

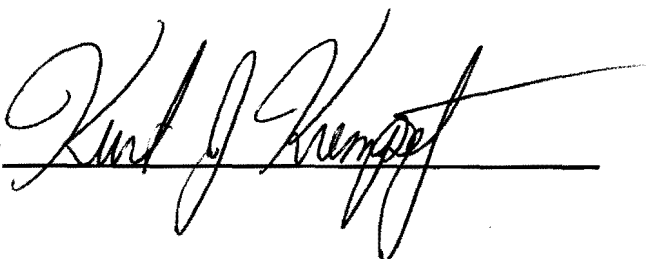
# Cryostat Filling Limitations for Proposed Ar Dewar Pressure Increase

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Checked by

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## **Cryostat Filling Limitations for Proposed Ar Dewar Pressure Increase**

In order to significantly decrease the amount of time required to fill the cryostats, it is desired to raise the setpoint of the "operating" relief valve on the argon storage dewar to 20 psig from its existing 16 psig setting. This additional pressure increases the flow to the cryostats and will overwhelm the relief capacity if the temperature of the modules within these vessels is warm enough. Using some conservative assumptions and simple calculations within this note, the maximum average temperature that the modules within each cryostat can be at prior to filling from the storage dewar with liquid argon is at least 290 K.

### **Some Assumptions Used in the Analysis**

1. Pressure in the argon storage dewar is at 20 psig.
2. The flow to the ECN cryostat is the most hazardous due to greater limitations on venting (see attached calculations).
3. The maximum flow of argon to the cryostat is 12.3 gpm (see attached calculations).
4. Gaseous nitrogen is concurrently flowing in the vent piping at a rate of 4861 lb/hr, this is derived from both ECS and CC cooling at their maximum rate and ECN condenser attempting to maintain pressure at its maximum.
5. Mixture mass flows are at the maximum at junction of relief devices on ECN( $\text{gN}_2$  mass flow actually increases gradually at junctions toward the ECS).
6. The temperature increase in the vent piping is negligible (large majority of piping is insulated).
7. All flows are treated as incompressible fluids (max. Mach No. = 0.2).

8. Temperature of the gaseous nitrogen prior to mixing in the vent manifold is 84 K, saturated property at 2 atm.
9. Flow equations apply to weight-averaged mixture densities and viscosities.
10. All liquid argon flashes to the bulk module temperature in the cryostat prior to entering the piping.

### **Explanation of Methodology**

The basic purpose of the spreadsheet was to provide a complete model so that the maximum bulk temperature of the modules (line 2) could be determined. The maximum flow of argon to the ECN (line 3) was calculated separately and included after the spreadsheet. A number was picked as a guess for the bulk temperature (line 2). Then a number was picked as a guess for the percent of mass flow to the relief valve (line 18). The actual flow through the relief valve (line 98) was determined using the total flow and the percent of flow to the relief valve. The pressure drops across the inlet and outlets of the relief devices were then calculated. This allowed the calculation of the pressure drops across the relief valve and rupture disk. The various properties of argon were taken from tables at the bulk temperature of the modules.

The section " $\Delta P$  Across Relief Valve" calculated the maximum theoretical flow of argon through the relief valve (line 108). Then the theoretical percent of relief flow (line 109) was calculated based on the theoretical relief valve flow divided by the total flow through both the relief valve and rupture disk. The number guessed for the percent of flow to the relief valve (line 18) was then adjusted by iteration until it was close to, but not greater than, the theoretical value (line 109). At this point, the relief valve was operating near its full capacity, which could be checked by noting that the actual flow (line 98) was close to the maximum theoretical flow (line 108).

The next step was to examine the section " $\Delta P$  Across Rupture Disk". All of the total argon flow not going through the relief valve would be flowing through the rupture disk. In order to insure that the rupture disk could handle the flow, the maximum theoretical rupture disk flow (line 181) was calculated, and compared to the actual flow (line 182). The actual flow had to be under the maximum theoretical flow, but should be close to the maximum value to obtain the highest total flow. In the case that the actual flow was calculated to be higher than the maximum theoretical flow, the bulk temperature was lowered. Using the new temperature, the first set of iterations was repeated to determine the percent of flow to the relief valve, and the rupture disk flow was compared again. The temperature was lowered through iteration until an acceptable value was found.

Note that the sections on pressure drops were only needed to calculate inlet and outlet pressures for the relief valve and rupture disk. Other sections calculated the changes in various properties of the argon at certain points. Each time the temperature was changed, the values for density and viscosity were changed to reflect the new temperature. The maximum flow of nitrogen from the condensers was also accounted for, since it had an effect on the pressure drops of the outlets of the relief devices.

### Notes on Maximum Module Temperature Calculation

\*> means that this value is to be re-entered each time the bulk module temperature is changed.

> means that this value is a number, not a formula, but should only be entered once, i.e., it doesn't need to change with the temperature.

(conv.) means that this value is the same as a previous value, but converted to different units.

EN-263, Russ Rucinski, should be referred to for pressure drop calculations.

### General Procedure:

In the first section, "Conversion of Liquid to Gas at Module Temp.," enter the bulk temperature of the modules. This is also the temperature that will be used for pressure drops in the relief and rupture disk inlets, and for the relief devices themselves. Enter the gas density at 2.2 bars and 2.4 bars, and at the bulk temperature, so that the density at the cryostat pressure can be calculated. Enter some percent of mass flow to the relief valve. This will be used to assume some mass flow to each relief device for pressure drop calculations. It will be adjusted by iteration later.

In the next section, " $\Delta P$  Across Relief Valve Inlet," enter the viscosity at 2.4 bars (or 2.375 bars for more accuracy) and the bulk temperature. The rest of the section is calculated.

The next section, " $\Delta P$  Across Rupture Disk Inlet," needs no entries, since it assumes the same gas properties as the previous section.

The section, " $\Delta P$  Across Relief Valve Outlet" requires the gas density, and the viscosity at an verge pressure of 2 bars and at the bulk temperature. This just accounts for the drop in pressure to about 1.5 bars. If more accuracy is required, the new pressure could be calculated by adding the common outlet pressure drops to atmospheric pressure.

The " $\Delta P$  Across Rupture Disk Outlet" section is completely calculated, based on the assumption that the gas properties remain the same as for the relief valve outlet.

The next section, "Change in Gas at Common Outlet to Outside" reflects the change in properties of the fluid at the junction of the relief device outlets due to the mixing of argon from the relief devices and nitrogen from the condensers.

The " $\Delta P$  Across Relief Valve" is completely calculated (ref.1, 3). The specific heat ratio,  $k$ , has been determined using the  $C_p$  and  $C_v$  at the correct temperature and pressure. Also, the flowing temperature is converted from the original bulk temperature, to the equivalent Rankine

temperature. The basic purpose of this section is to compare the "Theoretical Percent of Relief Flow" to the actual percent that was entered in section 1. Since the theoretical percent of the relief flow is the maximum flow possible at the given inlet and outlet parameters, this number should be checked such that it does not fall below the "guessed" percentage in the first section of calculations.

The " $\Delta P$  Across Common Outlet to Platform" is calculated based on the properties from the "Change in Gas..." section. Also, all pressure drop calculations are based on a equation which relates the friction factor,  $f$ , to the Reynolds number and the relative roughness,  $e/D$ . The "Friction Factor Guess" is based on an equation in Introduction to Fluid Mechanics (ref.1) and that value is used in another equation in the same reference to find the actual friction factor. Calculations to determine equivalent lengths and relative roughness were based on dimensions from sketches and drawings of the ECN piping and platform manifold.

The section on the " $\Delta P$  from Platform Bayonet to Outside" is completely calculated like the previous section, but with a different diameter and equivalent length.

The "Summation of Equivalent  $\Delta P$ s" is basically a summary of the pressure drops, where the "Rupture Disk Pressure Drop" is calculated based on the three relief valve values, and the rupture disk inlet and outlet values.

The " $\Delta P$  Across Rupture Disk Device" is calculated like the relief valve. The complete equation for the "Gas Flow Constant for Subsonic Flow ( $C_1$ )" is found in reference 2. The specific heat ratio,  $k$ , was adjusted according to the actual pressure and temperature. In both the relief valve and the rupture disk, the outlet pressure should be compared to the critical pressure, which it must exceed for the flow to be subsonic. In all cases analyzed, the flow was subsonic.

## Conclusions and Recommendations

The average temperature of the module mass for any of the three cryostats can be as high as 290 K prior to filling that particular cryostat. This should not be confused with the average temperature of a single type or location which is useful in protecting the modules-not necessarily the vessel itself. A few modules of each type and at different elevations should be used in an average which would account for the different weights of each module. Note that at 290 K, the actual flow of argon through the relief valve and the rupture disk was under the maximum theoretical flows for each relief device. This means that the bulk temperature could actually have been raised to flow argon through the reliefs at their maximum capacity. Therefore, the temperature of 290 K is a conservative value for the calculated flow rate of 12.3 gpm.

Safeguards in addition to and used in conjunction with operating procedures shall be implemented in such a way so that the above temperature limitation is not exceeded and such that it is exclusive of the programmable logic controller (PLC). One suggestion is using a toggle switch for each cryostat mounted in the PLC I/O box which would maintain control of the signals to open the cold fill valves of each cryostat.

With the safeguards in place while carefully monitoring the temperatures during a cooldown cycle in each cryostat, the set pressure in the argon storage dewar can safely be increased to 20 psig.

**References**

1. Introduction to Fluid Mechanics, 3rd Ed., Robert W. Fox, Alan T. McDonald, John Wiley & Sons, 1985.
2. "Fike Technical Bulletin TB 8102, Rupture Disk Sizing", Fike Metal Products Corp.
3. "Catalog 1900-Series 90 Safety Relief Valves", Anderson, Greenwood & Co., 1980.
4. "DØ CC Pressure Vessel and Vacuum Vessel Safety Note", DØ Engineering Note #3740-EN-263, R. Rucinski/R. Luther, Nov., 1990.



# Maximum Module Temperature Calculation 10/17/91

|    | A   | B  | C         | D          |
|----|---|--|-----------|------------|
| 1  | Conversion of Liquid to Gas at Module Temp. |  |           | Units      |
| 2  | *> Bulk Temp. of Modules                    | 290  | 290       | K          |
| 3  | > Max. Flow of Liquid Argon to Cryostat     | 12.3   | 12.3      | gpm        |
| 4  | > Pressure in Cryostat                      | 19.75  | 19.75     | psig       |
| 5  | Pressure in Cryostat (conv.)                | $=(B4/14.696+1)*1.01325$                             | 2.375     | bars       |
| 6  | > lAr Density @ 2.2 bars                    | 1.342421   | 1.34      | g/cc       |
| 7  | > lAr Density @ 2.4 bars                    | 1.335861   | 1.34      | g/cc       |
| 8  | lAr Density @ 2.375 bars                    | $=(B5-2.2)/0.2*(B7-B6)+B6$                           | 1.337     | g/cc       |
| 9  | *> gAr Density @ 2.2 bars                   | 3.655  | 3.655     | mg/cc      |
| 10 | *> gAr Density @ 2.4 bars                   | 3.987  | 3.987     | mg/cc      |
| 11 | gAr Density @ 2.375 & Temp.                 | $=(B5-2.2)/0.2*(B10-B9)+B9$                          | 3.945     | mg/cc      |
| 12 | gAr Density @ 2.375 bars (conv.)            | $=B11/1000*62.428$                                   | 0.246     | lbm/ft^3   |
| 13 | Maximum Flow of Argon Gas                   | $=B3*B8/B11*1000$                                    | 4167      | gpm        |
| 14 | Maximum Flow of Argon Gas (conv.)           | $=B13*0.13368$                                       | 557       | cfm        |
| 15 | Air Equivalent Flow @STP                    | $=6.32*B17*356/B16*SQRT(B99/(520*B177*28.97))$       | 1443      | scfm air   |
| 16 | Specific Heat Constant, C, for Ar           | $=520*SQRT(B168*(2/(B168+1))^{((B168+1)/(B168-1)))}$ | 378       |            |
| 17 | Max. Mass Flow of Argon Gas                 | $=B14*B12*60$  | 8232      | lbm/hr     |
| 18 | *> Percent of Mass Flow to Relief Valve     | 0.48   | 0.48      |            |
| 19 |   |  |           |            |
| 20 | ΔP Across Relief Valve Inlet                |  |           | Units      |
| 21 | > Inner Pipe Diameter                       | 0.206  | 0.206     | ft         |
| 22 | Inner Pipe Diameter (conv.)                 | $=B21*12$  | 2.472     | in         |
| 23 | > Equivalent Length                         | 38   | 38        | ft         |
| 24 | Ar Gas Density @ 2.375 & Temp.              | $=(B5-2.2)/0.2*(B10-B9)+B9$                          | 3.945     | mg/cc      |
| 25 | Ar Gas Density @ 2.375 bars (conv.)         | $=B24/1000*62.428$                                   | 0.246     | lbm/ft^3   |
| 26 | *> gAr Viscosity @ 2.4 bars & Temp.         | 0.0002228  | 0.0002228 | g/cm-s     |
| 27 | gAr Viscosity @ 2.4 bars (conv.)            | $=B26*100$   | 0.02228   | centipoise |
| 28 | Max. Mass Flow to Relief Valve              | $=B17*B18$   | 3952      | lbm/hr     |
| 29 | Reynolds Number                             | $=6.31*B28/(B22*B27)$                                | 453000    |            |
| 30 | > Relative Roughness (e/D)                  | 0.0007   | 0.0007    |            |
| 31 | Friction Factor Guess                       | $=0.25*(LOG(B30/3.7+5.74/(B29^0.9)))^{-2}$           | 0.019     |            |
| 32 | Friction Factor                             | $=0.25*(LOG(B30/3.7+2.51/(B29*B31^0.5)))^{-2}$       | 0.0189    |            |
| 33 | Pressure Drop                               | $=0.00000336*B32*B23*(B28^2)/B25/(B22^5)$            | 1.655     | psi        |
| 34 |   |  |           |            |

