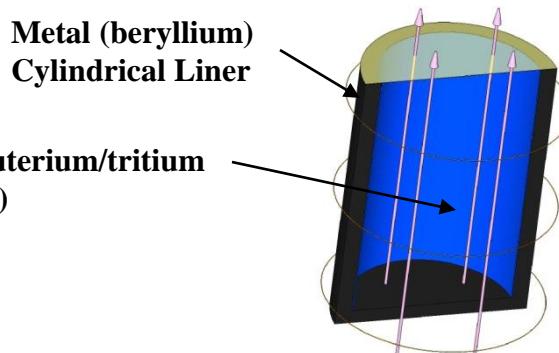


# 3 Dimensional Magneto-hydrodynamic modeling of liner implosions on the Z Generator

C.A. Jennings, R.D. McBride, D.B. Sinars, J. Chittenden,  
S.A. Slutz, M.E. Cuneo, M.C. Herrmann,

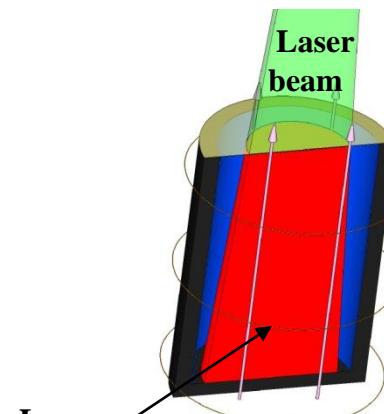
\* Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

# Magnetized Liner Inertial Fusion (MagLIF)\* may be a promising path to high fusion yields on Z

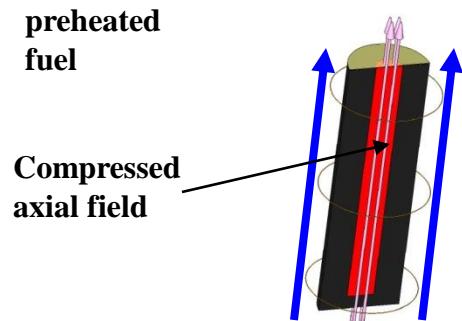


**Idea: Directly drive solid liner containing fusion fuel**

1. An axial magnetic field ( $B_z$ ) is applied to inhibit thermal conduction and enhance alpha particle deposition



2. Z Beamlet preheats the fuel



3. The Z accelerator efficiently drives a z-pinch implosion

**Liner Integrity is Critical !**

\*S. A. Slutz *et al.*, Phys. Plasmas **17**, 056303 (2010).

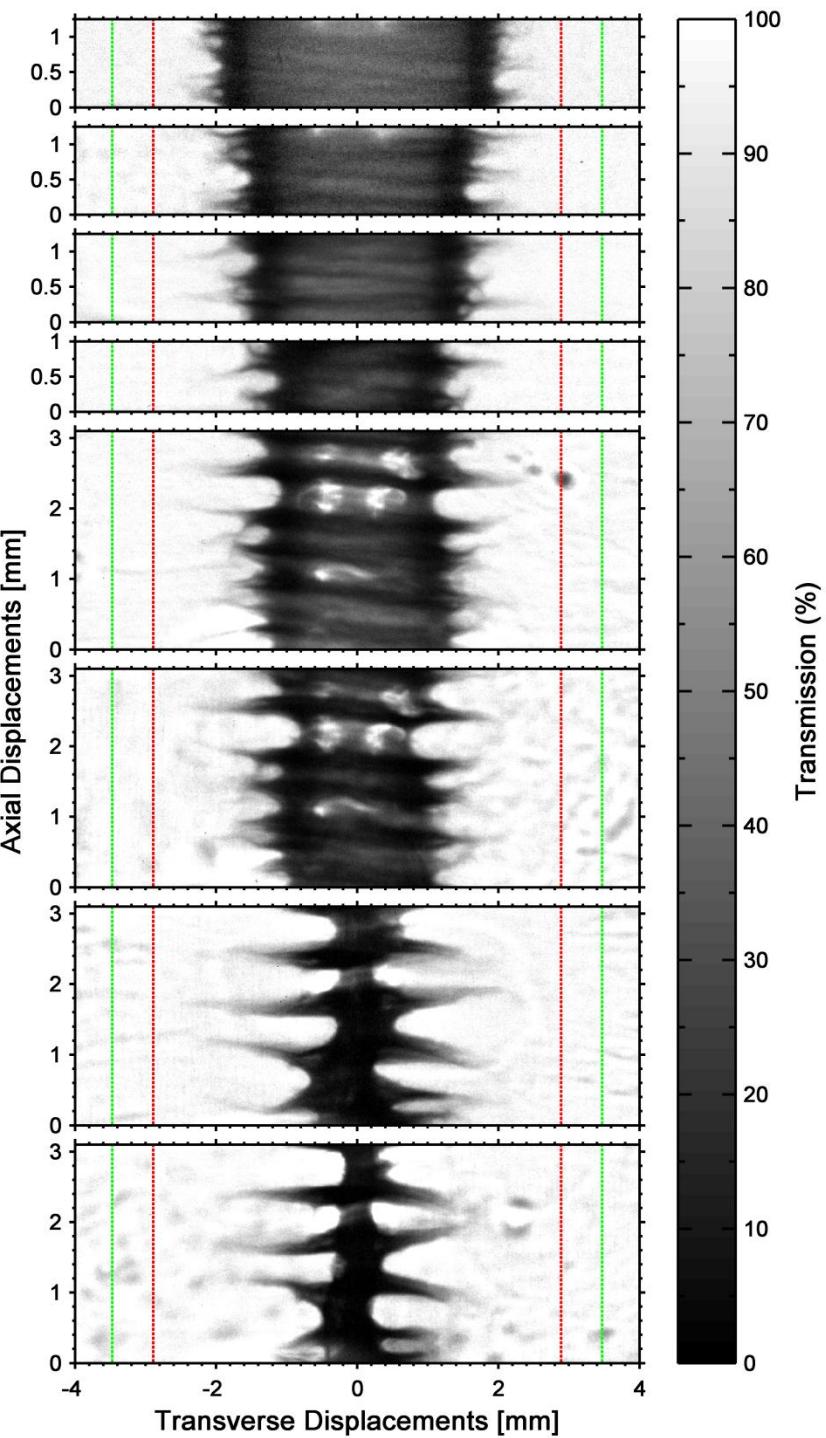
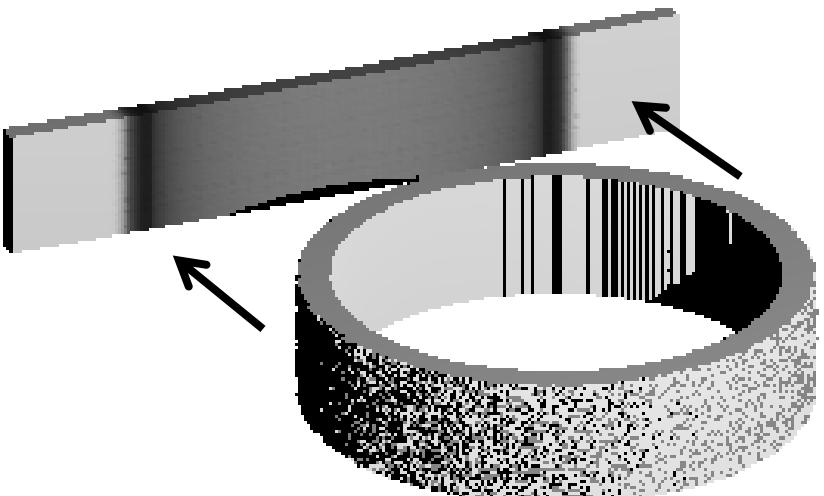


# Liner Implosion

Experiments have been performed on the Z generator to study the evolution instabilities in Be liner implosions.

Ryan McBride talking Thursday

Transmission Radiographs taken of imploding liners



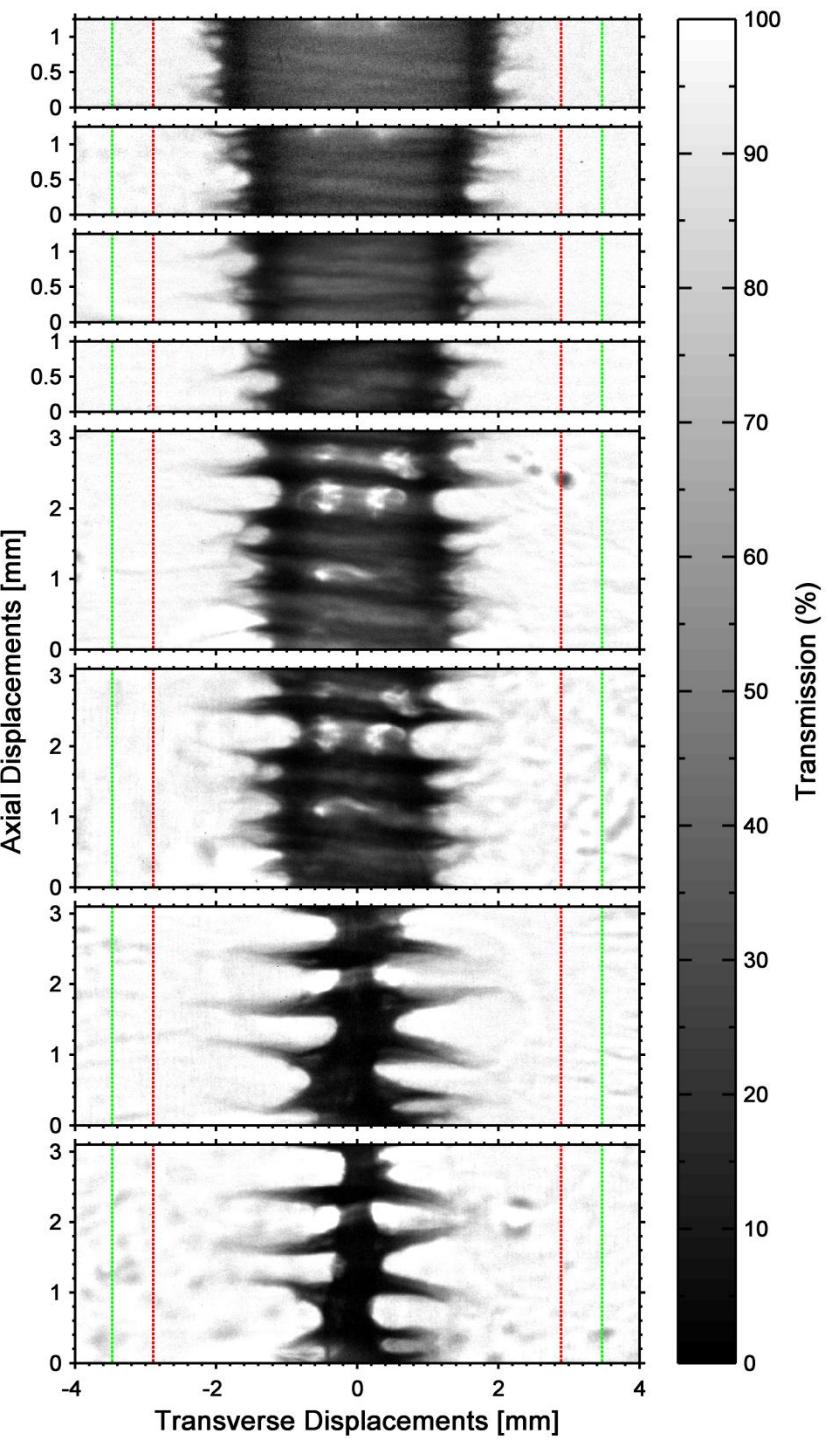
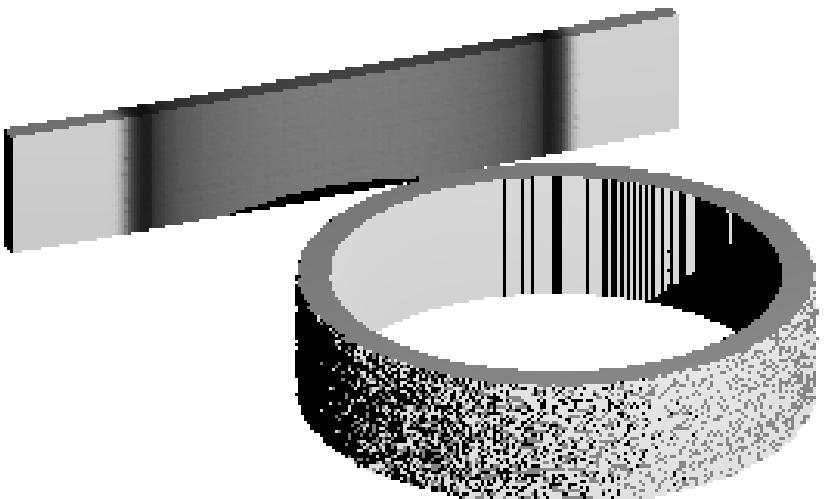


