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Title: Simulations of Richtmyer-Meshkov Instabilities in Planar
and Gas-Curtain Shocktube Experiments (U)

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Ristorcelli

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Simulations of Richtmyer-Meshkov Instabilities in Planar and Gas-Curtain Shocktube Experiments

F.F. Grinstein, A.A. Gowardhan, and J.R. Ristorcelli

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Abstract

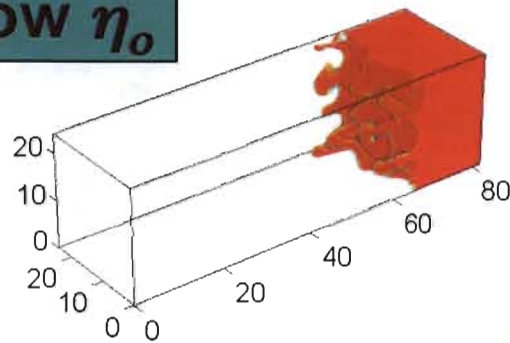
Our particular focus in this presentation is devoted to initial material interface characterization impact on shock-driven turbulent material mixing. Progress in addressing relevant issues of initial condition effects in studies of mixing driven by Richtmyer-Meshkov instabilities in planar and gas-curtain shock-tube laboratory experiments is reported.

Simulations of Richtmyer-Meshkov Instabilities in Planar and Gas-Curtain Shocktube Experiments

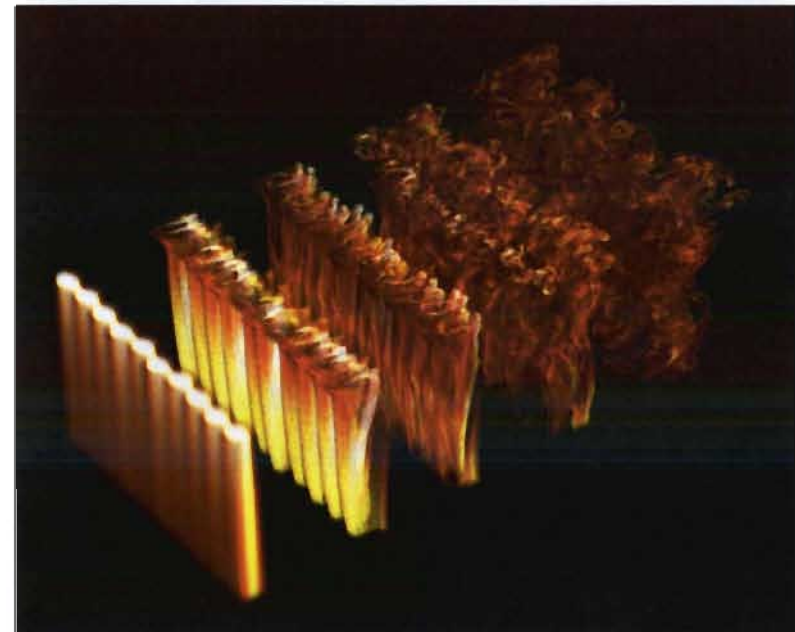
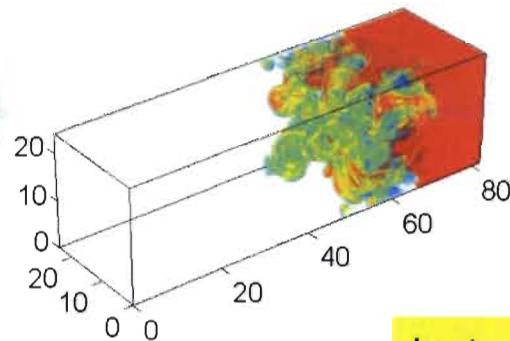


Fernando F. Grinstein (simulations), Akshay A. Gowardhan (post-doc),
J. Ray Ristorcelli (theory)

low η_o



high η_o



instantaneous material mixing

Simulations of Initial Condition Effects on Shock-Driven Turbulent Mixing

Background, Motivations

- Understand effects of initial material interface conditions
- Assess predictability of simulation models

The **(single-interface)** planar RM experiment

- Challenges to Moment Closures: *the bipolar RM behavior*
→ *Reshock effects (on mix & transition) on first-shock*

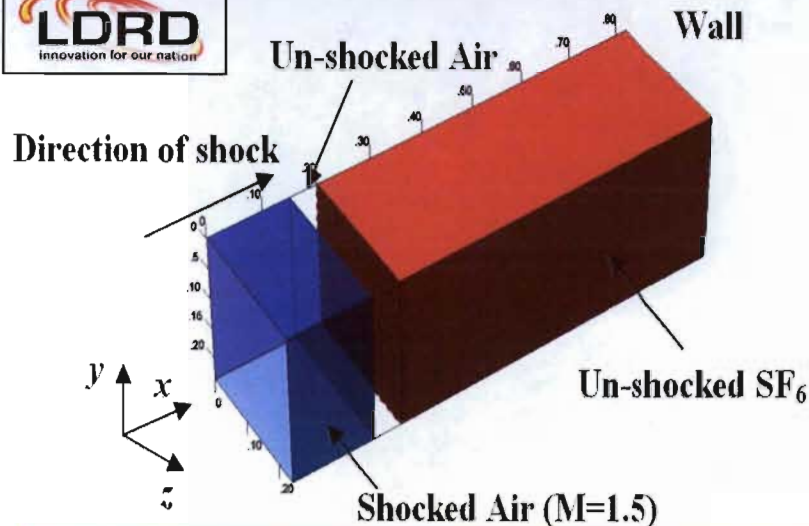
The **(two-interface)** Gas Curtain RM experiment

- Initial 3D GC characterization and modeling issues
- Sensitivity of shocked / reshocked GC to ICs
- Data reduction and **bipolar RM behavior**
→ *Opportunities for defining a RM test case*

Conclusions

Shock-Driven Turbulence Simulations

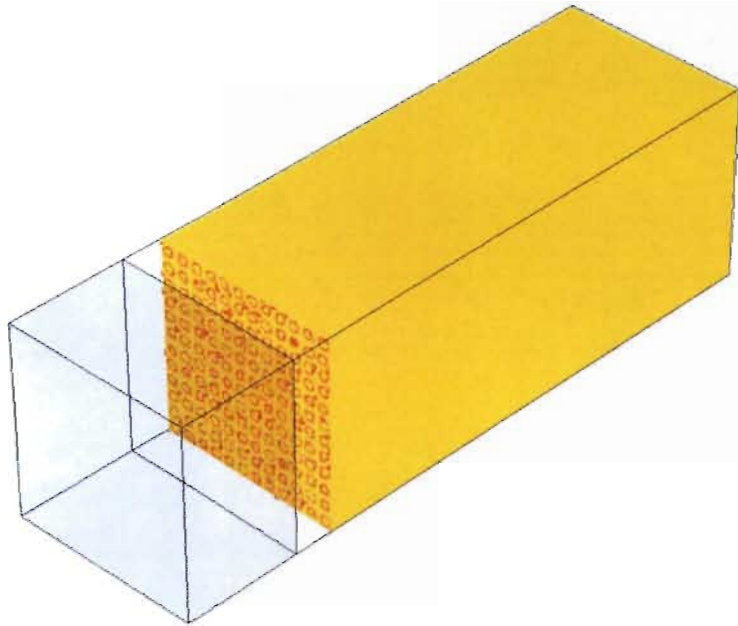
shocks and turbulence must be emulated



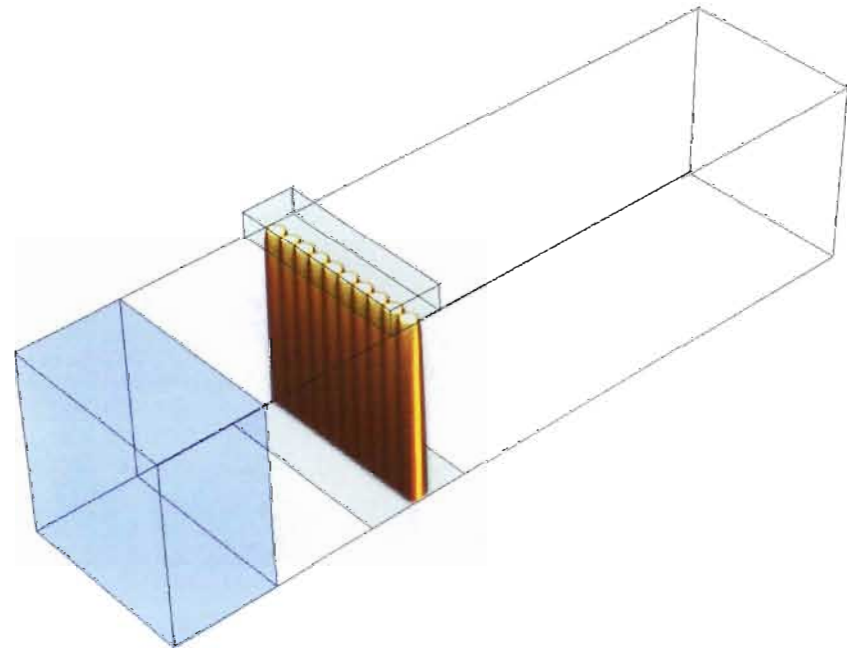
- shocks and turbulence, unsteady
- wide range of length and time scales, non-linear interactions
- Implicit Large Eddy Simulation (ILES), e.g., ILES book, 2nd printing: 2010

- Richtmyer '60; **planar shocktube expts.** (V&S '95, Poggi '97, Leinov '09, ...); **LANL P-23 gas curtain expts.**,
- **hybrid WENO / classical LES**, ..., Pullin et al. – *JFM* 2006, ..., 2011
- **ILES** , 2002 – 2011: Cohen et al. (FV-PPM), ..., Schilling et al. (FD-WENO), Leinov et al. (FV-ALE), Thornber-Drikakis-Youngs-Williams et al. (FV-Godunov), ...
- **ILES-RAGE**; FV-Godunov, van Leer limiter, no interface treatment, AMR
↑ planar V-S expts., *P. Scripta* 2010, IWPCTM12; **PoF March 2011**;
↓ planar Bipolar RM, **PoF Letters July 2011**; AIAA-Hawaii-2011 / ETC13 → **PoF**
shocked (double interface) **gas-curtains**, *J. Turbulence* 2011, in press.

ILES RAGE simulations (SF_6 mass fraction distributions)



planar single-interface (V&S, Caltech)



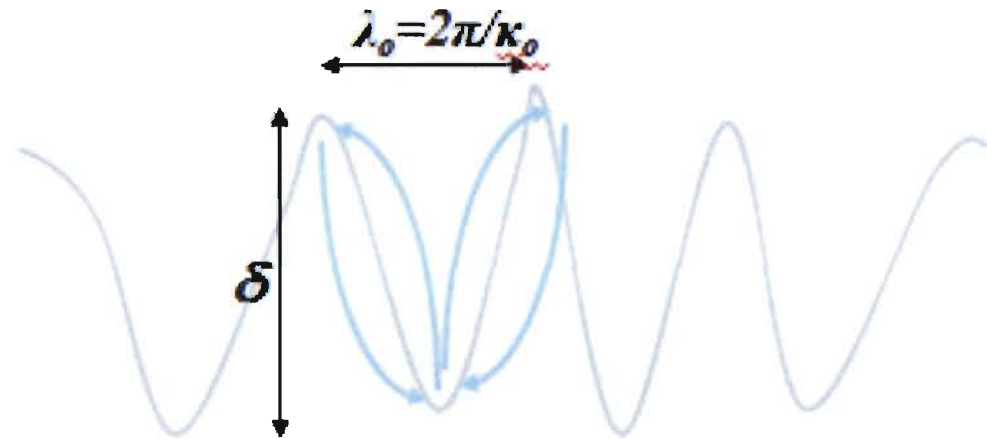
gas-curtain two-interface (P-23)

- Understand Effects of Initial Material Interface Conditions
- Practical Goal: control (promote or inhibit) RM instability

How does interfacial morphology control the evolution of RM ?

