

*Exceptional service in the national interest*



# Determining Coefficients for the Sandia Array Performance Model

2<sup>nd</sup> PV System Modeling Workshop

May 1, 2013

*Clifford Hansen and Daniel Riley*  
Sandia National Laboratories, New Mexico (USA)

# Outline and Summary

- Sandia Array Performance Model
  - Predicts on-sun module performance with good accuracy
- Calibration using outdoor testing
  - Proven techniques, but,
  - Testing can take weeks
  - Documentation is lacking
- Calibration using indoor testing:
  - Proof of concept presented at 38<sup>th</sup> PVSC
  - Independently, D. King arrived at a similar approach
  - Cut turnaround time for module testing from weeks to hours
  - Predictions of on-sun module performance show similar accuracy
  - However, not all coefficients can be estimated using indoor testing

# The Sandia Array Performance Model

- Describes module output at SC, OC and MP points
- As a function of beam and diffuse irradiance ( $E_b$  and  $E_{diff}$ ), cell temperature ( $T_C$ ), air mass ( $AM_a$ ) and angle of incidence ( $AOI$ )
- 14 empirical coefficients, 2 empirical functions ( $f_1$  and  $f_2$ )
- With exception of  $f_2$ , coefficients determined for individual modules

$$V_{OC} = V_{OC0} + N_S n \delta(T_C) \ln(E_e) + \beta_{OC} (T_C - T_0)$$

$$V_{MP} = V_{MP0} + C_2 N_S n \delta(T_C) \ln(E_e) + C_3 N_S (n \delta(T_C) \ln(E_e))^2 + \beta_{MP} (T_C - T_0)$$

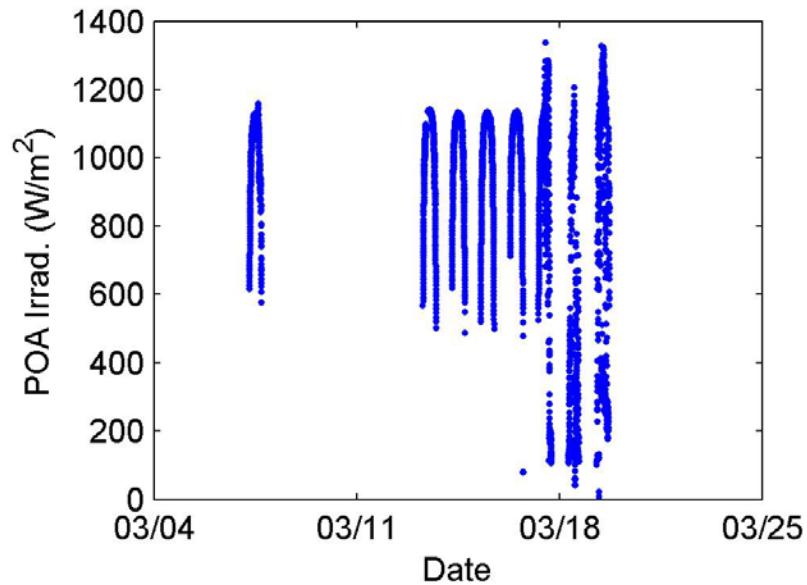
$$I_{SC} = I_{SC0} f_1(AM_a) E_e (1 + \alpha_{SC} (T_C - T_0))$$

$$I_{MP} = I_{MP0} (C_0 E_e + C_1 E_e^2) (1 + \alpha_{MP} (T_C - T_0))$$

$$E_e = E_b f_2(AOI) + E_{diff} f_d$$

# SAPM calibrated by Outdoor Testing

- I-V curves measured on 2-axis tracker during three sequential tests:
  - Thermal performance
  - Electrical performance
  - Incident angle
- Can take several weeks to obtain I-V curves during all important conditions



