

# Simulations and Theory of Model Microtubule Self-Assembly

**Shengfeng Cheng and Mark Stevens**

Sandia National Laboratories

**Ankush Aggarwal**

University of California Los Angeles

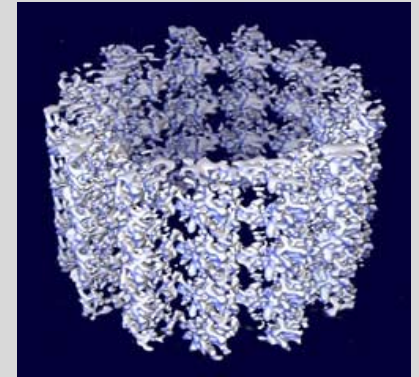
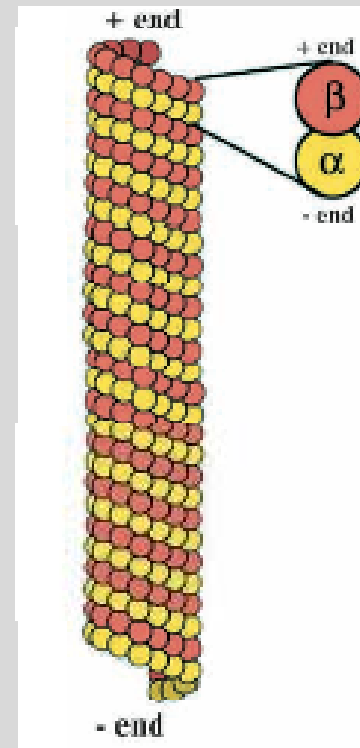
[arXiv:1201.2328: Self-assembly of artificial microtubules]

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# Microtubules and Tubular Structures

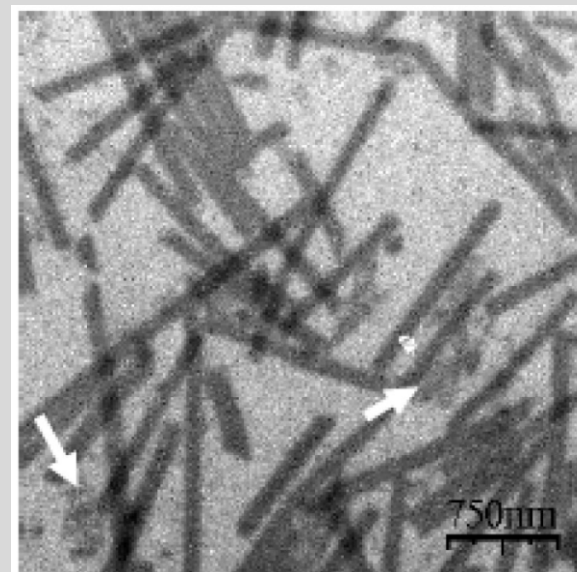
- monomer is  $\alpha$ - $\beta$  tubulin
- binding involves GTP/GDP
- tube contains 13 protofilaments
- polymerization/depolymerization  
catastrophe  
polarity
- $\gamma$ -tubulin is a nucleation seed



microtubule

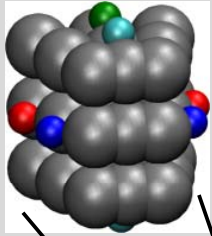
- Tube-like structures of  
S-layer proteins  
amphiphilic macromolecules  
coiled nanofibers

...



SEM of tubelike  
S-layer structures  
(Bobeth et al.  
2011, Langmuir)

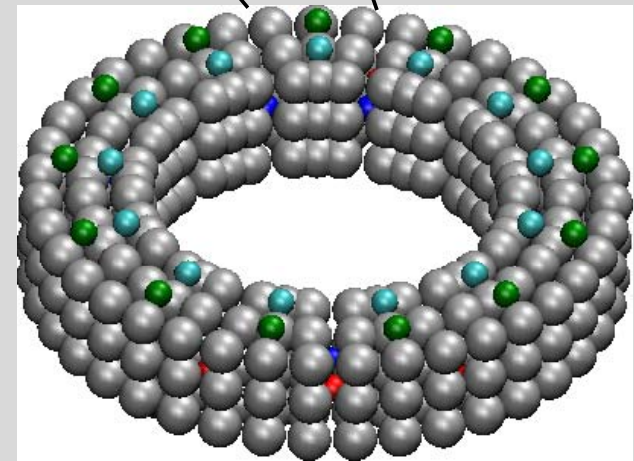
# We use wedges as building blocks in MD simulations



