

# **Identification and Validation of Environmental Load Models Based on Structural Response**

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# Motivation

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- **Accurate assessment of system response requires**
  - Accurate model of system (and its IC and BC)
  - Accurate model of excitation
- **Validation assures accuracy (or adequacy) of models**
  - Validation of system models is amply treated in the literature (e.g., validation of FE models)
  - Validation of excitation environments is trivial in some situations and very difficult in others – Usually ignored



# Introduction

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- Model validation - “the process of determining the degree to which a model is an accurate representation of the real world from the perspective of the intended uses of the model”
  - Involves comparison of model-predicted results to experimental results to assess adequacy/accuracy of model
  - Adequacy/level of accuracy depends on intended model uses
- *We consider validation of unmeasurable environments that are nonstationary random processes*



# Outline

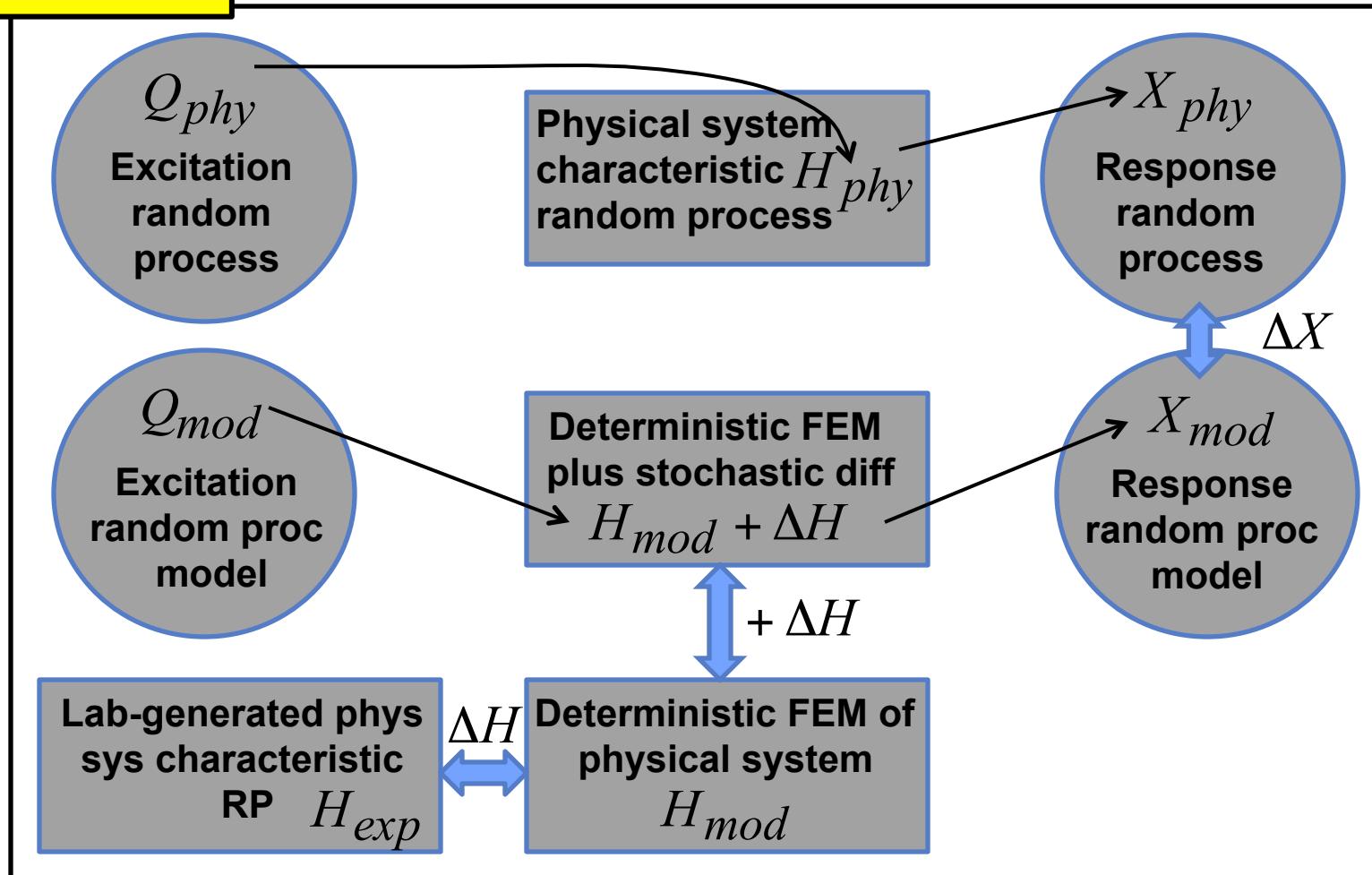
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**This talk will cover**

