



Evolution of Microstructure in the Deformation of Nanocrystalline Metals

**Garritt J. Tucker^{1,3}, Shreevant Tiwari¹,
and David L. McDowell^{1,2}**

¹ *School of Materials Science and Engineering*

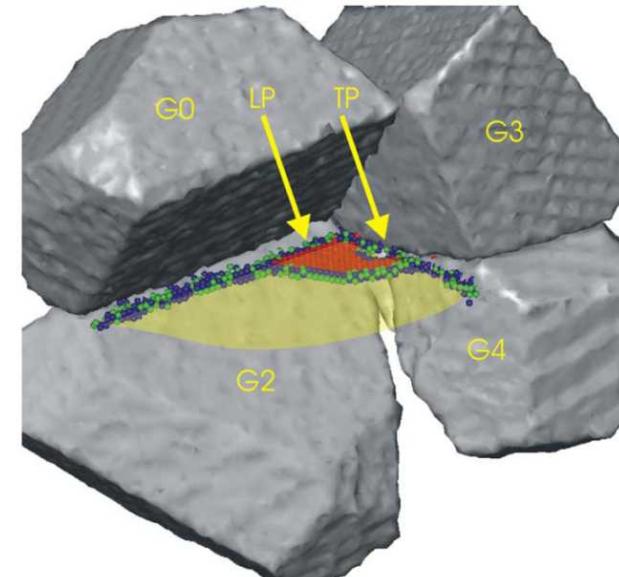
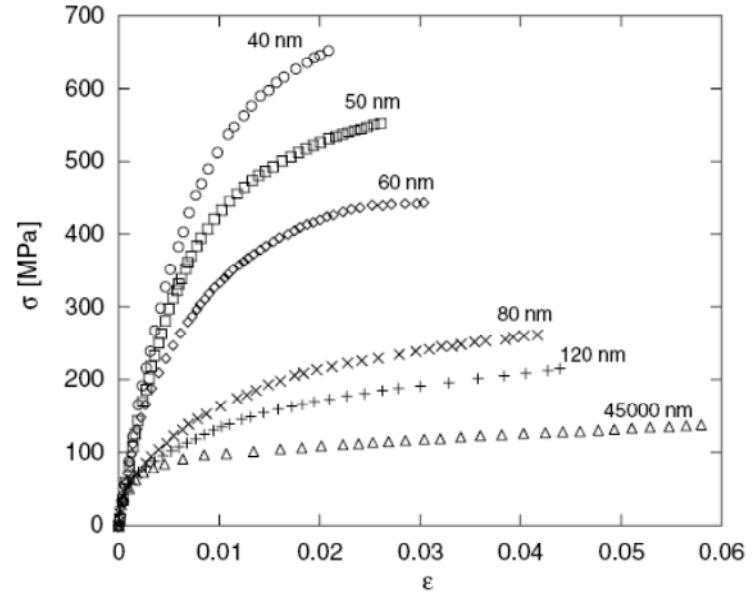
² *Woodruff School of Mechanical Engineering*
Georgia Institute of Technology, Atlanta, GA USA

³ **Sandia National Laboratories**, Albuquerque, NM , USA

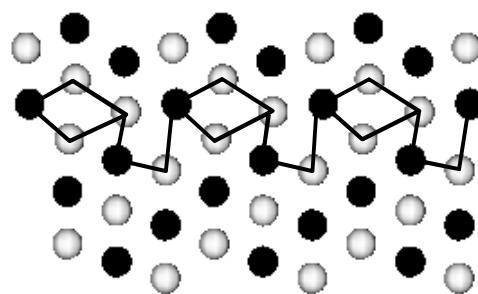
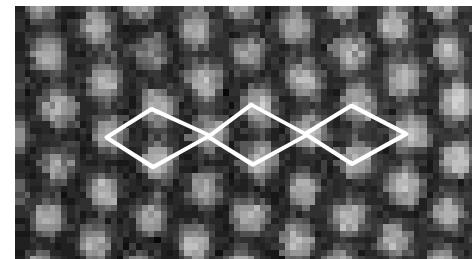
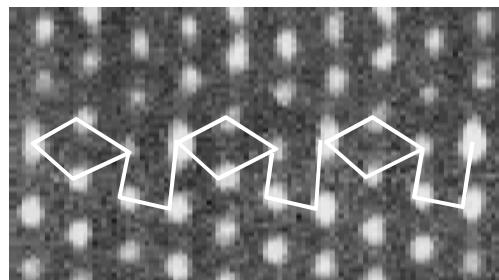
SES 2011, October 12-14, 2011

- Mechanical properties of nanocrystalline (NC) materials show potential improvement compared to larger grained polycrystalline materials (e.g., yield strength, fracture/fatigue resistance, and superplasticity).
- In NC materials, a higher number density of atoms are located in grain boundary (GB) regions.
- A deeper understanding of the role of interfaces (e.g., GBs) in NC deformation processes is still needed.

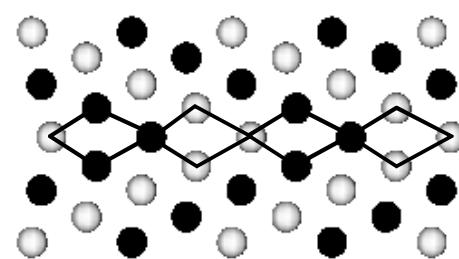
**Important to understand influence of
GBs and related deformation
mechanisms in nanoscale plasticity**



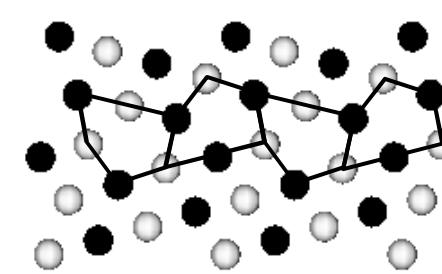
- Interface structures are in agreement with published HRTEM data, e.g. Al (Mills *et al.* (1992) and Medlin *et al.* (1993))



$\Sigma 3 (112) 70.5^\circ$



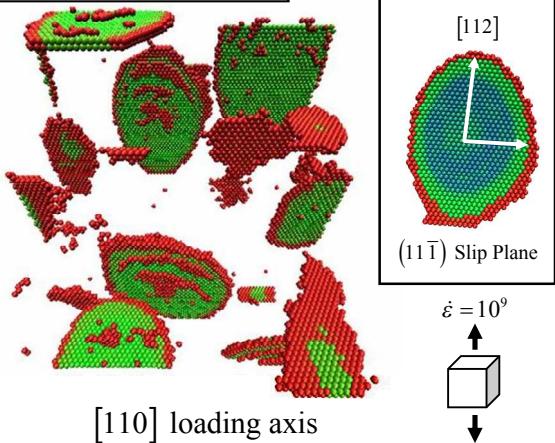
$\Sigma 11 (113) 50.5^\circ$



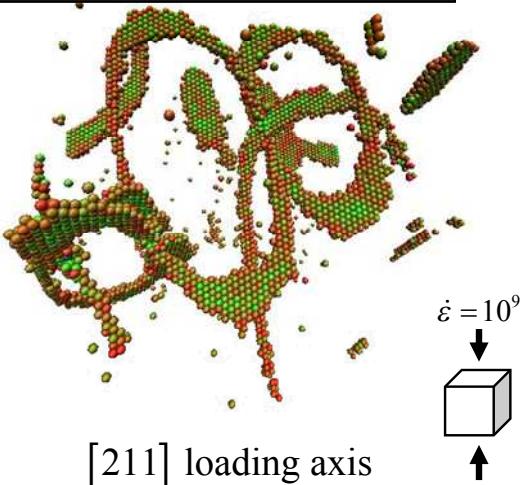
$\Sigma 9 (221) 141.1^\circ$

- General (high-angle) interface structure
 - Structural unit model (SUM) ([Sutton and Vitek, 1983](#))
 - High-angle grain boundaries are composed of combinations of structural units from ‘favored’ orientations

TENSION

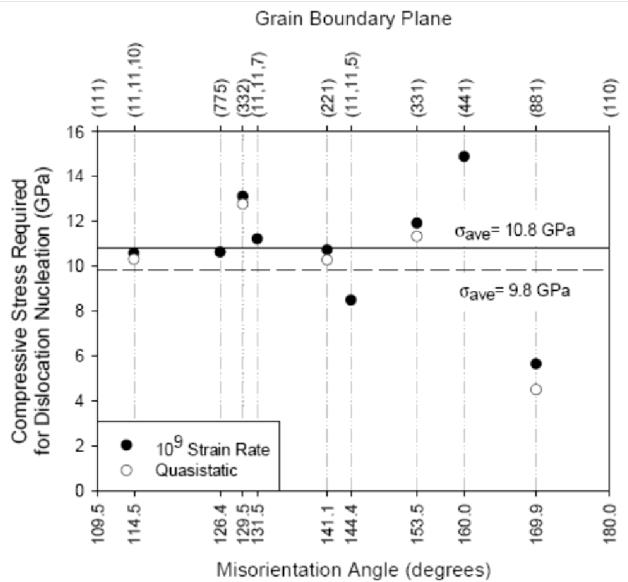
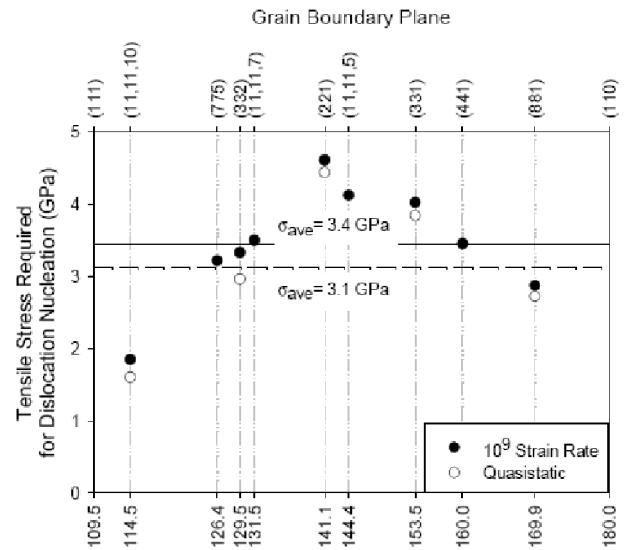
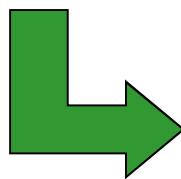


