

Modeling experiments on Z where chemistry matters: polymers, CO₂, and explosives

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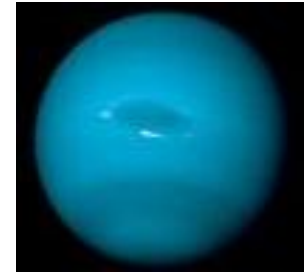


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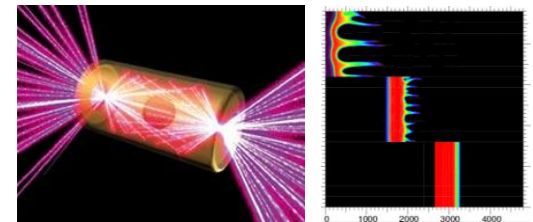


Properties of light elements in the Mbar regime are important for several reasons

- **Planetary science – Uranus & Neptune and exo ice-giants**
 - High-pressure mixtures of H, He, C, O, N
- **Planetary science – earths and super-earths**
 - Equation of state of Fe and subducted CO₂
 - Mbar, 1000 – 4000 K
- **Inertial confinement fusion (ICF) materials**
 - Fundamental behavior of carbon and carbon compounds
 - Mbar, +10 000 K
- **Chemistry at high pressure and temperature**
 - Reactions driven by pressure and temperature
 - Composition under shock compression
 - Complex Hugoniot – flat sections



Ice giants: C-H-N-O mixtures at Mbar



ICF concepts: irradiated hohlraum (left) and Sandia's MagLIF (right)

Overview of systems with chemistry: first-principles simulations and Z experiments

- **CO₂**

- Liquid initial state – to 5 Mbar with high precision

- **Hydrocarbons**

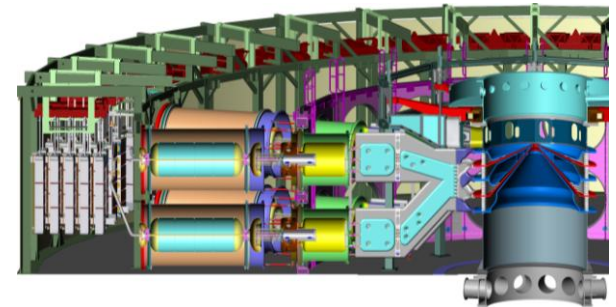
- Polymethyl pentene (PMP/TPX)
- Polyethylene, Polystyrene
- Liquid ethane
- *See poster yesterday by Kyle Cochrane*

- **High explosives**

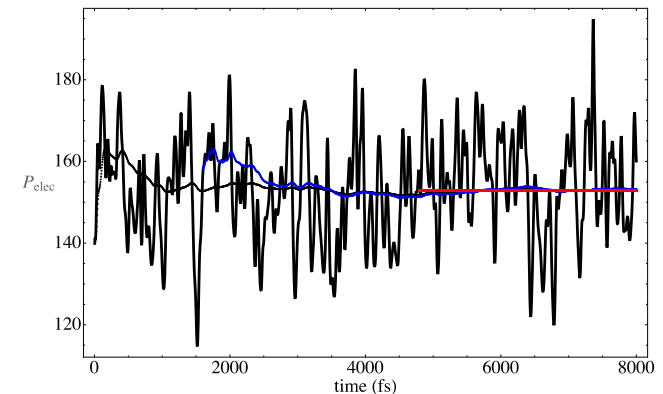
- Initial results on PETN
- *See poster yesterday by Ryan Wixom*

- **Chemistry at high pressure and temperature**

- Reactions driven by pressure and temperature
- Composition under shock compression
- Complex Hugoniot – flat sections



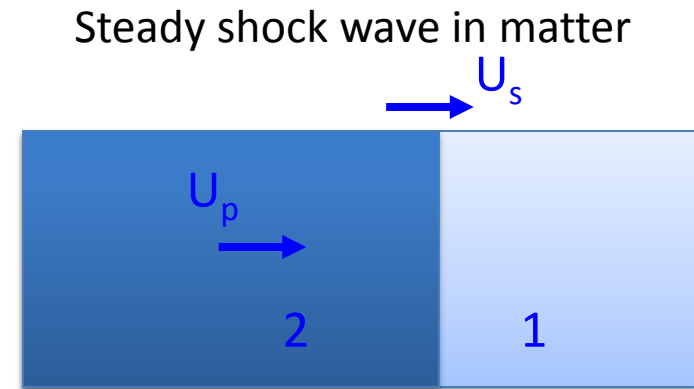
Shock experiments on Sandia's Z machine



Density Functional Theory simulations

We reach Mbar pressures in liquids and solids by executing flyer-plate impact experiments

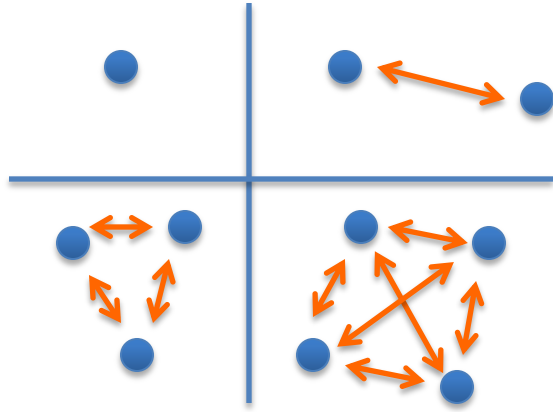
- **Advantages of liquid and transparent solids**
 - Uniform sample
 - Initial state EOS well-defined
 - Reproducible state
 - Reflective shock fronts allow very high precision measurements
 - 30 km/s impact velocities
- **Straightforward to analyze**
 - Conservation of mass, momentum, and energy
 - Rankine-Hugoniot relation



$$2(E_2 - E_1) = (P_2 + P_1)(u_1 - u_2)$$

With high accuracy measure and/ or calculate thermo-physical properties

Density functional theory (DFT) based MD is an established approach - HEDP sets additional demands



Treating quantum many-body interactions between electrons correctly is very demanding



Large-scale simulations on supercomputers like cielo and Red Sky

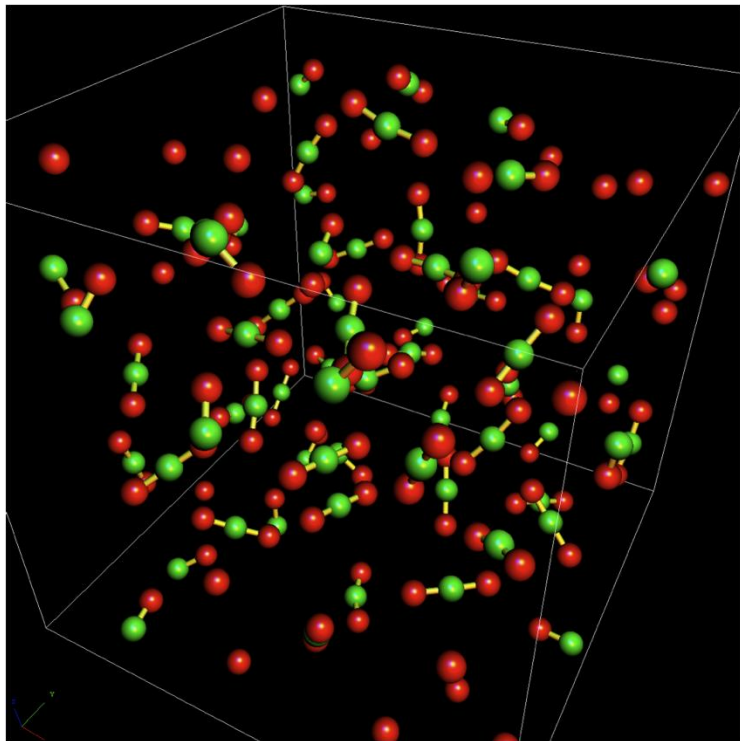
DFT calculations can be predictive

- *Accuracy* set by the exchange-correlation (xc) functional:
- *Convergence* of simulation parameters to desired precision
- W. Kohn won the 1998 Noble prize in chemistry

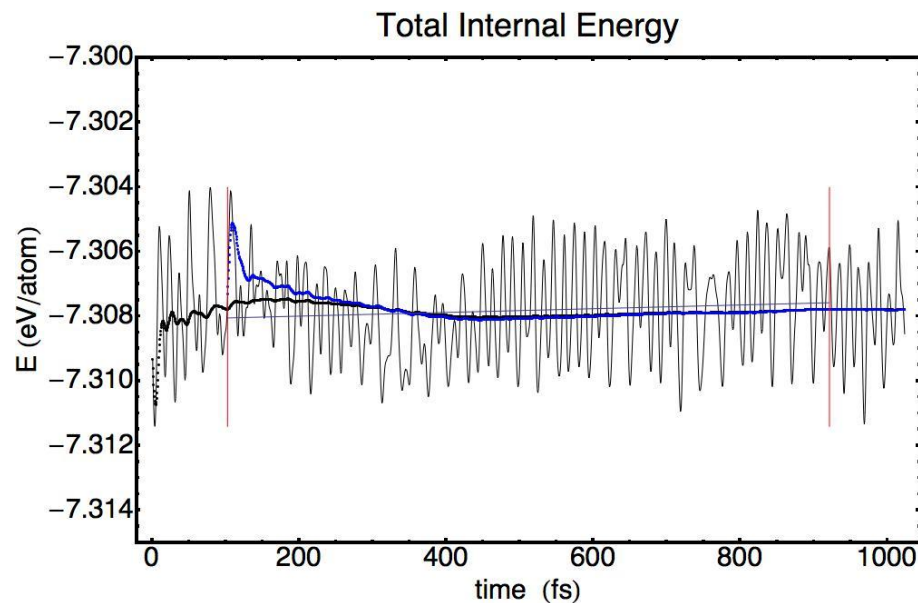
VASP code (Georg Kresse, Vienna, Austria)

