



Scaling of Waves in Heterogeneous Materials

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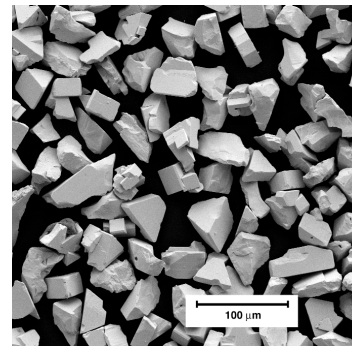
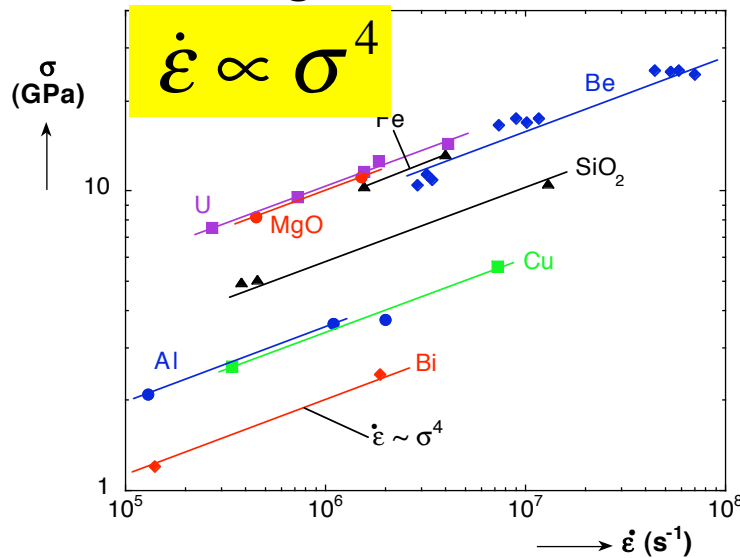
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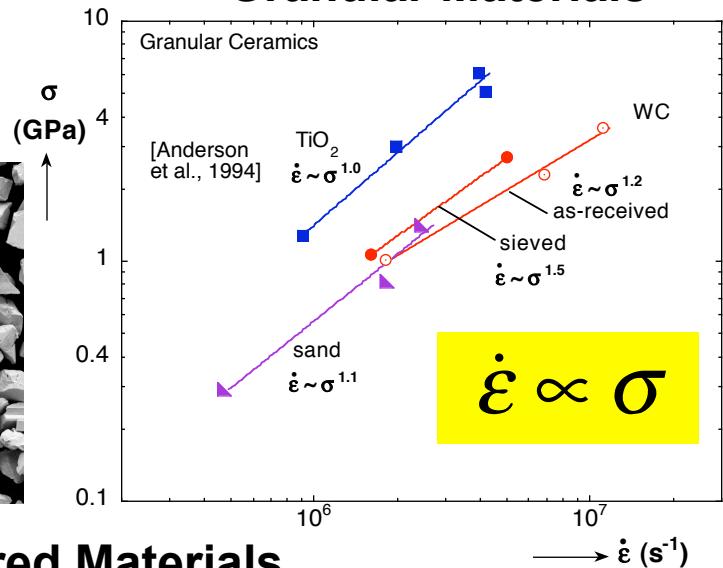


Scaling of Waves in Homogeneous Materials

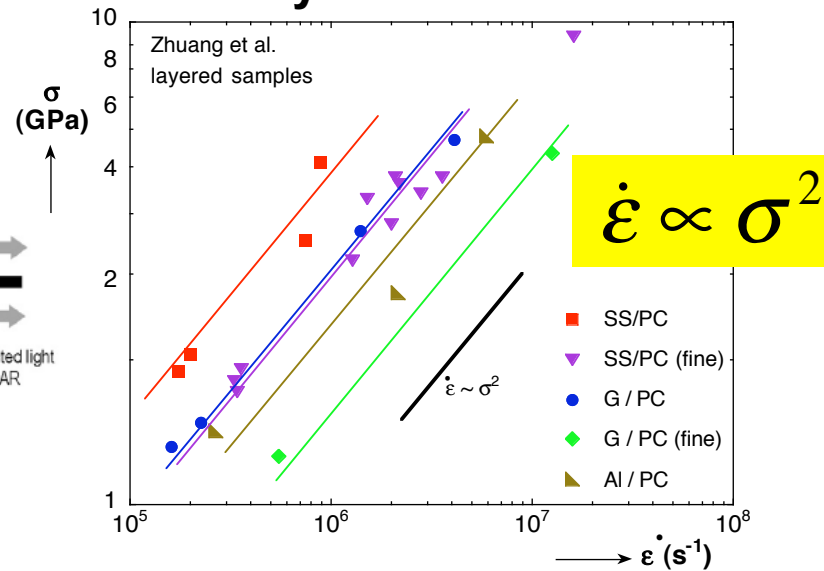
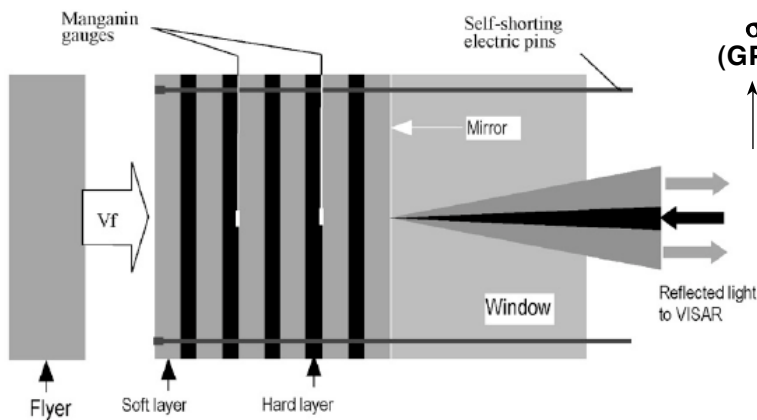
“Homogeneous” Materials



