



SAND2011-7230C

Modeling the Spread of Public Opinion on Smart Grid technology and Electric Vehicles through Online Social Networks

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Presentation Outline:

1. Objective
2. Motivation
3. Network Structure
4. Opinion Propagation
 - a. “Nowak” Model
 - b. Multivariate Linear Model
 - Standard Simulation
 - Strongly Opinionated Individuals
 - Current Work – Group Conformity
5. Future Work





Project Objective

- 1. Develop a mathematical model which predicts how opinions regarding smart grid technology and consumers' willingness to purchase electric vehicles are spread through an online social network**
- 2. Use this model to optimize smart grid public education approaches**

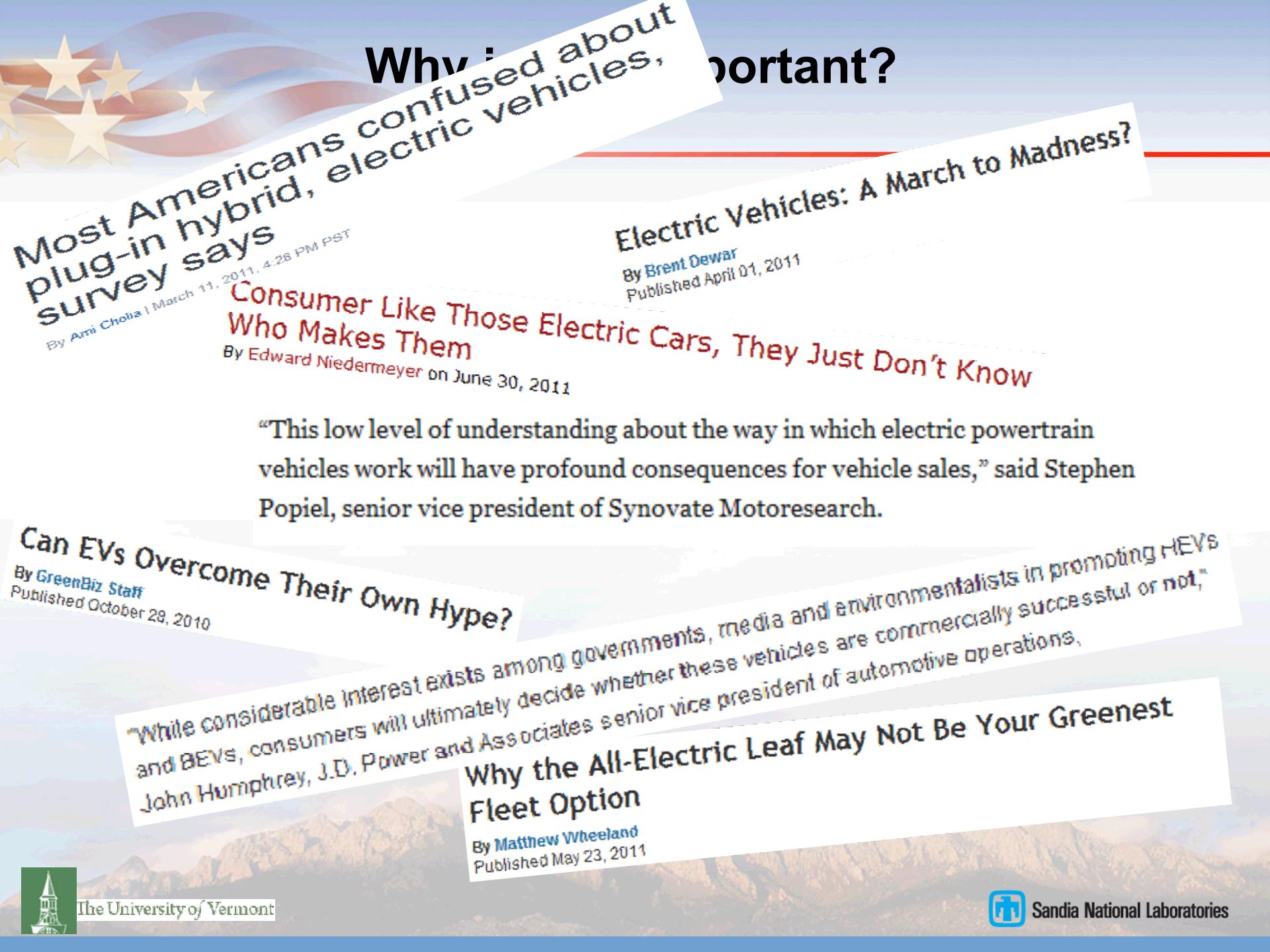




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In order for the implementation of smart grid technology to be successful,

Consumer support is essential – There are many questions

Are the batteries in electric cars reliable?
How does the cold affect the batteries?

Is my privacy compromised by any of the smart grid technology?

What are the economical savings?

Are there health risks associated with this technology?

What is the charge time for Plug in Hybrid Electric Vehicles?

What are the differences between on peak and off peak hours? How does this affect carbon emissions?



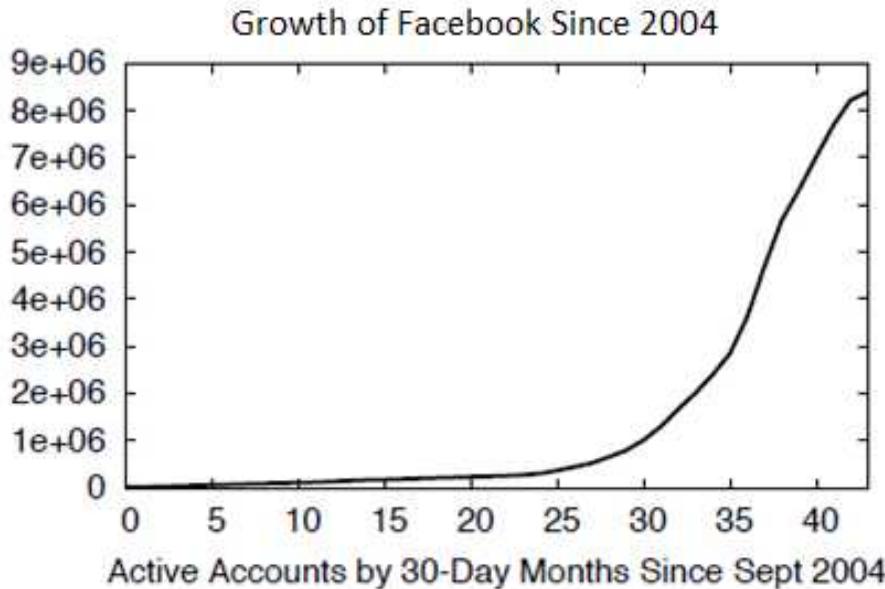
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Why Online Networks?

Network Size



- People spend over 700 billion minutes per month on Facebook

Facebook.com



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Currently:

- More than 750 million active users
- 41.6% of the US population has a Facebook account
- 50% of Facebook users go on daily
- 20% of the US population goes on Facebook daily

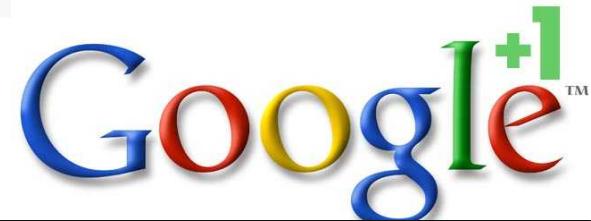


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Online Social Networks:

Have added new aspects to the way people communicate

- Information spreads more quickly
- Users are influenced by:
 - A greater quantity of people
 - People located at large geographical distances away from them
 - People who they do not have strong relationships with



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Online Social Network Analysis

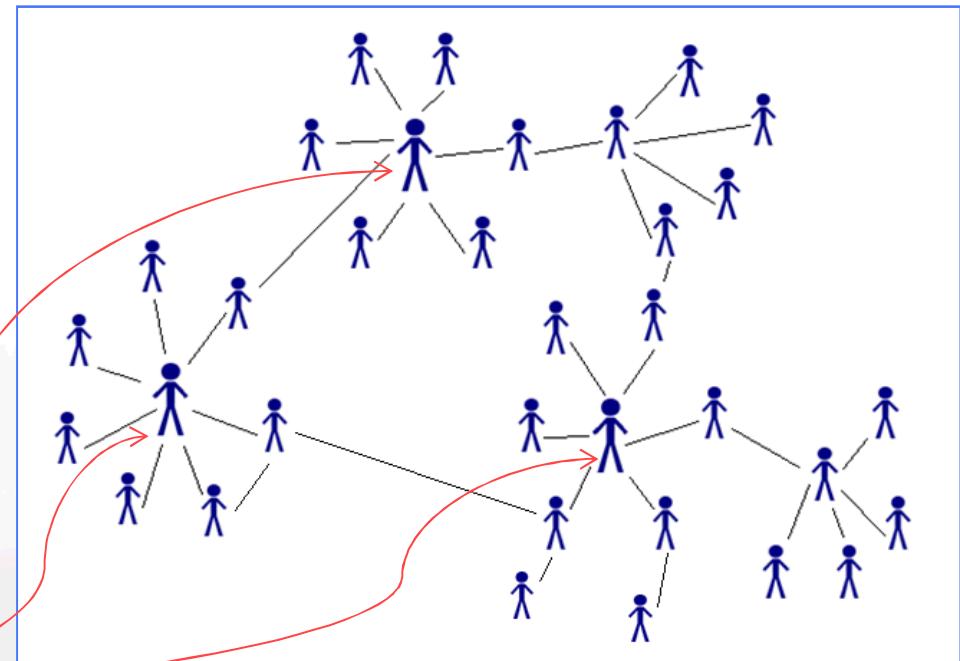
Display *scale free* and *small world* properties

Scale Free Network Characteristics:

- Degree distribution follows a power law

Degree: The number of connections a node has

- Existence of “hubs”



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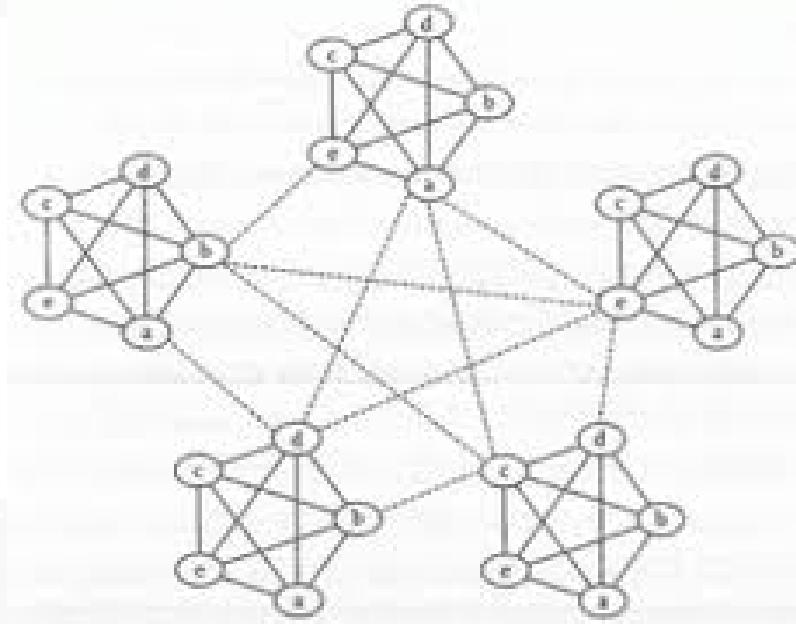


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Online Social Network Analysis

Small World Network Characteristics:

- High clustering coefficients
- Short characteristic path lengths



$$\text{Clustering Coefficient} = C = \sum_{i \in N} \frac{T_i}{0.5 * k_i(k_i - 1)}$$