# Example of parameter estimation

- Estimate temperature coefficient for VOC from thermal performance test

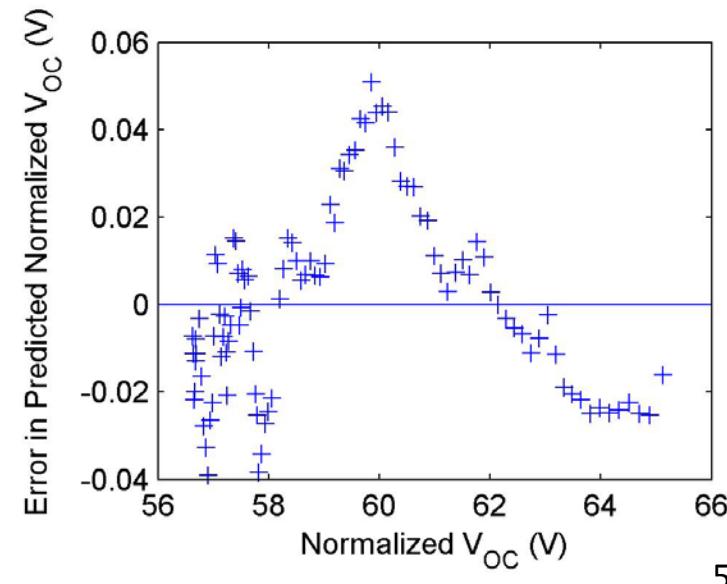
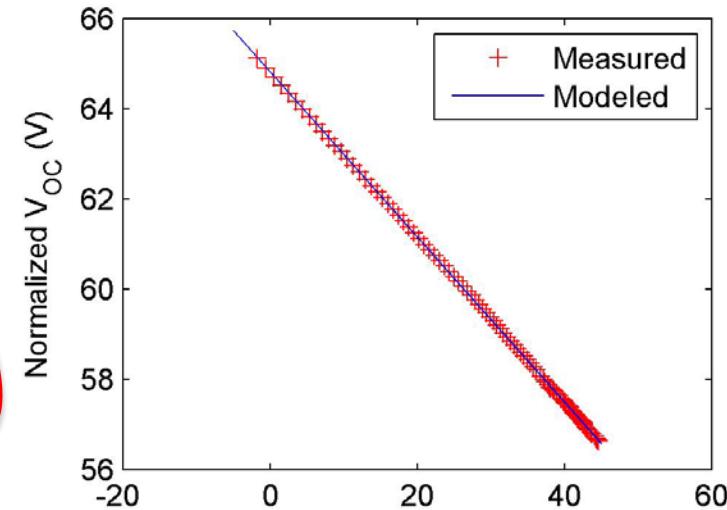
- Maintain  $AOI = 0$
- Clear-sky conditions

