



Simulations of Nanoparticle Ordering in Polymers via Solvent Evaporation

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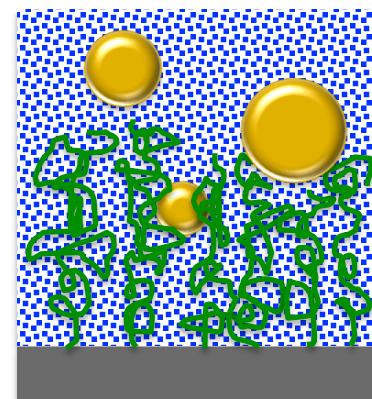


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- Generally, composites are made in order to have material properties better than the components
- Polymer film may be container for nanoparticles that possess key property
 - Responsive polymer could turn on/off nanoparticle property
- What determines the material properties?
 - Structure of composite
- How to control nanoparticle placement/distribution?
 - Interactions
 - Nonequilibrium effects (e.g. evaporation)

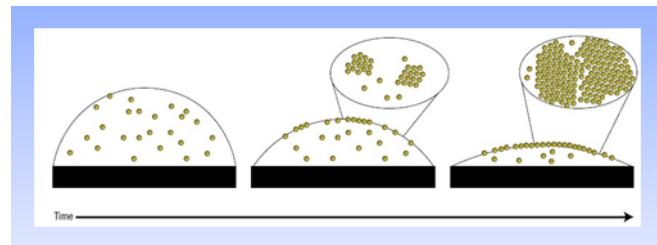
General system is polymer + nanoparticles + solvent



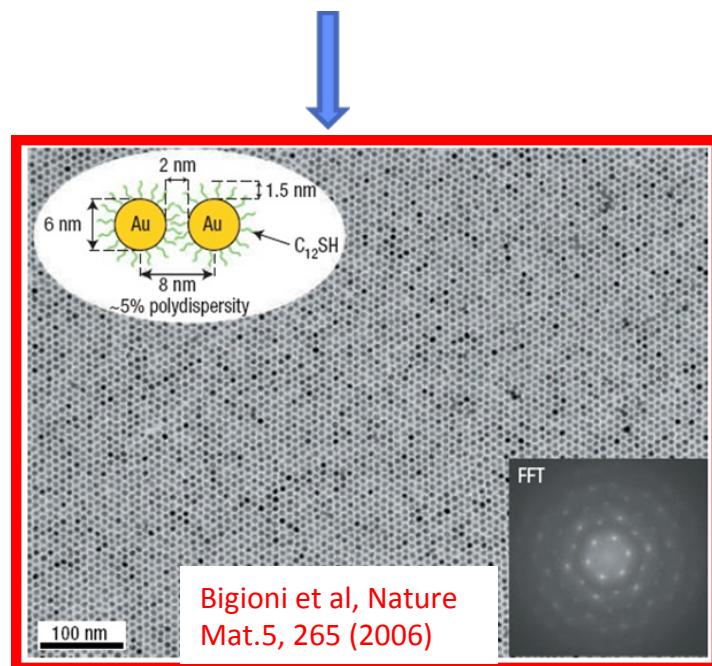
Assembly by Solvent Evaporation

- Monolayer assembly with long-range order
- Extremely strong but flexible
(Young's modulus of several GPa)
- Assembled nanoparticles retaining unique properties without acting like a bulk metal

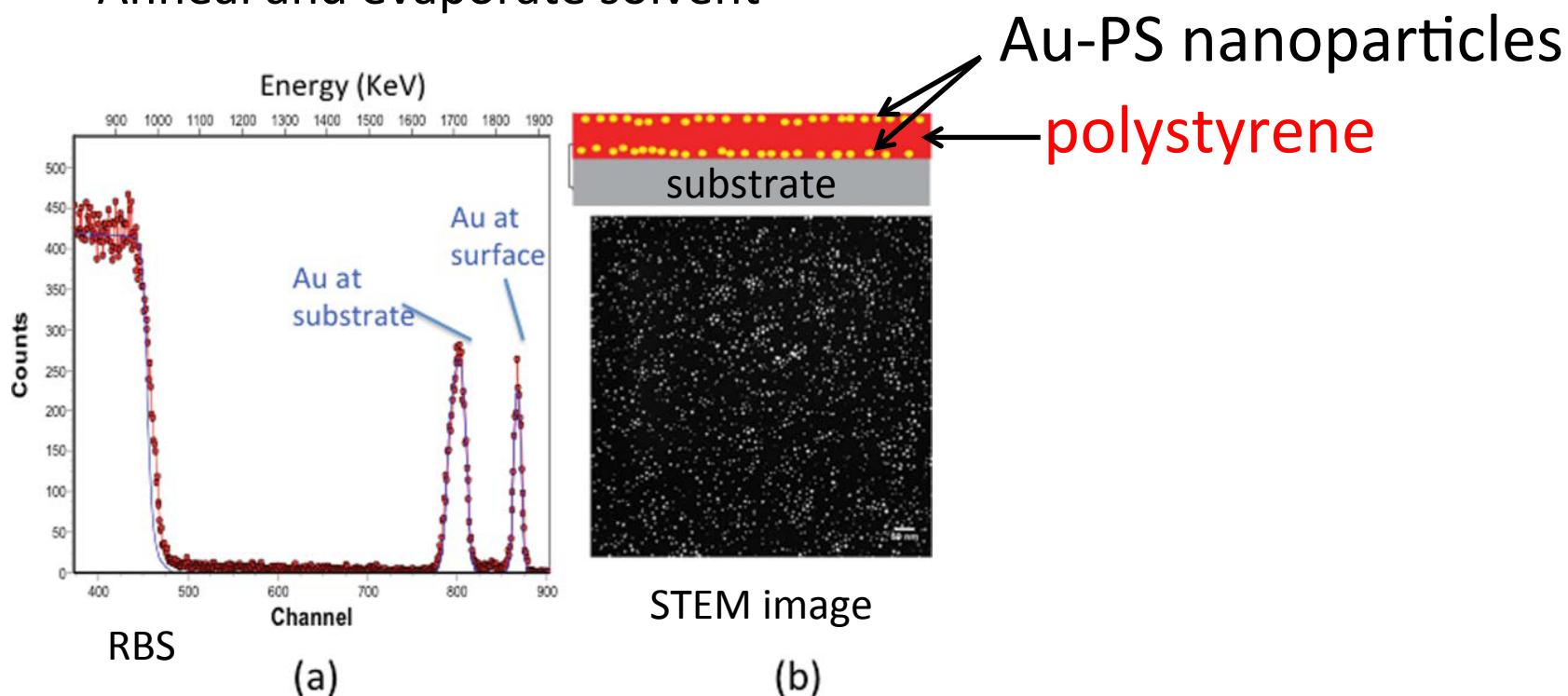
Solvent + Nanoparticles



Slow evaporation of solvent



- Polymer thin film of polystyrene (PS)
- Gold nanoparticles with grafted PS
- Spin coat film
- Anneal and evaporate solvent



Green, Soft Matter (2012)

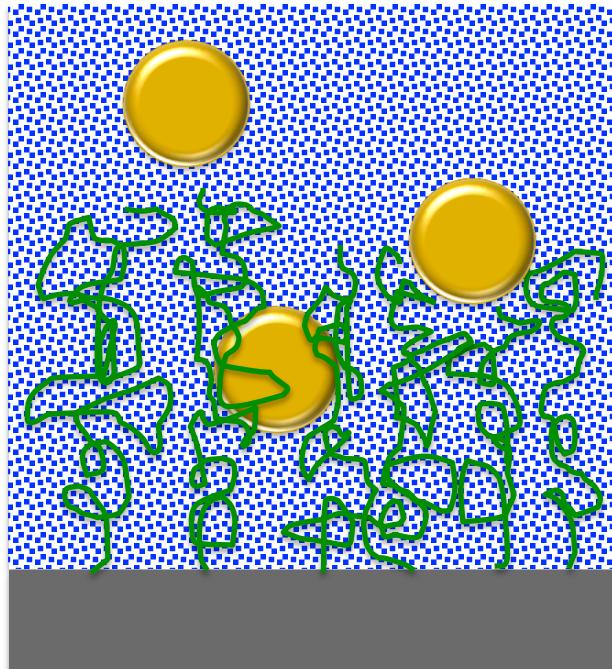
Simulation System

Polymer Brush + Nanoparticles + Solvent

- no molecular coating on nanoparticle
- effective interaction between nanoparticle and polymer or solvent
- vary strength of nanoparticle interaction
- vary brush grafting density

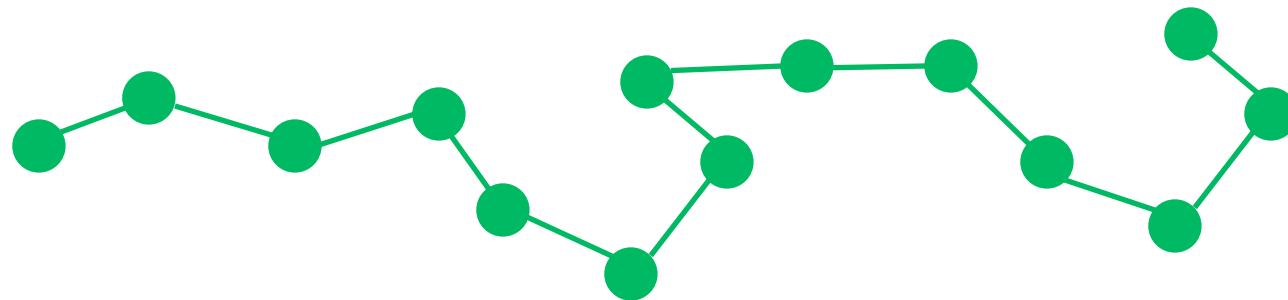
Where does nanoparticle go?

What conditions create an array of nanoparticles?