T_i = Number of triangles with vertex i

k_i = degree of i



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Scale Free Network Creation

Barabási–Albert (BA) model

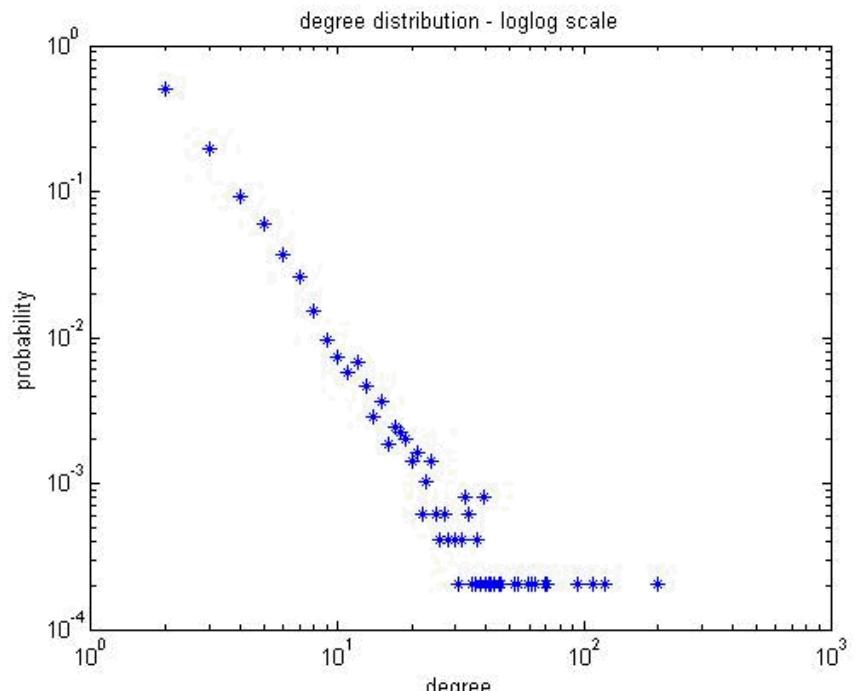
- Start with a small number of nodes
- Every time step add a new node which makes connections a certain number of existing nodes
- The probability of a new node connecting to an existing node i depends on i 's degree (Preferential Attachment)

$$P(i) = \frac{k_i}{\sum_j k_j}$$

$$P(k) \sim k^\alpha$$

$k = \text{degree}$

$-3 \leq \alpha \leq -2$



$$P(k) = k^{-2.451}$$

$$N = 4900$$



Small World Aspect Addition: Large Clustering Coefficient

Relative Preferential Attachment Model

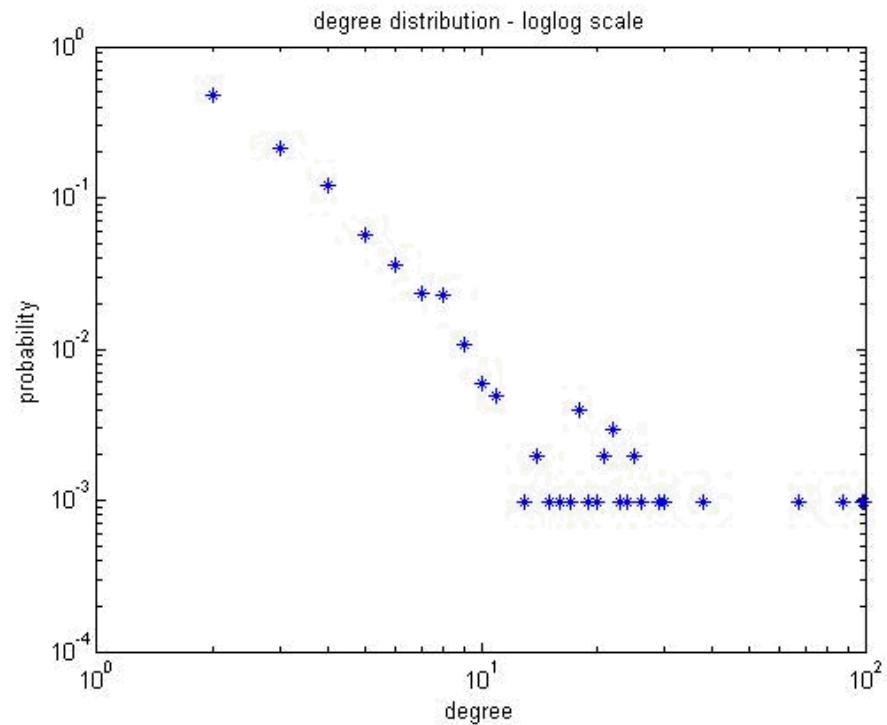
- Adds an adjustable clustering coefficient to the BA model

$$P(i) = \frac{k_i}{\sum_j k_j}$$

$$P(i) = (1 - \vartheta) \frac{k_i}{\sum_j k_j} + \vartheta \frac{h_i}{\sum_v h_v}$$

$$(0 \leq \vartheta \leq 1)$$

ϑ : Controls the amount of clustering



$$P(k) = k^{-2.343}$$

$$N = 1024$$

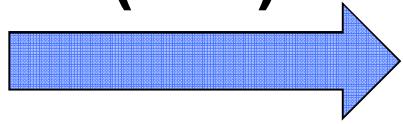
$$c_{avg} = 0.3962$$

$$\vartheta = 0.7$$

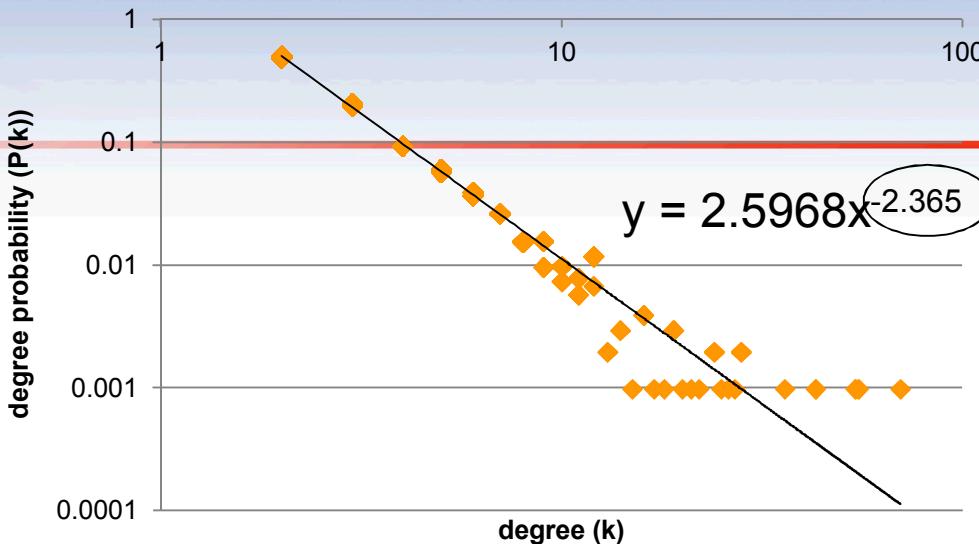




No Clustering
($\delta=0$)

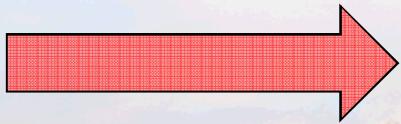


Degree Distribution-1024 Nodes

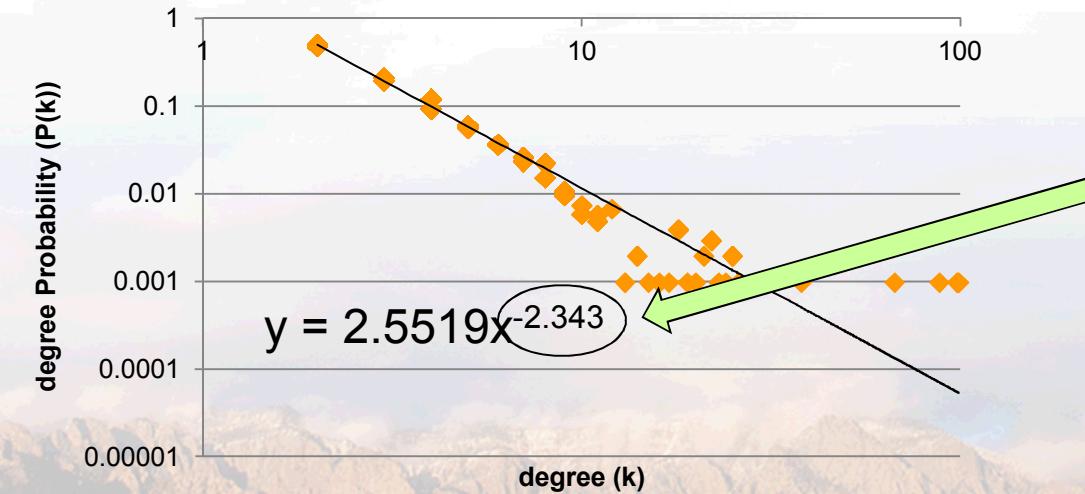


Power law is
conserved

Clustering
($\delta=0.7$)



