



Preliminary Validation of a Complex Aerospace Structure

**Michael Arviso, D. Gregory Tipton, & Patrick S.
Hunter**

Sandia National Laboratories

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Introduction

- **Modal Vibration test data >> Validate FEM**
- **Uncertainty >> Validation process**
 - Measurements
 - Analysis predictions
- **Uncertainty quantification**
 - Fabrication uncertainty
 - Analysis uncertainty
 - Mesh convergence, Material modulus, Joint stiffness
- **Validation**
 - Final Configuration



Purpose

- **Uncertainty Investigation**
 - Test hardware
 - Finite Element Model
- **Validation of FEA Model**
 - Includes Uncertainty
- **Experimental Uncertainty**
 - Manufacturing (part to part)
 - Assembly
 - Measured data
- **Modeling Uncertainty**
 - Part tolerances / sizes
 - Material properties



Model Development / Validation Process

- Create finite element mesh*
- Calculate frequencies and mode shapes
- Calibrate model using test data
 - Test data collected from different input locations on structure than validation data
- Model verification
- Run uncertainty analysis
 - Determine properties to vary and probable ranges
 - Use Latin hypercube approach to generate multiple realizations of model
 - Run all realizations and compute model FRFs
- Evaluate validation metrics
- Measure FRFs / mode shapes on final configuration

*Steps completed previously and presented at IMAC XXVI & XXVII

Simplified Aerospace Structure

- **Structural Elements**

- **Outer Shell**

- includes 3 mounting holes at base

- **Interior Bracing**

- riveted & welded in place
 - rivets/welds not modeled explicitly

- **Payload Brackets**

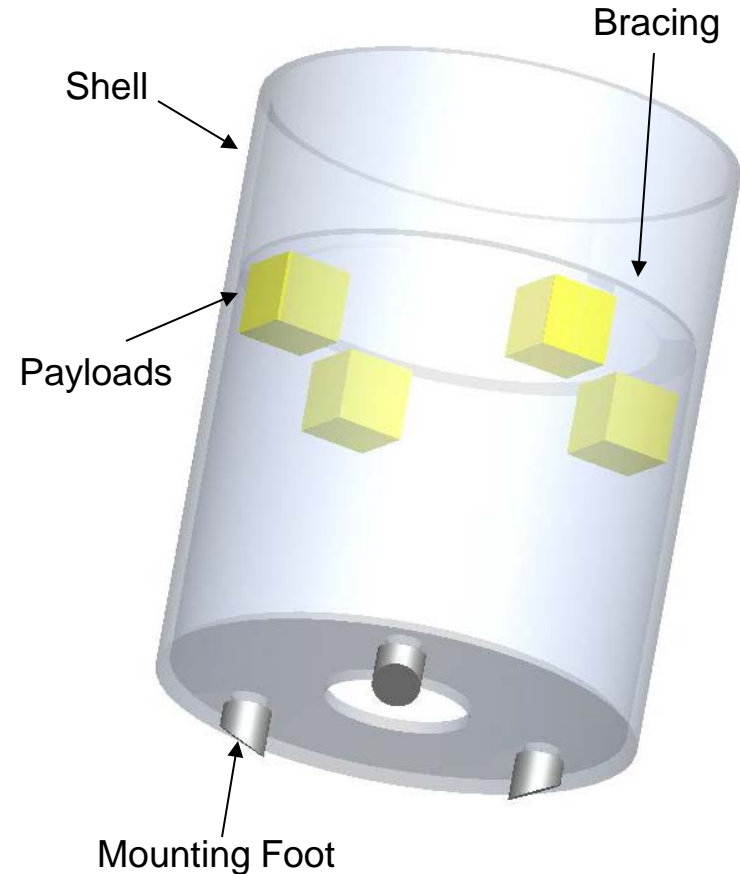
- bolted to bracing
 - bolts modeled with 1D springs