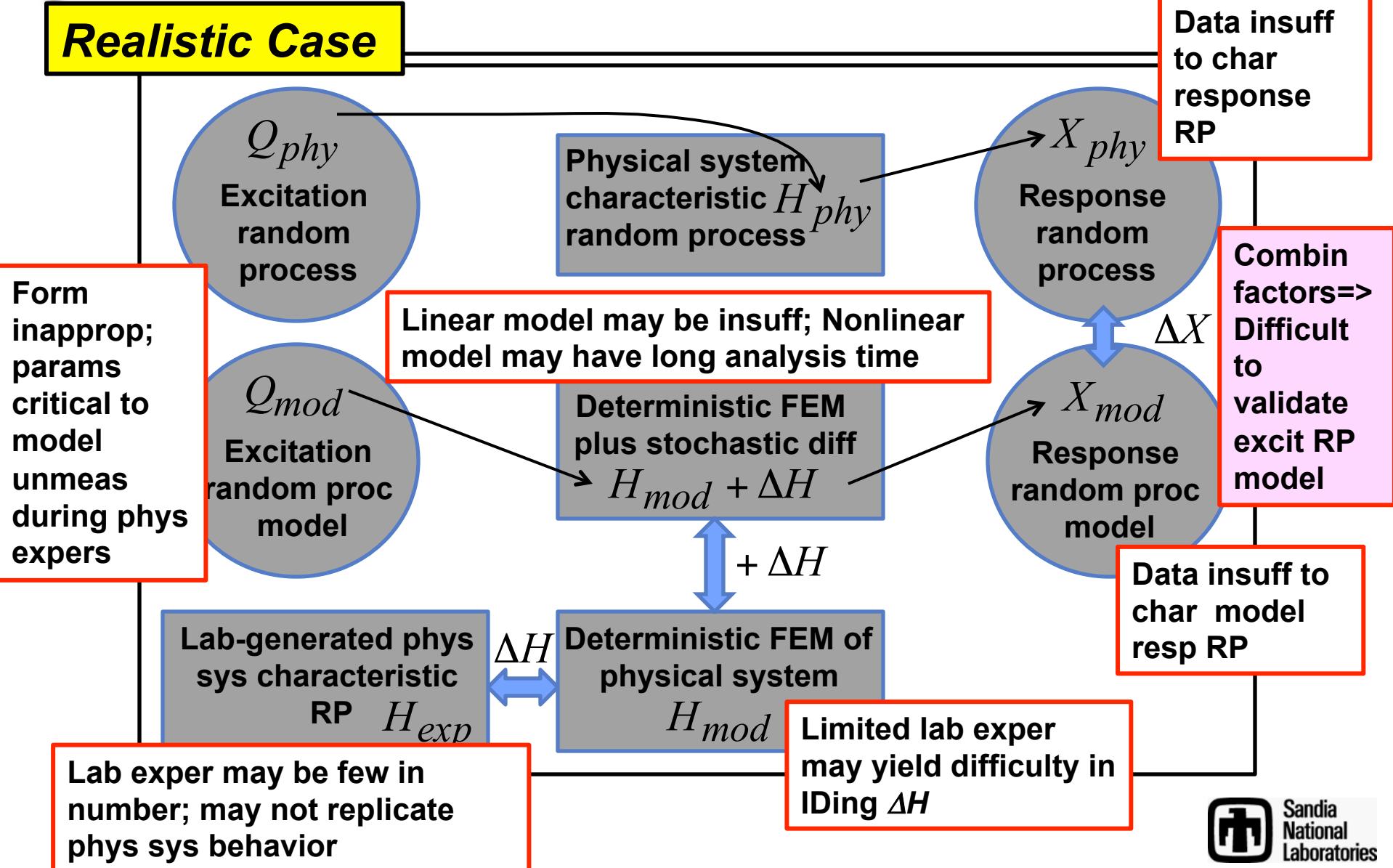
- **Approach to stochastic environment model validation – Ideal case**
- **Approach to stochastic environment model validation – Practical case**
- **Example – Structural dynamics during atmospheric re-entry – Validation**

# Environment Validation – Procedure

## Ideal Case



# Environment Validation – Procedure





# Environment Validation

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- Consider case where
  - Deterministic FEM used, alone
  - Model assumed accurate – Validated
- Measure of response – Evolutionary spectral density of nonstationary, random acceleration response process
- Priestley's model:  $\{X(t), 0 \leq t \leq T\}$  is a nonstationary random process that may be expressed

$$X(t) = \int_{-\infty}^{\infty} A_X(\omega, t) e^{i\omega t} dZ(\omega) \quad 0 \leq t \leq T$$



# Environment Validation

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- The evolutionary (time-varying) spectral density (ESD) of the response random process  $\{X(t), 0 \leq t \leq T\}$  is

$$S_{XX}(\omega, t) = |A_X(\omega, t)|^2 S_0(\omega) \quad -\omega_L < \omega < \omega_L, 0 \leq t \leq T$$

- When the ESD of the response computed using the model excitation is “close enough” to the ESD of the experimental response, the excitation model is validated
- How do we establish what is close enough?