**rigid body**  
**6 dof  $\rightarrow$  3 kT**

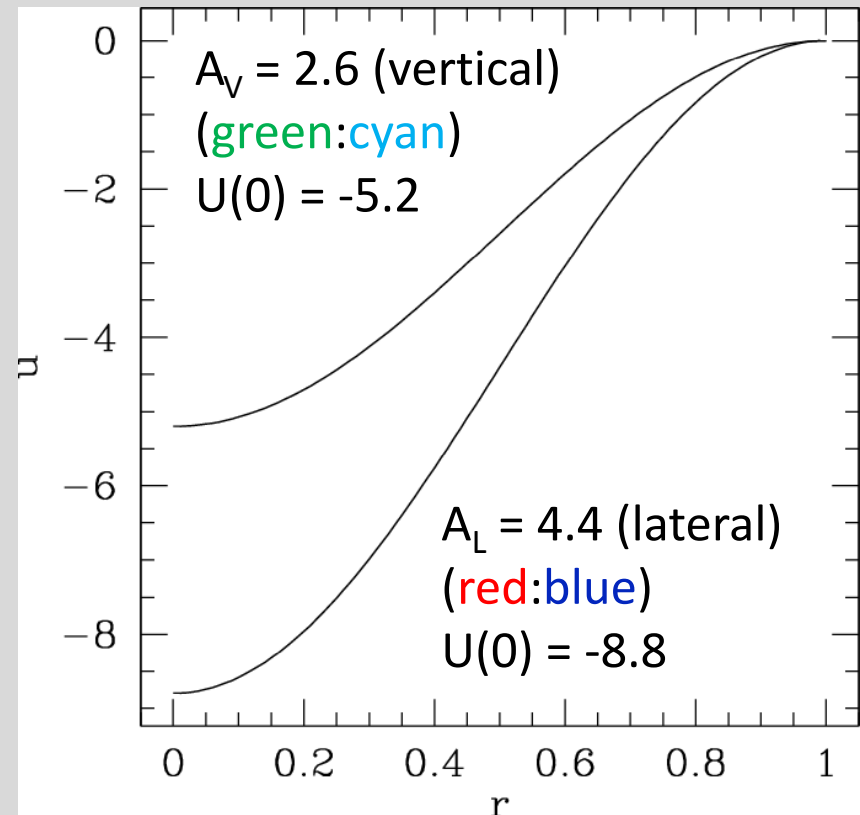
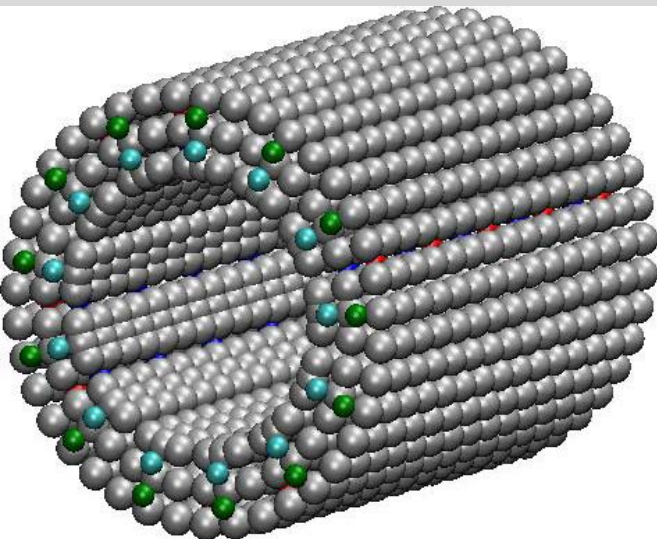
wedge particle

- similar to Rapaport for virus capsids
- designed to produce rings
- rings stack into tubes (13 wedges per ring)
- attraction only between specified sites
- gray particles interact purely repulsively



**soft potential**

$$U(r) = A \left[ 1 + \cos \left( \frac{\pi r}{r_c} \right) \right]$$
$$U(0) = 2A$$