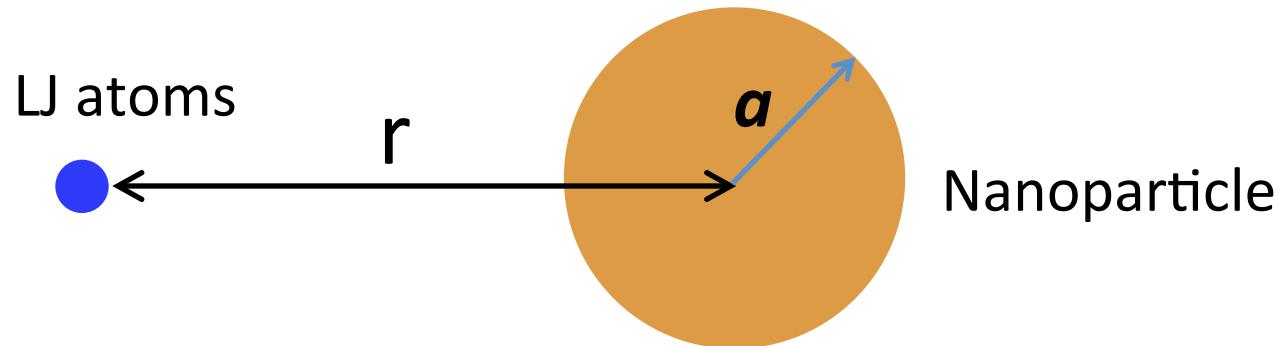


Lennard-Jones potential $U(r) = 4\epsilon \left[\left(\frac{r}{\sigma} \right)^{12} - \left(\frac{r}{\sigma} \right)^6 \right]$



polymer chains (bead-spring model)

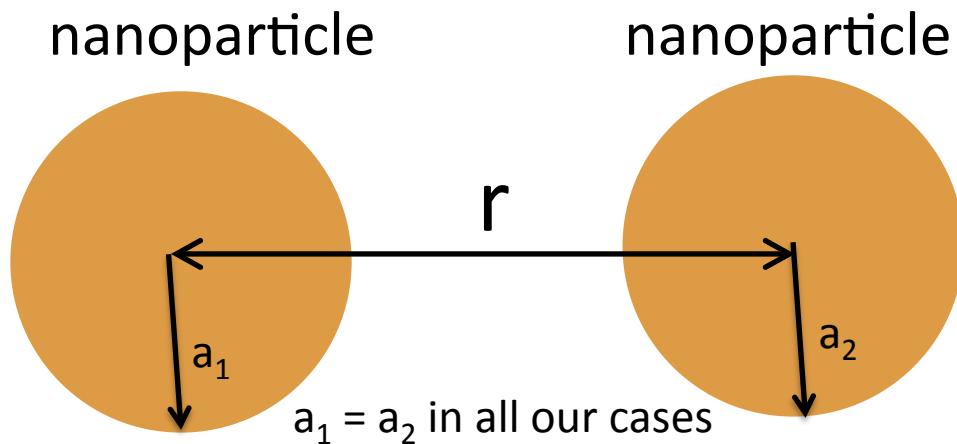
bond potential $U(r) = -0.5KR_0^2 \ln \left[1 - \left(\frac{r}{R_0} \right)^2 \right] + 4\epsilon \left[\left(\frac{r}{\sigma} \right)^{12} - \left(\frac{r}{\sigma} \right)^6 \right] + \epsilon$



np:bead potential

$$U(r) = \frac{2}{9} \frac{a^3 \sigma^3 A_{cs}}{(a^2 - r^2)^3} \left[1 - \frac{(5a^6 + 45a^4 r^2 + 63a^2 r^4 + 15r^6) \sigma^6}{15(a - r)^6 (a + r)^6} \right]$$

- Each nanoparticle is made of uniformly distributed LJ atoms
- integrate LJ potentials to obtain np:bead or np:np interactions
- np:bead interaction strength controlled by A_{cs}



NP-NP interaction strength controlled by A_{cc}

$$U = U_A + U_R$$

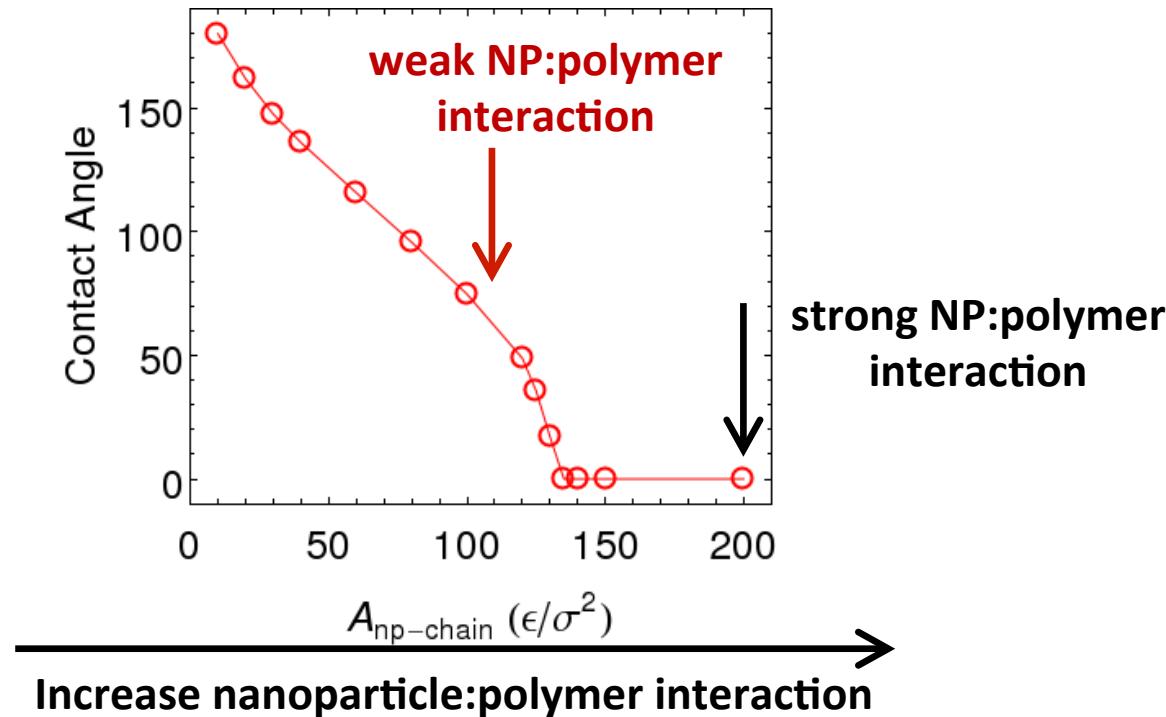
$$U_A = -\frac{A_{cc}}{6} \left[\frac{2a_1a_2}{r^2 - (a_1 + a_2)^2} + \frac{2a_1a_2}{r^2 - (a_1 - a_2)^2} + \ln \left(\frac{r^2 - (a_1 + a_2)^2}{r^2 - (a_1 - a_2)^2} \right) \right]$$

Note: range of attractive part is long!

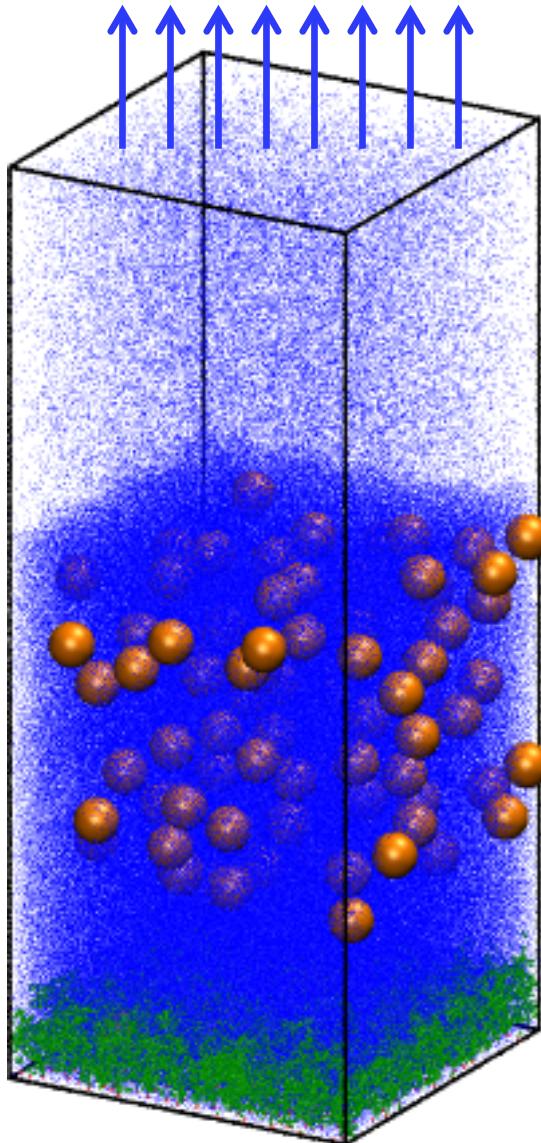
$$U_R = \frac{\cancel{A_{cc}}}{37800} \frac{\sigma^6}{r} \left[\frac{r^2 - 7r(a_1 + a_2) + 6(a_1^2 + 7a_1a_2 + a_2^2)}{(r - a_1 - a_2)^7} + \frac{r^2 + 7r(a_1 + a_2) + 6(a_1^2 + 7a_1a_2 + a_2^2)}{(r + a_1 + a_2)^7} \right. \\ \left. - \frac{r^2 + 7r(a_1 - a_2) + 6(a_1^2 - 7a_1a_2 + a_2^2)}{(r + a_1 - a_2)^7} - \frac{r^2 - 7r(a_1 - a_2) + 6(a_1^2 - 7a_1a_2 + a_2^2)}{(r - a_1 + a_2)^7} \right]$$

Nanoparticle:Polymer Interaction

Determine 'weak' and 'strong' Nanoparticle:Polymer strengths from contact angle simulations



Evaporating Solvent

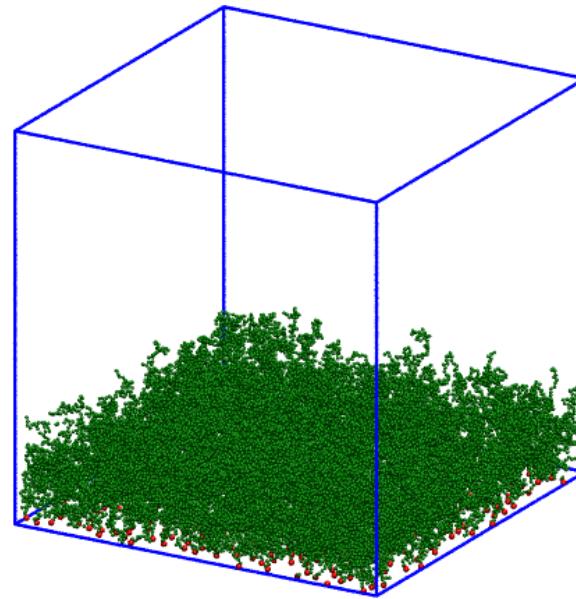
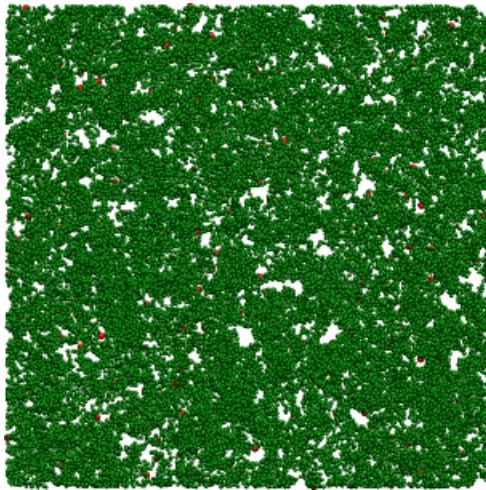


