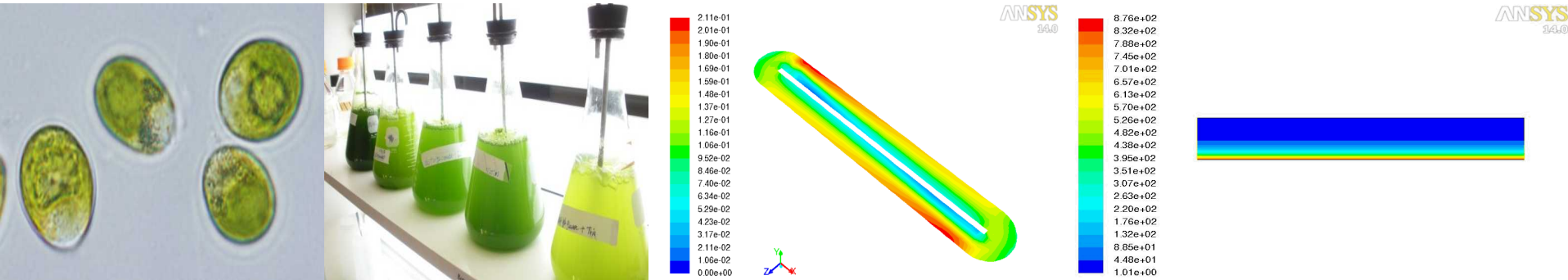


*Exceptional service in the national interest*



# A Computational Model of Algal Growth

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# Algal Biofuels

- Alternative to petroleum based fuels
- Can be grown on non-arable land
- Can be grown using wastewaters such as municipal and industrial effluent and saline waters.
- Can consume carbon dioxide from waste sources such as power and ammonia plants



# Goals of Computational Models

- Make accurate predications of algal growth
- Reduce experimentation on large scales which is costly and time consuming
- Optimize existing systems for higher yields

# Current Models

## Photobioreactor Models

- Typically control over one or more environmental parameters
- Small fluctuations of parameters can be important due to small volumes

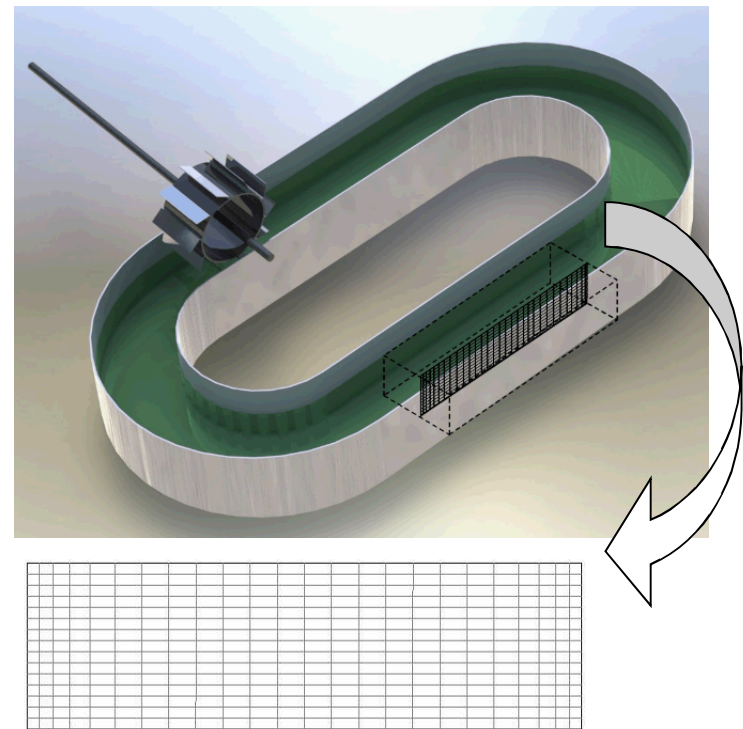
## Water Quality Models

- Model large systems
- No control over environmental parameters
- Small fluctuations of parameters typically not important due to large volumes