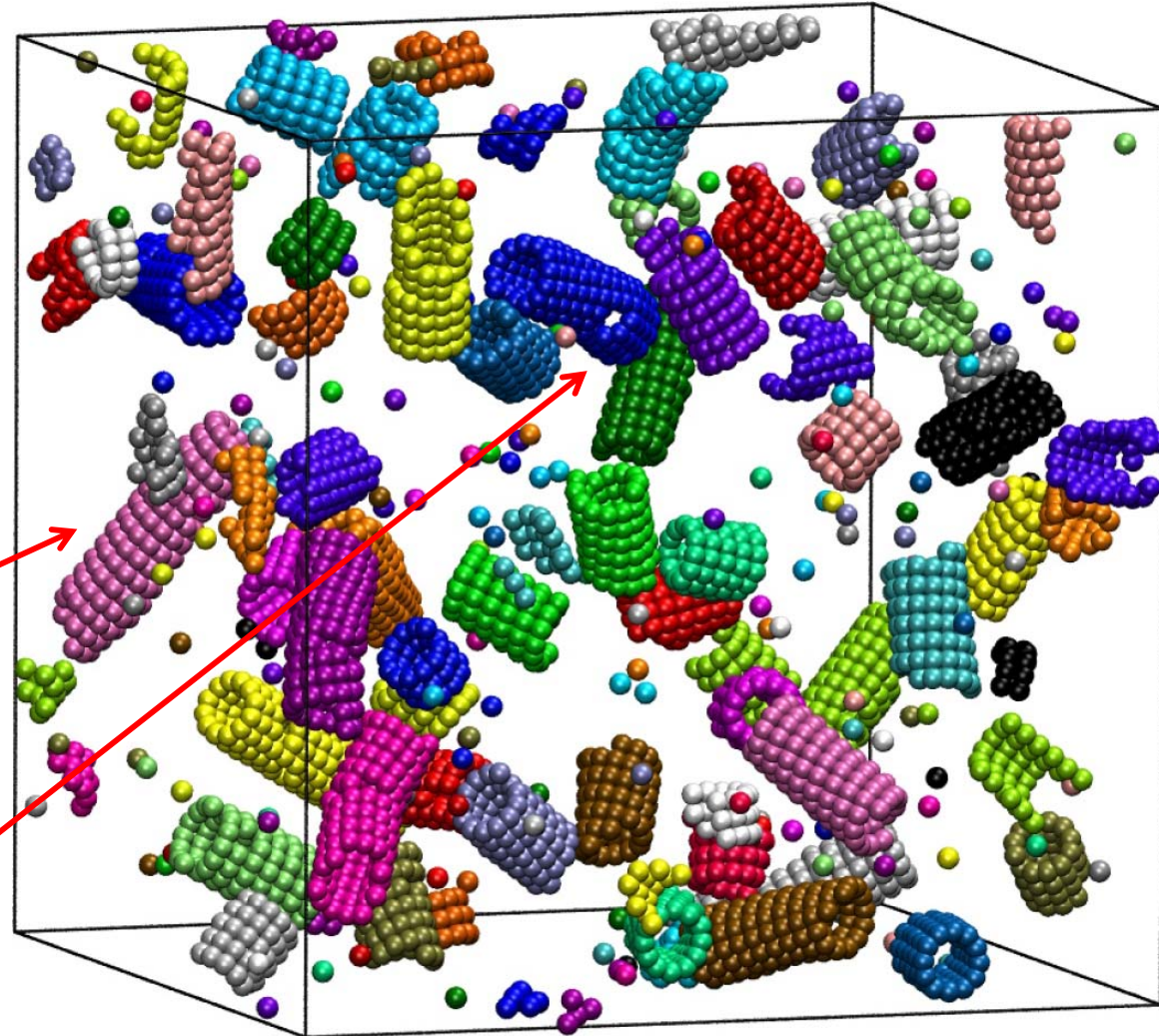


# Self-Assembly of Wedges: An Example

$A_L = 4.4$  and  $A_V = 2.6$   
monomer volume fraction  $\sim 4\%$   
5000 wedge monomers  