- **Payloads**

- bolted to brackets
 - bolts modeled with 1D springs

- **Mounting Feet**

- suspension points for free-free modal test





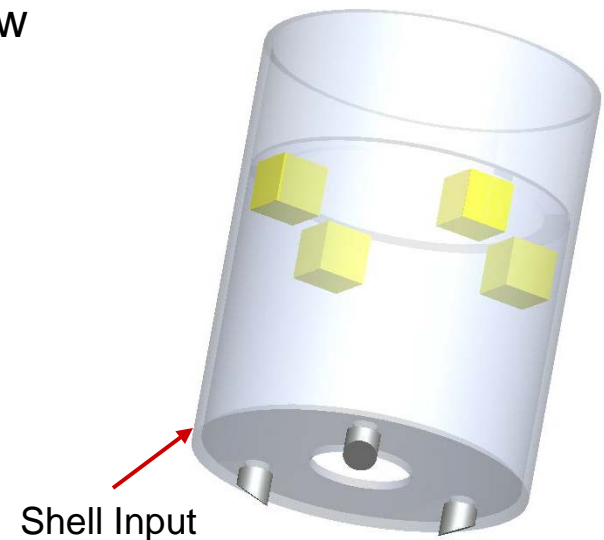
Analysis Model

- **Finite Element Model**
 - 400,000 2nd order elements
 - 5.6 million degrees of freedom
- **Computing**
 - **Model run using Salinas***
 - 5 hours on 100 processors
 - Computed modes and FRFs up to 2000 Hz

*Structural dynamics code developed at Sandia National Laboratories

Test Program

- **Lightly damped system**
 - $\frac{1}{2}$ - 1% across frequency range (100 - 1000 Hz)
- **Modal shaker used to excite system**
 - continuous random input with Hanning window
 - minimize nonlinearities
 - accurate constraint of input locations and directions
- **Input location on shell**
 - oriented input 30° from vertical
- **Modes extracted up to 1000 Hz using SMAC* algorithm**
- **Data Collected**
 - Modal frequencies
 - Mode shapes
 - FRFs
 - Modal damping

