



# **Coupled Thermo/Hydro Dynamic Models of High Temperature Interface Evolution**

**Frank van Swol (1814)**

**Kent Van Every (1831)**

**Aaron Hall (1831)**

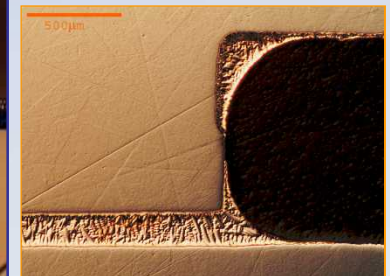
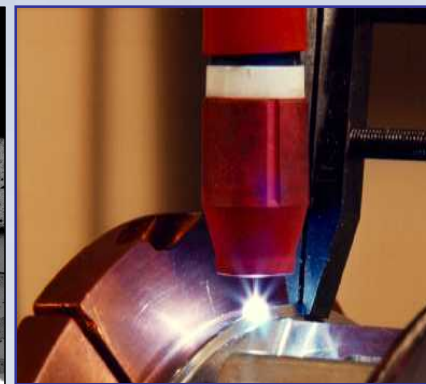
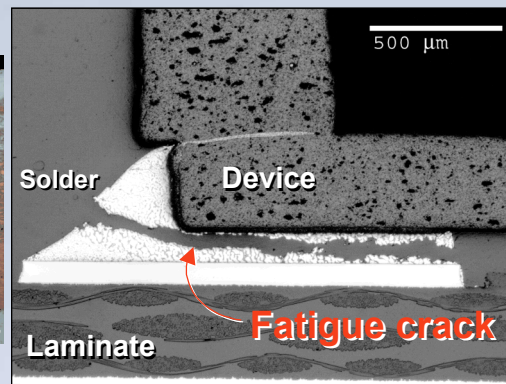
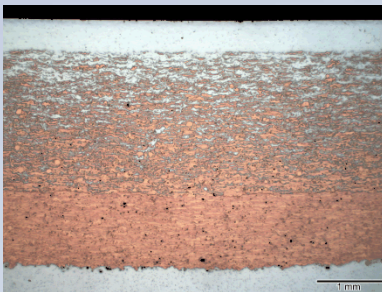
**Jeremy Lechman (1516)**

**Edmund Webb III (Lehigh Univ.)**



# The Problem: Reactive Wetting and Spreading

- Reactive wetting and solidification are critical to interface formation in soldered, brazed, and welded joints, along with thermal spray coatings
- Continuum models of interface are needed to
  - Improve fundamental understanding
  - Predict/enhance interface performance & reliability

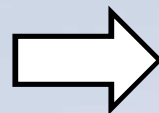
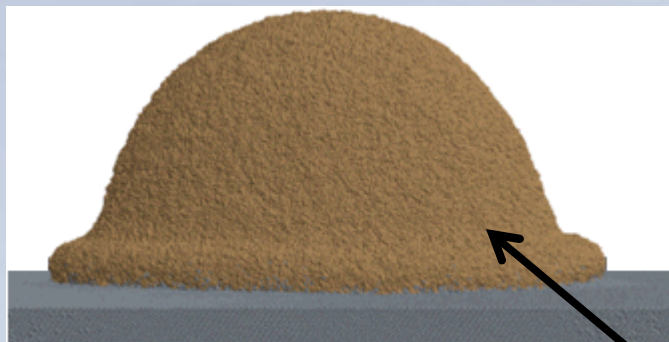




# Continuum Model Challenges

## Reactive interface problem combines:

- Large gradients (temperature, velocity, etc.)
- Moving boundaries
- Chemical-dependent boundary conditions
- Nonequilibrium thermodynamics