# Environment Validation

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- **One validation possibility (when parameters critical in model are unmeasured during physical re-entry):**
  - **Generate multiple realizations of response ESD using model and spectrum of environment parameters**
  - **Compute ESD of available experimental re-entry responses**
  - **Establish whether model-generated ESDs lie (satisfactorily) within model-predicted ESDs**



# Environment Validation

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- **Validation scheme:**

- At a pre-established set of times  $T_j, j = 1, \dots, N$
  - Estimate Karhunen-Loeve expansion of experimental response spectra

$$G = \nu w^{1/2} U + \mu_G$$

- Solve for underlying random variates of experimental spectra

$$u = w^{-1/2} \nu^T (g - \mu_G)$$

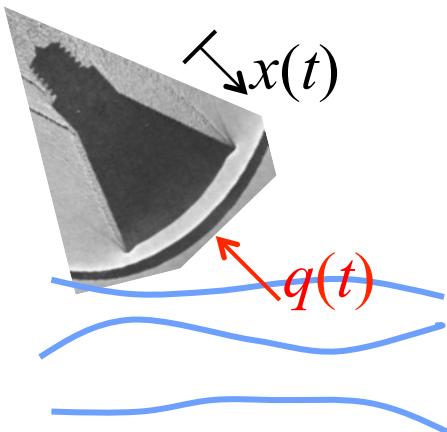
- Use model-generated spectra,  $g_{mod}$ , in this formula, in place of  $g$ , to obtain  $u_{mod}$
  - Use statistical test of hypothesis framework to establish whether  $u_{mod}$  lie among the  $u$



# Environment Validation – Example

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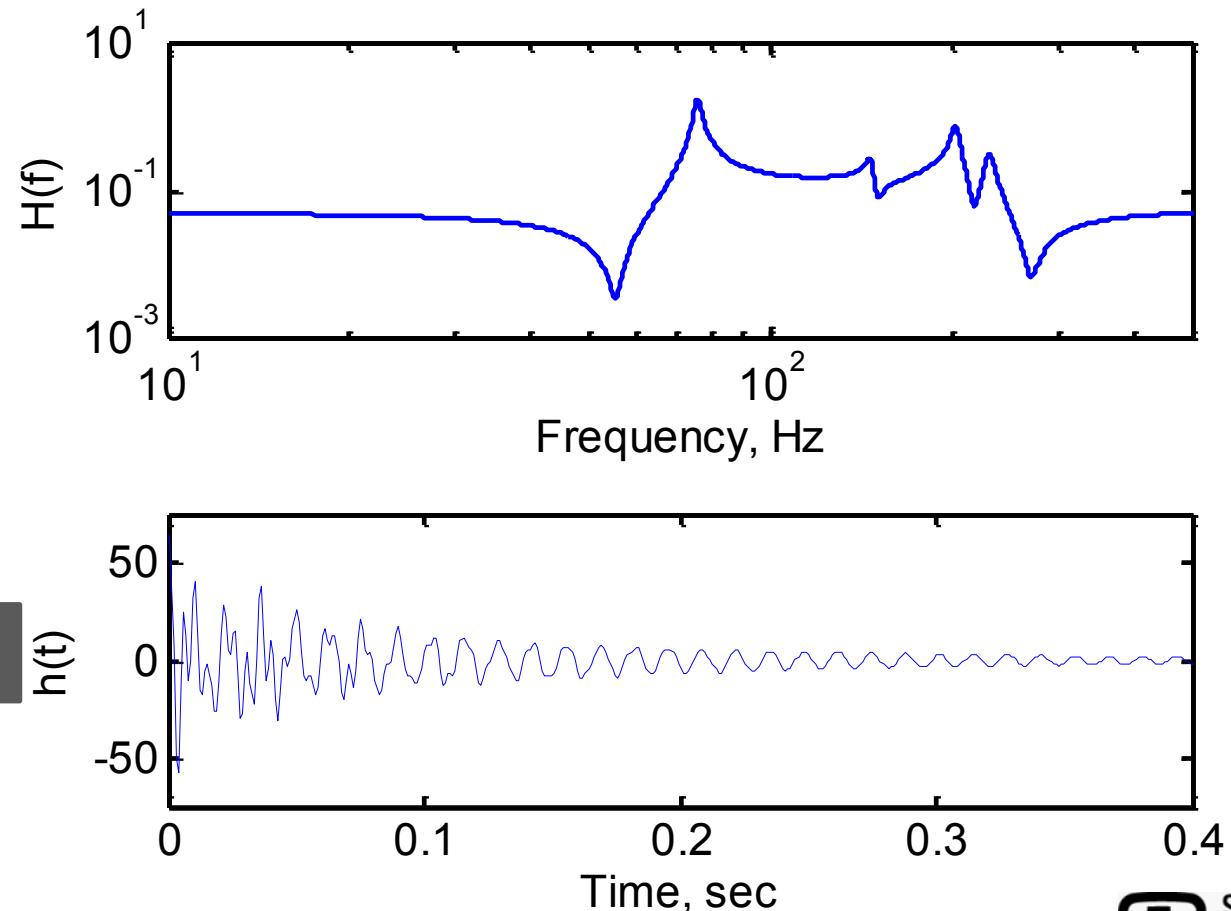
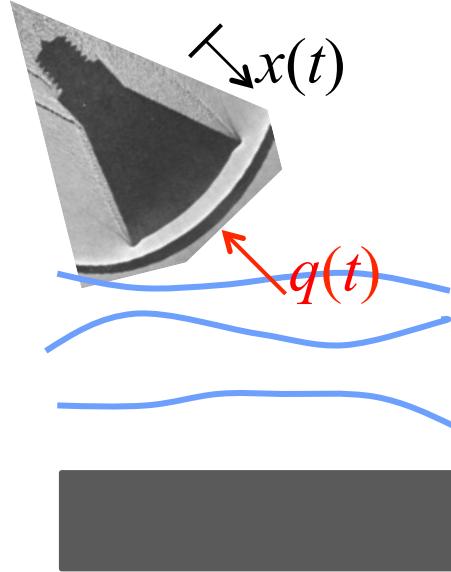
- Consider aerospace structure re-entering atmosphere- Loads cannot be measured
- Load model accommodates temperature layering in atmosphere
  - Load is nonstationary random process – Priestley model w/ evolutionary (time-varying) spectral density
  - Response modeled in same frame
  - Experimental responses available, but conditions unmeasured
  - Validate using ESD as specified





