

1 **Heterogeneous fatigue damage in a nickel-based single-crystal**

2 **superalloy unraveled using correlative 3D X-ray technology**

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Heterogeneous fatigue damage in a nickel-based single-crystal superalloy unraveled using correlative 3D X-ray technology

Abstract

Nickel-based single-crystal (Ni-SX) superalloys under cyclic stress are susceptible to cracking at stress-concentration sites, eventually leading to low-cycle fatigue (LCF) failure. LCF cracks typically originate from intrinsic defects (e.g., voids and carbides) within solidified dendrites. However, systematic quantitative experimental analyses of defect-mediated local damage remain limited. To thoroughly understand the microscopic origins and evolution of LCF damage, correlated 3D mapping of dendrites across various regions is essential. Here, macroscale micro-computed tomography (μ -CT) was initially used to capture internal interdendritic secondary cracks within bulk DD413 superalloy after LCF testing at 760 °C. Subsequently, a multimodal methodology combining synchrotron 3D microdiffraction (3D- μ XRD), high-resolution μ -CT, and electron microscopy was established. This approach allowed precise localization of internal damage zones near interdendritic secondary cracks and detailed mapping of the 3D correlated distributions of dendrites, defects, and residual stress/strain fields within these zones at submicron spatial resolution. Finally, the same approach was applied to specimens subjected to interrupted loading at approximately 40% of the fatigue life to uncover the early damage states of dendrites. The dendrite cores (DCs) and interdendritic regions (IDs) exhibit microscale heterogeneous mechanical responses: nearly defect-free DCs accumulate local irreversible slip along specific slip systems to generate slip bands, while the IDs containing various defects accommodate local microplasticity through the activation of multiple slip systems around these defects. The local tensile stress near defects in the IDs exceeds that in the DC slip band regions by more than threefold, leading to the generation of local damage zones within the IDs. Chain-like defect distributions facilitate the interconnection of these local zones into a continuous damage region, further elevating the overall tensile stress in the IDs. Additionally, geometrically necessary dislocations alone are insufficient as indicators of LCF damage; both the internal stress state and its magnitude must be considered. These experimental results provide critical data and insights for the development of multi-physics fatigue models.

Keywords: Ni-based superalloy; Synchrotron microdiffraction; Low-cycle fatigue; X-ray microscopy; Localized deformation

48 **1. Introduction**

49 Nickel-based single-crystal (Ni-SX) superalloys achieved through directional solidification have been
50 widely used in advanced aerospace engines and industrial gas turbine blades due to their significantly
51 enhanced fatigue resistance, which benefits from the lack of high-temperature slip-prone grain
52 boundaries [1-3]. As demands for higher turbine performance and thermal efficiency increase, the high-
53 temperature endurance of turbine blades faces ever more stringent challenges. The addition of refractory
54 elements such as Mo, W, and Re has been shown to enhance the high-temperature capabilities of
55 superalloys [3-5]. However, due to their low diffusion rates and high atomic mass, these elements
56 intensify the disparity in solidification characteristics between dendrite cores (DCs) and interdendritic
57 regions (IDs) during Bridgman solidification, inevitably leading to microstructural heterogeneity [6, 7].
58 Solidified DCs generally exhibit a regular γ/γ' microstructure enriched with W, Mo, and Re, while IDs
59 are characterized by a coarser irregular γ/γ' microstructure with segregated elements (primarily Ti, Ta,
60 and Al) as well as most intrinsic defects, such as carbide inclusions, micropores, and residual eutectics
61 [8]. The conventional heat treatments are still insufficient in fully eliminating the dendrite-scale
62 microstructural heterogeneity, and such heterogeneity can greatly complicate the micromechanical
63 response of the alloy under cyclic loading. The accuracy of structural integrity assessments for critical
64 components is thus not guaranteed.

65 Intermediate-temperature low-cycle fatigue (LCF) failure poses a significant risk to the safe and
66 reliable operation of aerospace engines [9-13]. Studies have demonstrated that intermediate-temperature
67 LCF failure in Ni-SX superalloys is closely linked to intrinsic defects retained in solidified dendrite
68 structures, which act as stress singularities that trigger localized microplasticity and initiate fatigue cracks
69 [9, 10, 14-17]. The complex interactions among multiple defects within IDs complicate local irreversible
70 plastic deformation processes, resulting in considerable variability in LCF life [18-21]. However,
71 conventional macroscopic theories struggle to explain the microscopic heterogeneous LCF deformation
72 phenomena [9, 10, 22], such as defect-mediated stress concentrations, lattice rotations, and dislocation
73 pile-ups, highlighting the need for cross-scale investigations to uncover the underlying micromechanisms.
74 Furthermore, the local three-dimensional (3D) stress/strain distributions and their evolution during LCF
75 loading remain unclear, as conventional characterization approaches cannot non-destructively capture
76 residual strains triggered by heterogeneous deformation. LCF loading induces dislocation self-
77 organization and pile-ups, forming persistent or planar slip bands (PSBs/PLBs) that generate

78 inhomogeneous stress fields and cause lattice rotations [13, 23]. These effects significantly raise the
79 stored energy density in certain slip systems, facilitating damage and crack initiation [24]. To accurately
80 predict and discern microscale fatigue damage, it is crucial to first reveal the stress distributions applied
81 during cyclic loading and the resulting strains. While macroscopic residual strains have been
82 experimentally measured [25], the distribution of local residual strains within DCs and defect-rich IDs
83 during LCF loading remains unknown.

84 In aviation, frequent inspections and proactive replacements help mitigate the effects of fatigue failure
85 to ensure operation safety. These conservative maintenance routines are however often costly and
86 inefficient. The widely adopted damage tolerance design principles offer a more efficient alternative [26],
87 which integrates non-destructive probes with fatigue fracture theory to ascertain the pre-critical growth
88 rates of embryonic cracks, establishing reliable failure criteria for precise residual strength assessment
89 and inspection intervals [27]. To achieve this, researchers need to thoroughly detect microcracks within
90 in-service components and perform quantitative analyses of the surrounding crystallographic information,
91 typically on a 3D scale. Particular attention is given to gradients in lattice curvature (indicative of the
92 plastic state) and lattice strain (elastic strain along a given crystallographic direction which is reflective
93 of the internal stress state), as these factors can reflect the evolution of local micromechanical fields and
94 serve as critical indicators for predicting microcrack propagation trends [23].

95 Accurately revealing crystallographic information within specific regions of bulk fatigued Ni-SX
96 superalloys remains challenging with conventional characterization methods. Neutron and standard X-
97 ray diffraction techniques only provide averaged volume information due to their millimeter or
98 submillimeter spatial resolution [28-31]. The latest high-resolution electron backscatter diffraction (HR-
99 EBSD) provides the high angular and spatial resolution necessary for surface strain analysis but typically
100 relies on focused ion beam (FIB) serial sectioning for 3D-scale analysis, a process that unavoidably
101 induces stress relaxation [32, 33]. More critically, the absence of a 3D perspective introduces
102 considerable uncertainty when studying microcrack propagation in relation to structural features.
103 Achieving a high spatial and angular resolution to non-destructively uncover crystallographic details
104 within targeted regions of bulk fatigued Ni-SX superalloys is also a challenge for the present study.

