



New  
approaches to  
solve the  
meshing  
problem

M. S. Ebeida  
S. A. Mitchell

Intro

Exist. All Hex

Our All-Hex

# New approaches to solve the meshing problem

M. S. Ebeida and S. A. Mitchell

Computing Research, Sandia National Laboratories

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# Collaborators

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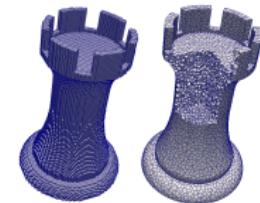
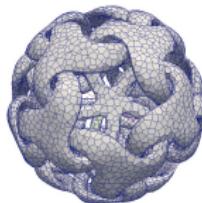
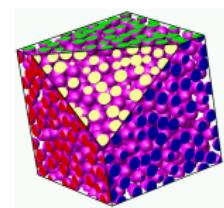
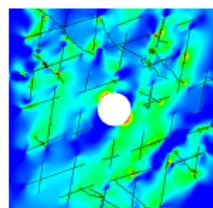
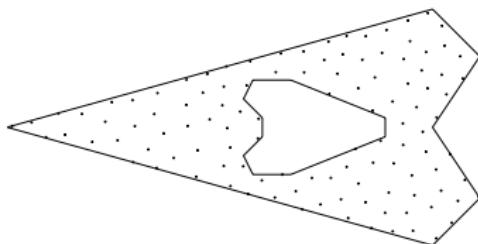
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## SNL

- P. M. Knupp
- V. J. Leung.
- J. E. Bishop
- M. J. Martinez

## UCDavis:

- A. Patney
- A. Davidson
- J. D. Owens





# Overview

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## 1 Introduction

## 2 Automatic All-Hex Meshing

## 3 Our new automatic method for all hex meshing



# General Principles in Our Meshing Algorithms

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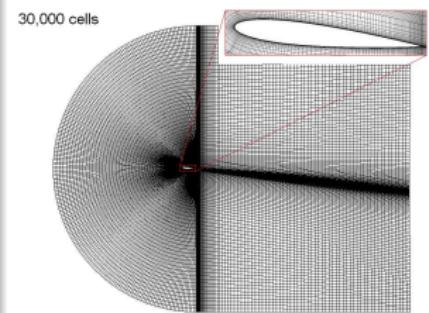
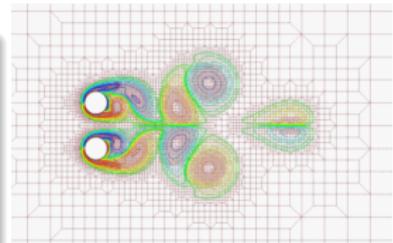
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## Quality

- Point Clouds should adequately represent the associated geometry and physics.
- Extra points needed to improve quality / maintain certain connectivity should be kept at a minimum level.
- Moving points to non-deterministic locations should also be avoided for generating a provably good mesh.



NACA0012 Image courtesy of  
<http://www.cfd-online.com>



# General Principles in Our Meshing Algorithms

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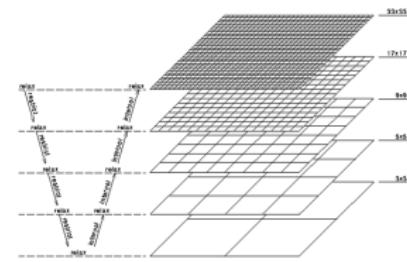
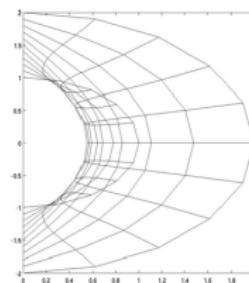
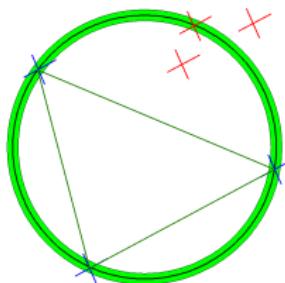
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Efficiency, robustness and ... Multi-Grid!

- Local meshing operations is easier for parallel applications
- Provable robustness (meshing failure is NOT ACCEPTABLE in dynamic simulations).
- Meshing Operations should have minimum storage requirement.
- Geometric MG need to be considered.





