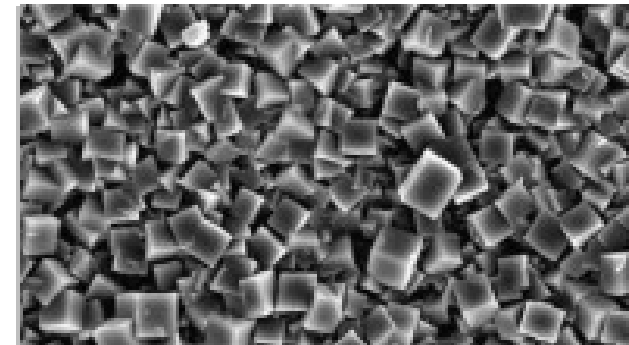


*Exceptional service in the national interest*



# Importance of Flexibility in Simulating Gas Diffusion through Metal-Organic Frameworks

Marie V. Parkes,<sup>\*</sup> Hakan Demir, David S. Sholl,  
Jeffery A. Greathouse, Mark A. Allendorf

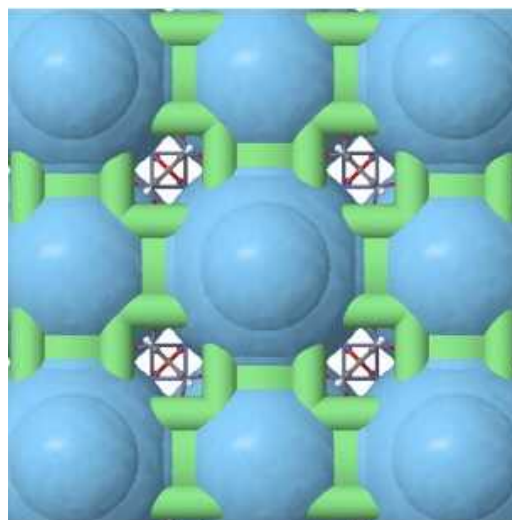
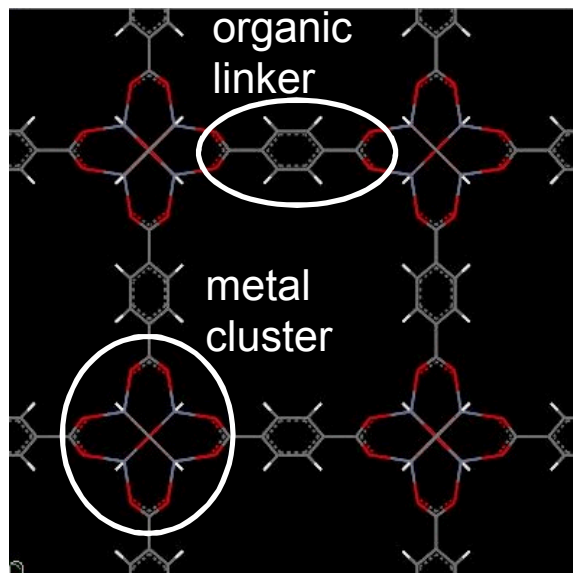
Sandia National Laboratories, Georgia Institute of Technology



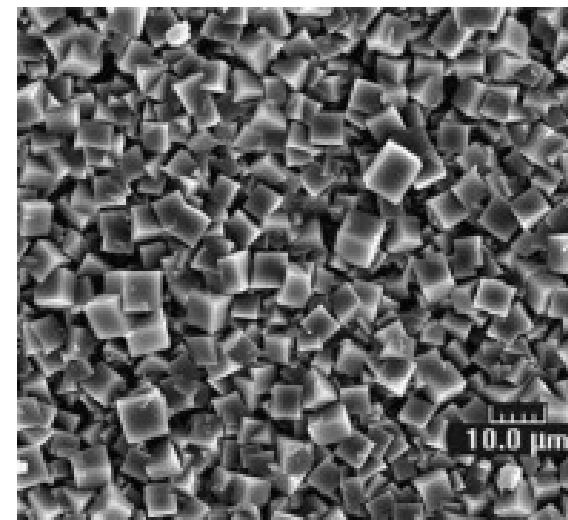
Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000. SAND NO. 2011-XXXXP

# Metal-Organic Frameworks (MOFs)

- Porous solids made of an extended network of metal clusters coordinated to multidentate organic linkers
- Surface areas up to  $5900 \text{ m}^2\text{g}^{-1}$
- “Crystalline sponges”



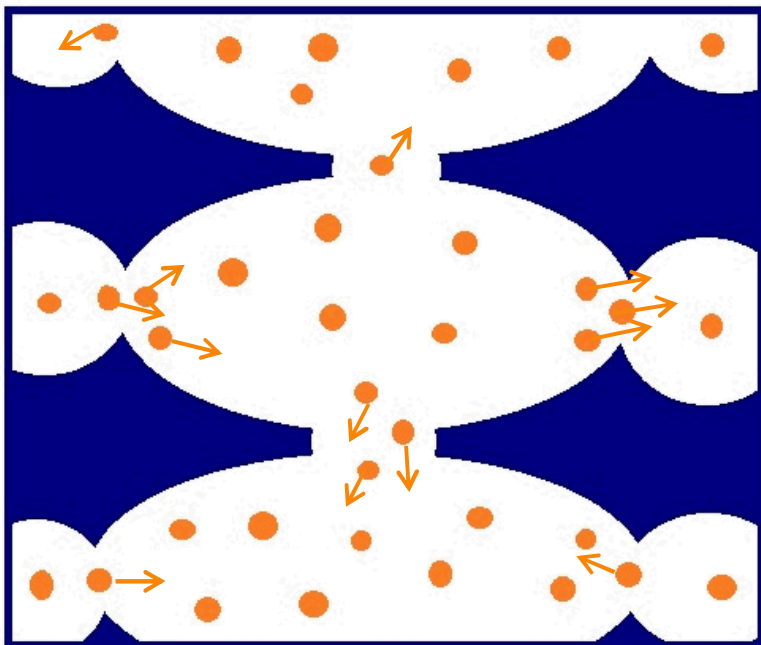
Reprinted from Microporous Mesoporous Mater. 165, E. L. First, C. A. Floudas, 32-39, Copyright 2013, with permission from Elsevier.



