

Modeling experiments on Z where chemistry matters: polymers, CO₂, and explosives

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and D. G. Flicker



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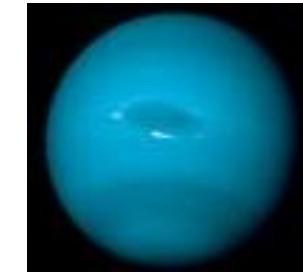


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Properties of light elements in the Mbar regime are important for several reasons

- **Planetary science – Uranus & Neptune and exo ice-giants**

- High-pressure mixtures of H, He, C, O, N

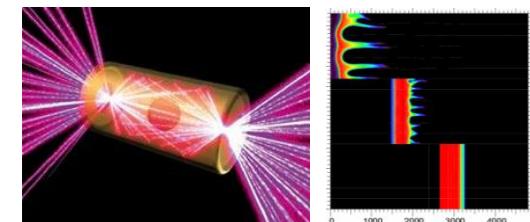


- **Planetary science – earths and super-earths**

- Equation of state of Fe and subducted CO₂
 - Mbar, 1000 – 4000 K

- **Inertial confinement fusion (ICF) materials**

- Fundamental behavior of carbon and carbon compounds
 - Mbar, +10 000 K



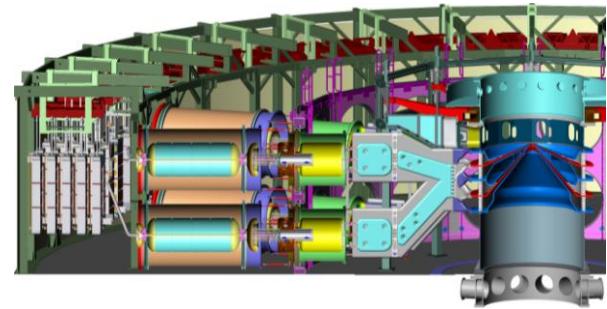
- **Chemistry at high pressure and temperature**

- Reactions driven by pressure and temperature
 - Composition under shock compression
 - Complex Hugoniot – flat sections

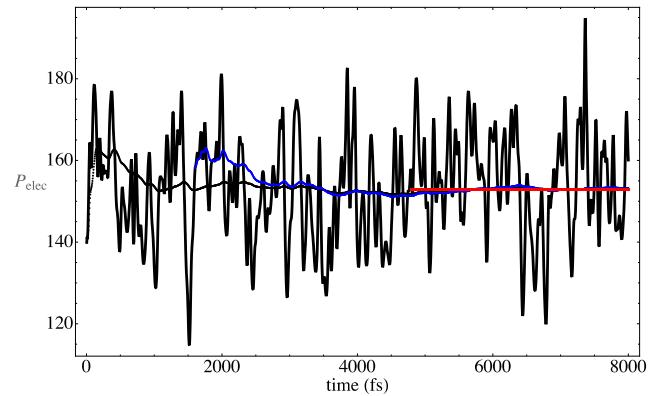
Ice giants: C-H-N-O mixtures at Mbar

Overview of systems with chemistry: first-principles simulations and Z experiments

- CO₂
 - Liquid initial state – to 5 Mbar with high precision
- Hydrocarbons
 - Polymethyl pentene (PMP/TPX)
 - Polyethylene, Polystyrene
 - Liquid ethane
 - *See poster yesterday by Kyle Cochrane*
- High explosives
 - Initial results on PETN
 - *See poster yesterday by Ryan Wixom*
- Chemistry at high pressure and temperature
 - Reactions driven by pressure and temperature
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Shock experiments on Sandia's Z machine

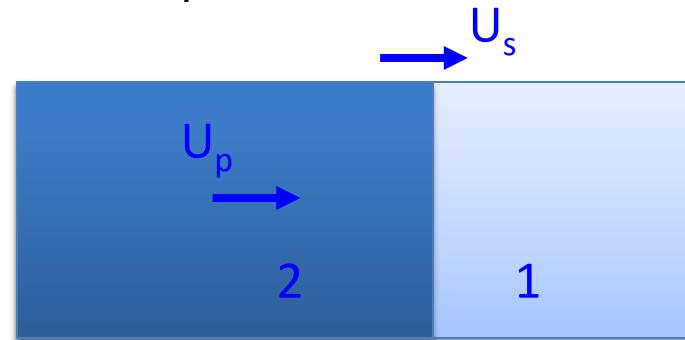


Density Functional Theory simulations

We reach Mbar pressures in liquids and solids by executing flyer-plate impact experiments

- **Advantages of liquid and transparent solids**
 - Uniform sample
 - Initial state EOS well-defined
 - Reproducible state
 - Reflective shock fronts allow very high precision measurements
 - 30 km/s impact velocities
- **Straightforward to analyze**
 - Conservation of mass, momentum, and energy
 - Rankine-Hugoniot relation

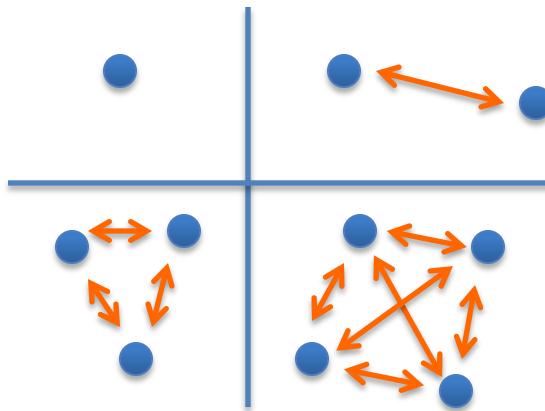
Steady shock wave in matter



$$2(E_2 - E_1) = (P_2 + P_1)(U_1 - U_2)$$

With high accuracy measure and/ or calculate thermo-physical properties

Density functional theory (DFT) based MD is an established approach - HEDP sets additional demands



Treating quantum many-body interactions between electrons correctly is very demanding



Large-scale simulations on supercomputers like cielo and Red Sky

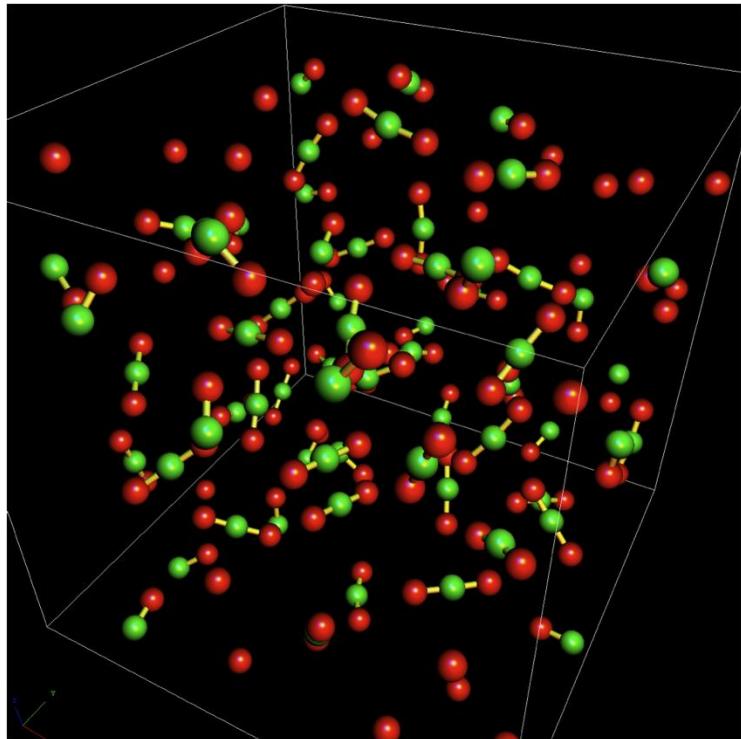
DFT calculations can be predictive

- *Accuracy* set by the exchange-correlation (xc) functional:
- *Convergence* of simulation parameters to desired precision
- W. Kohn won the 1998 Nobel prize in chemistry

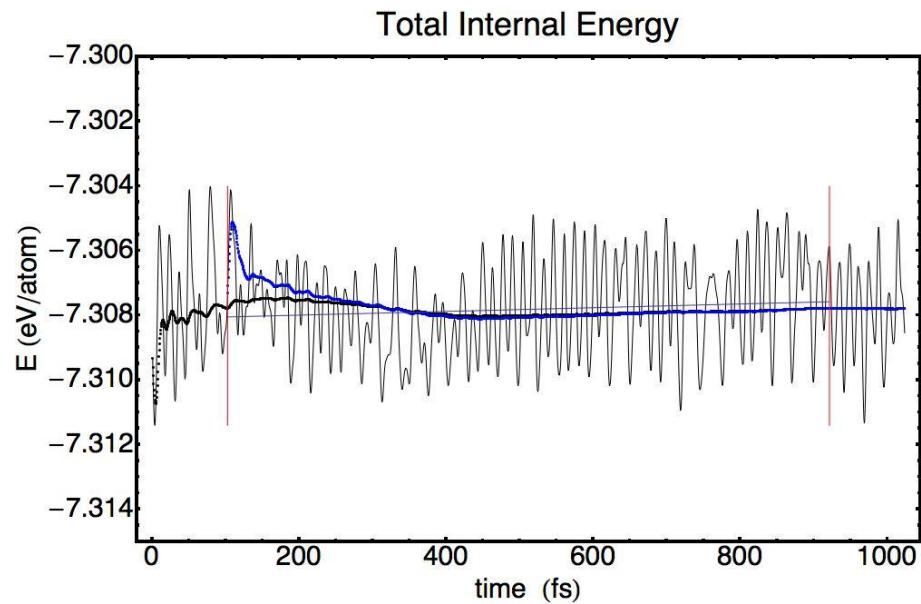
VASP code (Georg Kresse, Vienna, Austria)

- Finite-temperature DFT (Mermin)
- Plane-wave basis-set for controlled convergence and free electrons/ionization
- Projector augmented wave core functions (PAW)
- *First-principles thermodynamics – long simulations yield $P(\rho, T)$, $E(\rho, T)$, structure, diffusivity, etc.*

First-principles thermodynamics: gaining insights into the behavior of matter starting from quantum mechanics



Simulation of CO_2 :
64 molecules
one complex k-point
high plane-wave cutoff energy