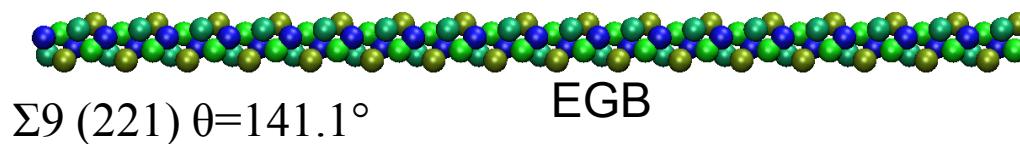
COMPRESSION



<110> GB structures

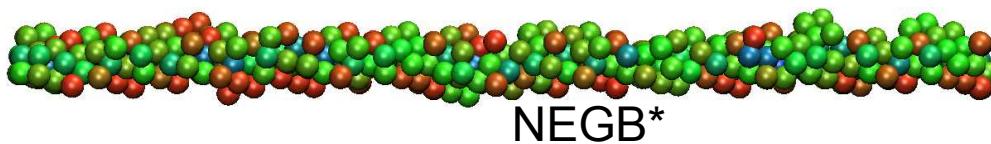
➤ Tschopp, Tucker, McDowell,
Acta Mater. 2008





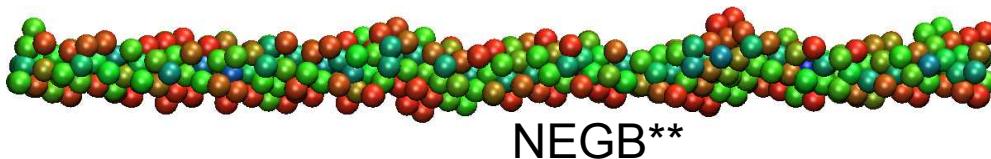
$$\gamma_{GB} = 833 \text{ mJ/m}^2$$

$$FV_{GB} = 6.22e-04$$



$$\gamma_{GB} = 890 \text{ mJ/m}^2$$

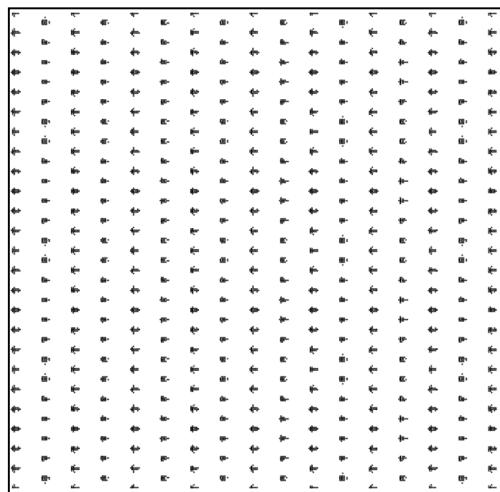
$$FV_{GB} = 6.28e-04$$



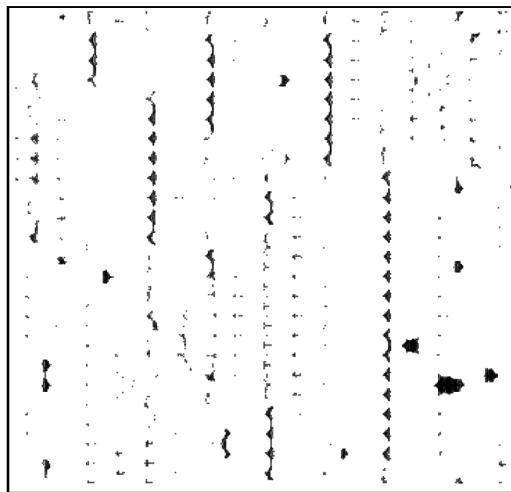
$$\gamma_{GB} = 919 \text{ mJ/m}^2$$

$$FV_{GB} = 7.94e-04$$

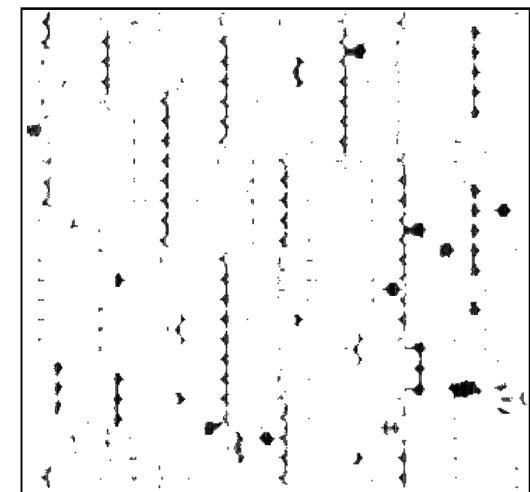
Free Volume (within GB plane)



EGB



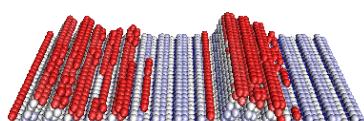
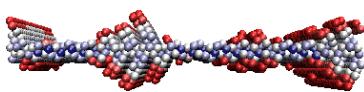
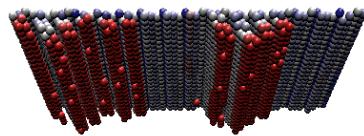
NEGB*



NEGB**

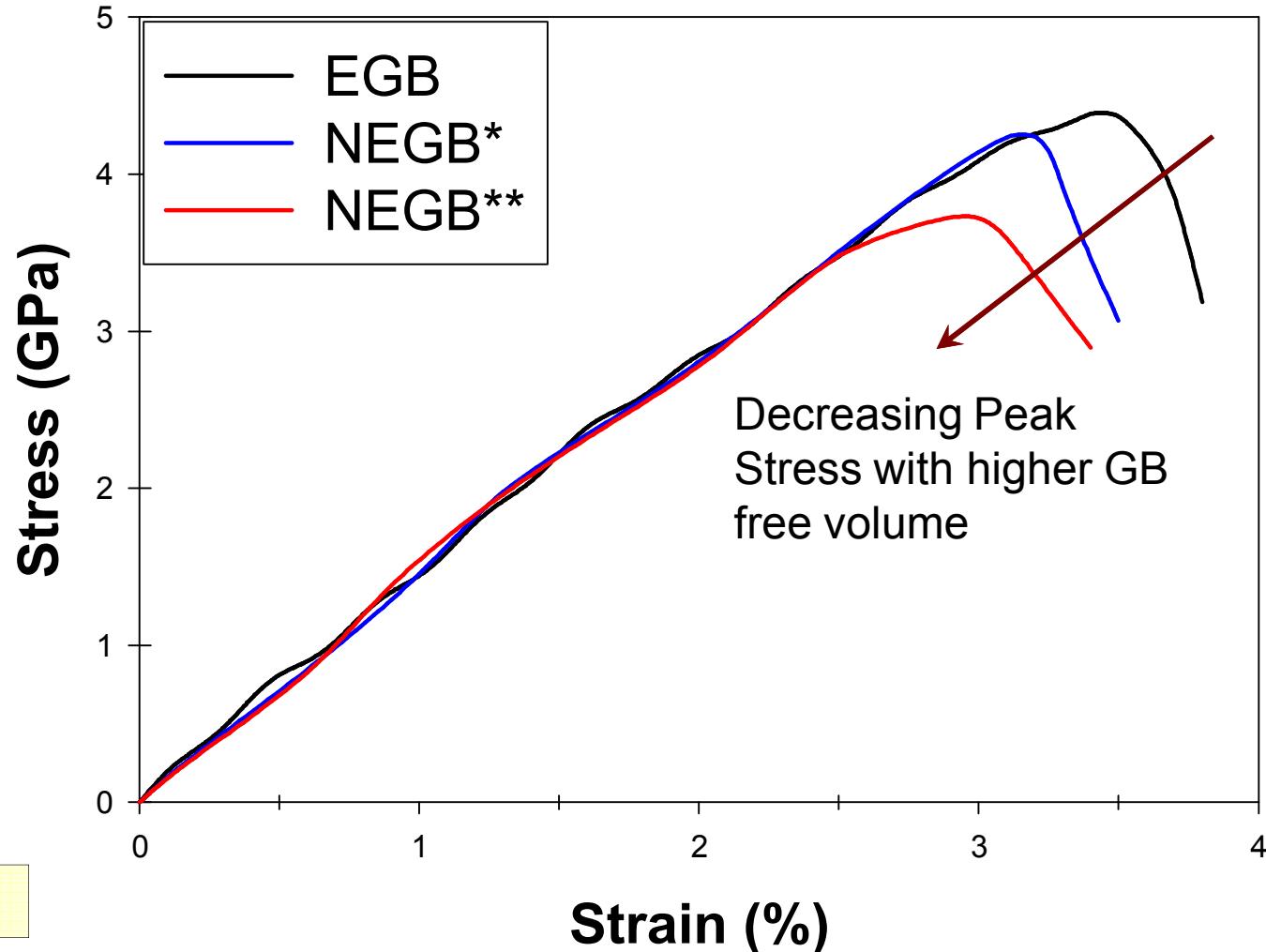
GB Dislocation Nucleation (Tension)