- Polymer brush with 100-bead chains
- LJ solvent in equilibrium with its vapor
- Spherical nanoparticles ($D=10\sigma$)
- Area = $100\sigma \times 100\sigma$
- Strong NP:solvent interaction \rightarrow solvated NP
- Vary NP:brush interaction
 - $A_{nb}=100\epsilon/120\epsilon$ (contact angle of $75^\circ/30^\circ$)
 - $A_{nb}=200\epsilon$ (contact angle of 0°)
- Vary NP and brush densities

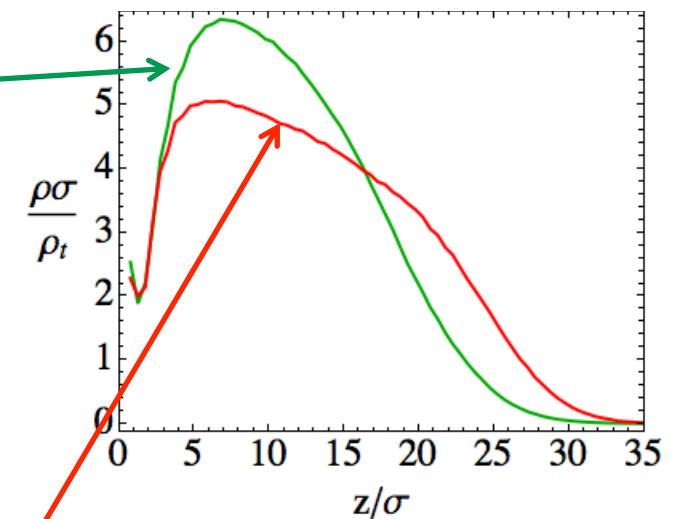
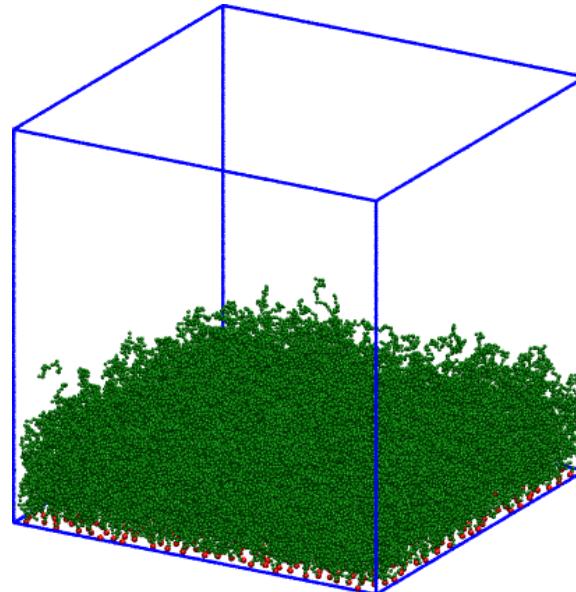
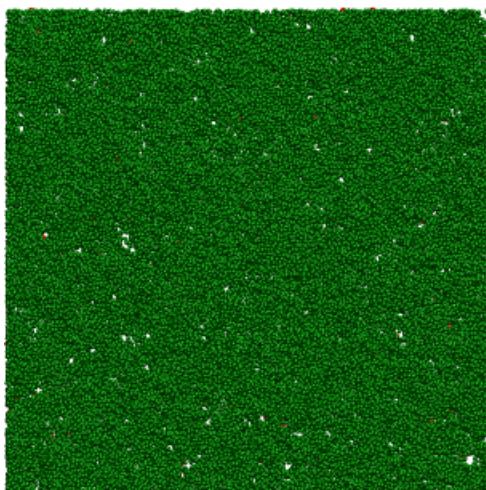
Nanoparticle 2D density:
$$\phi = \frac{N_{np} D^2}{A}$$

Brush Density:
$$\rho_b = \frac{N_{Brush}}{A}$$

Brush in Solvent



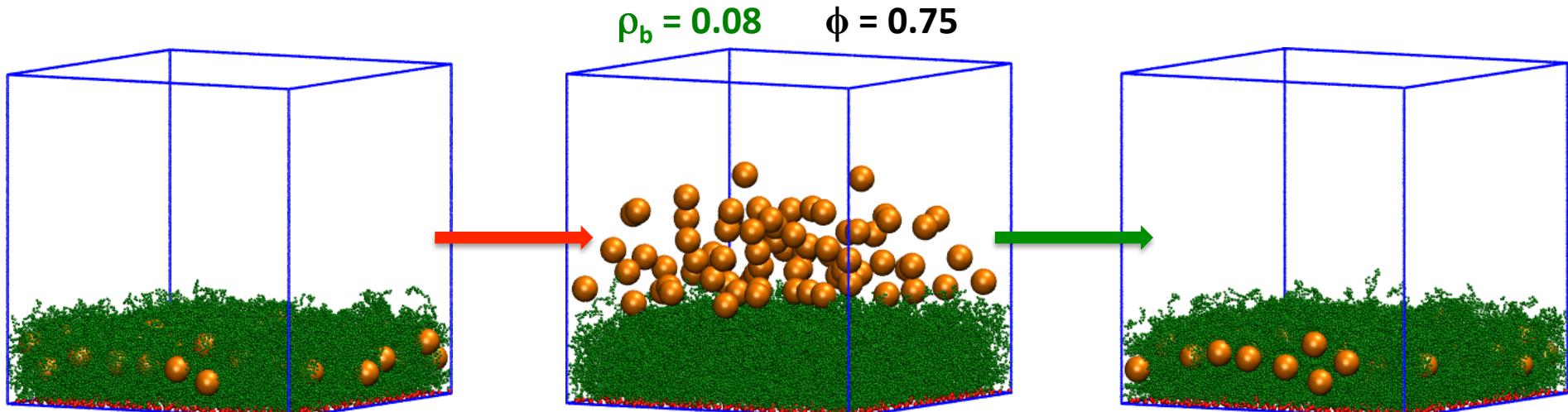
brush density = $0.04\sigma^{-2}$



Brush density normalized by
2D density of tether points

brush density = $0.08\sigma^{-2}$

Solvent not shown



Strong interaction:
NP within Brush

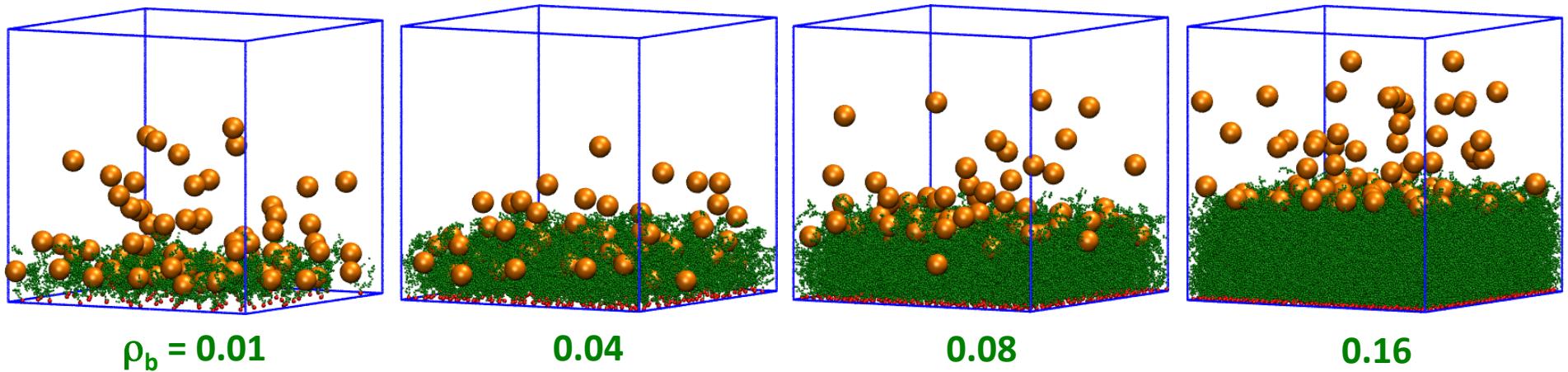
Reduce to weak strength:
NPs release into solvent

Reset to original:
NPs re-enter

Demonstrates can equilibrate nanoparticle distribution.

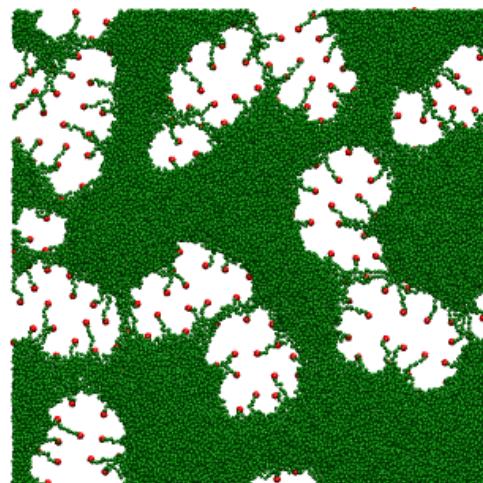
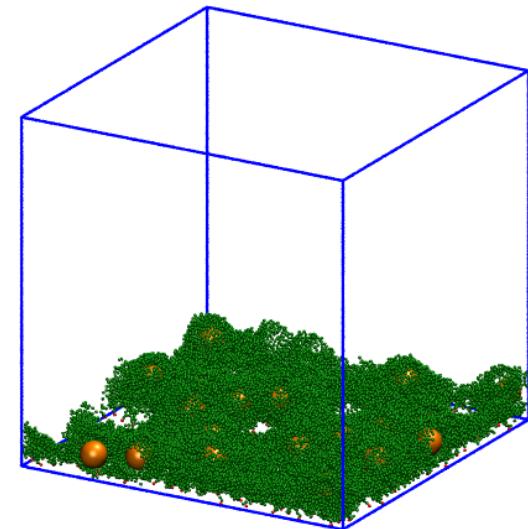
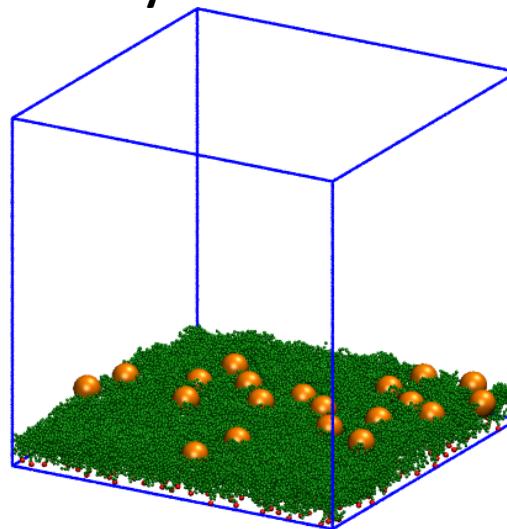
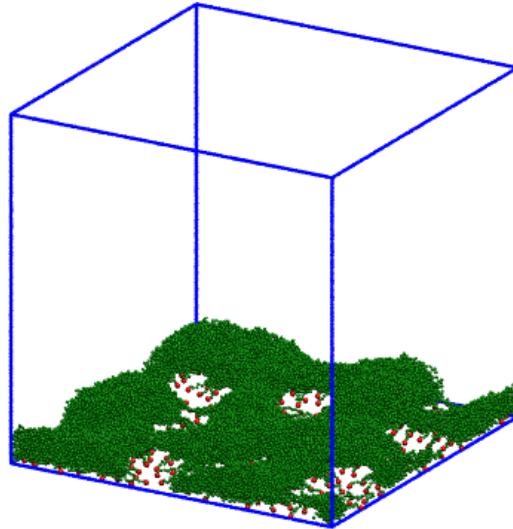
Solvent not shown

$$\phi = 0.75 \quad A_{nb} = 120 \varepsilon \text{ (weak)}$$

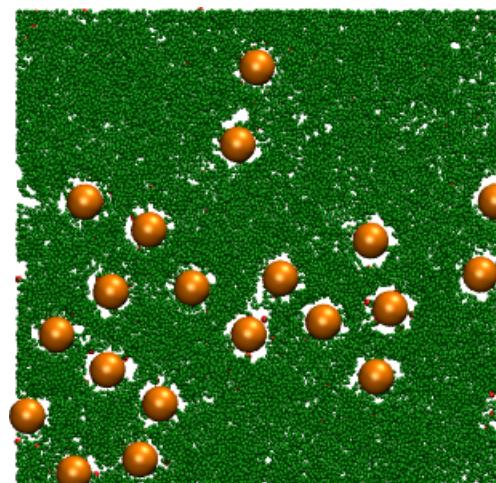


1. Need sufficiently high brush density to exclude nanoparticles
2. At high brush density NPs cannot enter brush; entropic cost too high.
Thus, intermediate brush density best for mixing NPs in brush.