- Finite-temperature DFT (Mermin)
 - Plane-wave basis-set for controlled convergence and free electrons/ionization
 - Projector augmented wave core functions (PAW)
-
- *First-principles thermodynamics – long simulations yield $P(\rho,T)$, $E(\rho,T)$, structure, diffusivity, etc.*

First-principles thermodynamics: gaining insights into the behavior of matter starting from quantum mechanics



Simulation of CO₂:
64 molecules
one complex k-point
high plane-wave cutoff energy



*Time averaging over long
equilibrated run – the figure shows
the last ps of a longer simulation*

Note the fine energy scale

We also analyze the chemical composition in the cell

- **Bond-distances between atoms**

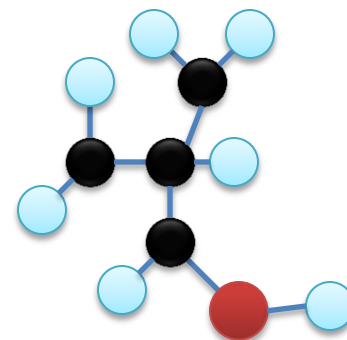
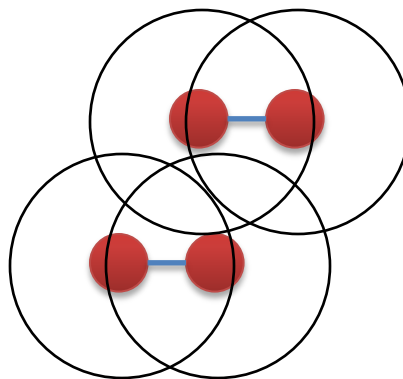
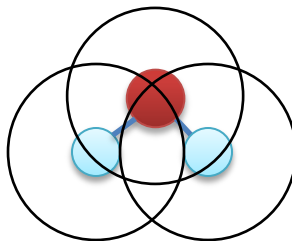
- C-C, C-O, O-O
- Distances from analyzing pair correlation functions

- **Bond Time**

- Remain bonded over several vibration times – verify using different times

- **Molecule accounting**

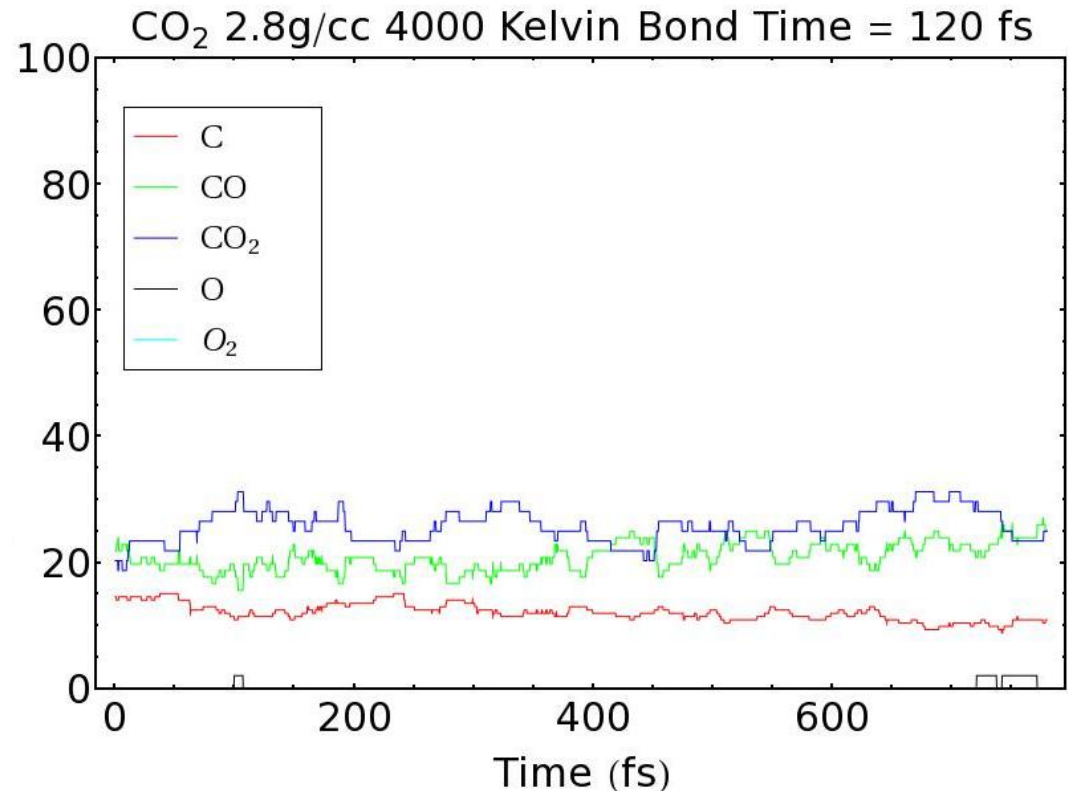
- Identify molecules
- O₂ is easy
- Branching
- Rings
- Use a recursive algorithm
- Tracking in time



Identifying molecules, including branching and rings, using a recursive algorithm

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Chemical composition during the last 800 fs of a simulation

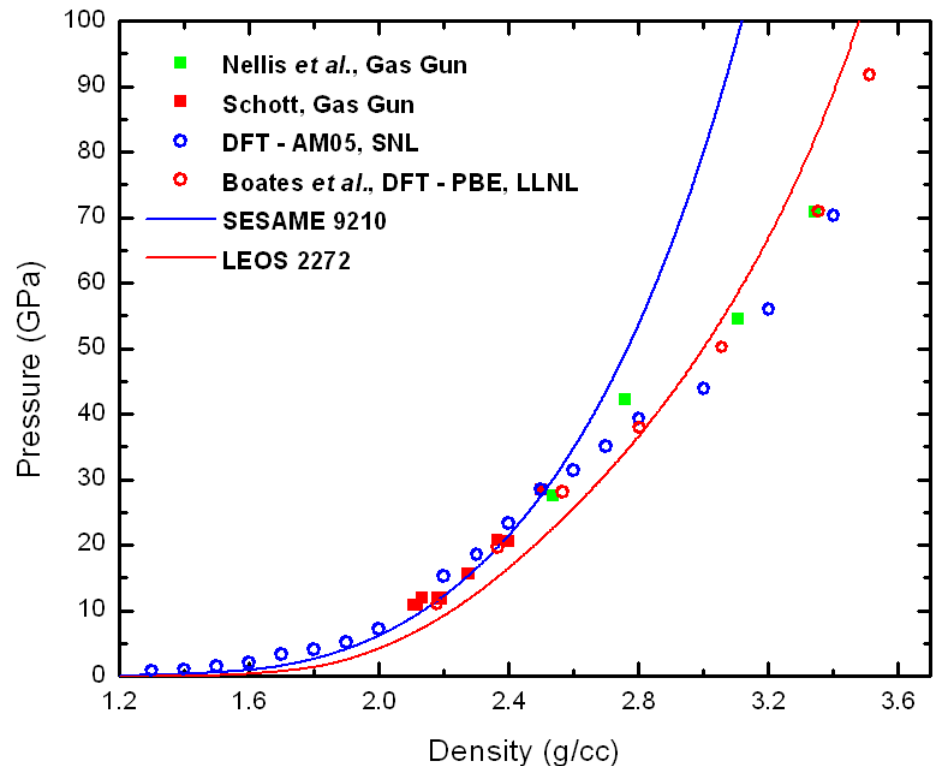
DFT calculations on CO₂ are in agreement with available experimental data and predictions up to 100 GPa

• DFT simulations

- Quantitative and qualitative agreement with Schott (High Press. Res. 6, 187 (1991)) and Nellis et al (J. Chem. Phys. 95, 5268 (1991)).
- Minor difference between PBE and AM05 exchange-correlation functionals
- Existing EOSs do not capture the full behavior

• Behavior above 100 GPa

- Relatively steep raise in pressure beyond 3-fold compression
- We confirm very recent DFT results by Boates et al. (J. Chem. Phys. 134, 064504 (2011))



Excellent agreement between results from DFT/QMD and low-pressure gas-gun data

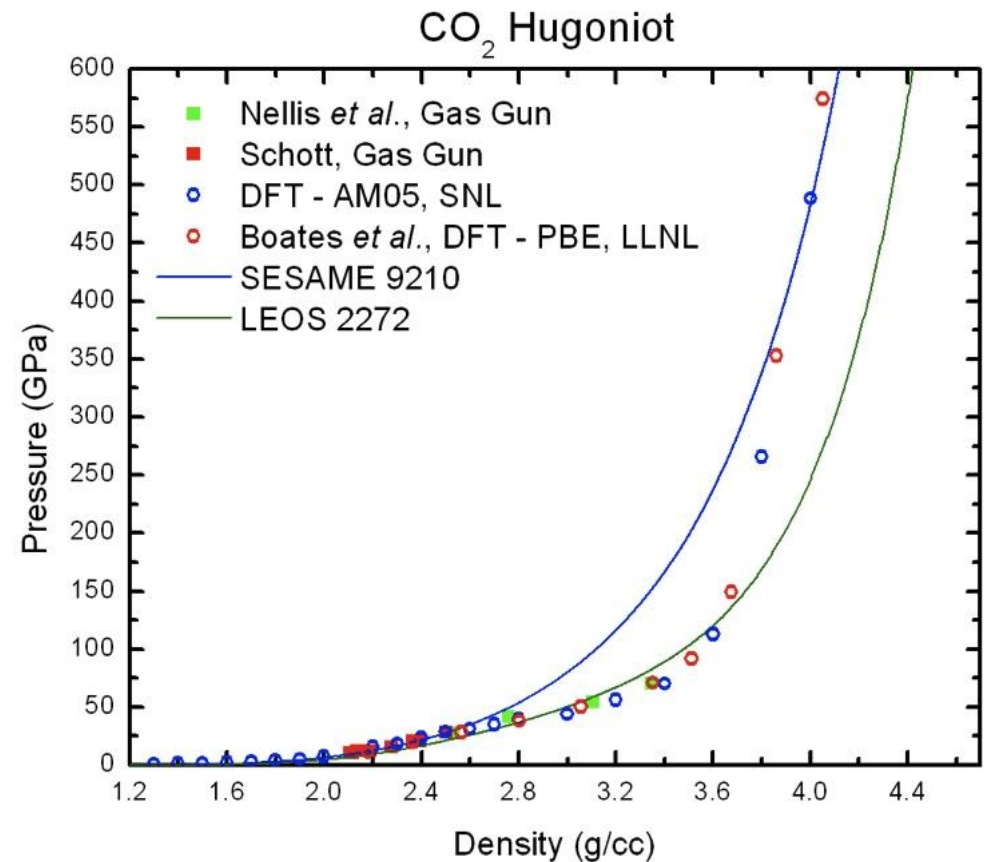
DFT calculations made predictions above 100 GPa – very steep Hugoniot towards 4 g/cm³