if $X_s(y,z)$ describes the material interface,
then, we define the rms slope of the interface “ η_o ”

$$\eta_o = \kappa_o \delta_o$$
$$\sim \langle \nabla X_s \nabla X_s \rangle^{1/2}$$



low η_o

Air

SF₆

$$(\kappa_o \delta_o \ll \pi)$$



Air

SF₆

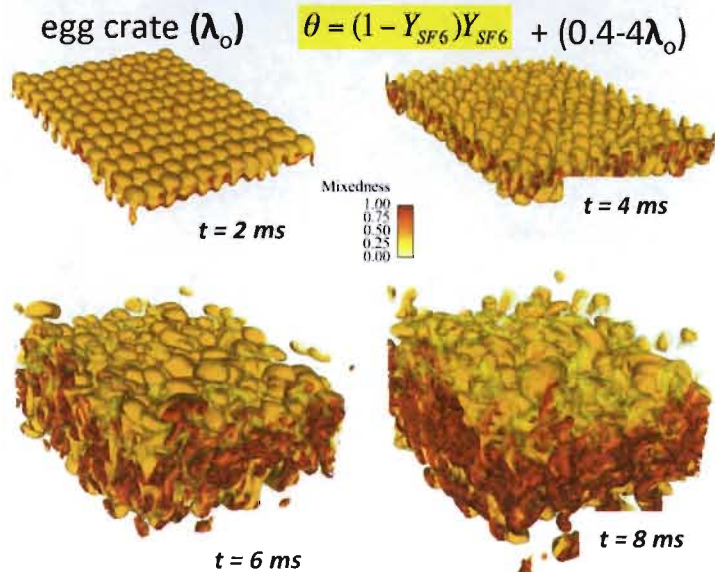
high η_o



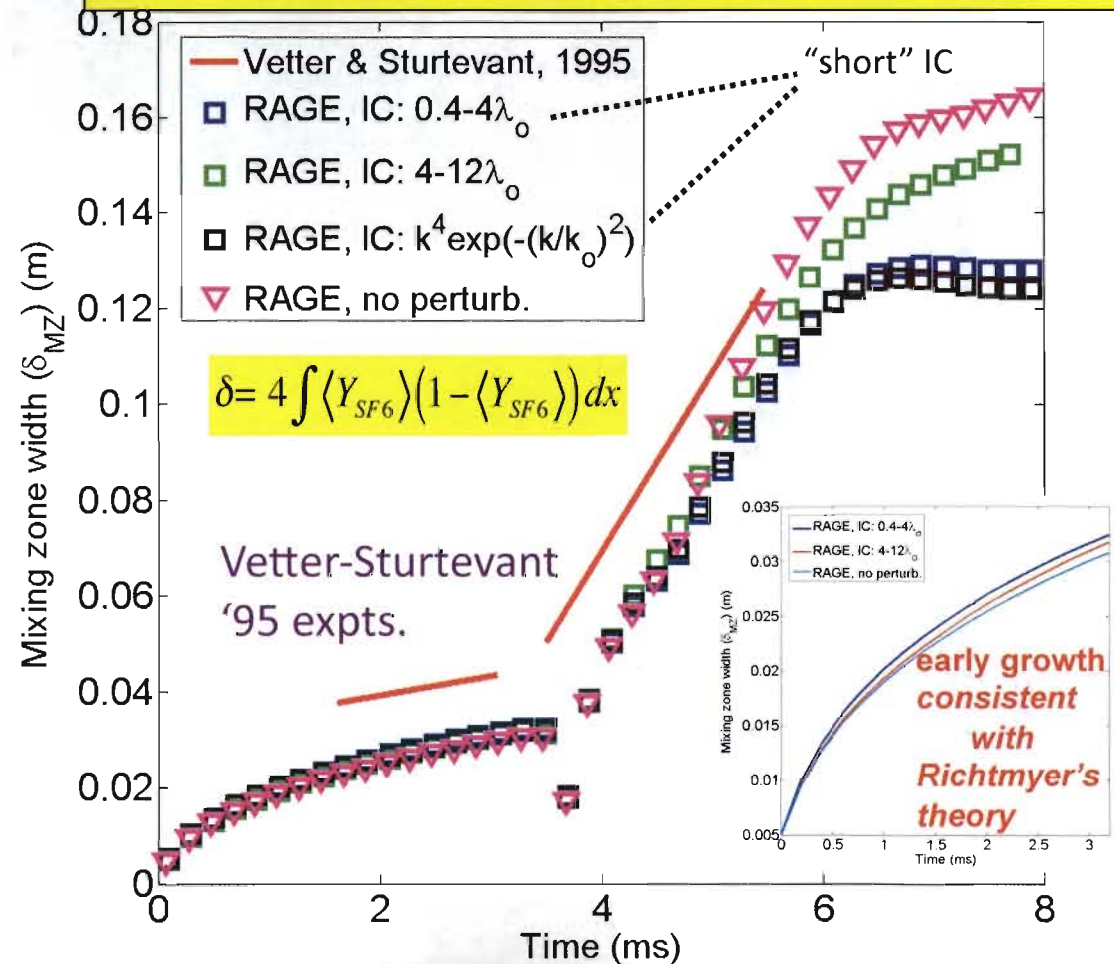
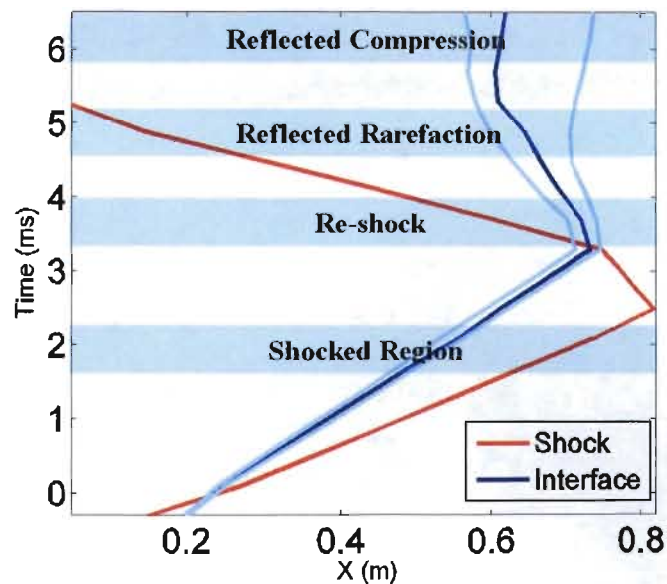
ILES RAGE – Planar RM Expts.

Spectral IC effects on material mixing

Grinstein, Gowardhan, and Wachtor, *PoF*, March 2011



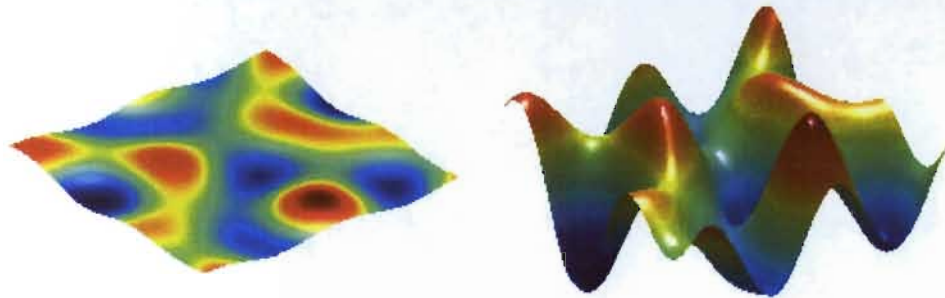
10% IC perturbation added to mode (λ_0)



- results for "thin" **low η_0** initial material interface
- **early-time ($t < \sim 5 \text{ ms}$) growth fairly IC insensitive**
- **late-time sensitive to ICs** (more so for "longer" IC
- **IC resolution issues ... separate discussion req'd ...**

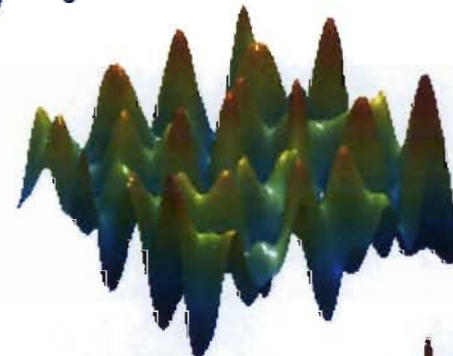
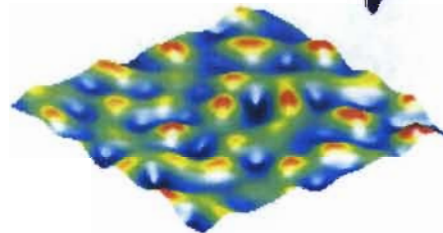
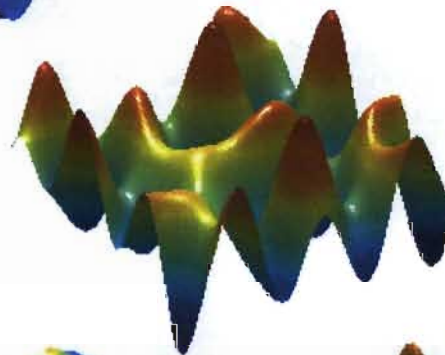
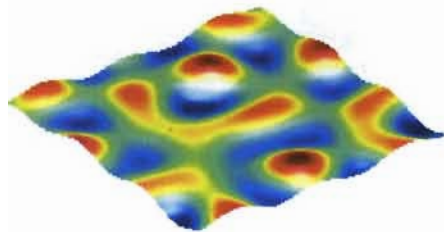
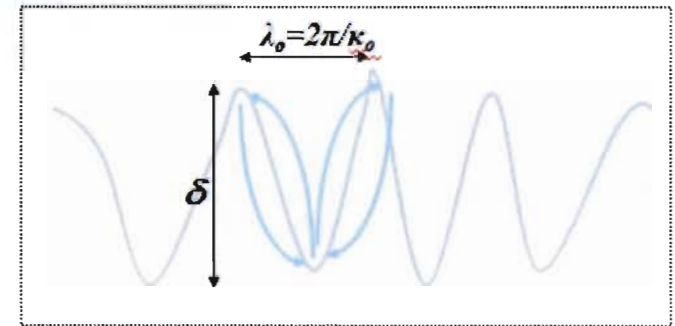
Initial (single) material interface parameterization

focus first on: no “egg-crate”, no reshock...



high η_o class ($\kappa_o \delta_o > \pi$)

$\eta_o = 10\pi/12, 10\pi/8, 10\pi/4, 10\pi/2$

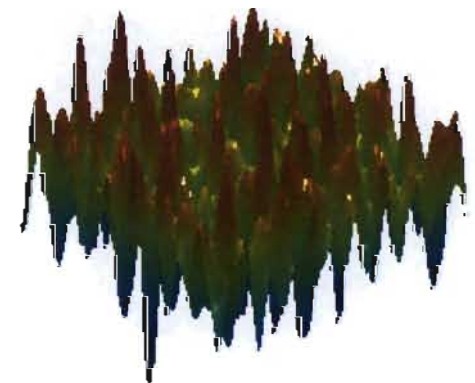
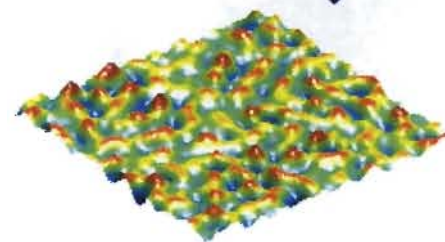


$$\eta_o = \kappa_o \delta_o$$

low η_o class

$\eta_o = \pi/12, \pi/8, \pi/4, \pi/2$

($\kappa_o \delta_o \ll \pi$)



Bipolar Behavior of planar RM

Ma=1.5, air/SF₆ – no egg-crate, no reshock
Gowardhan, Ristorcelli and Grinstein; *PoF* Letters, July 2011

Impact of *rms* slope $\eta_o = \kappa_o \delta_o$ of Initial Material Interface

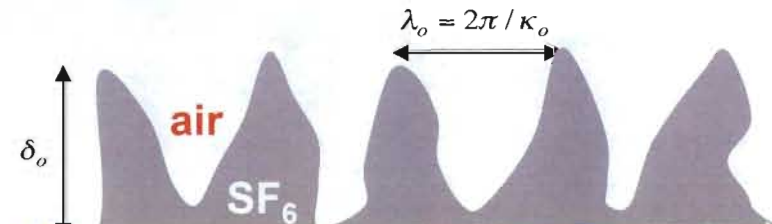
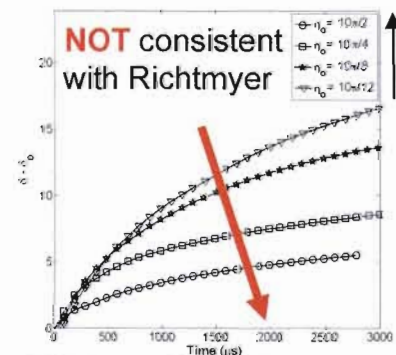
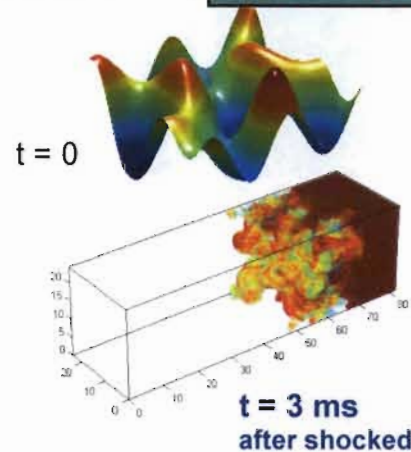
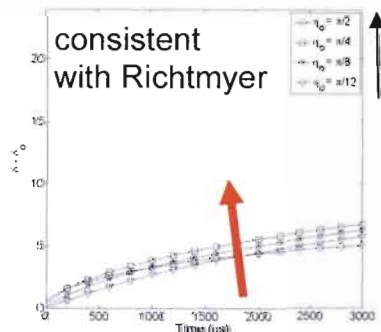
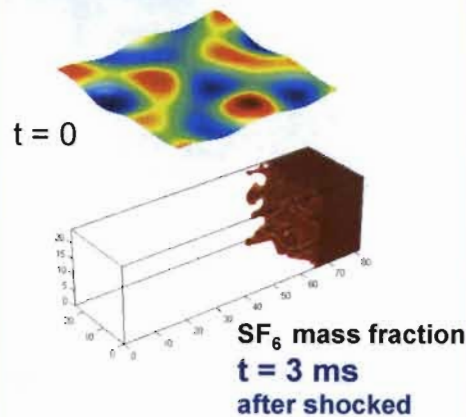
Beyond Richtmyer (growth = constant $\times \eta_o$):

