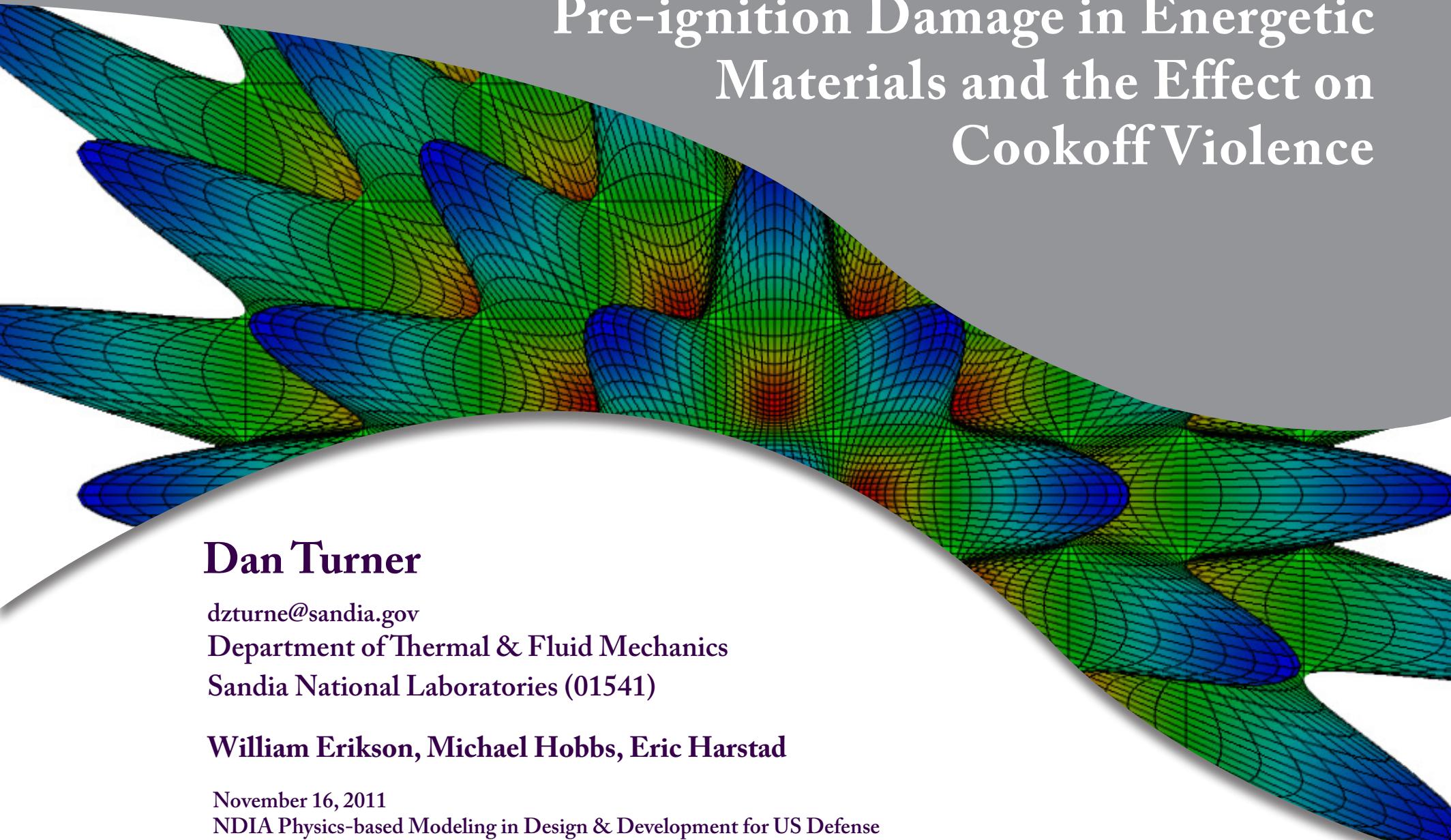


# Multiphysics Modeling of Pre-ignition Damage in Energetic Materials and the Effect on Cookoff Violence

SAND2011-8268C



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November 16, 2011

NDIA Physics-based Modeling in Design & Development for US Defense



- 1. Motivation and context**
- 2. Overview of coupling approach**
- 3. Decomposition model description**
- 4. Peridynamics**
- 5. Examples**
- 6. Future work and conclusions**

# Motivation and Context

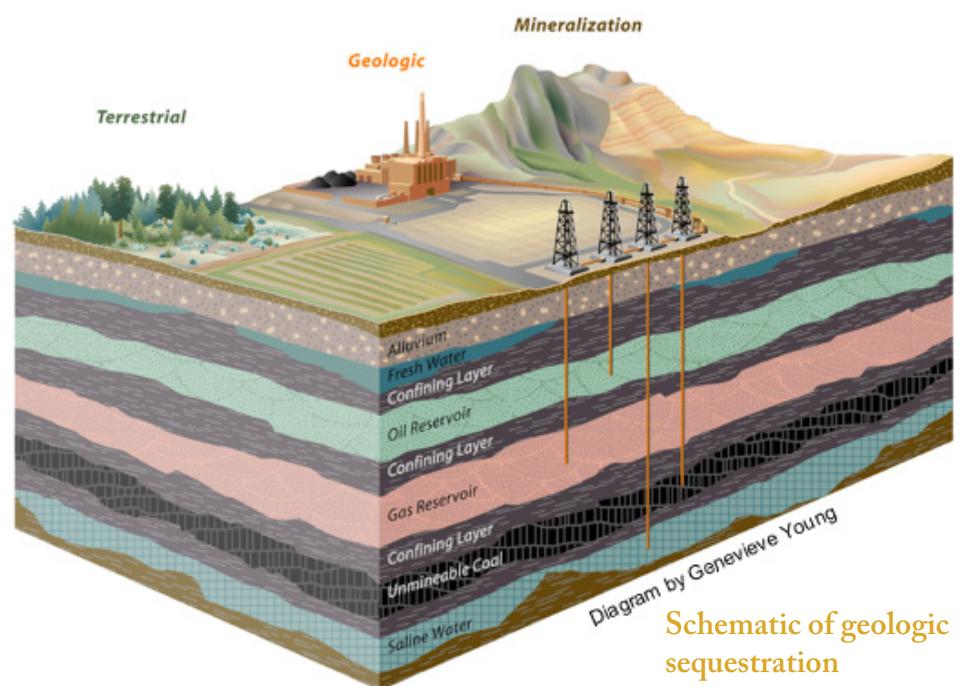
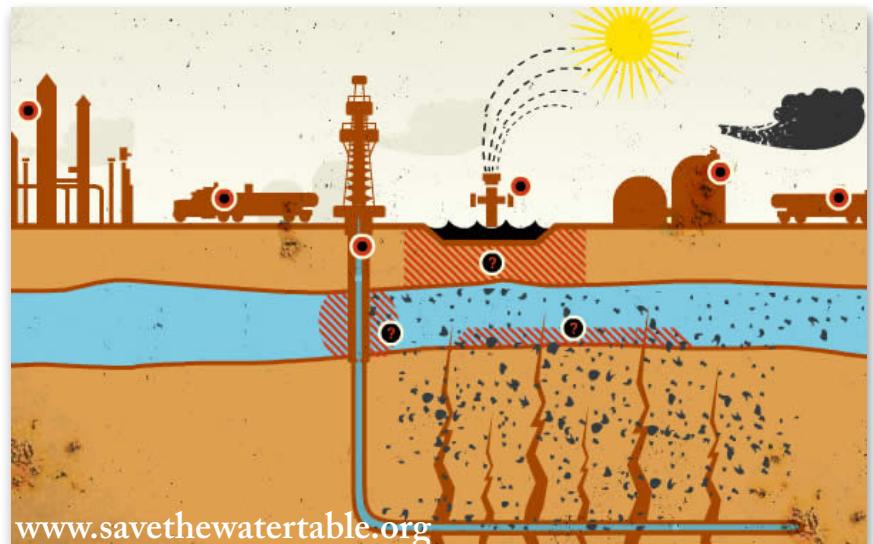
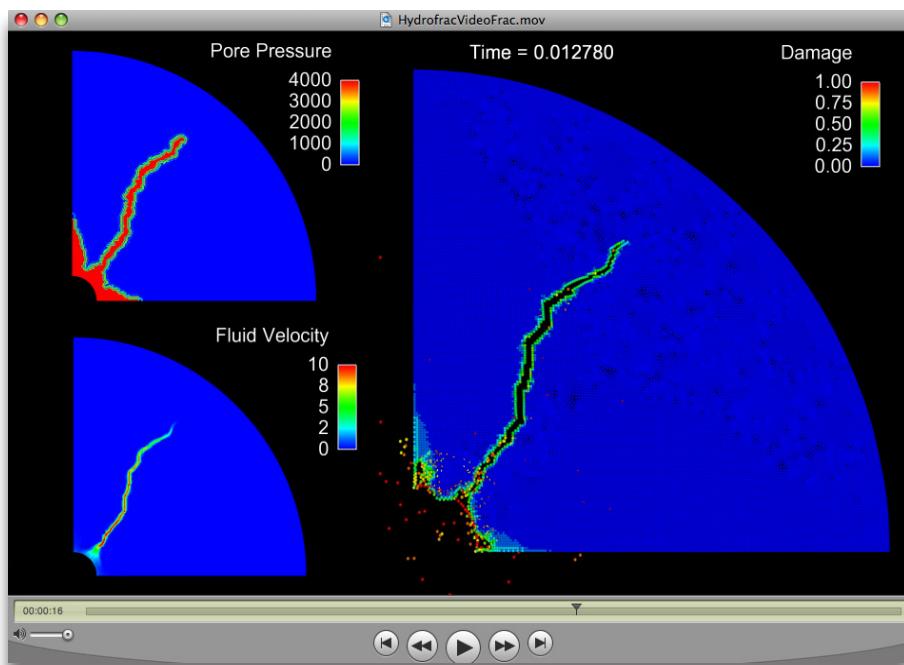


