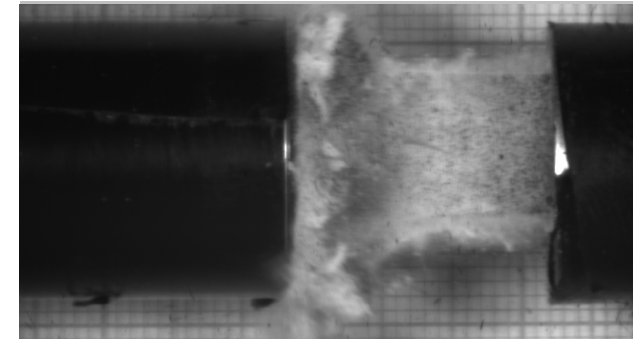
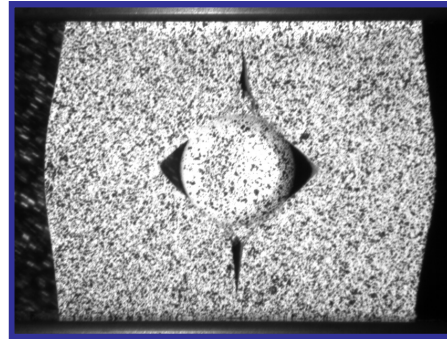
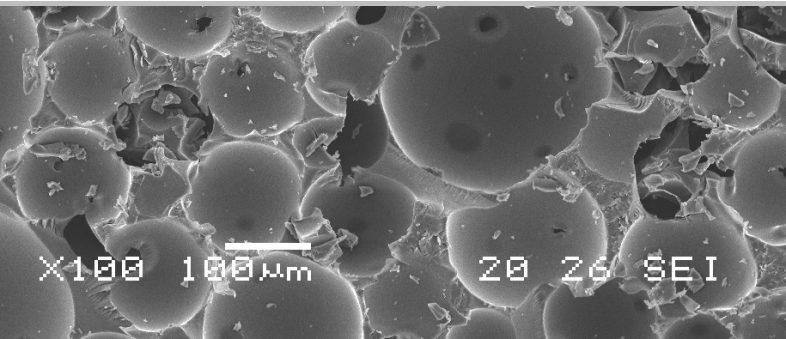


*Exceptional service in the national interest*



## Confined Compression of Rigid Foams - Experiment

Wei-Yang Lu, Kevin Connelly

# Collaborators

Modeler

Mike Neilsen

Analyst

Shivonne Haniff, Terry Hinnerichs

# Background

## Unified Creep Plasticity Model for Foam Neilsen, M et al (2006),

Yield Function from  
Plasticity Model

$$\varphi = \sigma^* - a = 0$$

where

$$\sigma^* = \sqrt{\bar{\sigma}^2 + \frac{a^2}{b^2} p^2}$$

Inelastic Rate is Given by

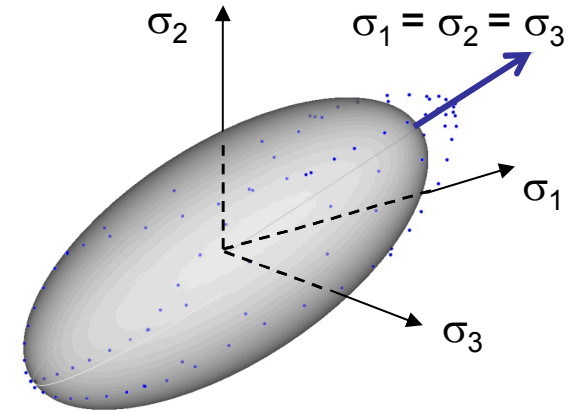
$$\dot{\boldsymbol{\varepsilon}}^{vp} = \begin{cases} h(\theta) \left\langle \frac{\sigma^*}{a} - 1 \right\rangle^{n(\theta)} \mathbf{g} & \text{when } \frac{\sigma^*}{a} - 1 > 0 \\ \mathbf{0} & \text{when } \frac{\sigma^*}{a} - 1 \leq 0 \end{cases}$$