→ bipolar RM behavior vs. IC morphology
→ different instability mechanisms & late-time flow

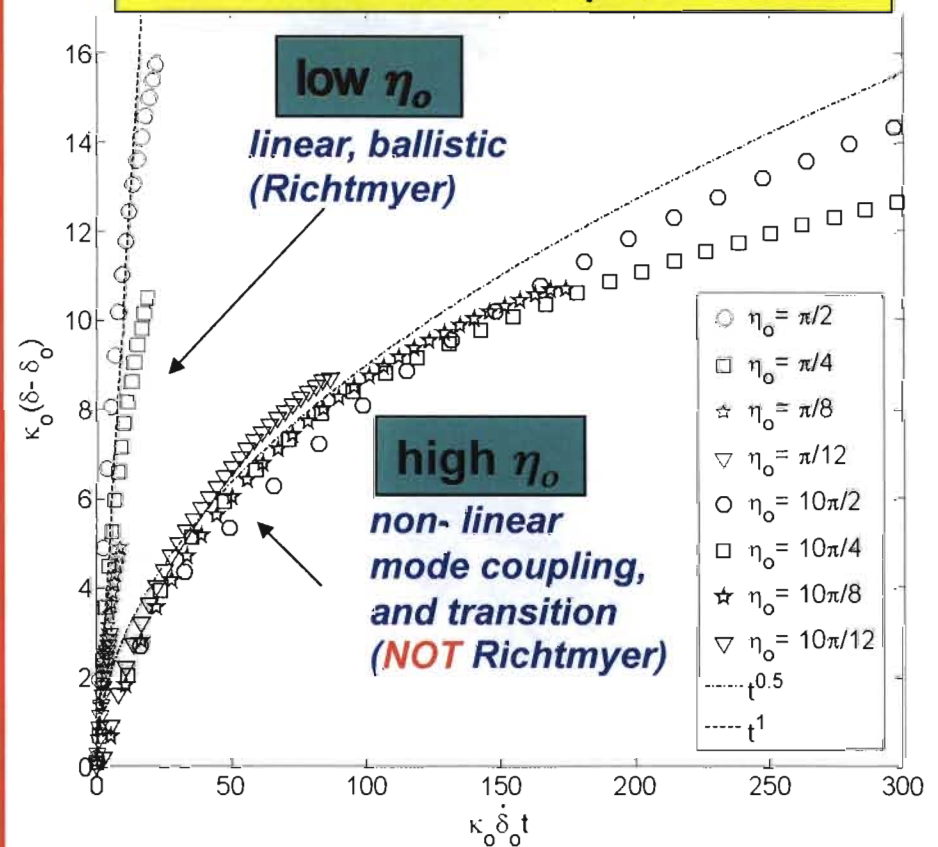
low η_o

Dimensional results

high η_o

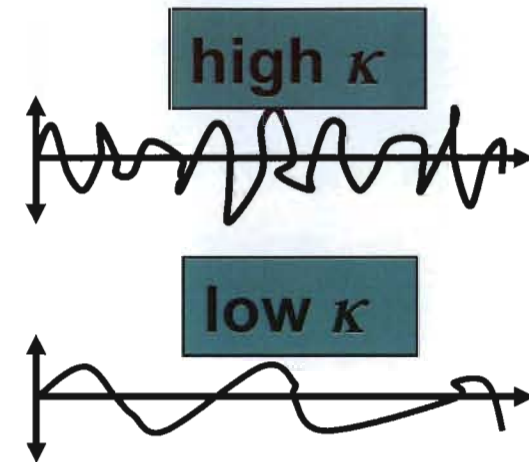
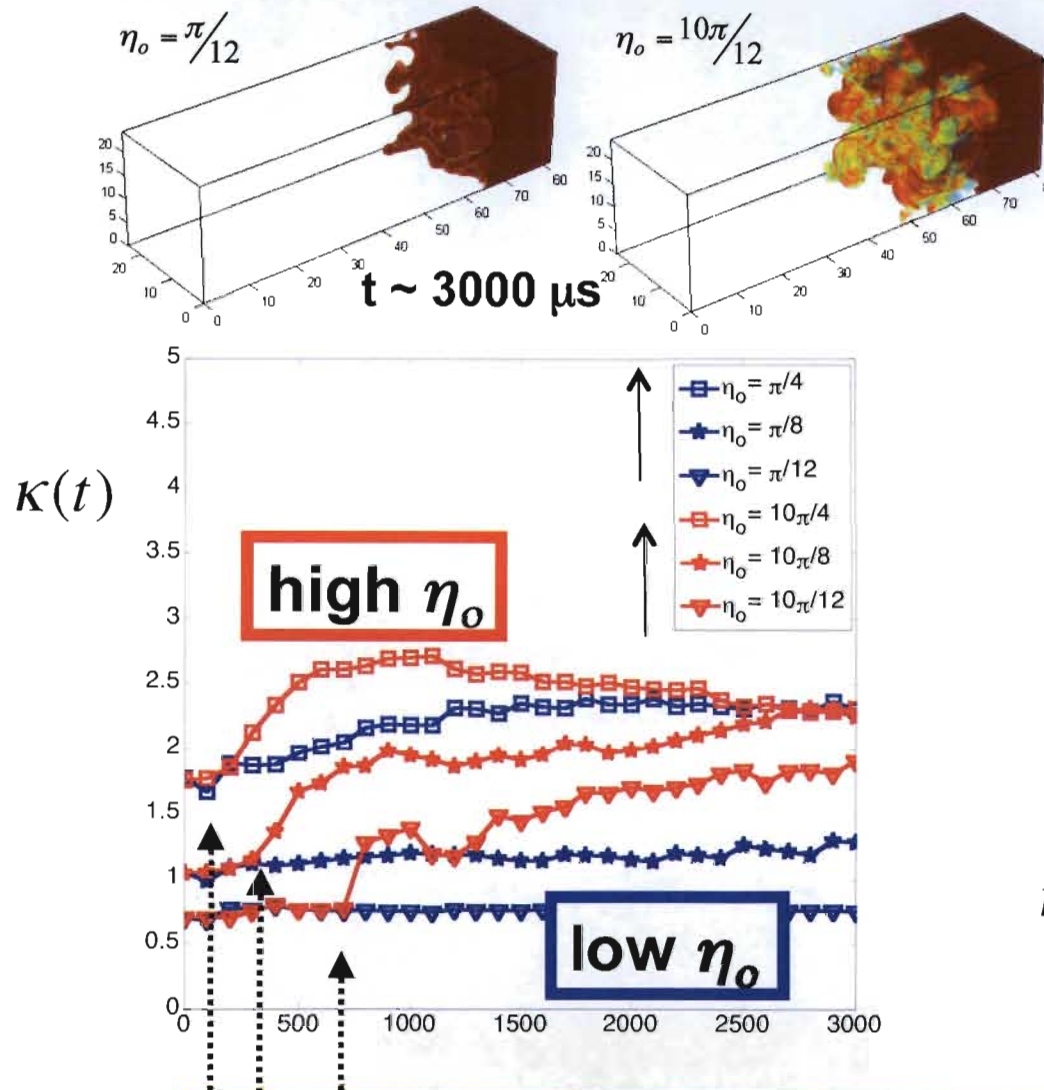


Non-Dimensional "Bipolar" results



Characterizing Small-Scale Production

→ zero-crossing wavenumber κ (e.g., Sreenivasan et al. JFM '83)



κ is the “zero crossing” wavenumber of the mass density fluctuation

$$\kappa(t) \sim \frac{1}{\lambda(t)} = \frac{1}{\text{Taylor length scale}}$$

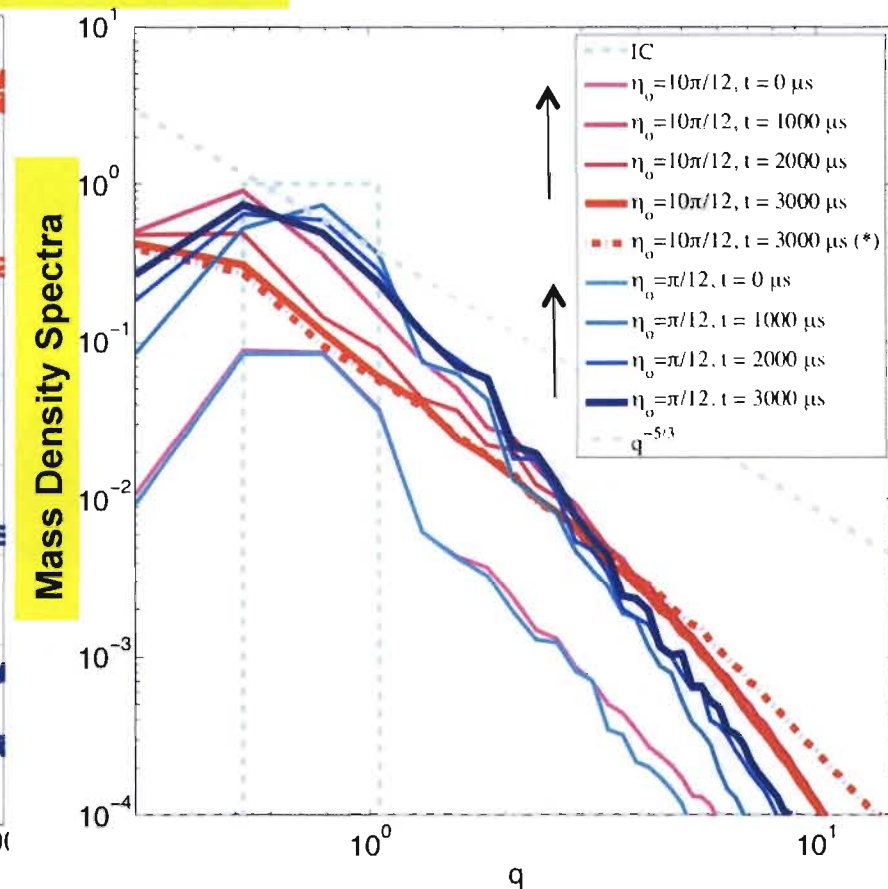
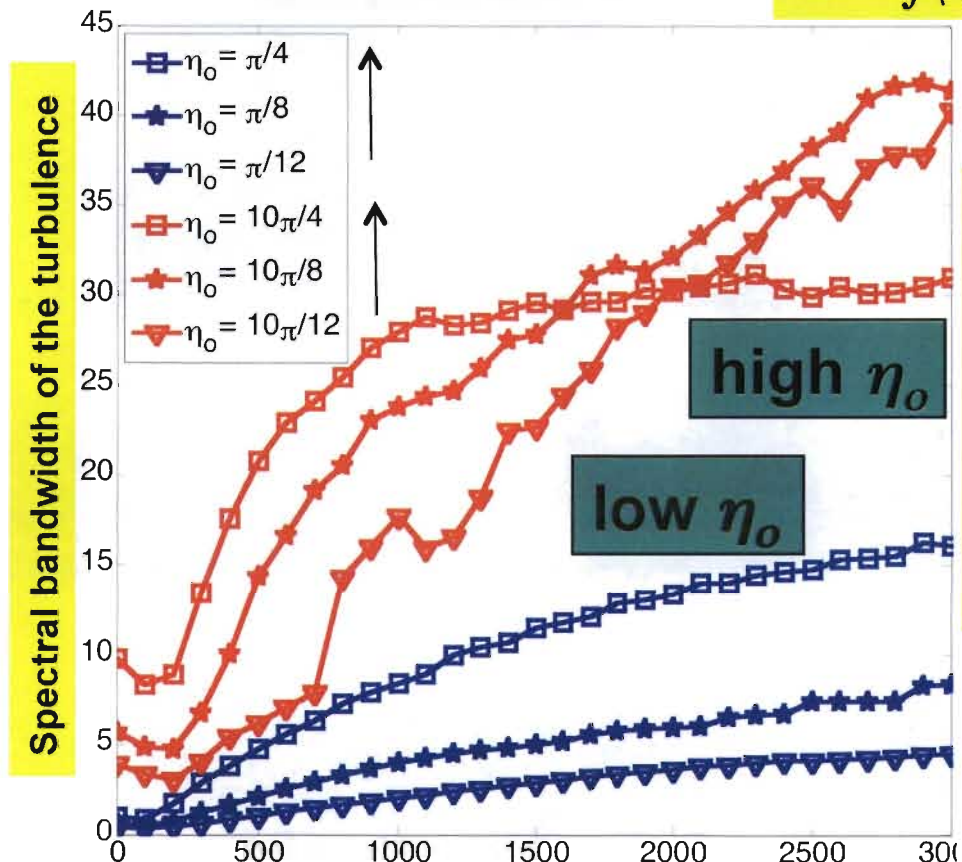
“transition” process indicated by rapid increase of κ

Spectral bandwidth of the turbulence

**Spectral bandwidth proxy
provides a measure of how
“turbulent” the flow is**

$$\eta(t) = \kappa(t)\delta(t) = \frac{\delta(t)}{\lambda(t)} \sim \frac{\text{Integral scale}}{\text{Taylor length scale}} \sim \text{Re}_\lambda$$

