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Title: The Bipolar Behavior of the Richtmyer–Meshkov Instability
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THE BIPOLAR BEHAVIOR OF THE RICHTMYER–MESHKOV INSTABILITY

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A numerical study of the evolution of the multimode planar Richtmyer-Meshkov instability (RMI) in a light-heavy (air-SF₆, Atwood number $A=0.67$) configuration involving a Mach number $Ma=1.5$ shock is carried out. Our results demonstrate that the initial material interface morphology controls the evolution characteristics of RMI (for fixed A , Ma), and provide a significant basis to develop metrics for **transition** to turbulence. Depending on initial rms slope of the interface, RMI **evolves** into linear or nonlinear regimes, with distinctly different flow features and growth rates, turbulence statistics, and material mixing rates. We have called this the bipolar behavior of RMI. Some of our findings are not consistent with heuristic notions of mixing in equilibrium turbulence: more turbulent flow—as measured by **spectral** bandwidth, can be associated with higher material mixing but, **paradoxically**, to lower measures of turbulent kinetic energy and integral mixing layer width.

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The Bipolar Behavior of the Richtmyer-Meshkov Instability

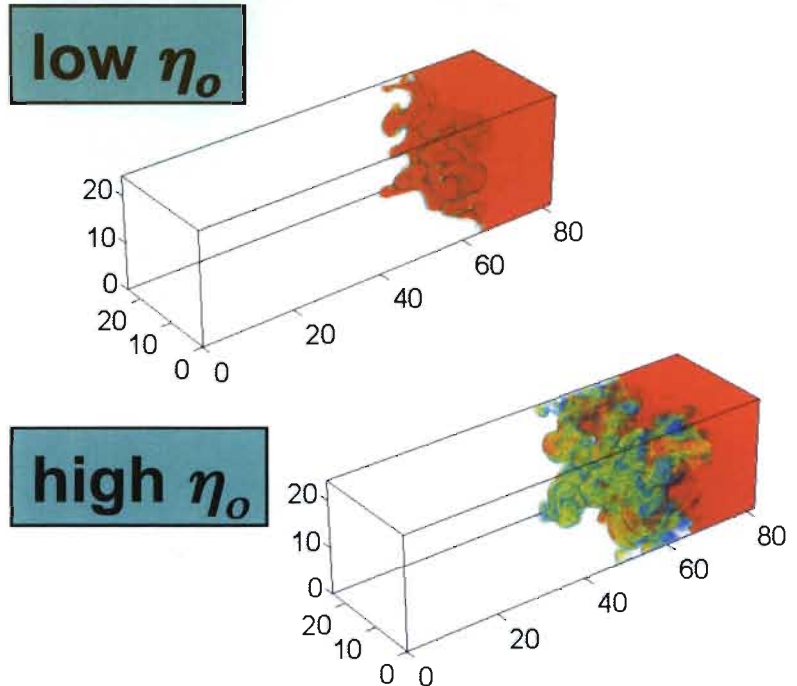
F.F. Grinstein, A.A. Gowardhan, and J.R. Ristorcelli

Motivation

- *Characterize Initial condition effects on transition and mixing*
- *Goal: control instability*

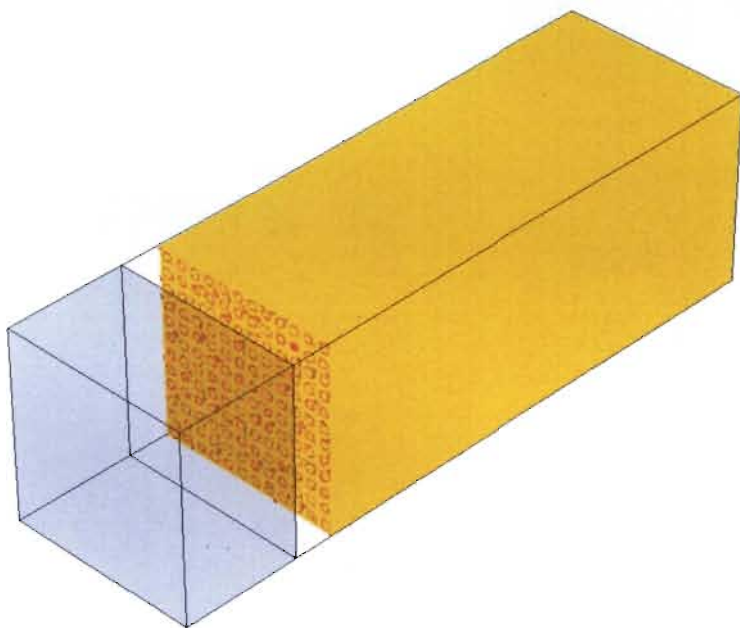
New results

- *Bipolar behavior of the RM instability*
 - *challenges to modeling*
 - *reshock effects on first shock*



