



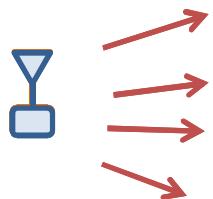
# Spatial focusing and nulling of RF signals using time-reversal

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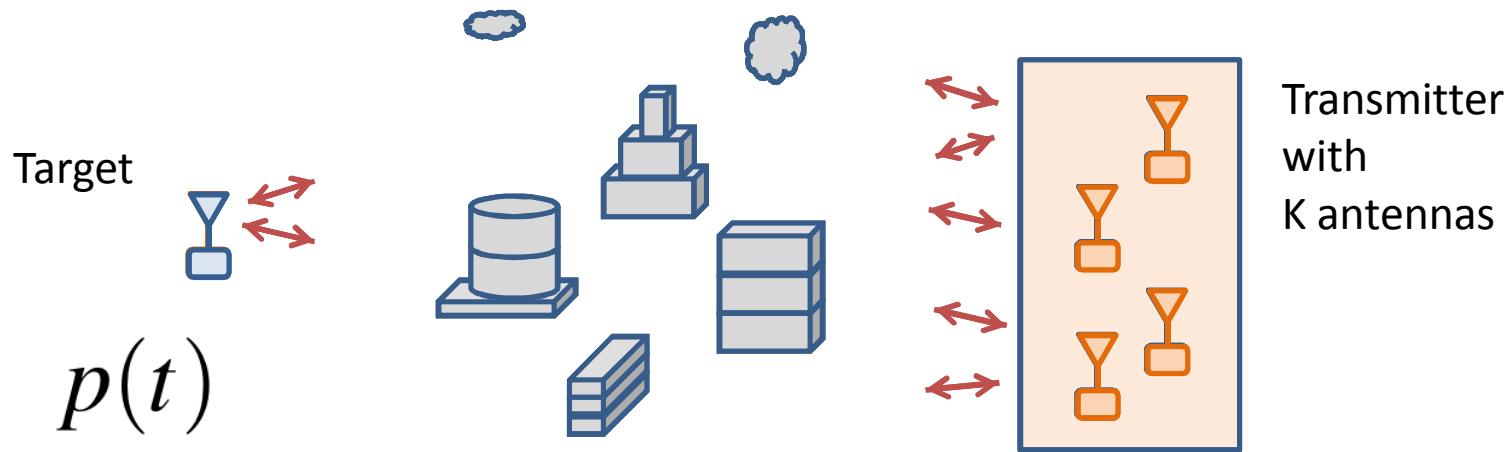
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# Time-Reversal ?

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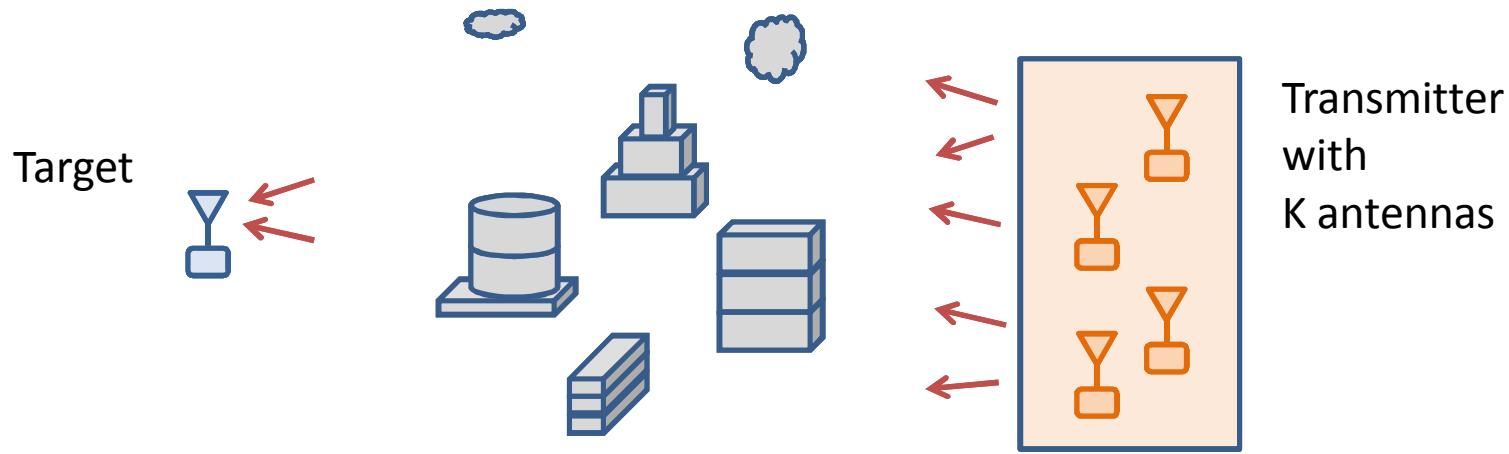