## Carbon dioxide (CO<sub>2</sub>) sequestration

- Potential for caprock fracture leading to large-scale release back into the atmosphere

## Hydraulic fracturing

- Extent of reservoir damage due to fracking and transport of chemicals





## Energetic materials

- Burn dynamics and reaction violence are strongly correlated with damage in explosive materials

## Goals

- Effect of pre-ignition damage on permeability of energetic materials
- Model enclosure breach and calculate gas production
- Determine fragmentation of confinement after ignition and relative energy of fragments



Sealed confinement

Hobbs, Kaneshige, and Wente. Correlating cookoff violence with pre-ignition damage. SAND2010-1183C

SITI experiments



Vented confinement



ODTX experiments: Evidence of breached confinement

Koerner, Maienschein, Burnham, and Wemhoff, UCRL-CONF-232590

# Theories for Damage Mechanisms

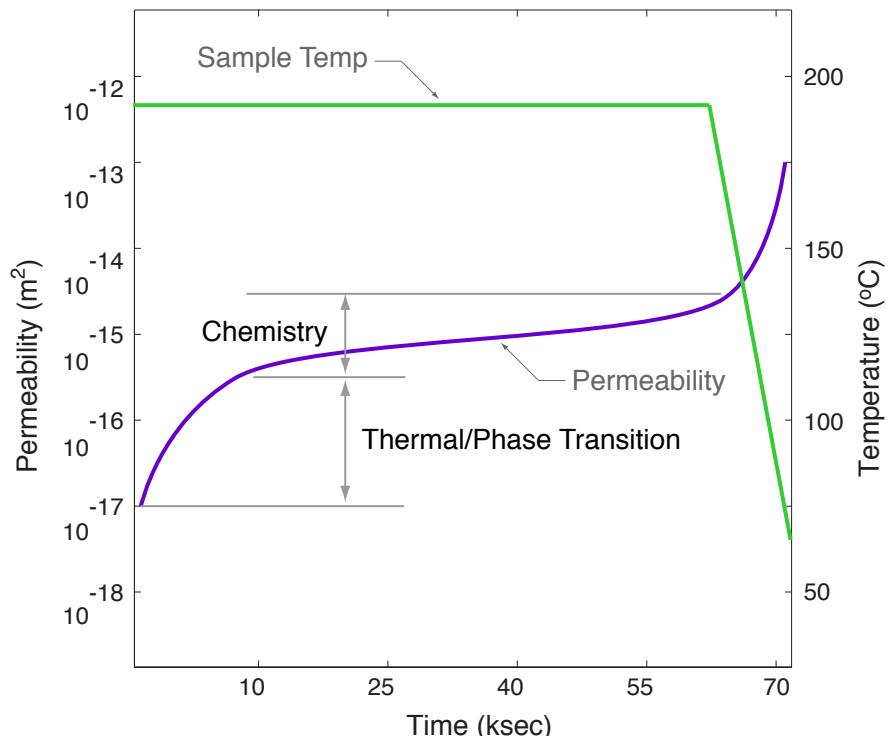


## Primary drivers

- Phase change from condensed to gas phase leads to material weakening
- Thermal expansion of both the condensed and gas phases creates confinement pressurization that stresses the material
- Pore pressure pushes bonds in the material apart leading to weakening (inter-grain or intra-grain)
- Compounding effects like chemical reaction acceleration due to increased surface area from damage

## Second order effects

- Dislocation movement and void coalescence
- Changes in crystal structure or packing



Stages of damage during heating

Diagram taken from Baine Asay lecture notes:  
Deflagration-to-Detonation Transition, Sept 2011

# Coupling Approach Overview

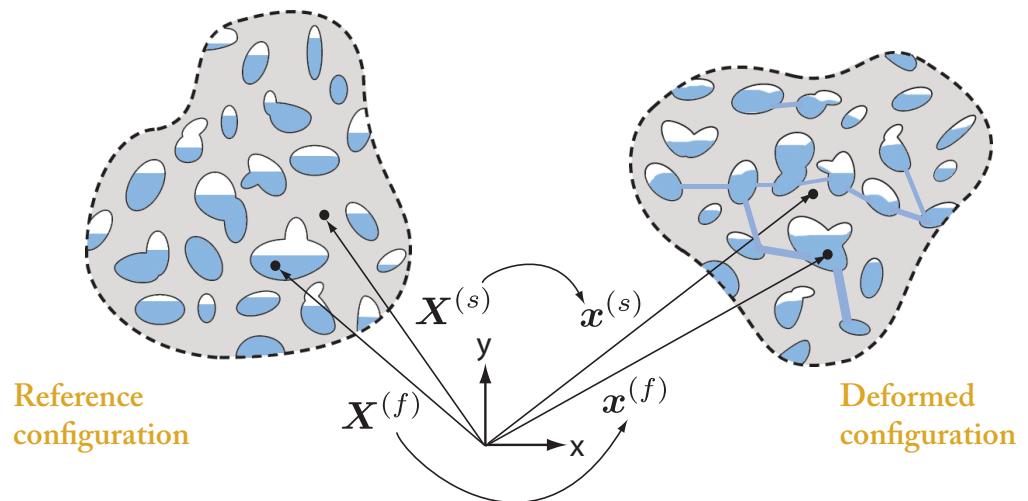


## Damage modified permeability

- Model rare tracking and decreased resistance to flow (added permeability)
- Incorporate pore volume changes resulting from deformation of the solid media (added compressibility)

$$\bar{\alpha} = S_n \left( 1.0 + \beta \frac{\|\mathbf{T}^{(s)} - \mathbf{T}_0\|}{\|\mathbf{T}_0\|} \right)$$