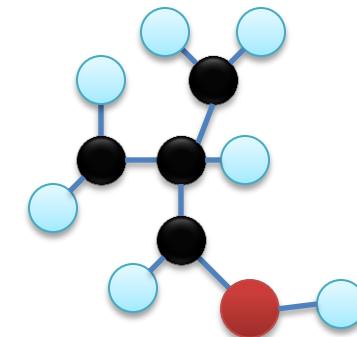
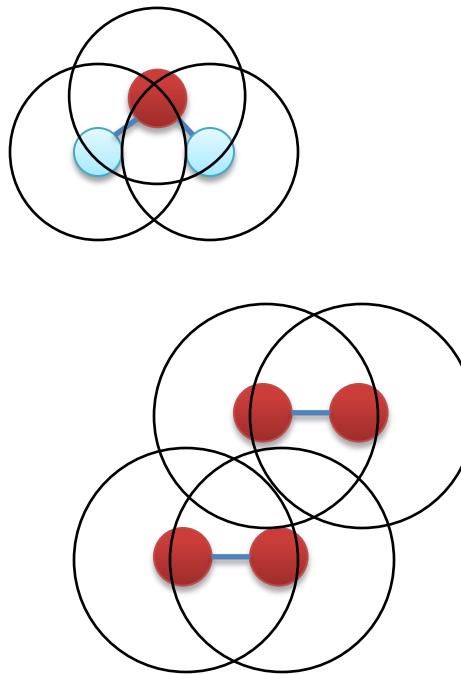


*Time averaging over long
equilibrated run – the figure shows
the last ps of a longer simulation*

Note the fine energy scale

We also analyze the chemical composition in the cell

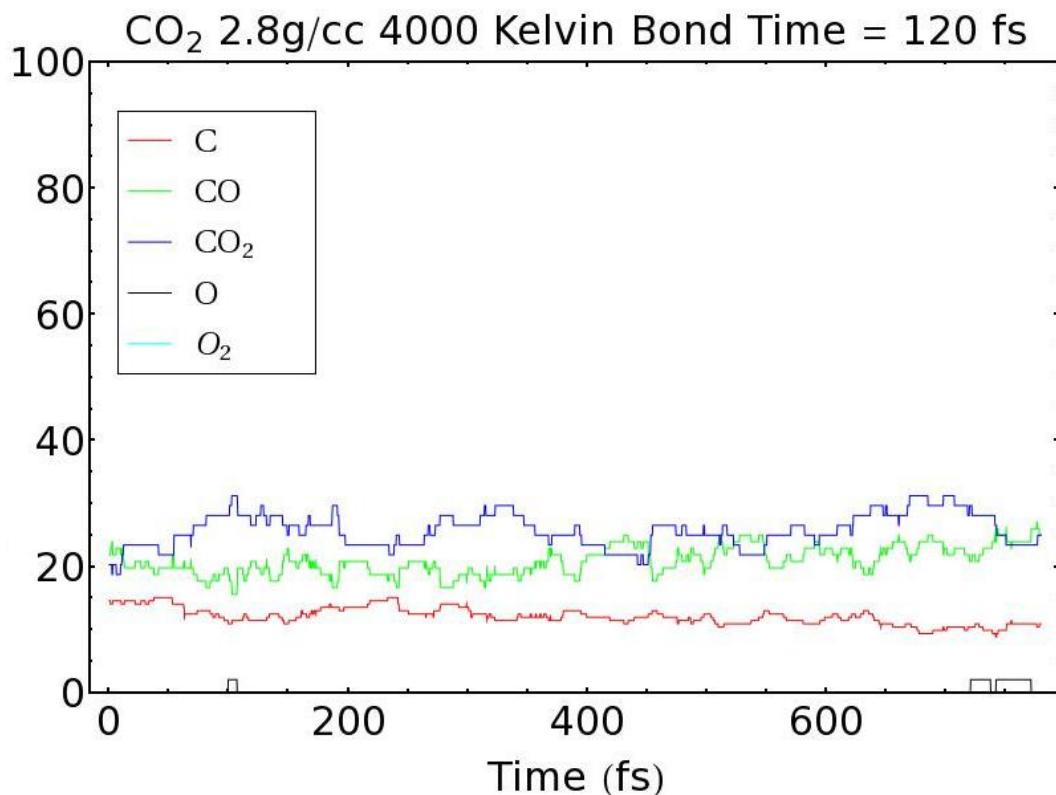
- **Bond-distances between atoms**
 - C-C, C-O, O-O
 - Distances from analyzing pair correlation functions
- **Bond Time**
 - Remain bonded over several vibration times – verify using different times
- **Molecule accounting**
 - Identify molecules
 - O_2 is easy
 - Branching
 - Rings
 - Use a recursive algorithm
 - Tracking in time



Identifying molecules, including branching and rings, using a recursive algorithm

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Chemical composition during the last 800 fs of a simulation

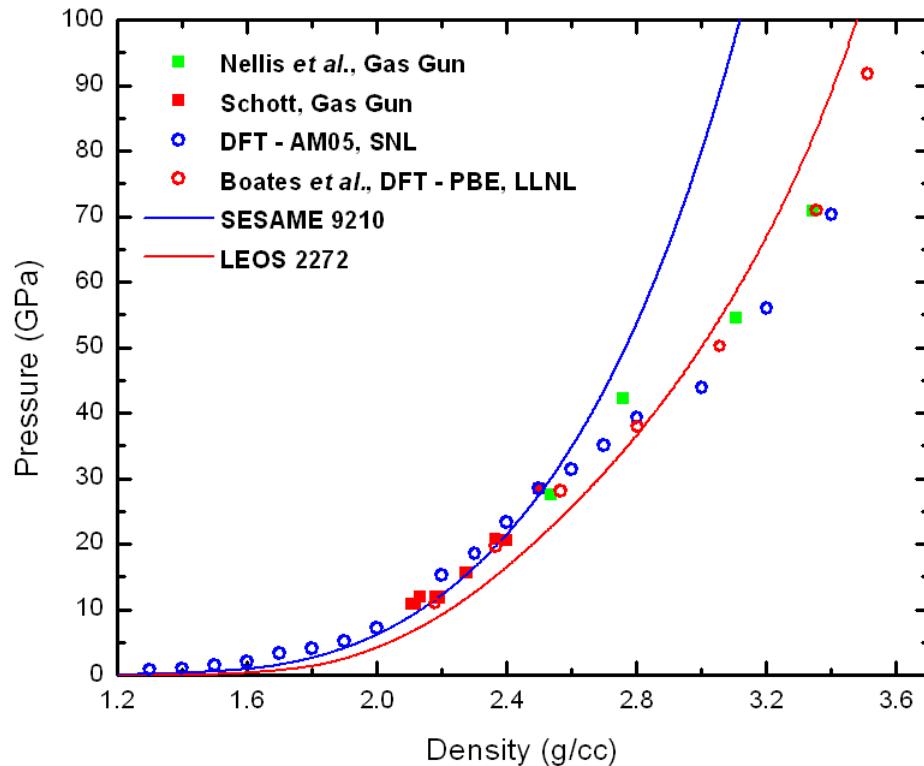
DFT calculations on CO₂ are in agreement with available experimental data and predictions up to 100 GPa

- **DFT simulations**

- Quantitative and qualitative agreement with Schott (High Press. Res. 6, 187 (1991)) and Nellis et al (J. Chem. Phys. 95, 5268 (1991)).
- Minor difference between PBE and AM05 exchange-correlation functionals
- Existing EOSs do not capture the full behavior

- **Behavior above 100 GPa**

- Relatively steep raise in pressure beyond 3-fold compression
- We confirm very recent DFT results by Boates et al. (J. Chem. Phys. 134, 064504 (2011))



Excellent agreement between results from DFT/QMD and low-pressure gas-gun data

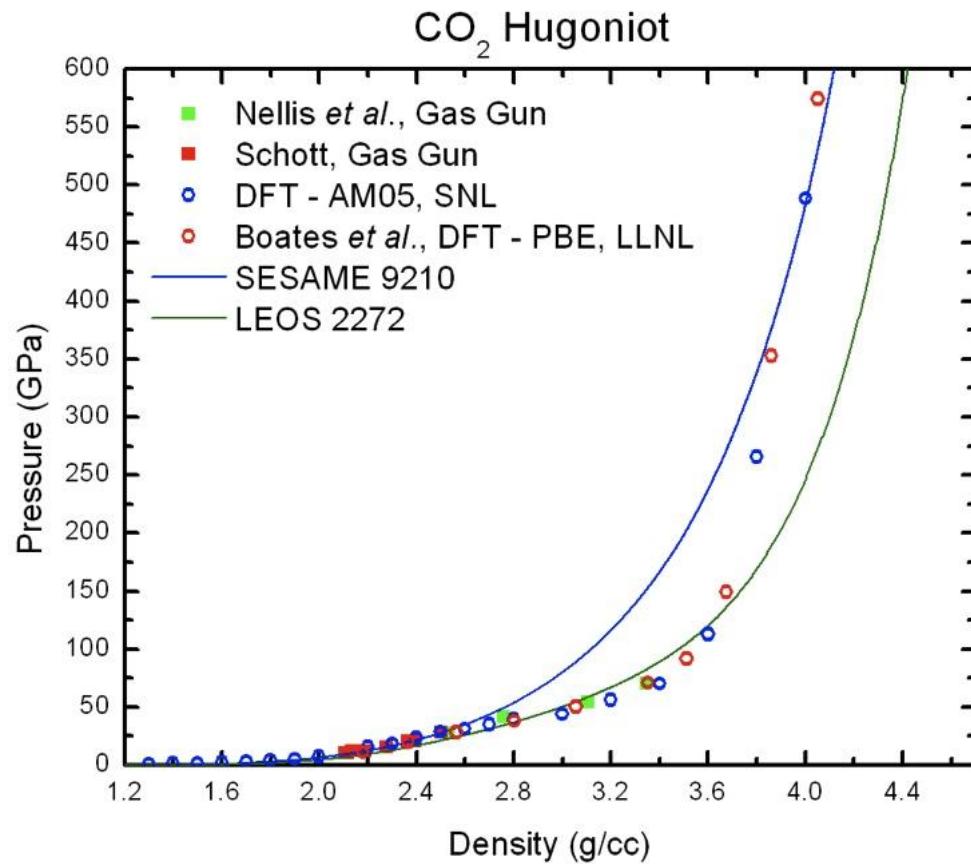
DFT calculations made predictions above 100 GPa – very steep Hugoniot towards 4 g/cm³