Granular Materials



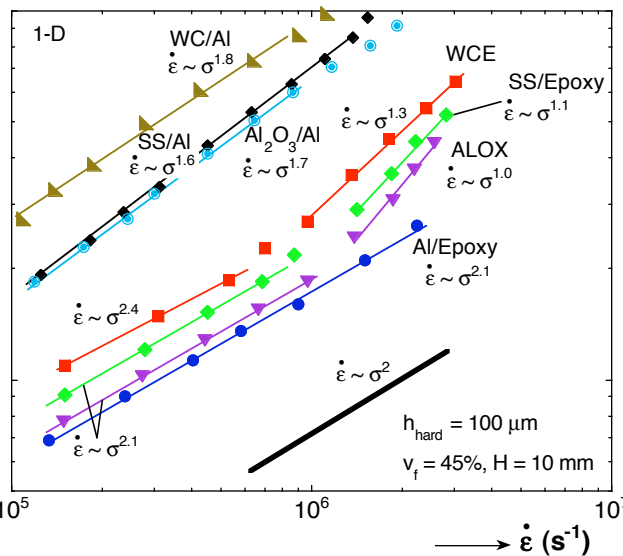
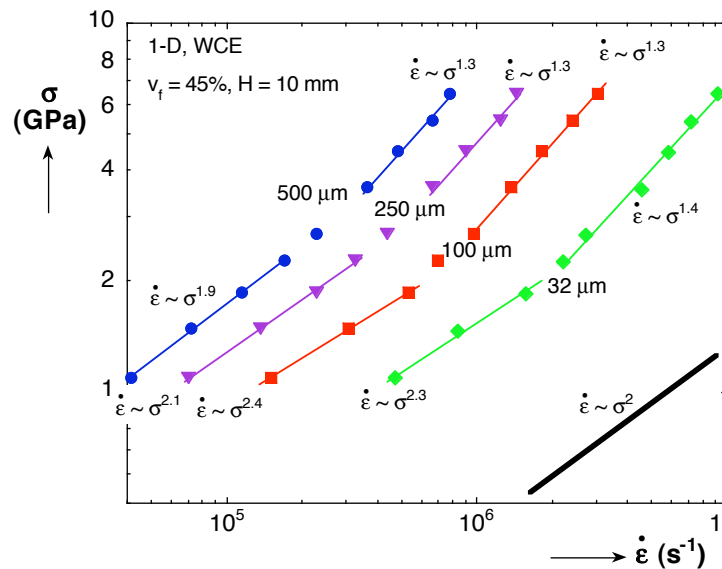
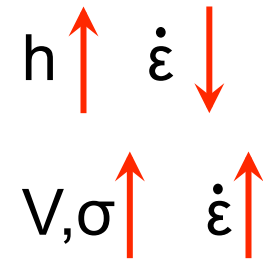
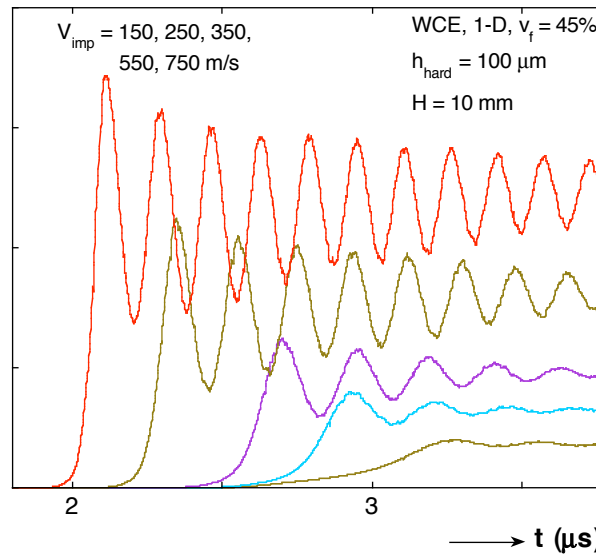
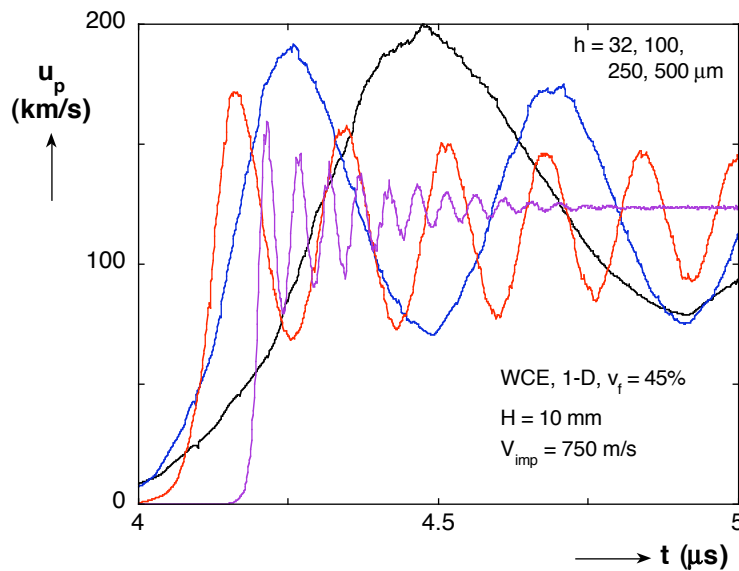
Layered Materials