Non-associated Flow

$$\mathbf{g} = (1 - \beta) \mathbf{g}_{associated} + \beta \mathbf{g}_{radial}$$

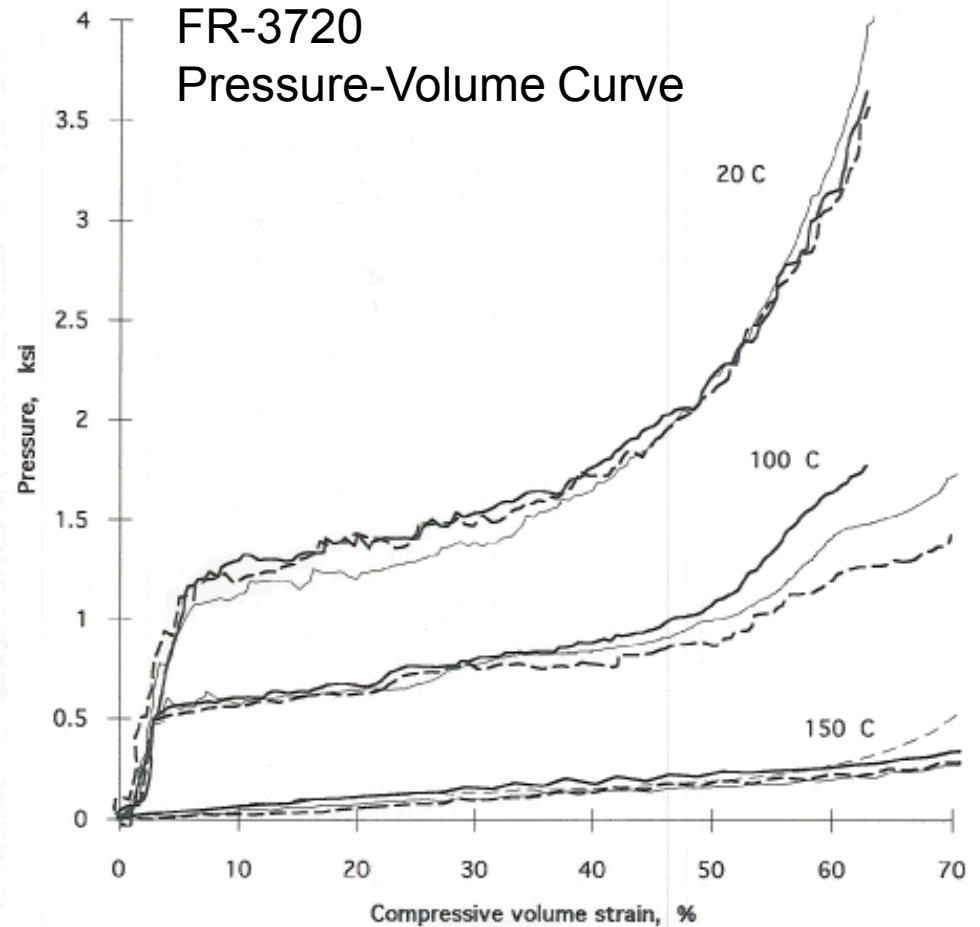
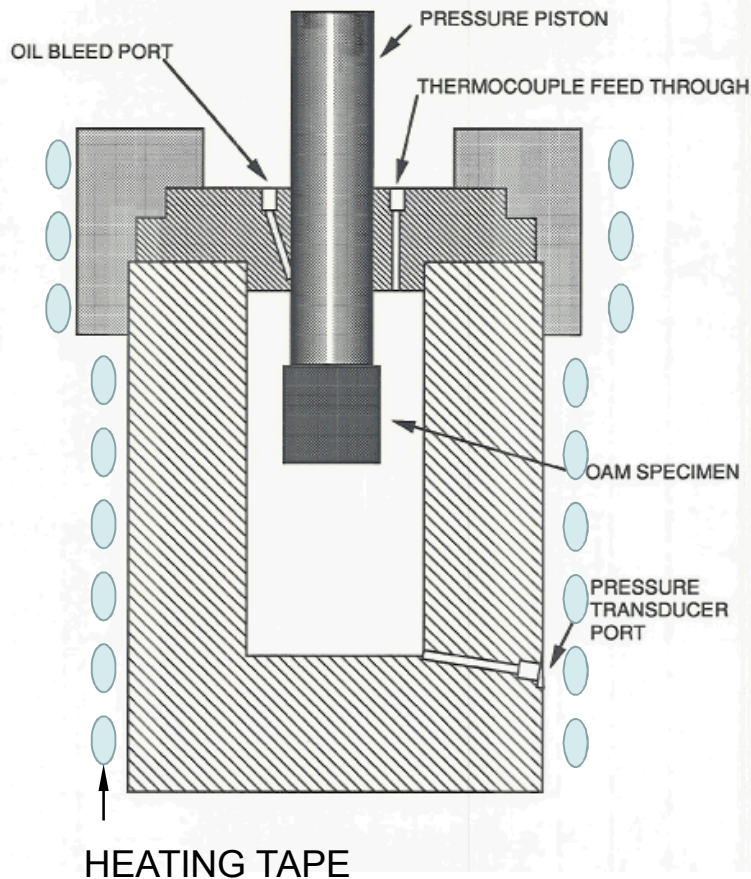
where

$$\mathbf{g}_{radial} = \frac{\boldsymbol{\sigma}}{|\boldsymbol{\sigma}|} = \frac{\boldsymbol{\sigma}}{\sqrt{\boldsymbol{\sigma} : \boldsymbol{\sigma}}}, \quad \mathbf{g}_{associated} = \frac{\frac{\partial \varphi}{\partial \boldsymbol{\sigma}}}{\left| \frac{\partial \varphi}{\partial \boldsymbol{\sigma}} \right|} = \frac{\frac{3}{a^2} \mathbf{s} - \frac{2}{3b^2} p \mathbf{i}}{\left| \frac{3}{a^2} \mathbf{s} - \frac{2}{3b^2} p \mathbf{i} \right|}$$