Degree Distribution- 1024 Nodes

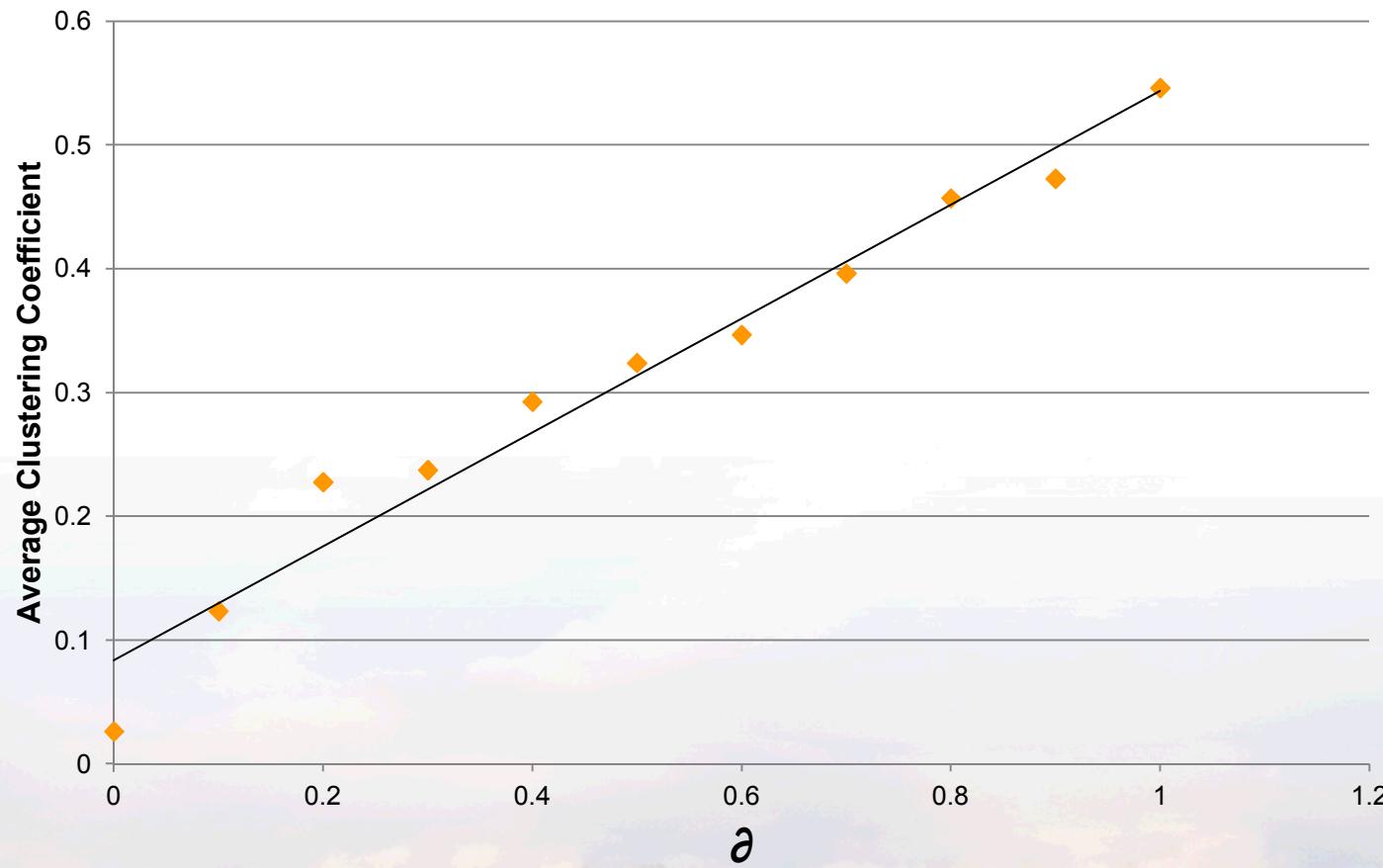


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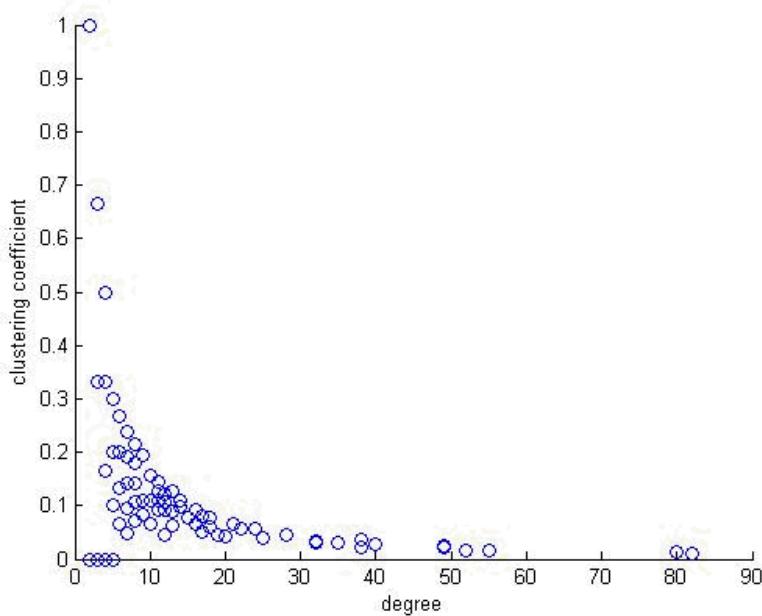


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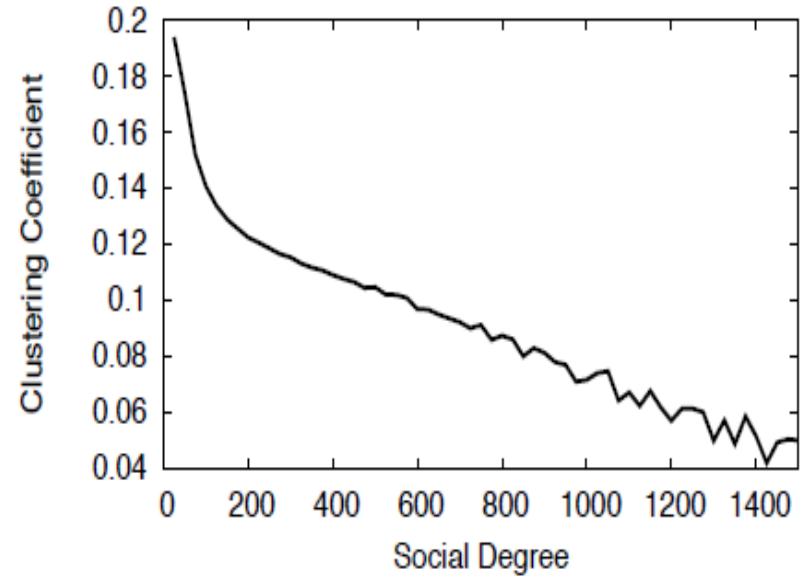
1024 Nodes- Clustering Vs. ∂



Degree Vs. Clustering Coefficient ($\partial=0.5$)



Real Facebook Data Degree Vs. Clustering Coefficient



Wilson



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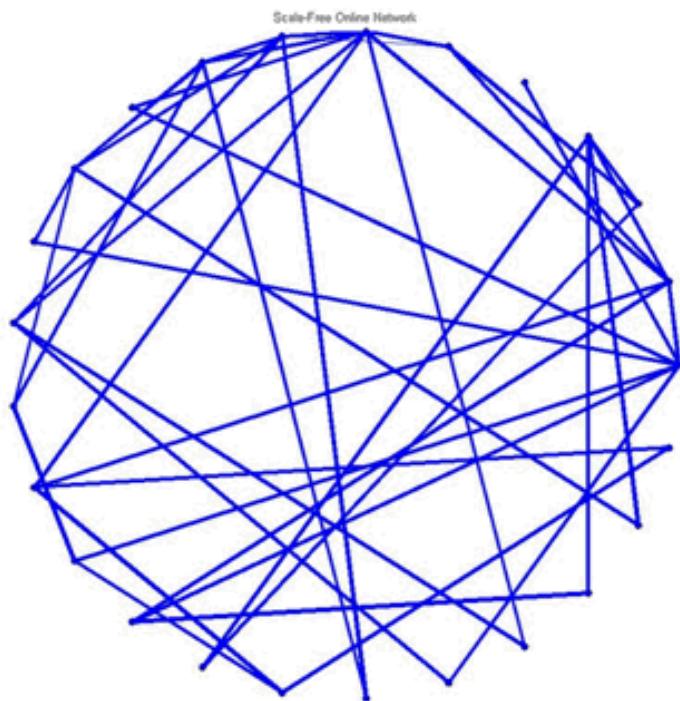


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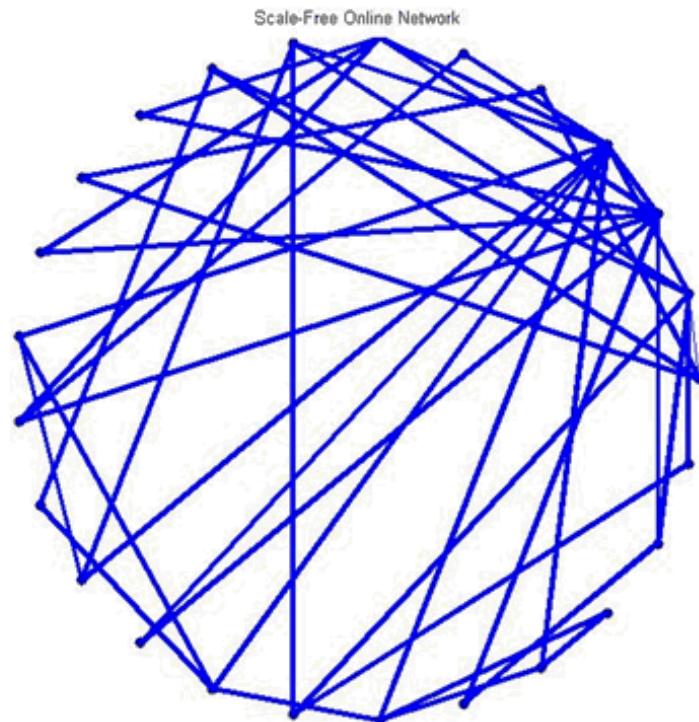


25 Node Network

$\partial=0.1$



$\partial=0.9$



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Opinion Propagation – Original Considerations (“Nowak” Model)

- Network: XY Cartesian (not Scale Free)
- Social Impact Model
- Predicts change of attitudes in a population resulting from social impact

$$i_s = N_s^{\frac{1}{2}} \left[\sum \frac{\frac{s_i}{d_i^2}}{N_s} \right]$$

d_i = distance between the agent i and the neighbor

N_o = number of neighbors with different opinion than agent i

$$i_p = N_o^{\frac{1}{2}} \left[\sum \frac{\frac{p_i}{d_i^2}}{N_o} \right]$$

N_s = number of neighbors with the same opinion as agent i

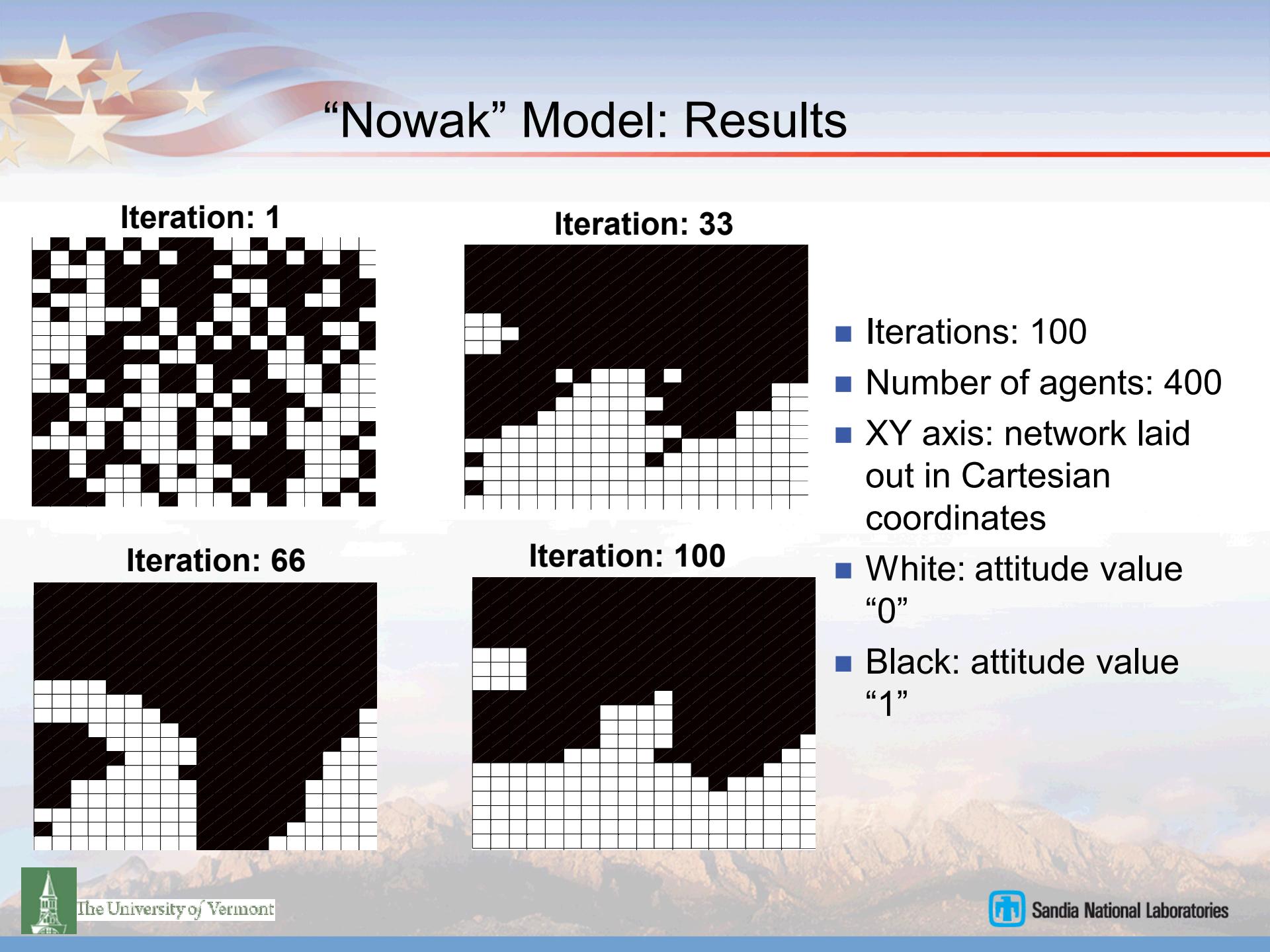
Original algorithm from Nowak, 1990



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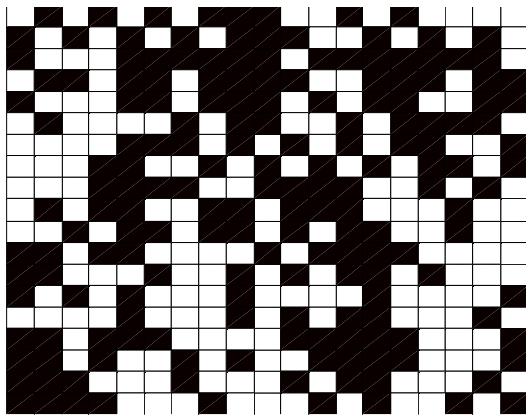