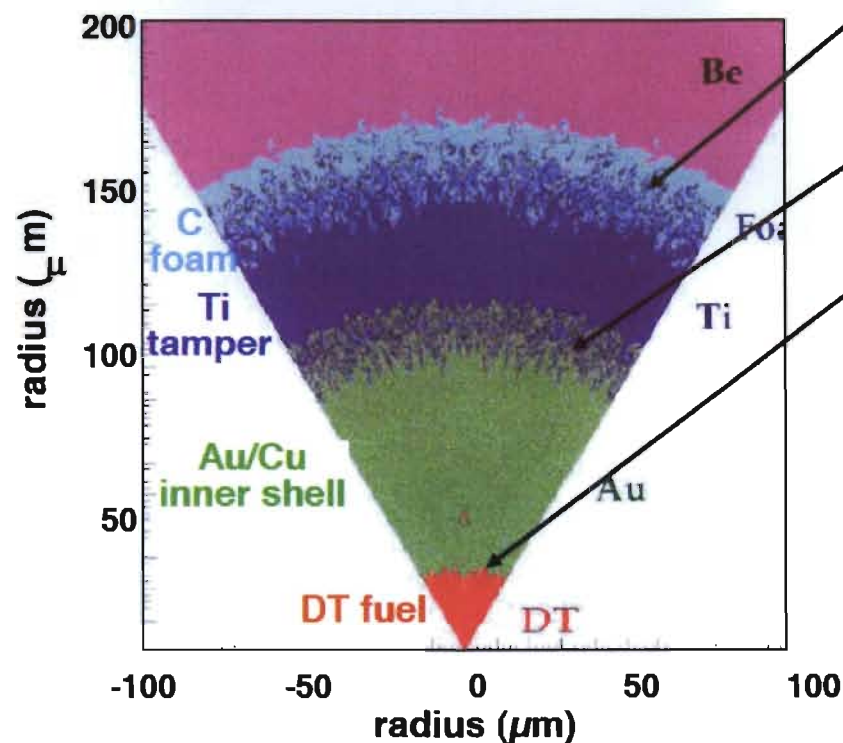
instantaneous material mixing

ILES RAGE simulations SF_6 mass fraction distributions



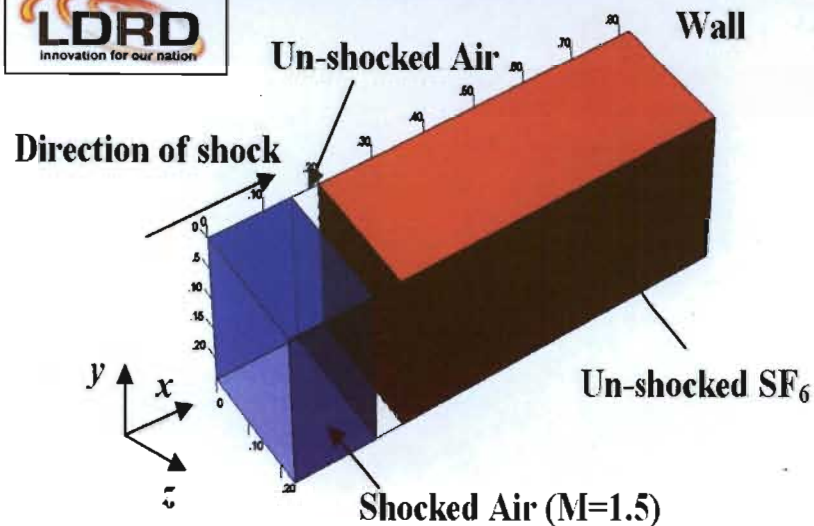
planar **single-interface** (V&S 95, Caltech)

**2D HYDRA simulation of NIF-scale
ignition double shell capsule**



- Understand Effects of Initial Material Interface Conditions
- Practical Goal: control (promote or inhibit) RM instability

Shock-Driven Turbulence Simulations



- shocks and turbulence, transitional flow
- wide range of length and time scales, non-linear interactions
- Implicit Large Eddy Simulation (ILES), e.g., ILES book, 2nd printing: 2010

- **planar** (Vetter & Sturtevant '95,), **gas curtain** (Prestridge et al., LANL P-23)
- **Hybrid WENO / classical LES**, Pullin et al. 2006, ..., 2011
- **ILES** , 2002 – 2011: Cohen et al. (FV-PPM), ... Schilling et al. (FD-WENO), Youngs, Drikakis et al. (FV-LR, FV-Godunov), Leinov et al. (FV-ALE), ...
- **ILES-RAGE**; FV-Godunov, van Leer limiter, no interface treatment, AMR
 - ↑ **planar V-S expts., PoF March 2011;**
 - ↓ **planar Bipolar RM, PoF Letters July 2011; AIAA-Hawaii-2011 / ETC13 → PoF shocked (double interface) gas-curtains, J. Turbulence 2011, in press.**

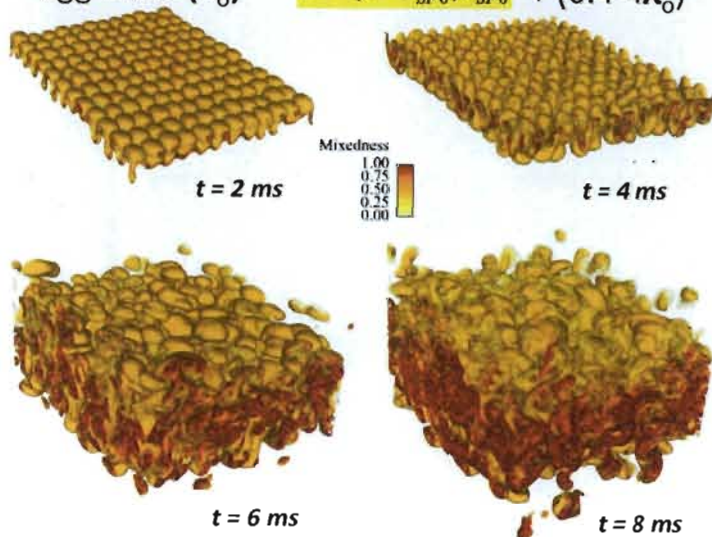
ILES RAGE – Planar RM Expts.