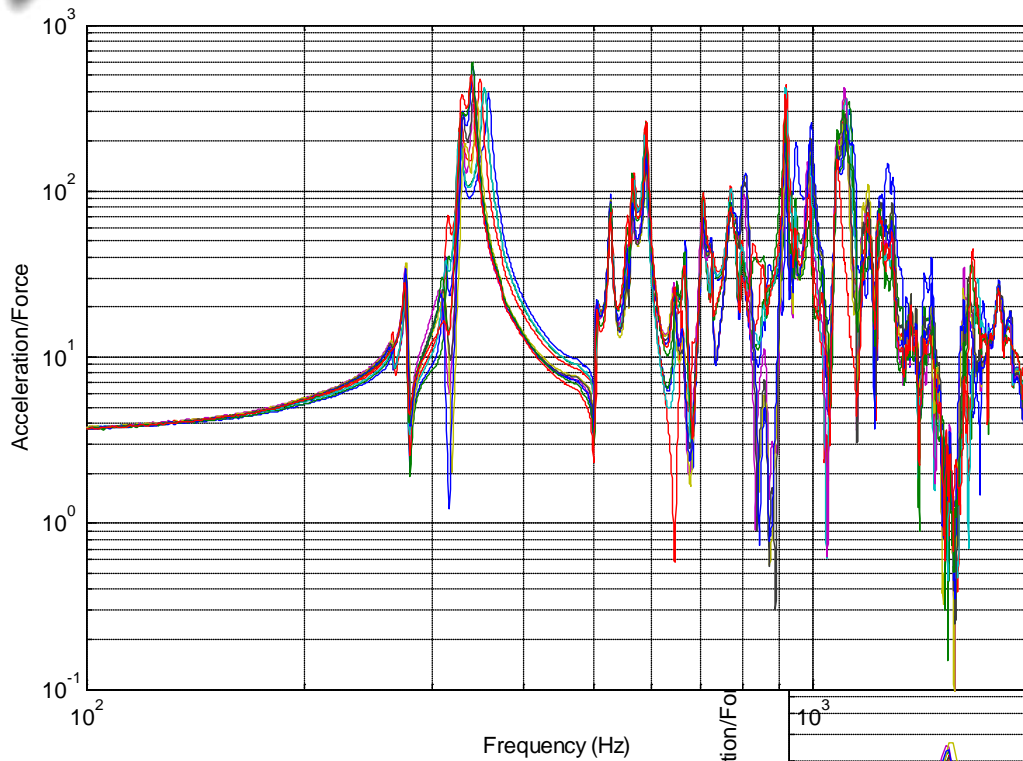




Uncertainty Quantification

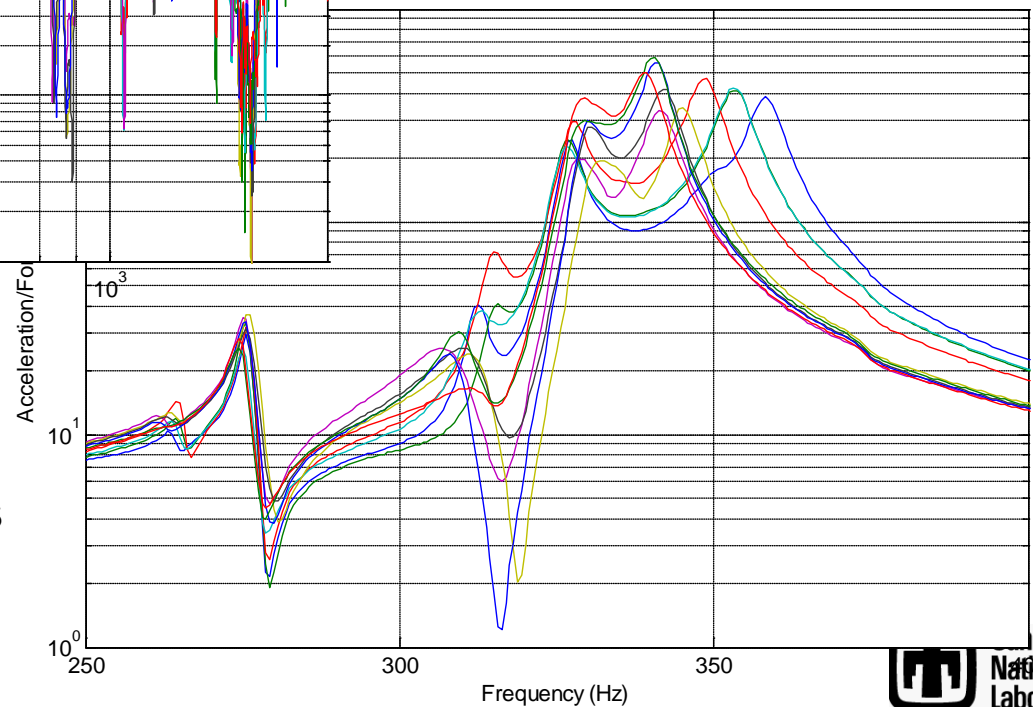
- **Areas of uncertainty**
 - Manufacturing (part to part variation)
 - **Assembly**
 - Measurement
 - Modeling
- **Assembly Uncertainty**
 - **Assembly - Disassembly – Reassembly**
 - **Different Individuals**
 - **Variations – Component Exchange**
 - **10 buildups**

Assembly Variability FRF's



Full Spectrum

First Lateral & Axial Modes





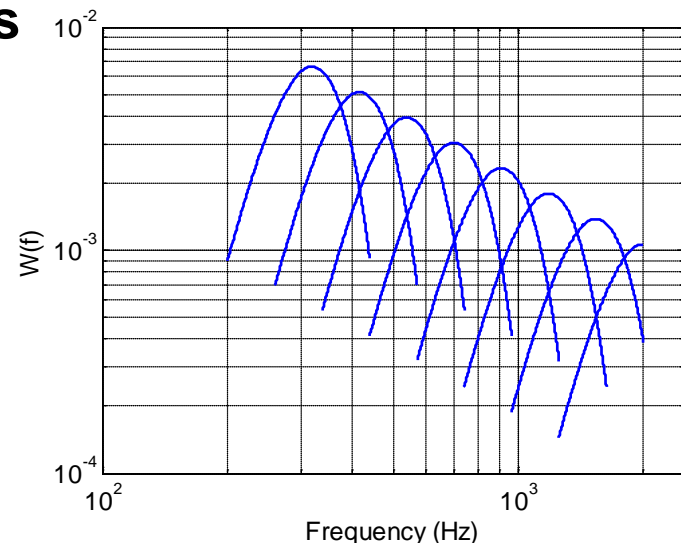
Uncertainty Quantification

- **Areas of uncertainty**
 - Manufacturing (part to part variation)
 - Assembly
 - Measurement
 - **Modeling**
- **Modeling Uncertainty**
 - Material Modulus of Elasticity
 - Sheet Metal Thickness
 - Bolted Joint Stiffness