# Application



$$\mathbf{y}(t) = p(t) * \mathbf{h}_m(t)$$

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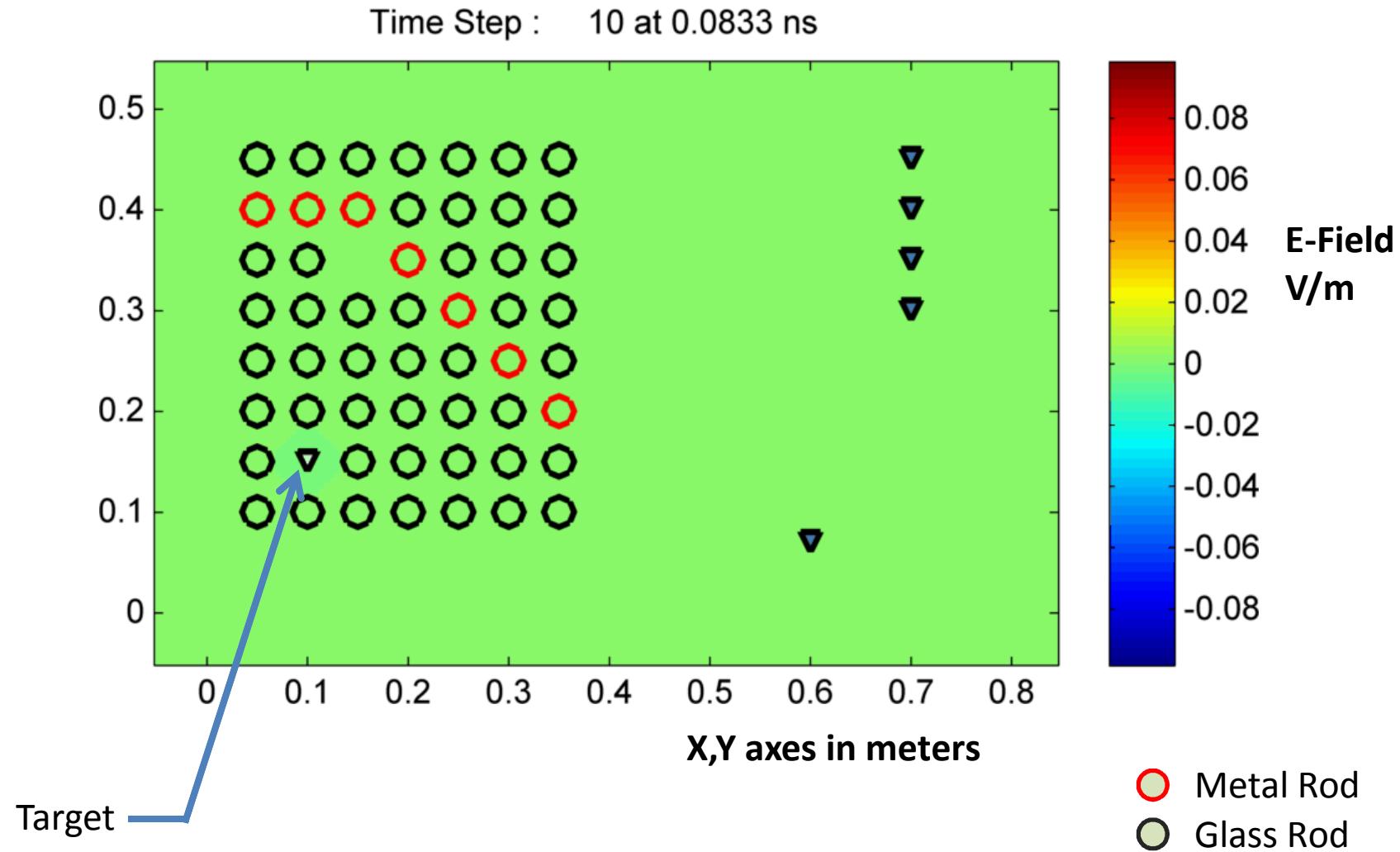


$$z(t) = \sum^K \mathbf{y}_{tr}(t) * \mathbf{h}_m(t)$$

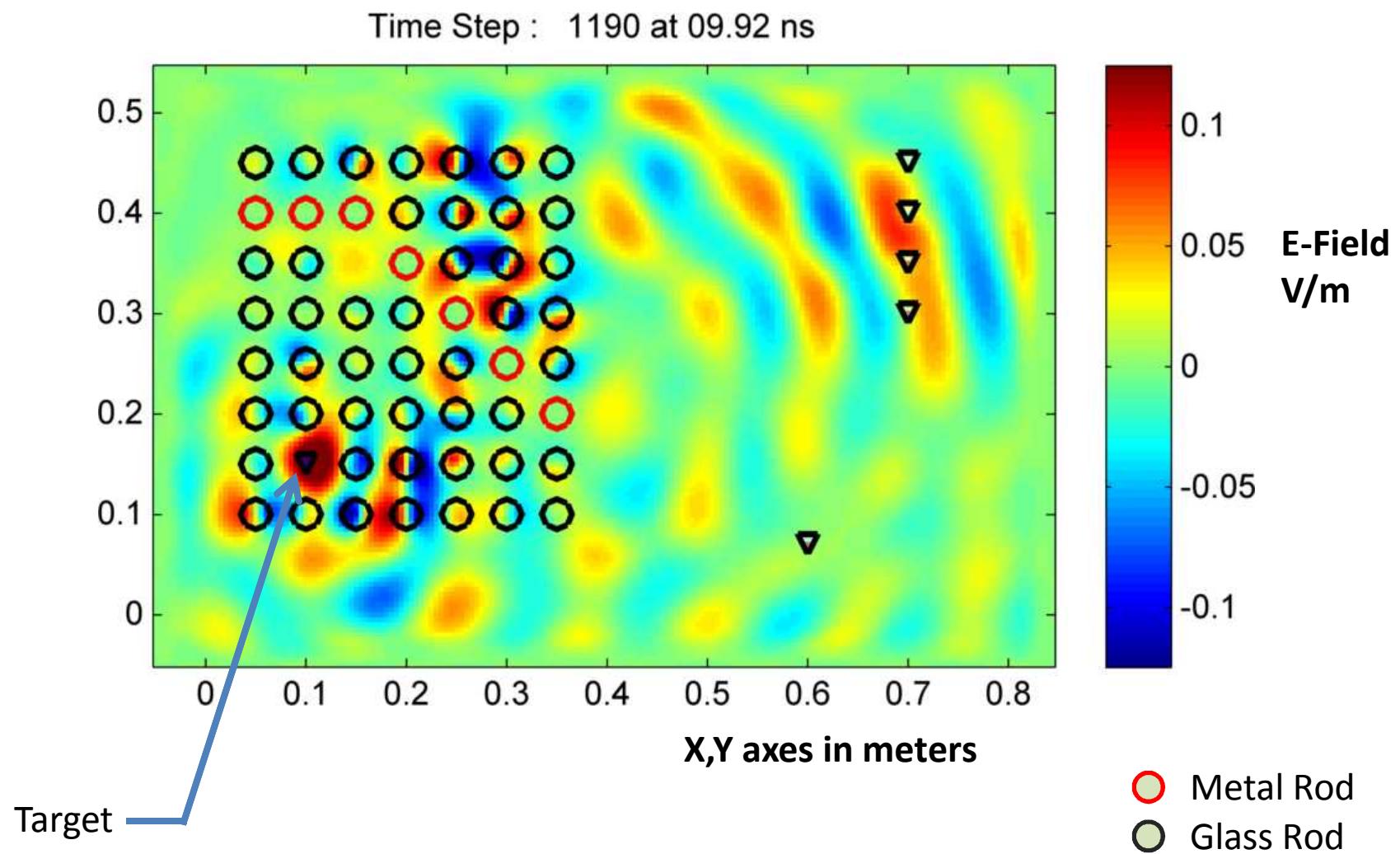
$$z(t) = \sum^K p(-t) * \mathbf{h}_m(-t) * \mathbf{h}_m(t)$$