Spectral IC effects on material mixing

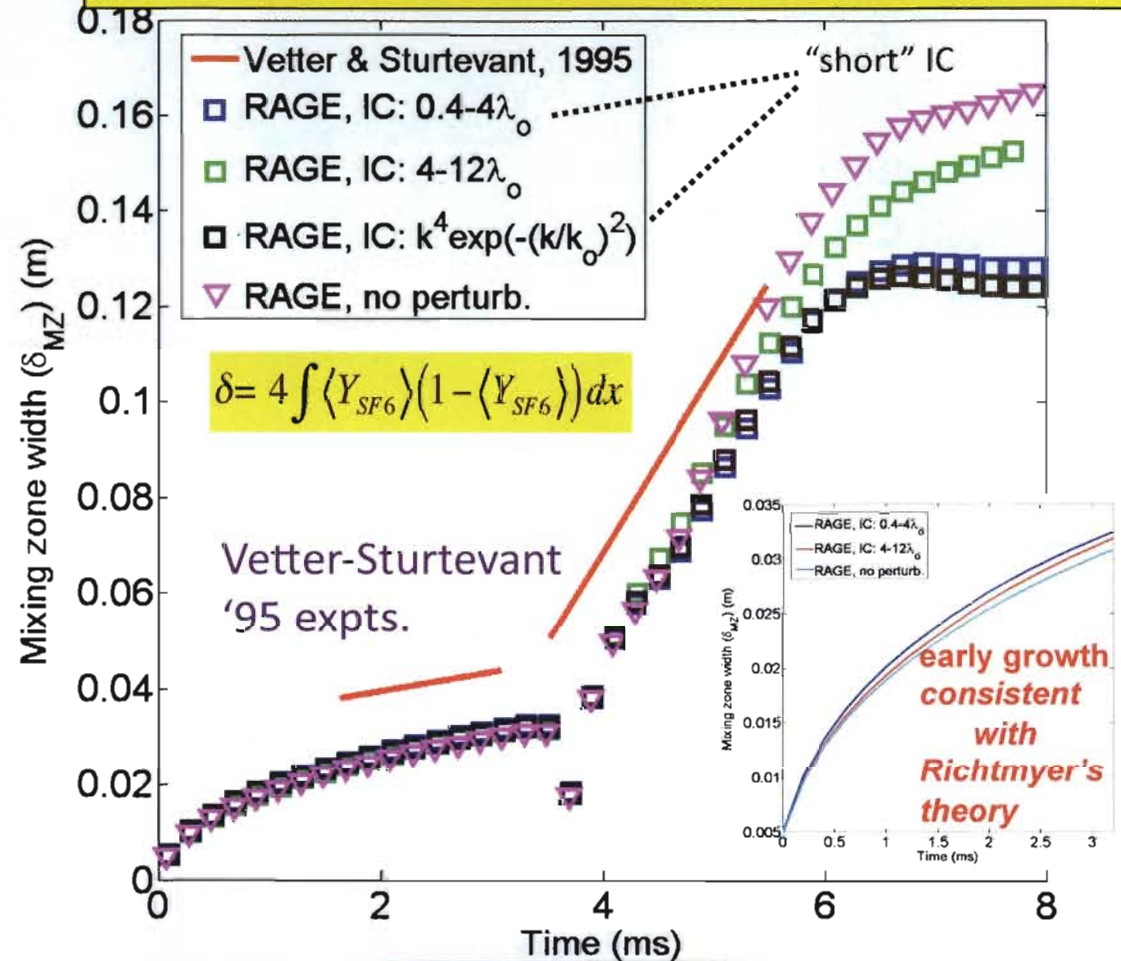
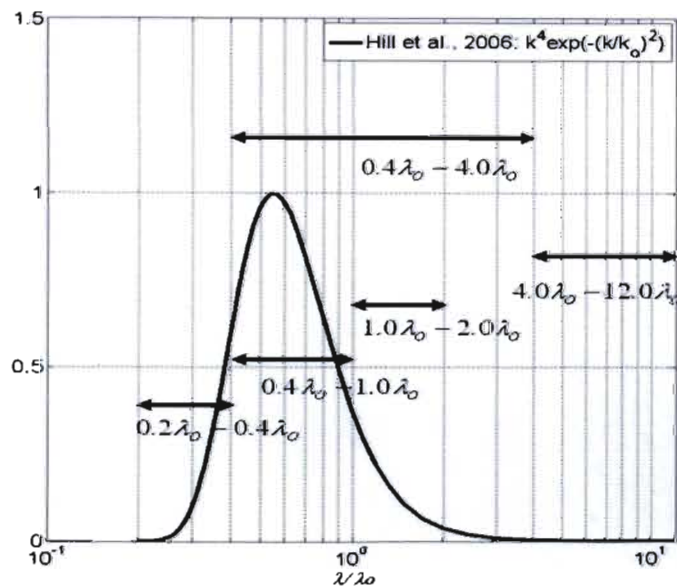
Grinstein, Gowardhan, and Wachtor, *PoF*, March 2011

egg crate (λ_0)

$$\theta = (1 - Y_{SF6})Y_{SF6} + (0.4 - 4\lambda_0)$$



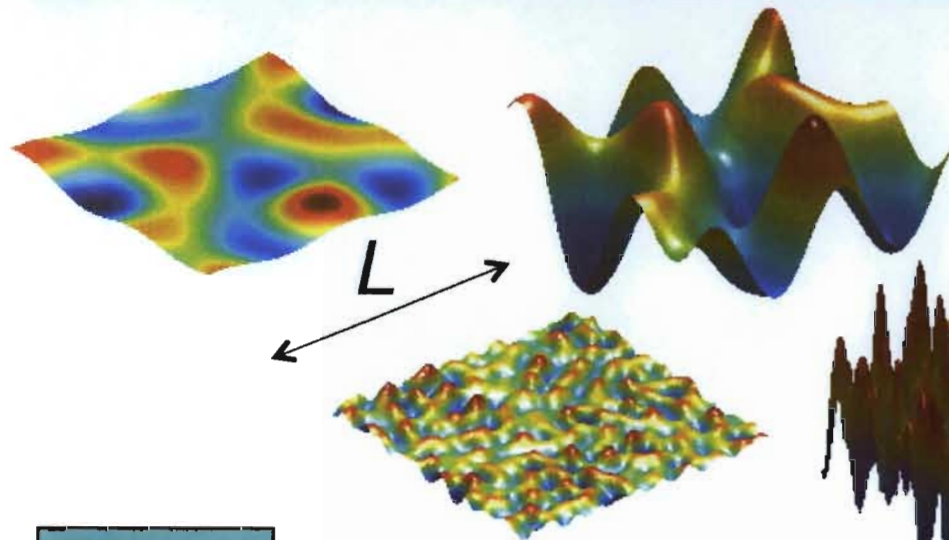
10% IC perturbation added to mode (λ_0)



- results for “thin” **low η_0** initial material interface
- **early-time** ($t < \sim 5\text{ms}$) growth fairly IC insensitive
- **late-time sensitive to ICs** (more so for “longer” IC
- **IC resolution issues ... separate discussion req'd ...**

Initial material interface parameterization

(no initial “egg-crate”, no reshock...)



high η_o class ($\kappa_o \delta_o > \pi$)

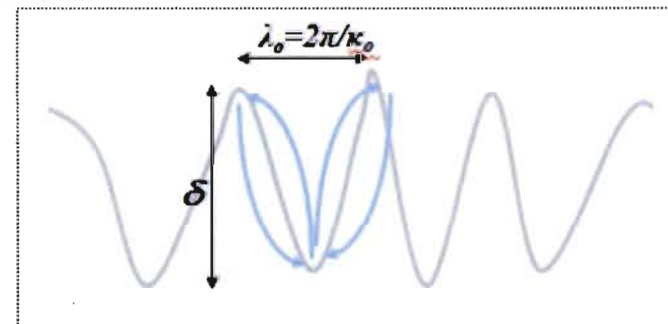
$\eta_o = 10\pi/12, 10\pi/8, 10\pi/4, 10\pi/2$

$$\eta_o = \kappa_o \delta_o$$

low η_o class

($\kappa_o \delta_o \ll \pi$)