Simulations for Layered Materials

1-D CTH Calculations



also a function of material parameters of layers



Dimensional Analysis for Layered Materials

variables of problem:

$$\sigma, \dot{\varepsilon}, h, v_f, C, (\rho_s, \rho_h) \text{ or } (z_s, z_h)$$

construct non-dimensional groups:

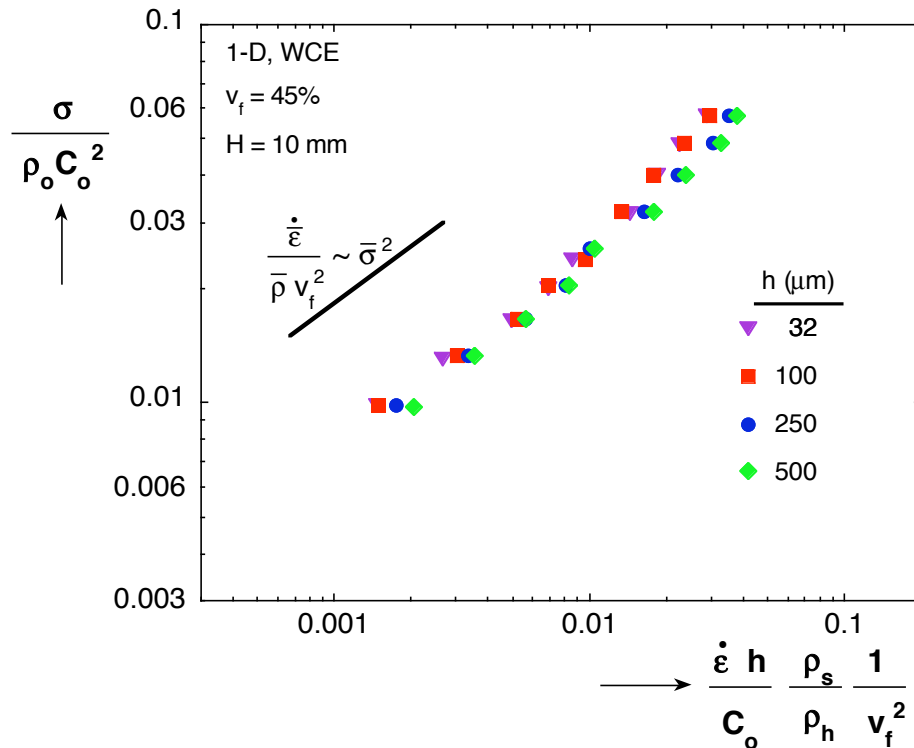
$$\dot{\bar{\varepsilon}} = \left(\frac{\dot{\varepsilon} h}{C_o} \right) \quad \bar{\sigma} = \left(\frac{\sigma}{\rho_o C_o^2} \right) \quad (v_f) \quad \bar{\rho} = \left(\frac{\rho_s}{\rho_h} \right)$$

$$C_o = \left(\frac{v_f}{C_h} + \frac{1-v_f}{C_s} \right)^{-1} \quad C_h, C_s = \begin{cases} C_B & \text{for polymers and metals} \\ C_L & \text{for ceramics} \end{cases}$$

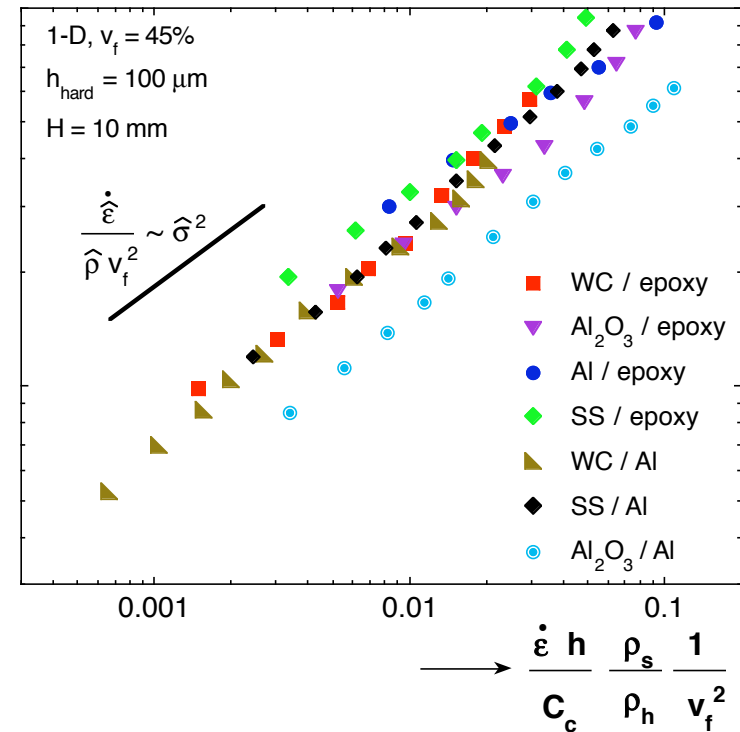
$$\rho_o = v_f \rho_h + (1-v_f) \rho_s$$