# Computational Fluid Dynamics

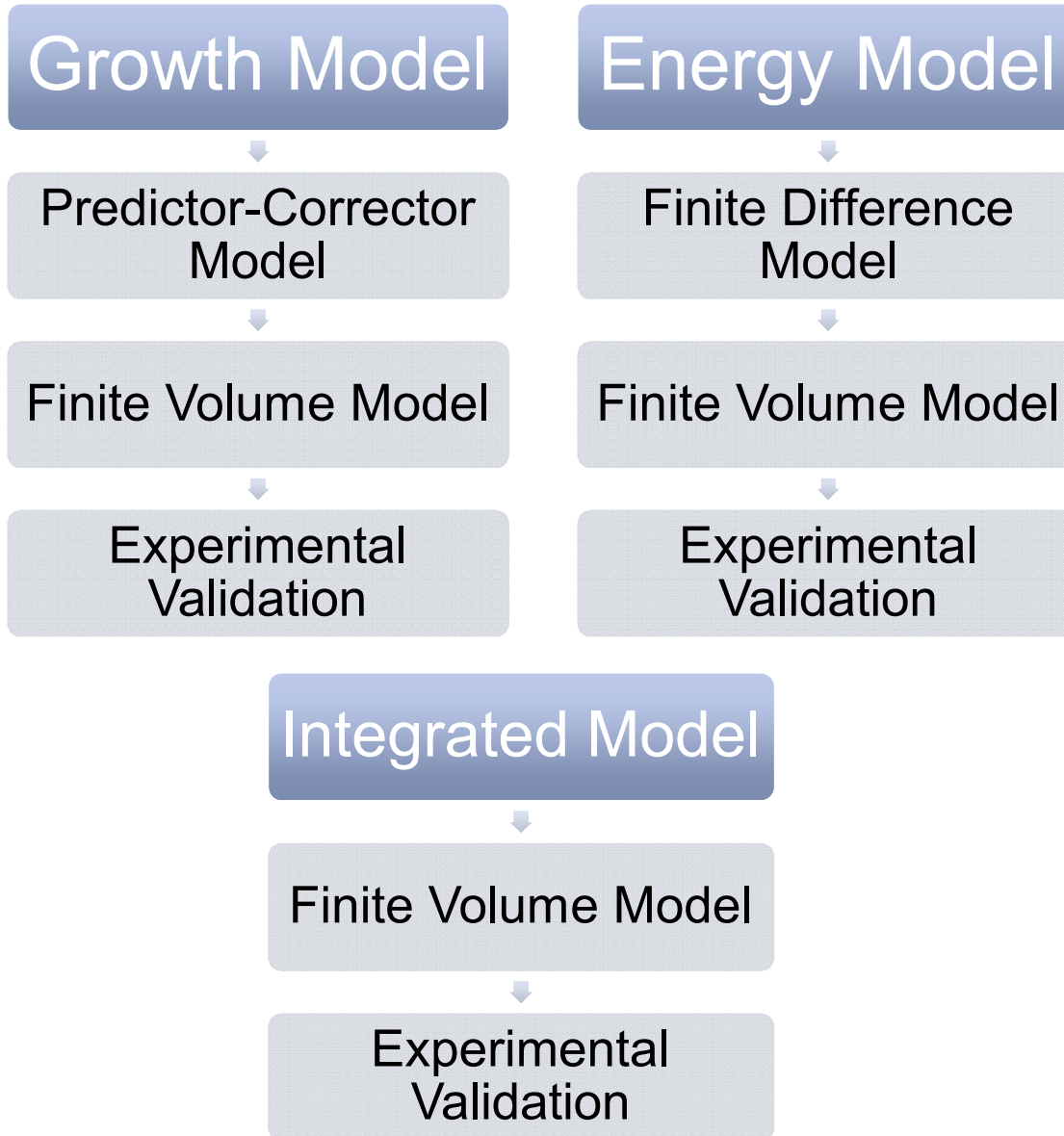
Numerical solution and visualization of mass, momentum and heat transfer equations.