# Maximum Module Temperature Calculation 10/17/91

|    | A                                  | B  | C         | D          |
|----|------------------------------------|--|-----------|------------|
| 35 | ΔP Across Rupture Disk Inlet       |  |           | Units      |
| 36 | Inner Pipe Diameter (conv.)        | =B37/12                                    | 0.172     | ft         |
| 37 | > Inner Pipe Diameter              | 2.067                                      | 2.067     | in         |
| 38 | > Equivalent Length                | 49   | 49        | ft         |
| 39 | gAr Density @ 2.375 & Temp.        | =(B5-2.2)/0.2*(B10-B9)+B9                  | 3.945     | mg/cc      |
| 40 | gAr Density @ 2.375 bars (conv.)   | =B39/1000*62.428                           | 0.246     | lbm/ft^3   |
| 41 | gAr Viscosity @ 2.4 bars           | =B26                                       | 0.0002228 | g/cm-s     |
| 42 | gAr Viscosity @ 2.4 bars (conv.)   | =B41*100                                   | 0.02228   | centipoise |
| 43 | Max. Mass Flow to Rupture Disk     | =B17*(1-B18)                               | 4281      | lbm/hr     |
| 44 | Reynolds Number                    | =6.31*B43/(B37*B42)                        | 587000    |            |
| 45 | > Relative Roughness (e/D)         | 0.0009                                     | 0.0009    |            |
| 46 | Friction Factor Guess              | =0.25*(LOG(B45/3.7+5.74/(B44^0.9)))^-2     | 0.0198    |            |
| 47 | Friction Factor                    | =0.25*(LOG(B45/3.7+2.51/(B44*B46^0.5)))^-2 | 0.0197    |            |
| 48 | Pressure Drop                      | =0.00000336*B47*B38*(B43^2)/B40/(B37^5)    | 6.394     | psi        |
| 51 |                                    |  |           |            |
| 52 | ΔP Across Relief Valve Outlet      |  |           | Units      |
| 53 | Inner Pipe Diameter (conv.)        | =B54/12                                    | 0.272     | ft         |
| 54 | > Inner Pipe Diameter              | 3.26                                       | 3.26      | in         |
| 55 | > Equivalent Length                | 51   | 51        | ft         |
| 56 | *> gAr Density @ 2.0 bar & Temp.   | 3.324                                      | 3.324     | mg/cc      |
| 57 | gAr Density @ 2.0 bar (conv.)      | =B56/1000*62.428                           | 0.208     | lbm/ft^3   |
| 58 | *> gAr Viscosity @ 2.0 bar & Temp. | 0.0002227                                  | 0.0002227 | g/cm-s     |
| 59 | gAr Viscosity @ 2.0 bar (conv.)    | =B58*100                                   | 0.02227   | centipoise |
| 60 | Max. Mass Flow to Relief Valve     | =B28                                       | 3952      | lbm/hr     |
| 61 | Reynolds Number                    | =6.31*B60/(B54*B59)                        | 343000    |            |
| 62 | > Relative Roughness (e/D)         | 0.00055                                    | 0.00055   |            |
| 63 | Friction Factor Guess              | =0.25*(LOG(B62/3.7+5.74/(B61^0.9)))^-2     | 0.0185    |            |
| 64 | Friction Factor                    | =0.25*(LOG(B62/3.7+2.51/(B61*B63^0.5)))^-2 | 0.0183    |            |
| 65 | Pressure Drop                      | =0.00000336*B64*B55*(B60^2)/B57/(B54^5)    | 0.642     | psi        |
| 66 |                                    |  |           |            |

# Maximum Module Temperature Calculation 10/17/91

|    | A   | B   | C         | D          |
|----|---|---|-----------|------------|
| 67 | ΔP Across Rupture Disk Outlet             |   |           | Units      |
| 68 | Inner Pipe Diameter (conv.)               | =B69/12                                   | 0.18      | ft         |
| 69 | > Inner Pipe Diameter                     | 2.157                                     | 2.157     | in         |
| 70 | > Equivalent Length                       | 1.75                                      | 1.75      | ft         |
| 71 | gAr Density @ 2.0 bar & Temp.             | =B56                                      | 3.324     | mg/cc      |
| 72 | gAr Density @ 2.0 bar (conv.)             | =B71/1000*62.428                          | 0.208     | lbm/ft^3   |
| 73 | gAr Viscosity @ 2.0 bar & Temp.           | =B58                                      | 0.0002227 | g/cm-s     |
| 74 | gAr Viscosity @ 2.0 bar (conv.)           | =B73*100                                  | 0.02227   | centipoise |
| 75 | Max. Mass Flow to Rupture Disk            | =B43                                      | 4281      | lbm/hr     |
| 76 | Reynolds Number                           | =6.31*B75/(B69*B74)                       | 562000    |            |
| 77 | > Relative Roughness (e/D)                | 0.0009                                    | 0.0009    |            |
| 78 | Friction Factor Guess                     | =0.25*(LOG(B77/3.7+5.74/(B76^0.9)))^2     | 0.0198    |            |
| 79 | Friction Factor                           | =0.25*(LOG(B77/3.7+2.51/(B76*B78^0.5)))^2 | 0.0197    |            |
| 80 | Pressure Drop                             | =0.00000336*B79*B70*(B75^2)/B72/(B69^5)   | 0.219     | psi        |
| 81 |   |   |           |            |
| 82 | Change in Gas at Common Outlet to Outside |   |           | Units      |
| 83 | Pressure in Cryostat                      | =B4                                       | 19.75     | psig       |
| 84 | Pressure in Cryostat (conv.)              | =(B83/14.696+1)*1.01325                   | 2.375     | bars       |
| 85 | gAr Density @ 2.2 bars                    | =B9                                       | 3.655     | mg/cc      |
| 86 | gAr Density @ 2.4 bars                    | =B10                                      | 3.987     | mg/cc      |
| 87 | gAr Density @ 2.375 & Temp.               | =(B84-2.2)/0.2*(B86-B85)+B85              | 3.945     | mg/cc      |
| 88 | Temp. at Common Outlet                    | =(B2*B17+84*B189)/(B17+B189)              | 214       | K          |
| 89 | > Pressure to Calculate Density           | 1.5                                       | 1.5       | bars       |
| 90 | *> gAr Density @ 1.5 bars & New Temp.     | 3.396                                     | 3.396     | mg/cc      |
| 91 | *> gAr Viscosity @ 1.5 bars & New Temp.   | 0.0001696                                 | 0.0001696 | g/cm-s     |
| 92 | gAr Viscosity @ 1.5 bar (conv.)           | =B91*100                                  | 0.01696   | centipoise |
| 93 |   |   |           |            |

**Maximum Module Temperature Calculation 10/17/91**

|     | A   | B   | C      | D               |
|-----|---|---|--------|-----------------|
| 94  | $\Delta P$ Across Relief Valve              |   |        | Units           |
| 95  | > Critical Ratio ( $P_{cr}/P_1$ ) for Argon | 0.487   | 0.487  |                 |
| 96  | > Specific Heat Ratio (k) for Argon         | =B168   | 1.67   |                 |
| 97  | > Area of 2" x 3" Relief Valve              | 2.29  | 2.29   | in <sup>2</sup> |
| 98  | Flow Through Relief Valve                   | =B28  | 3952   | lbm/hr          |
| 99  | Flowing Temperature                         | =1.8*B2   | 522    | deg R           |
| 100 | > Compressibility Factor                    | 1   | 1      |                 |
| 101 | > Nozzle Coefficient for type 93T           | 0.939   | 0.939  |                 |
| 102 | Flowing Inlet Pressure (P1)                 | =B4+14.696-B33  | 32.79  | psia            |
| 103 | > Molecular Weight of Argon                 | 39.948  | 39.95  | g/mol           |
| 104 | Critical Pressure ( $P_{cr}$ )              | =B95*B102   | 15.97  | psia            |
| 105 | Outlet Pressure (P2) (using delta p's)      | =14.696+B154+B133+B65                                     | 27.39  | psia            |
| 106 | Pressure Ratio ( $P_2^*/P_1$ )              | =(B102-0.55*((B102-B105)^0.98))/B102                      | 0.912  |                 |
| 107 | Theoretical Factor (F*) (using P2)          | =SQRT(((B96/(B96-1))^*(B106^(2/B96)-B106^((B96+1)/B96)))) | 0.284  |                 |
| 108 | Max. Theoretical Relief Flow (using F*)     | =735*B97*B101*B102*B107*SQRT(B103/B99/B100)               | 4072   | lbm/hr          |
| 109 | Theoretical Percent of Relief Flow          | =B108/B17   | 0.4947 |                 |
| 110 | Pressure Drop Across Relief Valve           | =B102-B105  | 5.403  | psi             |
| 111 |   |   |        |                 |

