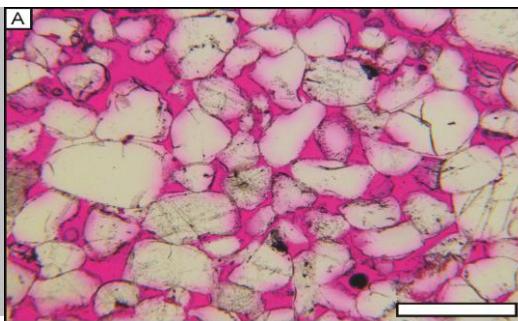
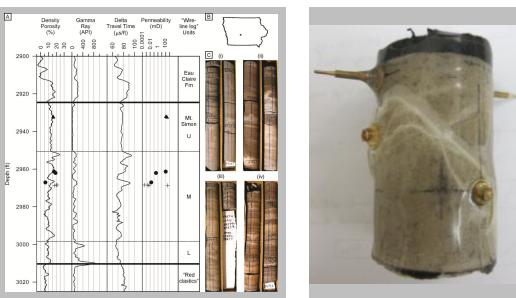


# Elasto-Plastic Constitutive Behavior in Three Lithofacies of the Cambrian Mt. Simon Sandstone, Illinois Basin, USA



<sup>1</sup>Thomas A. Dewers, <sup>2</sup>Pania Newell, <sup>1</sup>Scott Broome, <sup>1</sup>Jason Heath, and <sup>1</sup>Steve Bauer

<sup>1</sup>Geomechanics and <sup>2</sup>Mechanical Engineering  
Sandia National Laboratories  
Albuquerque, NM, USA

*AGU Annual Meeting, December 3, 2012*

*San Francisco, CA*



*Exceptional  
service  
in the  
national  
interest*



Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000. SAND No. 2012-xxxxP

# Acknowledgements

- Analysis and modeling was supported as part of the Center for Frontiers of Subsurface Energy Security, an Energy Frontier Research Center funded by the U.S. Department of Energy, Office of Science, Basic Energy Sciences under Award Number DE-SC0001114.
- Experimental testing and interpretation was funded by the Department of Energy, Office of Electricity.
- Thanks to Peter Mozley (NM Tech, geological interpretations), Randy Everett (SNL, testing), Tim Fuller (SNL, constitutive modeling).
- Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

# Outline

- Practical Considerations and Geologic Background
- Axisymmetric Compression Geomechanical Testing
- Nonlinear Elasticity and Elastic-Plastic Coupling
- Constitutive Modeling with Kayenta
- Conclusions

# Motivation and Regional Framework

## Precambrian Structure Map of Iowa and Location of CAES Keith #1 Well

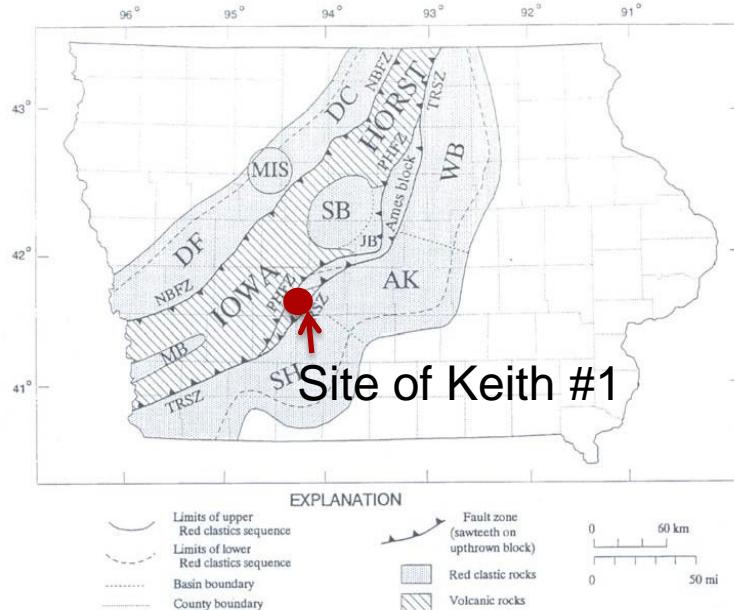
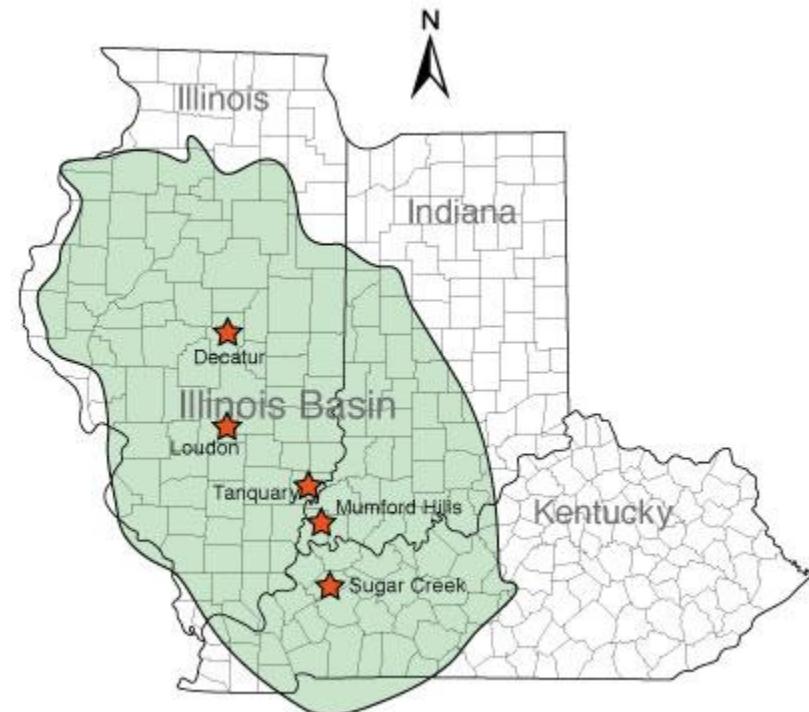


