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Title: Development of capabilities to simulate the coupled thermal-hydrological-mechanical-chemical (THMC) processes during in situ oil shale production

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# Development of capabilities to simulate the coupled thermal-hydrological-mechanical-chemical (THMC) processes during *in situ* oil shale production

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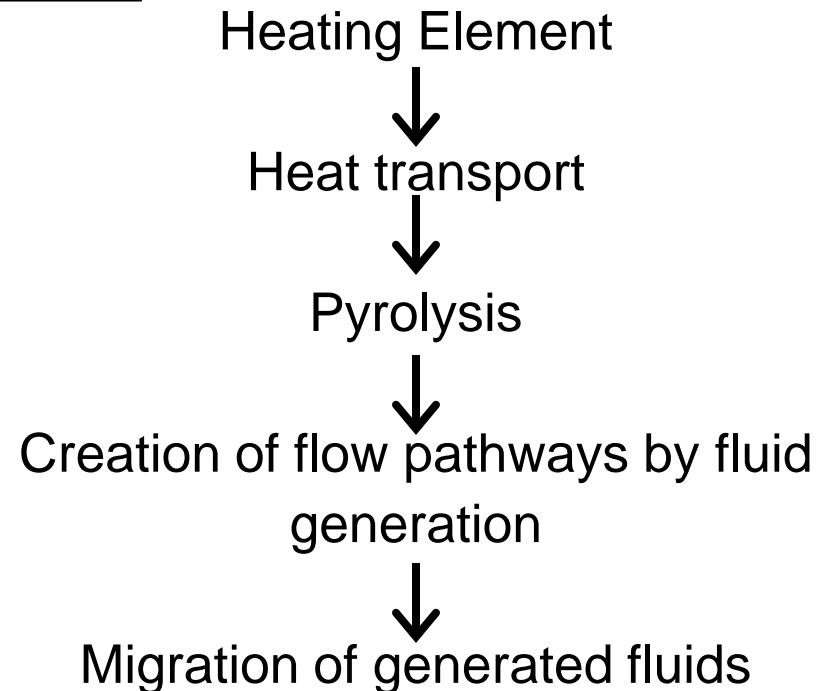
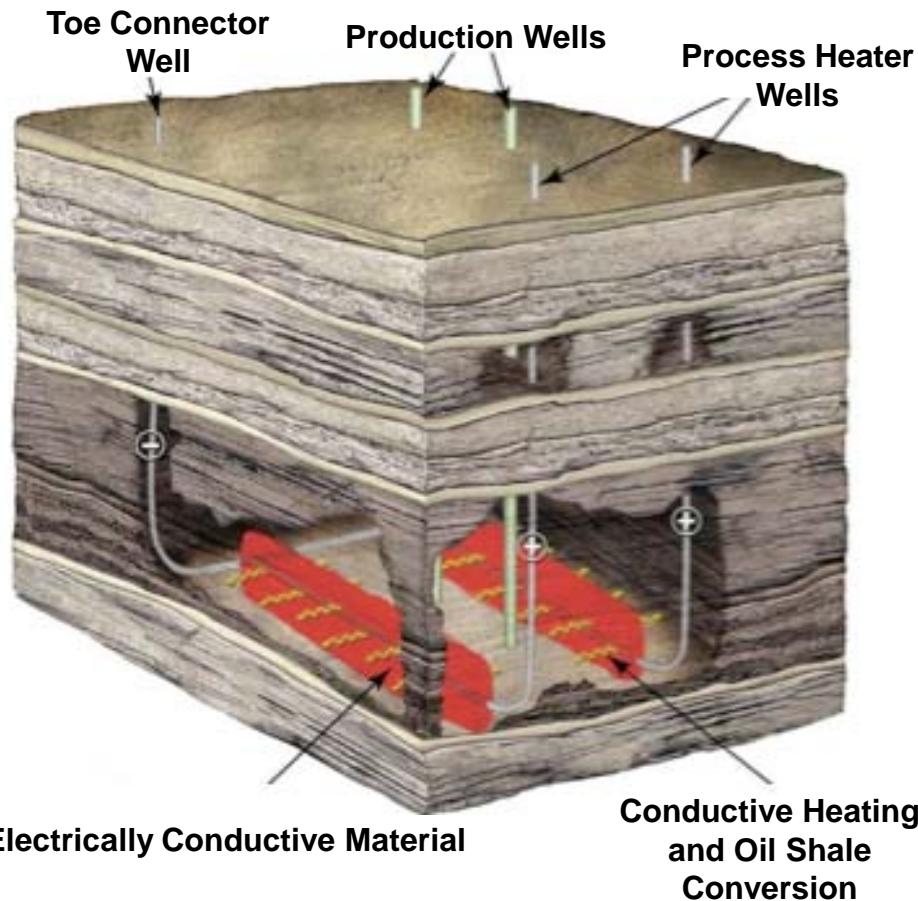
# Motivation

Coupled thermal-fluid flow-mechanical-chemical processes are important in many subsurface energy and environment applications including

- Unconventional oil and gas production
- $\text{CO}_2$  sequestration
- Geothermal energy production
- Nuclear waste storage

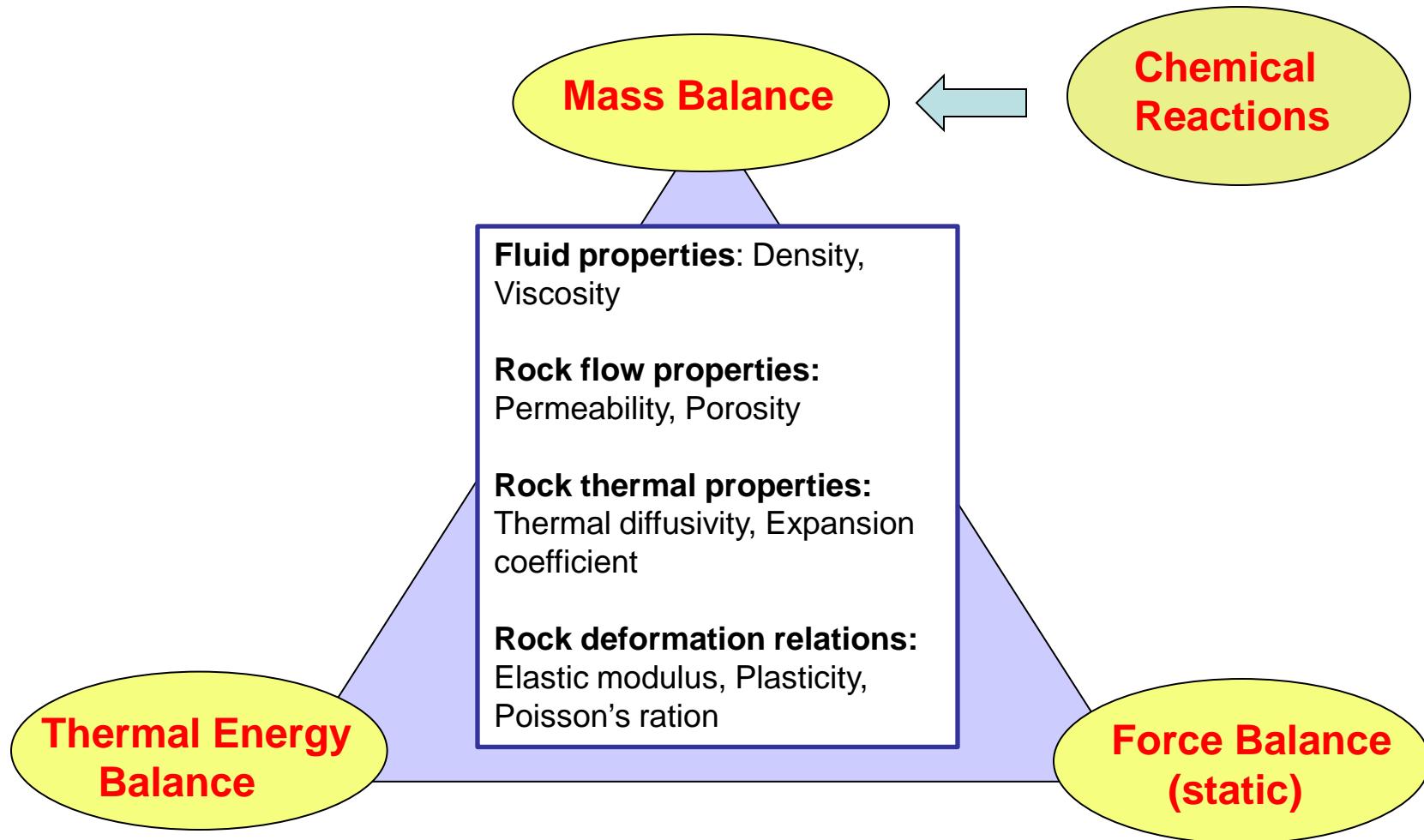
# Full physics modeling of *in situ* heating processes is challenging