Liquid      Solid

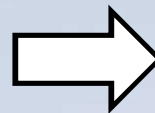
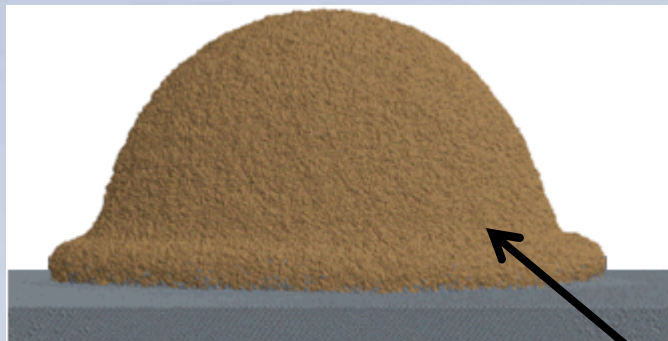


# Continuum Model Challenges

## Reactive interface problem combines:

- Large gradients (temperature, velocity, etc.)
- Moving boundaries
- Chemical-dependent boundary conditions
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Need  
Molecular  
Dynamics (MD)  
Simulations



Liquid      Solid





# MD State of the Art

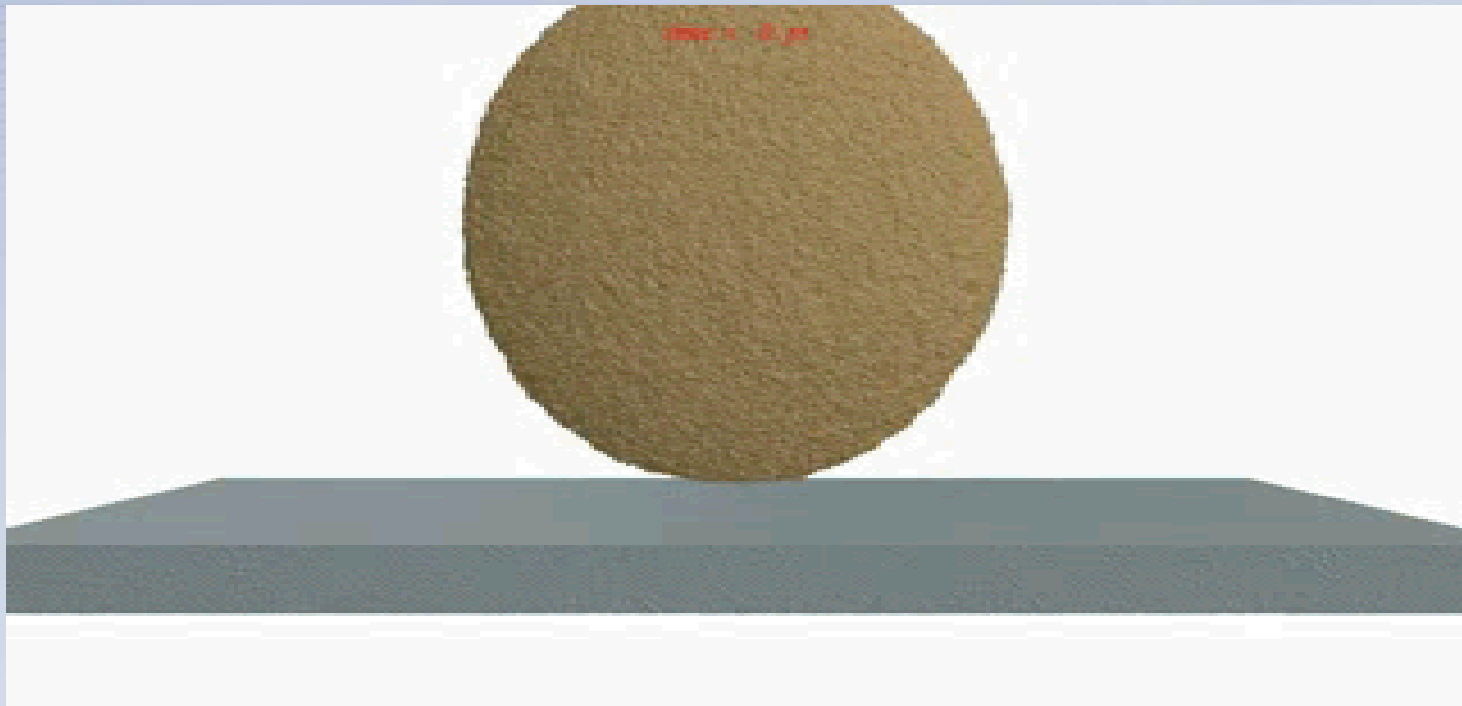
- **Recent MD simulations can accurately reproduce experimental droplet impact behavior**
  - MD can model the same dimensionless Weber #s as experiments
  - Same velocity and diameter dependence found between simulations and experiments
- **With MD, atom populations can provide detail and resolution of droplet and substrate physics not previously possible**