random distribution of monomers

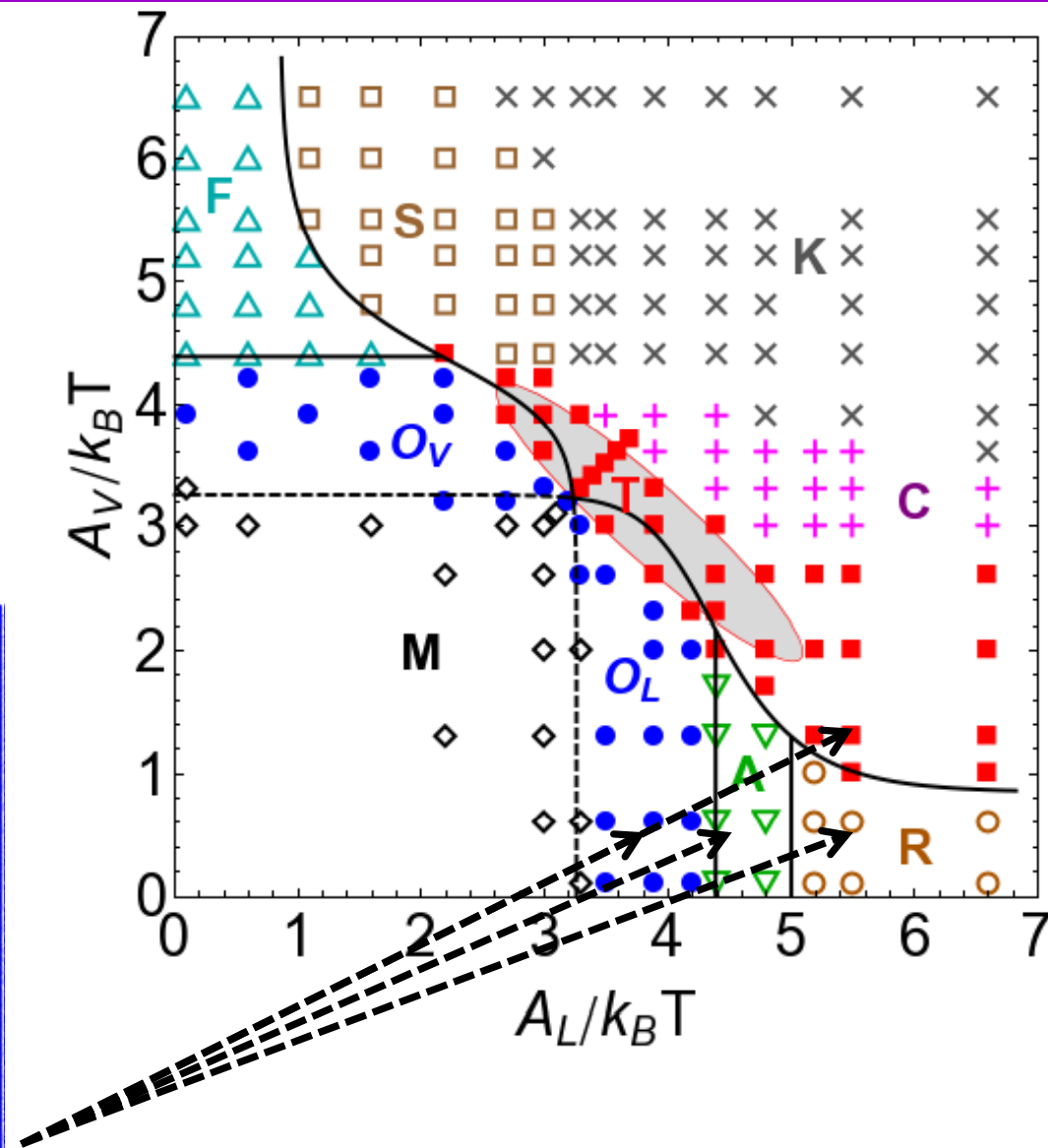
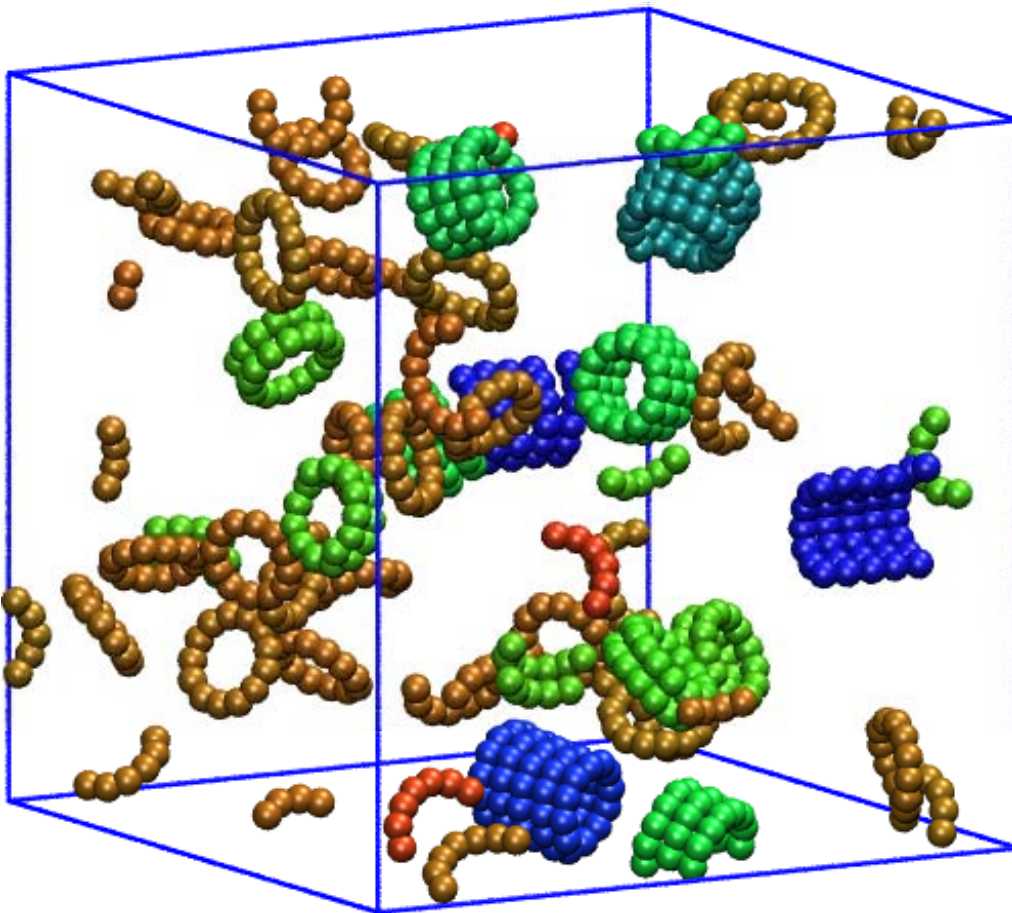
wedge shown as single particle  
clusters size  $> 12$  monomers