# **Convergence in Time and in Space**

# Illustration



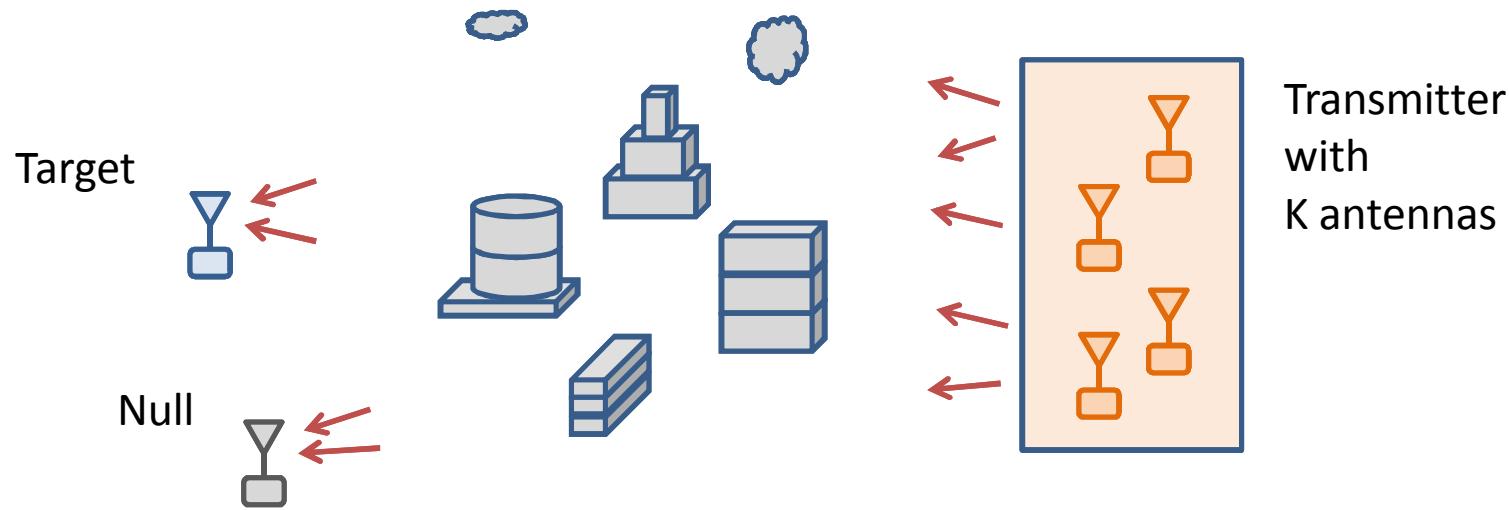
# Illustration



# Why?

- Focus in space
- Works without line-of-sight
- Receiver location can be unknown
- Multipath is not a problem