$$\phi = C_\phi (1 - (1 - \phi_0) / \det[\mathbf{F}])$$

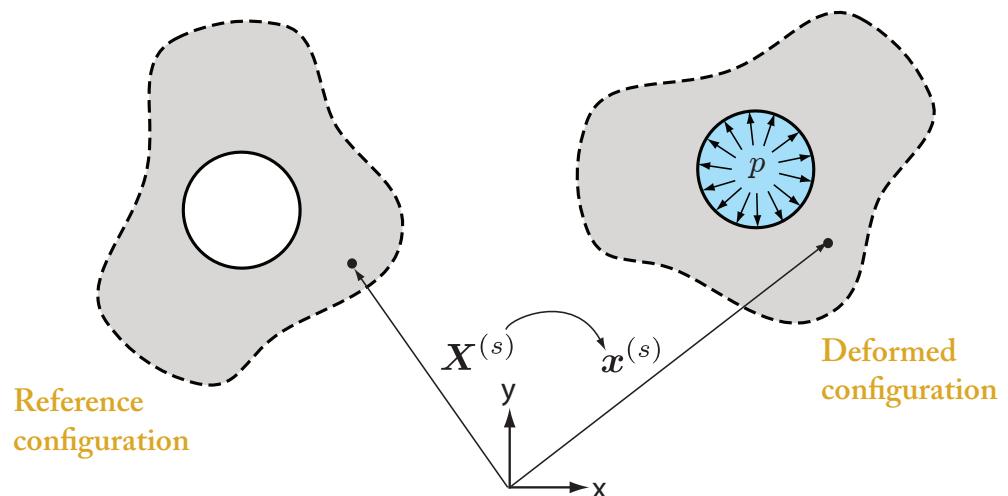


$$\alpha^{(f)} = \alpha^{(f)}(\text{damage, stress criterion})$$

$$\phi^{(s)} = \phi^{(s)}(\text{deformation gradient})$$

## Effective stress

- Internal force on pores brought about by the fluid/gas pressure (added stress)



$$\mathbf{T}^{(s)} = \mathbf{T}_e^{(s)} + p^{(f)} \mathbf{I}$$

# Decomposition Model



$$\rho C_p \frac{\partial T}{\partial t} - \operatorname{div}[\mathbf{q}] = \rho \dot{q} S$$

$$\mathbf{q} = k \operatorname{grad}[T]$$

$$\frac{dX}{dt} = -S$$

$$\frac{\partial \rho}{\partial t} + \rho \operatorname{div}[\mathbf{v}] = \rho S$$

$$\mathbf{v} = -\frac{K}{\mu} \operatorname{grad}[p]$$

$$S = A \exp \left( -\frac{E}{RT} \right) \left( \frac{p}{p_0} \right)^r X^n (1 - wX)^m$$

Arrhenius Pressure dependent Autocatalytic

$$K = f(\text{damage})$$

$$\int \mathbf{w} \cdot \mathcal{L}(\cdot) \, d\Omega = 0$$

Energy equation for temperature, T

Fickian diffusion

Species equation for species, X

Mass balance equation for pressure, p

Darcy's law (momentum balance) for velocity, v

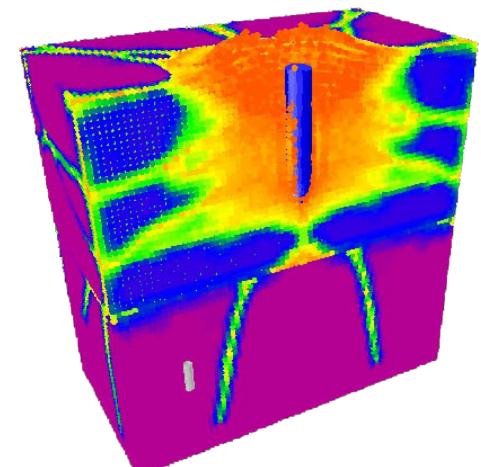
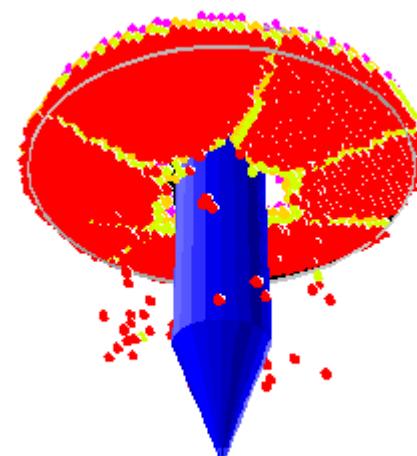
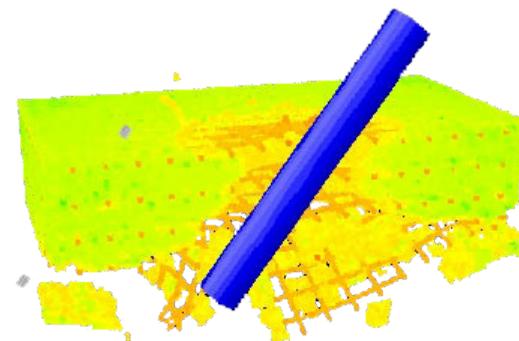
Reaction rate model for source, S

Damage modified permeability

Standard Galerkin single field weak form

## Peridynamics

- Integral based formulation rather than differential equations
- Nice features regarding crack propagation paths
- Scalable for massively parallel
- Similarities with molecular dynamics
- Efficient for large scale damage evolution
- Can be used effectively in an explicit or implicit context
- Traditional elasticity theory can be recovered under the right circumstances



Various peridynamics simulations of projectile impact

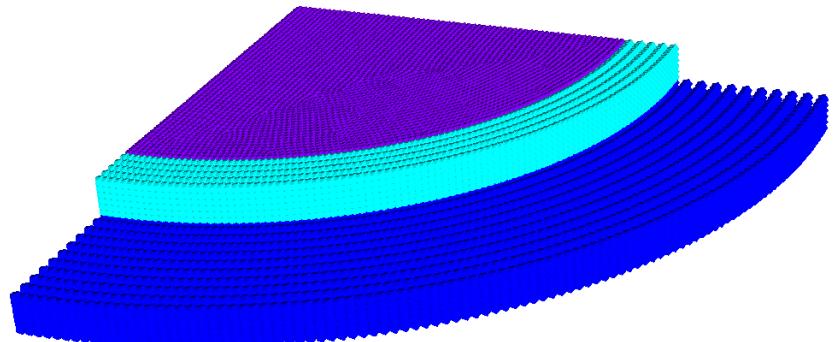
Images taken from EMU web page. Simulations done by Stewart Silling and co-workers

# Deformation and Damage Evolution

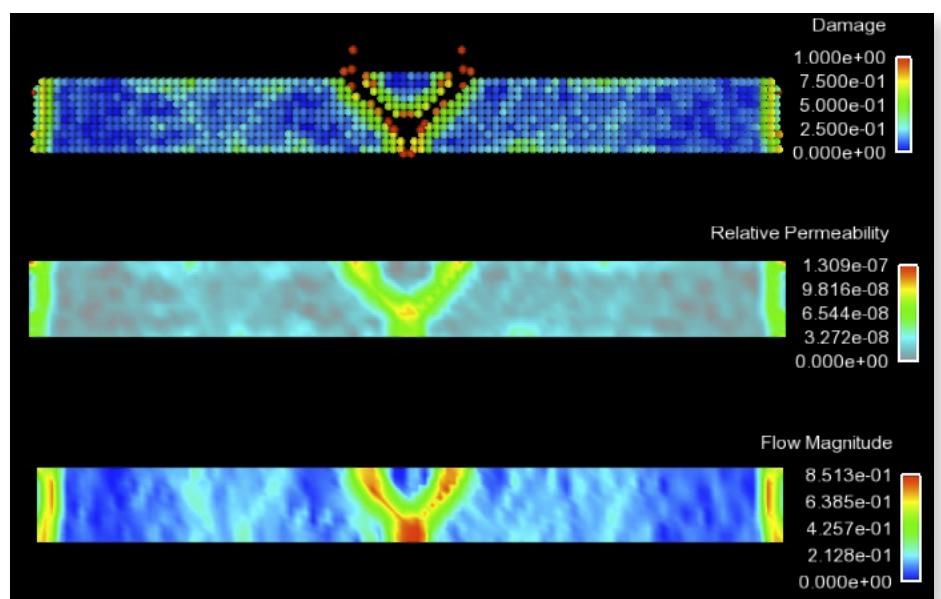


## Various uses of peridynamics for modeling damage

- Mechanical deformation and fracture in the confinement
- Model for computing permeability due to damage caused by fluid-structure interaction (mixture theory)
- Cracking and void formation in the energetic material
- Combinations of the above