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We expect a steep rise in shock pressure towards four-fold compression

We reach Mbars in CO₂ by starting from the liquid phase: it requires an experimental cell under pressure

- **Advantages of liquid**

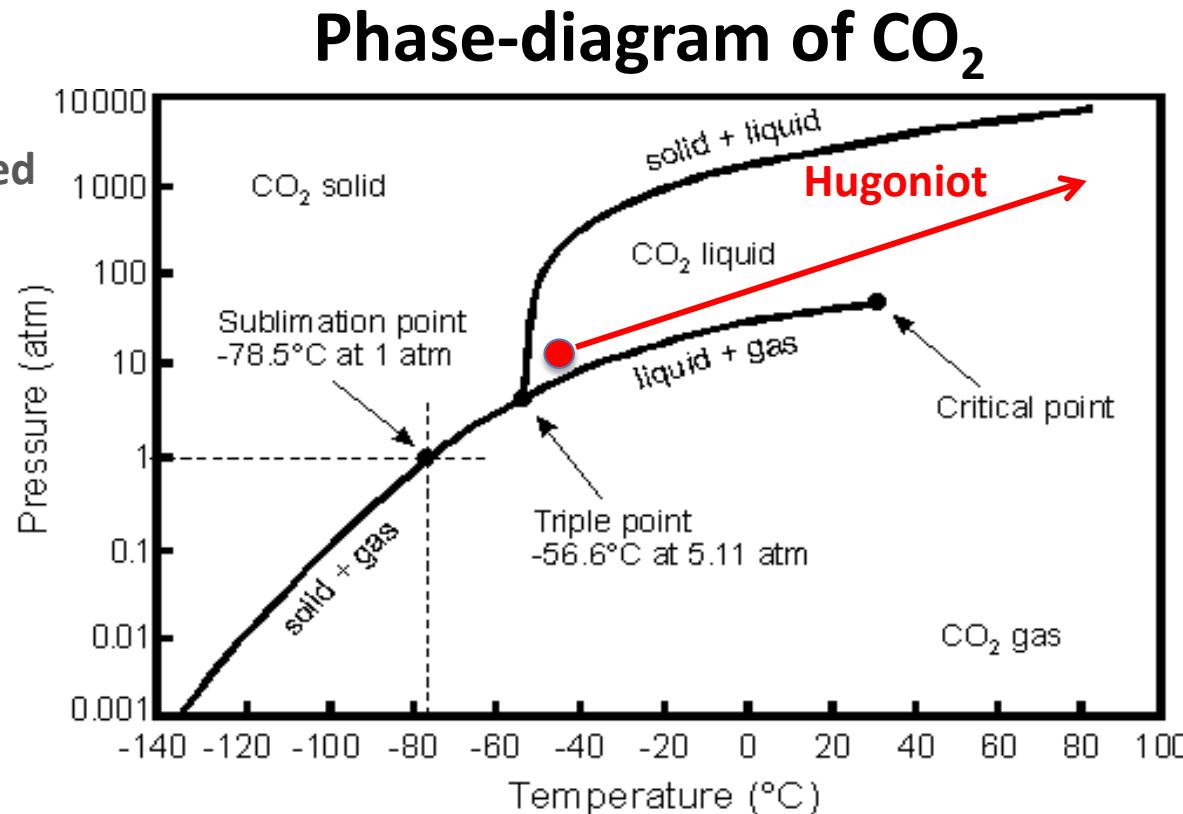
- Uniform sample
- Initial state EOS well-defined
- Reproducible state

- **Phase-diagram of CO₂**

- Sublimation at 1 atm

- **Initial state in liquid**

- 9 bar/ 900 kPa
- 1.173 g/cm³
- 220 K



The initial state for experiments on Z was a liquid close to the triple points

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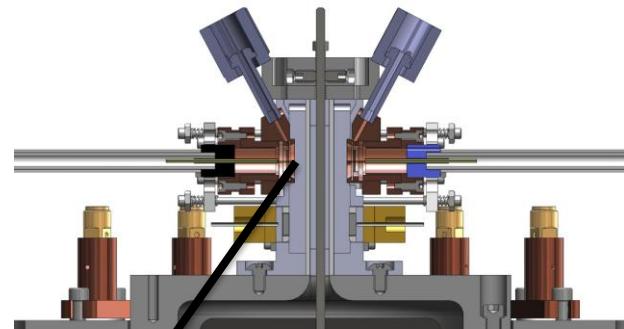
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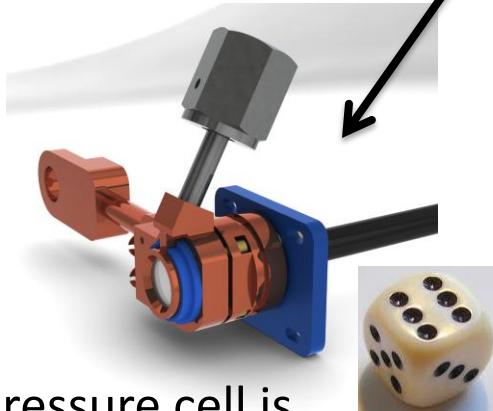
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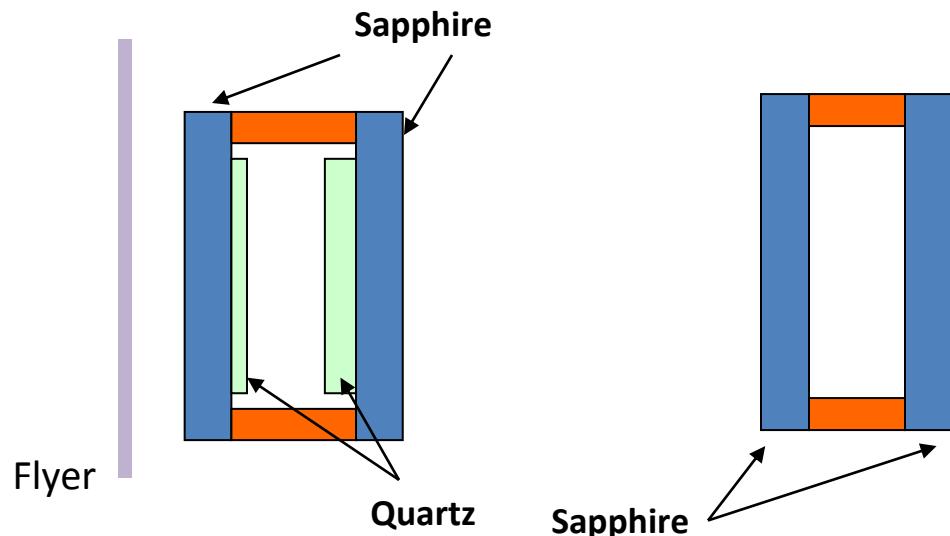
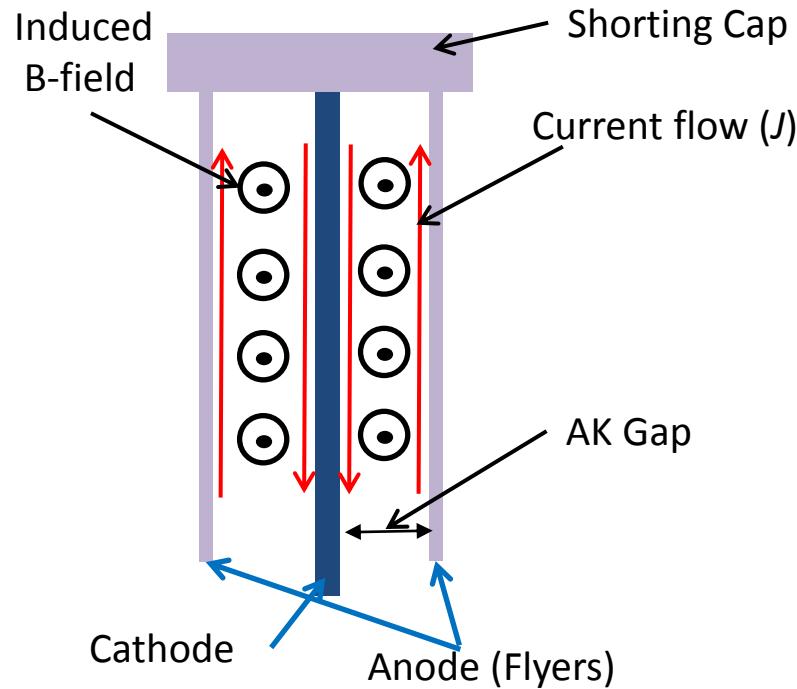


New experimental setup
allows for dual cryogenic
experiments



The pressure cell is
the size of a die

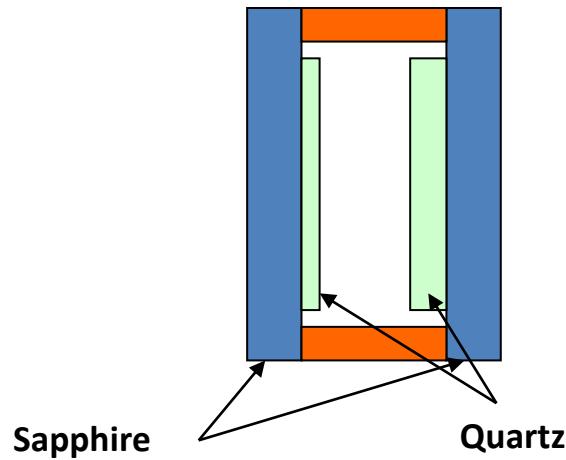
Experimental setup on Z: high-precision temperature control and hypervelocity impact experiments



- Current pulse loops through shorting cap inducing a B – field.
- Resulting $J \times B$ force accelerates anodes (flyers) outward (Here 18-30 km/s)
- Asymmetric AK Gaps result in two different flyer velocities (two Hugoniot points per experiment)

- Target filled to 16.7 PSI CO_2 at 220 K
- Designed the window thickness with margin for break
- Sapphire Reflective above 600 GPa
- Will use quartz plates to measure shock speeds at pressures lower than 600 GPa.
- **Expected CO_2 pressure range: 150 GPa – 600 GPa**

We measure shock velocities in CO_2 and other transparent samples with sub-percent accuracy