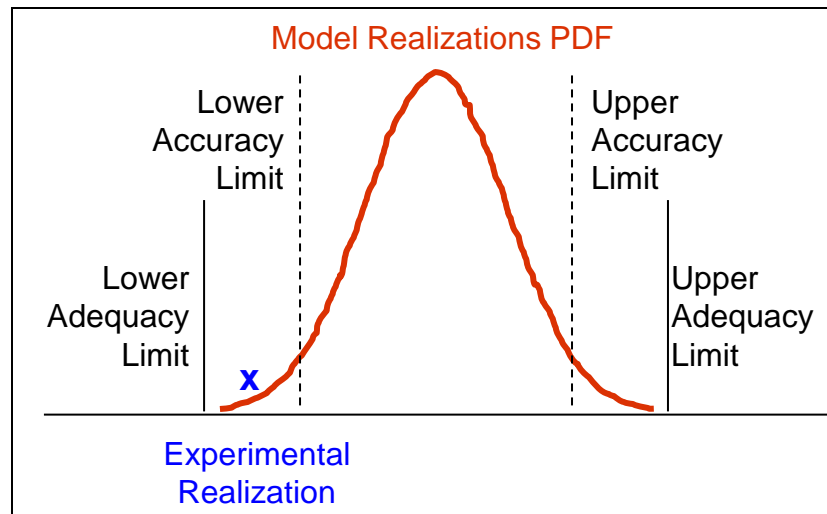
Model Validation

- **Numerical Comparison**
 - 50 Analytical FRF's
 - 10 Experimental FRF's
- **Simplification**
 - 2 locations on payloads used as validation points
 - FRF's calculated in 3 directions
 - Total of 6 validation FRF's
- **Comparison**
 - Multiply FRFs by weighting function to compare response in frequency bands

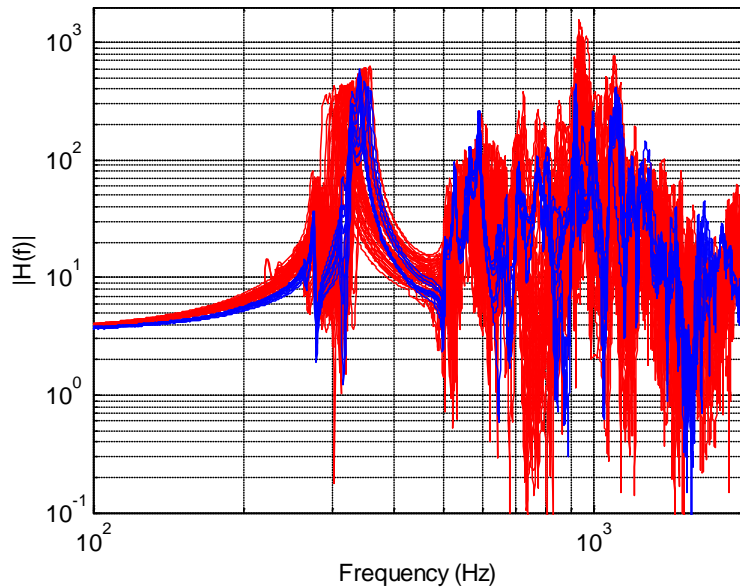


Validation Process

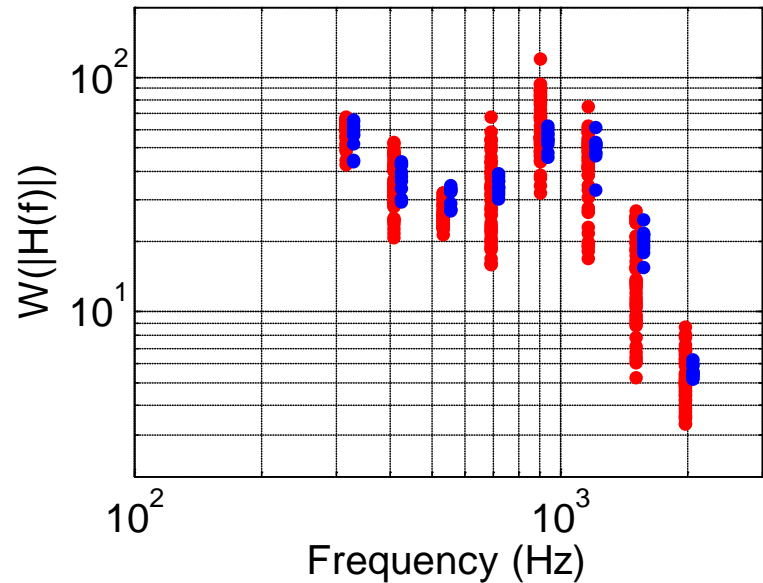
- At each validation point and each frequency window
 - 50 model realizations and 10 experimental realizations
 - FRF is multiplied by weighting function and integrated
 - Probability density function (PDF) created from model realizations
 - Each experimental realization is compared to model PDF
 - **Accuracy assessment** – falls within 90% probability window
 - **Adequacy assessment** – “good enough” model (often ± 6 dB)



Validation Point 1 – Payload 1, Axial



**Experimental FRFs (blue) and
Model FRFs (red)**



**Experimental and Model
Validation Metrics**



Validation Statistics

Validation Point	Location	Direction	Validated Data Points		
			Adequate $\pm 6\text{dB}$	Adequate $\pm 3\text{dB}$	Accurate
1	Payload 1	Axial	100%	100%	90%
2	Payload 1	Lateral	100%	89%	26%
3	Payload 1	Lateral	100%	74%	41%
4	Payload 2	Axial	100%	100%	75%
5	Payload 2	Lateral	100%	85%	30%
6	Payload 2	Lateral	100%	94%	25%

