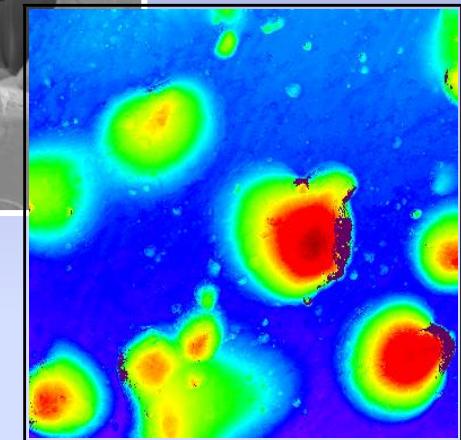
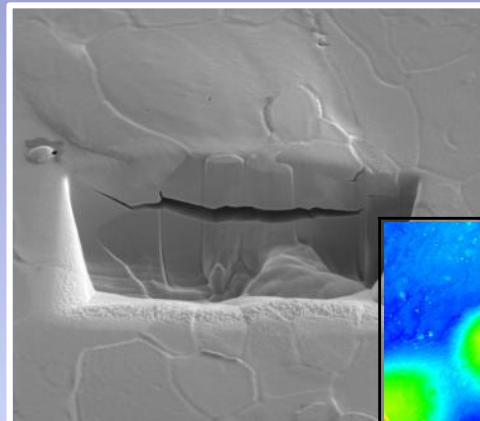
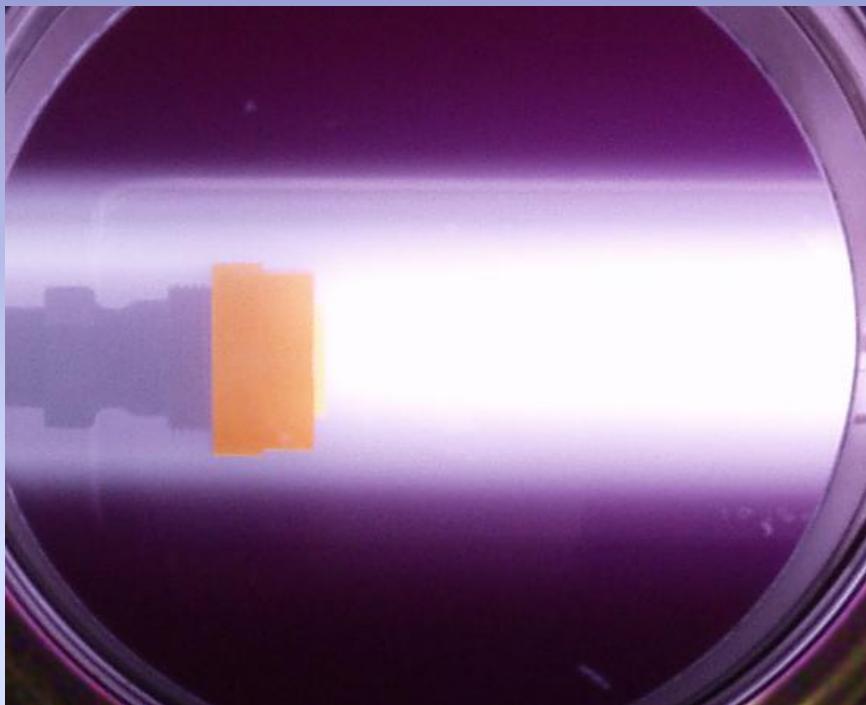


A CONTINUUM-SCALE MODEL OF HYDROGEN PRECIPITATION AND BUBBLE GROWTH IN METALS

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Sandia National Laboratories

OVERVIEW

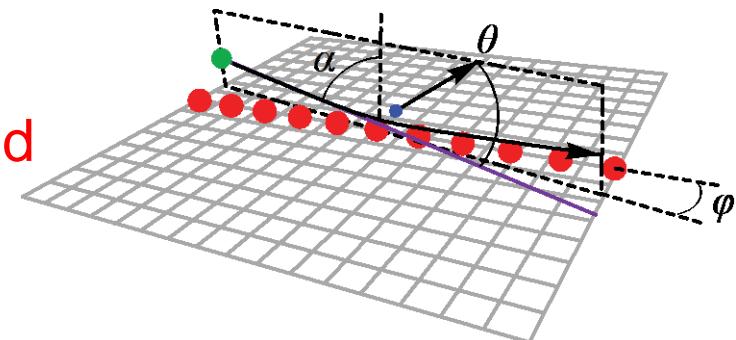
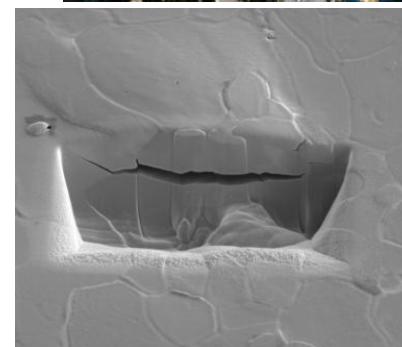
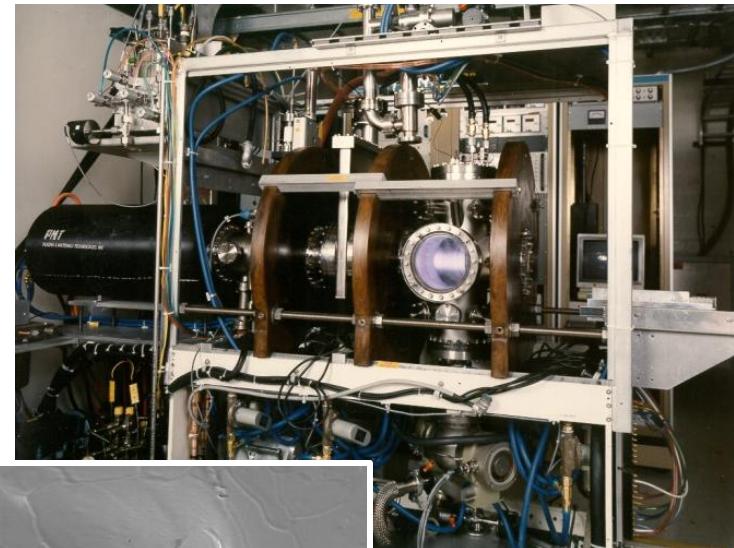
Hydrogen interaction with materials is relevant to:

- Tritium storage
- Hydrogen energy infrastructure
- Magnetic fusion energy

In this talk, I will discuss:

- Tritium retention in metals
- Experimental motivation
- Continuum-scale bubble model

The basic physics governing how hydrogen behaves in different materials can be applied to a wide range of systems.

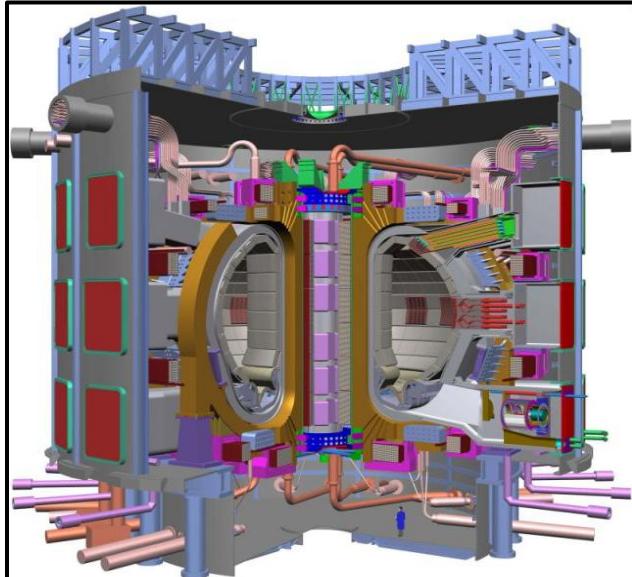


MAGNETIC FUSION ENERGY PROGRAM COUPLES WITH OTHER HYDROGEN RESEARCH AT SANDIA

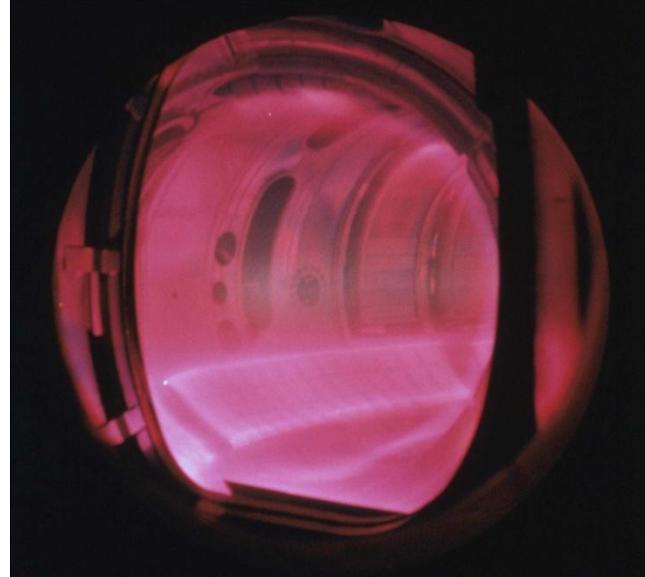
Basic concept:
Same as
hydrogen bomb

ITER:
international
fusion project
(€ 15 billion)

Key issue:
Trapped tritium



ITER baseline design



Interior view showing plasma discharge

We leverage Sandia tritium
and GTS expertise for
fusion:

- Simulate neutron damage
- Understand tritium trapping
- Model bubble growth



**Common interest benefits
the science behind GTS:**

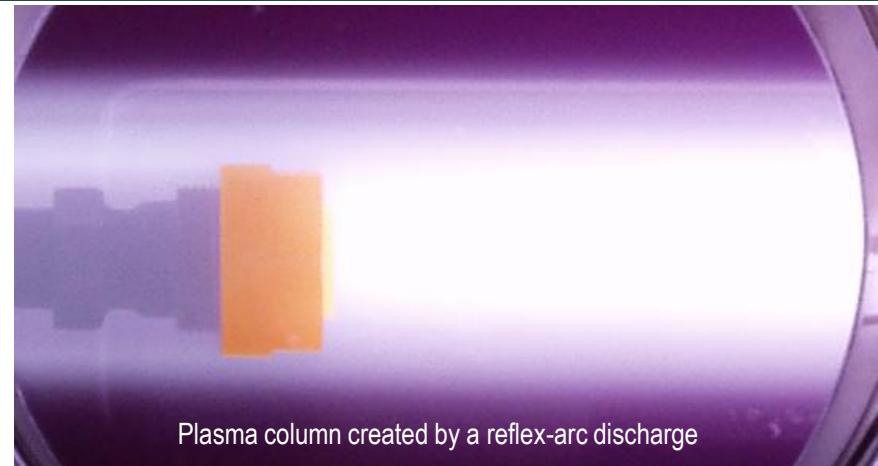
- Fosters collaboration
- Provides access to
international expertise
- Outside funding to enhance
capabilities

