

A GLOBAL 3D P-VELOCITY MODEL OF THE EARTH'S CRUST AND MANTLE FOR IMPROVED SEISMIC EVENT LOCATION

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W. Scott Phillips²

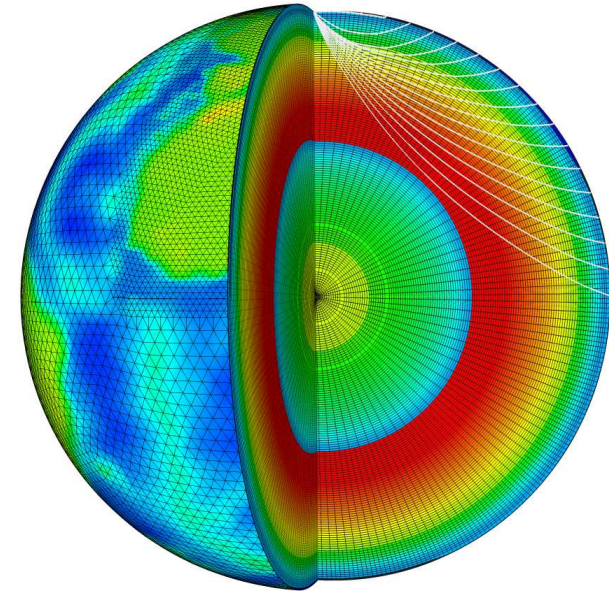
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Introduction

- Monitoring the CTBT requires the ability to quickly locate small seismic events anywhere on the Earth with great accuracy and precision.
- This requires the ability to accurately predict the travel time of seismic energy from source to receiver, at local, regional and teleseismic distance ranges.
- The accuracy and precision of travel time prediction is directly related to the fidelity of the Earth models used to make the predictions.
- To date, monitoring agencies have used 1D and 2½D Earth models for travel time prediction, which cannot match the accuracy and precision of full 3D Earth models.
- In this study, we have developed a full 3D velocity model of the Earth's crust and mantle with the single-minded goal of improving the accuracy and precision of seismic event locations.
- Included with our model is software that meets demanding computational requirements.

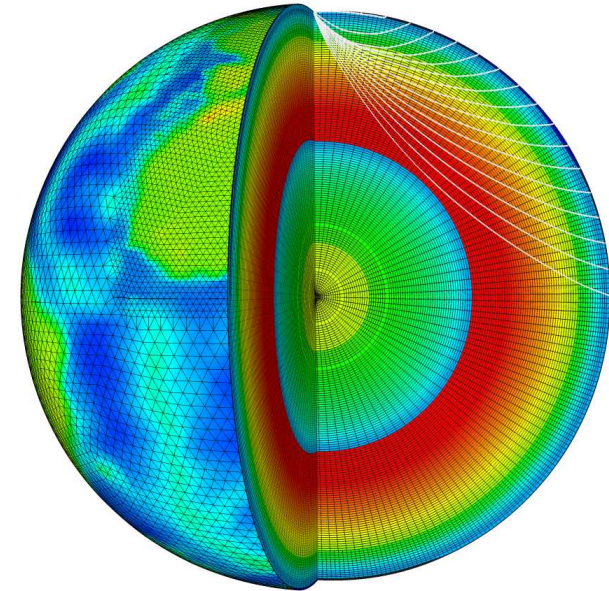
SALSA3D



Outline

- **Tomography**
 - Data
 - Adaptive Gridding
 - Results
- **Validation**
 - Travel time residuals
 - Test Events
- **Model Uncertainty**
 - Model Covariance Matrix