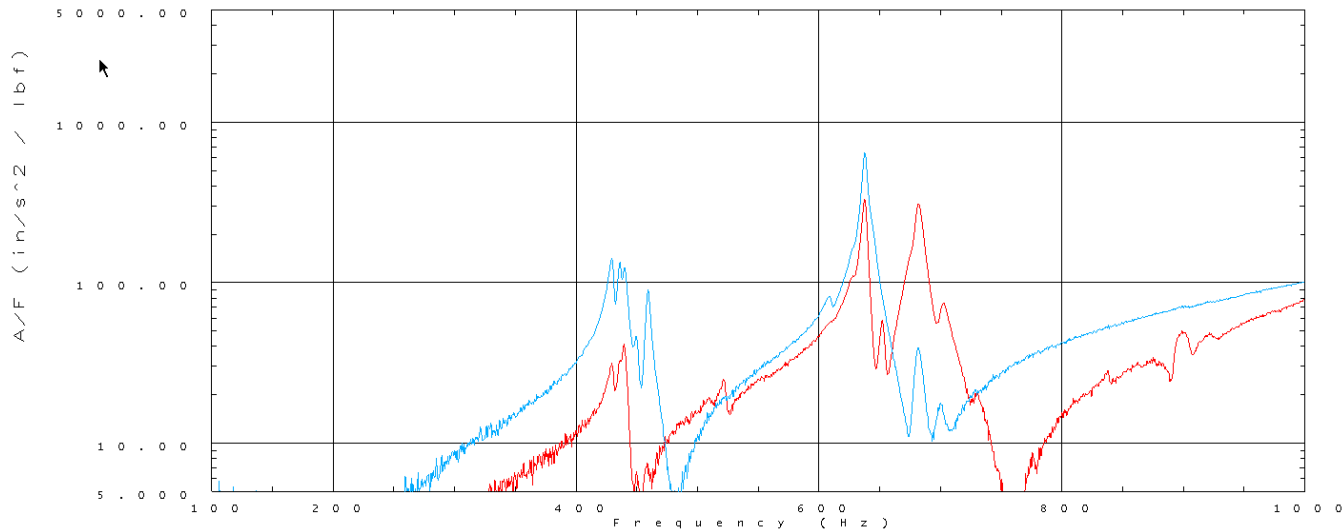
84% of assessments must meet criteria for model to be validated



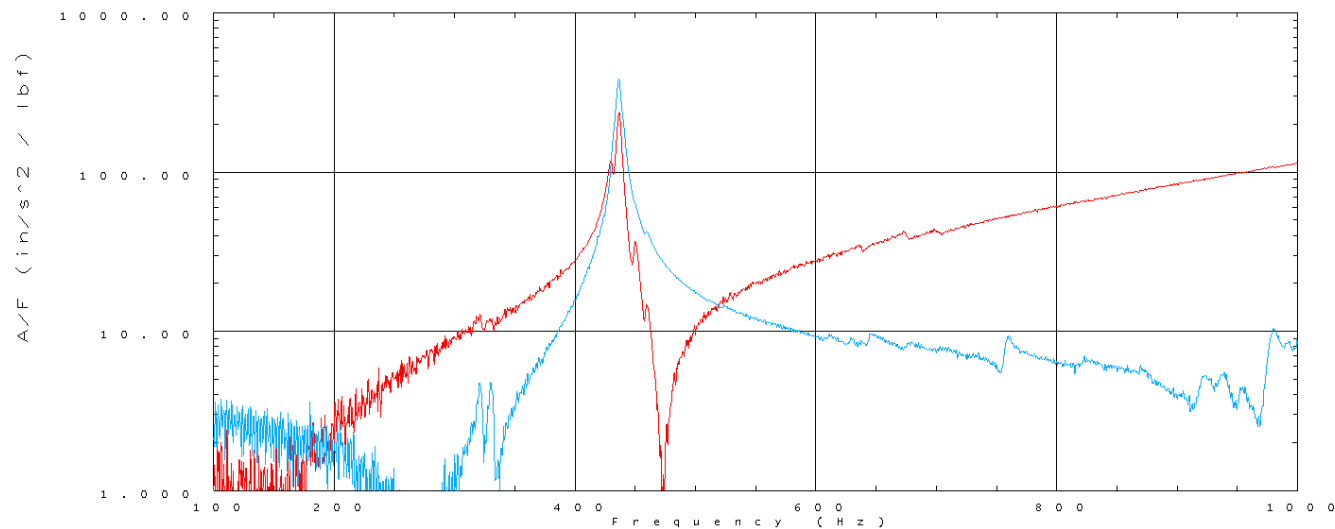
Final Configuration Testing

- **Excitation**
 - Modal Hammer
 - Shaker
- **Instrumentation**
 - 204 Accelerometers
- **Data Acquisition**
 - 0 to 2000 Hz
- **Data**
 - 30 modes
 - Damping $\frac{1}{4}\%$ to 2%