## ExxonMobil's *in situ* oil-shale recovery process



Mimicking *in situ* heating processes requires coupled thermal, mechanical, chemical, and multiphase flow modeling

# Numerical Model-Conservation Equations



Variables: pressure, temperature, saturation, composition, deformation

# LANL's FEHM simulator is being modified for oil shale simulator development

- **FEHM: Finite Element Heat and Mass**
  - Had the coupled thermal-flow-mechanics simulation capability applicable to elastic response
  - Control-volume-finite-element (CVFE) approximation:
    - Control volume for mass/energy balance
    - Finite element for stress
- **FEHM has been verified through extensive applications:**
  - Over 30 years of development and application
    - Groundwater modeling
    - Contaminant transport and reactions
    - Methane hydrate reservoir production
    - CO<sub>2</sub> sequestration
    - Geothermal

# Developing new thermal-hydrological-mechanical-chemical (THMC) modeling capabilities in FEHM

- **Thermal:**
  - Anisotropic, temperature-dependent thermal properties
- **Hydrological (multiphase flow):**
  - Black oil model (k-value based phase equilibrium)
  - EOS based properties
- **Mechanical:**
  - Anisotropic, temperature-dependent mechanical properties
  - Plastic/elastic deformation models
  - Stress-dependent changes in porosity and permeability
- **Chemical:**
  - Kerogen conversion into oil/gas/coke and subsequent reactions

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# Component mass conservation

$$\frac{\partial A_n}{\partial t} + \bar{\nabla} \cdot \bar{f}_n + q_n + q_{nr} = 0 \quad n - \text{oil, water, gas}$$

$$A_n = \phi (S_o \rho_o x_n + S_g \rho_g y_n + S_w \rho_w w_n) \quad \text{Accumulation}$$

$$\bar{f}_n = x_n \rho_o \bar{v}_o + y_n \rho_g \bar{v}_g + w_n \rho_w \bar{v}_w \quad \text{Advection}$$

$$q_n = \bar{q}_o x_n + \bar{q}_g y_n + \bar{q}_w w_n \quad \text{Source/sink}$$

$$q_{nr} = f(\text{Kerogen Content}) \quad \text{Reaction}$$

$\phi$  – Total porosity which includes solid with kerogen plus liquids and gas

$$\bar{v}_l = -\frac{kk_{rl}}{\mu_l} (\bar{\nabla} P_l - \rho_l \bar{g}) \quad k_{rl} = f \left( S'_l = \frac{S_l}{S_w + S_o + S_g} \right)$$

# Total energy conservation

$$\frac{\partial A_e}{\partial t} + \bar{\nabla} \cdot \bar{f}_e + q_e + q_{er} = 0$$

$$A_e = (1 - \phi) \rho_r u_r + \phi (S_o \rho_o u_o + S_g \rho_g u_g + S_w \rho_w u_w + S_s \rho_s u_s) \quad \text{Accumulation}$$

$$\bar{f}_e = \rho_o h_o \bar{v}_o + \rho_g h_g \bar{v}_g + \rho_w h_w \bar{v}_w - K \bar{\nabla} T \quad \text{Advection + conduction}$$

$$q_e = \bar{q}_o h_o + \bar{q}_g h_g + \bar{q}_w h_w \quad \text{Source/sink}$$

$$q_{er} = \text{Heat of reaction} \quad \text{Reaction}$$

# Static Stress Equilibrium Equations-Finite Element Formulation for infinitesimal elastic deformation, with pore pressure and thermal terms

$$\sum_i \left\{ \int \left[ \frac{\partial N_j}{\partial x_l} (\lambda + 2G) \frac{\partial N_i}{\partial x_l} + \frac{\partial N_j}{\partial x_m} G \frac{\partial N_i}{\partial x_m} + \frac{\partial N_j}{\partial x_n} G \frac{\partial N_i}{\partial x_n} \right] dv \right\} U_{l_i}$$

$$+ \sum_i \left\{ \int \left[ \frac{\partial N_j}{\partial x_l} \lambda \frac{\partial N_i}{\partial x_m} + \frac{\partial N_j}{\partial x_m} G \frac{\partial N_i}{\partial x_l} \right] dv \right\} U_{m_i}$$

$$+ \sum_i \left\{ \int \left[ \frac{\partial N_j}{\partial x_l} \lambda \frac{\partial N_i}{\partial x_n} + \frac{\partial N_j}{\partial x_n} G \frac{\partial N_i}{\partial x_l} \right] dv \right\} U_{n_i}$$

$$- \sum_i \left\{ \int \left[ N_j \frac{\partial N_i}{\partial x_l} \frac{K}{H} \right] dv \right\} \Delta P_i - \sum_i \left\{ \int \left[ N_j \frac{\partial N_i}{\partial x_l} \frac{\alpha E}{(1-2\nu)} dv \right] \right\} \Delta T_i$$

+ Body Force Terms + Surface Terms = 0

$U_{l_i}$  = nodal displacements

$E$	Young's modulus
$\nu$	Poisson's ratio
$u_i$	Displacement
$\alpha$	Coeff. of Thermal Expansion
$\frac{\alpha_B}{K}$	Biot coeff.