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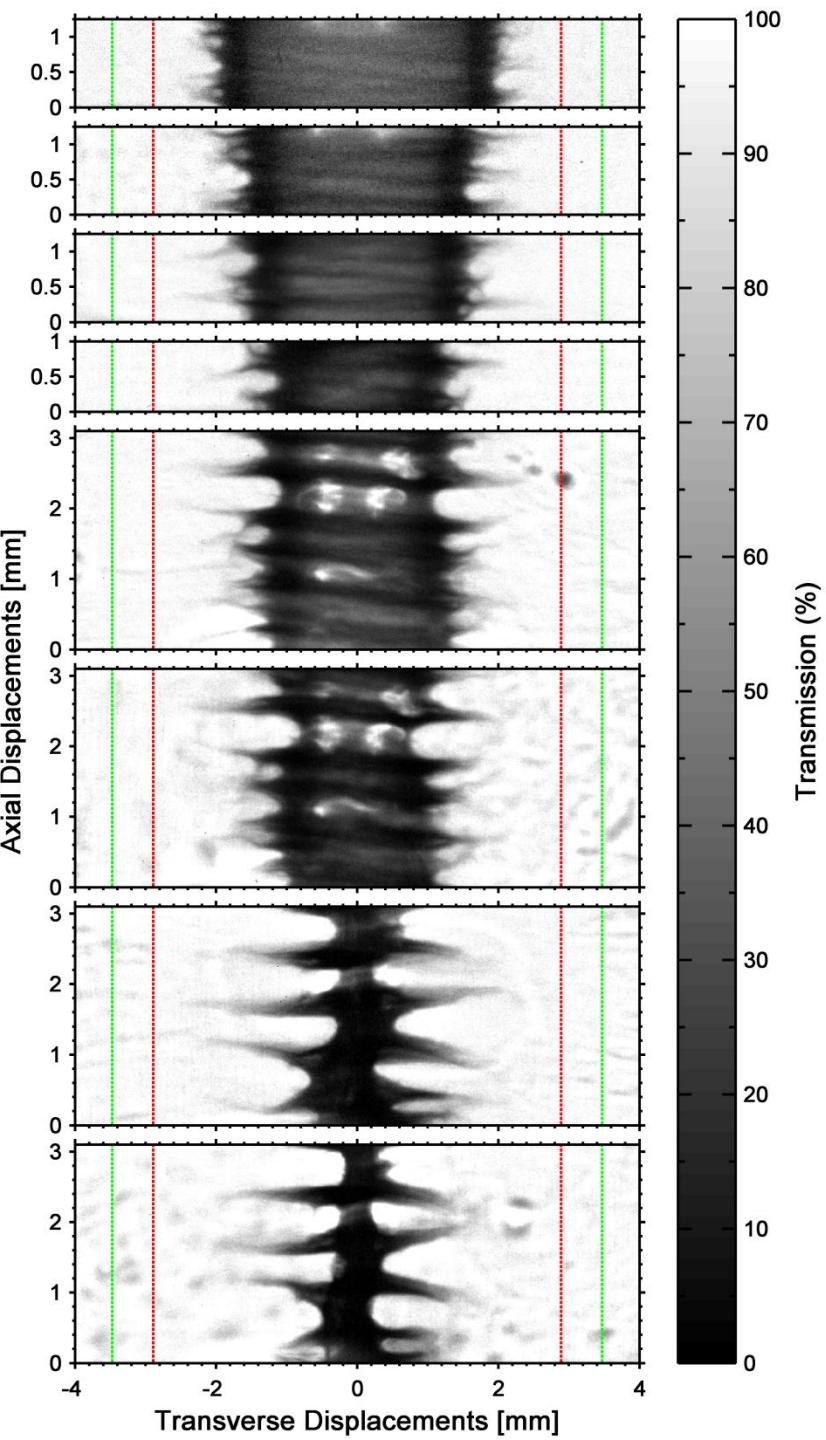
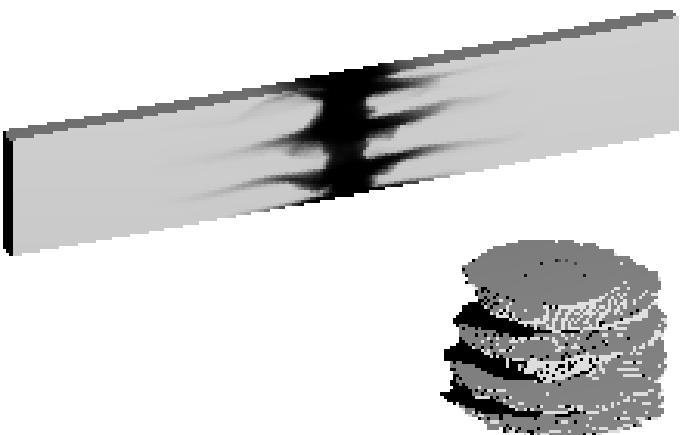


# Liner Implosion

Experiments have been performed on the Z generator to study the evolution instabilities in Be liner implosions.

Ryan McBride talking Thursday

Transmission Radiographs taken of imploding liners





# GORGON 3D resistive MHD code used to study the development of implosion instabilities

## GORGON – 3D Resistive MHD

Fixed square grid finite volume hydrodynamics

Single fluid – separate electron and ion temperatures

Explicit electro-magnetic field solution (wave equation in vacuum / diffusion equation in plasma)

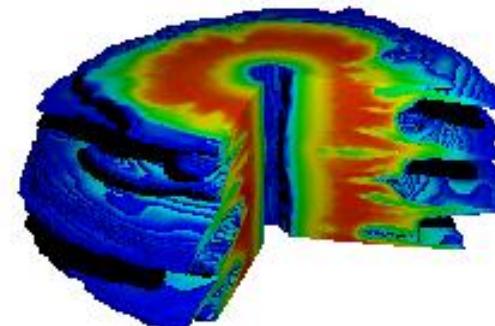
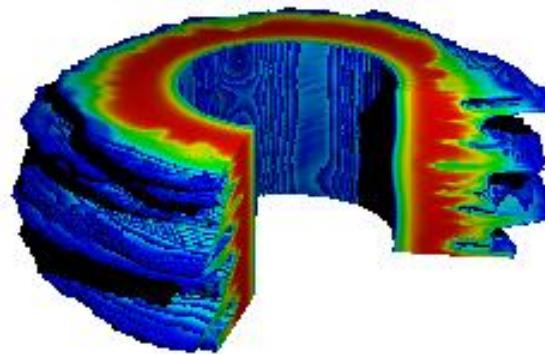
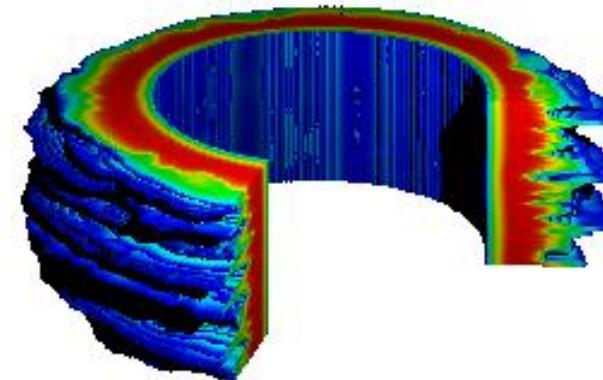
Van Leer Advection

Driven from measured generator current



Density used to construct synthetic radiographs for direct comparison with experimental measurements

