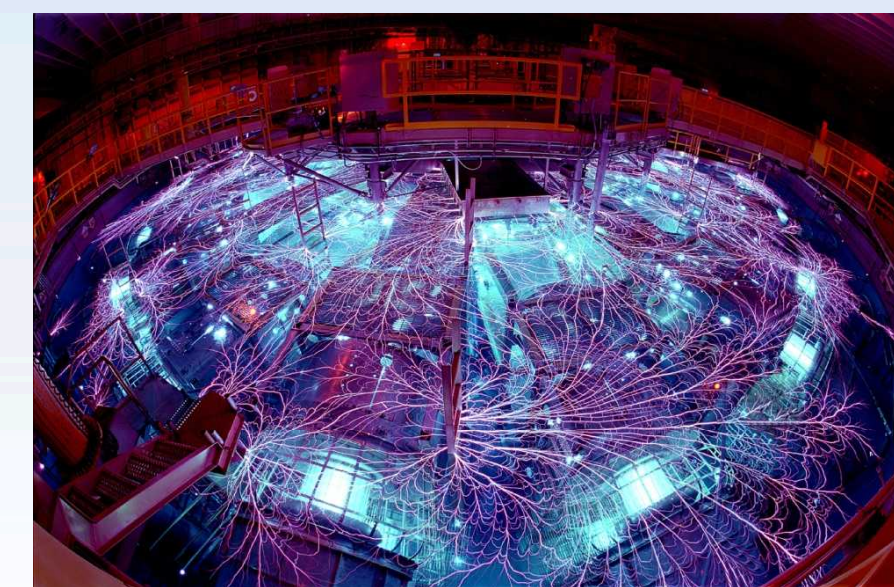
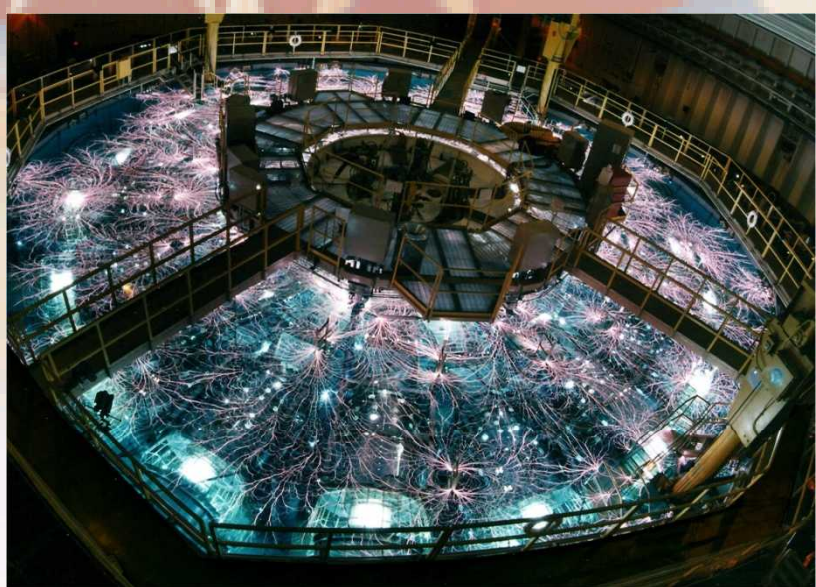