Non-Dimensional Simulation Results



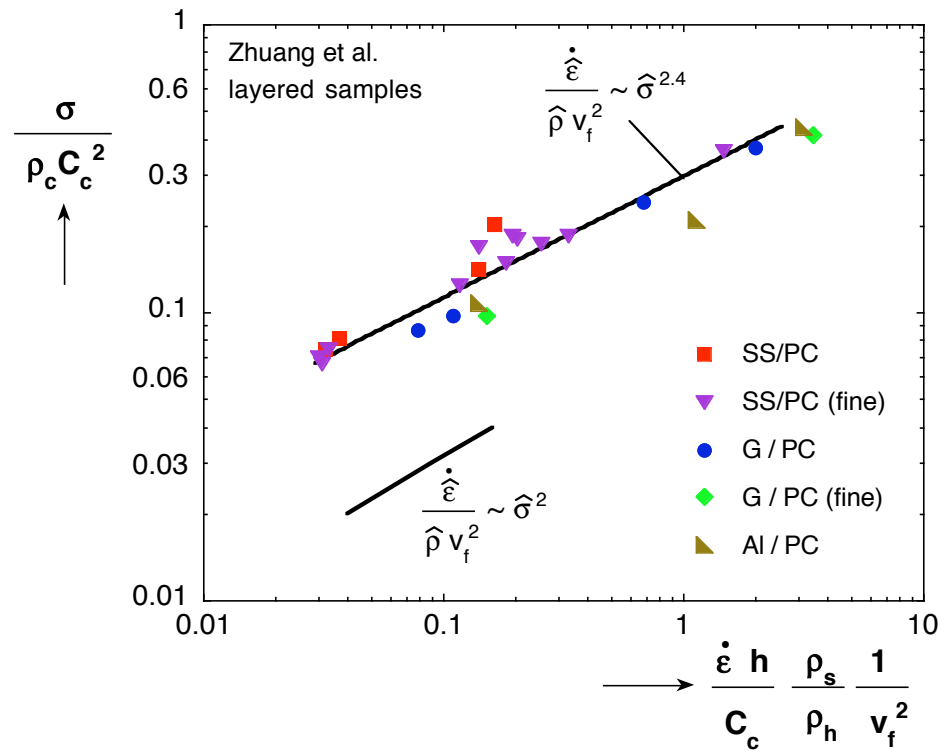
- non-dimensionalization collapses data for different layer thicknesses



- data for different material combinations collapse well using density ratio (with one exception)



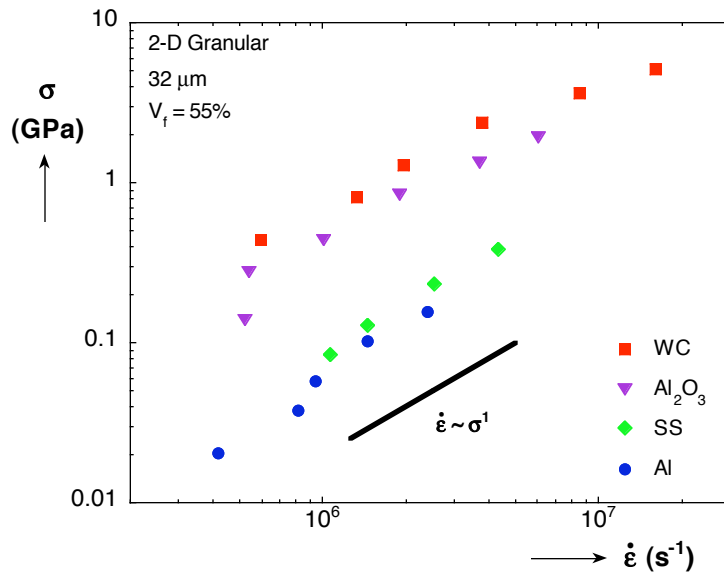
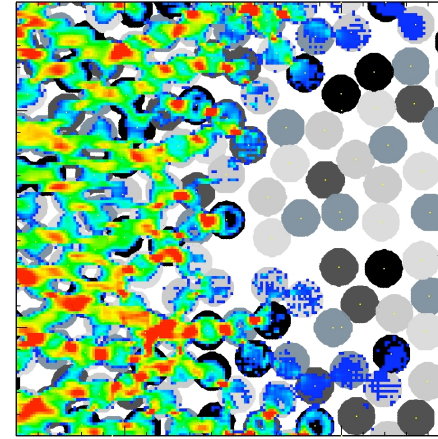
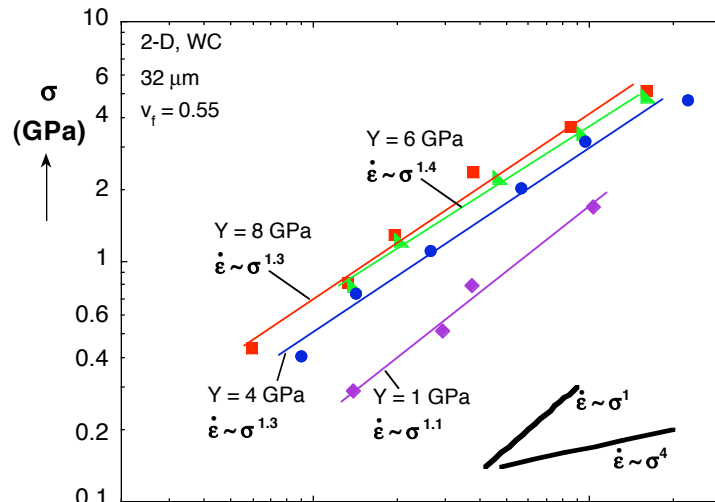
Non-Dimensionalized Experimental Results