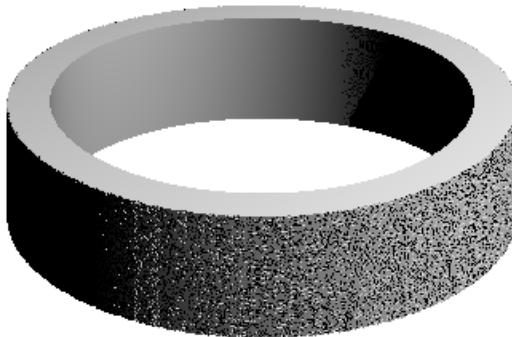
Log Density





# Calculations are initialized with a randomized 20 micron surface roughness

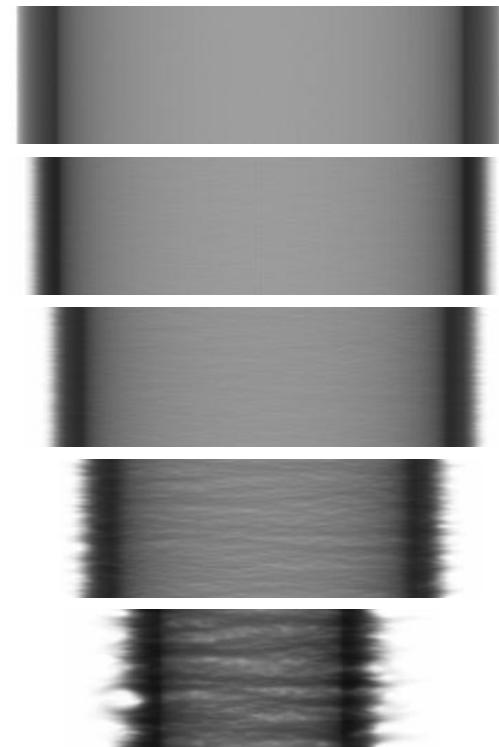
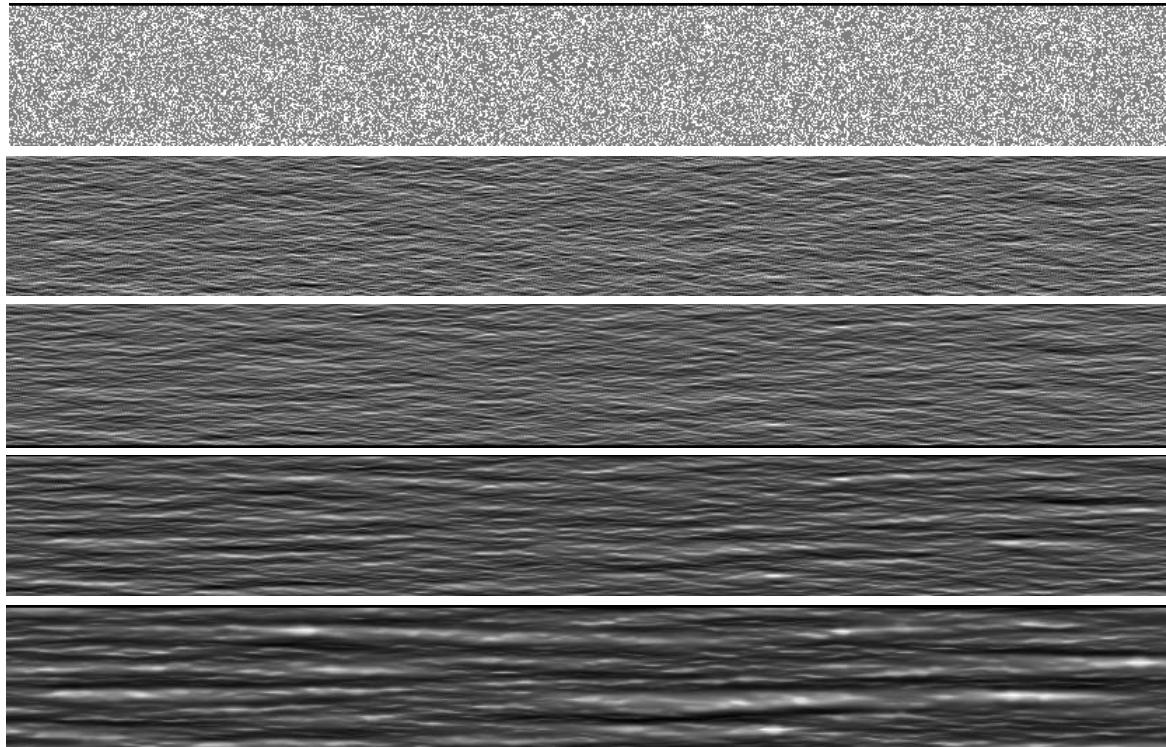
Liner radiograph unwrapped to study growth of surface structures



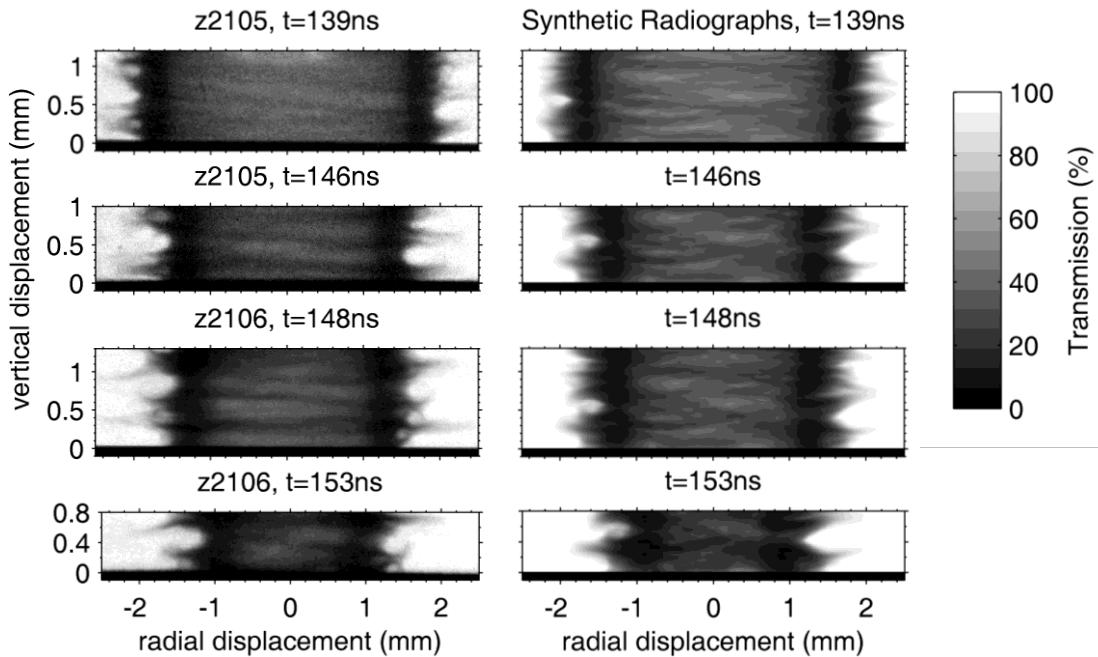
This initialization is not intended to study how different surface structures develop, and does not attempt to reproduce initial liner surface

Synthetic Radiographs

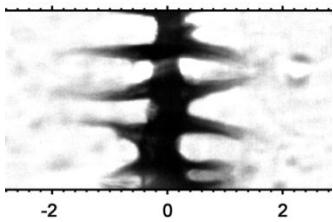
Time  
↓



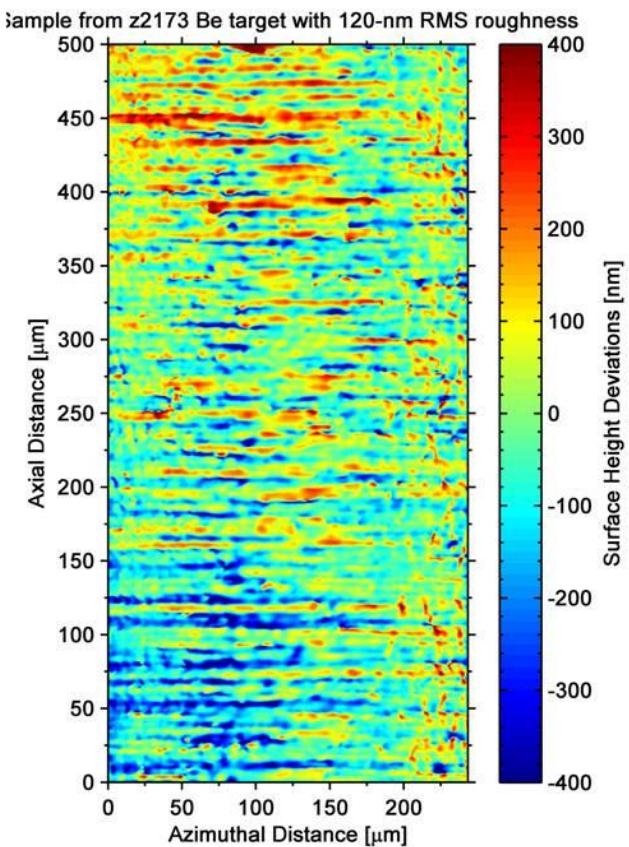
# Reasonable early time agreement with measured radiographs, but late time discrepancies



Level of disruption different at late times



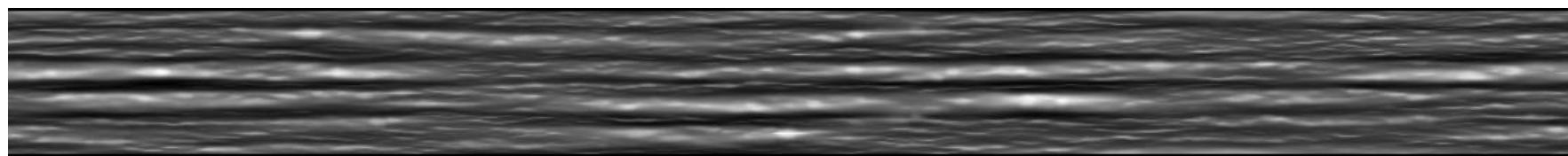
Measured surface roughness is not random, but has some azimuthal correlation





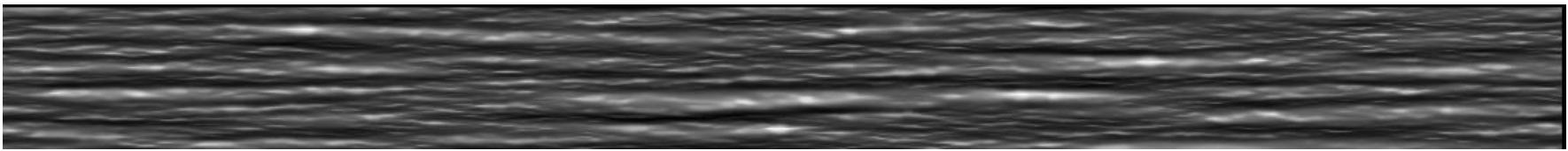
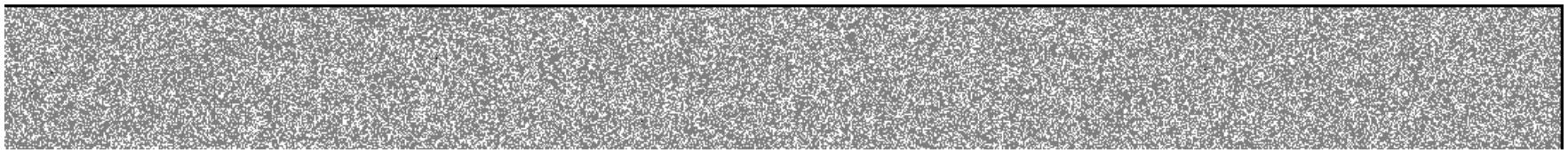
# A small degree of azimuthal correlation is able to persist late in time

20 % random number generator bias correlation at 6 random heights



3110ns

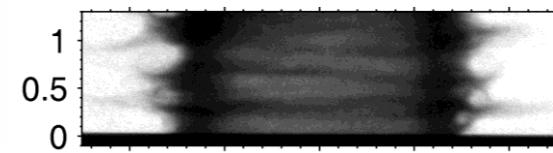
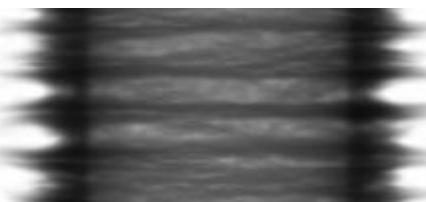
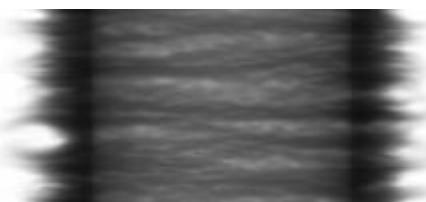
No Correlation