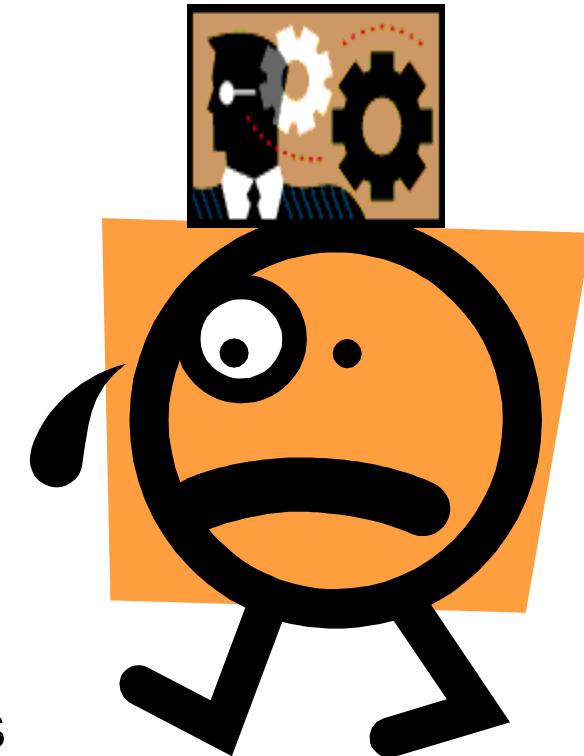
$$G = \frac{E}{2(1+\nu)}$$

$$\lambda = \frac{E_\nu}{(1+\nu)(1-2\nu)}$$

$$K = \frac{E}{3(1-2\nu)}$$

# Modeling challenges

- Large changes in fluid pressure
- Large changes in temperature
- Large changes in stress
- Large problem size
- Highly nonlinear
- Many different space and time scales
- Matrix rock and fractures/faults are both important



# How coupling occurs in the equations

- **Explicit terms in equations**

effective stress and thermal stress in the Force Balance

- **Dependence of coefficients**

$$\phi(\varepsilon, \sigma, p, T) \quad K(\varepsilon, \sigma, p, T)$$

In fractured media, permeability has power (cubic or higher) dependence on aperture . Growing body of literature, a number of permeability-deformation models

- **Dependence of rock properties and reaction kinetic parameters**

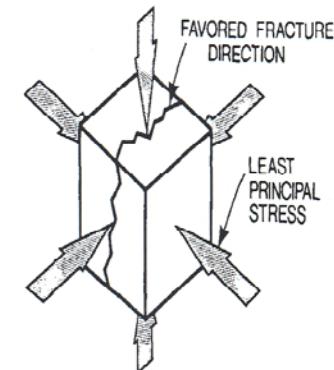


Figure 1. Stress element and preferred plane of fracture (after Hubbert and Willis, 1957).

# Flow and stress coupling

## Permeability – Aperture – Deformation – Strain - Stress

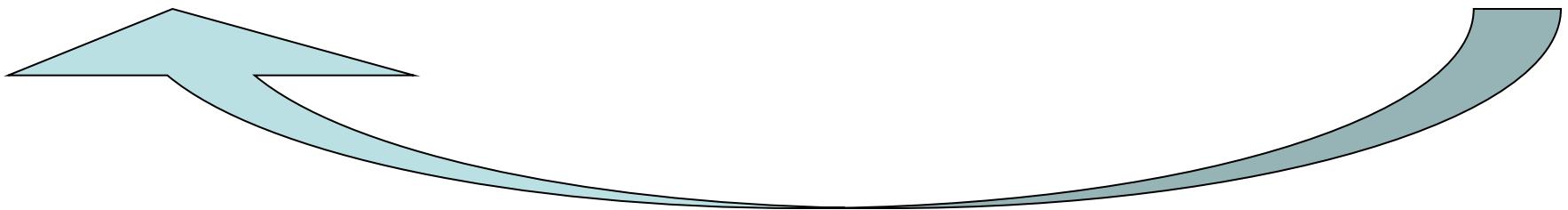
- Power Law

- Mechanical
- Hydraulic

- Tensile
- Shear

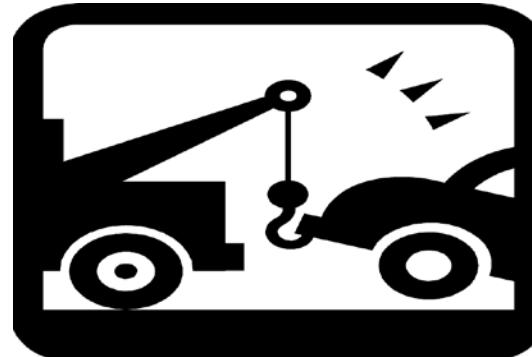
- Elastic
- Plastic

- Tectonic
- Gravity
- Thermal
- Pore Pressure



Growing body of literature, a number of permeability-deformation models

# Levels of coupling



**Desirable to be able to choose between fully implicit coupling and explicit coupling, depending upon the domain of interest**

For example, near-field (~10's m) strong gradients might be expected requiring full coupling (microseismicity, surface deformation, fracture generation due to pore pressure) where as in the mid-field (~km) (microseismicity, surface deformation) explicit coupling may be sufficient, and far-field (10's km) may be adequately treated by uncoupled models.

# **Example: coupled flow-stress modeling (permeability change)**

# Comparison with field data

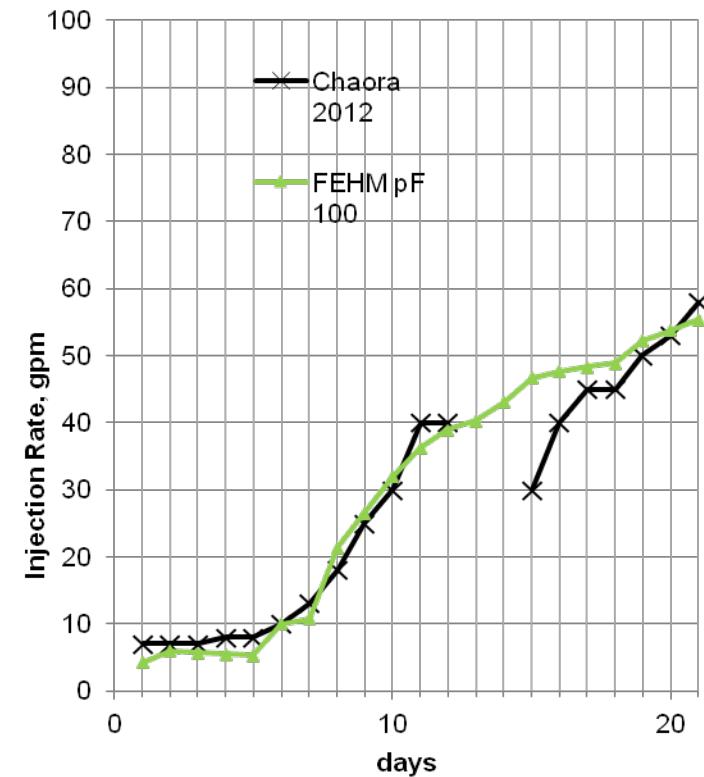
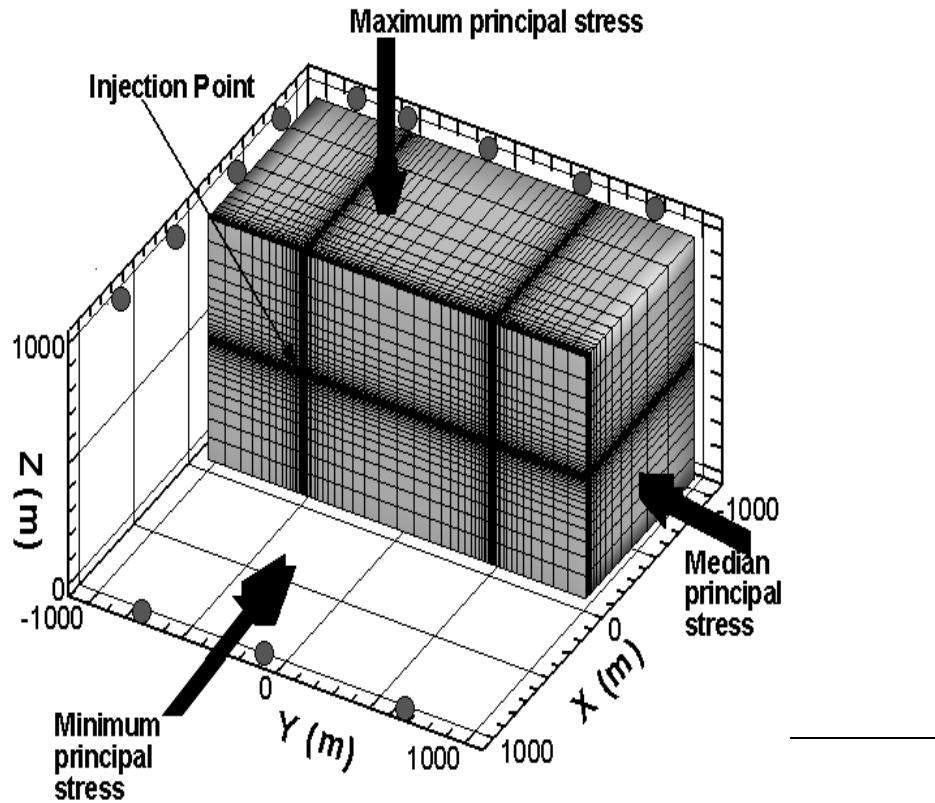
Injection of cold water into a geothermal reservoir at pressure below fracture opening.