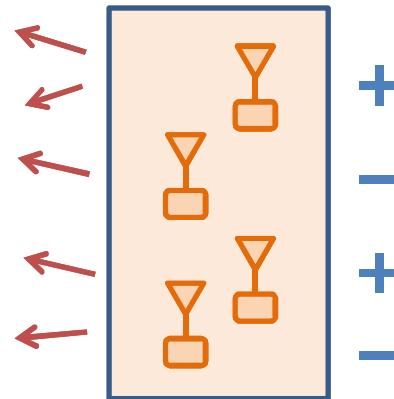
# Focus at A, Null at B



- Decrease co-channel interference to other users

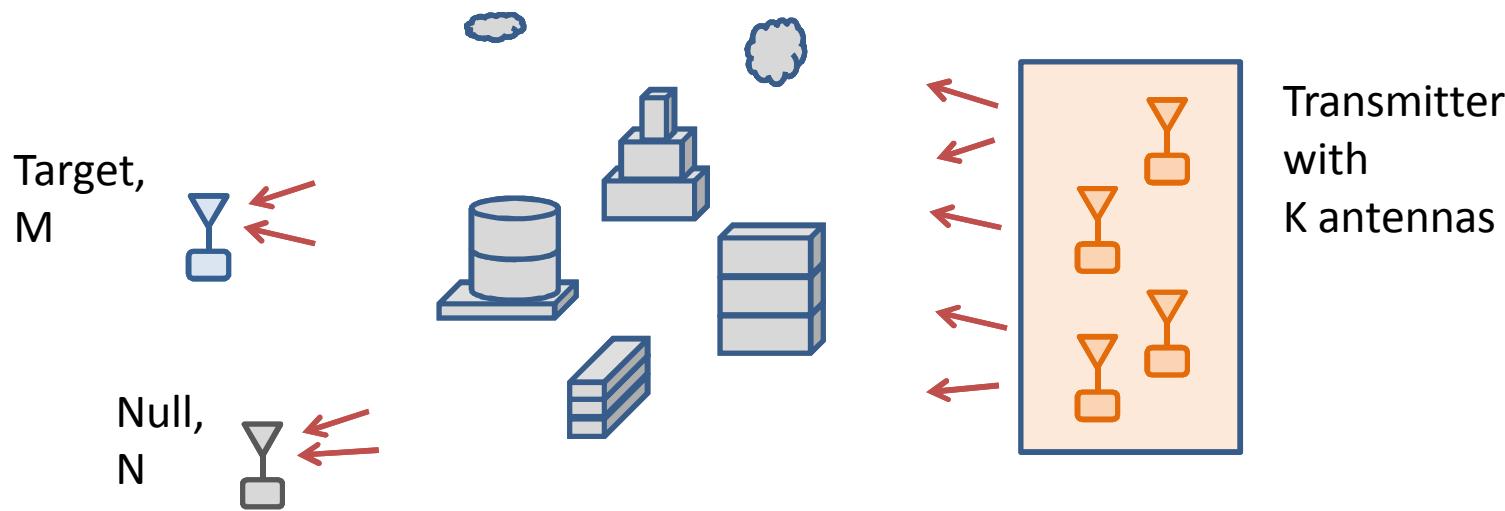
# Prior approaches

## 1. Heuristic



## 2. Optimal: Complicated and requires knowledge of the channel to the null location

# This work: simplified focus and null



Transmit beam-forming filter,  $\mathbf{g}(\omega) = \gamma \begin{bmatrix} \frac{h_{m,1}^*(\omega)}{\|h_{n,1}(\omega)\|^2} \\ \frac{h_{m,2}^*(\omega)}{\|h_{n,2}(\omega)\|^2} \\ \vdots \\ \frac{h_{m,K}^*(\omega)}{\|h_{n,K}(\omega)\|^2} \end{bmatrix}$

# This work: simplified focus and null

- Does not need full channel to the null location.  
Only needs PSD (easily measured without cooperation).

$$\text{Transmit beam-forming filter, } \mathbf{g}(\omega) = \gamma \begin{bmatrix} \frac{h_{m,1}^*(\omega)}{\|h_{n,1}(\omega)\|^2} \\ \frac{h_{m,2}^*(\omega)}{\|h_{n,2}(\omega)\|^2} \\ \vdots \\ \frac{h_{m,K}^*(\omega)}{\|h_{n,K}(\omega)\|^2} \end{bmatrix}$$