Model of energetic material, seal, and portion of the anvil



Flow across a porous tensile specimen

# Deformation and Damage Evolution



## Peridynamics formulation

- Equation of motion

$$\rho(\mathbf{x})\ddot{\mathbf{u}}(\mathbf{x}, t) = \mathbf{L}_u(\mathbf{x}, t) + \mathbf{b}(\mathbf{x}, t) \quad \forall \mathbf{x} \in \mathcal{B}, \quad t \geq 0,$$

$$\mathbf{L}_u(\mathbf{x}, t) = \int_{\mathcal{B}} \{ \underline{\mathbf{T}}[\mathbf{x}, t] \langle \mathbf{x}' - \mathbf{x} \rangle - \underline{\mathbf{T}}[\mathbf{x}', t] \langle \mathbf{x} - \mathbf{x}' \rangle \} dV_{\mathbf{x}'}$$

- Discretized equation of motion

Cells in neighborhood of  $\mathbf{x}$   
(horizon)

$$\rho(\mathbf{x})\ddot{\mathbf{u}}_h(\mathbf{x}, t) = \sum_{i=0}^N \{ \underline{\mathbf{T}}[\mathbf{x}, t] \langle \mathbf{x}'_i - \mathbf{x} \rangle - \underline{\mathbf{T}}'[\mathbf{x}'_i, t] \langle \mathbf{x} - \mathbf{x}'_i \rangle \} \Delta V_{\mathbf{x}'_i} + \mathbf{b}(\mathbf{x}, t)$$

Force state  
(associates bond with force  
density per unit volume)

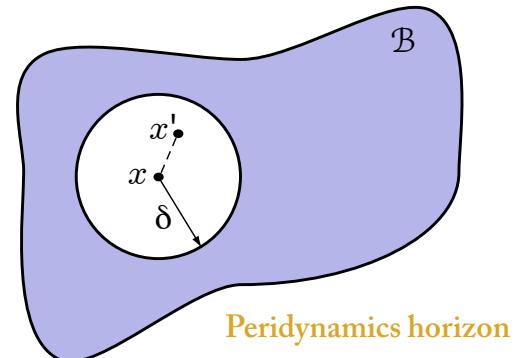
- Material model

$$\underline{\mathbf{T}}[\mathbf{x}, t] \langle \mathbf{x}'_i - \mathbf{x} \rangle = t \underline{\mathbf{M}}[\mathbf{x}, t] \langle \mathbf{x}'_i - \mathbf{x} \rangle$$

Pairwise force based on the  
deformation of all cells in  
the neighborhood of  $\mathbf{x}$

$$t_e = \underline{t} + \tilde{t}(p^{(f)})$$

Effective stress contribution

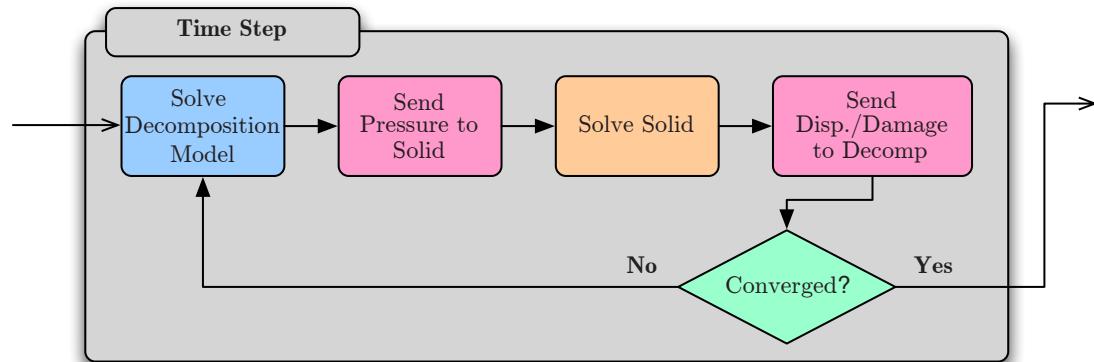


Peridynamics horizon

# Coupling Approach Overview



## Solution procedure



Lockstep solution procedure

```
Begin Solution Control Description

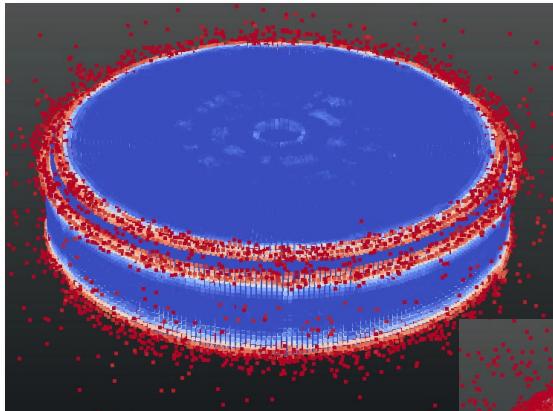
  Use System Main
  Begin System Main
    Begin Transient The_Time_Block
      Advance AriaRegion
      Transfer Aria_to_Presto
      Transfer Aria_to_Presto_Bond
      begin subcycle PrestoSubcycle
        Advance PrestoRegion
      end
      Transfer Presto_to_Aria
    End
  End
```

Sierra solution control input block

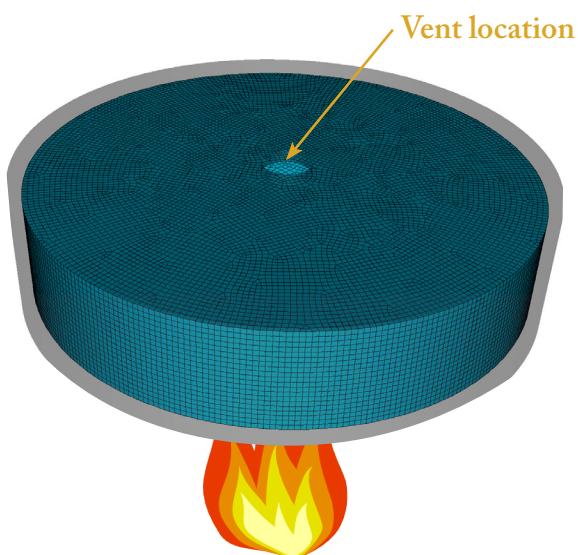
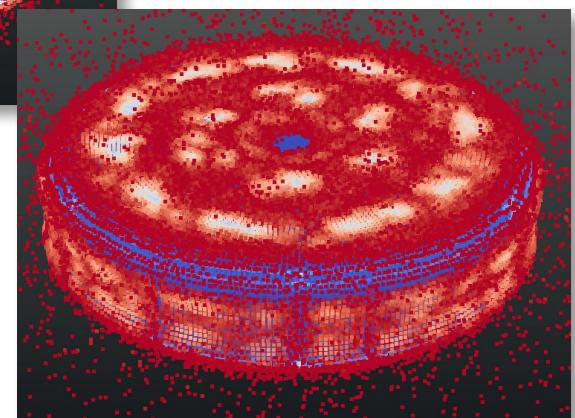


## Questions for accident scenarios

- Will ignition occur? Or will the reaction gases escape before pressurizing or reacting?
- How might the enclosure fragment and with how much energy will the pieces be projected?
- Does damage to the energetic material change the ignition location or the volume that simultaneously ignites?
- How can safety mechanisms like vents be designed to ensure insensitive munitions without inadvertently encouraging reaction violence?
- How does ullage effect reaction violence if at all?