SALSA3D



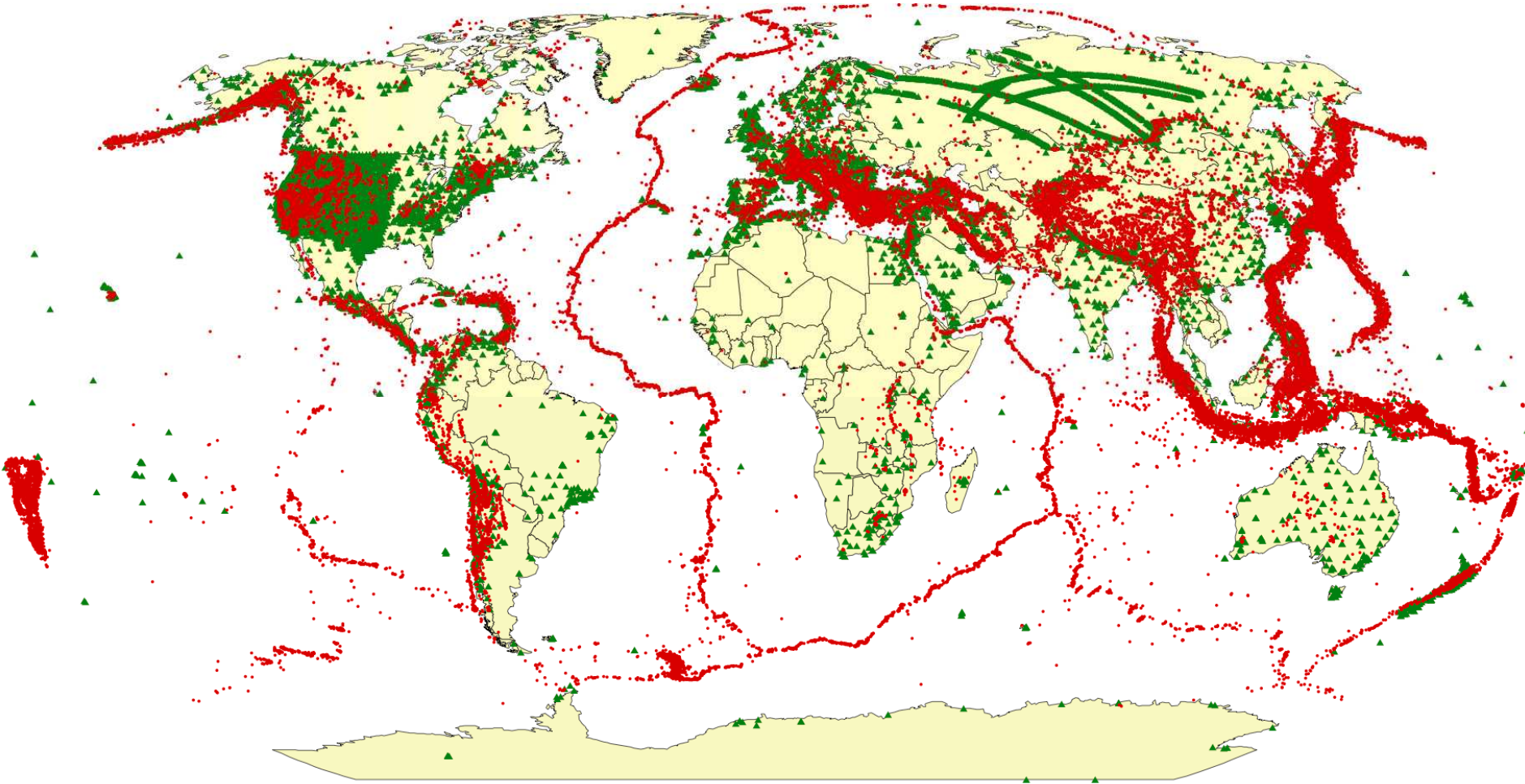
Data

Ground Truth (GT) 25 km or better *(Bondár et al., 2004)*

122K events

13K stations

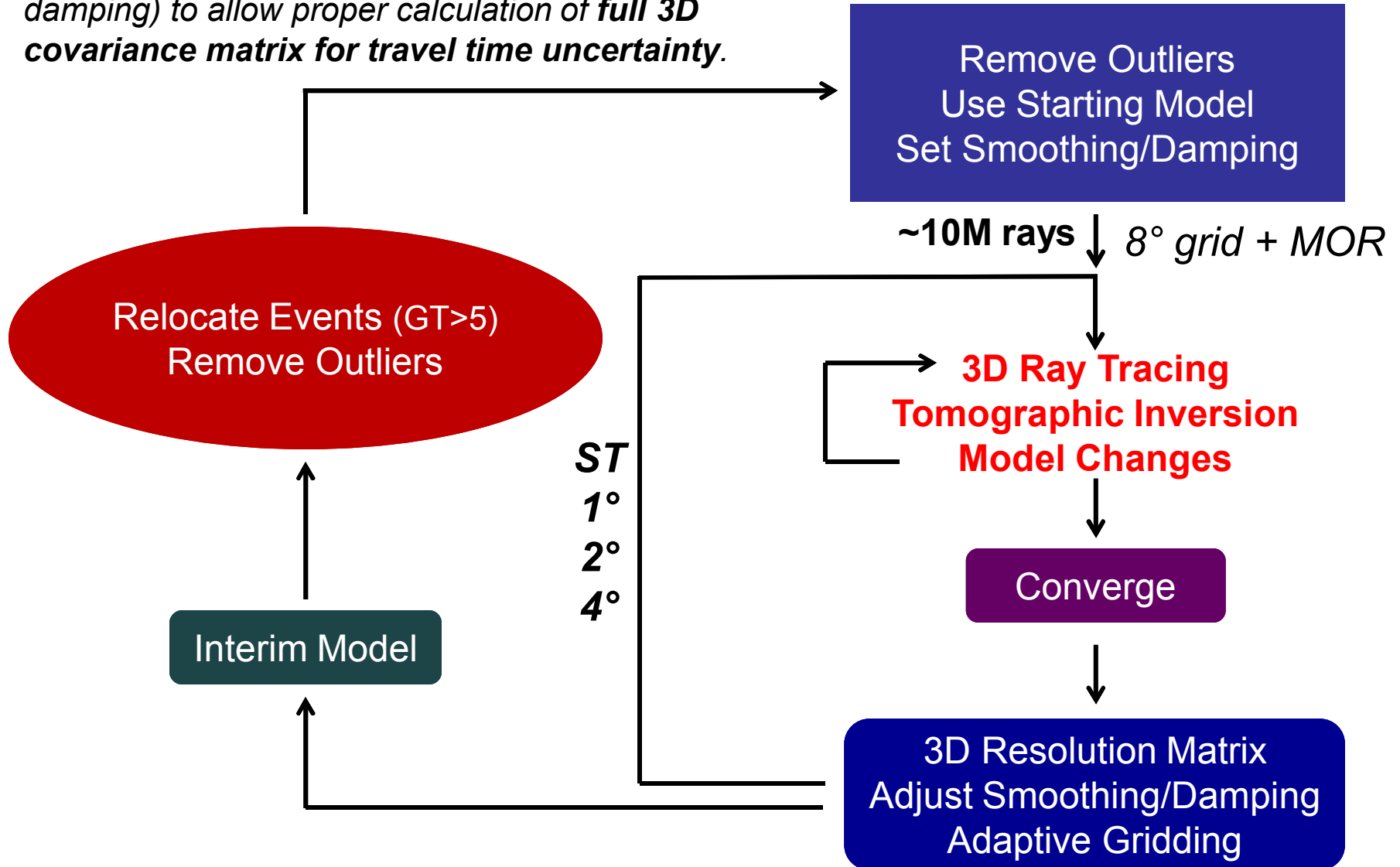
10M ray paths



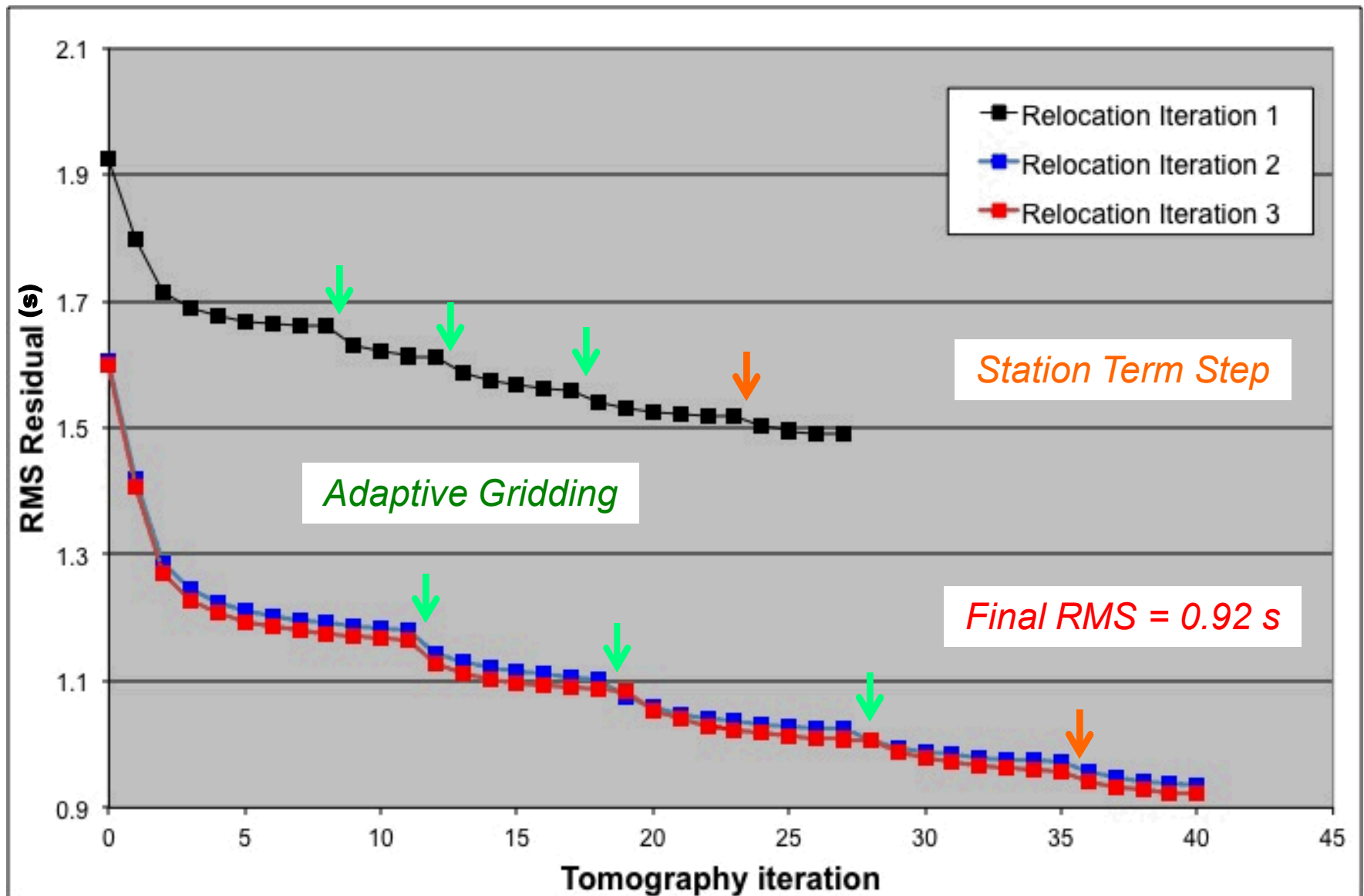
Tomographic Procedure

LSQR algorithm of Paige and Saunders (1982)