# Liquid Krypton Hugoniot at Megabar Pressures

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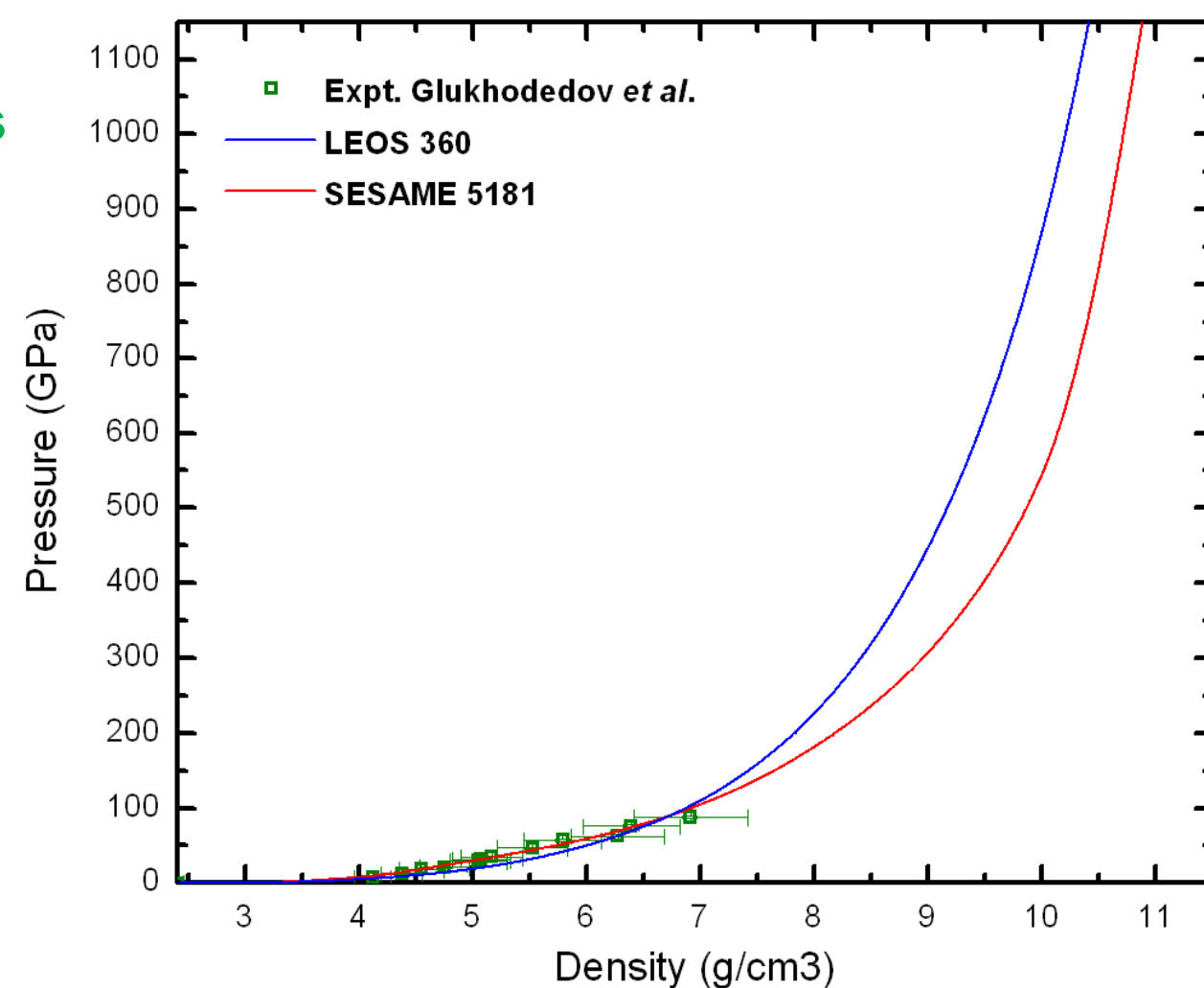
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## Shock Compression of Krypton

• Krypton is a model element to study high pressure effects on filled-shell electron configurations

- Liquid Kr Hugoniot experimentally determined to 100 GPa
- Current EOS tables show good agreement below 100 GPa
- EOS tables diverge above experimental data



### Objectives

- Use Density Functional Theory simulations to calculate the krypton Hugoniot
- Experimentally measure the liquid krypton Hugoniot
- Use the DFT and experimental results to validate an EOS model

## Density Functional Theory

- DFT-MD simulations performed using VASP 5.1.40\*
- Electronic states occupied according to Mermin's finite-temperature formulation
- Projector augmented wave core functions (PAW) potential for core electrons – 8 valence electrons
- Calculate energy and pressure for a given density and finite temperature
- Solve the Hugoniot Condition:  $2(E - E_{ref}) - (P + P_{ref})(v_{ref} - v) = 0$

- Initial conditions:  $\rho_0 = 2.41$  g/cc,  $T_0 = 118$  K, 32 atoms
- LDA and AM05 exchange correlation functionals
- Convergence tested: number of atoms, energy cut off
- Methods demonstrated successfully on Xe, H<sub>2</sub>O, C, quartz

\* G. Kresse and J. Hafner, Phys. Rev. B 47, 558 (1993) and Phys. Rev. B 49, 14251 (1994).