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We expect a steep rise in shock pressure towards four-fold compression

We reach Mbars in CO₂ by starting from the liquid phase: it requires an experimental cell under pressure

- **Advantages of liquid**

- Uniform sample
- Initial state EOS well-defined
- Reproducible state

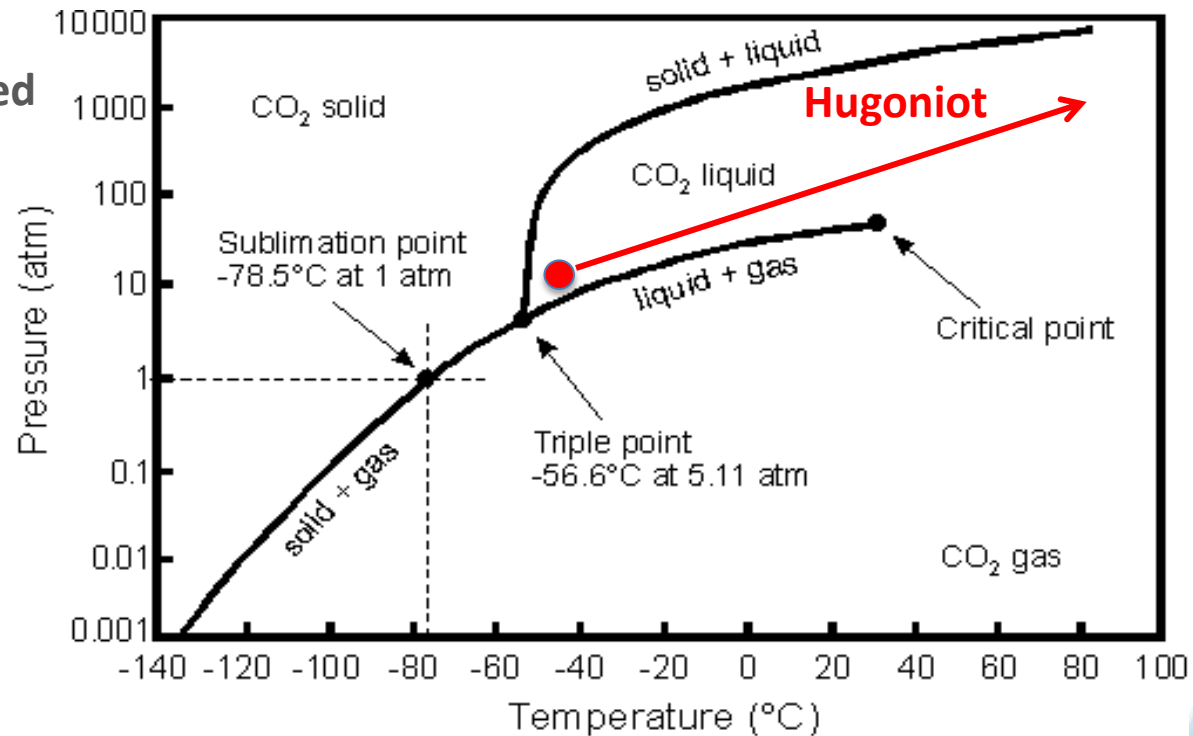
- **Phase-diagram of CO₂**

- Sublimation at 1 atm

- **Initial state in liquid**

- 9 bar/ 900 kPa
- 1.173 g/cm³
- 220 K

Phase-diagram of CO₂



The initial state for experiments on Z was a liquid close to the triple points

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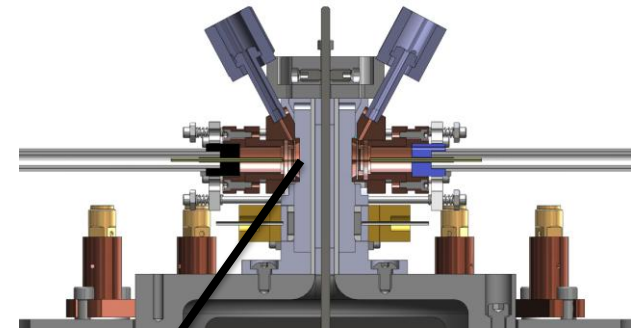
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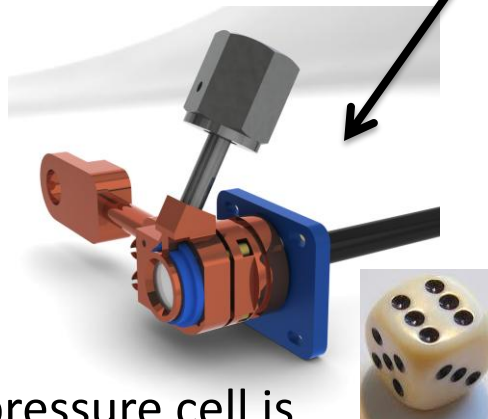
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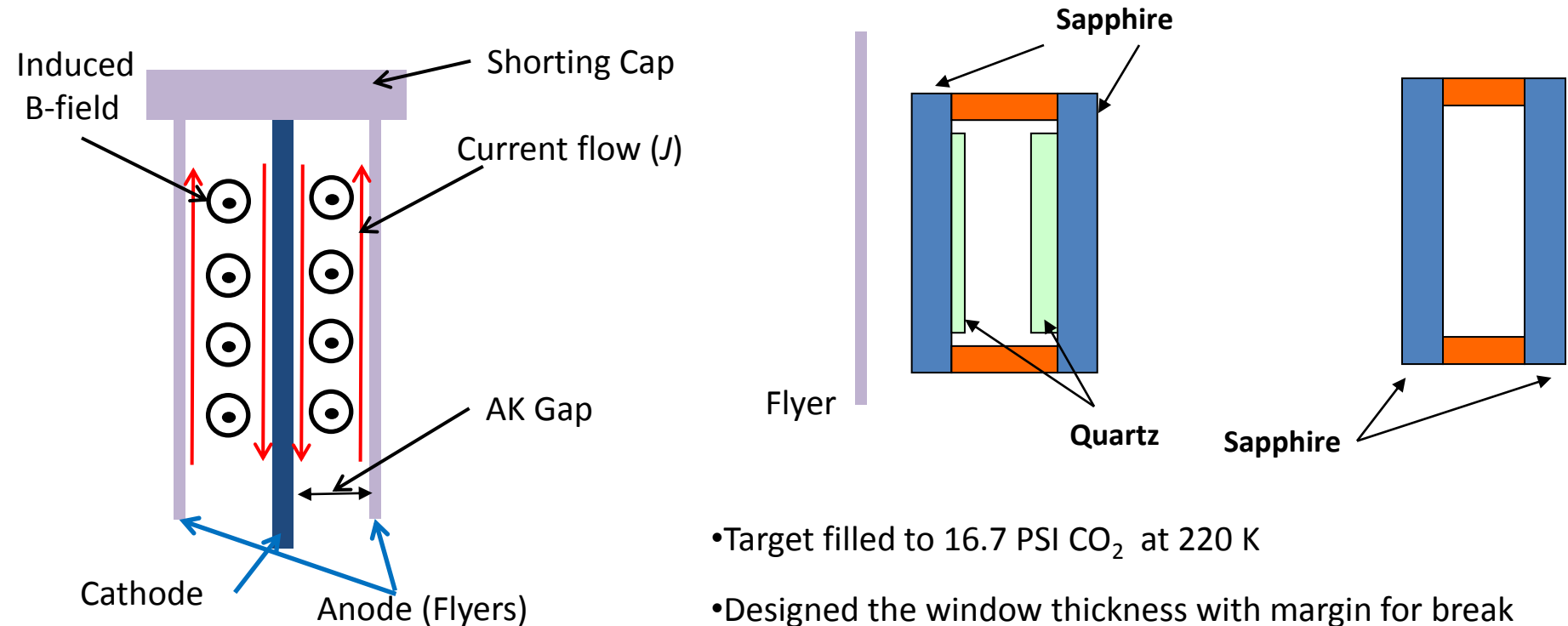


New experimental setup allows for dual cryogenic experiments



The pressure cell is the size of a die

Experimental setup on Z: high-precision temperature control and hypervelocity impact experiments



- Current pulse loops through shorting cap inducing a B – field.
- Resulting $J \times B$ force accelerates anodes (flyers) outward (Here 18-30 km/s)
- Asymmetric AK Gaps result in two different flyer velocities (two Hugoniot points per experiment)

- Target filled to 16.7 PSI CO_2 at 220 K
- Designed the window thickness with margin for break
- Sapphire Reflective above 600 GPa
- Will use quartz plates to measure shock speeds at pressures lower than 600 GPa.
- **Expected CO_2 pressure range: 150 GPa – 600 GPa**