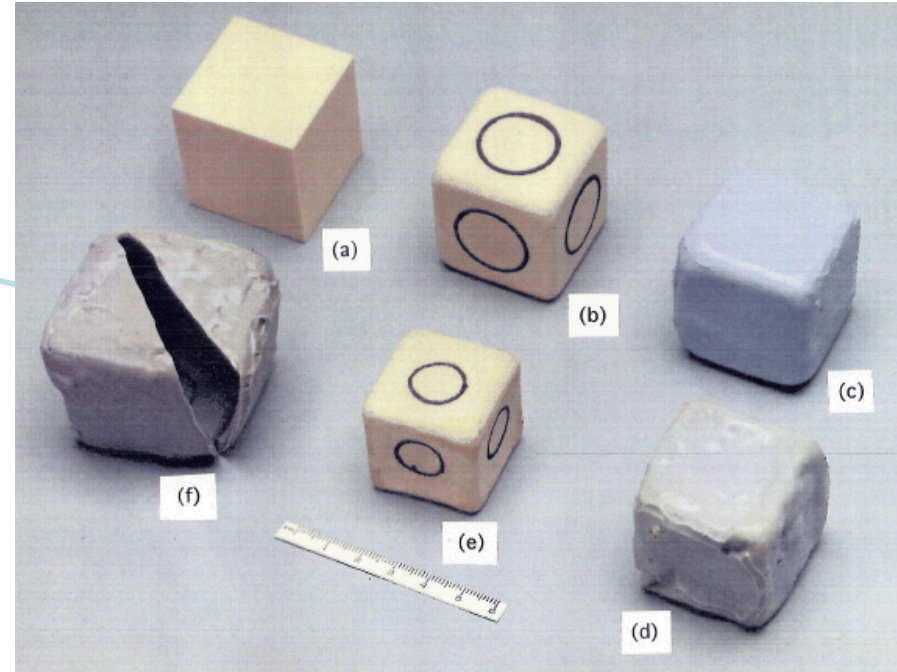
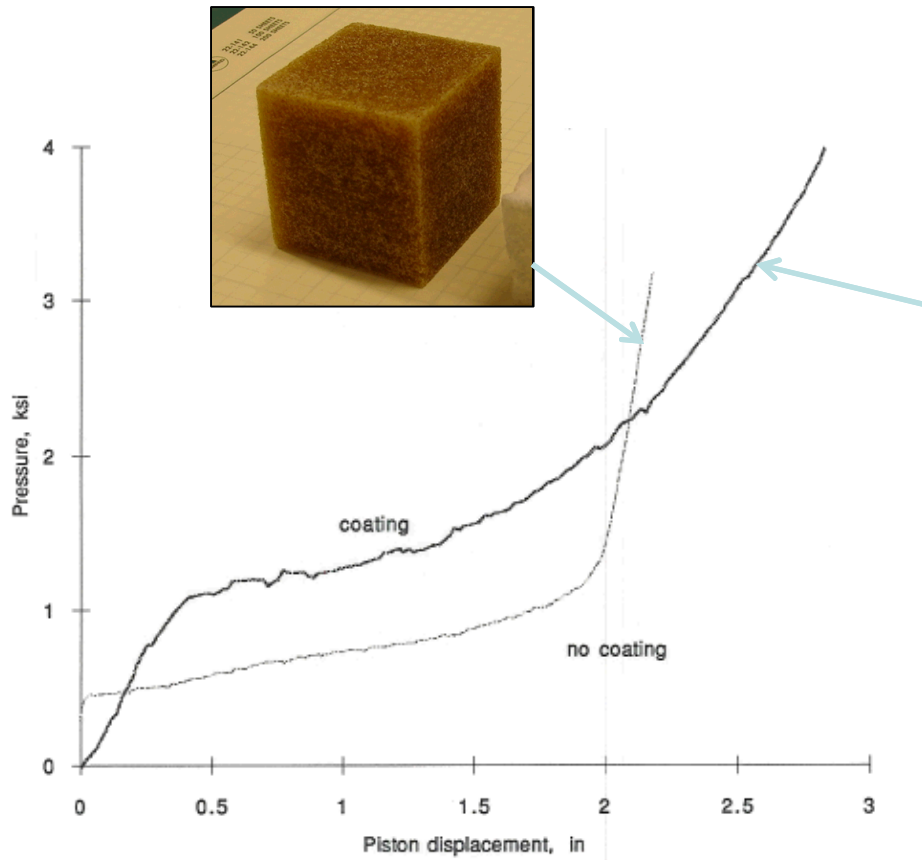
- References: Perzyna, P (1971) "Thermodynamic theory of viscoplasticity." *Advances in Applied Mechanics* 11: 313-354.  
 Zhang, J et al (1998) "Constitutive Modeling of Polymeric Foam ....." *Int. J. Impact Engng* 21-5: 369-386.  
 Neilsen, M et al (2006) IMECE2006-14551, *Proceedings of IMECE, ASME Press*.  
 Neilsen, M et al (2013) "Unified Creep Plasticity Damage (UCPD) Model for Rigid Polyurethane Foams"

# Hydrostatic Compression



W-Y Lu ; J Korellis ; K Lee ; R Grishaber, "Hydrostatic and uniaxial behavior of a high density polyurethane foam (FR-3720) at various temperatures," SAND93-8227, March 1993.