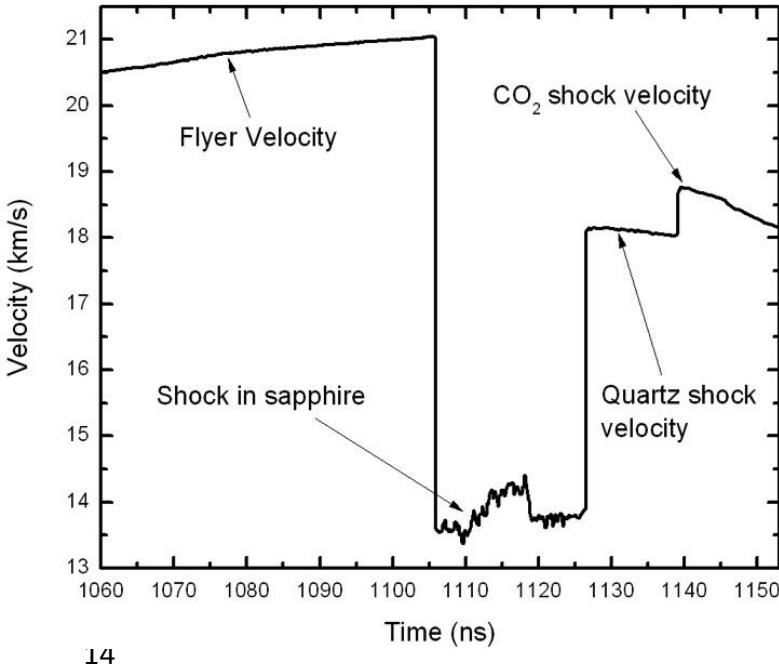


VISAR main diagnostics

Flyer velocity, time of impact

Arrival at interfaces and breakout

Shock velocity in samples



Monte-Carlo error analysis

Accuracy of shock standards

Correlation among parameters

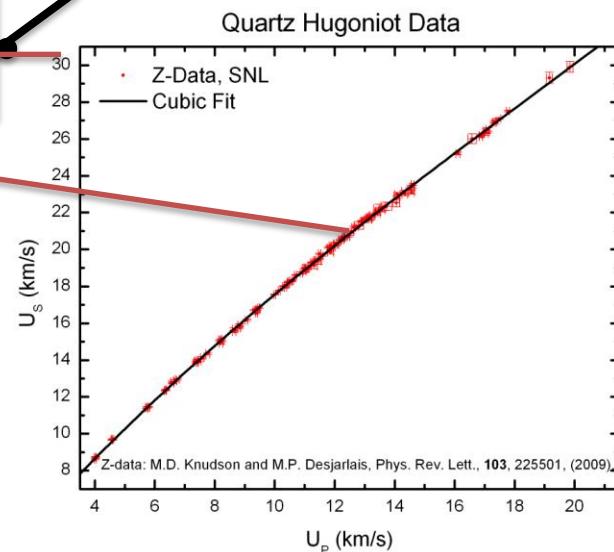
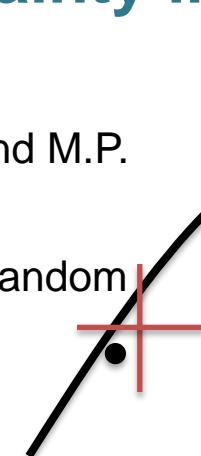
Error propagation

VISAR trace from a CO_2 experiment with 21 km/s impact velocity

The Monte Carlo Impedance match method provides accurate EOS and uncertainty information from the data

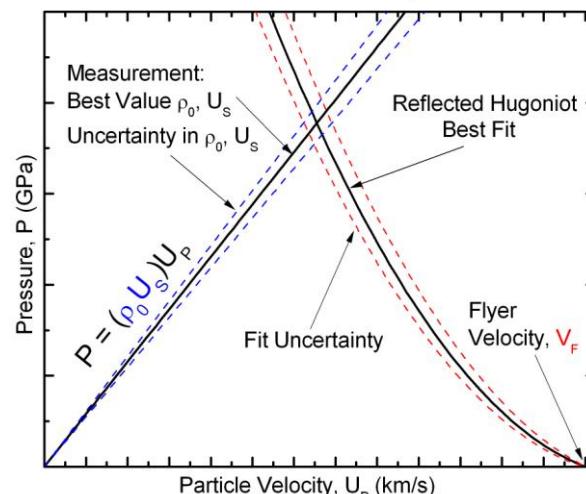
Quartz

- 180+ Hugoniot data points (M. Knudson and M.P. Desjarlais, PRL 2009)
- Varying each U_S - U_P by an *uncorrelated* random number with σ = experimental uncertainty
- Solve for the cubic fit parameters
- Determine mean, σ , and correlation of fit parameters



For CO_2

- Vary *measured* parameters V_F , U_S , r_0 by an *uncorrelated* random number with σ of experimental uncertainty
- Vary *quartz Hugoniot fit parameters* using *correlated* random numbers
- Calculate U_P , r , and P – determine the mean and σ



The reported uncertainties in the CO_2 data include the uncertainty in the quartz standard

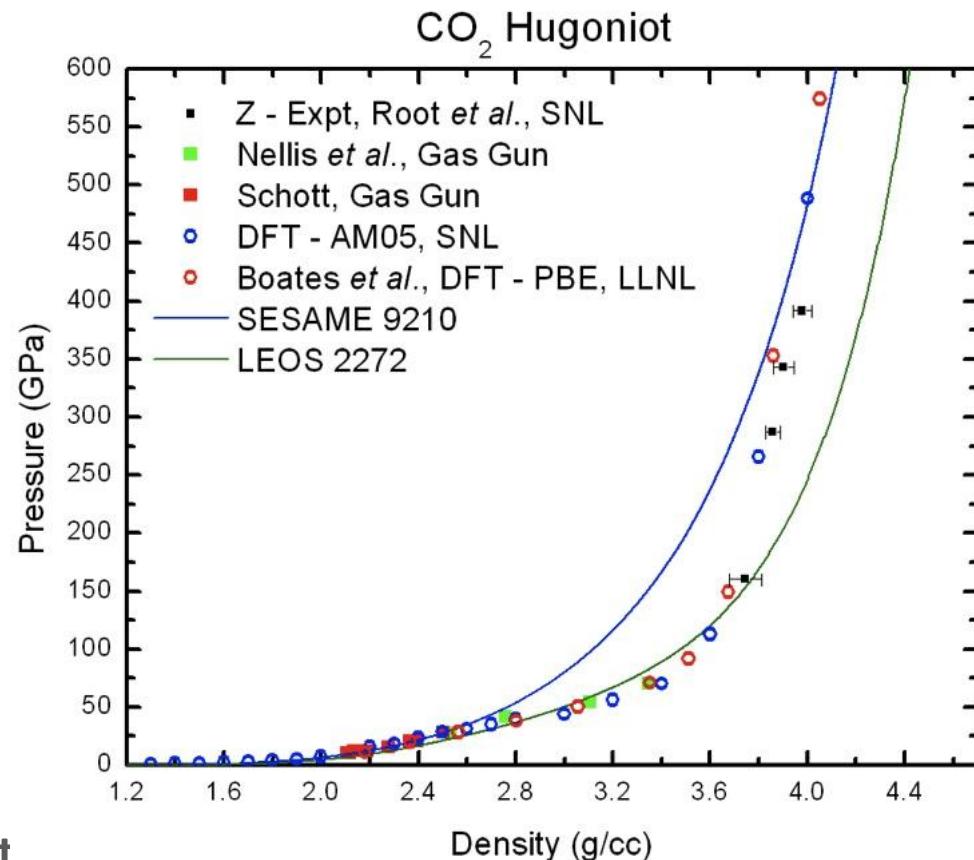
Experiments on Z validate DFT simulations to 400 GPa – including the sharp rise post dissociation

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- **Z-experiments**

- Reflected Hugoniot: expect -1% shift in density due to quartz release
- 4 shots 100% data return
- Reproducible initial state with tight temperature and pressure control



