

Coherence of Donor Electron Spins in Isotopically Enriched Silicon

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What limits electron spin coherence in Silicon?

In particular, from spin noise:

Nuclear Spins	Electron Spins
^{29}Si , SiGe, other impurities.	P-donors, surface defects.
Hyperfine as well as dipolar interactions.	Only dipolar interactions.
Relatively weak dipolar interactions between nuclei.	Interactions all of comparable strength.
About 5% in natural Si, 50ppm has been achieved.	Coherence meas.: $10^{14}/\text{cm}^3$ Techn. limits: $10^{12}/\text{cm}^3$ - $10^{12}/\text{cm}^3$
Thermal polarization not feasible (sub-mK).	Thermal polarization is feasible (sub-K).

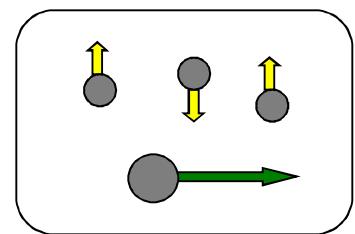
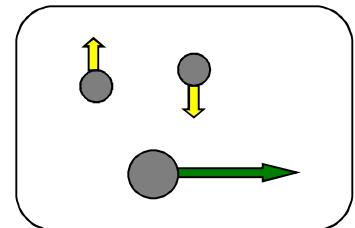
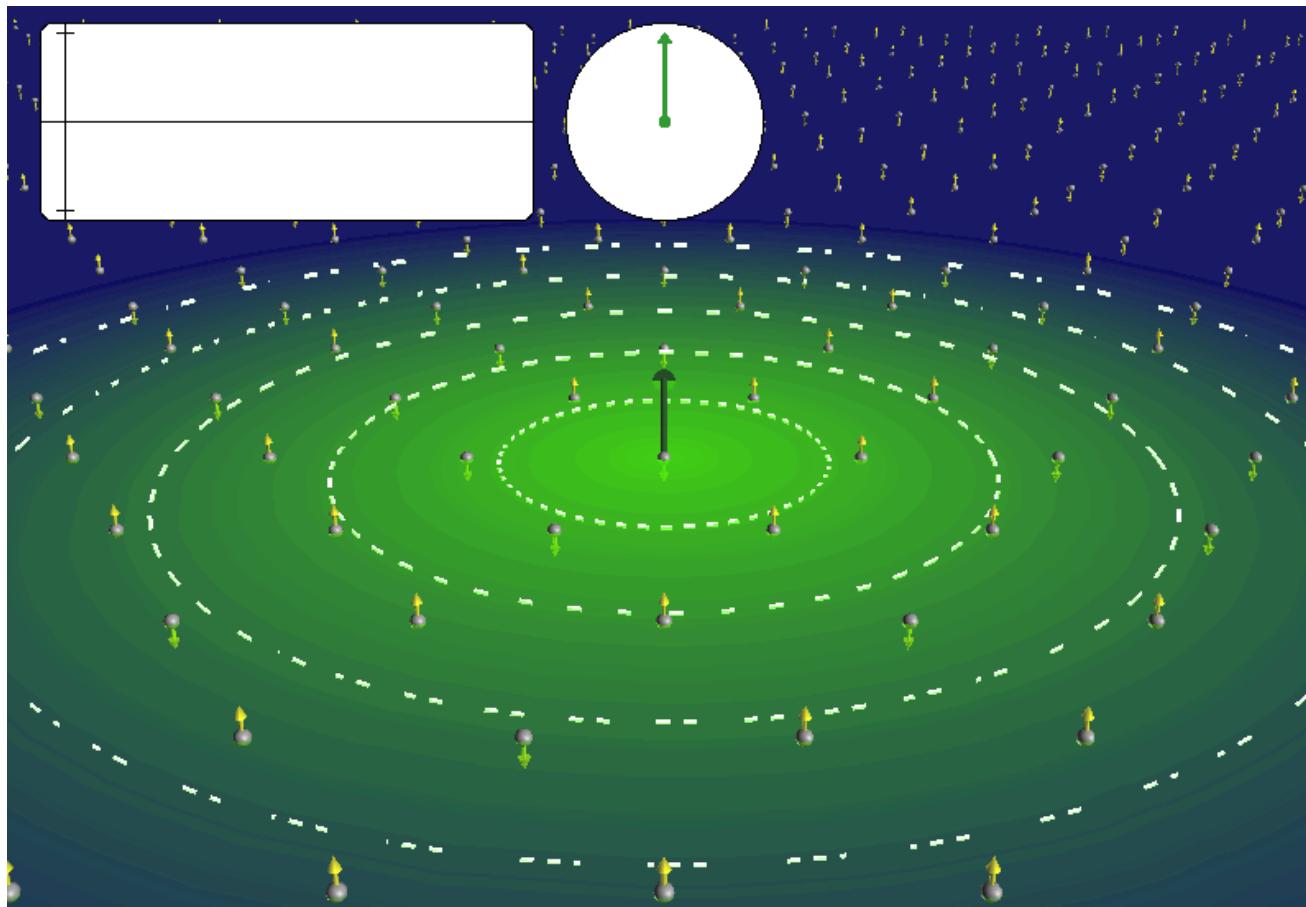
Experiments show $T_2=600$ ms. What limits this?

Donors: $1.2 \times 10^{14}/\text{cm}^3$, ^{29}Si : ~50 ppm

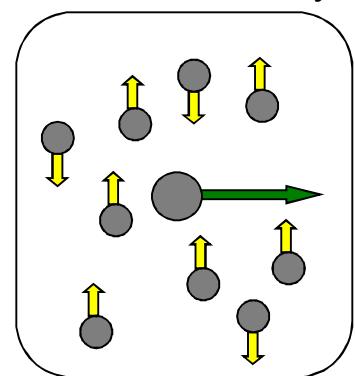
QuickTime™ and a
decompressor
are needed to see this picture.

A. M. Tyryshkin et al, Silicon Qubit Workshop,
August 2009, Berkeley, CA, USA

Central Spin Decoherence Problem



Exponential increase in difficulty



Spin Echo: decompressor
are needed to see this picture.

$$\rho(t) = \hat{U}\rho(0)\hat{U}^\dagger, \quad \rho_q(t) = \text{Tr}_B \rho(t)$$

Cluster Expansions Provide a Solution

Cluster Expansion Method¹

No fitting
Parameters!

Experiment:

A.M. Tyryshkin, J.J.L. Morton, S.C. Benjamin, A. Ardavan, G.A.D. Briggs, J.W. Ager, S.A. Lyon, J. Phys.: Condens. Matter **18**, S783 (2006).

¹ W. M. Witzel, Rogerio de Sousa, S. Das Sarma, Phys. Rev. B **72**, 161306(R) (2005); W. M. Witzel, S. Das Sarma, Phys. Rev. B **74**, 035322 (2006).

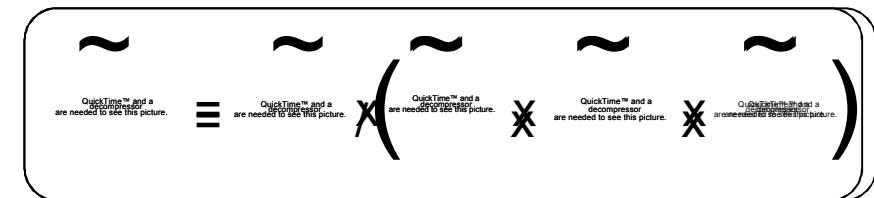
² Wen Yang, Ren-bao Liu, Phys. Rev. B **78**, 085315 (2008).