**Maximum Module Temperature Calculation 10/17/91**

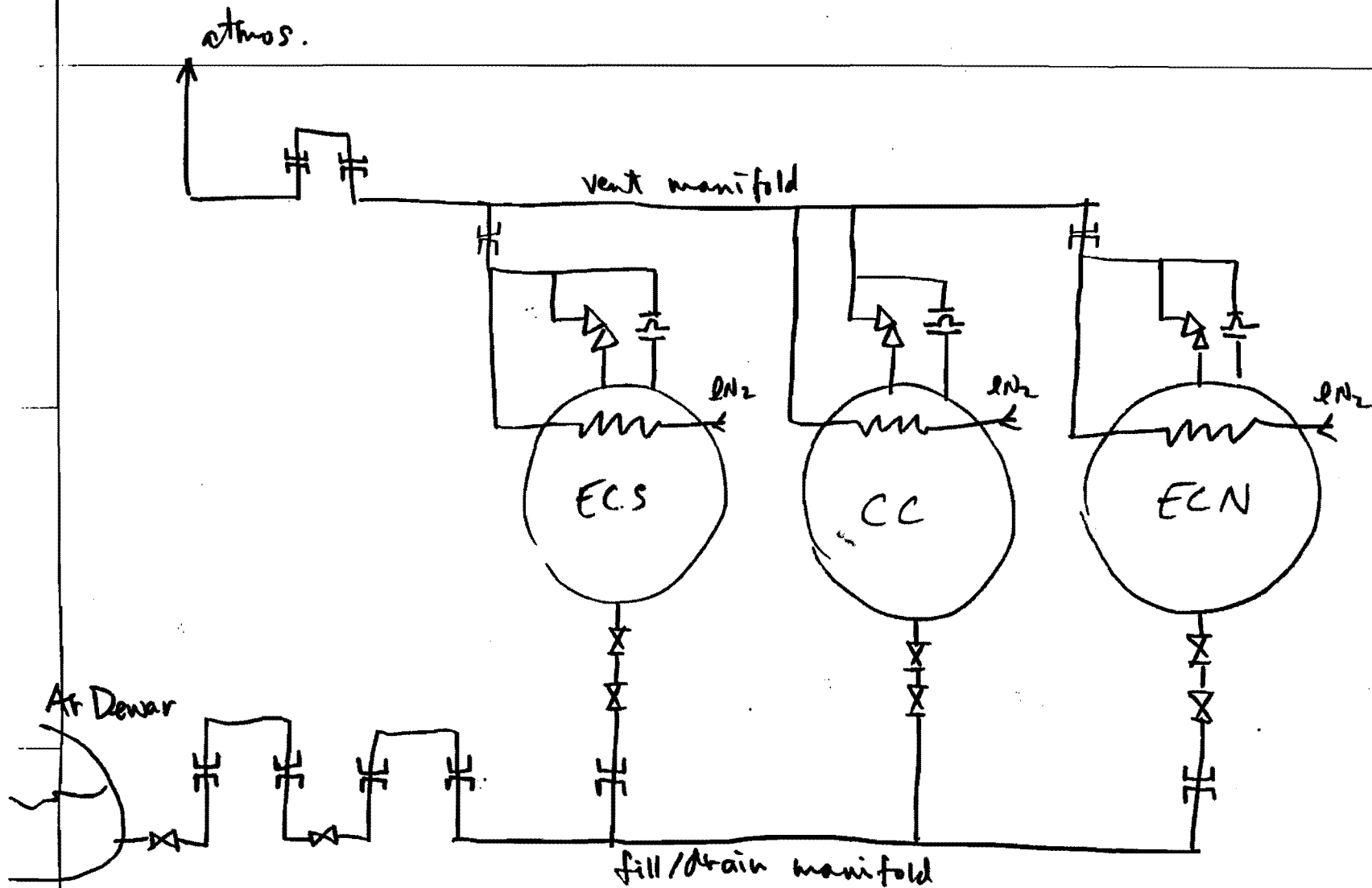
|     | A   | B   | C         | D          |
|-----|---|---|-----------|------------|
| 112 | ΔP Across Common Outlet to Platform Bayonet |   |           | Units      |
| 113 | > Inner Pipe Diameter                       | 0.355   | 0.355     | ft         |
| 114 | Inner Pipe Diameter (conv.)                 | =B113*12  | 4.26      | in         |
| 115 | > Equivalent Length                         | 273   | 273       | ft         |
| 116 | gAr Density @ 1.5 bar & New Temp.           | =B90  | 3.396     | mg/cc      |
| 117 | gAr Density @ 1.5 bar (conv.)               | =B116/1000*62.428                               | 0.212     | lbm/ft^3   |
| 118 | *> gN2 Gas Density @ 1.5 bar & New Temp.    | 2.411028  | 2.411     | mg/cc      |
| 119 | gN2 Gas Density @ 1.5 bar (conv.)           | =B118/1000*62.428                               | 0.151     | lbm/ft^3   |
| 120 | Gas Mixture Density @1.5 bar                | =(B17*B117+B127*B119)/B128                      | 0.189     | lbm/ft^3   |
| 121 | gAr Viscosity @ 1.5 bar & New Temp.         | =B91  | 0.0001696 | g/cm-s     |
| 122 | gAr Viscosity @ 1.5 bar (conv.)             | =B121*100                                       | 0.01696   | centipoise |
| 123 | *> gN2 Viscosity @ 1.5 bar & New Temp.      | 0.000136454                                     | 0.0001365 | g/cm-s     |
| 124 | gN2 Viscosity @ 1.5 bar (conv.)             | =B123*100                                       | 0.01365   | centipoise |
| 125 | Mixture Viscosity @1.5 bar                  | =(B17*B122+B127*B124)/B128                      | 0.01573   | centipoise |
| 126 | Max. Mass Flow of Argon Gas                 | =B17  | 8232      | lbm/hr     |
| 127 | Max. Flow of Nitrogen Gas                   | =B189   | 4861      | lbm/hr     |
| 128 | Mass Flow of Mixture                        | =B126+B127                                      | 13093     | lbm/hr     |
| 129 | Reynolds Number                             | =6.31*B128/(B114*B125)                          | 1230000   |            |
| 130 | > Relative Roughness (e/D)                  | 0.0004  | 0.0004    |            |
| 131 | Friction Factor Guess                       | =0.25*(LOG(B130/3.7+5.74/(B129^0.9)))^(-2)      | 0.0165    |            |
| 132 | Friction Factor                             | =0.25*(LOG(B130/3.7+2.51/(B129*B131^0.5)))^(-2) | 0.0164    |            |
| 133 | Pressure Drop                               | =0.00000336*B132*B115*(B128^2)/B120/(B114^5)    | 9.705     | psi        |
| 134 |   |   |           |            |

# Maximum Module Temperature Calculation 10/17/91

|     | A                                     | B   | C         | D          |
|-----|---------------------------------------|---|-----------|------------|
| 135 | ΔP from Platform Bayonet to Outside   |   |           | Units      |
| 136 | > Inner Pipe Diameter                 | 0.53  | 0.53      | ft         |
| 137 | Inner Pipe Diameter (conv.)           | =B136*12                                      | 6.36      | in         |
| 138 | > Equivalent Length                   | 516   | 516       | ft         |
| 139 | gAr Gas Density @ 1.5 bar & New Temp. | =B90  | 3.396     | mg/cc      |
| 140 | gAr Gas Density @ 1.5 bar (conv.)     | =B139/1000*62.428                             | 0.212     | lbm/ft^3   |
| 141 | gN2 Gas Density @ 1.5 bar & New Temp. | =B118   | 2.411     | mg/cc      |
| 142 | gN2 Gas Density @ 1.5 bar (conv.)     | =B141/1000*62.428                             | 0.151     | lbm/ft^3   |
| 143 | Gas Mixture Density @1.5 bar          | =(B17*B140+B189*B142)/B149                    | 0.189     | lbm/ft^3   |
| 144 | gAr Viscosity @ 1.5 bar & New Temp.   | =B121   | 0.0001696 | g/cm-s     |
| 145 | gAr Viscosity @ 1.5 bar (conv.)       | =B144*100                                     | 0.01696   | centipoise |
| 146 | gN2 Viscosity @ 1.5 bar & New Temp.   | =B123   | 0.0001365 | g/cm-s     |
| 147 | gN2 Viscosity @ 1.5 bar (conv.)       | =B146*100                                     | 0.01365   | centipoise |
| 148 | Gas Mixture Viscosity @1.5 bar        | =(B17*B145+B189*B147)/B149                    | 0.01573   | centipoise |
| 149 | Max. Mass Flow of Gas Mixture         | =B128   | 13093     | lbm/hr     |
| 150 | Reynolds Number                       | =6.31*B149/(B137*B148)                        | 826000    |            |
| 151 | > Relative Roughness (e/D)            | 0.00027                                       | 0.00027   |            |
| 152 | Friction Factor Guess                 | =0.25*(LOG(B151/3.7+5.74/(B150^0.9)))^-2      | 0.0156    |            |
| 153 | Friction Factor                       | =0.25*(LOG(B151/3.7+2.51/(B150*B152^0.5)))^-2 | 0.0155    |            |
| 154 | Pressure Drop                         | =0.00000336*B153*B138*(B149^2)/B143/(B137^5)  | 2.345     | psi        |
| 155 |                                       |   |           |            |
| 156 | Summation of Equivalent ΔPs           |   |           | Units      |
| 157 | Relief Valve Inlet Pressure Drop      | =B33  | 1.655     | psi        |
| 158 | Relief Valve Outlet Pressure Drop     | =B65  | 0.642     | psi        |
| 159 | Relief Valve Pressure Drop            | =B110   | 5.403     | psi        |
| 160 | Relief Valve/Disk Branch              | =B33+B65+B110                                 | 7.7       | psi        |
| 161 | Rupture Disk Inlet Pressure Drop      | =B48  | 6.394     | psi        |
| 162 | Rupture Disk Outlet Pressure Drop     | =B80  | 0.219     | psi        |
| 163 | Rupture Disk Pressure Drop            | =B157+B158+B159-B161-B162                     | 1.087     | psi        |
| 164 | Common Outlet Pressure Drop           | =B133   | 9.705     | psi        |
| 165 | Platform to Outside Pressure Drop     | =B154   | 2.345     | psi        |
| 166 |                                       |   |           |            |

**Maximum Module Temperature Calculation 10/17/91**

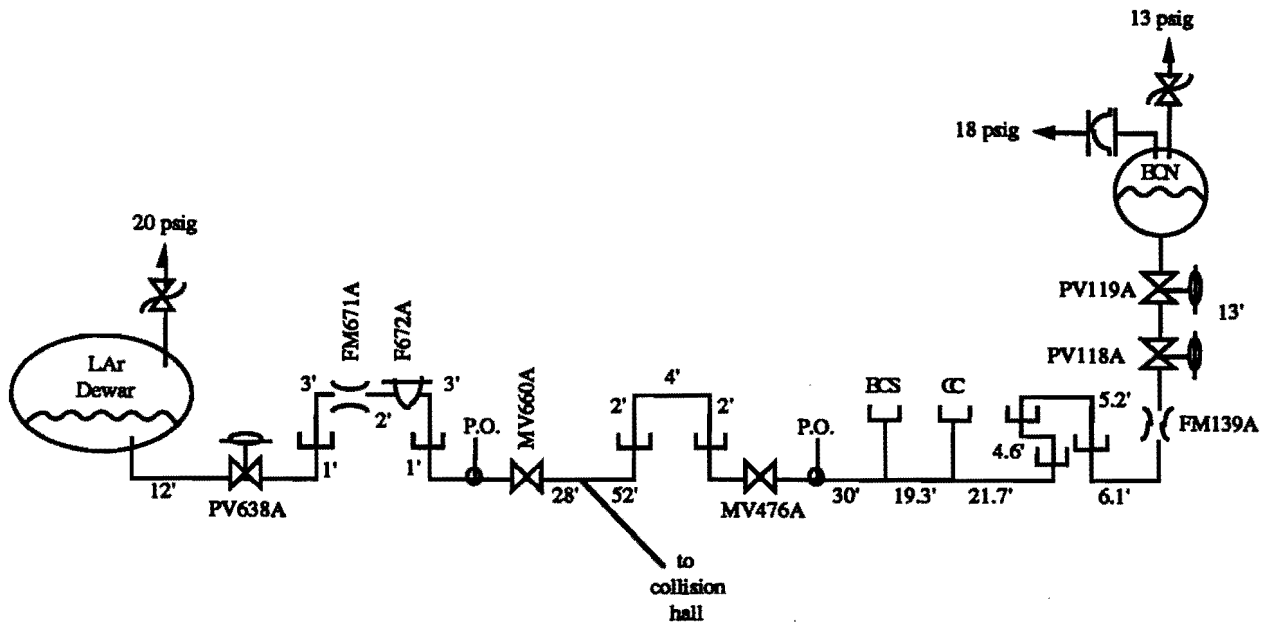
|     | A                                       | B  | C       | D        |
|-----|---|--|---------|----------|
| 167 | $\Delta P$ Across Rupture Disk          |  |         | Units    |
| 168 | > Argon Specific Heat Ratio (k)         | 1.673  | 1.673   |          |
| 169 | Critical Ratio                          | $=(2/(B168+1))^{(B168/(B168-1))}$                                      | 0.486   |          |
| 170 | > Area of 3" Rupture Disk               | $=3.14159*(3^2)/4$   | 7.069   | in^2     |
| 171 | Flow Through Rupture Disk               | =B43   | 4281    | lbm/hr   |
| 172 | Flowing Temperature                     | =1.8*B2  | 522     | deg R    |
| 173 | > ASME Coefficient (K)                  | 0.62   | 0.62    |          |
| 174 | Pressure Ratio (Pe/Po)                  | =B179/B176   | 0.961   |          |
| 175 | gAr Flow Constant for Subsonic Flow(C1) | $=SQRT(2*32.2/1545*(B168/(B168-1))*(B174^{(2/B168)}-B174^{(1/B168)}))$ | 0.039   |          |
| 176 | Flowing Inlet Pressure (Po)             | =B4+14.696-B48   | 28.05   | psia     |
| 177 | > Molecular Weight of Argon             | 39.948   | 39.948  | g/mol    |
| 178 | Critical Pressure (Pcr)                 | =B169*B176   | 13.64   | psia     |
| 179 | Outlet Pressure (Pe) (using delta p's)  | =14.696+B154+B133+B80  | 26.97   | psia     |
| 180 | Pressure Drop Across Rupture Disk       | =B176-B179   | 1.087   | psi      |
| 181 | Maximum Theoretical Rupture Disk Flow   | =B170*B173*B175*B176*SQRT(B177/B172)*60*60                             | 4833    | lbm/hr   |
| 182 | Actual Rupture Disk Flow                | =B43   | 4281    | lbm/hr   |
| 183 |   |  |         |          |
| 184 | Maximum Flow from Condensers            |  |         | units    |
| 185 | > Max. Flow of Liquid Nitrogen          | 13   | 13      | gpm      |
| 186 | Max. Flow of Liquid Nitrogen (conv.)    | =B185/7.48   | 1.74    | ft^3/min |
| 187 | Density of LN2 @ 3.5 atm                | 0.747  | 0.747   | g/cc     |
| 188 | Density of LN2 (conv.)                  | =B187*62.4   | 46.6128 | lbm/ft^3 |
| 189 | Mass Flow of LN2                        | =B186*B188*60  | 4861    | lbm/hr   |



Simplified Cryostat Fill/Vent Arrangement



# Calculation of Max. Flowrate from LAr Dewar to ECN



$$d = 1.682 \text{ in} = 0.1402 \text{ ft}$$

[1 1/2" SCH. 10 inner pipe dia.]

$$A = 0.01543 \text{ ft}^2$$

[cross-sectional area]

| Reference: drawings<br>from Tony Parker | up to cryocomer | cryocomer to CC | CC to ECN | TOTAL |
|---|-----------------|-----------------|-----------|-------|
| # of elbows, 90°                        | 17              | 4               | 19        | 40    |
| # of elbows, 45°                        | 1               | 3               | 1         | 5     |
| # of tees, branch                       | 3               | 0               | 0         | 3     |
| # of tees, thru                         | 0               | 2               | 0         | 2     |

