

# Atomistic simulations of valley splitting in silicon quantum dots in the presence of disorder

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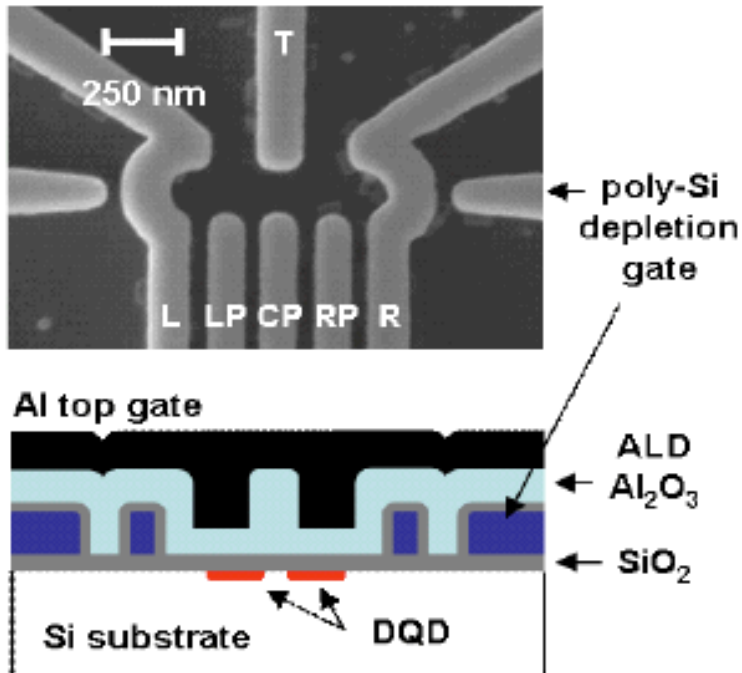
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Acknowledgement: N. Kharche (RPI), W. Witzel (Sandia)

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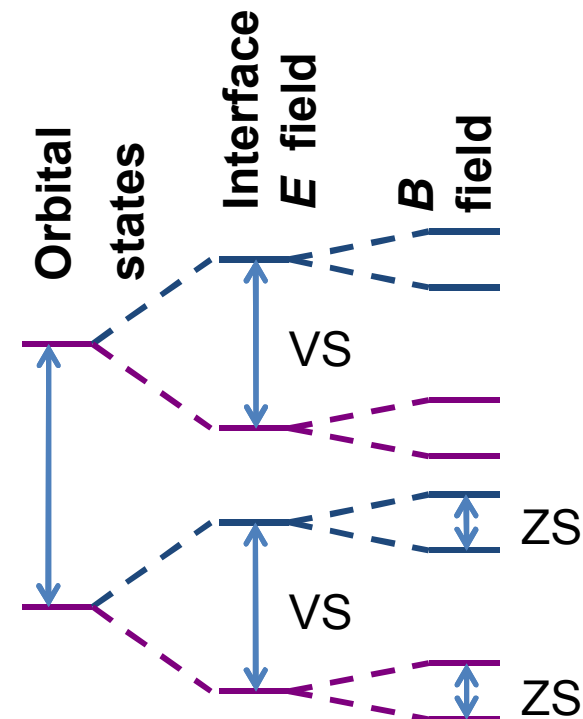
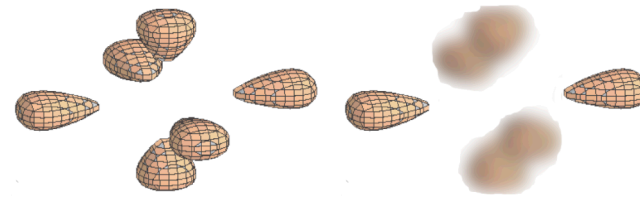
# Valley splitting in Si QDs

SNL QIST: DQD S-T Qubits in Si



Tracy et. al., APL 97, 192110 (2010)

Conduction band valleys in Si



# Outline

## 1. Valley Splitting in SQD:

- Miscut (Tilt / Ideal steps)
- E-field
- Barrier material (alloy disorder + strain)
- Surface roughness

Method: Atomistic tight-binding (NEMO 3D)