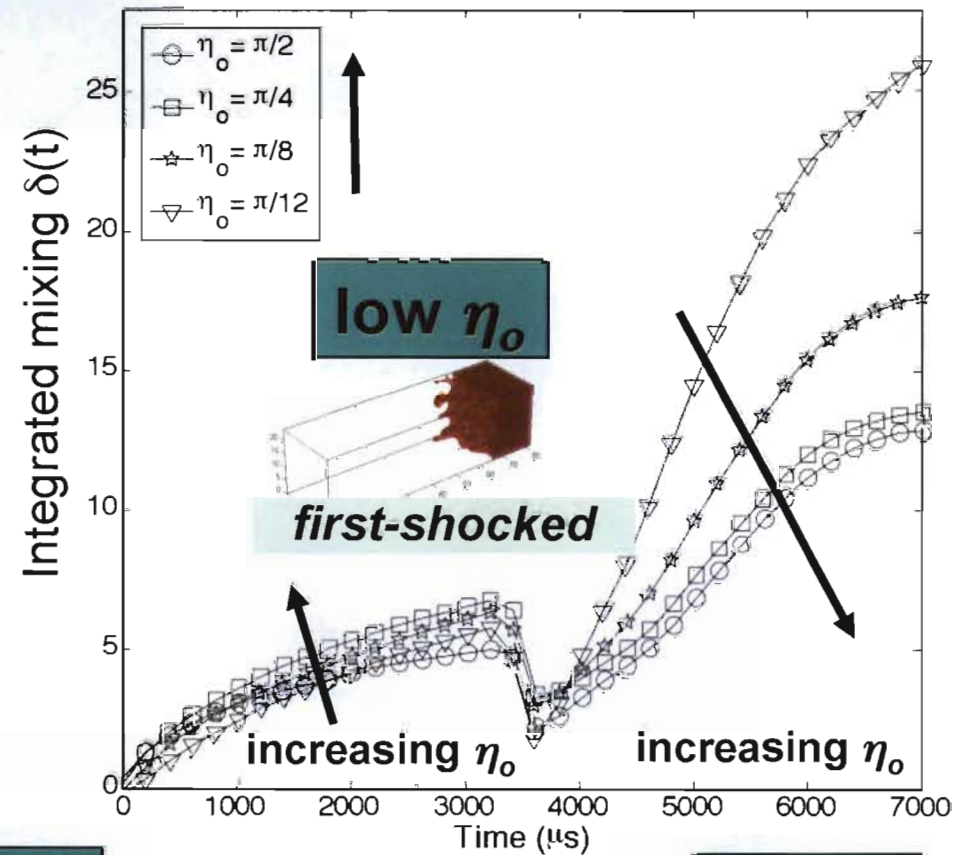
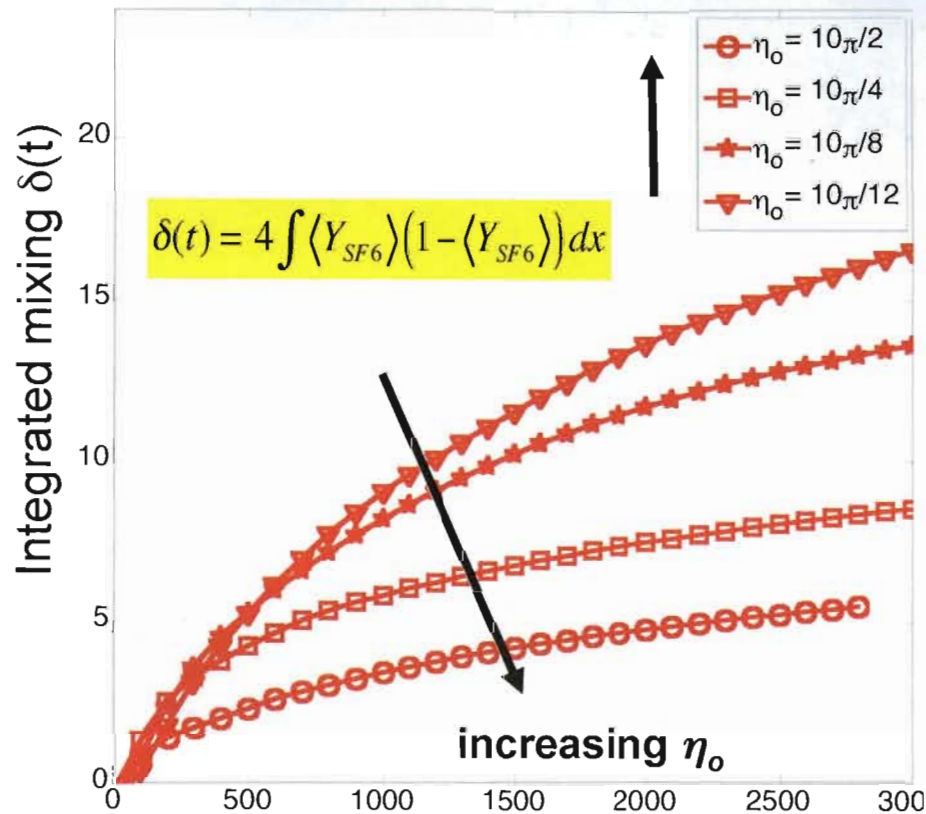
$$\delta(t) = 4 \int \langle Y_{SF6} \rangle (1 - \langle Y_{SF6} \rangle) dx$$



Higher initial η_0 leads to higher $\eta(t)$ at late times

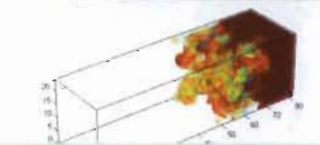
Consequences of Bipolar RM Behavior

low η_o reshock effects ~ high η_o first shock effects



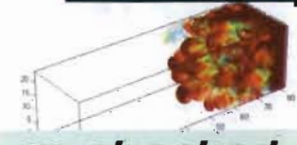
Y_{SF6} visualizations at
 $t \sim 3000 \mu s$
after first-shock
(or after reshock)

high η_o



first-shocked

low η_o

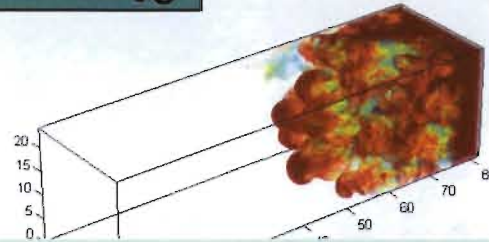
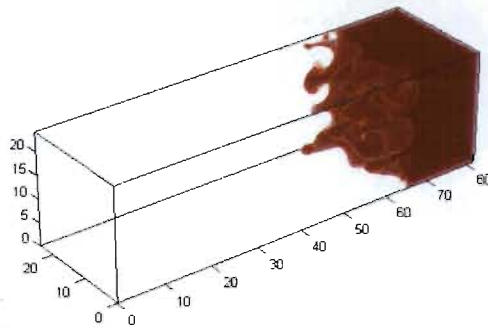


re-shocked

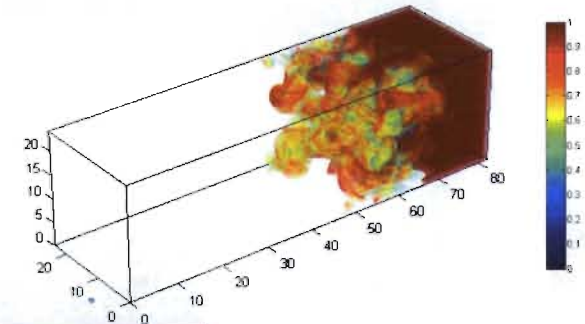
Consequences of Bipolar RM Behavior

low η_o reshock effects ~ **high η_o** first shock effects

low η_o re-shocked



instantaneous material mixing



low η_o first-shocked

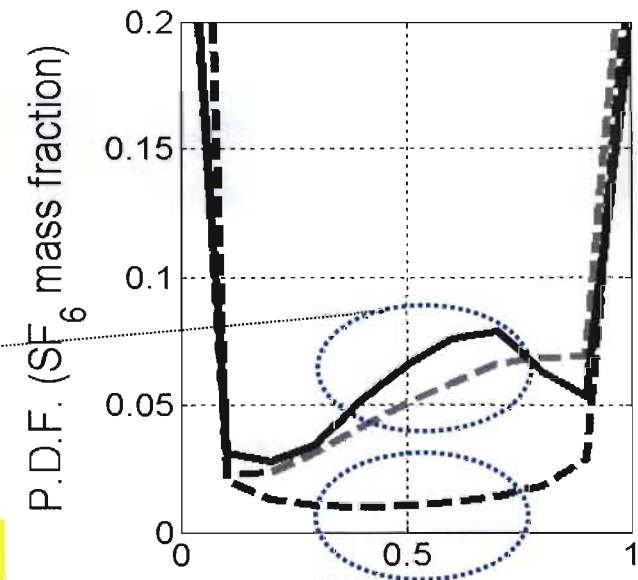
high η_o first-shocked

$t \sim 3000 \mu s$ after first-shock
(or after reshock)

— **low η_o** reshocked **mixed**

- - **high η_o** first-shocked **mixed**

- - **low η_o** first-shocked **unmixed**



Planar Shock-Driven Turbulence



Grinstein, Gowardhan, and Wachtor, *PoF*, 2011; Gowardhan, Ristorcelli and Grinstein; *PoF Letters*, 2011

Shocked (double interface) Gas Curtain → Gowardhan and Grinstein, *J. of Turb.* 2011, in press

- RM bipolar behavior: **switch for $\eta_o = \kappa_o \delta_o \sim 1$**

low η_o : *linear, ballistic, mix-width $\delta \sim t$*

high η_o : *non-linear, mode coupling, mix-width $\delta \sim t^{1/2}$*

→ *transition to turbulence suggested*

→ *more material mixing & smaller scales*

- **Reshock effects on first shock, if $\eta_o > 1$**

- **The modeler's (initial condition) challenge**

- **two different instabilities & growth trends**

low η_o

→ as $\eta_o \uparrow$ *enstrophy* $\uparrow$ *isotropy* $\uparrow$ *TKE* $\uparrow$ $\delta \sim t \uparrow$ ALL GROW with η_o

high η_o

→ as $\eta_o \uparrow$ *enstrophy* $\uparrow$ *isotropy* $\uparrow$ GROW with η_o

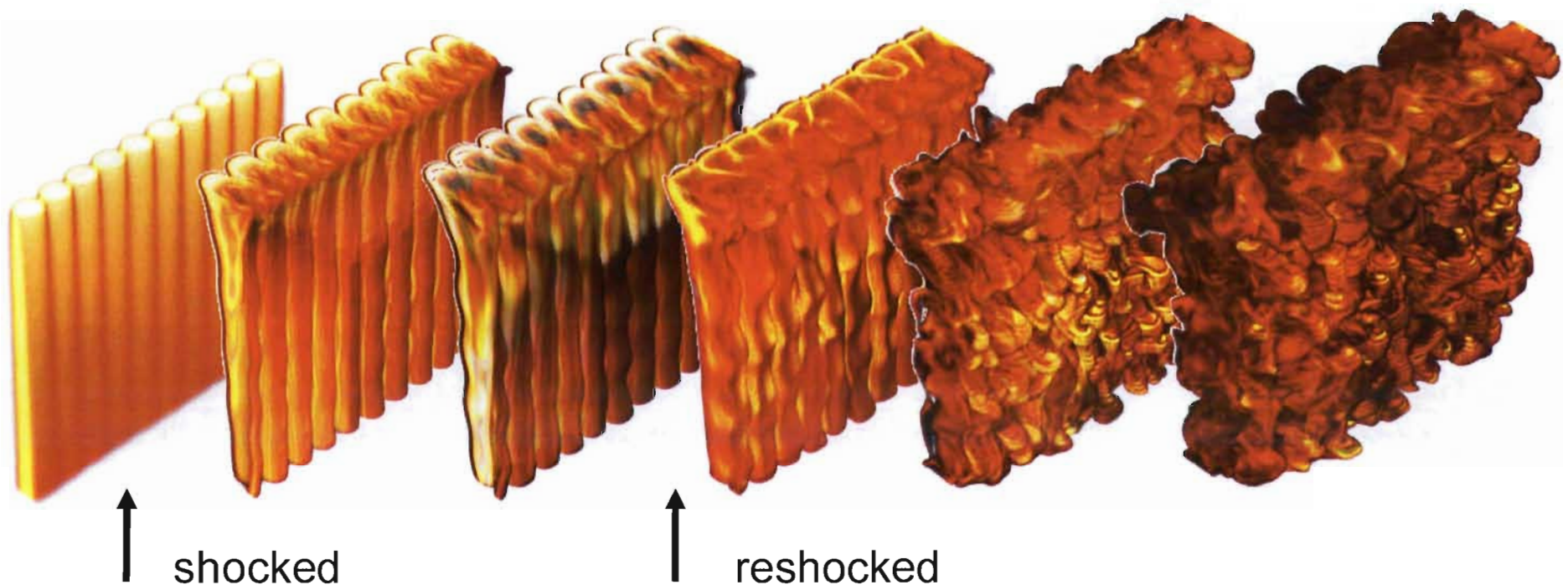
TKE $\downarrow$ $\delta \sim t^{1/2} \downarrow$ DECREASE with η_o