EXPERIMENTAL MOTIVATION: UNDERSTANDING TRITIUM RETENTION IN METALS

- Implant high concentrations of tritium into materials
- Study **tritium trapping and permeation**
- Joint experiment between **Sandia** and **Idaho National Laboratory (INL)**



TPE glove box



Plasma column created by a reflex-arc discharge

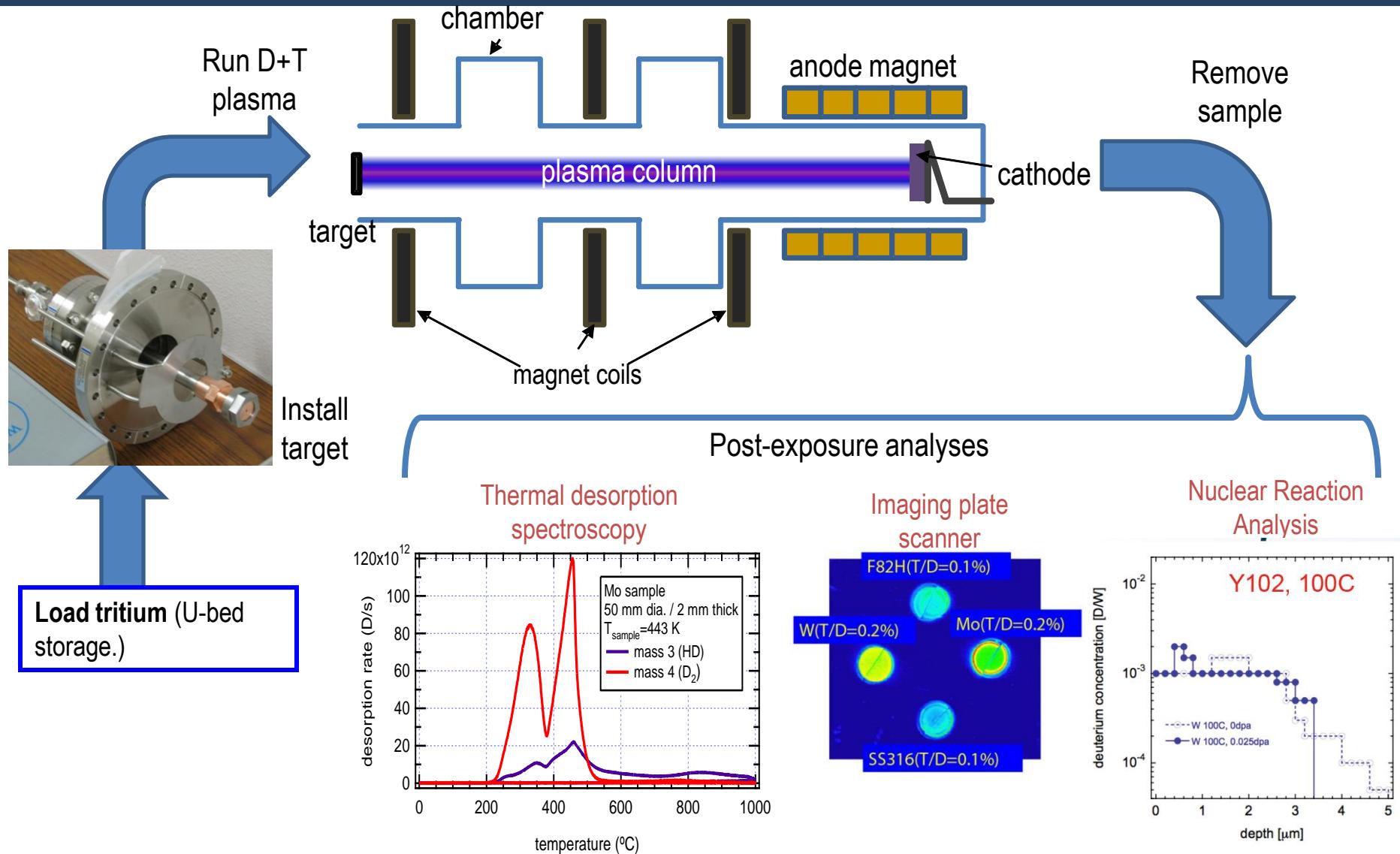
Unique features

- Only high-flux tritium plasma generator in the world
- Handles **neutron irradiated samples**
- Plasma-driven permeation
- Tritium surface/depth profiling

Experiment History:

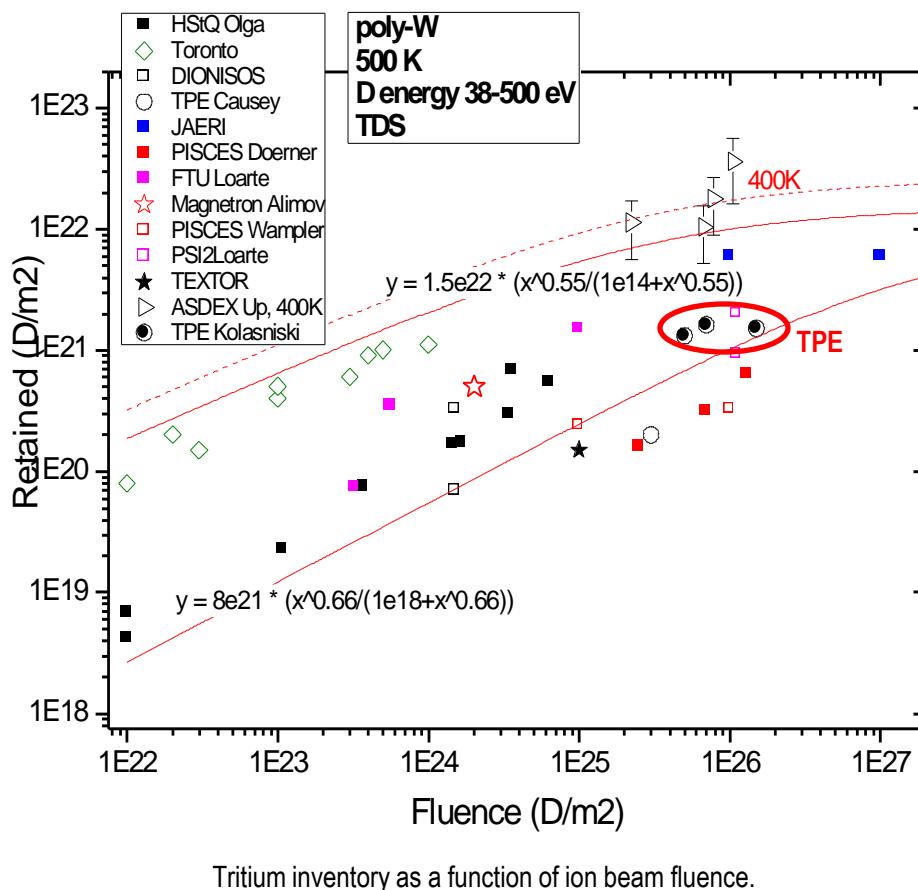
- Developed at SNL, later moved to INL (2002).

THERMAL DESORPTION SPECTROSCOPY ENABLES US TO MEASURE THE TOTAL TRITIUM INVENTORY

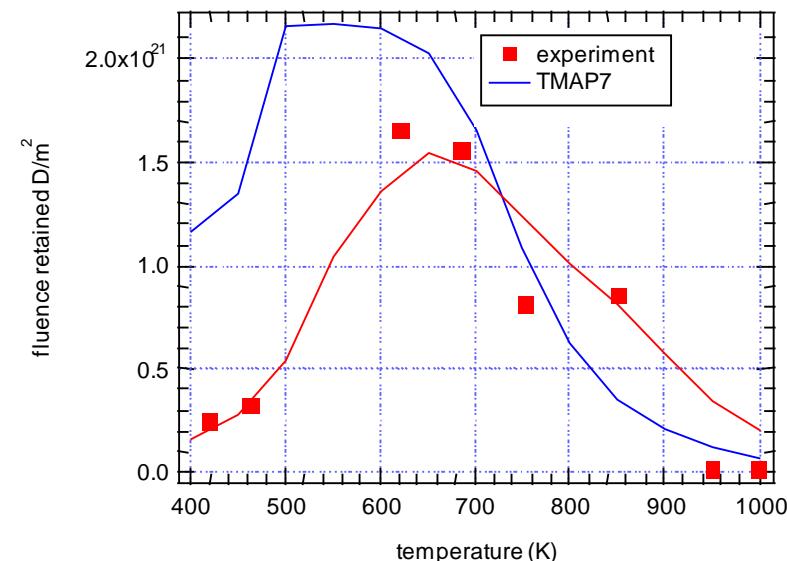


TPE CONTRIBUTES TO UNDERSTANDING TRITIUM RETENTION AT HIGH CONCENTRATIONS

Retention measurements: Used to predict tritium accumulation in reactors



Retention variation with temperature:



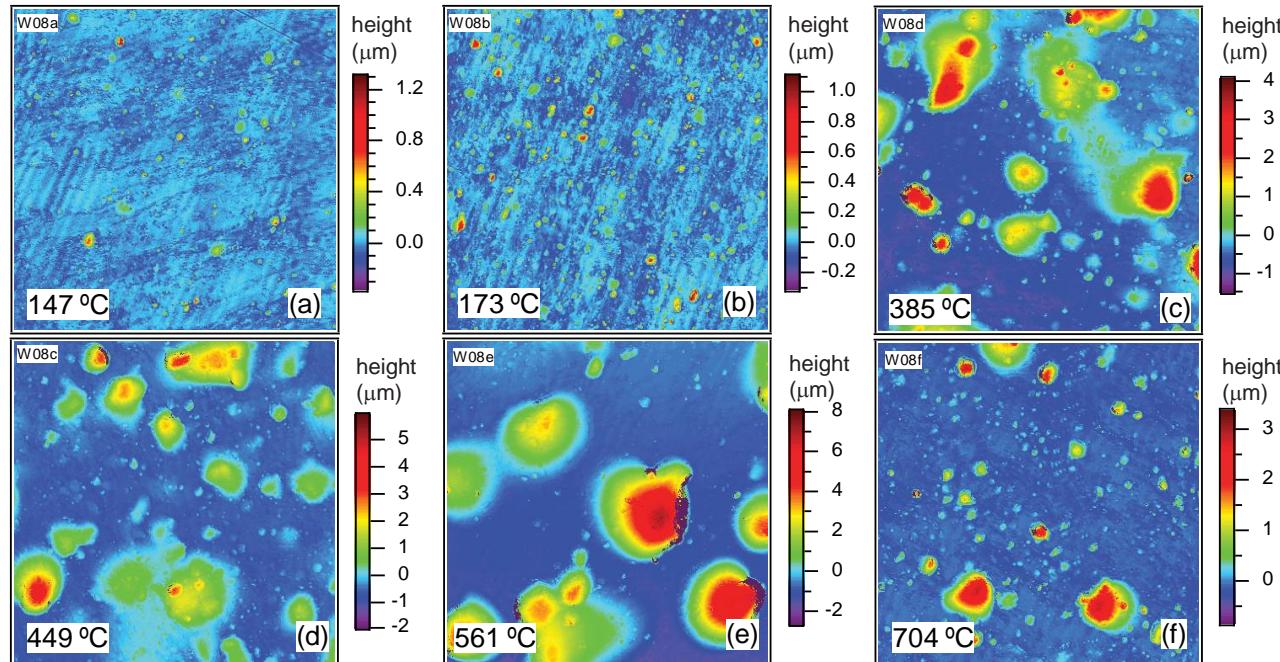
- Existing models over-predict retention
- Extrapolations to higher fluence questionable