2km x 2km x 1km grid with specified far-field stresses.

Shear failure using Mohr-Coulomb criteria (Permeability function of shear stress)

Key Conclusion:

Good match of field observations with model, permeability enhancement due to thermal stresses is important.



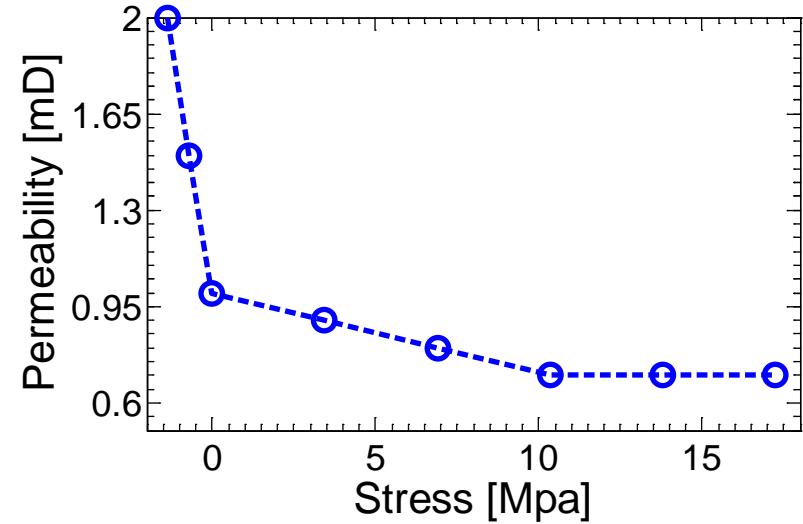
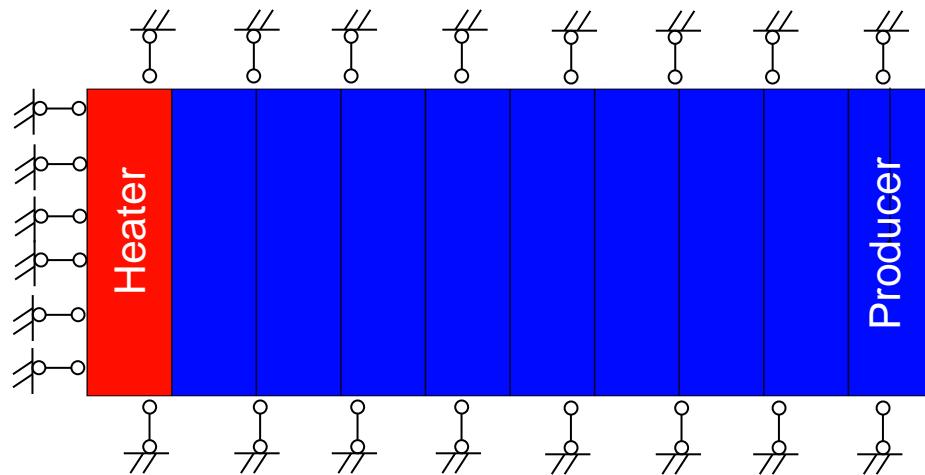
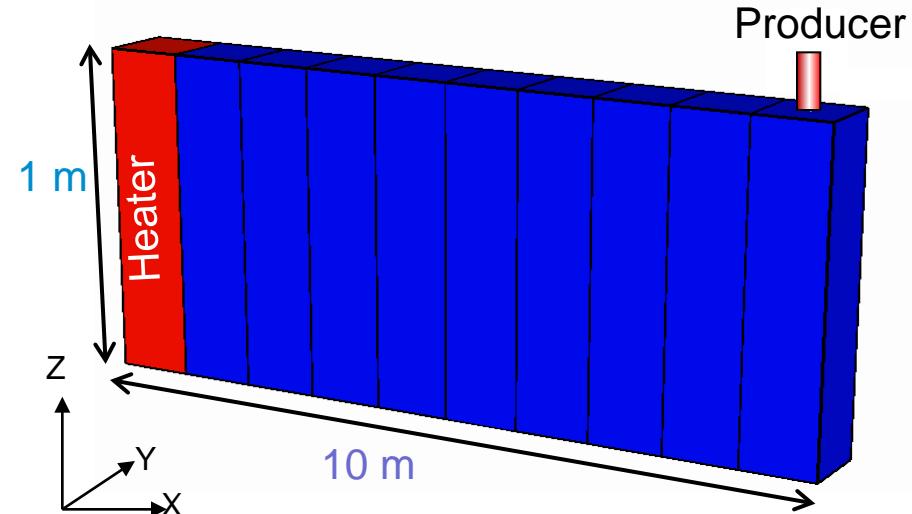
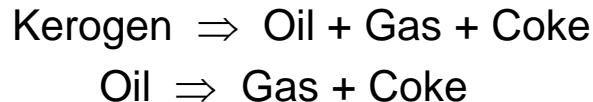
# **Cross-validation of FEHM's oil-shale simulation capability with CMG's STARS**