Numerical simulations of the proposed method

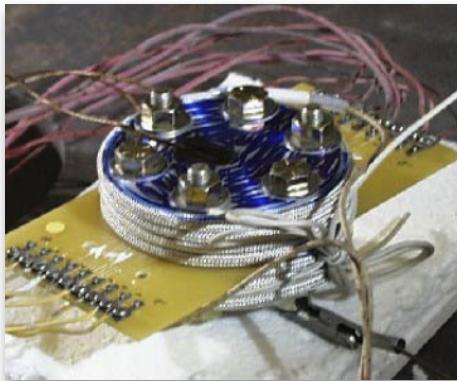


# Experiment Description



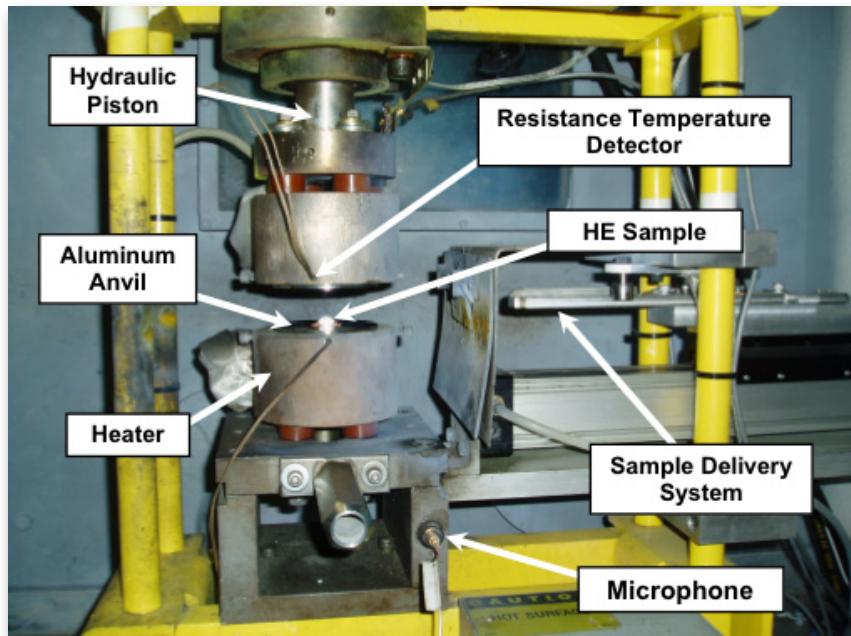
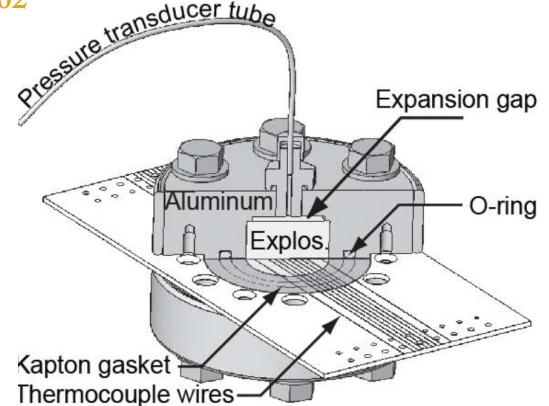
## Problem description

- Heating drives the reaction rate which may or may not run away
- Pressure causes material damage which allows for both pressure relaxation and transport of heat via fluid through the cracks
- Enclosure breach or seal damage allows gas to escape potentially stalling reaction
- Multiphysics coupling:  
mass balance (pressure)  
energy (temperature)  
species transport (concentration)  
peridynamics (displacements)



SITI device

Kaneshige, Renlund,  
Schmidtt, and Erikson,  
2002



ODTX device

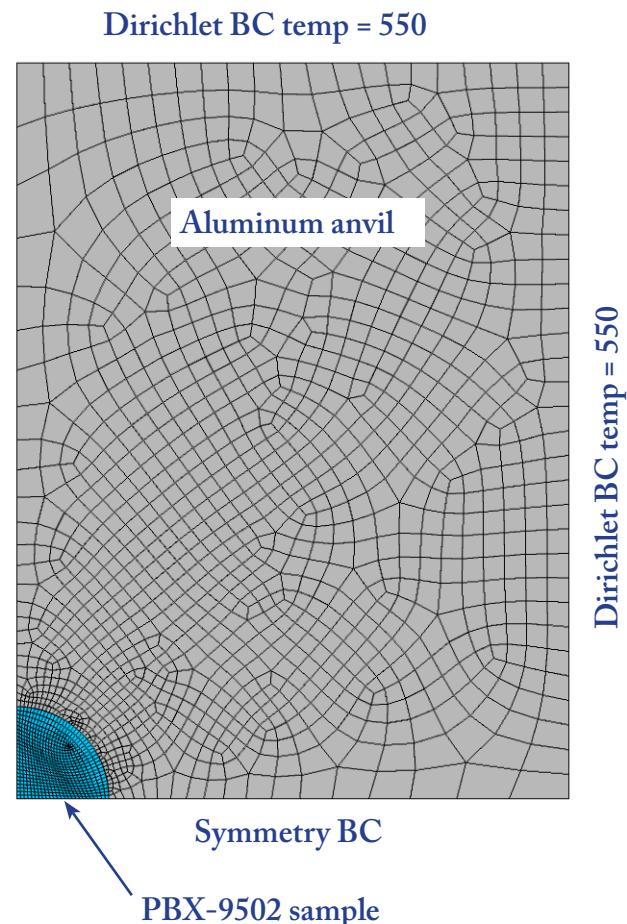
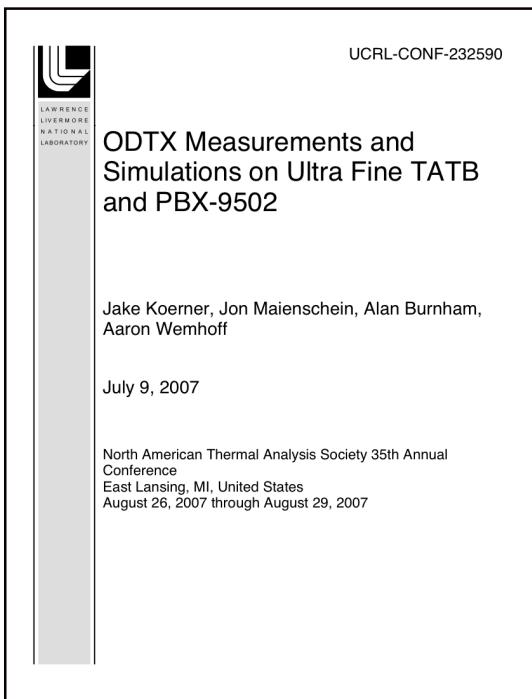
Koerner,  
Maienschein,  
Burnham, and  
Wemhoff, UCRL-  
CONF-232590

# Decomp Model Validation (No Damage)



## ODTX with PBX-9502

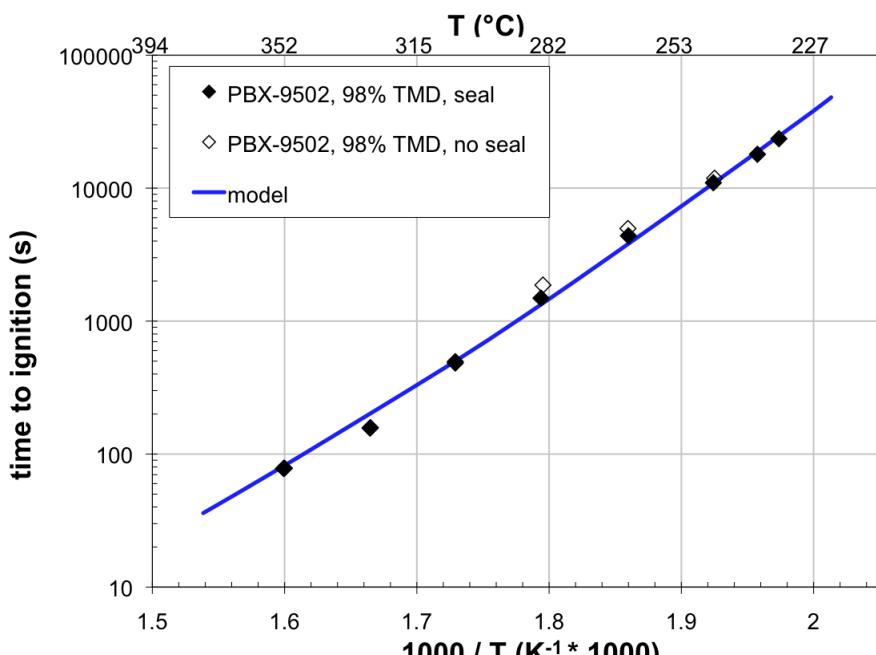
- Vary anvil temperature measure time to ignition
- No pressure dependence
- No damage model
- No enclosure deformation
- Assuming sealed confinement