## 2. Valley Splitting in DQD:

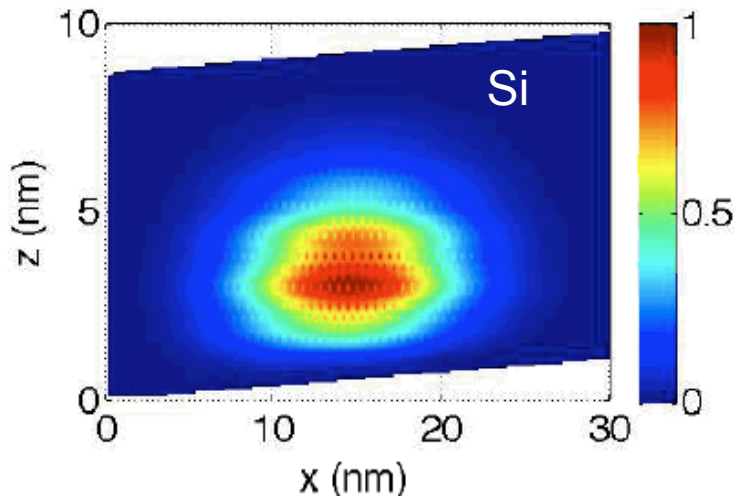
- $2e$  states with fields, tilt

Method: Tight-binding (NEMO 3D) + Full Configuration Interaction

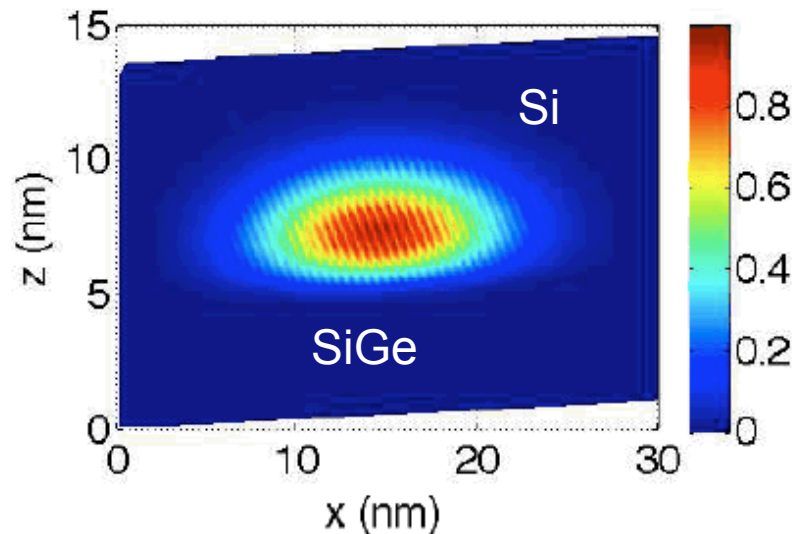
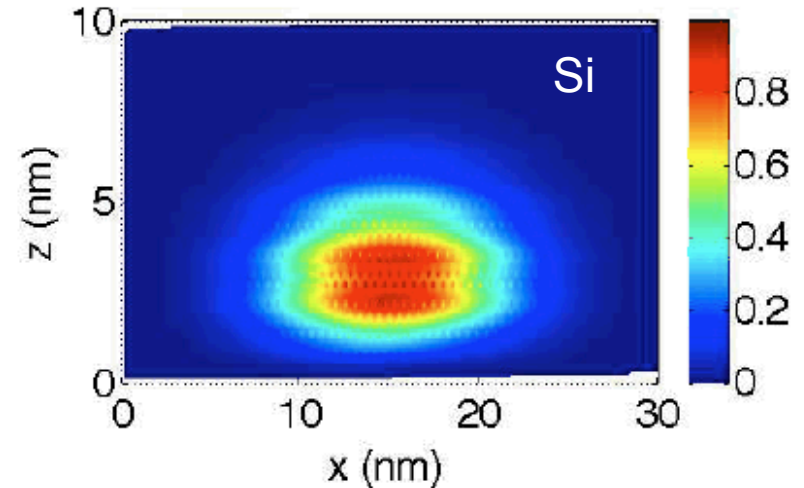
(Thanks to Erik Nielsen)

# Atomistic models of interfaces : Miscuts

2 degrees (step length 3.8 nm)

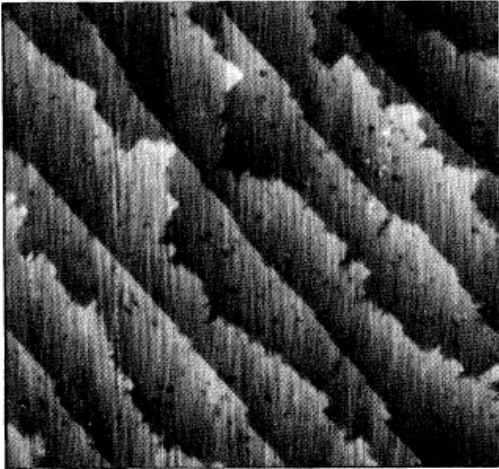


0.5 degrees (step length 15 nm)



- QDs parabolic in x, y
- Uniform E-field in z (5-10 MV/m)
- 20% Ge, 80% Si
- Kharche et. al., APL 90, 092109 (2007)