Cluster correlation expansion²:

$$L = \rho_q^{+-}(t)/\rho_q^{+-}(0)$$

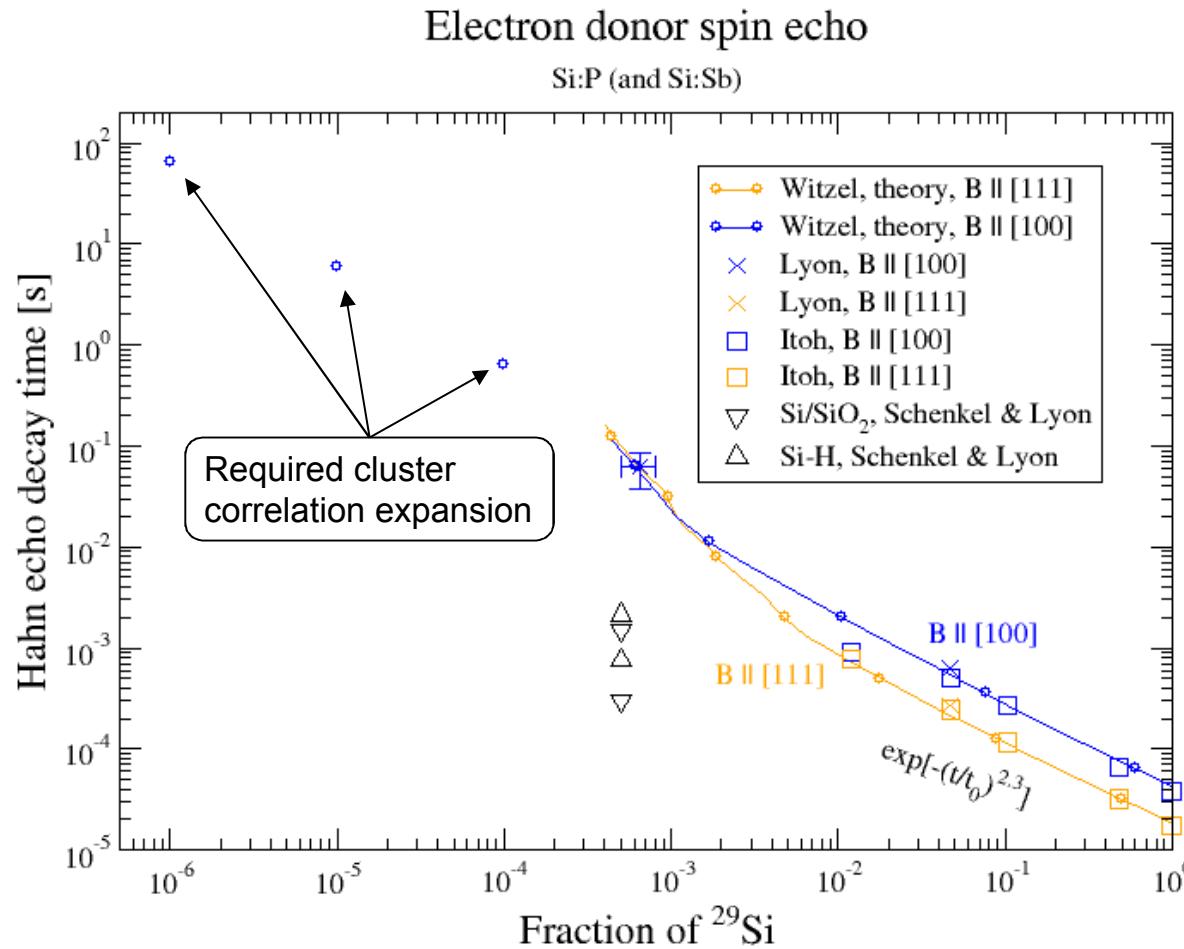
$L_S = L$ with the exclusion of spins outside of set S

$$L = \prod_S \tilde{L}_S, \quad \tilde{L}_S = L_S / \prod_{C \subset S} \tilde{L}_C$$

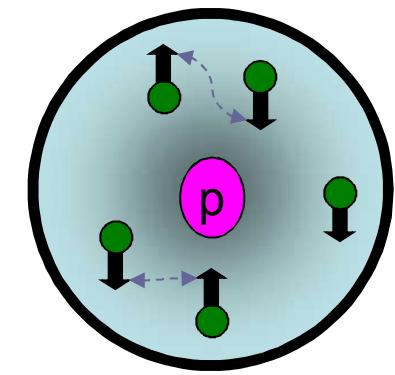
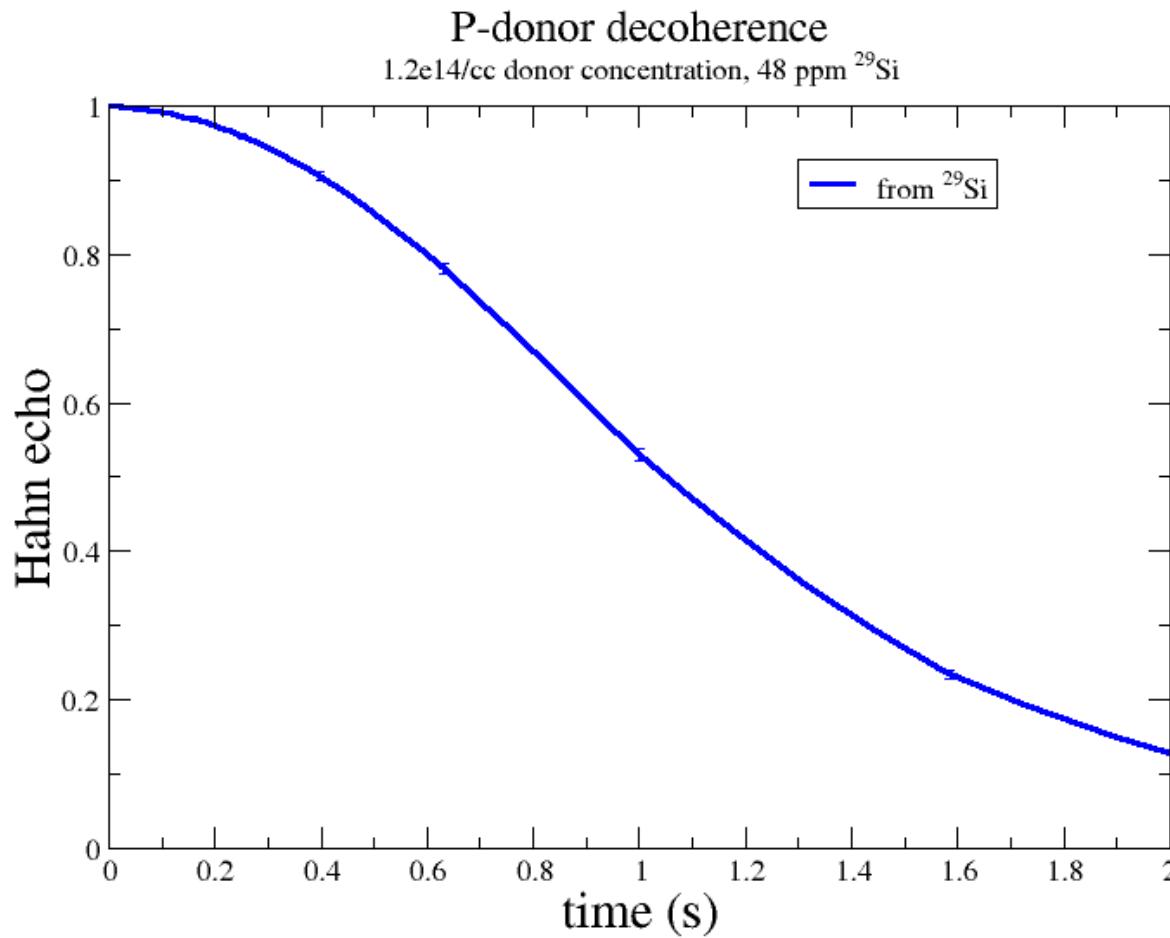


$$L_{\text{CCE}}^{(k)} = \prod_{|\mathcal{S}| \leq k} \tilde{L}_S.$$

Dephasing due to ^{29}Si , T_2



Theory: ^{29}Si spin noise



Sparse Electron Spin Systems Present New Challenges

Internal spin averaging:

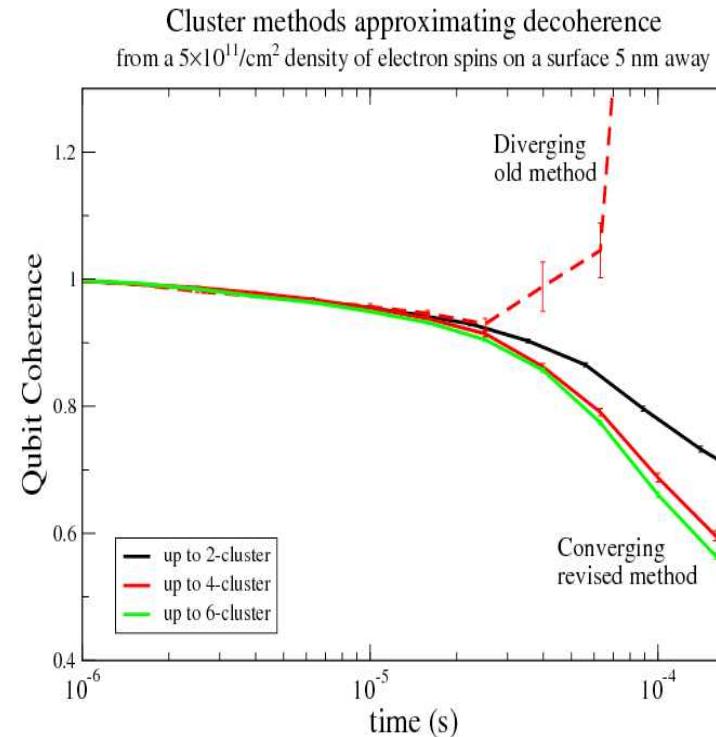
$$\tilde{L}_{\mathcal{S}}^{\mathcal{J}} = \frac{\langle L_{\mathcal{S}}^J \rangle_{J \in \mathcal{J}}}{\prod_{\mathcal{C} \subset \mathcal{S}} \tilde{L}_{\mathcal{C}}^{\mathcal{J}}},$$

Set of spin configurations Spin configuration

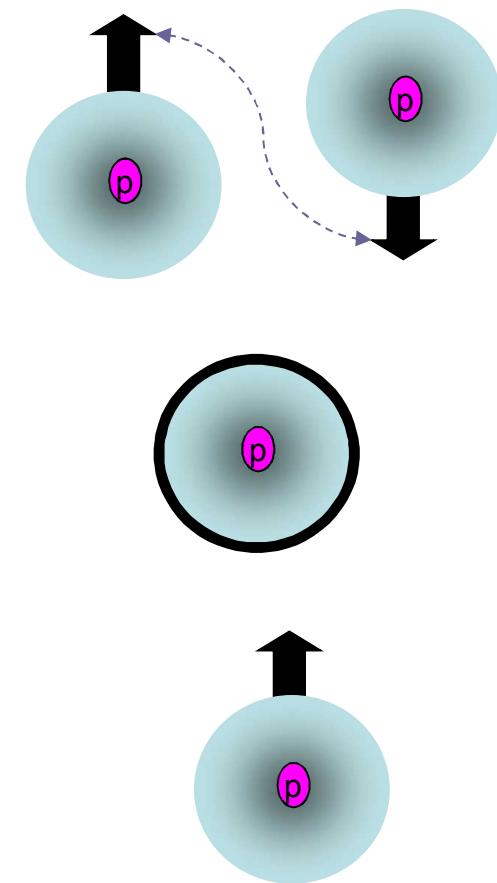
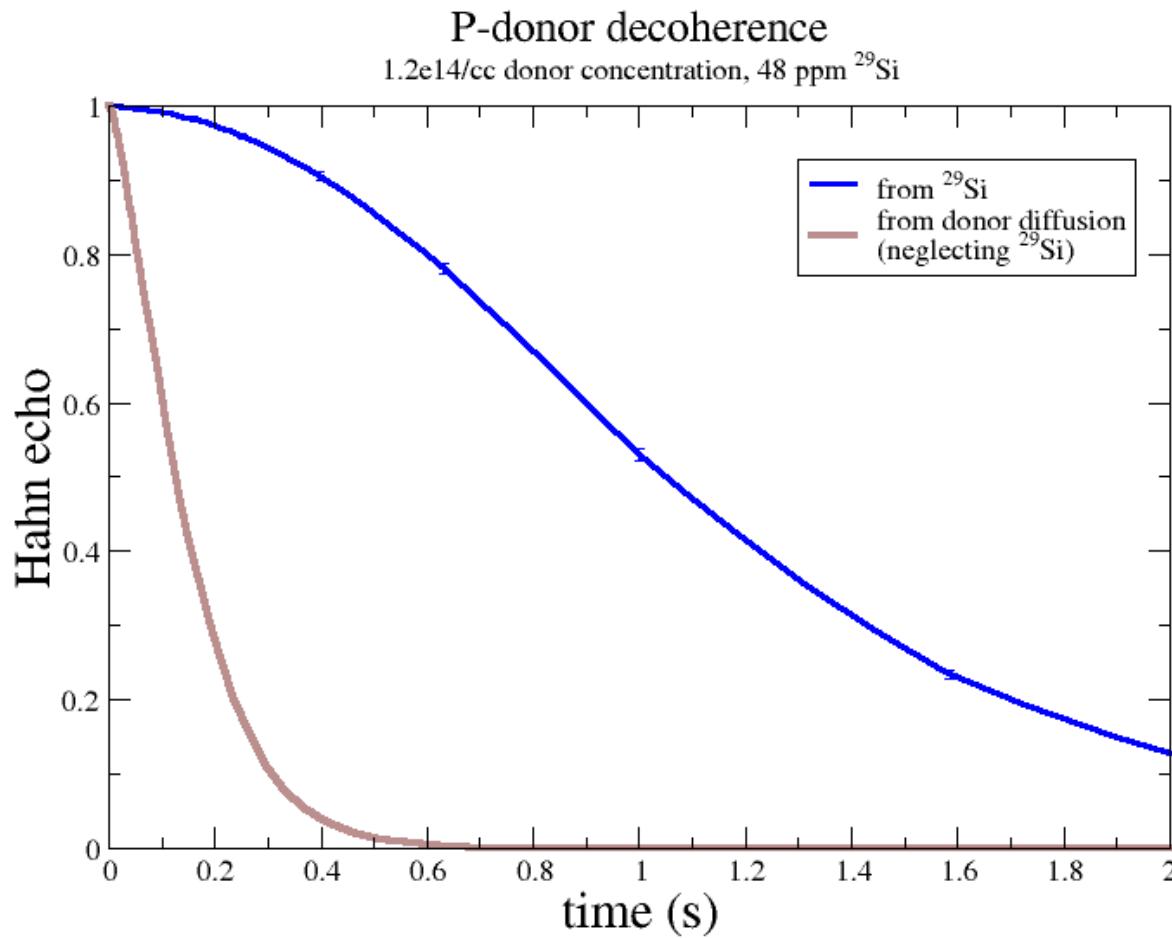
$$L^{(k)} = \left\langle \prod_{\|\mathcal{S}\| \leq k} \tilde{L}_{\mathcal{S}}^{\mathcal{T}(J, \mathcal{S}, k)} \right\rangle_J$$

QuickTime™ and a decompressor are needed to see this picture.