# Existing Methods: Domain Decomposition

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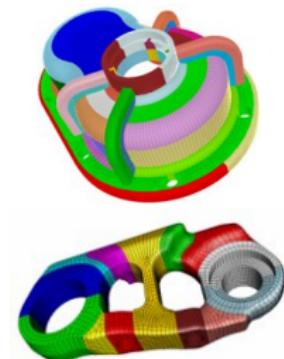
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## Pros

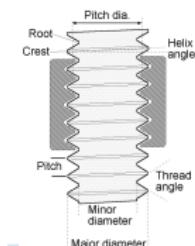
- High Quality.
- Complex geometries.
- Domains with multiple material.

## Cons:

- Requires a lot of manual operations.
- Quality is not predicted.
- Number of regions in contact is limited.
- Retrieving a solution can be a challenging / time consuming process.



Images courtesy of  
<http://cubit.sandia.gov/>





# Existing Methods: Octree-based (projection)

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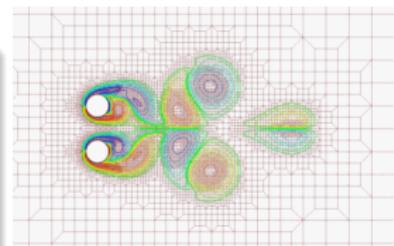
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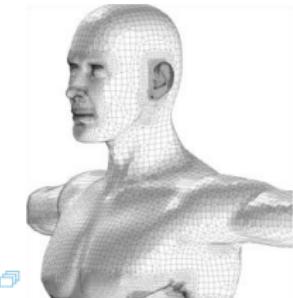
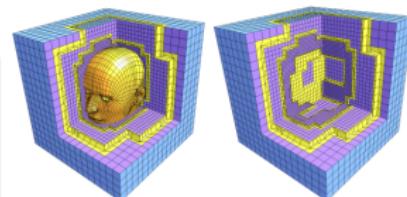
## Pros

- Guaranteed quality
- Dynamic remeshing.
- Multigrid.



## Cons:

- Domains with a single material only.
- Sharp Features may result in invalid elements.
- Sharp Features cannot be even represented
- Conforming refinement requires some propagation.





# Existing Methods: Dual Contouring

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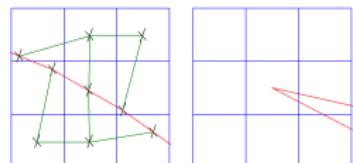
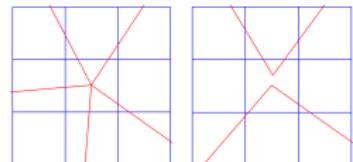
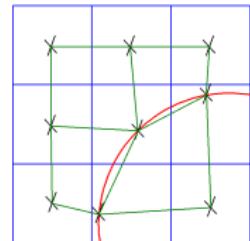
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## Pros

- Bounded radius for inscribed circles.
- Handles Multiple domains ?!

## Cons:

- Not robust.
- Captures input geometry using uniform grids
- Sharp Features represent a BIG issue
- Narrow regions increase the output size significantly
- Invalid/low quality elements are generated even for some extremely nice geometries.





# All-hex meshing: Main issues

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- Robust Automatic algorithm.
- Conforming Refinement THEN capturing geometry.
- Generation of boundary layers
- Guaranteed quality.
- Adequate mesh size.
- Handling of non-manifold surfaces.

... Challenging Problems usually require a new Language!



# Our All-hex meshing: The Alphabets

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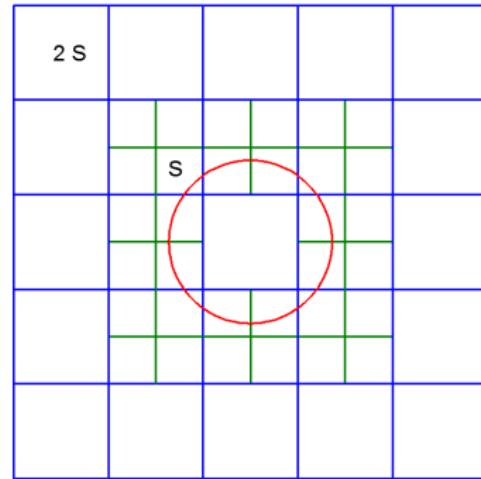
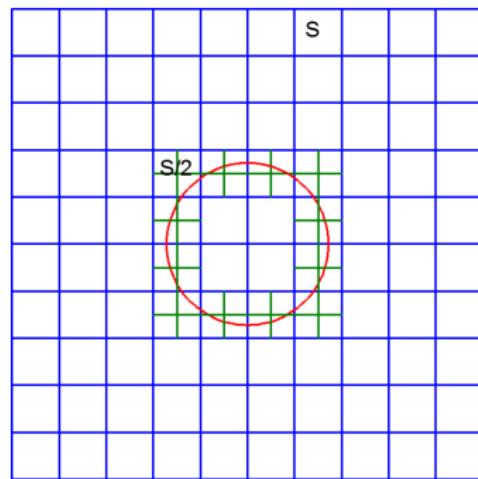
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1. Refinement of all elements in a grid based method is not a bad idea.