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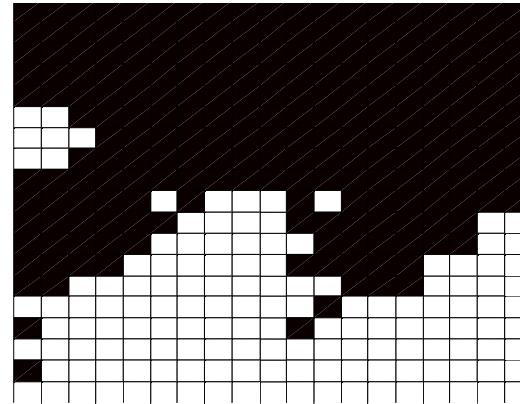


“Nowak” Model: Results

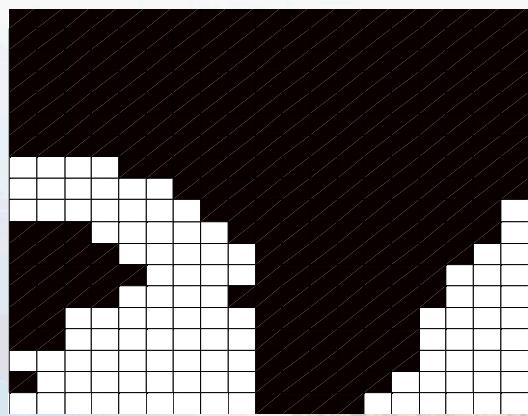
Iteration: 1



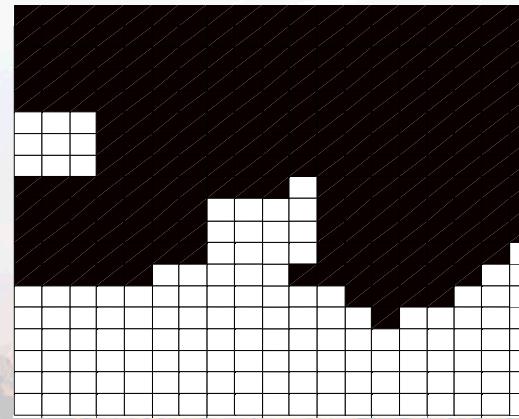
Iteration: 33



Iteration: 66



Iteration: 100



- Iterations: 100
- Number of agents: 400
- XY axis: network laid out in Cartesian coordinates
- White: attitude value “0”
- Black: attitude value “1”





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Multivariate Linear Model

- **Assumption:** opinions are likely to be influenced by the attitudes and beliefs of peers
 - Uses a weighted average

Opinion Update

$$O_{ik,t+1} = O_{ik,t} + \frac{1}{2(N-1)} \sum_{i \neq j} W_{ij} (O_{jk,t} - O_{ik,t})$$

Weight Update

$$W_{ij,t+1} = 1 - \frac{|1 - M_{ij}| + |O_{jk,t} - O_{ik,t}|}{2}$$

Parameters:

$k = k^{\text{th}}$ attitude or issue

$O_{ik,t}$ = agent i's opinion on k at time t

W_{ij} = social distance between i and j

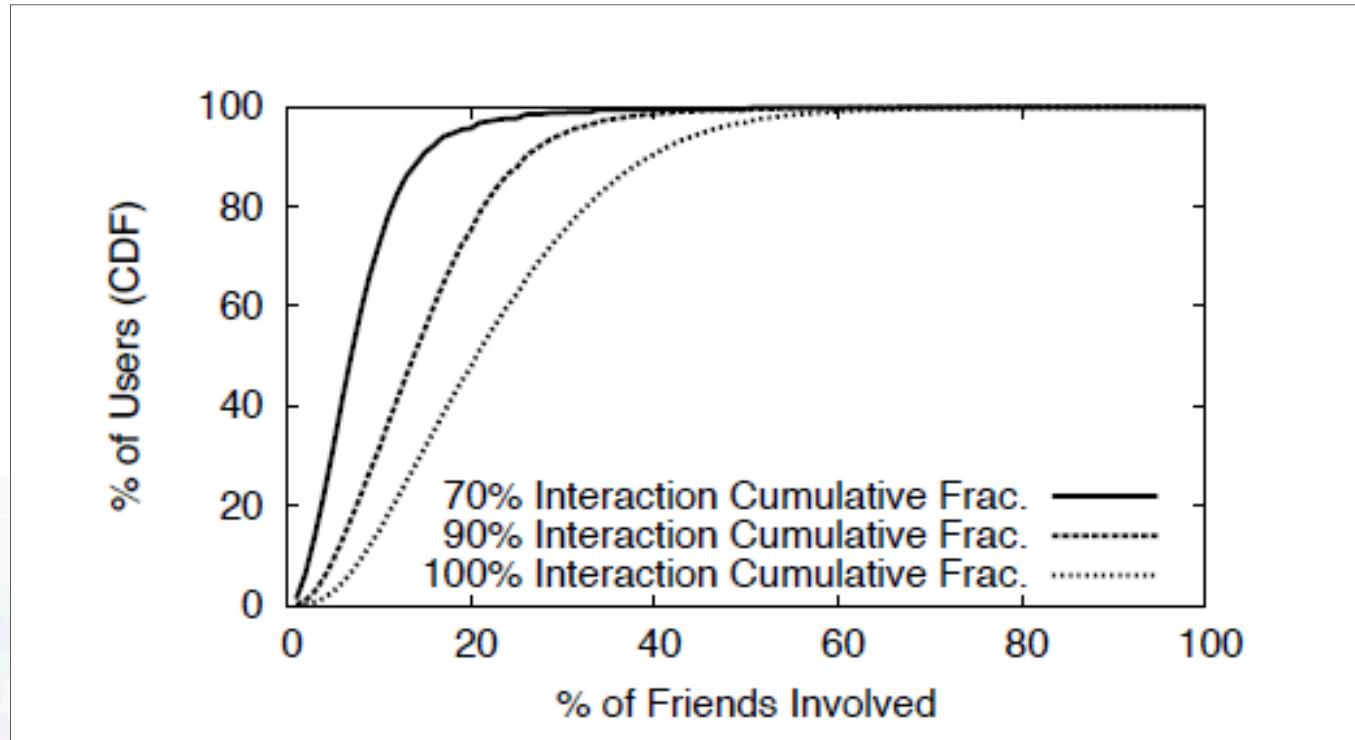
M_{ij} = mutual friend weight



Multivariate Linear Model: Side Note

Facebook - Distribution of Users' Interaction Among Their Friends

- Realistic to actual social networks, with the assumption that a given individual can only interact with a small number of people



Conclusion Drawn: User will only interact with a small subset of social links, so connections must be weighted

Graph taken from Wilson, 2009



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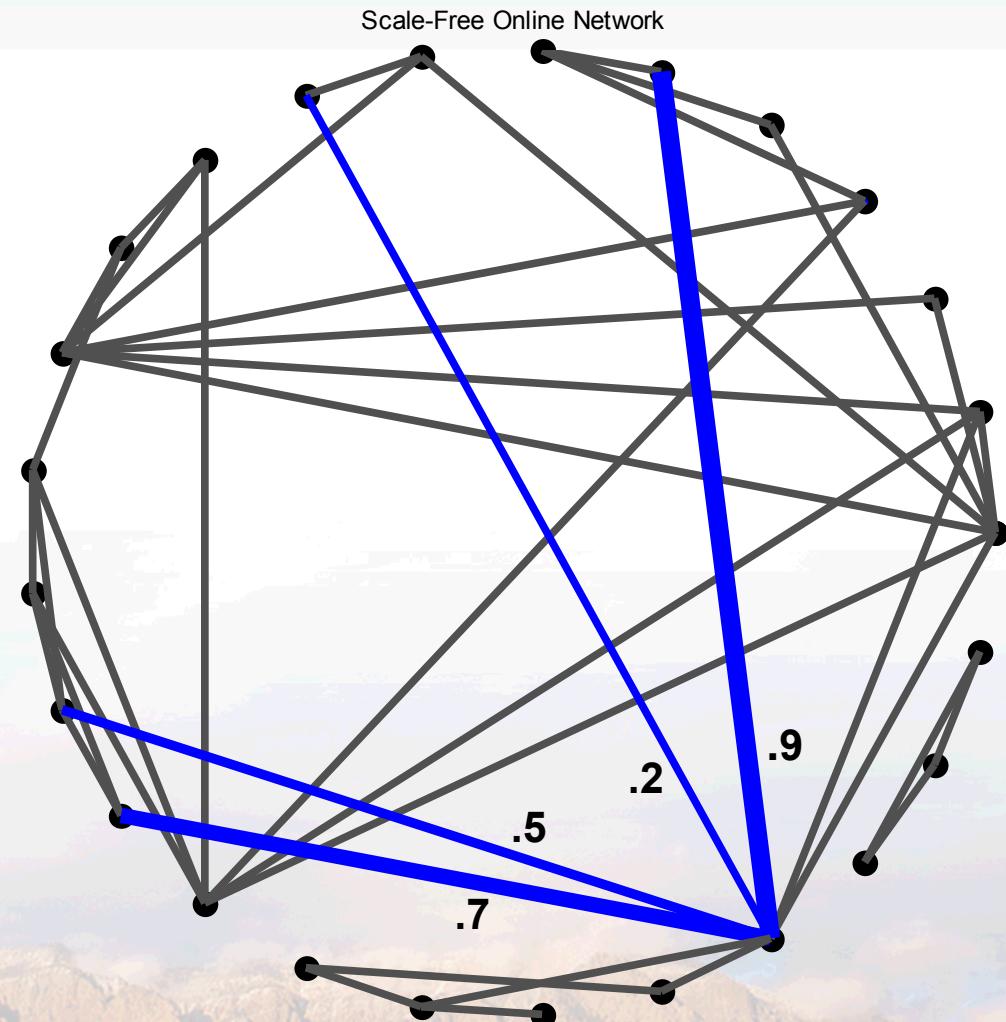
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Multivariate Linear Model: Mutual Friend Weight