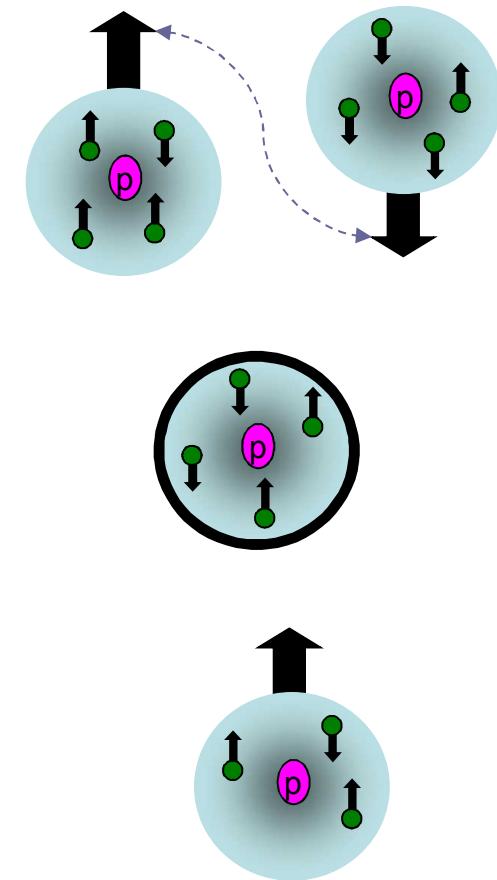
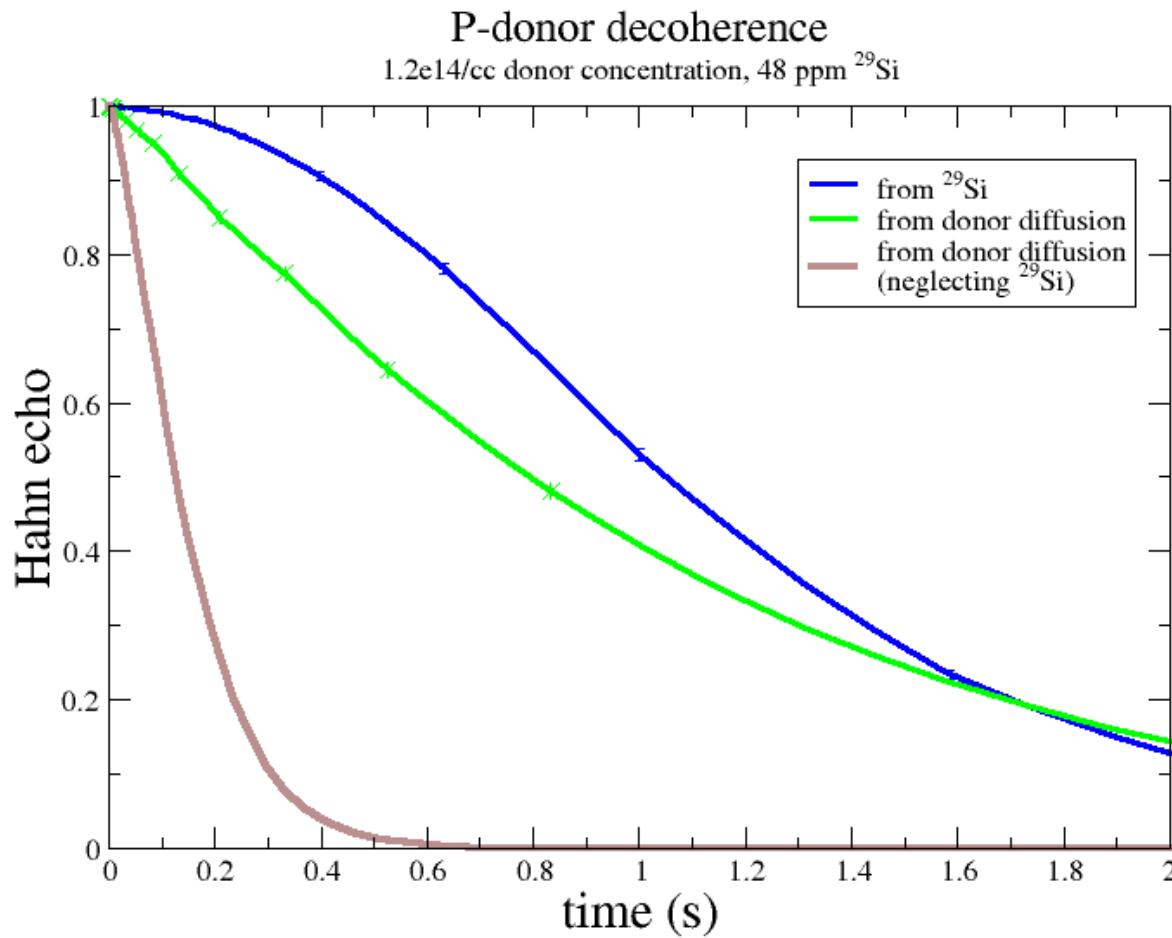
$$\mathcal{T}(J, \mathcal{S}, k) = \{J' \mid \|\mathcal{D}(|J\rangle, |J'\rangle) \cup \mathcal{S}\| \leq k\}$$