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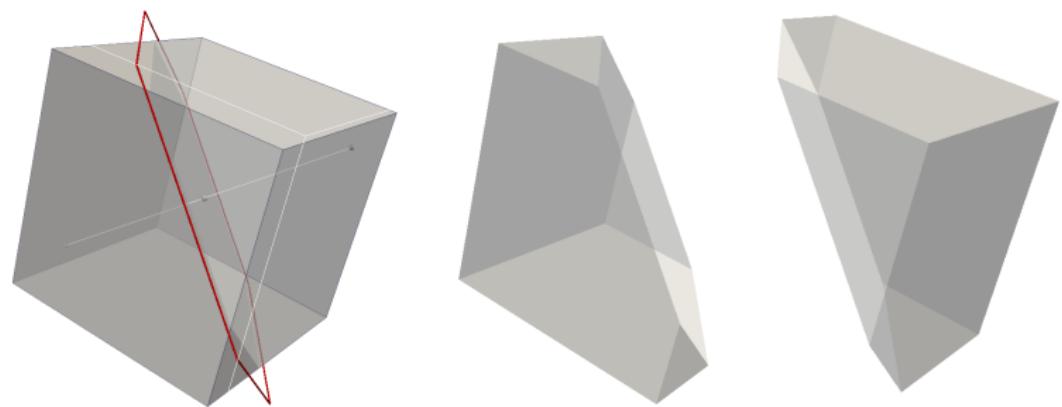
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2. Clipping of a region with tri-valent corners using a surface that does not pass through any of these corners will result in two region with tri-valent corners.





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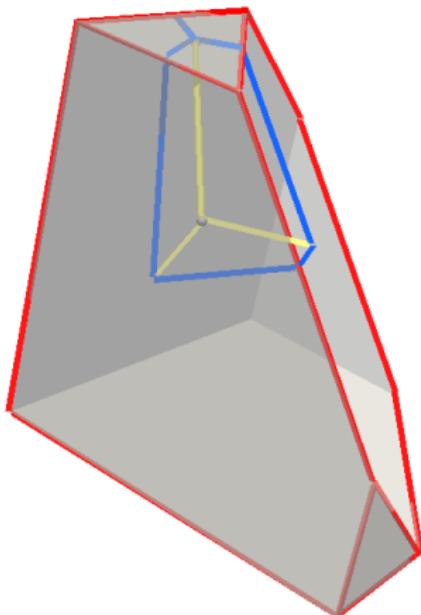
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3. Refinement of a region with tri-valent corners result in all-hex regions with an automatic generation of a boundary layer



- ➊ Split each edge, add a face point to each face and a region point.
- ➋ A Region point: 3 face points
- ➌ A face point: 2 edge points and region point
- ➍ An edge point: 2 face points and a corner
- ➎ A corner: 3 edge points



# Our All-hex meshing: Representing two manifold smooth surfaces using a uniform grid

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- ① Generate a uniform grid covering the input geometry with an appropriate spacing.
- ② Move grid points “away” from the boundaries.
- ③ Clip the regions intersecting with the geometry.
- ④ Refine all the elements resulting in an All hex mesh.
- ⑤ A boundary layer is generated around the input geometries.