$\eta_o = \pi/12, \pi/8, \pi/4, \pi/2$



$(\lambda_{\min}, \lambda_{\max})$	$L(\frac{1}{24}, \frac{1}{6})$	$L(\frac{1}{12}, \frac{1}{4})$	$L(\frac{1}{6}, \frac{1}{3})$	$L(\frac{1}{4}, \frac{1}{2})$	$L(\frac{1}{24}, \frac{1}{6})$	$L(\frac{1}{12}, \frac{1}{4})$	$L(\frac{1}{6}, \frac{1}{3})$	$L(\frac{1}{4}, \frac{1}{2})$
δ_o (cm)	0.5 (low η_o)				5 (high η_o)			
κ_o (cm ⁻¹)	π	$\pi/2$	$\pi/4$	$\pi/6$	π	$\pi/2$	$\pi/4$	$\pi/6$

Bipolar Behavior of planar RM

Ma=1.5, air/SF₆ – no egg-crate, no reshock
Gowardhan, Ristorcelli and Grinstein; *PoF* Letters, July 2011

Initial *rms* slope $\eta_o = \kappa_o \delta_o$ of Initial Material Interface

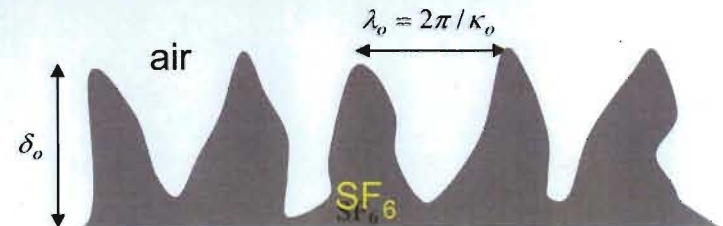
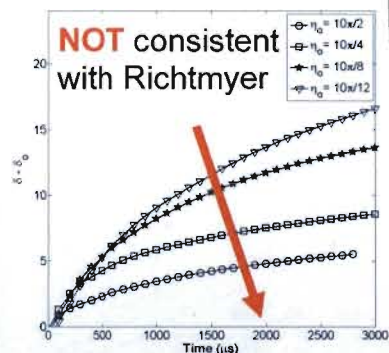
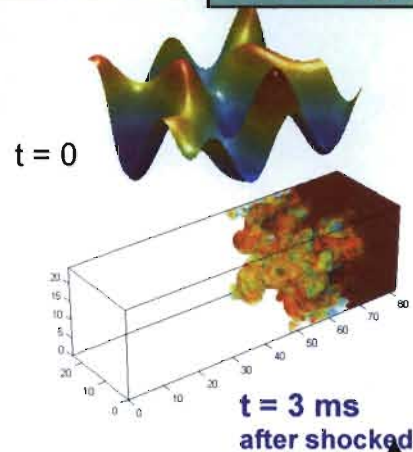
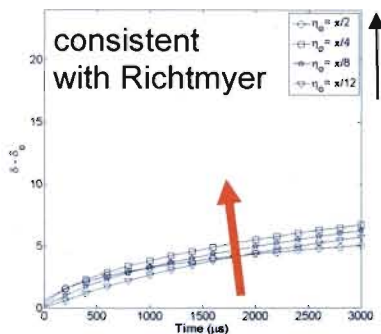
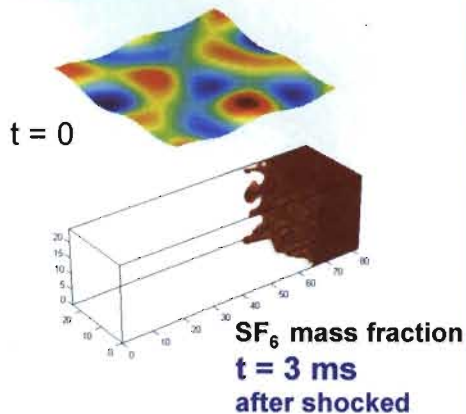
Beyond Richtmyer (growth = constant $\times \eta_o$):

→ bipolar RM behavior vs. IC morphology
→ different instability mechanisms & late-time flow