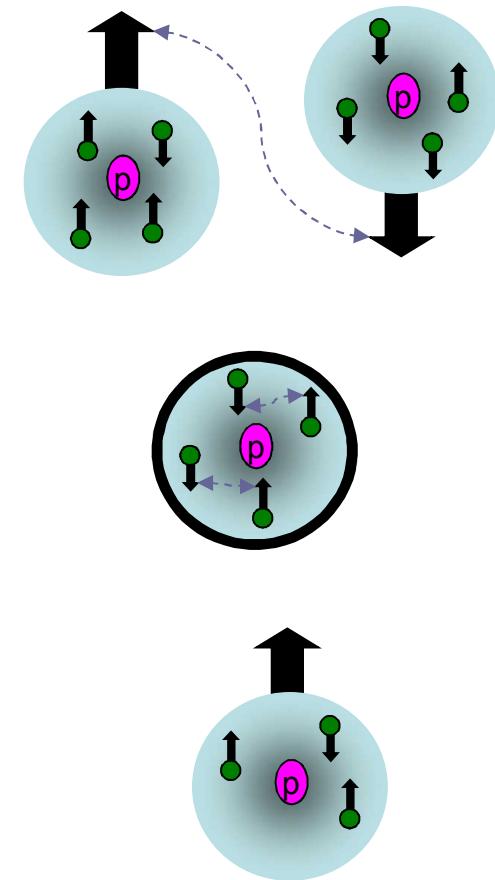
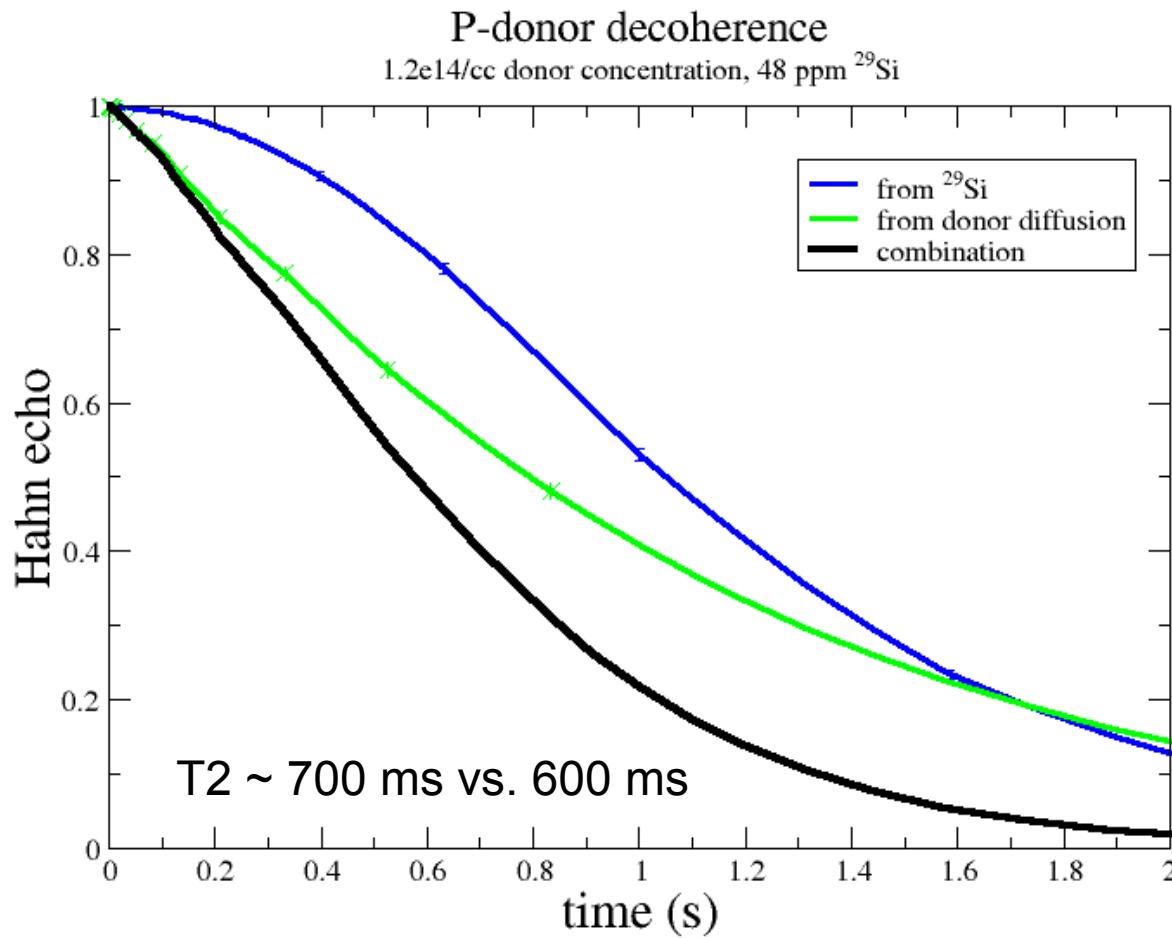
Theory: donor diffusion noise (neglecting ^{29}Si)



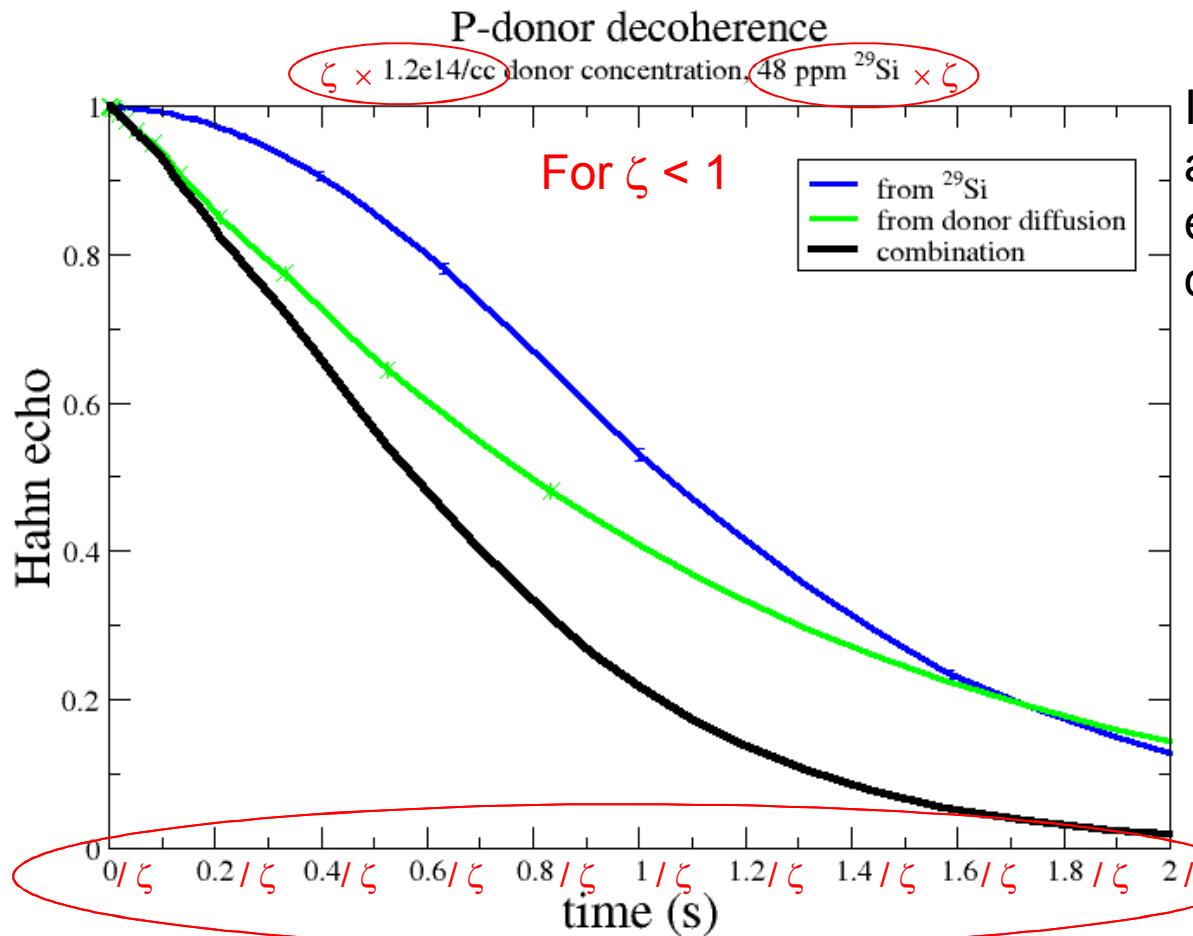
Theory: donor diffusion noise (with ^{29}Si)



Theory: donor diffusion noise and ^{29}Si noise

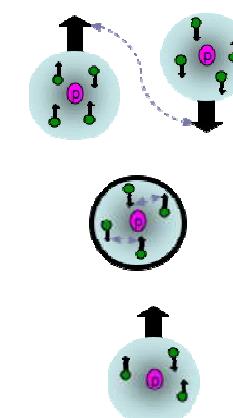


Benefit of theory: changing concentration



In this regime of low ^{29}Si and high B-field, the effective Hamiltonian has only dipolar interactions.

QuickTime™ and a decompressor are needed to see this picture.

