

The Derivation of System Responses for a Mil-Standard Road*

**84th Shock and Vibration Symposium.
November 4-8, 2013
Atlanta, Georgia**

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Outline

- **Background**
- **Measurement of Road Environment**
- **Derivation of Mil Std Inputs and Responses**
- **Derivation of Shaker Test Specifications**
- **Summary**



Background

- **The Mil Std 810 (MS810) truck transportation vibration specifications [1] have historically been implemented as a set of three single axis vibration tests applied to the store at the base of its shipping configuration (i.e., the truck bed)**
 - Force limited vibration theory indicates that such an approach is overly conservative
- **The purpose of this study is twofold**
 - To generate realistic worst case Multi-Degree-of-Freedom (MDOF) inputs and responses consistent with MS810
 - To develop a set of multi-point response limit test control spectra based on those inputs



Measurement of Road Environment

- **The key to defining realistic test specifications is to measure the true field environment**
- **A series of road tests were performed to measure responses for the following configurations**
 - A 5-ton uni-body flatbed and a flatbed tractor trailer
 - Interstate, rural highway, city streets, and dirt roads
- **As one might expect the measured responses were well below MS810 levels**
 - Hard to find worst case road

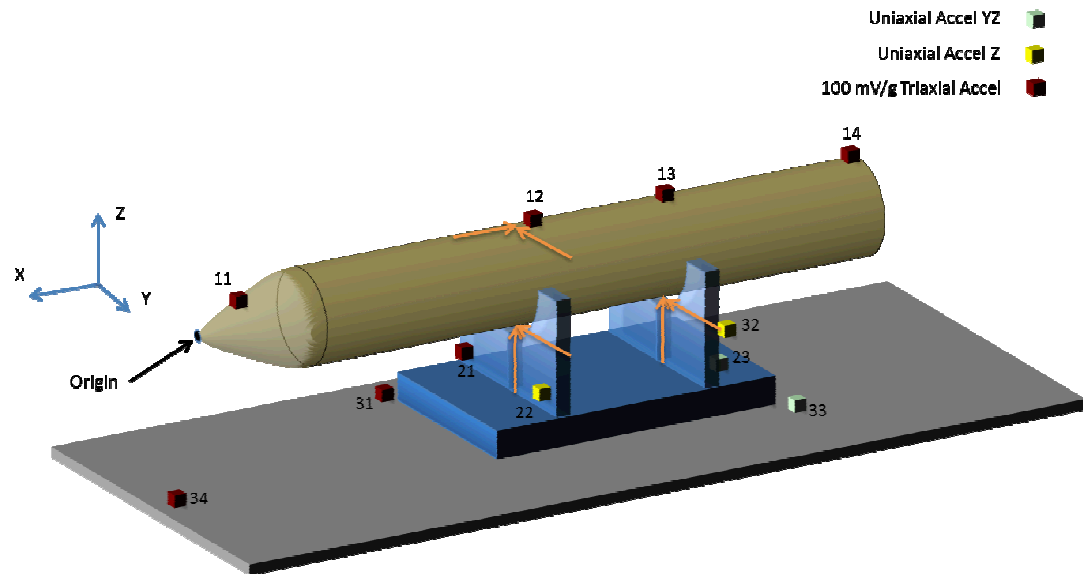
Measurement of Road Environment

Simulator on 5-ton Flatbed



Note that the H-Gear is resting on wooden chocks

Instrumentation Layout for Simulator



Responses were measured on the truck bed, the H-Gear deck, and the exterior of the simulator



Derivation of Mil Std Inputs and Responses

- **Must scale responses up to MS810 levels**
- **The responses were grouped into Spectral Density Matrices (SDMs)**
 - Truck bed (input), H-Gear, and simulator
 - Multiple-Input-Multiple-Output (MIMO) Transmissibility Response Functions (TRFs) were generated between the input SDM and the two response SDMs
- **Two issues had to be resolved**
 - The appropriate method for scaling the amplitude
 - Method for preserving the phase and coherence between the inputs