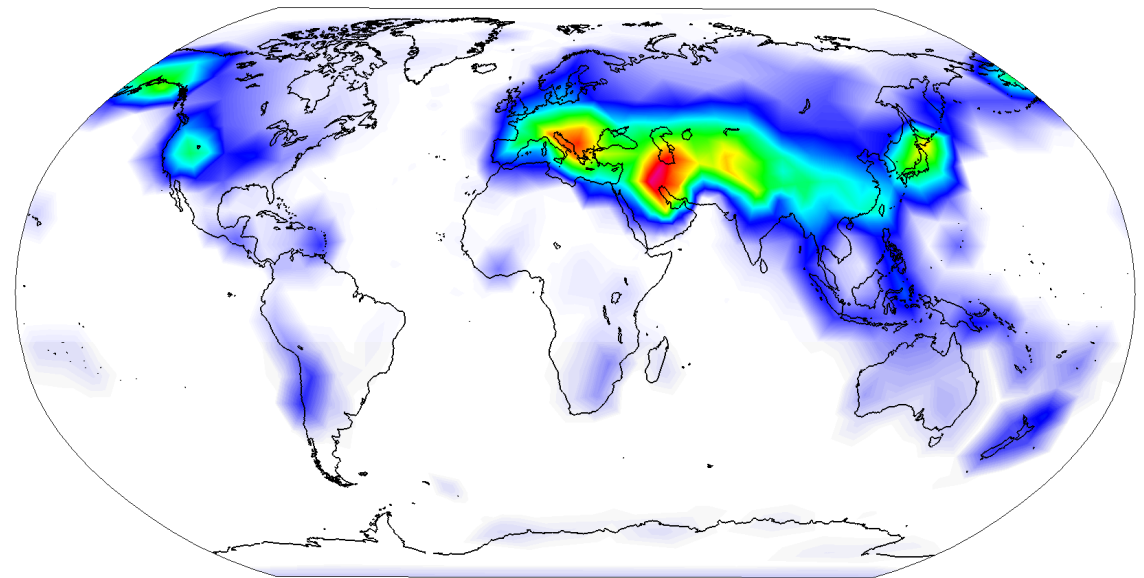
*Model Slowness Uncertainties added (smoothing, damping) to allow proper calculation of **full 3D covariance matrix for travel time uncertainty.***



Tomography Iterations and RMS



Variable Resolution Grids

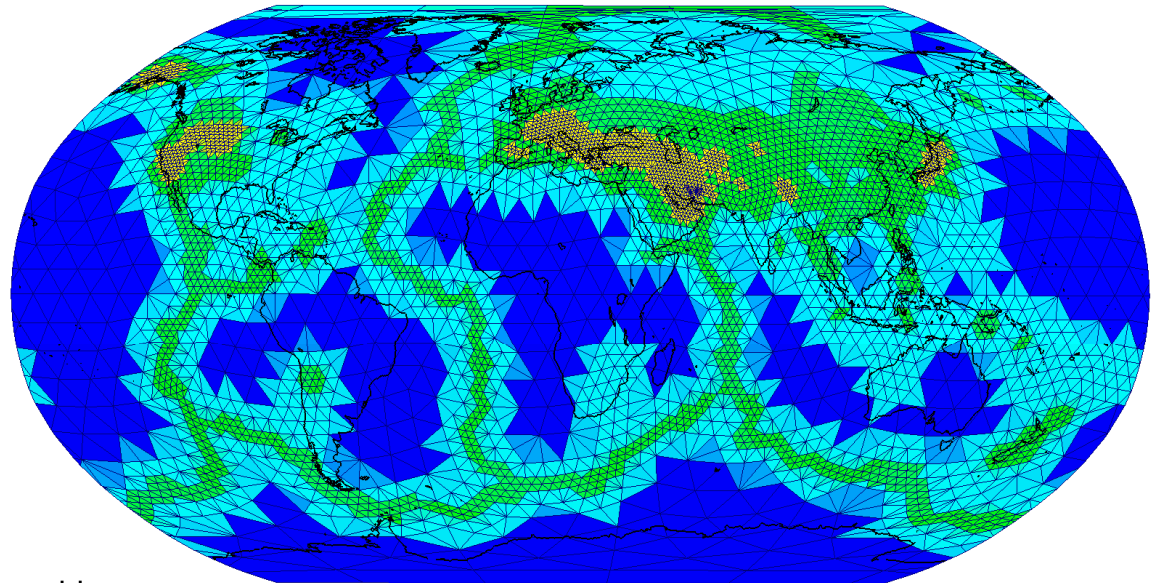


Upper Mantle

RESOLUTION

0 0.2 0.4 0.5

First Refinement



Upper Mantle

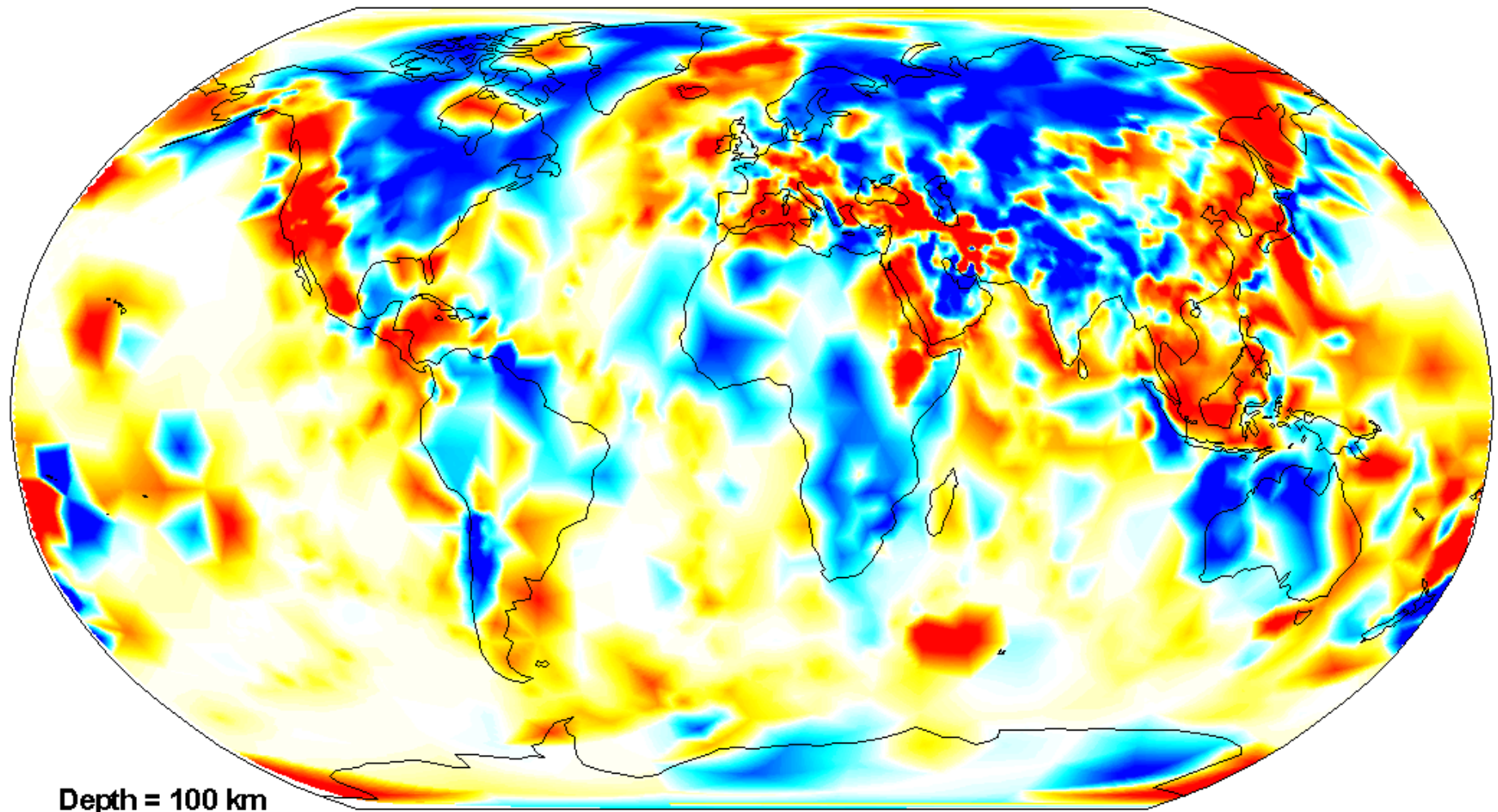
Triangle Size (degrees)