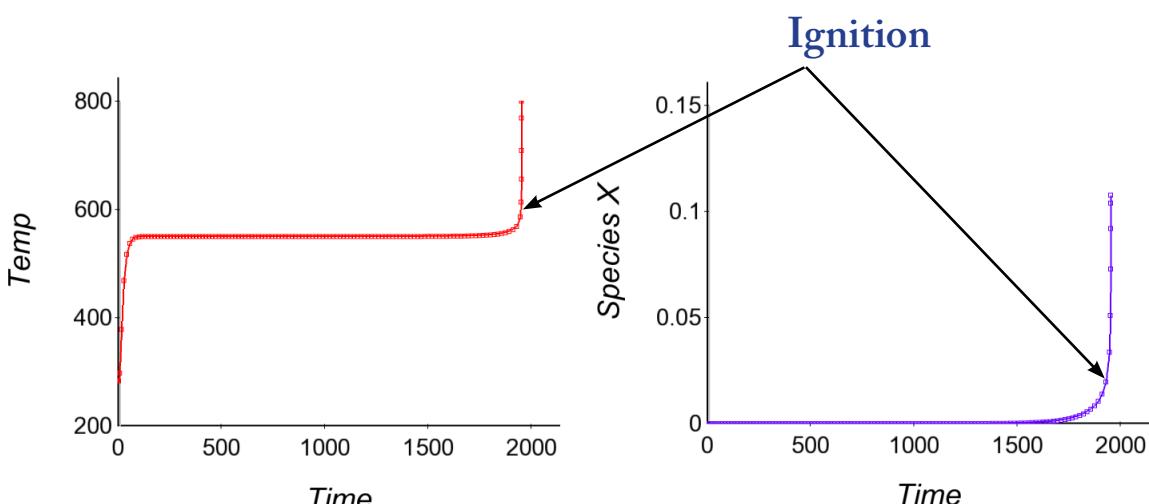
$$S = A \exp \left( -\frac{E}{RT} \right) X^n (1 - wX)^m$$

Reaction rate model for source, S

# Decomp Model Validation (No Damage)



Time to ignition vs. anvil temperature



Temperature vs. time

Species X vs. time

# Permeability Changes Due to Damage



## Unconfined PBX-9501

- Leading prediction is that permeability changes are mainly due to phase change
- Pressure dependent rate model
- Random initialization of bond strength
- Measure average flux/pressure and back calculate the permeability
- Specific permeability  $K/\mu$

Reaction rate model for source,  $S$

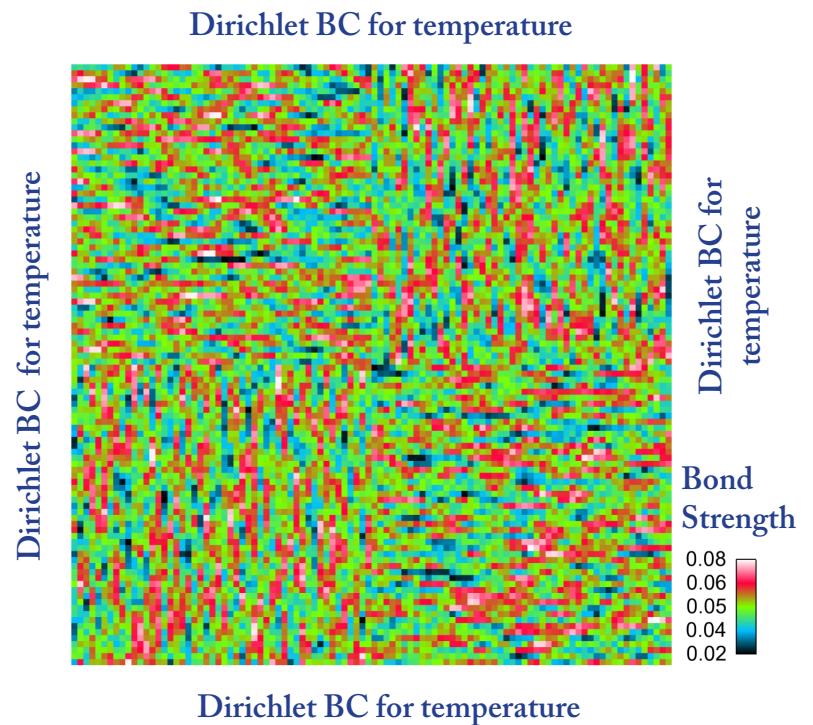
$$S = A \exp \left( -\frac{E}{RT} \right) \left( \frac{p}{p_0} \right)^r X^n (1 - wX)^m$$

Darcy Flow

$$\mathbf{v} = -\frac{K}{\mu} \operatorname{grad}[p]$$

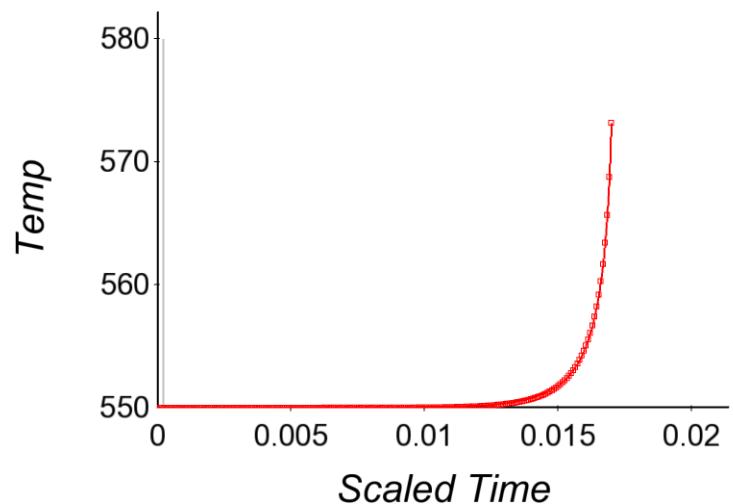
Local permeability model

$$K = f(\text{damage})$$

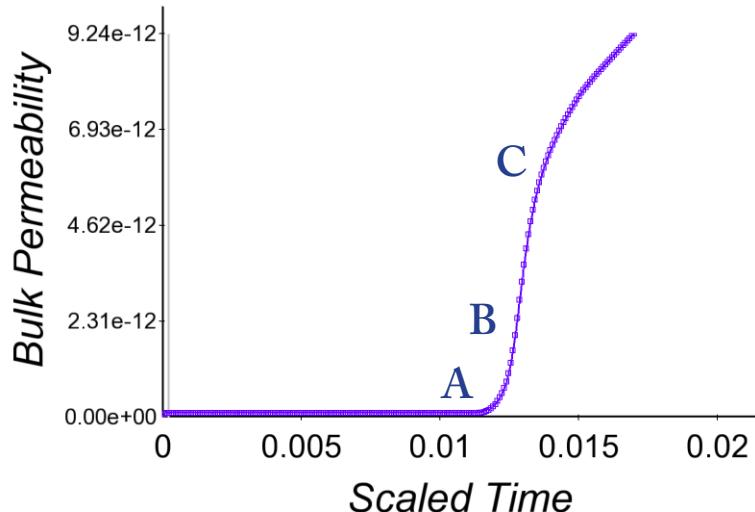
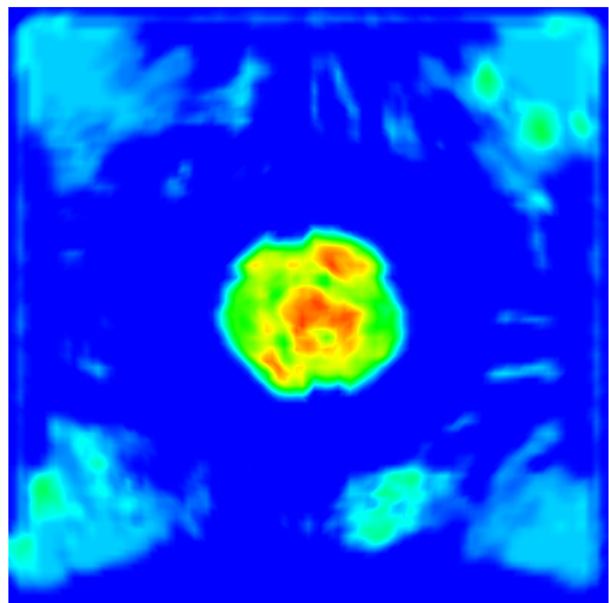