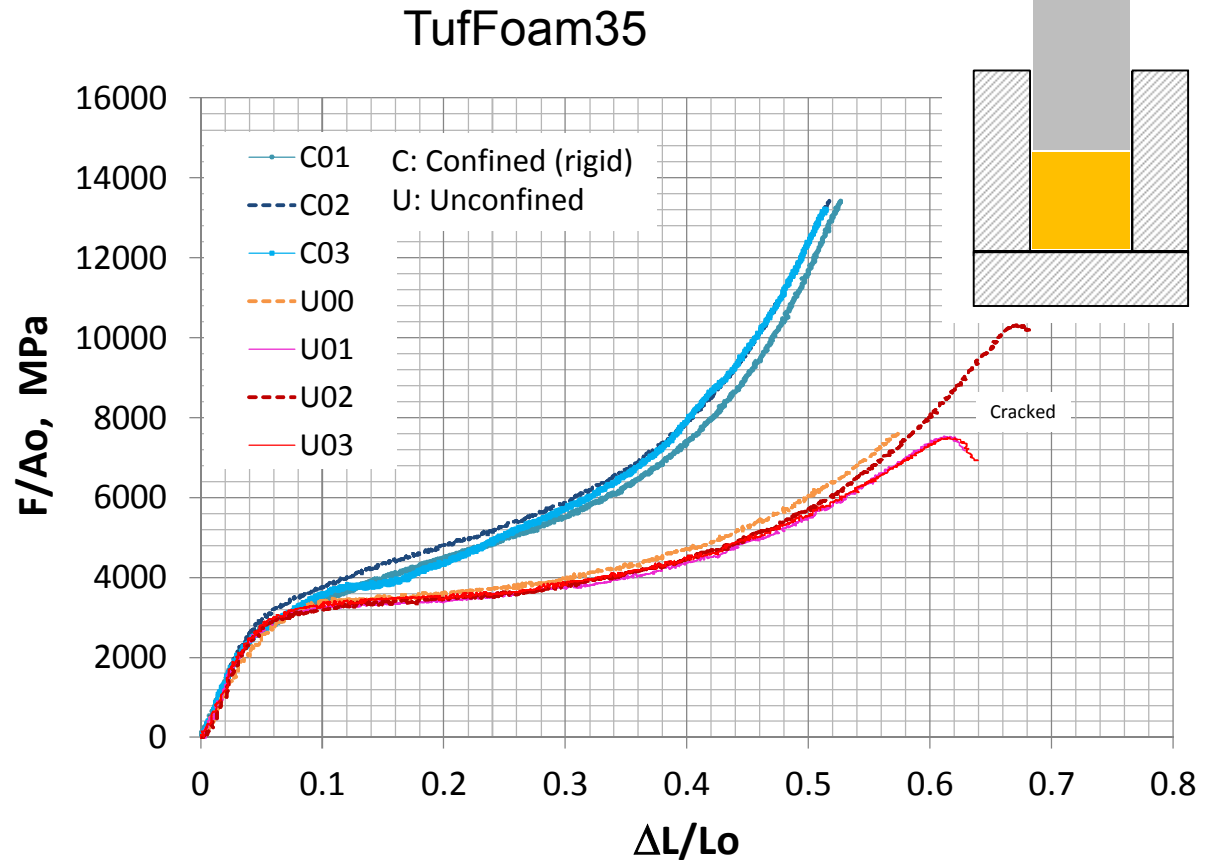
# Specimen Coating



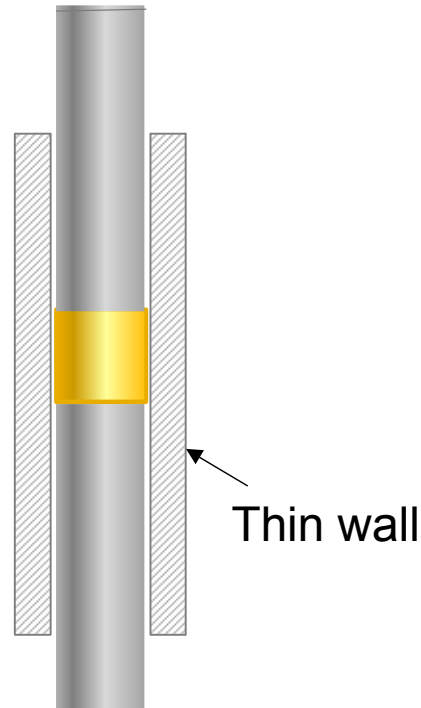
# Triaxial Compression



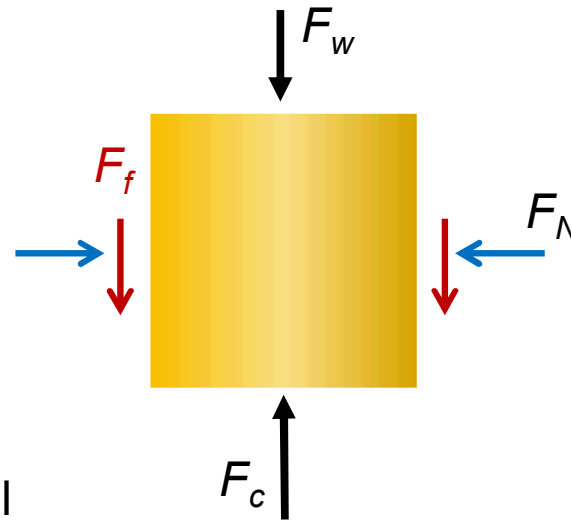
Thick wall for rigid confinement.



# Elastic Confinement

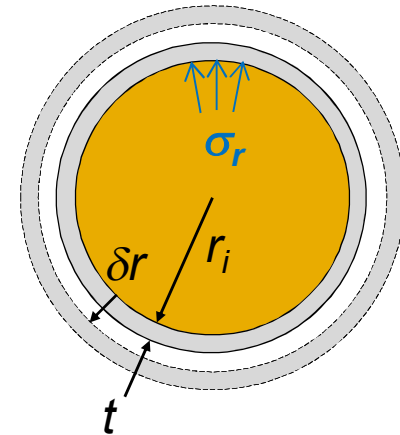


## Foam specimen



$$F_c = F_w + F_f$$
$$\sigma_z = F_w / (\pi r_i^2)$$
$$\sigma_r = F_N / (2\pi r_i h)$$

