiosk user.)

1) *Proving the Protocol Correct:* We will use BAN logic to analyze the correctness of this protocol. To do so, we first establish the following assumptions:

$$\begin{aligned} A \equiv g^a & \quad B \equiv g^b \\ A \equiv A \Rightarrow g^a & \quad B \equiv B \Rightarrow g^b \\ A \equiv B \Rightarrow g^b & \quad B \equiv A \Rightarrow g^a \\ A \equiv \sharp(R_b) & \quad B \equiv \sharp(R_b) \\ A \equiv \dagger(g^a) & \quad B \equiv \dagger(g^b) \\ A \equiv \dagger(g^b) & \quad B \equiv \dagger(g^a) \\ A \equiv \dagger(R_b) & \quad A \equiv B \Rightarrow R_b \end{aligned}$$

Next, we idealize the protocol. According to [1], idealization of protocols involves removing any messages not encrypted. Doing so would leave us with the following idealized protocol:

$$\text{Message 1 : } B \rightarrow A : H(g^a, g^b, R_b)$$

While this is technically correct, according to the BAN logic analysis process, we must point out that we require additional information to be transmitted for the Hash verification step of the protocol. [1] argues that cleartext messages can be forged. However the hashing element of the protocol prevents cleartext messages, such as  $g^a$  and  $g^b$ , from being forged. Effectively, the hash component verifies the correctness of these values, and therefore they should be included in the protocol idealization. We also add the fifth message, the manual user interaction step "verify" between  $A$  and  $B$ , because this step also serves to validate information sent in cleartext during the protocol.

$$\begin{aligned} \text{Message 1 : } A \rightarrow B : g^a \\ \text{Message 2 : } B \rightarrow A : H(g^a, g^b, R_b) \\ \text{Message 3 : } B \rightarrow A : R_b \\ \text{Message 4 : } B \rightarrow A : g^b \\ \text{Message 5 : } A \rightarrow B : \text{ verification} \end{aligned}$$

Now we can prove the correctness of the protocol, the goal of which is for each device to believe the public key

of the other device, so secure key establishment may occur. Formally, this is:

$$\begin{aligned} A &\equiv g^b \text{ and} \\ B &\equiv g^a \end{aligned}$$

We begin by proving  $A \equiv g^b$ . In message 2, we see  $H(g^a, g^b, R_b)$  sent via LLC from  $B$  to  $A$ . By the side channel communication (SCC) rule, we obtain:

$$\begin{aligned} A &\triangleleft H(g^a, g^b, R_b) \text{ and} \\ A &\equiv B \triangleright H(g^a, g^b, R_b) \end{aligned}$$

Next, we apply the hash analysis rule. Because we assume  $A \equiv B \Rightarrow g^b$ ,  $A \equiv B \Rightarrow R_b$ ,  $A \equiv \dagger(g^b)$ ,  $A \equiv \dagger(g^a)$ , and  $A \equiv \dagger(R_b)$ , and we have deduced that  $A \equiv B \triangleright H(g^a, g^b, R_b)$ , knowing that  $A \equiv A \Rightarrow g^a$ , we combine these with message 4,  $A \triangleleft g^b$  to get:

$$A \equiv B \triangleright g^b$$

Next, we consider another component of BAN logic not yet mentioned, a freshness rule that states: if  $A$  believes one part of a formula is fresh, then the entire formula must also be fresh [1]. This is shown as follows:

$$\frac{P \equiv \sharp(X)}{P \equiv \sharp(X, Y)}$$

Using this rule, we can establish that since we assume  $\sharp(R_b)$ , we can deduce:

$$\begin{aligned} \sharp(g^a) \\ \sharp(g^b) \end{aligned}$$

Knowing that  $\sharp(g^b)$  and  $A \equiv B \triangleright g^b$ , we can apply the nonce-verification rule to obtain:

$$A \equiv B \equiv g^b$$

And because we assume  $A \equiv B \Rightarrow g^b$ , we can use the jurisdiction rule to obtain the desired result:

$$A \equiv g^b$$

This shows the first half of the protocol results. What about  $B \equiv g^a$ ? Actually,  $A$  establishes this for  $B$ . Consider what happens during step 10 of the protocol (shown in III).  $A$  verifies that the information from  $B$  is correct, according to what  $A$  sent and received using the LLC. So message 5 of the idealized protocol verifies for  $B$  that it has the correct information, allowing  $B$  to conclude the  $g^a$  it received in message 1 was actually said by  $A$  ( $A \triangleright g^a$ ). This also provides the belief in a fresh  $g^a$  for  $B$ , since  $A$  must have established  $\sharp(g^b)$  prior to the verification step (thus implying  $\sharp(g^a)$  by the freshness rule). We can apply these beliefs to the nonce-verification rule and jurisdiction rule to obtain the second half of the desired result:

$$B \equiv g^a$$

## VI. CONCLUSION AND FUTURE WORK

We have shown that device authentication in ubiquitous computing environments is not possible using only a single broadcast communication channel. However, using LLCs, we can achieve device authentication. Proving such a protocol correct requires extensions of BAN logic, which we proposed and demonstrated by analyzing two different device authentication protocols. Future work will include more detailed analysis of existing solutions, and the potential generation of new device authentication protocols for ubiquitous computing.

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