Figure 12. Structural components of the Midcontinent Rift System (MRS) in Iowa (modified from Anderson, 1992; and Anderson, 1995, fig. 1, p. 56, copyright ©1995 Kluwer Academic Publishers, used with kind permission from Kluwer Academic Publishers). NBFZ, Northern Boundary Fault Zone; TRSZ, Thurman-Redfield Structural Zone; PHFZ, Perry-Hampton Fault Zone; DF, Defiance Basin; DC, Duncan Basin; SH, Shenandoah Basin; AK, Ankeny Basin; WB, Wellsburg Basin; SB, Stratford Basin; JB, Jewell Basin; MB, Mineola Basin; MIS, Manson Impact Structure.

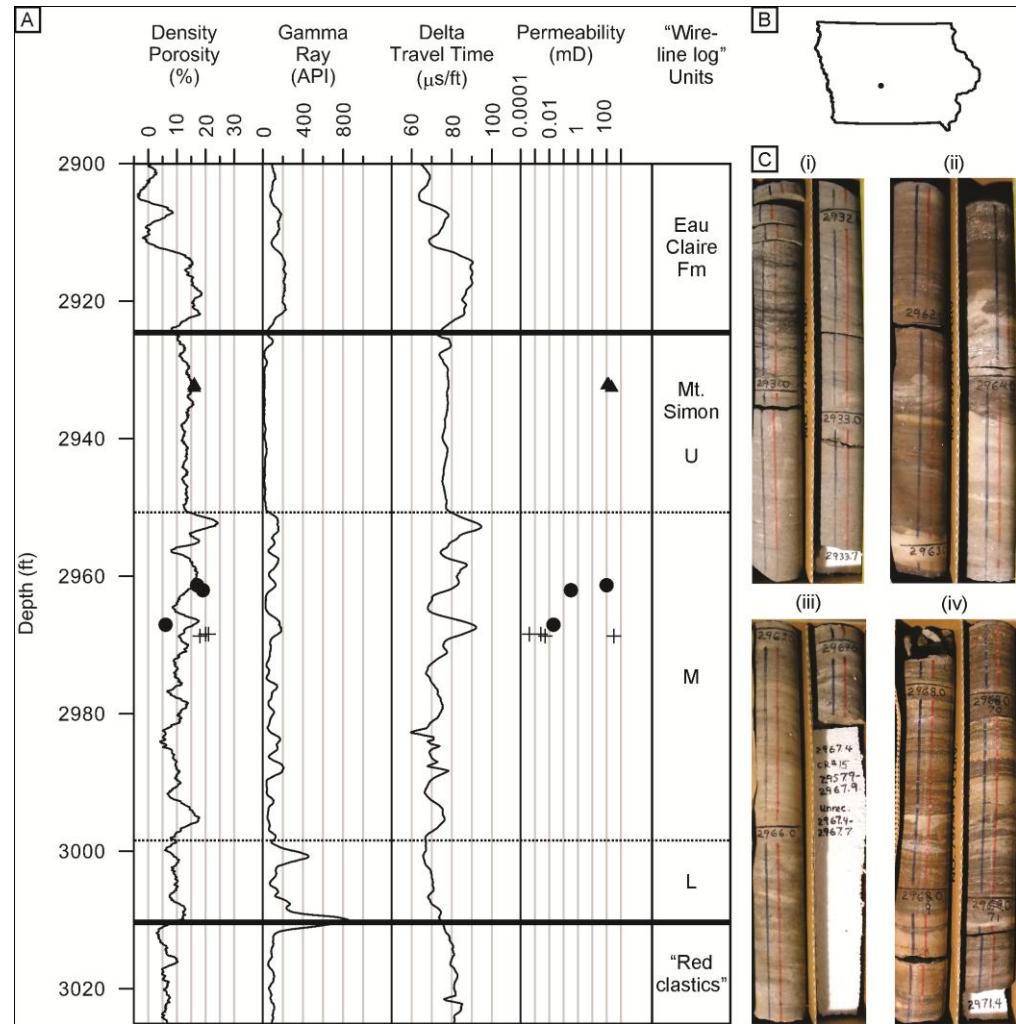
## Mount Simon, Illinois Basin and CCS Injection Projects