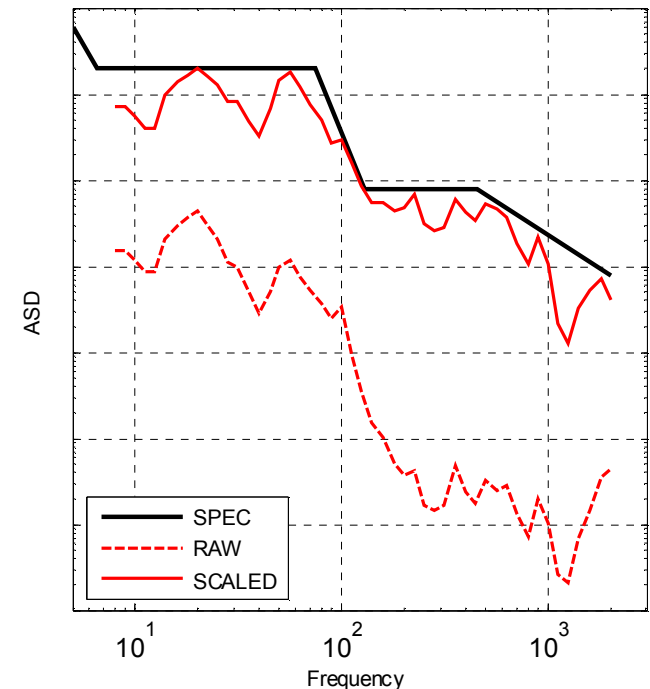


Magnitude Scaling of Responses

- **When scaling the field response amplitudes up to MS810 levels, it would certainly be conservative to scale the responses frequency-by-frequency**
 - However, if one considers how specifications are typically derived, the straight line segment specifications tend to hug the peaks and fill in the valleys
 - It is the filling in of the valleys in the input specifications that tend to over drive the store responses
- **Two types of scaling were considered**
 - Peak Scaling
 - Grms scaling

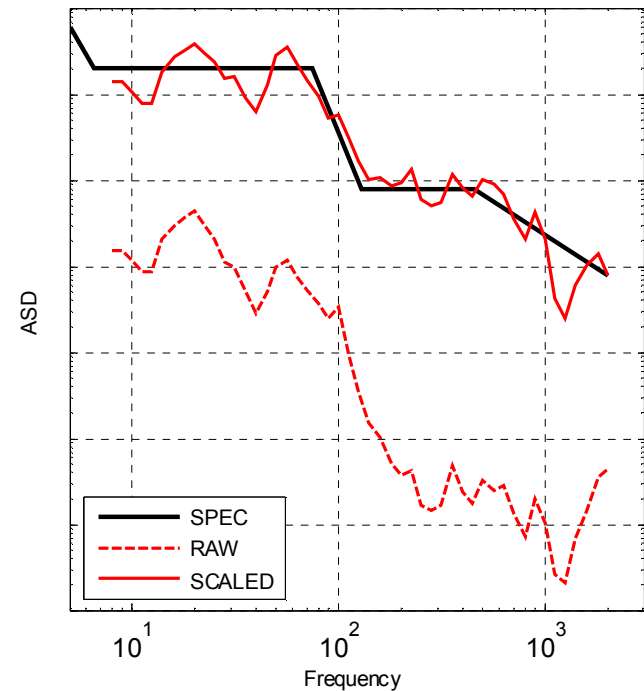
Peak Scaling

- An algorithm was developed to scale the peaks in the raw field data until they touch the specification and to let the valleys be scaled as a linear function of the scale factors for the peaks on either side



Grms Scaling

- The original MS810 specifications were based on VIBRAN spectra using extremely coarse analysis bands
- Therefore, it makes sense to adjust the peak scaled ASD to match the Grms of the MS810 spectra in each analysis band





