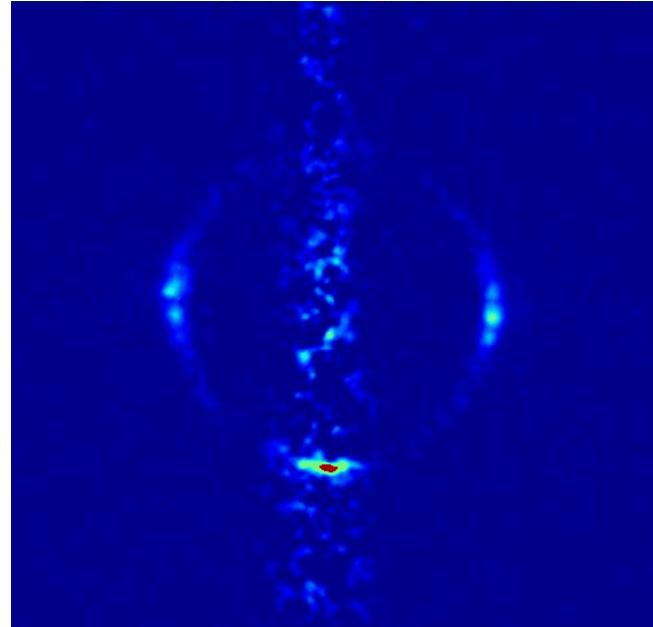


# Crossed Molecular Beam Studies of Scattering and DEFCOM Spectroscopy

SAND2012-5036C

**David W. Chandler, Kevin E. Strecker, Jeffrey J. Kay, and Jeff Steill**  
Sandia National Laboratories, Livermore, CA



**Sandia  
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# Outline

- Short History of Collisional Energy Transfer studies
- Description of Ion Imaging with Velocity Mapping for Inelastic scattering as backdrop.
- Quantum-State-Selective Inelastic Scattering
  - Differential cross sections for single rotational states
  - Scattering of Electronically excited states.
  - Scattering of Kr atoms ( $\mu$ Kelvin samples of atoms and molecules)
  - DEFCOM spectrometer: Dual-Etalon Frequency-Comb  
Spectrometer, A new way to do several sorts of spectroscopies.

# Short History of Collisional Energy Transfer

The modern concept of Potential Energy Surfaces came from thinking about collisional energy transfer. **Roger Boscovich (1711-1787)**

One of the great philosophical arguments at the time took place between the adherents of Descartes who—following Aristotle—thought that forces can only be the result of immediate contact and those who followed Newton and believed in his concept of force acting at a distance.

Imagine 2 equal bodies, one fast one (10m/s) gaining upon a slower one (5m/s). Upon collision the faster one will slow down and the slower one will speed up. How does this happen?

The change in speed can't be instantaneous Boscovich argued, as that would not be continuous and a body can't be going both faster and slower at same time. Therefore the change in speed must take some time but if the change only happens at contact then because they are moving at different speeds for a period of time, while in contact, then one would travel into the other, impossible. **Therefor repulsive interaction must take place over a small space and time.**

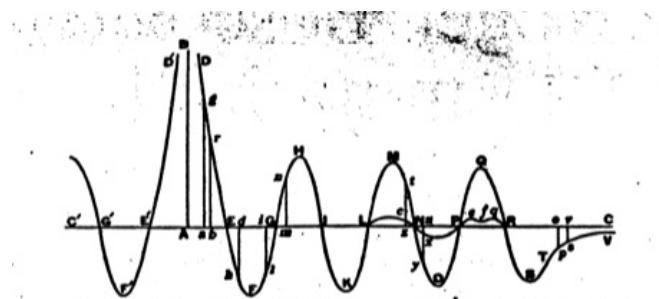
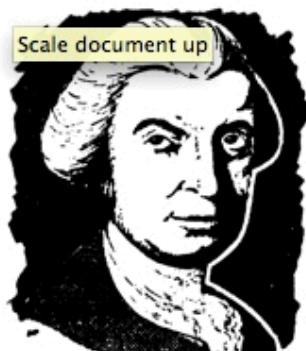
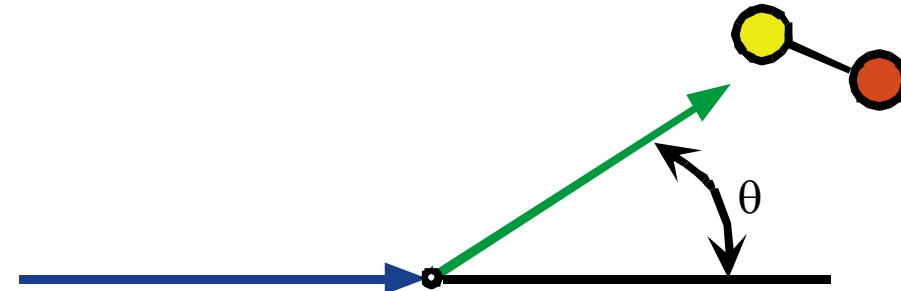


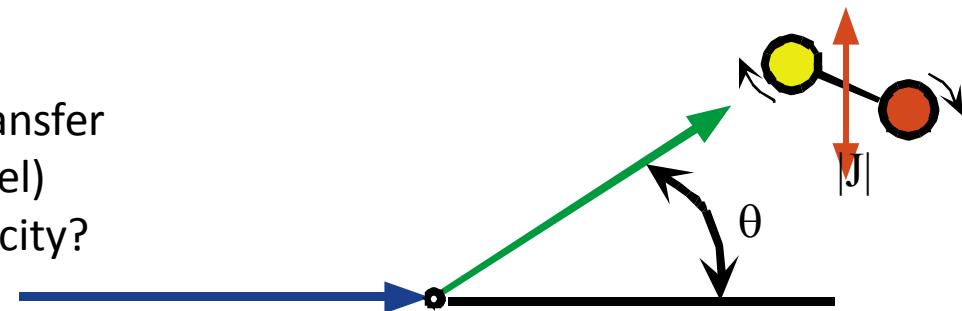
Diagram from Boscovich's "Theory of Natural Philosophy reduced to a single law of forces" showing the type of interaction between point atoms. There is a very large repulsion for close approach and an approximation to the inverse square law at large distances with several stable interatomic distances in between.

# Fast Forward a Few Hundred Years: A Molecular Dynamics Approach to Rotational Energy Transfer Collisions

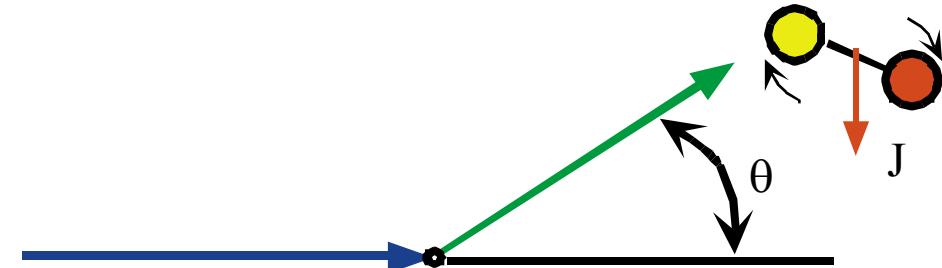
State-to-state Differential Cross Sections  
For NO+ Ar electronic and rotationally  
inelastic collisions (scattering angle)



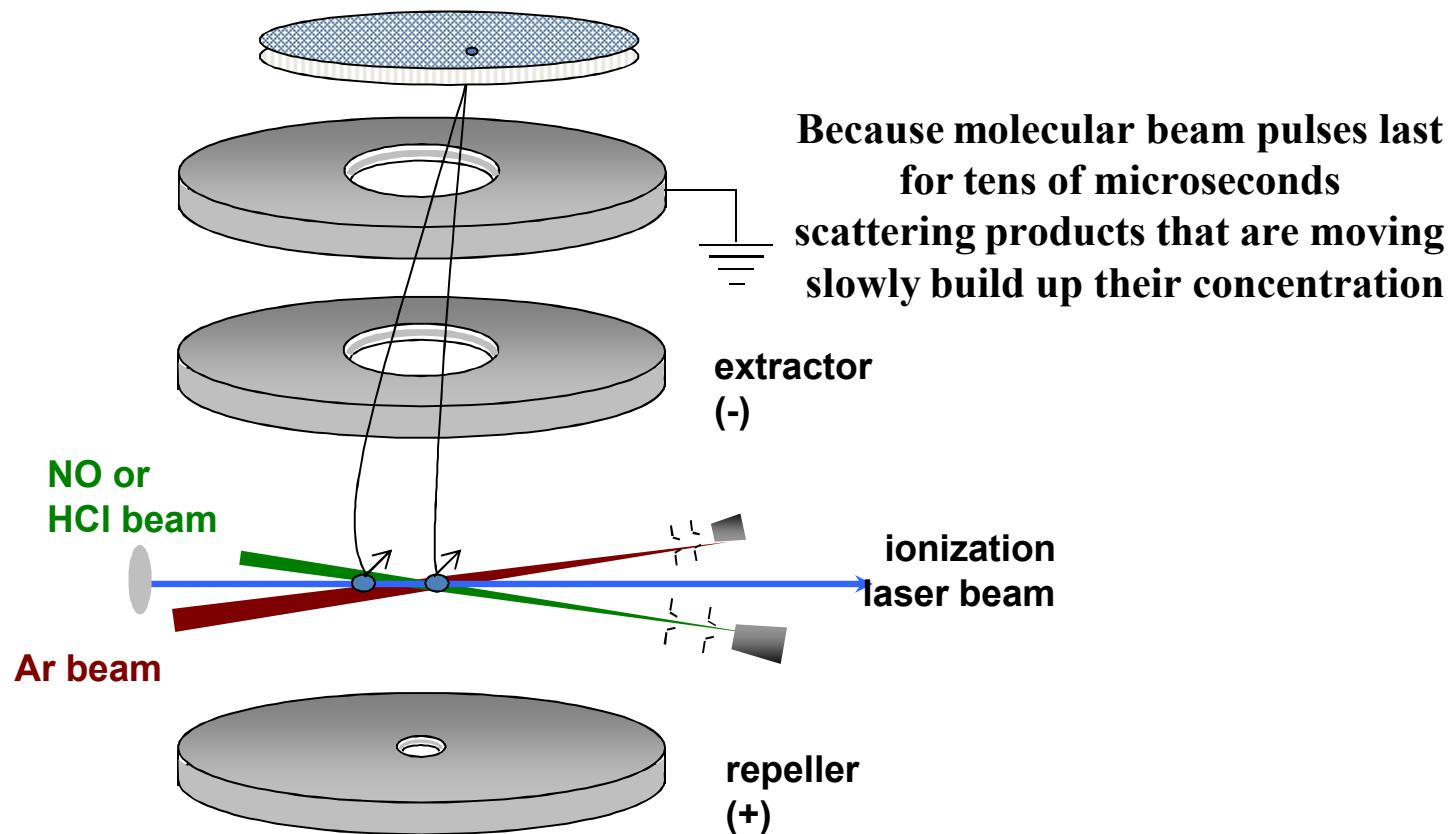
Rotational Alignment in Collisional Energy Transfer  
NO +Ar Products (Frisbee, propeller, cartwheel)  
How is J vector pointed relative to recoil velocity?



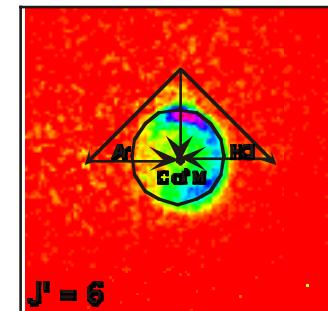
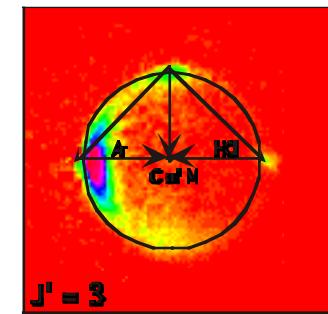
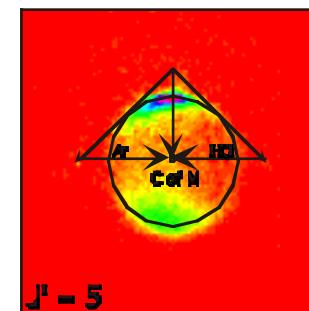
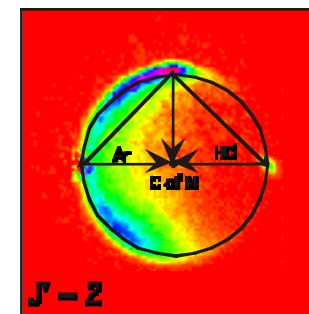
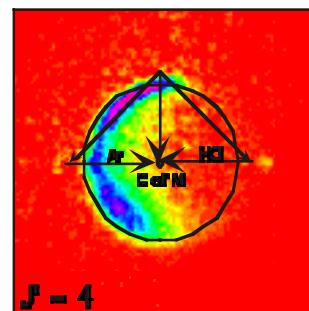
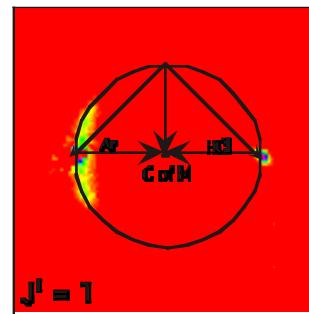
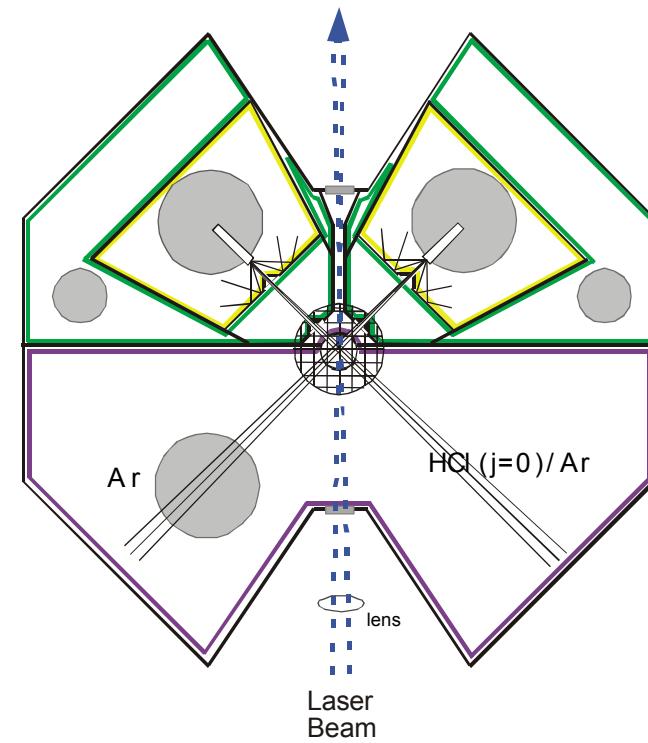
Rotational Orientation in NO +Ar  
Products (clockwise – counterclockwise)  
can also be measured, J vector up or down?

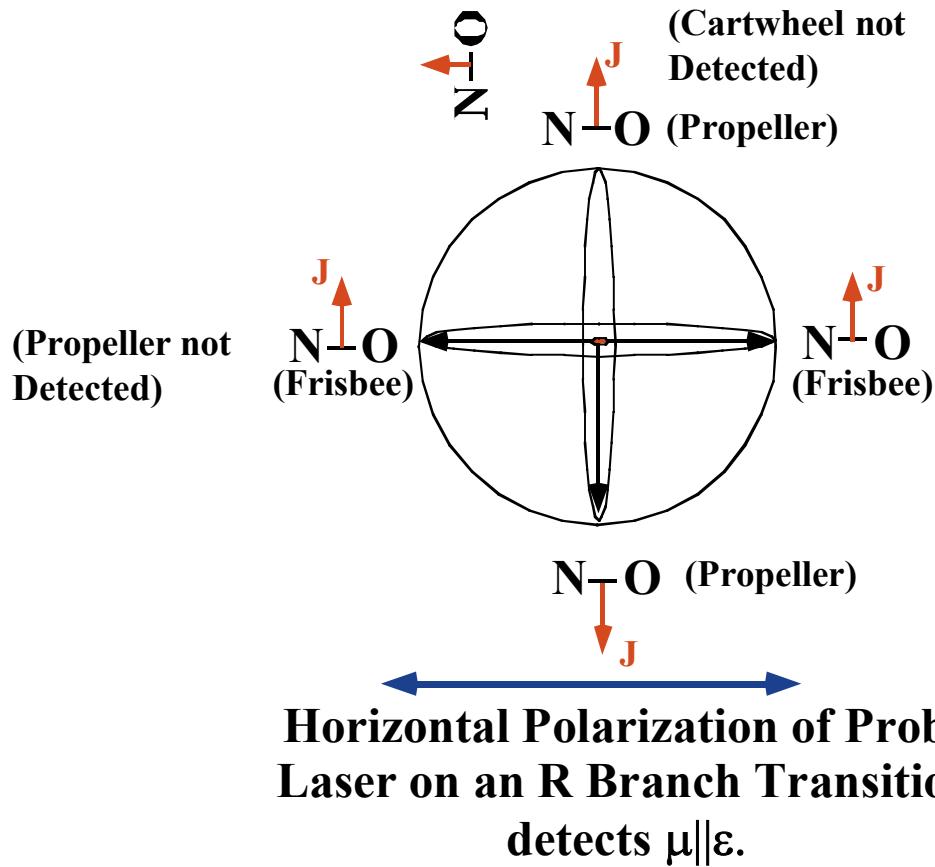


# Velocity Mapping is Very Important for Studying Bimolecular Reactions in Crossed Beam Arrangement With Ion Imaging.



A distorted view of the Differential Cross Section is directly measured.  
This is because products with different lab-frame velocities  
are detected with different efficiencies. Note even-odd alternation