What materials science are we missing?

PROFILOMETRY REVEALS THAT SMALL HYDROGEN BUBBLES HAVE GROWN

Note:

Each panel depicts a $500 \mu\text{m} \times 500 \mu\text{m}$ area.

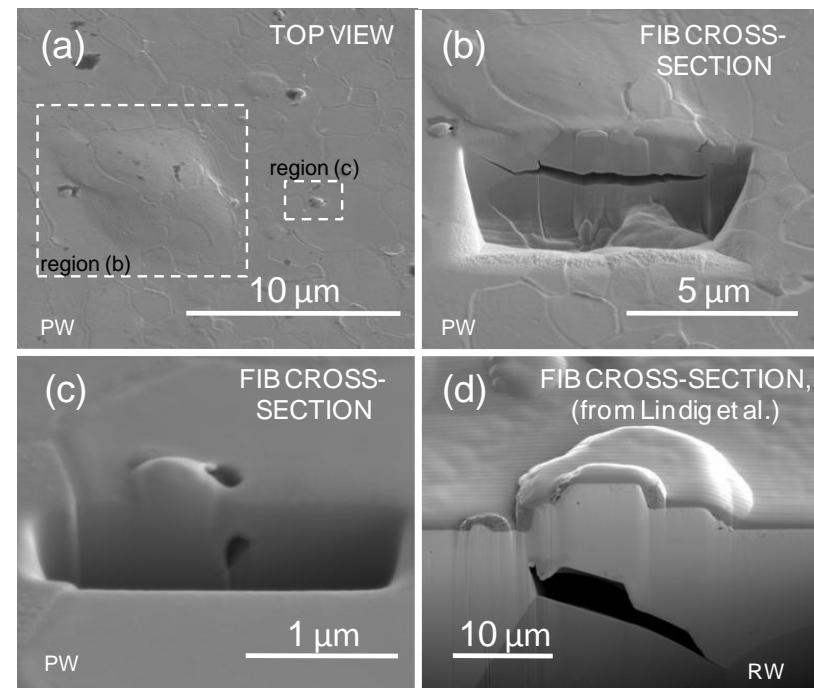


- Difficult to keep hydrogen in solution in W.
- **Precipitation** of H_2 in bubbles preferred.
- Trapping by bubbles inhibits permeation.
- Standard models (TMAP7, DIFFUSE) don't account for bubble growth and precipitation.

HYDROGEN PRECIPITATE GROWTH IN TUNGSTEN: EXPERIMENTAL FINDINGS

Focused ion beam (FIB) results:

- Profiled PLANSEE W previously exposed in TPE:
 - 70 eV D⁺ ions
 - $\Phi = 1.1 \times 10^{18} \text{ cm}^{-2}\text{s}^{-1}$
 - $F = 8.7 \times 10^{21} \text{ cm}^{-2}$
 - $T = 385^\circ \text{ C.}$
- Large blister in (b) enlarged by crack growth.
- Small blister in (c) has grown by dislocation loop punching.
- FIB profile of re-crystallized tungsten exposed under similar conditions shown in (d). Image from [Lindig et al., *Phys. Scr.* (2009).] Growth mechanism also appear to be due to dislocation loop punching.



Bubble growth mechanisms:

- Crack propagation
- Dislocation loop punching
- Vacancy clustering

CONTINUUM-SCALE FINITE DIFFERENCE MODEL ENABLES SIMULATIONS OF BUBBLE GROWTH

Precipitation affects hydrogen diffusion in metals [W.R. Wampler, *Nucl. Fusion* (2009)]

Motivation for further model development:

- DFT, MD, and Kinetic Monte Carlo reveal key nucleation and growth mechanisms.
- Incorporate insight into continuum approach to model experimental environment
- Existing continuum models (TMAP, DIFFUSE) exclude important physics (e.g. precipitation)

- ❑ We leverage metal tritides expertise at Sandia from **^3He bubble** growth models [D.F. Cowgill, *Fusion Sci. & Technol.* (2005)]
- ❑ Altered to simulate hydrogen bubbles:
 - Different nucleation process [Henricksson *Appl. Phys. Lett.* (2008).]
- ❑ Use experiments to refine model.

DIFFUSION AND TRAPPING WERE MODELED USING A CONTINUUM-SCALE APPROACH

Diffusion:

Basic 1-D diffusion equation assuming uniform temperature.