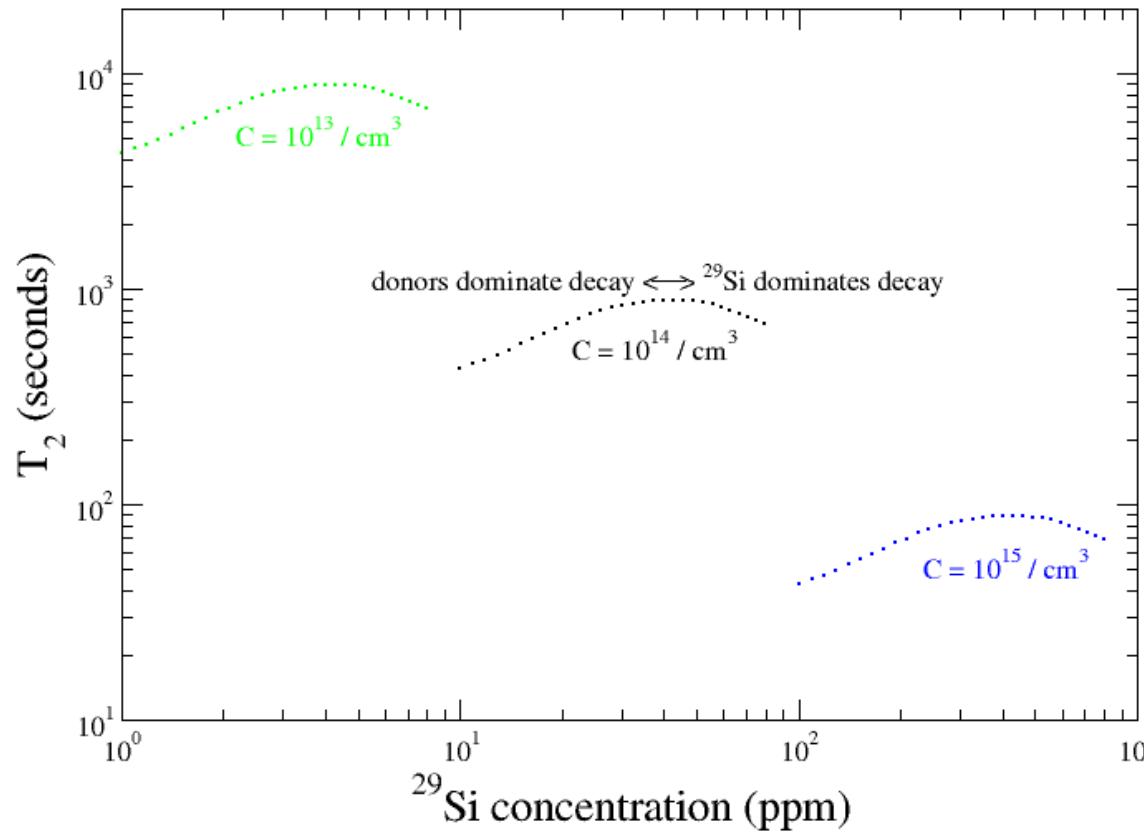


QuickTime™ and a decompressor are needed to see this picture.

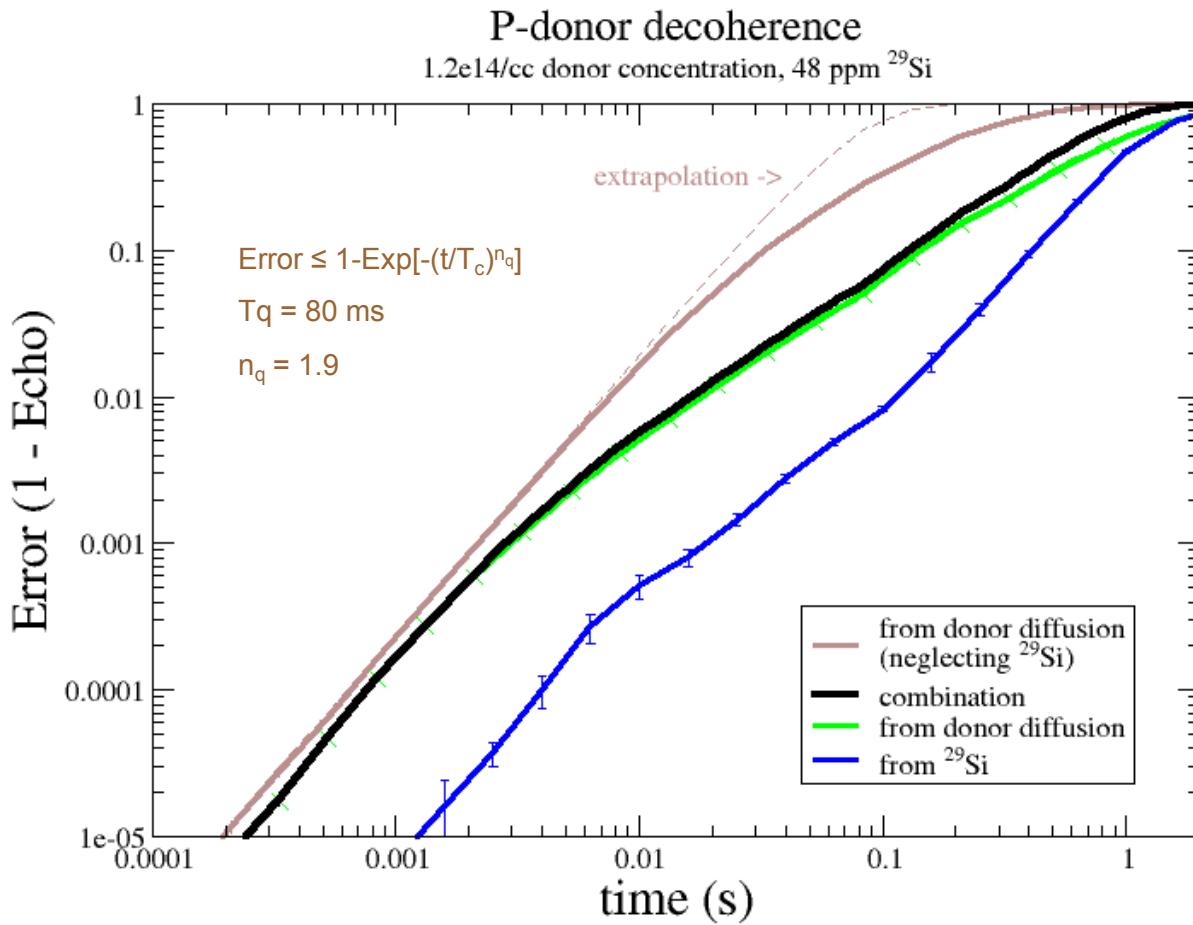
QuickTime™ and a decompressor are needed to see this picture.

Benefit of theory: changing concentration

T_2 can actually improve with increasing ^{29}Si !