- non-dimensional experimental results also collapse to a single curve (approximately to second power)



2-D CTH Simulations of Granular Materials

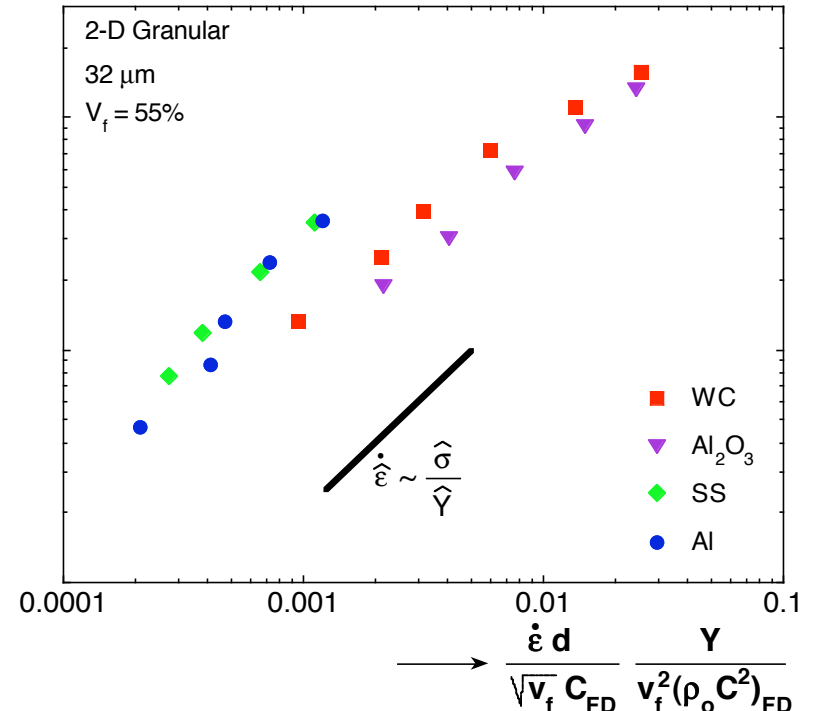
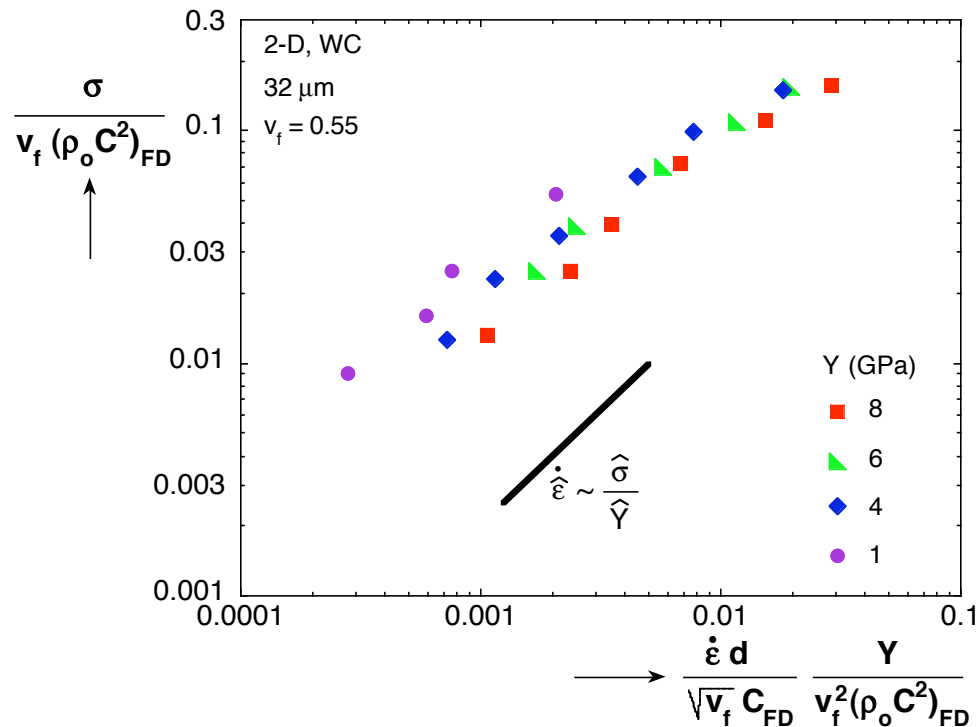


- non-planar shock structure
- CTH simulations reproduce first power scaling
- some dependence on Y , strong material dependence
- non-dimensionalization suggested by Grady (2010):

$$\frac{\sigma}{\dot{\epsilon}} \propto \left(\frac{\rho_o}{\rho_s} \right)^m \sqrt{\rho_o d^2 \sigma_c}$$