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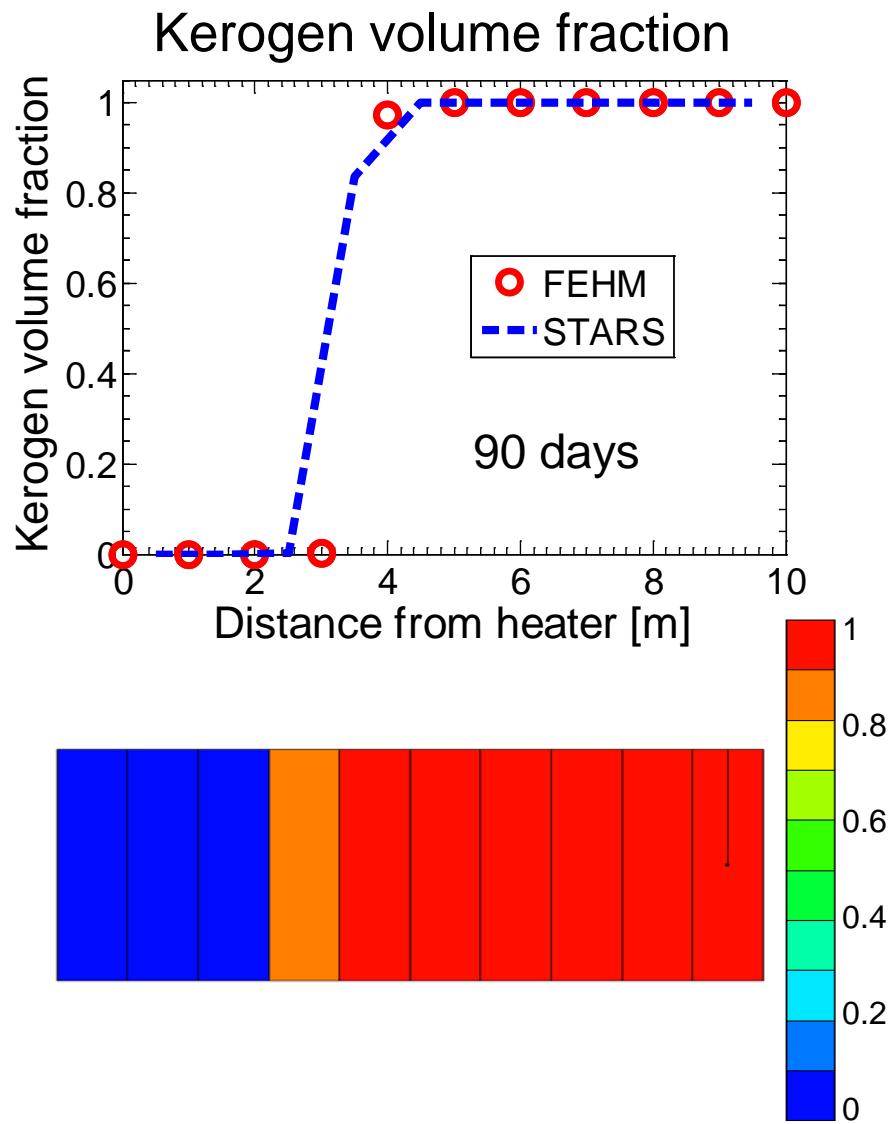
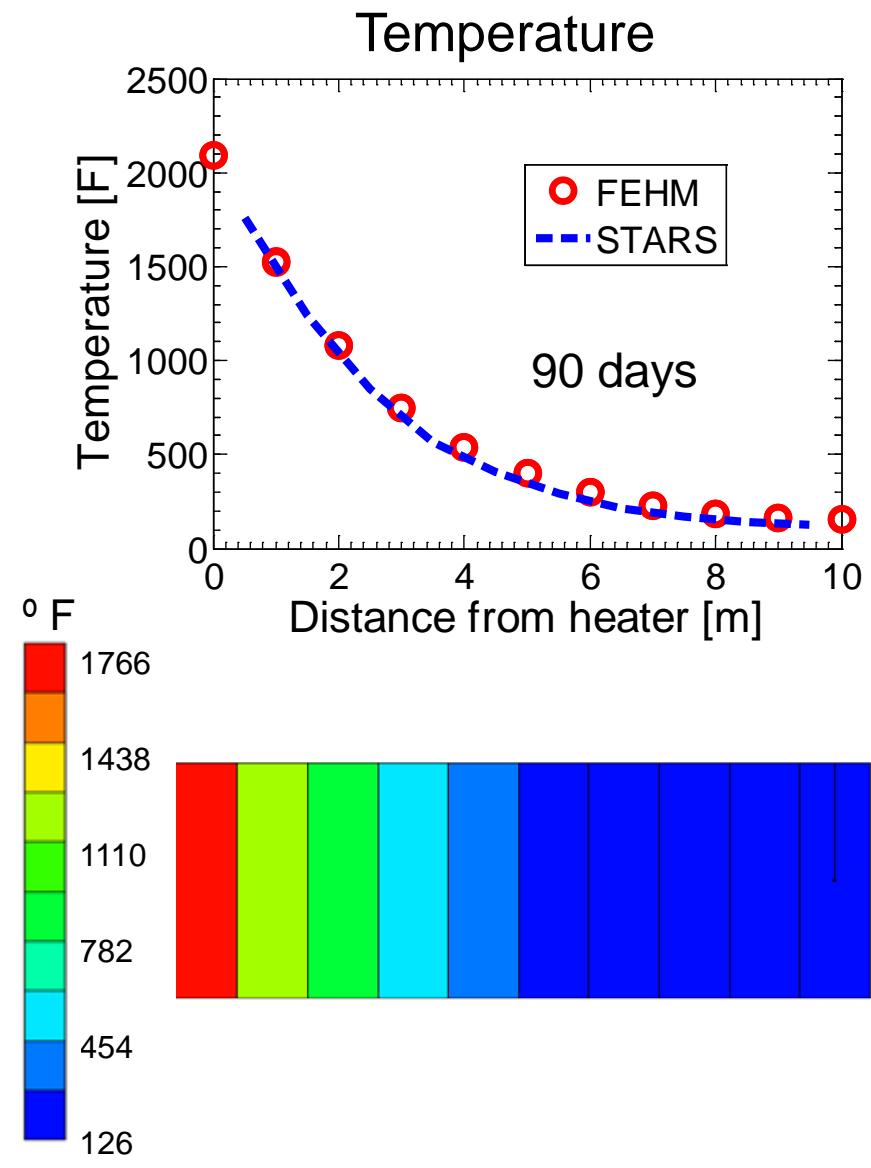
# Benchmarked some of FEHM's new THMC modeling capabilities against CMG's STARS

## Problem description:

- Richness 35 gal/ton (GPT)
- $P_{\text{Initial}} = P_{\text{well}} = 5.54 \text{ Mpa}$
- Stress-dependent permeability (empirical)
- $Q = 0.7 \text{ kW}$
- Reactions:

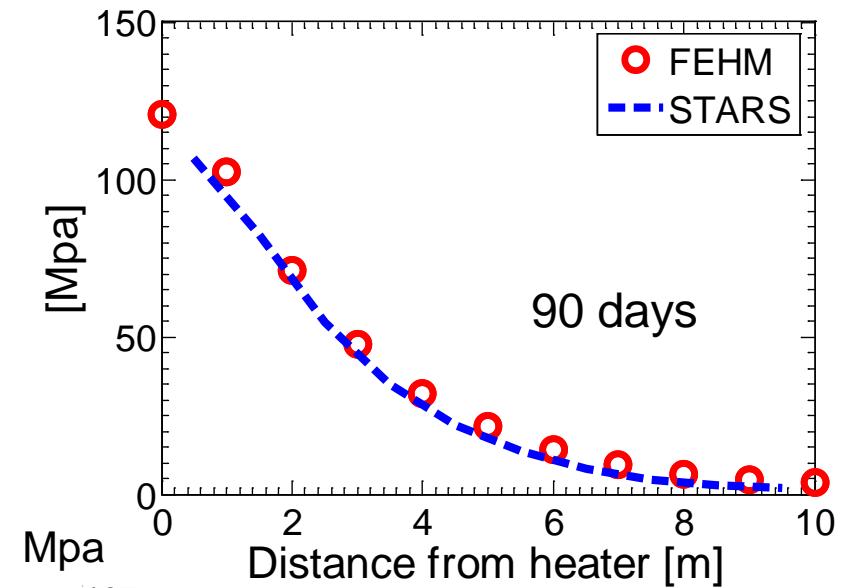


# FEHM's new THMC modeling predictions compare well with CMG's STARS

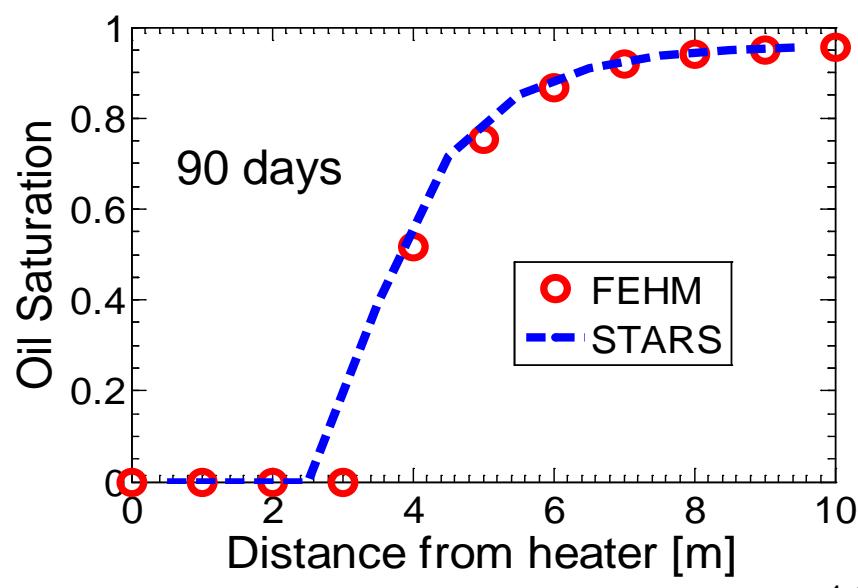


# FEHM's new THMC modeling predictions compare well with CMG's STARS

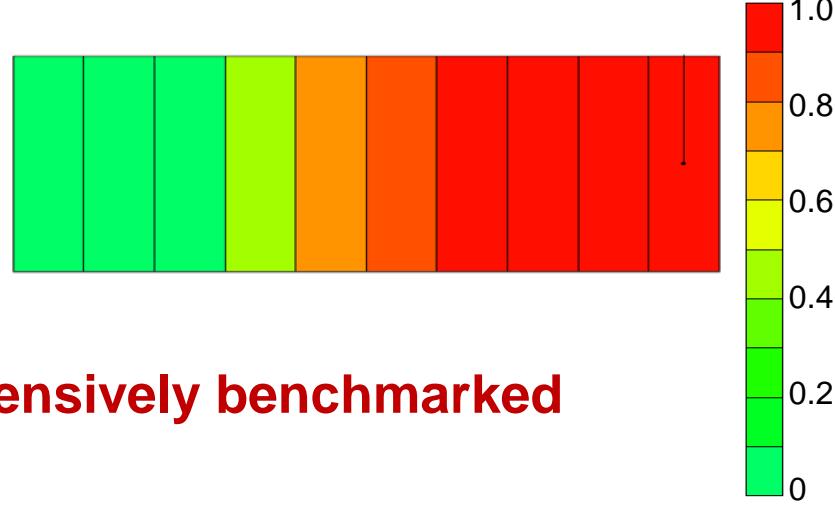
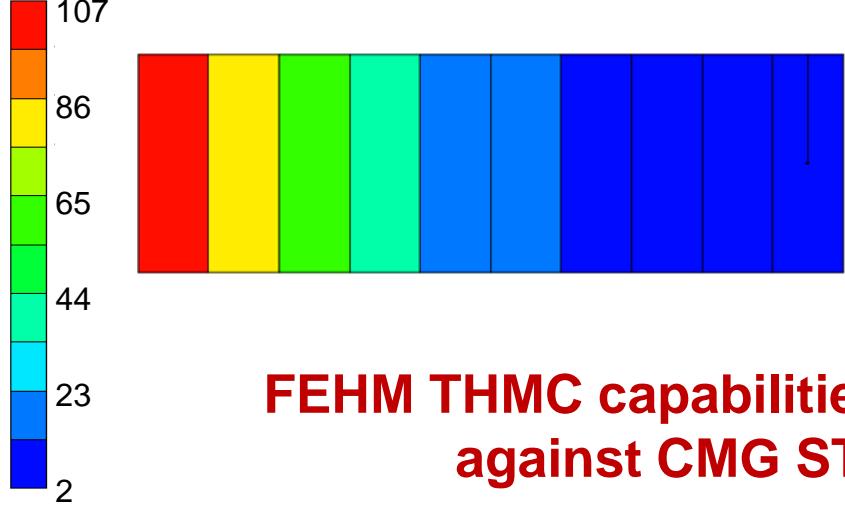
Effective normal stress in Z