# MD Simulation

- **50 nm Cu droplet onto Pb (111) Solid Surface**

$$v_d = 400 \text{ m/s} \quad T_{\text{Cu}} = 2500 \text{ K} \quad T_{\text{Pb}} = 300 \text{ K} \quad N_{\text{atom}} \sim 40 \times 10^6$$

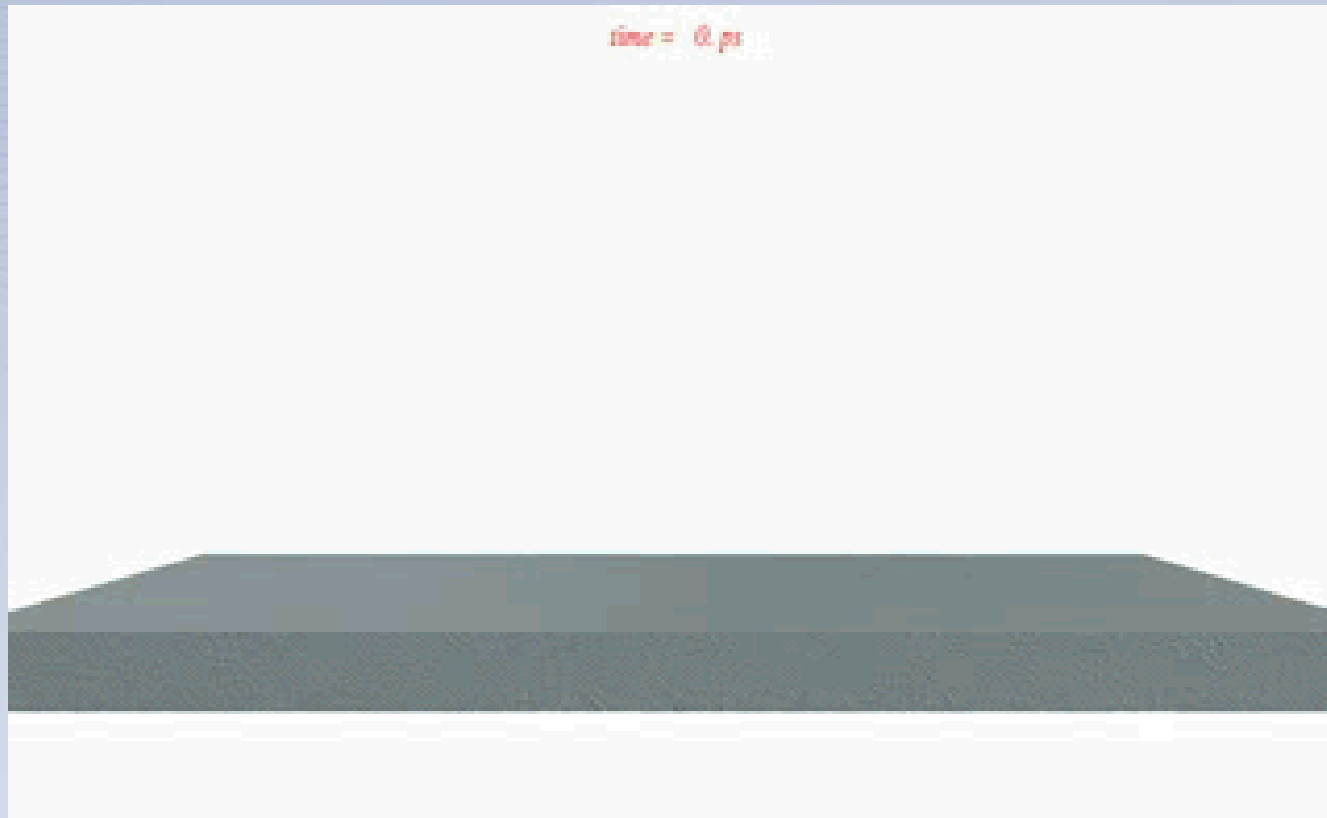




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# Project Approach

Jeremy Lechman

Continuum  
Modeling  
(Sierra/Aria)