Point defects:

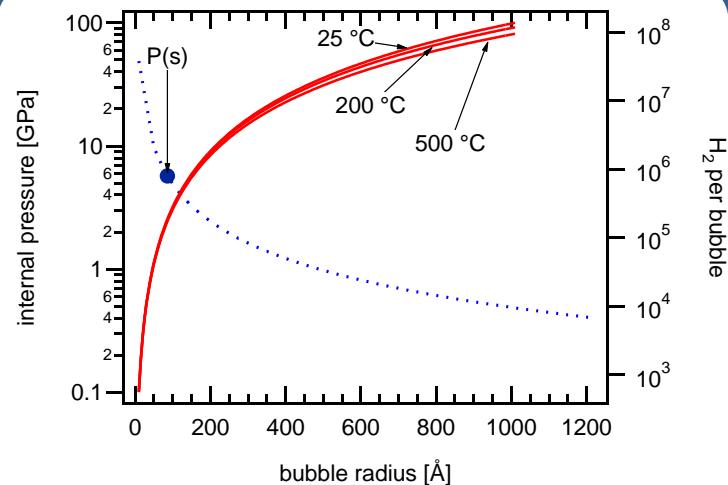
Point defects modeled as 1.4 eV saturable traps (not permitted to serve as nucleation sites for bubbles.) Used approach of Ogorodnikova [J. Nucl. Mater. 2009] to address trapping and release:

$$\partial C_t(x,t) / \partial t = (2Da/3)[C_m(N_t - \delta C_t) - (12\delta C_t / a^3) \exp(-E_t / kT)]$$

δ = inverse trap saturability; N_t = trap density; C_t = H concentration in traps.

Trapping by bubbles:

Modeled using a simple approach developed by Mills [J. Appl. Phys. (1959)].



Bubble growth by loop punching

Loop punching condition:

$$p_{LP} \geq 2\gamma/r_b + \mu b/r_b$$

γ = surface energy r_b = bubble radius

b = Burgers vector μ = shear stress

Plot above shows the p_{LP} for W. For small bubbles, p_{LP} is >10 GPa. Need equation of state to calculate H₂ per bubble from loop punching stress.

H_2 equation of state (EOS):

Very high pressures (>1 GPa) expected within small hydrogen bubbles.

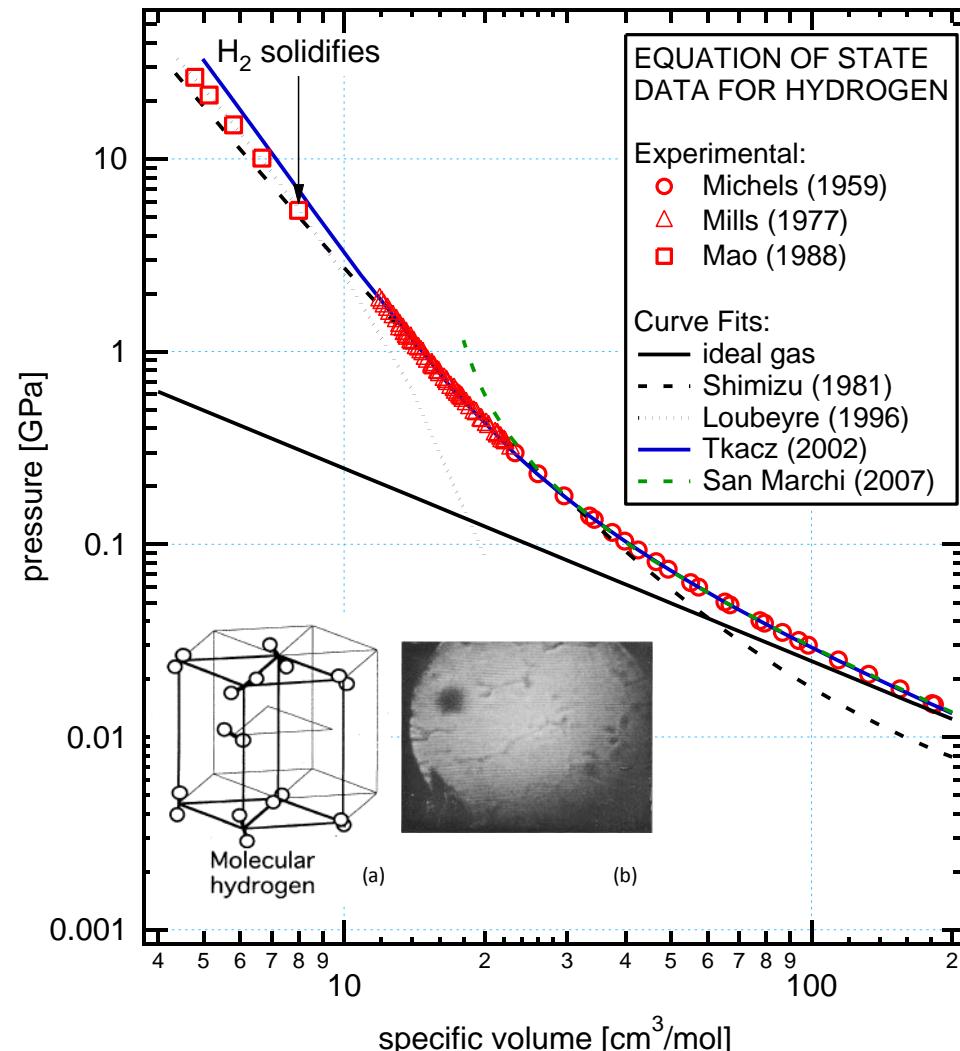
At 25 ° C, H_2 solidifies at $p=5.7$ GPa, forming an hexagonal close-packed molecular solid.