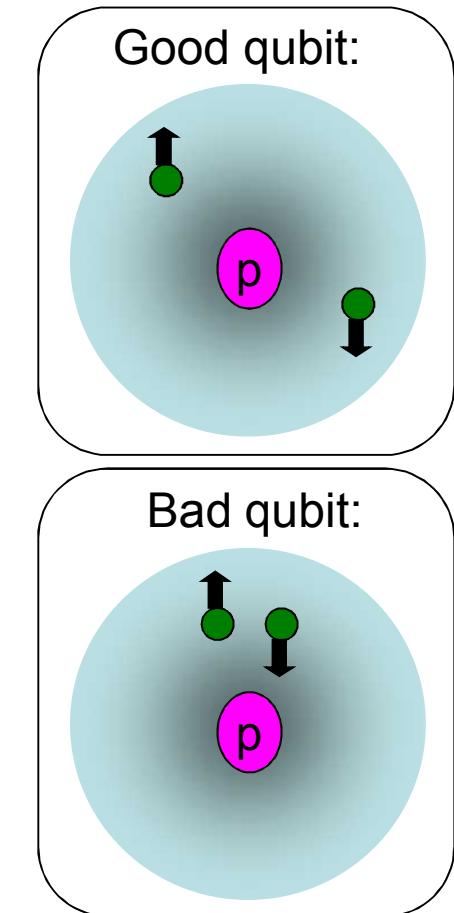
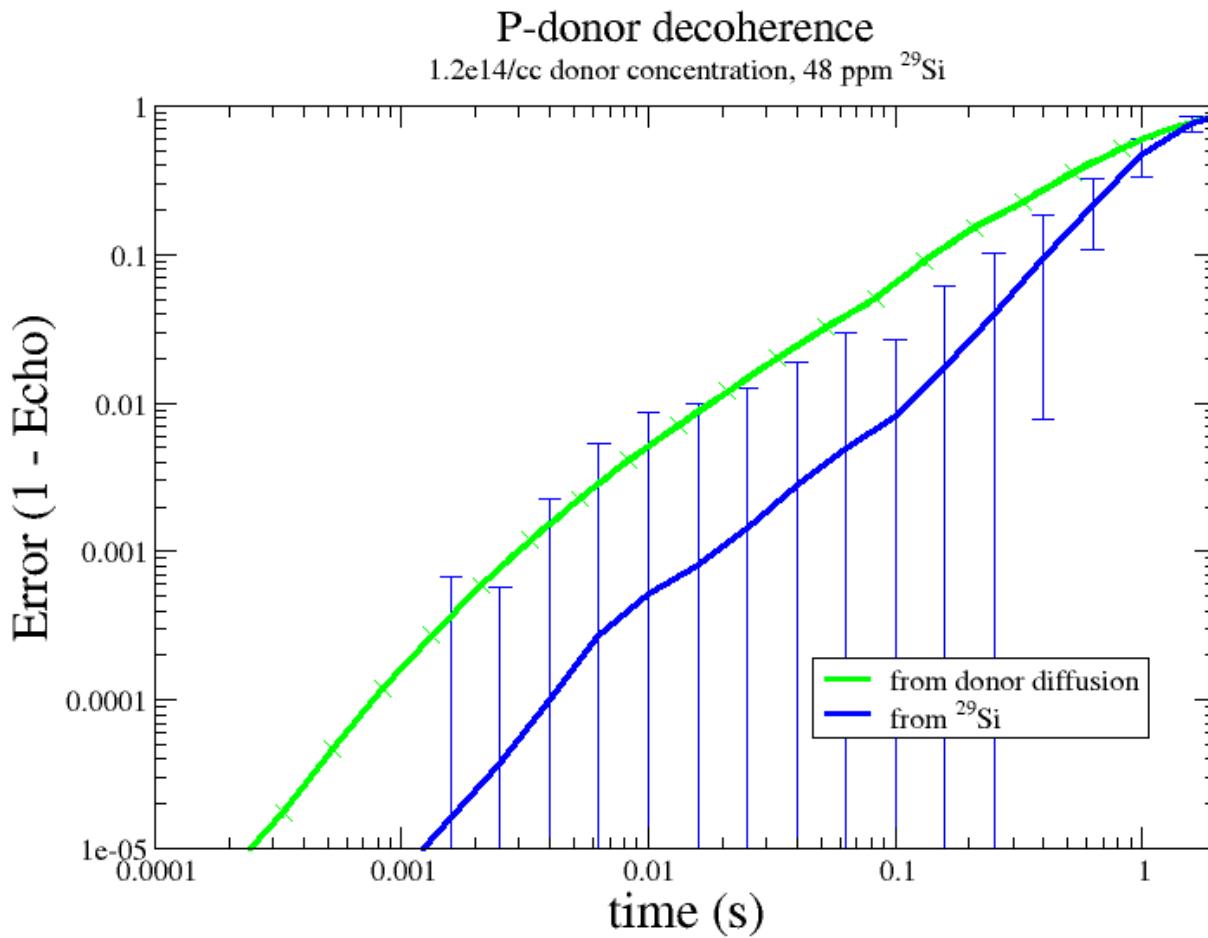


Benefit of theory: low error behavior

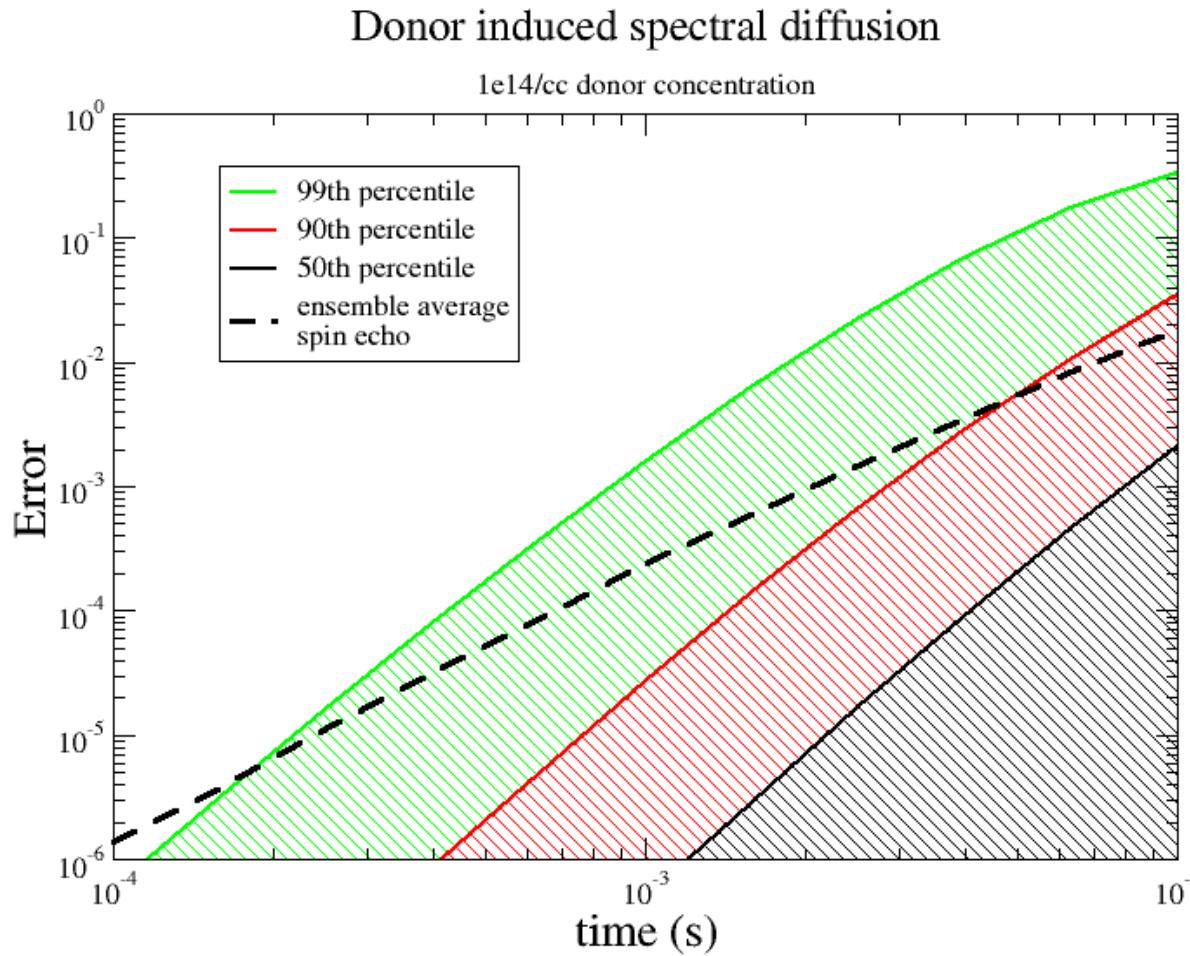


For Q. C., it's better to characterize the low error behavior. For this, we introduce T_q and n_q . An example is given in the “donor diffusion without ^{29}Si ” case.