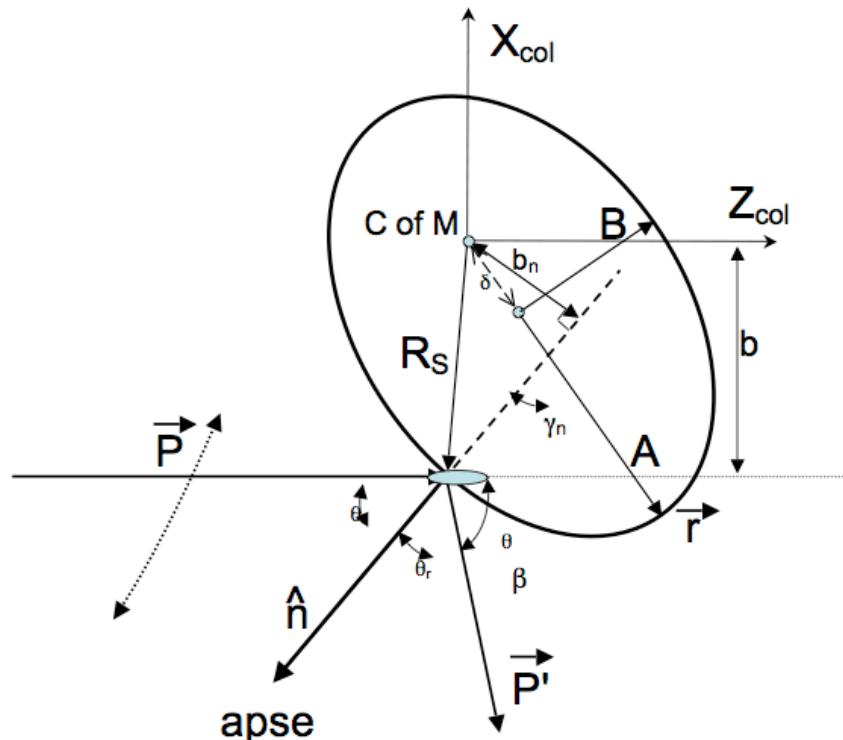
**The alignment is described by moments.....(Thanks you Dick Zare et al....)**

$$A^2_0(j') = J' \text{ along } z \text{ axis } 1 \text{ to } -1/2$$

$$A^2_{2+}(j') = J' \text{ along } X (3/4)^{1/2} \text{ or } Y (-3/4)^{1/2}$$

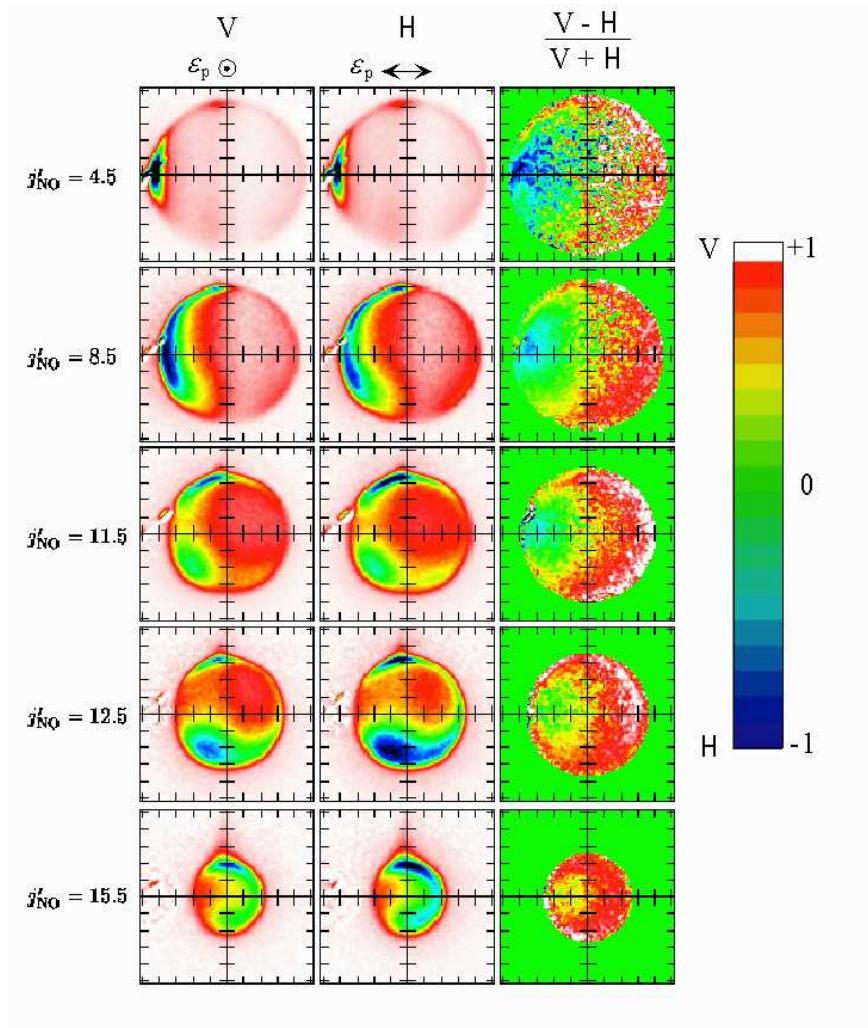
# Collisions at high collision energy can be thought of as hard and sudden.

The classical dynamics associated with hard ellipse scattering can be analytically described. The Apse vector is the vector along which angular momentum is transferred

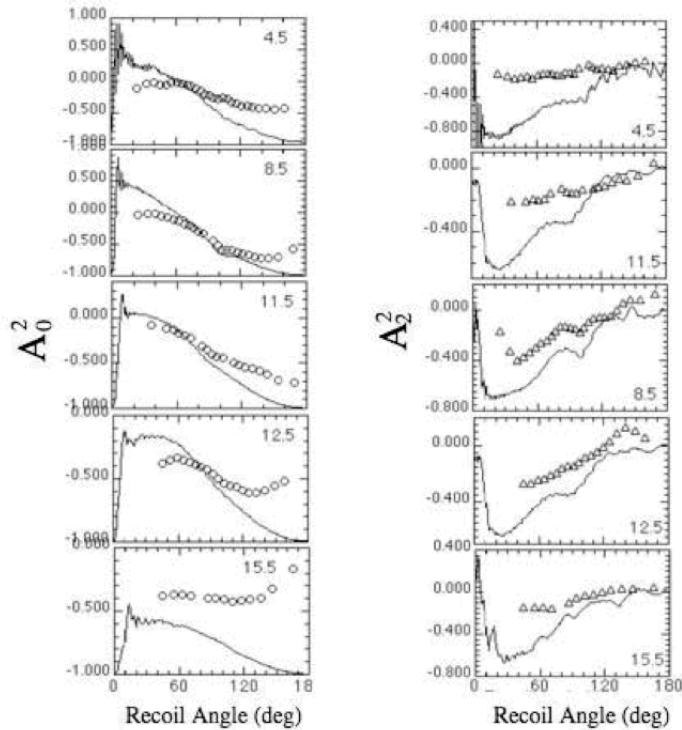


J cannot be transferred along the Apse angle.

- We take the difference between the vertical and horizontal images and normalize by the sum of the images to get an image we can fit using three alignment moments. We fit each line of data (top to bottom) with the moments. We can then plot the moments as a function of scattering angle.



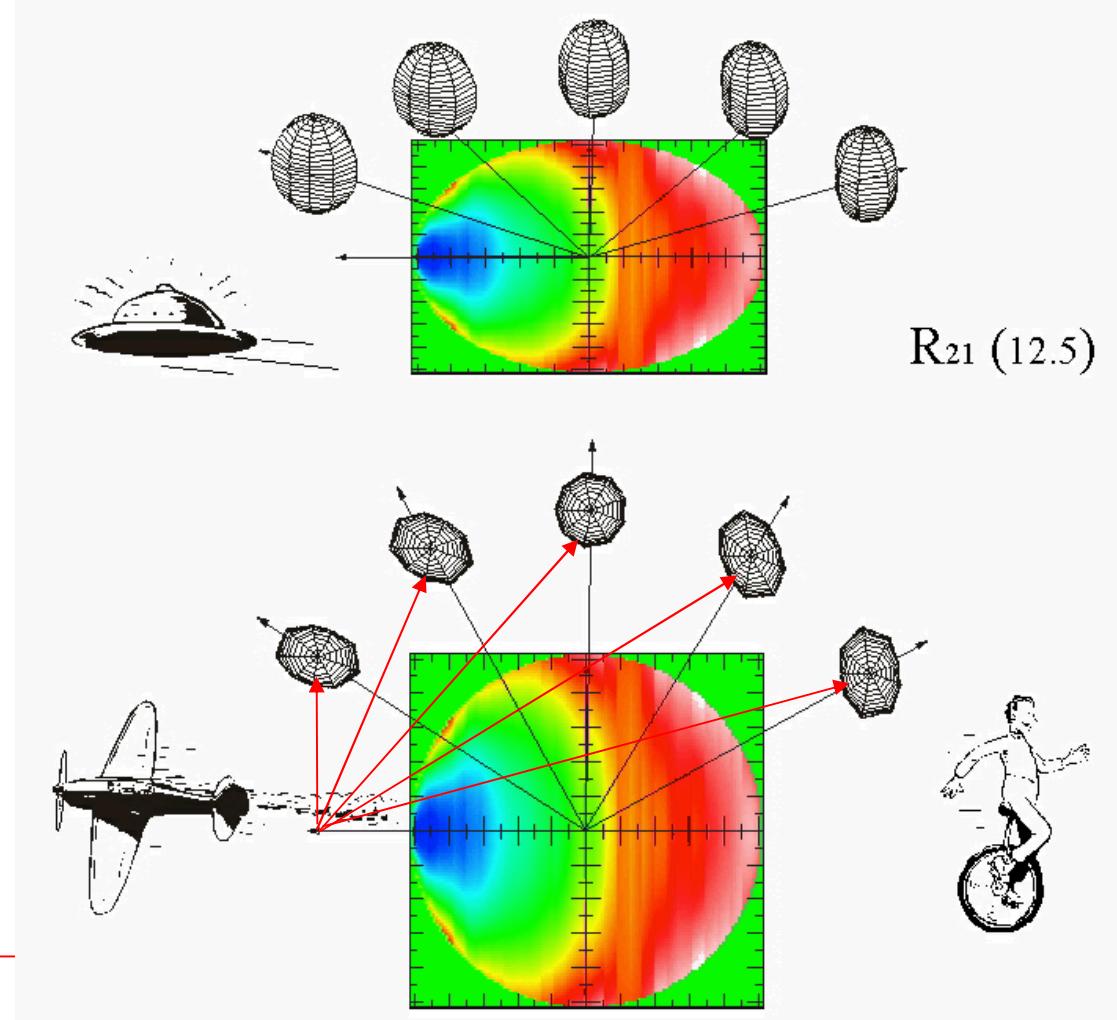
# Alignment Moments Were Measured for NO(X) + Ar and Compared to Quantum Calculations



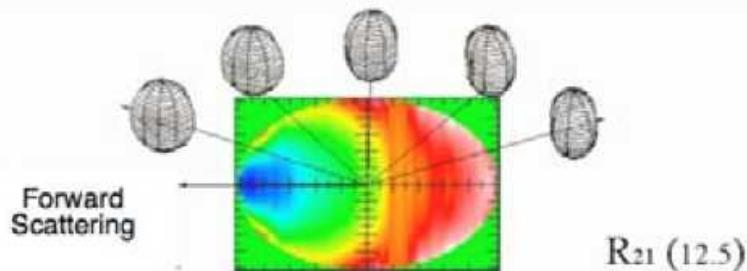
Alignment moments describe  
The extent that the angular  
momentum vector,  $J$ , lies parallel  
the center-of-mass collision vector  
or perpendicular to  
the center-of-mass collision vector

**Figure 22.** Alignment moments,  $A_0^2$  and  $A_2^2$  are obtained for many angles of recoil from the difference in images obtained between images recorded with horizontal and vertically polarized light for several final rotational states, see previous Fig.21. These alignment moments are compared to those expected from quantum close-coupling calculations on ab initio coupled-cluster CCSD(T) potential energy surfaces performed using the HIBRIDON 4.1 software for time-independent quantum calculations. (improved results Wade et al. 2004).

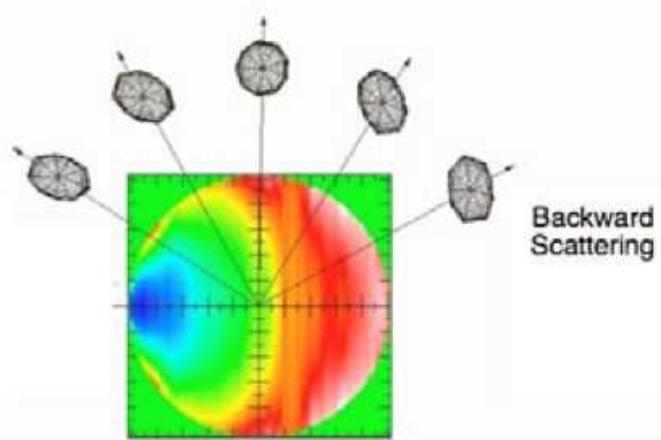
- The Three Alignment moments define the 3-D distribution and they are drawn here for  $J=12.5$
- Obloids represent the  $J$  distribution as a function of the final scattering velocity.
- Scattering products are dominantly aligned orthogonal to the scattering plane- as is predicted by a classical hard ellipse model.
- **With short axis along Apse angle**



# Alignment of J 12.5 as function of scattering angle.



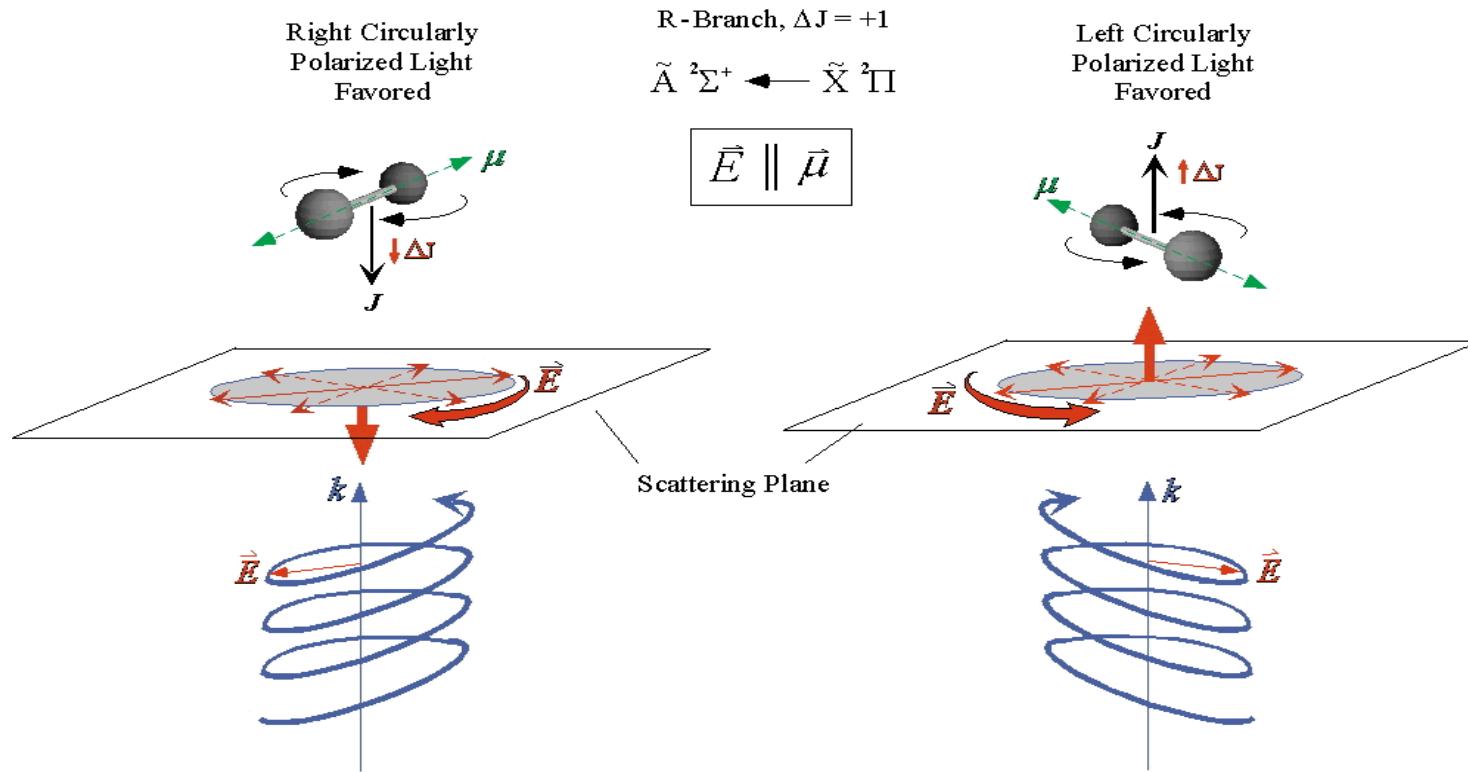
One can convert the Alignment moments of the Angular Momentum into plots of the angular momentum vector,  $J$ .



One sees a dimple in the  $J$  distribution  
Associated with the Apse Angle.