## 2D Thin tube



$$\delta_r = \frac{\sigma_r r_i^2}{tE} \left( 1 + \frac{t}{2r_i} \right)$$

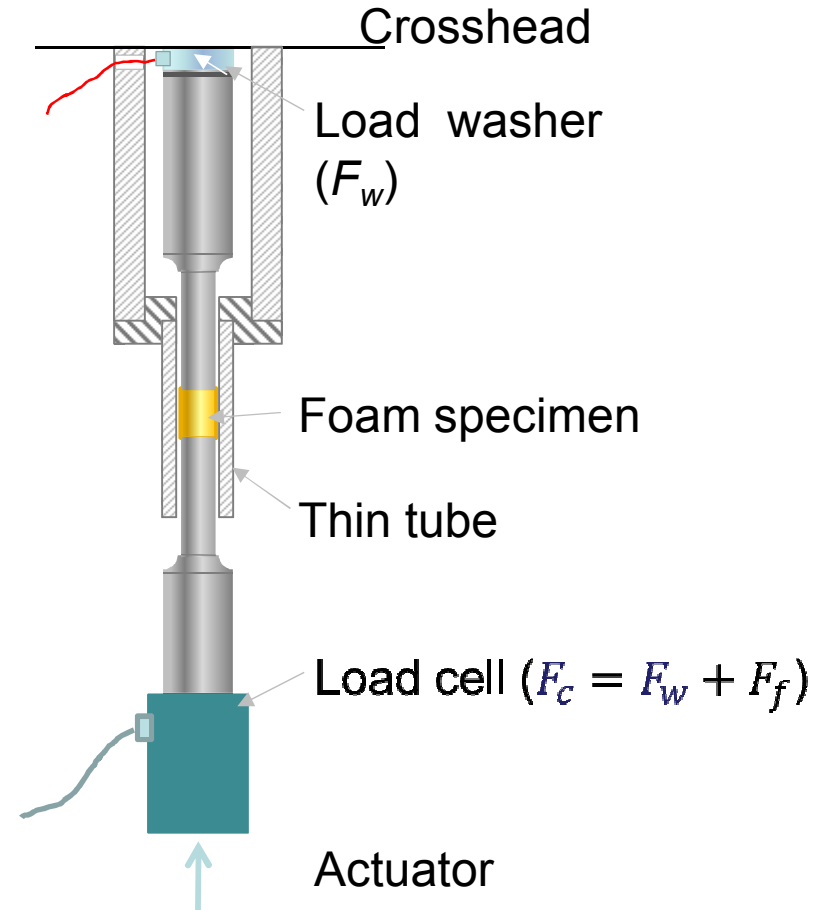
*(if  $\sigma_r$  is uniform)*

# New Confined Compression of Foams

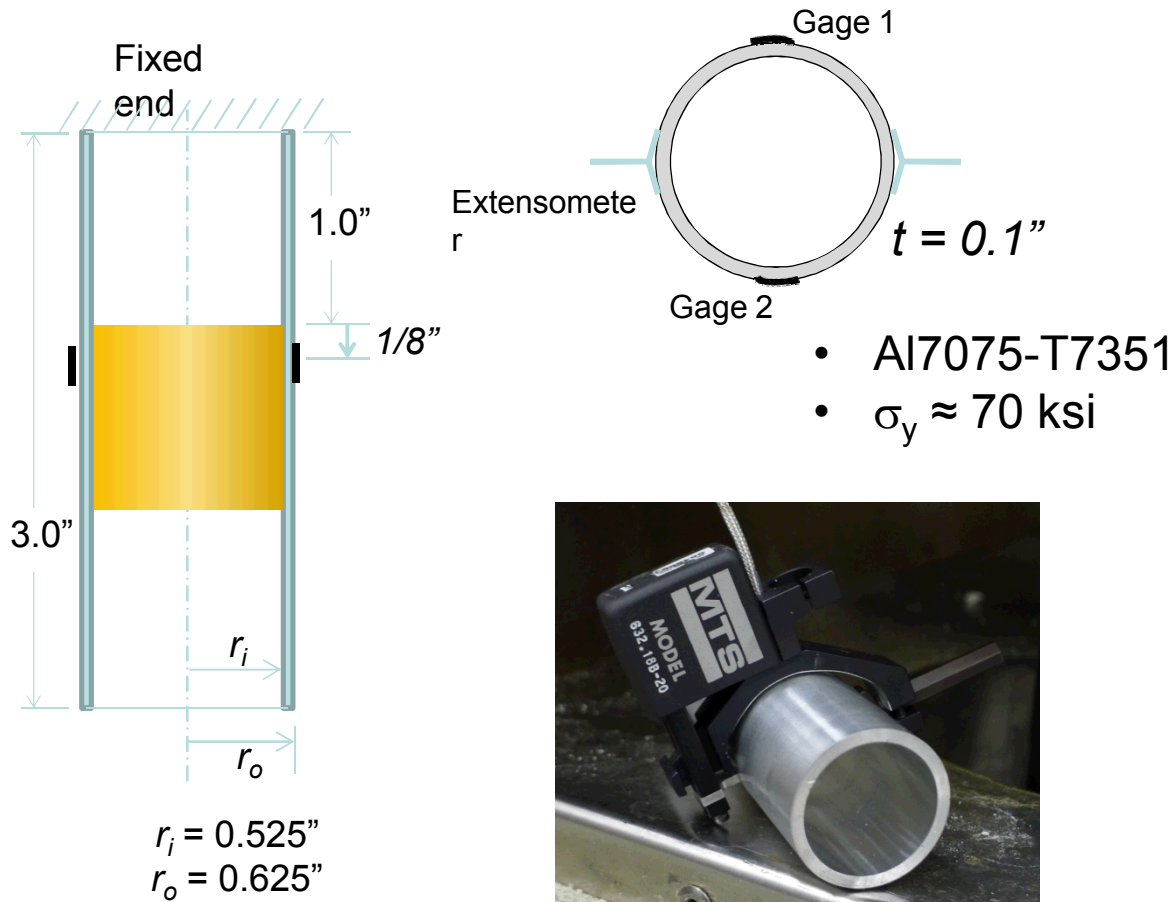