### Calculation of Equivalent Length

Calculate the equivalent length of the piping from the LAr dewar to the inner vessel of the ECN.

$$L_{\text{piping}} = L_{1.7'' \text{ dia.}} + L_{1.0'' \text{ dia.}}$$

Adjust 169 ft length to CC (ref. Kelly Dixon) to include ECN.

$$L_{1.7'' \text{ dia.}} = 169 \text{ ft (length to CC)} - 8.3 \text{ ft (CC drain line)} + 21.7 \text{ ft (CC to rotary bayonet assembly)} + 4.6 \text{ ft} + 5.2 \text{ ft (rotary U-tube dimensions)} + 6.1 \text{ ft} + 13 \text{ ft (ECN drain line)} = 211.3 \text{ ft total.}$$

Equivalent lengths of the flowmeters are accounted for by including a 4 foot length of 1.0" diameter piping. Convert 1.0" diameter equivalent length to 1.7" dia. equivalent length:

Reference: Crane Technical Paper No. 410

(1" SCH. 40 to 1 1/2" SCH. 10)

$$L_{1.0'' \text{ dia.}} = \left( \frac{1.682}{1.049} \right)^5 \times 4' = 42.4'$$

$$L_{\text{piping}} = 211.3 \text{ ft} + 42.4 \text{ ft} = 253.7 \text{ ft total}$$

Convert elbows and tees into equivalent lengths of pipe.

$$L_{\text{fittings}} = [40(20) + 5(14) + 3(60) + 2(20)] \times 0.1402 \text{ ft} = 152.8 \text{ ft}$$

$$L_{\text{eq}} = 253.7 \text{ ft} + 152.8 \text{ ft} = 406.5 \text{ ft}$$

**Calculation of Resistance Coefficient**

Reference: Crane Technical Paper No. 410

Calculate the resistance coefficient for the piping and fittings.

$$K_{\text{piping, fittings}} = f \left( \frac{L_{\text{eq}}}{d} \right)$$

let  $f = 0.022$  [friction factor guess]

$$K_{\text{piping, fittings}} = 0.022 \left( \frac{406.5 \text{ ft}}{0.1402 \text{ ft}} \right) = 63.79$$

Include inlet and outlet losses (ref. Kelly Dixon).

$$K_{\text{inlet}} = 0.5$$

$$K_{\text{outlet}} = 1.0$$

Calculate resistance coefficient for the valves.

$$K_{\text{valves}} = \left( \frac{29.9 d^2}{C_v} \right)^2 \times (\# \text{ of valves}) = \left( \frac{29.9 (1.682)^2}{34} \right)^2 \times 4 = 24.76$$

where the diameter,  $d$ , is in inches, not feet.

$$\Sigma K = 63.79 + 1.5 + 24.76 = 90.05$$

### Driving Pressure

Calculate the differential pressure available under relieving conditions.

max. head available = 720.3 ft (dewar @ 16,000 gallons)

- 715.2 ft (bottom of ECN)

---

5.1 ft (total elevation difference)

Calculate the pressure due to elevation difference.

Density of liquid argon @ 19.75 psig = 1.337 g/cc, which corresponds to a specific weight of 0.580 psi/ft.

$\Delta p$  due to head = 5.1 ft x 0.580 psi/ft = 2.96 psi

$\Delta p_{\text{relieving}} = (\text{LAr dewar pressure}) - (\text{ECN pressure}) + (\text{head pressure})$   
 $= 34.7 \text{ psia} - 34.45 \text{ psia} + 2.96 \text{ psi} = 3.21 \text{ psid}$

Determine the pressure drop across the cryofilter.

Actual experience shows that with a 30 gpm flow, the pressure drop across the cryofilter is 4 psid.

$$\Delta p_{\text{filter}} = \left( \frac{q}{30} \right)^2 \times 4 \text{ psid} = 0.00444 q^2$$

where  $\Delta p_{\text{filter}}$  is in psid if  $q$  is in gpm.

$\Delta p_{\text{available}} = \Delta p_{\text{relieving}} - \Delta p_{\text{filter}}$

### Calculation of Flowrate

Calculate the flowrate,  $q$ , by rearranging Darcy's formula (ref. Crane 410).

modified Darcy's formula:

$$\Delta p = \frac{\rho \Sigma K}{144} \frac{v^2}{2 g_c}$$

where:  $\Delta p$  is in psid,

$\rho$  is in  $\text{lb}_m/\text{ft}^3$ ,

and  $v$  is in ft/s.

(144 is a conversion factor of  $\text{in}^2/\text{ft}^2$ .)

Rearrange to solve for the velocity,  $v$ .

$$v = \sqrt{\frac{2 g_c (144 \Delta p)}{\rho \Sigma K}} = \sqrt{\frac{2 \left( 32.174 \frac{\text{lb}_m \cdot \text{ft}}{\text{lb}_f \cdot \text{s}^2} \right) \left( 144 \frac{\text{in}^2}{\text{ft}^2} \right) \Delta p_{\text{available}}}{\left( 83.47 \frac{\text{lb}_m}{\text{ft}^3} \right) (90.05)}}$$

$$v = 1.110 \sqrt{\Delta p_{\text{available}}}$$

where  $v$  is in ft/s if  $\Delta p_{\text{available}}$  is in psid.

Substitute formulas with  $q$  into both sides of the equation for  $v$  and  $\Delta p$ .

Substitute for  $v$ : (Let  $Q$  be the flow rate in cfs.)

$$v = \frac{Q}{A} = \frac{4Q}{\pi d^2} = \frac{4Q}{\pi (0.1402 \text{ ft})^2} = 64.78Q$$

where  $v$  is in ft/s if  $Q$  is in cfs.

Convert the equation so that  $v$  will be in ft/s if  $q$  is in gpm.

$$v = 64.78 \left( q \frac{\text{gal}}{\text{min}} \times \frac{\text{min}}{60 \text{ sec}} \times 0.13368 \frac{\text{ft}^3}{\text{gal}} \right) = 0.1443q$$

where  $v$  is in ft/s if  $q$  is in gpm.

Substitute for  $\Delta p$ :

From before,  $\Delta p_{\text{available}} = \Delta p_{\text{relieving}} - \Delta p_{\text{filter}}$ .

$$\Delta p_{\text{available}} = 3.21 \text{ psid} - 0.00444q^2$$

where  $\Delta p_{\text{available}}$  is in psid if  $q$  is in gpm.

From before,

$$v = 1.110 \sqrt{\Delta p_{\text{available}}}$$

where  $v$  is in ft/s if  $\Delta p_{\text{available}}$  is in psid.

Substitute formula for  $\Delta p_{\text{available}}$  to get  $v$  in terms of  $q$ .

$$v = 1.110 \sqrt{3.21 - 0.00444q^2}$$

where  $v$  is in ft/s if  $q$  is in gpm.

Set the two equations for  $v$  in terms of  $q$  equal, and solve for  $q$ .

$$v = 0.1443q = 1.110\sqrt{3.21 - 0.00444q^2}$$

$$q = \sqrt{\frac{3.21}{\left(\frac{0.1443}{1.110}\right)^2 + 0.00444}}$$

$$q = 12.26 \text{ gpm}$$

### Check Friction Factor

$$Re_{d\text{relieving}} = \frac{\rho V_{\text{rel.}} d}{\mu}$$

$$\mu = 2.4185 \times 10^{-3} \frac{\text{g}}{\text{cm-s}} @ \text{sat. 1.3 bars} = 1.6252 \times 10^{-4} \frac{\text{lb}_m}{\text{ft-s}}$$

$$q_{\text{relieving}} = 12.26 \text{ gpm}$$

$$v_{\text{rel.}} = \frac{q_{\text{relieving}}}{A} = \frac{4 q_{\text{relieving}}}{\pi d^2} = \frac{4 \left( 12.26 \text{ gpm} \times \frac{1 \text{ cfs}}{448.83 \text{ gpm}} \right)}{\pi (0.1402 \text{ ft})^2} = 1.769 \frac{\text{ft}}{\text{s}}$$

$$Re_{d\text{relieving}} = \frac{\left( 83.47 \frac{\text{lb}_m}{\text{ft}^3} \right) \left( 1.769 \frac{\text{ft}}{\text{s}} \right) (0.1402 \text{ ft})}{1.6252 \times 10^{-4} \frac{\text{lb}_m}{\text{ft-s}}} = 1.274 \times 10^5$$

Assuming a value of 0.00015 roughness for commercial steel pipe, the relative roughness is 0.001, and the friction factor is 0.022, which checks.

### TK Solver Plus Analysis

The following two pages are printouts of the variable and rule sheet from a TK Solver model set up to verify the hand calculations for the maximum flow rate to the ECN from the Argon dewar. The first page is the variable sheet, which shows the typed inputs and calculated outputs for various parameters. The complete solution requires guessing a number for the friction factor. The program then iterates to find the exact solution. Also note that the columns have a set width, so that not all of the entries are shown completely, specifically,  $g$  has units of  $\text{lbm-ft/lbf-s}^2$ . The second sheet is the rule sheet, which shows the various formulas used. The complete model has been saved in the Co-op Mac, under the name "TK LAD Flow to ECN".



| <u>St</u> | <u>Input</u> | <u>Name</u> | <u>Output</u> | <u>Unit</u> | <u>Comment</u>                   |
|-----------|--------------|-------------|---------------|-------------|----------------------------------|
|           | 1.682        | D           |               | in          | inner pipe dia.                  |
|           |              | d           | .14016667     | ft          | inner pipe dia. (converted)      |
|           |              | A           | .01543046     | ft^2        | cross-sectional area             |
| 40        |              | Els90       |               |             | number of 90° elbows             |
| 5         |              | Els45       |               |             | number of 45° elbows             |
| 3         |              | TeesBr      |               |             | number of tees, branch           |
| 2         |              | TeesTh      |               |             | number of tees, thru             |
| 253.7     |              | Lpiping     |               | ft          | equivalent length of 1.7" piping |
|           |              | Lfittin     | 152.78167     | ft          | equivalent length of fittings    |
|           |              | Leq         | 406.48167     | ft          | equivalent length                |
|           |              | f           | .02195416     |             | friction factor (guess)          |
| .5        |              | Kinlet      |               |             | inlet resistance                 |
| 1         |              | Koutlet     |               |             | outlet resistance                |
|           |              | Kpiping     | 63.66681      |             | resistance of piping             |
| 34        |              | Cv          |               |             | coeff. of valves                 |
| 4         |              | valves      |               |             | number of valves counted         |
|           |              | Kvalves     | 24.759878     |             | resistance of valves             |
|           |              | SumK        | 89.926688     |             | summation of resistances         |
| 5.1       |              | elev        |               | ft          | max. head available              |
| 83.47     |              | rho         |               | lbm/ft^3    | density of argon                 |
|           |              | SpWt        | .57965278     | psi/ft      | specific weight of argon         |
|           |              | DPhead      | 2.9562292     | psi         | delta p from head                |
|           |              | DPrel       | 3.2062292     | psi         | delta p relieving                |
|           |              | DPfilte     | .66797323     | psi         | delta p from filter              |
|           |              | DPavail     | 2.5382559     | psi         | delta p available                |
|           |              | Vrel        | 1.7701374     | ft/s        | relieving velocity               |
|           |              | Re          | 127431.07     |             | Reynold's number                 |
| .00016252 |              | visc        |               | lbm/ft-s    | viscosity                        |
| .00015    |              | e           |               |             | roughness coefficient            |
|           |              | rough       | .00107015     |             | relative roughness (e/d)         |
|           |              | pi          | 3.14159       |             | pi constant                      |
|           |              | g           | 32.174        | lbm-ft/lb   | gc conversion constant           |
|           |              | q           | 12.259444     | gpm         | flow rate                        |

# S Rule

```
* pi = 3.14159      "constant for pi
* g = 32.174      "constant for gc, in units of (lbm-ft)/(lbf-s^2)
* d = D/12      "conversion of inner pipe dia. from inches to feet
* A = pi*(d^2)/4      "cross-sectional area of pipe
  Lfittings = d*(Els90*20+Els45*14+TeesBr*60+TeesTh*20)      "equivalent length
* Leq = Lpiping + Lfittings      "total equivalent length of 1.7" dia piping
* Kpiping = f*Leq/d      "resistance coeff. for piping and fittings
* Kvalves = valves*((29.9*(D^2)/Cv)^2)      "resistance of valves
* SumK = Kpiping+Kvalves+Kinlet +Koutlet      "summation of K coeff.
* SpWt = rho/144      "specific weight at correct density
* DPhead = elev * SpWt      "delta p due to max. head pressure
* DPrel = 34.7 - 34.45 + DPhead      "delta p due to elevation difference
* DPfilter = 4*((q/30)^2)      "pressure drop across cryofilter
* DPavail = DPrel - DPfilter      "available differential driving pressure
* DPavail = (rho*SumK*(Vrel^2))/(144*2*g)      "modified Darcy's formula
* Vrel = (q*.13368/60)/A      "velocity in ft/s from flow rate in gpm
* Re = rho*Vrel*d/visc      "Reynold's number for pipe flow
* rough = e/d      "relative roughness for commercial steel of 1 1/2" dia.
* 1/(f^.5) = -2.0*log((rough/3.7) + (2.51/(Re*(f^.5))))      "Moody chart
```