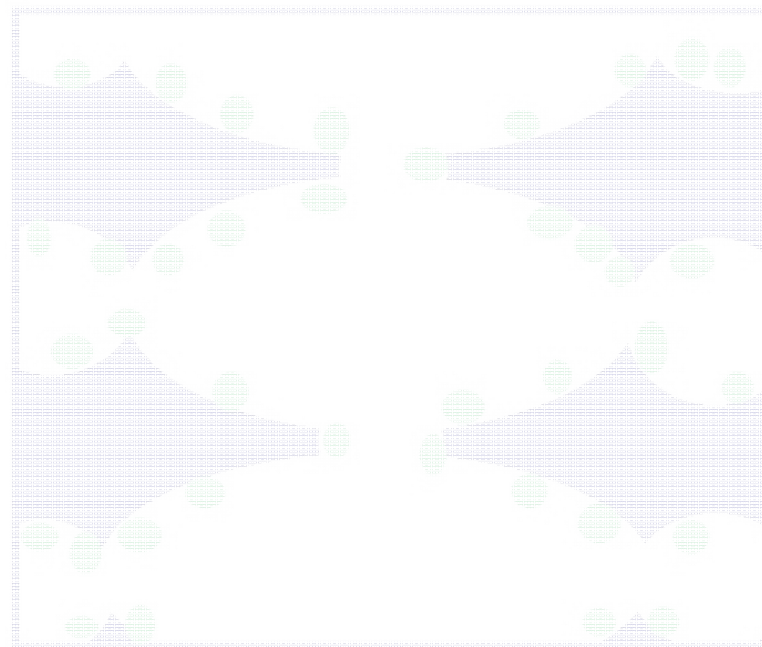
Reprinted from Microporous Mesoporous Mater. 123, Y. Yoo, Z. Lai, H.-K. Jeong, 100-106, Copyright 2009, with permission from Elsevier.

# Separation of Gases in MOFs

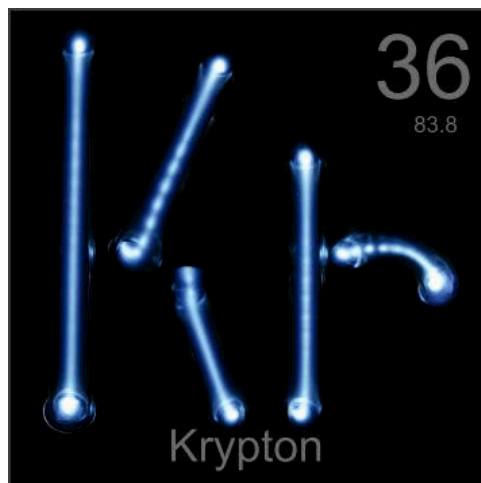
## Diffusion between MOF cages



## Adsorption on MOF surface



# Noble Gas Separations



Stock photos from [www.periodictable.com](http://www.periodictable.com).

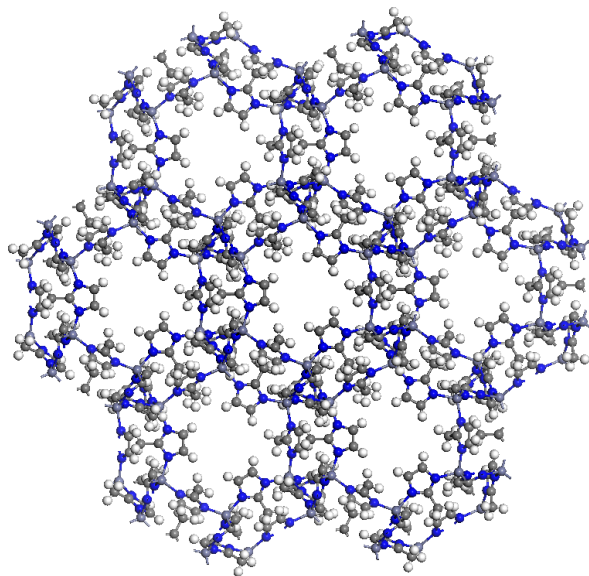
Noble gas uses:

- Cryogenic refrigerants
- Carrier gases
- Lighting
- Laser applications

Capture and separation are challenging:

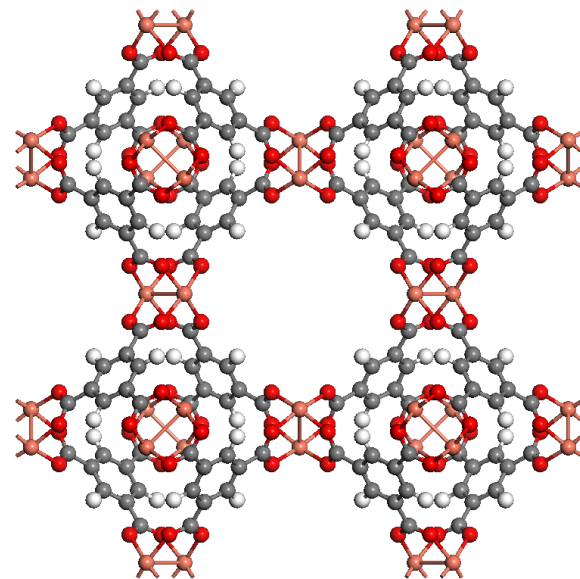
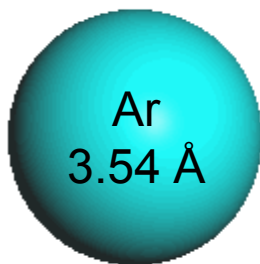
- Low natural abundance
- Relatively inert

# Noble Gas Diffusion



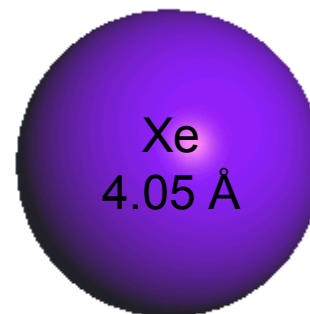
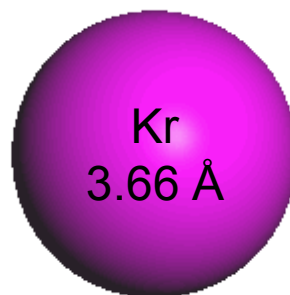
ZIF-8