## Setup



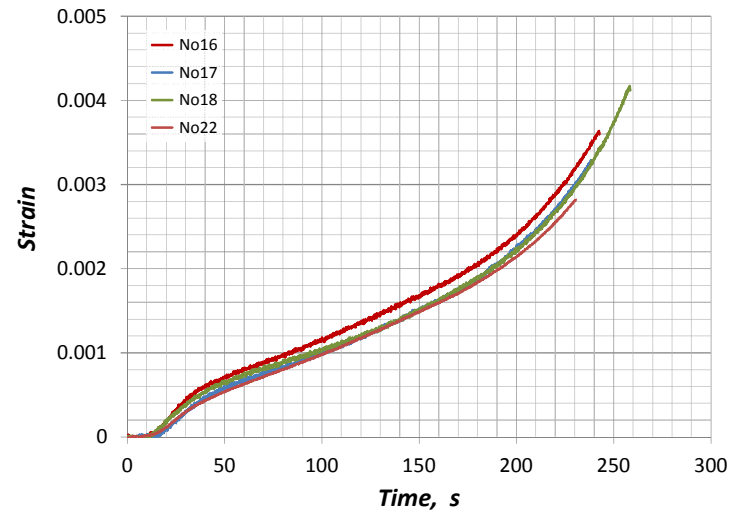
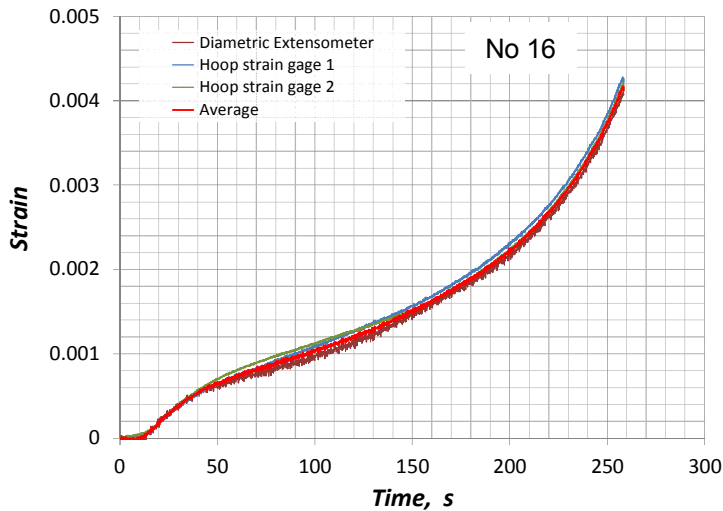
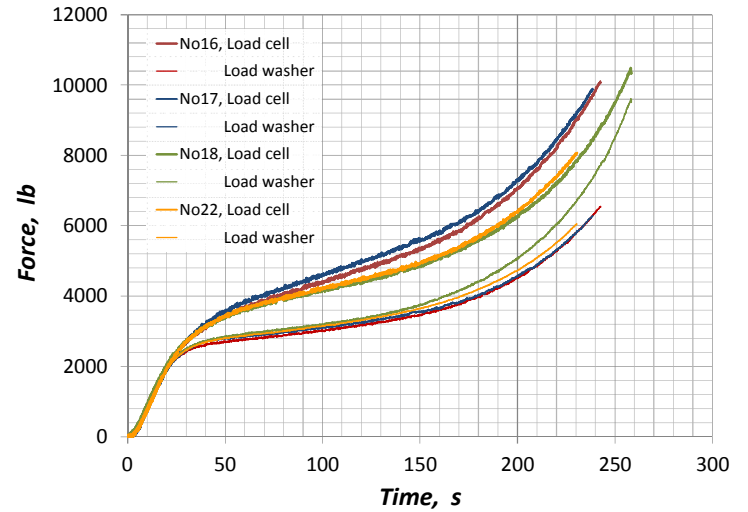
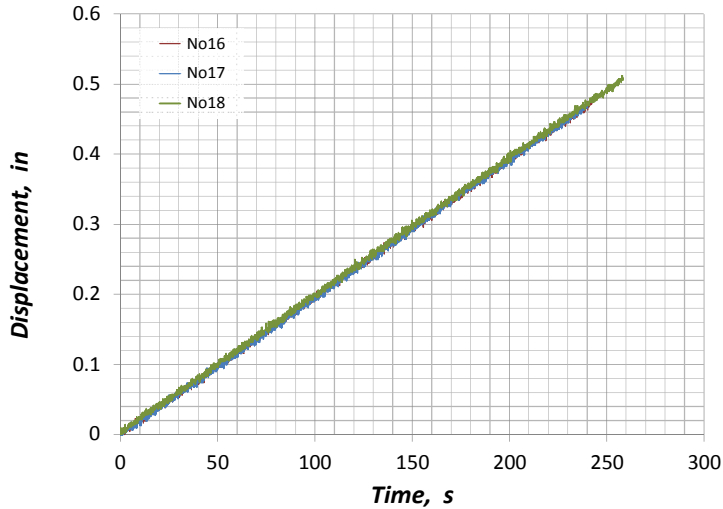
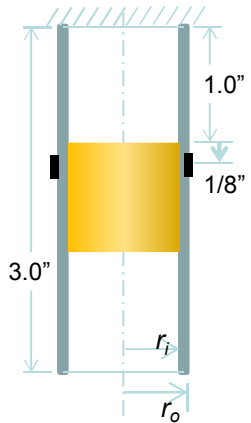
## Schematics