Many tubules & some fragments  
with rings/tubes



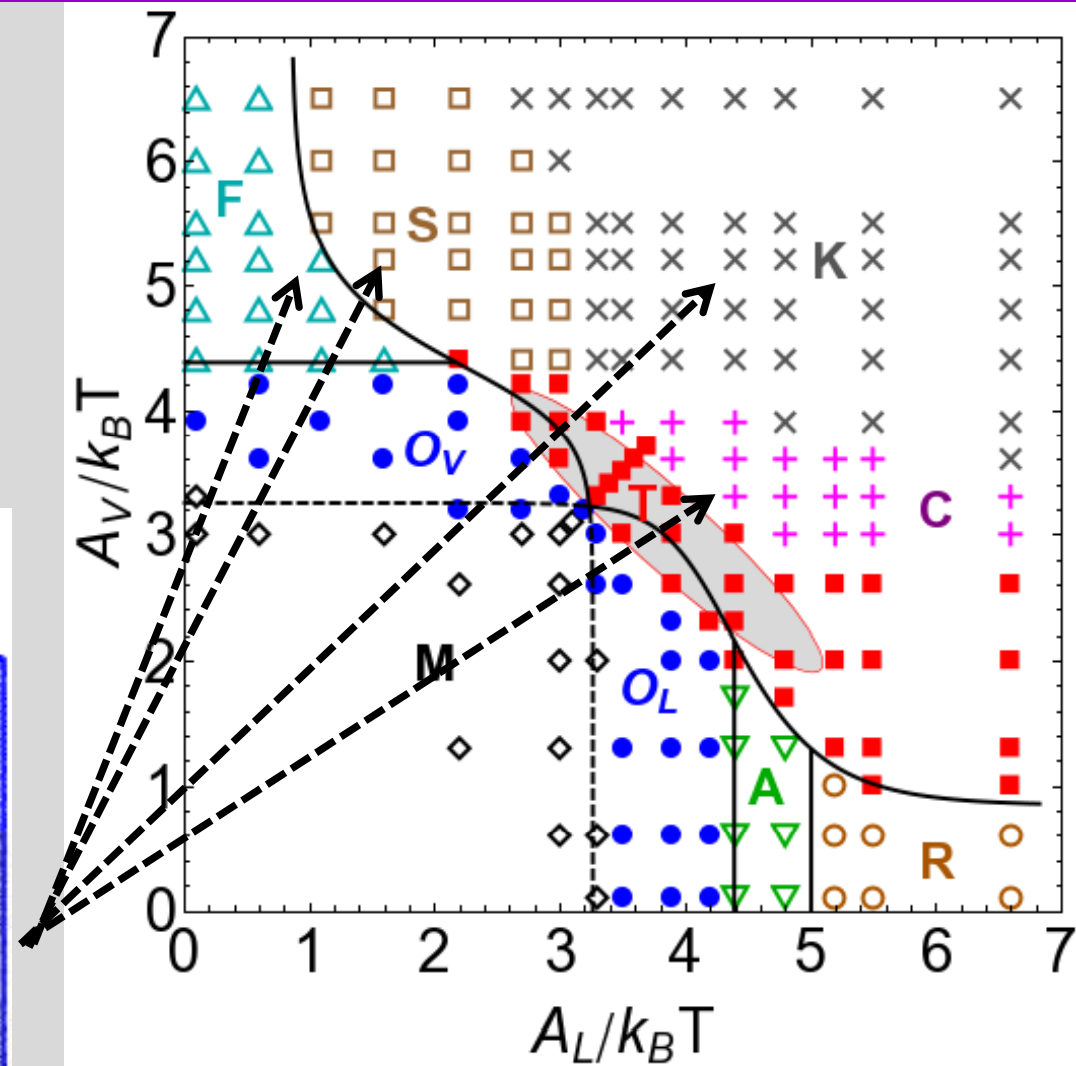
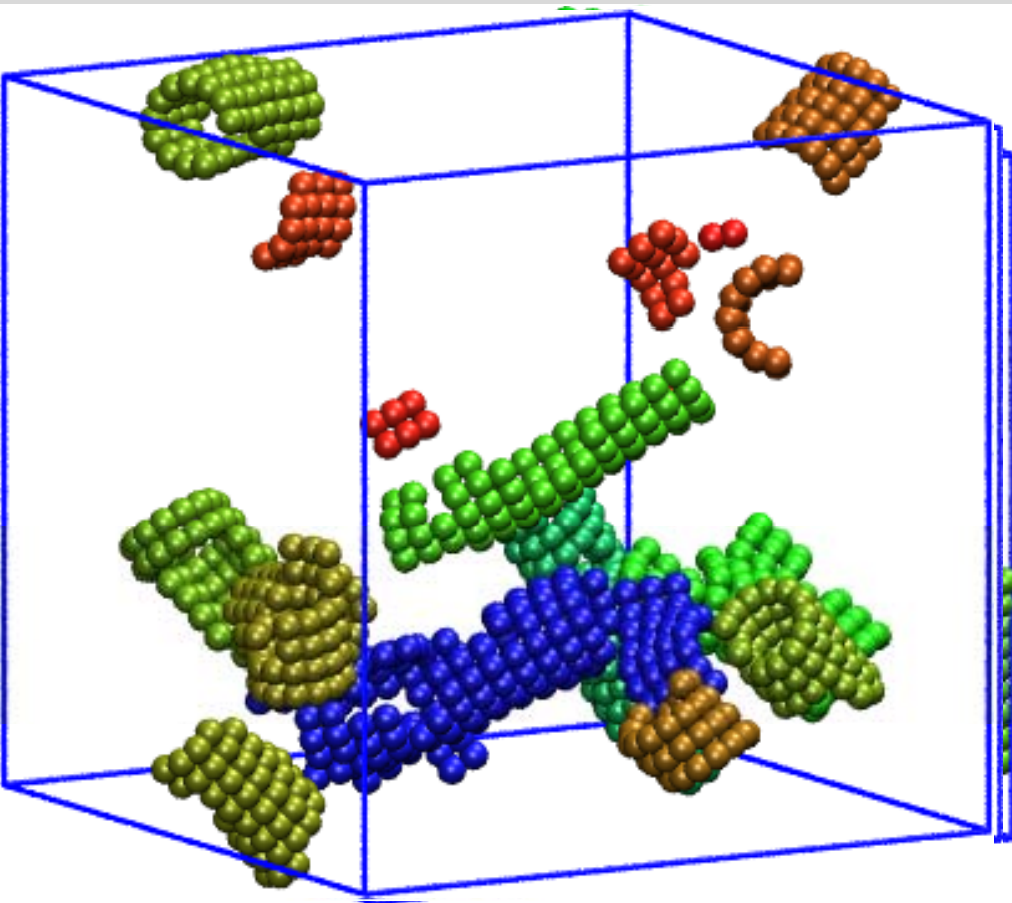
# Structure Diagram: Various structures can occur

$A_L = 3.9$  &  $A_V = 0.6$   
 a few (oligomers)