Oil Saturation

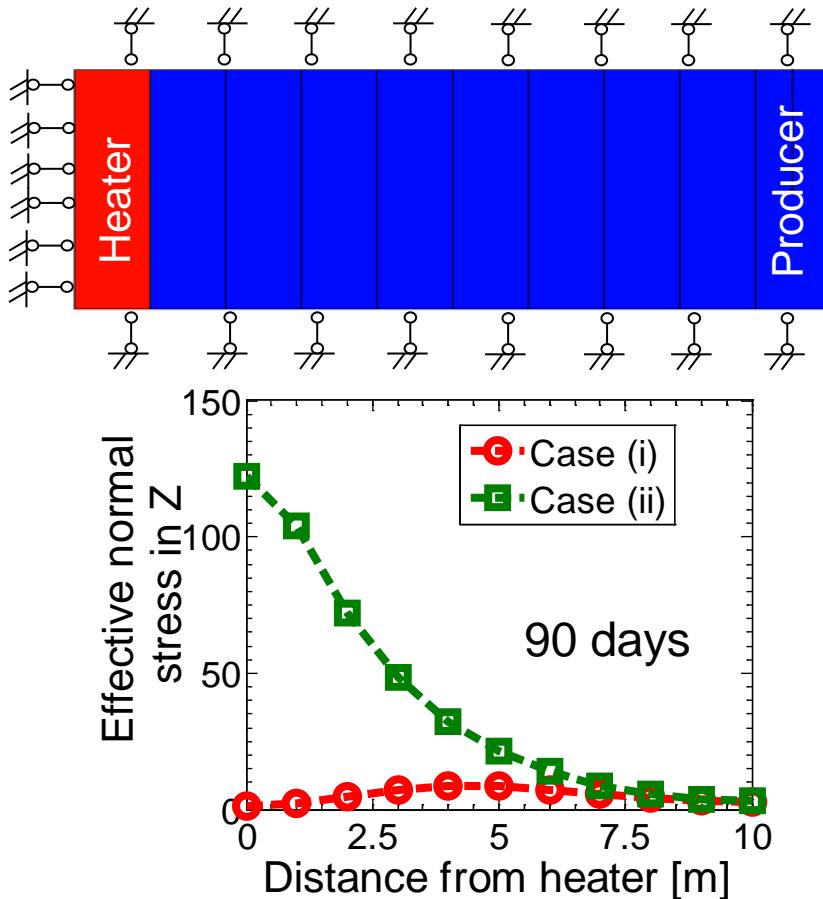


FEHM THMC capabilities extensively benchmarked  
against CMG STARS

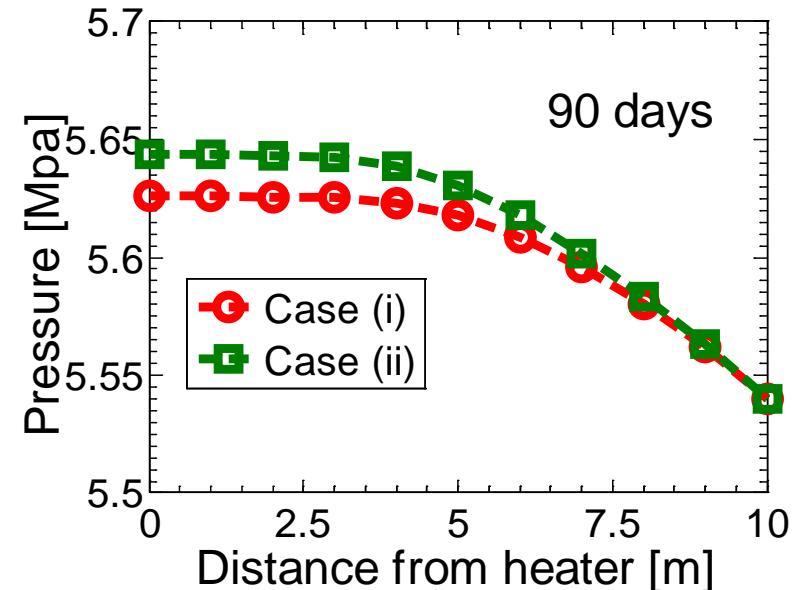


# FEHM's new THMC modeling capabilities go beyond contemporary commercial simulators

## Thermal softening



Case (i): thermal softening  
Case (ii): no temp. dependence



**Changes in rock properties with temperature will impact fluid recovery and formation stability**

# It's critical to model change in permeability with stress

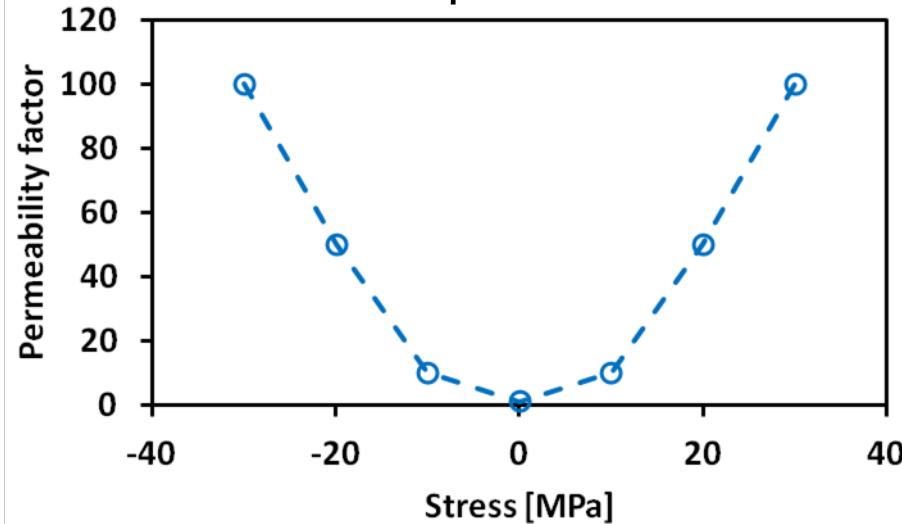
- Creation of permeable pathways due to change in stresses is critical for success of *in situ* process
- Permeability creation due to pore pressure change
  - Local effect
  - Need models that accurately capture change in permeability at continuum scale
- Our stress-perm model is limited in its ability to capture these sub-continuum scale pore-pressure effects
  - We used another hypothetical model in order to demonstrate how sub-continuum scale effects can be captured in continuum models

# Model to demonstrate effect of pore-pressure change on permeability

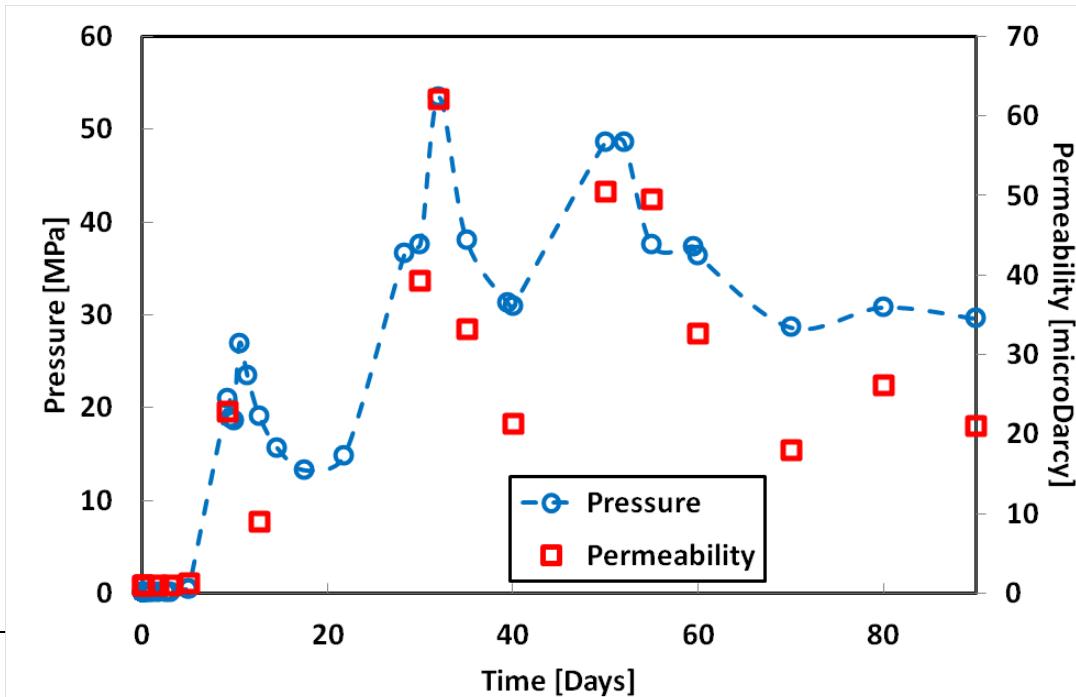
## Stress-perm model

### Problem description:

- Same as before except:
- Initial permeability 1  $\mu$ -Darcy
- Different stress-dependent permeability (hypothetical)
- No thermal stress effect (thermal expansion coefficient 0.0)