105 In recent years, various 3D X-ray techniques have become increasingly integral to materials research,
106 enabling non-destructive, spatially resolved analysis of microstructures within materials for a deeper

107 understanding of their structure and properties. Notable examples include X-ray computed tomography
108 (X-CT) [34], 3D X-ray microdiffraction (3D- μ XRD) [35], diffraction contrast tomography (DCT) [36],
109 and dark-field X-ray microscopy (DFXM) [37]. Among these, synchrotron-based 3D- μ XRD offers both
110 high spatial (< 500 nm) and angular ($< 0.01^\circ$) resolution, making it ideal for capturing ultra-low-strain
111 deformation and stress localization within bulk metals [38]. Nevertheless, the structural heterogeneity,
112 complex internal stress states, and localized fatigue damage in Ni-SX superalloys complicate diffraction
113 signal analysis in 3D- μ XRD, potentially reducing result reliability and risking the omission of critical
114 features. X-CT with micro- or sub-micron resolution (μ -CT) offers high efficiency and broader coverage
115 and has been proven effective for detecting intrinsic defects and microcracks in bulk metals [38, 39]. As
116 such, μ -CT can guide 3D- μ XRD measurements to ensure critical features are captured and assist in
117 distinguishing and analyzing internal diffraction signals. The combined use of the two 3D X-ray
118 techniques enables precise localization of fatigue-sensitive zones and provides reliable insights into
119 microscopic deformation mechanisms.

120 In this study, we present the submicron-scale 3D correlative distributions of residual stress/strain fields,
121 dendritic microstructures, defects, and dislocation configurations in Ni-SX superalloys subjected to
122 intermediate-temperature LCF loading. This work aims to elucidate the heterogeneous fatigue damage
123 mechanisms within monocrystalline dendritic structures, providing a detailed description of defect-
124 mediated incompatible deformation and quantitatively confirming the mechanical heterogeneity between
125 DCs and IDs. A novel multimodal analytical framework that integrates synchrotron 3D- μ XRD and μ -CT
126 techniques with submicron spatial resolution has been strategically established. This correlative approach
127 enables precise acquisition, subdivision, and integration of crystallographic orientations and elastic
128 strains within target regions of bulk Ni-SX superalloys, facilitating accurate localization and
129 quantification of internal damage in cast alloys with solidification dendritic structures. This study
130 significantly deepens our understanding of the microscopic origins and progression of embryonic crack
131 nucleation and subcritical growth driven by stress/strain localization around defects under intermediate-
132 temperature LCF loading, underscoring its fundamental scientific and practical importance.

133 **2. Experiment**

134 2.1. Material description and fatigue test

135 The nominal composition of the DD413 alloy is listed in Table 1. DD413 rods with a diameter of 16 mm

136 were directionally solidified along the [001] orientation using the spiral grain selection method in a
137 vacuum directional solidification furnace (Bridgeman process). A two-stage solution heat treatment was
138 applied (1230 °C for 2 hours followed by 1250 °C for 4 hours), followed by a precipitation hardening
139 treatment at 1080 °C for 4 hours. The primary misorientations of the single-crystal rod axes relative to
140 the [001] orientation were determined via EBSD, and rods with deviations within 5° were selected for
141 further fatigue testing. The cylindrical dog-bone shape specimens machined from the heat-treated rods
142 were prepared with a gauge length of 14 mm and a diameter of 6 mm. Before testing, mechanical and
143 electrochemical polishing were conducted to eliminate surface-machined scratches and work hardening
144 inherited from the machining process to avoid any possible recrystallization during fatigue straining.
145 Fatigue tests were conducted at 760 °C under total strain control of $\Delta\varepsilon/2 = 1.1\%$ along the [001]
146 orientation using a servo-hydraulic testing machine (MTS Series 809 A/T). A triangular waveform at a
147 constant strain rate of $5 \times 10^{-3} \text{ s}^{-1}$ and a strain ratio of $R = -1$ was utilized, with total strain monitored
148 by an extensometer on the specimen ledges. Temperature fluctuations across the gauge length were
149 maintained within $\pm 3 \text{ }^\circ\text{C}$. Tests were performed to failure, with additional interruptions at approximately
150 40% of the expected lifespan. Completed samples were air-cooled to room temperature under a constant
151 10 MPa load. Four specimens were tested on the same machine to ensure data stability and minimize
152 equipment-induced variance. Further details on the alloy microstructure and LCF damage at different
153 strain amplitudes are available in Ref. [8].

154 2.2. Micro-computed tomography

155 μ -CT scans were acquired using an X-ray microscope (XRM, YXLON FF35CT) operating at 180 kV,
156 achieving a voxel resolution of $3.86 \times 3.86 \times 3.86 \text{ }\mu\text{m}^3$. A rod sample with a 3 mm diameter was extracted
157 from the middle of the gauge section of the failed specimen. X-ray projection images were recorded with
158 an exposure time of 1.2 seconds per image, typically capturing 1801 images during a stepwise specimen
159 rotation. The acquired data were reconstructed using VG Studio Max to reduce noise and enable 3D
160 visualization, while Avizo software was used to segment microcracks and intrinsic defects via grayscale
161 thresholding for further analysis. Longitudinal projection images parallel to the loading direction were
162 generated from the reconstructed dataset to highlight key fatigue cracking features. The selected cross-
163 section was meticulously positioned and manually ground to expose it for subsequent inspections.
164 Vickers indentations ($\sim 15 \text{ }\mu\text{m}$) were used to mark the start and endpoints of a transverse synchrotron scan

165 and indicated the X-ray penetration direction. The marked region was subsequently identified using a
166 field emission gun scanning electron microscope (FEG-SEM, Zeiss Gemini 450) at 20 kV, with a 20-
167 minute surface irradiation that caused minimal damage (a few nanometers) to create visible markers. A
168 thin slice sample ($1 \times 1 \times 0.5 \text{ mm}^3$) was then extracted using electric discharge machining, positioning
169 the burned area near the sample center. High-resolution μ -CT scans of the extracted slice were conducted
170 with an XRM (Zeiss Xradia 620 Versa) at 140 kV, achieving a voxel resolution of $1.18 \times 1.18 \times 1.18$
171 μm^3 . The sample was mounted using an aluminum tube adapter and rotated 360° with discrete angle
172 pauses for 2D projection imaging, capturing 991 exposures at 1 second each. Data were reconstructed
173 using ORS Dragonfly software, and Avizo was utilized for visualization and data registration. Noise
174 reduction was accomplished using median filtering [40], with data points smaller than two voxels
175 excluded during threshold segmentation to enhance clarity and accuracy.

176 2.3. Electron microscopy

177 EBSD scans were conducted using an FEG-SEM (Zeiss Gemini 450) equipped with a CMOS
178 symmetry EBSD detector, operating at 20 kV with step sizes of 0.2 to 1.0 μm . Analyses of orientations,
179 slip traces, and geometrically necessary dislocations (GNDs) were performed using AZtecCrystal
180 software and custom MATLAB code based on the MTEX toolbox [41]. Specimen preparation involved
181 meticulous mechanical grinding followed by vibration polishing. For a detailed examination of the
182 microstructure and dislocation configurations, imaging was performed using a bright-field (BF) detector
183 (scattering angle: 9 mrad) and a low-angle annular dark-field (LAADF) detector (DF2, scattering angle:
184 12~19 mrad) on a 200 kV scanning transmission electron microscope (STEM, FEI Talos F200X). Thin
185 foils near the crack tip were prepared using a dual-beam FIB instrument (FEI Helios Nano Lab 600i). A
186 1.0 μm platinum protective layer was deposited with a 12 kV ion beam to safeguard the cross-sectional
187 surface. The thinning process was optimized by first using a high-energy ion beam (30 kV), followed by
188 a low-energy ion beam (2 kV) to remove any amorphous regions, yielding final lamellae approximately
189 80 nm thick. Additional electro-polishing was carried out using a twin-jet polisher with a solution of 10%
190 perchloric acid and 90% ethanol at -30°C and 30 V.