- Over the range of pressures of interest for this work, we found Tkacz's [J. Alloys & Compounds (2002)] EOS to provide the best fit:

$$v = Ap^{-1/3} + Bp^{-2/3} + Cp^{-4/3} + (D + ET)p^{-1}$$

- San Marchi's simplified EOS is also quite accurate at lower pressures:

$$v = \frac{RT}{p} + b$$



EQUILIBRIUM CONDITIONS DICTATE WHEN THE BUBBLES WILL GROW

Calculation of equilibrium pressure:

When will the precipitate gas be in equilibrium with the hydrogen in solution?

- Equate the **chemical potentials** of the gas phase and solution.
- Account the non-ideal behavior of the gas in bubbles by incorporating hydrogen **fugacity**:

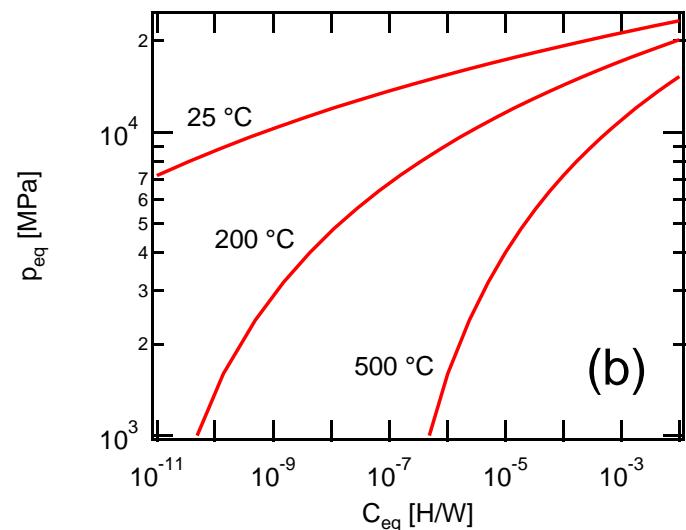
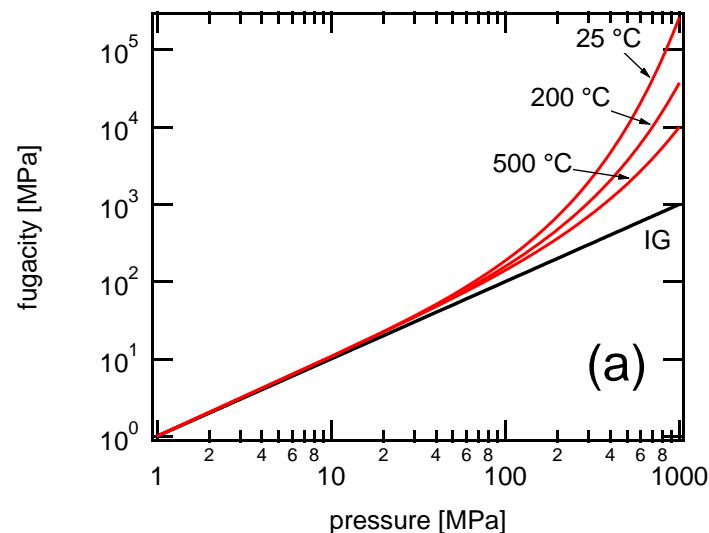
$$\ln(f/p) = \int_0^p (v(p, T)/RT - 1/p) dp$$

- The **equilibrium concentration** is then given by the following expression:

$$C_{eq} = \sqrt{f} S_0 \exp(-H_s/RT)$$

S_o and H_s are solubility parameters from Frauenfelder [J. Vac. Sci. & Tech., 1969].

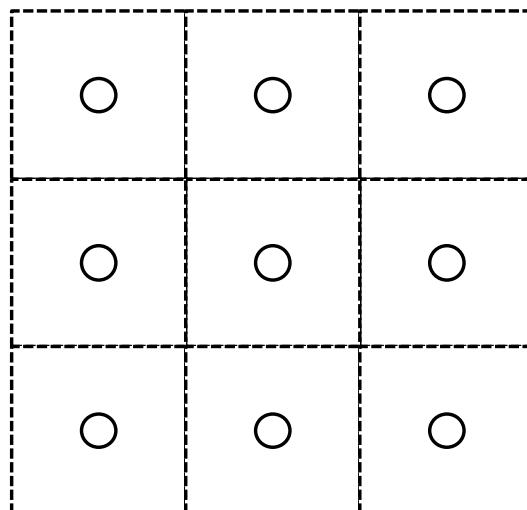
Equilibrium conditions predict when precipitation is favorable.



CONTINUUM-SCALE APPROACH ENABLES RAPID SOLUTION OF DIFFUSION EQUATION

Assume:

- (a) Point defects saturable, do not behave as bubble nucleation sites.
- (b) Array of evenly-spaced spherical bubbles.
- (c) Bubble diameter smaller than inter-bubble spacings
- (d) Slow thermal ramp (quasi-equilibrium is satisfied.)



Array of evenly-spaced spherical bubbles.