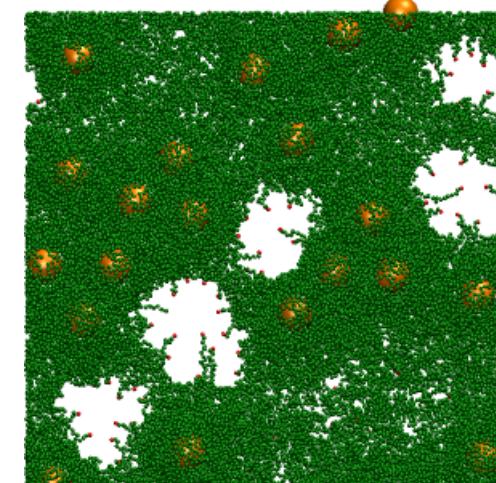
Brush Density = 0.04 & NP density = 0.2



dry brush



$A_{nb} = 100\epsilon$



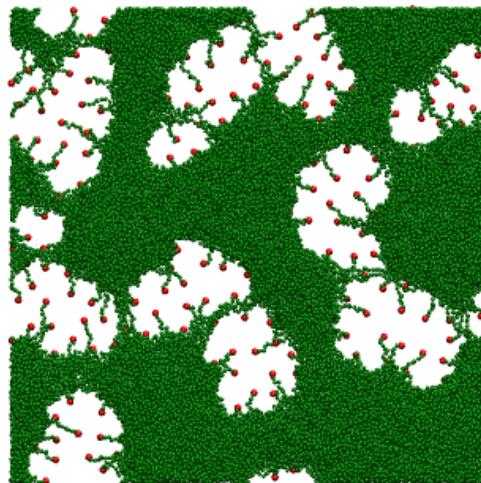
$A_{nb} = 200\epsilon$

Brush Density = 0.04 & NP density = 0.2

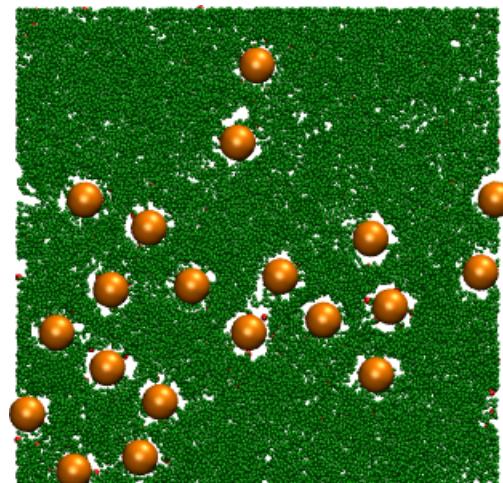
no solvent =
'poor solvent'

weak interactions &
density match =
void filling

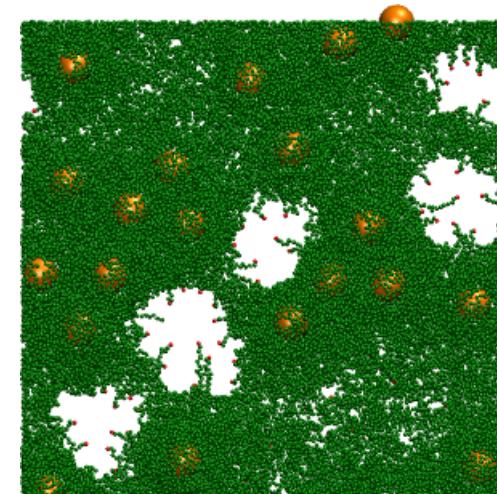
strong interactions =
NPs in brush,
not voids