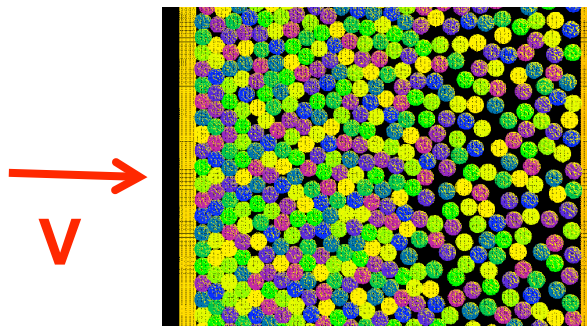
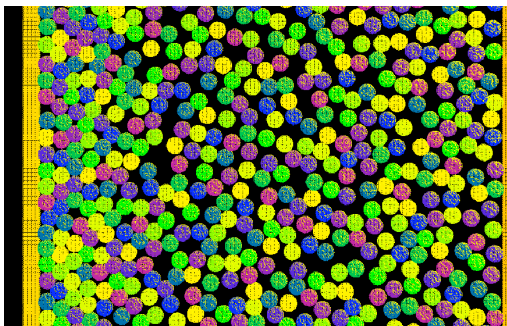
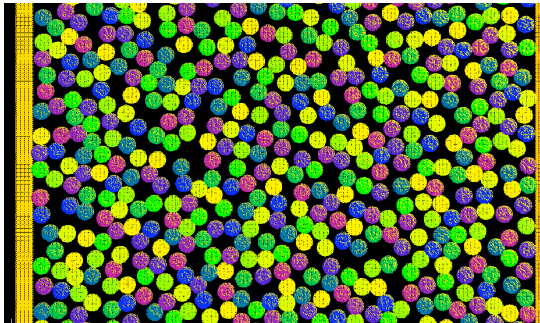
Non-Dimensionalization of CTH Results



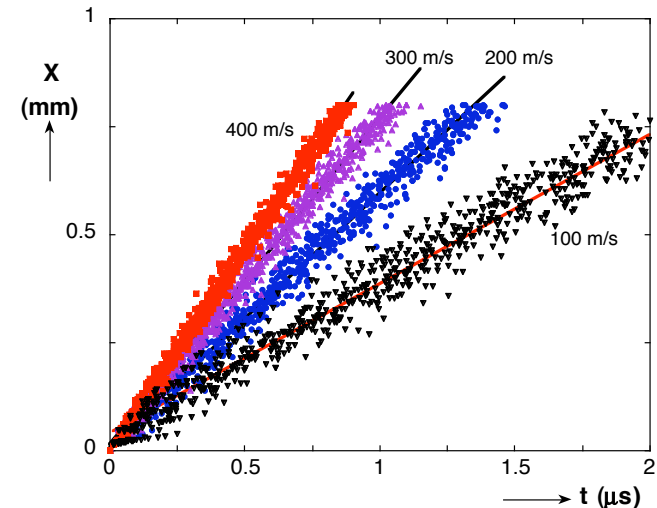
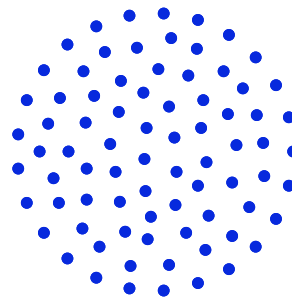
- scale wave speeds by square root of volume fraction (suggested by Steinberg, some validation by Bless)
- Y needed to collapse data, though metals and ceramics separated somewhat



Results from a Particle-Based Code



EMU - Parallel, particle-based implementation of peridynamics (Silling, S. A. (2000). *J. Mech. Phys. Solids* 48, 175-209



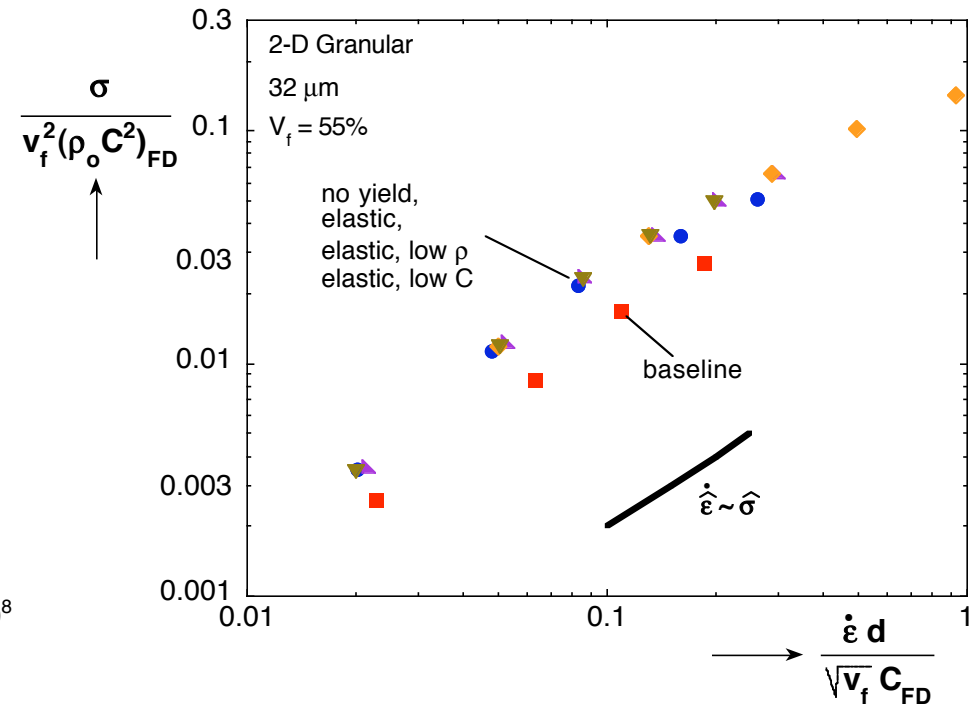
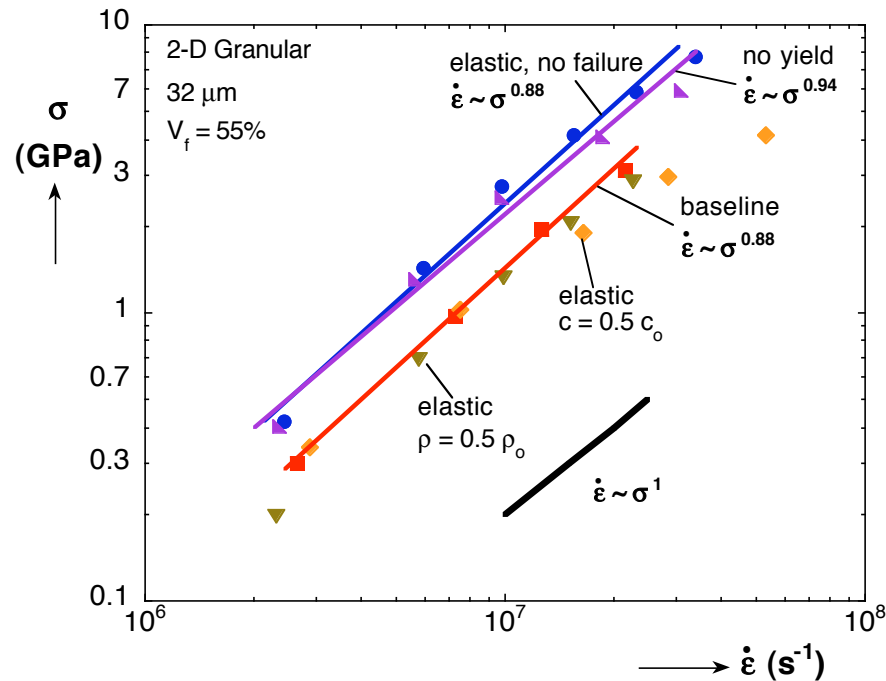
- waves appear steady
- wave speed increases with V
- width of band decreases with V
- elastic simulations yield same scaling
 - Grady's scaling doesn't work