191 2.4. Three-dimensional X-ray microdiffraction

192 The 3D- μ XRD measurements were performed at beamline 34-ID-E of the Advanced Photon Source,
193 Argonne National Laboratory (APS, ANL), US. A polychromatic X-ray beam with energies ranging from

194 7 to 30 keV was focused into a $0.3 \mu\text{m} \times 0.3 \mu\text{m}$ spot using a Kirkpatrick-Baez mirror pair. Overlapping
195 Laue diffraction patterns, generated by the penetration of the X-ray beam through the specimen, were
196 recorded on a 2048×2048 pixel Perkin-Elmer area detector (pixel size: $200 \mu\text{m} \times 200 \mu\text{m}$) positioned
197 0.5 m above the sample in a 90° reflection geometry. Depth resolution was achieved by scanning a 100-
198 μm -diameter platinum wire across the sample surface, serving as a differential aperture. Triangulation
199 enabled the identification of diffracted rays, providing a depth resolution of $0.5 \mu\text{m}$. A horizontal X-ray
200 line scan was performed approximately 4 mm from the fatigue crack region and perpendicular to the
201 loading direction, covering a scanning length of $400 \mu\text{m}$ with a step size of $1.0 \mu\text{m}$, reaching a penetration
202 depth of about $100 \mu\text{m}$. Slices inclined at a 45° angle to the specimen surface were measured via depth-
203 resolved line scanning. An additional horizontal scan was conducted near the gauge section midpoint of
204 a specimen at $\sim 40\%$ of its fatigue life, covering $250 \mu\text{m}$ with $1 \mu\text{m}$ steps. Depth reconstruction and
205 indexing of Laue patterns were completed at APS using the LaueGo software. Post-processed
206 crystallographic data, including crystallographic orientations, grain boundaries, GND densities, slip
207 traces, and elastic strain components [42], were analyzed using in-house MATLAB code. High-angle
208 grain boundaries (HAGBs) were defined with a misorientation threshold of 10° , and kernel average
209 misorientation (KAM) was evaluated using a 3×3 kernel size with a 2° cut-off angle. The minimum
210 total GND densities were calculated following methodologies proposed by Pantleon [43] and Muránsky
211 [44]. Potential variations in lattice rotation gradients perpendicular to the scan surface were disregarded,
212 and the calculation relied on the minimum line energy criterion. Despite the influence of elastic strain
213 gradients on Nye's dislocation tensor [45], the magnitude of the lattice curvature change induced by it is
214 considerably lower than that resulting from the measured rotation gradients. Thus, GND densities were
215 derived from the six available rotation gradients [46]. Denoising of crystal orientation maps was
216 performed using variational methods [47]. The elastic strain gradients, calculated similarly to KAM,
217 were assigned to the central pixel based on the average differences among neighboring pixels within a 3
218 $\times 3$ kernel. The mean reference orientation deviation angle (MROD- ω) was calculated as the
219 misorientation between each pixel's orientation and the average orientation of all pixels. Lattice rotation
220 axes for MROD- ω were visualized on a color-mapped sphere representing the specimen frame, with
221 separate color keys for the upper and lower hemispheres.

222 **3. Results**

223 3.1. Fatigue microcracking

224 Supplementary Fig. S1 presents the tension-compression LCF curve of the DD413 alloy at 760 °C under
225 $\pm 1.1\%$ strain control with the loading direction along the [001] crystallographic axis. The specimen
226 initially exhibited strain hardening for the starting 10 cycles, followed by cyclic softening until failure
227 after 268 cycles. Additional tests were interrupted at 98 cycles (corresponding to 40% fatigue lifetime)
228 to investigate early-stage fatigue damage. As shown in Fig. 1, a miniature sample was extracted from the
229 gauge section (starting at the fracture surface) of a post-mortem dog-bone-shaped specimen subjected to
230 268 cycles to enhance spatial resolution during μ -CT imaging. Carbide inclusions in the extracted
231 specimen display a regular chain-like distribution at specific intervals, primarily situated in IDs. Two
232 zig-zag secondary cracks extending from the fracture surface into the interior were also captured (Fig.
233 1). A detailed comparison between the magnified crack path and the distribution trajectory of chain-like
234 intrinsic defects reveals that the crack initially propagated along the right-side ID before deflecting
235 toward the left ID, as indicated by orange dashed lines in Fig. 1. These 3D observations offer a more
236 reliable identification of microstructural components or regions in DD413 alloys prone to damage
237 accumulation and cracking under LCF loading.

238 The reconstructed miniature specimen was sectioned at 4 μm intervals along the X-Y plane to show
239 the secondary cracks and microstructural features, as displayed in Fig. 2. A selected tomography slice
240 reveals crack growth characteristics along chain-like intrinsic defects, where white particles represent
241 carbide inclusions and black microregions correspond to micropores (Fig. 2). This slice was located and
242 carefully polished for EBSD characterization, with the inverse pole figure (IPF), MROD- ω , and GND
243 density maps presented in Fig. 3a-e. Low-angle grain boundaries (LAGBs) are evident in the IDs where
244 the two cracks are situated (Fig. 3a), alongside a notable increase in MROD- ω (Fig. 3b). The microcrack
245 growth path follows the trace of an FCC {111} crystallographic plane, marked by the black dashed line
246 in Fig. 3c. Randomly oriented carbide inclusions are observed to the right of the crack path.

247 Near the microcrack, LAGBs and high-density GNDs extend alongside the crack path to its tip before
248 deflecting toward two carbides approximately 30 μm apart, suggesting a potential trend for further
249 microcrack propagation (Fig. 3d and e). Supplementary Fig. S2 provides additional details of the fatigue
250 crack regions, highlighting two critical features: (i) the presence of carbides at the crack path deflection
251 sites and (ii) an MROD- ω increase of over 2° near these carbides, underscoring their significant role in
252 microcrack initiation and propagation under LCF. Contrasting to the ID where the fatigue crack originates,

253 the neighboring defect-free DC exhibits minimal microplasticity (Fig. 3e). It is necessary to note that
254 EBSD provides only a conservative estimate of dislocation density [43, 44], as it cannot measure
255 statistically stored dislocations (SSDs) that contribute to strain hardening, nor can it visualize dislocation
256 configurations. TEM foils were further prepared from specific sites of the DC and ID, as displayed in
257 Fig. 3d. Location A in the DC reveals a lower dislocation density, consistent with EBSD results, with
258 most dislocations confined to the softer γ channels instead of shearing the γ' phase (Fig. 3f and g). In
259 contrast, location B within the ID shows a higher dislocation density near the carbide, where dislocation
260 entanglements in the γ channels begin to shear the γ' phase, as displayed in Fig. 3h and i. These findings
261 highlight the local stress variations due to inconsistent micromechanical responses of DCs and IDs under
262 LCF loading, manifesting as dislocation entanglements in the γ channels and slip activity within the γ'
263 ordered phases [48].

264 3.2. Lattice orientation field in fatigued microstructures

265 The correlative 3D X-ray microscopy integrating 3D- μ XRD and μ -CT was employed to analyze lattice
266 rotation and elastic strain in fatigued microstructures within a 1.5 mm thickness specimen containing the
267 selected slice (Fig. 3a), positioned approximately 4 mm from the fatigue crack region (Fig. 4a). A
268 transverse 3D- μ XRD scan was conducted at a 45° angle to the specimen surface, spanning ~ 400 μ m
269 along the X direction (penetrating ~ 100 μ m) and oriented perpendicular to the loading axis (Fig. 4a).
270 Post-processing of Laue patterns at different depths revealed three void regions without diffraction
271 signals, identified as micropores (Supplementary Fig. S3c), with one representative Laue pattern shown
272 at point 2 in Supplementary Fig. S4. A high-resolution μ -CT scan of a $1 \times 1 \times 0.5$ mm³ region surrounding
273 the synchrotron scan trace aided in analyzing diffraction signals. The identification, labeling, and
274 extraction of this trace for high-resolution μ -CT imaging are detailed in Supplementary Fig. S3a and b.
275 Two-dimensional (2D) slices from the reconstructed high-resolution μ -CT dataset aligned with the
276 penetration direction and depth of the 3D- μ XRD scan were generated for data registration, identifying
277 the 3D- μ XRD scanning range within the bulk interior based on spatial distances among the three voids,
278 as displayed in Supplementary Fig. S3c. The range spanned three IDs and two DCs from left to right
279 (outlined by black dashed lines on the transparent cross-section in Fig. 4b), with voids 1, 2, and 3 located
280 within the IDs. The 3D morphology of the three microvoids shows considerable size variation (Fig. 4c),
281 and minor deviations in slicing angle may cause discrepancies in void morphology on the 2D slices, as

282 illustrated in Supplementary Fig. S3c.