$$V_{OC} = V_{OC0} + N_S n \delta(T_C) \ln(E_e) + \beta_{OC} (T_C - T_0)$$

↓ simplifies to

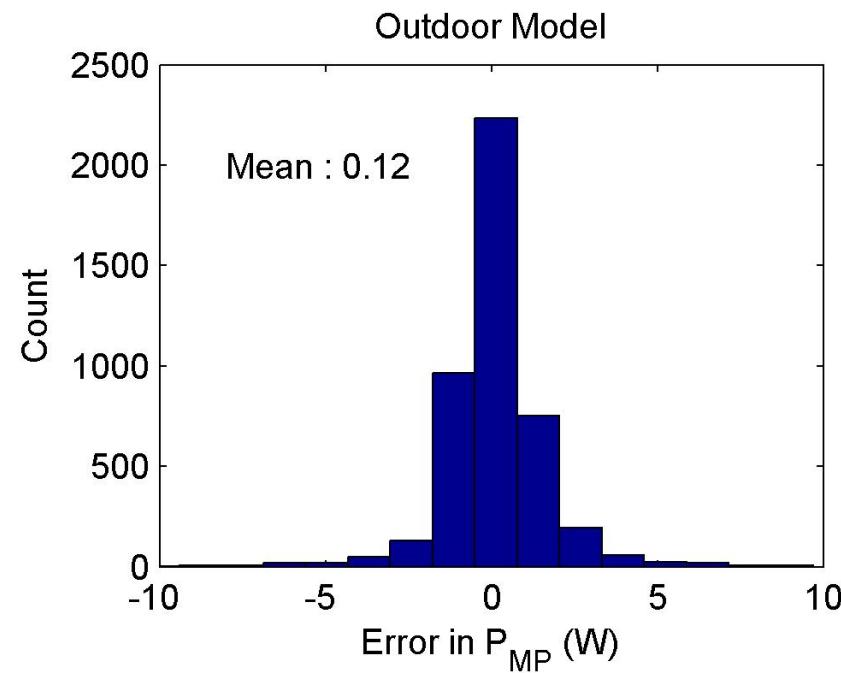
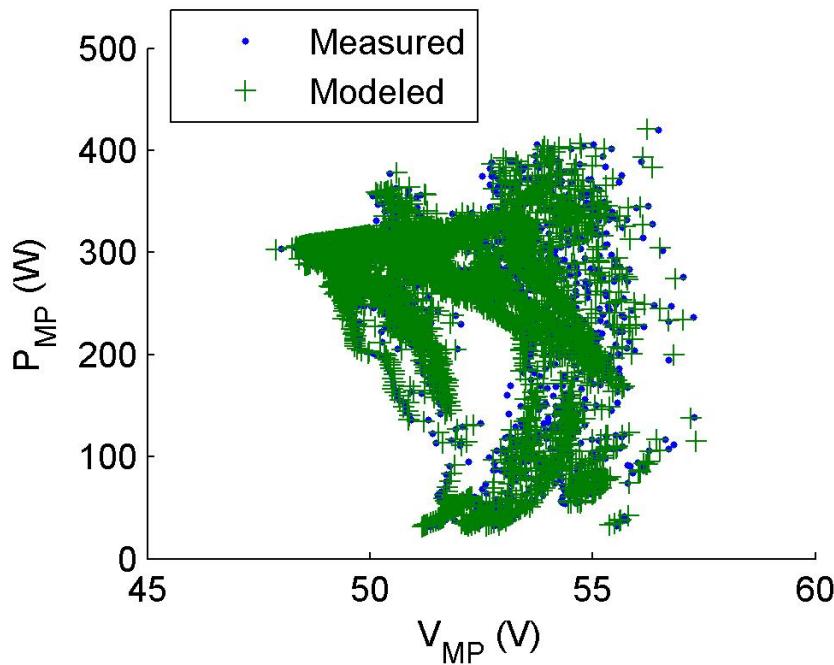
$$V_{OC} = V_{OC0} + \beta_{OC} (T_C - T_0)$$

- Cover module and cool to ambient
- Uncover and measure I-V curves while module heats to operating temperature
- Normalize measured  $V_{OC}$  to 1000 W/m<sup>2</sup>
- $\beta_{OC}$  estimated from  $(T_C, V_{OC})$  by linear regression



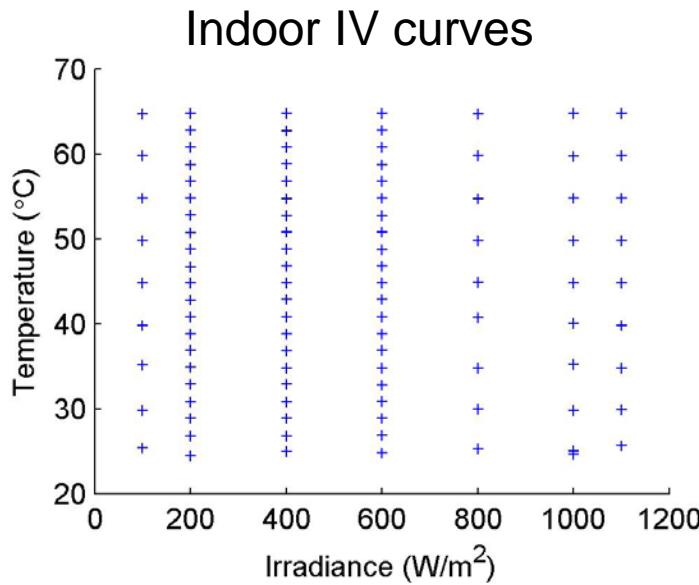
# Performance of “outdoor” model

- One SunPower 305W cSi module
- Albuquerque, NM, in March 2012
- “In sample” model verification