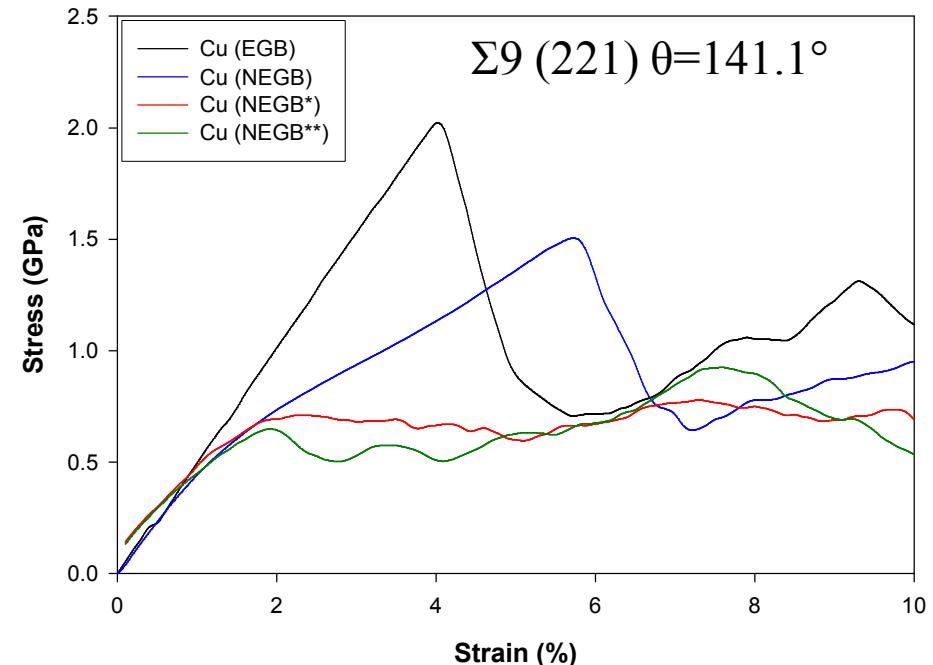
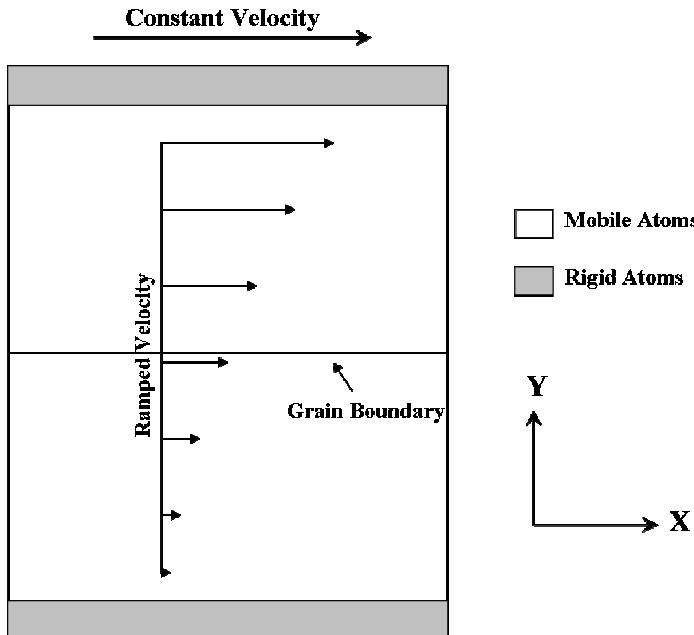
$\Sigma 9 (221) \theta=141.1^\circ$



EGB

$\sigma_{\max} = 4.38 \text{ GPa}$

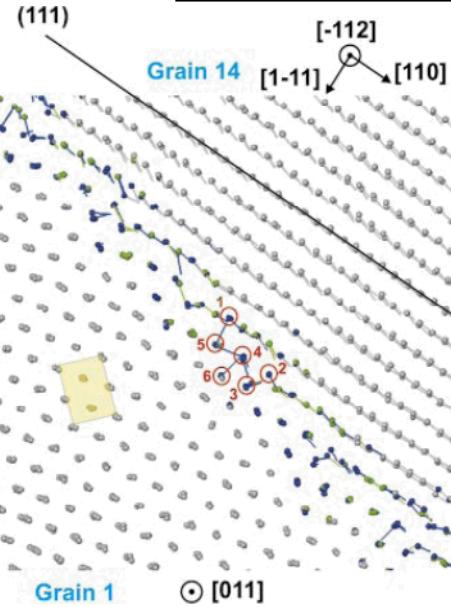




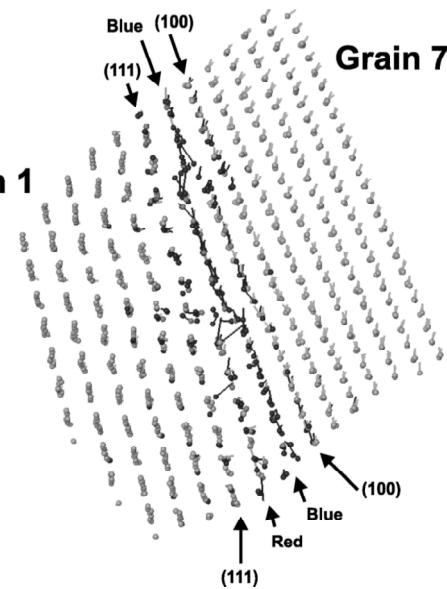
- 2D periodic boundary conditions (parallel to GB plane)
- ‘Constrained’ free vertical faces
- Constant applied velocity deformation
- 10^9 s^{-1} constant shear strain rate
- NVT at 10 K

- Grain boundary sliding and significant atomic shuffling occurs in all boundaries
- Behavior is nearly elastic-perfectly plastic
- Reordering and restructuring processes during hardening stage of NEGGBs

GB Sliding/Atomic Shuffling

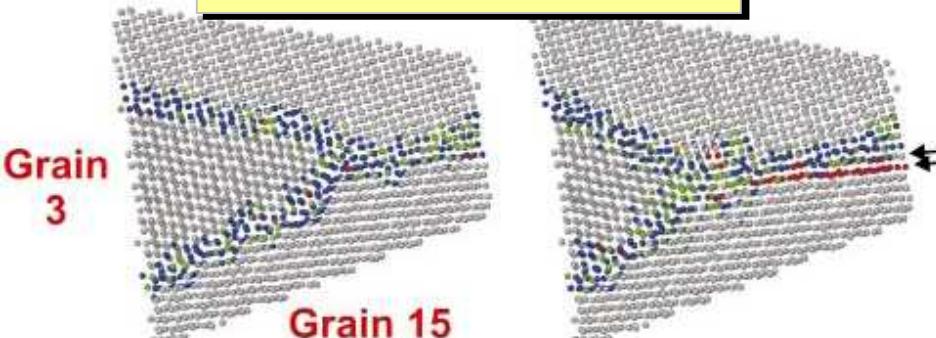


Grain 1



Grain 7

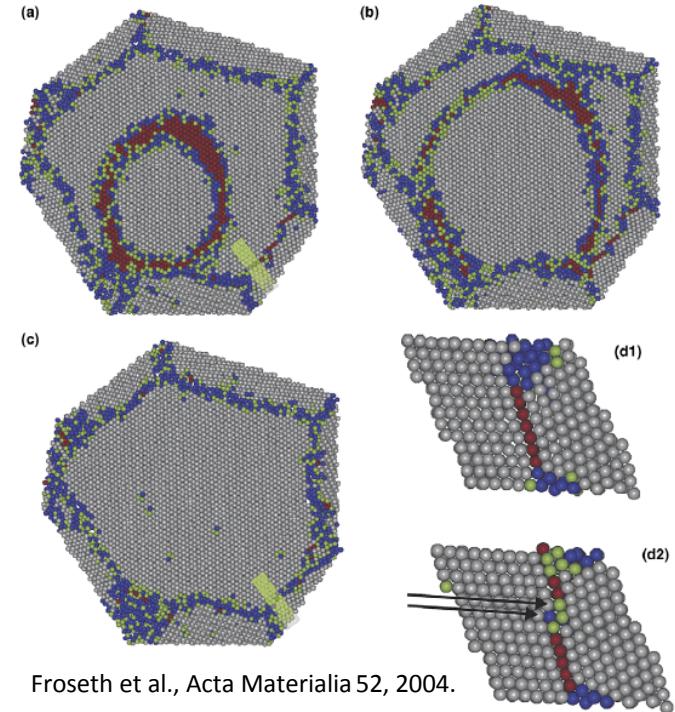
GB/TJ Migration



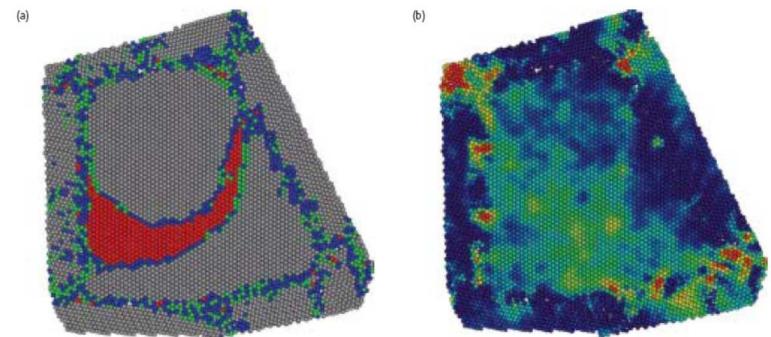
Grain 15

Van Swygenhoven and Derlet., PRB 64, 2001.