283 Fig. 5a-e presents a series of maps depicting lattice orientation derived from Laue patterns after depth
284 reconstruction. By estimating the proportions of DCs and IDs in the μ -CT slices shown in Fig. 4b, the
285 IPF-Y map within a $\sim 1^\circ$ range (Sharp-IPF-Y) was subdivided along black dashed lines, unveiling notable
286 lattice orientation fluctuations within the three IDs (ID1, ID2, and ID3), whereas the two DCs (DC1 and
287 DC2) displayed homogeneous lattice orientations (Fig. 5a). In the IDs, localized zones exhibit
288 misorientations exceeding 10° (indicated by gray HAGBs), possibly associated with MC-type carbide
289 inclusions (Fig. 5a). TEM analysis confirmed that most carbide inclusions in this alloy share the Fm-3m
290 space group with the Ni phase (Supplementary Fig. S5), allowing them to be indexed, but their Laue
291 patterns are markedly distinct from those of the matrix (Supplementary Fig. S4). Detailed
292 crystallographic parameters for both the carbides and the matrix are summarized in Table 2. The GND
293 density in ID1 through ID3 is notably elevated due to carbide inclusions, reaching values up to 1.1×10^{14}
294 m^{-2} between two carbides in ID1, suggesting the role of carbide clusters in accommodating plastic
295 deformation within the surrounding matrix (Fig. 5b). In contrast, DC1 and DC2 display low and uniform
296 GND density values, with DC1 recording a lowest value of only $1.7 \times 10^{12} \text{ m}^{-2}$, indicating homogeneous
297 deformation in these regions (Fig. 5b).

298 Fig. 5c and e depict the MROD- ω map and rotation axis map generated with high angular resolution
299 via 3D- μ XRD technology, indicating the lattice rotation distinctions between the DCs and IDs. MROD-
300 ω values are consistently low and uniform in DCs, ranging from 0.16° to 0.22° (Fig. 5c). In contrast, IDs
301 show notable fluctuations with high (exceeding 1°) and low (below 0.1°) rotation angles concentrating
302 and departing from intrinsic defects (Fig. 5c). The derivative of MROD- ω along the X-direction (Fig. 5d)
303 further provides a quantitative assessment of the plastic deformation gradient within the analyzed region
304 (highlighted by the transparent white area in Fig. 5c), revealing that ID2 and ID1 which are closest
305 and furthest to intrinsic defects displays the sharpest and moderate plastic deformation gradients,
306 and ID3 falls in between (Fig. 5c and d). Both defect-free DCs show only minor gradients, indicating
307 that regions closer to intrinsic defects undergo more heterogeneous deformation for local mechanical
308 accommodation (Fig. 5c and d).

309 Fig. 5e presents a rotation axis map where each spot signifies a specific axis on a colored sphere
310 corresponding to MROD- ω in the specimen frame. Consistent coloring in DC1 and DC2 indicates shared

311 rotation axes for MROD- ω within these subdivided zones, implying minimal local lattice rotations and
312 limited heterogeneous deformation in the DCs during LCF loading. In contrast, the three IDs exhibit
313 clear coloring subdivisions, especially around intrinsic defects, with a noticeable divergence in axis
314 projection distributions. Simultaneously, the alignment of interfacial boundaries among multiple color
315 blocks with the superimposed $\{111\}$ traces (red lines marking the alignment plane traces) implies the
316 activation of multiple slip systems within the IDs [49] (Fig. 5e).

317 3.3. Dislocation configurations in fatigued microstructures

318 TEM was used to analyze the dislocation configurations of DCs and IDs with the results presented in
319 Fig. 6. The TEM-imaged electron beam-transparent region was located near the lower side of the 3D-
320 μ XRD cross-section. In the DCs, dislocations having a Burgers vector of $a/2[0\bar{1}1]$ (through dual-beam
321 visibility analysis [48] as indicated by the white arrow in Fig. 6b) were observed to align unidirectionally
322 at regular intervals along the $(\bar{1}11)$ plane under the $[110]$ crystallographic zone axis (Fig. 6a), which
323 arises from local irreversible $(\bar{1}11)[0\bar{1}1]$ slip upon LCF loading. This process begins with the random
324 capture and storage of dislocations in the low-strength γ phases [50], followed by a rising dislocation
325 density as plastic strain accumulates, leading to dislocation entanglement (Fig. 6c) and eventually
326 initiating γ' phase shearing [48]. Despite these activities, the overall dislocation density in the DCs
327 remains relatively low, with dislocations primarily concentrated near the slip bands, which decrease as
328 the distancing from the slip bands increases.

329 The γ' particles in the IDs display coarsening and irregular morphologies and are accompanied by
330 numerous carbide inclusions (Fig. 6d). Unlike in the DCs, where slip bands are well-defined, the IDs
331 feature entangled dislocations within the γ channels and bidirectional arrangements of super-dislocation
332 pairs along the $(1\bar{1}1)$ and $(\bar{1}11)$ planes within the γ' phase. The $a/2[0\bar{1}1]$ and $a/2[\bar{1}01]$ dislocations, as
333 marked by white arrows in Fig. 6d and e, were identified. Additionally, one dislocation with a Burgers
334 vector different from the above was also identified near a carbide inclusion in the γ' phase (indicated by
335 a white triangle), suggesting the activation of other assisting slip systems beyond $(1\bar{1}1)[\bar{1}01]$ and
336 $(\bar{1}11)[0\bar{1}1]$, as illustrated in Fig. 6e. An interfacial dislocation array between the carbide and the matrix
337 reflects how the matrix accommodates deformation around the plastically rigid inclusions (Fig. 6f). This
338 dislocation configuration in the IDs arises from the physical and mechanical property disparities between
339 the matrix and intrinsic defects, necessitating the activation of additional slip systems to reconcile

340 incompatible deformations under cyclic loading. Dislocations from multiple slip systems are further
341 activated as deformation progresses, leading to stronger interactions, shorter slip distances, more
342 dislocation pile-ups [48, 49], and severe stress localization. These findings were reproducible across
343 electron beam-transparent areas encompassing several DCs and IDs. Although not all regions were fully
344 analyzed, evidence indicates that at least two identical slip systems were active within the IDs, as inferred
345 from dislocations aligned in the same directions and becoming invisible under identical reflections.

346 3.4. Elastic strain field in fatigued microstructures

347 Fig. 7a-d displays maps related to elastic strain tensors to unveil the local stress states in fatigued
348 microstructures. One representative normal elastic strain component (ϵ_{yy}) and one shear elastic strain
349 component (ϵ_{zy}) are selected for detailed analysis (the remaining four components ϵ_{xx} , ϵ_{zz} , ϵ_{xy} , ϵ_{zx} are
350 available in Supplementary Fig. S6). Note that to illustrate the relationship between stress states and
351 crack paths intuitively, the directions of these strain components are shown in the sample frame in Fig.
352 7a. In regions DC1 and DC2, ϵ_{yy} and ϵ_{zy} exhibit relatively low strain levels, with localized zones showing
353 elevated tensile or compressive strain values in a subtle banded distribution (Fig. 7b and c), which align
354 with the red $\{111\}$ traces (Fig. 5e). In contrast, strain levels of both ϵ_{yy} and ϵ_{zy} are significantly higher in
355 the three IDs, with localized strain enhancements particularly pronounced near intrinsic defects (Fig. 7b
356 and c). Additionally, the maximum tensile elastic strain of 9.6×10^{-3} observed between two carbides in
357 ID1 exceeds the 7.1×10^{-3} tensile strain between the void at the top and the adjacent carbide, which is
358 due to the more inhomogeneous deformation in the matrix surrounding carbide clusters than regions near
359 voids (Fig. 5b and 7b). The role of these intrinsic defects in LCF damage accumulation will be further
360 explored in Section 4.1.