No correlation

Correlation

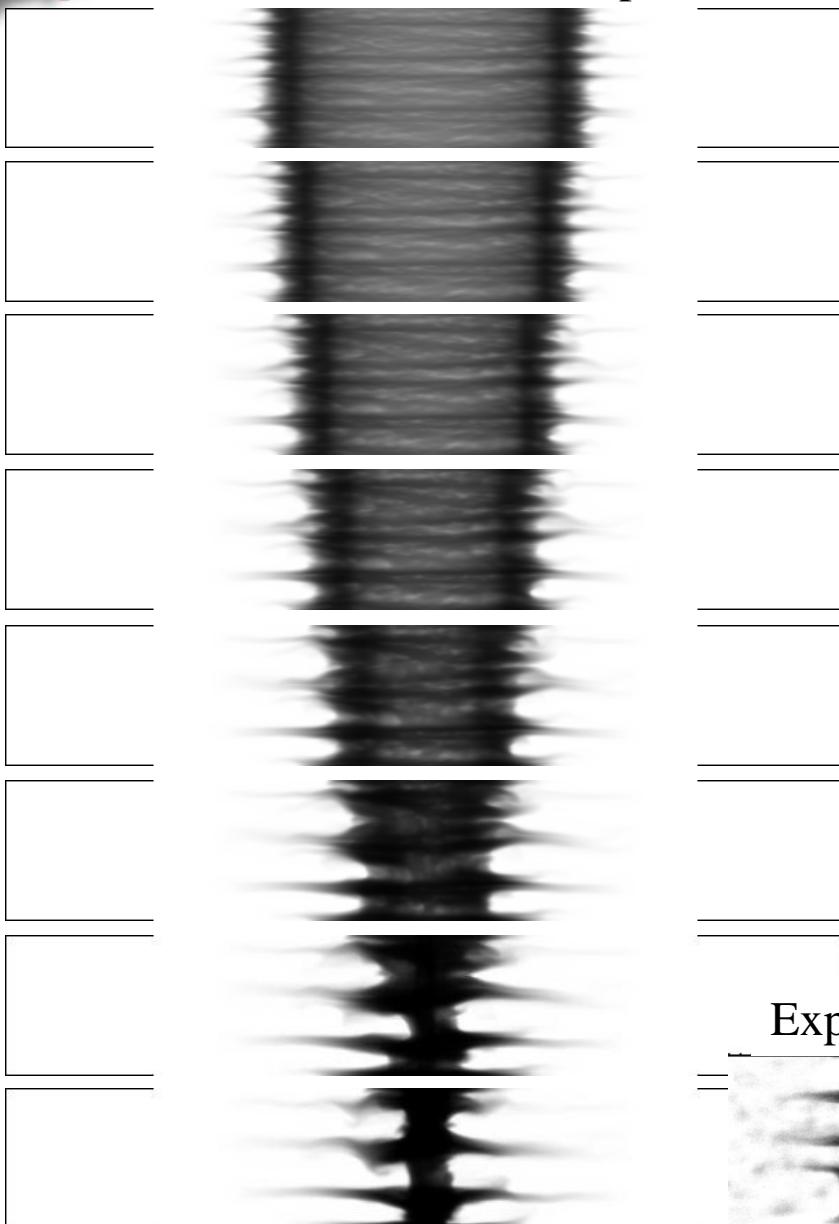
Experiment  
z2106, t=148ns



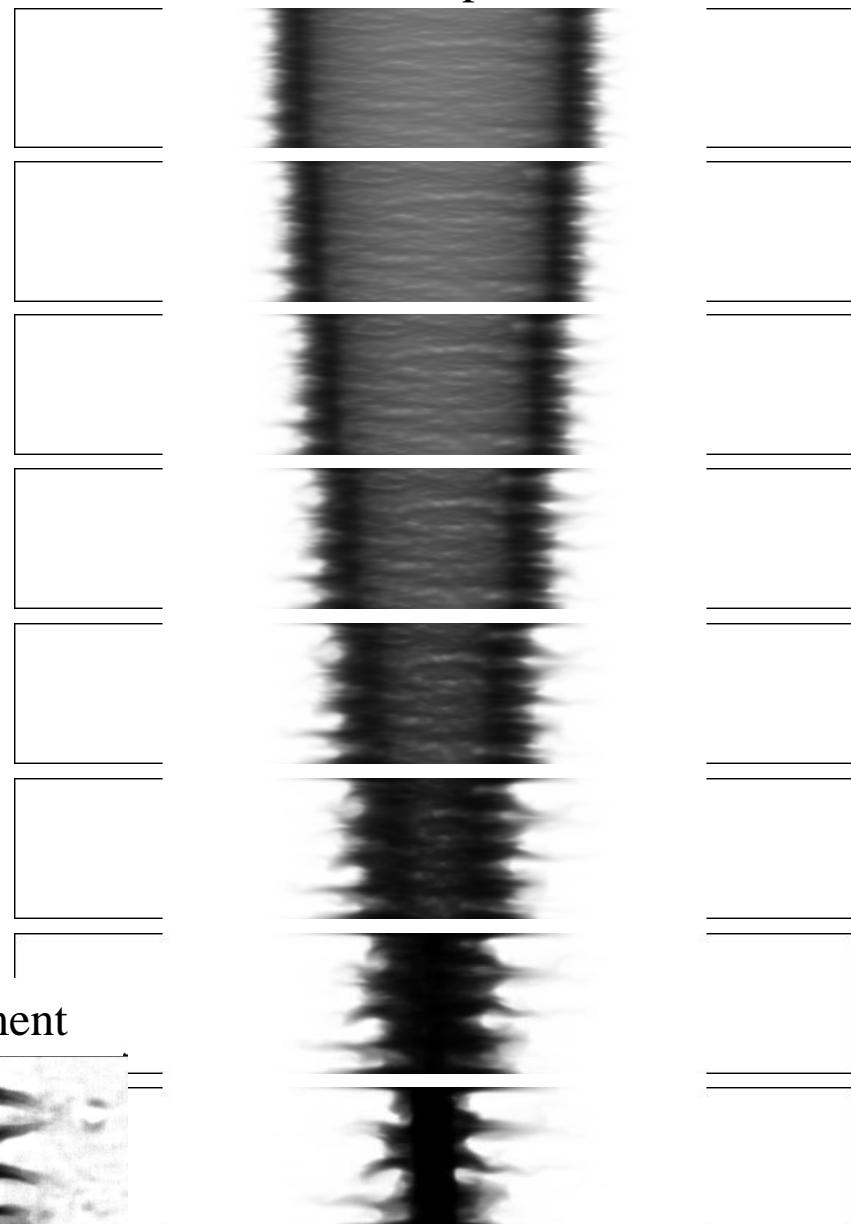


# Effect of correlation more evident later in time

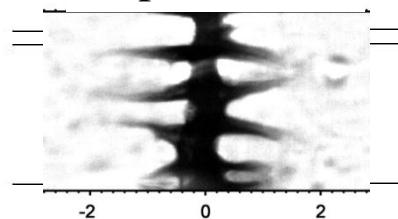
Azimuthal Correlate pert.



random pert.

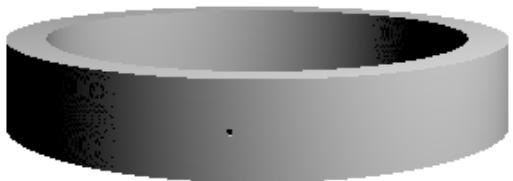


Experiment

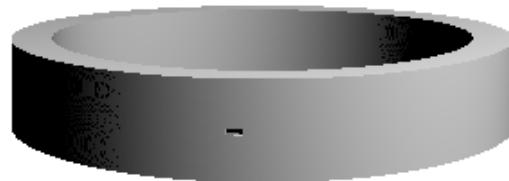




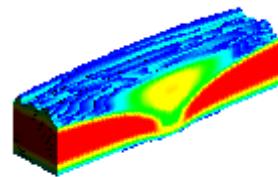
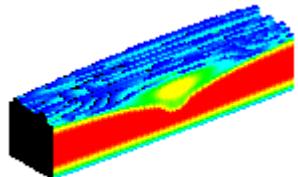
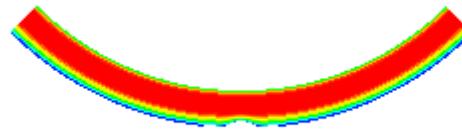
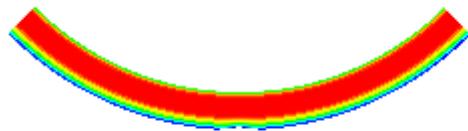
The degree of azimuthal correlation of an instability affects how much it can penetrate and disrupt an imploding shell



60 micron long

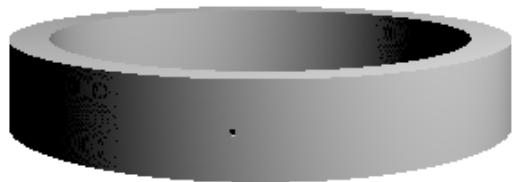


180 micron long





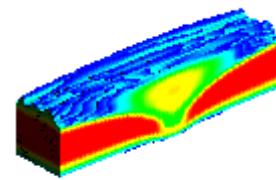
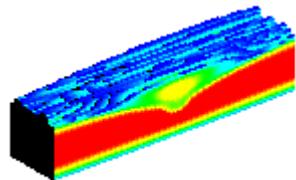
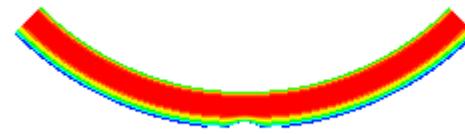
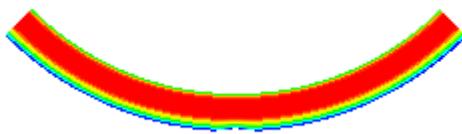
The degree of azimuthal correlation of an instability affects how much it can penetrate and disrupt an imploding shell



60 micron long

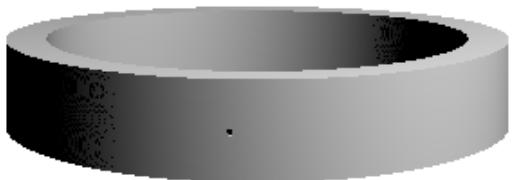


180 micron long





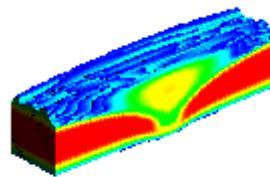
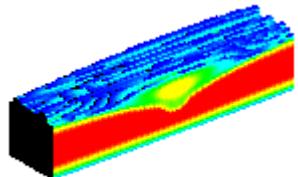
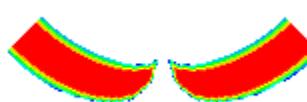
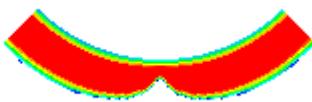
The degree of azimuthal correlation of an instability affects how much it can penetrate and disrupt an imploding shell



60 micron long



180 micron long

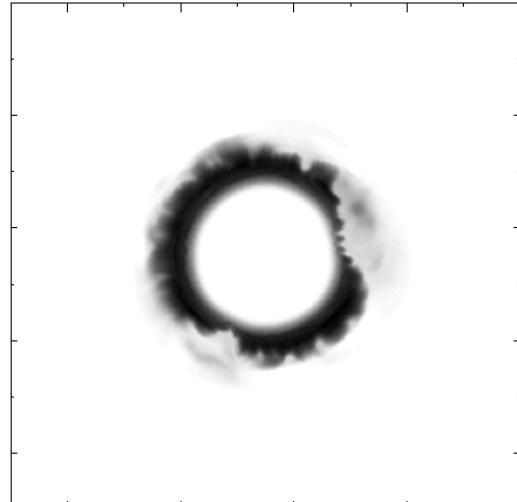




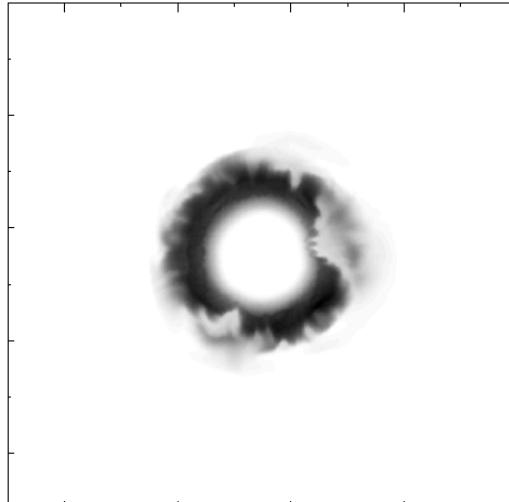
# The degree of azimuthal correlation of an instability affects how much it can penetrate and disrupt an imploding shell