# Atomistic models of interfaces: roughness



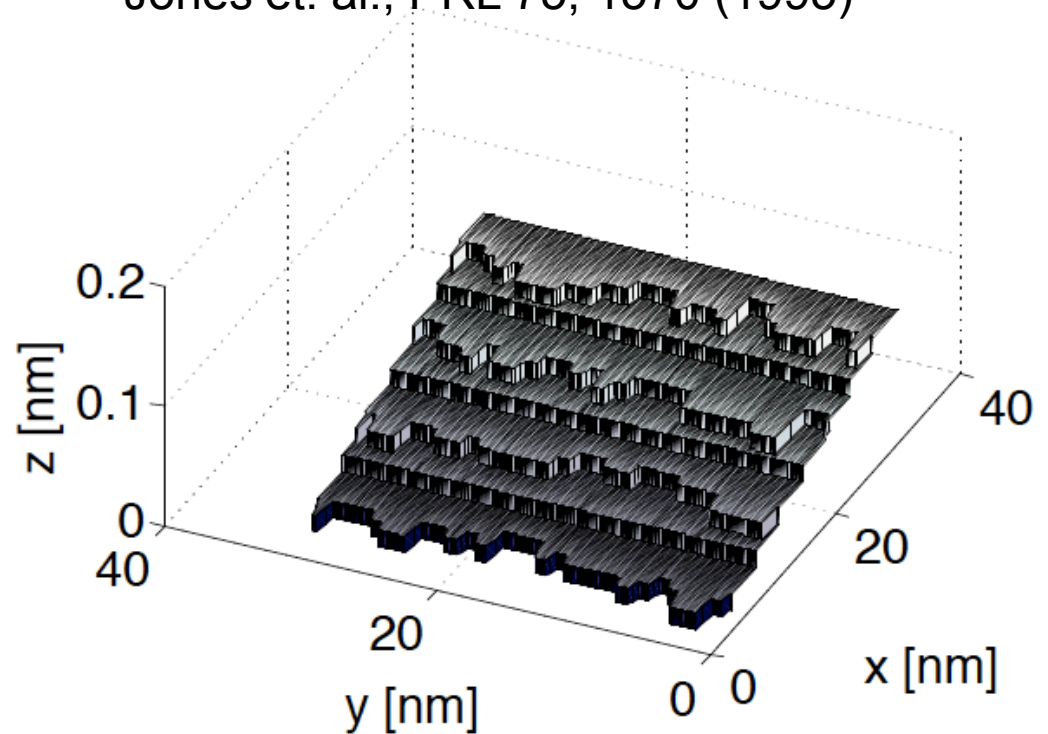
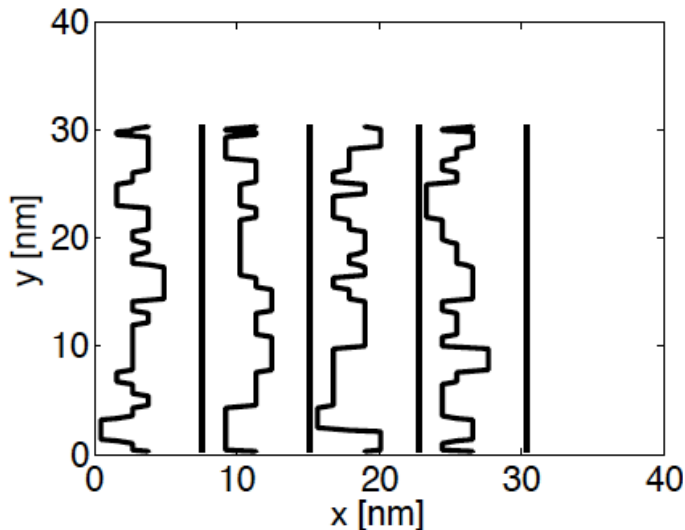
Roughness model: alternate ideal and rough steps, Zandvliet & Elswijk, PRB 48, 14269 (1993).

Other models:

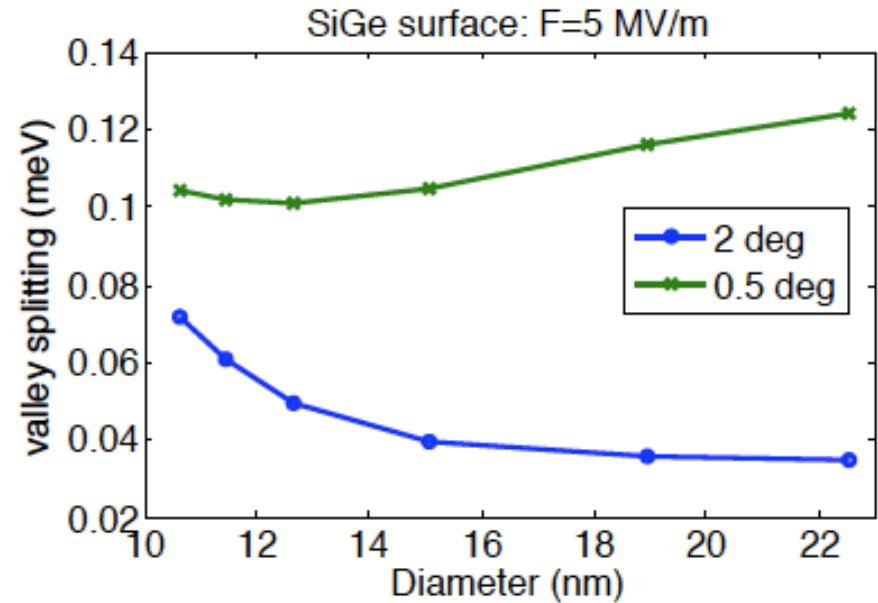
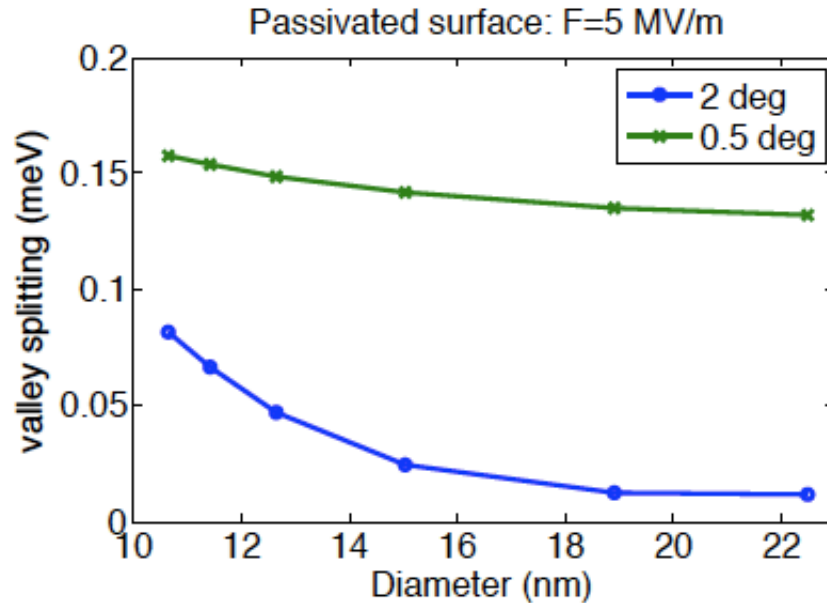
Goodnick et al., PRB 32, 8171 (1985)