0 2 4 6 8

Third Refinement

Grids are constructed and managed using GeoTess open source software
www.sandia.gov/geotess

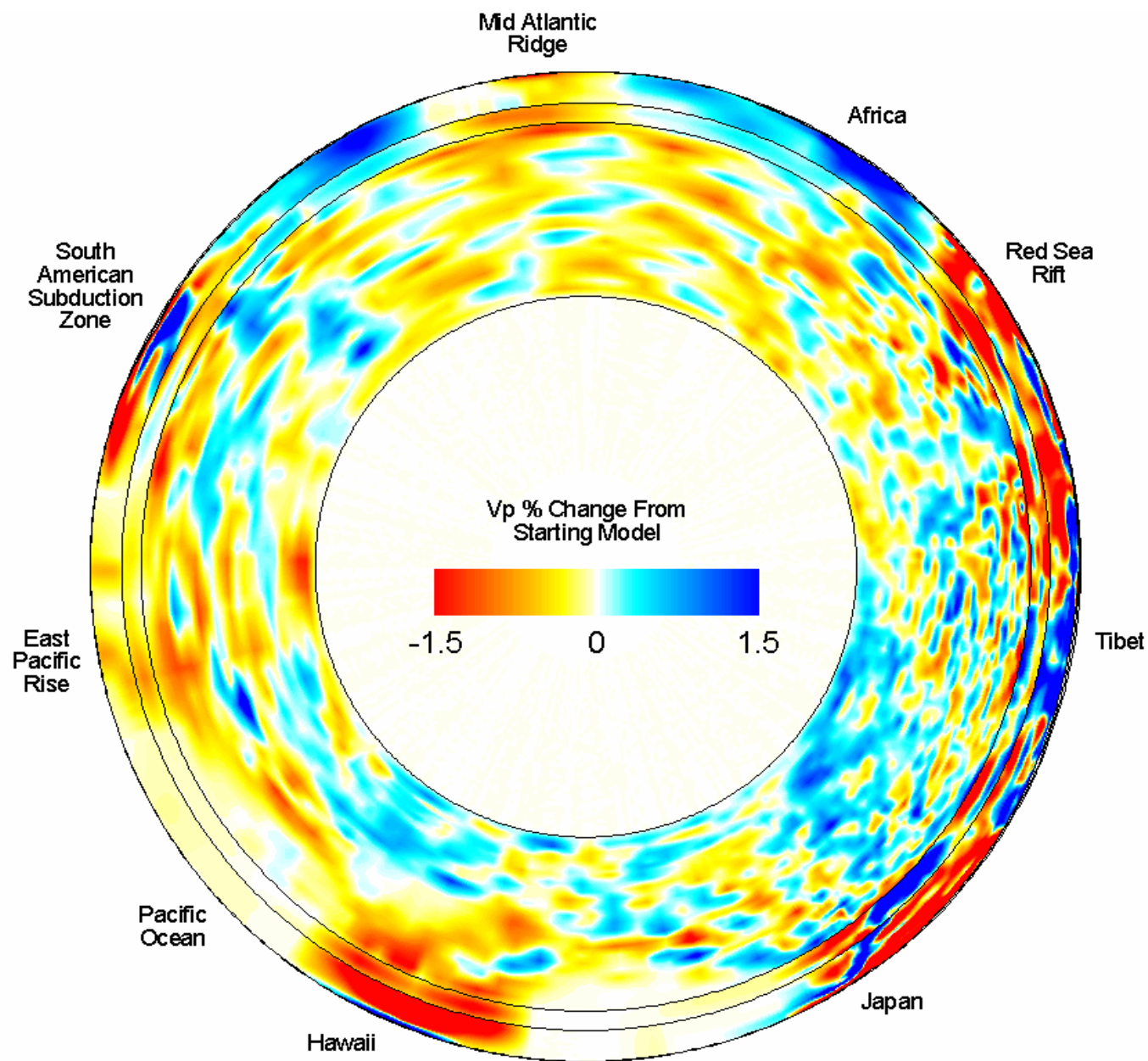
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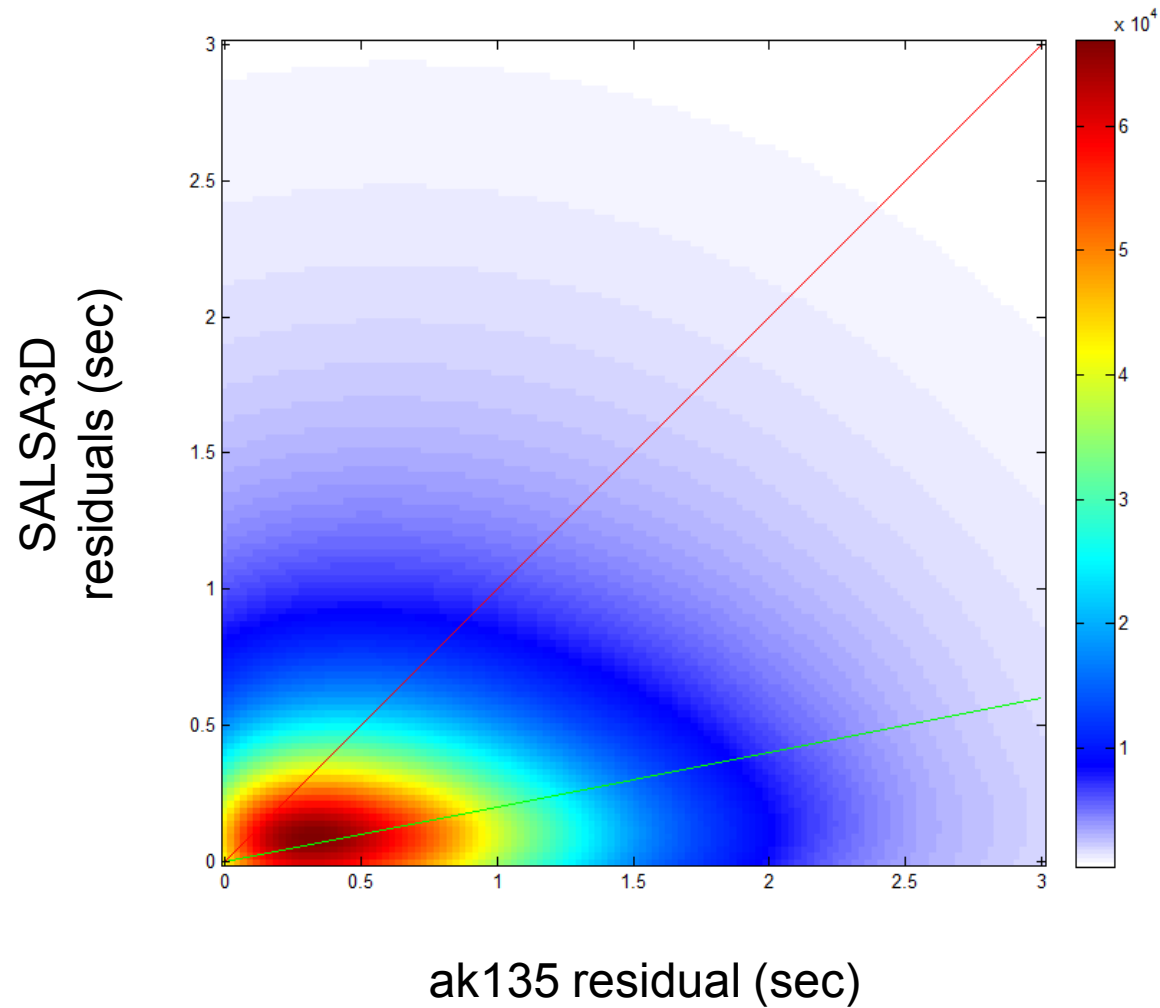
V_p % Change from AK135