- Window diameter 3.4 Å



HKUST-1

- Window diameters 4.1 Å, 6.9 Å



# Molecular Dynamics Simulations

## LAMMPS software

- MOF
  - ZIF-8
  - HKUST-1
- Gas
  - Ar
  - Kr
  - Xe
- Gas loading (0.3 to 65 bar)
  - 16/40/80 gas atoms (HKUST-1)
  - 32/80/160 gas atoms (ZIF-8)
- Force fields
  - UFF (rigid)
  - ZIF-8 FF<sup>1</sup> (flexible and rigid)
  - HKUST-1<sup>2</sup> FF (flexible and rigid)
- Initial structures
  - Published crystal structure
  - Force-field-optimized structure
  - DFT-optimized structure

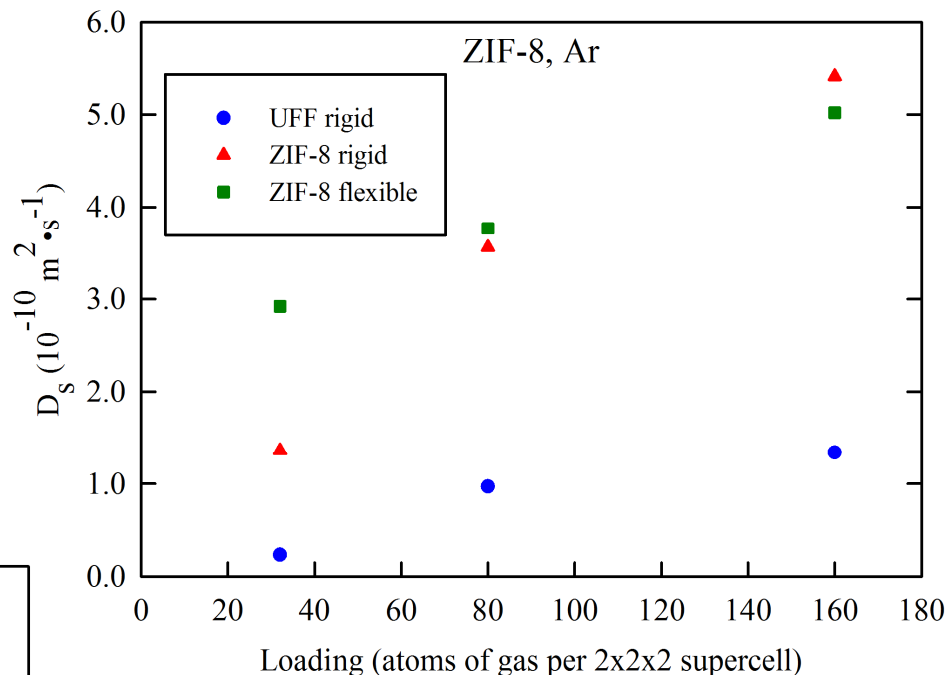
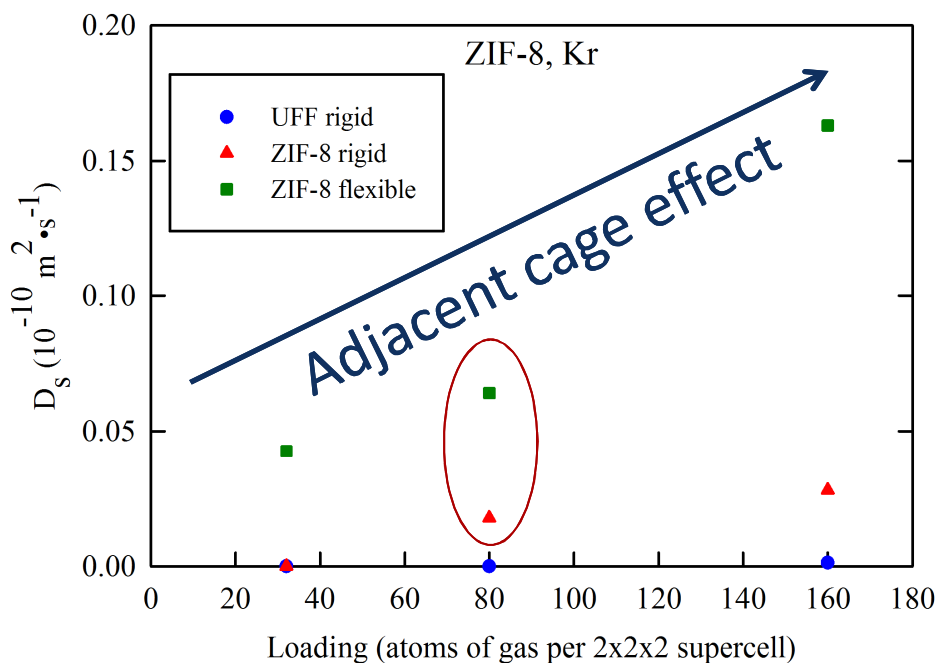
Equilibration (NVT, NVE) followed by data-gathering (20 ns NVE)