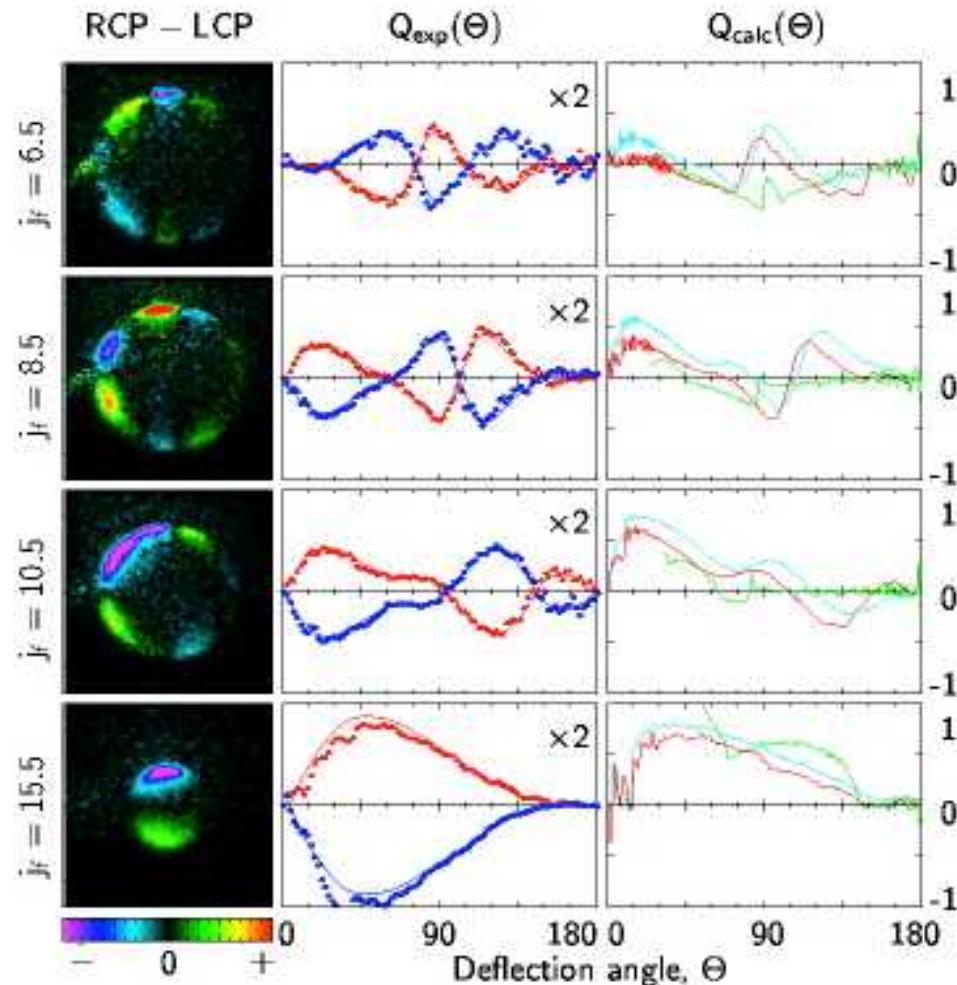
We were not able to measure the very forward scattered molecules. New predictions about alignment moments for the most forward scattering are "interesting"

## The Absolute Sense of Rotation of the NO Collision Products Can Be Probed Using Circularly Polarized Light

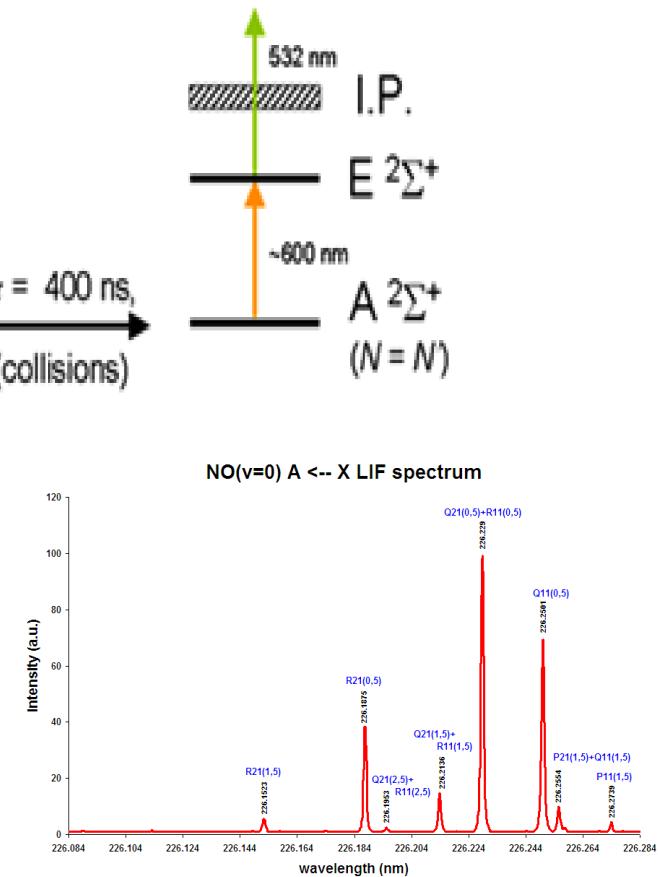
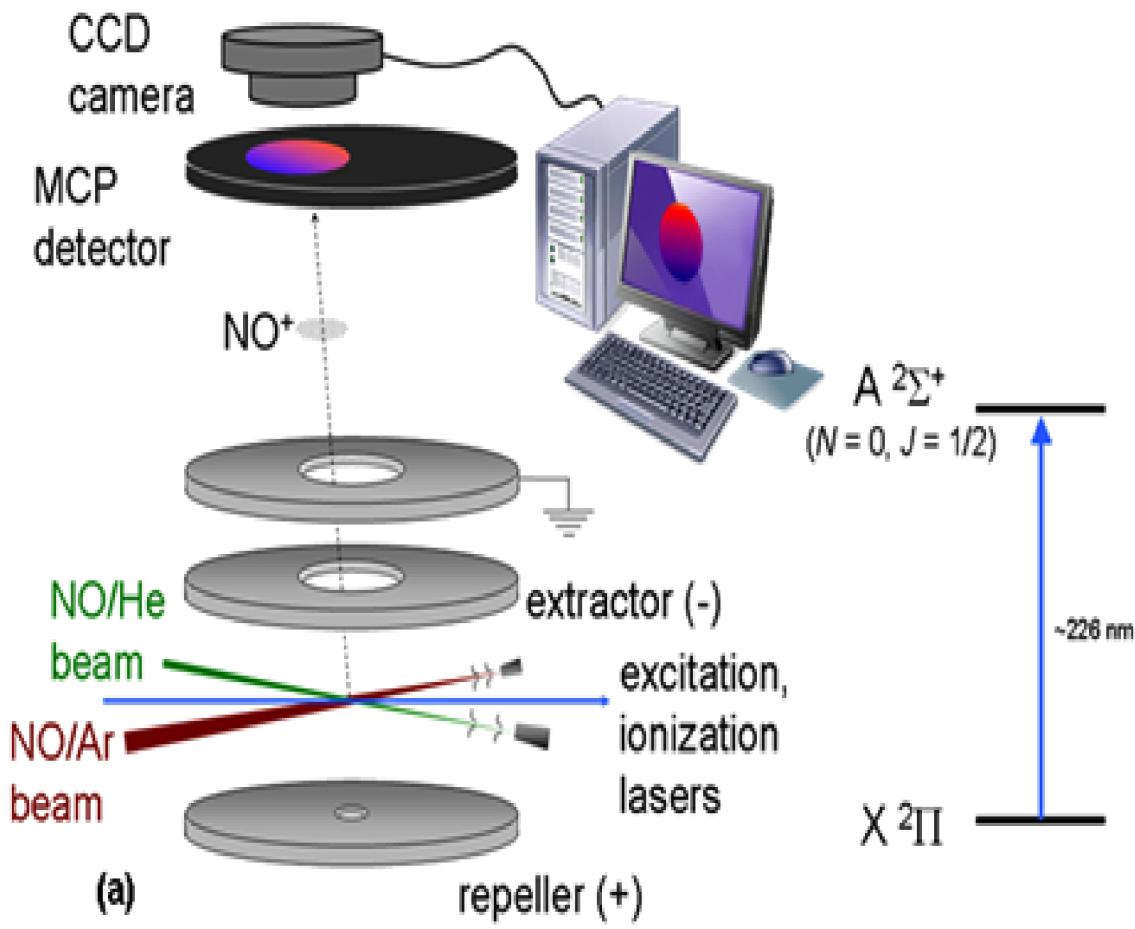


# Difference Images With Perimeter Plots and Calculated $A_{-1}^1$ Moments.

- Calculations are done using full close-coupled quantum calculations using two recent ab initio NO-Ar potentials of Alexander and the Hybirdon scattering package.

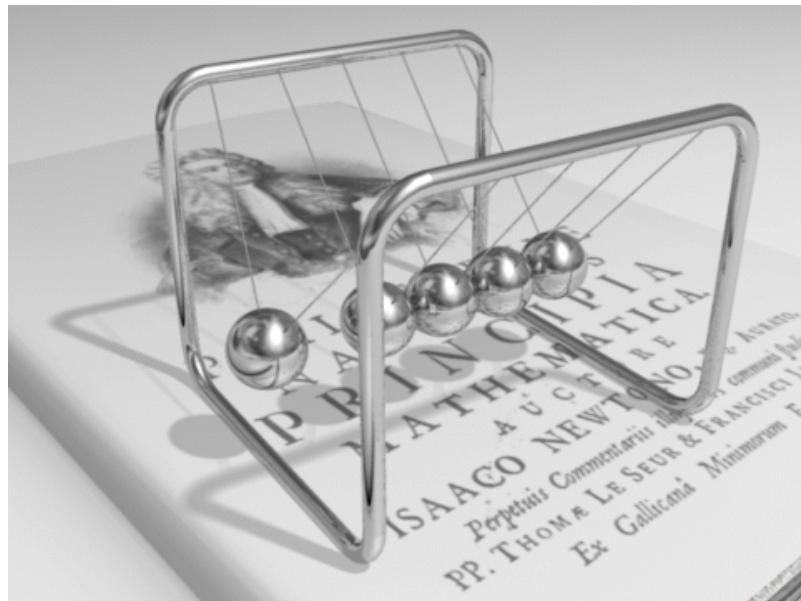


# Apparatus and Detection Mode for measuring DCS and Alignment of Electronically Excited State Molecules.



# Collisions are Subject to Conservation of Energy and Momentum!

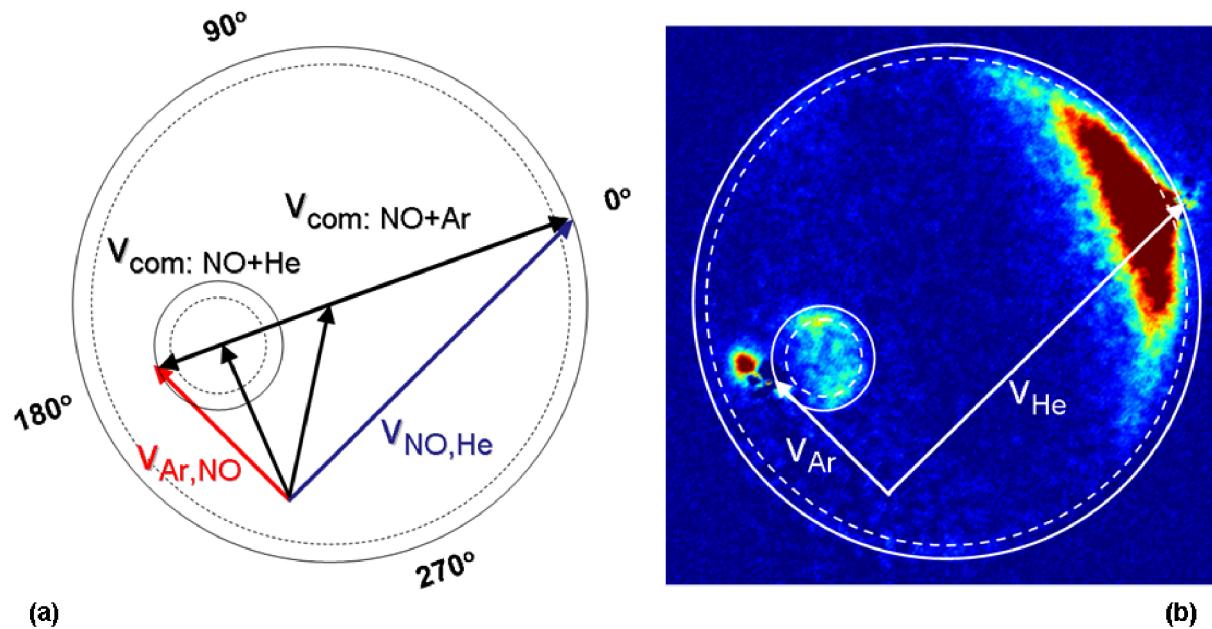
Think of it as a Newton's cradle



**Particles with equal mass. One has initial momentum, The other does not. The collision transfers “all” the energy from the moving particle leaving it stationary.**

**Only one way to conserve both momentum and energy simultaneously**

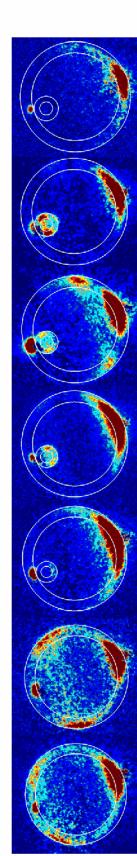
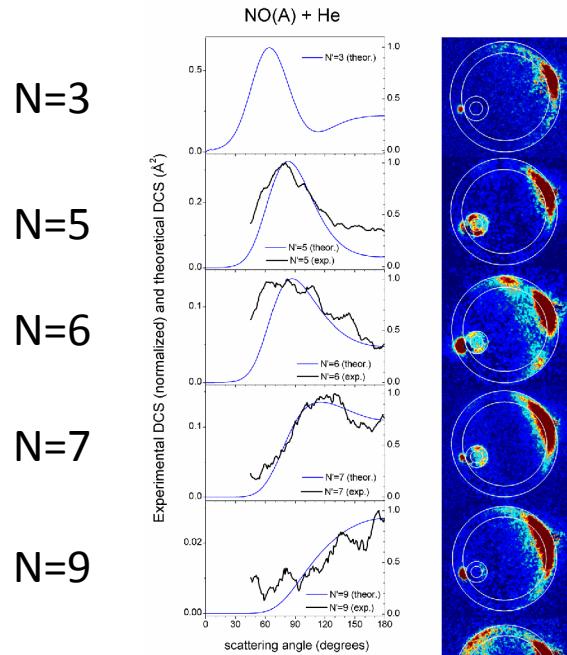
# Expected Collision Dynamics From NO/Ar Beam Scattering From NO/He beam



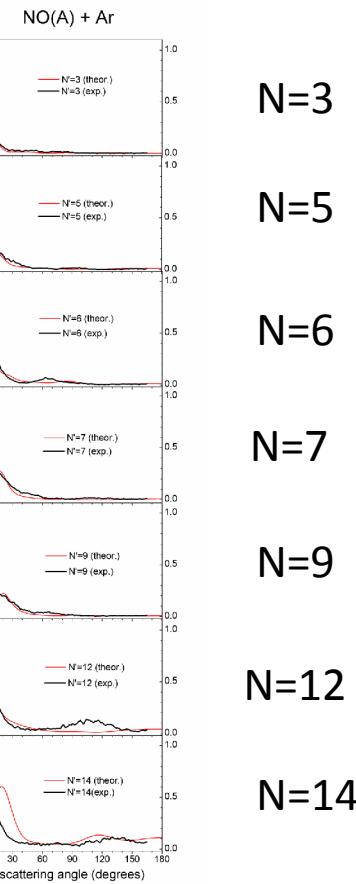
Three dimensional scattering of unequal mass particles capable of inelastic processes are Also constrained by conservation of energy and momentum, The Newton Sphere

# Background Subtracted Scattering Data and the Differential Cross Sections Obtained from Data.

NO scattering from He

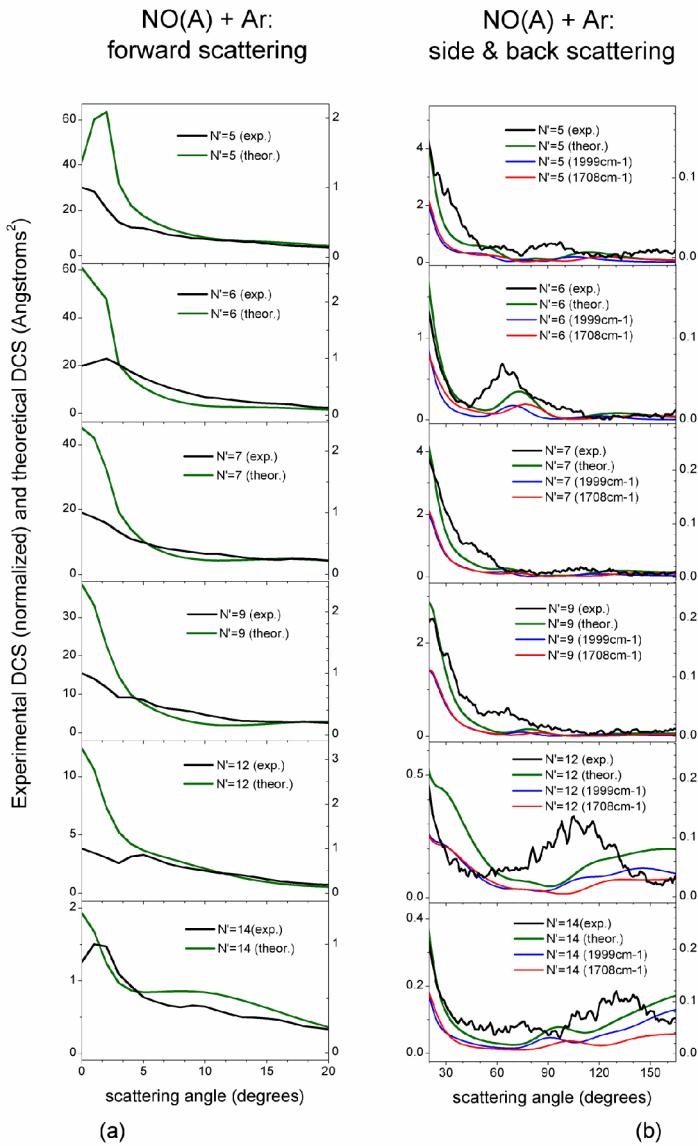


NO scattering from Ar



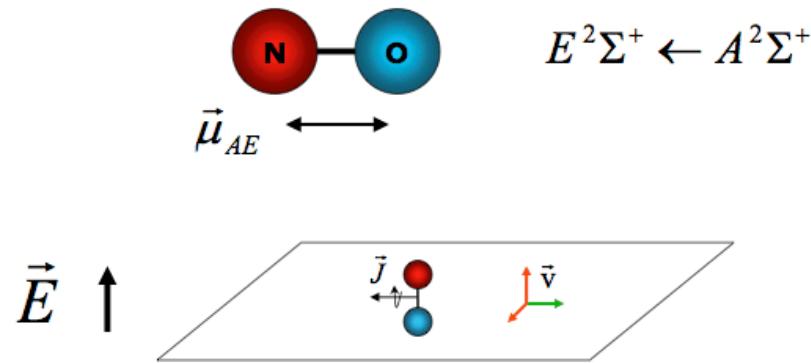
# Expanded view of Differential Cross Sections

Experiment under  
Estimates the forward  
scattering due  
background  
subtraction procedure

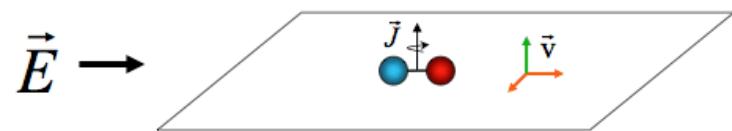


Theory to predict the  
position of the Rainbow  
Scattering at too  
large and angle.

Is the scattering is polarization dependent? Can we alignment of electronically excited state scattering?

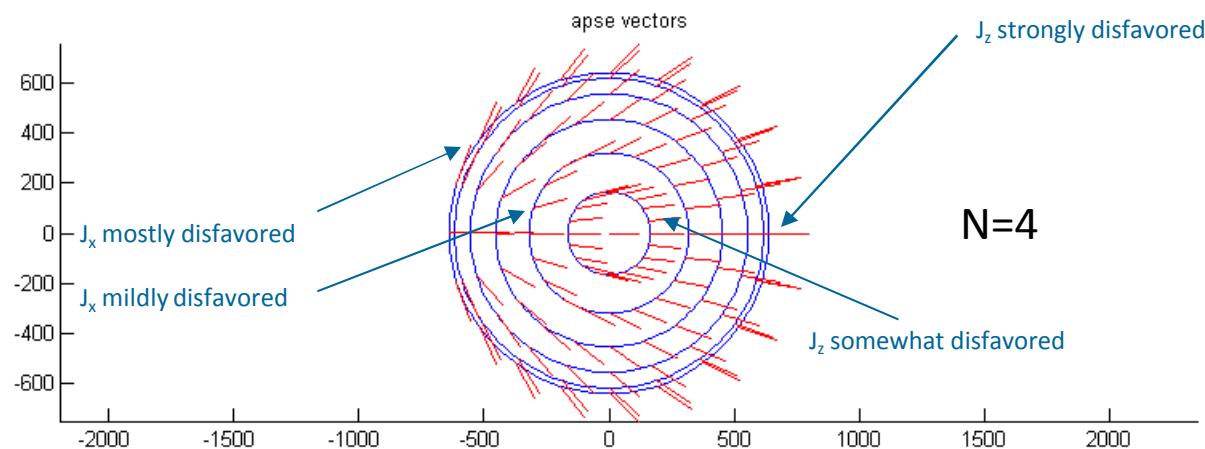


For NO traveling toward or away from laser beam perpendicular polarization is sensitive to cartwheel and propeller rotation.