<http://sequestration.org/mgscprojects/index.html>

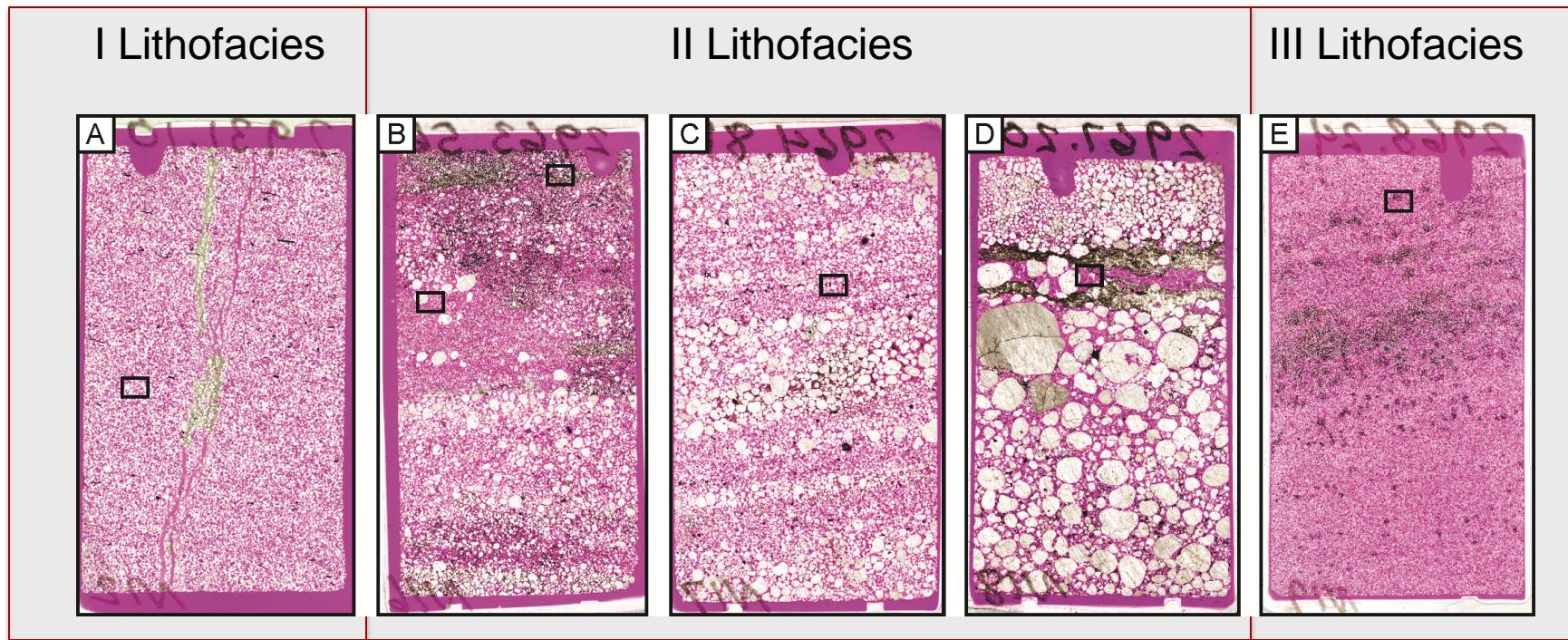
# Core, Well Logs and Sampling

- Three well-log units (U, M, L)
- Three sampled lithofacies (I, II, III)
- Similar porosities but markedly different permeabilities
- Distribution of facies similar to those on east flank of Illinois Basin (Saeed and Evans, 2012)
- Similar to lower portions of Illinois Basin lithofacies (Bowen et al. 2011) incl. main injection horizon but lacking upper “B-cap” muddy facies