# Thin Tube 1



# TufFoam 35

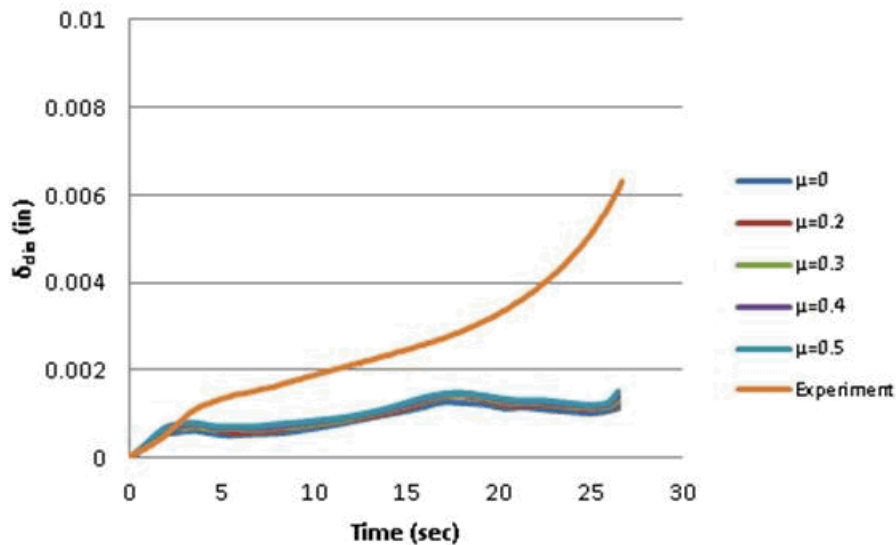


# Model Parameters

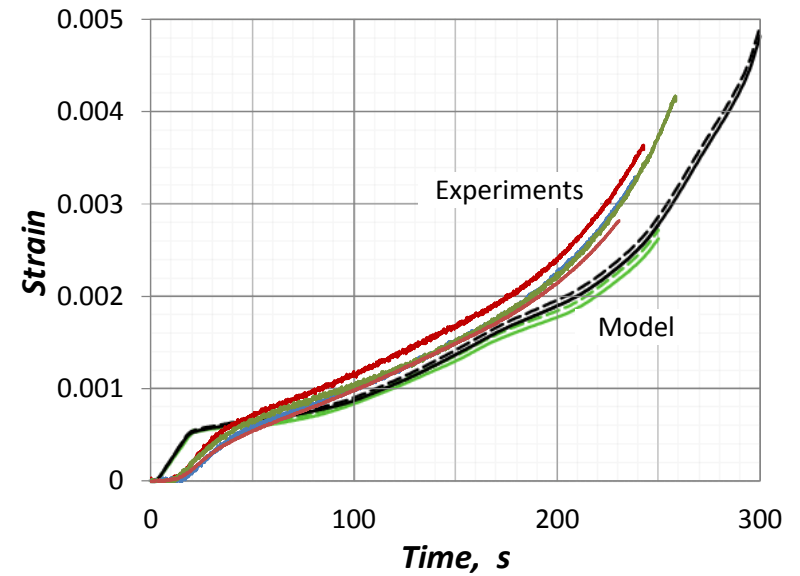
Flow direction

$$\mathbf{g} = (1 - \beta) \mathbf{g}_{associated} + \beta \mathbf{g}_{radial}$$

Initial prediction with  $\beta = 0.9$

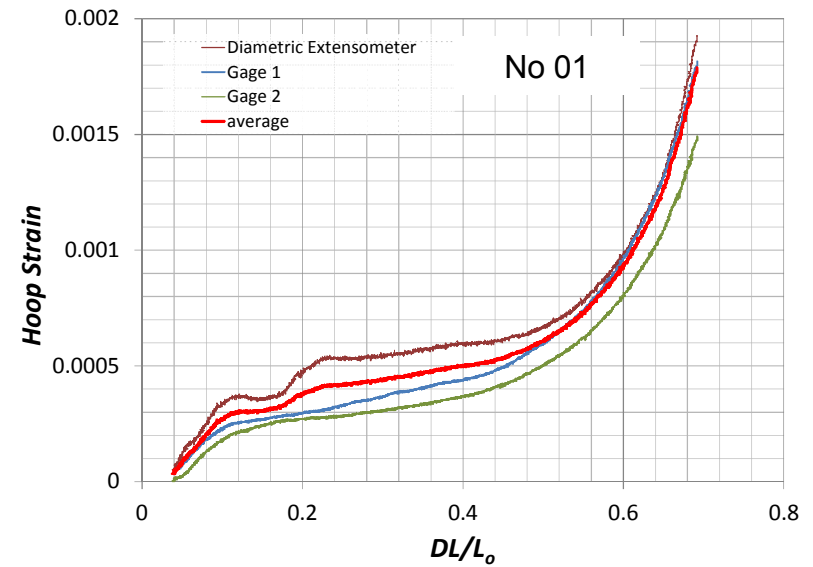
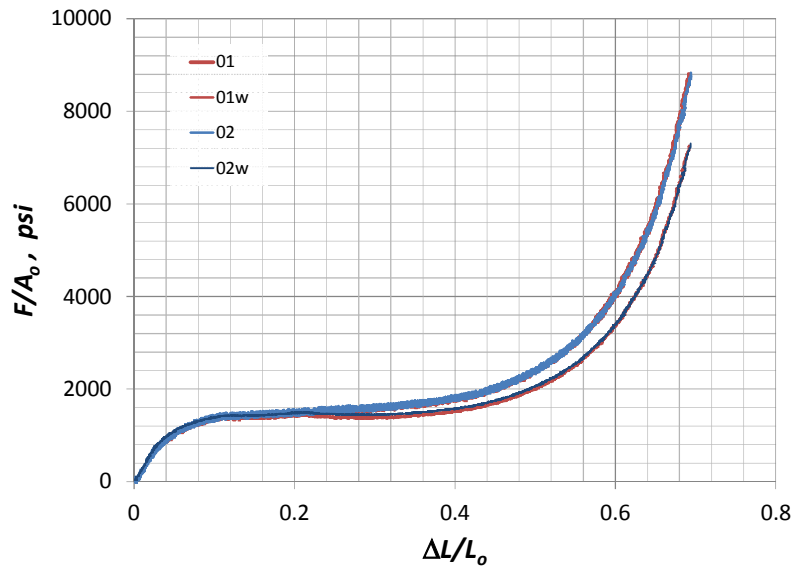


Simulation with  $\beta = 0$

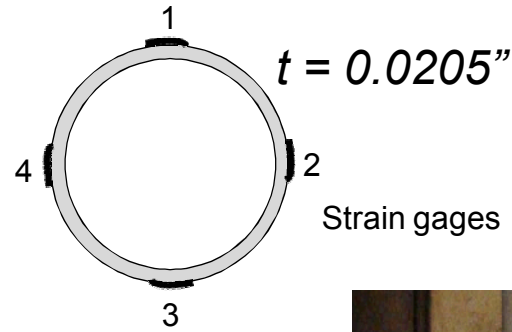
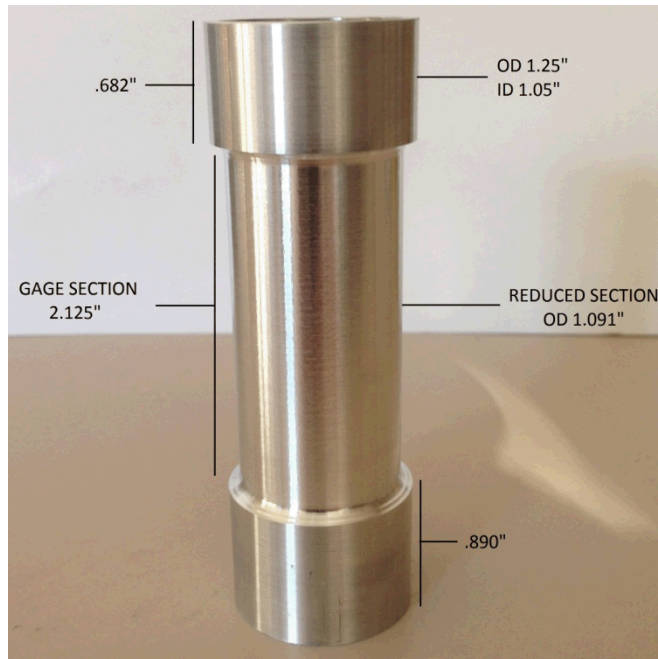