## PAW Potential Improvement

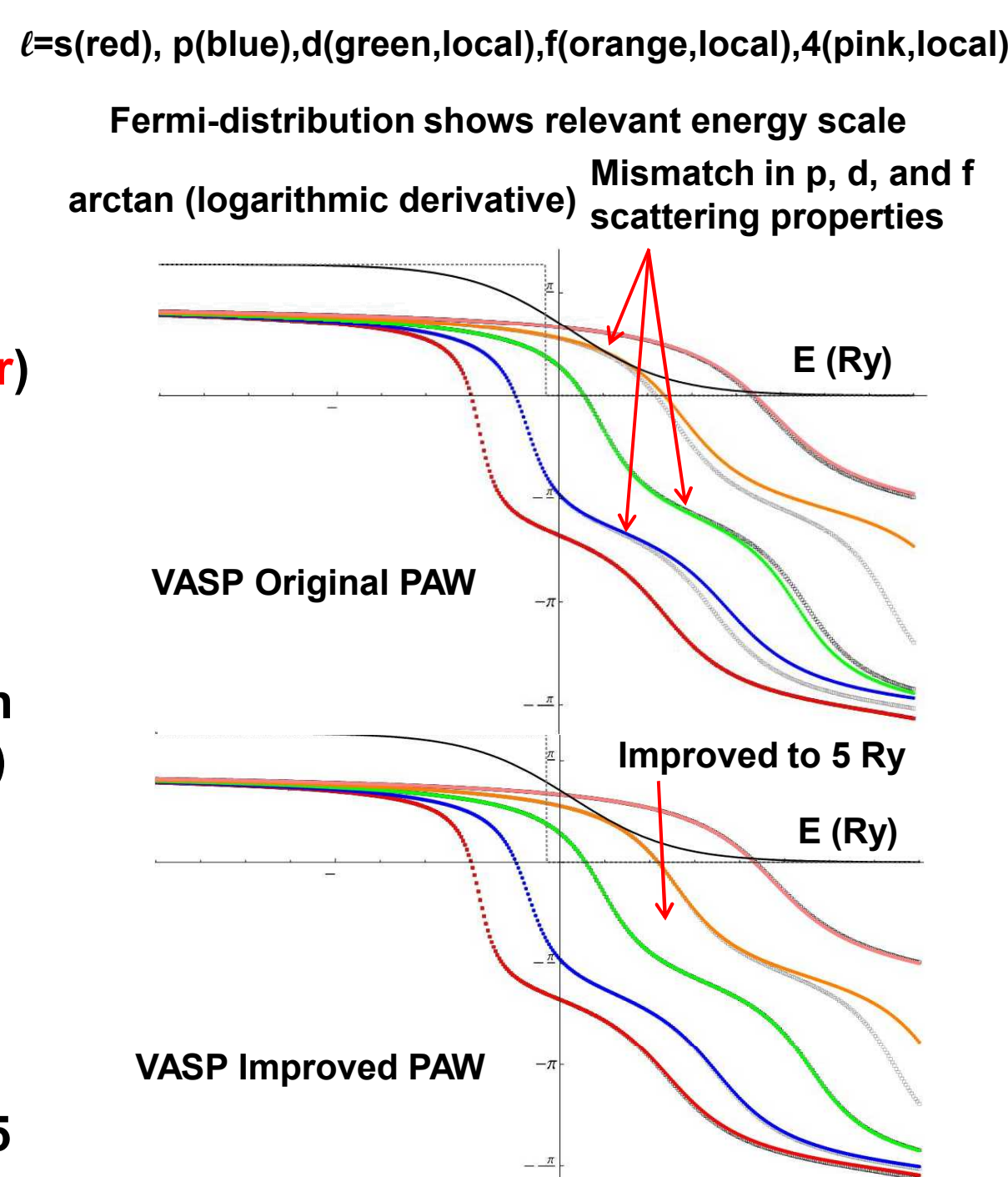
• Scattering properties an issue first discovered in our work on Xe (Root et al., PRL 105, 085501 (2010))

• PAW core potential/function (color) should display same scattering properties as the full electron atom (gray)

• The original VASP 8e PAW is adequate for low T, but mismatch in logarithmic derivative as T (energy) increases