1. ZIF-8 FF: Zheng, B.; Sant, M.; Denontis, P.; Suffritti, G. *B. J. Phys. Chem. C* **2012**, *116*, 933-938.

2. HKUST-1 FF: Zhao, L.; Yang, Q.; Ma, Q.; Zhong, C.; Mi, J.; Liu, D. *J. Mol. Model.* **2011**, *17*, 227-234.

# Diffusion in ZIF-8

- No diffusion seen for Xe
- Ar diffusion greater than Kr diffusion

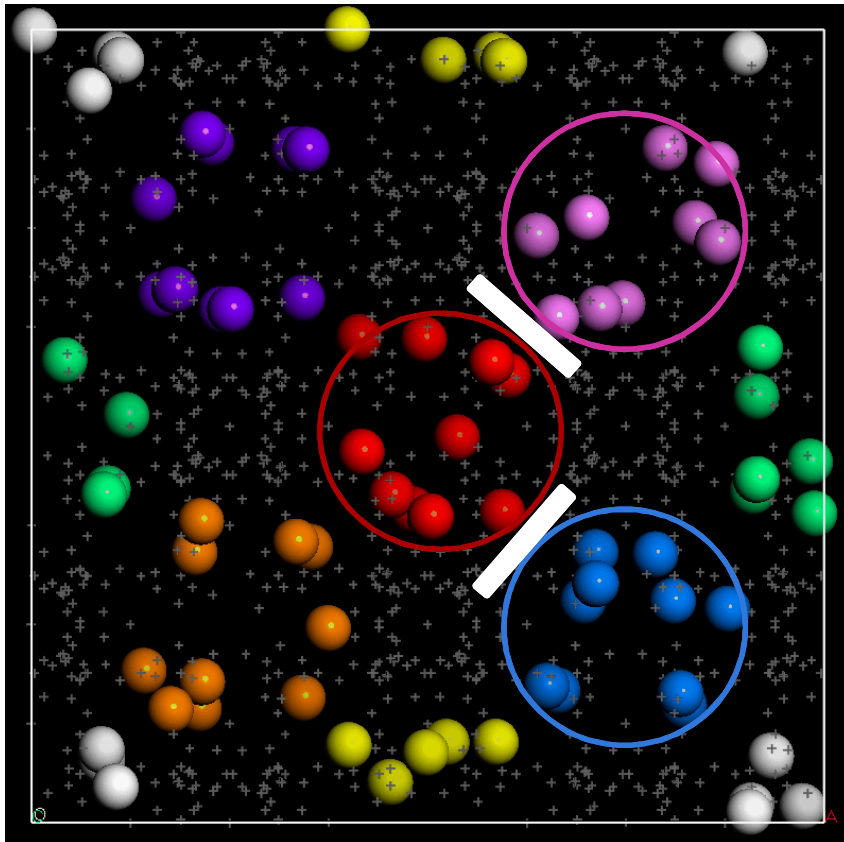


- Diffusion increases as loading increases (adjacent cage effect)
- Diffusion is greatest with flexible force field