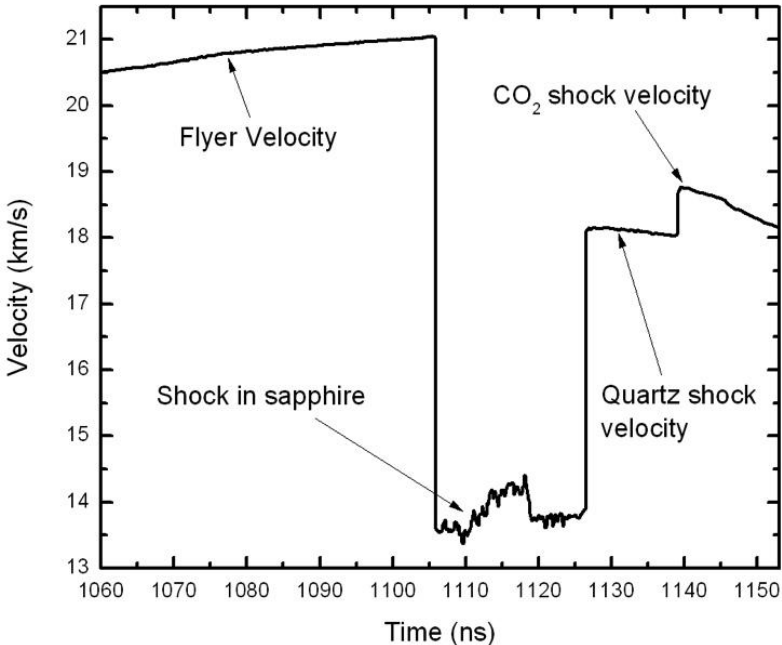
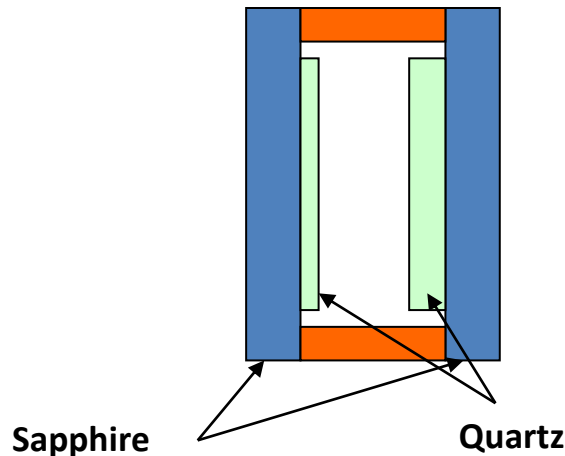
We measure shock velocities in CO₂ and other transparent samples with sub-percent accuracy

VISAR main diagnostics

Flyer velocity, time of impact

Arrival at interfaces and breakout

Shock velocity in samples



Monte-Carlo error analysis

Accuracy of shock standards

Correlation among parameters

Error propagation

VISAR trace from a CO₂ experiment with 21 km/s impact velocity

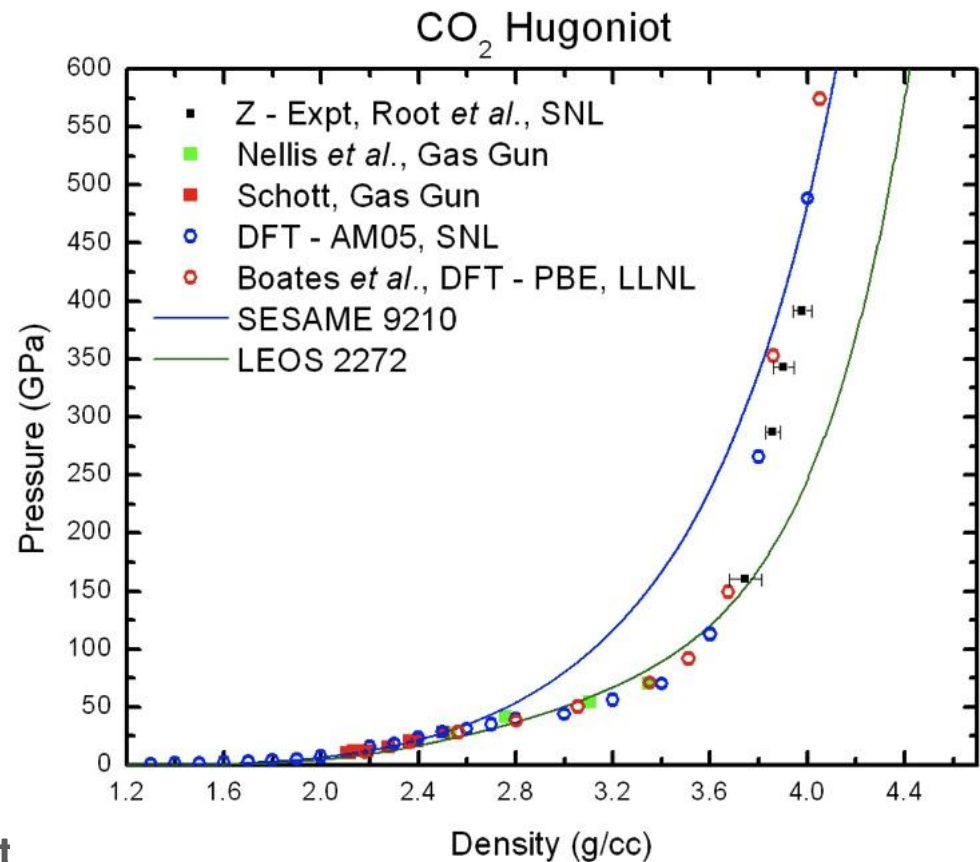
Experiments on Z validate DFT simulations to 400 GPa – including the sharp rise post dissociation

• DFT simulations

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- New EOS developed by Wu and Sterne at LLNL.

• Z-experiments

- Reflected Hugoniot: expect -1% shift in density due to quartz release
- 4 shots 100% data return
- Reproducible initial state with tight temperature and pressure control



We measure a steep rise in shock pressure towards four-fold compression

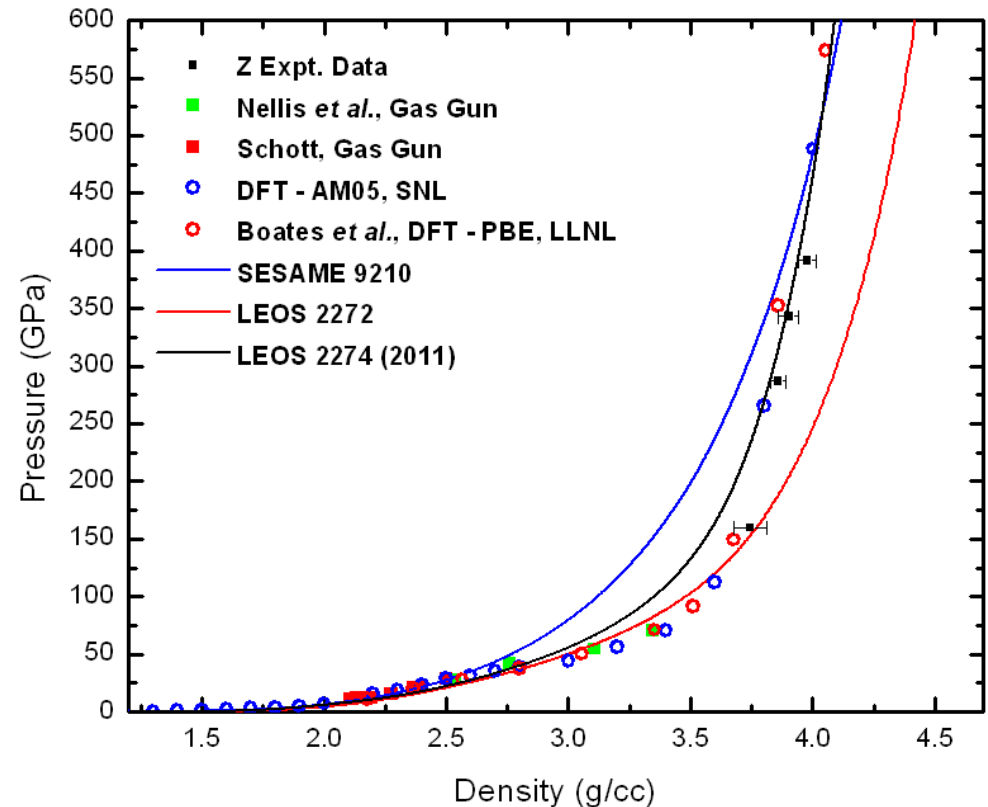
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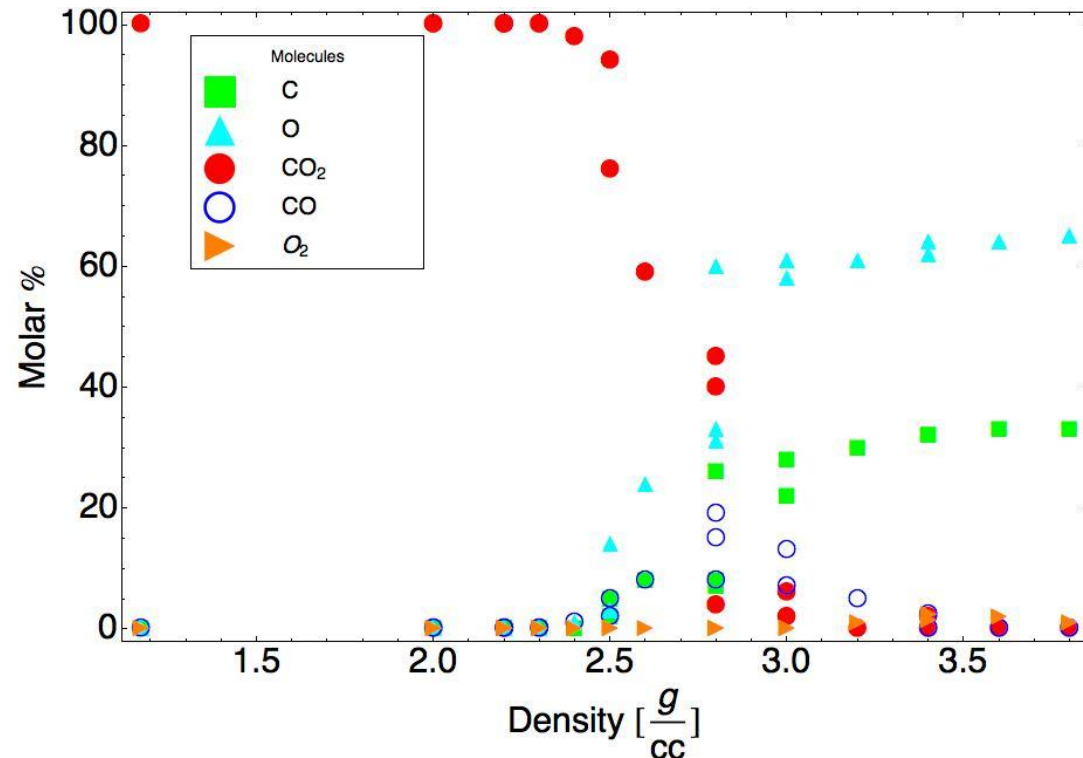
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LEOS 2274, preliminary (C. Wu and P. Sterne, 2011).