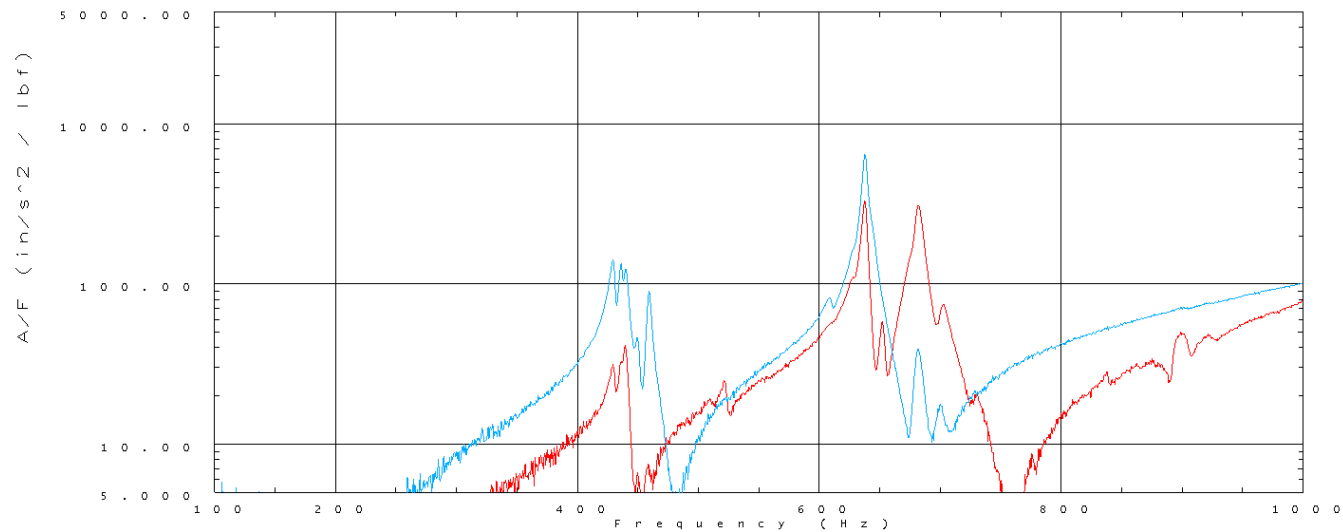
Driving point FRF for inputs normal to shell



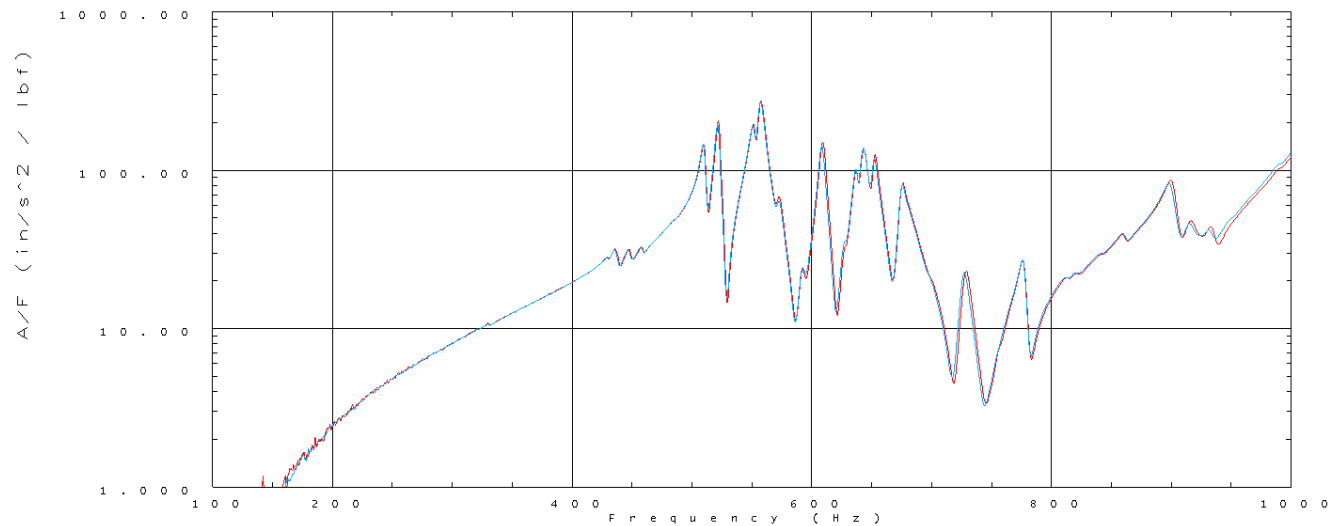
Driving point FRF for inputs axial to shell