We measure a steep rise in shock pressure towards four-fold compression

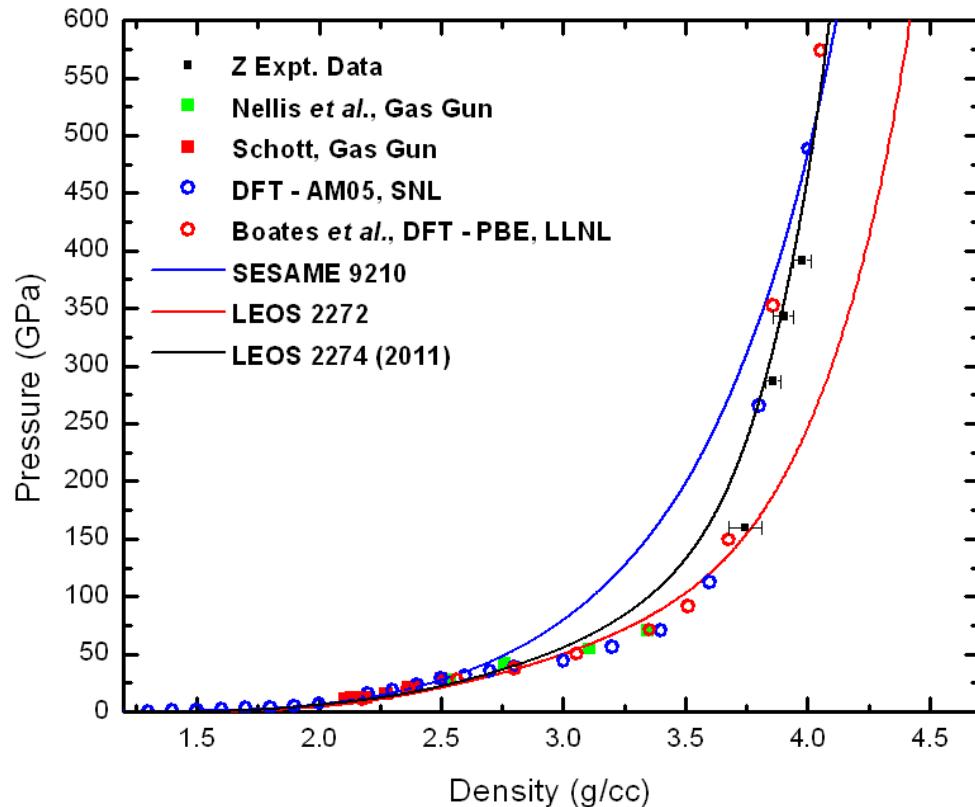
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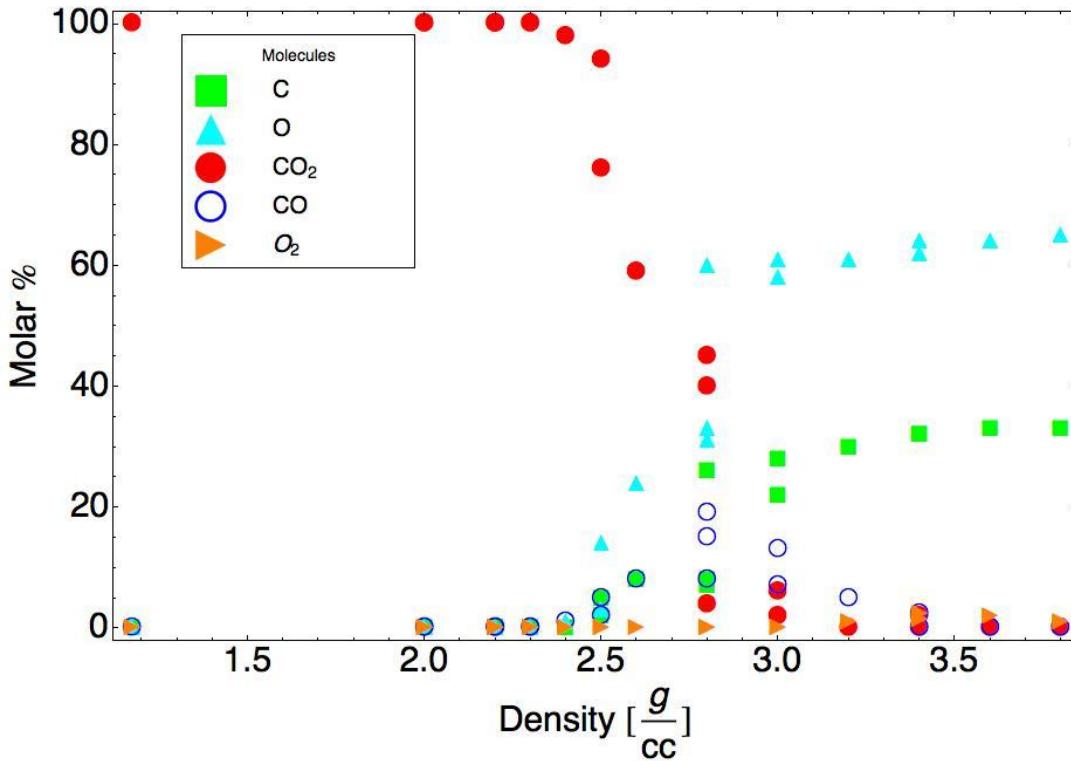
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LEOS 2274, preliminary (C. Wu and P. Sterne, 2011).

DFT simulations contribute to understanding the physical behavior of the system

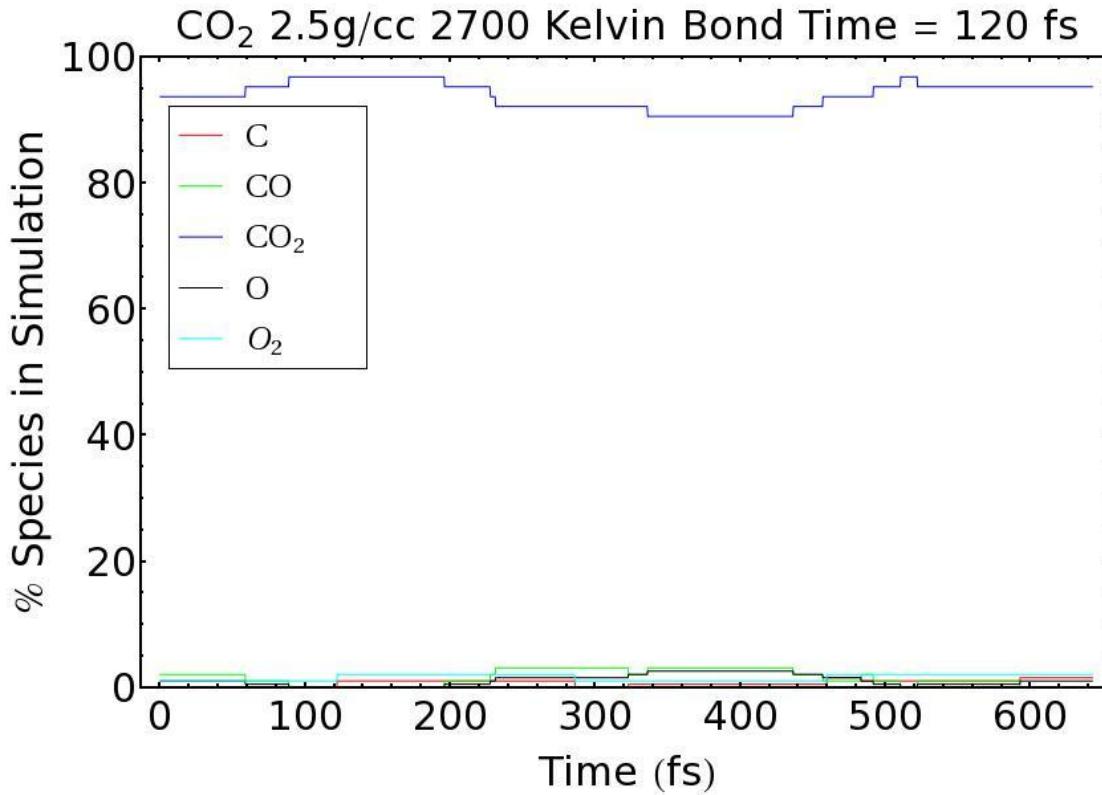
- Shoulder in shock pressure
 - Nellis et al attributed it to dissociation
- We analyze the simulations along the Hugoniot
 - Dissociation begins at 2.5 g/cm^3 and is completed above 3.0 g/cm^3
 - Confirm dissociation as the cause for a shoulder in the Hugoniot pressure
- After dissociation is complete, we predicted and measured a strong increase in shock pressure



Mole % of CO, CO₂, O, C, and O₂ as a function of density along the Hugoniot

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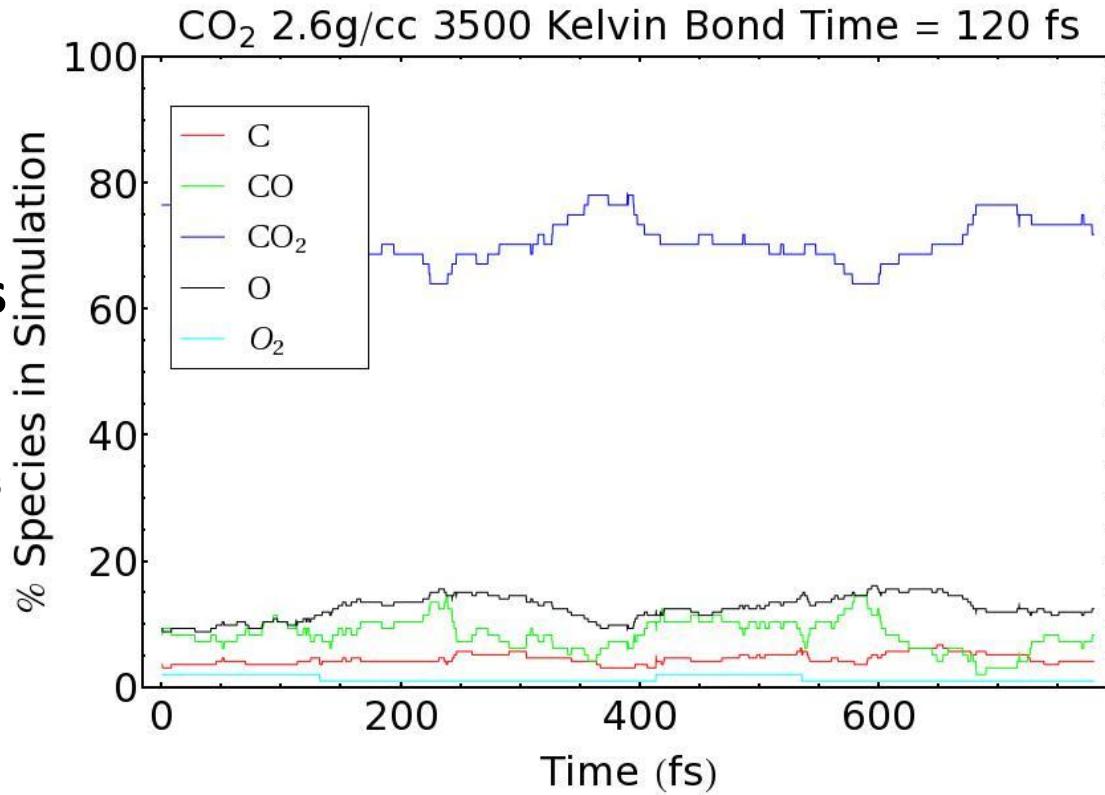
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Chemical composition during the last 800 fs of a simulation