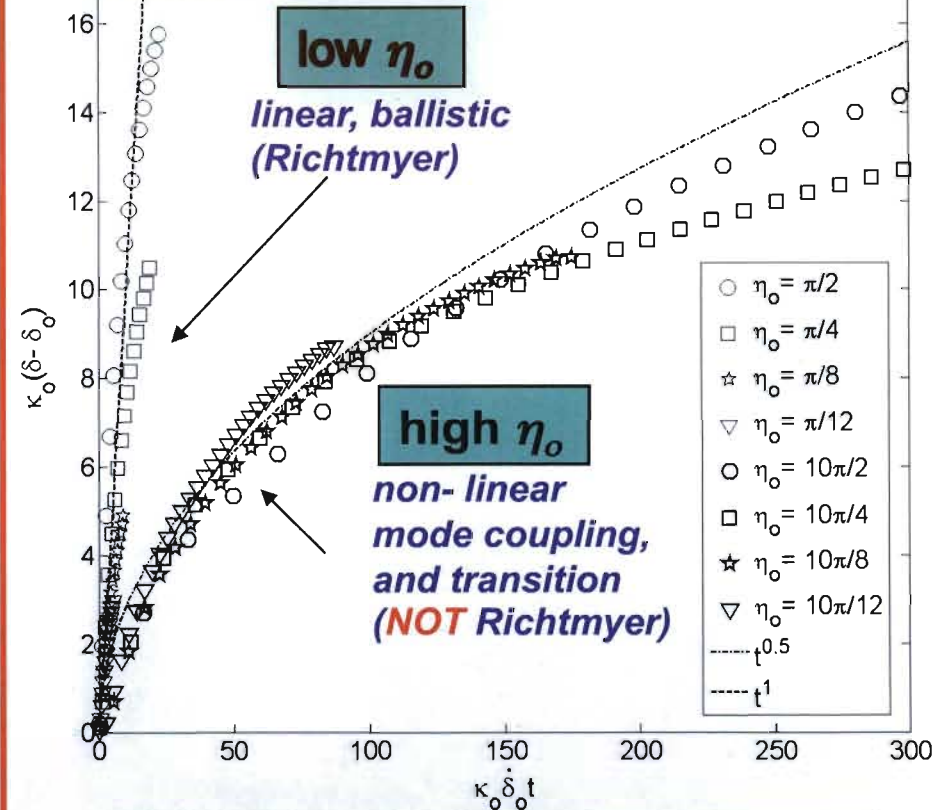
low η_o

Dimensional results

high η_o

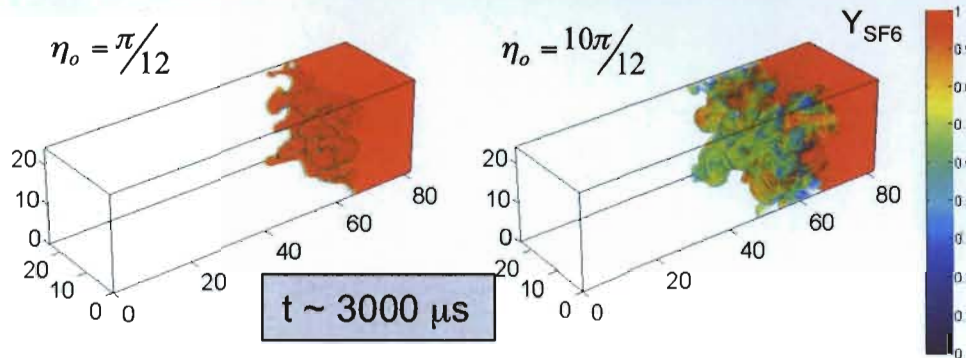


Non-Dimensional "Bipolar" results

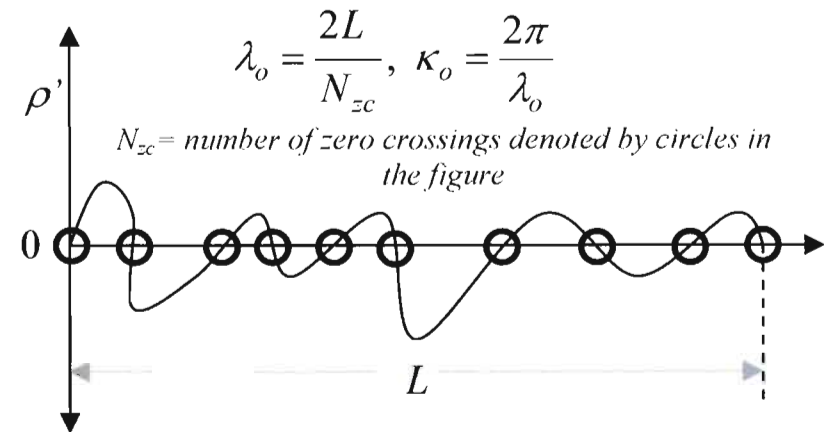
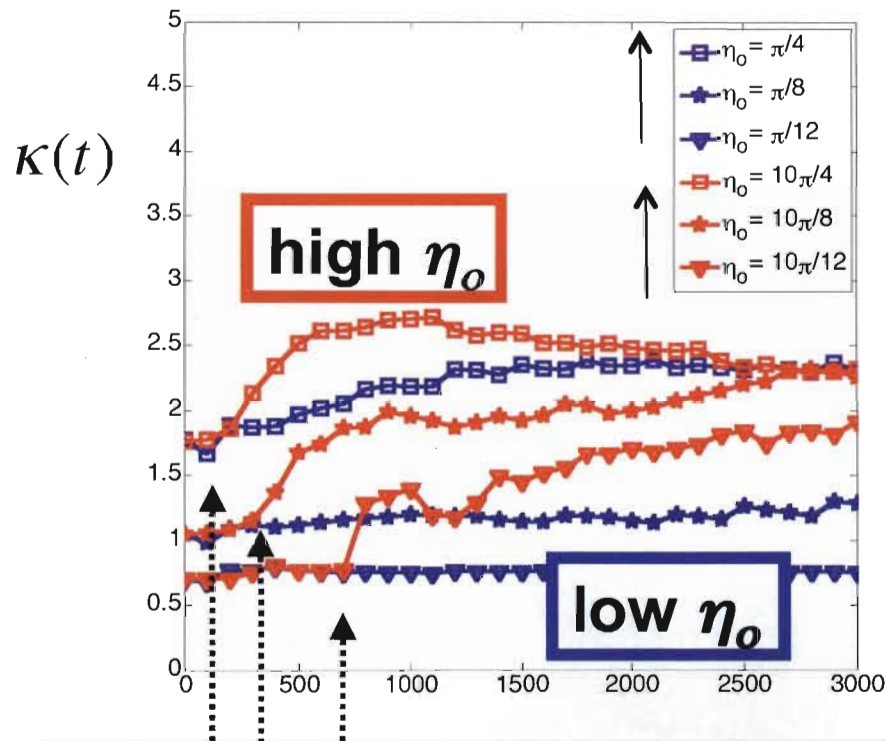


Characterizing Small-Scale Production

→ zero-crossing wavenumber κ (e.g., Sreenivasan et al. '83)