361 The change of micromechanical fields is often linked to the generation of specific dislocation
362 configurations in localized zones, such as strain gradients from incidental dislocation boundaries (IDBs)
363 and orientation gradients from geometrically necessary boundaries (GNBs) [44]. In the ID2 region, a
364 subdivided yet interconnected zone of elevated tensile and compressive elastic strains is observed
365 between two carbides approximately $50 \mu\text{m}$ apart, arising from dislocation pile-ups at the mesoscopic
366 scale, as illustrated in Fig. 7b and further highlighted by the magnified view within the black dashed box
367 in Fig. 7c. The compressive strain zone corresponds to one side with an extra half atomic plane, while
368 the tensile strain zone forms on the opposite side [23, 51], as illustrated in Fig. 7d. This dislocation

369 configuration gives rise to a localized damage zone, where the tensile strain region reflects a long-range
370 tensile stress state that facilitates damage under external loading, accompanied by a substantial elastic
371 strain gradient (ε_{zy} Grad) extending 5~8 μm along the depth direction. Meanwhile, quantitative analysis
372 of this zone (marked by rectangles and arrows in Fig. 7d₂ and d₃) indicates a maximum KAM variation
373 of only 0.07°, compared to a ε_{zy} Grad variation exceeding 6×10^{-3} , designating it as a potential site for
374 fatigue crack initiation and propagation, as illustrated in Fig. 7e. It is worth mentioning that such analysis
375 is made possible by the high angular resolution of 3D- μXRD technology, which is beyond the reach of
376 conventional EBSD techniques. Moreover, the elastic strain distribution in the DCs and IDs after
377 intermediate-temperature LCF loading was statistically analyzed, revealing that intrinsic defects in the
378 IDs (ID1~ID3) induce a higher proportion of regions with elevated tensile elastic strain values (ε_{yy}
379 ranging from 4×10^{-3} to 8×10^{-3} and ε_{zy} from 5×10^{-3} to 9×10^{-3}) compared to the DCs (D1 and D2).
380 The increased localized tensile elastic strain accounts for the higher frequency of fatigue cracks observed
381 in the IDs, as displayed in Fig. 8a and b.

382 3.5. Early fatigue damage of microstructures

383 The lattice orientation field within the ~40%-fatigue-interrupted sample (at the early fatigue stage) is
384 shown in Fig. 9a-d. The multimodal analysis segmented the Sharp-IPF-Y map (within $\sim 1^\circ$) into two
385 regions: a nearly defect-free DC on the left and an ID on the right containing carbide inclusions and
386 micropores (Fig. 9a). At the early fatigue stage, the DC region is characterized by parallel bands
387 approximately 7 μm wide with highly close lattice orientations, indicative of localized irreversible slip
388 along a specific slip system. The MROD- ω values between these bands remain below 0.2°, signifying
389 minimal orientation gradients within the DC (Fig. 9c). In contrast, the ID exhibits substantial orientation
390 variation, particularly near intrinsic defects (Fig. 9a). Local lattice rotations in these regions exceed 0.5°
391 with varying rotation axes (Fig. 9c and d), indicating the early onset of marked heterogeneous
392 deformation within the ID.

393 Fig. 10a-f depicts maps of six elastic strain components of the microstructure during the early stages
394 of LCF loading. In the DC, banded zones with elevated local elastic strain are clearly visible (Fig. 10a-
395 c). Conversely, high strain values are primarily localized around intrinsic defects in the ID, while regions
396 farther from these defects exhibit significantly lower strain levels, with slip band features nearly absent
397 (Fig. 10a-c). The DC primarily accumulates local irreversible slip along specific slip systems, whereas

398 the ID undergoes incompatible deformation (Fig. 9b). Both the elastic strain levels and the proportion of
399 high-elastic-strain regions in the ID are relatively lower than the post-mortem specimen (Fig. 7b and
400 10b). Additionally, regions of elevated tensile elastic strain near carbide clusters in the ID are nearly
401 interconnected with adjacent DC slip bands (Fig. 10b). This connectivity likely explains the tendency for
402 interdendritic cracks to deflect into the DCs, enabling alternating propagation between neighboring IDs
403 (Fig. 1).

404 **4. Discussion**

405 In this study, we established a multimodal analytical framework that integrates synchrotron 3D- μ XRD,
406 μ -CT, and advanced electron microscopy to map the submicron-scale spatial correlations among 3D
407 residual stress/strain fields, dendritic structures, defects, and dislocation configurations within bulk Ni-
408 SX superalloys during the early stages of fatigue and post-failure. This approach quantitatively and
409 statistically reveals the mechanical heterogeneity in fatigue damage between DCs and IDs. This section
410 first discusses the LCF damage behavior of Ni-SX superalloys at intermediate temperatures, with a focus
411 on carbide effects, then compares damage levels between DCs and IDs to clarify the microscopic origins
412 and evolution of heterogeneous fatigue damage. Finally, the broader applicability of this multimodal
413 analytical approach to other cast alloys with dendritic structures is discussed.

414 4.1. The impact of intrinsic defects on LCF damage

415 The present research highlights the significant role of carbide morphology in LCF damage
416 accumulation, particularly when the orientation of carbide tips or sharp edges (those most likely to induce
417 localized plastic deformation) aligns with the external loading axis, thereby increasing the likelihood of
418 fatigue crack initiation [9, 46]. This effect is corroborated by the locally elevated GND density and tensile
419 elastic strain observed at sharper carbide corners compared to more rounded ones, as indicated by white
420 arrows in ID1 of Fig. 5b and 7b. Moreover, the GND density and tensile elastic strain are notably higher
421 around carbide clusters than around isolated carbides (as shown in ID2 of Fig. 5b and 7b and the ID
422 regions of Fig. 9b and 10b), which could explain the frequent occurrence of LCF cracks in regions with
423 mesh-like or chain-like carbide distributions reported in previous studies [10, 16, 52, 53]. Attempts to
424 correlate carbide morphology with local effective strain and GND distribution through finite element
425 analysis have been made [46]. These proposed models however often rely on data from random 2D plane

426 examinations, which may introduce incalculable uncertainty in their predictions due to the lack of robust
427 experimental validation. Given the complex 3D morphology of carbides (Fig. 4b and c), such 2D
428 constraints fail to capture critical details, further compromising modeling accuracy. Future studies should
429 focus on incorporating more comprehensive 3D analyses to improve the reliability of fatigue life
430 prediction models.

431 Previous work has indicated that carbides can activate multiple slip systems in the surrounding matrix,
432 resulting in pronounced heterogeneous deformation [46]. Similarly and more deeply, our work reveals
433 that local lattice rotations near carbides along different crystallographic axes (Fig. 5c and e) arise from
434 the activation of multiple slip systems in the matrix to accommodate local microplasticity around these
435 rigid carbides as directly evidenced by the dislocation configurations (Fig. 6d-e). While carbides
436 generally enhance fatigue resistance in superalloys by hindering dislocation motion (both SSDs and
437 GNDs) [9], our observations show that when carbides obstruct local irreversible slip along specific slip
438 systems, dislocation pile-ups can form, leading to an elevation in local tensile strain/stress levels that
439 substantially increase fatigue cracking risk. Consequently, optimizing alloy composition and refining the
440 casting process to control carbide morphology and distribution - avoiding network or chain-like
441 arrangements - could reduce stress concentrations and postpone damage accumulation under
442 intermediate-temperature LCF conditions.