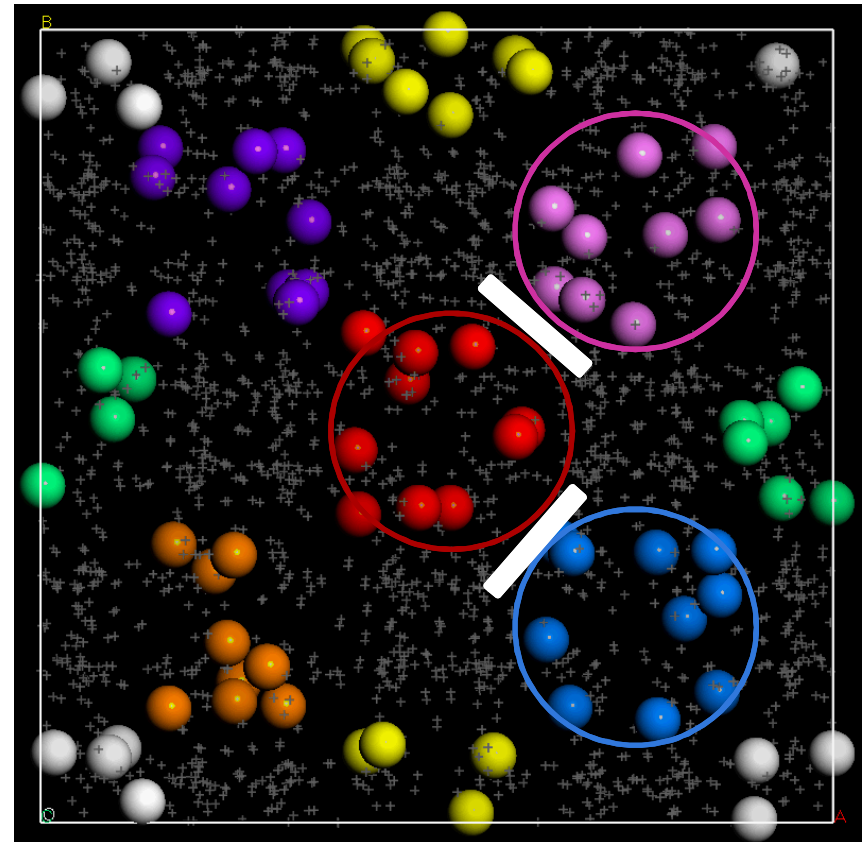


# Kr Diffusion in ZIF-8

Rigid

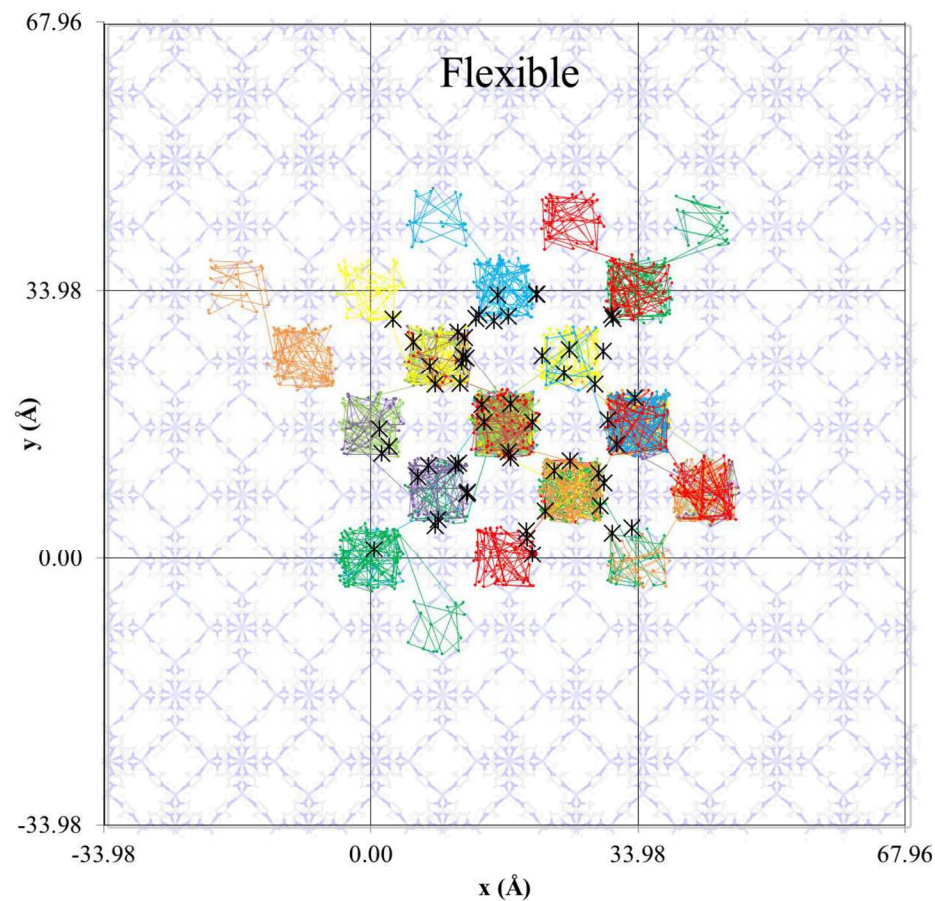
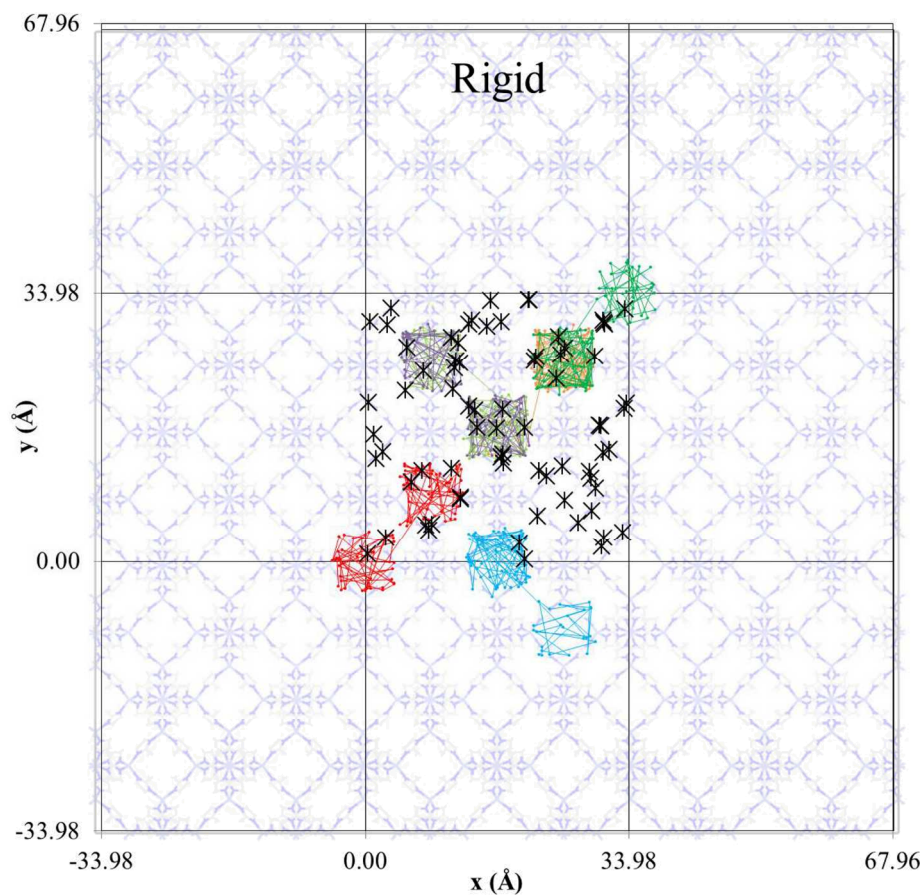