κ is the “zero crossing” wavenumber of the mass density fluctuation



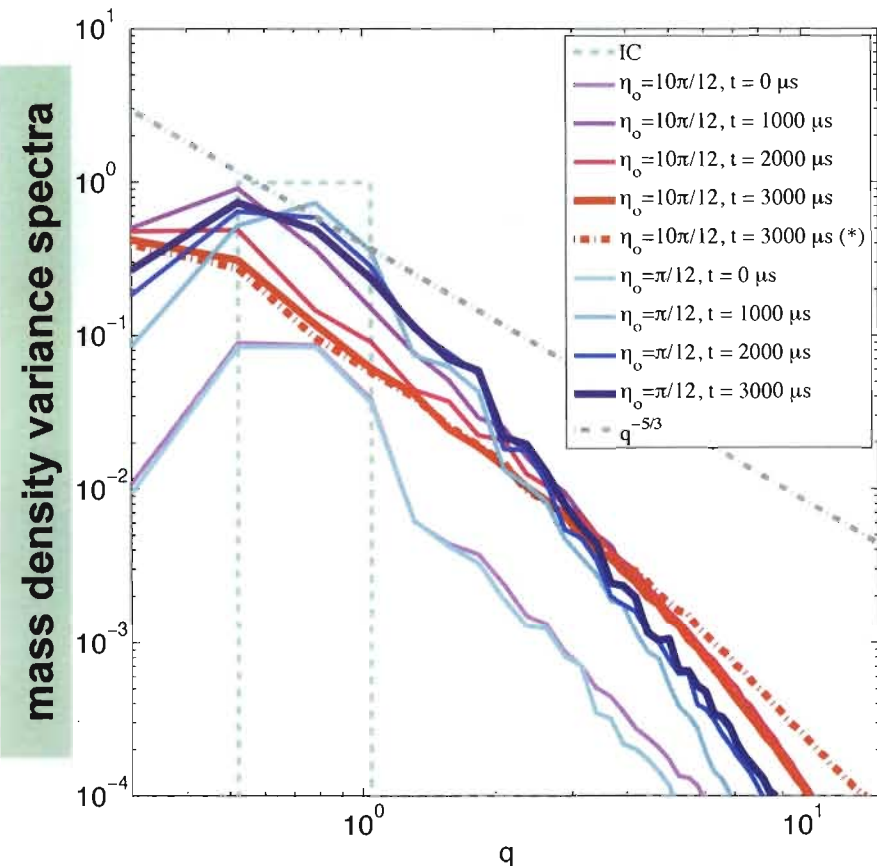
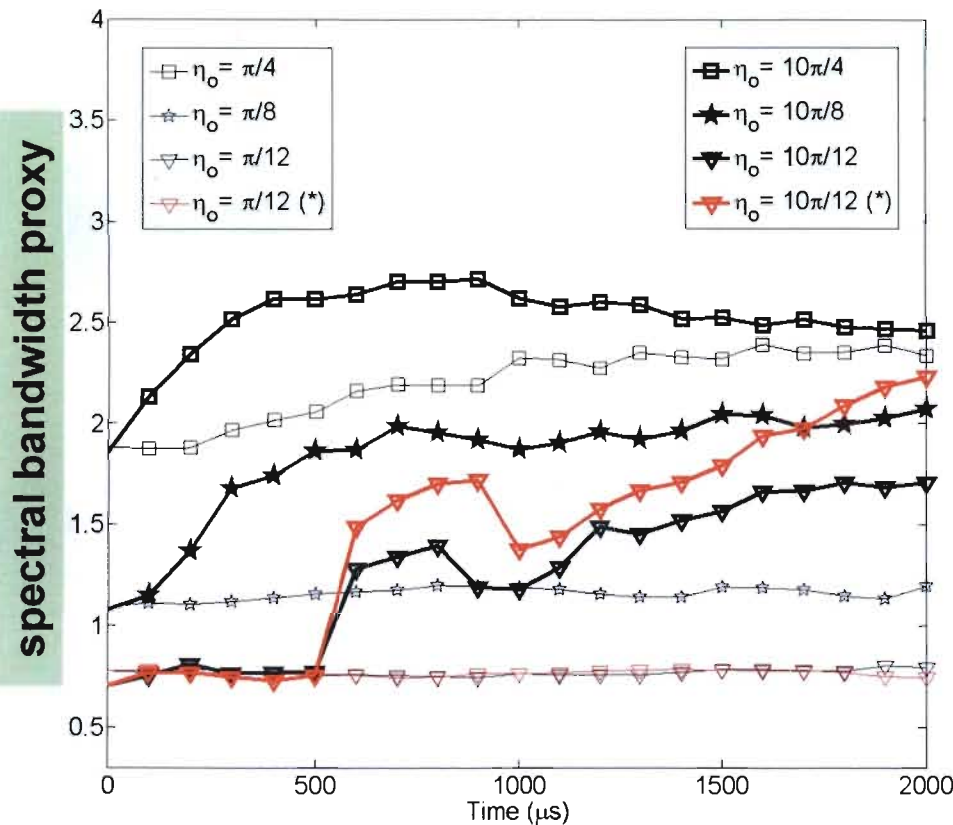
$$\kappa(t) \sim \frac{1}{\lambda(t)} = \frac{1}{\text{Taylor length scale}}$$

“transition” indicated by rapid increase of κ

Spectral bandwidth of the turbulence

*Spectral bandwidth proxy
provides a measure of how
“turbulent” the flow is*

$$\eta(t) = \kappa(t)\delta(t) = \frac{\delta(t)}{\lambda(t)} \sim \frac{\text{Integral scale}}{\text{Taylor length scale}} \sim \text{Re}_\lambda$$