possible first "generalization": $\eta_o \rightarrow \eta_o A Ma$

RAGE Simulations of Shocked (two-interface) Gas-Curtains

Gowardhan & Grinstein, JoT 2011, under review

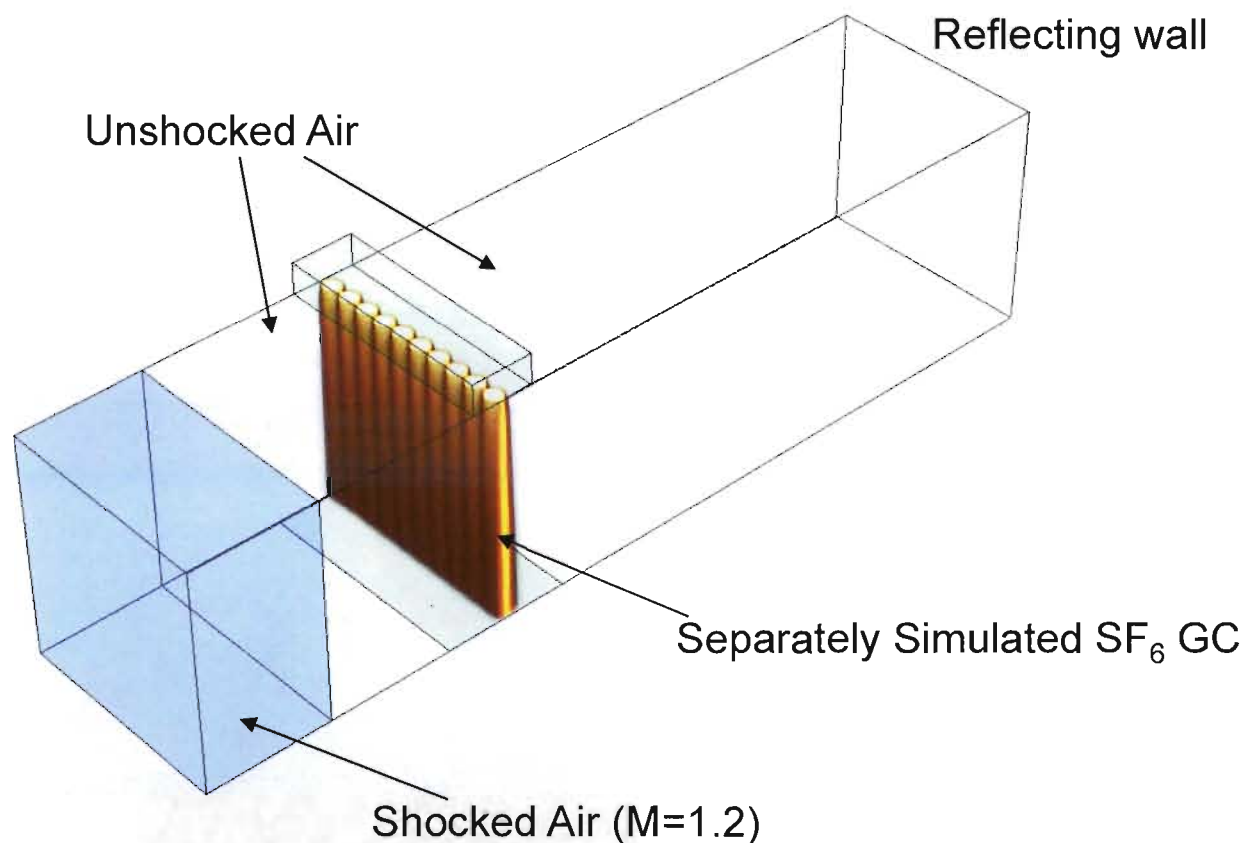
Thanks to K. Prestridge, S. Balasubramanian, B.J. Balakumar (P-23, LANL)
for stimulating discussions and for sharing information and data from their experiments.



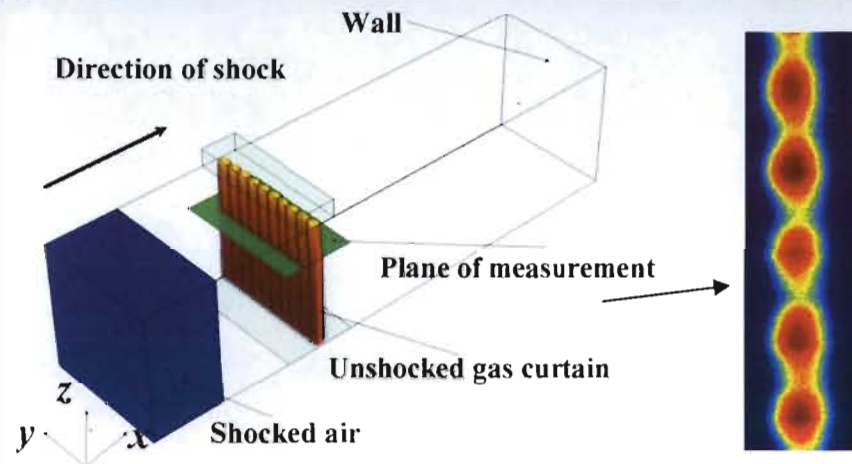
- Initial 3D GC characterization and modeling
- Sensitivity of turbulence characteristics to ICs
- Data reduction and bipolar RM behavior

Shocked Gas Curtain

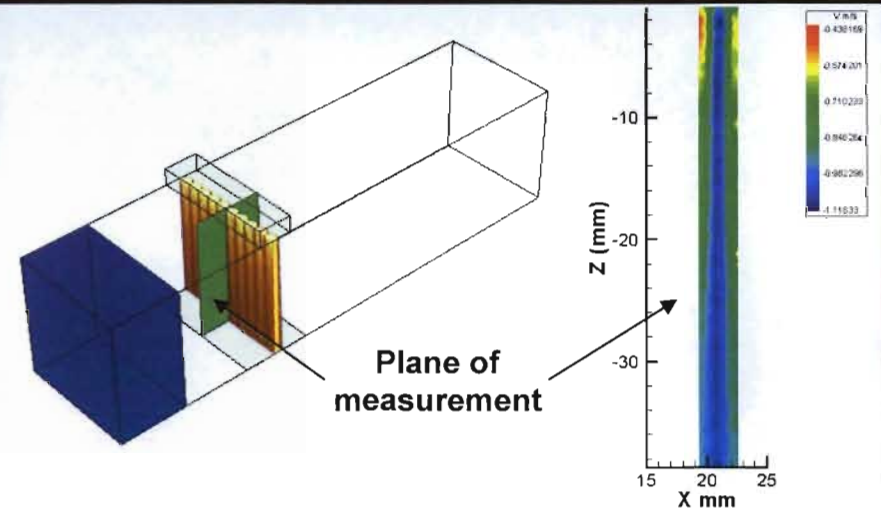
ILES RAGE simulations – SF_6 mass fraction distributions



Initial GC Characterization ...



2D *PLIF* SF_6 intensities (C / C_{max}) in a horizontal plane 2 cm from nozzle exits



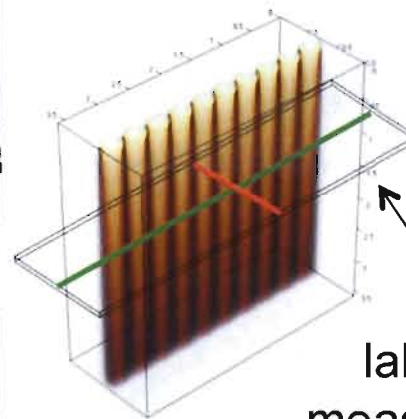
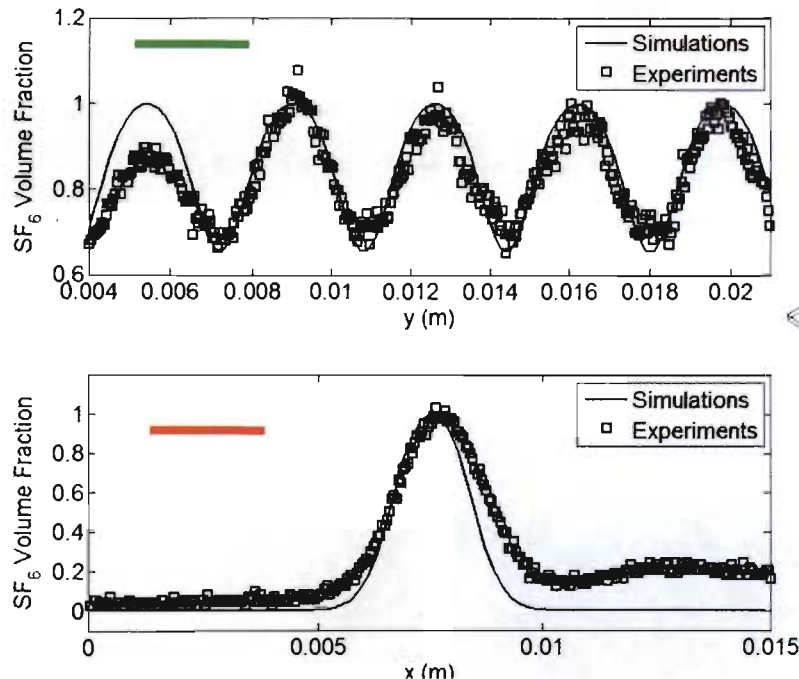
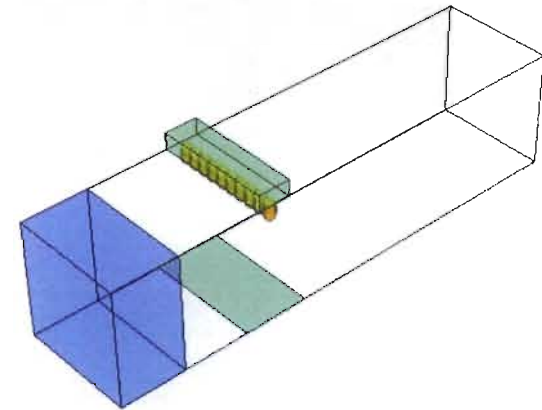
Vertical PIV @ center of GC, gives estimates of nozzle exit velocity (~ 100 cm/sec)

- Composition & fluctuations of SF_6 mixture at nozzle exits only estimated
50-80% SF_6 – rest Acetone (used as a tracer for PLIF), and air;
- Uncharacterized co-flow and bottom suction used to stabilize the GC

P-23 lab info insufficient to fully characterize
3D initial GC conditions for *RAGE* simulations

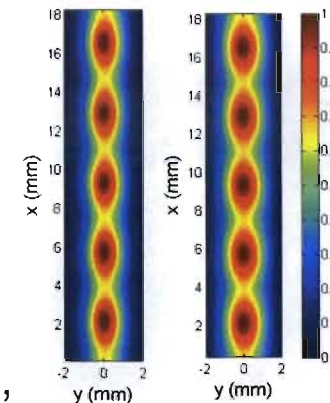
Simulated 3D Gas Curtain → Initial Conditions for RAGE

- separate laminar NS-Boussinesq simulation of SF_6 falling through nozzle arrangement
- available info from lab. expts. used to constrain 3D GC simulation
- no coflow, advective downstream BC
- 75% SF_6 – air (no acetone) at nozzle exits

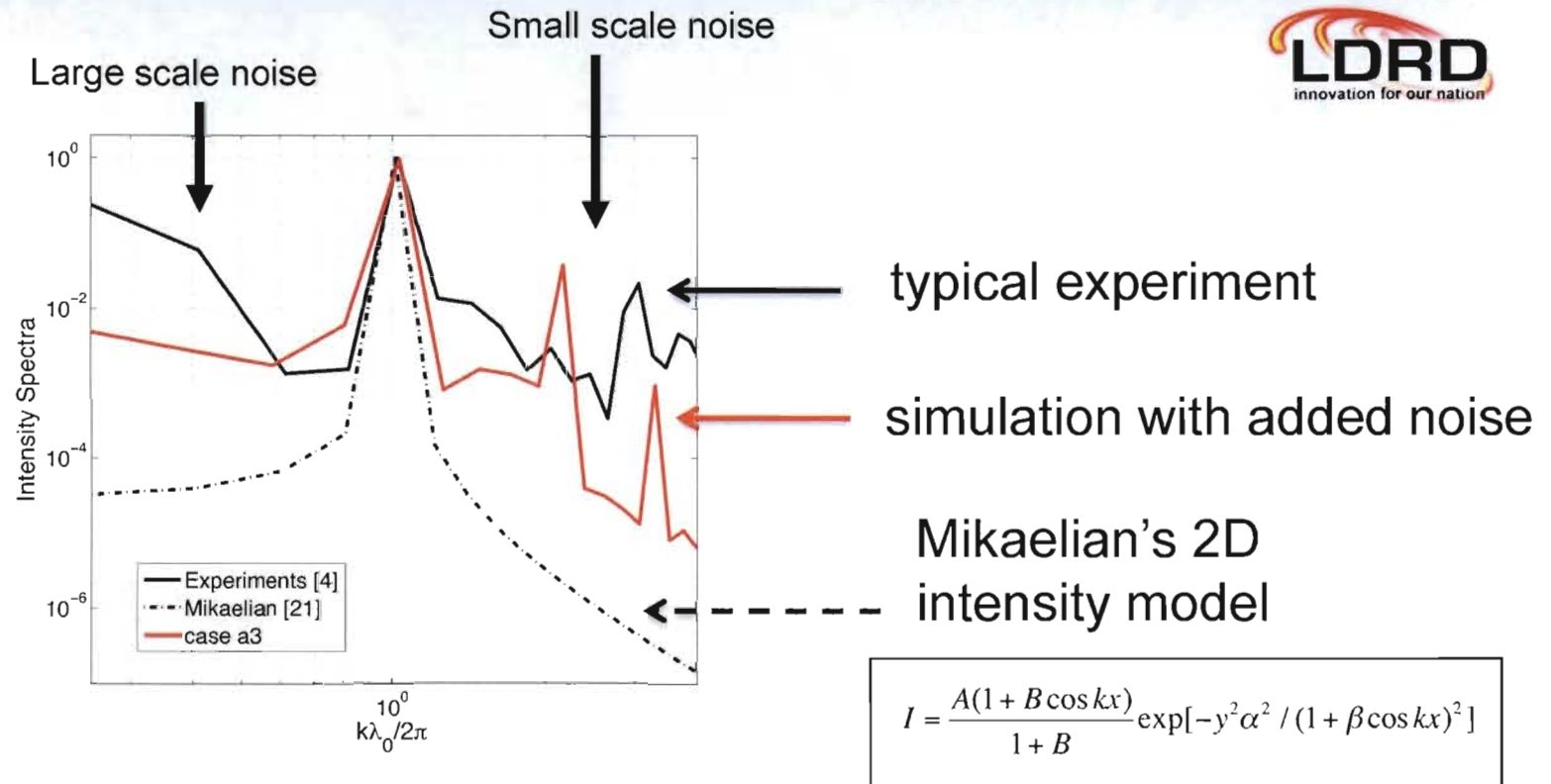


laboratory
measurements'
plane

Simulations Expts.