- Understanding the weight of each connection is crucial towards understanding how two given nodes might influence each other
- We define weight by the number of mutual friends two people have

$$W_{ij,t+1} = 1 - \frac{|1 - M_{ij}| + |o_{jk,t} - o_{ik,t}|}{2}$$

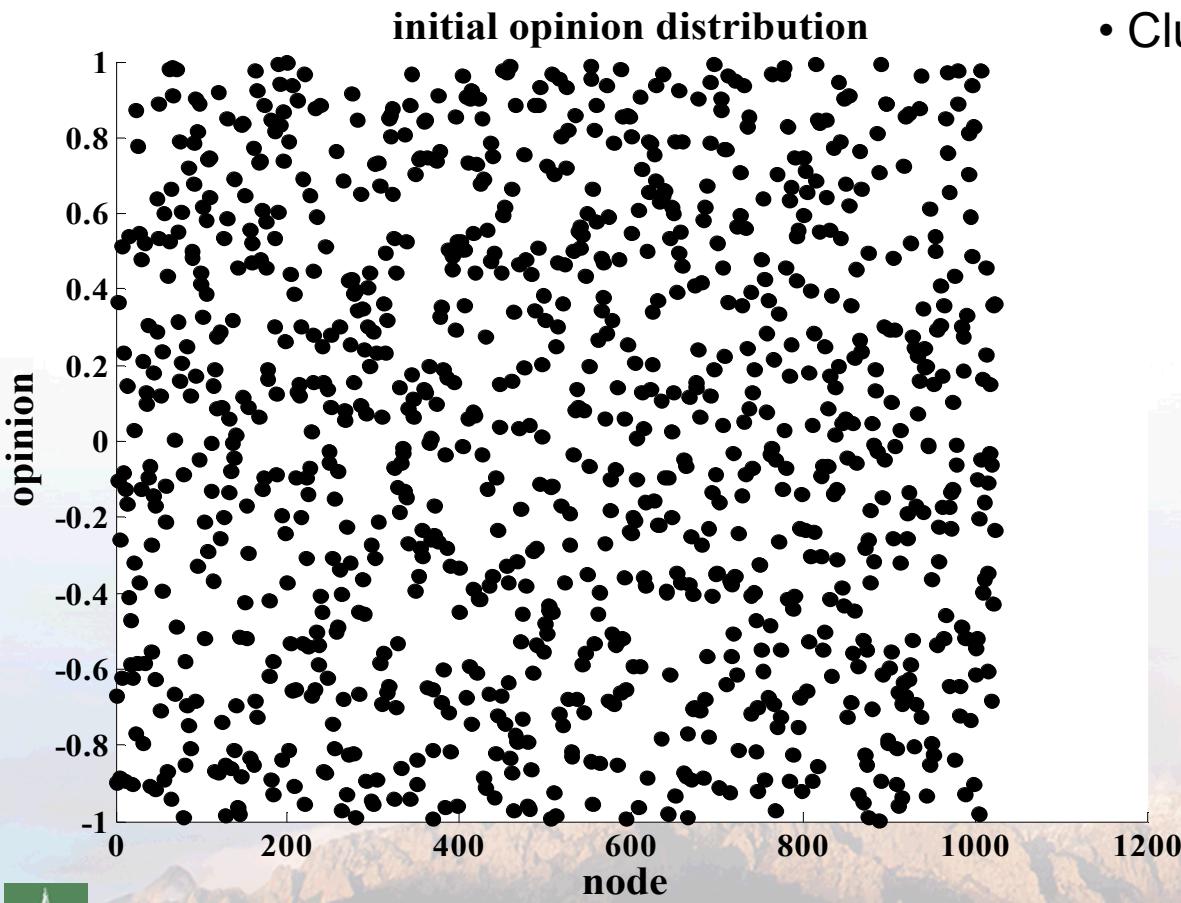




Multivariate Linear Model: Results

Using:

- Scale Free Network – $P(k) \sim k^{-2.02}$
- 1024 Nodes
- Clustering Coefficient = 0.0632



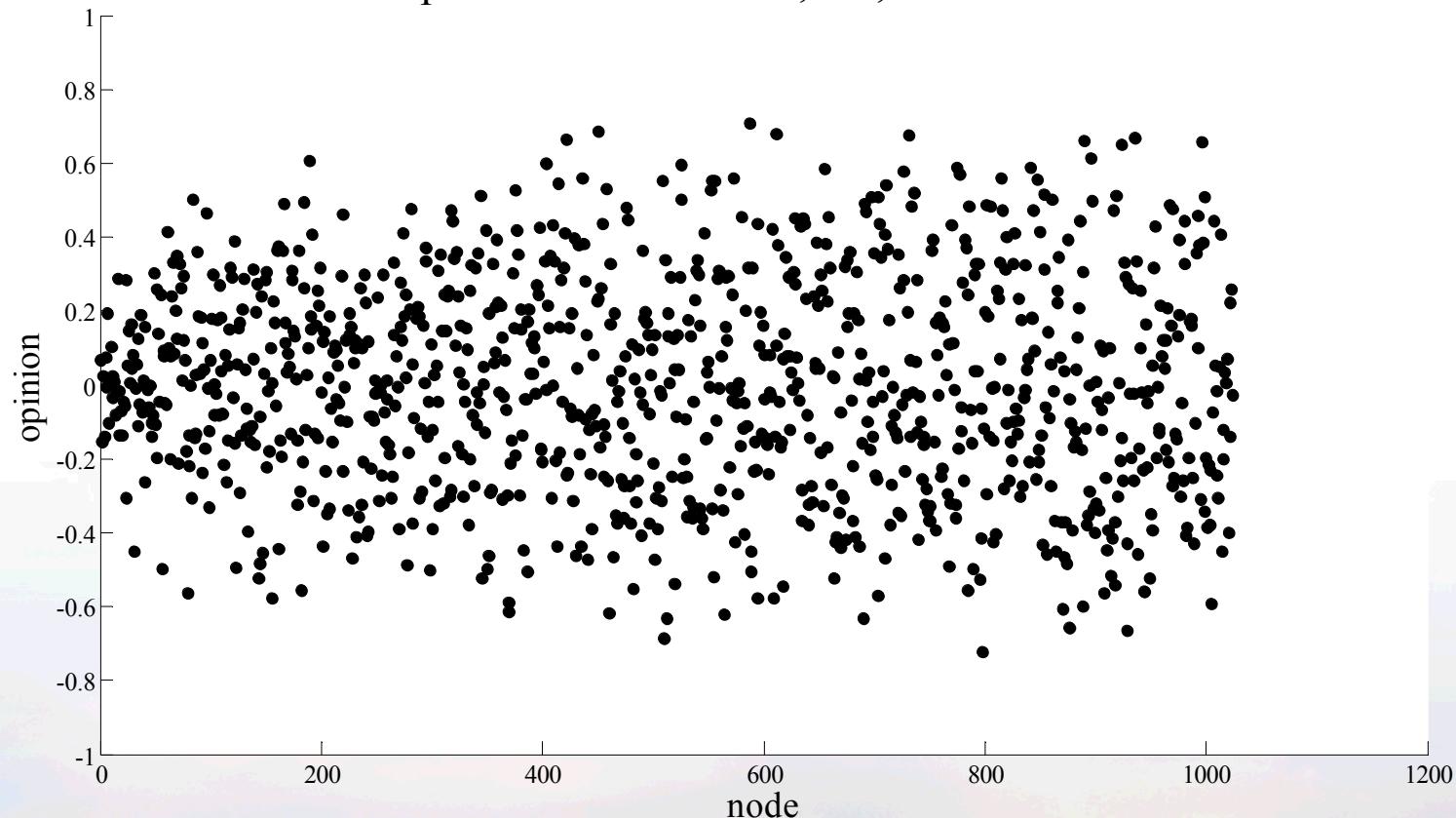
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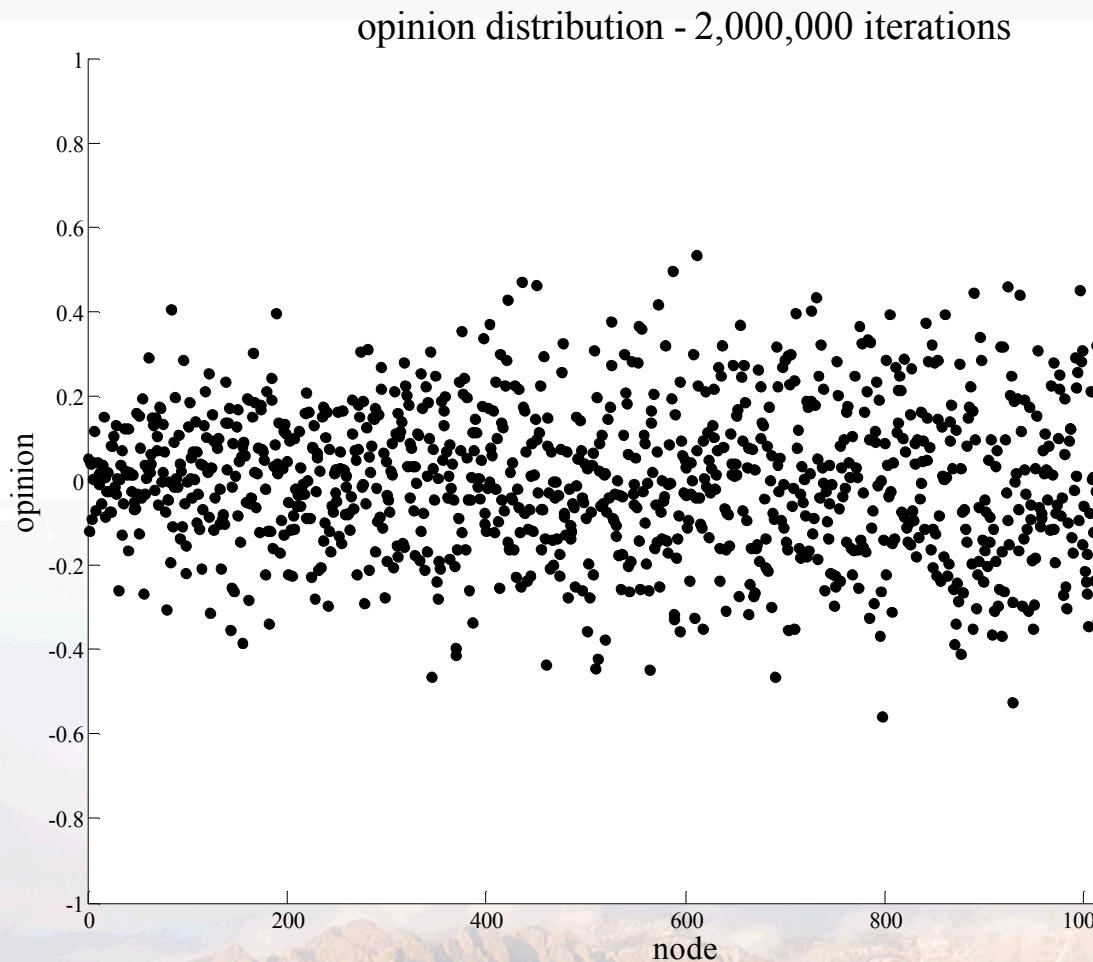
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Multivariate Linear Model: Results