Schematic of unconfined PBX-9501 sample showing random particle bond strength

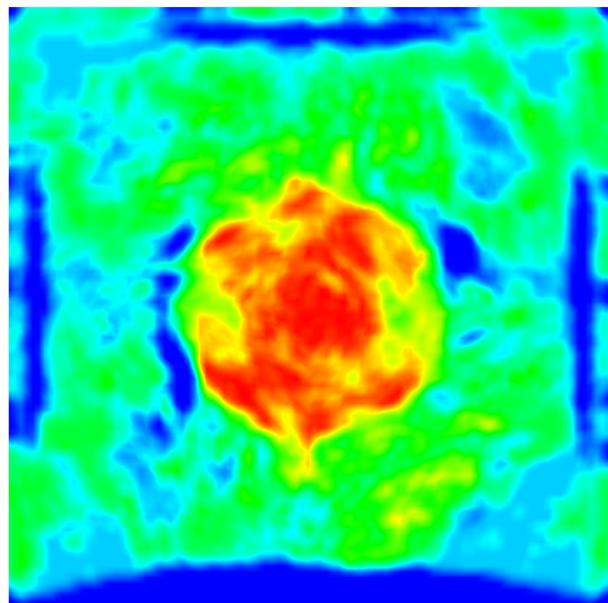
# Permeability Changes Due to Damage



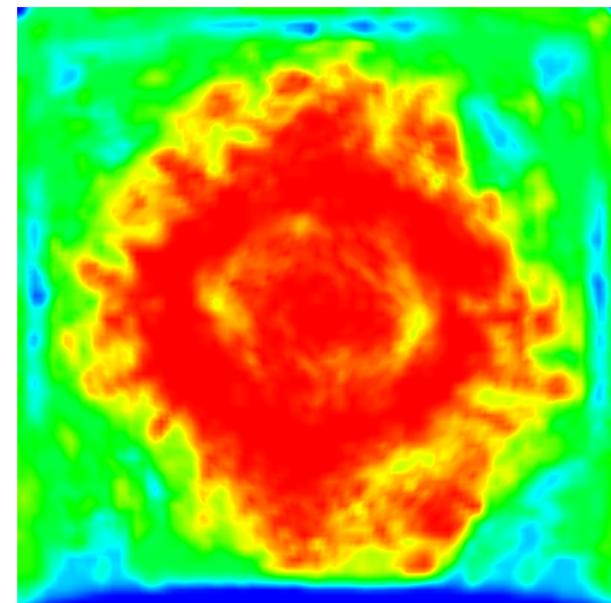
A



B



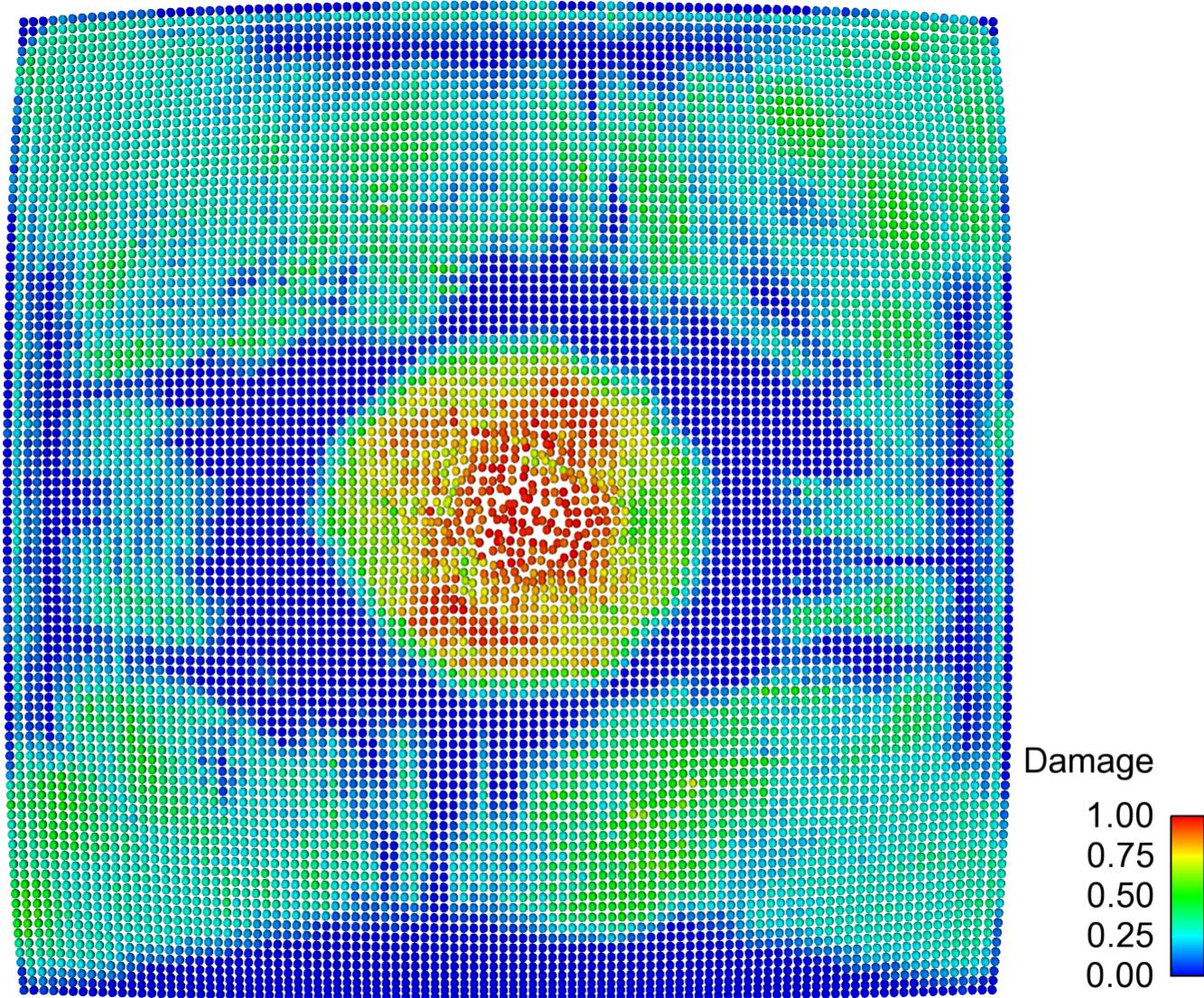
C



1.01e-11  
7.85e-12  
5.59e-12  
3.34e-12  
1.08e-12

Plots of local permeability due to damage  
for various points in time

# Permeability Changes Due to Damage



Deformed configuration of PBX-9501 sample  
immediately prior to ignition (point B)