dry brush

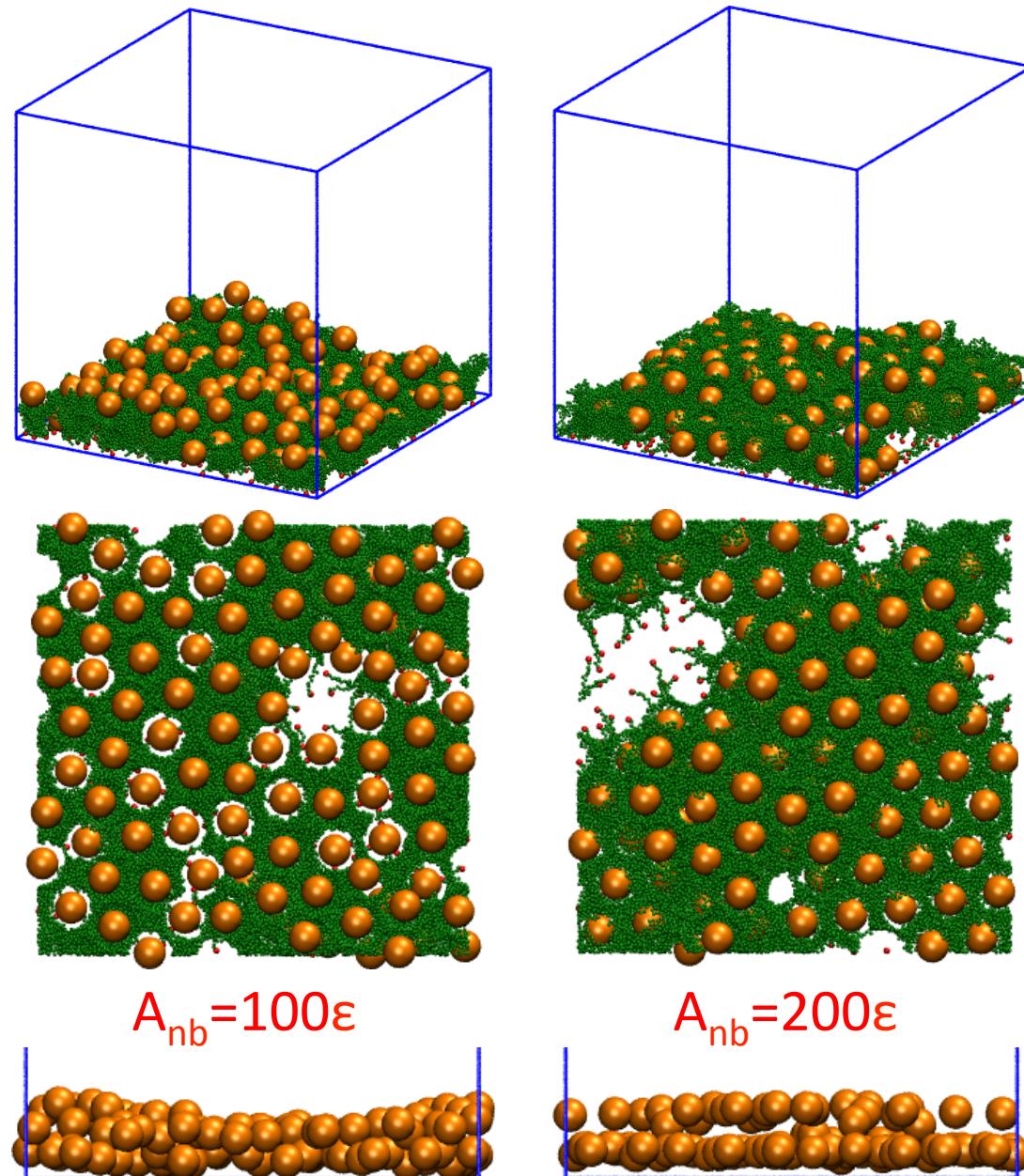


$A_{nb} = 100\epsilon$



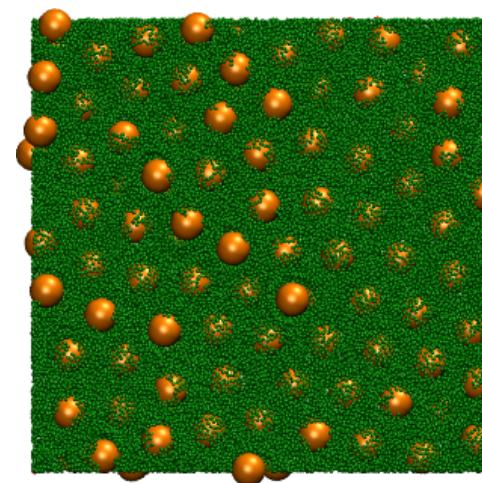
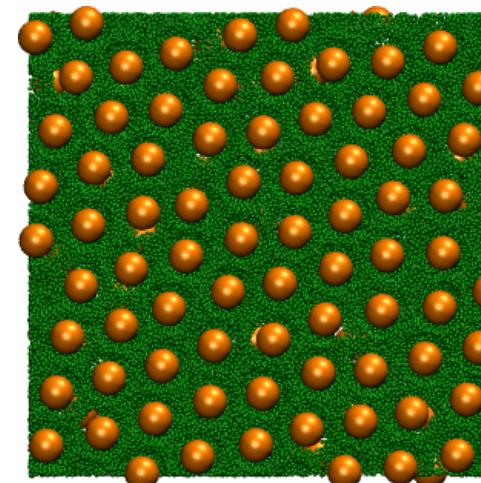
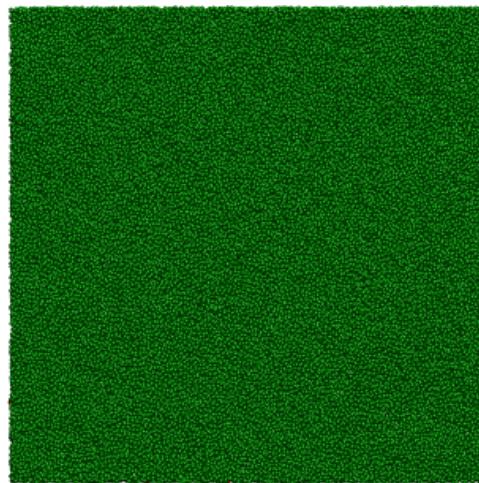
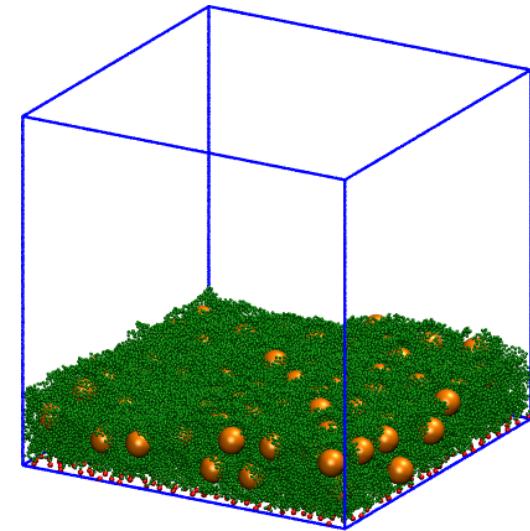
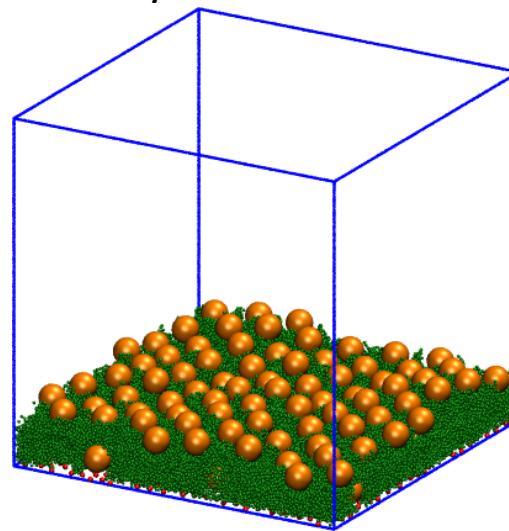
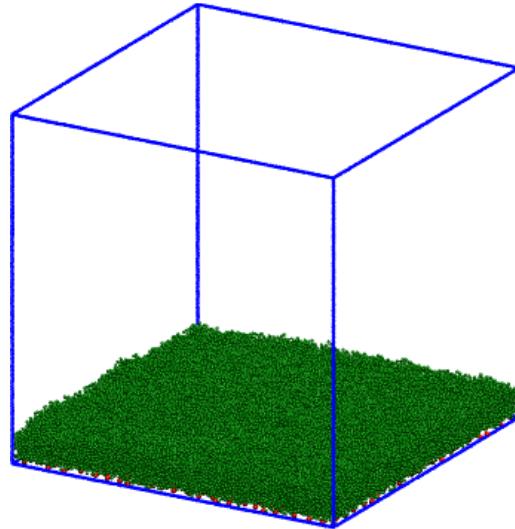
$A_{nb} = 200\epsilon$

- Get two layers of NPs
- Weak case: not all voids filled.
- Strong case: void coalesce.



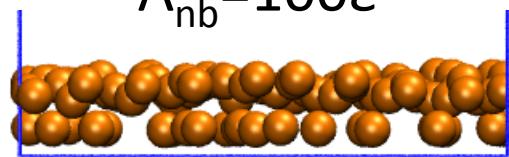
Forming Dense Arrays of Nanoparticles

Brush Density = 0.08 & NP density = 1

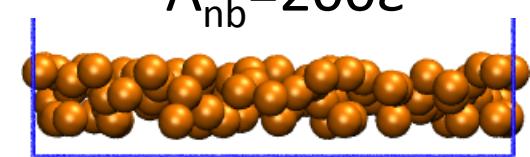


dry brush

$A_{nb} = 100\epsilon$



$A_{nb} = 200\epsilon$

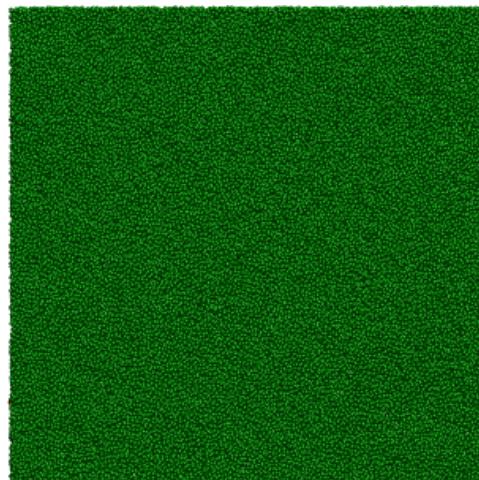


Forming Dense Arrays of Nanoparticles

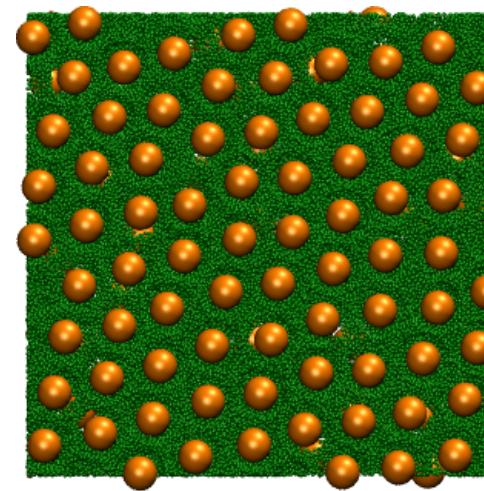
Brush Density = 0.08 & NP density = 1

two, distinct layers
top layer well ordered
& on top of brush

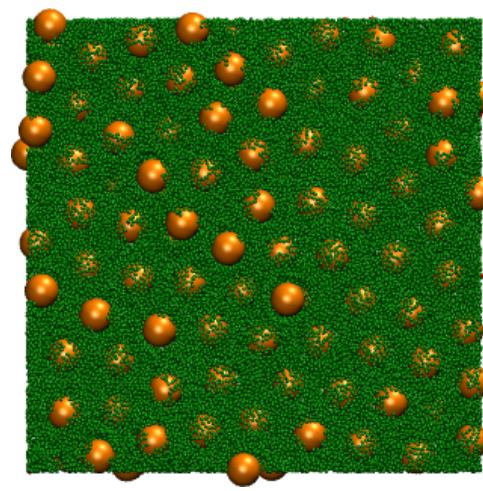
two overlapping layers
top layer immersed &
defected



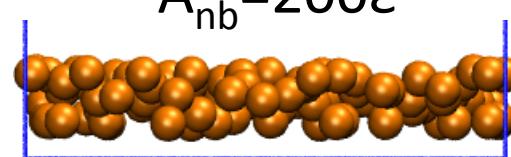
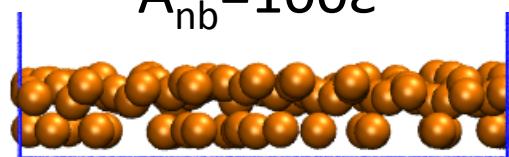
dry brush



$$A_{nb} = 100\epsilon$$



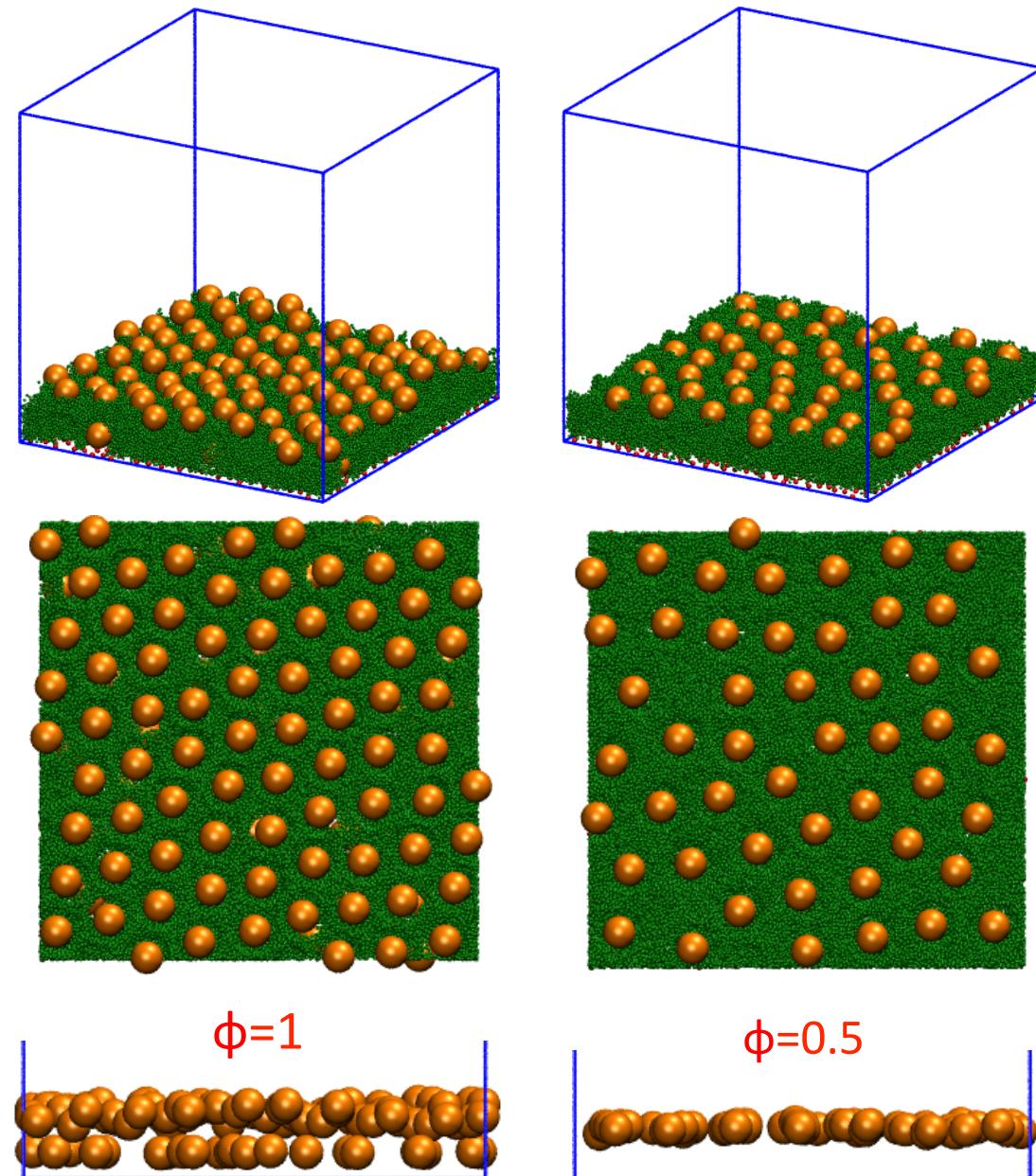
$$A_{nb} = 200\epsilon$$



Solvent Evaporation: vary NP density

Brush Density = 0.08
at $A_{nb} = 100 \epsilon$

Decrease ϕ to 0.5
Not enough NPs to form
monolayer.