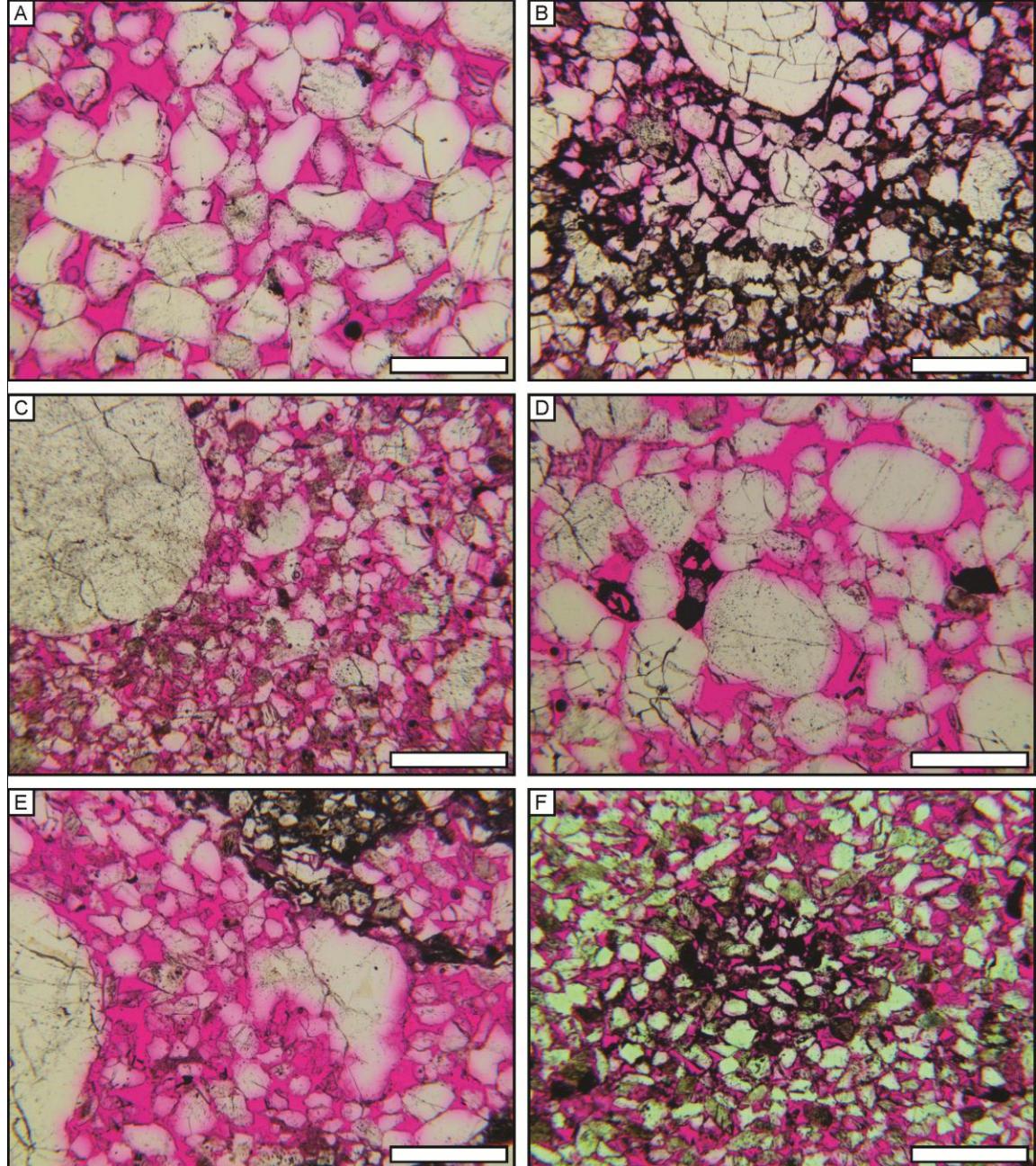
# Lithofacies Interpretation

- I Lithofacies (main injection unit in IB): quartz-rich sand flat B1 facies of *Saeed and Evans* [2012] or the “sandy tidal” facies of *Fischietto* [2009]
- II Lithofacies: heterolithic T2 “mixed flat” facies and “sand flat to tidal channel” B2 facies of *Saeed and Evans* [2012] or the “mixed fluvial-eolian tidal” and “braided fluvial” facies of *Fischietto* [2009]
- III Lithofacies: mud flat T1 facies of *Saeed and Evans* [2012] or the muddy tidal facies of *Fischietto* [2009]



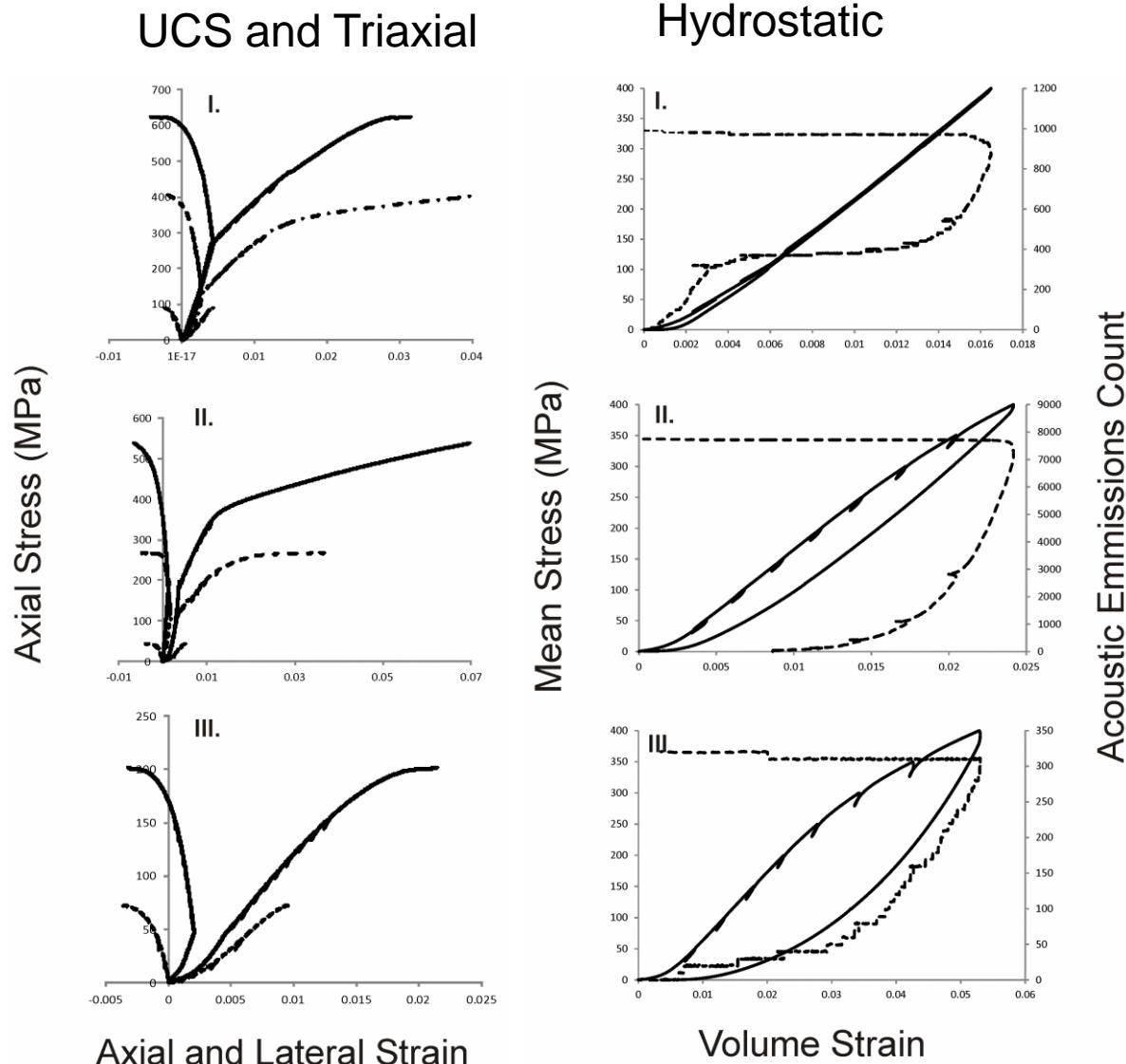
## Microstructure and Cements of I, II, and III lithofacies