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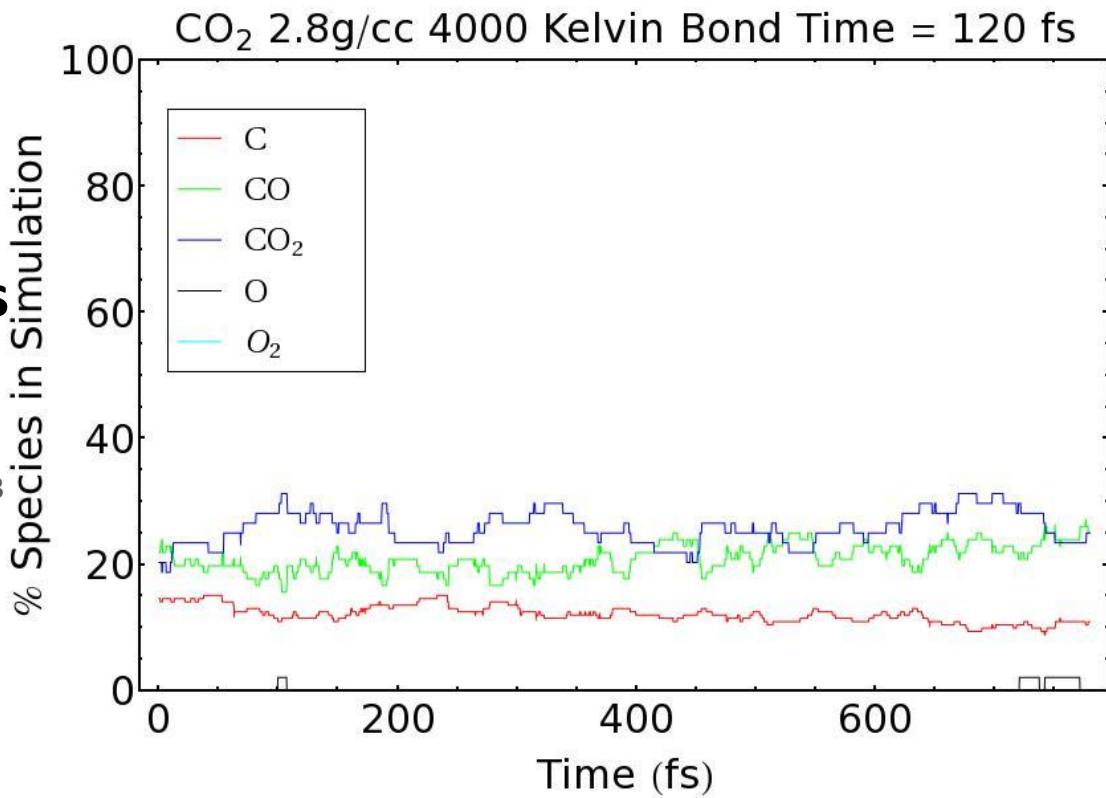
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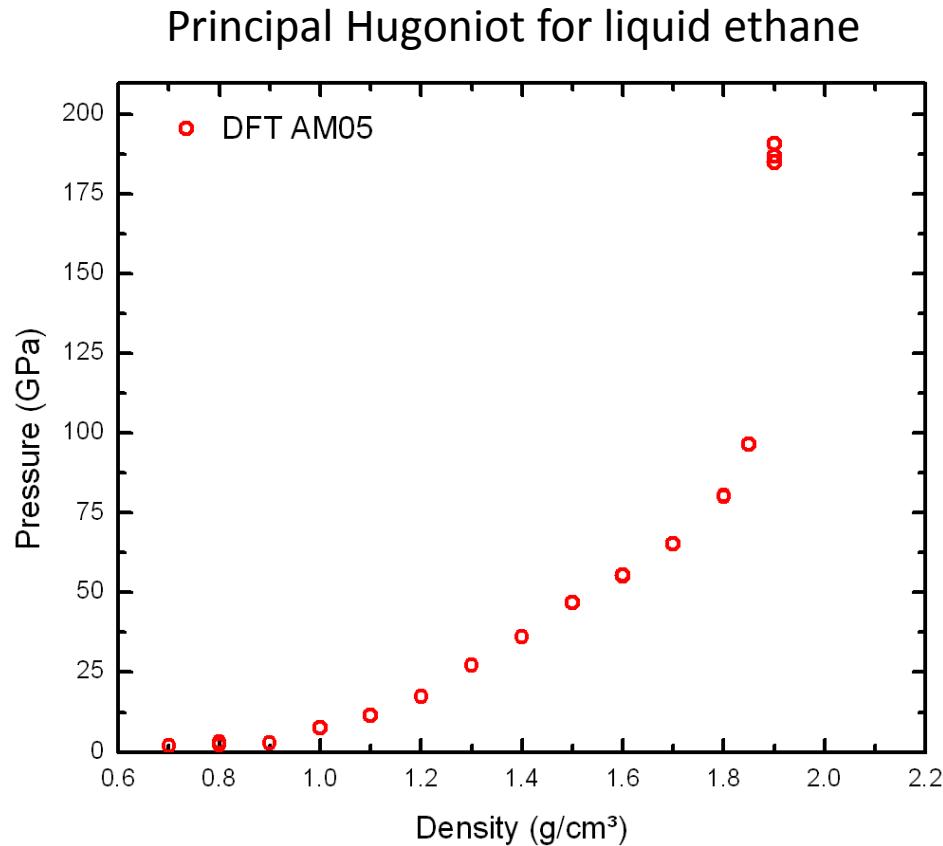


Chemical composition during the last 800 fs of a simulation

DFT/QMD simulations predicted the Hugoniot for ethane – shoulder at 50 GPa followed by a sharp rise

- DFT simulations

- 64 molecules 512 atoms
- Complex k-point (0.25,0.25,0.25)
- 800/1600 eV plane-wave energy
- Well described shoulder/dissociation
- 0.56 g/cm³; 163 K initial state



See Kyle's poster for more results on hydrocarbons

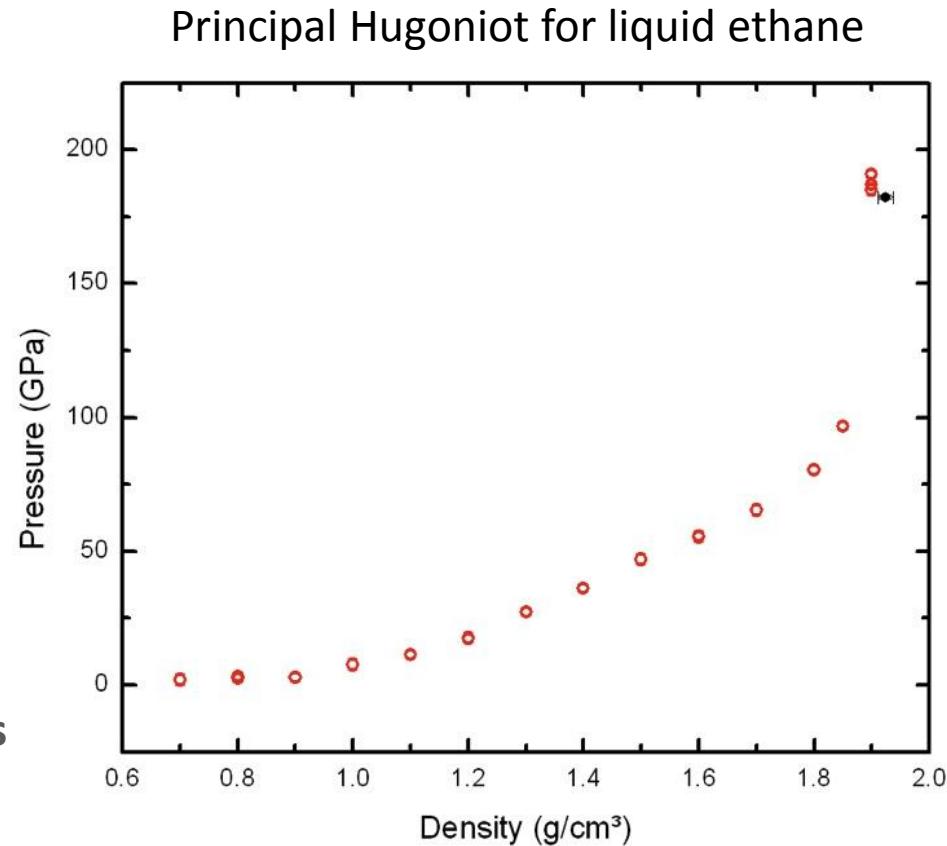
Initial data from Z validates the DFT/QMD results – obtaining a shock pressure of 180 GPa

- **DFT simulations**

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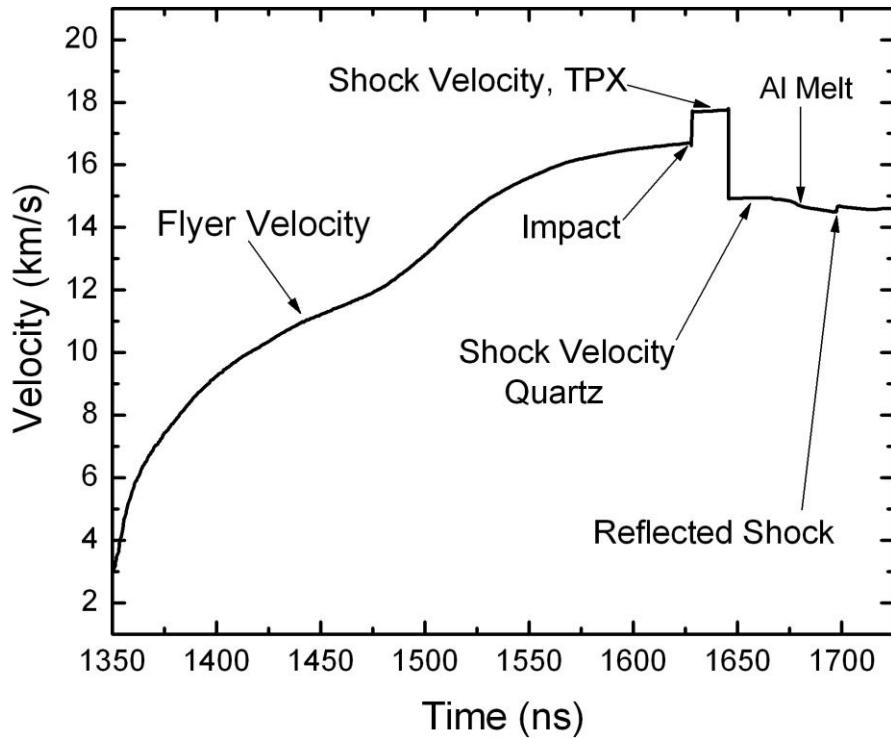
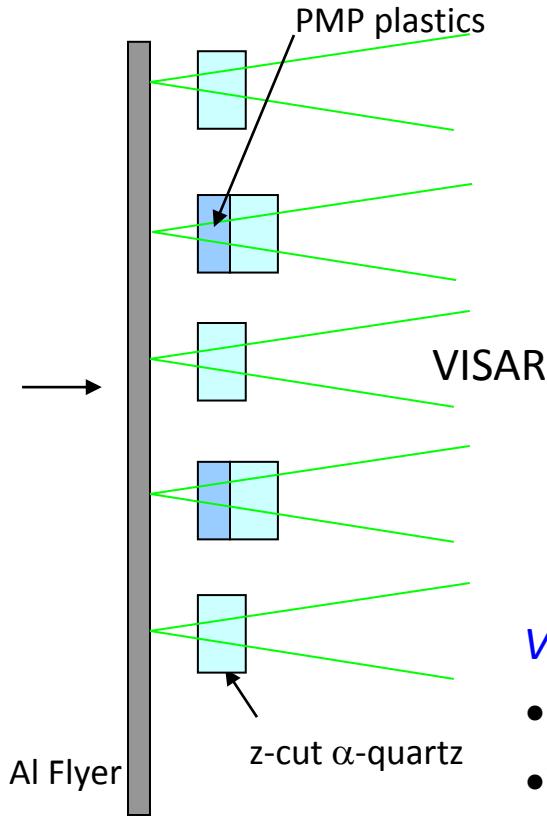
- **Z-experiments**