Jones et. al., PRL 75, 1570 (1995)

Reconstructed surfaces in y



# Effect of tilt

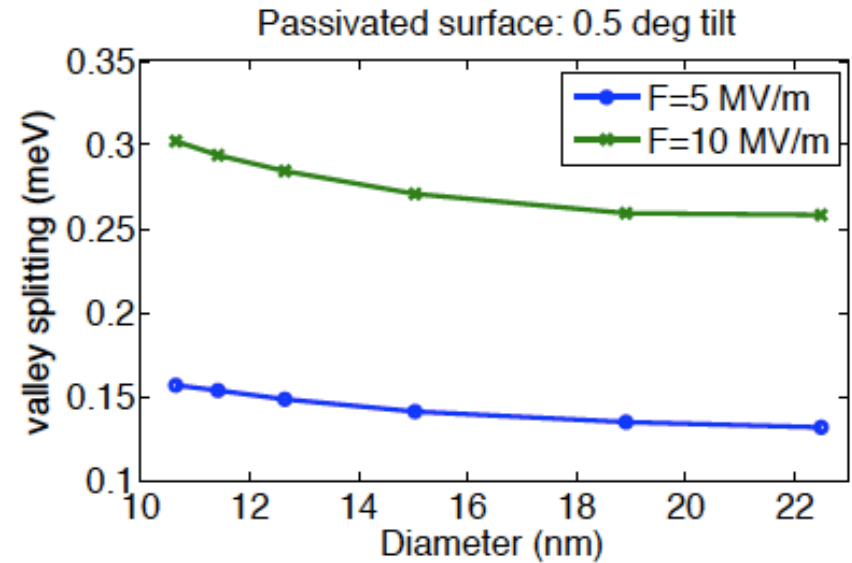
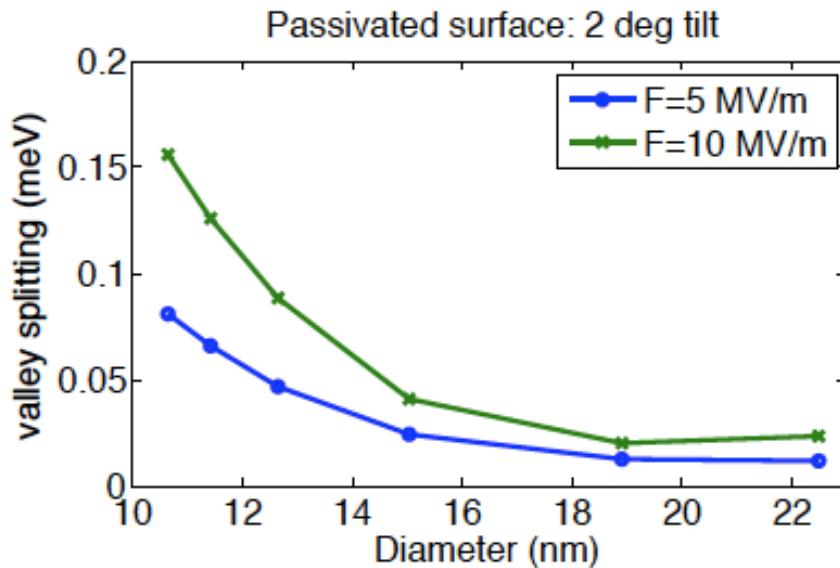


Higher tilt suppresses VS.

Larger dots experience smaller VS with tilt.

Alloy disorder at the interface plays a role

# Effect of E-field

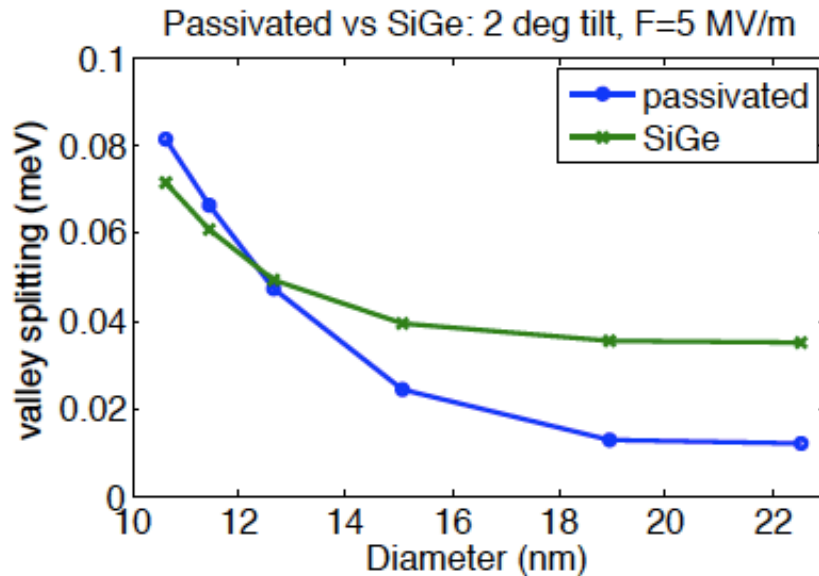


Higher vertical E-fields produce higher VS irrespective of tilt or disorder.