- I lithofacies (A) – fine grain size, well sorted, ubiquitous quartz cements
- II lithofacies (B,C,D,E) – poorly sorted, subarkosic, clay cement
- III lithofacies (F) – very fine to silty to mud grain size, abundant feldspar, clay and hematite cement



# Axisymmetric Testing Results

- 1 hydrostat, 1 UCS, and 2 Triaxial Tests per facies
- 3.82 cm x 7.62 cm right cylinders with UV-cured polyurethane jackets
- Room T and nominally dry
- AE Counts on many of the tests
- Samples taken to failure at lower mean stresses
- One triaxial test for III lithofacies failed to record lateral strain data



# Yield and Failure Envelopes

Failure envelope:

$$F_f(I_1) = a_1 - a_3 e^{-a_2 I_1} + a_4 I_1$$

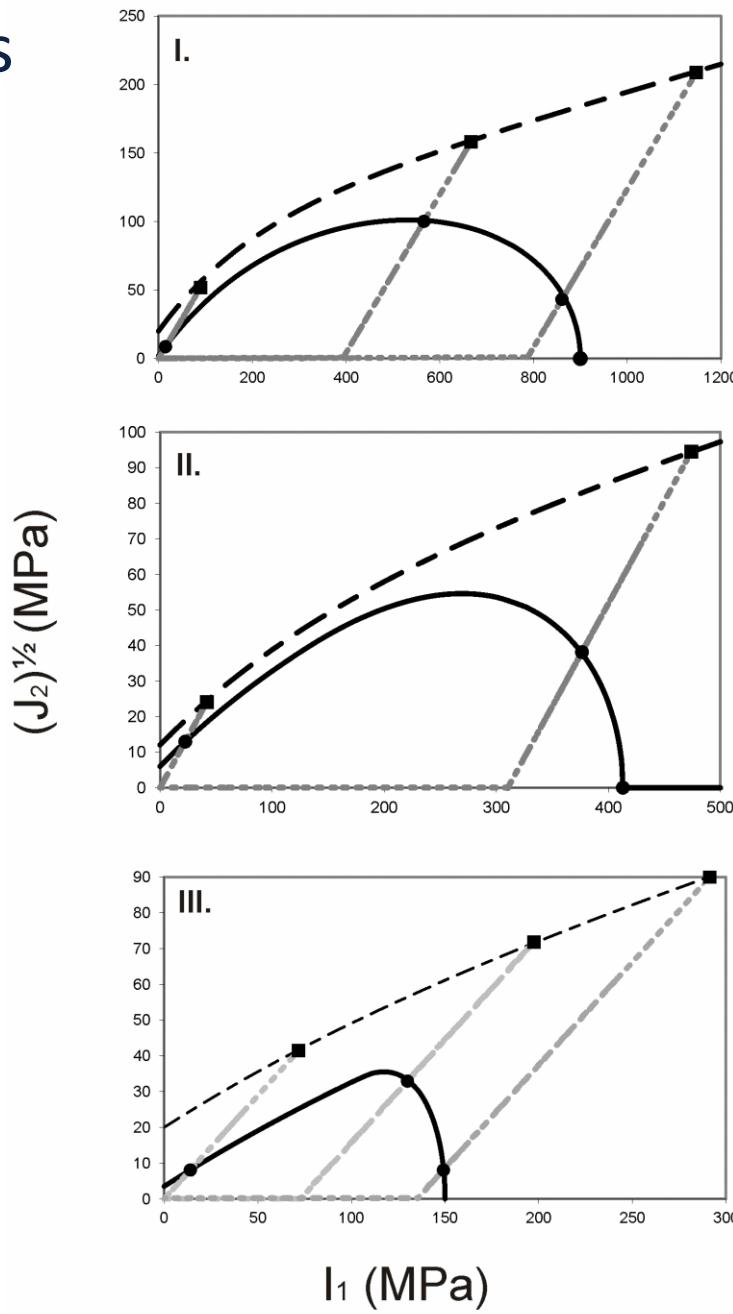
Yield Surface

$$\sqrt{J_2} = \frac{f_f(I_1) f_c(I_1)}{\Gamma(\theta)}$$

$$f_f(I_1) = F_f(I_1) - N$$

$$f_c^2(I_1, \kappa) = 1 - \frac{(I_1 - \kappa)(|I_1 - \kappa| + (I_1 - \kappa))}{2(X - \kappa)^2}$$

(After Brannon et al., 2009; Pelessone, 1989)