# Structure Diagram (continued)

**$A_L=4.4$  &  $A_V=5.2$**   
percolated cluster

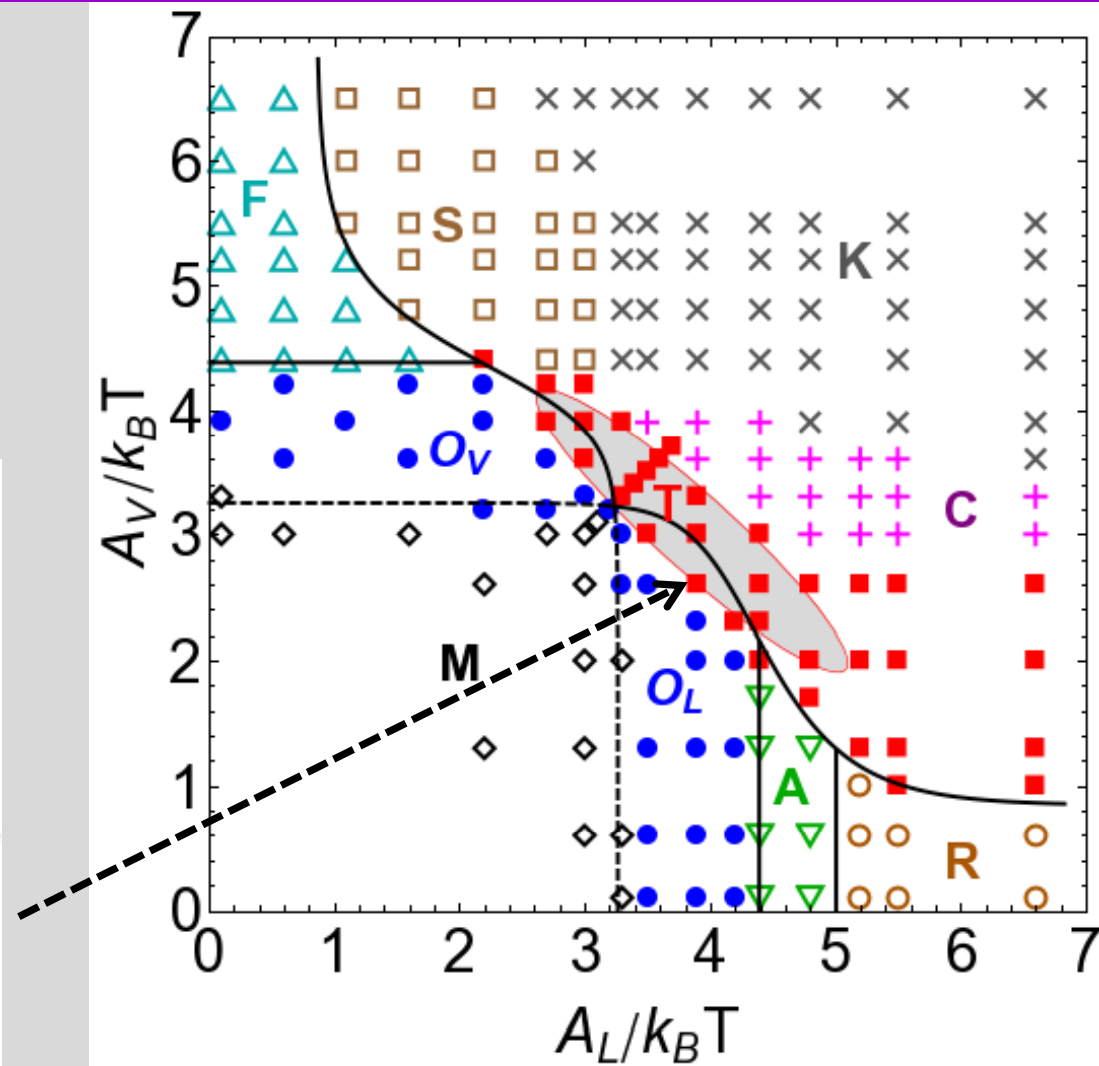
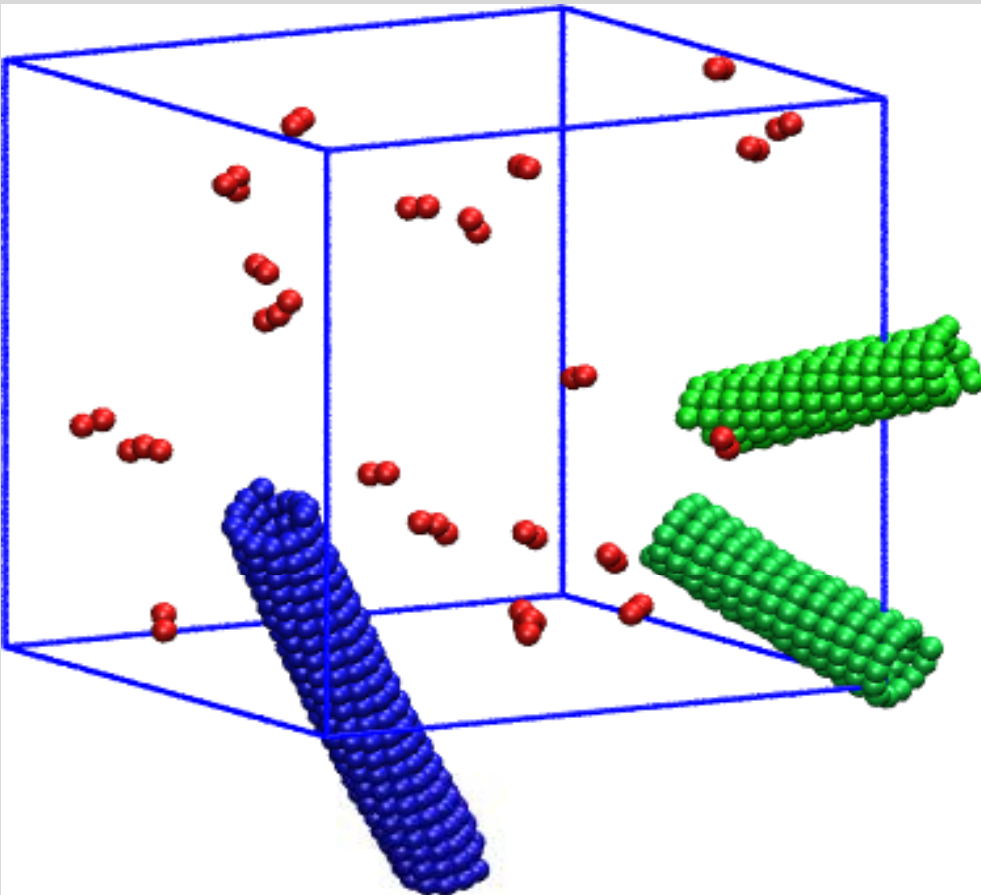