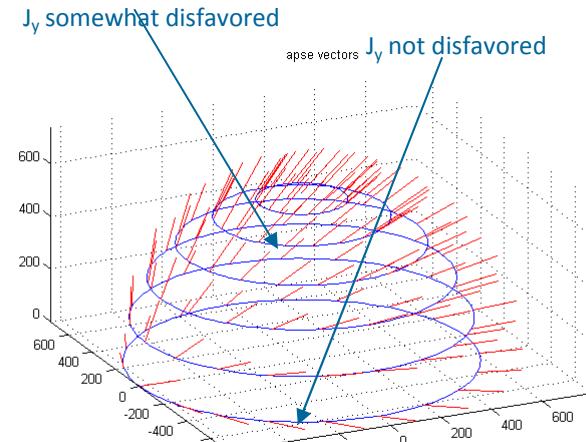
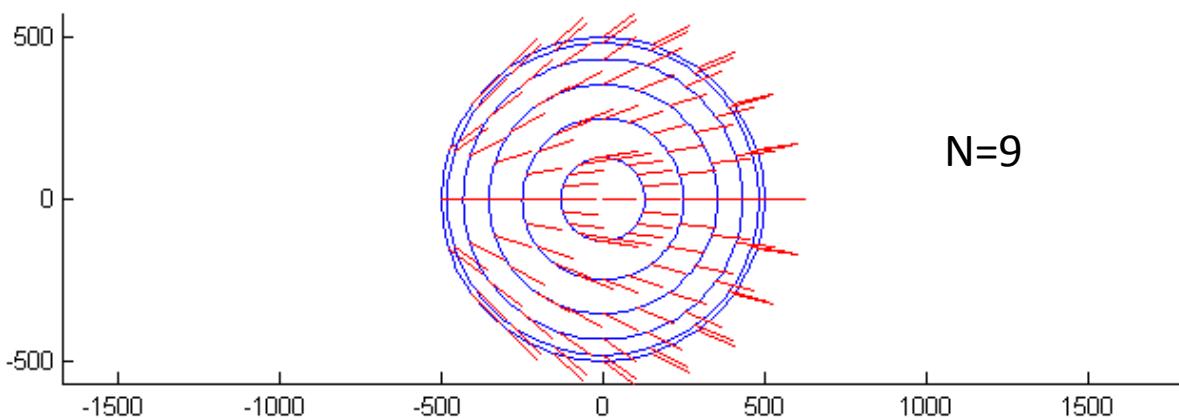


For NO traveling toward or away from laser beam horizontal polarization is sensitive to Frisbee or propeller motion.

# Classical ‘Apse’ model: Apse vectors



$x$ -axis =  $\vec{k}$  vector of probe laser

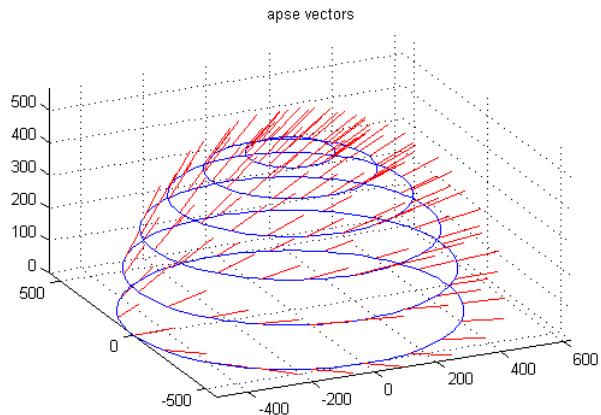


$z$ -axis defined as COM  $\vec{v}_{\text{initial}}$

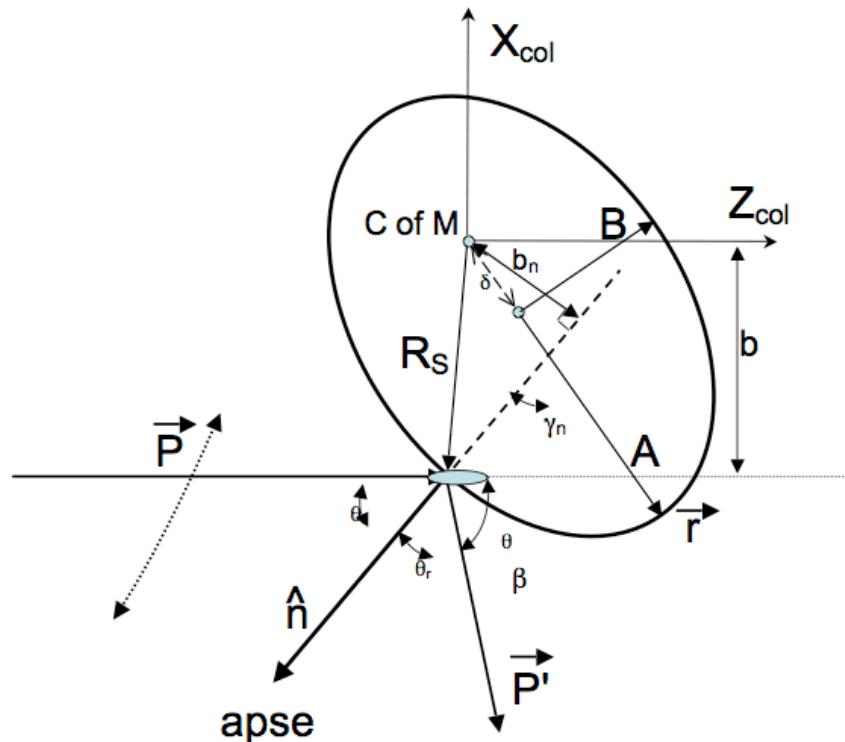
$x$ -axis is laser vector

$y$ -axis is  $m/z$  detection

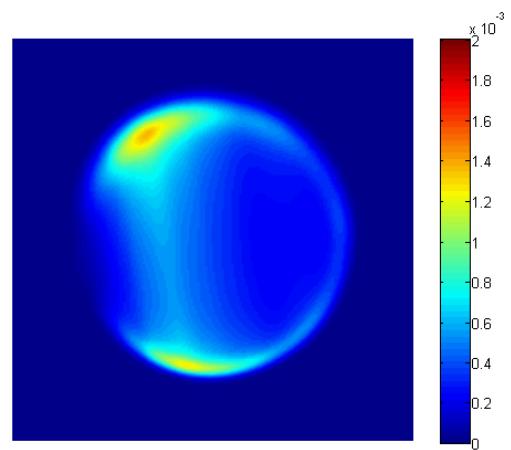
A 3D coordinate system with axes labeled x, y, and z. The y-axis is vertical, the x-axis is horizontal to the right, and the z-axis is diagonal.



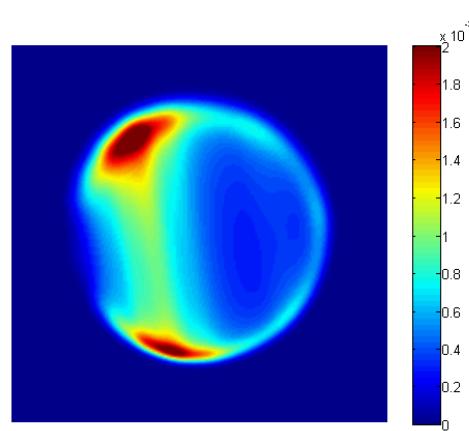
The classical dynamics associated with hard ellipse scattering can be analytically described. The Apse vector is the vector along which angular momentum is transferred



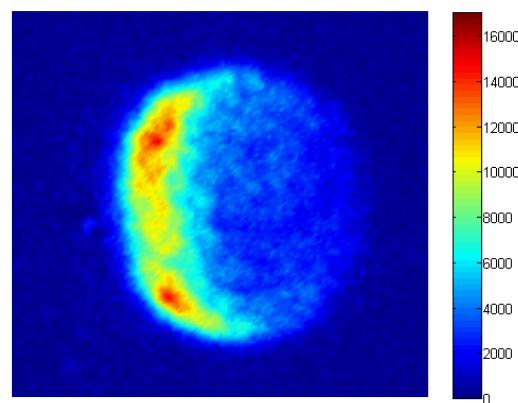
$\mathbf{J}$  cannot be transferred along the Apse angle.



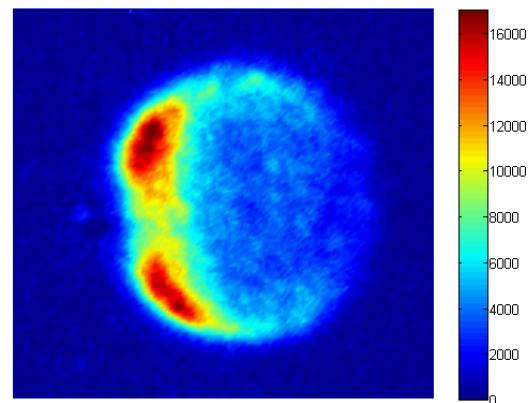
Exact model: V



Exact Model: H



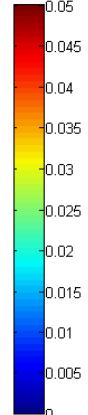
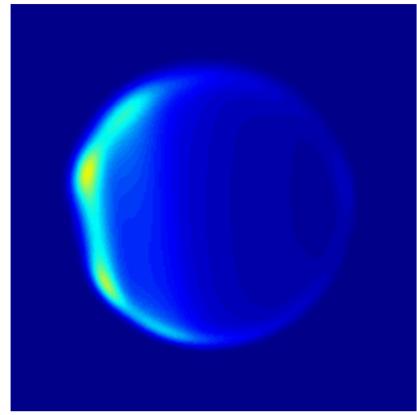
Experiment: V



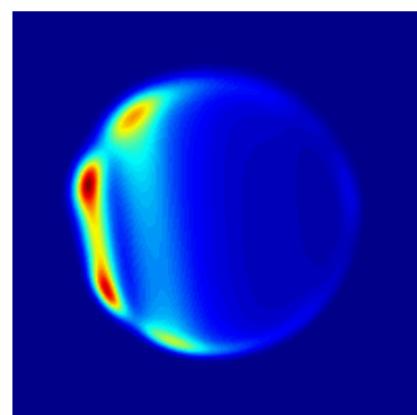
Experiment: H

# Images of NO ( $N' = 5$ ) for Vertical and Horizontal polarization of ionization beams

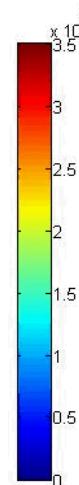
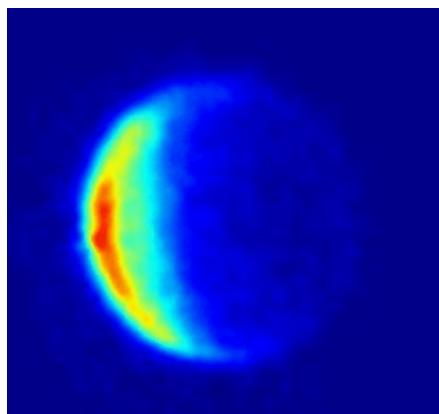
More forward scattering in experiment



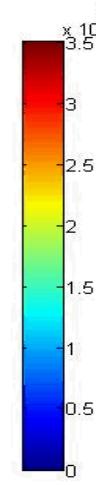
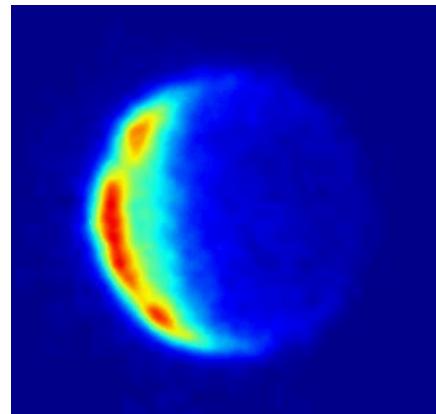
Exact model: V



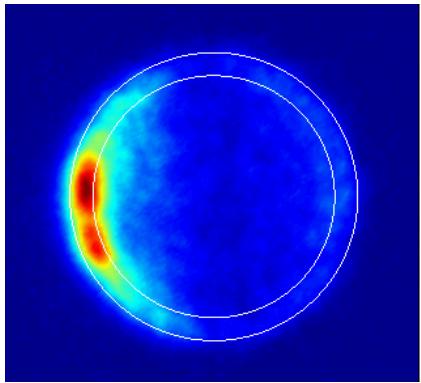
Exact Model: H



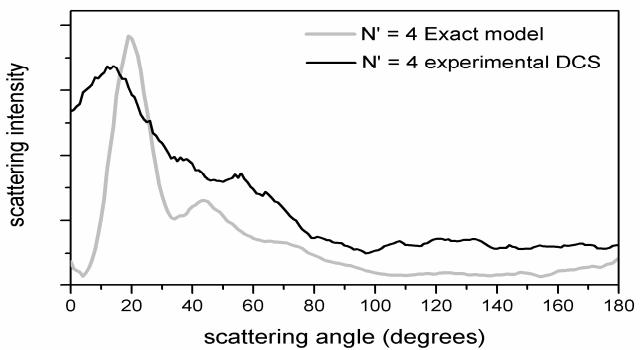
Experiment: V



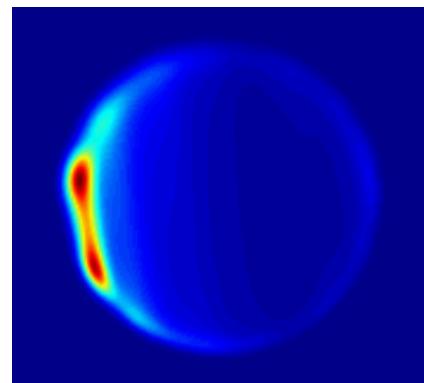
Experiment: H



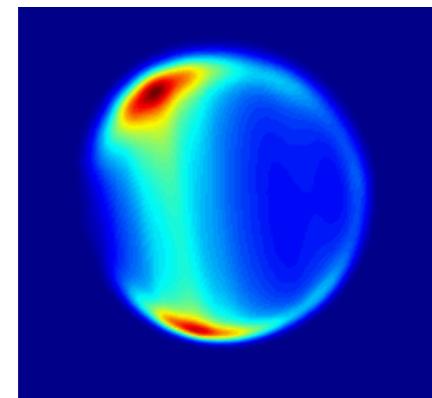
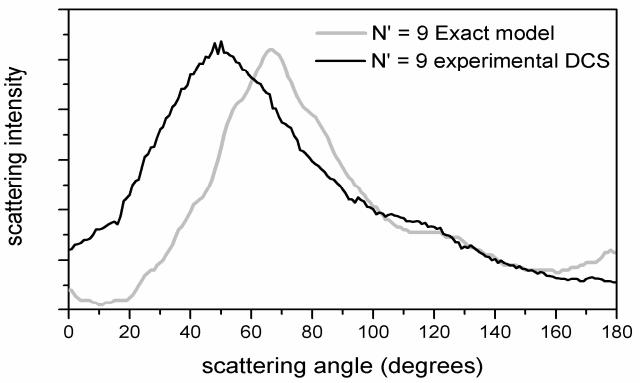
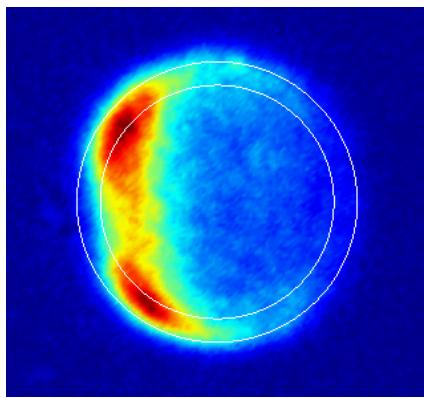
Experimental images



Annular profile comparison



Exact model



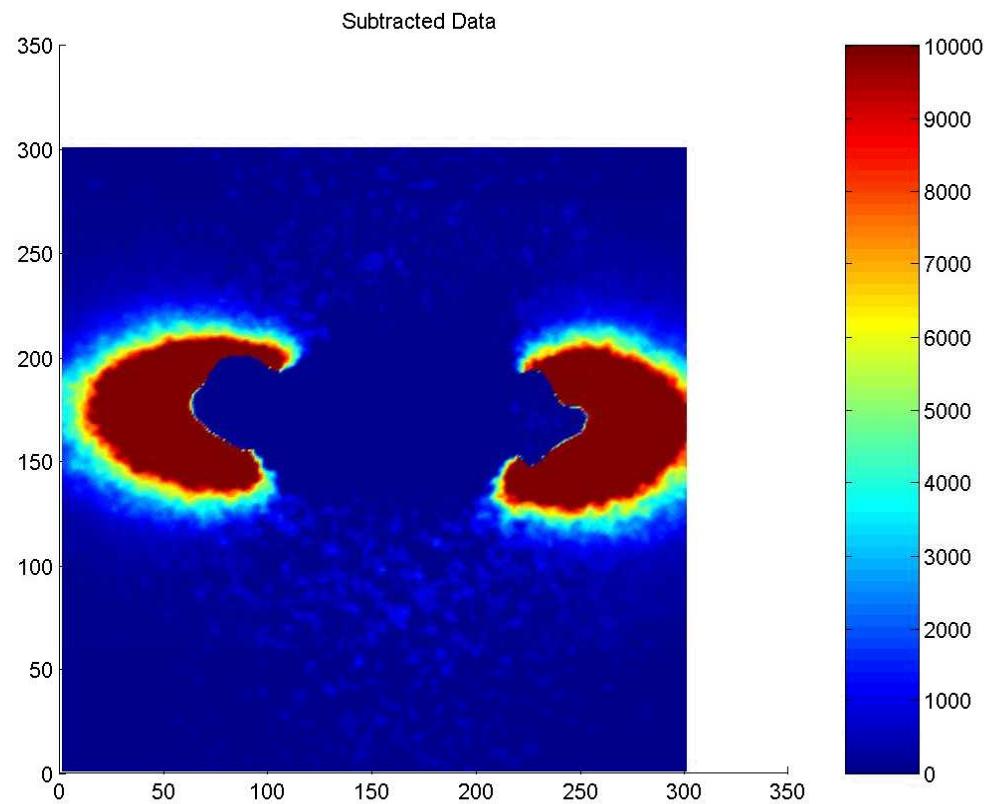
Elastic and Inelastic Scattering in Crossed Molecular Beams at 90° is One Techniques for Making milliKelvin Samples of Molecules.