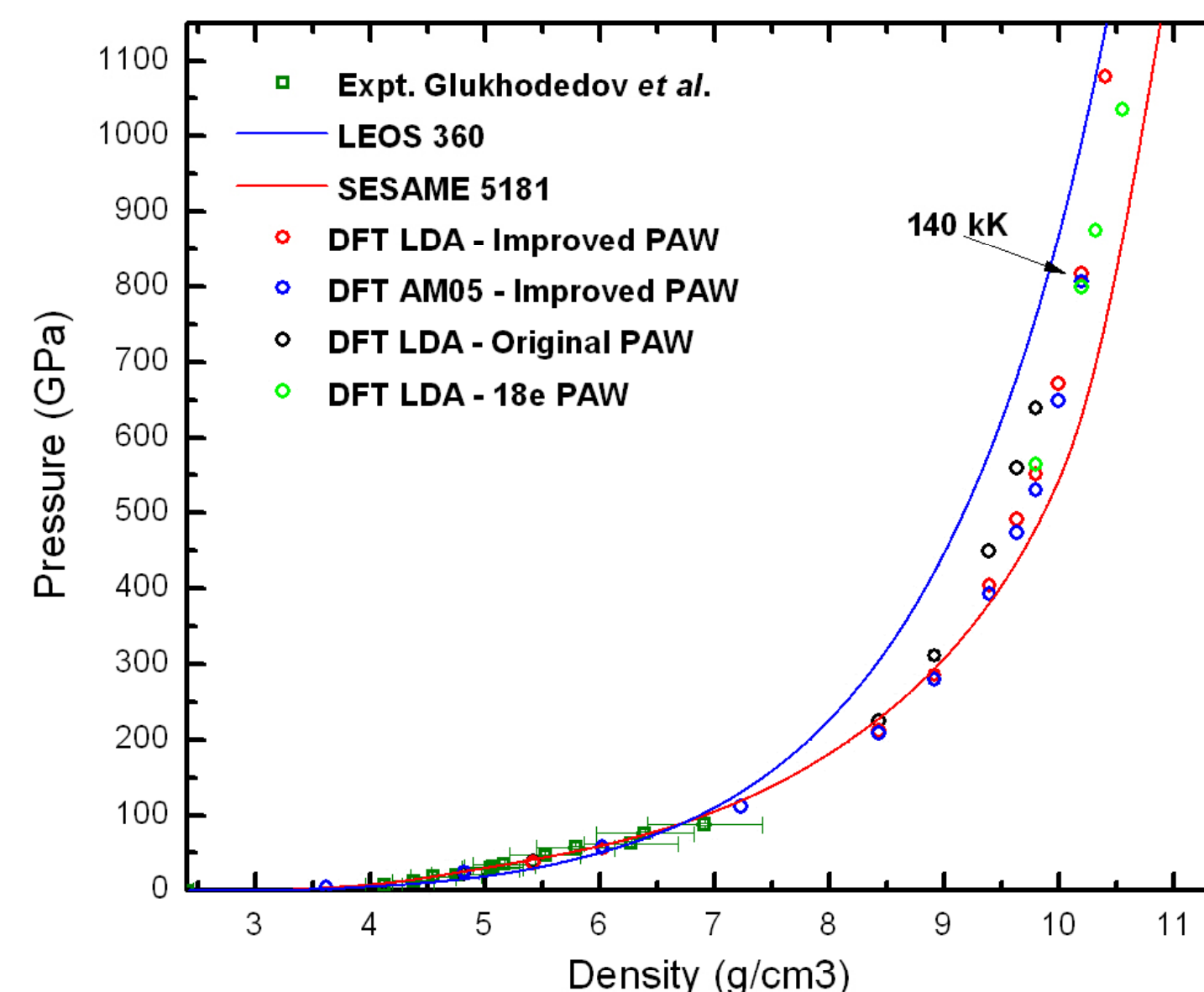
• The improved VASP 8e PAW has improved scattering properties at high energy and temperature

• Matches scattering properties to 5 Ry (68 eV)