# Our All-hex meshing: The Alphabets

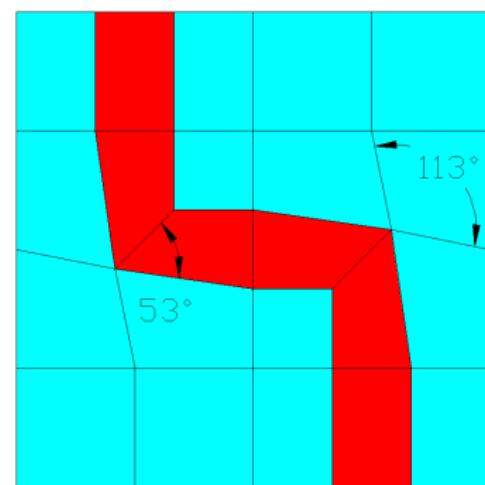
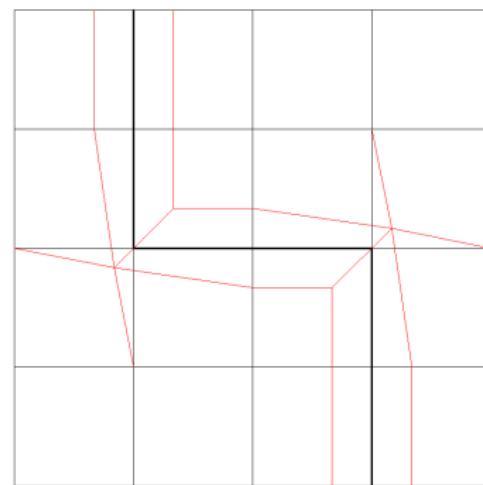
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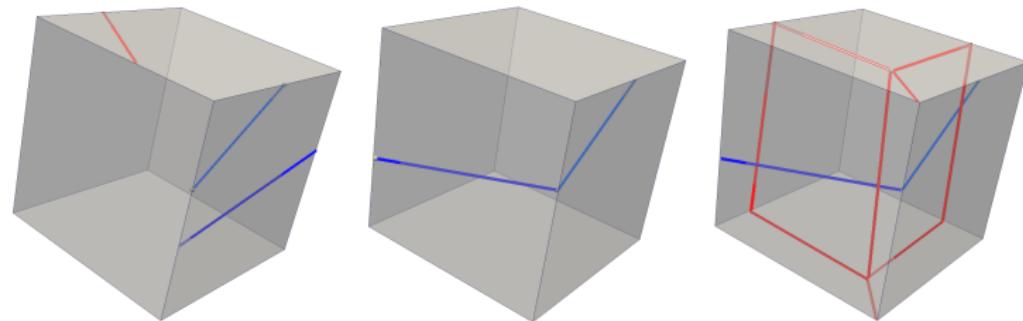
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5a. Edge imprints may / may not result in a tri-valent region:



... sharp features would have edge imprint on some cells.



# Our All-hex meshing: The Alphabets

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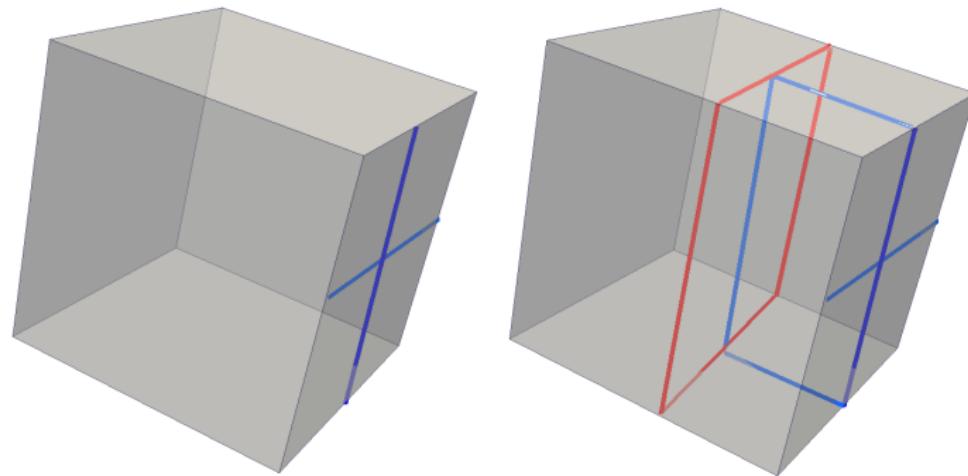
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5b. Edge imprints may / may not result in a tri-valent region:



... and this is how we generate a conforming octree.



# Questions?!

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# Thank you!

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