Dislocation Nucleation

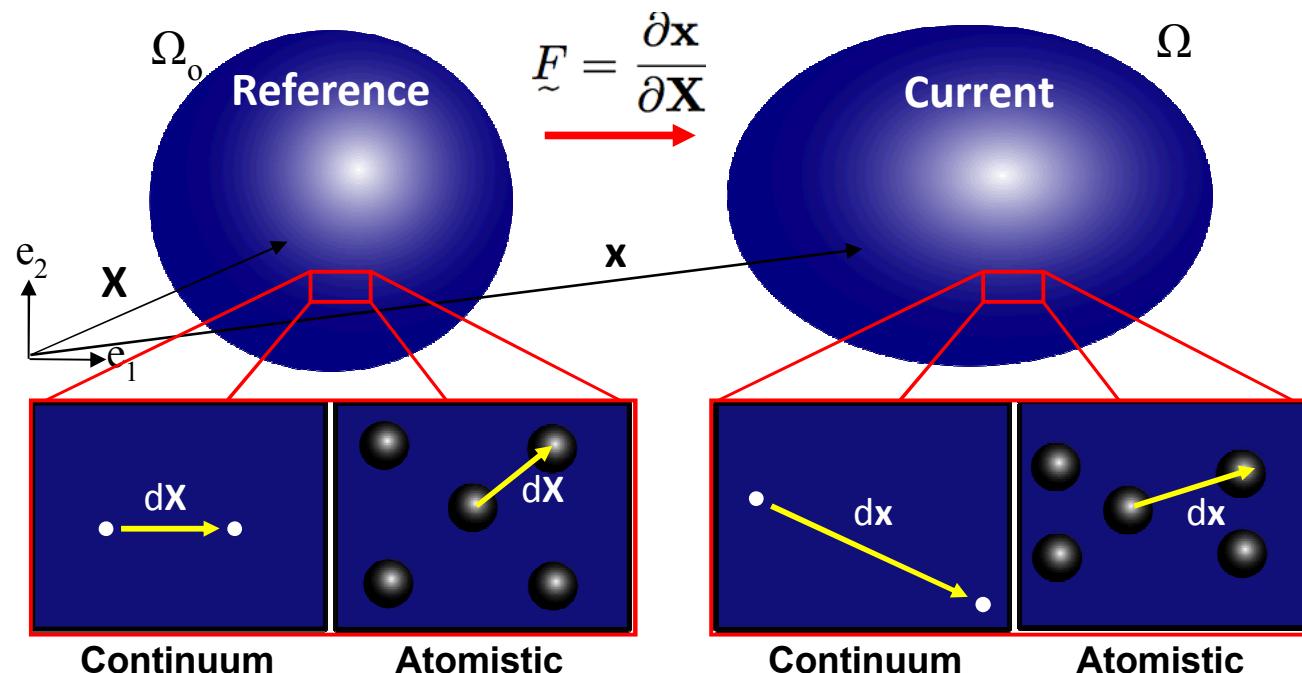


Froseth et al., Acta Materialia 52, 2004.



Van Swygenhoven, Materials Today 9, 2006.

- ✓ Non-Schmid effects
- ✓ Tension-compression asymmetry
- ✓ Competing/combined effects of
 - GB reordering, shuffling/sliding, and/or migration
 - dislocation nucleation/desorption/absorption
- Sensitive to GB network
- Affected by excess free volume – NEGB structures



Deformation Gradient $F_{iI} = \frac{\partial x_i}{\partial X_I} \rightarrow dx_i = F_{iI}dX_I$

$$\sum_{\beta=1}^n (x_i^{\alpha\beta} X_M^{\alpha\beta} - F_{iI}^{\alpha} X_I^{\alpha\beta} X_M^{\alpha\beta}) = 0$$

where

$$\omega_{iM}^{\alpha} = \sum_{\beta=1}^n x_i^{\alpha\beta} X_M^{\alpha\beta} \quad \text{and} \quad \eta_{IM}^{\alpha} = \sum_{\beta=1}^n X_I^{\alpha\beta} X_M^{\alpha\beta}$$

$$\longrightarrow F_{iI}^{\alpha} = \omega_{iM}^{\alpha} (\eta^{\alpha})_{MI}^{-1}$$

Deformation Gradient



* Zimmerman *et al.*, IJSS (2009)

See also Gullett *et al.* MSMSE (2008),
Hartley and Mishin (2005)

- $\tilde{F} = \tilde{R} \tilde{U}$ where $\tilde{R} = \tilde{R}_{sym} + \tilde{R}_{skew}$
 - $\tilde{R}_{skew} = \frac{1}{2}(\tilde{R} - \tilde{R}^T)$ → $\boxed{\phi_k} = -\frac{1}{2}\epsilon_{ijk}(\tilde{R}_{skew})_{ij}$
microrotation vector
- $\tilde{L} = \tilde{D} + \tilde{W}$
 - $\tilde{W} = \frac{1}{2}(\tilde{L} - \tilde{L}^T)$ → $\boxed{\omega_k} = -\frac{1}{2}\epsilon_{ijk}W_{ij}$
vorticity vector

• Tucker, G.J., Zimmerman, J.A., and McDowell, D.L., MSMSE 18(1) 2010, 015002.

• Tucker, G.J., Zimmerman, J.A., and McDowell, D.L., Int. J. Engineering Science in memoriam to C. Eringen, in press.

Metal plasticity at the nanoscale is complex

- Use of centrosymmetry, CN, slip vector, etc. is complicated in terms of characterization and visualization of high density of evolving line defects
- These continuum metrics can address either history of process or current configuration – useful for understanding mechanisms

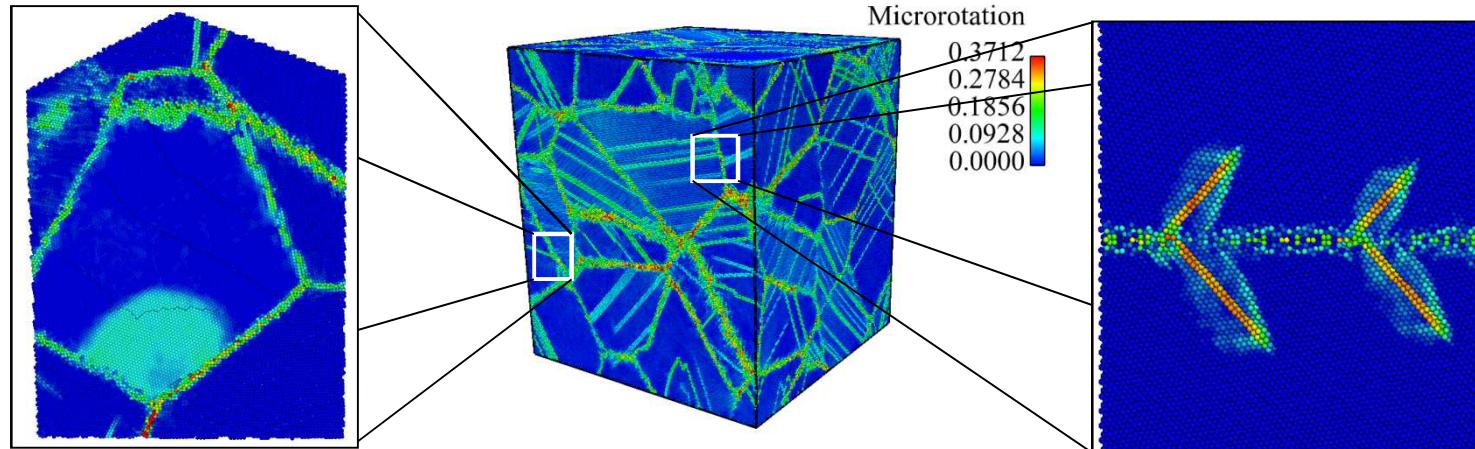
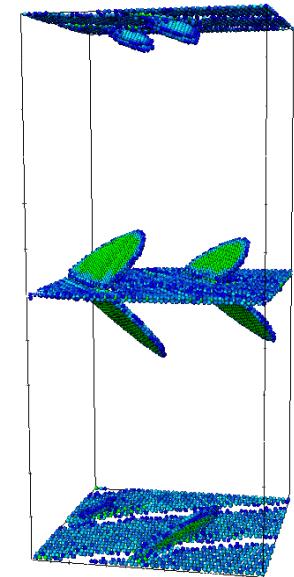
Informing continuum models

- Kinematics of continuum description can perhaps be bridged in terms of understanding based on statistical fields from atomistic simulations
- Check assumptions, trends from proposed continuum constitutive models (e.g., Khan et al. (2006), Capolungo et al. (2007), Wei and Anand (2004) and Wei et al.(2006))

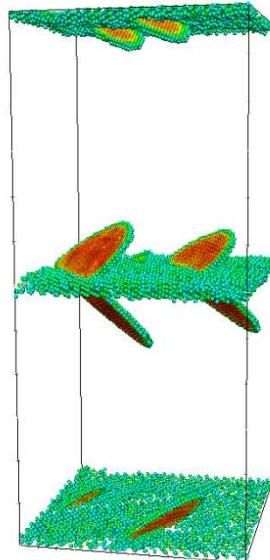
Some connections

- microrotation (Φ) gradient [Atomistics]
- torsion-flexure tensor [Continuum]

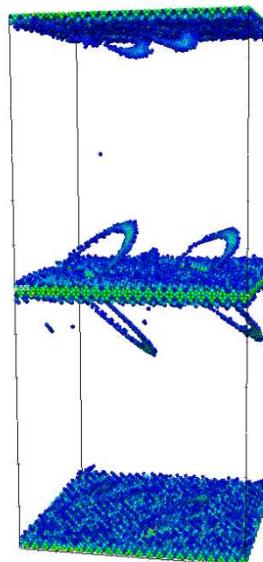
- ❖ Formulate nonlocal metrics from continuum mechanics for use in atomistic simulation analysis
- ❖ Investigate the evolution of kinematic metrics for various deformation mechanisms in NC metals
- ❖ Resolve the contribution of different deformation mechanisms during uniaxial deformation of NC copper
 - ❖ Dislocation Nucleation
 - ❖ GB Sliding/Atomic Shuffling



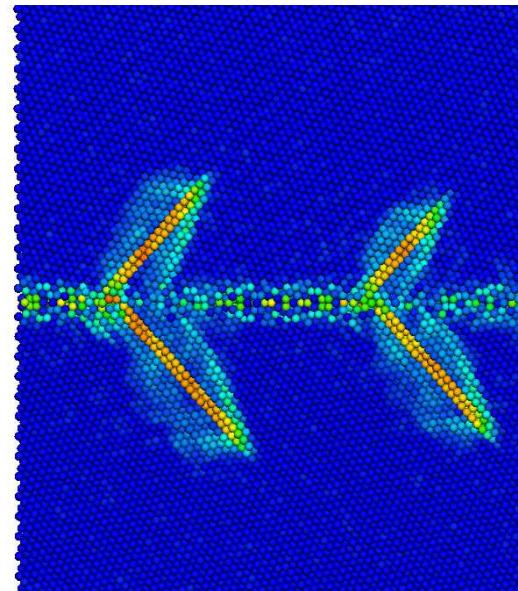
- Tucker, G.J., Zimmerman, J.A., and McDowell, D.L., MSMSE 18(1) 2010, 015002.
- Tucker, G.J., Zimmerman, J.A., and McDowell, D.L., Int. J. Engineering Science in memoriam to C. Eringen, in press.