**Pool balls “always” scatter at 90°.**

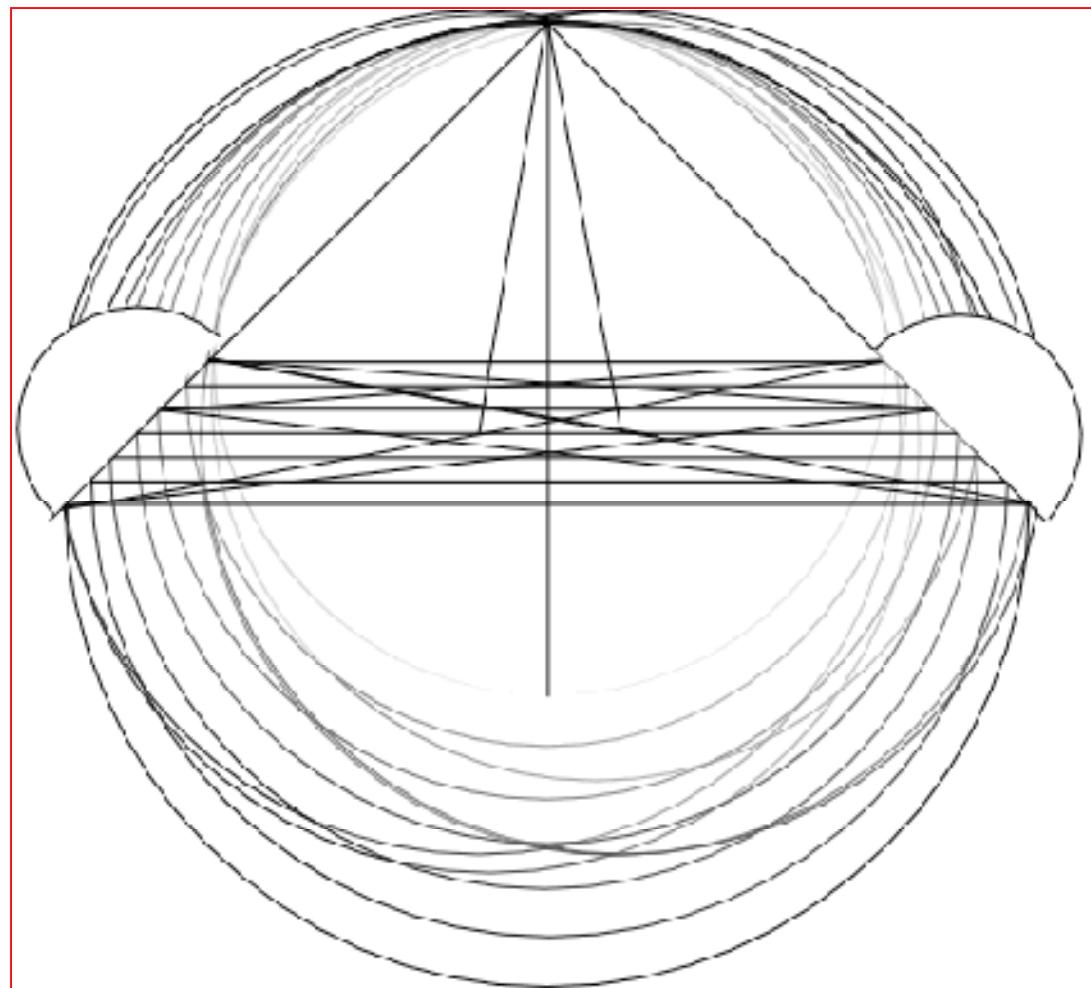


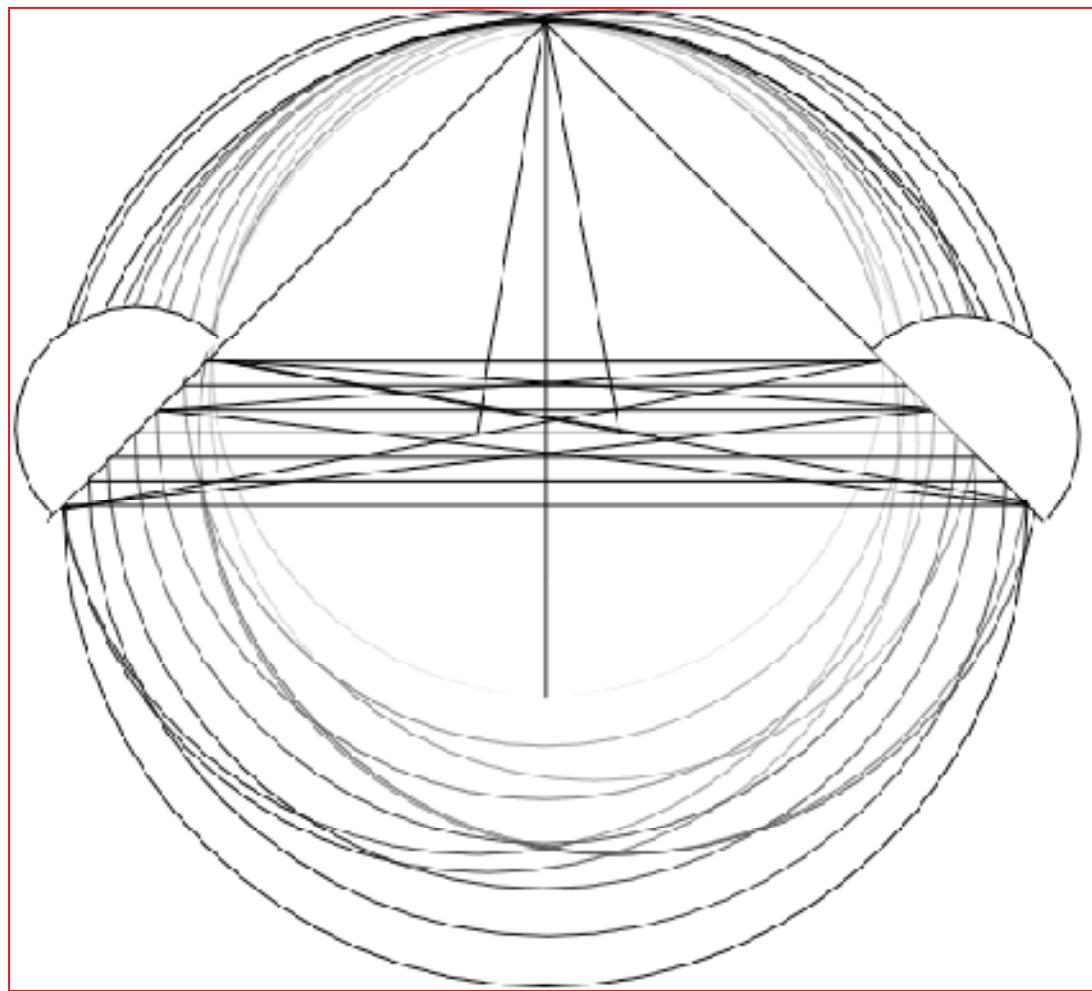
**Run the classical trajectory backwards**

**Not so easy as REMPI on Kr creates charge explosion of Atomic Beams**

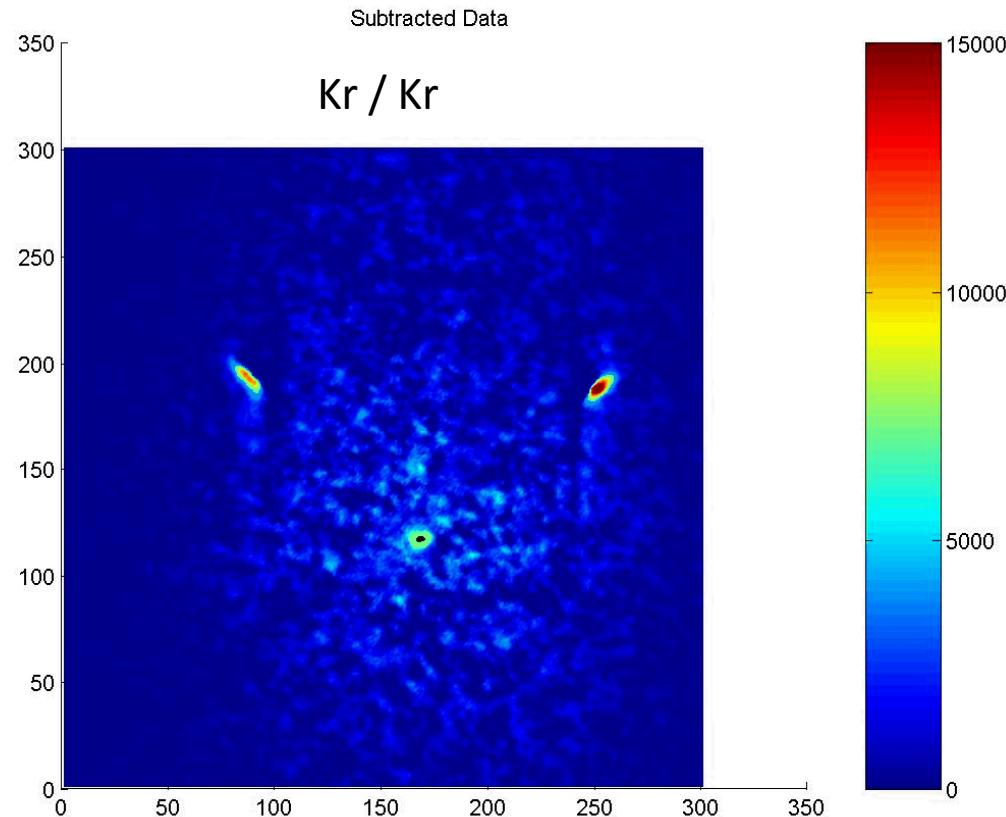


For molecular beams at  $90^\circ$  and of equal mass then the scattered molecules that have 0 lab frame velocity (elastically scattered) have no spread in velocity. Unfortunately  $J=0$  is forward scattered not side!?



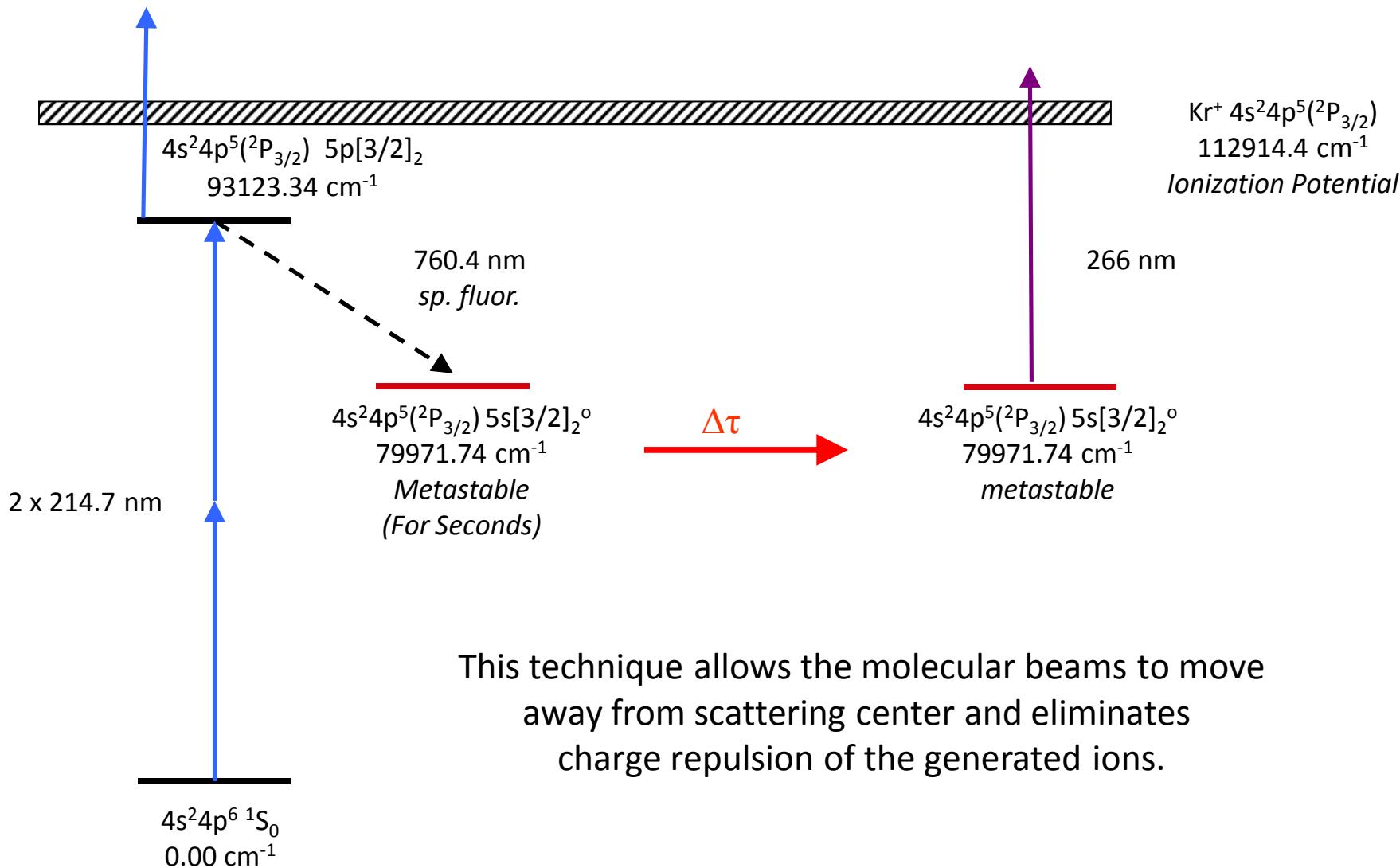


**Elastic Atom - Atom scattering allows us to optimize the Apparatus and Conditions for Trapping.**

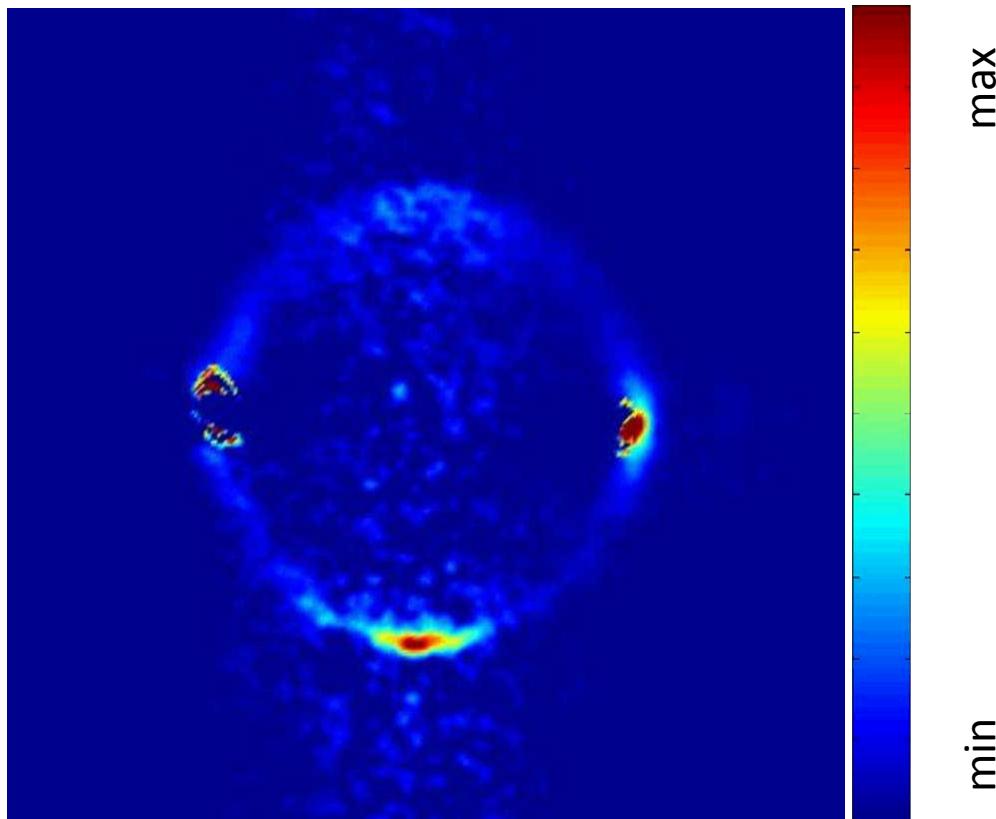


$$\Delta v'_{Kr} = \left( \frac{v_{Kr}}{v_{cm}} \right) \left( \frac{m_{Kr}^2 - m_{Kr}^2}{(m_{Kr} + m_{Kr})^2} \right) \Delta v_{Kr} = 0!$$

# How do we Eliminate Charge explosion of the Atomic Beams and Monitor cold Kr? Create Metastable Kr and Use Delayed Ionization and Ion Imaging of Cold Kr After Beams are Gone.

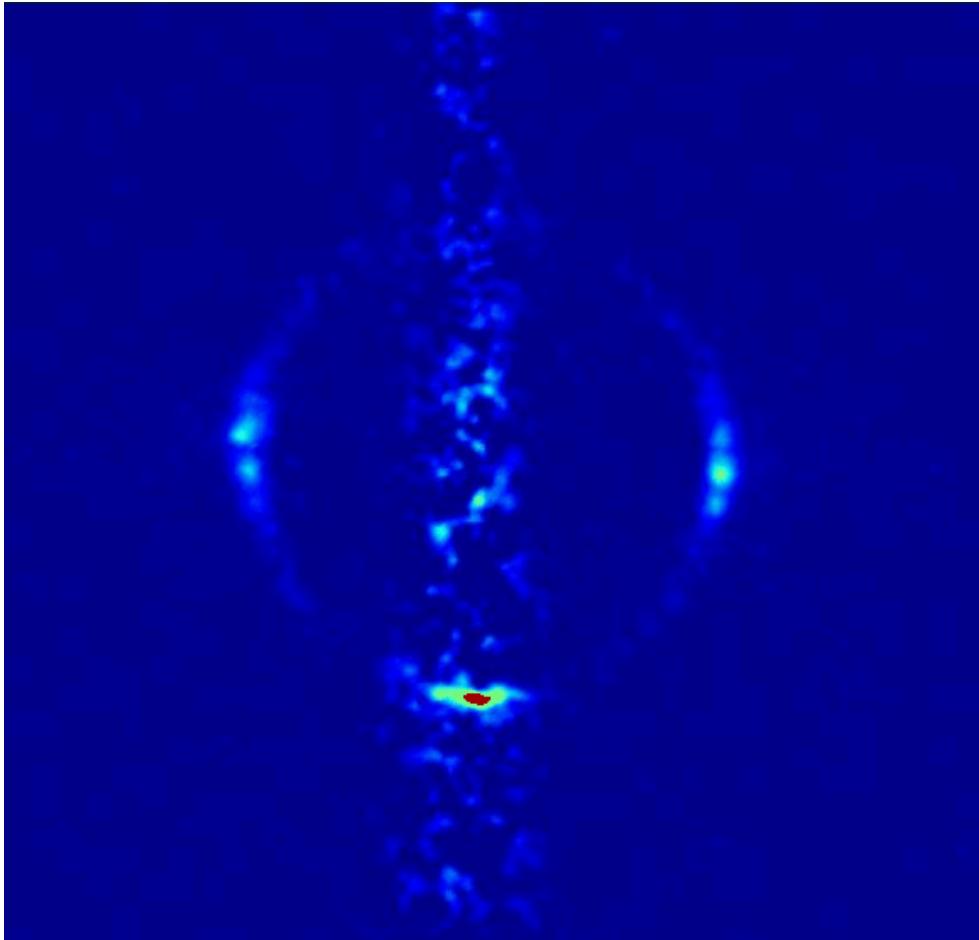


# We have detected Cold Kr Atoms (500 nsec delay)



We observe not only cold atoms but the entire elastic scattering differential cross section by letting the fast molecular beam mainly travel from our observation region.