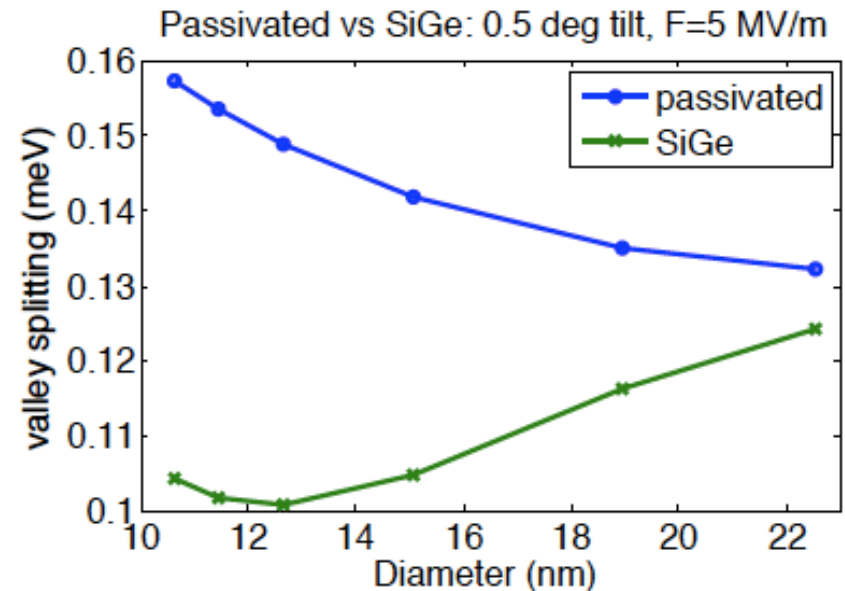
Holds in SiGe-Si dots also.

# Effect of barrier material

## Passivated vs. SiGe



2 degree tilt



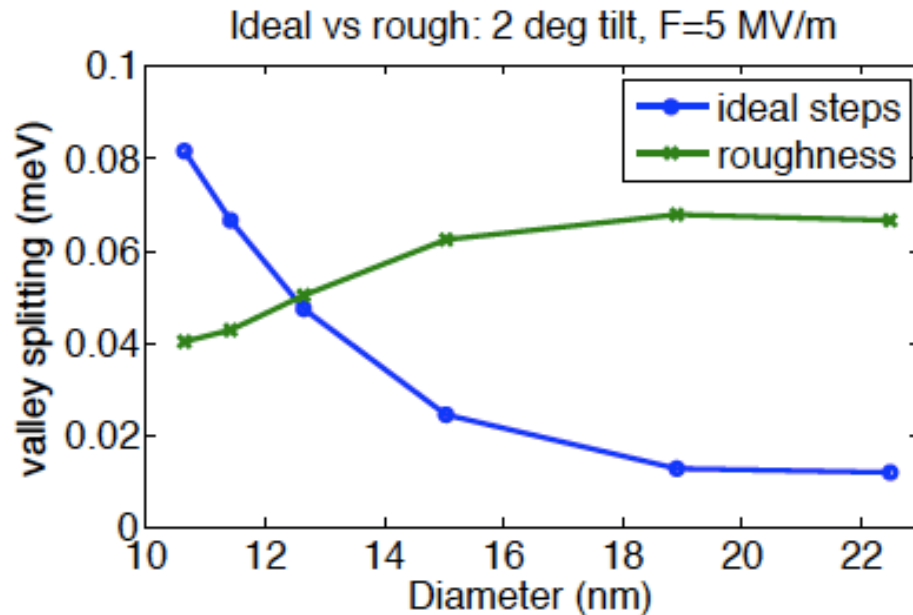
0.5 degree tilt

Alloy disorder introduces atomistic roughness in CB edge.