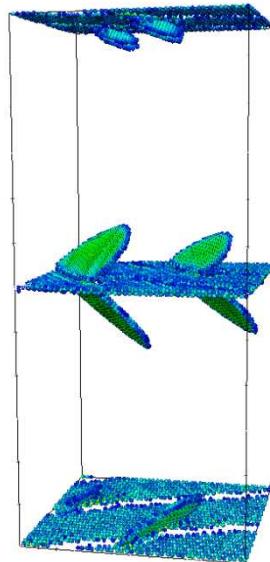
Slip Vector
1.4974
1.2395
0.9815
0.7236
0.4657



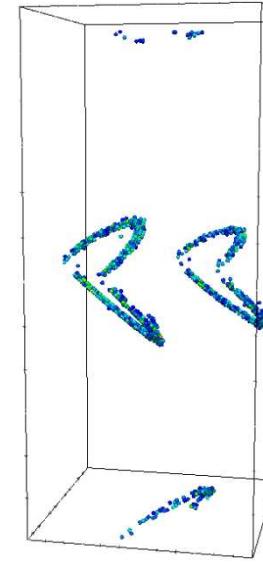
Energy
-3.2790
-3.3326
-3.3863
-3.4399
-3.4935



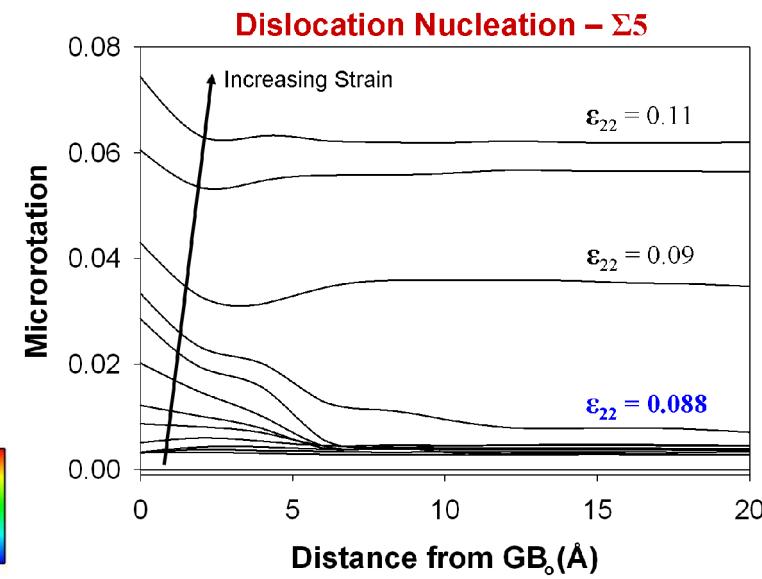
Microrotation
0.083619
0.063488
0.043358
0.023227
0.003097



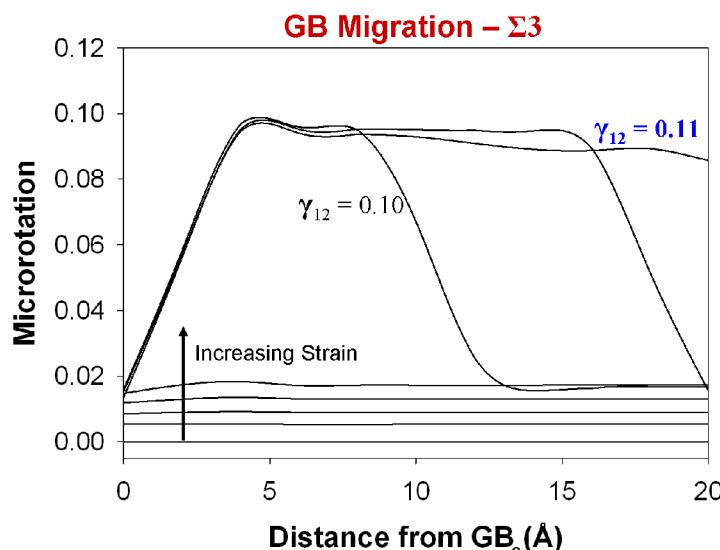
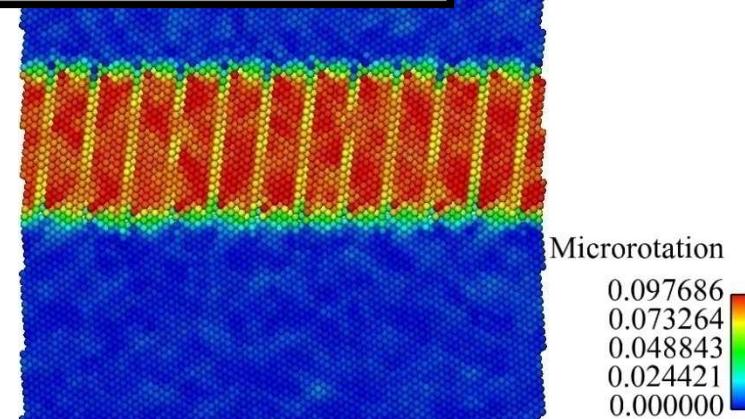
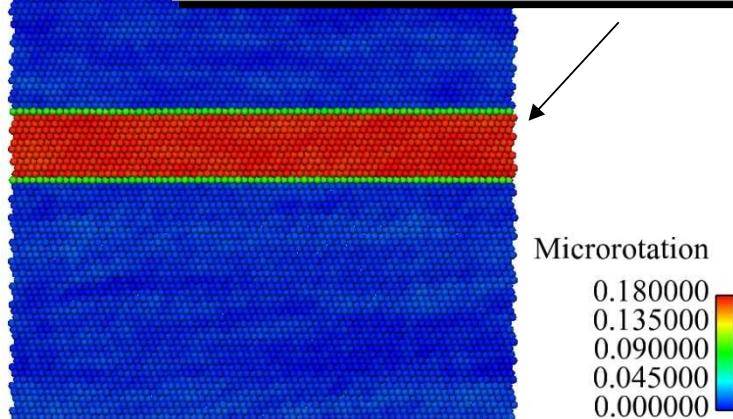
Microrotation
0.101506
0.086130
0.070753
0.055376
0.040000



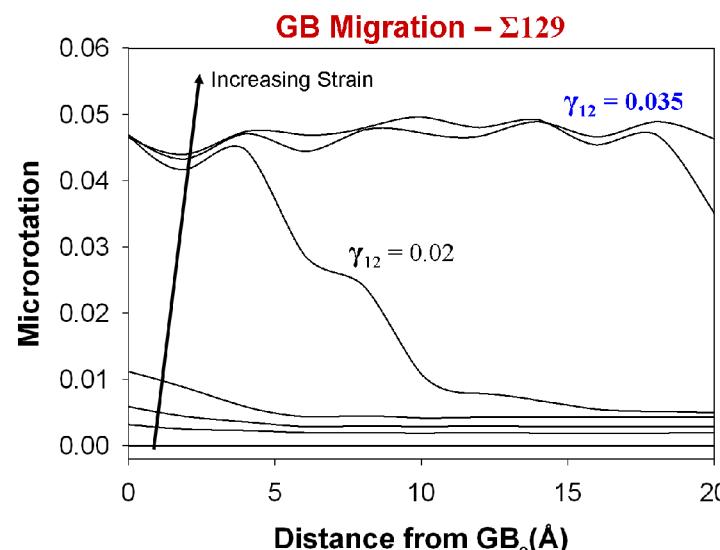
Vorticity
0.3739
0.3342
0.2945
0.2547
0.2150



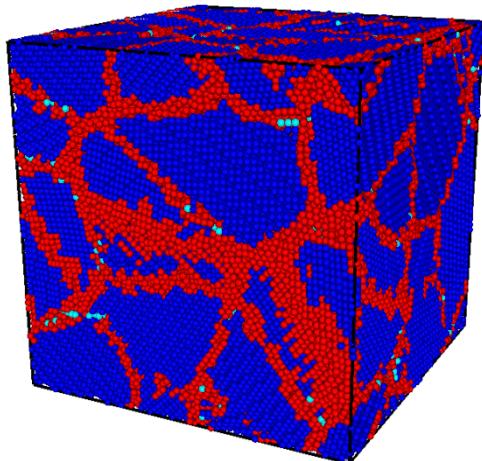
Can distinguish differences in deformation fields produced during GB migration



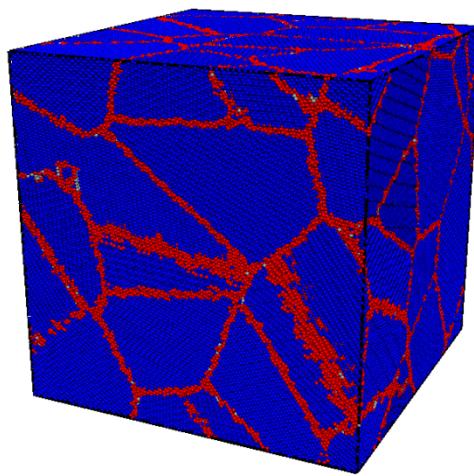
Average microrotation over slices \parallel to boundary