- Initial results at 180 GPa
- Will continue the experimental series
- Temperature measurements using optical pyrometry – analysis in progress will add new data to EOS comparisons



See Kyle's poster for more results on hydrocarbons

We measure shock velocities in plastic and other transparent materials with sub-percent accuracy



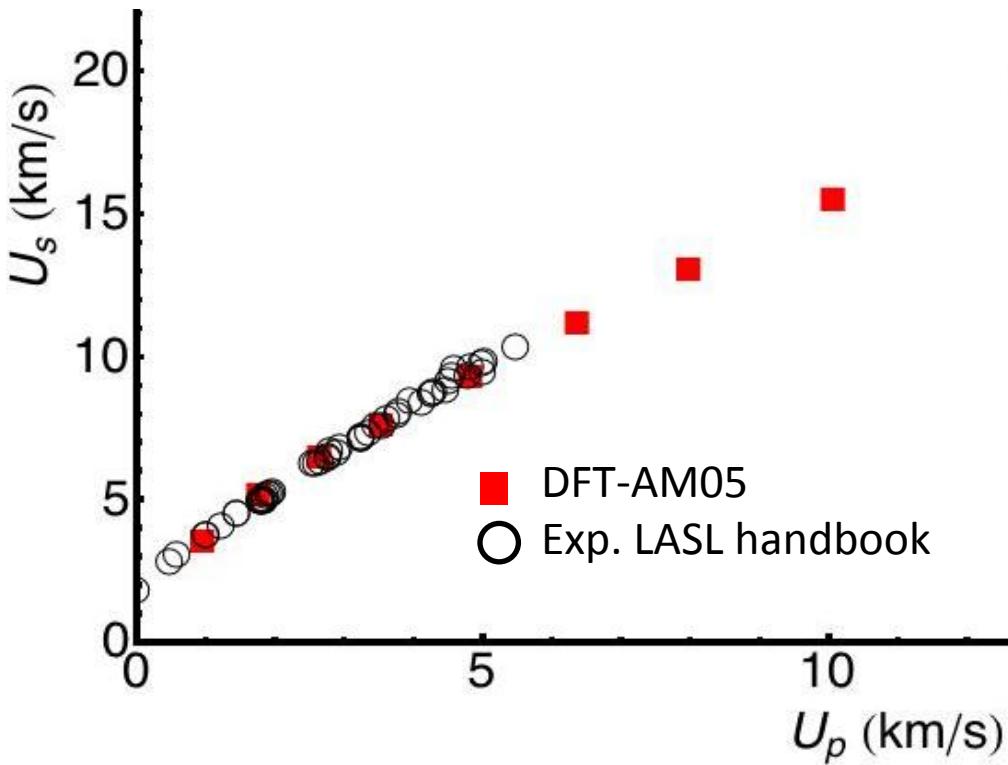
VISAR measurements as main tool:

- Flyer velocity
- Time of impact
- Shock arrival at plastics/quartz interface
- Shock velocity in sample and breakout time
- *Steady shocks, large samples, and long times yield high precision measurements*

DFT-AM05 is of high fidelity for shock compression of poly(4-methyl 1-pentene) (PMP) to 50 GPa

Principal Hugoniot for poly(4-methyl 1-pentene)

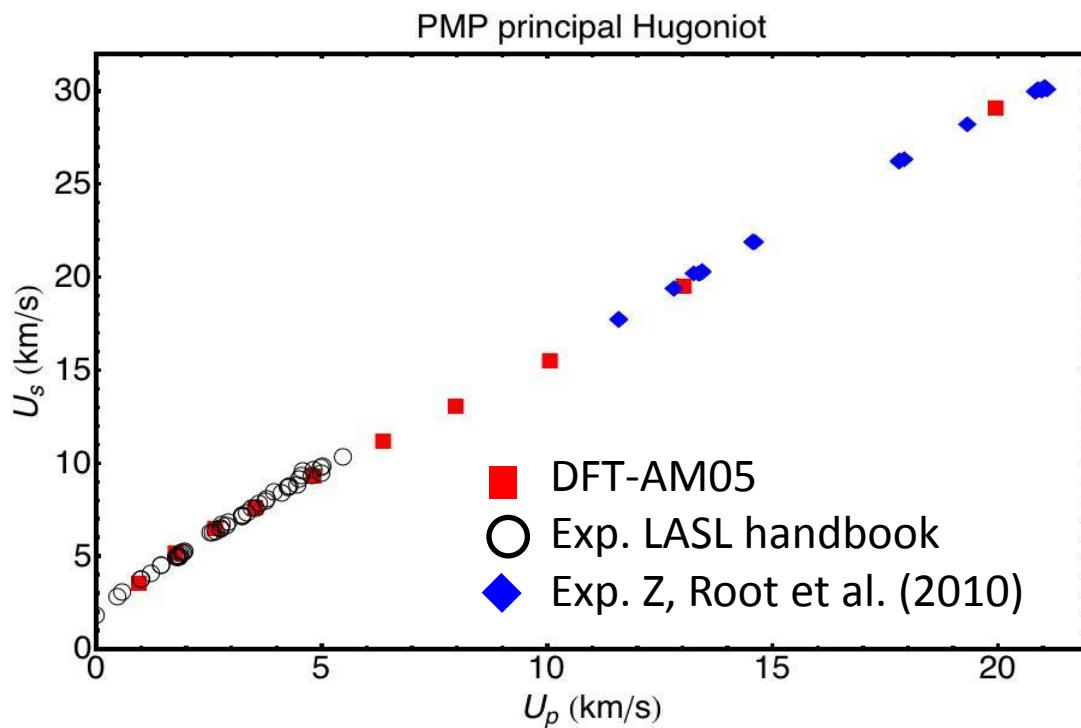
- 440 atom simulations
- DFT-AM05 is of high fidelity also for PMP
- Curvature for low shock speeds



T.R. Mattsson et al. Phys. Rev. B **81**, 054103 (2010).

Results from recent shock experiments on Z for poly(4-methyl 1-pentene)

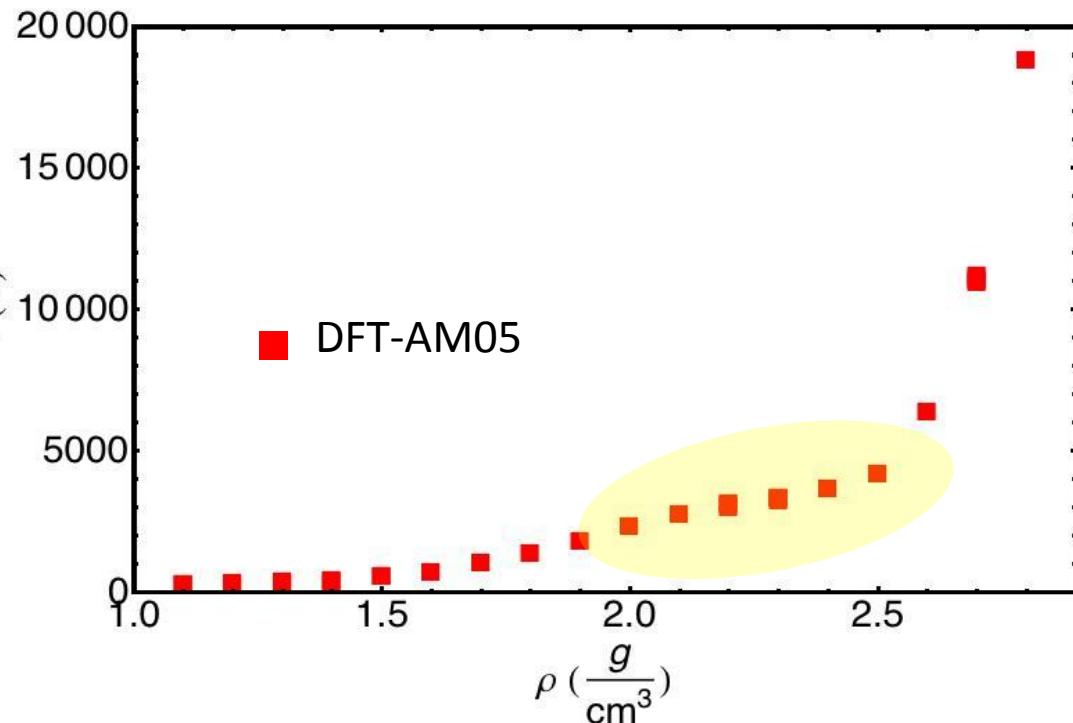
Principal Hugoniot for poly(4-methyl 1-pentene)



- Shock experiments up to 30 km/s shock velocity
- 200 – 530 GPa pressure
- *Also polymers can be modeled with high fidelity using DFT-AM05*
- Promising for extending beyond plastics to foams

Simulations allow a detailed analysis of the physics and chemistry of shock compression of hydrocarbon polymers

Temperature along the Hugoniot for polyethylene

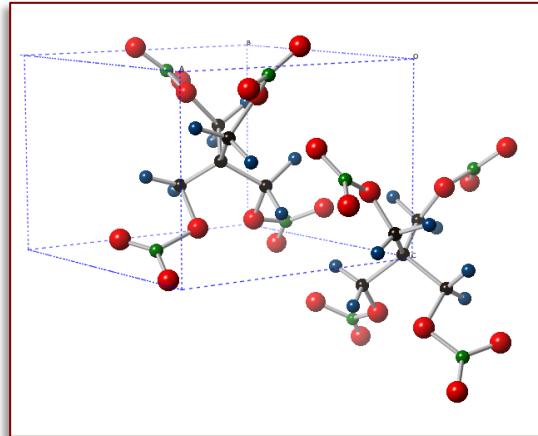


- Temperature is the missing link in P/rho; Us/Up analysis
- *Temperature almost flat during the shoulder in pressure*
- Detailed modeling of chemistry during the shock compression
- *Temperature measurements are being introduced on Z*