Driving point FRF for inputs tangential to shell



Driving point FRF with shaker input

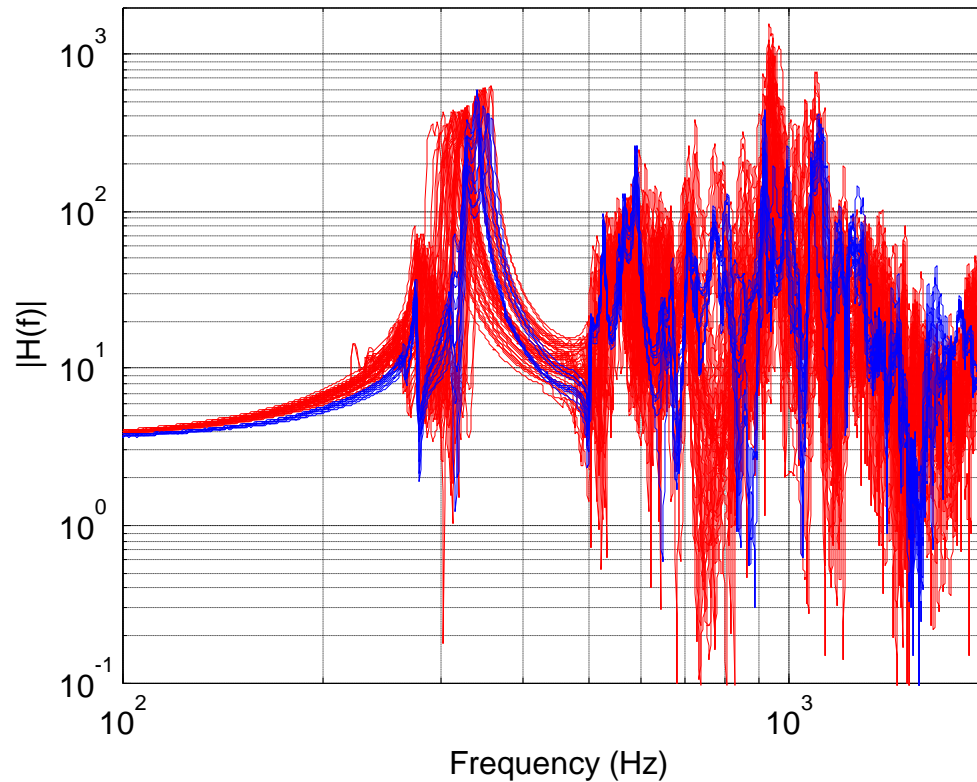




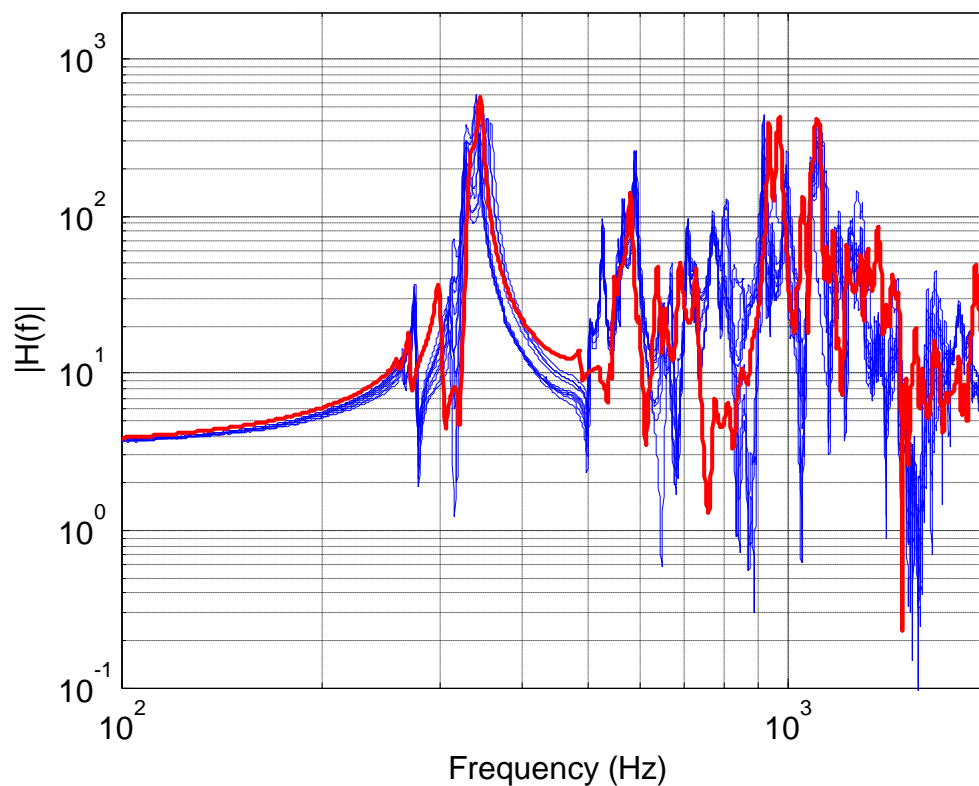
Analysis Mode Updating – Subassembly of Main Structure