# Nonlinear Elasticity and Elastic-Plastic Coupling

## Secant and Tangent Moduli

Shear Modulus Stress Dependence

$$G = G_0(1 + G_1\tau + G_2\sigma)$$

Bulk Modulus Stress Dependence

$$K = K_0(1 + K_1\sigma - K_2e^{-K_3\sigma})$$

Tangent Bulk Modulus

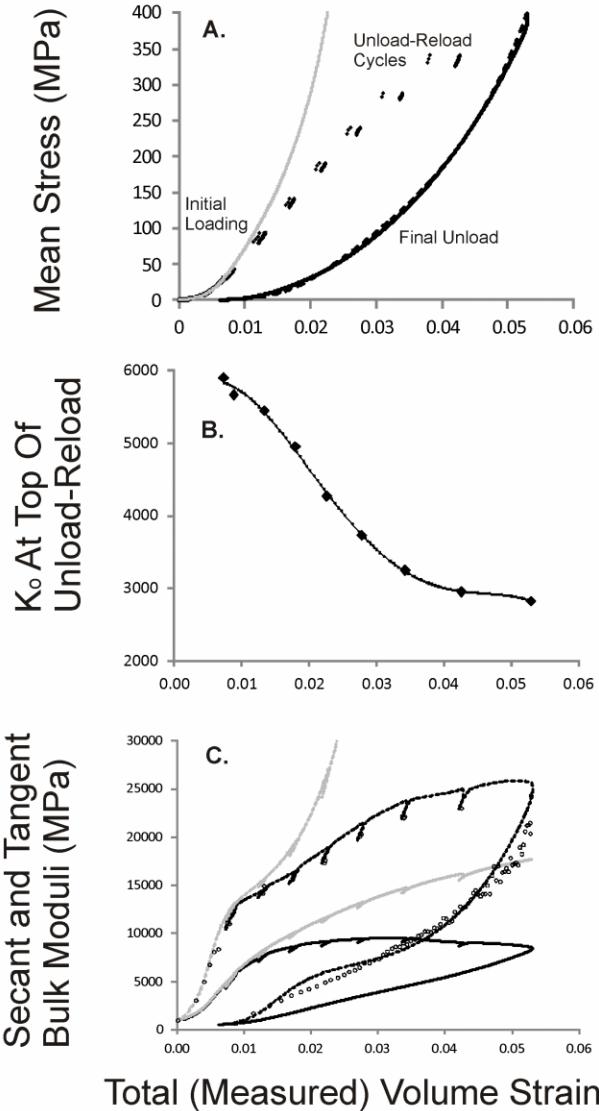
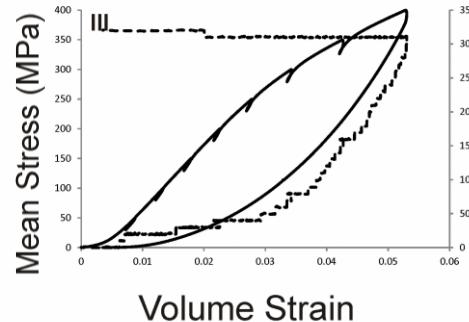
$$K_{\tan} = \left\{ \frac{1}{K} - \frac{\sigma}{K^2} (K_0 K_1 + K_0 K_2 K_3 e^{-K_3 \sigma}) \right\}^{-1}$$

## Evolution with Plastic Strain

$$K = K_0' (1 - K_4 e^{-K_5 / \varepsilon_p}) (1 + K_1 \sigma - K_2 e^{-K_3 \sigma})$$

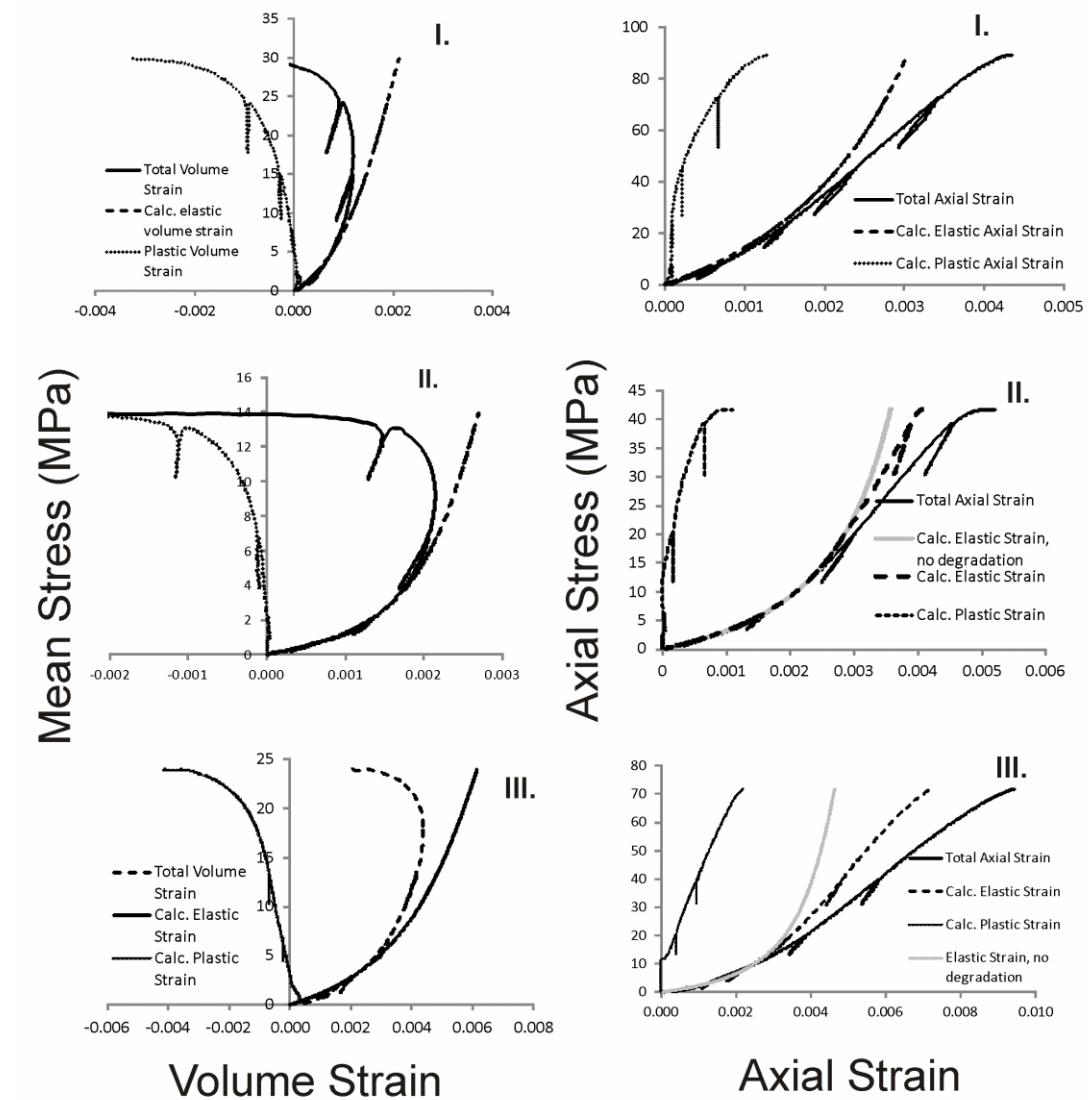
$$G = G_0' (1 - G_3 e^{-G_4 / \gamma_p}) (1 + G_1 \tau + G_2 \sigma)$$