(4)

## ECN Equivalent Lengths of Relief/ Exhaust Piping

ko  
22 Jul 91

### ① Relief Valve Inlet

$$L = 38', \quad d = 0.206' \quad \text{ref: EN-263}$$

### ② Rupture Disk Inlet

#els: 8

$$L_{\text{pipe}} = 51'' + 23 + 5 + 15 = 94'' = 7.8'$$

$$d = 0.172' \quad (2'' \text{ sch } 40)$$

$$L_e = 7.8' + 30(0.172) = 49'$$

### ③ Relief Valve Outlet

#tees (branch): 1

#els,  $90^\circ$  : 1 (mitered)

#els,  $45^\circ$  : 2 (mitered)

~~tee~~  $d = 0.27'$

$$L_e = 1.9' + (60 + 60 + 2(30))(0.27) = 51'$$

### ④ Rupture Disk Outlet

$$d = 0.180'$$

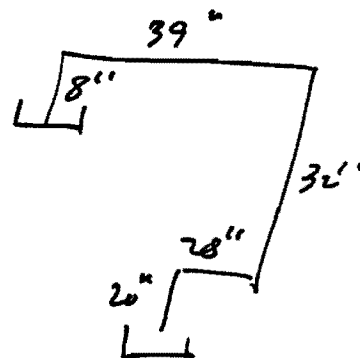
$$L_e = 1.75'$$

### ⑤ Relief Common Outlet to Platform Bayonet

$$d = 0.355'$$

length bot. bayonet spool assy

$$8'' + 39 + 32 + 28 + 20 = 127''$$



$$\begin{aligned} \text{Piping} &= 24'' + 127'' + 62'' + 2(157.5'') + 38 + 10 + 40 \\ &\quad + 67 + 210.5 + 457.5 + 74 + 16 \\ &= 1441'' = 120 \text{ ft} \end{aligned}$$

# els,  $90^\circ$ : 11

# els,  $45^\circ$ : 1 (approx)

# tees (thru): 2

# tees (brch): 1

$$\begin{aligned} L_e &= 120 + 0.355(11(20) + 2(20) + 1(60)) \\ &= 120 + 153 \\ &= 273' \end{aligned}$$

### ⑥ Platform Bayonet to Outside

$$d = 0.530'$$

$$L_e = 516'$$

Ref. EN263

October 18, 1991

### Determine Worst Case Cryostat to Fill Due to Pressure

#### Fill capacity

Reference: ECN numbers taken from previous "Calculation of Max. Flowrate from LAr Dewar to ECN".

$$(q_{\text{fill}}^{\text{ECN}})_{\text{max}} = 12.3 \text{ gpm}$$

$$\Sigma K^{\text{ECN}} = 90.05$$

$$\Sigma K^{\text{CC}} = \Sigma K^{\text{ECN}} - \frac{f(L_{eq})}{d} \cong 90.05 - \frac{(0.022)(30 \text{ ft})}{0.1402 \text{ ft}} = 85.34$$

$$\Sigma K^{\text{ECS}} = \Sigma K^{\text{CC}} - \frac{f(L_{eq})}{d} \cong 85.34 - \frac{(0.022)(27 \text{ ft})}{0.1402 \text{ ft}} = 81.10$$

The ECS has the smallest resistance coefficient because it has the shortest equivalent length of piping from the argon dewar. Therefore, the same driving pressure from the dewar will produce the largest inlet flow to the ECS. The flowrate is inversely proportional to the square root of the resistance coefficient:

$$q^{\text{cryostat}} \propto \frac{1}{\sqrt{\Sigma K^{\text{cryostat}}}}$$

Therefore, the flowrates of the ECS and ECN can be compared as follows:

$$\frac{q_{\text{fill}}^{\text{ECS}}}{q_{\text{fill}}^{\text{ECN}}} = \frac{\sqrt{\Sigma K^{\text{ECN}}}}{\sqrt{\Sigma K^{\text{ECS}}}} = \frac{\sqrt{90.05}}{\sqrt{81.10}} = 1.054$$

The maximum inlet flow to the ECS is greater than the maximum inlet flow to the ECN by about 5%. However, the ECS is not the worst case cryostat to fill because it also has a shorter equivalent length of relief piping.

### Venting capacity

Reference: DØ Engineering Note 3740.224-EN-323, ECN Pressure and Vacuum Vessel Engineering Notes.

The first spreadsheet in EN-323 calculates the ECN relief flow capacity. In the section, "ΔP Across Relief Valve", line 108 shows the maximum theoretical flow through the relief valve. In the section, "ΔP Across Rupture Disk", line 181 shows the maximum theoretical flow through the rupture disk. Therefore, the total mass flow can be calculated as:

$$\rho(q_{rel})_{max}^{ECN} = 7740 \frac{lb_m}{hr} (\text{relief valve}) + 7458 \frac{lb_m}{hr} (\text{rupture disk}) = 15,198 \frac{lb_m}{hr}$$

Note that q here represents the flow through the relief piping, out of the ECN, whereas the q on the previous page represented the inlet fill piping, into the ECN.

The calculation of the venting capacity of the ECS is more complicated, because the numbers can not be referenced from EN-323. To calculate the ECS capacity, the ECN spreadsheet was modified for the ECS, changing the section, "ΔP Across Common Outlet to Cryocorner". Line 115 is the equivalent length of this section of piping. ECN had an equivalent length of 273 ft, which was calculated in this note (see previous K. Dixon's hand calculations, "ECN Equivalent Lengths of Relief/Exhaust Piping"). The only difference in the relief piping of the ECS is that the equivalent length of the common outlet changes to 238 ft. Using this new equivalent length, the spreadsheet was re-calculated to find the maximum theoretical flows through the relief valve and rupture disk. The following pages show the actual spreadsheet, modified for the ECS.

# Maximum ECS Relief Flow Calculation 10/18/91

|    | A  | B  | C         | D          |
|----|--|--|-----------|------------|
| 1  | Conversion of Liquid to Gas at Module Temp.        |  |           | Units      |
| 2  | > Bulk Temp. of Modules                            | 96   | 96        | K          |
| 3  | >* Max. Liquid Equivalent Flow of Argon to Reliefs | 24.9   | 24.9      | gpm        |
| 4  | > Pressure in Cryostat                             | 19.75  | 19.75     | psig       |
| 5  | Pressure in Cryostat (conv.)                       | $=(B4/14.696+1)*1.01325$                             | 2.375     | bars       |
| 6  | > lAr Density @ 2.2 bars                           | 1.342421   | 1.342     | g/cc       |
| 7  | > lAr Density @ 2.4 bars                           | 1.335861   | 1.336     | g/cc       |
| 8  | lAr Density @ 2.375 bars                           | $=(B5-2.2)/0.2*(B7-B6)+B6$                           | 1.337     | g/cc       |
| 9  | > gAr Density @ 2.2 bars                           | 11.77  | 11.77     | mg/cc      |
| 10 | > gAr Density @ 2.4 bars                           | 12.75  | 12.75     | mg/cc      |
| 11 | gAr Density @ 2.375 & Temp.                        | $=(B5-2.2)/0.2*(B10-B9)+B9$                          | 12.627    | mg/cc      |
| 12 | gAr Density @ 2.375 bars (conv.)                   | $=B11/1000*62.428$                                   | 0.788     | lbm/ft^3   |
| 13 | Maximum Flow of Argon Gas                          | $=B3*B8/B11*1000$                                    | 2636      | gpm        |
| 14 | Maximum Flow of Argon Gas (conv.)                  | $=B13*0.13368$                                       | 352       | cfm        |
| 15 | Air Equivalent Flow @STP                           | $=6.32*B17*356/B16*SQRT(B99/(520*B177*28.97))$       | 1658      | scfm air   |
| 16 | Specific Heat Constant, C, for Ar                  | $=520*SQRT(B168*(2/(B168+1))^{((B168+1)/(B168-1)))}$ | 383       |            |
| 17 | Max. Mass Flow of Argon Gas                        | $=B14*B12*60$  | 16666     | lbm/hr     |
| 18 | *> Percent of Mass Flow to Relief Valve            | 0.474  | 0.474     |            |
| 19 |  |  |           |            |
| 20 | ΔP Across Relief Valve Inlet                       |  |           | Units      |
| 21 | > Inner Pipe Diameter                              | 0.206  | 0.206     | ft         |
| 22 | Inner Pipe Diameter (conv.)                        | $=B21*12$  | 2.472     | in         |
| 23 | > Equivalent Length                                | 38   | 38        | ft         |
| 24 | Ar Gas Density @ 2.375 & Temp.                     | $=(B5-2.2)/0.2*(B10-B9)+B9$                          | 12.627    | mg/cc      |
| 25 | Ar Gas Density @ 2.375 bars (conv.)                | $=B24/1000*62.428$                                   | 0.788     | lbm/ft^3   |
| 26 | > gAr Viscosity @ 2.4 bars & Temp.                 | 0.0000803  | 0.0000803 | g/cm-s     |
| 27 | gAr Viscosity @ 2.4 bars (conv.)                   | $=B26*100$   | 0.00803   | centipoise |
| 28 | Max. Mass Flow to Relief Valve                     | $=B17*B18$   | 7900      | lbm/hr     |
| 29 | Reynolds Number                                    | $=6.31*B28/(B22*B27)$                                | 2510000   |            |
| 30 | > Relative Roughness (e/D)                         | 0.0007   | 0.0007    |            |
| 31 | Friction Factor Guess                              | $=0.25*(LOG(B30/3.7+5.74/(B29^0.9)))^2$              | 0.0183    |            |
| 32 | Friction Factor                                    | $=0.25*(LOG(B30/3.7+2.51/(B29*B31^0.5)))^2$          | 0.0182    |            |
| 33 | Pressure Drop                                      | $=0.00000336*B32*B23*(B28^2)/B25/(B22^5)$            | 1.993     | psi        |
| 34 |  |  |           |            |

# Maximum ECS Relief Flow Calculation 10/18/91

|    | A                                 | B  | C         | D          |
|----|-----------------------------------|--|-----------|------------|
| 35 | ΔP Across Rupture Disk Inlet      |  |           | Units      |
| 36 | Inner Pipe Diameter (conv.)       | =B37/12                                    | 0.172     | ft         |
| 37 | > Inner Pipe Diameter             | 2.067                                      | 2.067     | in         |
| 38 | > Equivalent Length               | 49   | 49        | ft         |
| 39 | gAr Density @ 2.375 & Temp.       | =(B5-2.2)/0.2*(B10-B9)+B9                  | 12.627    | mg/cc      |
| 40 | gAr Density @ 2.375 bars (conv.)  | =B39/1000*62.428                           | 0.788     | lbm/ft^3   |
| 41 | gAr Viscosity @ 2.4 bars          | =B26                                       | 0.0000803 | g/cm-s     |
| 42 | gAr Viscosity @ 2.4 bars (conv.)  | =B41*100                                   | 0.00803   | centipoise |
| 43 | Max. Mass Flow to Rupture Disk    | =B17*(1-B18)                               | 8766      | lbm/hr     |
| 44 | Reynolds Number                   | =6.31*B43/(B37*B42)                        | 3330000   |            |
| 45 | > Relative Roughness (e/D)        | 0.0009                                     | 0.0009    |            |
| 46 | Friction Factor Guess             | =0.25*(LOG(B45/3.7+5.74/(B44^0.9)))^-2     | 0.0193    |            |
| 47 | Friction Factor                   | =0.25*(LOG(B45/3.7+2.51/(B44*B46^0.5)))^-2 | 0.0192    |            |
| 48 | Pressure Drop                     | =0.00000336*B47*B38*(B43^2)/B40/(B37^5)    | 8.185     | psi        |
| 51 |                                   |  |           |            |
| 52 | ΔP Across Relief Valve Outlet     |  |           | Units      |
| 53 | Inner Pipe Diameter (conv.)       | =B54/12                                    | 0.272     | ft         |
| 54 | > Inner Pipe Diameter             | 3.26                                       | 3.26      | in         |
| 55 | > Equivalent Length               | 51   | 51        | ft         |
| 56 | > gAr Density @ 2.0 bar & Temp.   | 10.55                                      | 10.55     | mg/cc      |
| 57 | gAr Density @ 2.0 bar (conv.)     | =B56/1000*62.428                           | 0.659     | lbm/ft^3   |
| 58 | > gAr Viscosity @ 2.0 bar & Temp. | 0.0000798                                  | 0.0000798 | g/cm-s     |
| 59 | gAr Viscosity @ 2.0 bar (conv.)   | =B58*100                                   | 0.00798   | centipoise |
| 60 | Max. Mass Flow to Relief Valve    | =B28                                       | 7900      | lbm/hr     |
| 61 | Reynolds Number                   | =6.31*B60/(B54*B59)                        | 1920000   |            |
| 62 | > Relative Roughness (e/D)        | 0.00055                                    | 0.00055   |            |
| 63 | Friction Factor Guess             | =0.25*(LOG(B62/3.7+5.74/(B61^0.9)))^-2     | 0.0174    |            |
| 64 | Friction Factor                   | =0.25*(LOG(B62/3.7+2.51/(B61*B63^0.5)))^-2 | 0.0173    |            |
| 65 | Pressure Drop                     | =0.00000336*B64*B55*(B60^2)/B57/(B54^5)    | 0.764     | psi        |
| 66 |                                   |  |           |            |