Phase and Coherence

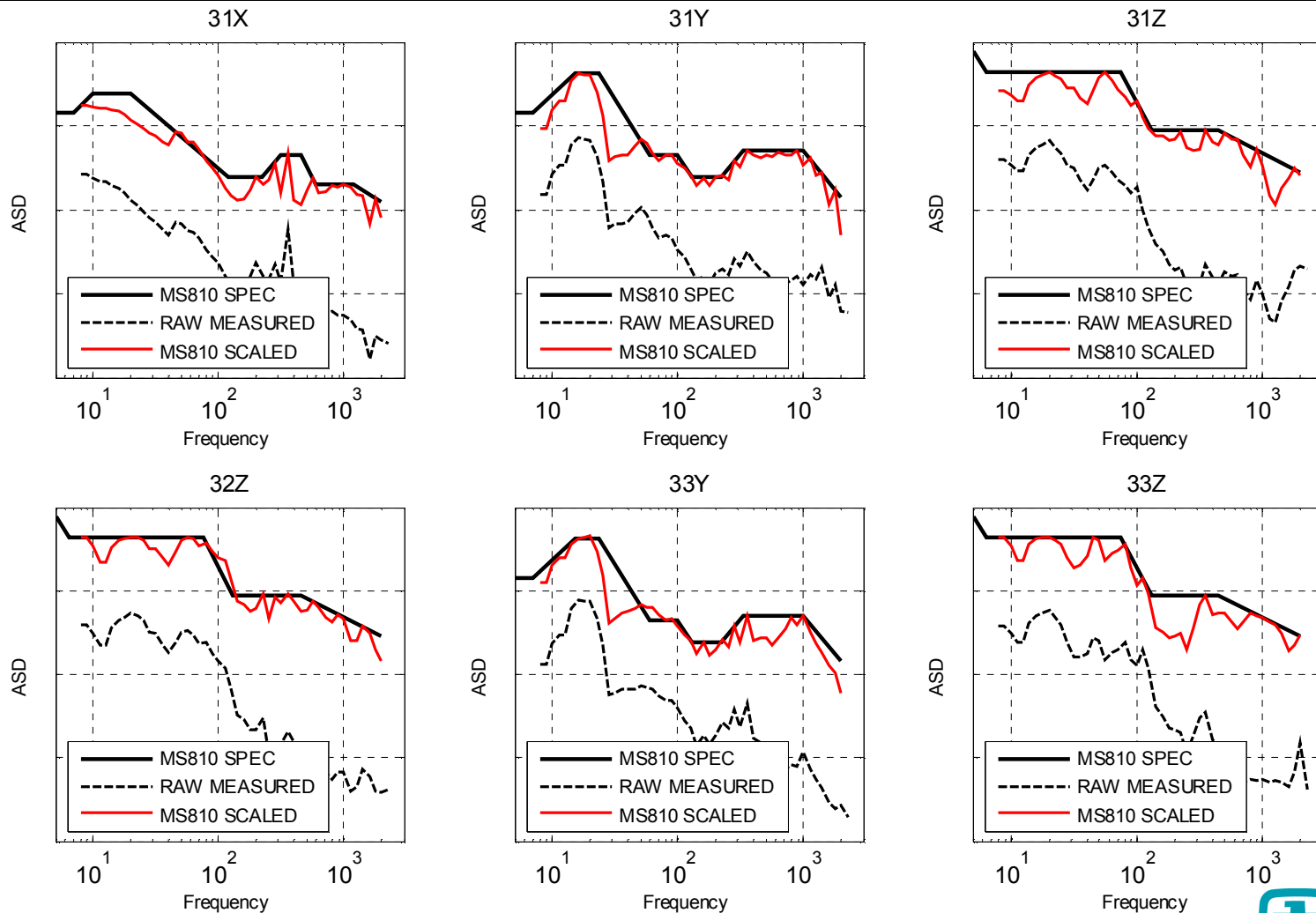
- **When scaling the road responses to MS810 levels it is crucial that we preserve the “true” phase and coherence between the inputs**
 - **Normalize the raw input SDM, S_{IJR} , by dividing each term in that SDM by the square root of the adjacent diagonal terms**

$$S_{IJN} = S_{IJR} / \text{sqrt}(S_{IIR} S_{JJR})$$

- **Multiply the terms in the normalized SDM, S_{IJN} by the desired peak or Grms scaled ASDs to produce a scaled SDM having the same phase and coherence as the raw SDM**

$$S_{IJS} = S_{IJN} \text{sqrt}(S_{IIS} S_{JJS})$$

Scaled Inputs (Peak Scaling)