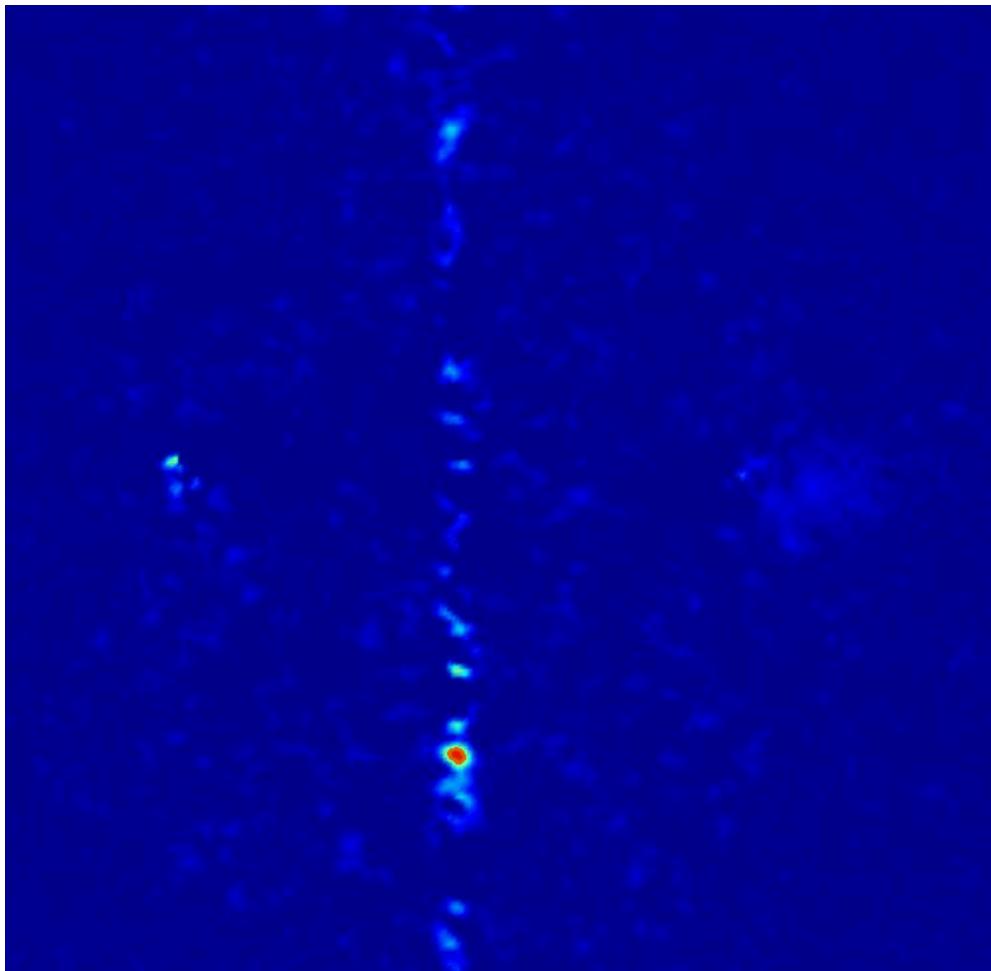
Is the scattering ground state atoms or excited state atoms?



Scattering Ring and cold atoms!

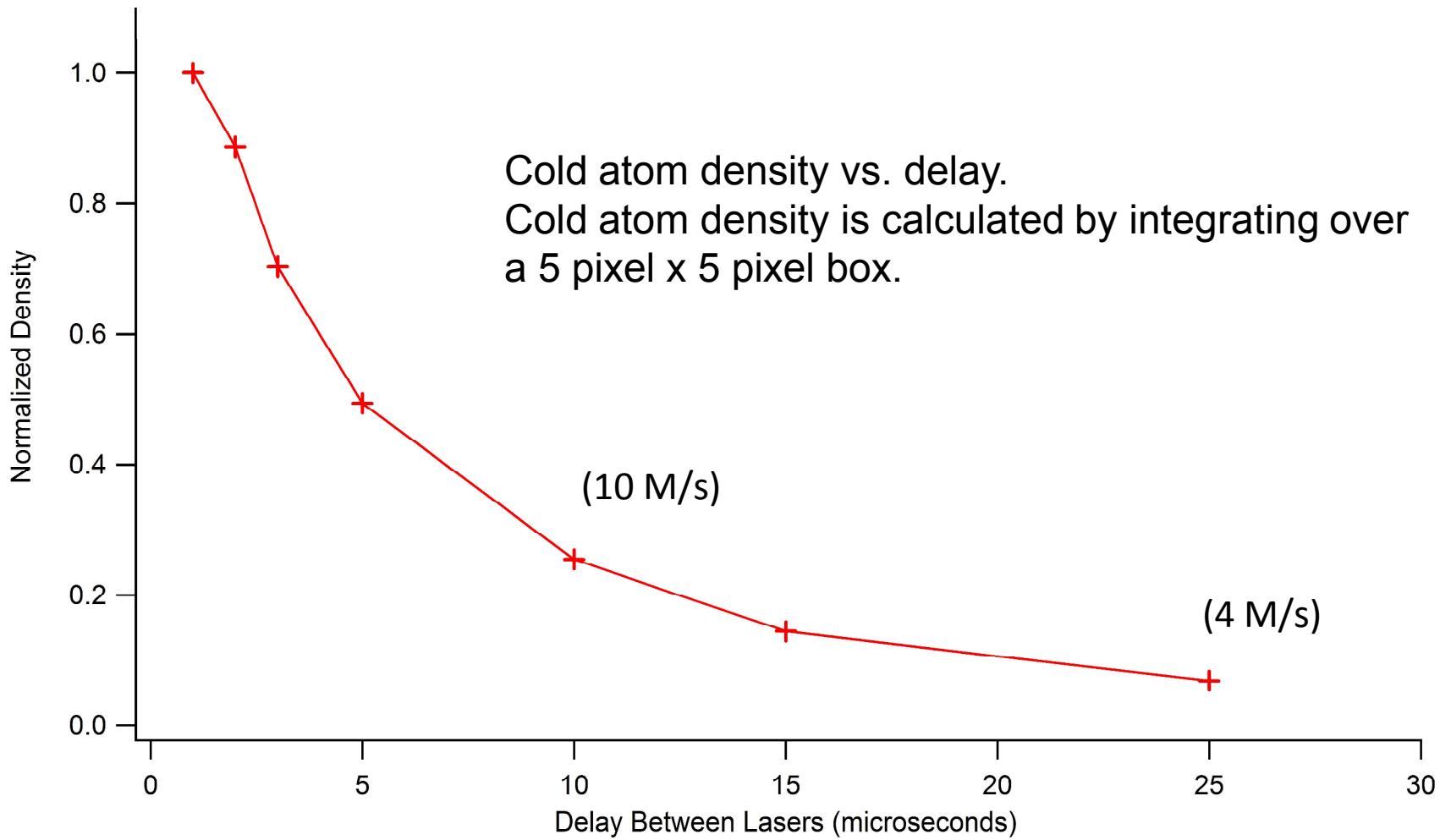
1 microsecond between  
214 nm laser pulse and  
266-nm laser pulses.

We can use this to study  
energy transfer in  
excited electronic states!



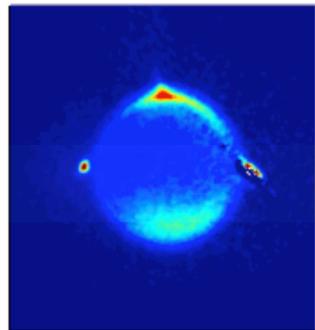
Only atoms that are moving  
Enough to be inside the ~100  
Micron laser beam width are  
Observed. Therefore the Kr atoms  
Must be moving less than 10 M/s

We observe cold atoms at  
25 microseconds so about 4 m/sec (tens of milliKelvin)

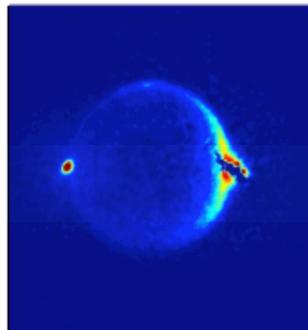


# Ammonia Scattering from Ne should produce very cold samples

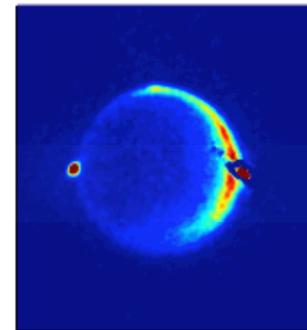
$\text{NH}_3$  ( $m = 17$ ,  $B=9.444 \text{ cm}^{-1}$ ) against Ne ( $m = 20$ )



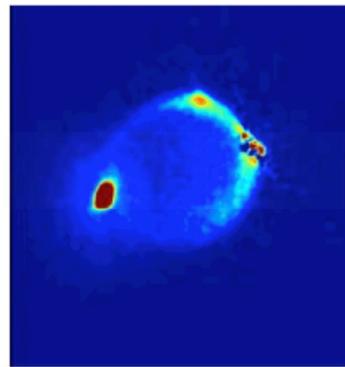
$J = 7, K = 7$



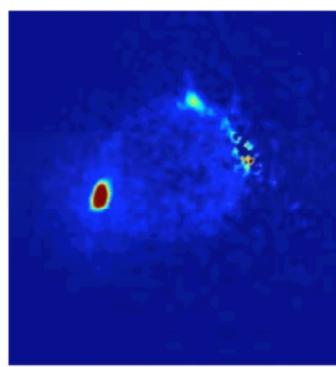
$J = 2, K = 2$



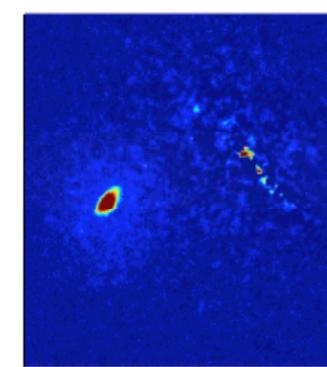
$J = 4, K = 4$



$t = 0 \mu\text{s}$

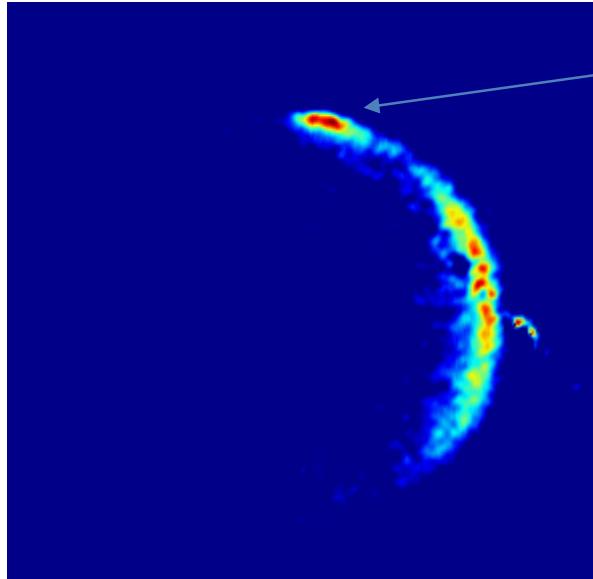


$t = 30 \mu\text{s}$

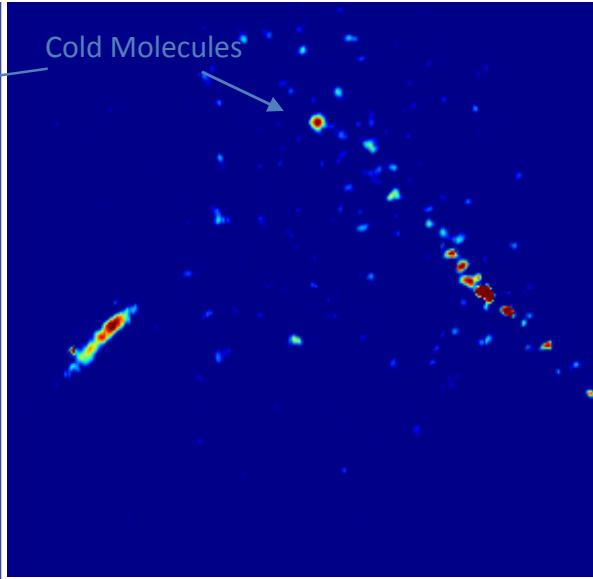


$t = 40 \mu\text{s}$

$\text{NH}_3$  seeded in Kr/Ar mix;  $J = 2$  is stationary in the lab



Peak of Molecular Beam Overlap  
With Atomic Beam



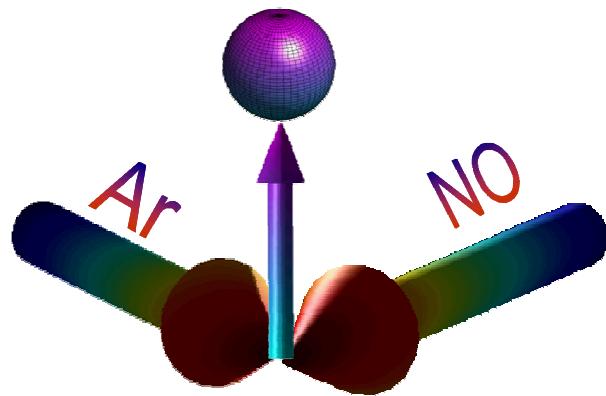
150  $\mu$ Sec after peak of Molecular Beam  
Overlap with Atomic Beam

**Inelastic Collisions are required for cooling if the atom and molecule do not have same mass.**

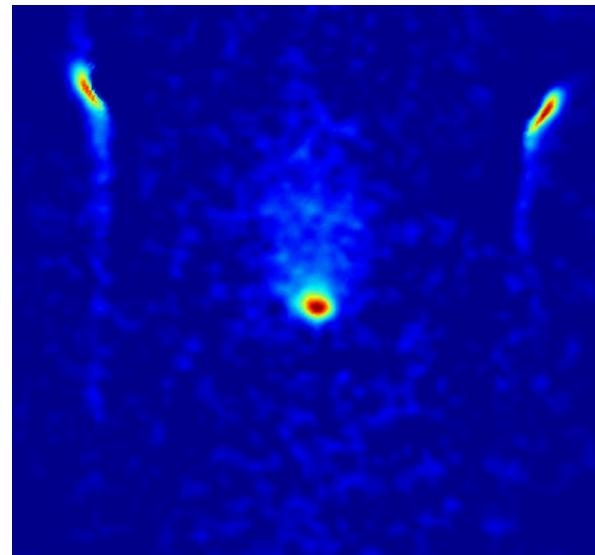
Determining the velocity distribution of these molecules is difficult.

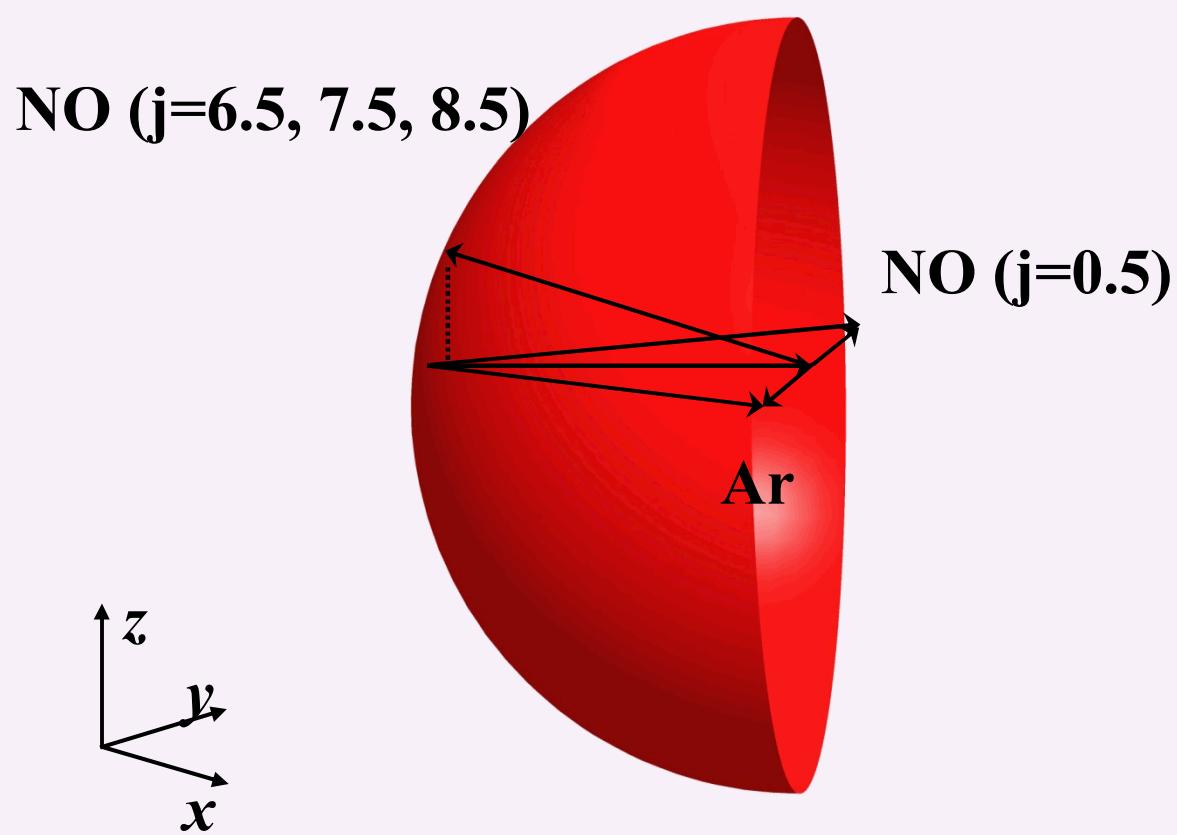
# Cold Molecules Scattered Out of Scattering Plane, Up in the Laboratory Frame are Easily Observed.