# Environment Validation – Example

- System FRF and IRF – Load is  $q(t)$ , response is  $x(t)$

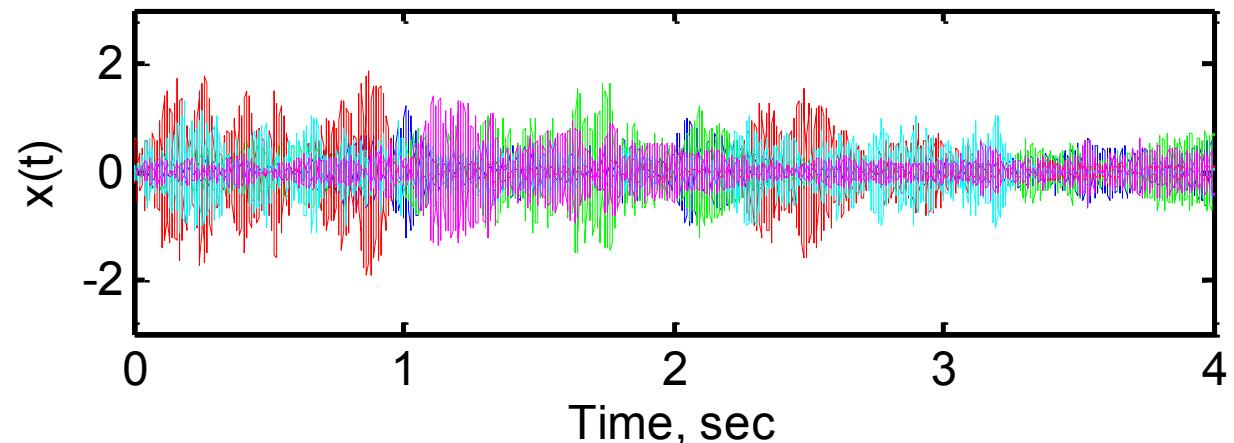
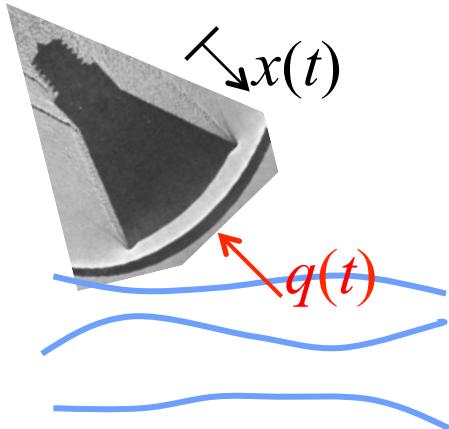