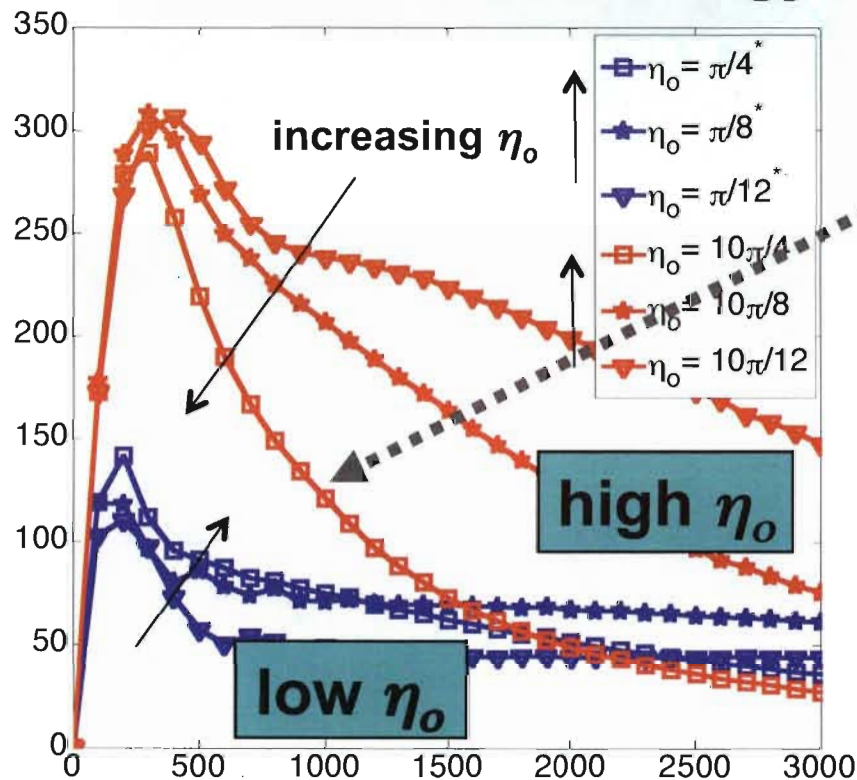


(*) *finer* (doubled) resolution

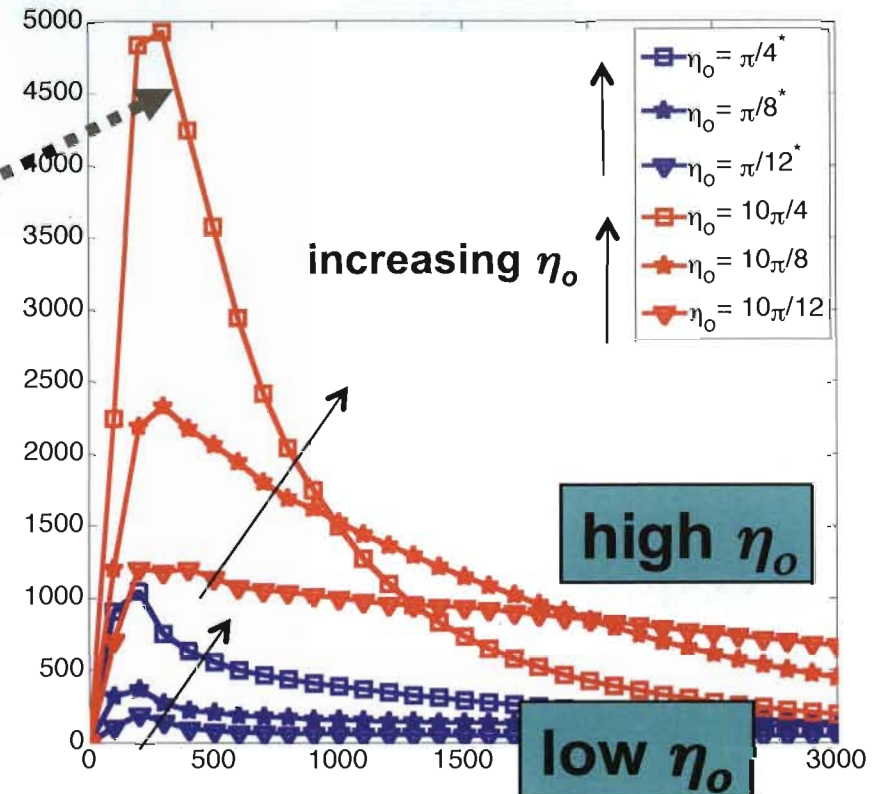
Higher initial η_0 leads to higher $\eta(t)$ at late times

Turbulence metrics

turbulent kinetic energy



enstrophy

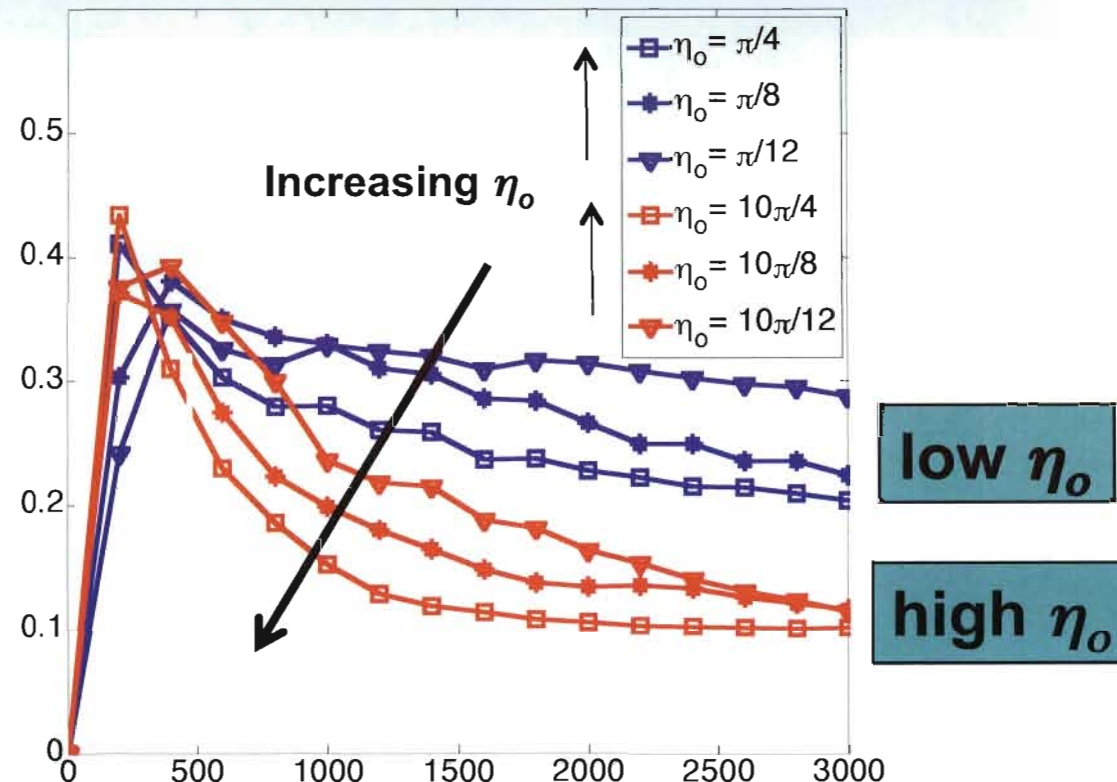


- **MORE** enstrophy – **LESS** turbulent kinetic energy
- **IC challenge:** enstrophy and energy -- *different* deposition mechanisms