443 4.2. Quantitative comparison of fatigue damage between DCs and IDs

444 Fig. 11 quantitatively compares the fatigue damage modes between DCs and IDs during the early
445 stages of LCF loading. Fig. 11a shows the crystallographic orientation at Point A from Fig. 9a (expressed
446 as Euler angles) alongside the calculated $\{111\}$ slip traces. Fig. 11b presents the Schmid factors for all
447 twelve slip systems, with the slip system having the highest Schmid factor highlighted. In the DCs, the
448 overall tensile components of ε_{yy} remain relatively low, typically below $1500 \mu\epsilon$ (Fig. 11c). Notably, the
449 largest local strain peaks coincide with the red slip traces, indicating activation of the $(111)[\bar{1}\bar{1}0]$ slip
450 system with the highest Schmid factor, while smaller peaks correspond to the blue slip traces (Fig. 11c).
451 In contrast, the tensile components of ε_{yy} in the IDs are higher, with prominent regions exceeding 3000
452 $\mu\epsilon$ and showing random orientations. Statistical analysis of ε_{yy} along Paths B and C in Fig. 10b confirms
453 that local stress concentrations arising from intrinsic defects in the IDs are more pronounced than the slip
454 band formation within the DCs under LCF (Fig. 11c). Using the approach outlined in Ref. [54], which

455 assumes that the three principal stress directions align with the sample's coordinate axes (X, Y, and Z),
456 the relative residual stress values parallel to the loading direction at the positions marked by the black
457 arrows in Fig. 11c were quantitatively compared. The Poisson's ratio and elastic modulus were taken
458 from Ref. [55]. The results show that the residual stress in the DCs is 139 MPa, whereas in the IDs it
459 reaches 458 MPa, indicating that the local damage level in the IDs is over three times higher than that in
460 the DCs. These high-tensile stress zones in the IDs when superimposed with the externally applied tensile
461 load serve as potential sites for crack nucleation.

462 Recently, the concept of GNDs has been more frequently used to explain the LCF crack initiation and
463 propagation mechanisms of superalloys containing inclusions [9, 10, 18, 56]. Regarding crack initiation,
464 some studies suggested that GND accumulation contributes to strain hardening and increases local shear
465 stress, potentially promoting crack initiation through energy storage and dissipation [57, 58]. However,
466 others argued that GND density alone is insufficient to predict crack initiation sites reliably, as elevated
467 GND density levels are not exclusive to these regions [56]. We believe that incorporating the analysis of
468 internal stress states in the corresponding regions can strengthen the robustness of LCF damage indicators.
469 Along Path A (highlighted by dashed lines in Figs. 9b and 10b), a quantitative correlation between the
470 distributions of ε_{yy} and GND density was established (Fig. 12). Within the DCs, three tensile strain peaks
471 were identified at approximately 11 μm intervals, corresponding to slip band regions (regions 1, 2 and 3
472 marked in light yellow). This spacing closely matches the shear band spacing (9~12 μm) measured by
473 high-resolution digital image correlation (DIC) in Ref. [59], although the measured strain values are
474 lower than those reported in the literature. This discrepancy likely reflects both the early stage of
475 deformation and differences in measurement tools, as displayed in Fig. 12. In the slip band regions, GND
476 density peaks exhibit elevated values at the edges and a dip at the center, indicating a pronounced
477 orientation gradient at the slip band edges and a smaller gradient within the band interior (Fig. 12). This
478 observation is consistent with the DIC and crystal plasticity finite element simulation results reported in
479 Ref. [24]. Notably, the highest tensile elastic strain occurs at the GND density trough (i.e., within the slip
480 band itself), revealing a micron-scale offset between the regions of maximum tensile strain and those
481 with the largest orientation gradients. Within the IDs, both the ε_{yy} and GND density distributions exhibit
482 significant fluctuations and elevated values (Fig. 12). In some areas (e.g., regions 4, 6, and 7), the peaks
483 of GND density and ε_{yy} nearly coincide. However, the highest ε_{yy} peak in region 6 (exceeding 5000 μe)

484 signals a high crack nucleation risk. Conversely, the highest GND peak appears in region 5, where
485 compressive strain partially counteracts the externally applied tensile load, reducing crack initiation risk.
486 Overall, incorporating the local stress state enhances the accuracy of LCF damage prediction and
487 identification.

488 Additionally, Guo et al. [24] employed stored energy density resolved on individual slip systems to
489 predict crack nucleation sites, demonstrating a robust and generalizable damage indicator. In our study,
490 we found that in the DCs, once the critical resolved shear stress of a favorable slip system is reached,
491 local irreversible slip accumulates and forms slip bands. This finding is consistent with Ref. [24], where
492 multiple favorable slip systems activate near a notch, leading to the emergence of localized deformation
493 bands and eventual crack initiation. Hence, the stored energy density approach shows promise in
494 predicting cracking in DCs. However, in the IDs, heterogeneous deformation dominates due to the
495 presence of defects with varying types, sizes, and morphologies. The local microplastic behavior varies
496 around these defects, emphasizing the need for further microscale validation to determine whether slip-
497 system-resolved stored energy density can reliably predict crack initiation in IDs. To some extent, elastic
498 strain reflects the magnitude of stored strain energy, capturing the potential energy accumulated after
499 heterogeneous deformation. Thus, it can serve as a valuable indicator for damage prediction in IDs.

500 4.3. Mechanisms of mechanical heterogeneous fatigue damage in dendritic structures

501 Based on the quantitative results and microstructural observations presented earlier, we now detail the
502 microscopic origins and evolution of mechanical heterogeneity of fatigue damage within the DCs and
503 IDs of Ni-SX superalloys under intermediate-temperature LCF conditions (Fig. 13a). In the DCs, the
504 relatively homogeneous microstructure and the absence of significant stress singularities enable local
505 irreversible slip accumulation along specific $\{111\}\langle 110\rangle$ slip systems, resulting in the generation of slip
506 bands without triggering local lattice rotations, as evidenced by the consistent orientation observed within
507 DCs (Fig. 5a and 9a). Conversely, IDs experience varying degrees and directions of matrix rotation near
508 intrinsic defects to accommodate lattice curvatures caused by incompatible deformations. This results in
509 variational lattice orientations in these regions (Fig. 5a and 9a), accompanied by dislocation pile-ups (Fig.
510 7d) and overall elevated tensile elastic strain levels (Fig. 8a and b). This heterogeneity in fatigue damage
511 facilitates the extensive propagation of fatigue cracks initiated in the IDs, as illustrated in Fig. 13b.
512 Intrinsic defects lower the local stress intensity threshold of the surrounding matrix [60], triggering strain

513 localization and forming fatigue damage zones. Additionally, the chain-like distribution of intrinsic
514 defects fosters the interlinkage of these localized damage zones, ultimately driving continuous fatigue
515 cracking. This finding provides foundational insights and experimental evidence to guide further
516 modeling efforts and enhance the understanding of LCF damage behavior in single-crystal superalloys.

517 This heterogeneous LCF damage micromechanism primarily applies to cast Ni-based superalloys with
518 solidification monocrystalline dendritic structures, where the IDs are rich in defects and the DCs are
519 nearly defect-free. In other cast monocrystalline Ni-based superalloys with different crystallographic
520 orientations, local variations in critical resolved shear stress may cause irreversible slip to accumulate
521 along different, more favorably oriented slip systems within the DCs. When dislocation climb is absent,
522 the microscopic mechanical response in the DCs remains largely unchanged, while in the IDs,
523 irreversible slip is still hindered by defects, leading to heterogeneous deformation.

524 However, the applicability of this heterogeneous LCF damage micromechanism to cast polycrystalline
525 Ni-based superalloys may be limited. Studies have shown that dendritic structures exhibit distinct
526 microscopic mechanical responses depending on grain size and crystallographic orientation. For instance,
527 local lattice rotations tend to occur in the IDs of large grains with Brass-type orientations and low Schmid
528 factors, whereas small grains with high Schmid factors display markedly different microscopic
529 deformation behaviors [9]. Additionally, grain boundaries can hinder the accumulation of local
530 irreversible slip on specific slip systems, further complicating the microscale deformation behavior of
531 dendritic structures. Consequently, comprehensive investigations focusing on grain size, crystallographic
532 orientation, and grain boundaries are needed to broaden the applicability of this micromechanism. Based
533 on the findings of this study, the average tensile elastic strain ϵ_{yy} in the IDs could serve as a parameter
534 for governing LCF damage processes in Ni-SX superalloys.