# Environment Validation – Example

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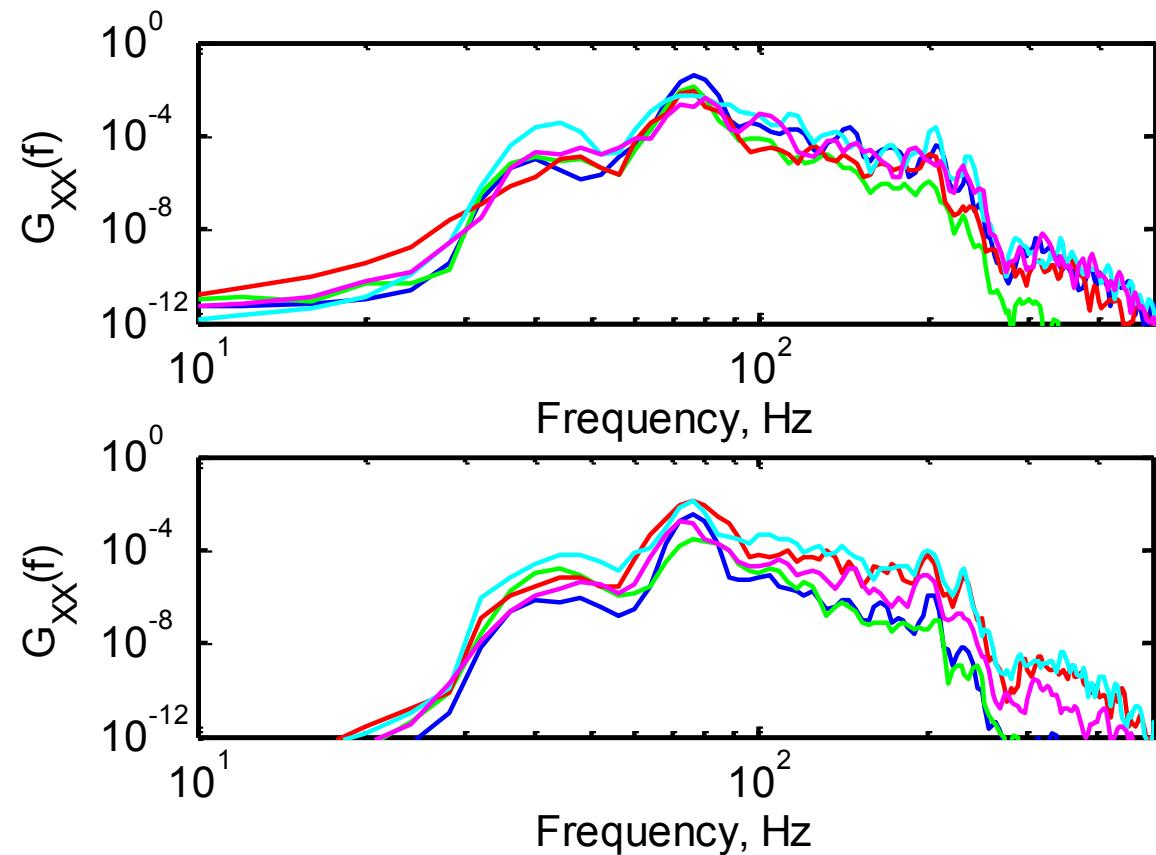
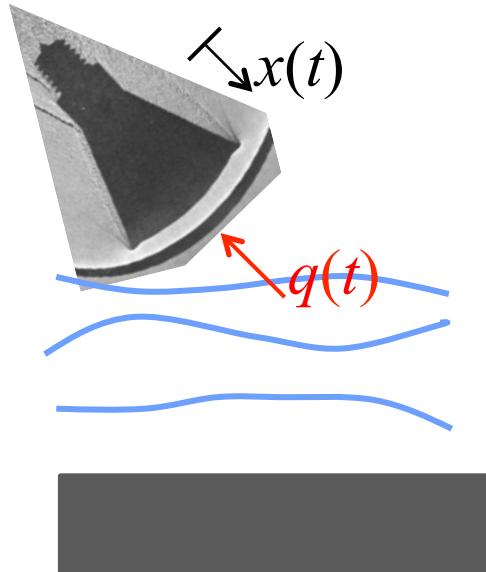
- Experimental inputs (unmeasured) excite experimental responses – Five realizations





# Environment Validation – Example

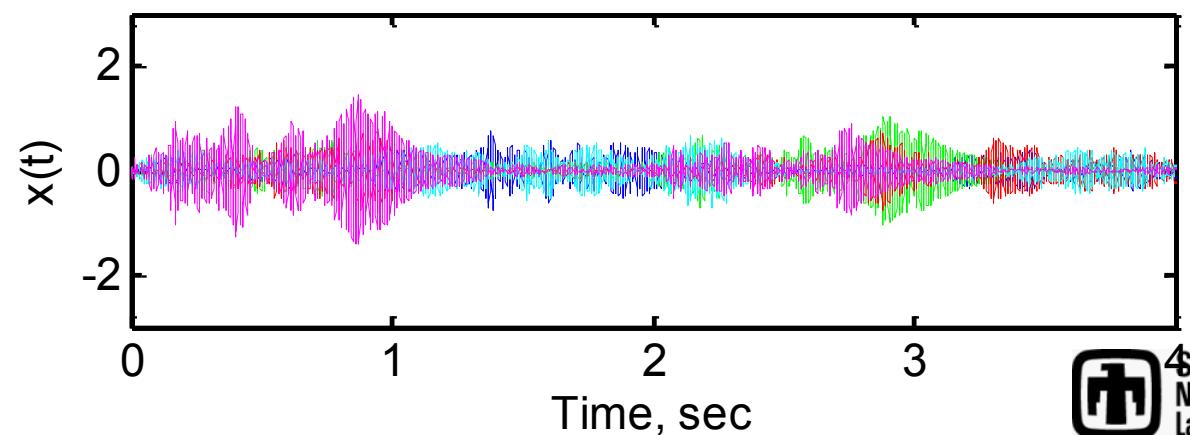
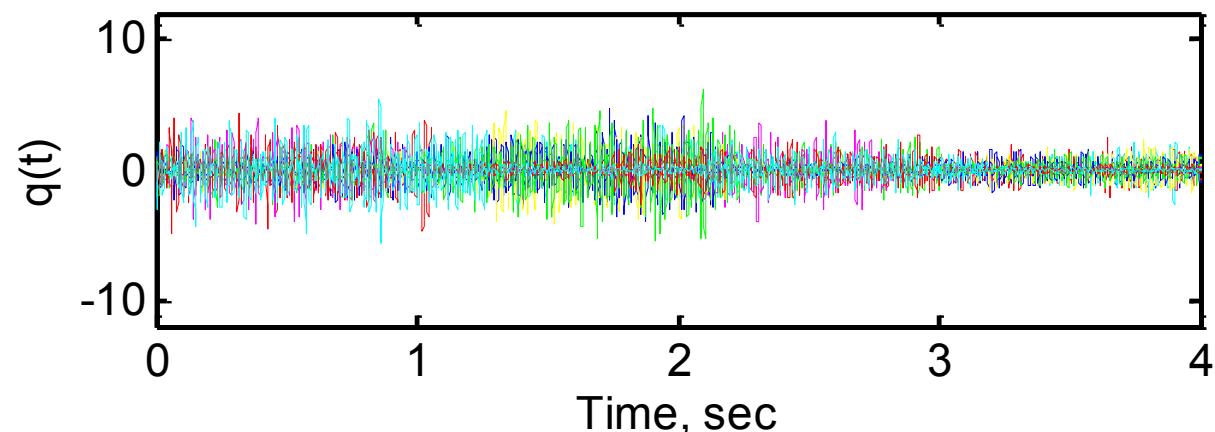
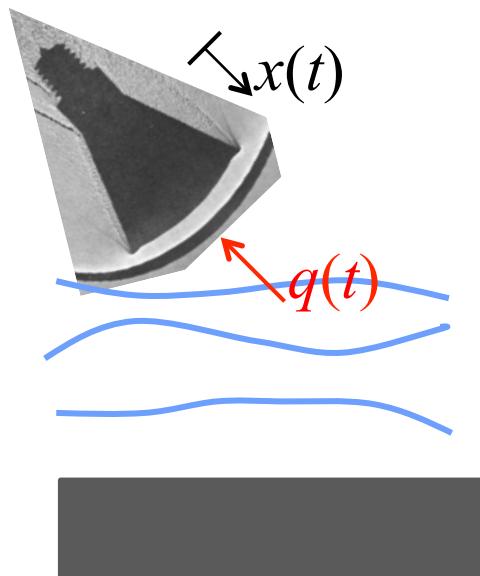
- Experimental ESDs at times 1 sec, and 3 sec