# Evaluation by simulation

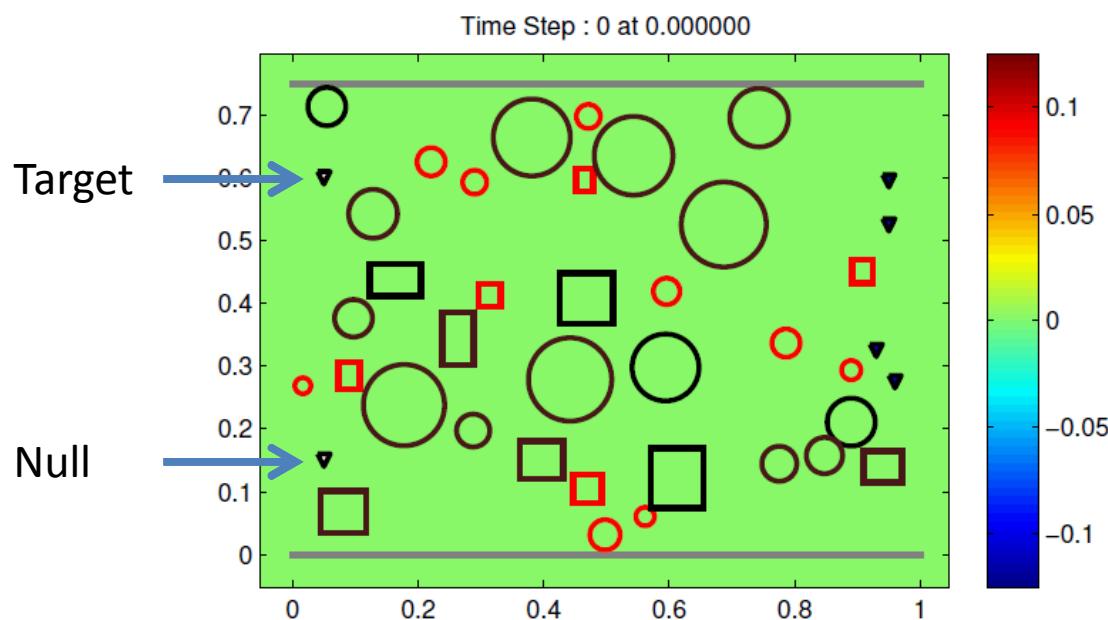
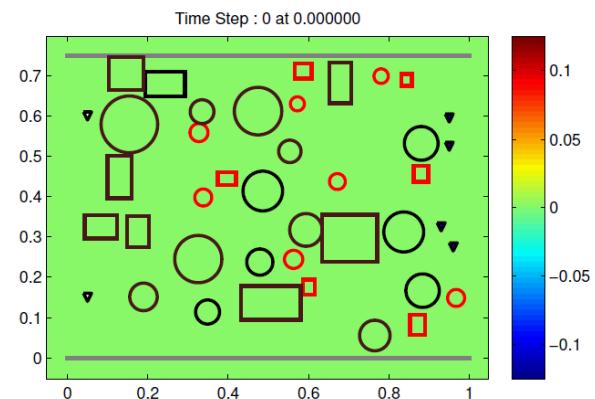
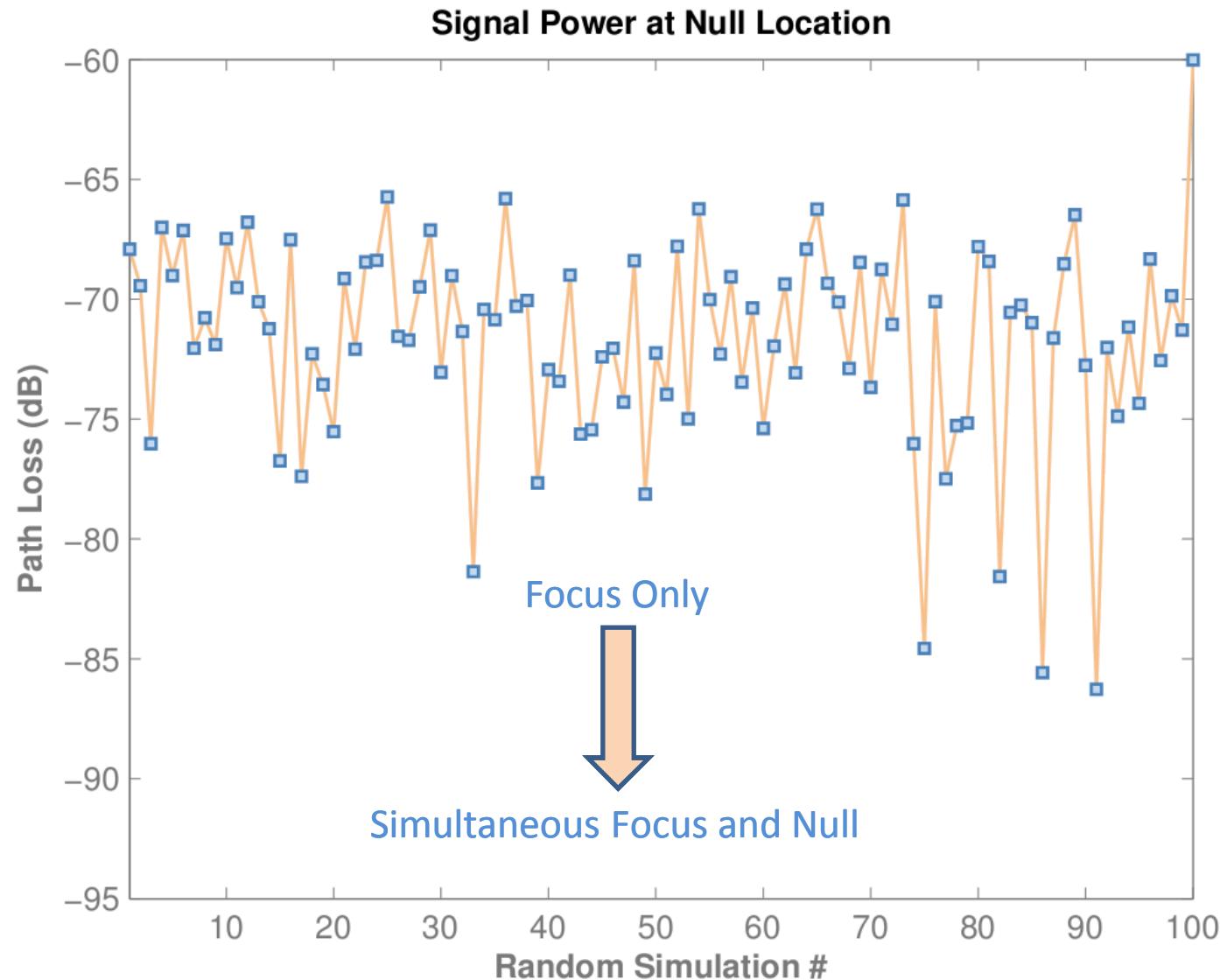


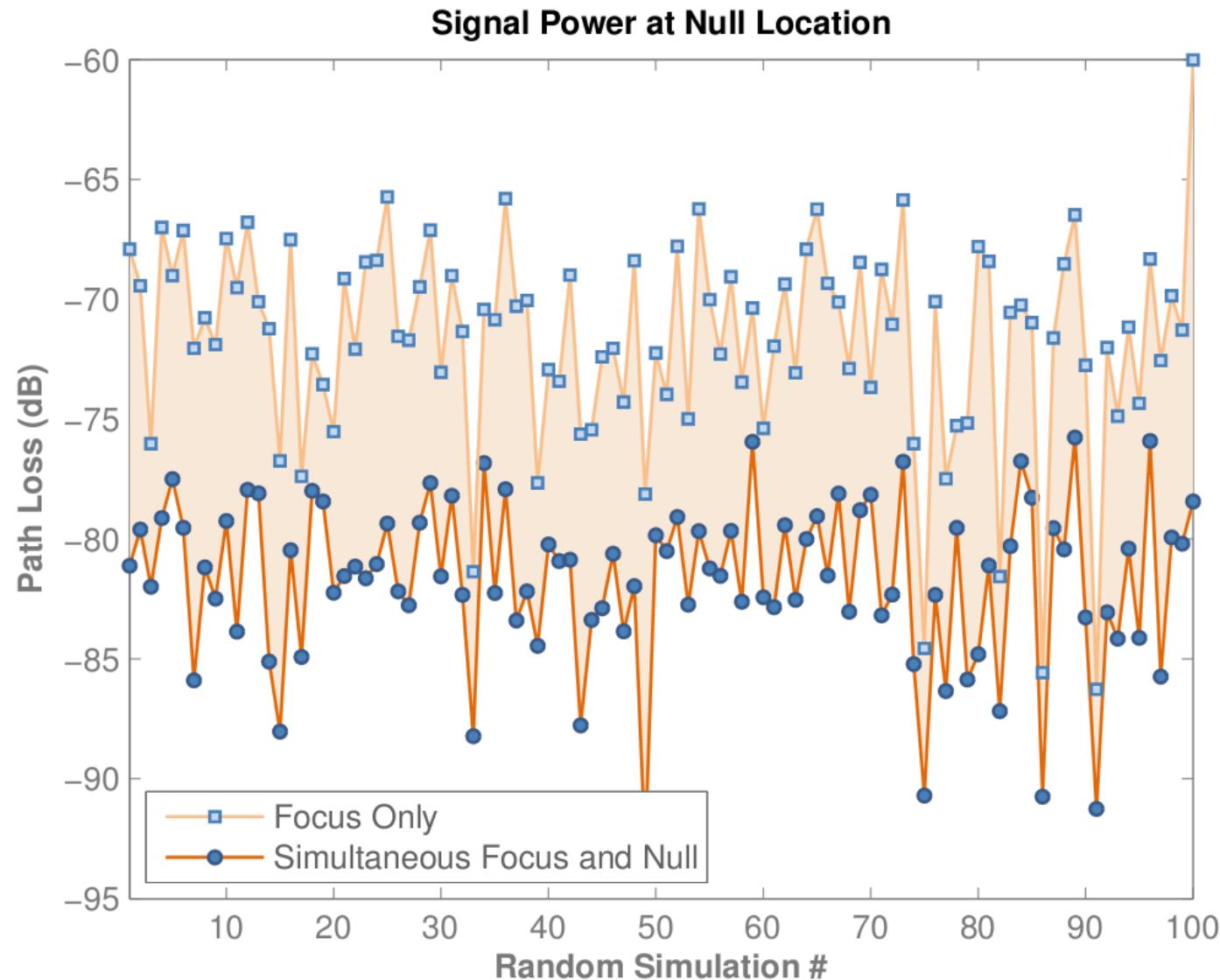
Fig. 5. Randomly created scenario for time-reversal processing.  $f_c = 3$  GHz, BW = 500 MHz. Black objects are glass columns, Brown objects are wooden columns, Red objects are metal pipes. All axes are in meters.