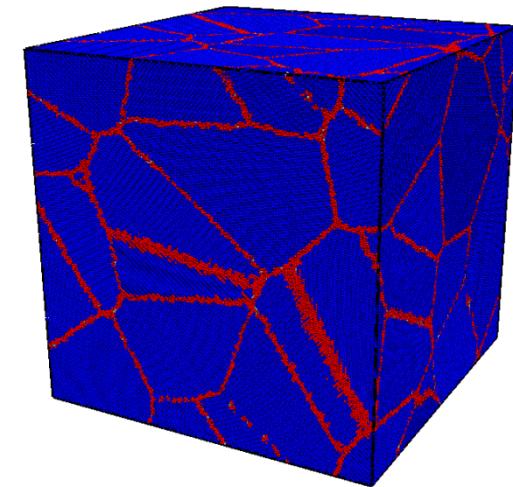
 FCC  Other



$\langle d_{gr} \rangle = 5\text{nm}$

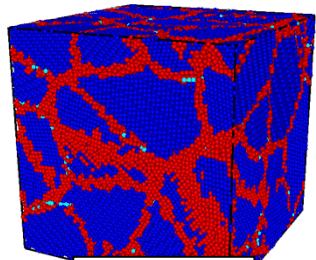


$\langle d_{gr} \rangle = 10\text{nm}$

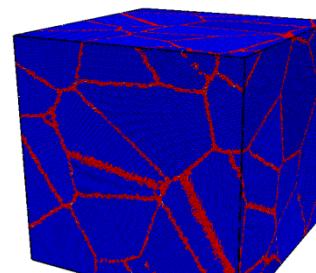


$\langle d_{gr} \rangle = 15\text{nm}$

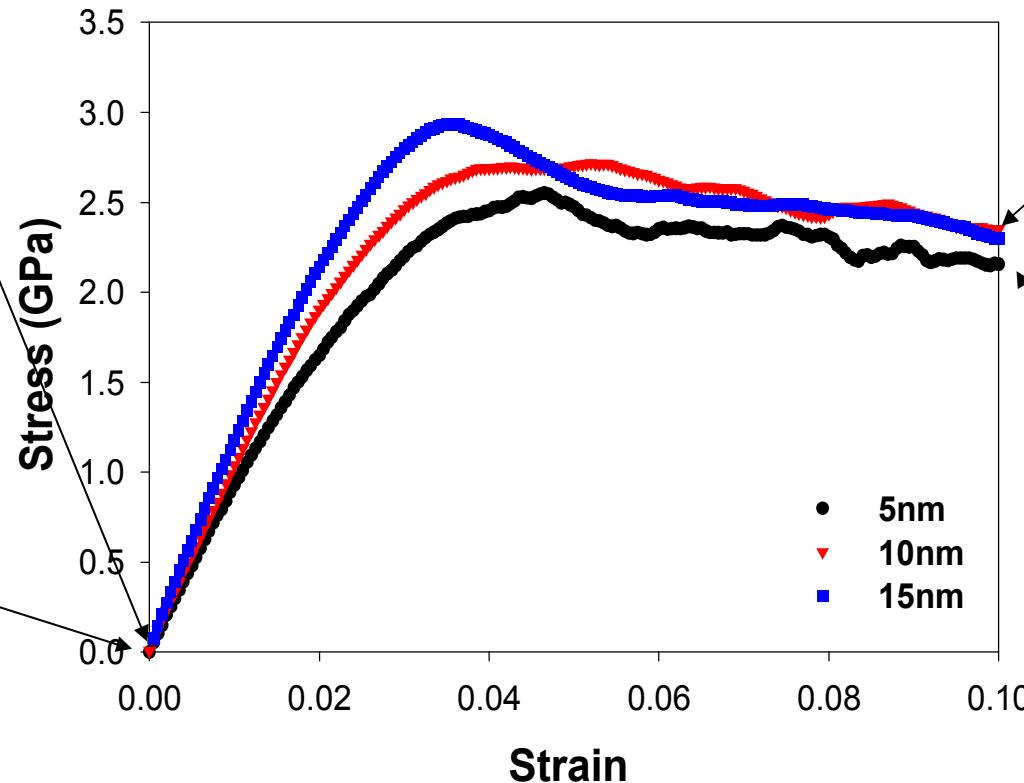
- Full 3D nanocrystalline structure (Voronoi Tessellation, random lattice orientations)
- 3D periodic BCs
- Atom overlap deletion and equilibration for 50 ps at 10K
- Uniaxial tension at 10K under NPT, constant strain rate of 10^9 s^{-1}
- Analysis of deformation mechanisms using microscale continuum metrics



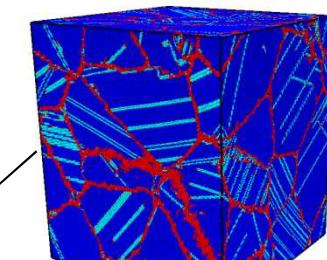
5nm



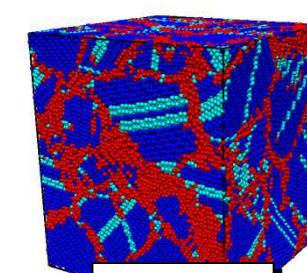
15nm



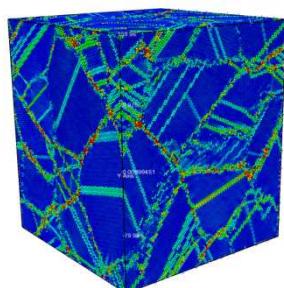
- 5nm
- ▼ 10nm
- 15nm



15nm

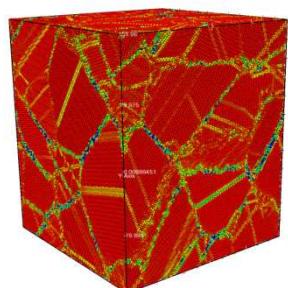


5nm



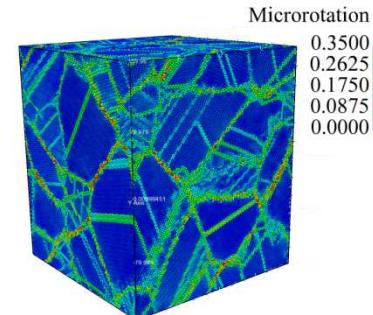
F22
1.70
1.53
1.35
1.17
1.00

Deformation Gradient



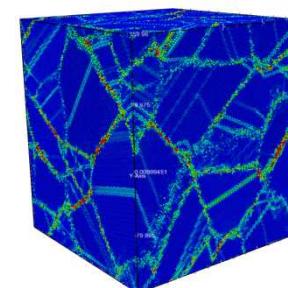
Rotation Metric

R22
1.00
0.95
0.90
0.85
0.80



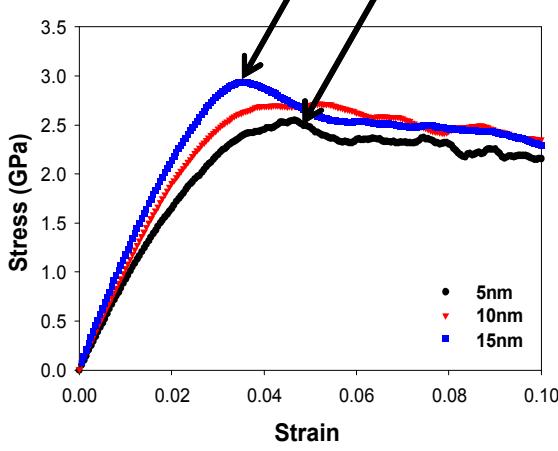
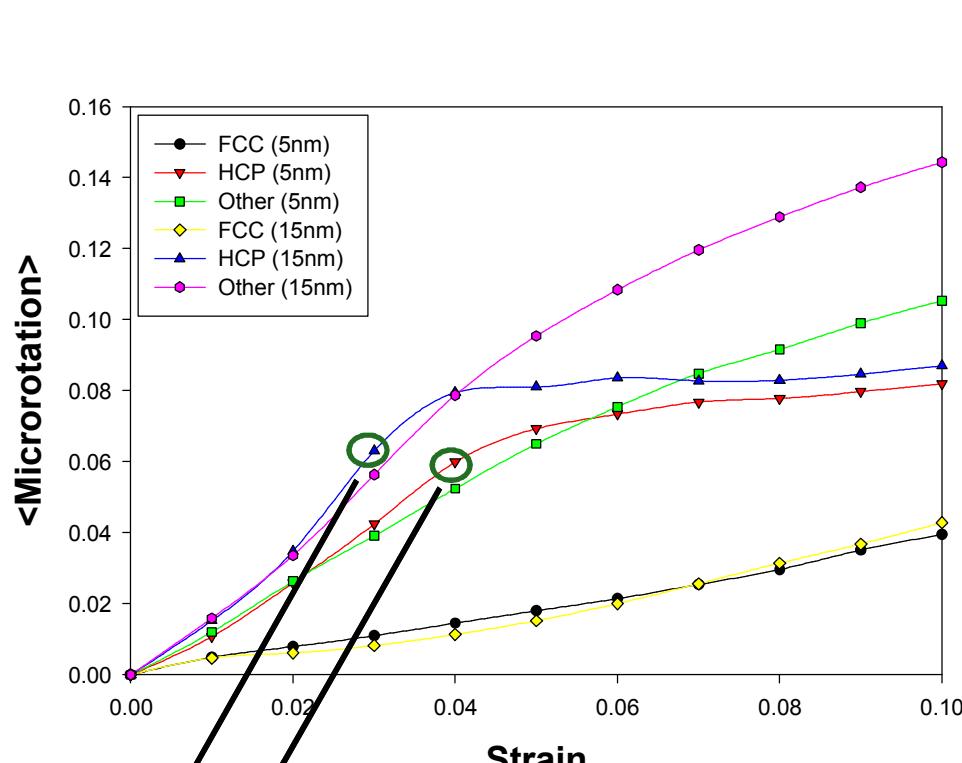
Microrotation