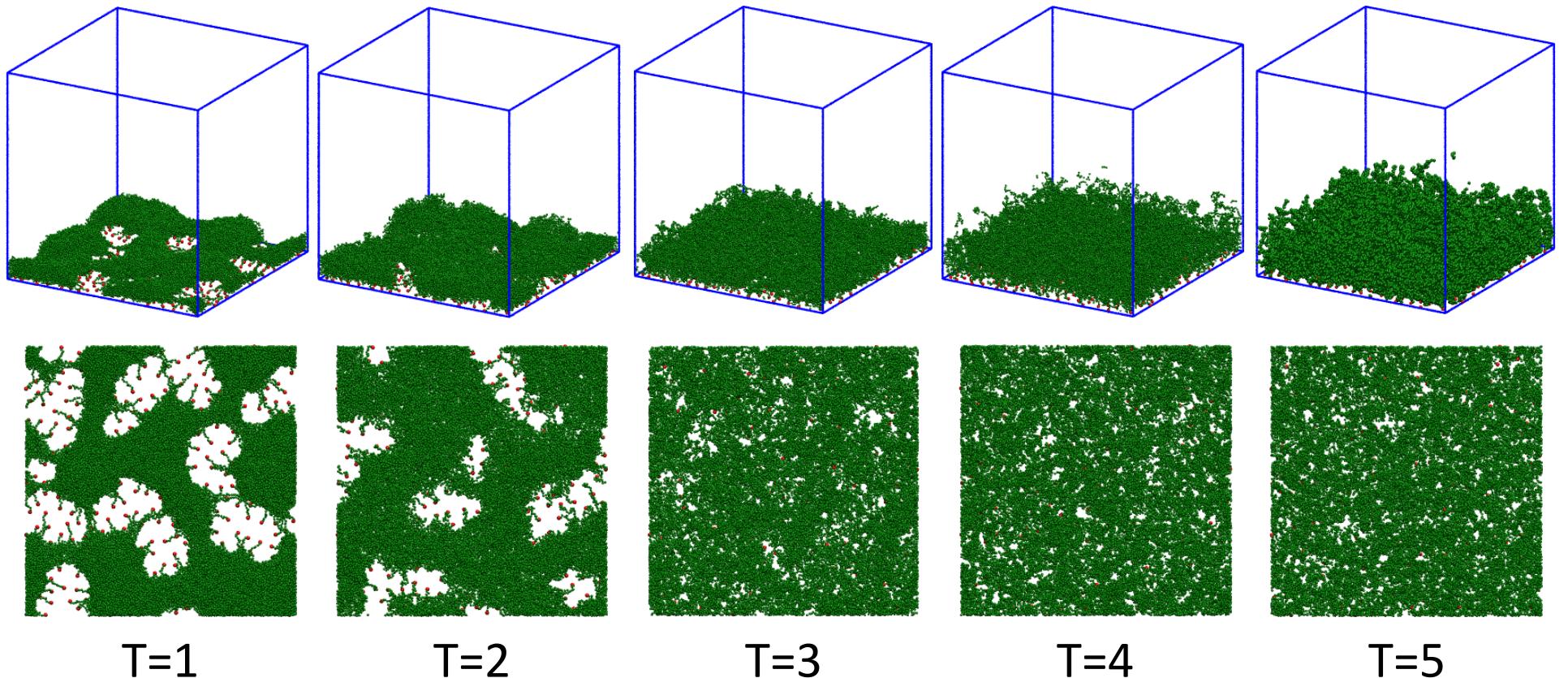


Summary

MD simulations of Nanoparticles in Polymer Brush with Solvent Evaporation

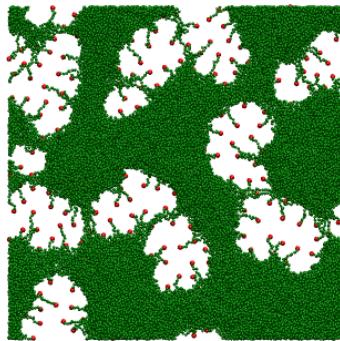
- We can achieve equilibrated dynamics of nanoparticles in brush & solvent
- Best nanoparticle ordering for high-density brush with weak nanoparticle:brush interaction
- Weakly interacting nanoparticles tend to reside on brush surface
- Strongly interacting nanoparticles tend to reside within brush
- Interesting behavior of nanoparticles filling voids at low brush density

Dry Brush at Low Density

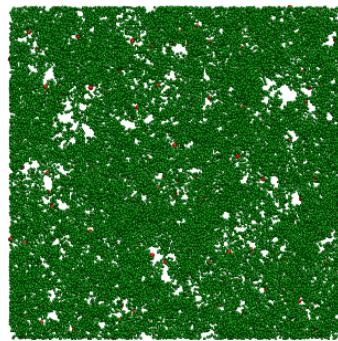


- Temperature unit ϵ/k_B
- Number of chains: 400 \rightarrow brush density $0.04\sigma^{-2}$ (experimental range: $0 \sim 0.2\sigma^{-2}$)
- Chain length: 100 beads
- Brush more uniform at higher T (but we will work at T=1)

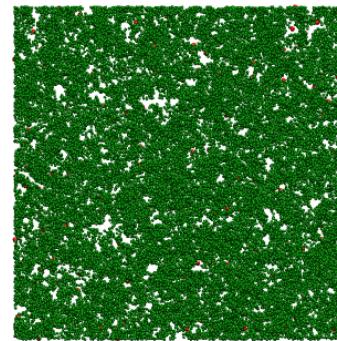
Dry Brush at High Density



$T=1$

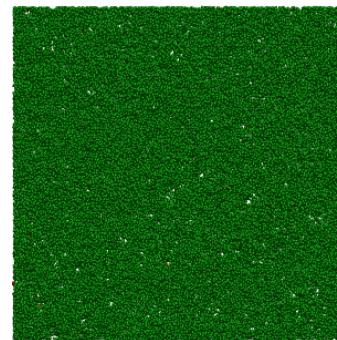
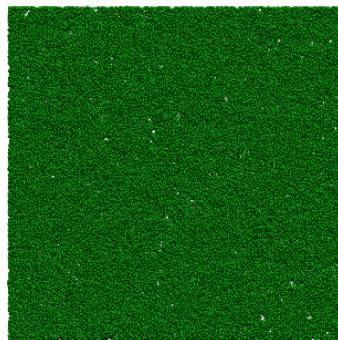
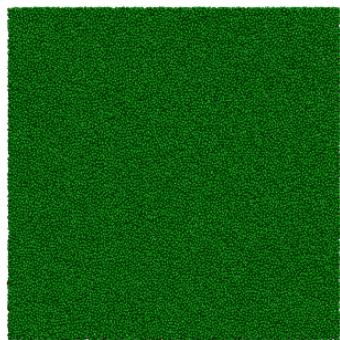


$T=3$

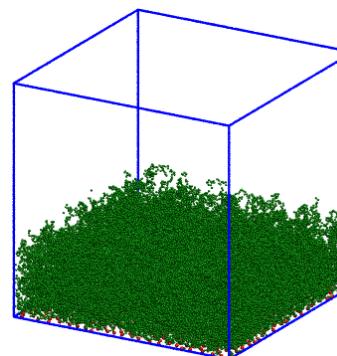
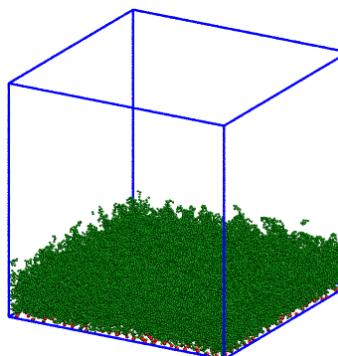
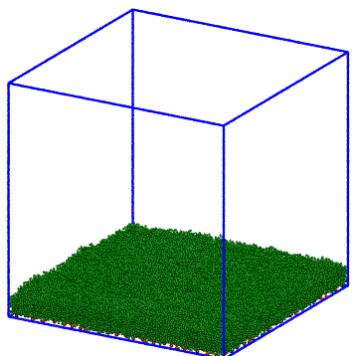


$T=5$

- brush density $0.04\sigma^{-2}$

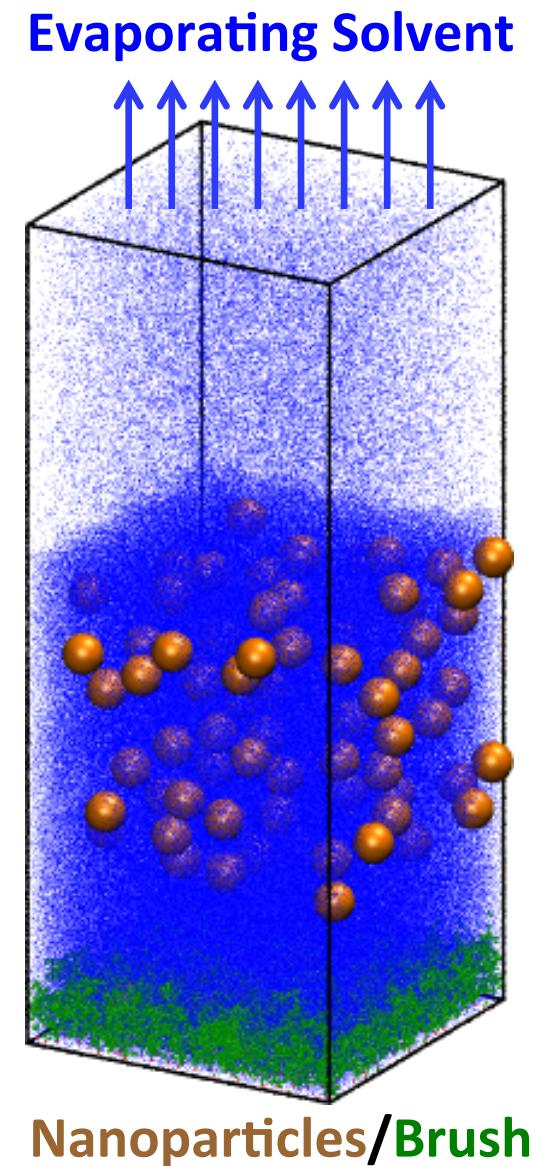
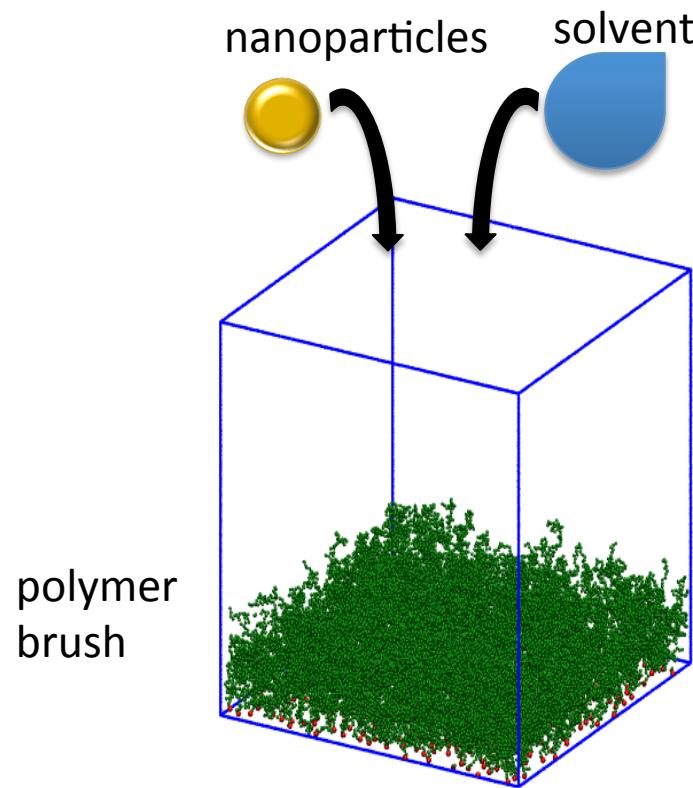