SALSA3D

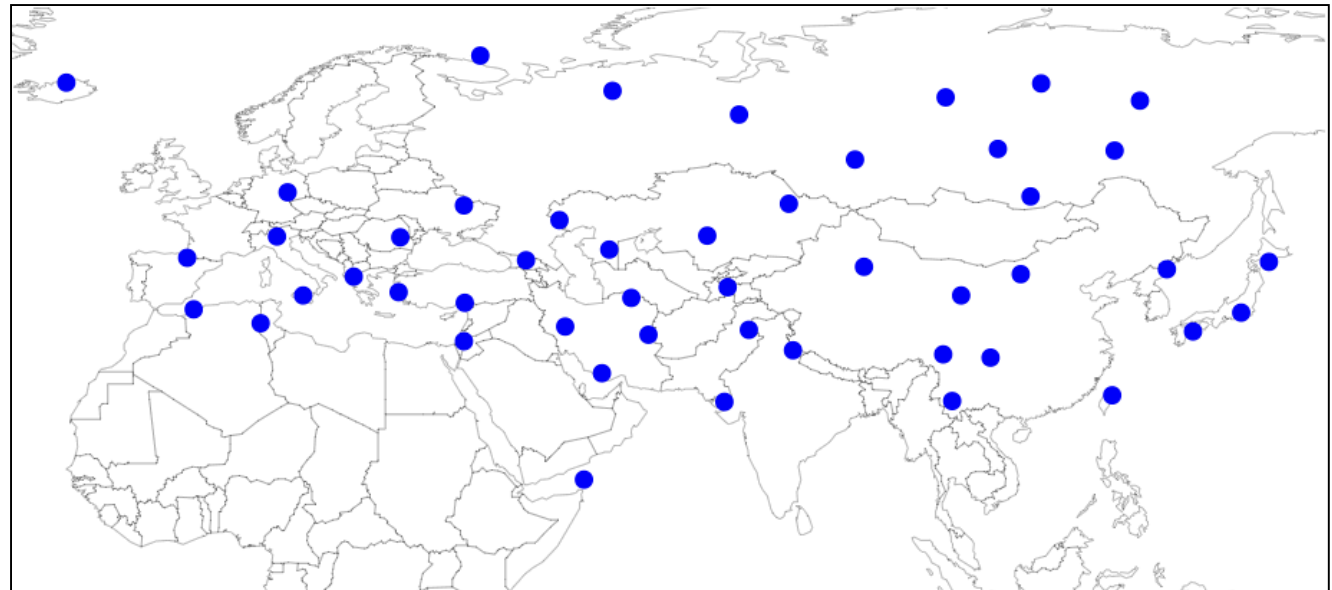


Residual Reduction



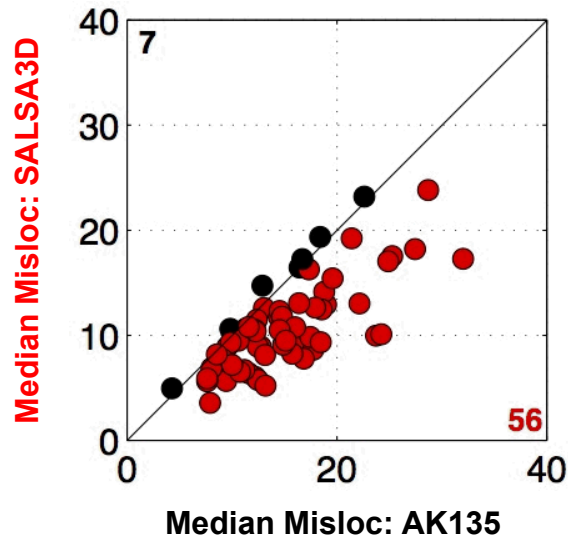
Validation and Model Comparison

- **ak135**
- **RSTT / ak135**
- **SALSA3D**

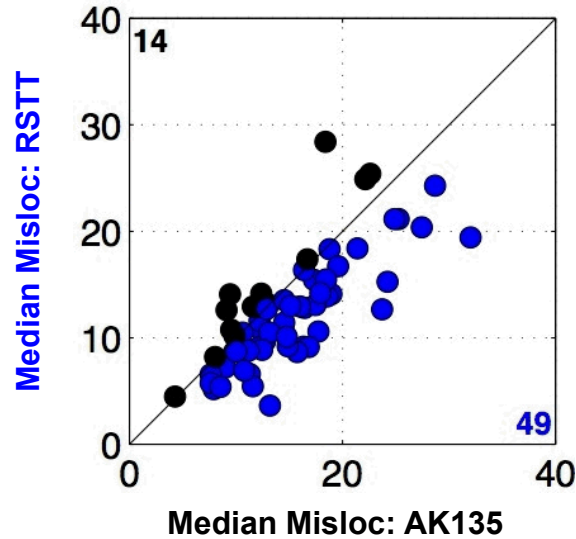


Event Mislocation Comparisons

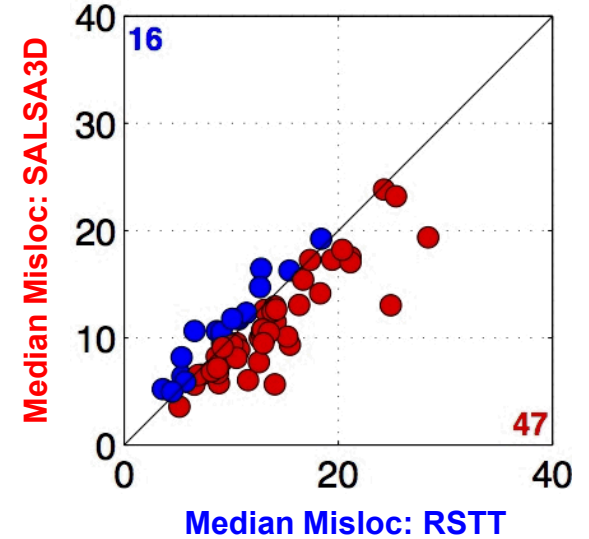