Flexible

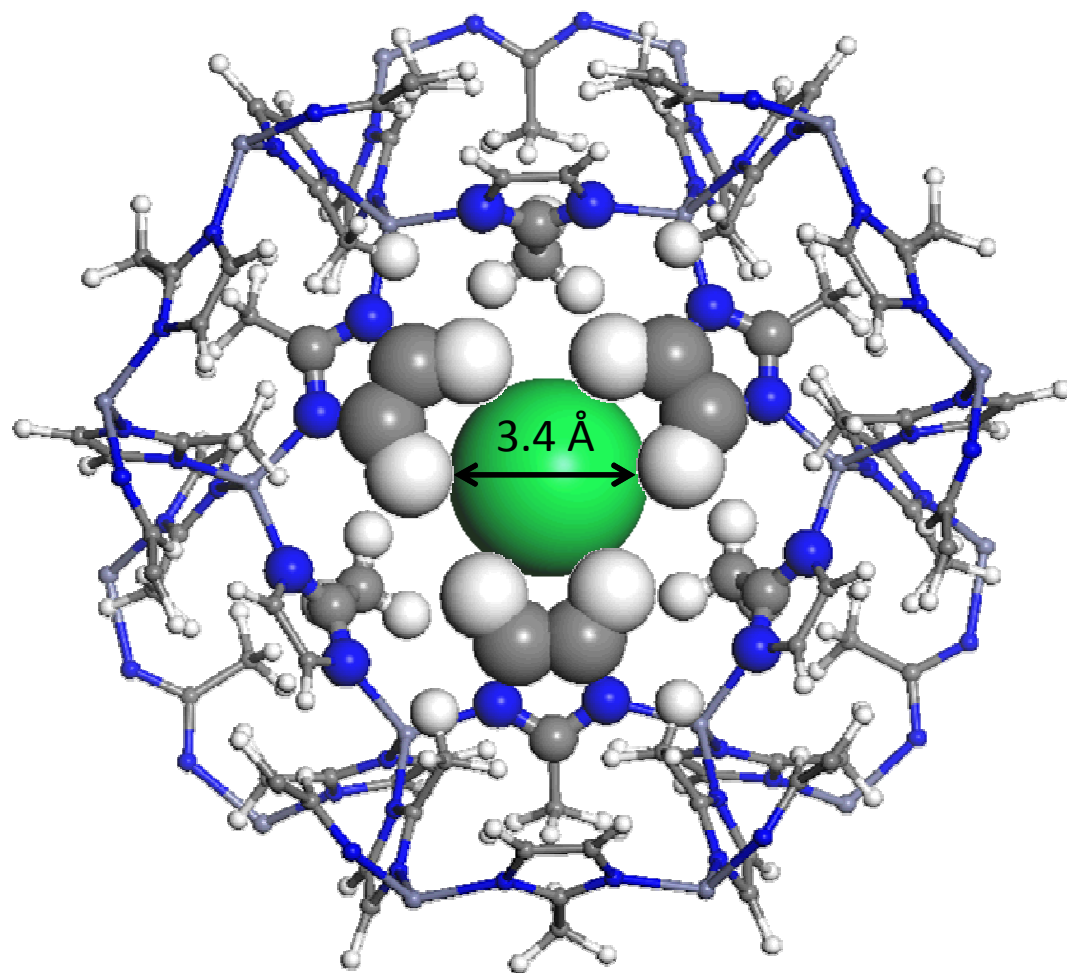




# Kr Diffusion in ZIF-8



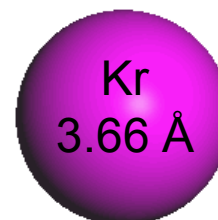
# Kr Diffusion in ZIF-8



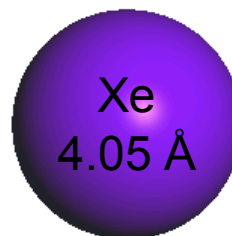
Fast diffusion



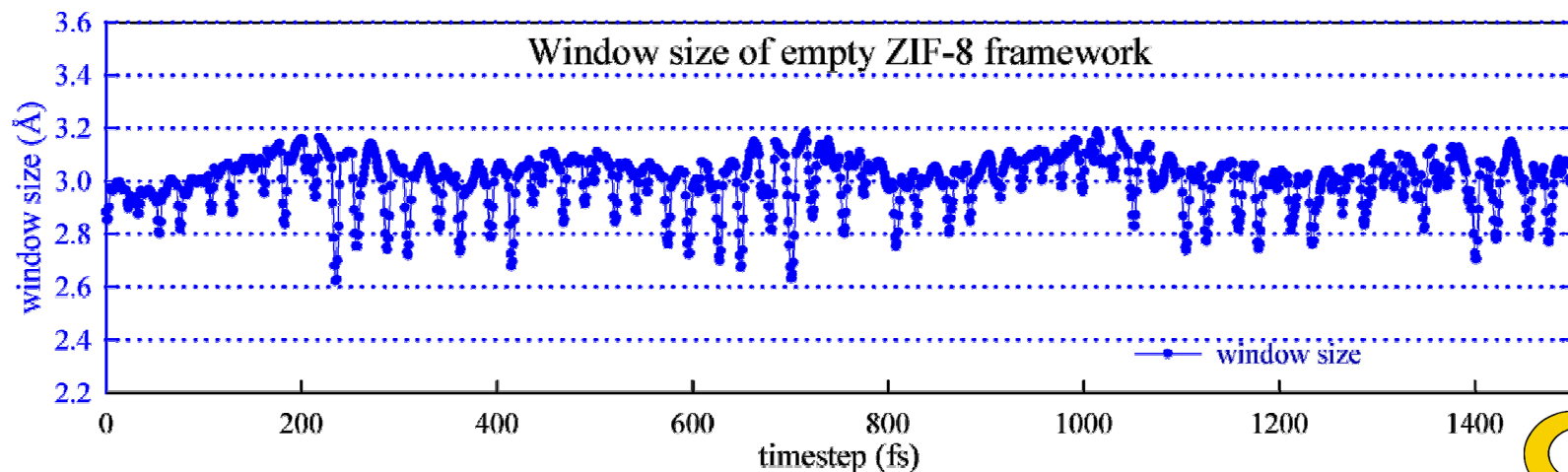
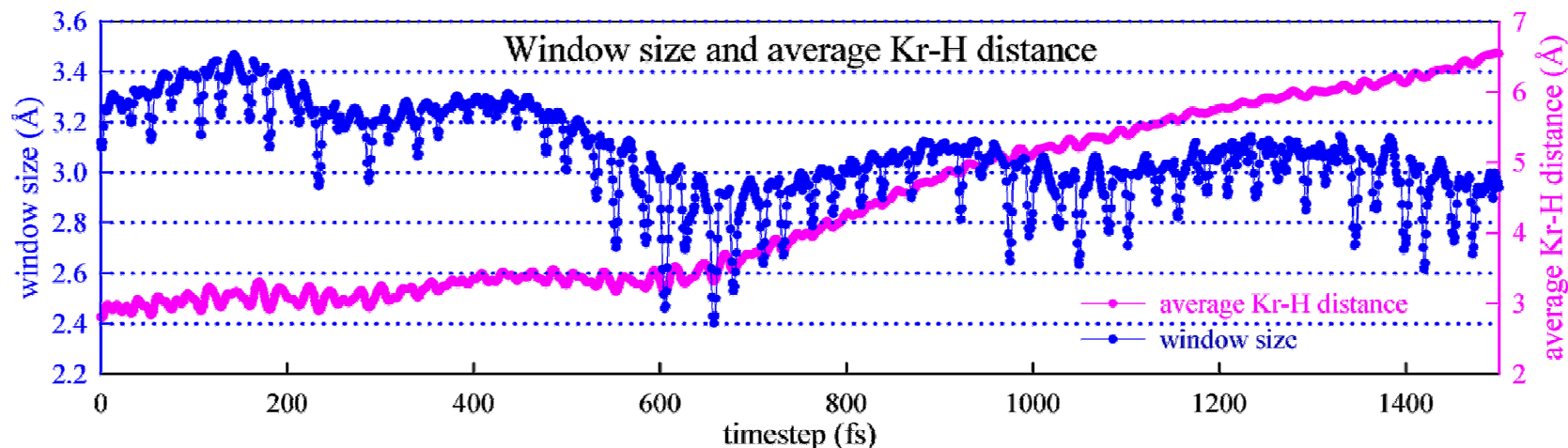
Limited diffusion



No diffusion



# Kr Diffusion in ZIF-8



# Conclusions

- Accurate description of guest diffusion in MOFs requires
  - MOF-specific force fields
  - Flexible frameworks (when MOF windows and guests are similar in size)
- Diffusion dependence on loading is greatest when MOF windows are similar in size to guest
- ZIF-8
  - Gas diffusion increases as loading increases (adjacent cage effect)
  - Kr diffusion strongly dependent on flexible framework
  - ZIF-8 window expands as Kr passes through