**Maximum ECS Relief Flow Calculation 10/18/91**

|    | A   | B  | C         | D          |
|----|---|--|-----------|------------|
| 67 | ΔP Across Rupture Disk Outlet             |  |           | Units      |
| 68 | Inner Pipe Diameter (conv.)               | =B69/12                                    | 0.18      | ft         |
| 69 | > Inner Pipe Diameter                     | 2.157                                      | 2.157     | in         |
| 70 | > Equivalent Length                       | 1.75                                       | 1.75      | ft         |
| 71 | gAr Density @ 2.0 bar & Temp.             | =B56                                       | 10.55     | mg/cc      |
| 72 | gAr Density @ 2.0 bar (conv.)             | =B71/1000*62.428                           | 0.659     | lbm/ft^3   |
| 73 | gAr Viscosity @ 2.0 bar & Temp.           | =B58                                       | 0.0000798 | g/cm-s     |
| 74 | gAr Viscosity @ 2.0 bar (conv.)           | =B73*100                                   | 0.00798   | centipoise |
| 75 | Max. Mass Flow to Rupture Disk            | =B43                                       | 8766      | lbm/hr     |
| 76 | Reynolds Number                           | =6.31*B75/(B69*B74)                        | 3210000   |            |
| 77 | > Relative Roughness (e/D)                | 0.0009                                     | 0.0009    |            |
| 78 | Friction Factor Guess                     | =0.25*(LOG(B77/3.7+5.74/(B76^0.9)))^-2     | 0.0193    |            |
| 79 | Friction Factor                           | =0.25*(LOG(B77/3.7+2.51/(B76*B78^0.5)))^-2 | 0.0192    |            |
| 80 | Pressure Drop                             | =0.00000336*B79*B70*(B75^2)/B72/(B69^5)    | 0.283     | psi        |
| 81 |   |  |           |            |
| 82 | Change in Gas at Common Outlet to Outside |  |           | Units      |
| 83 | Pressure in Cryostat                      | =B4  | 19.75     | psig       |
| 84 | Pressure in Cryostat (conv.)              | =(B83/14.696+1)*1.01325                    | 2.375     | bars       |
| 85 | gAr Density @ 2.2 bars                    | =B9  | 11.77     | mg/cc      |
| 86 | gAr Density @ 2.4 bars                    | =B10                                       | 12.75     | mg/cc      |
| 87 | gAr Density @ 2.375 & Temp.               | =(B84-2.2)/0.2*(B86-B85)+B85               | 12.627    | mg/cc      |
| 88 | Temp. at Common Outlet                    | =(B2*B17+84*B189)/(B17+B189)               | 94        | K          |
| 89 | > Pressure to Calculate Density           | 1.5  | 1.5       | bars       |
| 90 | *> gAr Density @ 1.5 bars & New Temp.     | 7.99                                       | 7.99      | mg/cc      |
| 91 | *> gAr Viscosity @ 1.5 bars & New Temp.   | 0.000078                                   | 0.000078  | g/cm-s     |
| 92 | gAr Viscosity @ 1.5 bar (conv.)           | =B91*100                                   | 0.0078    | centipoise |
| 93 |   |  |           |            |

**Maximum ECS Relief Flow Calculation      10/18/91**

|     | A                                       | B  | C      | D      |
|-----|---|--|--------|--------|
| 94  | ΔP Across Relief Valve                  |  |        | Units  |
| 95  | > Critical Ratio (Pcr/P1) for Argon     | 0.487  | 0.487  |        |
| 96  | > Specific Heat Ratio (k) for Argon     | =B168  | 1.75   |        |
| 97  | > Area of 2" x 3" Relief Valve          | 2.29   | 2.29   | in^2   |
| 98  | Flow Through Relief Valve               | =B28   | 7900   | lbm/hr |
| 99  | Flowing Temperature                     | =1.8*B2  | 173.   | deg R  |
| 100 | > Compressibility Factor                | 1  | 1      |        |
| 101 | > Nozzle Coefficient for type 93T       | 0.939  | 0.939  |        |
| 102 | Flowing Inlet Pressure (P1)             | =B4+14.696-B33   | 32.45  | psia   |
| 103 | > Molecular Weight of Argon             | 39.948   | 39.95  | g/mol  |
| 104 | Critical Pressure (Pcr)                 | =B95*B102  | 15.8   | psia   |
| 105 | Outlet Pressure (P2) (using delta p's)  | =14.696+B154+B133+B65                                    | 25.43  | psia   |
| 106 | Pressure Ratio (P2*/P1)                 | =(B102-0.55*((B102-B105)^0.98))/B102                     | 0.885  |        |
| 107 | Theoretical Factor (F*) (using P2)      | =SQRT((B96/(B96-1))*((B106^(2/B96)-B106^((B96+1)/B96)))) | 0.321  |        |
| 108 | Max. Theoretical Relief Flow (using F*) | =735*B97*B101*B102*B107*SQRT(B103/B99/B100)              | 7918   | lbm/hr |
| 109 | Theoretical Percent of Relief Flow      | =B108/B17  | 0.4751 |        |
| 110 | Pressure Drop Across Relief Valve       | =B102-B105   | 7.026  | psi    |
| 111 |   |  |        |        |

**Maximum ECS Relief Flow Calculation 10/18/91**

|     | A  | B   | C         | D          |
|-----|--|---|-----------|------------|
| 112 | ΔP Across Common Outlet to Cryocorner    |   |           | Units      |
| 113 | > Inner Pipe Diameter                    | 0.355   | 0.355     | ft         |
| 114 | Inner Pipe Diameter (conv.)              | =B113*12  | 4.26      | in         |
| 115 | > Equivalent Length                      | 238   | 238       | ft         |
| 116 | gAr Density @ 1.5 bar & New Temp.        | =B90  | 7.99      | mg/cc      |
| 117 | gAr Density @ 1.5 bar (conv.)            | =B116/1000*62.428                               | 0.499     | lbm/ft^3   |
| 118 | *> gN2 Gas Density @ 1.5 bar & New Temp. | 5.653   | 5.653     | mg/cc      |
| 119 | gN2 Gas Density @ 1.5 bar (conv.)        | =B118/1000*62.428                               | 0.353     | lbm/ft^3   |
| 120 | Gas Mixture Density @1.5 bar             | =(B17*B117+B127*B119)/B128                      | 0.474     | lbm/ft^3   |
| 121 | gAr Viscosity @ 1.5 bar & New Temp.      | =B91  | 0.000078  | g/cm-s     |
| 122 | gAr Viscosity @ 1.5 bar (conv.)          | =B121*100                                       | 0.0078    | centipoise |
| 123 | *> gN2 Viscosity @ 1.5 bar & New Temp.   | 0.0000643                                       | 0.0000643 | g/cm-s     |
| 124 | gN2 Viscosity @ 1.5 bar (conv.)          | =B123*100                                       | 0.00643   | centipoise |
| 125 | Mixture Viscosity @1.5 bar               | =(B17*B122+B127*B124)/B128                      | 0.007563  | centipoise |
| 126 | Max. Mass Flow of Argon Gas              | =B17  | 16666     | lbm/hr     |
| 127 | Max. Flow of Nitrogen Gas                | =B189   | 3477      | lbm/hr     |
| 128 | Mass Flow of Mixture                     | =B126+B127                                      | 20143     | lbm/hr     |
| 129 | Reynolds Number                          | =6.31*B128/(B114*B125)                          | 3940000   |            |
| 130 | > Relative Roughness (e/D)               | 0.0004  | 0.0004    |            |
| 131 | Friction Factor Guess                    | =0.25*(LOG(B130/3.7+5.74/(B129^0.9)))^(-2)      | 0.0161    |            |
| 132 | Friction Factor                          | =0.25*(LOG(B130/3.7+2.51/(B129*B131^0.5)))^(-2) | 0.0161    |            |
| 133 | Pressure Drop                            | =0.00000336*B132*B115*(B128^2)/B120/(B114^5)    | 7.838     | psi        |
| 134 |  |   |           |            |

**Maximum ECS Relief Flow Calculation 10/18/91**

|     | A                                     | B   | C         | D          |
|-----|---------------------------------------|---|-----------|------------|
| 135 | $\Delta P$ from Cryocorner to Outside |   |           | Units      |
| 136 | > Inner Pipe Diameter                 | 0.53  | 0.53      | ft         |
| 137 | Inner Pipe Diameter (conv.)           | =B136*12                                      | 6.36      | in         |
| 138 | > Equivalent Length                   | 516   | 516       | ft         |
| 139 | gAr Gas Density @ 1.5 bar & New Temp. | =B90  | 7.99      | mg/cc      |
| 140 | gAr Gas Density @ 1.5 bar (conv.)     | =B139/1000*62.428                             | 0.499     | lbm/ft^3   |
| 141 | gN2 Gas Density @ 1.5 bar & New Temp. | =B118   | 5.653     | mg/cc      |
| 142 | gN2 Gas Density @ 1.5 bar (conv.)     | =B141/1000*62.428                             | 0.353     | lbm/ft^3   |
| 143 | Gas Mixture Density @1.5 bar          | =(B17*B140+B189*B142)/B149                    | 0.474     | lbm/ft^3   |
| 144 | gAr Viscosity @ 1.5 bar & New Temp.   | =B121   | 0.000078  | g/cm-s     |
| 145 | gAr Viscosity @ 1.5 bar (conv.)       | =B144*100                                     | 0.0078    | centipoise |
| 146 | gN2 Viscosity @ 1.5 bar & New Temp.   | =B123   | 0.0000643 | g/cm-s     |
| 147 | gN2 Viscosity @ 1.5 bar (conv.)       | =B146*100                                     | 0.00643   | centipoise |
| 148 | Gas Mixture Viscosity @1.5 bar        | =(B17*B145+B189*B147)/B149                    | 0.007563  | centipoise |
| 149 | Max. Mass Flow of Gas Mixture         | =B128   | 20143     | lbm/hr     |
| 150 | Reynolds Number                       | =6.31*B149/(B137*B148)                        | 2640000   |            |
| 151 | > Relative Roughness (e/D)            | 0.00027                                       | 0.00027   |            |
| 152 | Friction Factor Guess                 | =0.25*(LOG(B151/3.7+5.74/(B150^0.9)))^-2      | 0.015     |            |
| 153 | Friction Factor                       | =0.25*(LOG(B151/3.7+2.51/(B150*B152^0.5)))^-2 | 0.0149    |            |
| 154 | Pressure Drop                         | =0.00000336*B153*B138*(B149^2)/B143/(B137^5)  | 2.13      | psi        |
| 155 |                                       |   |           |            |
| 156 | Summation of Equivalent $\Delta P$ s  |   |           | Units      |
| 157 | Relief Valve Inlet Pressure Drop      | =B33  | 1.993     | psi        |
| 158 | Relief Valve Outlet Pressure Drop     | =B65  | 0.764     | psi        |
| 159 | Relief Valve Pressure Drop            | =B110   | 7.026     | psi        |
| 160 | Relief Valve/Disk Branch              | =B33+B65+B110                                 | 9.782     | psi        |
| 161 | Rupture Disk Inlet Pressure Drop      | =B48  | 8.185     | psi        |
| 162 | Rupture Disk Outlet Pressure Drop     | =B80  | 0.283     | psi        |
| 163 | Rupture Disk Pressure Drop            | =B157+B158+B159-B161-B162                     | 1.313     | psi        |
| 164 | Common Outlet Pressure Drop           | =B133   | 7.838     | psi        |
| 165 | Cryocorner to Outside Pressure Drop   | =B154   | 2.13      | psi        |
| 166 |                                       |   |           |            |