Cold atoms with finite final velocities are scattered out of the interaction plane, and detected.



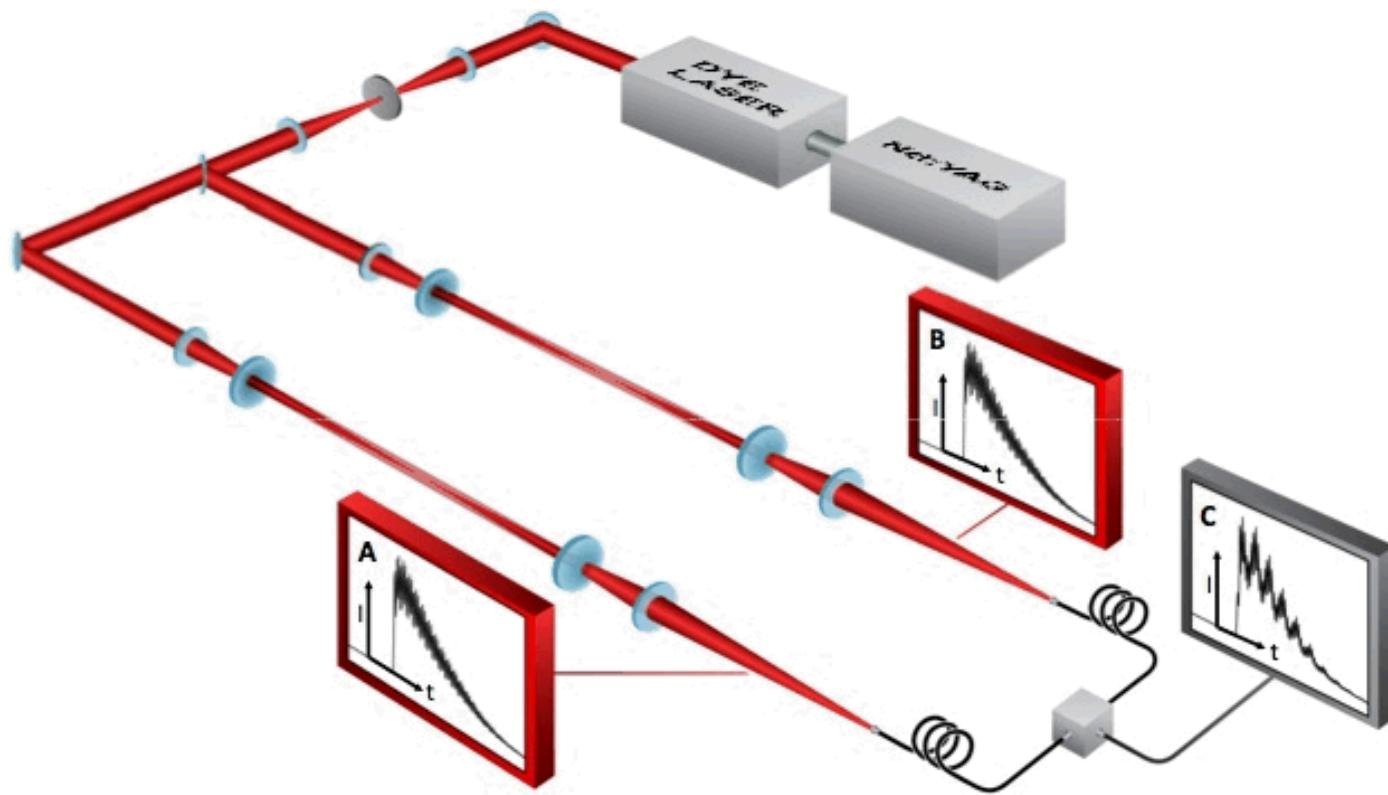
Separates cold atoms or molecules from remaining beam; molecular fountain for high resolution spectroscopy

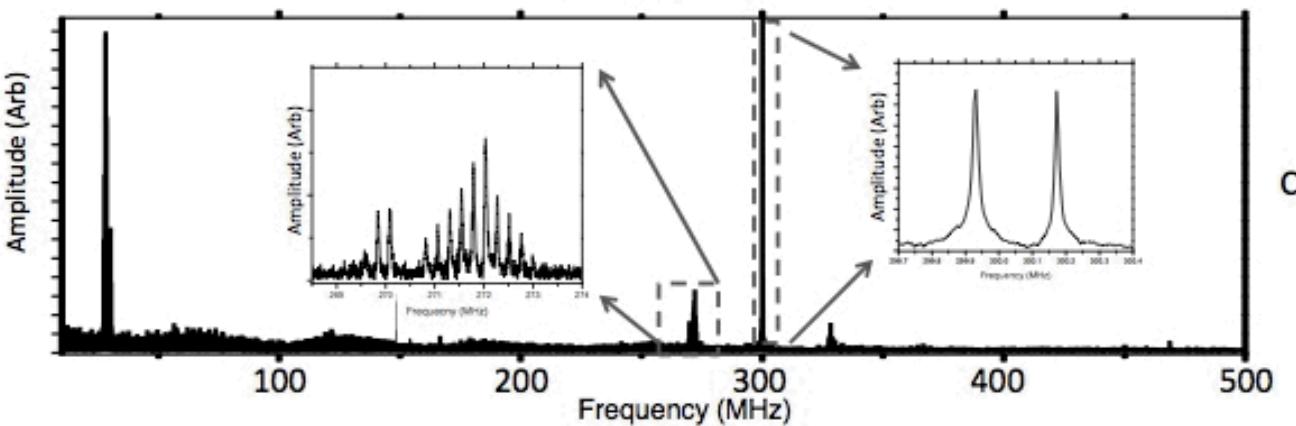
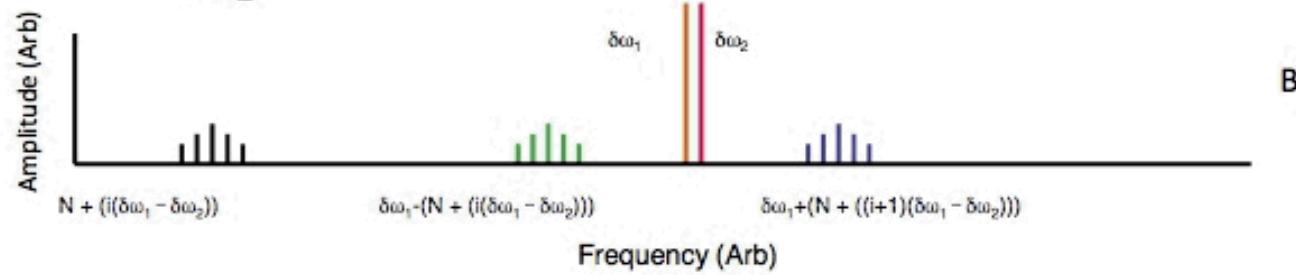
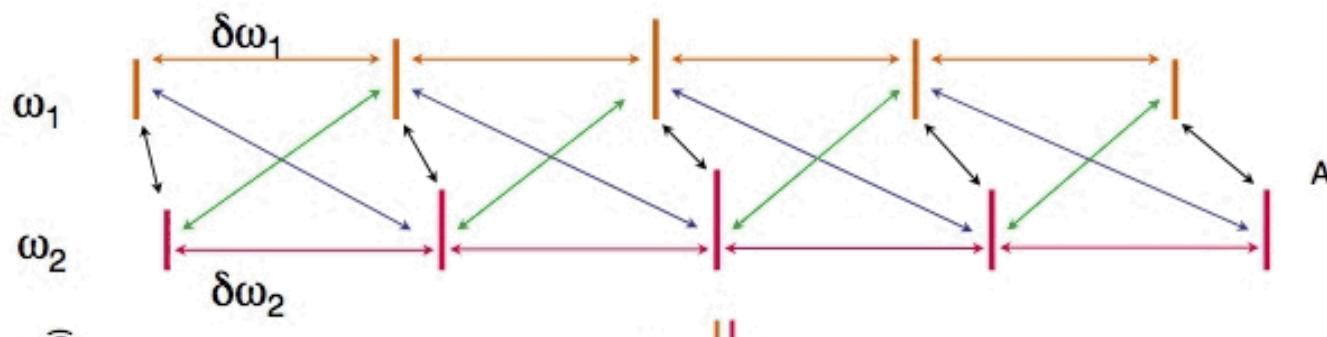


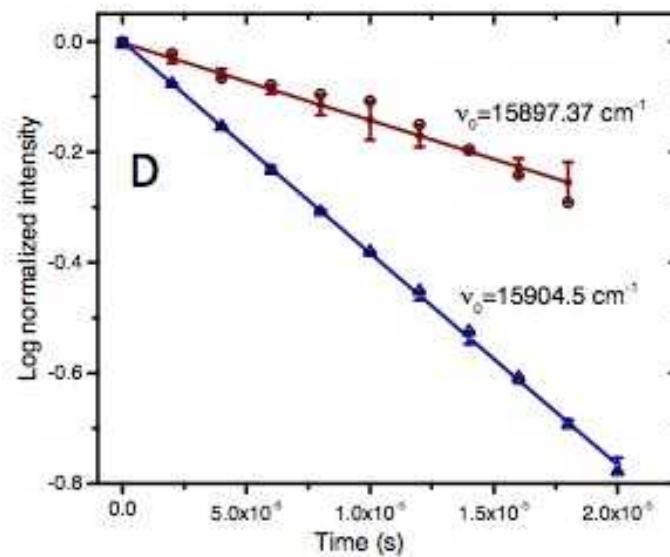
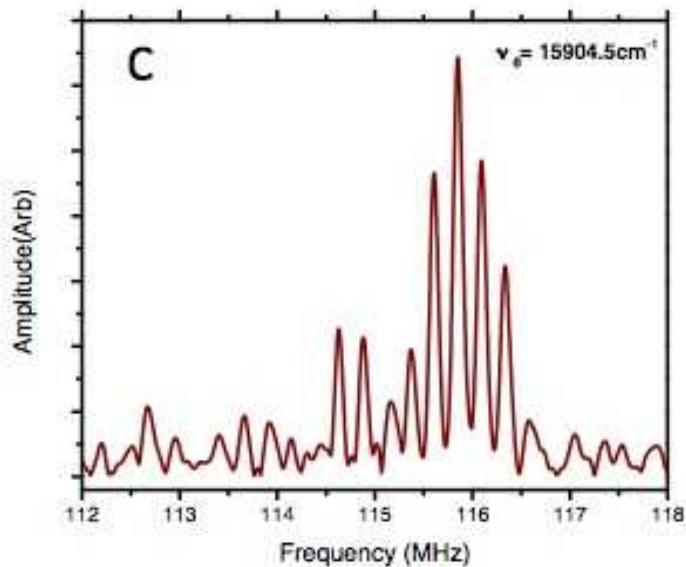
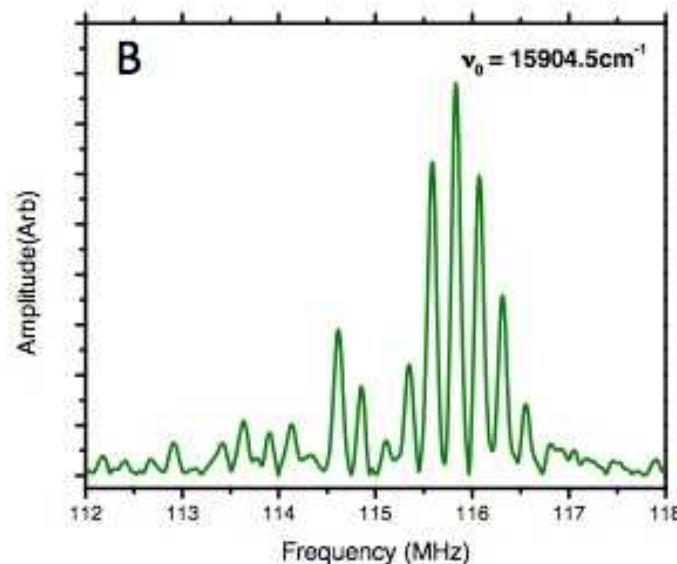
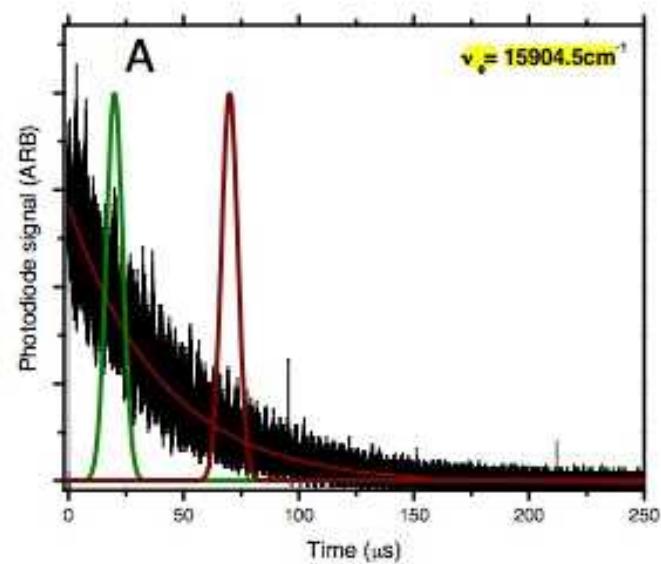


**A atom or Molecule that can be observed for 100 microseconds  
Can be subjected to about 2 kHz spectroscopy.**

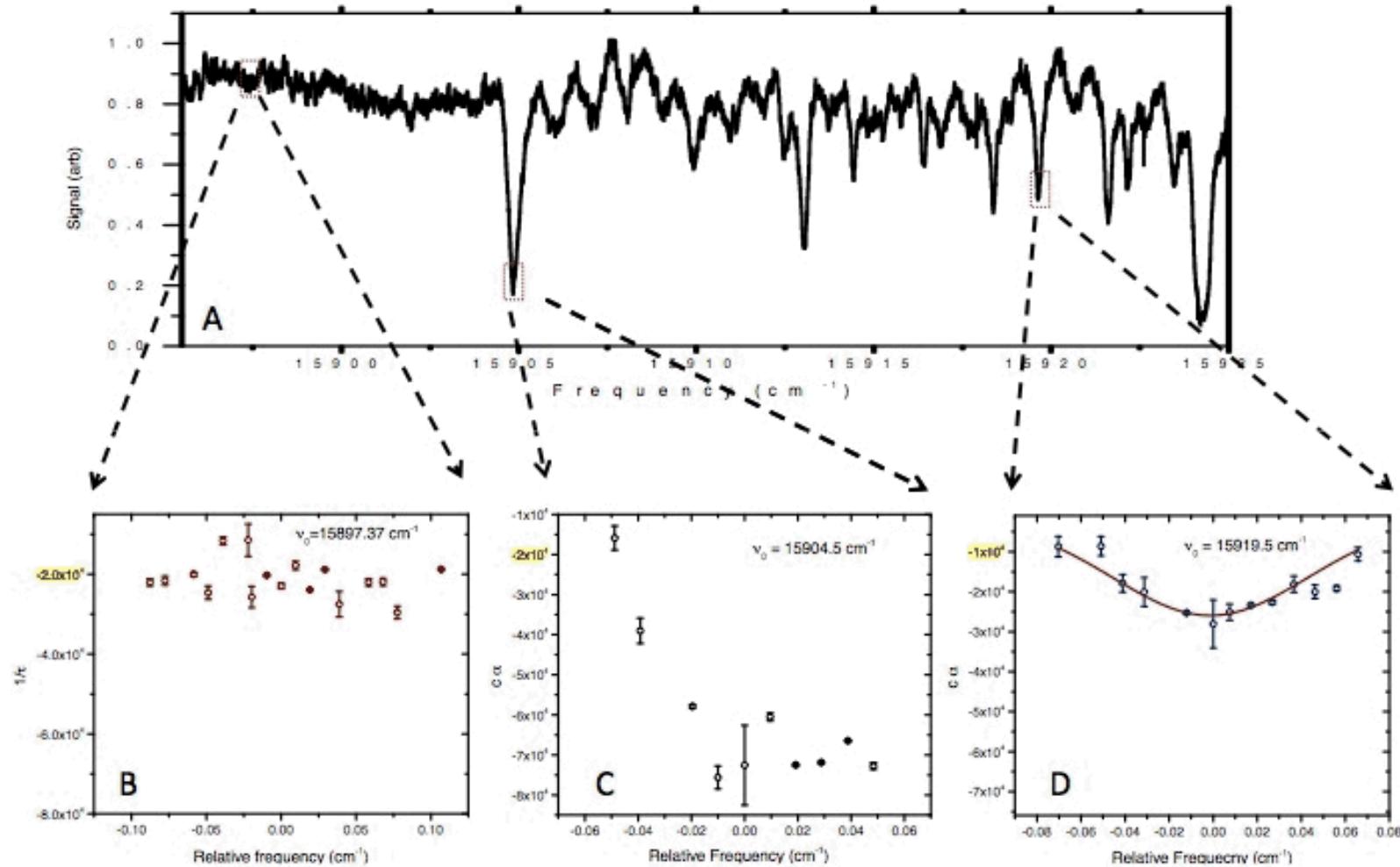
**How to makes high resolution light?  
Dual Etalon Frequency Comb Spectroscopy.**







$O_2$  forbidden  $b\ 1\Sigma_g^+ - X^3\Sigma_g^-$  and  $H_2O\ 4\nu+\delta$  (000)  $\rightarrow$  (113) overtone



# Memory Lane: Simple Cavity Ring Down Apparatus

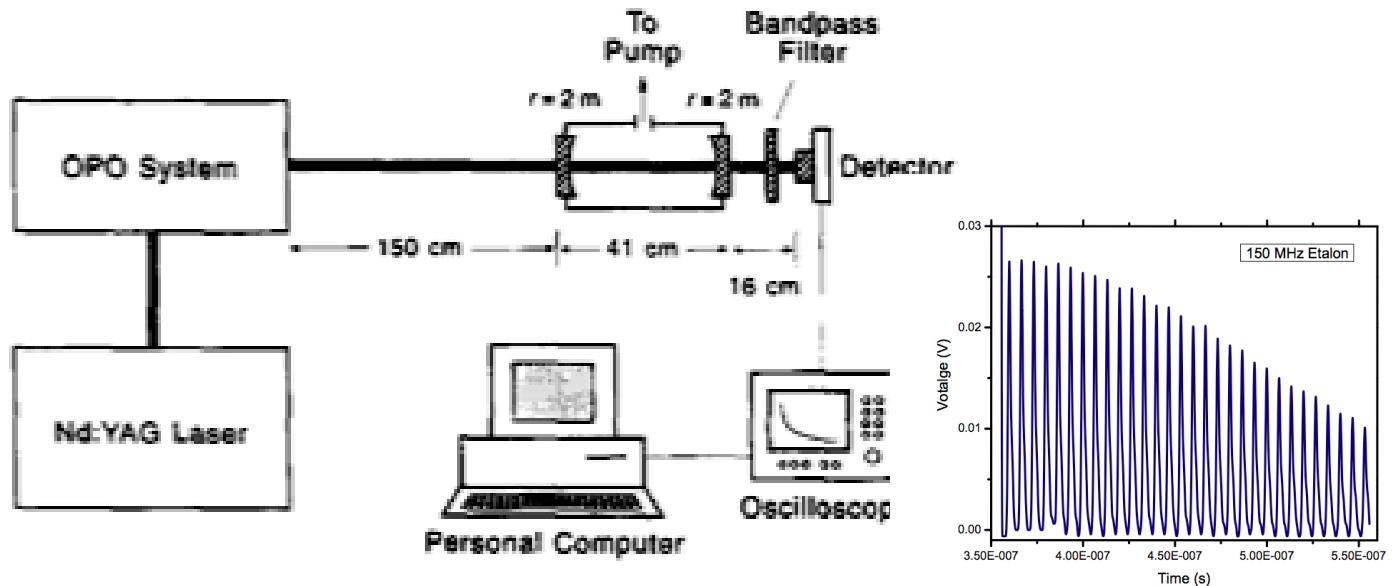


Fig. 2. Schematic view of the experimental setup.