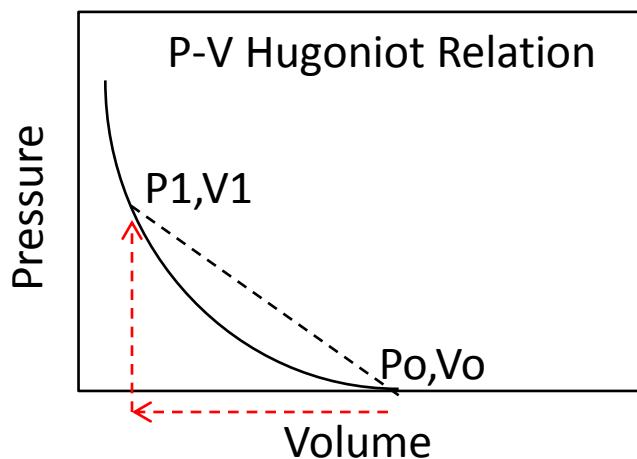
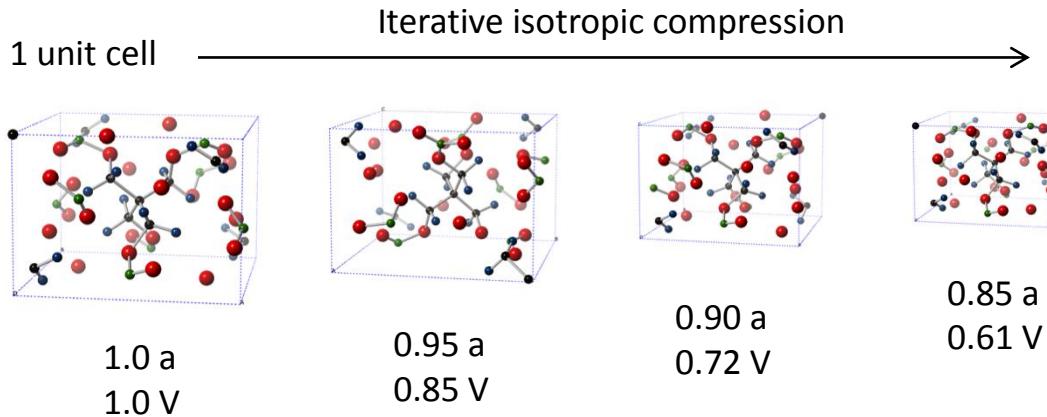
T.R. Mattsson et al. Phys. Rev. B 81, 054103 (2010).

We compress PETN in the simulations and tune the temperature to locate the Hugoniot State (P,T,E)

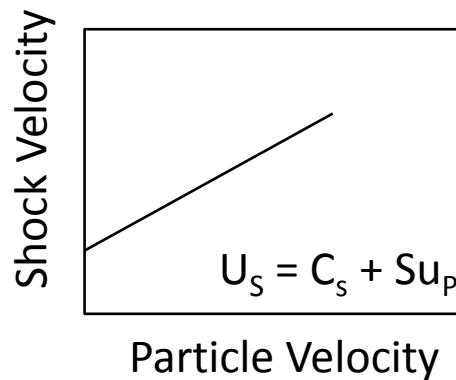
Density Functional Theory based
Molecular Dynamics (DFT-MD)



PETN, V_0 at 300K



$U_S - u_P$ Hugoniot Relation

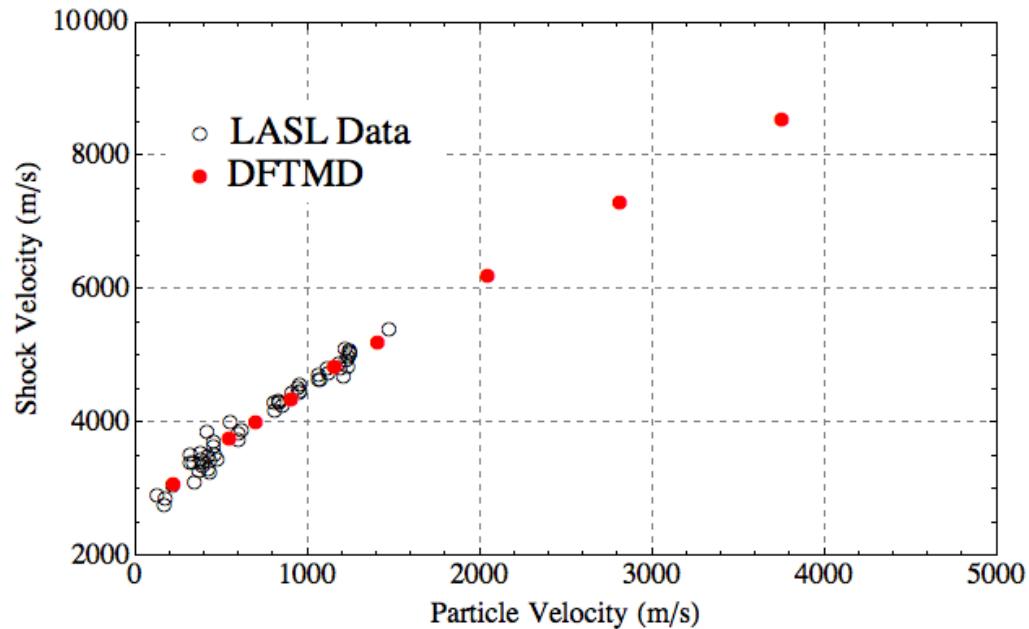


Mass Momentum Energy

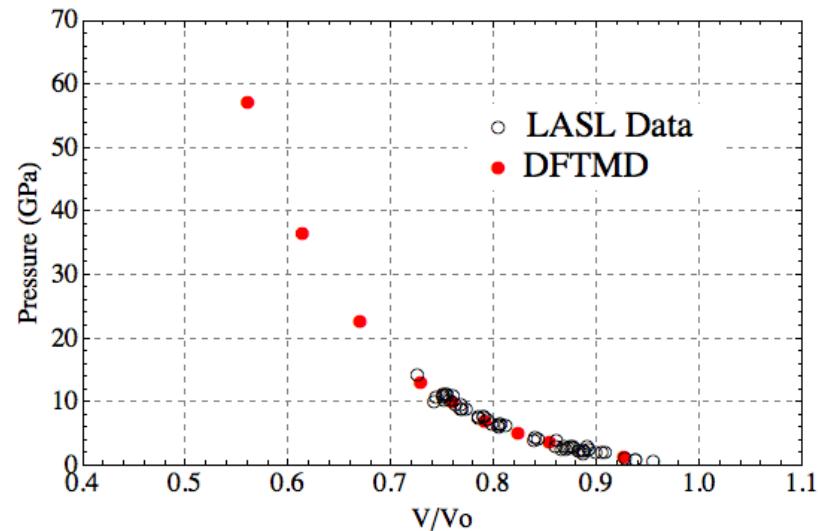
$$\begin{aligned} \rho_0 D &= \rho_1 (D - u_1) \\ P_1 &= \rho_0 D u_1 \\ E - E_0 &= \frac{1}{2}(P + P_0)(V_0 - V) \end{aligned}$$

Employed DFT-MD to calculate the PETN crystalline Hugoniot to 60 GPa; validating the approach to LASL data

Single Crystal Data



P-V Hugoniot



We obtain the un-detonated Hugoniot well above experimentally accessible regimes and reproduce low-pressure data

Ryan Wixom's poster yesterday and Mattsson, Wixom, Mattsson, *Proceedings to the 14th international Detonation Symposium (2010)*.

Integration of DFT/QMD and high-precision multi-Mbar experiments on Z serve as a solid foundation for understanding chemistry in dynamic extremes

- Employed DFT based MD simulations to model shock compression of CO_2 , C_2H_6 , CH_2 , and PETN

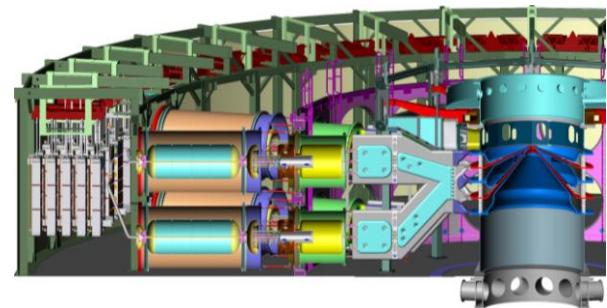
- Agreement with existing data
 - Confirm a CO_2 dissociation plateau at 60 GPa
 - Predictions for shock compression to 500 GPa in CO_2
 - Steep rise in shock pressure following the dissociation region for several materials with chemistry

- Executed experiments on Z to measure the shock Hugoniot of CO_2 , C_2H_6 , and CH_2

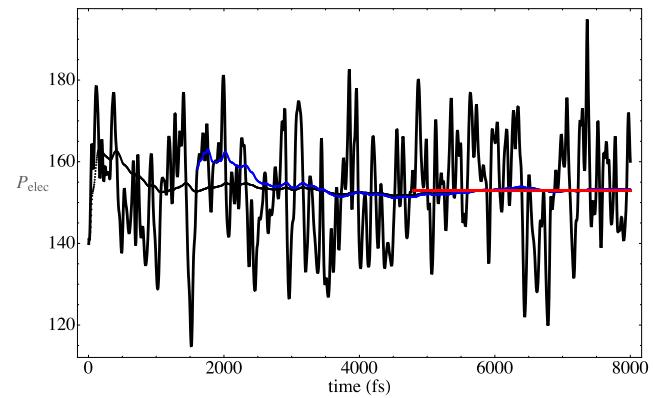
- High-precision measurements can distinguish between different EOS models
 - Broad platform for studying cryogenic liquids up to initial pressures of 1 MPa
 - Temperature measurements coming online - exciting

Acknowledgments

- The large team operating the Z-machine – Mike Lopez
 - The cryogenic team – Dave Hanson, Andrew Lopez, Keegan Shelton, and Jose Villalva
 - Sandia High-Performing Computing – Sophia Corwell
 - Program leadership – Dawn Flicker and Mark Herrmann
 - Scientific leadership – Mike Desjarlais



Shock experiments on Sandia's Z machine



Density Functional Theory simulations