DFT simulations contribute to understanding the physical behavior of the system

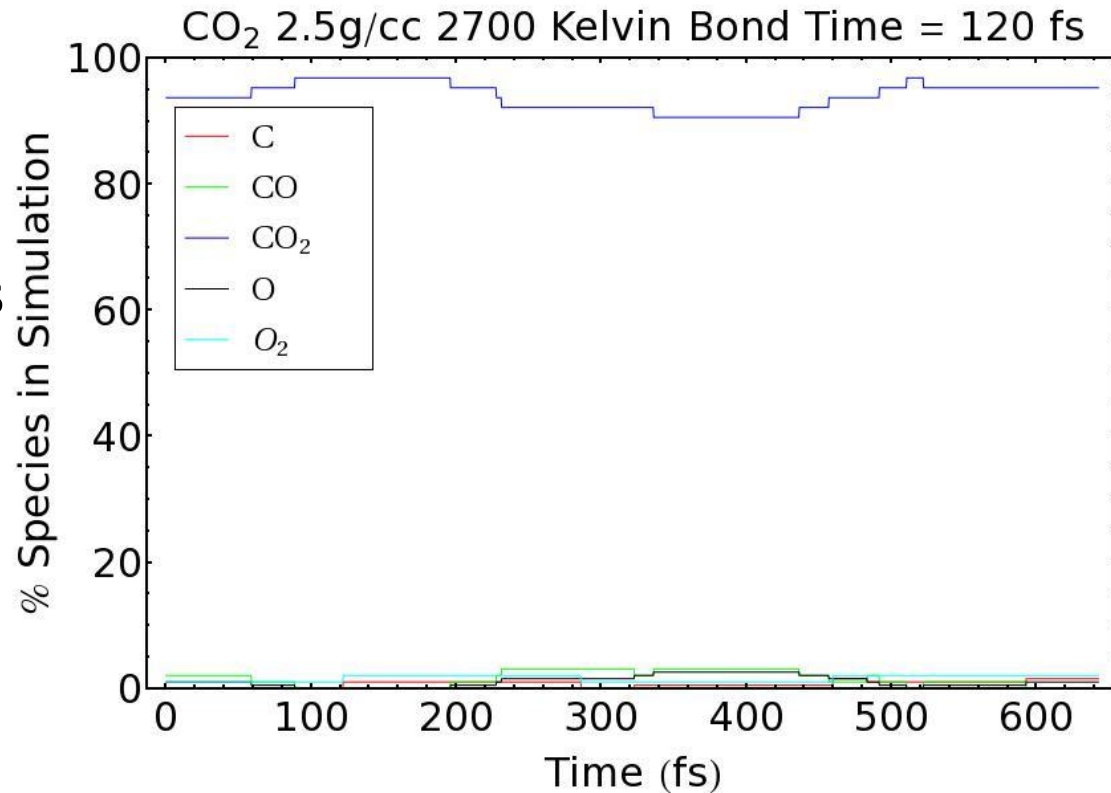
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 - Nellis et al attributed it to dissociation
- **We analyze the simulations along the Hugoniot**
 - Dissociation begins at 2.5 g/cm³ and is completed above 3.0 g/cm³
 - Confirm dissociation as the cause for a shoulder in the Hugoniot pressure
- **After dissociation is complete, we predicted and measured a strong increase in shock pressure**



Mole % of CO, CO₂, O, C, and O₂ as a function of density along the Hugoniot

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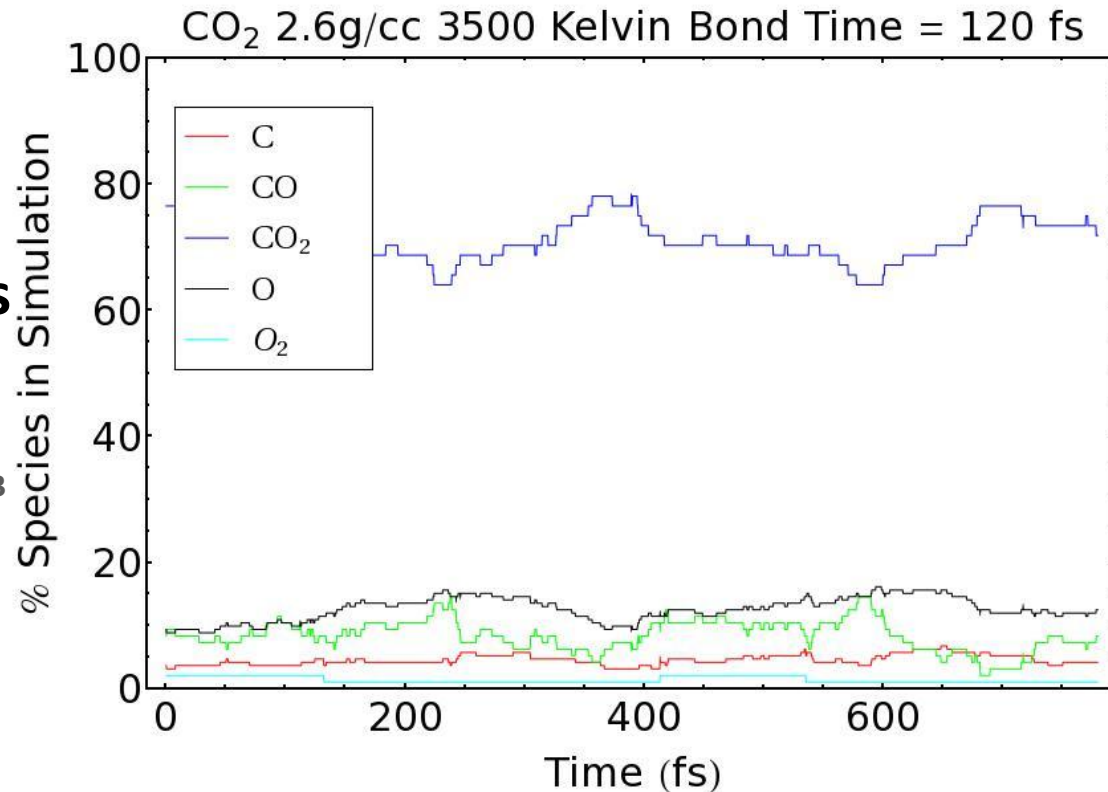
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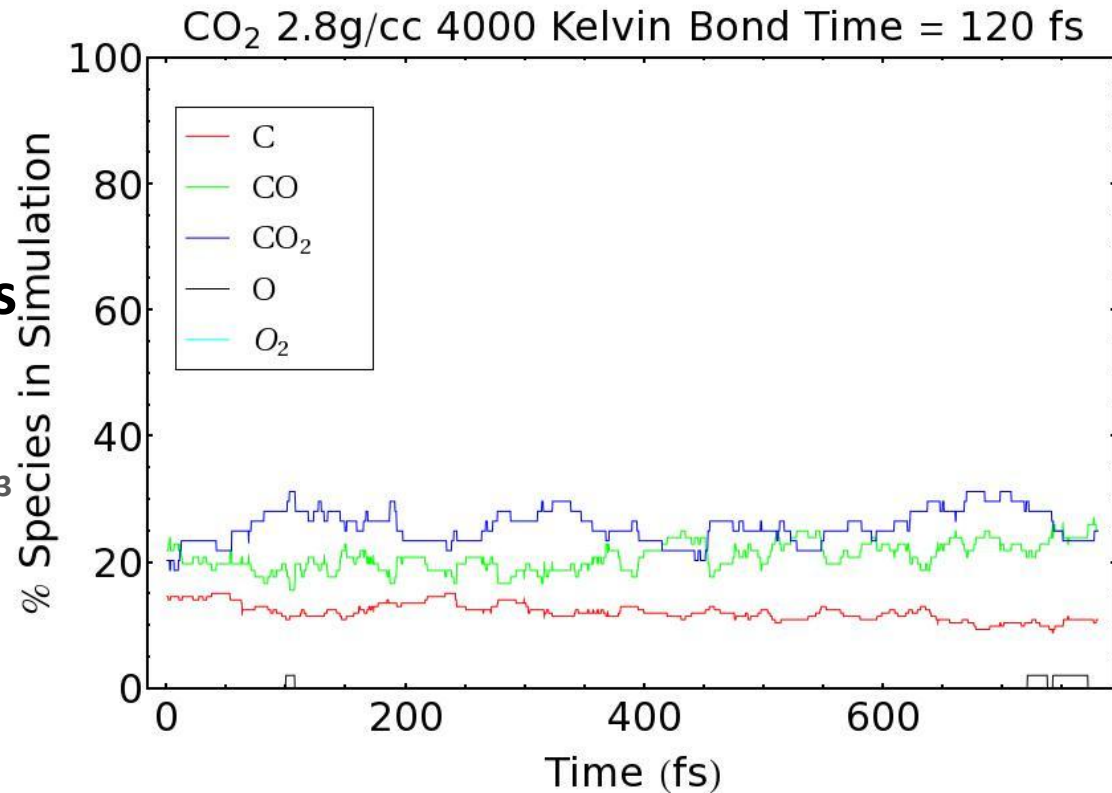
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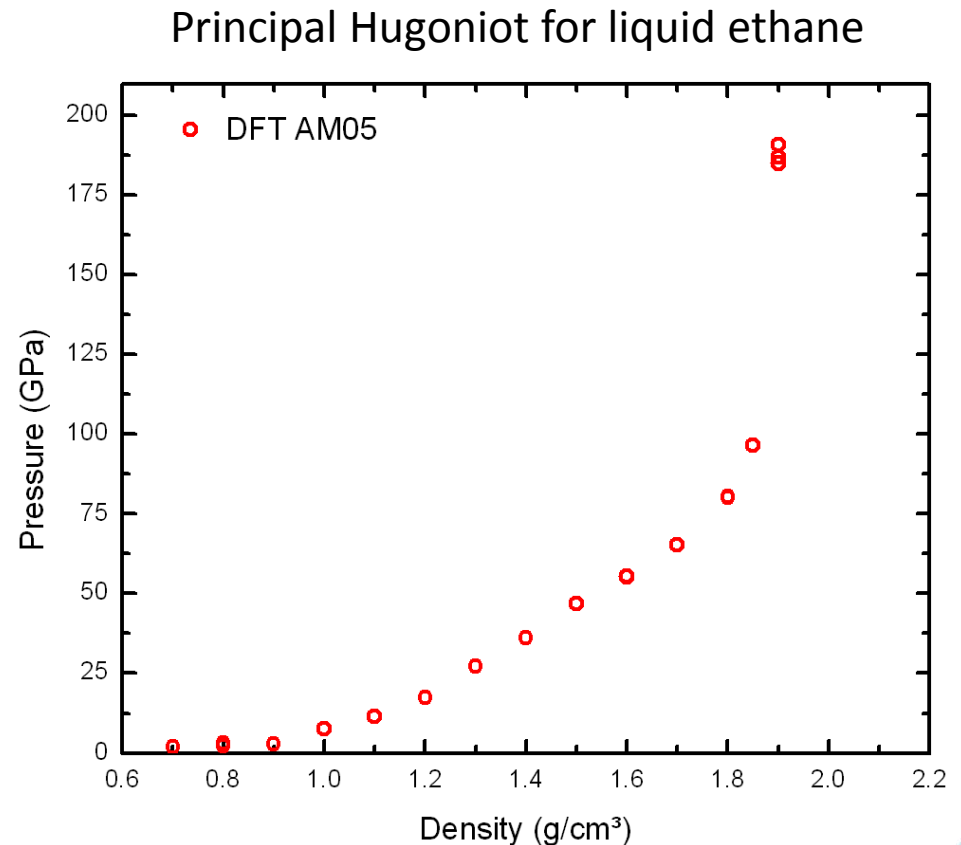