**Maximum ECS Relief Flow Calculation 10/18/91**

|     | A   | B   | C       | D        |
|-----|---|---|---------|----------|
| 167 | ΔP Across Rupture Disk                                |   |         | Units    |
| 168 | >Argon Specific Heat Ratio (k)                        | 1.745   | 1.745   |          |
| 169 | Critical Ratio  | $= (2 / (B168 + 1))^{(B168 / (B168 - 1))}$  | 0.476   |          |
| 170 | > Area of 3" Rupture Disk                             | $= 3.14159 * (3^2) / 4$   | 7.069   | in^2     |
| 171 | Flow Through Rupture Disk                             | =B43  | 8766    | lbm/hr   |
| 172 | Flowing Temperature                                   | =1.8*B2   | 173     | deg R    |
| 173 | > ASME Coefficient (K)                                | 0.62  | 0.62    |          |
| 174 | Pressure Ratio (Pe/Po)                                | =B179/B176  | 0.95    |          |
| 175 | gAr Flow Constant for Subsonic Flow(C1)               | $= \text{SQRT}(2 * 32.2 / 1545 * (B168 / (B168 - 1)) * (B174^{(2 / B168)} - B174))$ | 0.045   |          |
| 176 | Flowing Inlet Pressure (Po)                           | =B4+14.696-B48  | 26.26   | psia     |
| 177 | > Molecular Weight of Argon                           | 39.948  | 39.948  | g/mol    |
| 178 | Critical Pressure (Pcr)                               | =B169*B176  | 12.51   | psia     |
| 179 | Outlet Pressure (Pe) (using delta p's)                | =14.696+B154+B133+B80   | 24.95   | psia     |
| 180 | Pressure Drop Across Rupture Disk                     | =B176-B179  | 1.313   | psi      |
| 181 | Maximum Theoretical Rupture Disk Flow                 | =B170*B173*B175*B176*SQRT(B177/B172)*60*60  | 8897    | lbm/hr   |
| 182 | Actual Rupture Disk Flow                              | =B43  | 8766    | lbm/hr   |
| 183 |   |   |         |          |
| 184 | Maximum Flow from Condensers                          |   |         | units    |
| 185 | > Max. Flow of Liquid Nitrogen                        | 9.3   | 9.3     | gpm      |
| 186 | Max. Flow of Liquid Nitrogen (conv.)                  | =B185/7.48  | 1.24    | ft^3/min |
| 187 | Density of LN2 @ 3.5 atm                              | 0.747   | 0.747   | g/cc     |
| 188 | Density of LN2 (conv.)                                | =B187*62.4  | 46.6128 | lbm/ft^3 |
| 189 | Mass Flow of LN2                                      | =B186*B188*60   | 3477    | lbm/hr   |
| 190 |   |   |         |          |
| 191 | Notes:  |   |         |          |
| 192 | *> indicates that this value must be changed for a    |   |         |          |
| 193 | new flowrate  |   |         |          |
| 194 |   |   |         |          |
| 195 | > indicates variable not requiring change for new     |   |         |          |
| 196 | flowrates   |   |         |          |
| 197 |   |   |         |          |
| 198 | (conv.) indicates the previous value converted to new |   |         |          |
| 199 | units   |   |         |          |

As with the ECN, the total mass flow for the ECS can be calculated from line 108 for the maximum relief valve flow, and line 181 for the maximum rupture disk flow:

$$\rho(q_{rel})_{max}^{ECS} = 7918 \frac{lb_m}{hr} (\text{relief valve}) + 8897 \frac{lb_m}{hr} (\text{rupture disk}) = 16,815 \frac{lb_m}{hr}$$

Now the ECN and ECS relief piping flowrates can be compared:

$$\frac{q_{rel}^{ECS}}{q_{rel}^{ECN}} = \frac{\rho q_{rel}^{ECS}}{\rho q_{rel}^{ECN}} = \frac{16,815 \frac{lb_m}{hr}}{15,198 \frac{lb_m}{hr}} = 1.106$$

The maximum relief outlet flow from the ECS is greater than the maximum relief outlet flow from the ECN by about 10%.

## Conclusion

Since the flowrate out of the ECS relative to the flowrate out of the ECN (1.106 times ECN) is greater than the flowrate into the ECS relative to the flowrate into the ECN (1.054 times ECN), the ECN is the flowrate limiting vessel.

### **Relief Valve Capacity for Filling ECN at Maximum Operating Temperature**

Although the maximum temperature calculated by this engineering note is 290 K, the spreadsheet requires flow through both the relief valve and the rupture disk. Although this situation satisfies safety conditions regarding the overpressurization of the vessel, in reality, the operating procedures should limit the temperature to a much lower value, to prevent the rupture disk from bursting. This section calculates the temperature at which the maximum flow from the argon dewar requires only the relief valve, and not the rupture disk.

The procedure is the same as before, so the same spreadsheet is used. The only difference is that in the section, "Conversion of Liquid to Gas at Module Temp.", line 18 is not guessed through iteration, but is set initially to 100%. This forces all of the flow through the relief valve, and all of the sections related to the rupture disk, including the pressure drops before and after the rupture disk, are essentially excluded from the calculation. Rather than physically remove these sections, they remain in the spreadsheet, but have no effect on the temperature. The bulk temperature is guessed as before, and iterations proceed, changing the various gas properties of argon and nitrogen each time, until a suitable temperature is found. The conclusion was that with a maximum flow of 12.3 gpm, as calculated previously, the maximum module temperature at which only the relief valve is required is at least 110 K. Note that the theoretical percent of relief flow (line 109) is greater than 100%, indicating that the relief capacity is above the inlet flow. This can be verified by comparing line 98 (actual flow) and line 108 (maximum theoretical flow).

**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only      10/18/91**

|    | A   | B  | C         | D                   |
|----|---|--|-----------|---------------------|
| 1  | Conversion of Liquid to Gas at Module Temp. |  |           | Units               |
| 2  | *> Bulk Temp. of Modules                    | 110  | 110       | K                   |
| 3  | > Max. Flow of Liquid Argon to Cryostat     | 12.3   | 12.3      | gpm                 |
| 4  | > Pressure in Cryostat                      | 19.75  | 19.75     | psig                |
| 5  | Pressure in Cryostat (conv.)                | $=(B4/14.696+1)*1.01325$                             | 2.375     | bars                |
| 6  | > lAr Density @ 2.2 bars                    | 1.342421   | 1.34      | g/cc                |
| 7  | > lAr Density @ 2.4 bars                    | 1.335861   | 1.34      | g/cc                |
| 8  | lAr Density @ 2.375 bars                    | $=(B5-2.2)/0.2*(B7-B6)+B6$                           | 1.337     | g/cc                |
| 9  | *> gAr Density @ 2.2 bars                   | 9.979  | 9.979     | mg/cc               |
| 10 | *> gAr Density @ 2.4 bars                   | 10.922   | 10.922    | mg/cc               |
| 11 | gAr Density @ 2.375 & Temp.                 | $=(B5-2.2)/0.2*(B10-B9)+B9$                          | 10.804    | mg/cc               |
| 12 | gAr Density @ 2.375 bars (conv.)            | $=B11/1000*62.428$                                   | 0.674     | lbm/ft <sup>3</sup> |
| 13 | Maximum Flow of Argon Gas                   | $=B3*B8/B11*1000$                                    | 1522      | gpm                 |
| 14 | Maximum Flow of Argon Gas (conv.)           | $=B13*0.13368$                                       | 203       | cfm                 |
| 15 | Air Equivalent Flow @STP                    | $=6.32*B17*356/B16*SQRT(B99/(520*B177*28.97))$       | 881       | scfm air            |
| 16 | Specific Heat Constant, C, for Ar           | $=520*SQRT(B168*(2/(B168+1))^{((B168+1)/(B168-1)))}$ | 381       |                     |
| 17 | Max. Mass Flow of Argon Gas                 | $=B14*B12*60$  | 8232      | lbm/hr              |
| 18 | *> Percent of Mass Flow to Relief Valve     | 1  | 1         |                     |
| 19 |   |  |           |                     |
| 20 | ΔP Across Relief Valve Inlet                |  |           | Units               |
| 21 | > Inner Pipe Diameter                       | 0.206  | 0.206     | ft                  |
| 22 | Inner Pipe Diameter (conv.)                 | $=B21*12$  | 2.472     | in                  |
| 23 | > Equivalent Length                         | 38   | 38        | ft                  |
| 24 | Ar Gas Density @ 2.375 & Temp.              | $=(B5-2.2)/0.2*(B10-B9)+B9$                          | 10.804    | mg/cc               |
| 25 | Ar Gas Density @ 2.375 bars (conv.)         | $=B24/1000*62.428$                                   | 0.674     | lbm/ft <sup>3</sup> |
| 26 | *> gAr Viscosity @ 2.4 bars & Temp.         | 0.0000909  | 0.0000909 | g/cm-s              |
| 27 | gAr Viscosity @ 2.4 bars (conv.)            | $=B26*100$   | 0.00909   | centipoise          |
| 28 | Max. Mass Flow to Relief Valve              | $=B17*B18$   | 8232      | lbm/hr              |
| 29 | Reynolds Number                             | $=6.31*B28/(B22*B27)$                                | 2310000   |                     |
| 30 | > Relative Roughness (e/D)                  | 0.0007   | 0.0007    |                     |
| 31 | Friction Factor Guess                       | $=0.25*(LOG(B30/3.7+5.74/(B29^0.9)))^{-2}$           | 0.0183    |                     |
| 32 | Friction Factor                             | $=0.25*(LOG(B30/3.7+2.51/(B29*B31^0.5)))^{-2}$       | 0.0182    |                     |
| 33 | Pressure Drop                               | $=0.00000336*B32*B23*(B28^2)/B25/(B22^5)$            | 2.531     | psi                 |
| 34 |   |  |           |                     |



**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only     10/18/91**

|    | A                                     | B   | C         | D          |
|----|---------------------------------------|---|-----------|------------|
| 35 | $\Delta P$ Across Rupture Disk Inlet  |   |           | Units      |
| 36 | Inner Pipe Diameter (conv.)           | =B37/12                                   | 0.172     | ft         |
| 37 | > Inner Pipe Diameter                 | 2.067                                     | 2.067     | in         |
| 38 | > Equivalent Length                   | 49  | 49        | ft         |
| 39 | gAr Density @ 2.375 & Temp.           | =(B5-2.2)/0.2*(B10-B9)+B9                 | 10.804    | mg/cc      |
| 40 | gAr Density @ 2.375 bars (conv.)      | =B39/1000*62.428                          | 0.674     | lbm/ft^3   |
| 41 | gAr Viscosity @ 2.4 bars              | =B26                                      | 0.0000909 | g/cm-s     |
| 42 | gAr Viscosity @ 2.4 bars (conv.)      | =B41*100                                  | 0.00909   | centipoise |
| 43 | Max. Mass Flow to Rupture Disk        | =B17*(1-B18)                              | 0         | lbm/hr     |
| 44 | Reynolds Number                       | =6.31*B43/(B37*B42)                       | 0         |            |
| 45 | > Relative Roughness (e/D)            | 0.0009                                    | 0.0009    |            |
| 46 | Friction Factor Guess                 | 0   | 0         |            |
| 47 | Friction Factor                       | 0   | 0         |            |
| 48 | Pressure Drop                         | 0   | 0         | psi        |
| 51 |                                       |   |           |            |
| 52 | $\Delta P$ Across Relief Valve Outlet |   |           | Units      |
| 53 | Inner Pipe Diameter (conv.)           | =B54/12                                   | 0.272     | ft         |
| 54 | > Inner Pipe Diameter                 | 3.26                                      | 3.26      | in         |
| 55 | > Equivalent Length                   | 51  | 51        | ft         |
| 56 | *> gAr Density @ 2.0 bar & Temp.      | 9.04                                      | 9.04      | mg/cc      |
| 57 | gAr Density @ 2.0 bar (conv.)         | =B56/1000*62.428                          | 0.564     | lbm/ft^3   |
| 58 | *> gAr Viscosity @ 2.0 bar & Temp.    | 0.0000907                                 | 0.0000907 | g/cm-s     |
| 59 | gAr Viscosity @ 2.0 bar (conv.)       | =B58*100                                  | 0.00907   | centipoise |
| 60 | Max. Mass Flow to Relief Valve        | =B28                                      | 8232      | lbm/hr     |
| 61 | Reynolds Number                       | =6.31*B60/(B54*B59)                       | 1760000   |            |
| 62 | > Relative Roughness (e/D)            | 0.00055                                   | 0.00055   |            |
| 63 | Friction Factor Guess                 | =0.25*(LOG(B62/3.7+5.74/(B61^0.9)))^2     | 0.0174    |            |
| 64 | Friction Factor                       | =0.25*(LOG(B62/3.7+2.51/(B61*B63^0.5)))^2 | 0.0173    |            |
| 65 | Pressure Drop                         | =0.00000336*B64*B55*(B60^2)/B57/(B54^5)   | 0.969     | psi        |
| 66 |                                       |   |           |            |