SALSA3D vs. ak135



RSTT vs. ak135



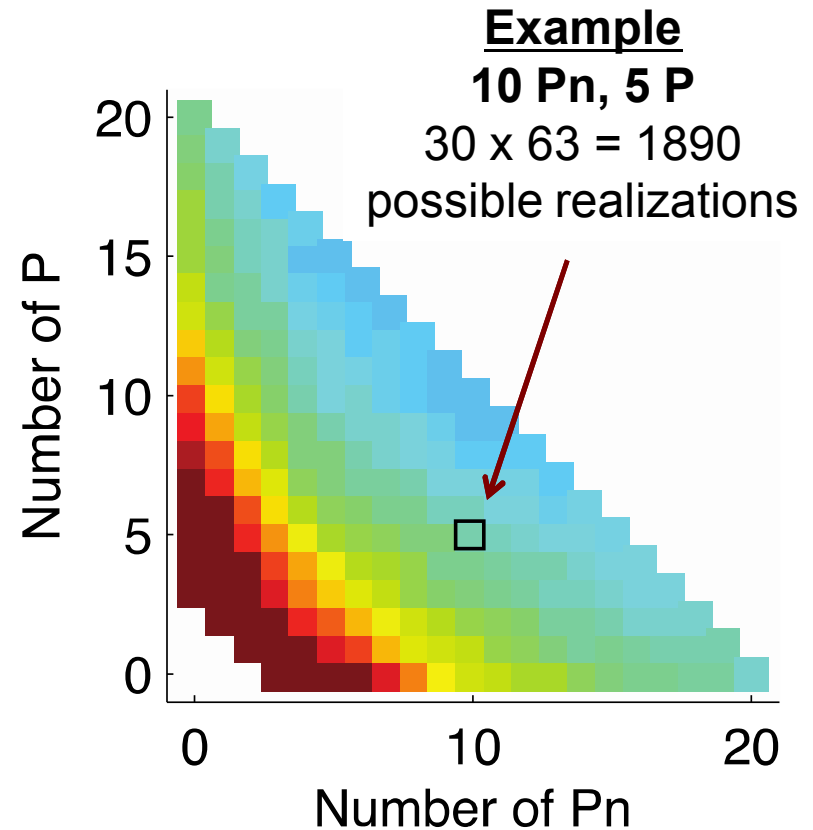
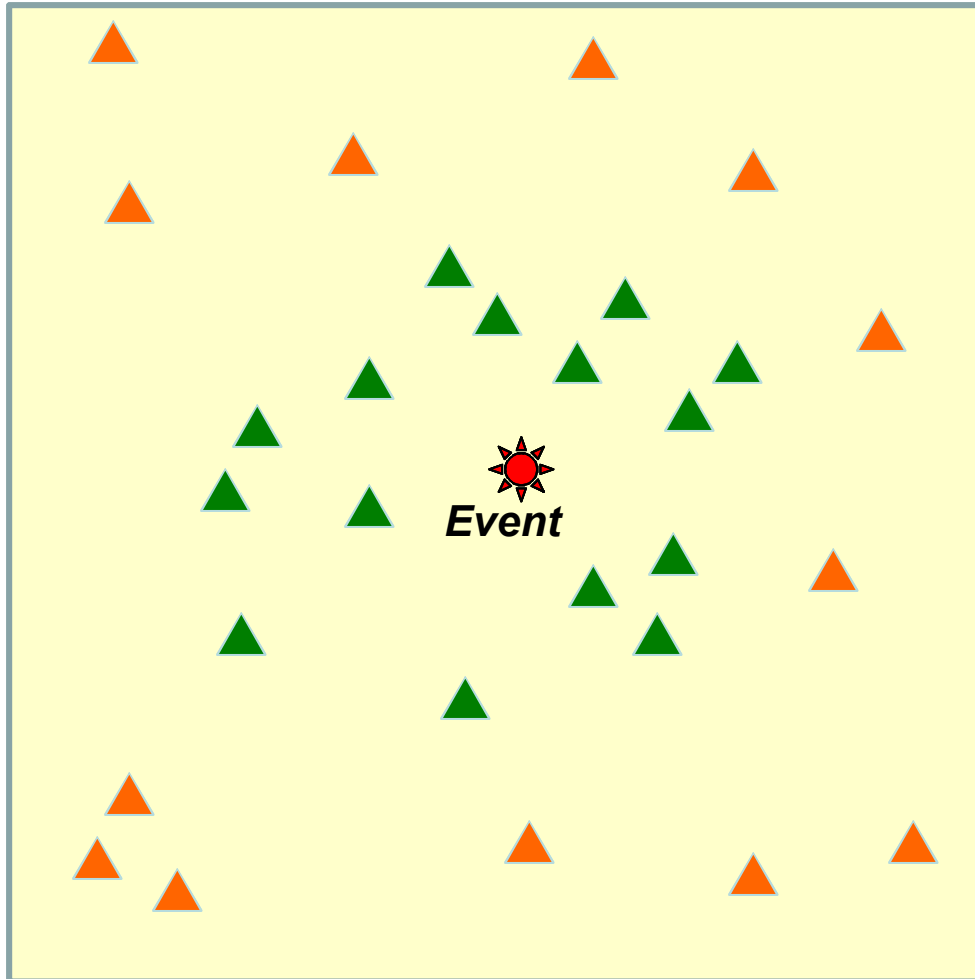
SALSA3D vs. RSTT



Generation of Random Realizations

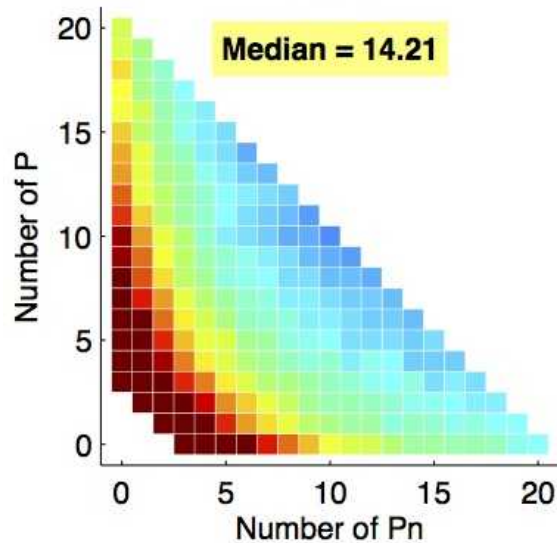
- For each validation event, randomly select many subsets of the available P and P_n arrivals