Initial Mass-Density Variance Spectra



Mass-density variance spectra of initial GC data indicates presence of *small* and *large* scale modes, in addition to 2D Mikaelian's dominant mode ...

To mimic the noise present in the experiments, nozzle offsets and/or SF₆ concentration perturbations were added to baseline simulated GC

3D simulated GC “noise” (Initial Conditions for RAGE)

Large scale perturbation: Achieved by slightly offsetting (randomly, $<0.05R$) the nozzles in the shock direction

Small scale perturbation: Achieved by adding multimode 3D concentration perturbation (s.d. $\sim 2\%$) to baseline 3D GC

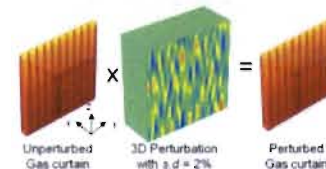
a0: no perturbation (baseline)



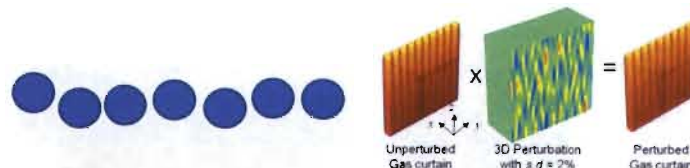
a1: nozzle offset



a2: 3D concentration perturb.



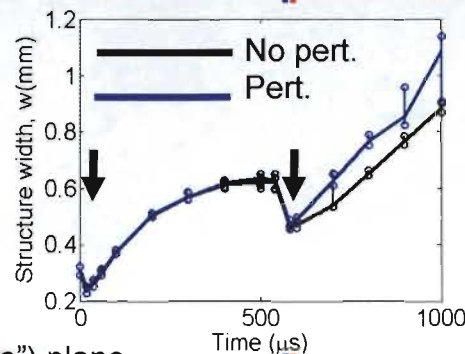
a3: nozzle offset and 3D conc. Perturb.



ILES RAGE of Shocked SF_6 Gas Curtain

Multi-mode IC Effects on Mixing & Transition

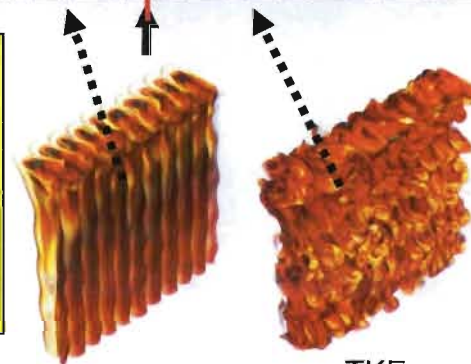
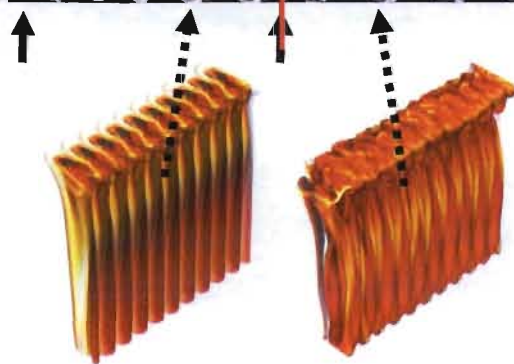
non-perturbed GC
“ballistic” growth dominates



Gowardhan & Grinstein, JoT (2011), under review

multi-mode perturbed GC
mode-coupling promoted

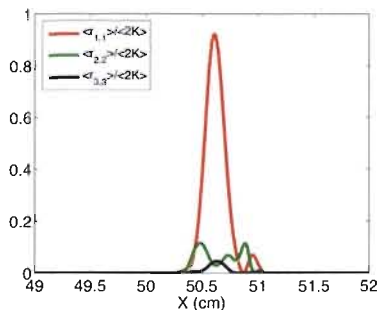
visualizations at horizontal (“measurements”) plane



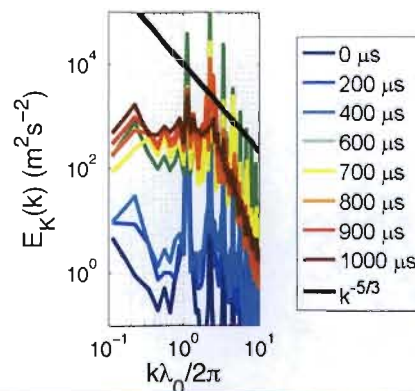
**perturbed GC “transitions”
after reshock**

- enhanced mixing
- more isotropic (late times)
- self-similar decay spectra

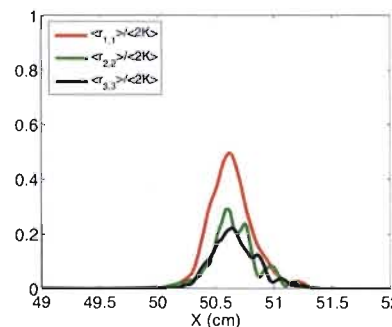
velocity variances @ $t=1000\mu\text{s}$



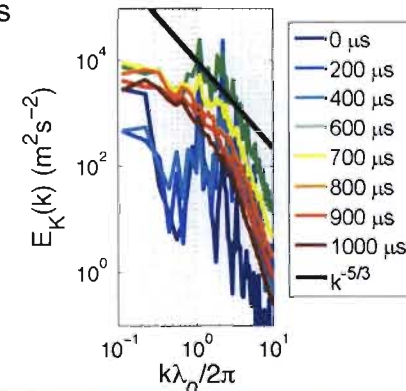
TKE spectra



velocity variances @ $t=1000\mu\text{s}$

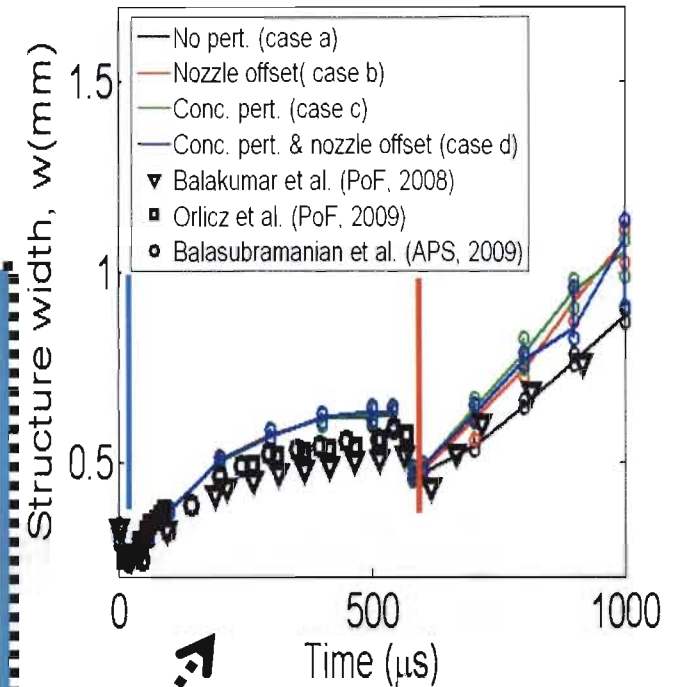
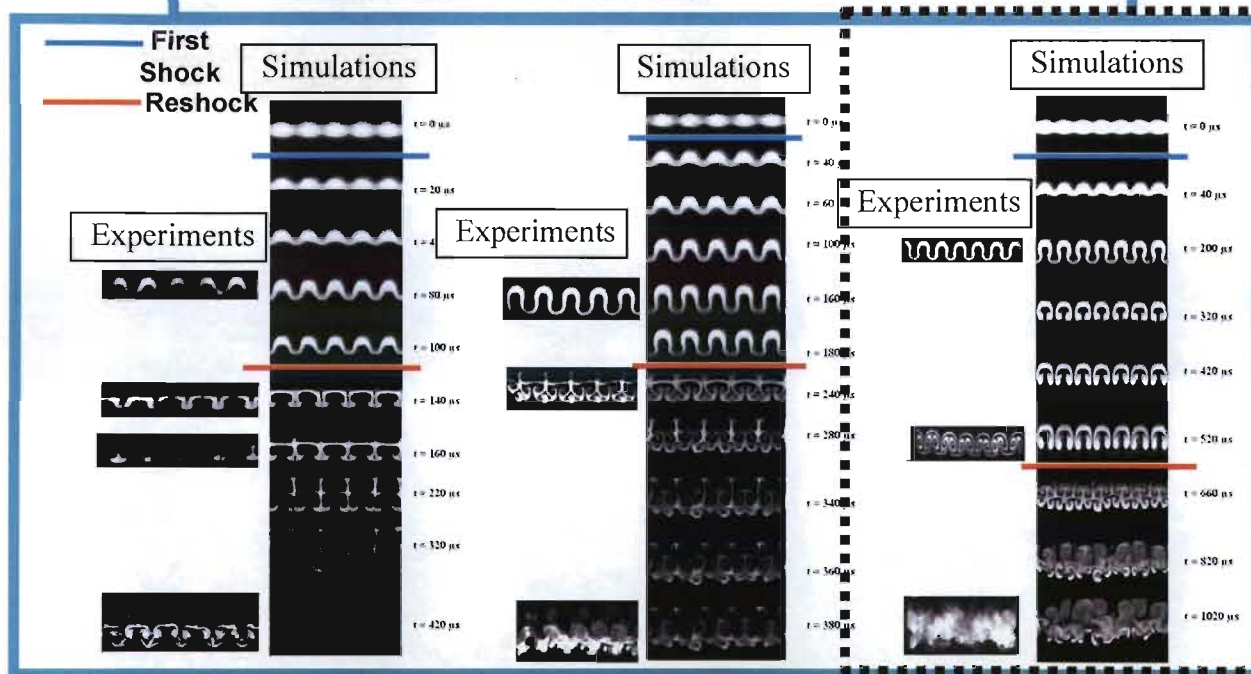
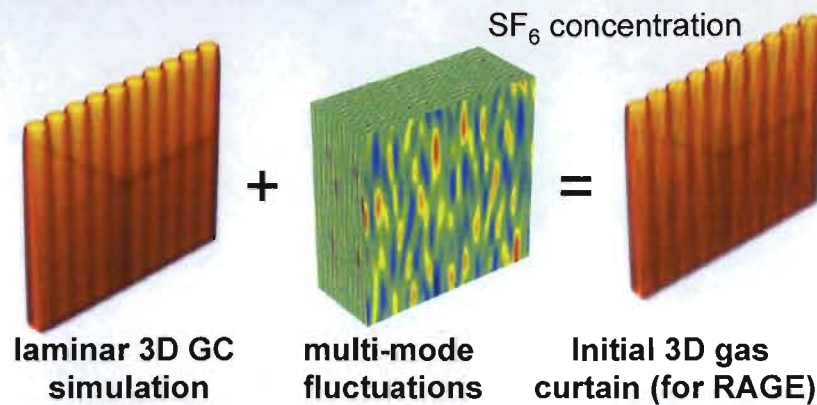


TKE spectra



ILES of Shocked SF_6 GC vs. Expts.