# Environment Validation – Example

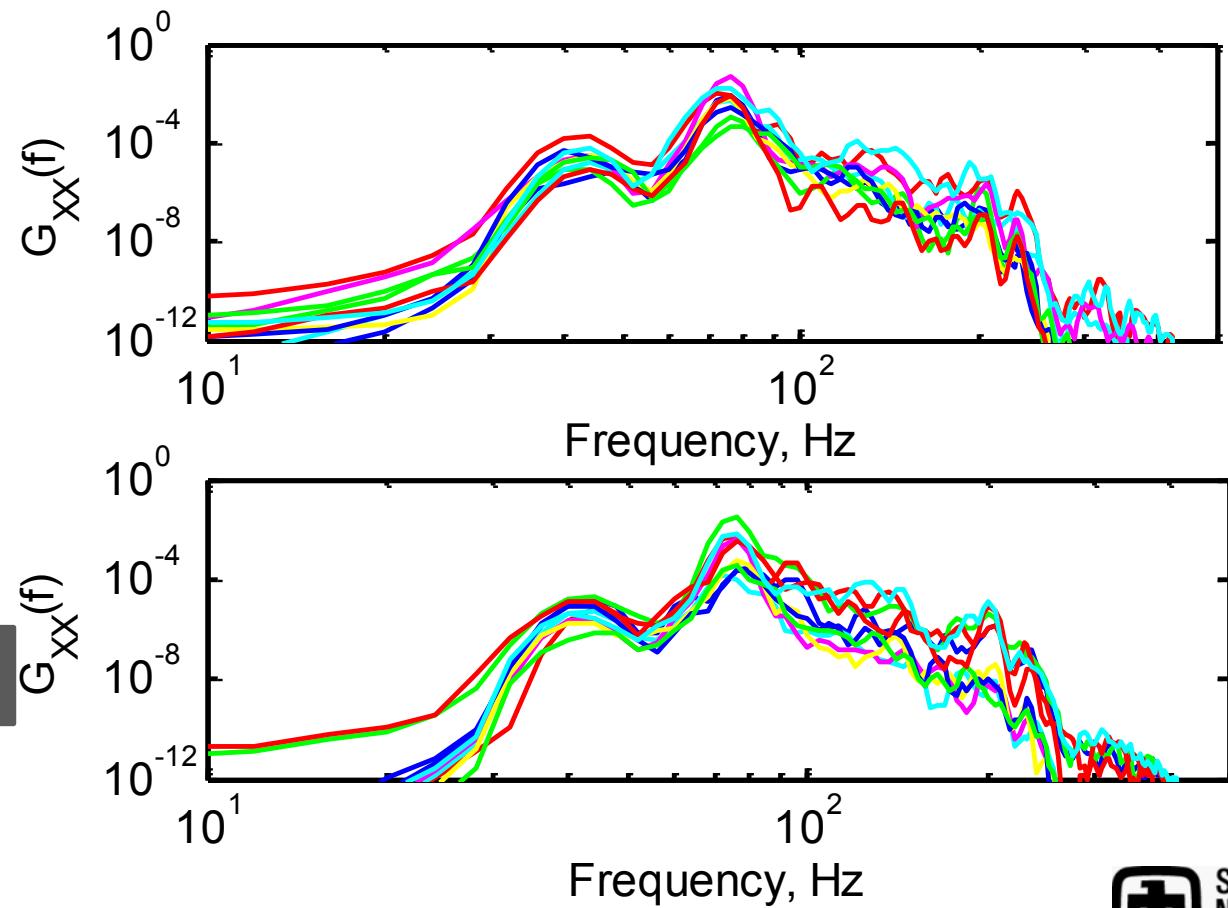
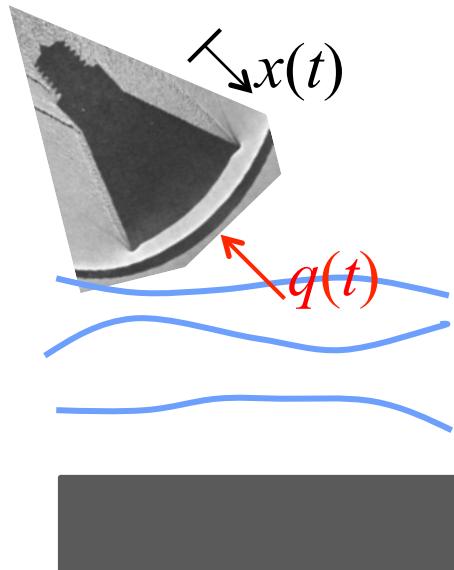
- Model inputs (generated) and responses (computed) – Ten realizations