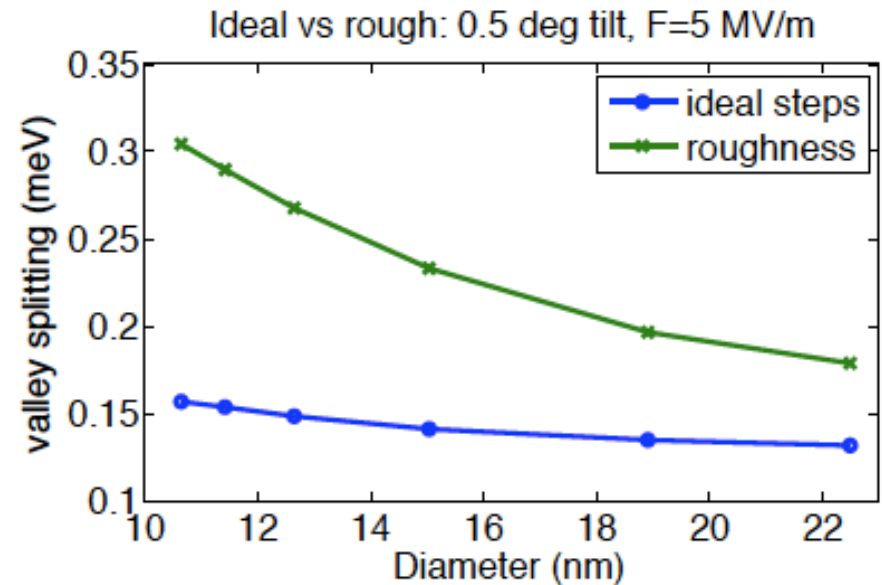


# Effect of roughness

Role of step roughness in passivated surfaces



2 degrees



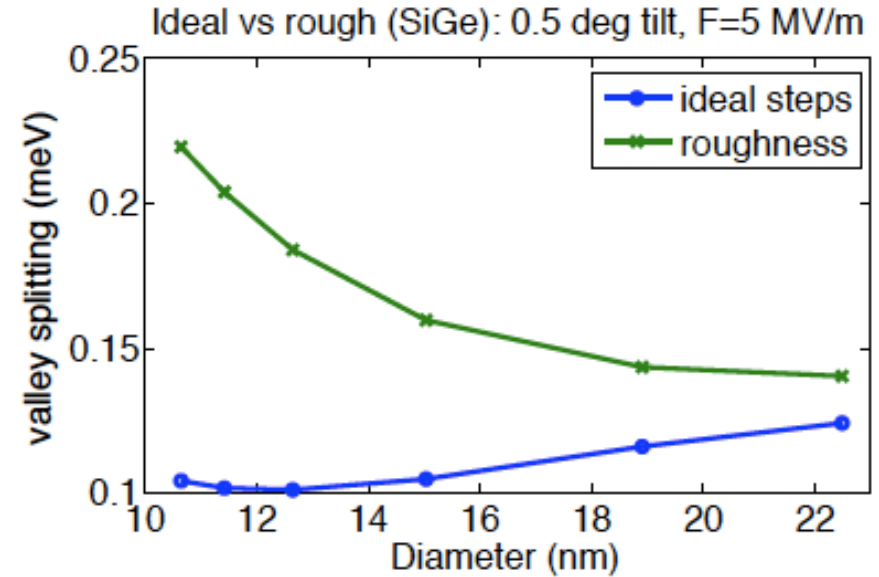
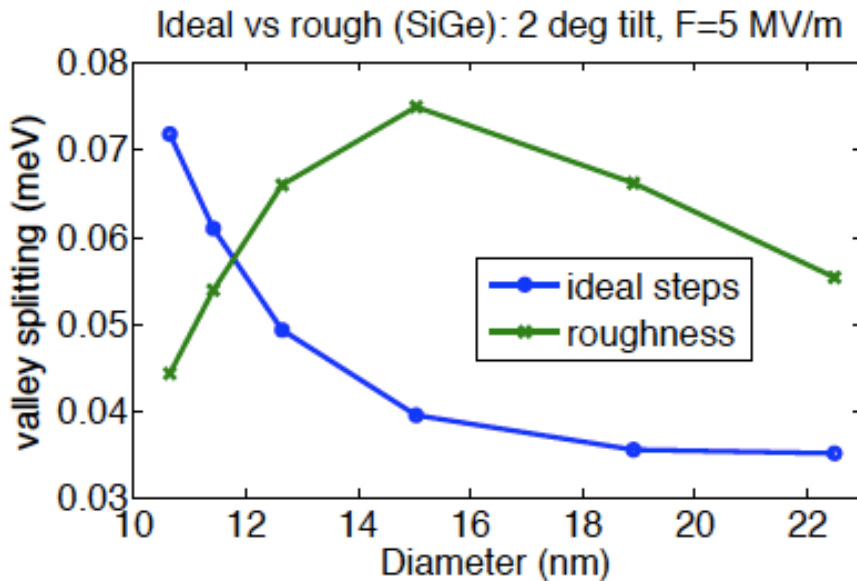
0.5 degrees

Roughness increases VS: Cancels the effect of tilt.