535 4.4. The potential application of the multimodal 3D X-ray microscopy method

536 Fatigue damage research in Ni-SX superalloys has long been confined to conventional surface
537 techniques, which simplify analysis due to the absence of 3D vision, thus increasing the uncertainty of
538 established failure criteria [15, 16, 20, 60, 61]. Nevertheless, large-scale 3D measurements often
539 encounter obstacles such as lengthy data acquisition times and the generation of excessively large
540 datasets [62-64], especially considering the scarcity and periodic availability at synchrotron facilities. To
541 overcome these limitations, this study adopted a combined approach: laboratory-based X-ray

542 microtomography was first used for comprehensive microstructural imaging, followed by targeted low-
543 dimensional characterization and preliminary analysis of damage micromechanisms. Synchrotron
544 measurements were subsequently performed outside the crack-tip plasticity zone to evaluate local stress
545 states in fatigued microstructures, further validating 2D-derived failure theories. This integrated
546 methodology proves instrumental in identifying and analyzing the micromechanisms of deformation
547 under load in cast materials with dendrite structures, such as aluminum cast alloys, certain austenitic cast
548 steels, and copper cast alloys, while optimizing the utilization of synchrotron resources.

549 **5. Conclusions**

550 This study conducted LCF testing on the Ni-SX superalloy DD413 at 760 °C. Post-mortem and ~40%-
551 fatigue-interrupted specimens were analyzed using a multimodal 3D X-ray microscopy approach
552 integrating synchrotron 3D- μ XRD, laboratory μ -CT, and complementary electron microscopy (EBSD,
553 SEM-FIB, STEM). This methodology revealed submicron-resolution 3D distributions of dendritic
554 microstructures, residual stress/strain fields, and solidification defects during both early fatigue damage
555 and final failure. It also uncovered the mechanical heterogeneity inherent in the fatigue micromechanisms
556 of the DD413 alloy. The study validates the synergistic use of 3D- μ XRD and μ -CT and provides critical
557 datasets and insights to advance multiphysics fatigue models and guide the design of novel fatigue-
558 resistant single-crystal superalloys. The main conclusions are as follows:

- 559 1. Under intermediate-temperature LCF loading, the DCs and IDs of the DD413 superalloy exhibit
560 heterogeneous microscale mechanical responses: the DCs accumulate local irreversible slip along
561 specific slip systems to generate slip bands, while the IDs accommodate local microplasticity around
562 intrinsic defects by activating multiple slip systems.
- 563 2. Local tensile stress near defects in the IDs is more than three times higher than in the slip bands of
564 the DCs, driving the generation of local fatigue damage zones in the IDs. The chain-like distribution
565 of defects promotes the interconnection of these local damage zones into continuous damage regions,
566 resulting in an overall increase in tensile stress levels in the IDs.
- 567 3. GND density alone is insufficient to indicate LCF damage; both the internal stress state (tension or
568 compression) and its magnitude must be considered.
- 569 4. Macroscale μ -CT effectively guides 3D- μ XRD measurements by targeting critical structural features,

570 while high-resolution μ -CT aids in interpreting internal diffraction signals for correlative analysis.
571 The combined use of multimodal μ -CT and 3D- μ XRD enables accurate localization of internal
572 damage zones within bulk fatigued Ni-SX superalloy and provides correlated 3D mapping of
573 residual stress/strain fields, dendritic microstructures, and defects at the submicron scale across
574 various regions.

575

576 **References**

- 577 1 T.M. Pollock, S. Tin, Nickel-based superalloys for advanced turbine engines: chemistry,
578 microstructure and properties, *J. Propul. Power* 22 (2) (2006) 361-374.
- 579 2 T.M. Pollock, Alloy design for aircraft engines, *Nat. Mater.* 15 (8) (2016) 809-815.
- 580 3 R.C. Reed, T. Tao, N. Warnken, Alloys-by-design: application to nickel-based single crystal
581 superalloys, *Acta Mater.* 57 (19) (2009) 5898-5913.
- 582 4 X. Wu, S.K. Makineni, C.H. Liebscher, G. Dehm, J. Rezaei Mianroodi, P. Shanthraj, B.
583 Svendsen, D. Bürger, G. Eggeler, D. Raabe, B. Gault, Unveiling the Re effect in Ni-based single
584 crystal superalloys, *Nat. Commun.* 11 (1) (2020) 389.
- 585 5 W. Xia, X. Zhao, L. Yue, Z. Zhang, A review of composition evolution in Ni-based single crystal
586 superalloys, *J. Mater. Sci. Technol.* 44 (2020) 76-95.
- 587 6 C. Yang, Q. Xu, X. Su, B. Liu, Multiphase-field and experimental study of solidification
588 behavior in a nickel-based single crystal superalloy, *Acta Mater.* 175 (2019) 286-296.
- 589 7 A. Heckl, R. Rettig, S. Cenanovic, M. Göken, R. Singer, Investigation of the final stages of
590 solidification and eutectic phase formation in Re and Ru containing nickel-base superalloys, *J.*
591 *Cryst. Growth* 312 (14) (2010) 2137-2144.
- 592 8 Z. Zhou, R. Li, Y. Wang, T. Li, S. Wang, S. Li, G. Xie, J. Zhang, Y.-D. Wang, Microscopic
593 heterogeneity of low cyclic fatigue damage in Ni-based single crystal superalloy DD413, *Mater.*
594 *Charact.* 207 (2024) 113551.
- 595 9 G. Liu, J.S. Cantó, S. Winwood, K. Rhodes, S. Biroasca, The effects of microstructure and
596 microtexture generated during solidification on deformation micromechanism in IN713C
597 nickel-based superalloy, *Acta Mater.* 148 (2018) 391-406.
- 598 10 G. Liu, S. Winwood, K. Rhodes, S. Biroasca, The effects of grain size, dendritic structure and
599 crystallographic orientation on fatigue crack propagation in IN713C nickel-based superalloy,

600 *Int. J. Plast.* 125 (2020) 150-168.

601 11 A. Pineau, D.L. McDowell, E.P. Busso, S.D. Antolovich, Failure of metals II: Fatigue, *Acta*
602 *Mater.* 107 (2016) 484-507.

603 12 J.J. Kruzic, Predicting Fatigue Failures, *Science* 325 (5937) (2009) 156-158.

604 13 S. Lavenstein, Y. Gu, D. Madiseti, J.A. El-Awady, The heterogeneity of persistent slip band
605 nucleation and evolution in metals at the micrometer scale, *Science* 370 (6513) (2020) eabb2690.

606 14 S. Steuer, P. Villechaise, T.M. Pollock, J. Cormier, Benefits of high gradient solidification for
607 creep and low cycle fatigue of AM1 single crystal superalloy, *Mater. Sci. Eng., A* 645 (2015)
608 109-115.

609 15 B. Ruttert, C. Meid, L.M. Roncery, I. Lopez-Galilea, M. Bartsch, W. Theisen, Effect of porosity
610 and eutectics on the high-temperature low-cycle fatigue performance of a nickel-base single-
611 crystal superalloy, *Scr. Mater.* 155 (2018) 139-143.

612 16 X. Ma, H.-J. Shi, In situ SEM studies of the low cycle fatigue behavior of DZ4 superalloy at
613 elevated temperature: Effect of partial recrystallization, *Int. J. Fatigue* 61 (2014) 255-263.

614 17 D. Texier, J.-C. Stinville, M.-A. Charpagne, Z. Chen, V. Valle, P. Villechaise, T.M. Pollock, J.
615 Cormier, Role of non-metallic inclusions and twins on the variability in fatigue life in alloy 718
616 nickel base superalloy, *Superalloys 2020: Proceedings of the 14th International Symposium on*
617 *Superalloys*, Springer, 2020, pp. 629-639.