Pressure and permeability at heater node

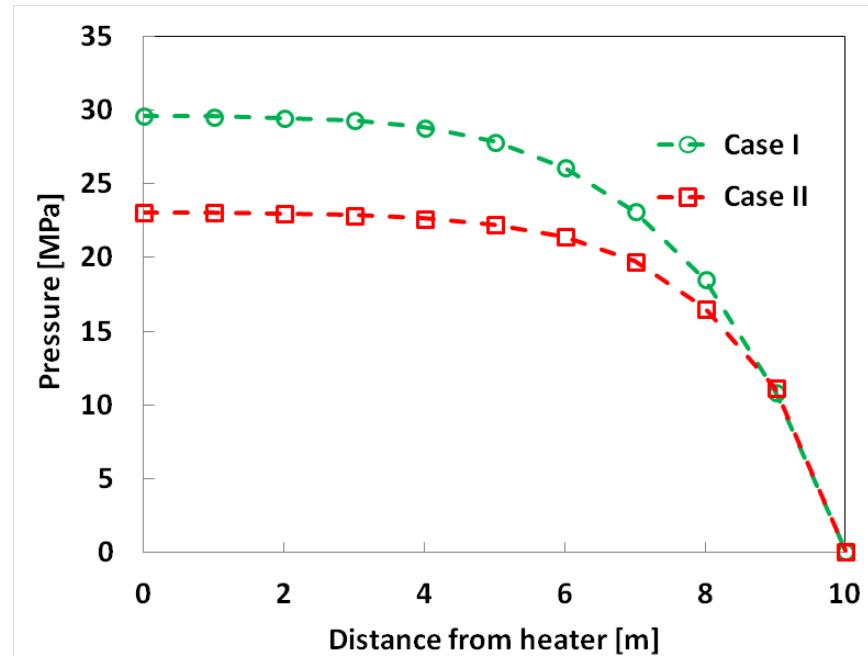
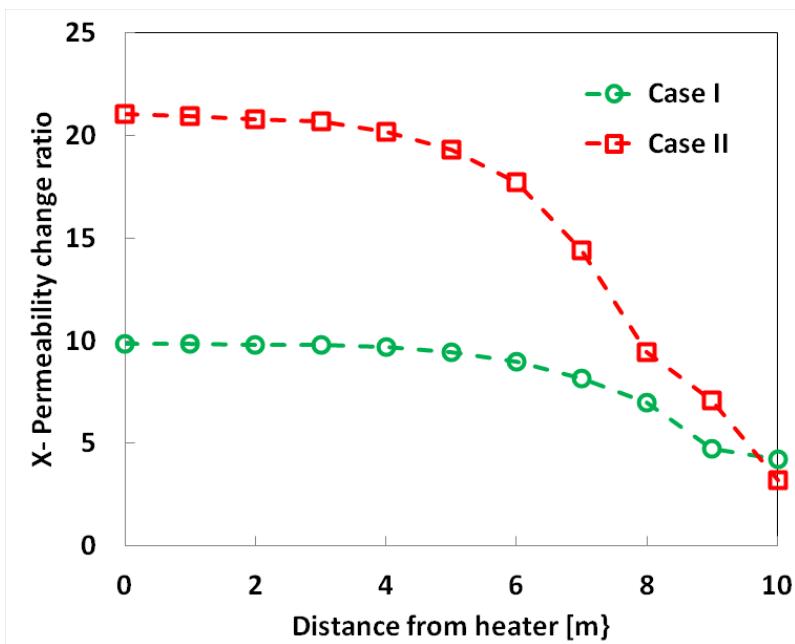


# FEHM's new THMC modeling capabilities go beyond contemporary commercial simulators

## Directional permeability-stress dependence

Case (i):  $K_i = f(\max_{j \neq i}(\sigma_{jj}))$

Case (ii):  $K = f(\sigma_{mean})$



**Impacts pressure and hence recovery**

# Implicit coupling of permeability change

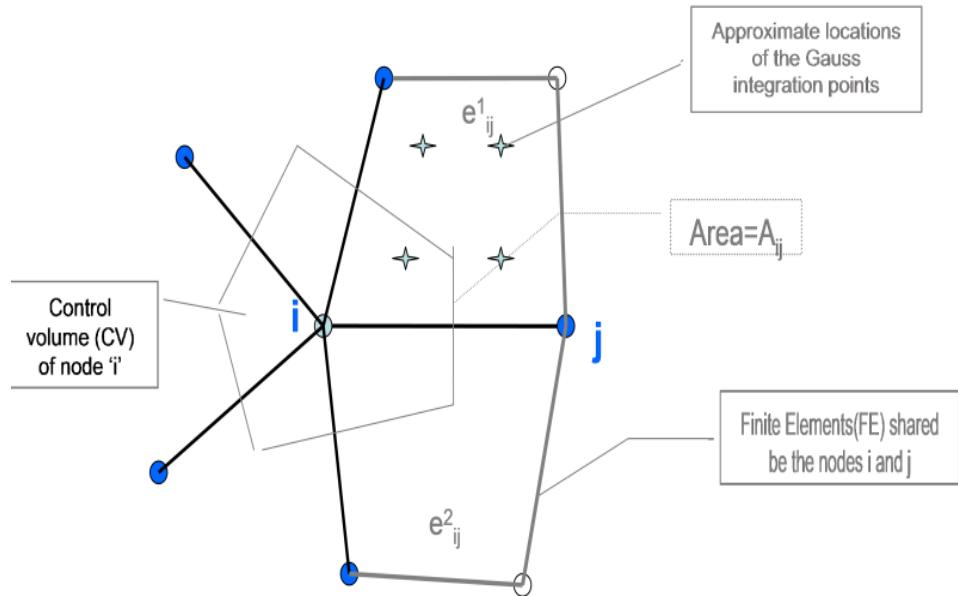
Derivative of the mass flux between two connected nodes **i** and **j** wrt a node **k** connected to one of them:

$$\frac{\partial q^{ij}}{\partial \bar{u}_k} = K^{ij} \cdot \frac{\rho}{\mu} \cdot (A_{ij} / l_{ij}) \cdot (P_j - P_i) * \frac{\partial pF^{ij}}{\partial \bar{u}_k}$$

$$\frac{\partial pF^{ij}}{\partial \bar{u}_k} = \frac{1}{N_{ij-e}} \sum_{elements-ij} \frac{\partial pF^{ij-e}}{\partial \bar{\sigma}_e} \cdot \frac{\partial \bar{\sigma}_e}{\partial \bar{u}_k}$$

$$\frac{\partial \bar{\sigma}_e}{\partial \bar{u}_k} = \frac{1}{Ve} \sum_{gp} |J| \bar{D} \cdot \bar{B} \cdot \bar{I}$$

$pF^{ij-e}$  is an effective permeability factor representing stress/deformation effects



NOTE: In FEHM, properties are input at nodes and assigned to the CV. properties on FE are obtained by using appropriate averages/interpolations

# New THMC modeling capabilities in FEHM enable comprehensive modeling of *in situ* conversion processes

- New thermal-hydrological-mechanical-chemical (THMC) capabilities have been developed in FEHM to numerically simulate *in situ* conversion processes
- Some THMC modeling capabilities extensively benchmarked against CMG's STARS and Abaqus
- FEHM's new THMC modeling capabilities go beyond commercial simulators. These capabilities are critical for effectively modeling the *in situ* conversion processes
- Models to effectively capture change in permeability due to stress change are needed in continuum-scale formulations
- We are currently developing capabilities to implicitly simulate change in permeability due to stress change
  - Multi-phase formulation
  - Plastic deformation

# Acknowledgements

- This work was partially funded by a Co-operative Research & Development Agreement (CRADA) between ExxonMobil and LANL.
- The capabilities for simulation of geomechanical processes have been developed through the Zero Emission Research & Technology (ZERT-II) project under DOE's Carbon Sequestration Program.
- The application to geothermal field test was funded through US DOE's Geothermal Technologies Program

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# Background Slides

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# Parameter values

PARAMETER	VALUE
Formation temperature	190 <sup>0</sup> C
Initial pore pressure	9 MPa
Bottom hole injection pressure	13.1 MPa
Injection temperature	170 <sup>0</sup> C
Principal in situ stresses	
Maximum	22.6 MPa (vertical)
Intermediate	18.1 MPa
Minimum	13.8 MPa
Thermal conductivity	3 W/m/K
Heat capacity	820 J/kg/K
Porosity	10%
Initial permeability*thickness	9 md.m
Shear failure-permeability model parameters	
Friction Coefficient	0.8
Cohesion	2 MPa
Permeability multiplier (all directions)	100
Young's modulus	30 GPa
Poisson' ratio	0.15
Coeffficient of Thermal Expansion	10 <sup>-4</sup> / <sup>0</sup> C
Biot poroelastic parameter	0.5

# Example of application to non-Orthogonal grid: Inclined, weak fault