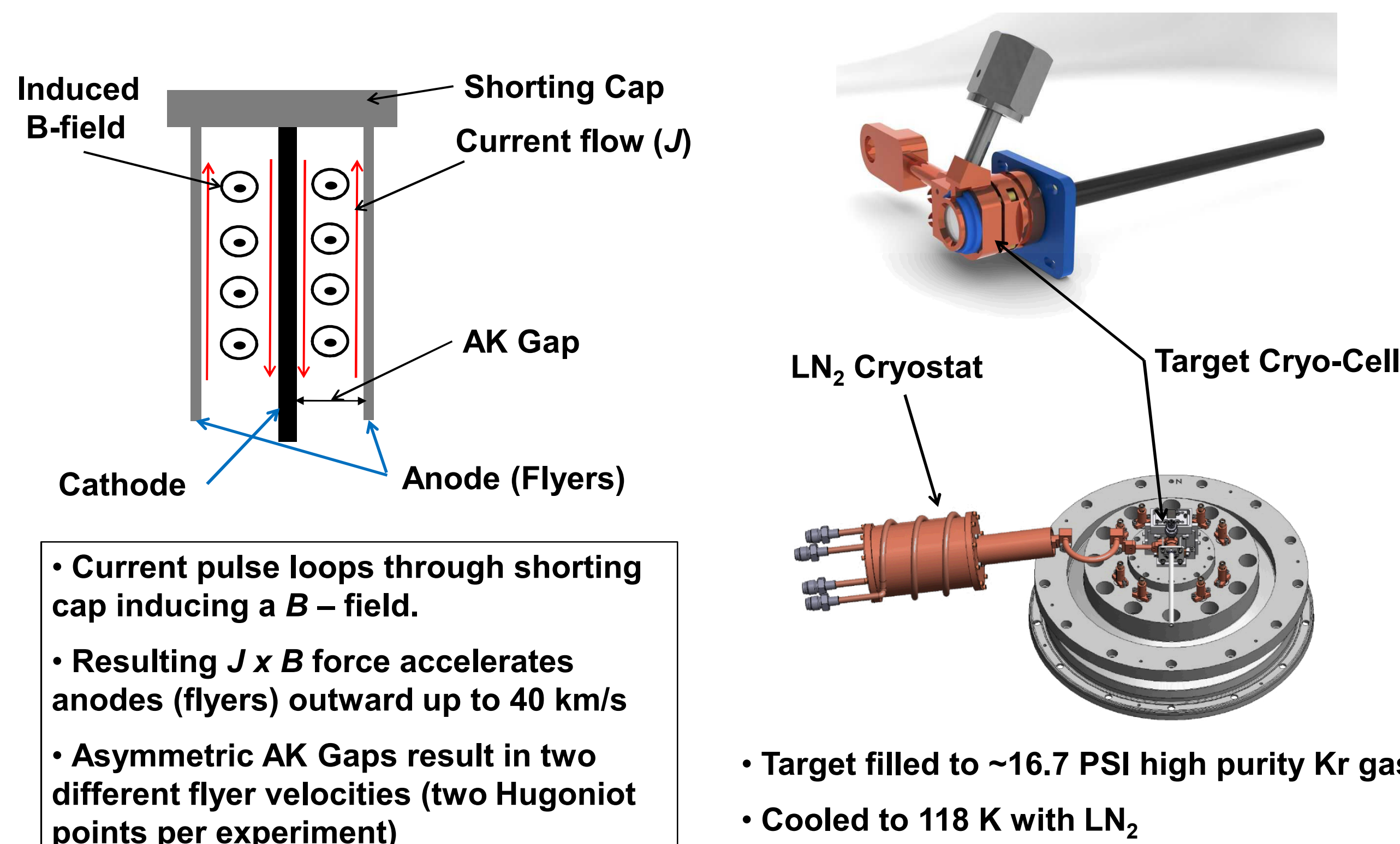
## DFT Results

- DFT Results consistent with experimental Hugoniot data < 1 Mbar
- SESAME 5181 and the DFT results agree up to 4 Mbar
- Original VASP PAW trends stiffer
- At high T the PAW potential for core electrons is incorrect
- Core electrons can be excited out of the potential
- A modified PAW (with 18 valence electrons) developed for high T
- The 18e PAW agrees with the improved 8e PAW results to 8 Mbar