Linear density slices. Range 0 -  $\sim 6\text{g/cc}$

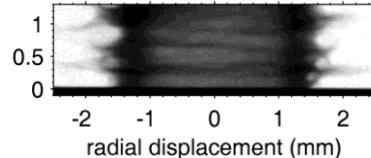
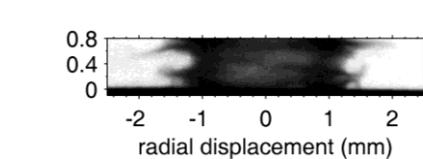
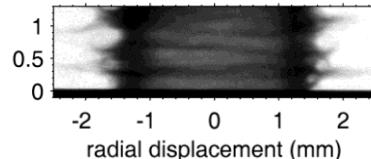
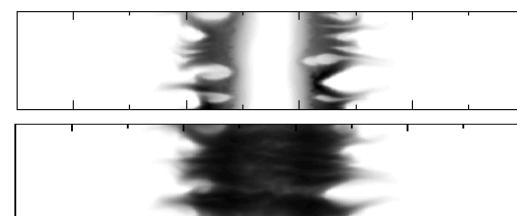
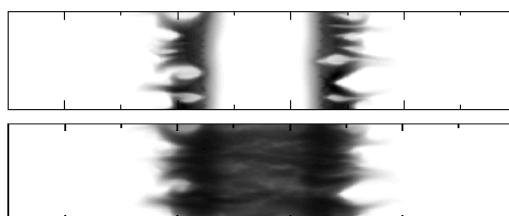
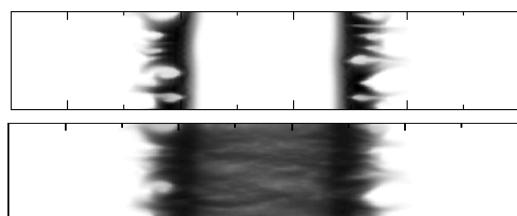
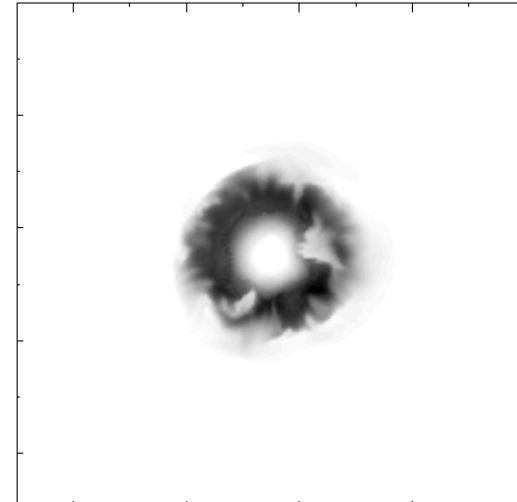
$t=148\text{ns}$



$t=153\text{ns}$



$t=157\text{ns}$





Assessing integrity of inside surface is complicated  
from side on radiography (R. McBride)

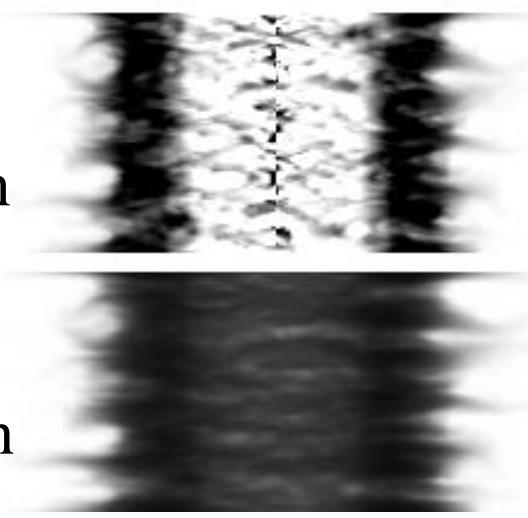


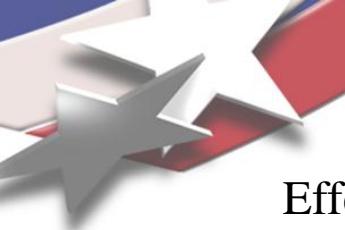
Density  
Slice



Abel  
Inversion

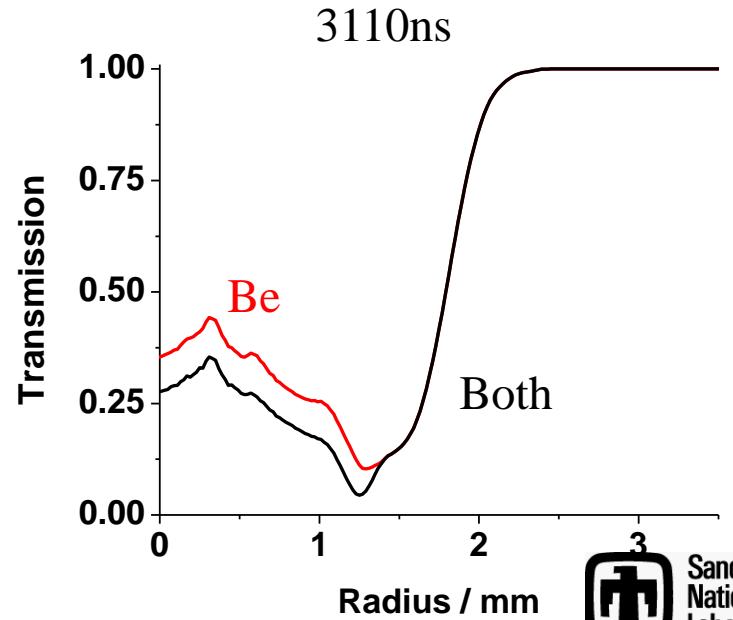
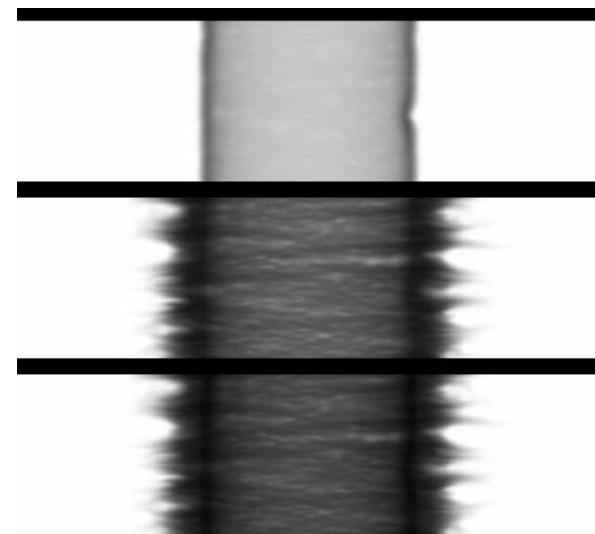
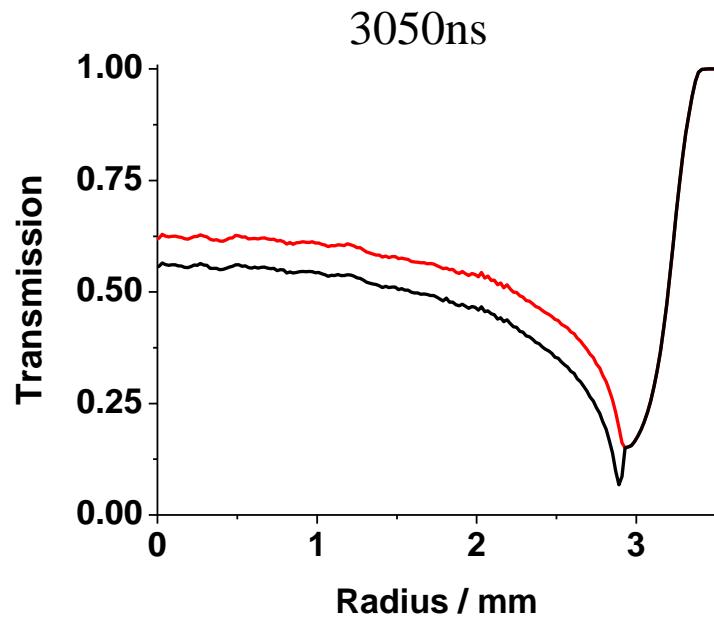
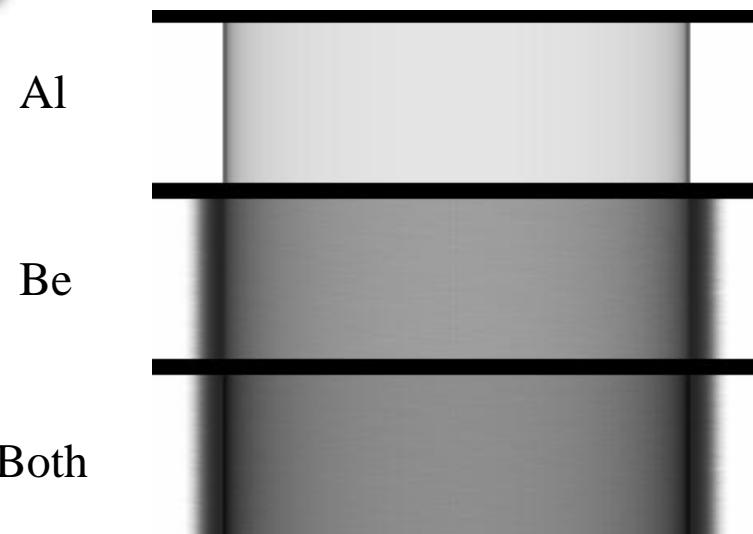
Synthetic  
Radiograph





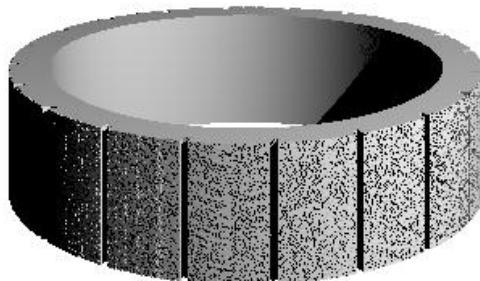
Inner surface can be better highlighted by coating inner surface (D. Ryutov)

## Effective 2 micron Al inner coating with Standard random cell by cell initial

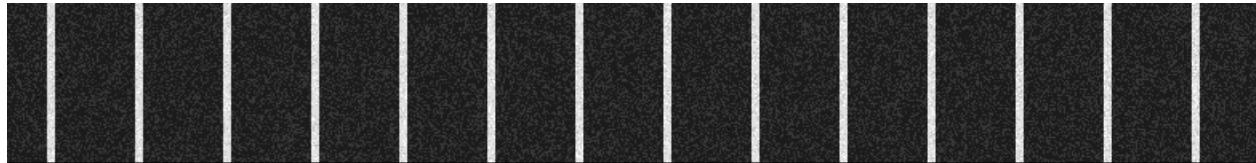




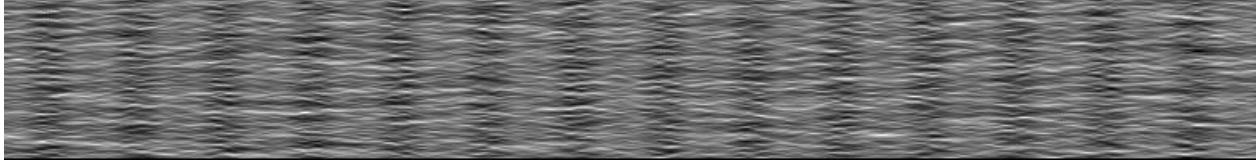
# Short Wavelength Vertical features do not grow.