Mode Description	Test Frequency (Hz)	Analysis Frequency Before (Hz)	Error Before	Analysis Frequency After (Hz)	Error After
2,0 Ovaling / Payloads In Phase with Shell	259	173	-33%	261	0.7%
2,0 Ovaling / Payloads In Phase with Shell	271	175	-35%	273	0.6%
2,0 Ovaling / Payloads Out of Phase with Shell	299	257	-14%	301	0.6%
2,0 Ovaling / Payloads Out of Phase with Shell	321	280	-13%	322	0.4%
Payloads Axial	348	236	-32%	356	2.2%
One Payload Rocking	527	406	-23%	535	1.5%
3,0 Ovaling / All Payloads Out of Phase with Shell	644	618	-4%	644	0.0%
3,0 Ovaling / 2 Payloads Out of Phase with Shell	678	634	-6%	672	-0.9%
3,0 Ovaling / 2 Payloads Out of Phase with Shell	696	657	-6%	694	-0.3%
3,0 Ovaling / 2 Payloads Out of Phase with Shell	702	698	-1%	678	-3.5%
3,0 Ovaling / 2 Payloads Out of Phase with Shell	722	717	-1%	739	2.3%

Validation Point 1, All Model Results (red) and Experimental Results (blue)



Validation Point 1, Calibrated Model Results (red) and Experimental Results (blue)





Preliminary Analysis vs. Test Frequencies

Mode Description	Test Frequency (Hz)	Preliminary Analysis Frequency (Hz)	Error
Payloads axial Out of Phase	322	323	-0.3%
Main Payload top rocking; Payloads axial In Phase	438	325	-25.8%
Payloads axial In Phase	331	326	-1.5%
Main Payload top rocking	459	327	-28.8%
Axial – Main top & bottom Payloads Out of Phase	448	415	-7.4%
Bending – Main bottom Payload rocking	430	462	7.4%
Bending – Main bottom Payload rocking	436	467	7.1%
2,1 Ovaling – Payloads Lateral Out of Phase	510	533	4.5%
Payload & Bottom bracing Axial	609	550	-9.7%
2,1 Ovaling – Payloads Lateral In Phase	551	561	1.8%
Payloads Lateral In Phase	558	578	3.6%
Payload 1 Lateral – Small Payload Axial	771	599	-22.3%
Torsion	638	618	-3.1%
2,2 Ovaling – Payload Lateral Out of Phase	522	625	19.7%
2,2 Ovaling – Payload 1 Lateral – Small Payload Axial	643	642	0.2%
2,2 Ovaling – Payload 1 Axial	675	674	-0.1%
2,3 Ovaling – Small Payload Axial	700	675	-3.6%
2,3 Ovaling	891	697	-21.8%
Top bracing rocking	728	767	5.4%



Discussion

- **Modeling uncertainty**
- **Uncertainties in this model reasonable?**
 - **Look at variation of mode at 350 Hz**
 - 10-15% variation in model
 - 5.5% variation in experiments
- **Is it possible to add too much uncertainty?**
 - **Yes, but it is impossible to completely eliminate it**
 - **Real parts & assemblies have variability**
- **Final configuration is single representation**



Conclusions

- **Model Validation**
 - Solution Verification
 - Uncertainty Quantification
 - Validation – Numerical comparison of experimental and model results
- **Test Data vs. Model Data**
 - Model correlation
 - Additional testing
 - Final Validation test