**BASIS FOR FINITE DIFFERENCE MODEL:
NEED TO INTEGRATE THREE COUPLED PDE'S**

Governing equation (1-D diffusion w / 2 sink terms):

$$\partial u(x, t) / \partial t = D(t) \partial^2 u(x, t) / \partial x^2 - q_T(x, t) - q_B(x, t)$$

$q_T = \partial u_T(x, t) / \partial t$

Flow into or out of the bubbles determined by local eq. conc.

$$q_B = \partial u_B(x, t) / \partial t = 4\pi D(t) r_B(x, t) N_B(x) [u(x, t) - u_{eq}(x, t)]$$

Concentration at bubble surface determined by Sievert's Law:

$$u_{eq}(x, t) = \sqrt{f} S_0 \exp(-E_s/RT)$$

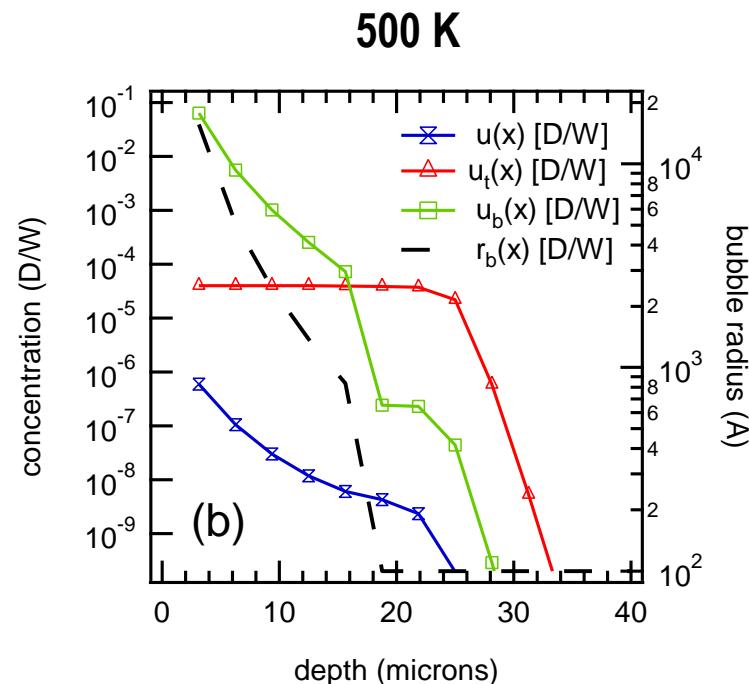
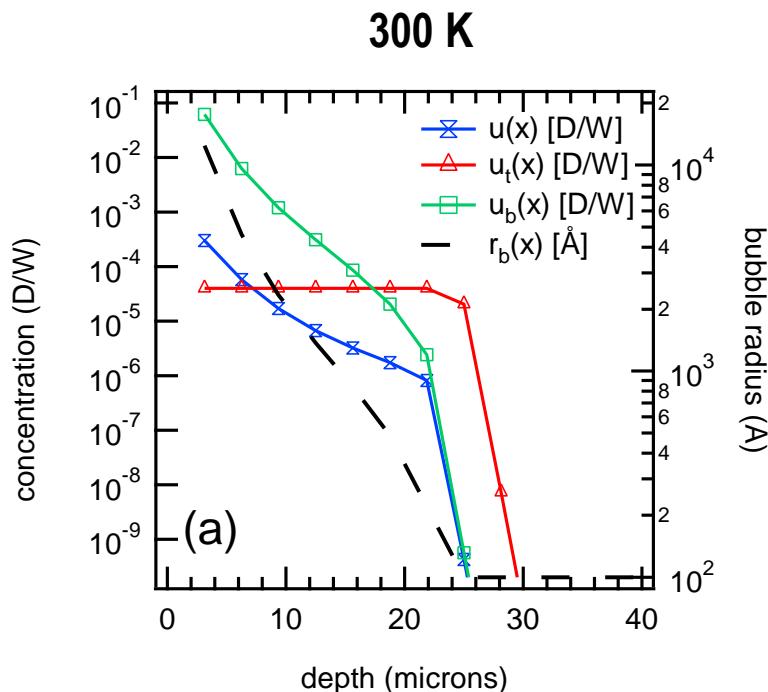
Fugacity (requires aforementioned EOS):

$$\ln(f/p) = \int_0^p (\nu(p, T)/RT - 1/p) dp$$

SIMULATED BUBBLE SIZES CONSISTENT WITH EXPERIMENTAL FINDINGS

- Assumed a pre-existing concentration of nucleation sites (eventually growing into bubbles.)
- Traps fill first, followed by bubble growth.
- Using realistic input conditions, depth profiles consistent with experimental findings.

$N_t = 4 \times 10^{-5} \text{ W}^{-1}$
 $N_b = 10^{-12} \text{ W}^{-1}$
 $F = 10^{18} \text{ D/cm}^2\text{-s}$, calculated near-surface conc. at the end of range from $F = Du/r$.
 $r = 2.5 \text{ nm}$ for 100 eV D⁺ ions



CONCLUDING REMARKS

We have studied....

- *Tritium trapping in metals*
 - TPE used to implant a large amount of hydrogen
 - Observed hydrogen bubble growth in tungsten
- *Hydrogen bubble growth*
 - Successfully adapted metal tritides code
 - Model accurately predicts bubble growth conditions
 - Further work:
 - Implementation of fast DAE solver
 - Modeling of thermal desorption from precipitates
 - Experiments to validate the model predictions
 - Application to high-temperature hydrogen attack.

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