Turbulence metrics: isotropy

Lumley's anisotropy tensor analysis

$$b_{11} = \frac{\langle u_1 u_1 \rangle}{2k} - \frac{1}{3}$$



Higher η_o – more mixing, more isotropy

Consequences of Bipolar RM Behavior

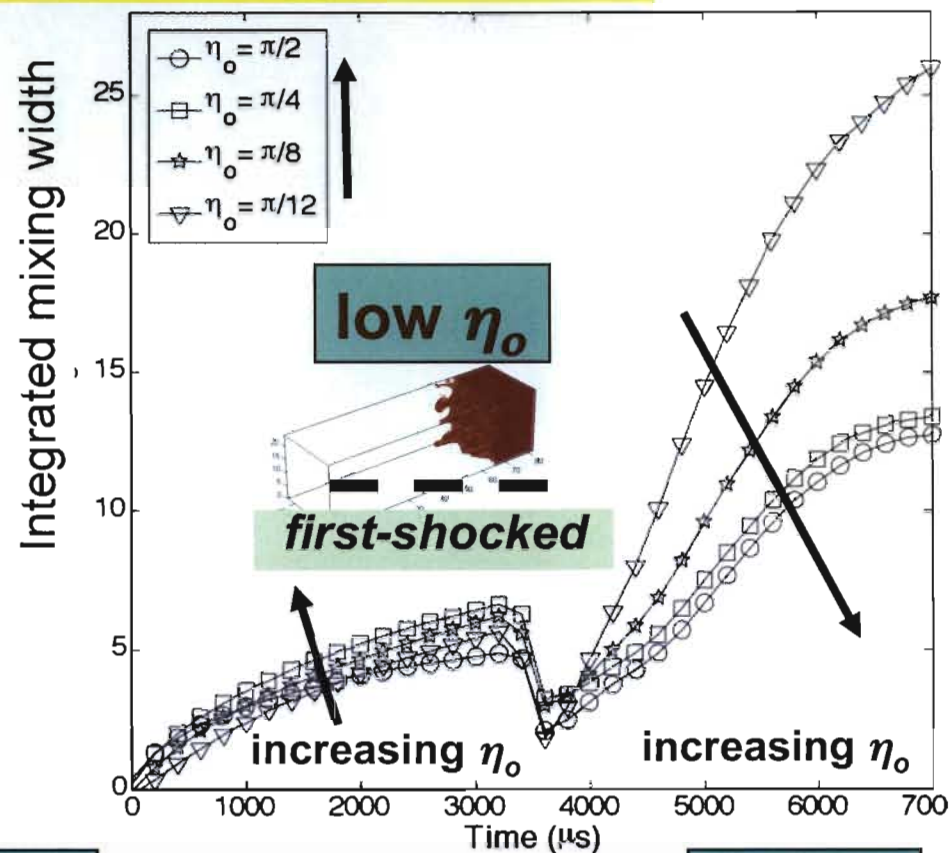
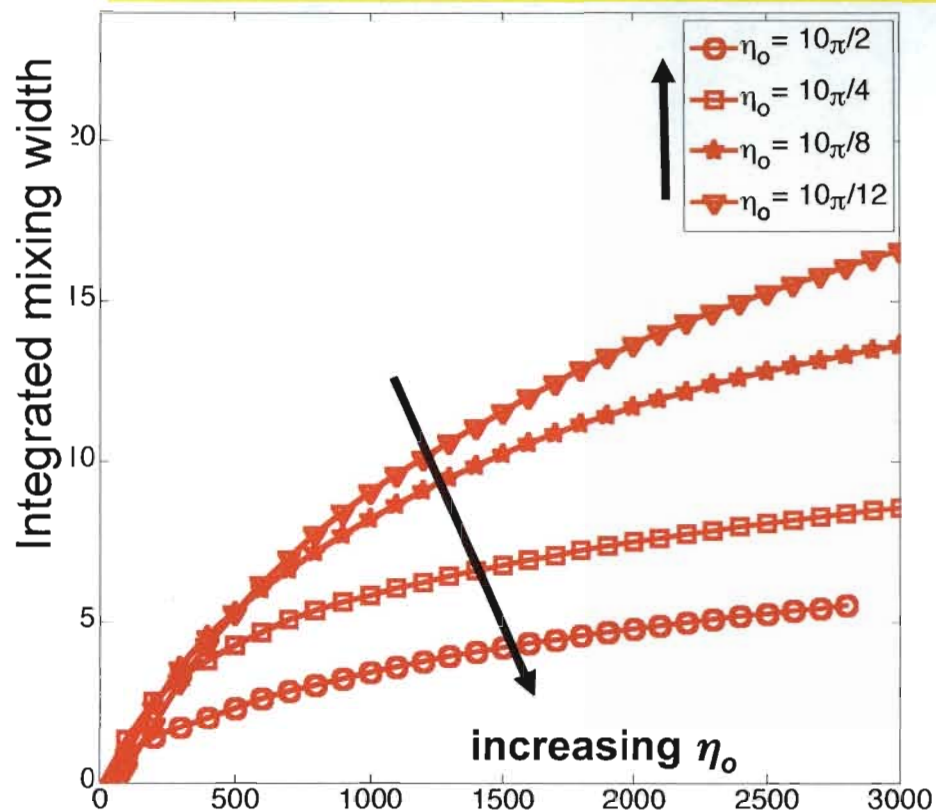
low η_o

reshock effects ~

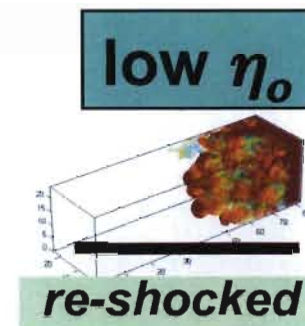
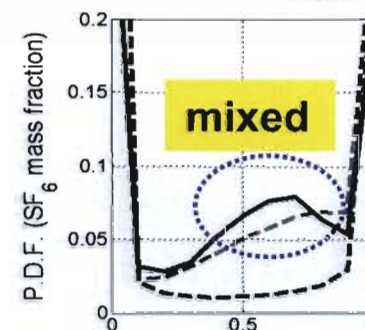
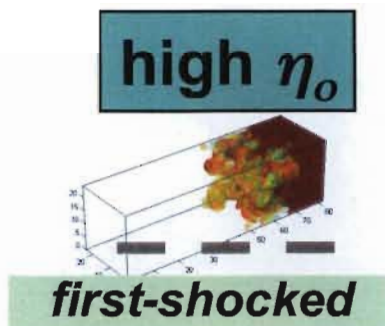
high η_o

first shock effects

AIAA-Hawaii-2011 / ETC13-Warsaw-2011 → PoF



Y_{SF6} visualizations
 $t \sim 3000 \mu s$
 after first-shock
 (or after reshock)



Planar Shock-Driven Turbulence

Grinstein, Gowardhan, and Wachtor, *PoF*, 2011; Gowardhan, Ristorcelli and Grinstein; *PoF Letters*, 2011
Shocked (double interface) Gas Curtain → Gowardhan and Grinstein, *J. of Turb.* 2011, in press



- RM bipolar behavior: **switch for $\eta_o = \kappa_o \delta_o \sim 1$**

low η_o : *linear, ballistic, mix-width $\delta \sim t$*

high η_o : *non-linear, mode coupling, mix-width $\delta \sim t^{1/2}$*

→ transition to turbulence suggested

→ more material mixing & smaller scales

- Reshock effects on first shock, if $\eta_o > 1$

- The modeler's (initial condition) challenge

- **two different** instabilities & growth trends

low η_o

→ as $\eta_o \uparrow$ *enstrophy* \uparrow *isotropy* \uparrow *TKE* \uparrow $\delta \sim t \uparrow$ ALL GROW with η_o

high η_o

→ as $\eta_o \uparrow$ *enstrophy* \uparrow *isotropy* \uparrow GROW with η_o

TKE \downarrow $\delta \sim t^{1/2} \downarrow$ DECREASE with η_o