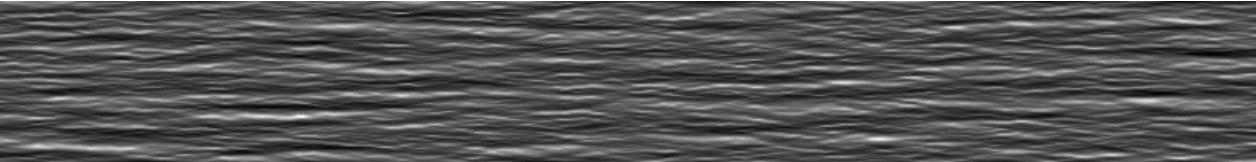
Initial



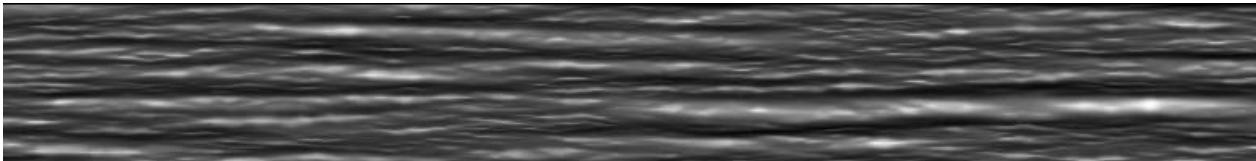
3070



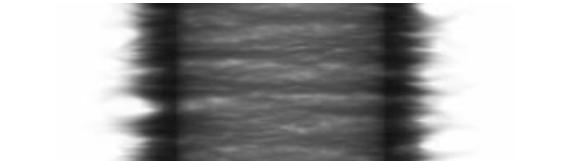
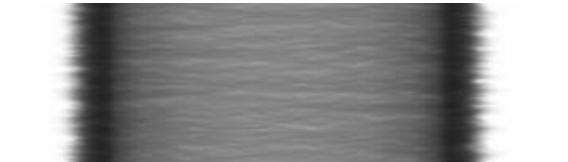
3090



3110



Initial 80 micron deep groove

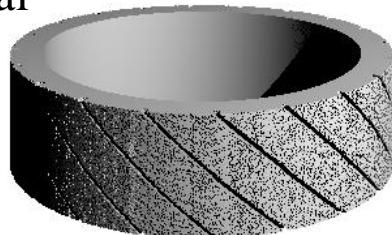




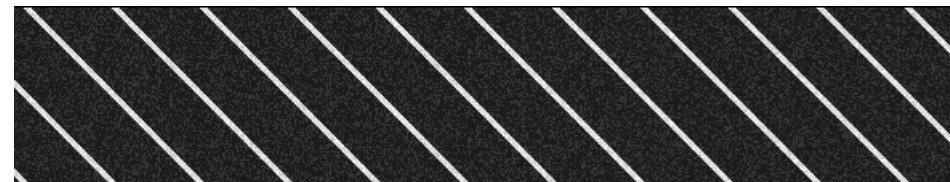
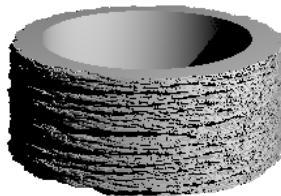
# Reorientation the perturbation away from azimuthal prevents it from growing

Periodic boundary conditions in Z to study helical perturbation growth

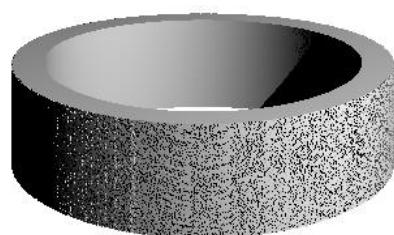
Initial



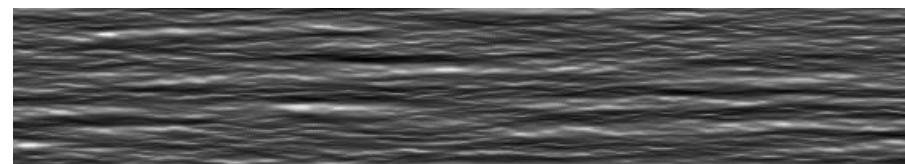
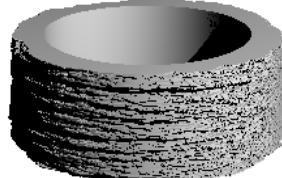
3095ns



Initial

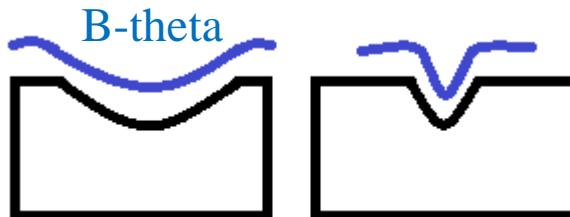
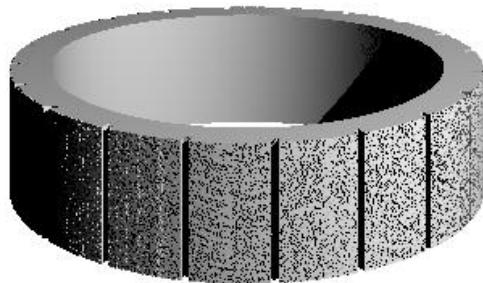


3095ns



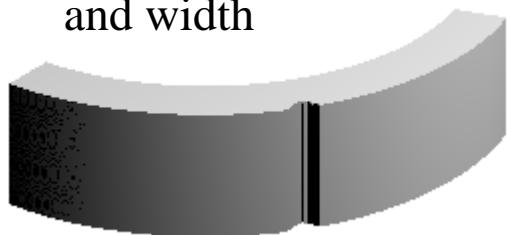


Vertically orientated perturbations do not persist as the field line tension does not allow them to grow and penetrate

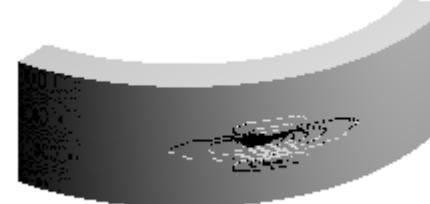
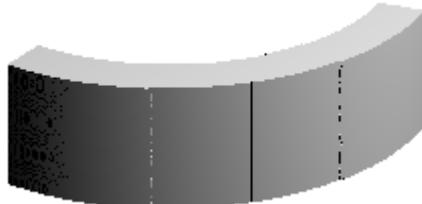
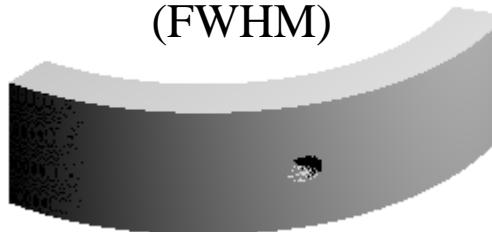


Field line tension will not allow us to simply drill a hole through the liner

Groove of same depth and width



~100 micron hole (FWHM)





Presence of a large initial  $B_z$  field does not significantly reduce instability growth, but can change their angle

Initial  $B_z$  field can re-orientate instabilities on outer surface, but does not seem to significantly inhibit growth

No initial  $B_z$  field

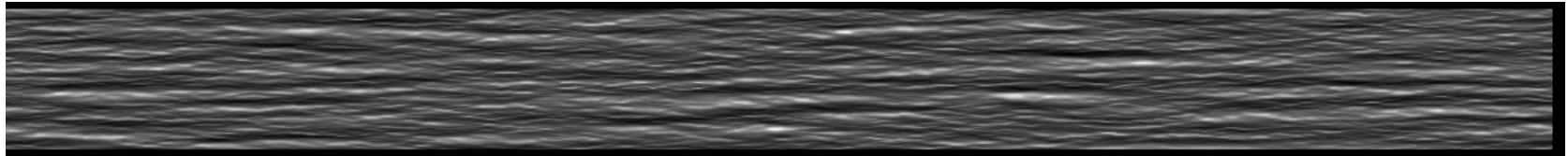
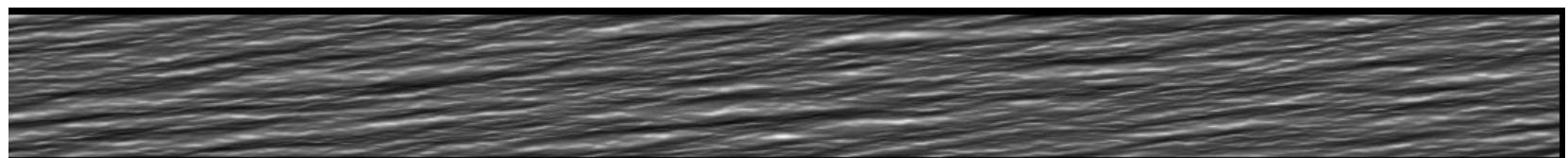
3095ns



100T initial  $B_z$  field



100T initial  $B_z$  field



No initial  $B_z$  field



3 different resolutions, essentially run with increasing smoothness  
does not significantly alter the level of late time disruption

Slices

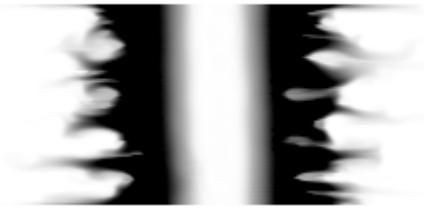
20 micron



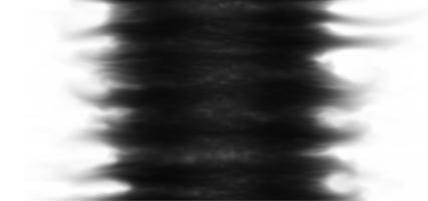
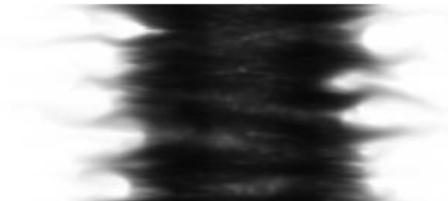
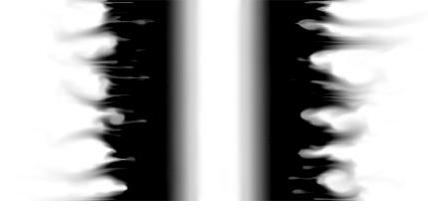
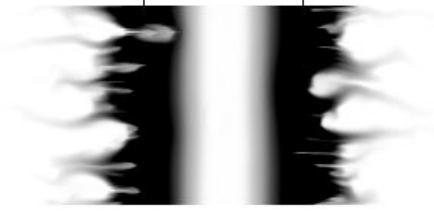
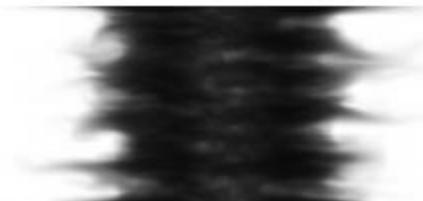
15 micron