## Facies III Hydrostat

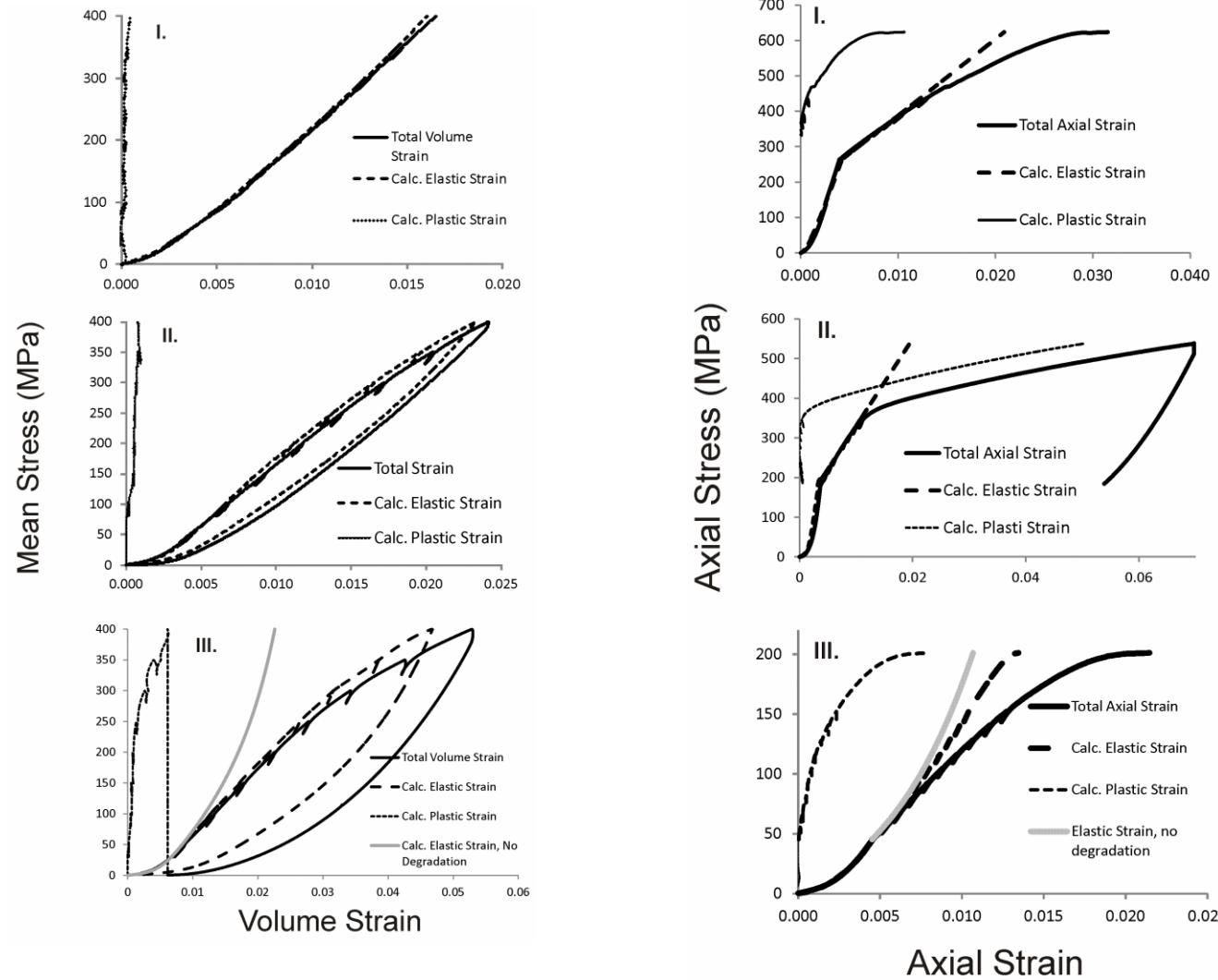


# Strain Partitioning, UCS Tests

- Determine Stress- and Plastic Strain Dependence of Elastic Moduli
- Calculate Elastic Strains
- Determine Plastic Strains By Difference
- Elastic-Plastic Coupling (compare dark dashed lines with grey lines) accounts for bulk of total volume strain post-yielding