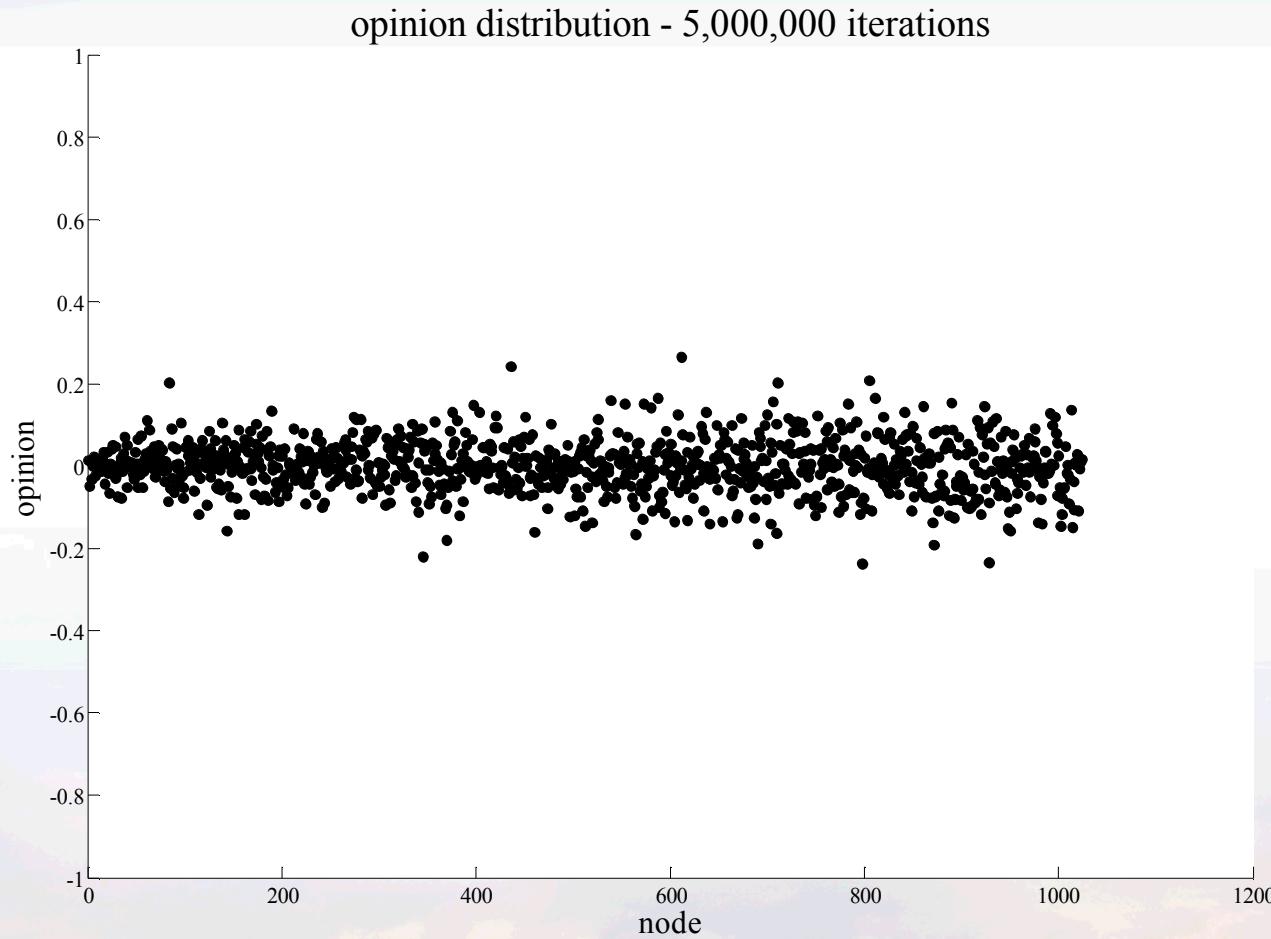
opinion distribution - 1,000,000 iterations



Multivariate Linear Model: Results



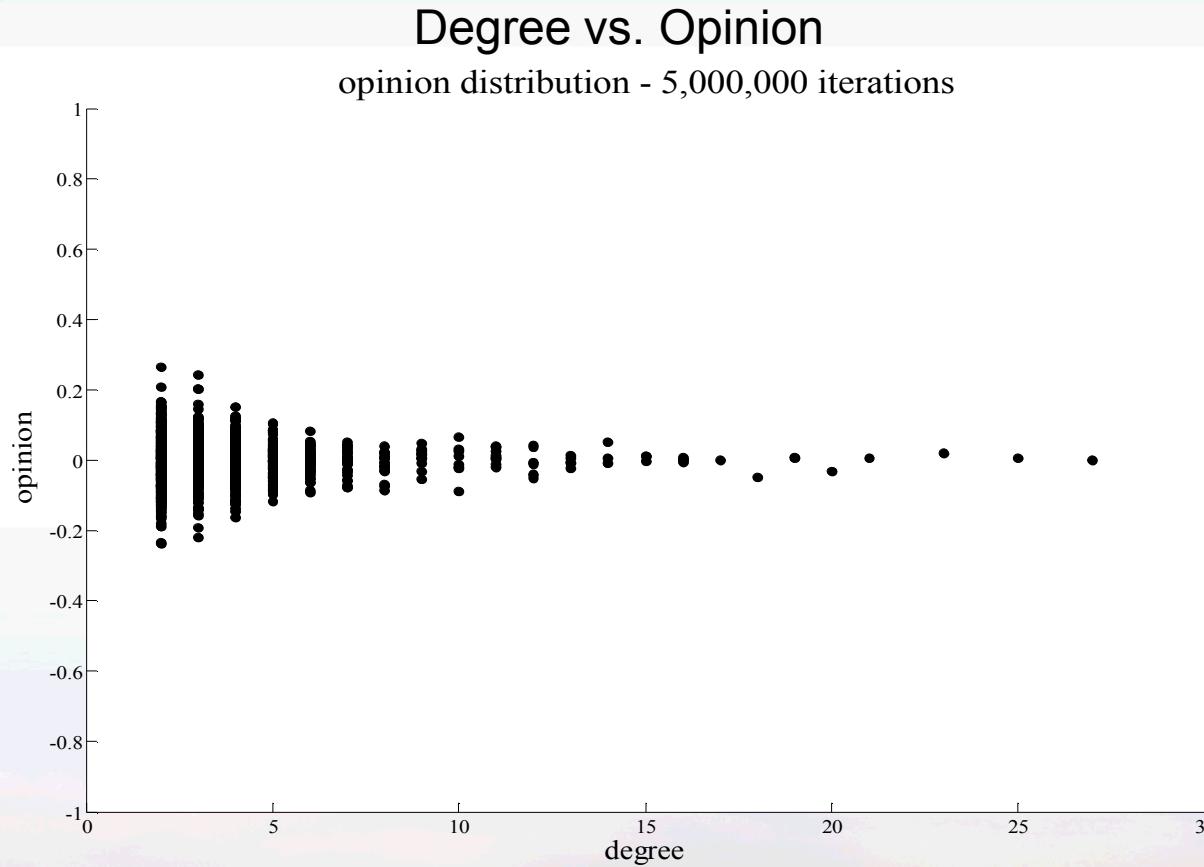
Multivariate Linear Model: Results



Conclusion: Opinion values converge to the mean with the presence of several outliers



Multivariate Linear Model: Why Outliers?



Conclusion: Those high degree nodes tend to agree with the majority in a fewer amount of time steps.





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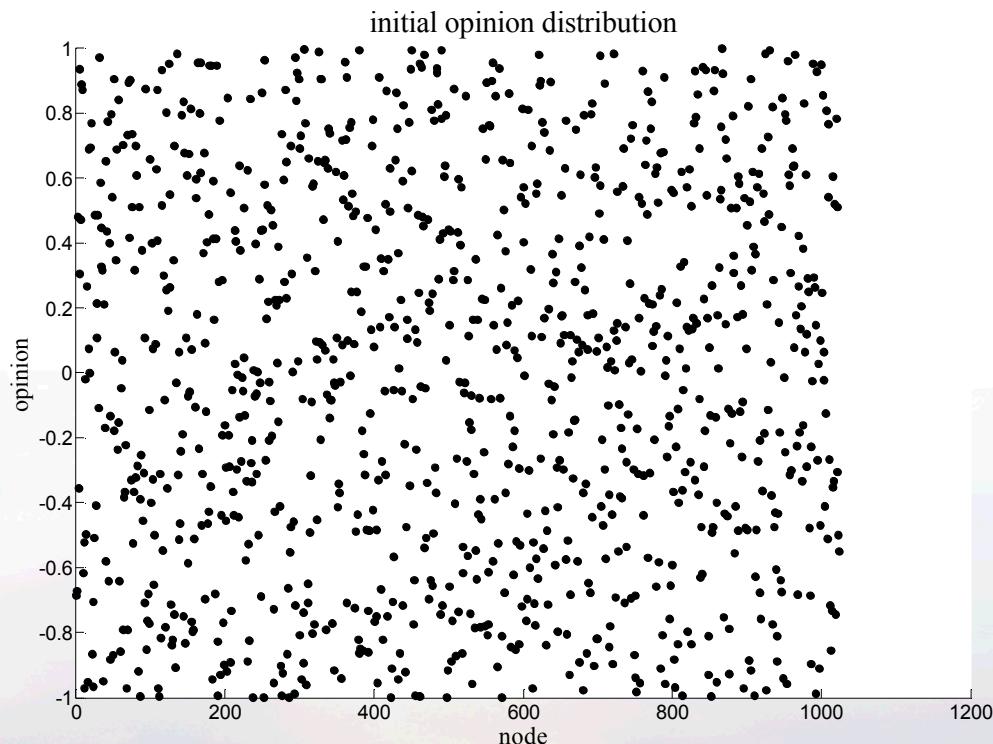


Strongly Opinionated Individuals

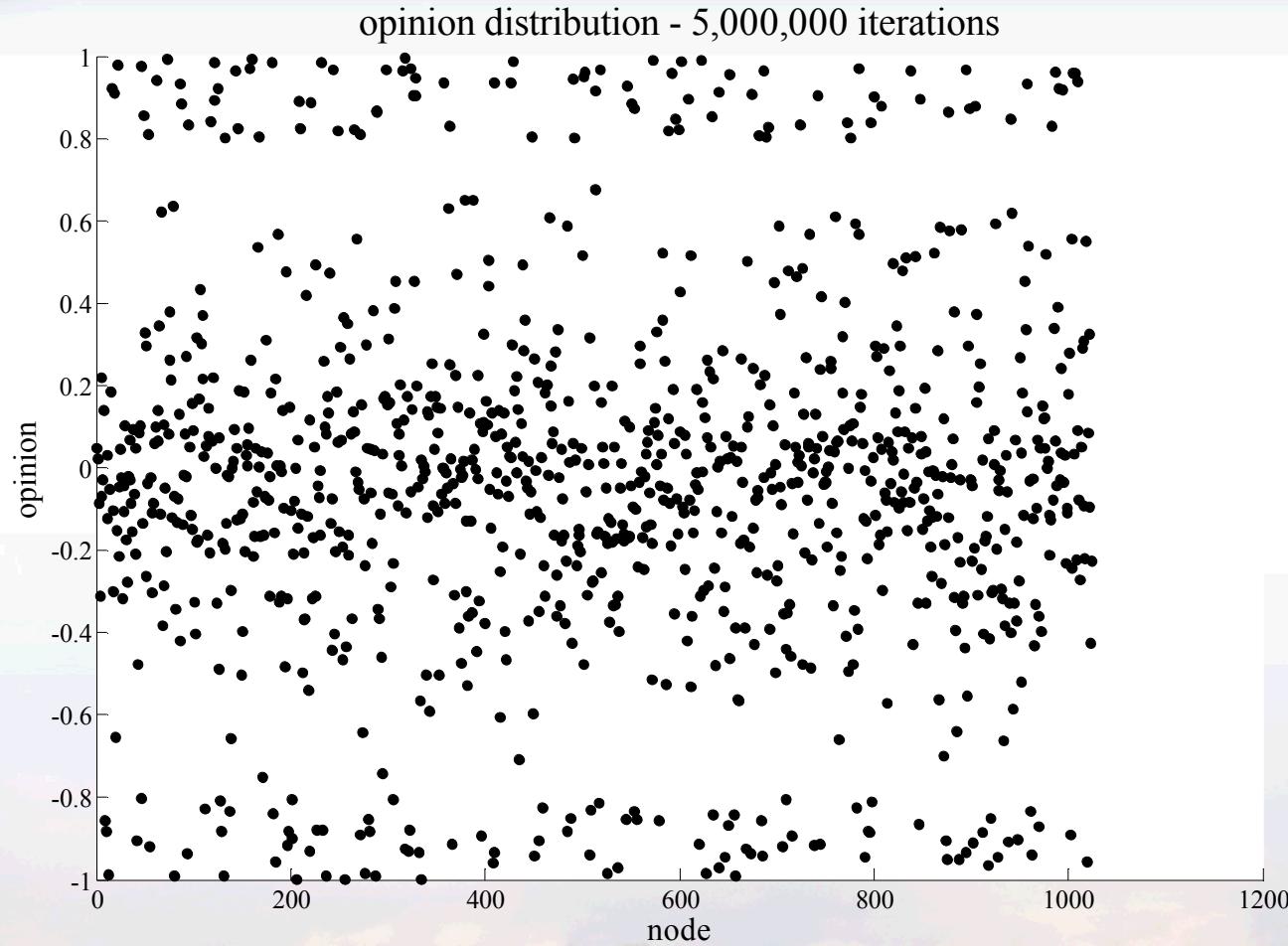
Sociological Question: If a small percentage of the group is strongly opinionated and not influenced by the beliefs of others, how does this affect the group as a whole?