# Tubes are only formed in a narrow range of A

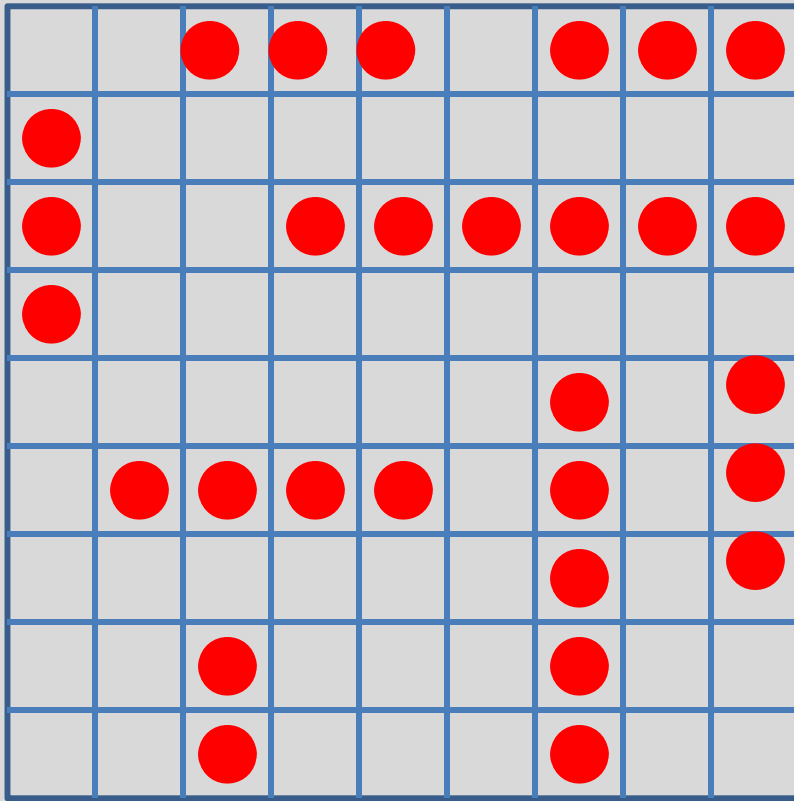
$$A_L=3.9 \text{ \& } A_V=2.6$$

defect-free tubes (helical)



Reversibility of bonding is essential to remove defects by allowing structural rearrangements

# A Flory-Huggins type lattice theory is developed to describe (straight) polymerization of wedges



When  $A_L = 0$ , wedges can only form straight chains through vertical bonding  $\rightarrow$  straight polymerization

$p$  : filament length

$n_p$  : number of filaments with length  $p$

$g$  : binding energy for each bond

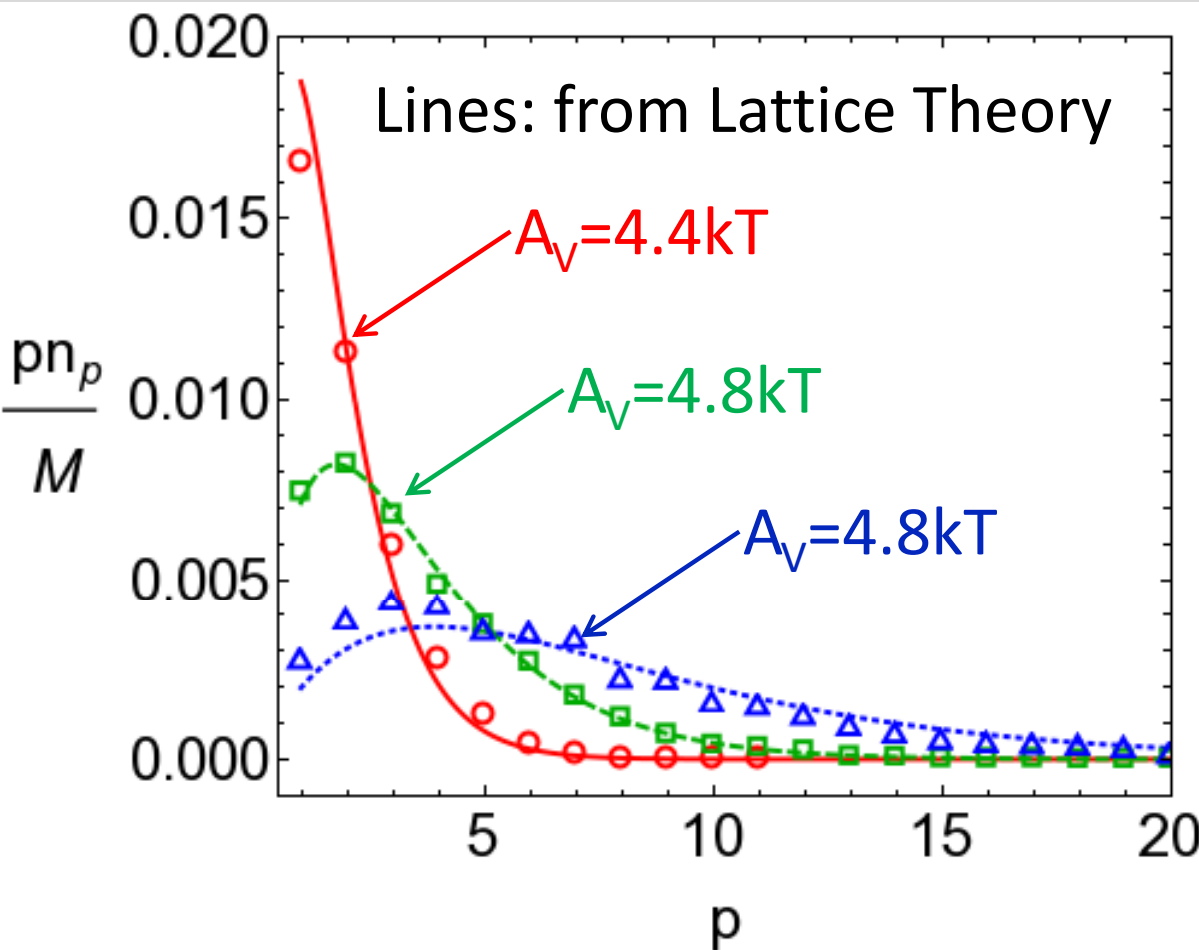
$$F = \sum_{p=1}^{p_{\max}} n_p \left( \underbrace{(p-1)g}_{\text{enthalpic contribution}} - \underbrace{kT \ln z + kT \ln \frac{n_p}{M}}_{\text{entropic contribution}} \right)$$

enthalpic contribution

entropic contribution



# Mapping A in simulations to g in theory



$A_L = 0$   
(straight polymerization)