# Environment Validation – Example

- Spectra of computed responses at 1 sec, and 3 sec

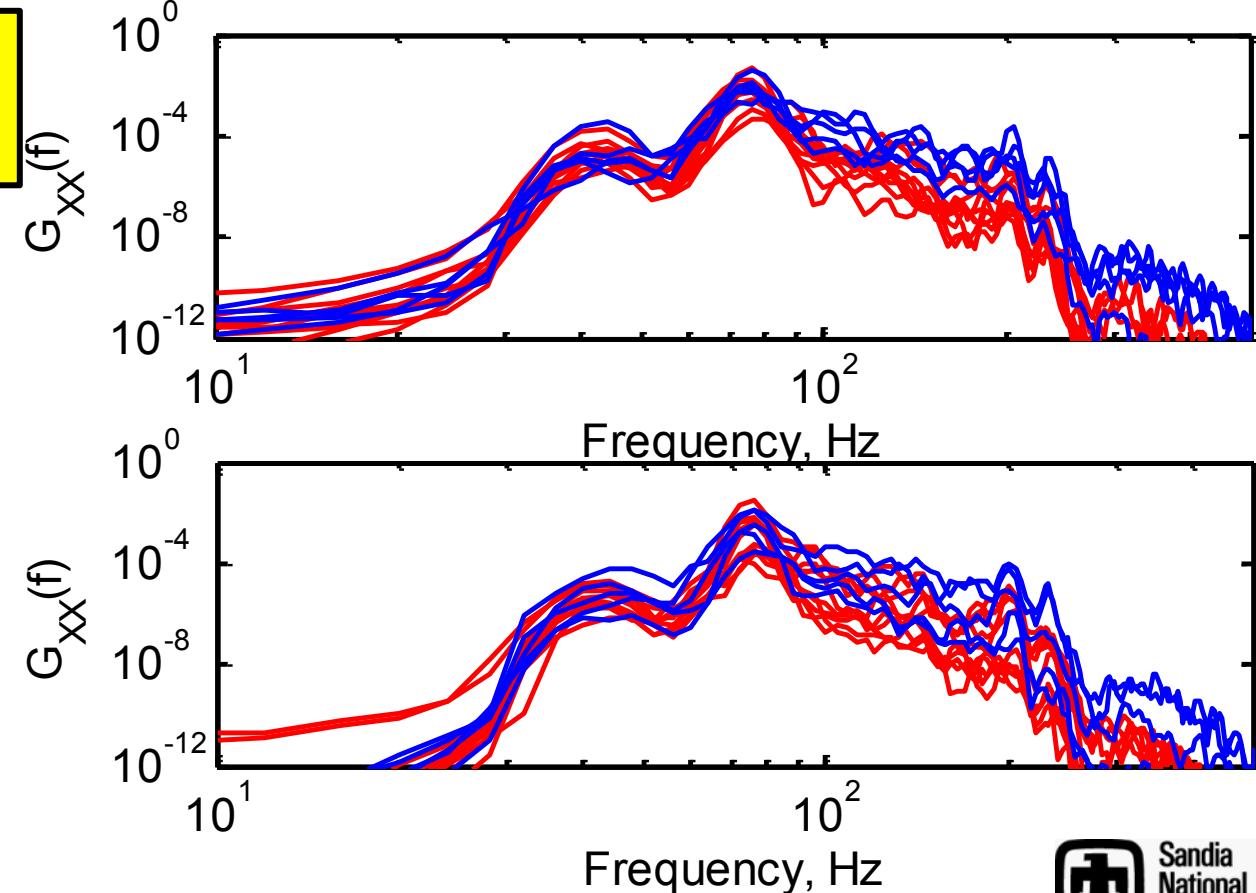
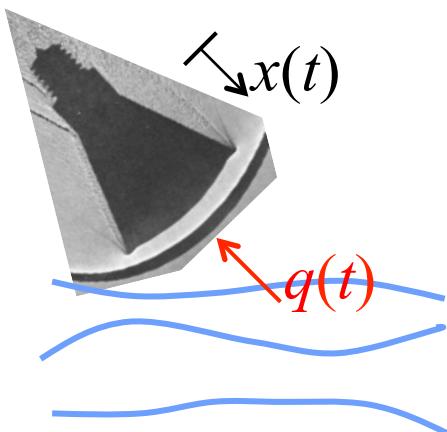