Aaron Hall  
Kent Van Every

Experimental  
Data

**Test  
Case**

Frank van Swol  
Edmund Webb III

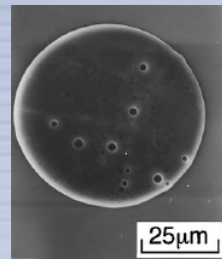
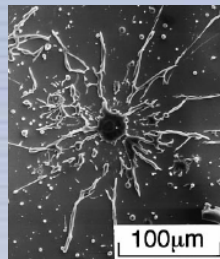
MD  
Modeling  
(LAMMPS)





# Archetypical Test Case

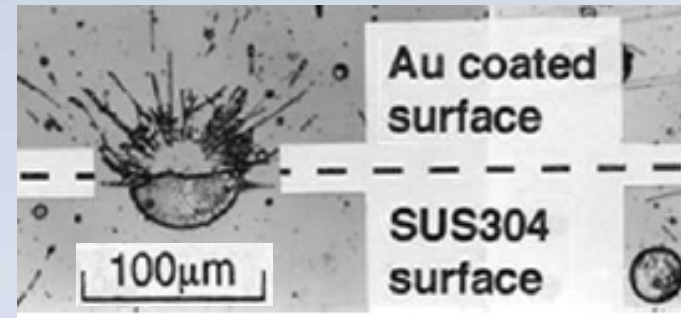
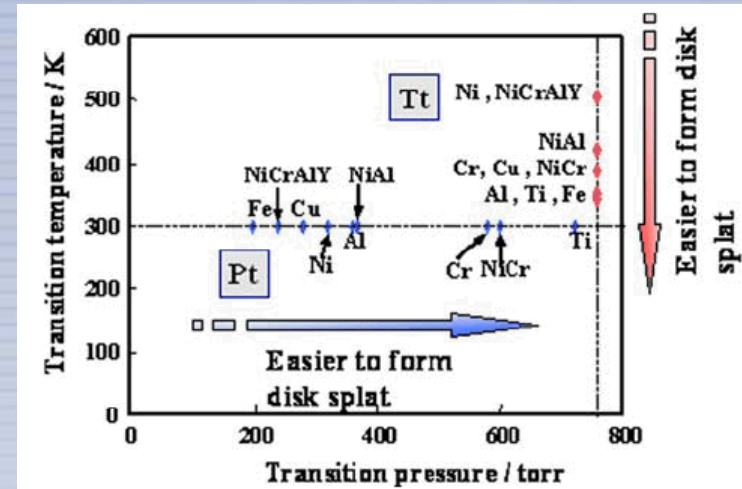
- **Droplet impacting on a solid surface**
  - Model splash-to-disk transition



- **Transition behavior depends on:**  
 $P_{amb}$ ,  $T_{sub}$ ,  $\gamma$ ,  $p_d$ ,  $t_{solid}$ , ...

- **Applicability to joining**

- $\gamma$  governs solder joint shape
- Heat transfer during arc welding depends upon  $p_d$
- $P_{amb}$  can alter weld pool surface