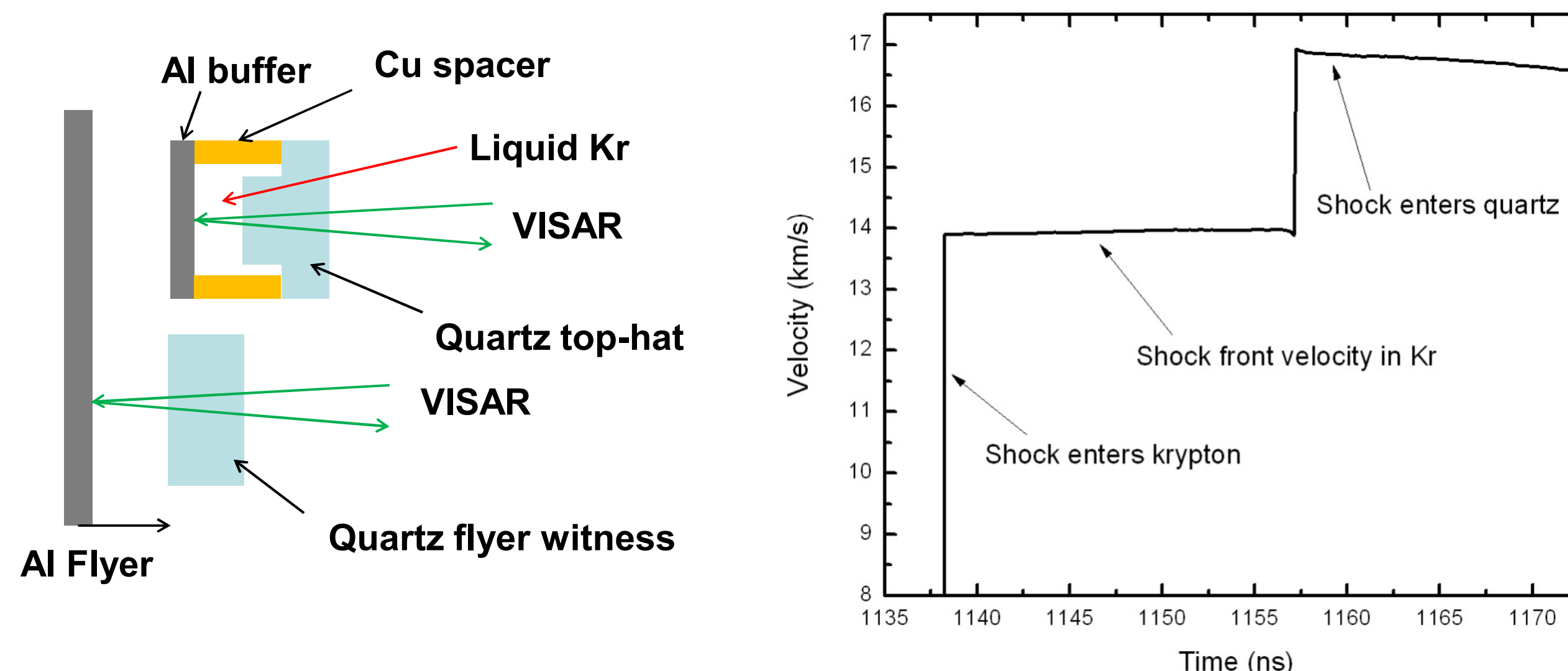


Need experimental data to validate the DFT simulations and EOS tables

## Z-Experiment Setup



## Experimental Approach

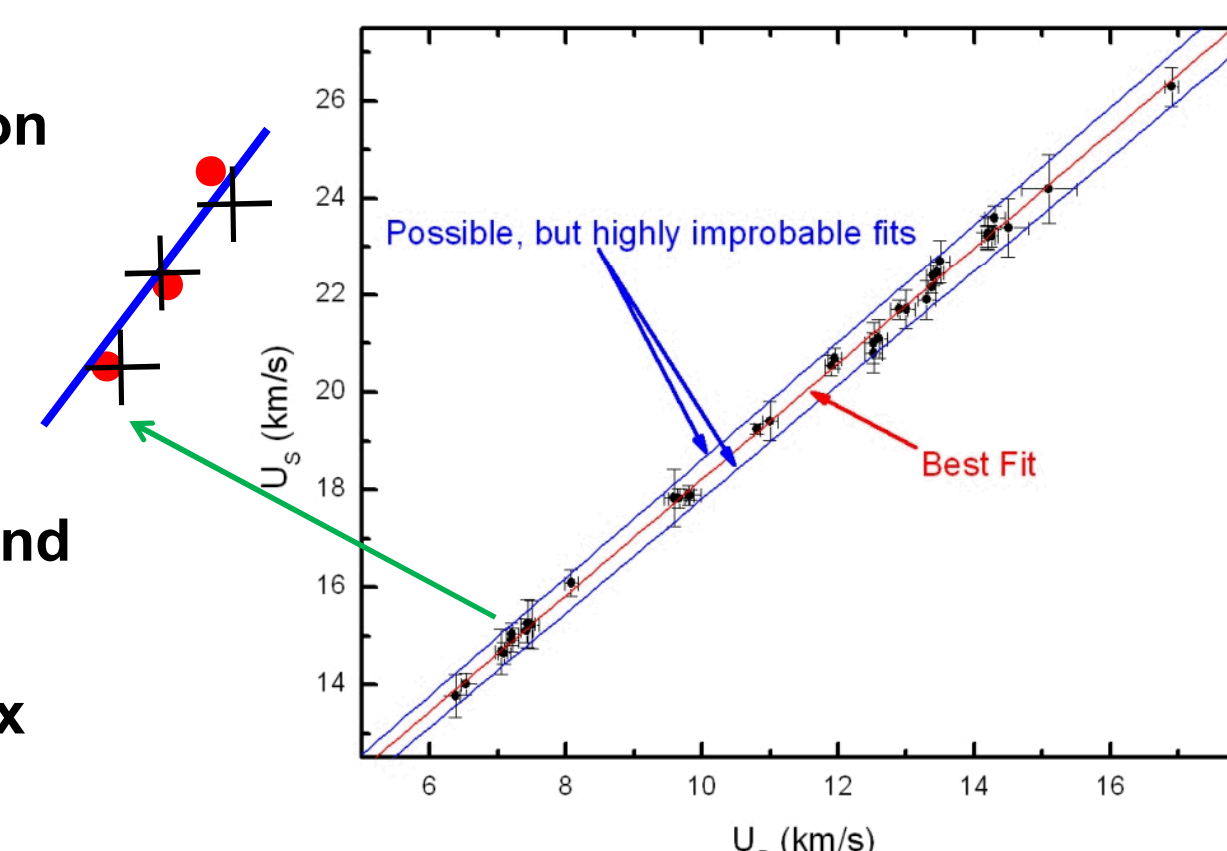


- Temperature = 118 K, Kr  $\rho_0 = 2.426$  g/cc, Sample size ~ 250  $\mu$ m
- Typically 4 different VPFs on target – reduce uncertainty
- Shock front in Kr is reflective – direct measurement of shock velocity
- Measure flyer velocity directly on the quartz flyer witness