- brush density $0.08\sigma^{-2}$
- Very uniform brush

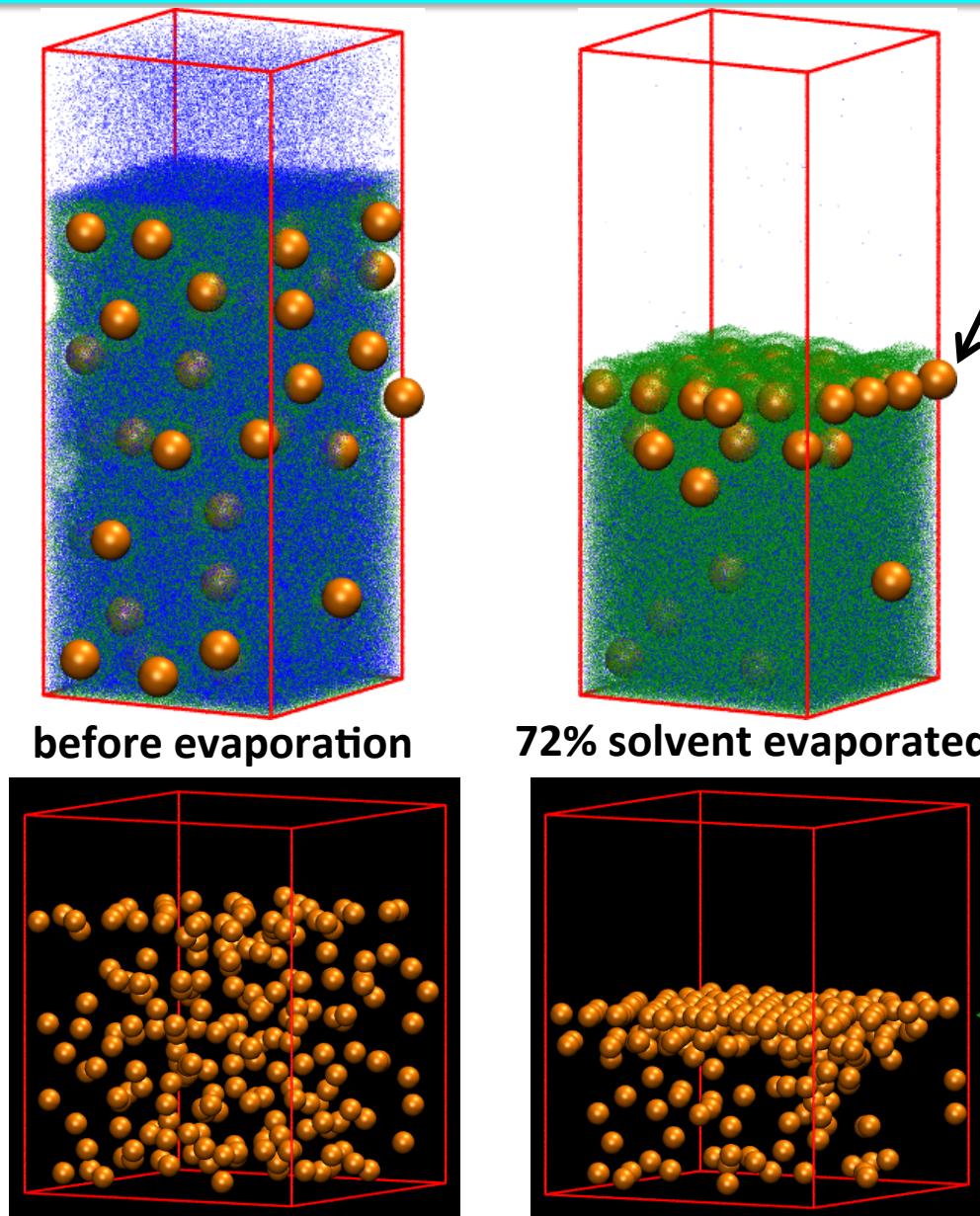


Molecular Dynamics Simulations

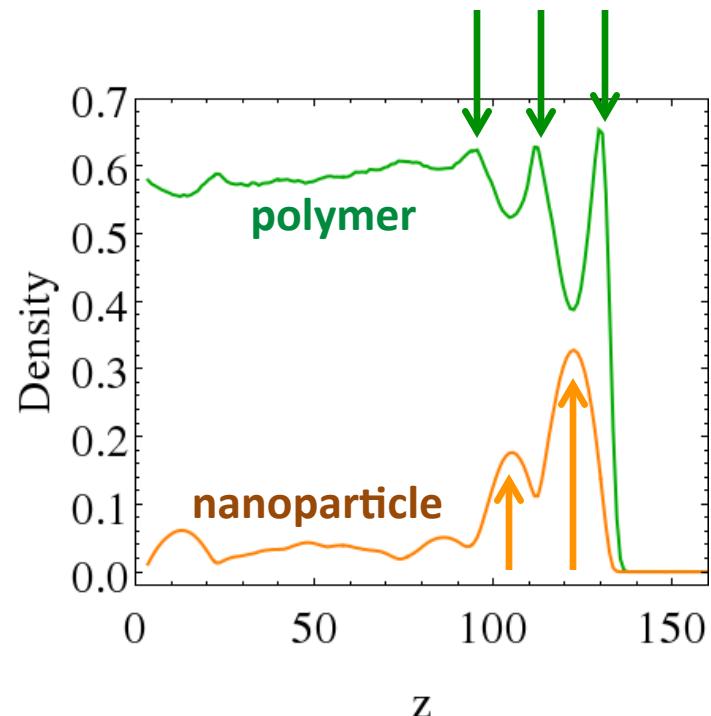
- System:
 - LJ solvent (~3 million)
 - 100-bead polymer chains (~ 3 million beads)
 - 200 Nanoparticles with $D=20\sigma$
- Starting volume fractions: polymer = 45% NP = 10%
- **Evaporation: remove vapor at top**
- Vary NP:solvent interaction strength



Nanoparticles in Polymer Film after Evaporation

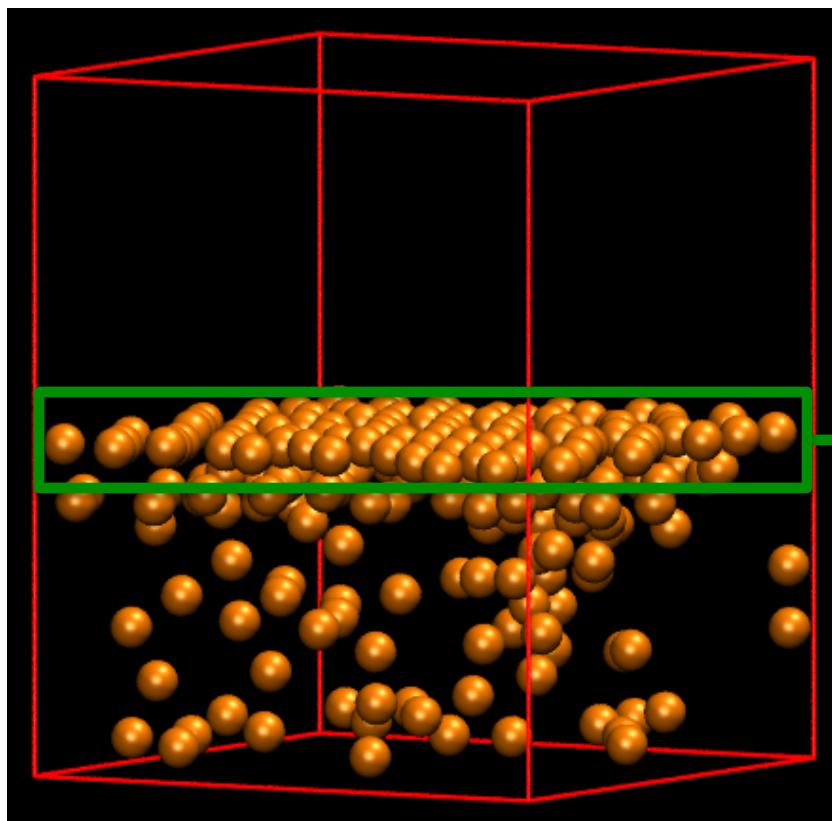


Nanoparticles accumulate near liquid/vapor interface
– polymer chain density is highest