10 micron



Radiograph

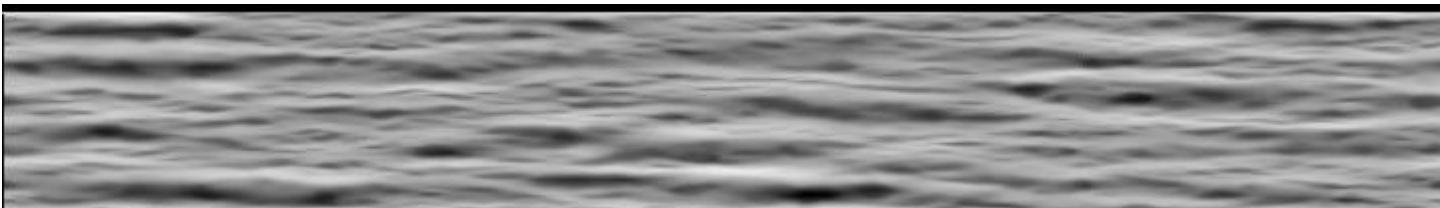




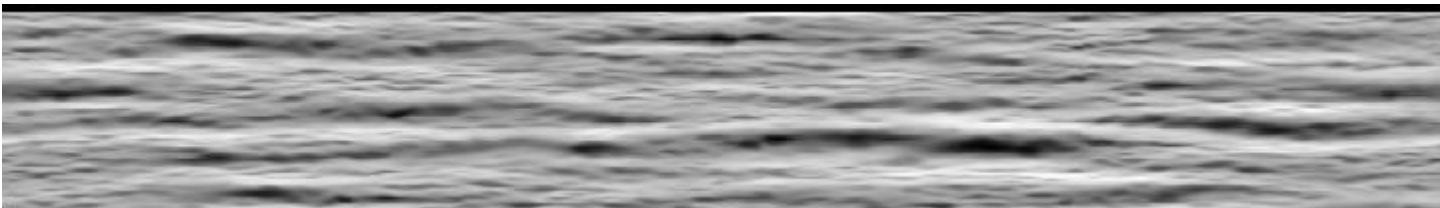
Unwrap surface to study extent to which instabilities grow at different resolutions

Some finer structures exist at higher resolution, but gross features are comparable

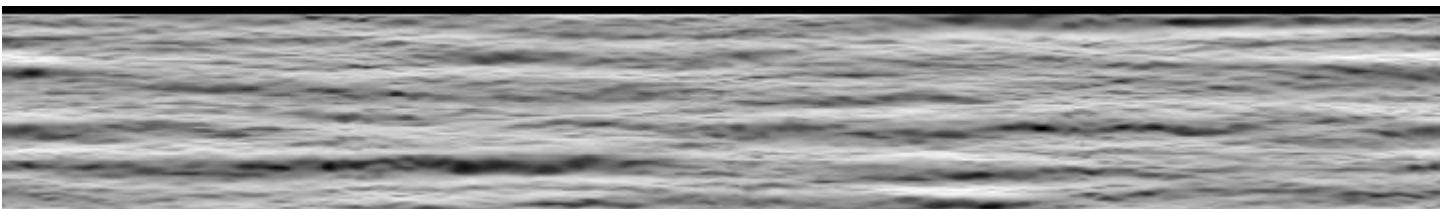
20 micron



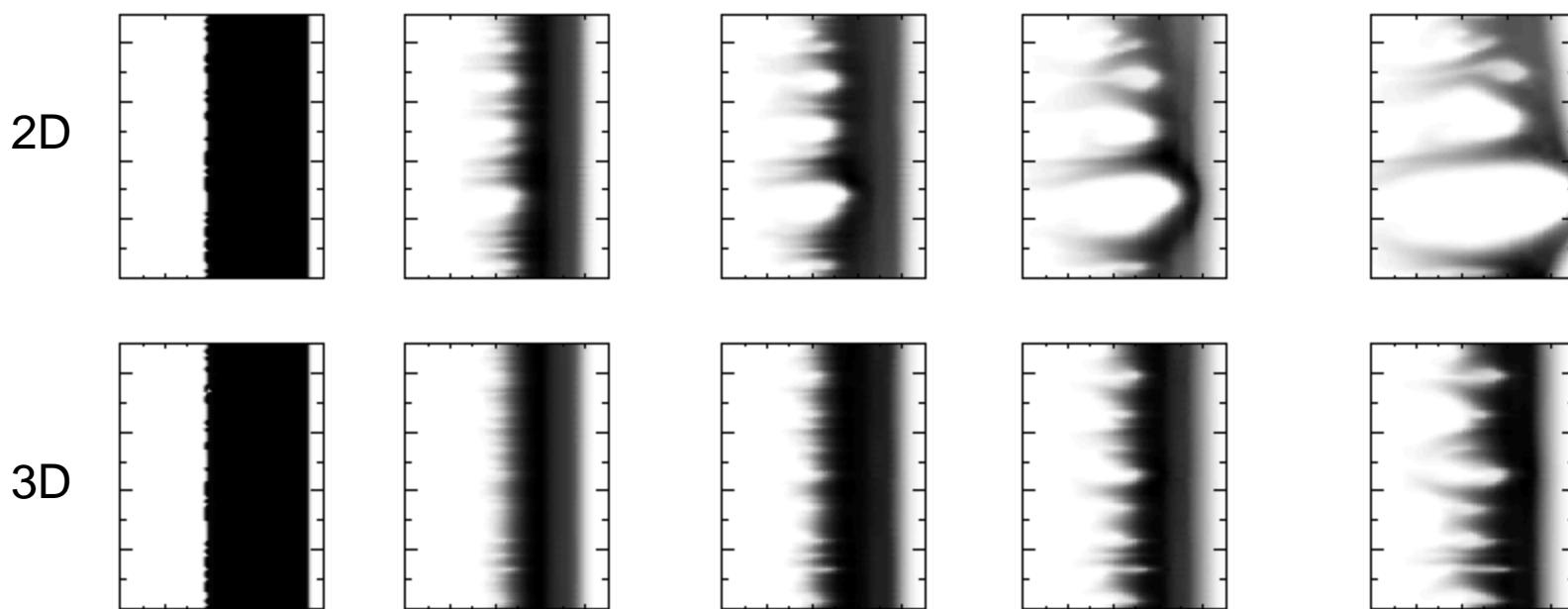
15 micron



10 micron



Liner R-T growth rate comparison of 3D full circumference, and 2D initialized with a slice through the 3D initial conditions. MRT perturbation growth far more aggressive in 2D from the same initial conditions. 3D initial perturbation was a random 1 cell perturbation to the outside surface over the entire surface.



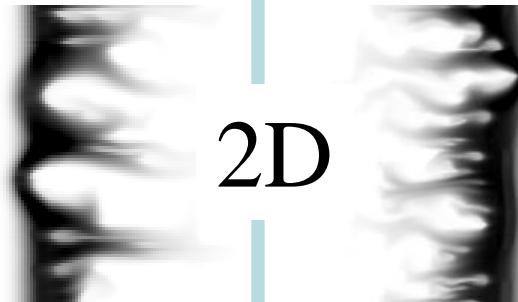
These calculations used EXACTLY the same physics packages, hydro routines, cooling rates, thermal diffusion rates etc... They were exactly the same code, just employing a geometry change



Finer resolution, and smoother initial surface in 2D, does reduce the level of disruption at later times