- Calculate the distribution of light, temperature, and species within the pond with high accuracy
- Integrate all aspects of algal growth through user defined functions (UDF)



# Objectives

- Identify key parameters of algal growth
- Develop a computational fluid dynamics (CFD) model of algal growth based on:
  - Species
  - Environmental conditions
  - Water quality conditions
- Develop and validate a CFD model of pond temperature based on:
  - An energy balance
  - Weather station data
- Validate the CFD model with more simple numerical models and experimental data



# Growth Model

$$\begin{aligned}
 \frac{d\Phi}{dt} = & \Phi_{in} - \Phi_{out} - \Phi_{loss} - \frac{\Phi^2}{V} \\
 & - \sum \frac{\Phi_{in} \Phi_{out}}{\sum \Phi_{in} + \Phi_{out} + \sum \Phi_{loss}}
 \end{aligned}$$

$$\frac{d\Phi}{dt} = \Phi_{in} - \Phi_{out} - \Phi_{loss} - \frac{\Phi^2}{V}$$

$$\frac{d\Phi}{dt} = \begin{cases} \exp\left(-\frac{\Phi}{V}(\Phi_{in} - \Phi)^2\right) & \Phi_{in} < \Phi_{out} \\ 1 & \Phi_{in} \leq \Phi \leq \Phi_{out} \\ \exp\left(-\frac{\Phi}{V}(\Phi - \Phi_{out})^2\right) & \Phi_{out} < \Phi \end{cases}$$

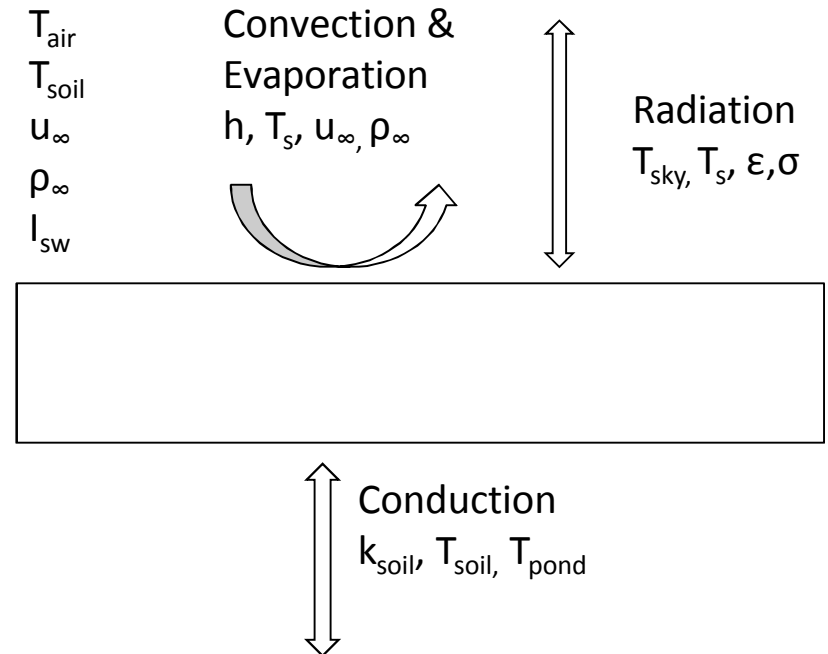
$$\frac{d\Phi}{dt} = \frac{\Phi_{in}}{V} \left( \frac{\Phi_{in}}{\Phi_{in} + \Phi_{out}}, \left( \frac{\Phi_{in}}{\Phi_{in} + \Phi_{out}} \right), \left( \frac{\Phi_{in}}{\Phi_{in} + \Phi_{out}} \right) \right)$$

$$\frac{d\Phi}{dt} = \left( \frac{\Phi_{in}}{V} \left( -\frac{\Phi}{V} + 1 \right) \right)$$