Chemical composition during the last 800 fs of a simulation

DFT/QMD simulations predicted the Hugoniot for ethane – shoulder at 50 GPa followed by a sharp rise

- **DFT simulations**

- 64 molecules 512 atoms
- Complex k-point (0.25,0.25,0.25)
- 800/1600 eV plane-wave energy
- Well described shoulder/dissociation
- 0.56 g/cm³; 163 K initial state



See Kyle's poster for more results on hydrocarbons

Initial data from Z validates the DFT/QMD results – obtaining a shock pressure of 180 GPa

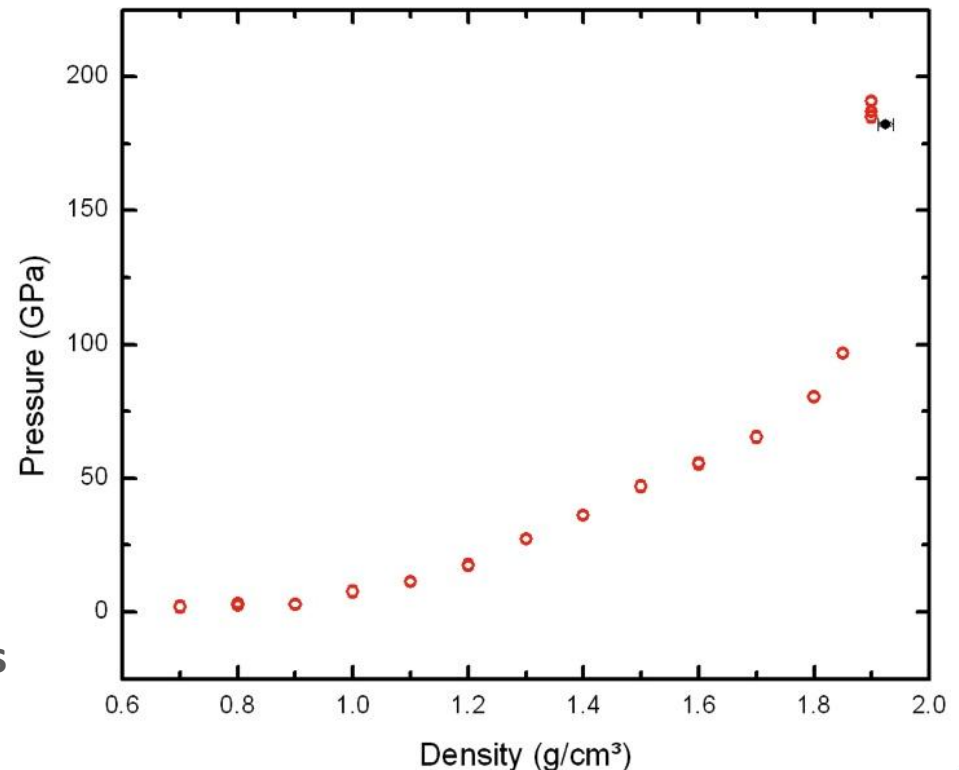
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- **Z-experiments**

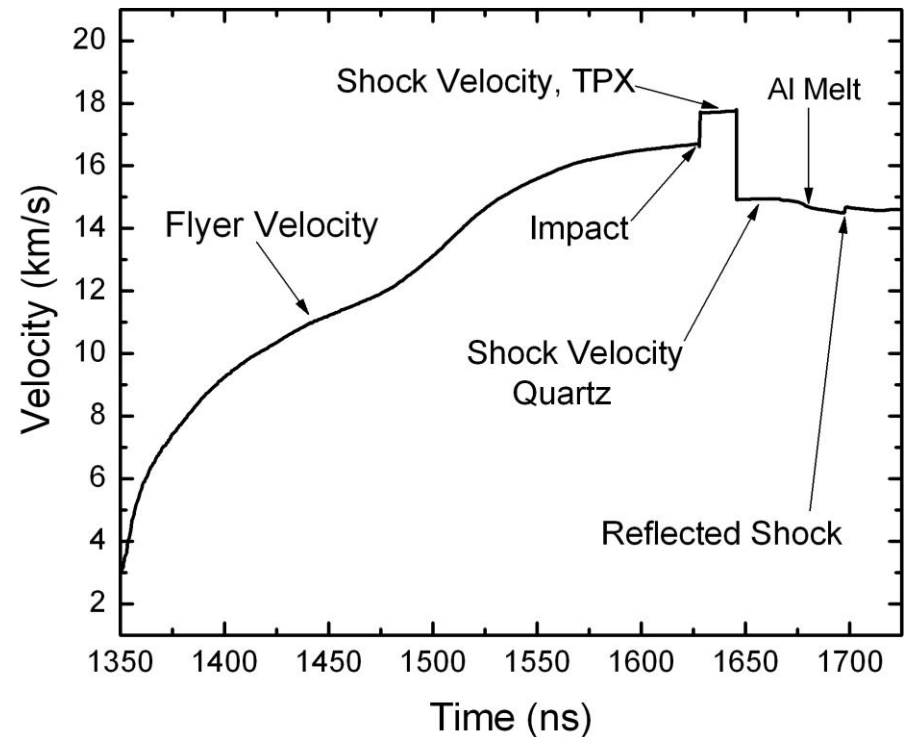
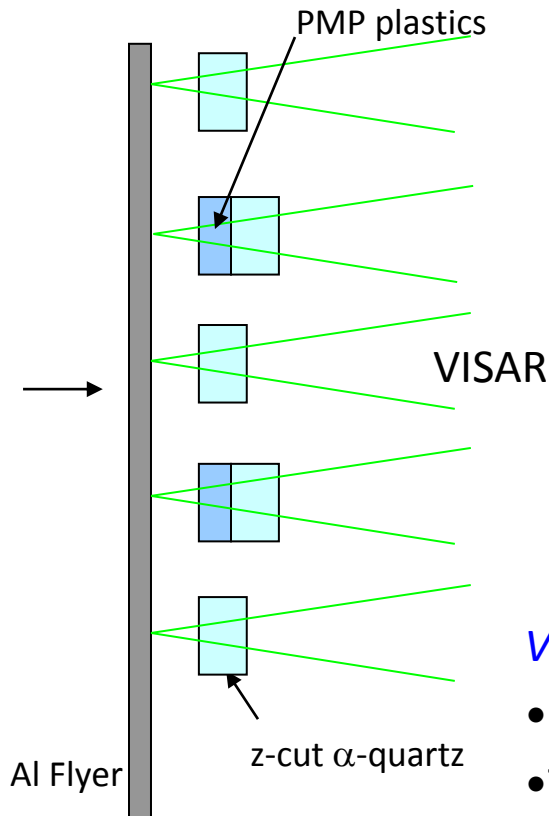
- Initial results at 180 GPa
- Will continue the experimental series
- Temperature measurements using optical pyrometry – analysis in progress will add new data to EOS comparisons

Principal Hugoniot for liquid ethane



See Kyle's poster for more results on hydrocarbons

We measure shock velocities in plastic and other transparent materials with sub-percent accuracy