- Starting from liquid provides a well-characterized, uniform initial state that is repeatable from experiment to experiment

## Monte Carlo (MC) Impedance Matching

### Aluminum

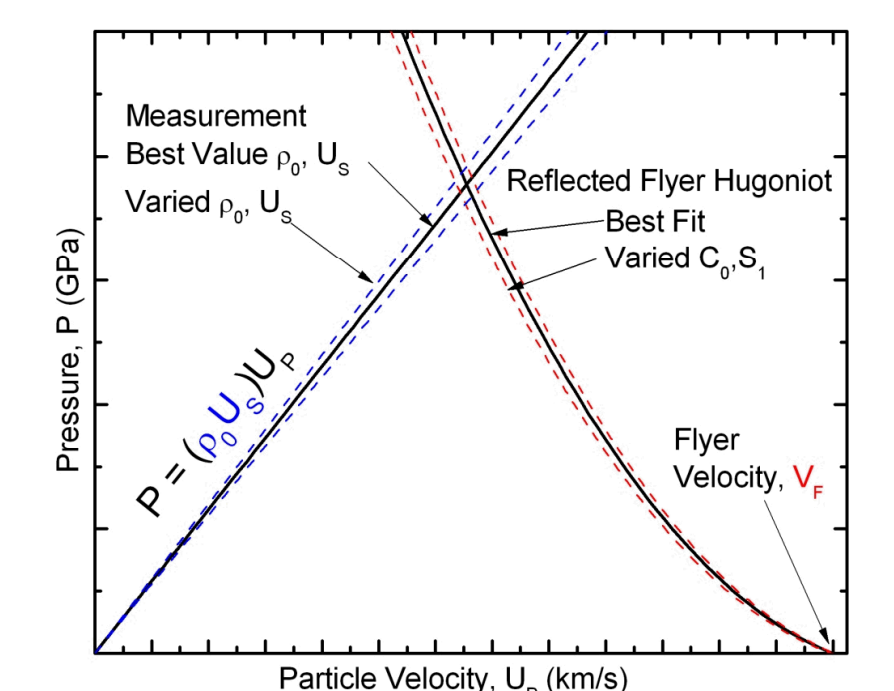
- Uncertainty in experimental data (Knudson et al., JAP 2003)
- Vary each  $U_S$ - $U_P$  point by an uncorrelated random number with  $\sigma$  = experimental uncertainty
- Solve for weighted linear fit parameters and generate a distribution of fits
- Determine mean,  $\sigma$ , and correlation matrix of the fit parameters