**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only      10/18/91**

|    | A   | B                            | C         | D          |
|----|---|------------------------------|-----------|------------|
| 67 | ΔP Across Rupture Disk Outlet             |                              |           | Units      |
| 68 | Inner Pipe Diameter (conv.)               | =B69/12                      | 0.18      | ft         |
| 69 | > Inner Pipe Diameter                     | 2.157                        | 2.157     | in         |
| 70 | > Equivalent Length                       | 1.75                         | 1.75      | ft         |
| 71 | gAr Density @ 2.0 bar & Temp.             | =B56                         | 9.04      | mg/cc      |
| 72 | gAr Density @ 2.0 bar (conv.)             | =B71/1000*62.428             | 0.564     | lbm/ft^3   |
| 73 | gAr Viscosity @ 2.0 bar & Temp.           | =B58                         | 0.0000907 | g/cm-s     |
| 74 | gAr Viscosity @ 2.0 bar (conv.)           | =B73*100                     | 0.00907   | centipoise |
| 75 | Max. Mass Flow to Rupture Disk            | =B43                         | 0         | lbm/hr     |
| 76 | Reynolds Number                           | =6.31*B75/(B69*B74)          | 0         |            |
| 77 | > Relative Roughness (e/D)                | 0.0009                       | 0.0009    |            |
| 78 | Friction Factor Guess                     | 0                            | 0         |            |
| 79 | Friction Factor                           | 0                            | 0         |            |
| 80 | Pressure Drop                             | 0                            | 0         | psi        |
| 81 |   |                              |           |            |
| 82 | Change in Gas at Common Outlet to Outside |                              |           | Units      |
| 83 | Pressure in Cryostat                      | =B4                          | 19.75     | psig       |
| 84 | Pressure in Cryostat (conv.)              | =(B83/14.696+1)*1.01325      | 2.375     | bars       |
| 85 | gAr Density @ 2.2 bars                    | =B9                          | 9.979     | mg/cc      |
| 86 | gAr Density @ 2.4 bars                    | =B10                         | 10.922    | mg/cc      |
| 87 | gAr Density @ 2.375 & Temp.               | =(B84-2.2)/0.2*(B86-B85)+B85 | 10.804    | mg/cc      |
| 88 | Temp. at Common Outlet                    | =(B2*B17+84*B189)/(B17+B189) | 100       | K          |
| 89 | > Pressure to Calculate Density           | 1.5                          | 1.5       | bars       |
| 90 | *> gAr Density @ 1.5 bars & New Temp.     | 7.458                        | 7.458     | mg/cc      |
| 91 | *> gAr Viscosity @ 1.5 bars & New Temp.   | 0.0000826                    | 0.0000826 | g/cm-s     |
| 92 | gAr Viscosity @ 1.5 bar (conv.)           | =B91*100                     | 0.00826   | centipoise |
| 93 |   |                              |           |            |

**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only 10/18/91**

|     | A                                       | B   | C      | D      |
|-----|---|---|--------|--------|
| 94  | ΔP Across Relief Valve                  |   |        | Units  |
| 95  | > Critical Ratio (Pcr/P1) for Argon     | 0.487   | 0.487  |        |
| 96  | > Specific Heat Ratio (k) for Argon     | =B168   | 1.72   |        |
| 97  | > Area of 2" x 3" Relief Valve          | 2.29  | 2.29   | in^2   |
| 98  | Flow Through Relief Valve               | =B28  | 8232   | lbm/hr |
| 99  | Flowing Temperature                     | =1.8*B2   | 198    | deg R  |
| 100 | > Compressibility Factor                | 1   | 1      |        |
| 101 | > Nozzle Coefficient for type 93T       | 0.939   | 0.939  |        |
| 102 | Flowing Inlet Pressure (P1)             | =B4+14.696-B33  | 31.91  | psia   |
| 103 | > Molecular Weight of Argon             | 39.948  | 39.95  | g/mol  |
| 104 | Critical Pressure (Pcr)                 | =B95*B102   | 15.54  | psia   |
| 105 | Outlet Pressure (P2) (using delta p's)  | =14.696+B154+B133+B65                                     | 21.22  | psia   |
| 106 | Pressure Ratio (P2*/P1)                 | =(B102-0.55*((B102-B105)^0.98))/B102                      | 0.824  |        |
| 107 | Theoretical Factor (F*) (using P2)      | =SQRT(((B96/(B96-1))*((B106^(2/B96)-B106^((B96+1)/B96)))) | 0.385  |        |
| 108 | Max. Theoretical Relief Flow (using F*) | =735*B97*B101*B102*B107*SQRT(B103/B99/B100)               | 8723   | lbm/hr |
| 109 | Theoretical Percent of Relief Flow      | =B108/B17   | 1.0596 |        |
| 110 | Pressure Drop Across Relief Valve       | =B102-B105  | 10.69  | psi    |
| 111 |   |   |        |        |

**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only 10/18/91**

|     | A   | B   | C          | D          |
|-----|---|---|------------|------------|
| 112 | ΔP Across Common Outlet to Platform Bayonet |   |            | Units      |
| 113 | > Inner Pipe Diameter                       | 0.355   | 0.355      | f t        |
| 114 | Inner Pipe Diameter (conv.)                 | =B113*12                                      | 4.26       | in         |
| 115 | > Equivalent Length                         | 273   | 273        | f t        |
| 116 | gAr Density @ 1.5 bar & New Temp.           | =B90  | 7.458      | mg/cc      |
| 117 | gAr Density @ 1.5 bar (conv.)               | =B116/1000*62.428                             | 0.466      | lbm/ft^3   |
| 118 | *> gN2 Gas Density @ 1.5 bar & New Temp.    | 4.76381                                       | 4.764      | mg/cc      |
| 119 | gN2 Gas Density @ 1.5 bar (conv.)           | =B118/1000*62.428                             | 0.297      | lbm/ft^3   |
| 120 | Gas Mixture Density @1.5 bar                | =(B17*B117+B127*B119)/B128                    | 0.403      | lbm/ft^3   |
| 121 | gAr Viscosity @ 1.5 bar & New Temp.         | =B91  | 0.0000826  | g/cm-s     |
| 122 | gAr Viscosity @ 1.5 bar (conv.)             | =B121*100                                     | 0.00826    | centipoise |
| 123 | *> gN2 Viscosity @ 1.5 bar & New Temp.      | 0.00007488                                    | 0.00007488 | g/cm-s     |
| 124 | gN2 Viscosity @ 1.5 bar (conv.)             | =B123*100                                     | 0.007488   | centipoise |
| 125 | Mixture Viscosity @1.5 bar                  | =(B17*B122+B127*B124)/B128                    | 0.007973   | centipoise |
| 126 | Max. Mass Flow of Argon Gas                 | =B17  | 8232       | lbm/hr     |
| 127 | Max. Flow of Nitrogen Gas                   | =B189   | 4861       | lbm/hr     |
| 128 | Mass Flow of Mixture                        | =B126+B127                                    | 13093      | lbm/hr     |
| 129 | Reynolds Number                             | =6.31*B128/(B114*B125)                        | 2430000    |            |
| 130 | > Relative Roughness (e/D)                  | 0.0004  | 0.0004     |            |
| 131 | Friction Factor Guess                       | =0.25*(LOG(B130/3.7+5.74/(B129^0.9)))^-2      | 0.0162     |            |
| 132 | Friction Factor                             | =0.25*(LOG(B130/3.7+2.51/(B129*B131^0.5)))^-2 | 0.0161     |            |
| 133 | Pressure Drop                               | =0.00000336*B132*B115*(B128^2)/B120/(B114^5)  | 4.489      | psi        |
| 134 |   |   |            |            |

**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only      10/18/91**

|     | A                                     | B   | C          | D          |
|-----|---------------------------------------|---|------------|------------|
| 135 | ΔP from Platform Bayonet to Outside   |   |            | Units      |
| 136 | > Inner Pipe Diameter                 | 0.53  | 0.53       | ft         |
| 137 | Inner Pipe Diameter (conv.)           | =B136*12                                      | 6.36       | in         |
| 138 | > Equivalent Length                   | 516   | 516        | ft         |
| 139 | gAr Gas Density @ 1.5 bar & New Temp. | =B90  | 7.458      | mg/cc      |
| 140 | gAr Gas Density @ 1.5 bar (conv.)     | =B139/1000*62.428                             | 0.466      | lbm/ft^3   |
| 141 | gN2 Gas Density @ 1.5 bar & New Temp. | =B118   | 4.764      | mg/cc      |
| 142 | gN2 Gas Density @ 1.5 bar (conv.)     | =B141/1000*62.428                             | 0.297      | lbm/ft^3   |
| 143 | Gas Mixture Density @1.5 bar          | =(B17*B140+B189*B142)/B149                    | 0.403      | lbm/ft^3   |
| 144 | gAr Viscosity @ 1.5 bar & New Temp.   | =B121   | 0.0000826  | g/cm-s     |
| 145 | gAr Viscosity @ 1.5 bar (conv.)       | =B144*100                                     | 0.00826    | centipoise |
| 146 | gN2 Viscosity @ 1.5 bar & New Temp.   | =B123   | 0.00007488 | g/cm-s     |
| 147 | gN2 Viscosity @ 1.5 bar (conv.)       | =B146*100                                     | 0.007488   | centipoise |
| 148 | Gas Mixture Viscosity @1.5 bar        | =(B17*B145+B189*B147)/B149                    | 0.007973   | centipoise |
| 149 | Max. Mass Flow of Gas Mixture         | =B128   | 13093      | lbm/hr     |
| 150 | Reynolds Number                       | =6.31*B149/(B137*B148)                        | 1630000    |            |
| 151 | > Relative Roughness (e/D)            | 0.00027                                       | 0.00027    |            |
| 152 | Friction Factor Guess                 | =0.25*(LOG(B151/3.7+5.74/(B150*0.9)))^-2      | 0.0152     |            |
| 153 | Friction Factor                       | =0.25*(LOG(B151/3.7+2.51/(B150*B152^0.5)))^-2 | 0.0151     |            |
| 154 | Pressure Drop                         | =0.00000336*B153*B138*(B149^2)/B143/(B137^5)  | 1.07       | psi        |
| 155 |                                       |   |            |            |
| 156 | Summation of Equivalent ΔPs           |   |            | Units      |
| 157 | Relief Valve Inlet Pressure Drop      | =B33  | 2.531      | psi        |
| 158 | Relief Valve Outlet Pressure Drop     | =B65  | 0.969      | psi        |
| 159 | Relief Valve Pressure Drop            | =19.75-B157-(B165+B164+B158)                  | 10.69      | psi        |
| 160 | Relief Valve/Disk Branch              | =B33+B65+B110                                 | 14.19      | psi        |
| 161 | Rupture Disk Inlet Pressure Drop      | =B48  | 0          | psi        |
| 162 | Rupture Disk Outlet Pressure Drop     | =B80  | 0          | psi        |
| 163 | Rupture Disk Pressure Drop            | 0   | 0          | psi        |
| 164 | Common Outlet Pressure Drop           | =B133   | 4.489      | psi        |
| 165 | Platform to Outside Pressure Drop     | =B154   | 1.07       | psi        |
| 166 |                                       |   |            |            |

**Maximum Module Temperature - Lar Dewar to ECN - Relief Valve Only 10/18/91**

|     | A                                       | B   | C       | D        |
|-----|---|---|---------|----------|
| 167 | ΔP Across Rupture Disk                  |   |         | Units    |
| 168 | *>Argon Specific Heat Ratio (k)         | 1.7186  | 1.7186  |          |
| 169 | Critical Ratio                          | $=(2/(B168+1))^{(B168/(B168-1))}$                       | 0.48    |          |
| 170 | > Area of 3" Rupture Disk               | $=3.14159*(3^2)/4$                                      | 7.069   | in^2     |
| 171 | Flow Through Rupture Disk               | =B43  | 0       | lbm/hr   |
| 172 | Flowing Temperature                     | =1.8*B2   | 198     | deg R    |
| 173 | > ASME Coefficient (K)                  | 0.62  | 0.62    |          |
| 174 | Pressure Ratio (Pe/Po)                  | =B179/B176  | 0.588   |          |
| 175 | gAr Flow Constant for Subsonic Flow(C1) | $=SQRT(2*32.2/1545*(B168/(B168-1))*(B174^(2/B168)-B174$ | 0.103   |          |
| 176 | Flowing Inlet Pressure (Po)             | =B4+14.696-B48  | 34.45   | psia     |
| 177 | > Molecular Weight of Argon             | 39.948  | 39.948  | g/mol    |
| 178 | Critical Pressure (Pcr)                 | =B169*B176  | 16.53   | psia     |
| 179 | Outlet Pressure (Pe) (using delta p's)  | =14.696+B154+B133+B80                                   | 20.26   | psia     |
| 180 | Pressure Drop Across Rupture Disk       | 0   | 0       | psi      |
| 181 | Maximum Theoretical Rupture Disk Flow   | =B170*B173*B175*B176*SQRT(B177/B172)*60*60              | 25250   | lbm/hr   |
| 182 | Actual Rupture Disk Flow                | =B43  | 0       | lbm/hr   |
| 183 |   |   |         |          |
| 184 | Maximum Flow from Condensers            |   |         | units    |
| 185 | > Max. Flow of Liquid Nitrogen          | 13  | 13      | gpm      |
| 186 | Max. Flow of Liquid Nitrogen (conv.)    | =B185/7.48  | 1.74    | ft^3/min |
| 187 | Density of LN2 @ 3.5 atm                | 0.747   | 0.747   | g/cc     |
| 188 | Density of LN2 (conv.)                  | =B187*62.4  | 46.6128 | lbm/ft^3 |
| 189 | Mass Flow of LN2                        | =B186*B188*60   | 4861    | lbm/hr   |