$p$  : filament length

$n_p$  : number of filaments  
with length  $p$

- Predictions of  $n_p$  from Lattice Theory depend on  $g$
  - Calculate  $n_p$  in simulations at various  $A_V$
- Mapping between  $A_V$  and  $g$

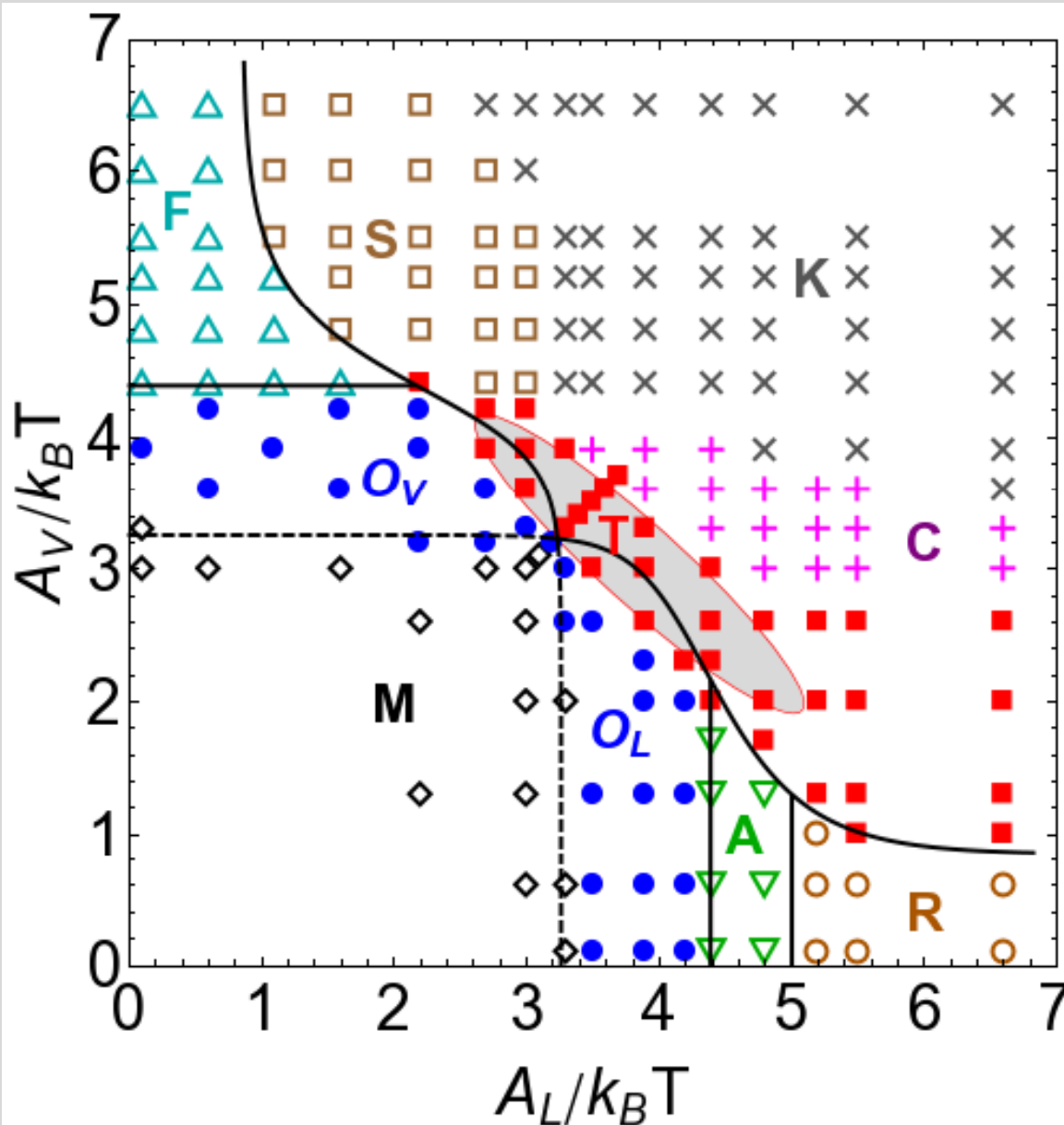
$$g = 4A - 3.4 - 9.6$$

2 attractive sites  $\times 2A$

thermal fluctuations

energy barrier

# Lattice theory explains structure diagram quite well



- Lattice theory for straight polymerization → **formation of filaments/arcs/rings**
- Two filaments/rings need to overcome energy barrier  $\sim 9.6kT$  to assemble → **filaments join to form sheets or rings stack into tubes**
- Sheet/cluster states are non-equilibrium structures and outside range of lattice theory

# Conclusions

- wedges can self-assemble into tubules
  - model has basic level of features
- see helical structures more than nonhelical
- tubules only formed in a narrow range of interaction strengths → reversibility is crucial
- see rearrangement of monomers within clusters
  - important for defect removal
  - but not disassembly (need solvent?)
- lattice-type theory captures essential features of self-assembly