# Acknowledgments

Jeffery Greathouse

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Stephanie Teich-McGoldrick

David Sholl

Hakan Demir

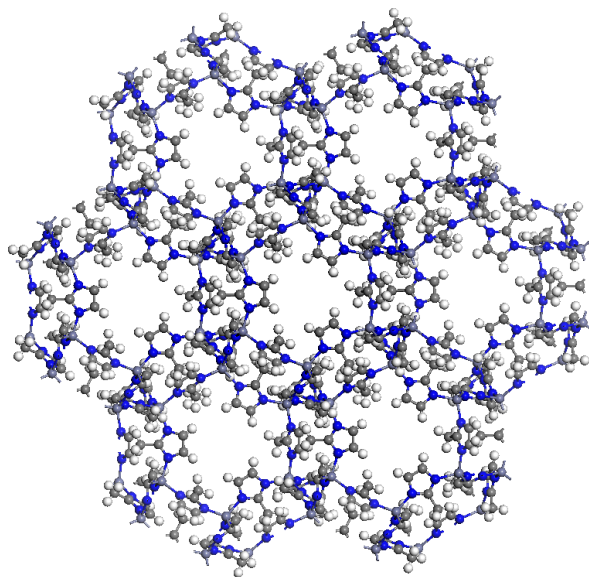


Funding provided by the  
U.S. Department of Energy



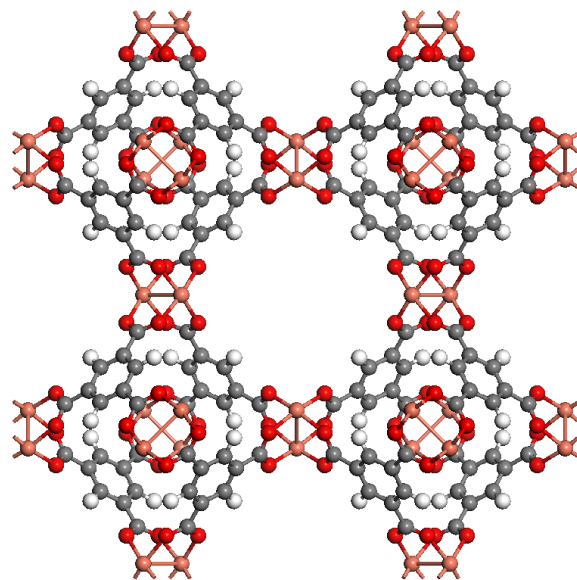
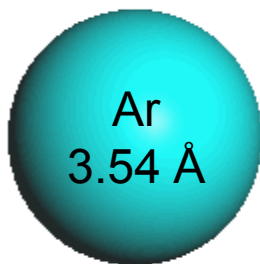
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# Noble Gas Diffusion



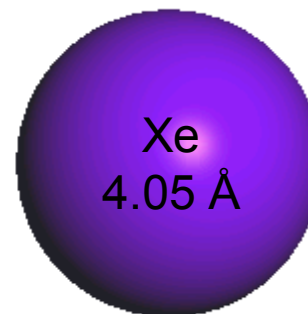
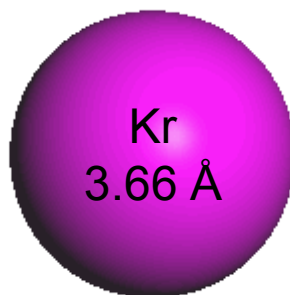
ZIF-8

- Window diameter 3.4 Å



HKUST-1

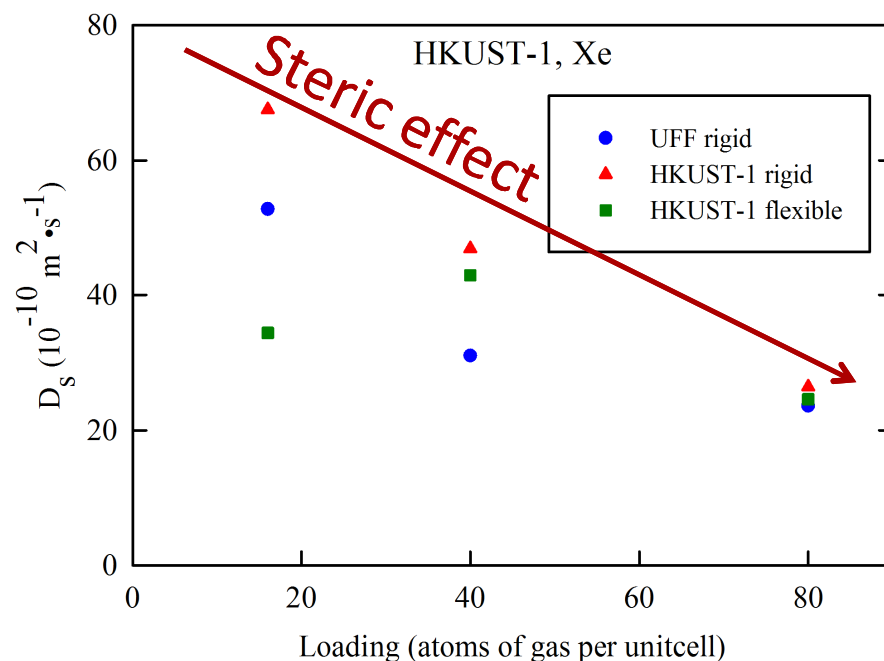
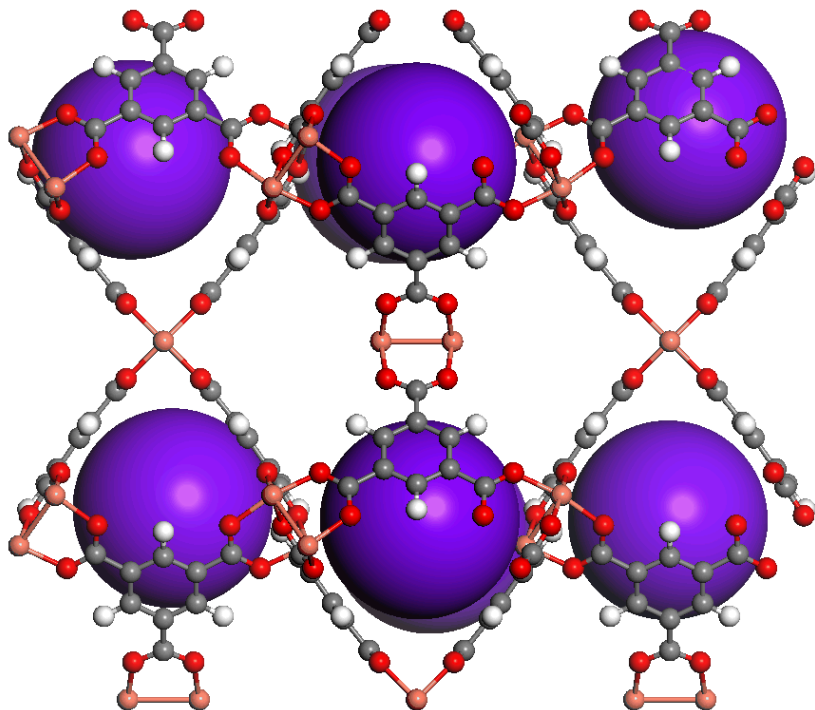
- Window diameters 4.1 Å, 6.9 Å