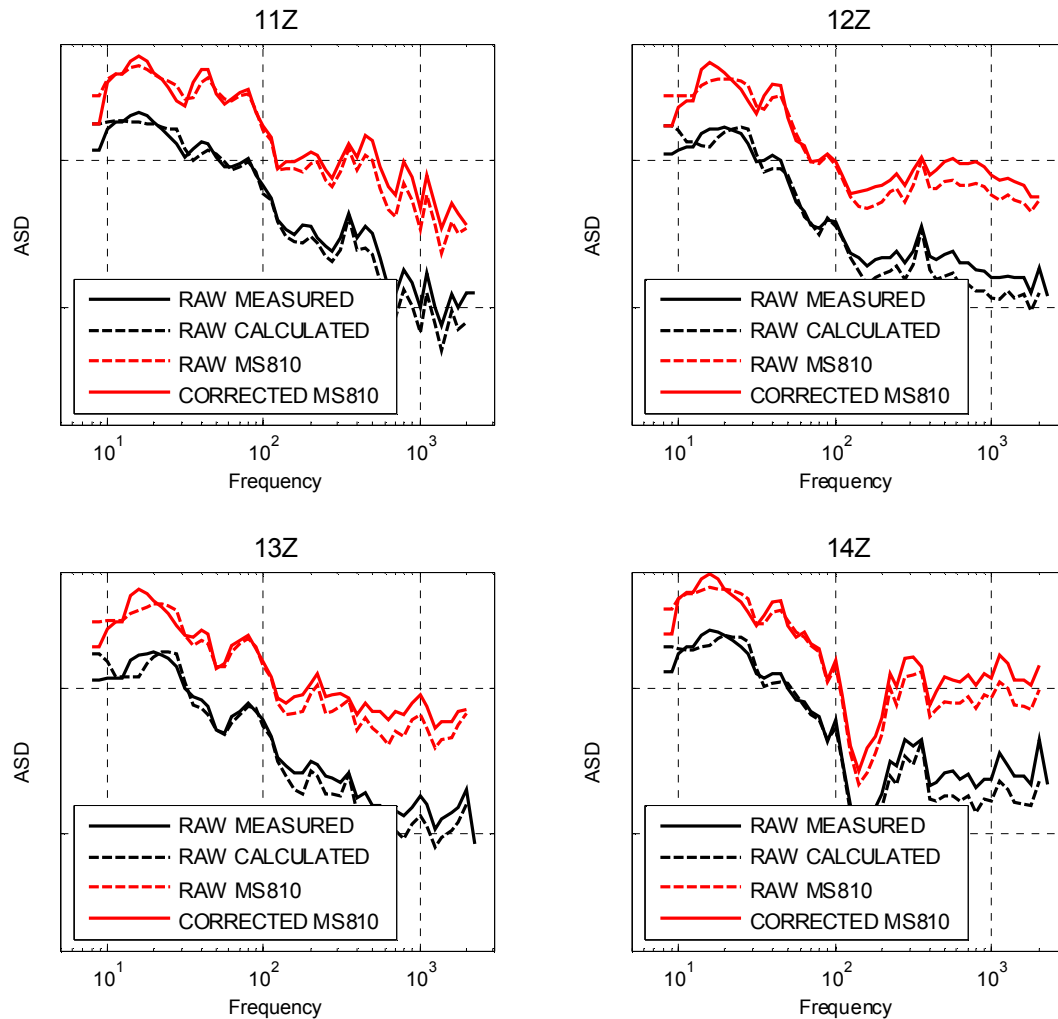
Derivation of Realistic Mil Std 810 Responses