Y. Tanaka, *Surf. Coat Tech.*, 120-121 (1999)  
 Fukumoto, *J. Therm. Spray Tech.*, 16 (2007)



# Thermal Spraying vs. Joining Process

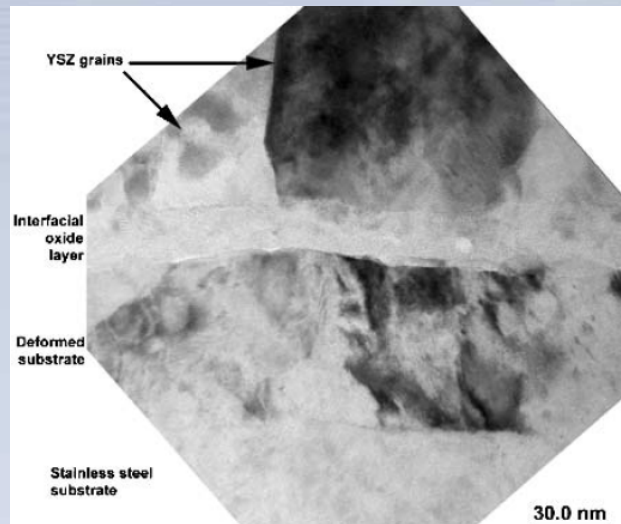
- **Droplet conditions are better controlled in a thermal spray process**
- **A wider range of droplet conditions are possible with thermal spraying**
  - Droplet velocity range: 50 – 500 m/s
  - Droplet temperature range: 100 – 3500°C
- **A wider range of droplet and substrate compositions are possible with thermal spraying**



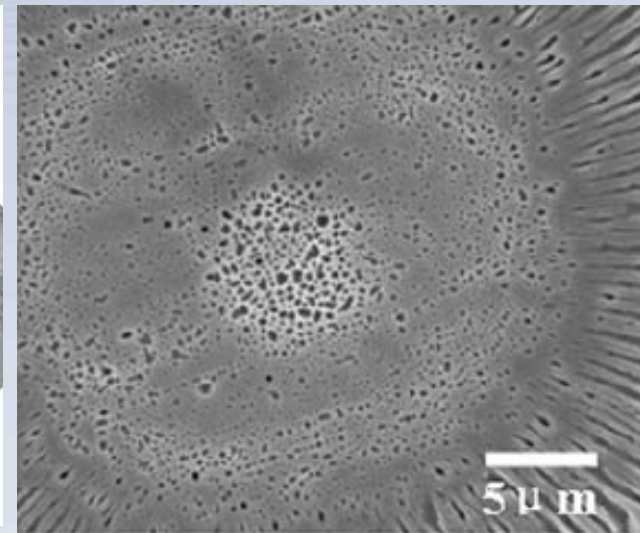
# Experimental Data for Simulations

- **Determine splash/disk regimes for Cu splats on Cu plate**
  - Deposit droplets via air plasma spray
  - Measure  $D_d$ ,  $T_d$ , and  $v_d$  @ impact

} Current TSRL capabilities
- **Splat & splat – substrate interface characterization**
  - Composition gradient
  - Grain structure
  - Porosity
  - Shape



TEM of splat-substrate interface

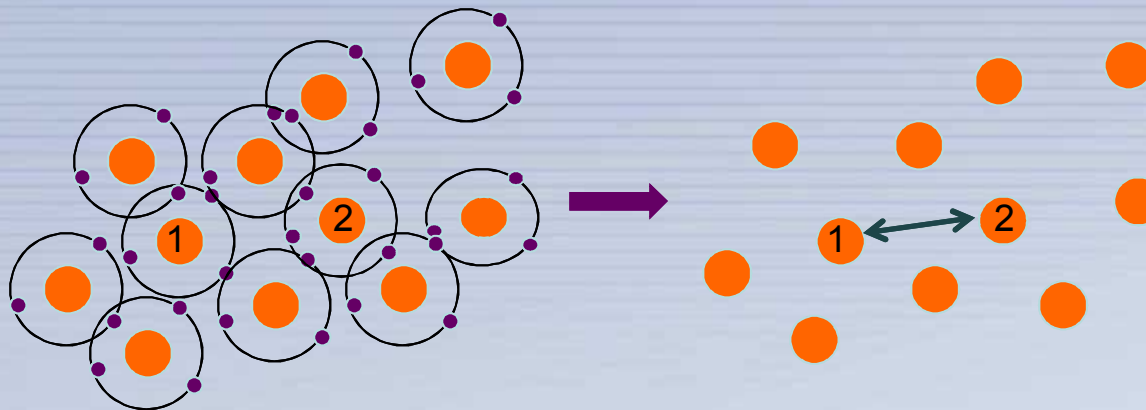


SEM of splat bottom



# Required MD Development

**Limitation:** Embedded Atom Method (EAM) integrates out electronic degrees of freedom



- Thermodynamics & metal ion dynamics captured in “atom” potentials
- Contribution of electrons to conduction is lost