Mathematical Approach:

- Assign some nodes a strong opinion value
- These nodes must maintain that strong opinion value throughout the simulation



Multivariate Linear Model: Implementation



**The effect of several strong opinions on a group as a whole:
It takes longer for a group to agree**



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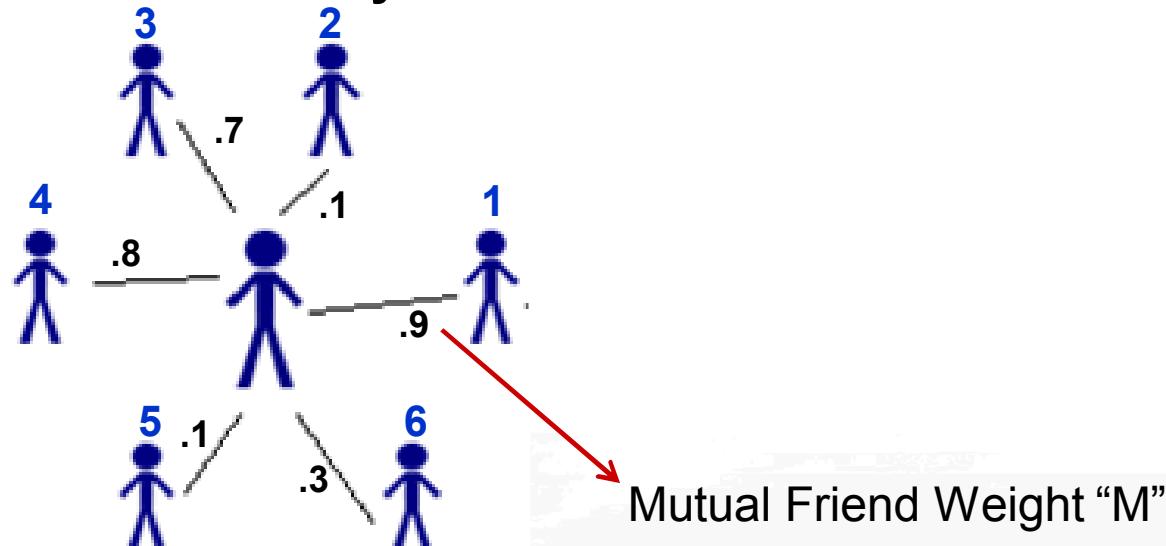
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Current Work – Group Conformity

Sociological Question: How might conformity in a friend group affect polarization in society?



Mathematical Approach:

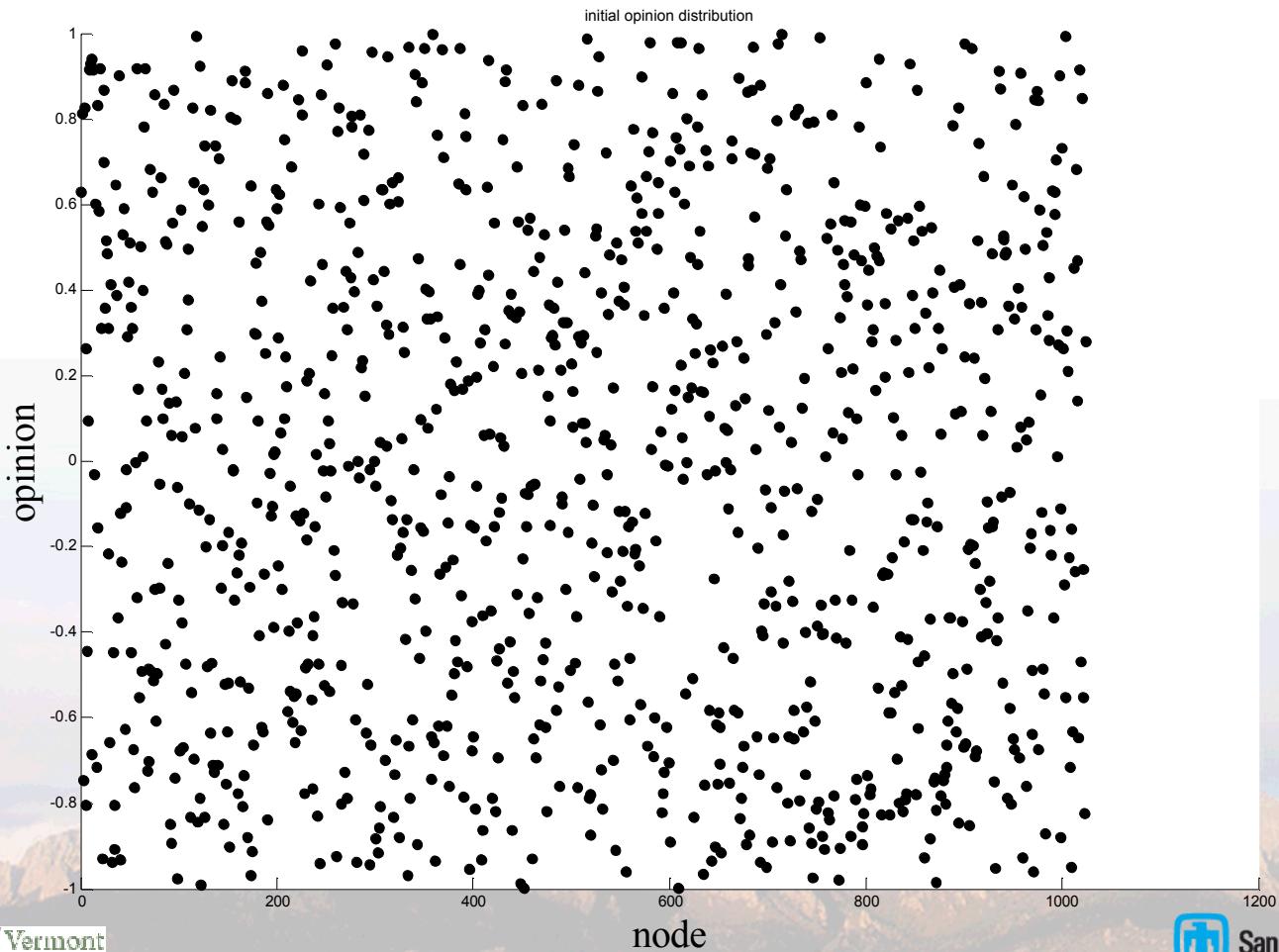
- Take average opinion value of those higher-weighted connections (those within friend group)
- $O_{avg} = (O_1 + O_3 + O_4)/3$
- If O_{avg} is influential (e.g. $> .7$ or $< -.7$)
 - Have $O_n =$ value closer to O_{avg}





Multivariate Linear Model: Group Conformity

Iteration = 1



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Multivariate Linear Model: Group Conformity

Iteration = 75,000



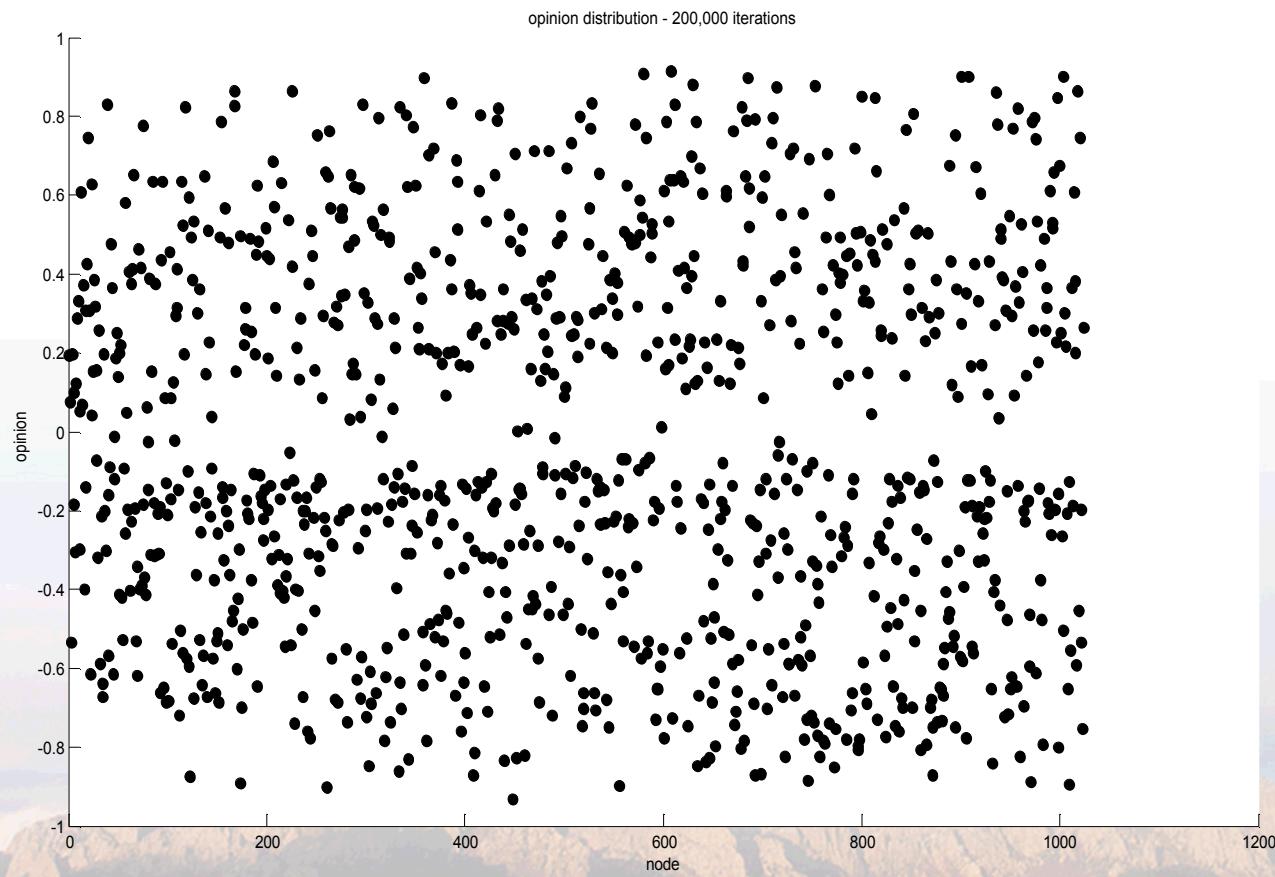
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Multivariate Linear Model: Group Conformity