$$\frac{d\Phi}{dt} = \frac{[\Phi]^+}{[\Phi]^+ + \Phi_{out} + [\Phi]^2 / V}$$

# Energy Model

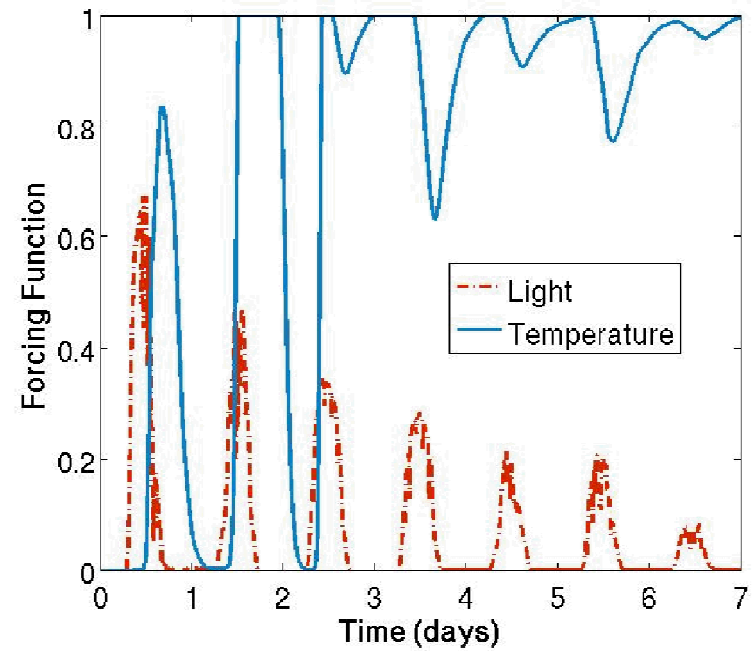
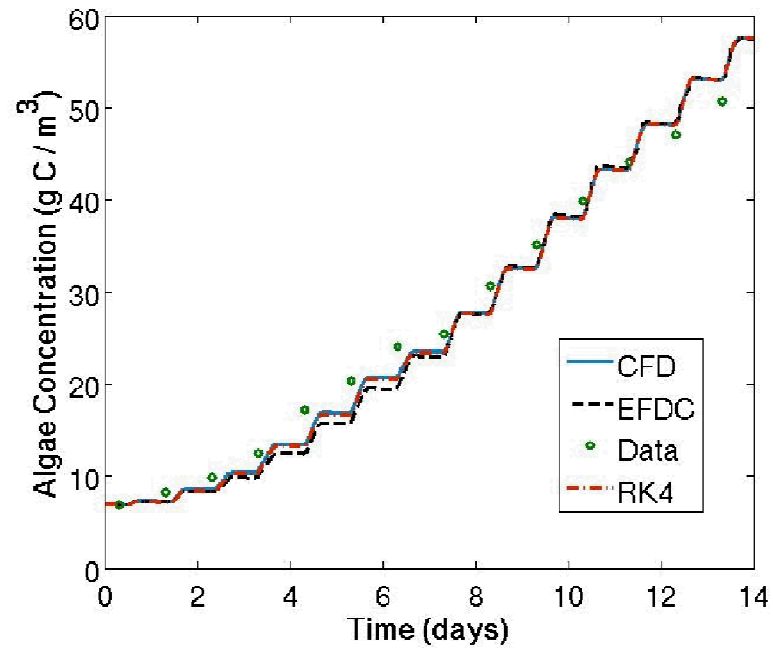
- $q''_{lw} = \epsilon\sigma(T_{sky}^4 - T_{surface}^4)$
- $q''_{conv} = \bar{h}(T_{\infty} - T_s)$
- $q''_{evap} = h_{fg}h_m(\rho_{sat} - \rho_{\infty})$
- $q''_{cond} = k(T_{pond} - T_{soil})$
- $q''_{sw}$ , from weather data



# Greenhouse Experiment

- Pond type
  - Open tank
- Dimensions
  - 0.211 m deep
  - .53 m<sup>3</sup> volume
- Location
  - Sandia National Labs  
(Albuquerque, NM)
- Species
  - *Nannochloropsis salina*
- Data Collected
  - Algae concentration
  - Nutrient concentration
  - Pond Temperature
  - Solar intensity
  - pH