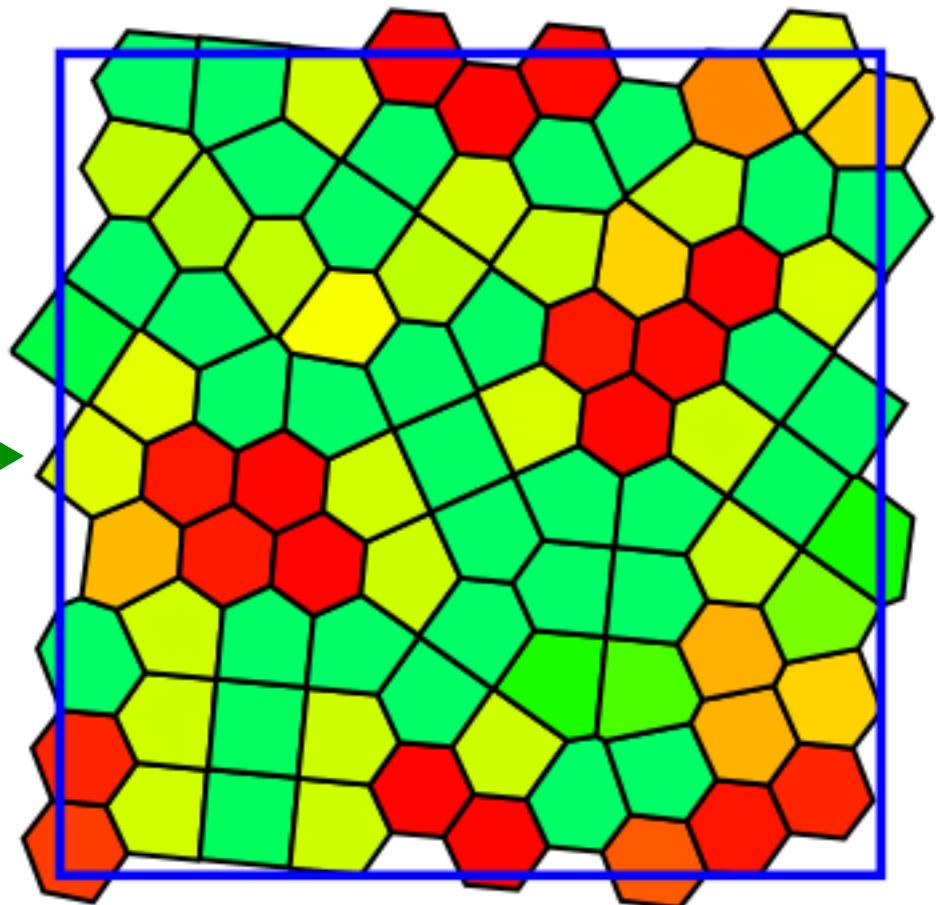


← higher polymer density

Packing in Top Layer with Strong NP:Polymer Interaction



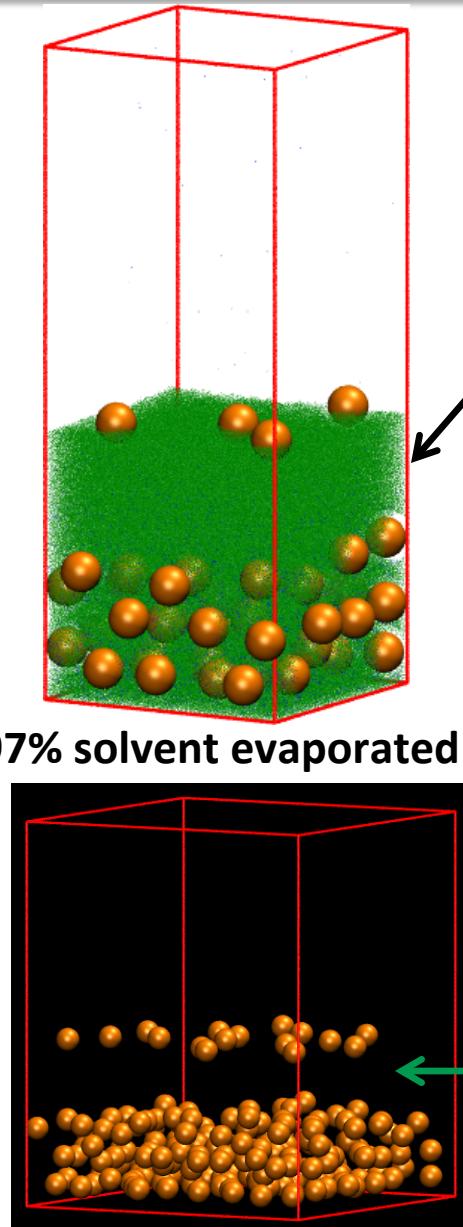
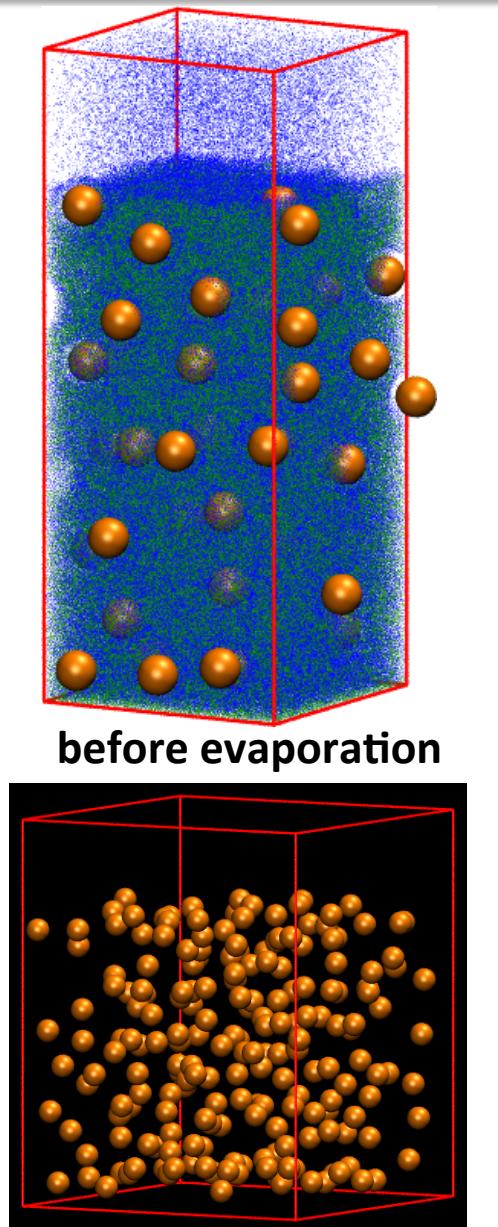
with 72% solvent evaporated



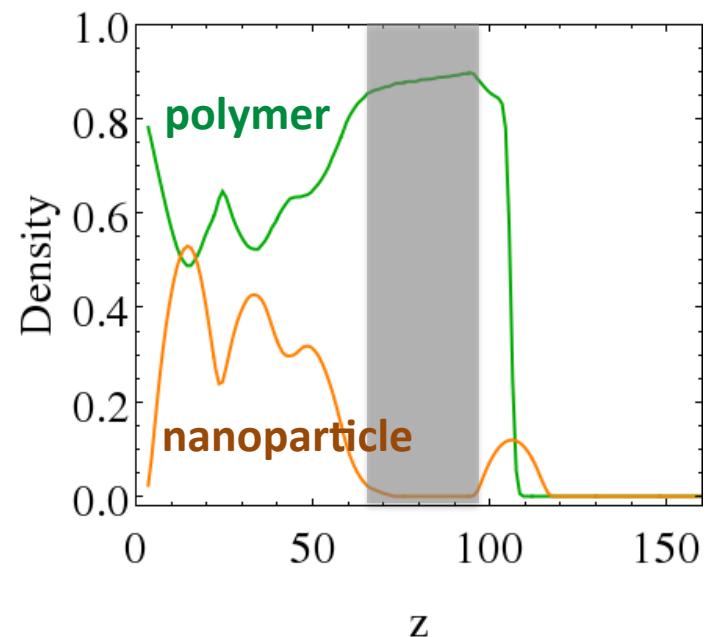
Nanoparticle packing:

- Number of neighbors: 4/5/6
- 4 neighbors: square
- 6 neighbors: hexagonal

Weak Nanoparticle:Polymer Interaction

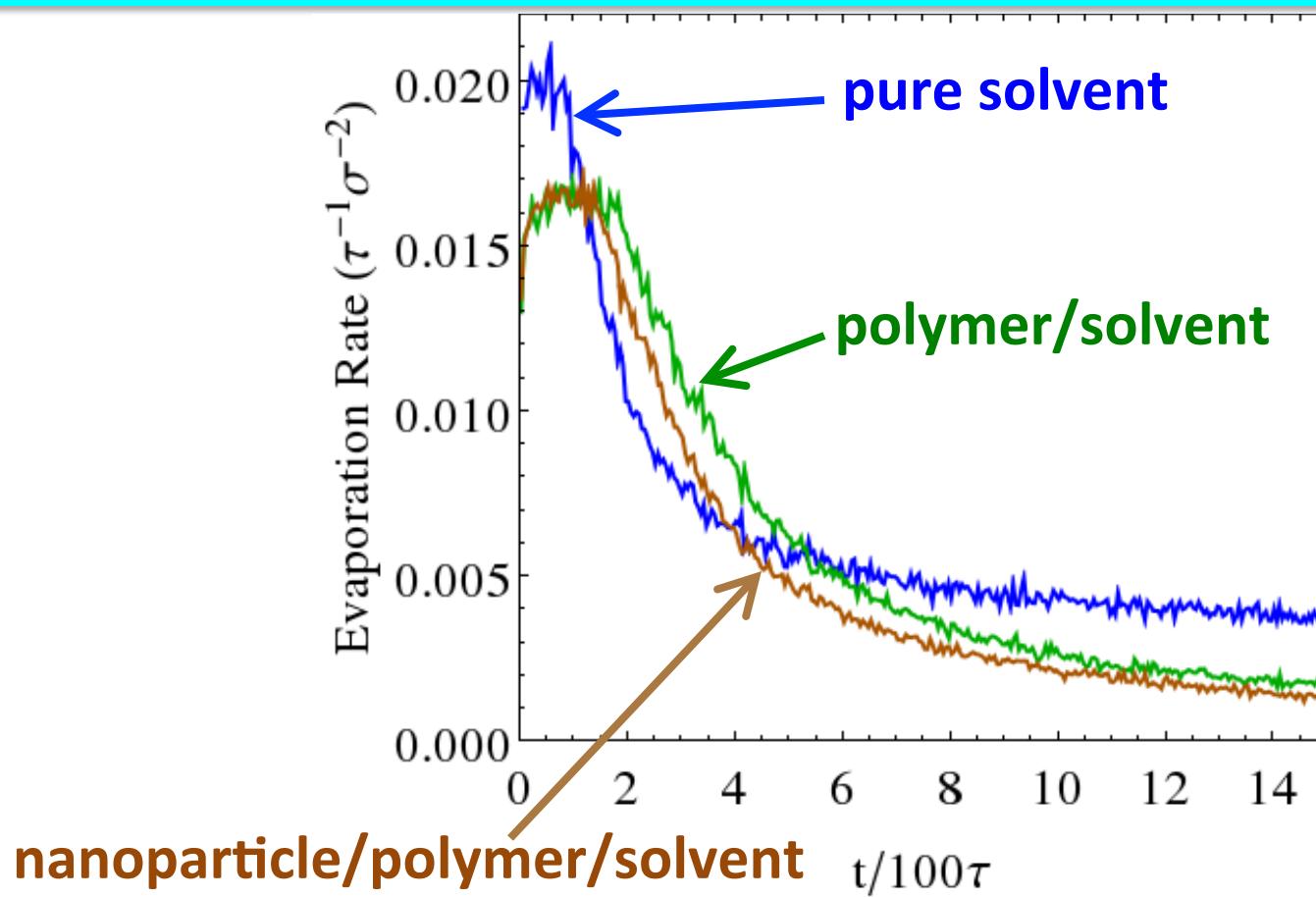


Nanoparticle depletion in dense polymer layer near liquid/vapor interface



higher polymer density
No nanoparticles

Effect of Nanoparticle/Polymer on Evaporation Rate



- Evaporation rate decreases with time quickly
 - Depletion of vapor
 - Evaporative cooling
 - Blockage of nanoparticles/polymers near liquid/vapor interface

→ evaporation rate decreases faster with more blockers