Benefit of theory: sample-to-sample variation (^{29}Si decay)



Benefit of theory: sample-to-sample variation (donor decay)



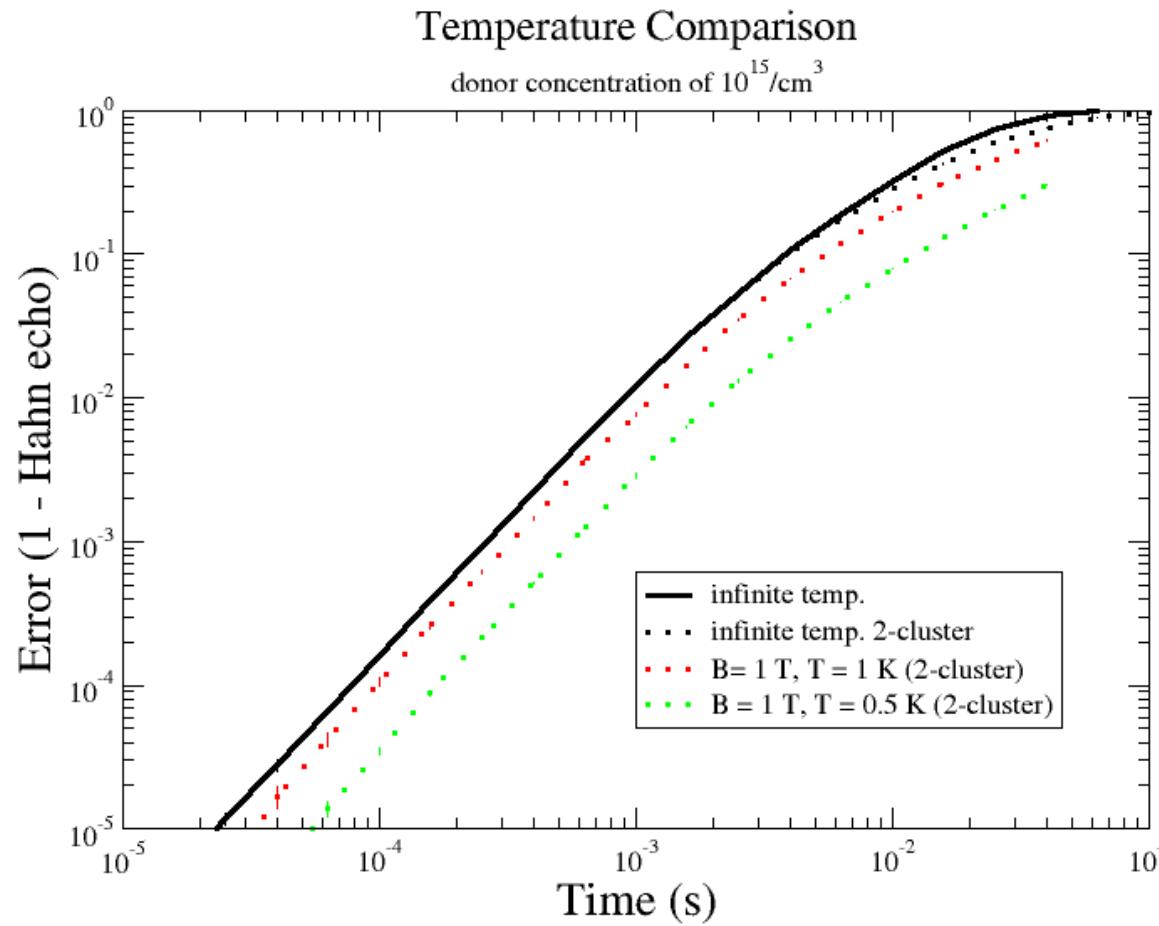
Good qubit:



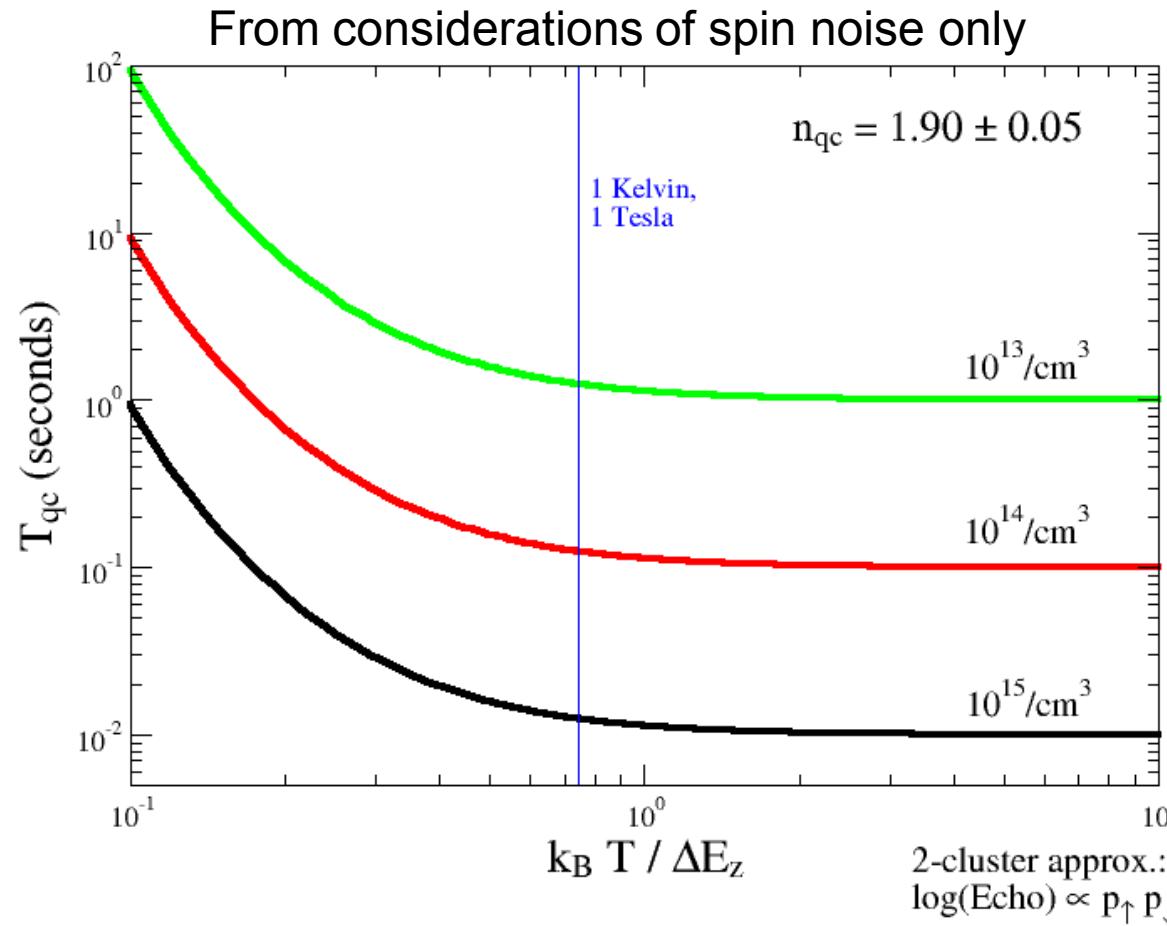
Bad qubit:



Benefit of theory: low temperature



Benefit of theory: low temperature



Conclusions

- Cluster expansions successfully solve the central spin decoherence problem.
- We have adapted the Cluster Correlation Expansion technique to have the versatility to solve problems of sparse electron spin baths.
- Coherence may be limited by ^{29}Si or background donors.
- Having some ^{29}Si improves T_2 at low donor concentrations.
- But T_2 isn't the right figure of merit! We present T_{qc} , n_{qc} as an alternative to capture low error behavior.
- For low errors, both ^{29}Si and dopants should be reduced.
- There is a large sample-to-sample variation in baths of sparse spins; yield is more informative than average decoherence.