0.3500
0.2625
0.1750
0.0875
0.0000

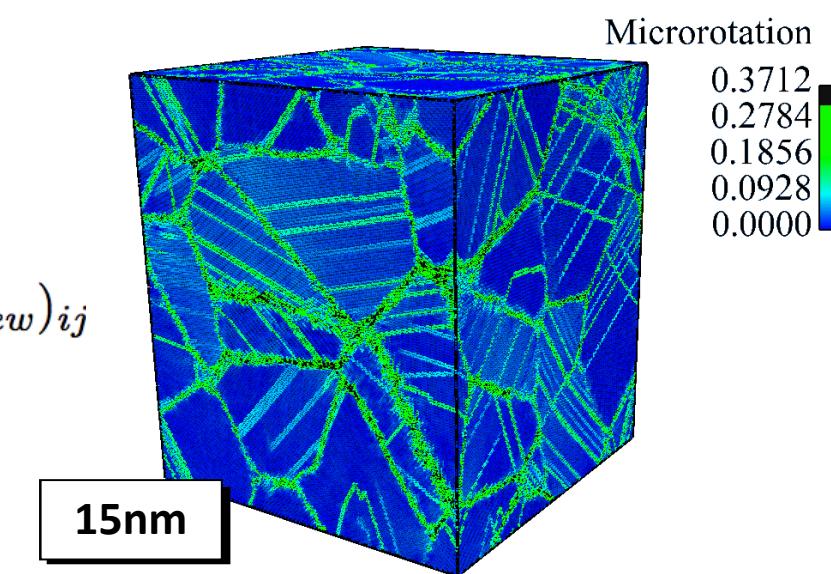
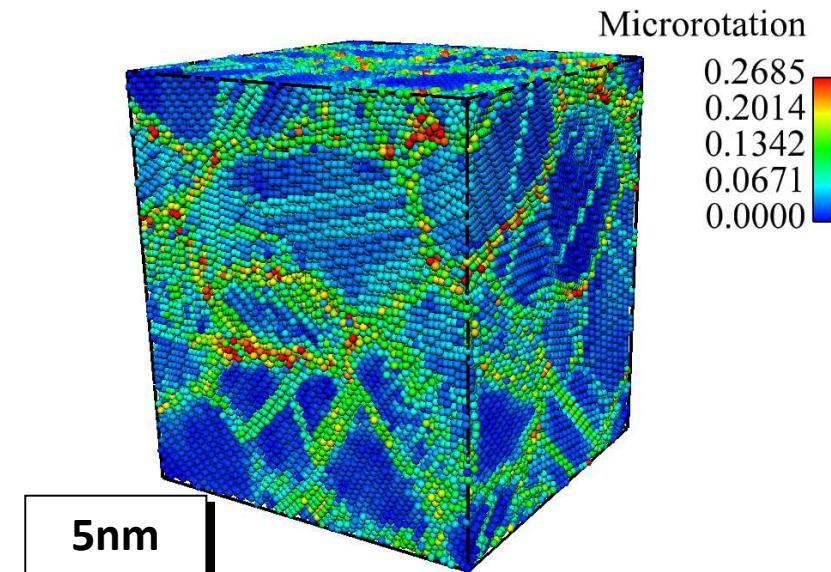


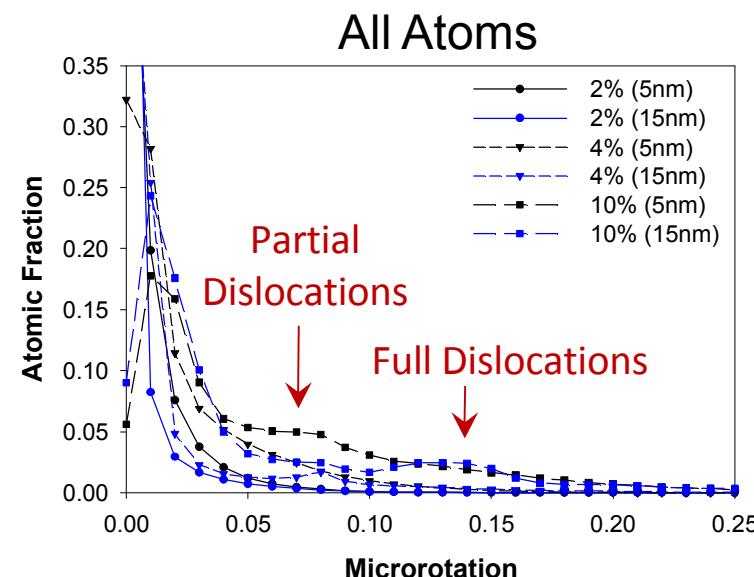
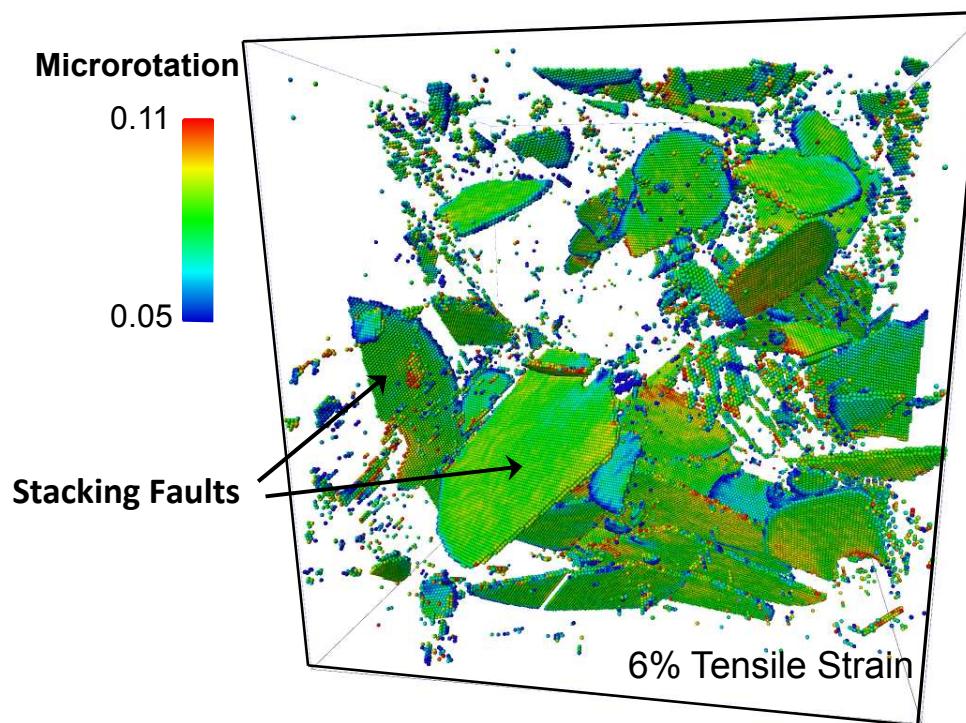
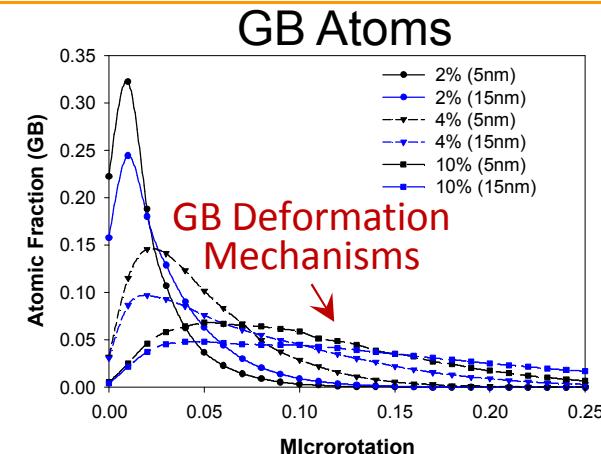
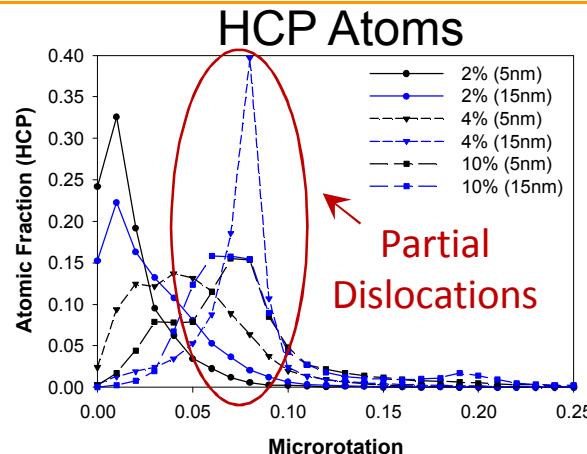
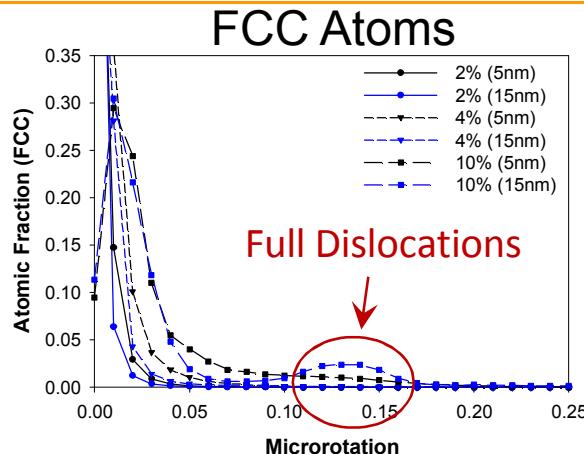
Dilatation

1.25
0.94
0.63
0.31
0.00

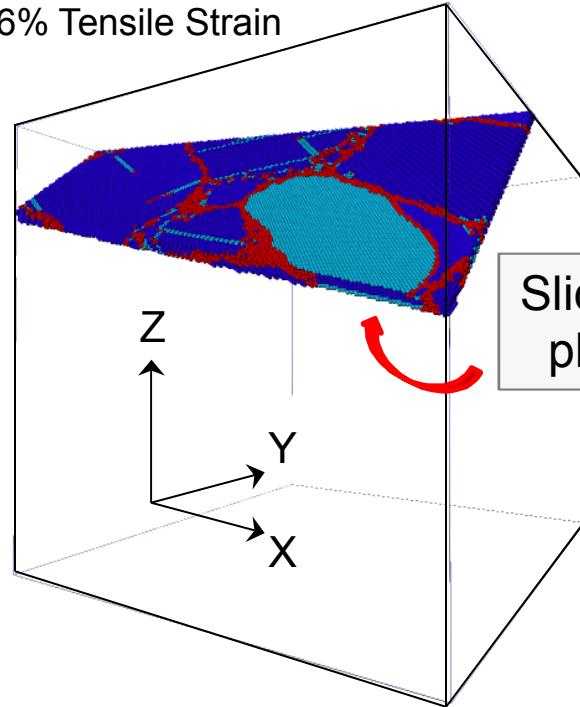


$$\phi_k = -\frac{1}{2}\epsilon_{ijk}(R_{skew})_{ij}$$

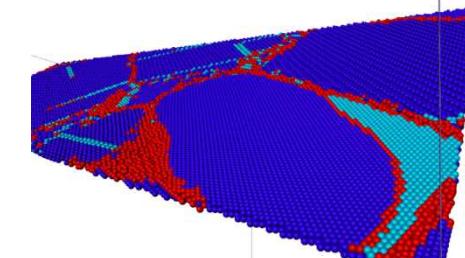
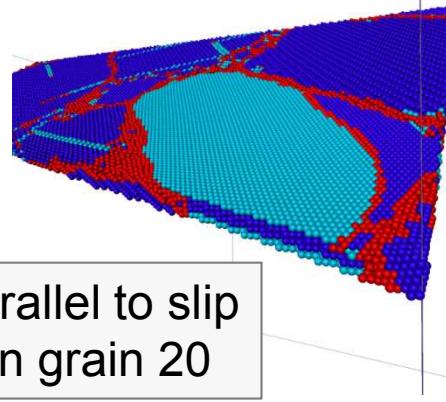