10:00 AM–10:15 AM Friday, Renaissance Ballroom AB

Chris Lammi - Mesoscale Simulations of Granular Materials with Peridynamics



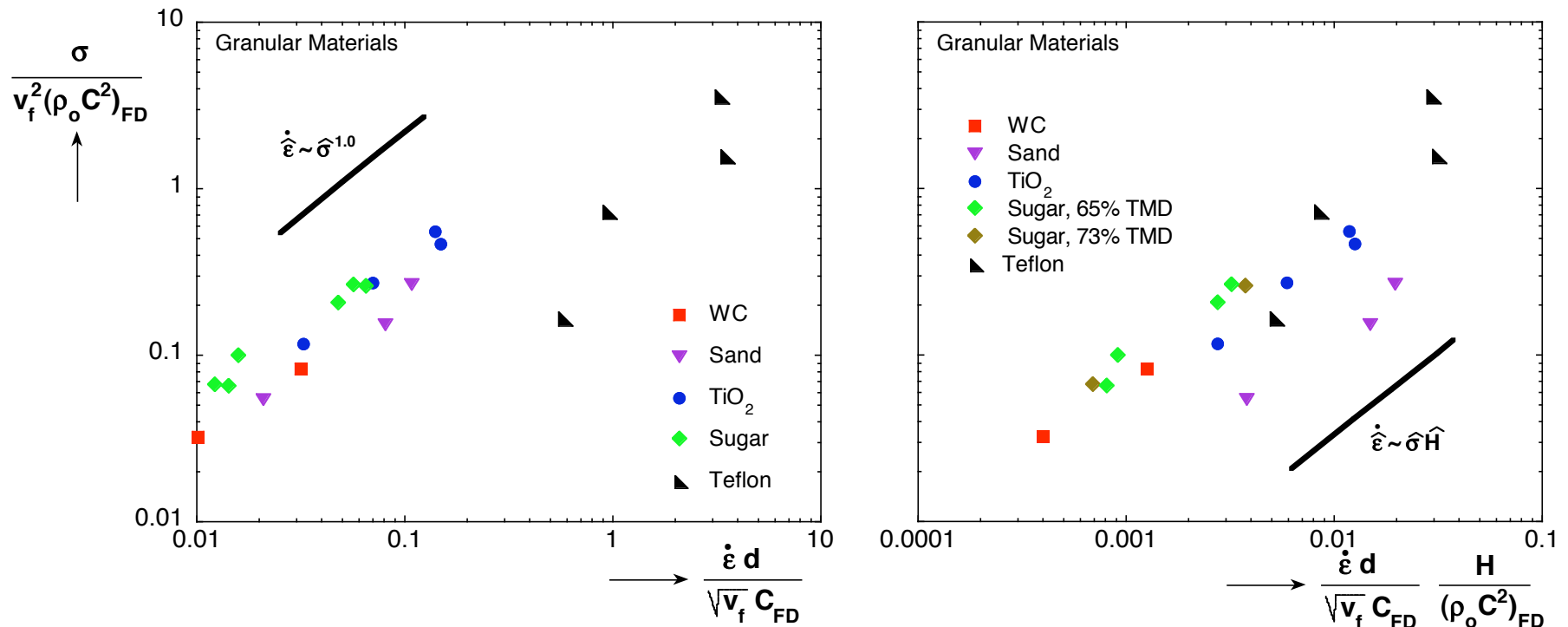
Non-Dimensionalization for EMU Results



- no strength in problem is material elastic
- fracture does not seem to affect scaling
- elastic-plastic material (baseline) has lower characteristic wave speed $\rightarrow$ will shift data upward