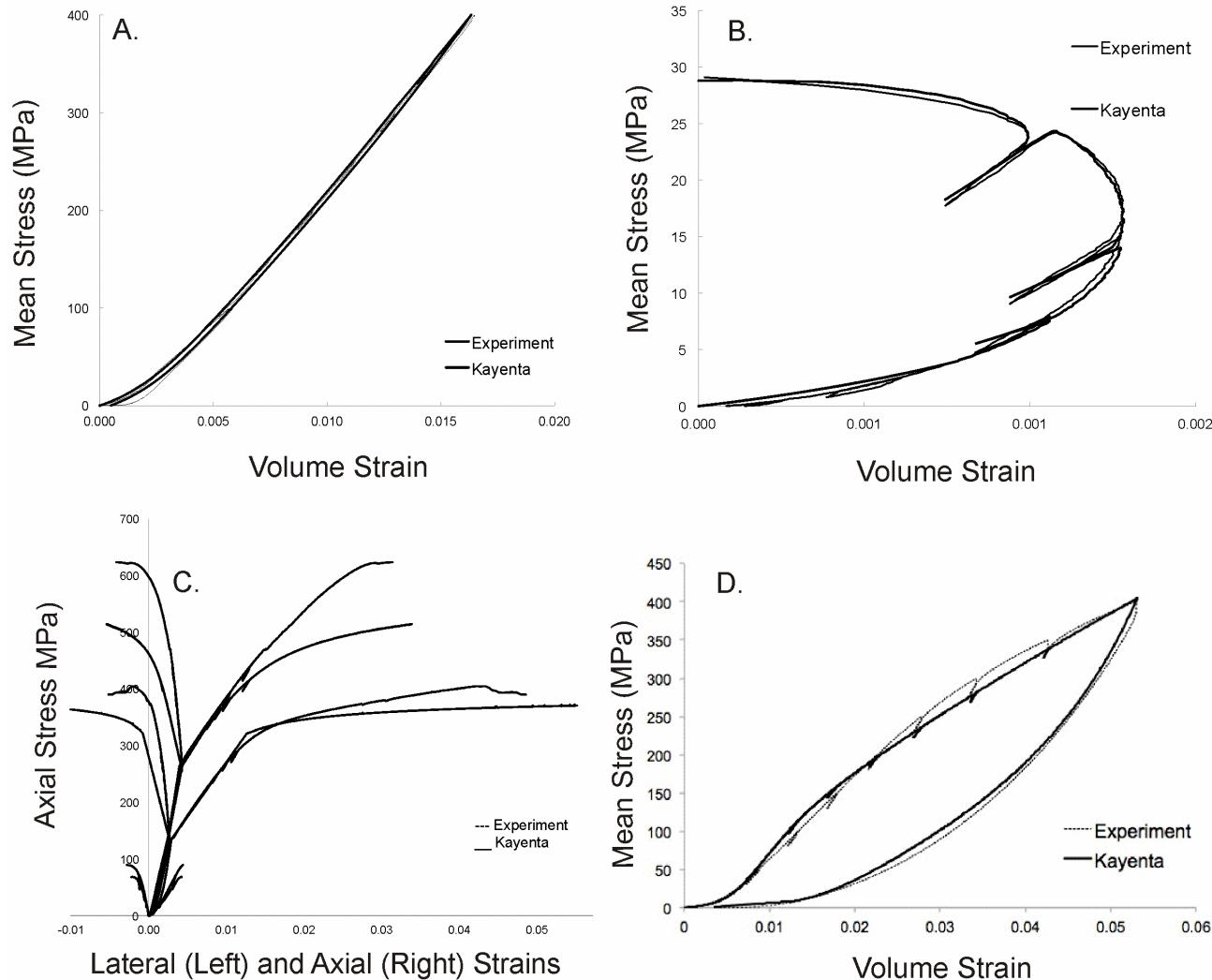
# Strain Partitioning; Hydro and Triaxial



# Elastic-Plastic Constitutive Modeling

## Kayenta Includes:

- Non-Associative Plasticity
- Stress Invariant Dep. Failure
- Elliptical Cap Surface
- Kinematic Hardening
- Isotropic Hardening
- Nonlinear Elasticity
- Elastic-Plastic Coupling



Developed by Brannon et al.  
2009

# Conclusions

- Facies I (equivant to main injection horizon in Illinois Basin) is largely elastic to 300 MPa
- Weaker facies II and III exhibit elastic-plastic coupling
- Big difference in in yielding and failure envelopes although porosities are similar. Strongest control is cement type.
- Kayenta constitutive model captures essential features of Mount Simon lithofacies elastic-plastic geomechanical behavior observed in experiments. It can be included in most FEM models.