Stations: *Regional (P_n)* *Teleseismic (P)*

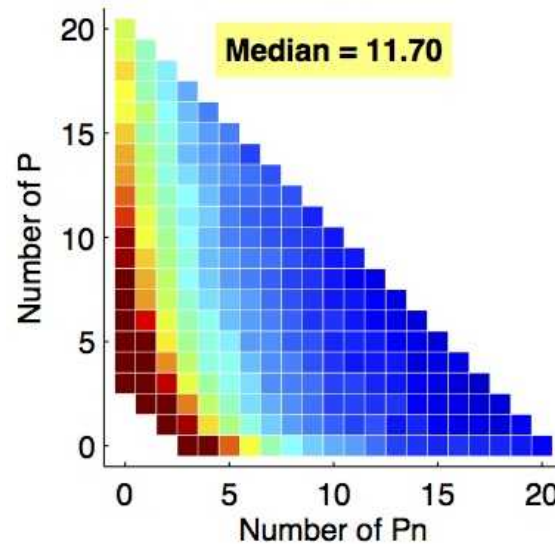


Mislocation Grids

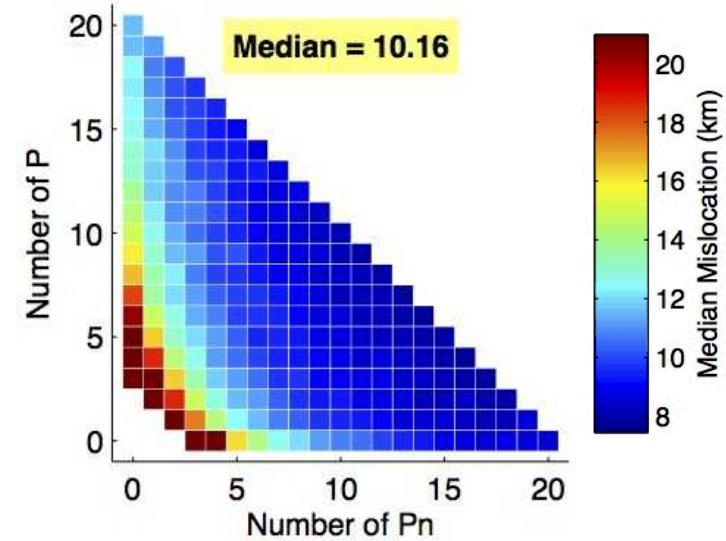
AK135



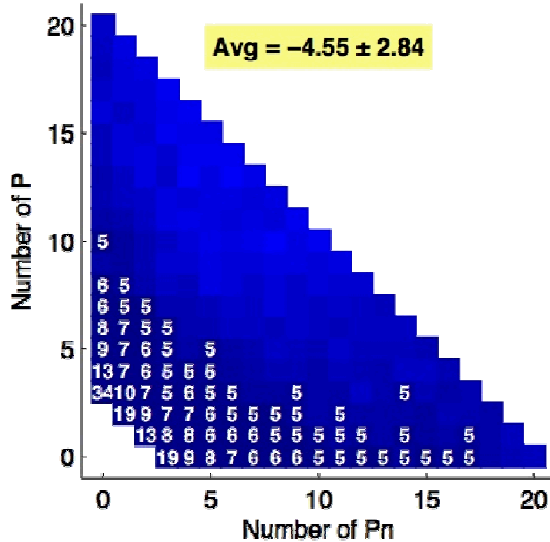
RSTT



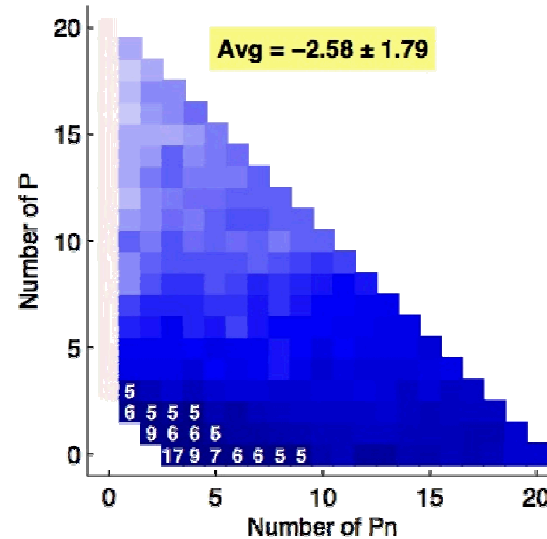
SALSA3D



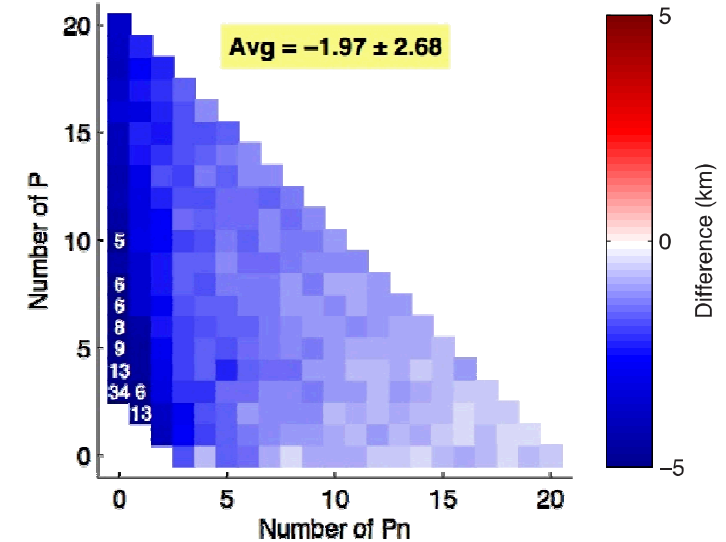
SALSA3D-ak135



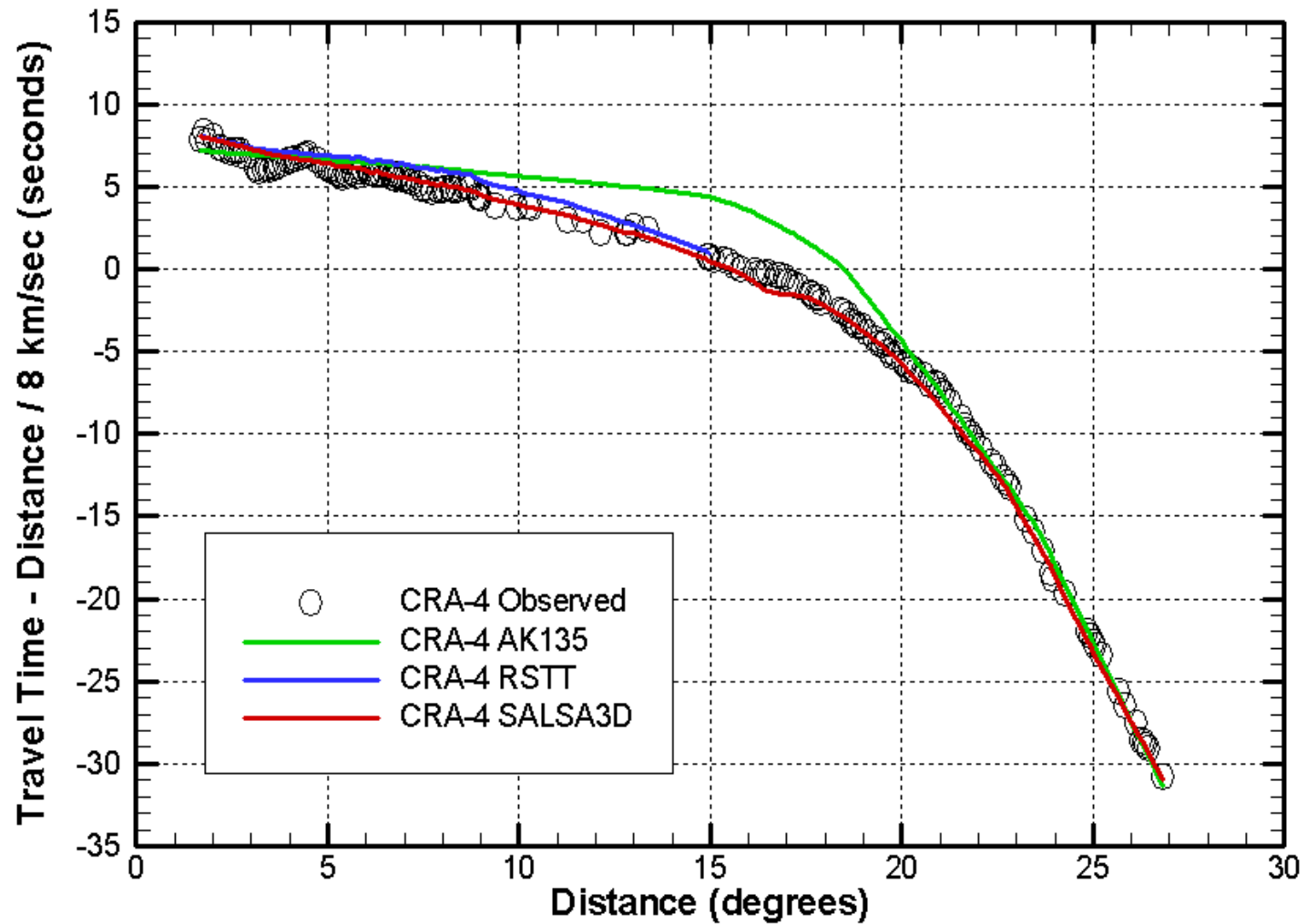
RSTT-ak135



SALSA3D-RSTT



DSS Lines Across the Siberian Platform



Uncertainty

Basic Tomography Equation

$$\begin{bmatrix} C_{d_0}^{-1/2} & 0 \\ 0 & C_{s_0}^{-1/2} \end{bmatrix} \begin{bmatrix} A \\ \alpha L \end{bmatrix} \Delta s = \begin{bmatrix} C_{d_0}^{-1/2} & 0 \\ 0 & C_{s_0}^{-1/2} \end{bmatrix} \begin{bmatrix} \Delta d \\ 0 \end{bmatrix}$$