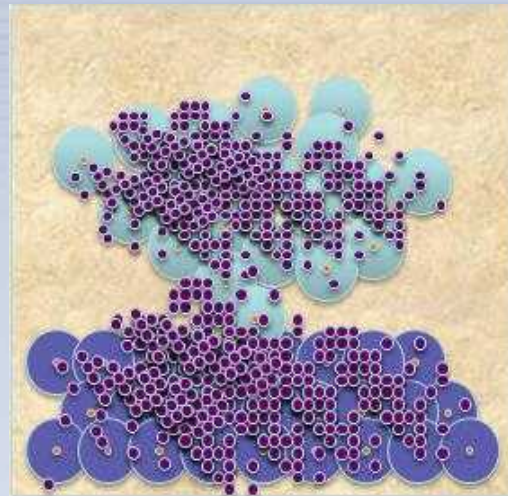
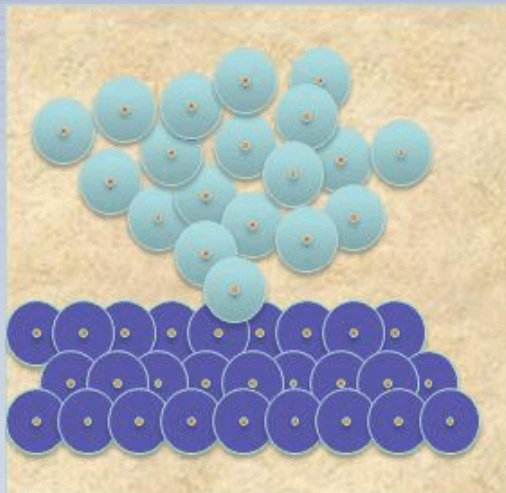




# Enabling Electronic Conductivity

## Novel Multiparticle Collision Dynamics (MPCD) Approach

- Integrate into LAMMPS a fluctuating background thermal fluid bound to metal ions
- Perform local “collisions” to update background fluid



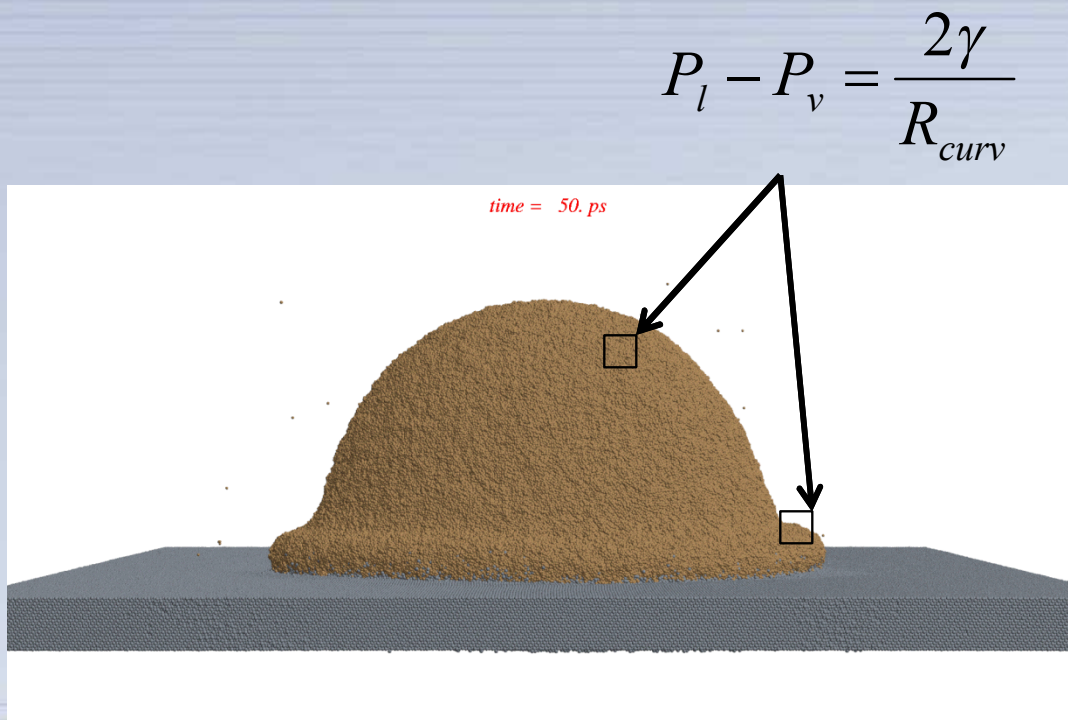
**Advantage:** Reflects local, strongly varying electron density.