# PMDI20

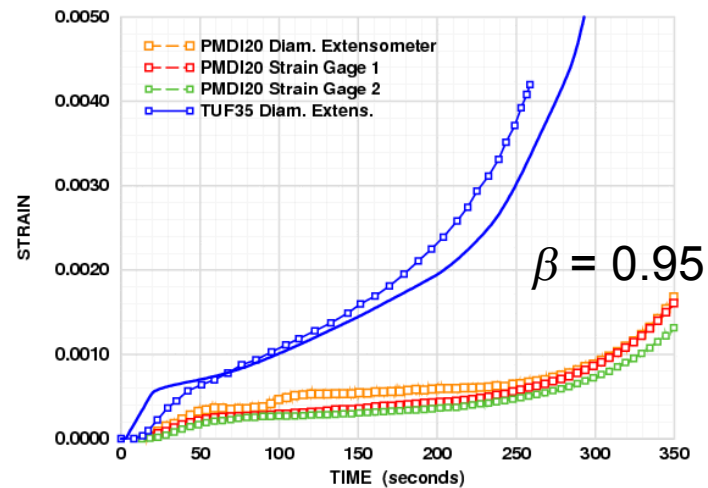
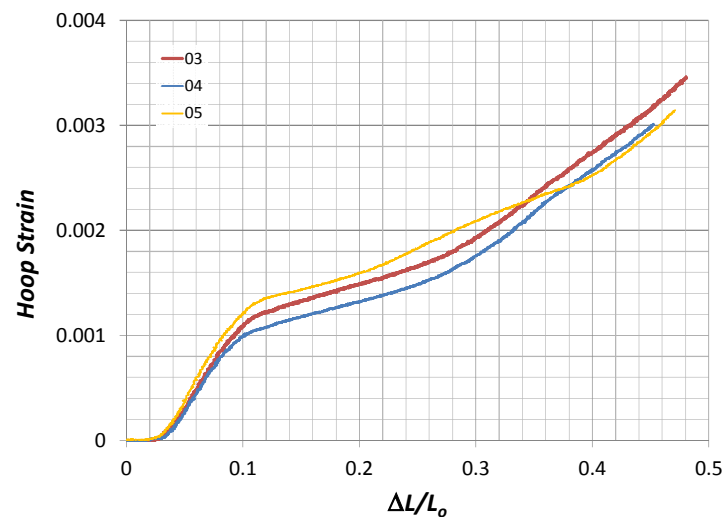
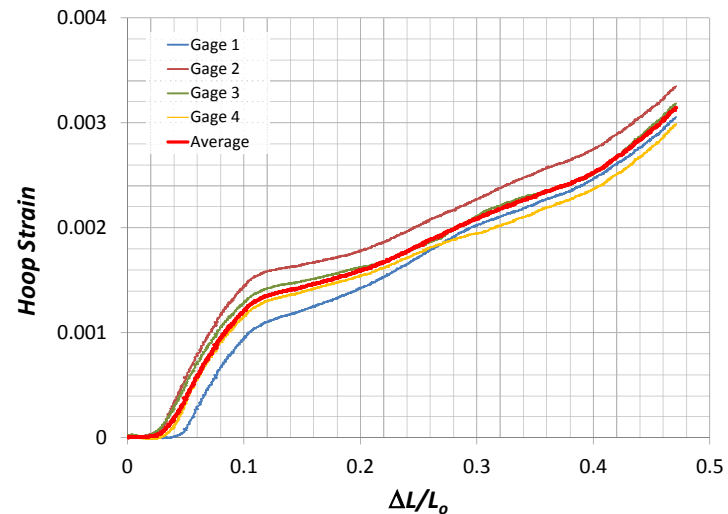
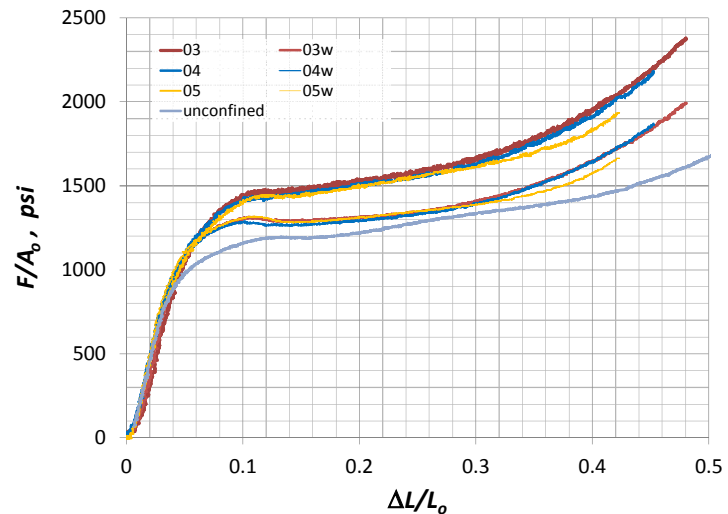
- Constant loading speed is about 0.002 in/s.
- Large scatter in hoop strain for lower density foams.



# Thin Tube 2



# PMDI20



# Summary

- Elastically confined compression provides critical data for calibrating foam model parameters.
- The data show the flow direction depends on the foam density: associate flow for high density foams (35 pcf) and non-associate flow for lower density foams (20 pcf).
- Confined compressions at different temperatures and loading rates are under investigation.