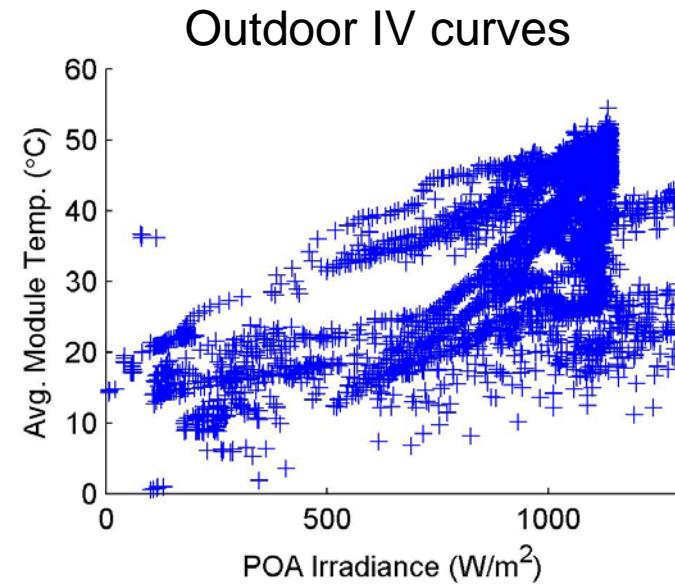


# Indoor testing (reported at 38<sup>th</sup> PVSC)

- Conducted by CFV Solar Test Laboratory, Inc (Albuquerque, NM)
- HALM solar simulator integrated with a thermal chamber
  - Varies irradiance between 0.1 and 1.1 suns
  - Temperature between 25C and 75C via laminar air flow heater
- We measured I-V curves for irradiance and temperature combinations following IEC 61853-1

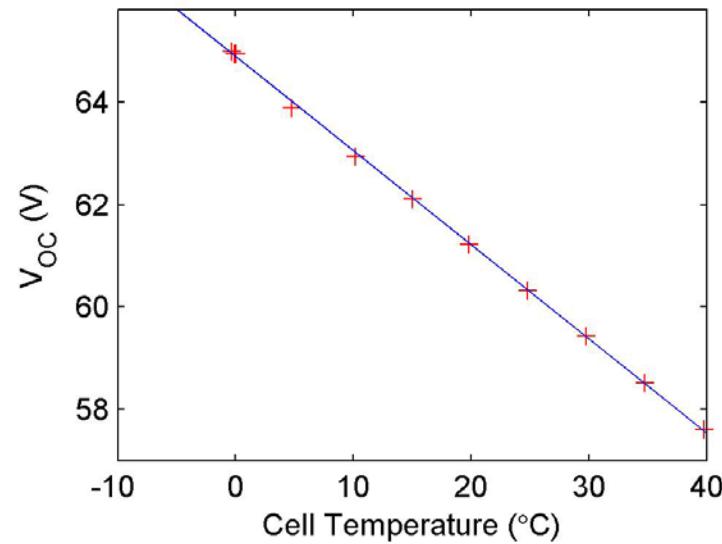
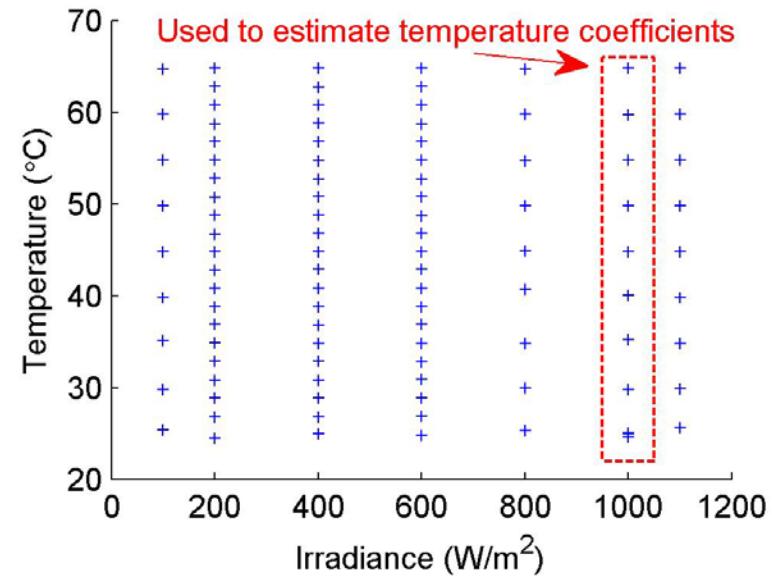