### 3. The Problems

## Connecting MD and continuum example



independently  
measure

$$\frac{2}{R_{curv}} = \frac{1}{R_x} + \frac{1}{R_y}$$

and

$$P_l - P_v$$



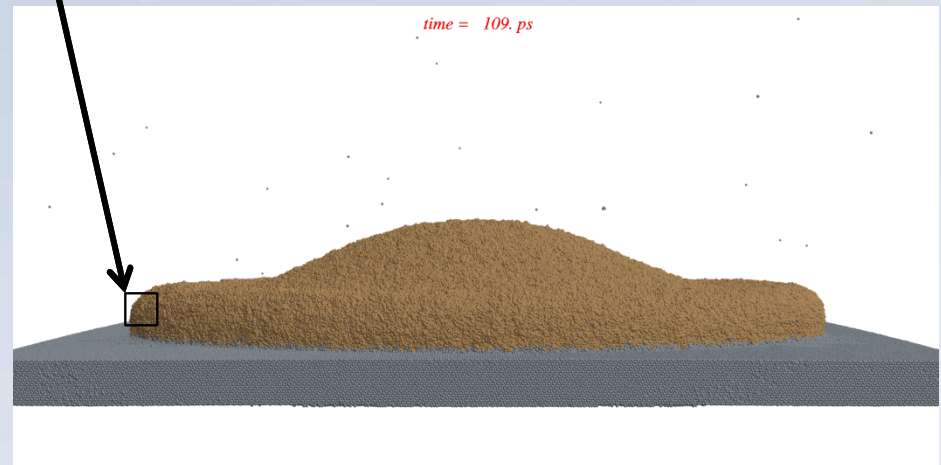
### 3. The Problems

**Reactive Wetting is a chemical boundary condition**

equilibrium

$$\left. \begin{aligned} \cos \theta &= \frac{\gamma_{SL} - \gamma_{SV}}{\gamma_{LV}} \\ \gamma_{SL} &= \gamma_{SL}(x) \end{aligned} \right\} \therefore \theta = \theta(x)$$

(bulk)  
equilibrium  
composition





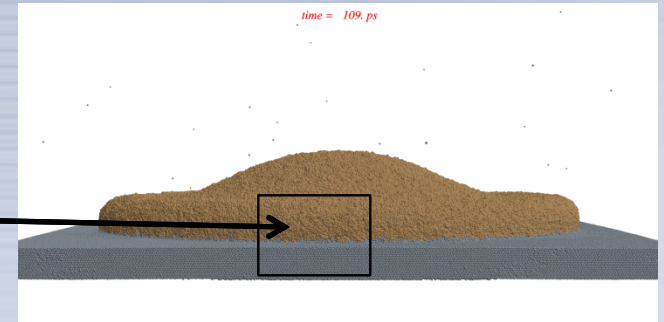
### 3. The Problems

**Solid-liquid interface is generally not at equilibrium**

conclude: SL surface free energy is a functional of the local composition profile

$$\gamma_{SL} = \gamma_{SL}[x(\mathbf{r})] \Rightarrow \theta = \theta[x(\mathbf{r})]$$

↑  
composition profile



**Novel solution:** two-step approach to obtaining  $\gamma_{SL}[x(\mathbf{r})]$

1. obtain profile  $x(\mathbf{r})$  from MD
2. generate  $\gamma_{SL}$  from  $x(\mathbf{r})$  with constrained fluids density functional theory (DFT)