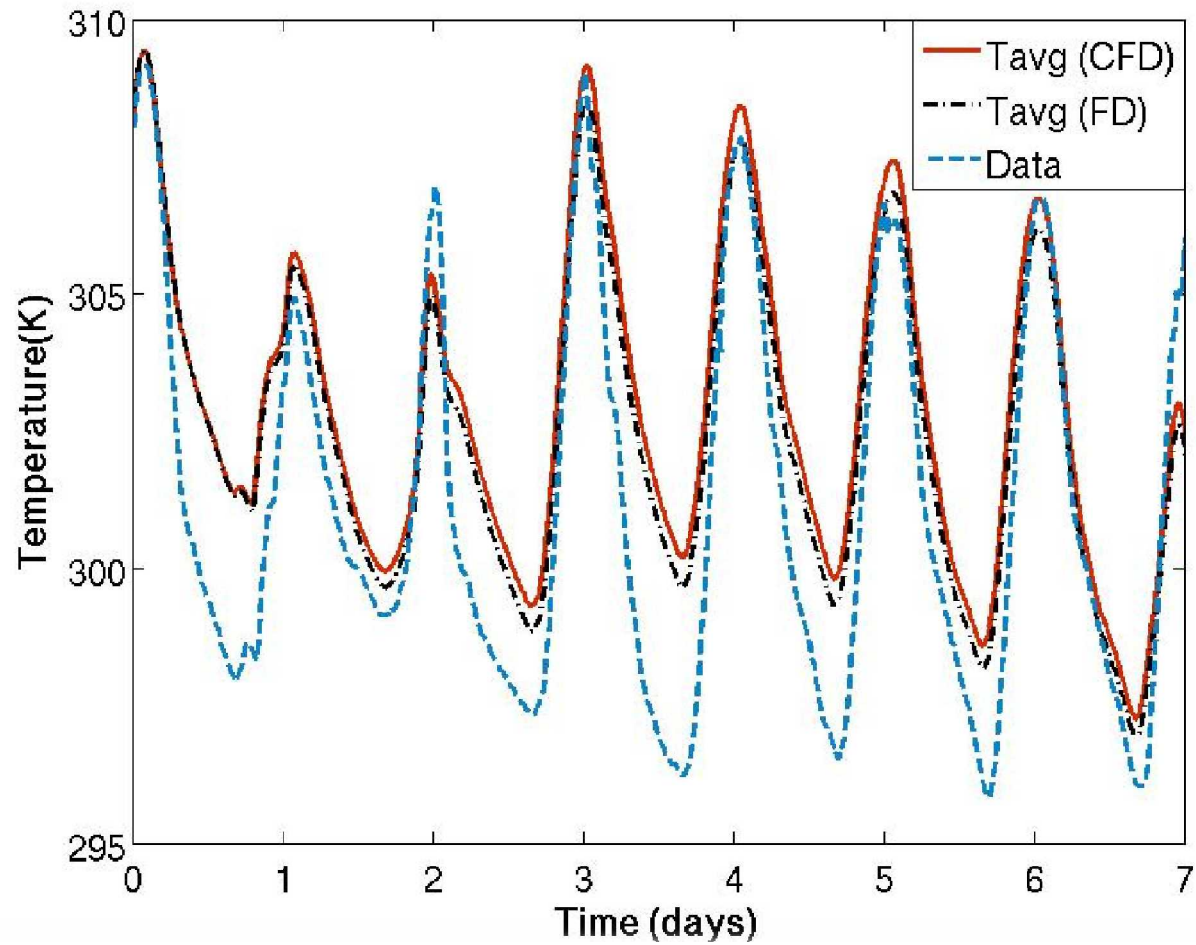
# Validation



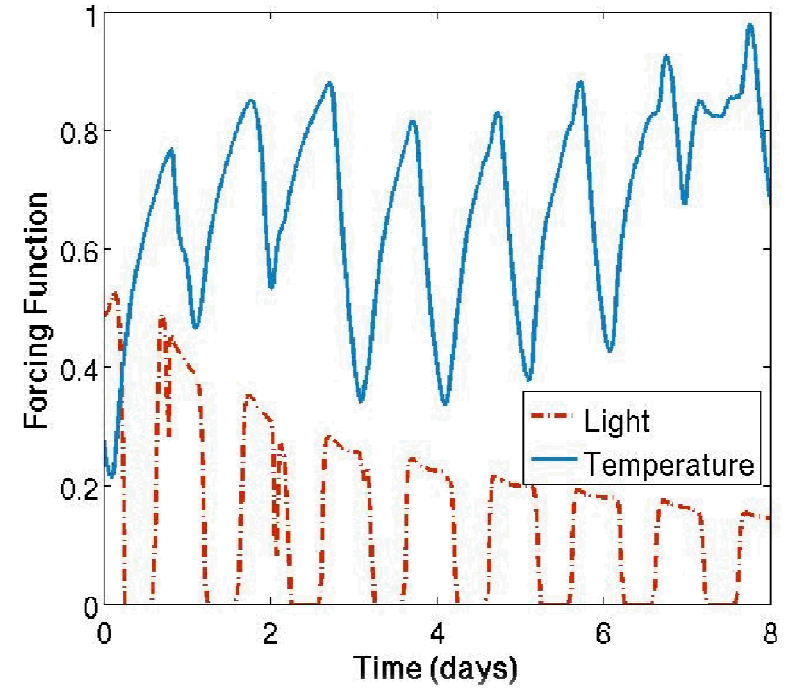
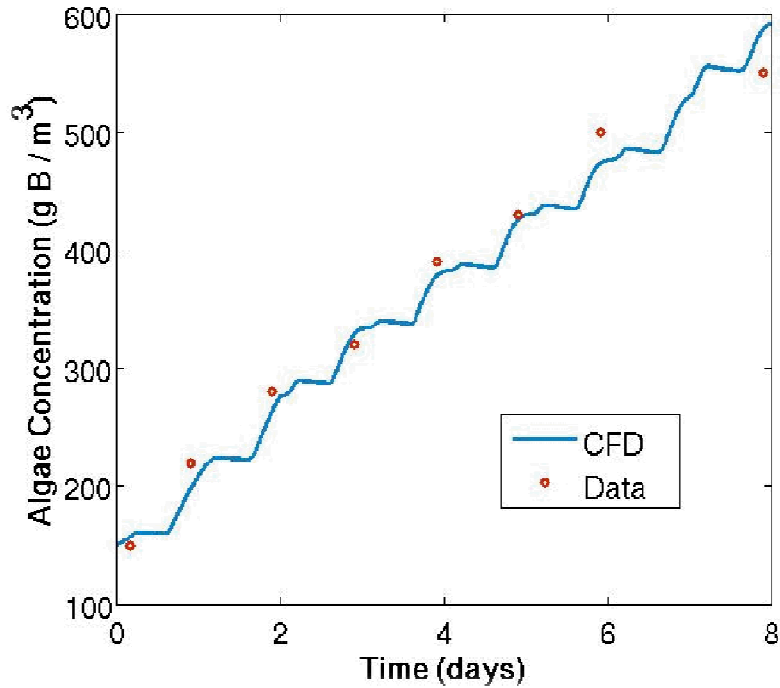
# Raceway Experiment

- Pond type
  - Open raceway
- Dimensions
  - 0.2 m deep
  - 59.3 m<sup>2</sup> surface area
  - 12 m<sup>3</sup>
- Location
  - Arizona State University  
(Mesa, AZ)
- Species
  - *Nannochloropsis granulata*
- Data Collected
  - Algae concentration
  - Nutrient Concentration
  - Pond Temperature

# Energy Balance Validation



# Validation



# Conclusion

- Upon initial validation, the model is able to predict pond temperature and algal biomass with no modification of the parameters
- The model can be easily adapted to a variety of locations and pond sizes
- Once validated, can serve as a predictive tool for modeling biomass yields

# Acknowledgments

- Dr. Patricia Gharagozloo, Org. 8365
- Dr. Christopher Choi (University of Wisconsin)
- Dr. Scott James (Exponent, Scientific and Engineering Consulting)