# Environment Validation – Example

- Experimental (blue) and model (red) response spectra at 1 sec and 3 sec

Model spectra low at high frequencies

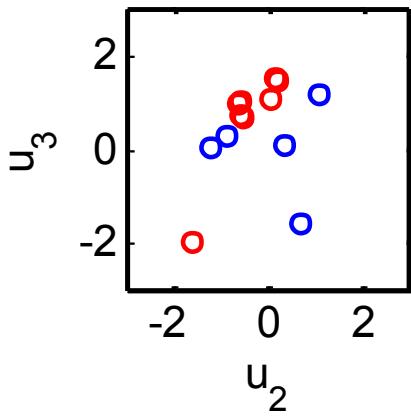
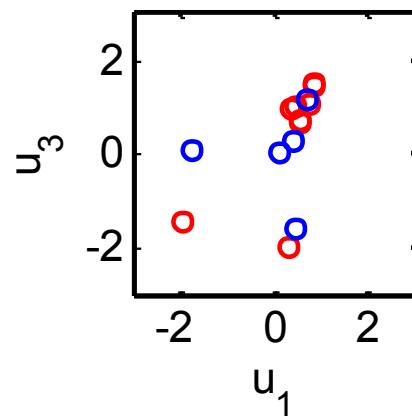
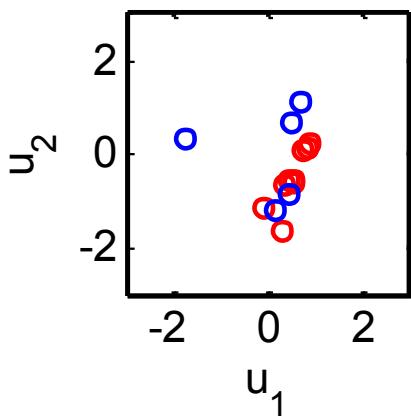




# Environment Validation – Example

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- Compute KLE of experiment, then u-values (blue)
- Compute u-values of model prediction - 1 sec



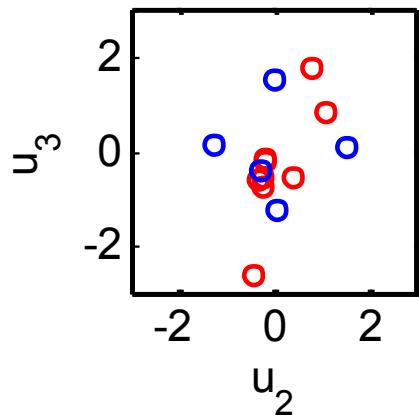
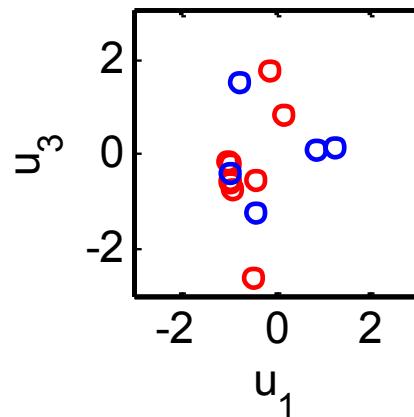
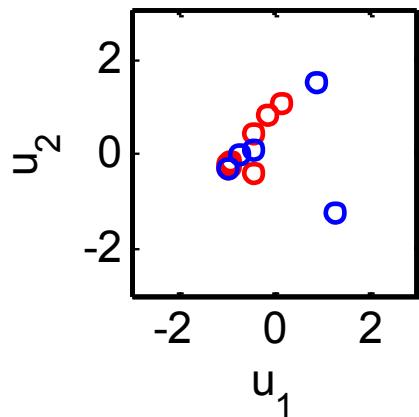
u2 versus u1 – Simulation not very good



# Environment Validation – Example

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- 3 sec



Simulation better at 3 sec.



# Summary

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- Method presented for validation of nonstationary random process environment
  - Based on evolutionary spectral density (ESD) from Priestley model
  - Karhunen-Loeve expansion (KLE) of ESDs obtained from measured experimental responses
  - Random variates of ESDs inferred from experiments
  - Random variates of model-generated responses obtained
  - Test of hypothesis performed – Can model-generated responses be rejected as products of experimental random process?