# Xe Diffusion in HKUST-1

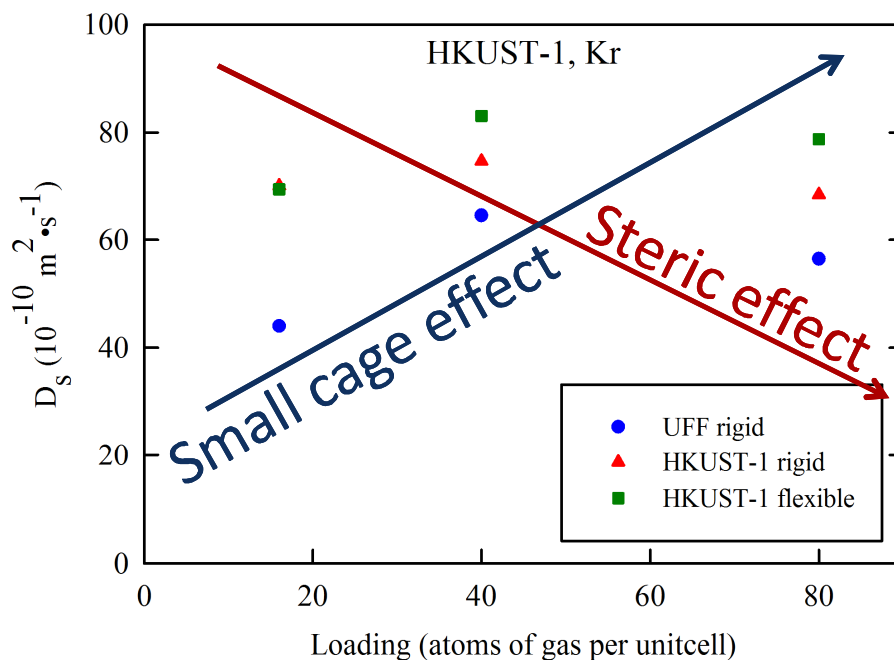
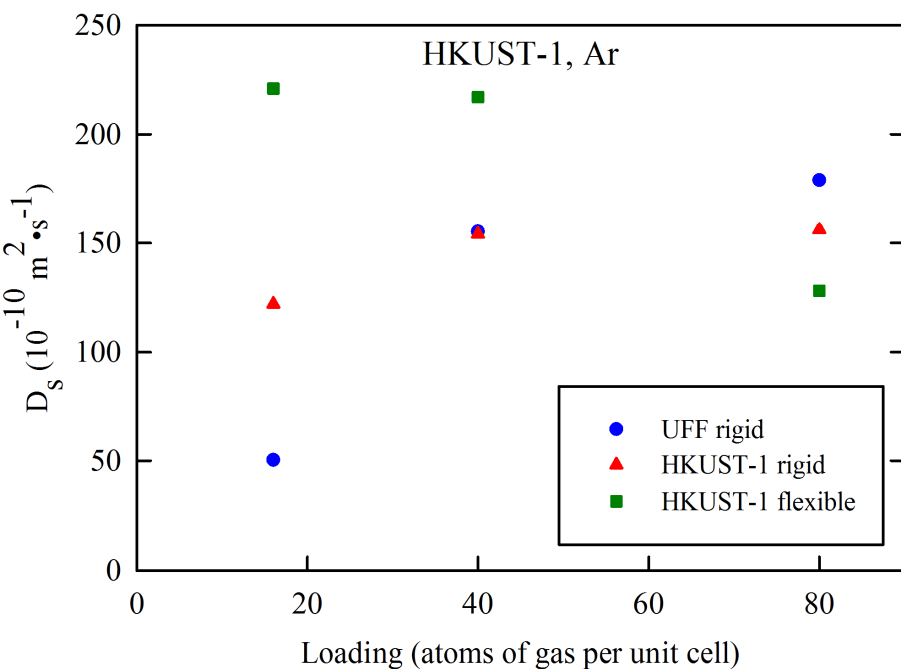
- Diffusion decreases as loading increases (steric effect)



- Eight gas atoms strongly adsorbed in octahedral cages with small windows (small cage effect)

# Kr/Ar Diffusion in HKUST-1

- Diffusion is greatest with flexible force field



- Loading dependence: steric effect and small cage effect compete

- Accurate description of guest diffusion in MOFs requires
  - MOF-specific force fields
  - Flexible frameworks (when MOF windows and guests are similar in size)
- Diffusion dependence on loading is greatest when MOF windows are similar in size to guest
- ZIF-8
  - Gas diffusion increases as loading increases (adjacent cage effect)
  - Kr diffusion strongly dependent on flexible framework
  - ZIF-8 window expands as Kr passes through
- HKUST-1
  - “Small cage effect” due to strong adsorption sites and small windows
  - Small cage effect and steric effect compete

# Acknowledgments

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Mark Allendorf



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Stephanie Teich-McGoldrick

David Sholl

Hakan Demir



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