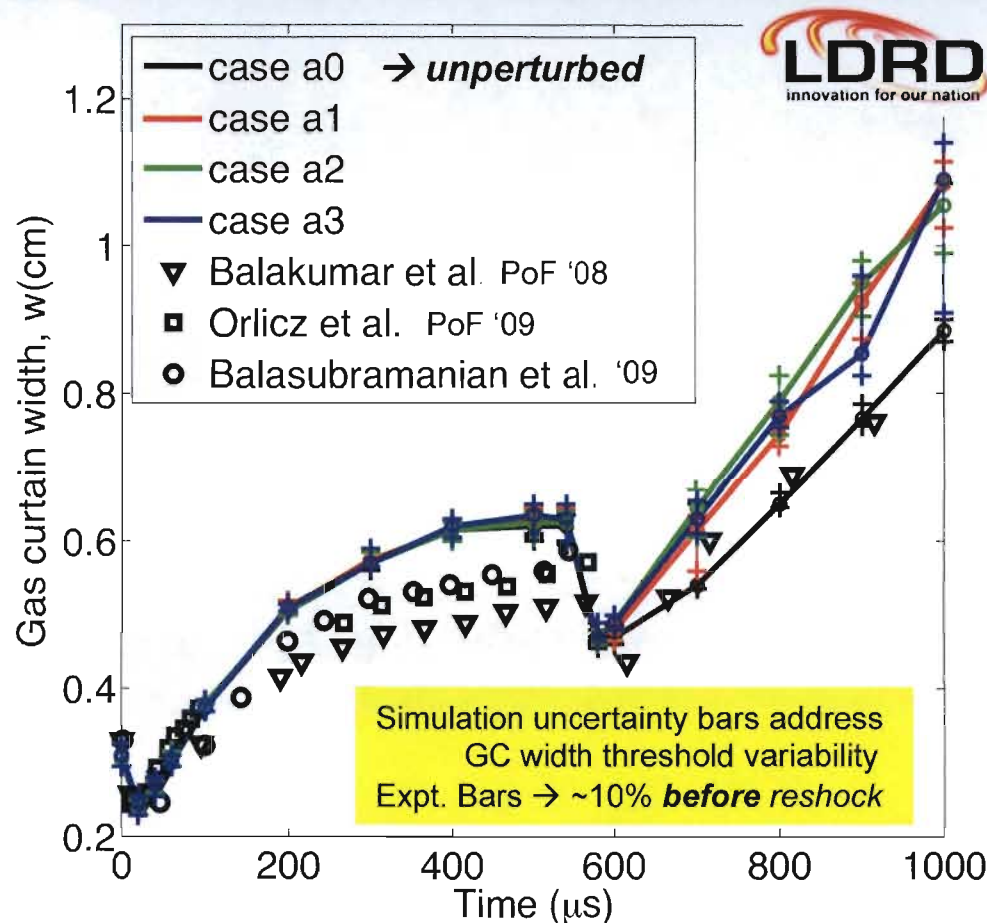
Gowardhan, Balasubramanian, Grinstein, Prestridge, AIAA Paper 2011



**Robust agreement with lab. flow patterns and growth rates before reshock
but sensitive to ICs after reshock !
over-predicted early growth reflects lower effective Atwood number in expts.**

GC Width: Simulations vs. Expts.

Gowardhan, Balasubramanian, Grinstein, Prestridge, AIAA Paper 2011



GC width is defined as shockwise distance over which $\chi(x) > \chi_h$ based on a selected threshold $\chi_h \sim 0.95$, where $\chi(x) = 4\zeta(x)(1 - \zeta(x))$, and

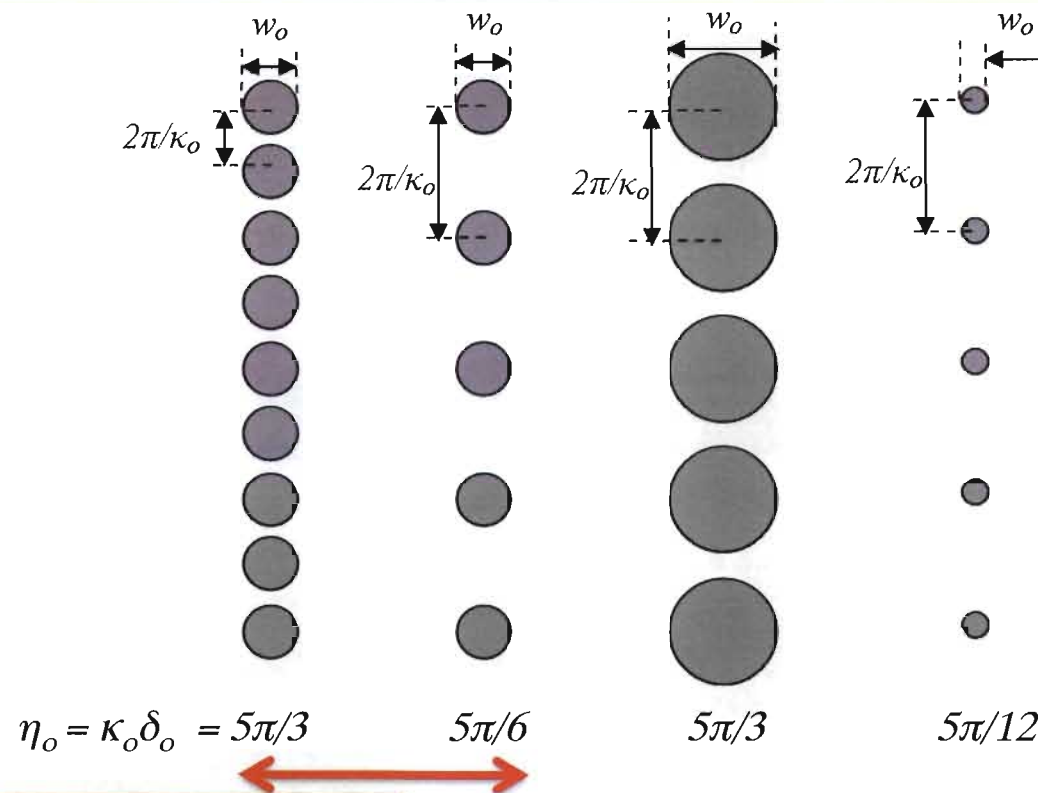
$$\zeta(x) = \frac{1}{L_y} \int_0^{L_y} \left(\frac{\rho_{SF_6}(x, y, z=2)}{\rho(x, y, z=2)} \right) dy$$

- Simulated growth qualitatively consistent with P-23 experiments
- **Before reshock**, GC widths for all simulations are in close agreement; discrepancies with expts. mainly attributed to **different SF_6 (air, and acetone) mixtures** in initial GCs
- **After reshock**, GC width growth rates are consistent but, **“perturbed” $\neq$ “non-perturbed”** → **very sensitive to ICs and consequent interface conditions** at reshock time

Characterizing Reshock effects
difficult for Expts. and LES !

Data Reduction in Shocked GC (before reshock)

- IC parameterization & additional GC cases
 - Data reduction to compare results associated with different ICs
 - Bipolar RM behavior also for the shocked GC ?

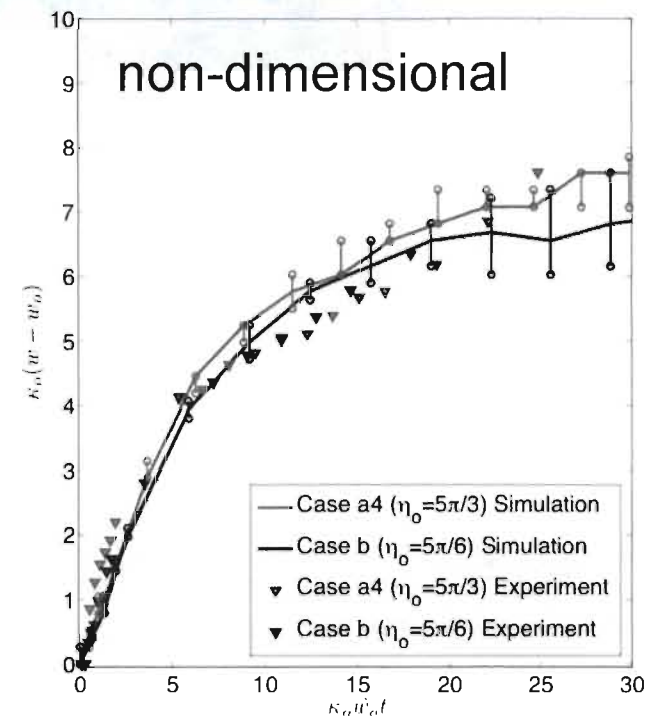
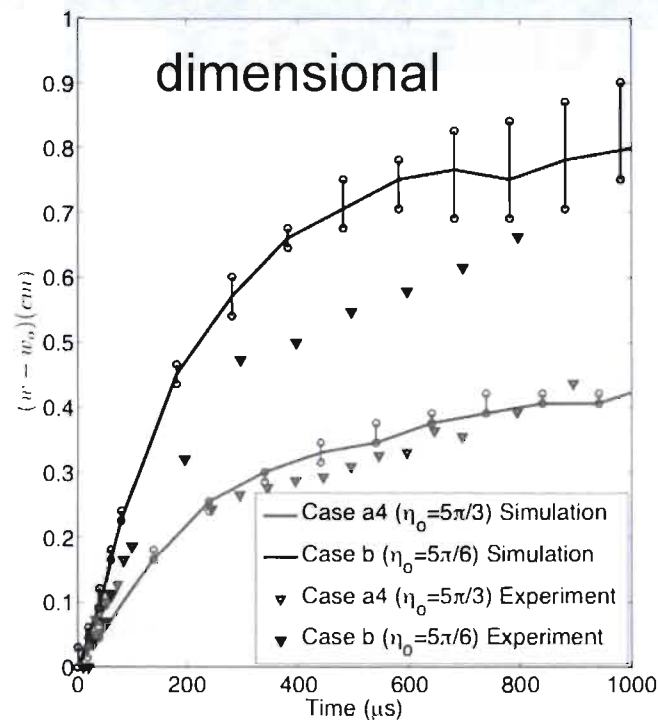
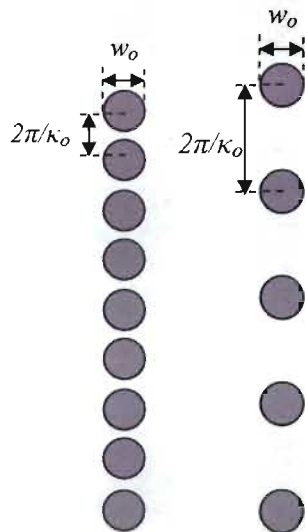


lab. expts. available only
for these two cases

RM Behavior in Shocked GCs (simulations & expts., no reshock)

Gowardhan, Balasubramanian, Grinstein, Prestridge, AIAA Paper 2011

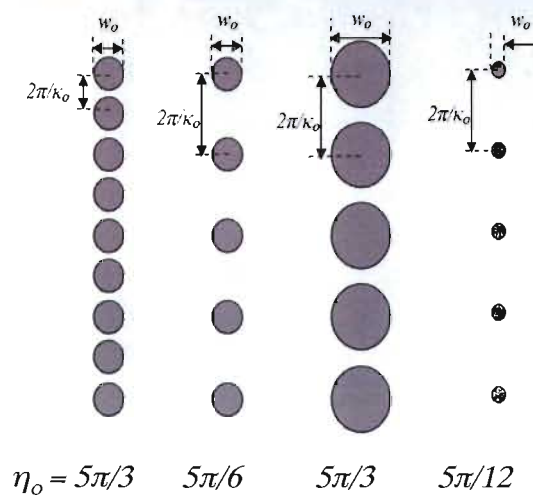
$$\eta_o = \kappa_o \delta_o = 5\pi/3 \quad 5\pi/6$$



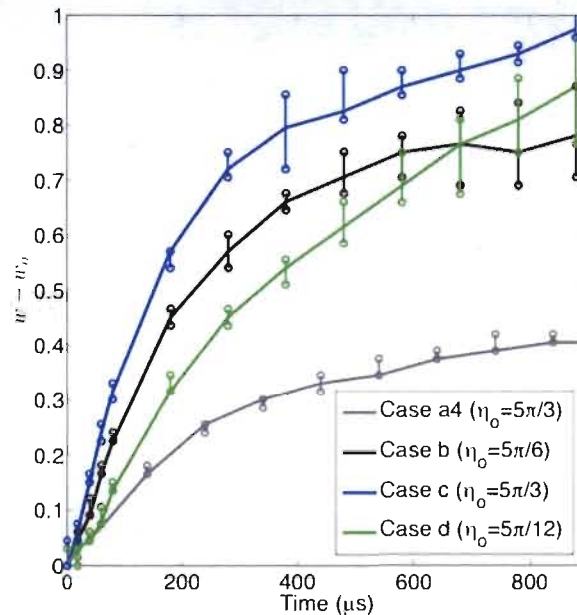
- **Non-dimensionalized results compare well for both GC cases**
- GC widths scaled with κ_o ; time scaled with **actual** initial width growth rates (*first proposed by Jacobs et al. 1996*)
→ **curves collapse well in a “non-linear” ($\sim t^{1/2}$) group**

Bipolar RM Behavior in Shocked GCs (simulations, no reshock)