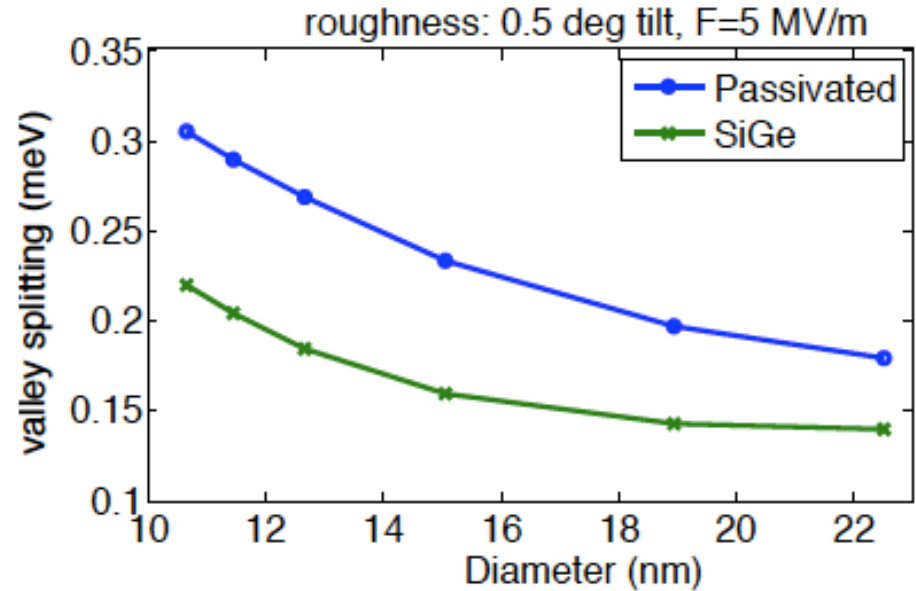
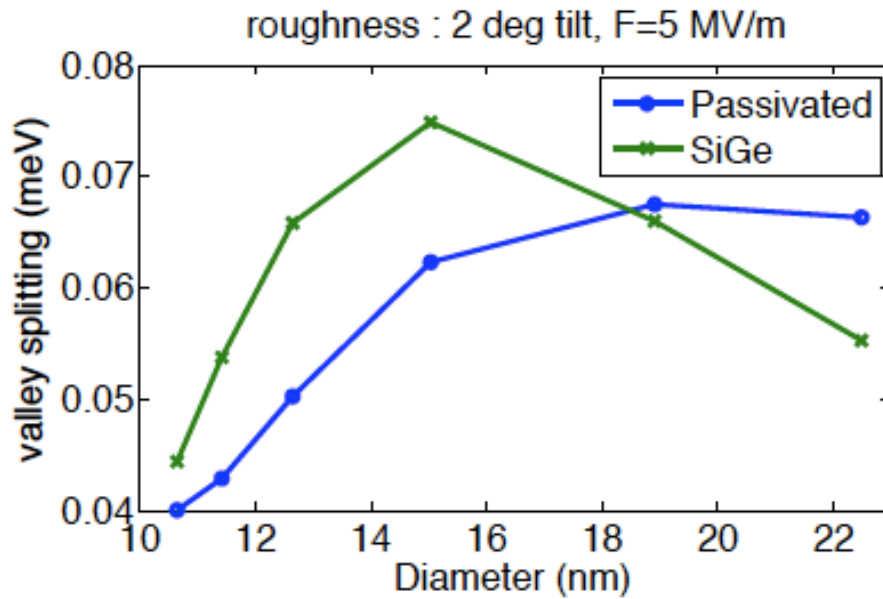
M. Friesen et. al., APL 89, 202106 (2007).