20 micron

3105ns



10 micron

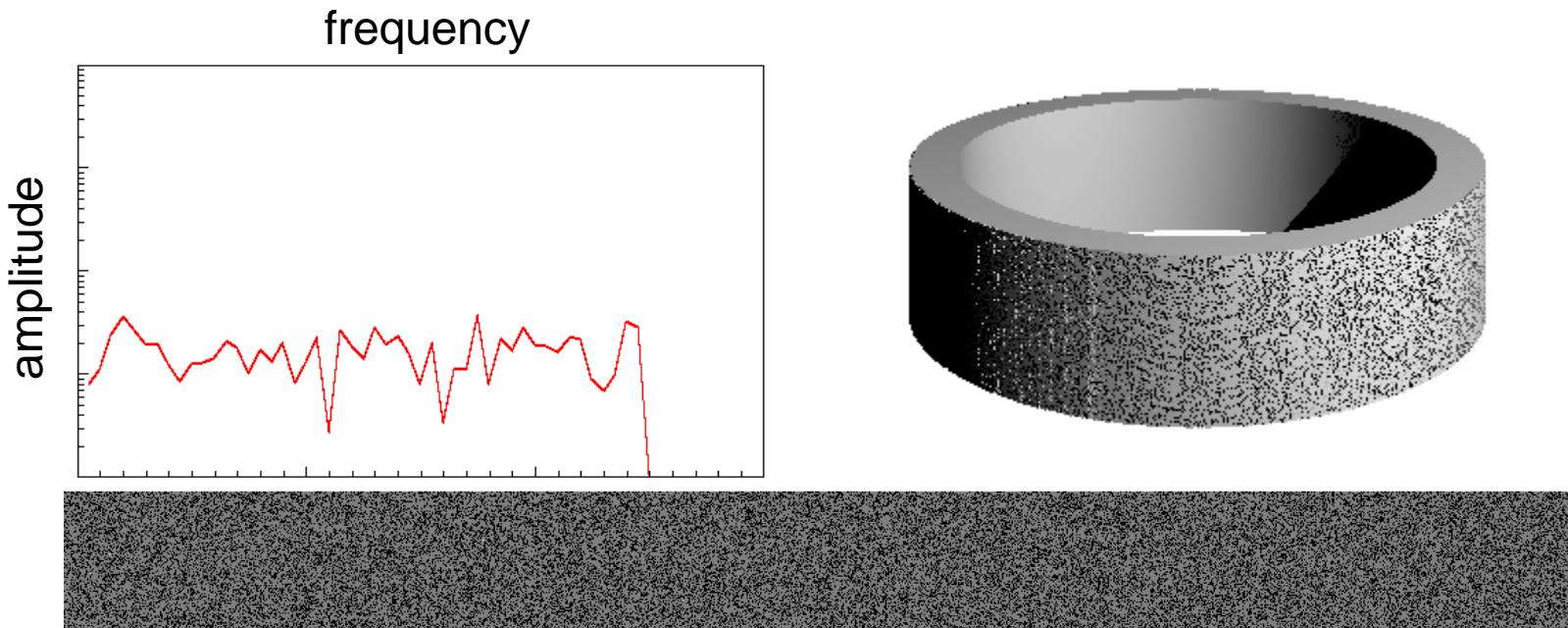


2D

3D



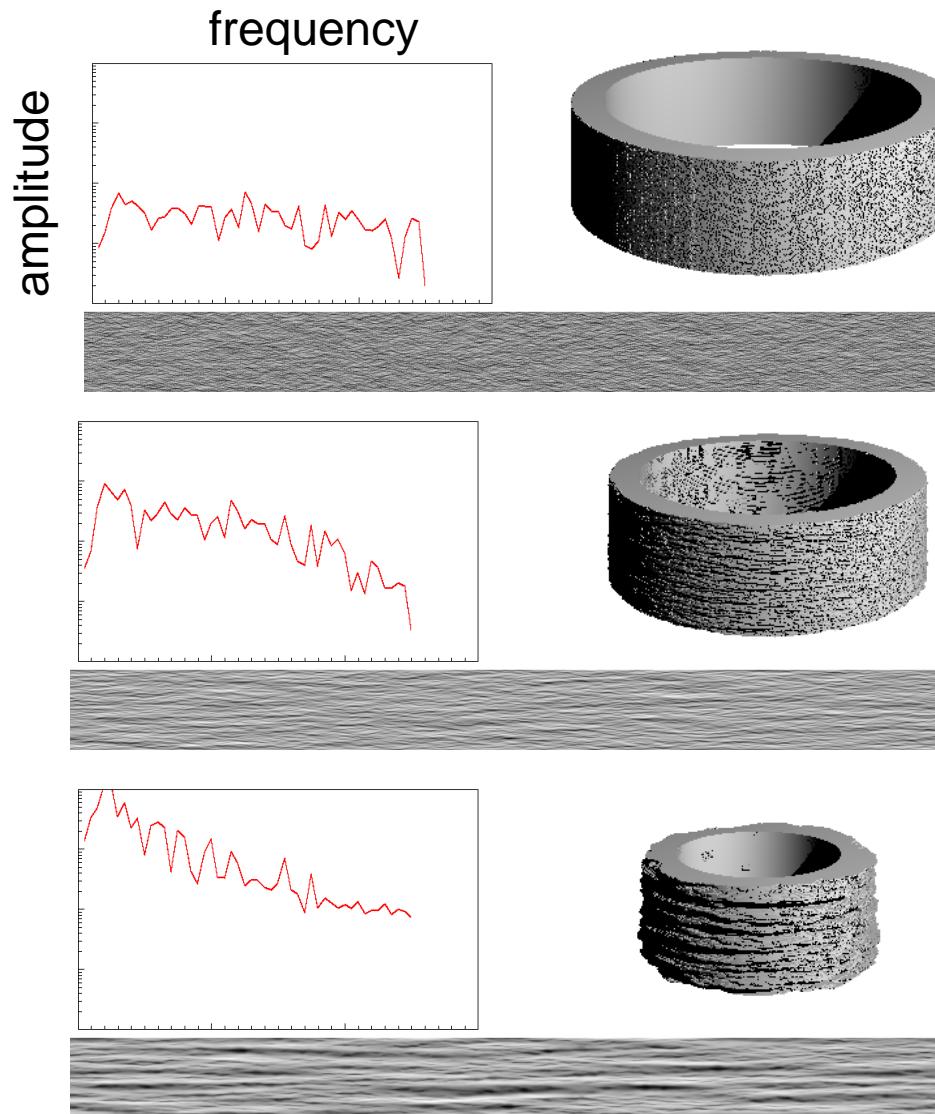
# Fourier transform of initial random surface finish



Essentially a white noise spectrum cutting off around the highest frequency supported by the grid (~20 microns)



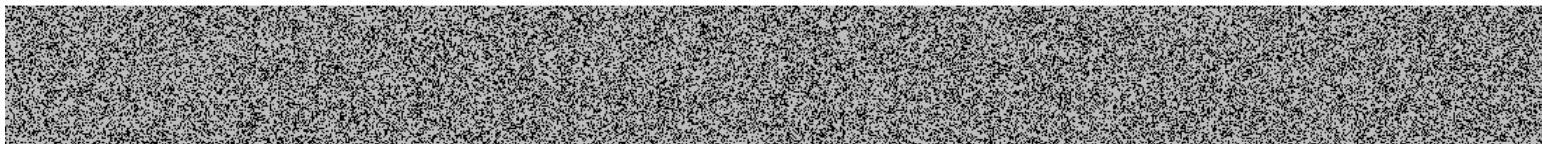
# Lower frequency modes grow faster and ultimately dominate



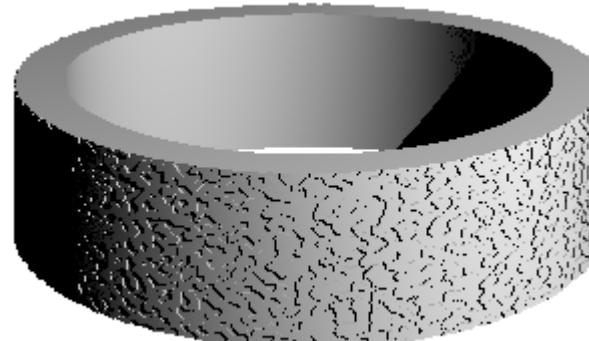
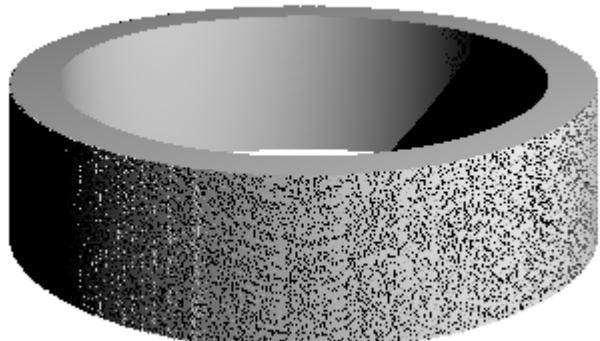
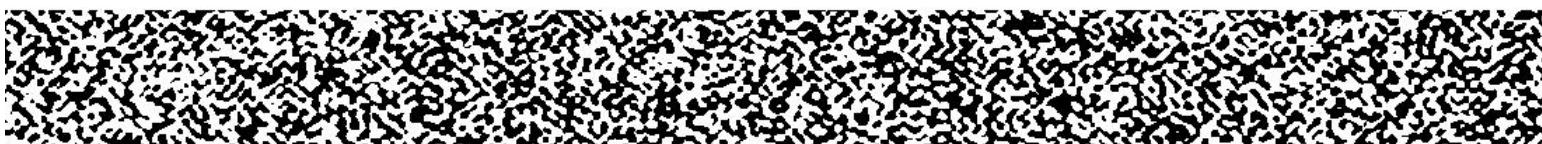


Clip off all the high frequency components and we are left with the low frequency component of the initialization

Standard white noise initialization



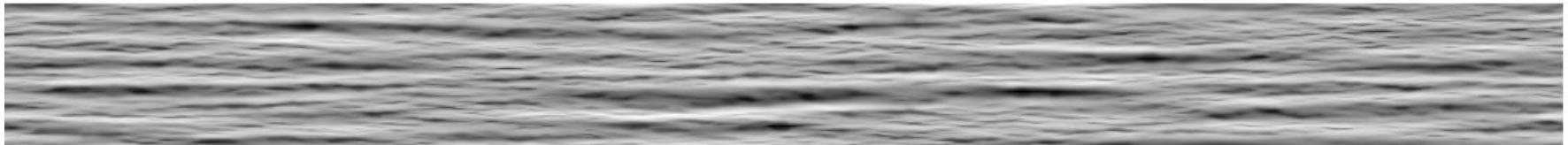
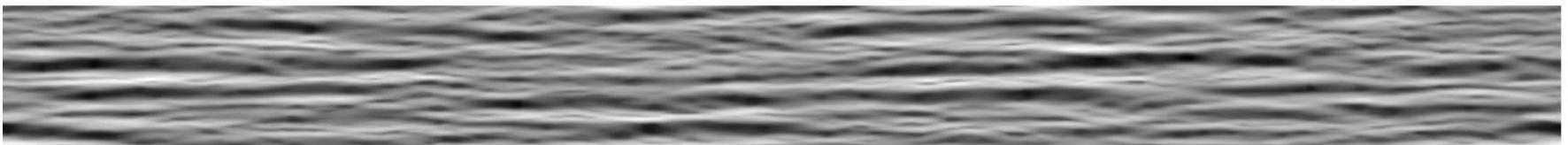
High frequency component of instabilities removed





# Location of late time disruption does not depend on evolution of short wavelength instabilities

High frequency component of instabilities removed (3095 ns)



Standard white noise initialization (3110ns)



# Conclusions

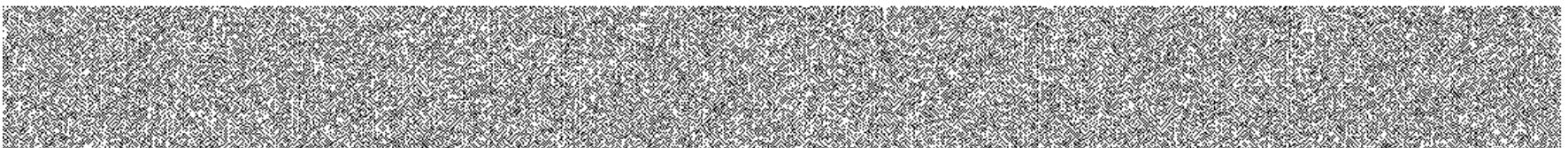
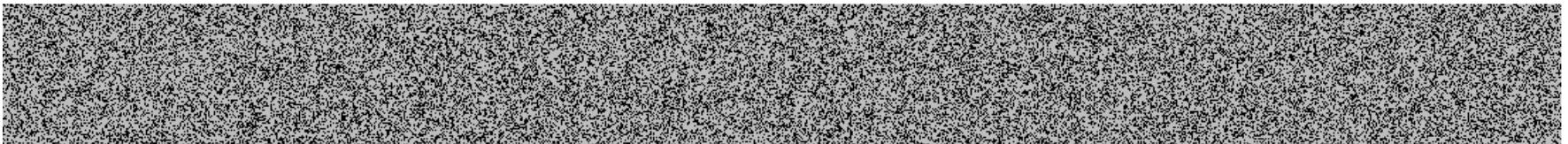
If surface perturbations are seeding late time instabilities then:

- To disrupt an imploding shell a perturbation needs some azimuthal extent.
- Perturbations grow and correlate quite slowly in the azimuth
- Real damage can be done if the initial seed perturbation has any azimuthal correlation
- If an infinitely smooth liner is an unrealistic ideal, then there are surface structures we can pick to leave behind that are better than others
- Local surface smoothness is potentially not as important as macroscopic longer wavelength structures that underpin the shorter wavelength instabilities.

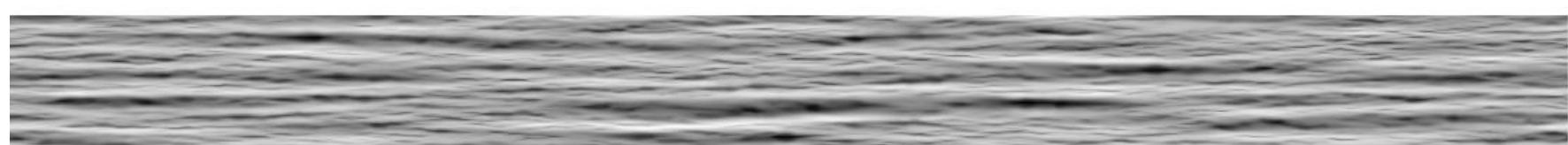


(Backup)

Alternatively, retain the high frequency component  
and loose the longer wavelength



Standard white noise initialization



Standard white noise initialization