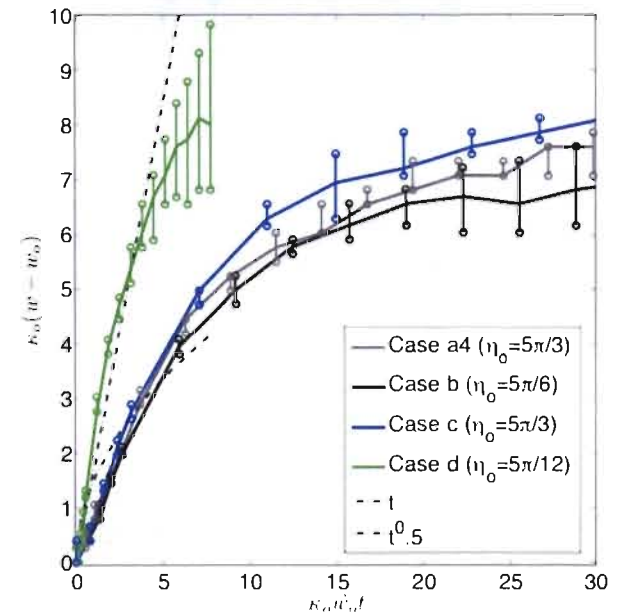
Gowardhan and Grinstein, JoT 2011, under review



dimensional



non-dimensional



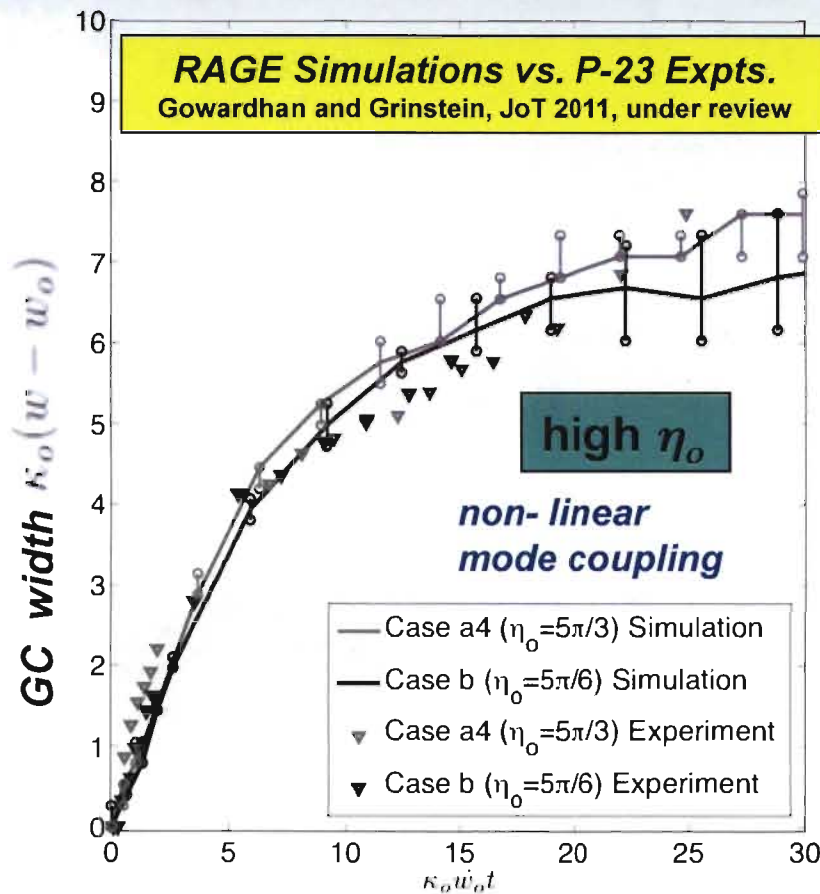
When simulated results are plotted in non-dimensional form

- cases with $\eta_0 > \pi/2$ collapse in “non linear” group,
- case with $\eta_0 < \pi/2$ falls on “linear” group

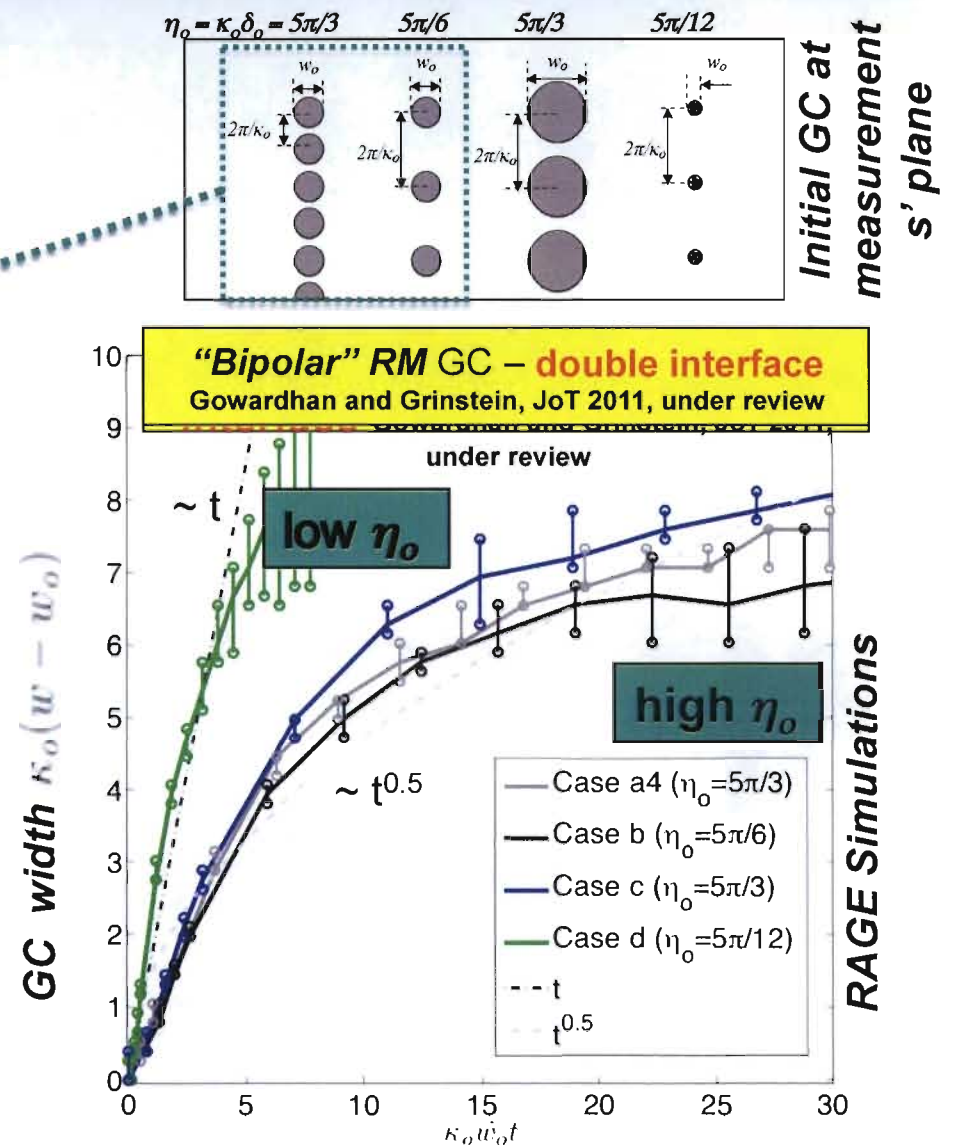
This demonstrates the bipolar RM behavior also for shocked GC

Bipolar RM also demonstrated for shocked GC

GC test case ? Initial 3D GC conditions available ...



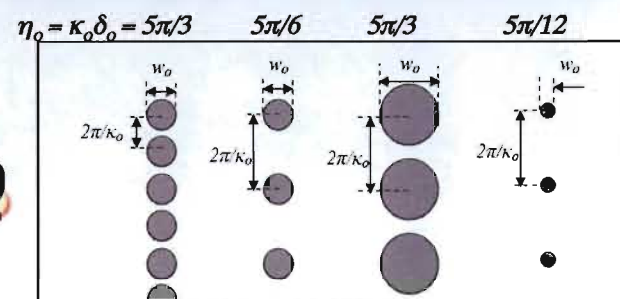
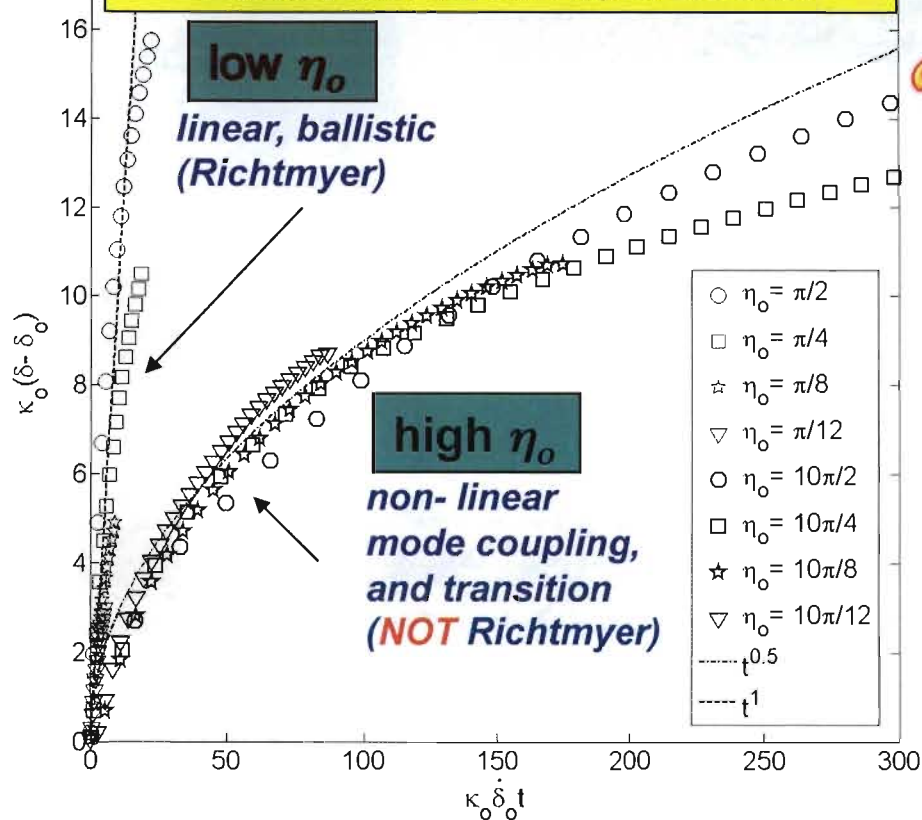
- **Modeler's Initial Condition Challenge:**
different instabilities,
growth trends,
late-time characteristics
- **Instability behavior switches for $\eta_o \sim 1$**



Bipolar RM behavior also demonstrated in terms of single IC parameter η_o for shocked GCs

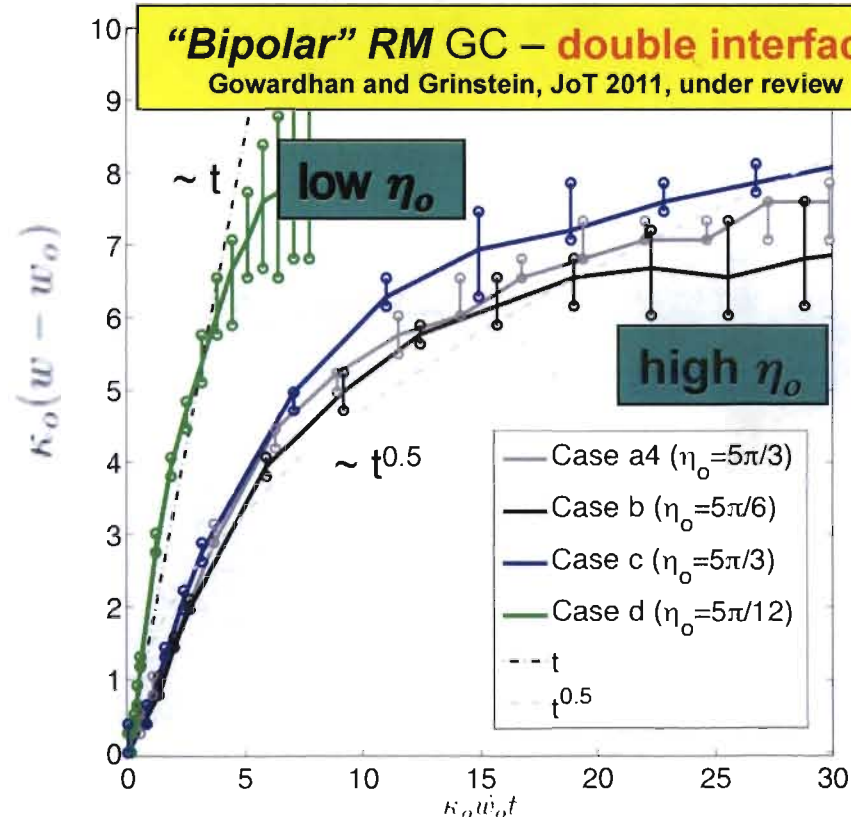
"Bipolar" RM – single interface

Gowardhan, Ristorcelli, Grinstein, PoF Letters 2011



"Bipolar" RM GC – double interface

Gowardhan and Grinstein, JoT 2011, under review



- **Modeler's Initial Condition Challenge:** different instabilities, growth trends, late-time characteristics
- Instability behavior switches for $\eta_o \sim 1$

ILES-RAGE of Shocked GC

Main Conclusions

**Simulated initial 3D GC (constrained by lab. data)
+ fluctuations $\rightarrow$ ICs for ILES RAGE**



Effective GC width data reduction (*before reshock*) with single parameter

- robust agreement with expts. (despite IC uncertainties)
(opportunities for defining RM test case)
- bipolar behavior demonstrated for double-interface RM
(a possible first “generalization” might involve: $\eta_o \rightarrow \eta_o A Ma$)
- RM behavior switches for $h_o \sim 1$ (as in planar case)
 - low- h_o : linear, ballistic, GC width $\sim t$
 - high- h_o : non-linear, mode coupling, GC width $\sim t^{1/2}$

Outstanding Challenge for Experiments and LES (ILES)
(high- η_o) IC characterization (data-reduction) at reshock time