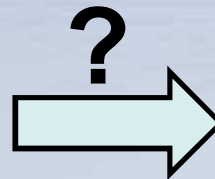
(Note, DFT for EAM potentials is a new idea)



# Linking MD and Continuum Models

Solid-liquid (SL) interface is generally not at equilibrium

- SL surface free energy ( $\gamma_{SL}$ ) is a function
- of the local composition profile,  $x(r)$



- Provides  $x(r)$
- $\gamma_{SL}$  hard to obtain

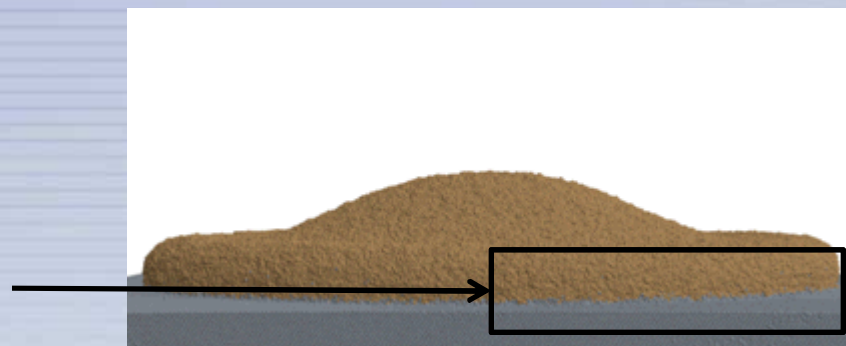
- Needs  $\gamma_{SL}$  to calculate wetting contact angle



# Linking MD and Continuum Models

## Novel Approach to Obtaining $\gamma_{SL}[x(r)]$

1. Obtain profile composition profile,  $x(r)$ , from MD



2. Utilize constrained fluids density functional theory (DFT) in Tramonto code to calculate  $\gamma_{SL}$  directly from  $x(r)$





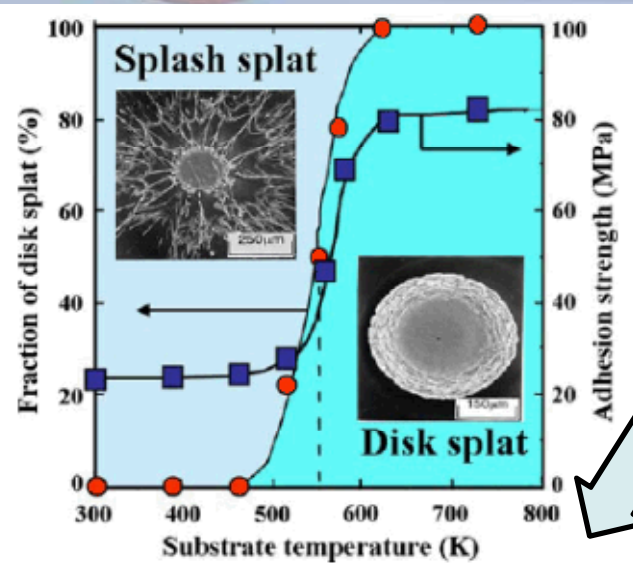
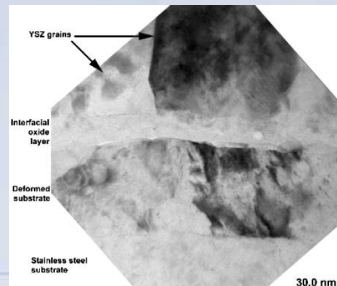
# Summary

Continuum  
Modeling



Experimental  
Data

MD  
Modeling





# Milestones

- **Determine splash and disk temperature regimes for Cu splats on Cu plates**
- **Utilize MD droplet simulations to reproduce Cu on Cu splash to disk transition behavior**
- **Evaluate capabilities of current continuum codes to model the test case**
- **Sandia is a multi-program laboratory operated by Sandia Corporation, a Lockheed-Martin Company, for the U.S. DOE under Contract No. DE-AC04-94AL85000.**