Much  
less  
data  
than for  
outdoor  
testing



# Parameters from indoor testing

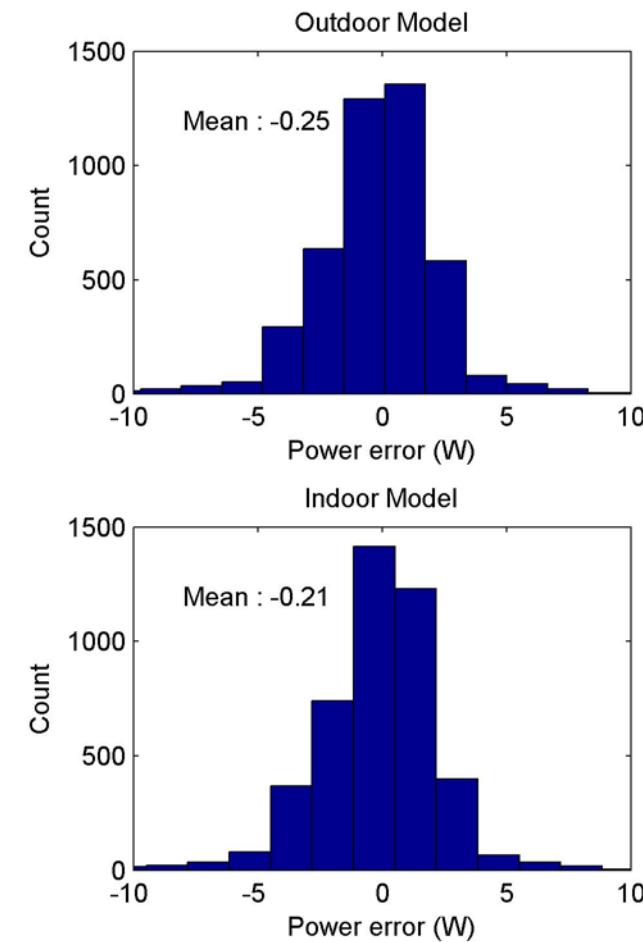
- IEC 61853 test matrix
- Two-stage process analogous to outdoor test methods
  - Estimate thermal coefficients, then
  - Use thermal coefficients in estimation of other parameters
- Other methods (e.g., full simultaneous) performed worse
- D. King independently arrived at similar approach



# Performance of “indoor” model

- Parameter values obtained are similar for outdoor and indoor models
- Similar accuracy predicting outdoor performance

Parameter	Outdoor Model	Indoor Model
$\beta_{OC}$ (V/°C)	-0.195	-0.197
$V_{OC0}$ (V)	65.044	64.882
$\beta_{MP}$ (V/°C)	-0.183	-0.184
$V_{MP0}$ (V)	54.193	54.15
$\alpha_{MP}$ (1/°C)	-0.00017	-0.000169
$I_{MP0}$ (A)	5.623	5.631
$\alpha_{SC}$ (1/°C)	0.000425	0.000378
$I_{SC0}$ (A)	5.976	5.969
$n$ (unitless)	1.12	1.074
$C_0; C_1$ (unitless)	1.0121; -0.0121	1.0069; -0.0069
$C_2; C_3$ (unitless)	0.3114; -5.0257	0.3379; -4.7201
$N_s$ (cells in series)	96	96



# Conclusions, and Future Work

- For outdoor testing:
  - Testing and parameter estimation methods have proven reliable but should be better documented
- For indoor testing:
  - Most (but not all) parameters for SAPM can be determined from indoor testing if irradiance and module temperature can be varied separately
  - Currently, we cannot determine  $f_1$  or  $f_2$  from indoor measurements
  - Using surrogate  $f_2$  function from analog modules has been acceptable
  - Methods need better documentation

# Available references

## Sandia Array Performance Model

- King et al. 2004, *Photovoltaic Array Performance Model*, Sandia Report 2004-3535

## Generating coefficients for SAPM

- Hansen et al. 2011 PVSC Paper, *Parameter Uncertainty in the Sandia Array Performance Model for Flat-Plate Crystalline Silicon Modules*
- Hansen et al. 2012 PVSC Paper, *Calibration of the Sandia Array Performance Model Using Indoor Measurements*

Copies available at [pv.sandia.gov](http://pv.sandia.gov), PV Publications page