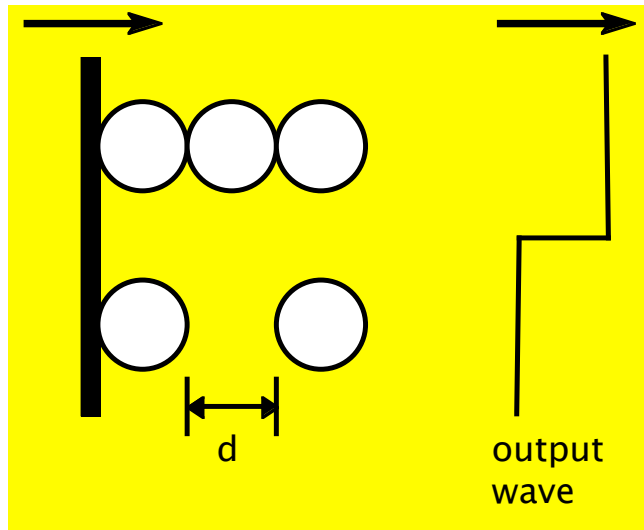
Non-Dimensionalization of Experimental Results



- use hardness (H) as characteristic strength
- does volume fraction enter in separately?
- ceramics collapsed better without H, teflon collapsed better with H → additional data needed to distinguish two possibilities



A Simple Scaling Argument for Granular Materials (1)



$$\varepsilon = \frac{u_p}{U_s}$$

$$\dot{\varepsilon} \propto \frac{\varepsilon}{\Delta t} \propto \frac{u_p / U_s}{d / u_p}$$

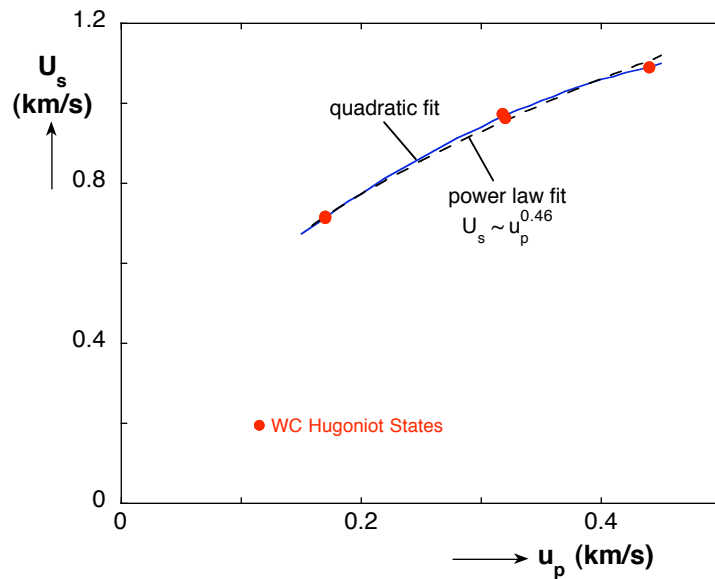
mass
traversing
pores controls
width of
shock front

$$\dot{\varepsilon} \propto \frac{u_p^2}{d U_s}$$



A Simple Scaling Argument for Granular Materials (2)

$$\sigma = \rho_{oo} U_s u_p \quad \dot{\epsilon} \propto \frac{u_p^2}{d U_s}$$

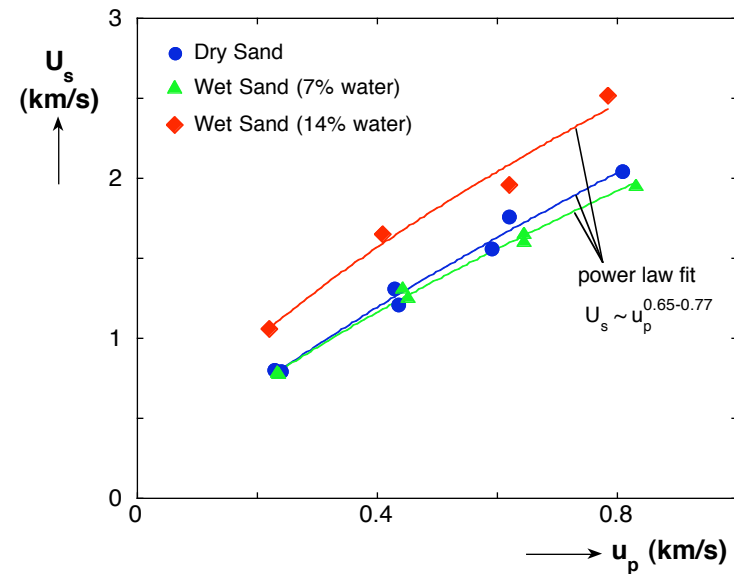


$$\text{if } U_s \propto u_p^{0.5}$$

$$\sigma \propto u_p^{3/2}$$

$$\dot{\epsilon} \propto u_p^{3/2}$$

$$\longrightarrow \dot{\epsilon} \propto \sigma$$



$$\text{if } U_s \propto u_p^{0.75}$$

$$\dot{\epsilon} \propto \sigma^{0.7}$$

mass transfer across void is critical aspect, thus granular WC and WC/epoxy behave very differently



Conclusions

- power law dependence of strain rate with stress occurs in materials with microstructure:
 - 2nd - layered materials - wave reverberation due to density differences
 - 1st - granular materials - mass transport
- non-dimensionalization collapse both experimental and simulated data for layered materials
- a simple argument based on mass transport yields first power scaling for granular materials
- non-dimensionalization for granular materials can be done (at least) two ways
- how to apply to mixtures of granular materials?