Iteration = 200,000



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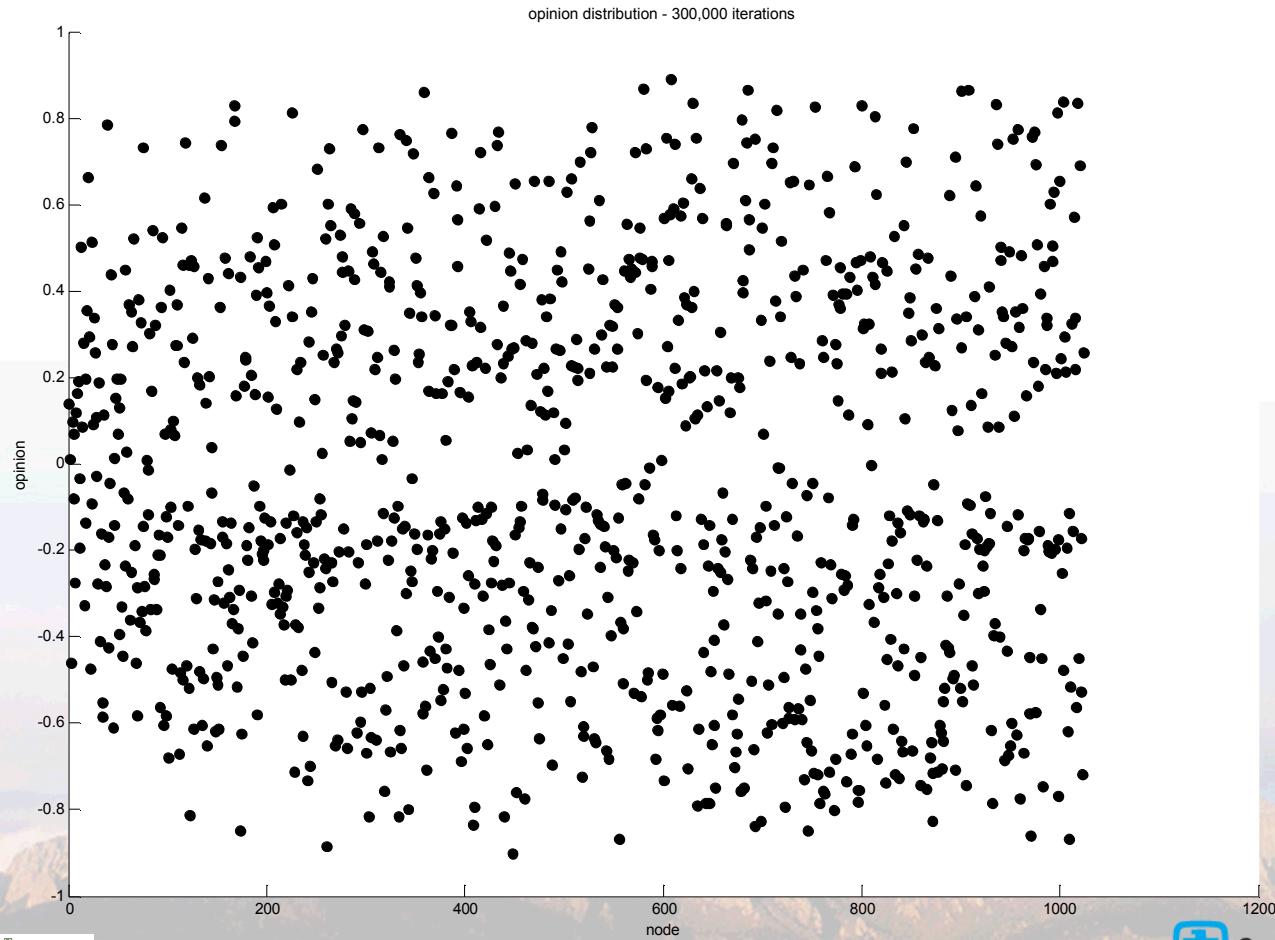


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Multivariate Linear Model: Group Conformity

Iteration = 300,000



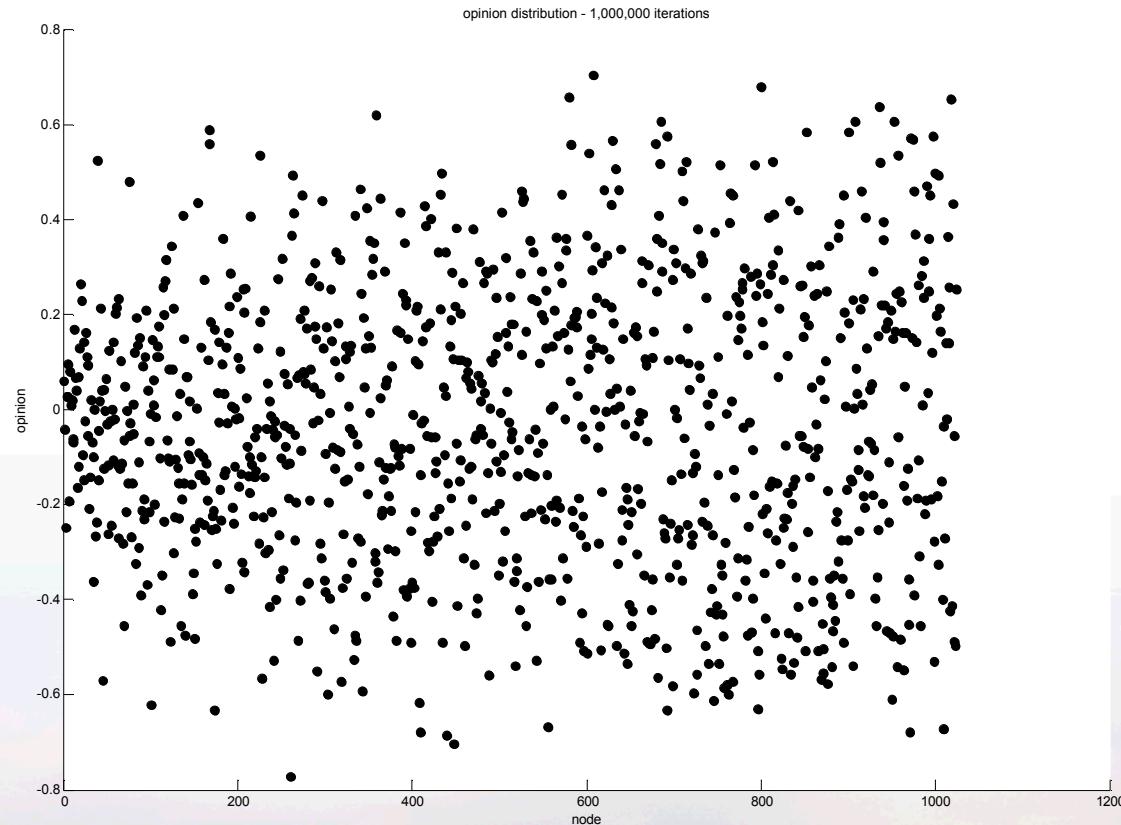
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Multivariate Linear Model: Group Conformity

Iteration = 1,000,000



Observations: Opinions seem to polarize at first away from the mean, but the majority eventually overpowers the groups and the opinion values will converge to zero.



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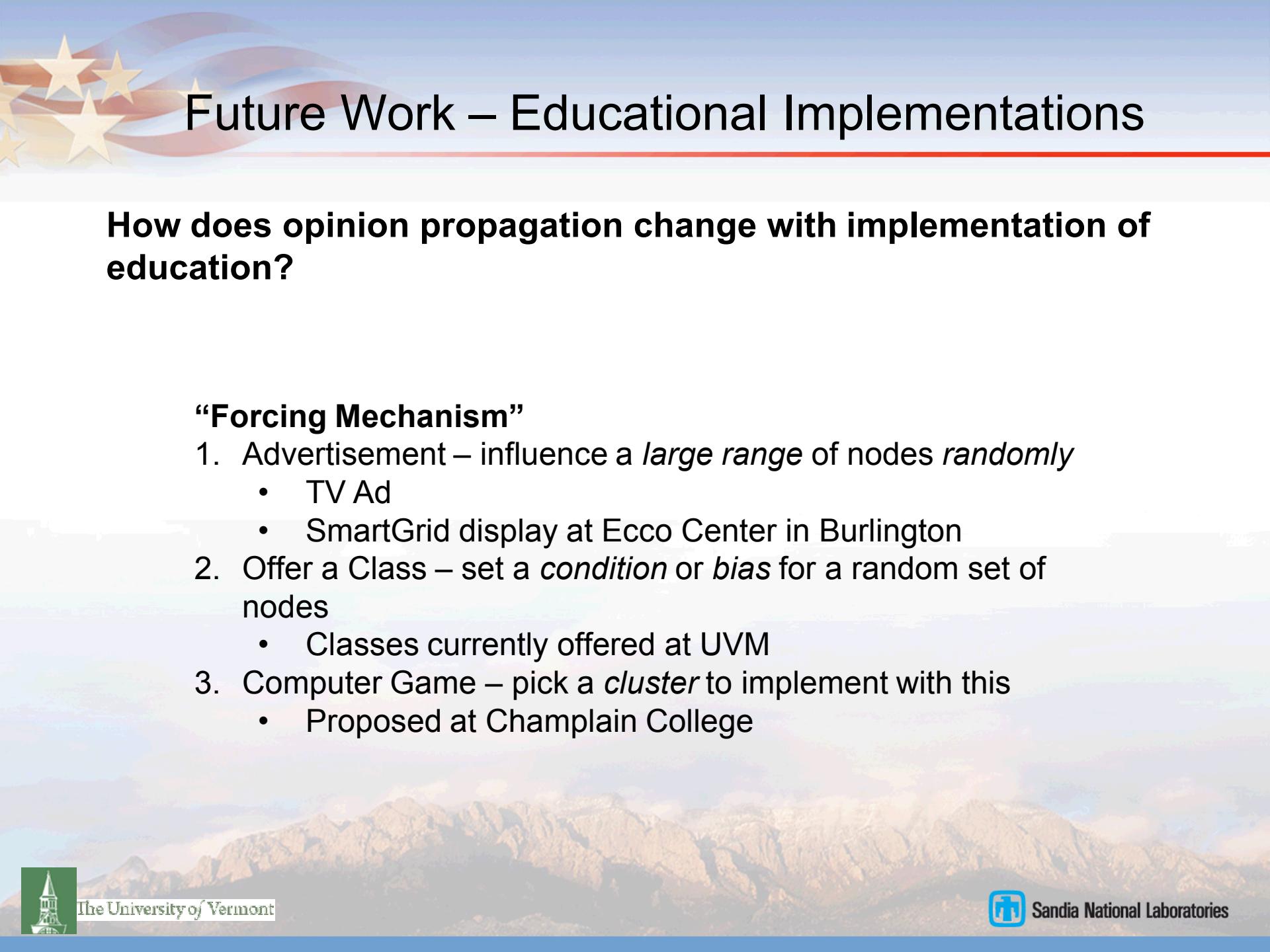
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Future Work – Educational Implementations

How does opinion propagation change with implementation of education?

“Forcing Mechanism”

1. Advertisement – influence a *large range* of nodes *randomly*
 - TV Ad
 - SmartGrid display at Ecco Center in Burlington
2. Offer a Class – set a *condition* or *bias* for a random set of nodes
 - Classes currently offered at UVM
3. Computer Game – pick a *cluster* to implement with this
 - Proposed at Champlain College





References

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