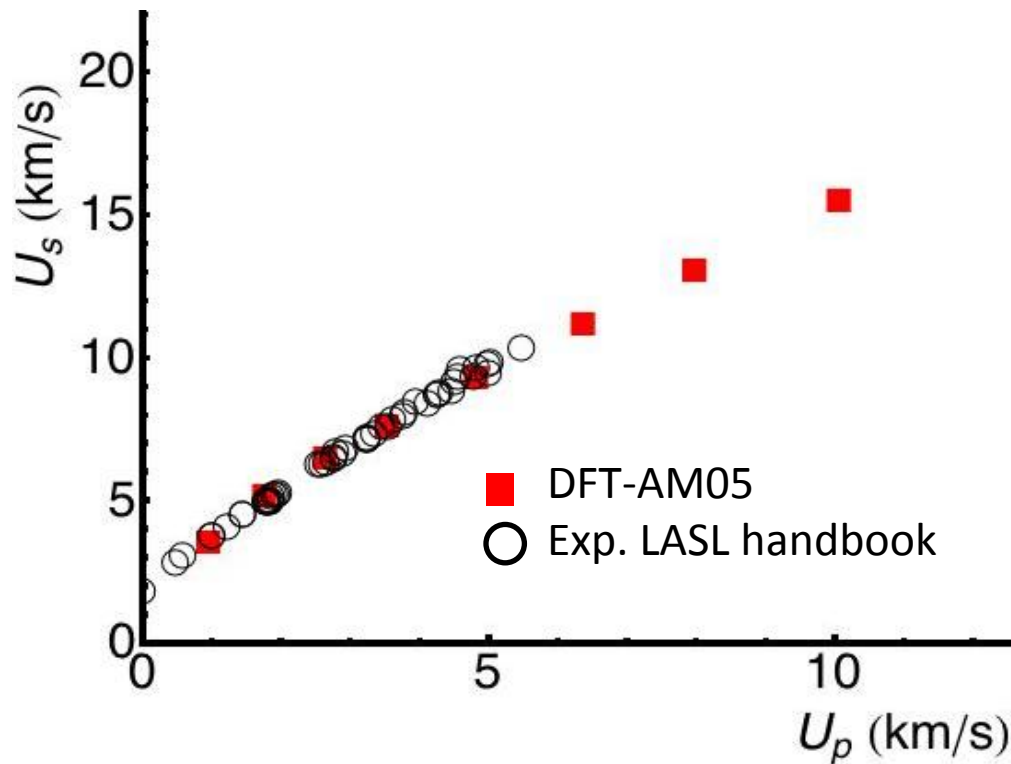


VISAR measurements as main tool:

- Flyer velocity
- Time of impact
- Shock arrival at plastics/quartz interface
- Shock velocity in sample and breakout time
- *Steady shocks, large samples, and long times yield high precision measurements*

DFT-AM05 is of high fidelity for shock compression of poly(4-methyl 1-pentene) (PMP) to 50 GPa

Principal Hugoniot for poly(4-methyl 1-pentene)

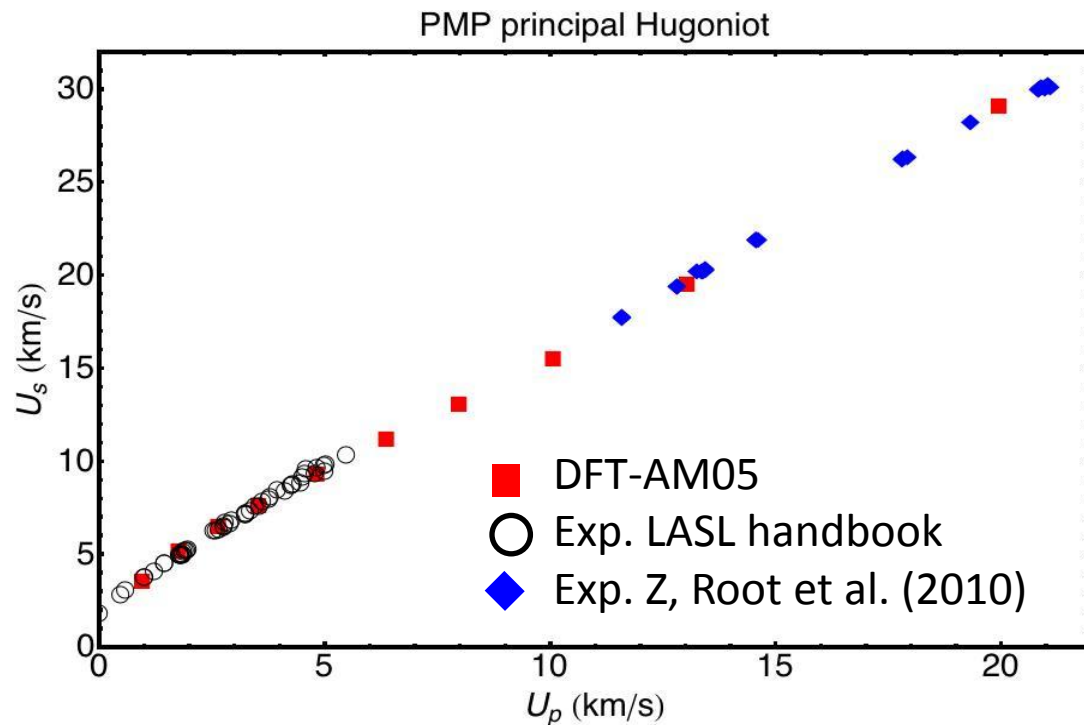


- 440 atom simulations
- DFT-AM05 is of high fidelity also for PMP
- Curvature for low shock speeds

T.R. Mattsson et al. Phys. Rev. B **81**, 054103 (2010).

Results from recent shock experiments on Z for poly(4-methyl 1-pentene)

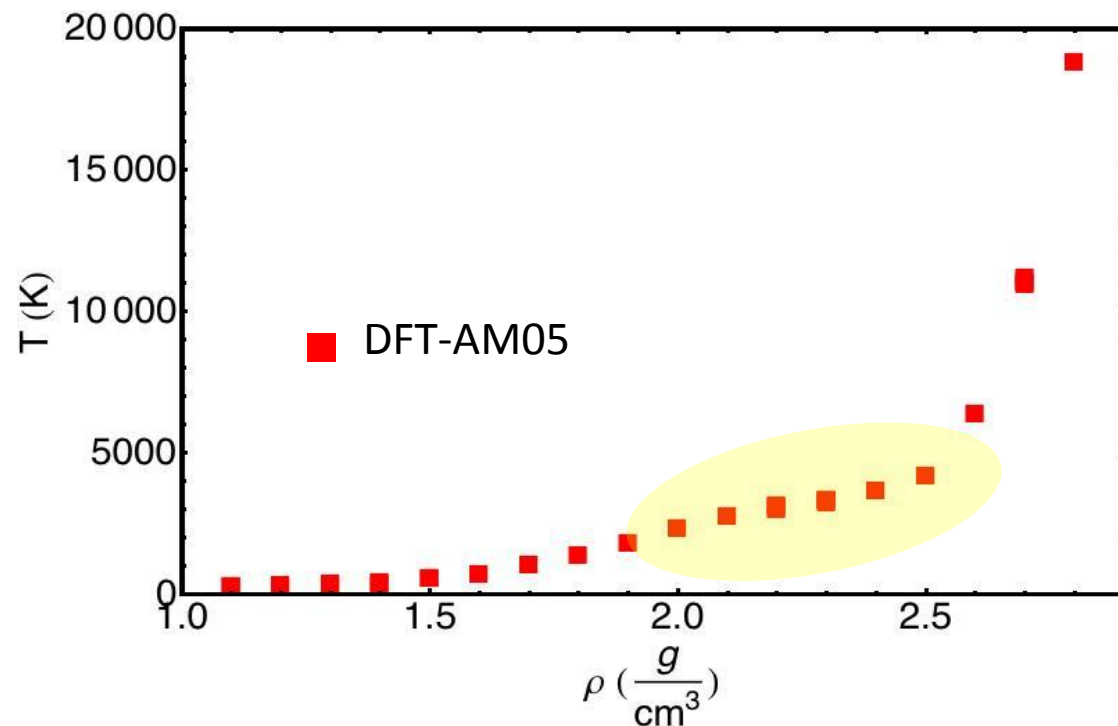
Principal Hugoniot for poly(4-methyl 1-pentene)



- Shock experiments up to 30 km/s shock velocity
- 200 – 530 GPa pressure
- *Also polymers can be modeled with high fidelity using DFT-AM05*
- Promising for extending beyond plastics to foams

Simulations allow a detailed analysis of the physics and chemistry of shock compression of hydrocarbon polymers

Temperature along the Hugoniot for polyethylene

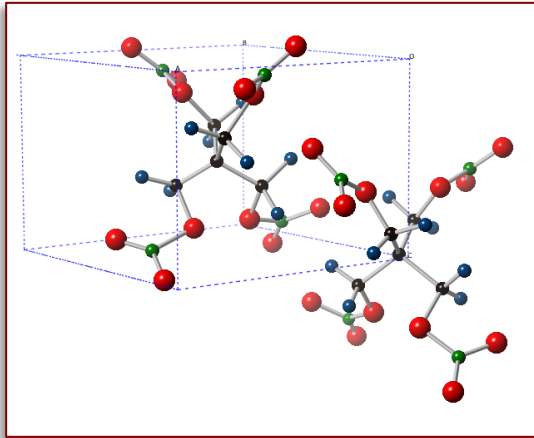


- Temperature is the missing link in P/rho; U_s/U_p analysis
- *Temperature almost flat during the shoulder in pressure*
- Detailed modeling of chemistry during the shock compression
- *Temperature measurements are being introduced on Z*