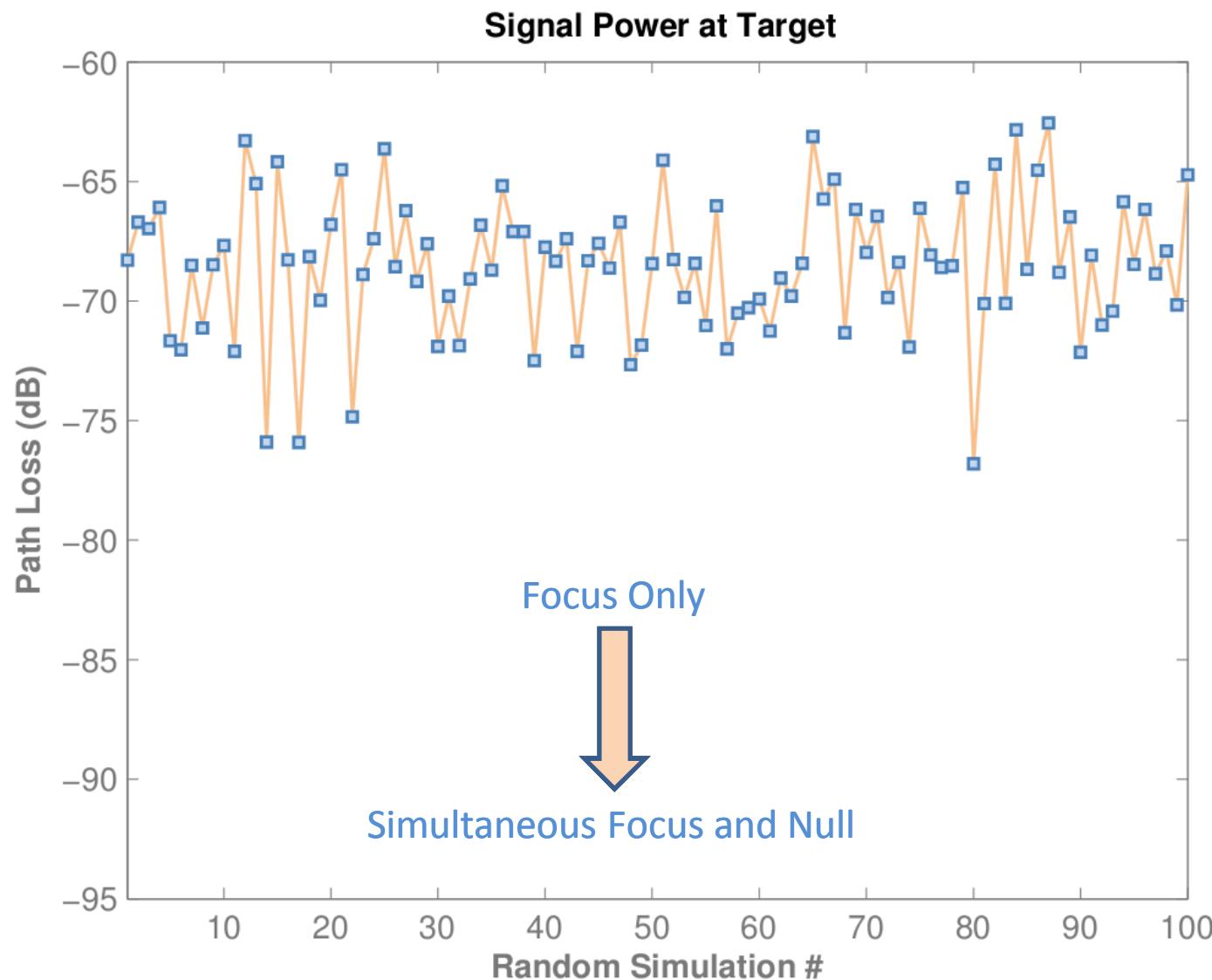
# Nulling



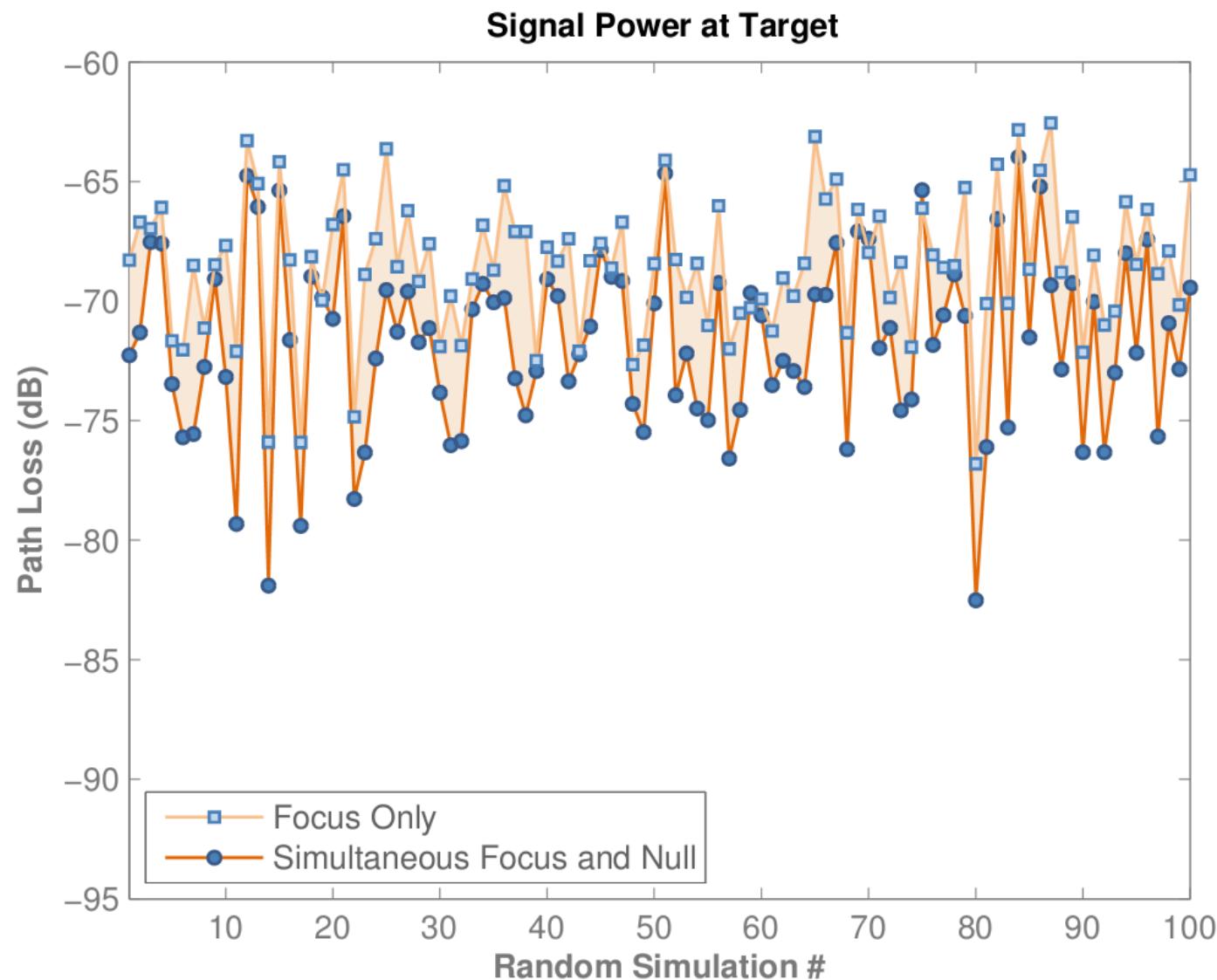
# Nulling



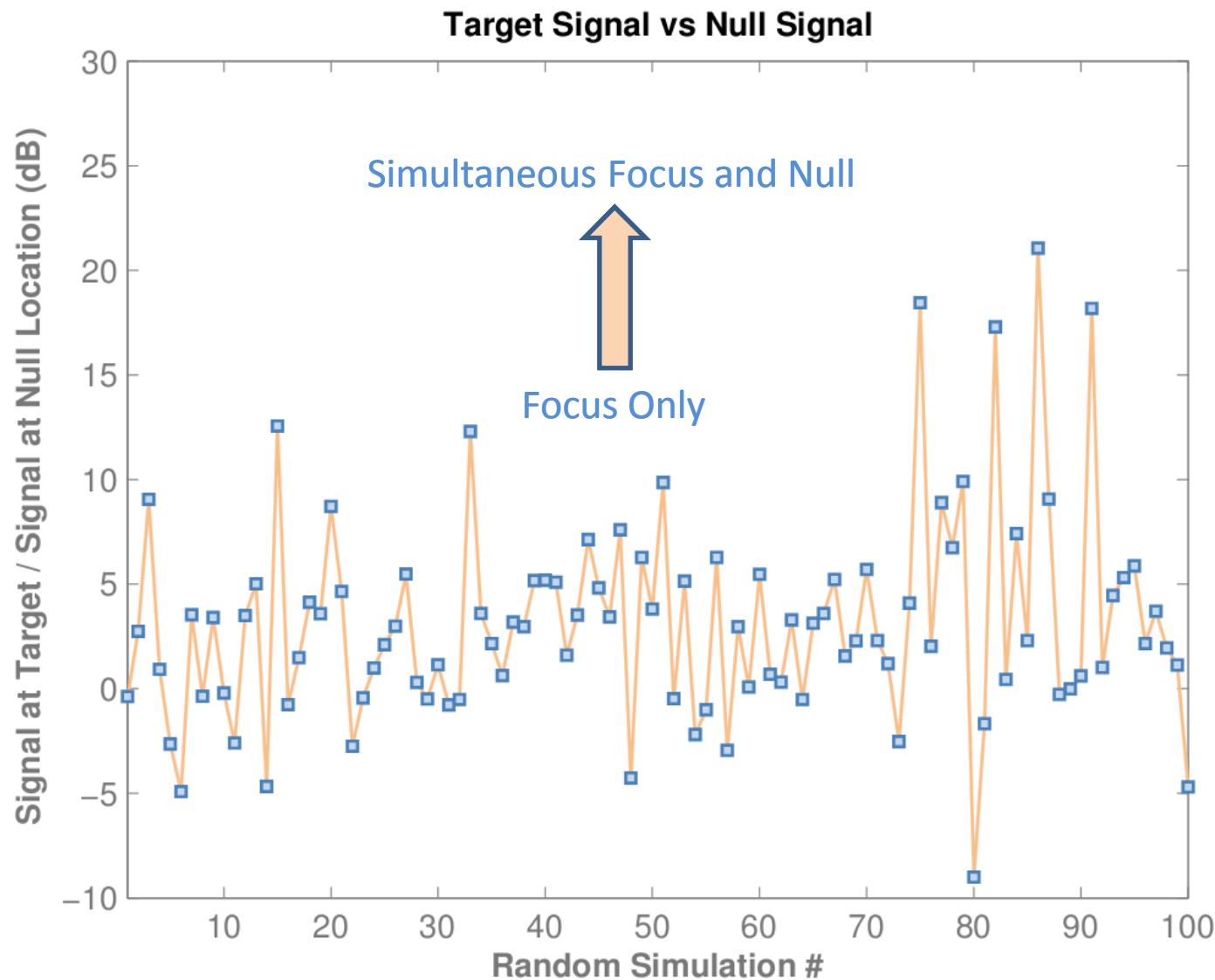
# Cost



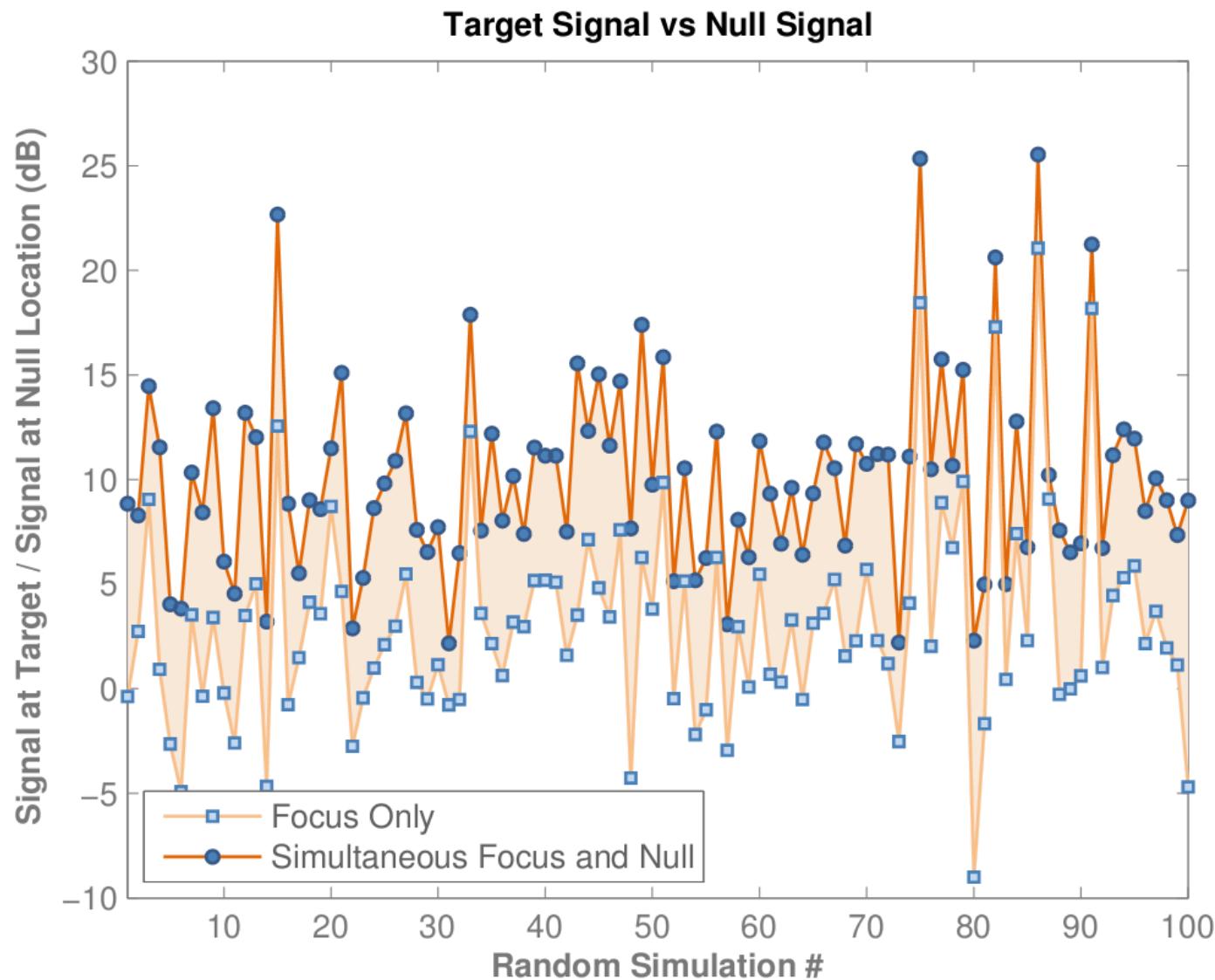
# Cost



# Target/Null



# Target/Null



# Experimental Results

# Summary

- Radio signals can be focused at one location and nulled at a different location using time-reversal.
  - Does not need knowledge of detailed channel to null location.
- Other effects
  - number of antennas
  - bandwidth