### Krypton

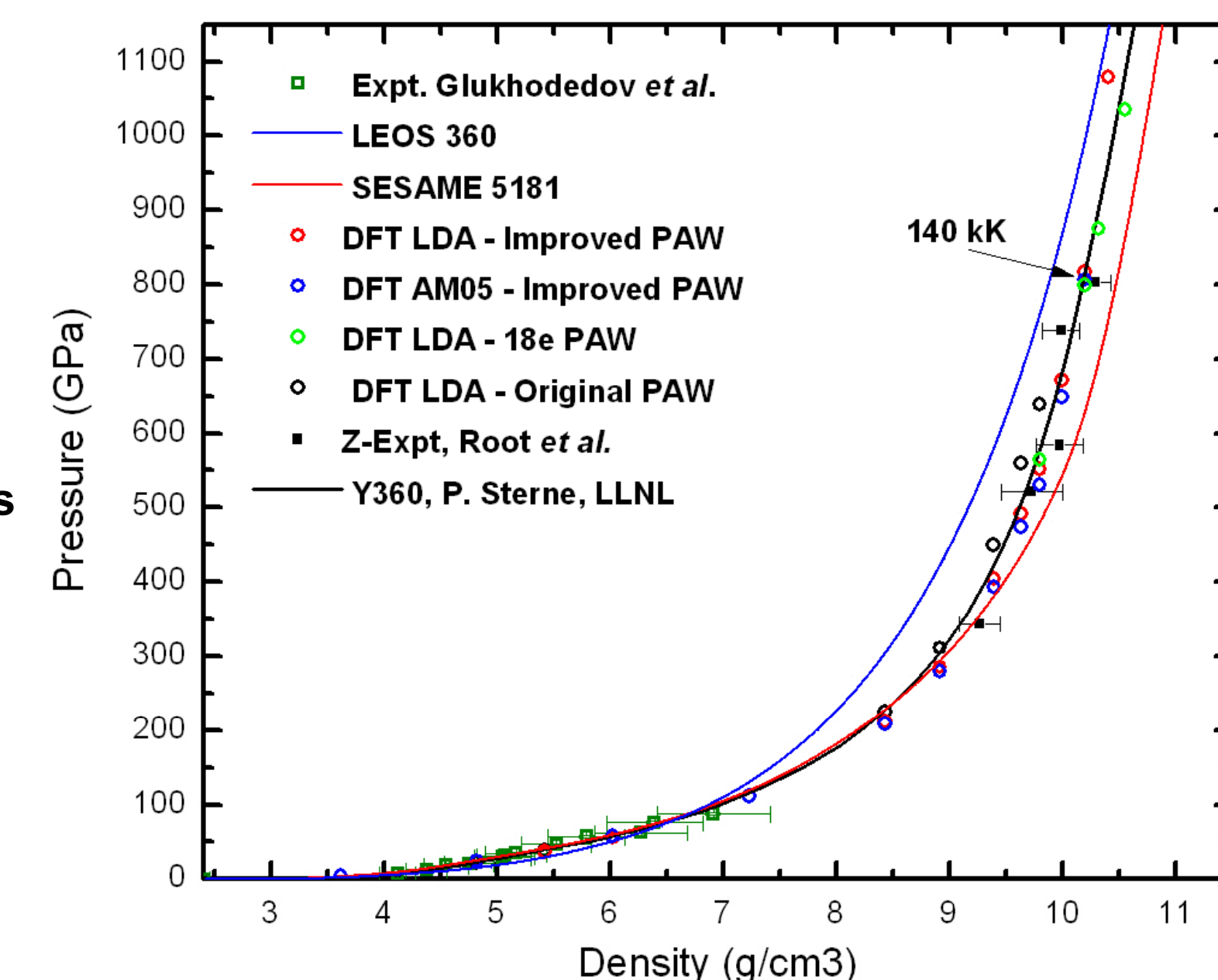
- Vary measured parameters ( $V_P$ ,  $U_S$ ,  $\rho_0$ ) with uncorrelated random numbers,  $\sigma$  = experimental uncertainty
- Vary AI fit parameters using correlated random numbers
- Calculate  $U_P$ , P, and  $\rho$
- Determine mean and  $\sigma$

Monte Carlo technique accounts for experimental uncertainty and propagates error in the AI standard into the resulting Kr data.



## Experimental Results

- Hugoniot determined to 8 Mbar
- Used reflected AI Hugoniot to calculate Kr state
- Using SESAME 3700 release shifts density lower ~ 1%
- Improved PAW and 18e PAW results agree with experimental data
- Original VASP PAW too stiff
- SESAME 5181 agrees to 4 Mbar



- Phil Sterne (LLNL) developing Y360 using DFT and Z-Expt. Results

## Summary

- Experimentally measured the liquid Kr Hugoniot to 8 Mbar
- Demonstrated the need for accurate PAW potentials at high temperatures
- Validated DFT results to 8 Mbar
- Showed that SESAME 5181 is reasonable to 4 Mbar
- Sterne's Y360 EOS reliably reproduces the Hugoniot to multi-Mbar pressures

## Acknowledgments

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