## Stalling ignition

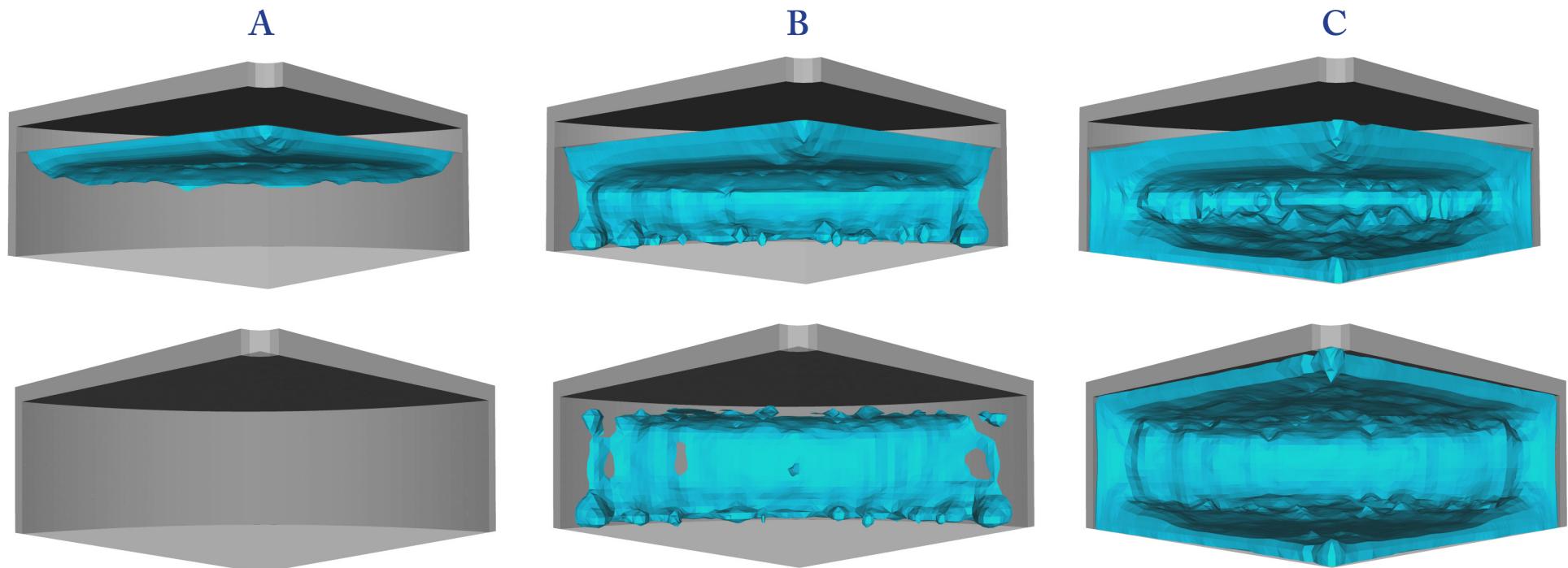
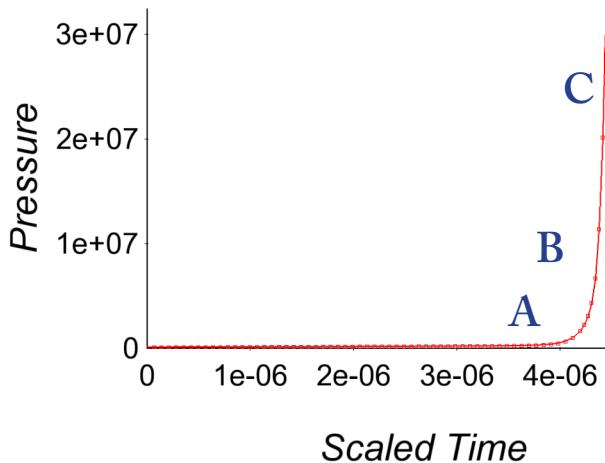
- For certain cases an explosion may or may not occur depending on the integrity of the confinement
- If reaction gases escape during heating, the confinement may depressurize leading to slower reaction rates

# Damage Evolution Characteristics



## Damage evolution characteristics

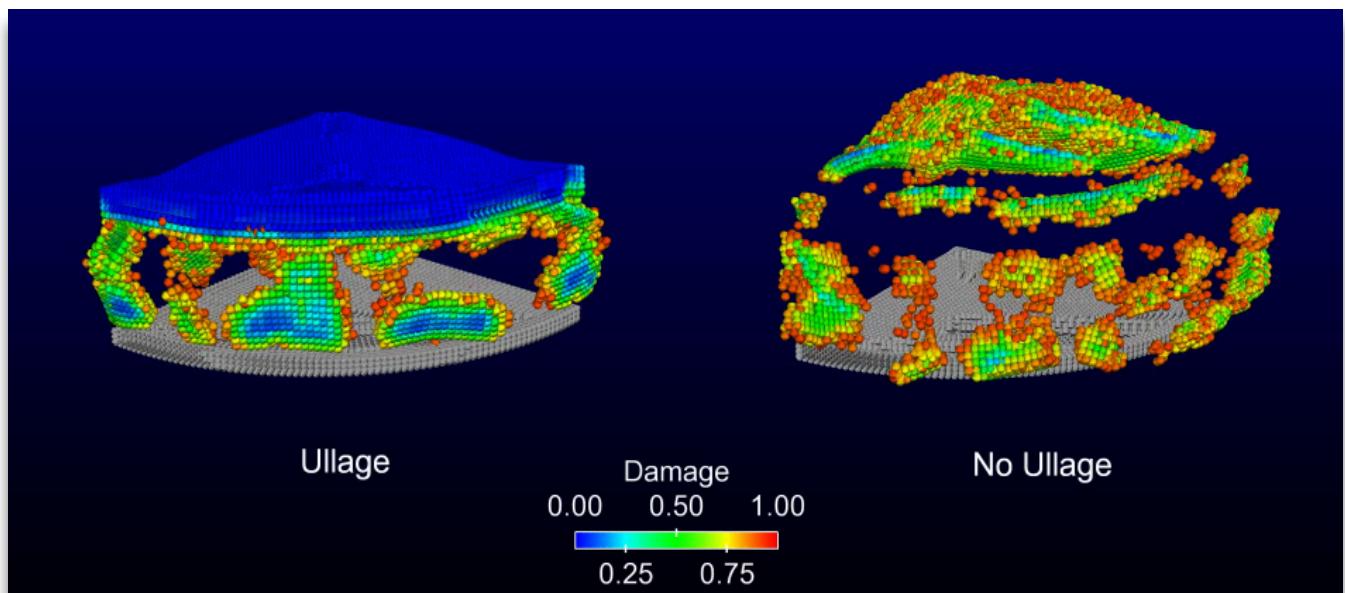
- How does the material decompose inside the confinement at ignition?
- How does damage propagate inside the energetic material?



Isosurface of damage in (top) confinement with ullage  
(bottom) confinement with no ullage  
at various times during ignition

## Fragmentation and projectile energy

- How does ullage in the confinement affect the resulting fragmentation?
- For a given scenario, how large will the fragments be and with how much energy will they project?





## Overview of numerical approach

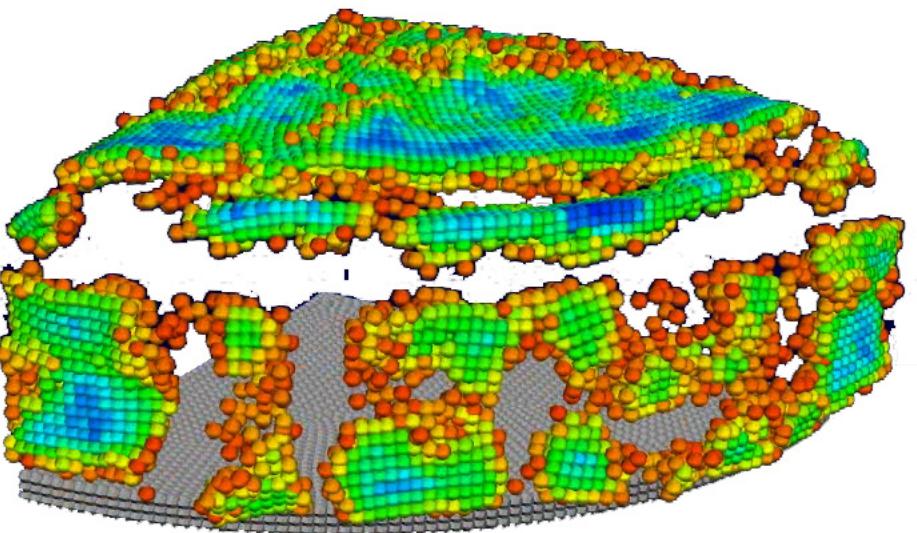
- Pore pressure / effective stress addition to peridynamics
- Modified permeability based on peridynamics damage criteria

## Problems of interest

- Enclosure breach
- Permeability changes due to damage
- Fragmentation of confinement

## Future work

- Experimental validation
- Model development
- Justification for peridynamics effective stress from first principles



Fragmentation pattern for simple confinement at ignition

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