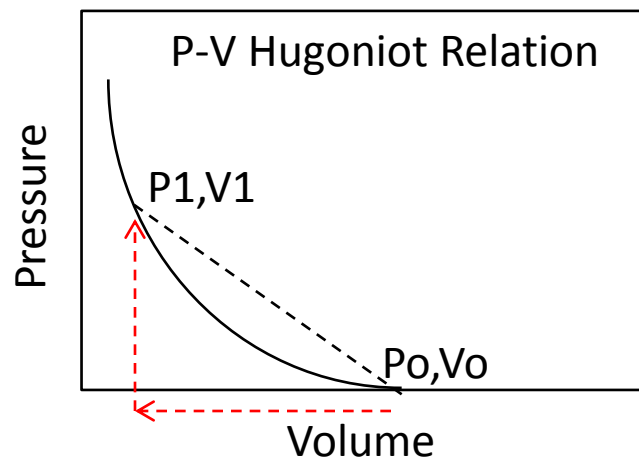
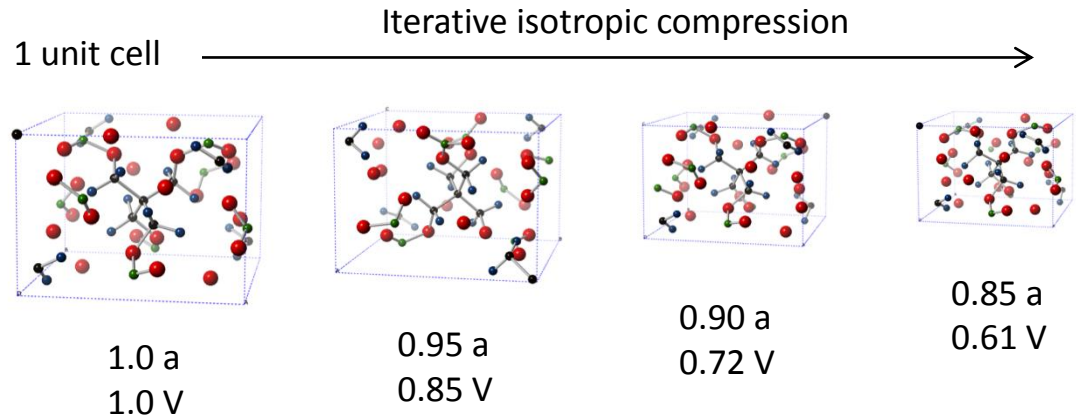
T.R. Mattsson et al. Phys. Rev. B 81, 054103 (2010).

We compress PETN in the simulations and tune the temperature to locate the Hugoniot State (P,T,E)

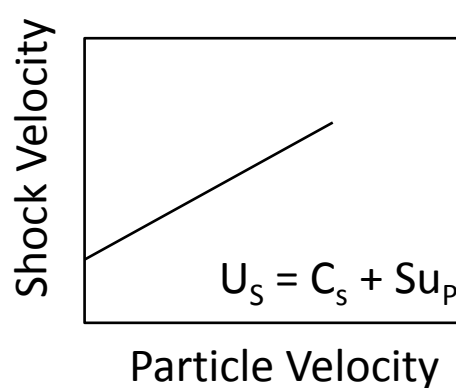
Density Functional Theory based
Molecular Dynamics (DFT-MD)



PETN, V_0 at 300K



$U_s - u_p$ Hugoniot Relation

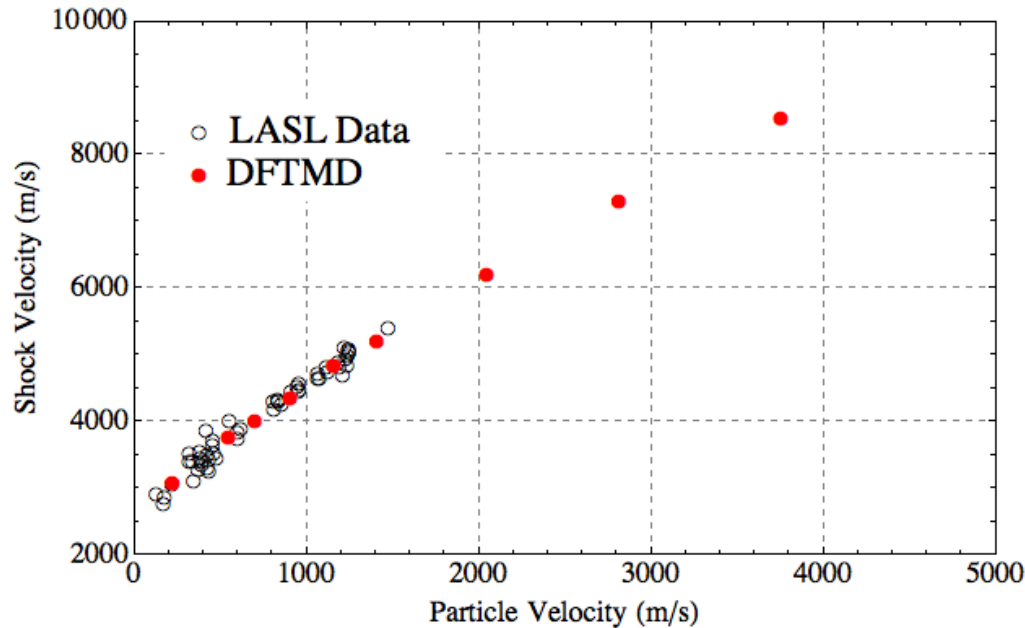


Mass Momentum Energy

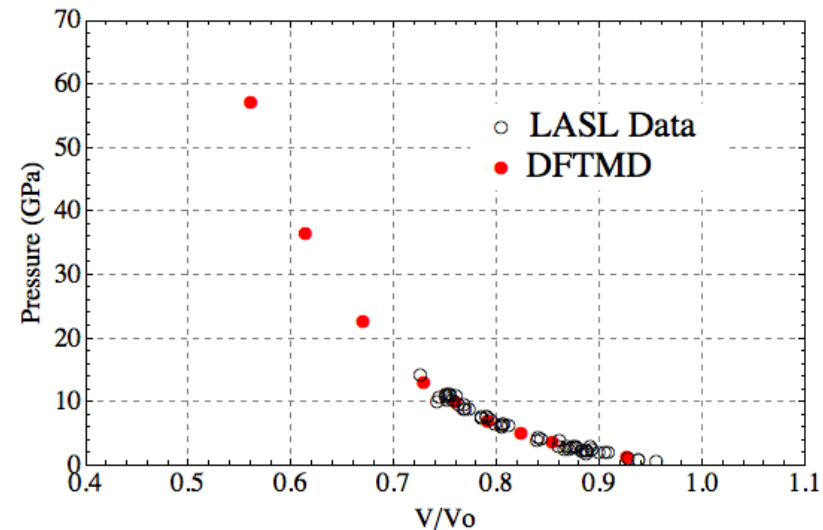
$$\begin{aligned} \rho_0 D &= \rho_1 (D - u_1) \\ P_1 &= \rho_0 D u_1 \\ E - E_0 &= \frac{1}{2} (P + P_0) (V_0 - V) \end{aligned}$$

Employed DFT-MD to calculate the PETN crystalline Hugoniot to 60 GPa; validating the approach to LASL data

Single Crystal Data



P-V Hugoniot



We obtain the un-detonated Hugoniot well above experimentally accessible regimes and reproduce low-pressure data

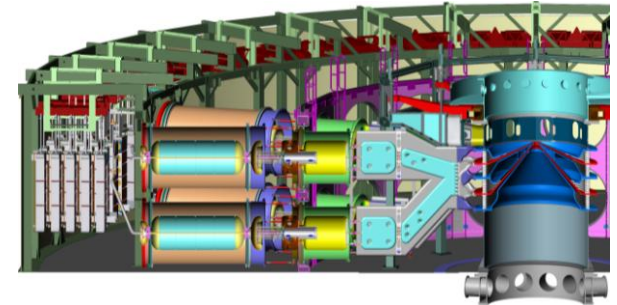
Ryan Wixom's poster yesterday and Mattsson, Wixom, Mattsson, Proceedings to the 14th international Detonation Symposium (2010).

Integration of DFT/QMD and high-precision multi-Mbar experiments on Z serve as a solid foundation for understanding chemistry in dynamic extremes

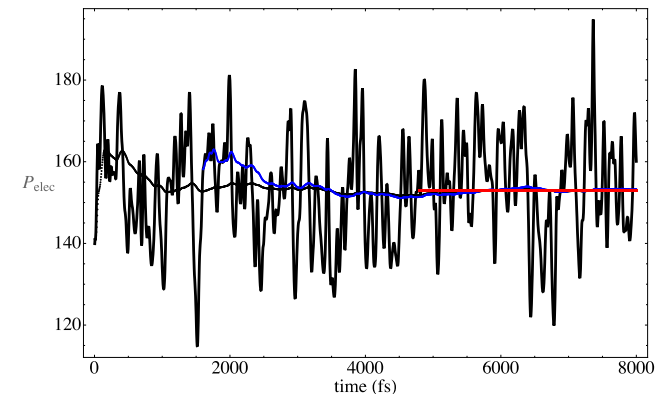
- Employed DFT based MD simulations to model shock compression of CO_2 , C_2H_6 , CH_2 , and PETN
 - Agreement with existing data
 - Confirm a CO_2 dissociation plateau at 60 GPa
 - Predictions for shock compression to 500 GPa in CO_2
 - Steep rise in shock pressure following the dissociation region for several materials with chemistry
- Executed experiments on Z to measure the shock Hugoniot of CO_2 , C_2H_6 , and CH_2
 - High-precision measurements can distinguish between different EOS models
 - Broad platform for studying cryogenic liquids up to initial pressures of 1 MPa
 - Temperature measurements coming online - exciting

Acknowledgments

- The large team operating the Z-machine – Mike Lopez
- The cryogenic team – Dave Hanson, Andrew Lopez, Keegan Shelton, and Jose Villalva
- Sandia High-Performing Computing – Sophia Corwell
- Program leadership – Dawn Flicker and Mark Herrmann
- Scientific leadership – Mike Desjarlais



Shock experiments on Sandia's Z machine



Density Functional Theory simulations