- The response SDM, S_{RSP} , is computed using the scaled input SDM, S_{INP} , and the TRFs, H

$$S_{RSP} = S_{INP} H S'_{INP}$$

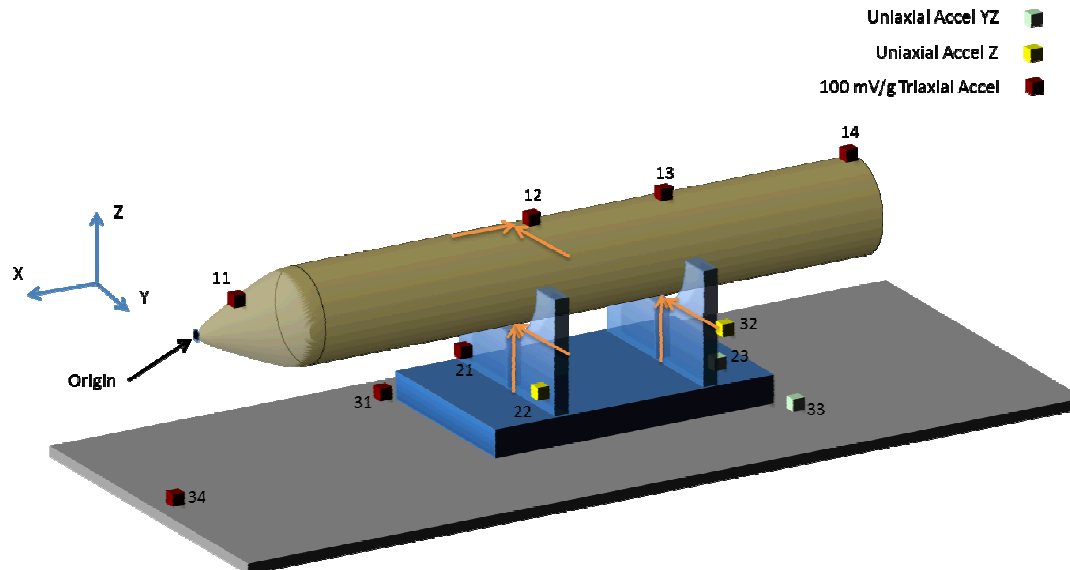
- The TRFs do not account for the incoherent portion of the response so the values of S_{RSP} are under predicted when the coherence is less than 1
 - The under prediction can be estimated by computing the response to the raw input
 - The diagonal terms in S_{RSP} were then multiplied by the ratio of the measured and synthesized raw response ASDs

Example of Scaled Responses



Derivation of Shaker Inputs

- A single axis shaker test can only match one response location exactly
- Therefore, the decision was made to derive an input that reproduced the response at the four simulator response points in a least squares sense