Uncertainty of the P Wave Velocity in the Mantle

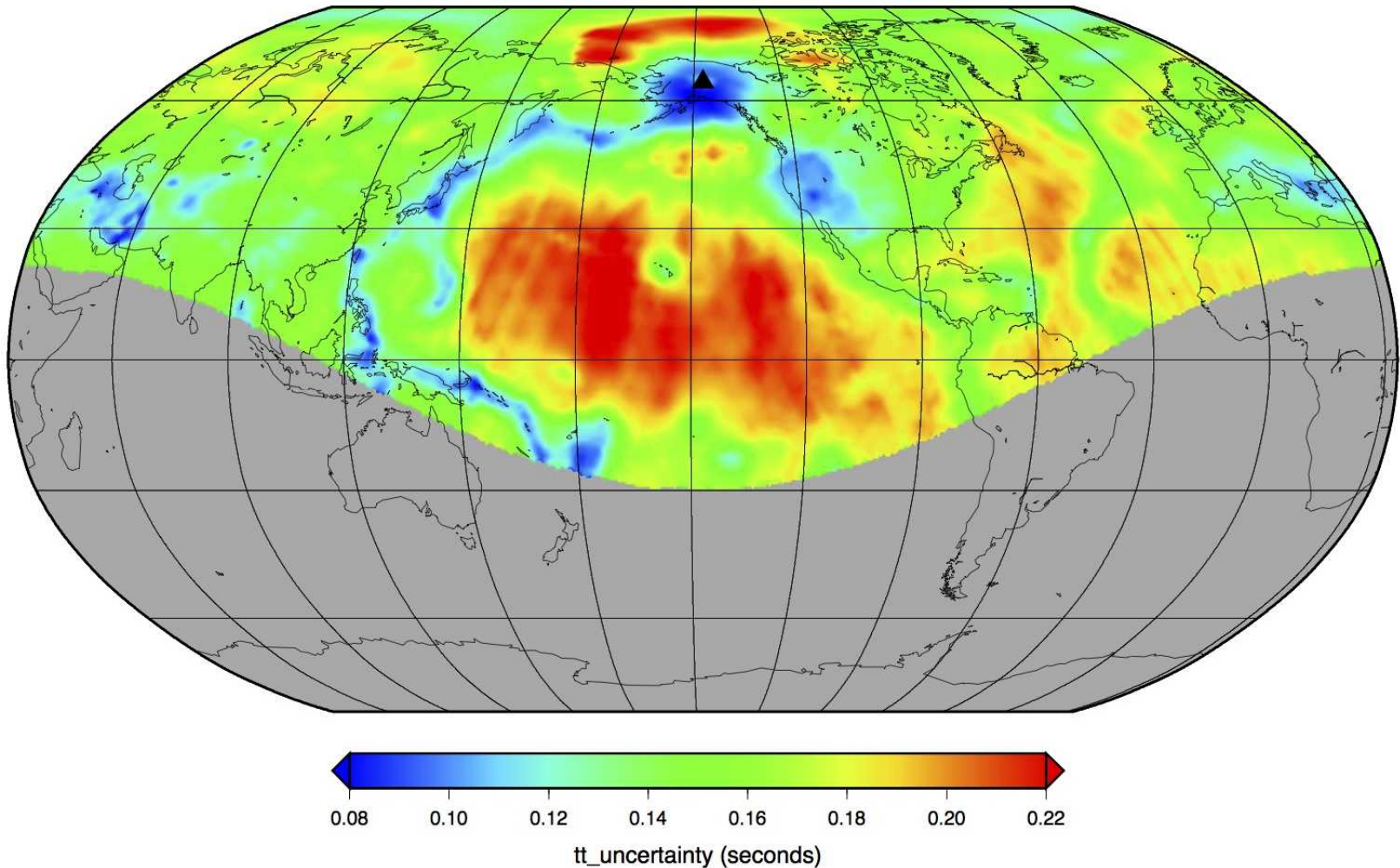
$$C_{m_w} = \left[C_{s_0}^{-1} + A^T C_{d_0}^{-1} A \right]^{-1}$$

Travel Time Uncertainty for a Single Ray Through the Earth

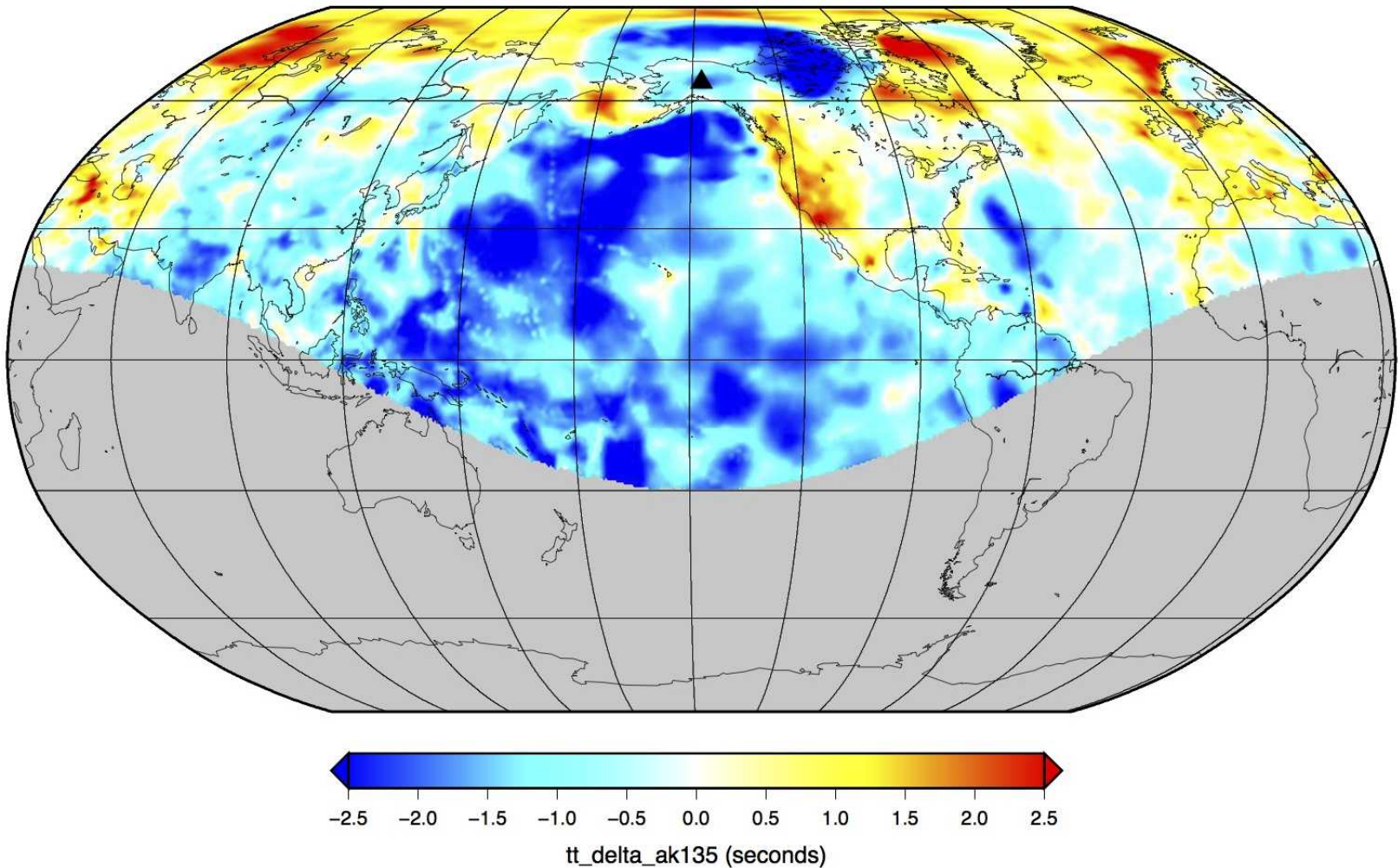
$$\sigma_{tt}^2 = \iint_{path} C_M dx$$

Travel Time Prediction Uncertainty

ILAR, depth=0km



Travel Time Δ_{ak135}



Travel time and uncertainty stored in 3D lookup tables using
GeoTess software (www.sandia.gov/geotess)

Conclusions

- SALSA3D is a 3D multi-resolution model of the compressional wave speed in the Earth constructed with the goal of improving the accuracy and precision of seismic event location.
- SALSA3D successfully images many tectonic features within the Earth.
- Unambiguous improvement in travel-time prediction and event location compared to ak135 and RSTT/ak135, especially for events observed by a network of stations that is small or has poor geometry.
- Path dependent travel time prediction uncertainties are calculated using the full model covariance matrix computed during tomography.
- Station-phase specific travel time predictions and uncertainties are pre-calculated for a network and stored in 3D lookup tables. Retrieval is very fast and accurate using open source GeoTess software (www.sandia.gov/geotess).