If Ring Down Cell was in Confocal Etalon Arrangement Interference  
Between Equally Spaced Modes are Seen in Decay

# What to do About Those Interferences? Get Rid of Them!

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## Coherent cavity ring down spectroscopy

Gerard Meijer, Maarten G.H. Boogaarts, Rienk T. Jongma, David H. Parker

Department of Molecular and Laser Physics, University of Nijmegen, Toernooiveld, 6525 ED Nijmegen, The Netherlands

and

Alec M. Wodtke <sup>1</sup>

Department of Chemistry, University of California, Santa Barbara, CA 93106, USA

Received 29 October 1993

In a cavity ring down experiment the multi-mode structure of a short resonant cavity has been explicitly manipulated to allow a high spectral resolution, which is advantageous for the overall detection sensitivity as well. Coherent cavity ring down spectroscopy is performed around 298 nm on OH in a flame.

- Mess up the cavity
- Average for a while
- Low Pass Filter

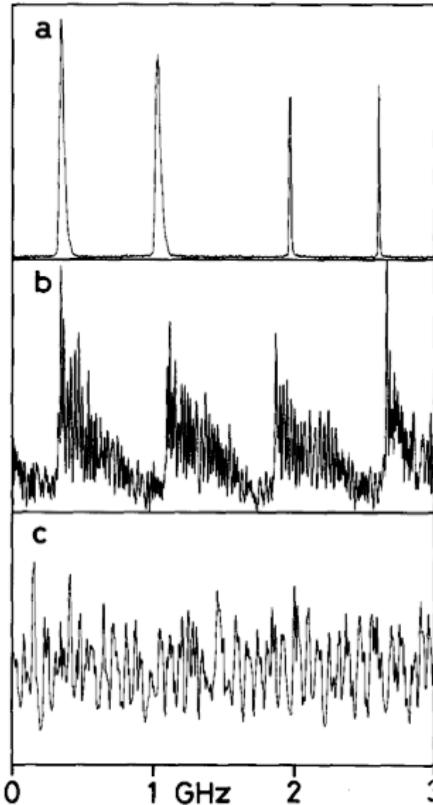
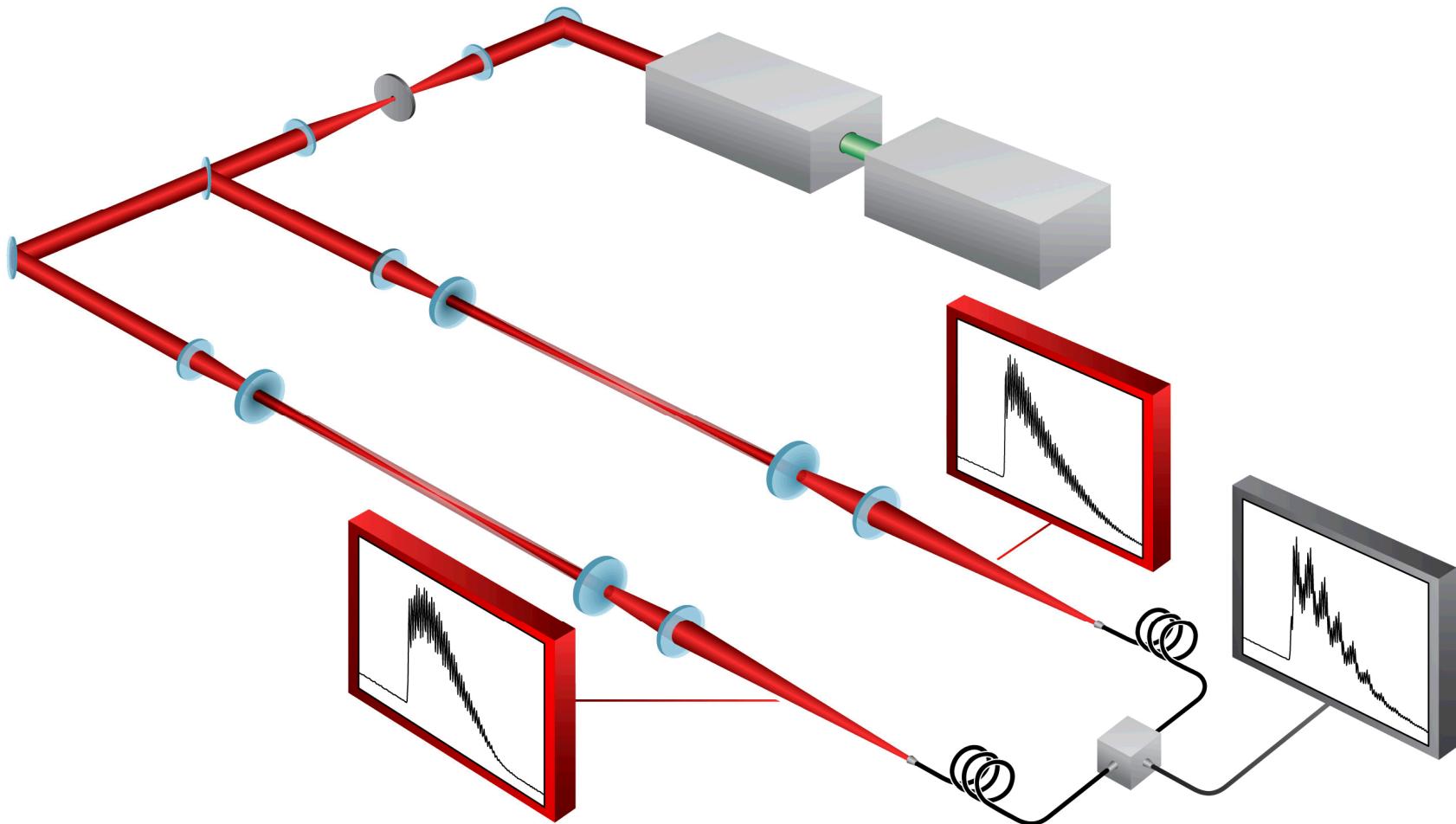


Fig. 1. Mode-spectrum of the ring down cavity for three different mirror separations  $d$ : (a)  $d=10.0$  cm; (b)  $d=10.2$  cm; (c)  $d=11.5$  cm. A rapid congestion of the spectrum is seen when the cavity is detuned from confocal. The spectra are measured by monitoring the transmission of the cavity while a narrowband ( $\leq 5$  MHz) cw UV laser is scanned over 3 GHz (6 GHz/min scan-rate) around 318 nm.

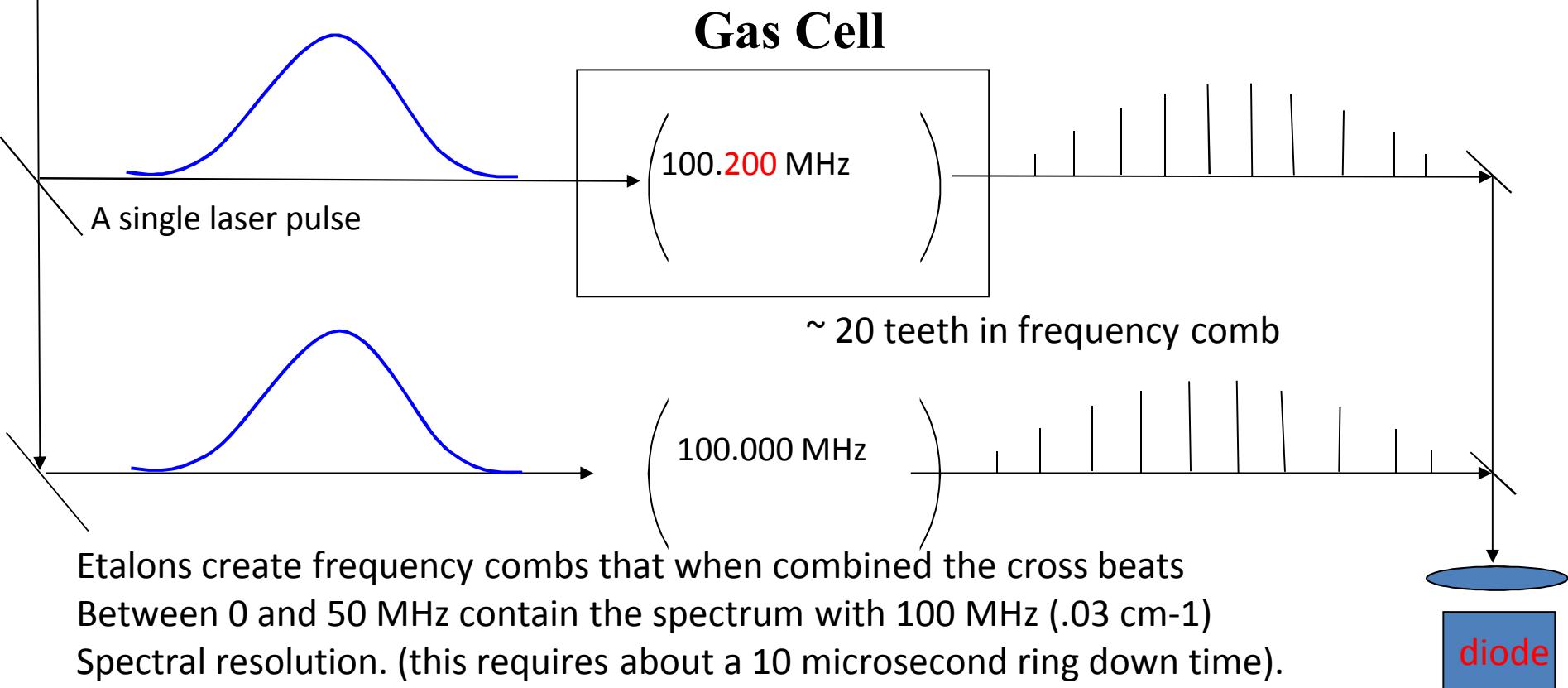
- Uses traditional laser sources (3 GHz Dye Lasers ( $1/10 \text{ cm}^{-1}$ ) for example)
- On single laser shot gives  $\sim 300 \text{ MHz}$  resolution ( $1/100 \text{ cm}^{-1}$ ) over bandwidth of laser source
- With averaging one can get  $\sim 30 \text{ KHz}$  resolution ( $1/1,000,000 \text{ cm}^{-1}$ ).
- Works in absorption and in fluorescence.
- Cavity Ring Down Spectroscopy is natural with the technique.
- It is inexpensive and easy to build, single photodiode detector.

# DEFCOM Spectrometer



# DEFCOM apparatus.

Use two  $\sim 100$  MHz etalons and a 2 GHz Dye laser (or OPO, or ASE, or Femtosecond pulse)



Reference: S. Schiller Opt. Lett. 27, 766 (2002),

Hansch (2006), Keilmann (2005), Jun Ye (2007), Nathalie Picque 2010

# Spectrometry with frequency combs

S. Schiller

Institut für Experimentalphysik, Heinrich-Heine-Universität Düsseldorf, 40225 Düsseldorf, Germany

Received December 19, 2001

A method is proposed for performing accurate spectral characterization of samples with frequency combs, e.g., from mode-locked lasers, over the spectral range covered by the combs. The essence of the method is the use of two combs of slightly different mode spacing to achieve spectral resolution. The advantages of the method are speed, frequency resolution, sensitivity, absence of dispersive components, and high spatial resolution. © 2002 Optical Society of America

OCIS codes: 300.6190, 140.4050.

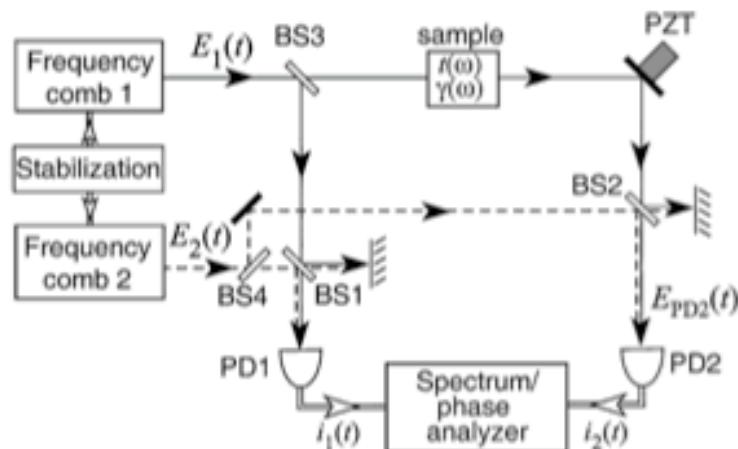


Fig. 1. Setup for measurement of transmission spectrum  $t(\omega)$  and (or) phase spectrum  $\gamma(\omega)$  of the sample. BS1–BS4, beam splitters; PD1–PD2, rf photodetectors; PZT, translator.

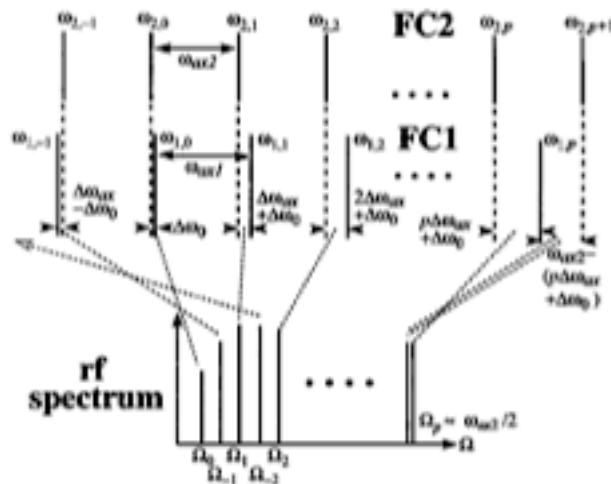
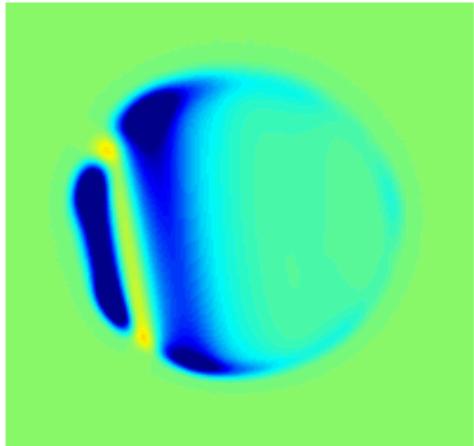
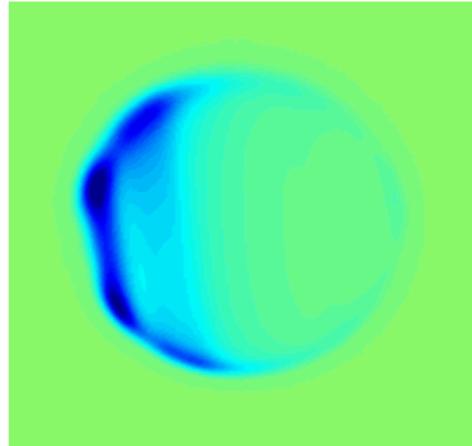
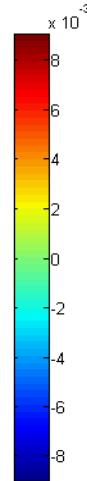


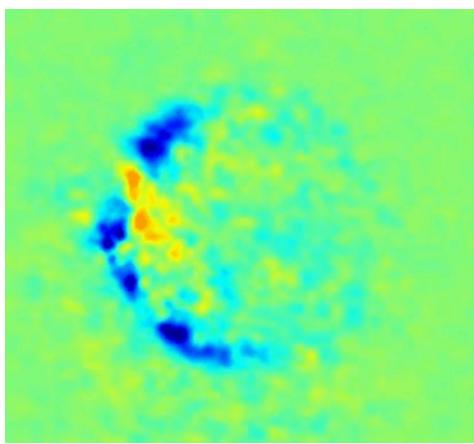
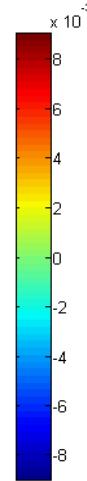
Fig. 2. Schematic of the modes of the two combs and relevant beats. The beats between modes  $\omega_{1n}$  and  $\omega_{2n}$  of equal index give rise to a rf spectrum with interleaving. Its discrete frequencies  $\Omega_0, \Omega_{-1}, \Omega_1, \Omega_{-2}, \dots$  arise alternately from modes below and above  $\omega_{10}$ . Beats between modes of different index, e.g.,  $\omega_{2n+1} - \omega_{1n} = \omega_{ax2} - (\Delta\omega_0 + n\Delta\omega_{ax})$  decrease in frequency with increasing  $n$  and will overlap the rf spectrum of beats of equal index starting at the beat frequency  $\Omega_p = \omega_{ax2}/2$ , once  $n$  is sufficiently large (see the double dashed lines).



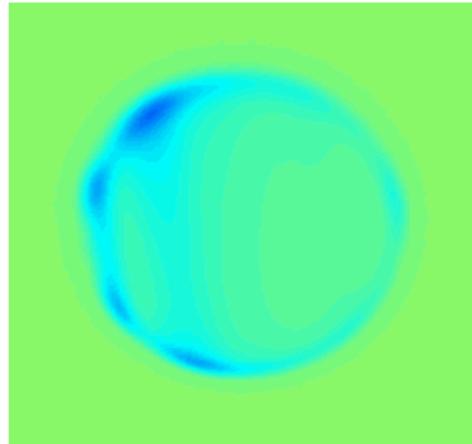
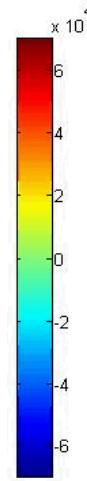
Exact model



Fraunhofer model



Experimental image



Apse model