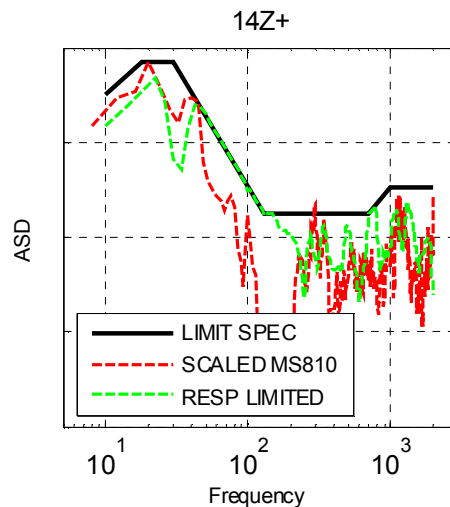
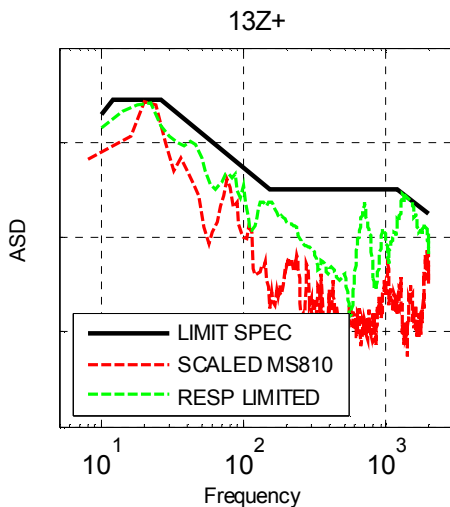
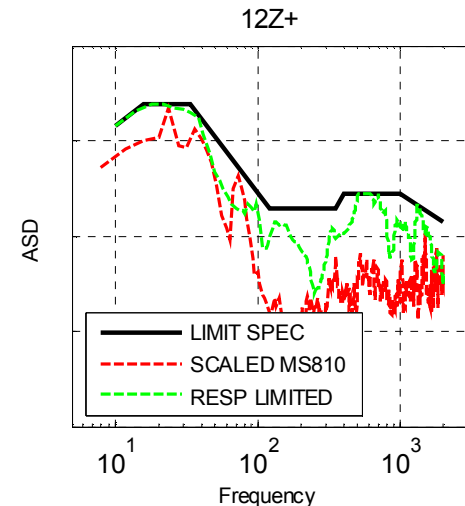
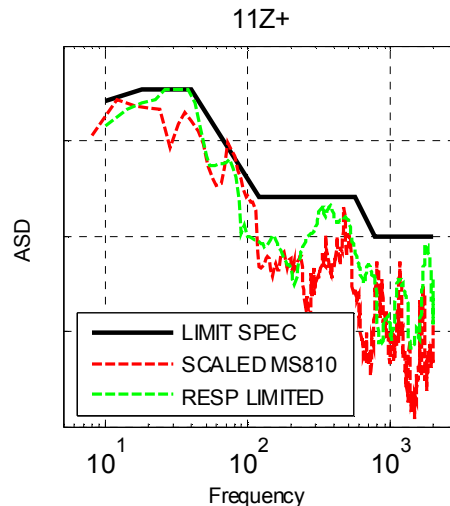
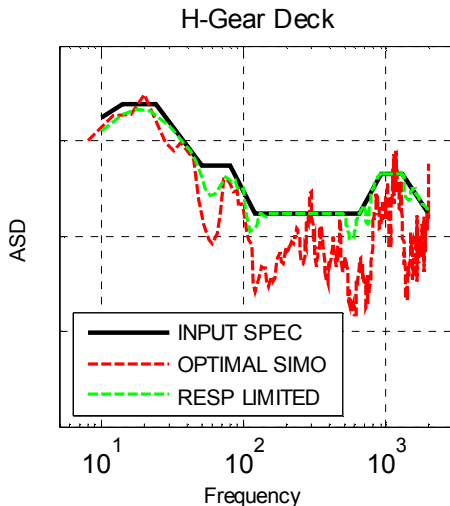




Derivation of Shaker Test Specifications

- **A single input / multiple output (SIMO) model was used to derive the optimum least squares input to the H-gear [2]**
 - The actual input specification is the straight line segment envelope of the optimal SIMO input
- **Response limits were developed for the four external locations on the simulator**
 - The response limits were primarily defined so as to prevent overdriving of the unit in frequency bands where the input spectra filled in valleys in the SIMO spectra
 - Good limit spectra should allow for frequency shifts associated with unit-to-unit variability while keeping the lab test responses in line with the scaled MS810 responses

Example of Response Limiting Test Specifications



In a perfect test the “Resp Limited” spectra should slightly exceed the “Scaled Response”



Summary

- **This methodology provides a greater degree of realism than the traditional single axis base input control scheme**



References

- **[1] MIL-STD-810E; "Environmental Test Methods and Engineering Guidelines."**
- **[2] Cap, J. S., C' de Baca, M. K., and Smallwood, D. O.; "A Technique for the Identification of the Optimum Inputs for a Vibration or Acoustic Test"; Proceedings of the 76th Shock & Vibration Symposium; October 31st – November 3rd, 2005; Destin, FL.**