6% Tensile Strain



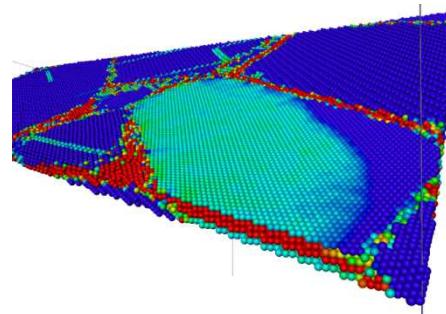
Slice parallel to slip
plane in grain 20



CNA

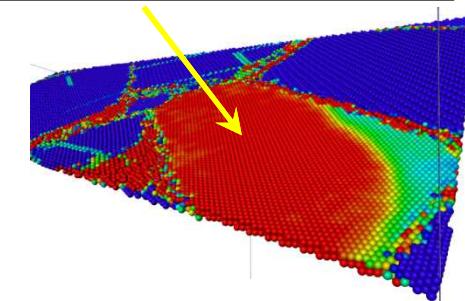
5
2
1

Microrotation
captures twinning



Microrotation

0.16
0.05



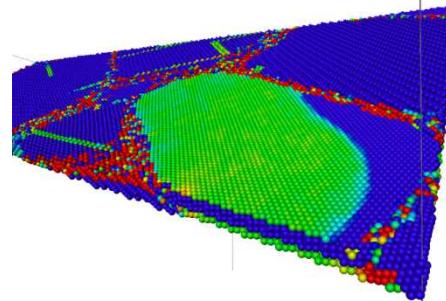
Slip Vector

1.8
1.1

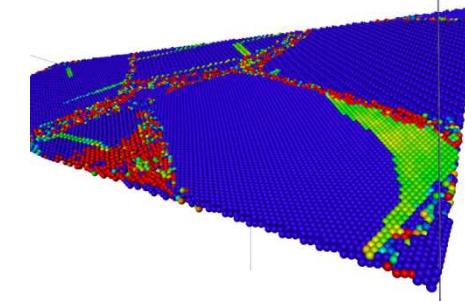


- *Microrotation* is able to capture important deformation behavior (e.g. **dislocation slip**) and structural features (e.g. **stacking fault**) usually visualized using **CNA** and atomic **slip vector** together.
- Potential to be passed into continuum level models as kinematic variable.

4 Atomic Planes



2 Atomic Planes

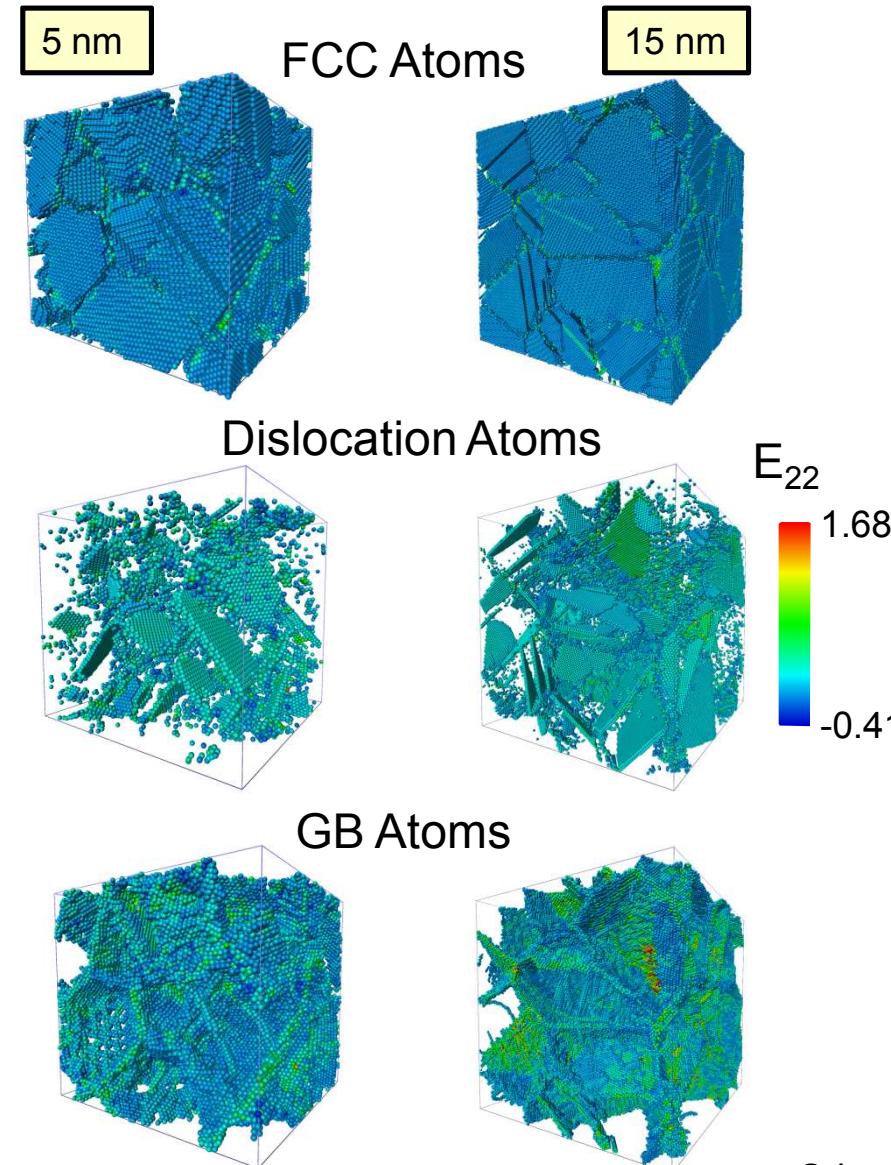
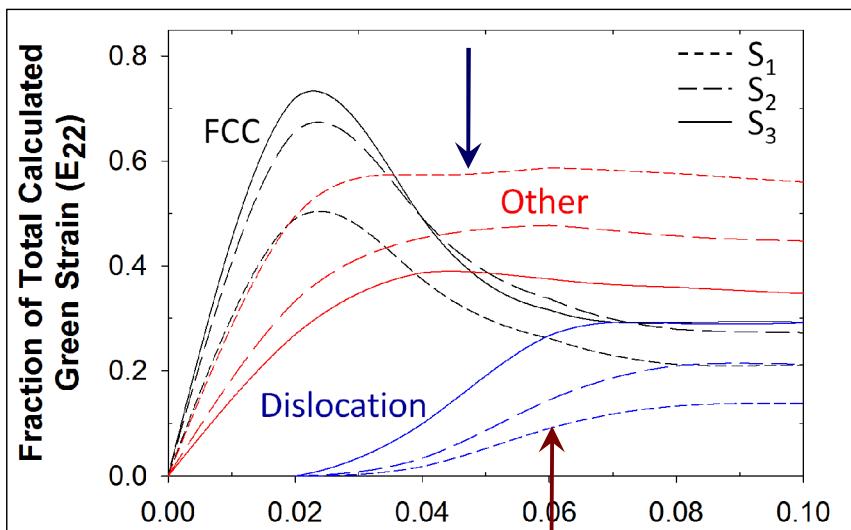


!0

Green Strain Tensor

$$\mathbf{E} = \frac{1}{2} (\mathbf{F}^T \cdot \mathbf{F} - \mathbf{I})$$

- E_{22} from all atoms in a group (e.g. FCC, GB, Dislocation).
- Overall, GBs account for a higher fraction of tensile strain in smaller grain structures. In contrast, *dislocation activity accounts for a higher fraction in larger grain structures*.



- Different mechanisms provide distinct kinematic signatures and a sense of deformation history is captured by certain metrics.
- The non-locality of various mechanisms can be probed by employing the volume-averaging scheme using atomic neighbor lists (*1st, 2nd, 3rd, and reference/current*).
- Insight into complex deformation landscape in NC materials is provided through the implementation of microscale continuum metrics, and we can begin to resolve mechanism contributions to overall deformation.
- Deformation avalanches are of interest (inversion points and plateaus), also from point of view of distribution of shedding of microkinetic energy.
 - ❖ Investigate tension/compression asymmetry and stress-state dependent behaviors
 - ❖ Quantify the distribution of dislocation slip vs. GB processes during deformation as a function of grain size.



- **NSF CMMI #0758265** - Multiresolution, Coarse-Grained Modeling of 3D Dislocation Nucleation and Migration (metrics)
- **NSF DMI #1030103** - Methods for Atomistic Input into Initial Yield and Plastic Flow Criteria for Nanocrystalline Materials (nanocrystals)
- **Dr. Jonathan Zimmerman (Sandia National Labs)**
- Sandia National Laboratories (*EPSRI Internship – Summer 2008*)
- Carter N. Paden Jr. Distinguished Chair in Metals Processing
- **NSF TeraGrid** Science Gateways program.



* Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.