# Step roughness + alloy disorder

## SiGe barriers



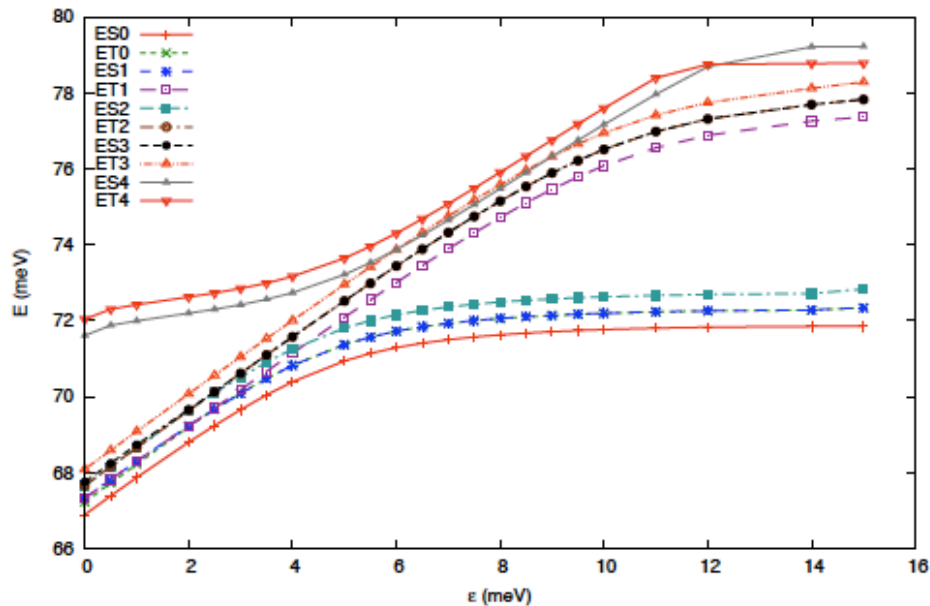
# Role of alloy disorder



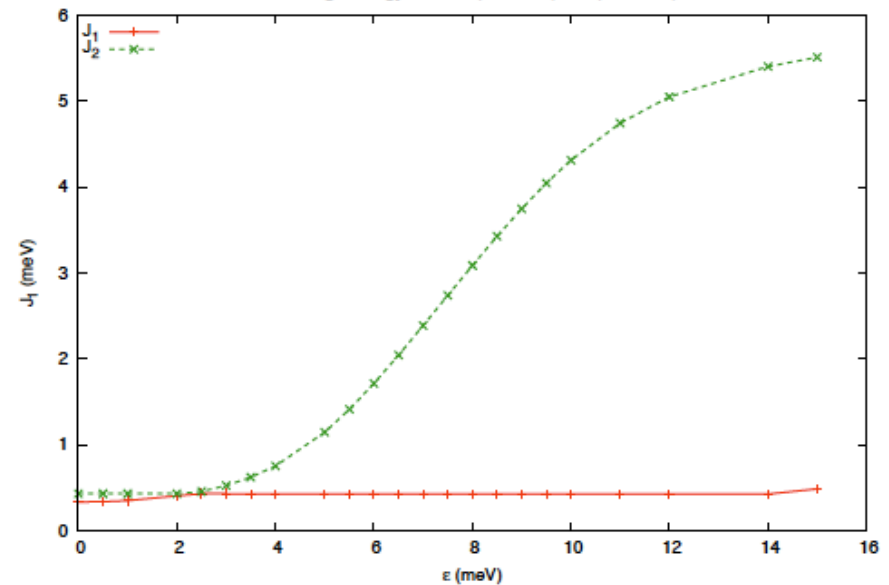
# DQD 2e states with small VS

$F=5$  MV/m

System: geo1 7nmDots L20 B0 Ez5  
2-electron energies



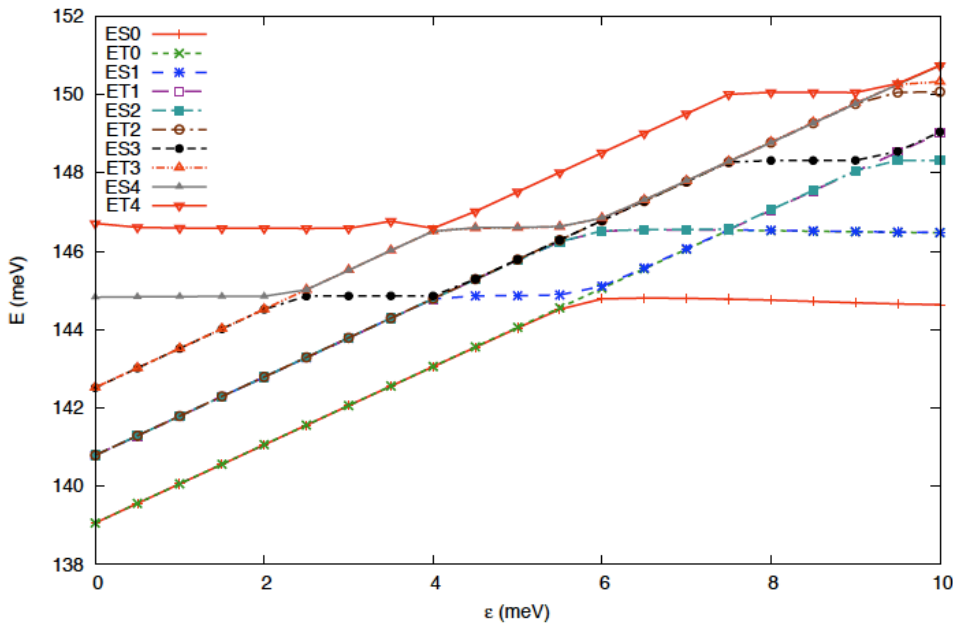
Exchange Energy 1 and 2: (ET0-ES0) and (ET1-ES0)



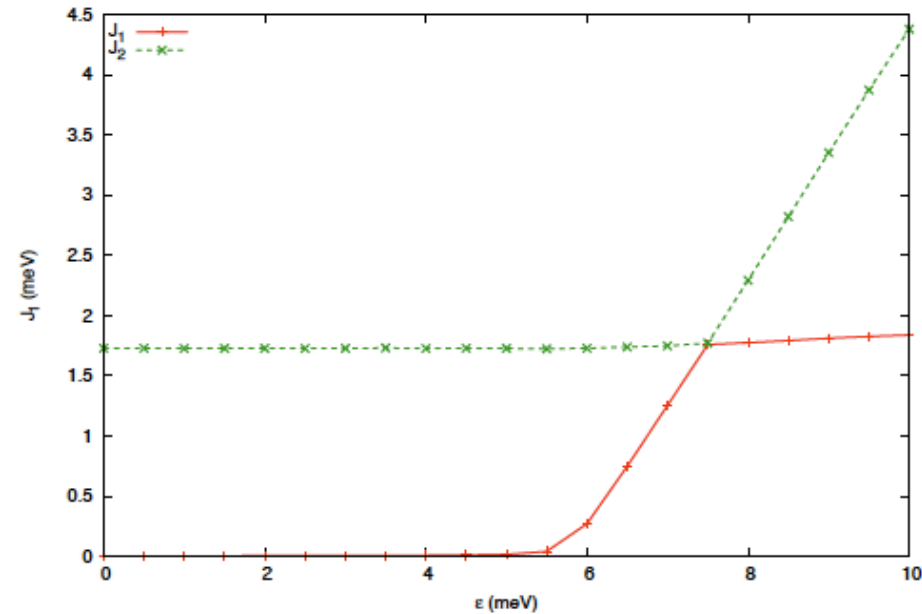
# DQD 2e states with large VS

$F=20$  MV/m

System: geo2 7nmDots L30 B0 Ez20  
2-electron energies



Exchange Energy 1 and 2: (ET0-ES0) and (ET1-ES0)



# Conclusions

- Tilted lattice suppresses VS in Si QDs
- Step roughness reduces the suppression
- E-fields increase the magnitude of VS
- Barrier material and alloy disorder are important
- TB + CI combined to obtain  $2e$  states of a multi-valley Si DQD
- Effect of VS shown on the exchange splitting