618 18 J. Jiang, J. Yang, T. Zhang, F.P.E. Dunne, T.B. Britton, On the mechanistic basis of fatigue crack
619 nucleation in Ni superalloy containing inclusions using high resolution electron backscatter
620 diffraction, *Acta Mater.* 97 (2015) 367-379.

621 19 R. Jiang, D.J. Bull, A. Evangelou, A. Harte, F. Pierron, I. Sinclair, M. Preuss, X.T. Hu, P.A.S.
622 Reed, Strain accumulation and fatigue crack initiation at pores and carbides in a SX superalloy
623 at room temperature, *Int. J. Fatigue* 114 (2018) 22-33.

624 20 X. Ren, J. Lu, J. Zhou, X. Liu, W. Jiang, J. Wang, Y. Zhang, Z. Zhang, In-situ fatigue behavior
625 study of a nickel-based single-crystal superalloy with different orientations, *Mater. Sci. Eng.,*
626 *A* 855 (2022) 143913.

627 21 J.C. Stinville, P.G. Callahan, M.A. Charpagne, M.P. Echlin, V. Valle, T.M. Pollock, Direct
628 measurements of slip irreversibility in a nickel-based superalloy using high resolution digital

629 image correlation, *Acta Mater.* 186 (2020) 172-189.

630 22 G. Liu, L. Kong, S. Ruan, S. Biroasca, Microstructure and phases structure in nickel-based
631 superalloy IN713C after solidifications, *Mater. Charact.* 182 (2021) 111566.

632 23 R. Li, Q. Xie, Y.-D. Wang, W. Liu, M. Wang, G. Wu, X. Li, M. Zhang, Z. Lu, C. Geng, T. Zhu,
633 Unraveling submicron-scale mechanical heterogeneity by three-dimensional X-ray
634 microdiffraction, *PNAS* 115 (3) (2018) 483-488.

635 24 Z. Guo, X. Lu, C. Paramatmuni, H. Gao, F.P.E. Dunne, W. Yan, Y.-W. Zhang, Y. Xu, Slip system-
636 resolved GNDs and SEDs: A multi-scale framework for predicting crack nucleation in single-
637 crystal metals, *Acta Mater.* 288 (2025) 120853.

638 25 Z. Liu, Z. Zhao, T. Zheng, J. Mu, G. Xie, J. Zhang, L. He, Y. Wang, A mechanism on multiscale
639 heterogenous deformation of nickel-based single crystal superalloys unraveled by time-of-flight
640 neutron diffraction technology, *Acta Mater.* 281 (2024) 120430.

641 26 T. Swift, Damage tolerance capability, *Int. J. Fatigue* 16 (1) (1994) 75-94.

642 27 M.M. Omar, J.A. El-Awady, Foreseeing metal failure from its inception, *Science* 377 (6610)
643 (2022) 1047-1048.

644 28 R. Li, Y.-D. Wang, W. Liu, C. Geng, Q. Xie, D.E. Brown, K. An, Multiscale mechanical fatigue
645 damage of stainless steel investigated by neutron diffraction and X-ray microdiffraction, *Acta*
646 *Mater.* 165 (2019) 336-345.

647 29 Z. Yan, K. Srikakulapu, Y. Gao, H. Qin, Y. Rong, Z. Bi, Q. Xie, K. An, Y.-d. Wang, Q. Tan, γ' -
648 size effect on the deformation microstructure and texture in a Ni-based superalloy using in-situ
649 neutron diffraction, *Scr. Mater.* 236 (2023) 115665.

650 30 Z. Zhang, Y. Feng, Q. Tan, J. Zou, J. Li, X. Zhou, G. Sun, Y. Wang, Residual stress distribution
651 in Ni-based superalloy turbine discs during fabrication evaluated by neutron/X-ray diffraction
652 measurement and thermomechanical simulation, *Mater. Des.* 166 (2019) 107603.

653 31 Z. Zhu, C. Xiong, J. Wang, R. Li, Y. Ren, Y. Wang, Y. Li, In situ synchrotron X-ray diffraction
654 investigations of the physical mechanism of ultra-low strain hardening in Ti-30Zr-10Nb alloy,
655 *Acta Mater.* 154 (2018) 45-55.

656 32 T. Britton, J. Hickey, Understanding deformation with high angular resolution electron
657 backscatter diffraction (HR-EBSD), IOP Conference Series: Materials Science and Engineering,

658 IOP Publishing, 2018, p. 012003.

659 33 S. Kalácska, J. Ast, P.D. Ispánovity, J. Michler, X. Maeder, 3D HR-EBSD Characterization of
660 the plastic zone around crack tips in tungsten single crystals at the micron scale, *Acta Mater.*
661 200 (2020) 211-222.

662 34 P.J. Withers, C. Bouman, S. Carmignato, V. Cnudde, D. Grimaldi, C.K. Hagen, E. Maire, M.
663 Manley, A. Du Plessis, S.R. Stock, X-ray computed tomography, *Nat. Rev. Methods Primers* 1
664 (1) (2021) 18.

665 35 B.C. Larson, W. Yang, G.E. Ice, J.D. Budai, J.Z. Tischler, Three-dimensional X-ray structural
666 microscopy with submicrometre resolution, *Nature* 415 (6874) (2002) 887-890.

667 36 M. Herbig, A. King, P. Reischig, H. Proudhon, E.M. Lauridsen, J. Marrow, J.-Y. Buffière, W.
668 Ludwig, 3-D growth of a short fatigue crack within a polycrystalline microstructure studied
669 using combined diffraction and phase-contrast X-ray tomography, *Acta Mater.* 59(2) (2011)
670 590-601.

671 37 H. Simons, A. King, W. Ludwig, C. Detlefs, W. Pantleon, S. Schmidt, F. Stöhr, I. Snigireva, A.
672 Snigirev, H.F. Poulsen, Dark-field X-ray microscopy for multiscale structural characterization,
673 *Nat. Commun.* 6 (1) (2015) 6098.

674 38 Y. Hu, S. Wu, Y. Guo, Z. Shen, A.M. Korsunsky, Y. Yu, X. Zhang, Y. Fu, Z. Che, T. Xiao, S.
675 Lozano-Perez, Q. Yuan, X. Zhong, X. Zeng, G. Kang, P.J. Withers, Inhibiting weld cracking in
676 high-strength aluminium alloys, *Nat. Commun.* 13 (1) (2022) 5816.

677 39 P.M. Sarosi, J. Furmanski, W.C. Reese, D.L. Carpenter, M.A. Nittoli, M.G. Myers, N.M. Callen,
678 T. Neeraj, Damage evolution during fracture by correlative microscopy with hyperspectral
679 electron microscopy and laboratory-based microtomography, *Sci. Adv.* 8 (14) (2022) eabj6738.

680 40 E.F.F. Knipschildt, X. Lei, Y.B. Zhang, T. Yu, S. Fæster, W. Liu, R.E. Sanders, D. Juul Jensen,
681 Registration of data from a multimodal investigation of particle stimulated nucleation in
682 aluminum, IOP Conference Series: Materials Science and Engineering 1249 (1) (2022) 012049.

683 41 F. Bachmann, R. Hielscher, H. Schaeben, Grain detection from 2d and 3d EBSD data—
684 Specification of the MTEX algorithm, *Ultramicroscopy* 111 (12) (2011) 1720-1733.

685 42 A. Poshadel, P. Dawson, G. Johnson, Assessment of deviatoric lattice strain uncertainty for
686 polychromatic X-ray microdiffraction experiments, *J. Synchrotron Radiat.* 19 (2) (2012) 237-

687 244.

688 43 W. Pantleon, Resolving the geometrically necessary dislocation content by conventional
689 electron backscattering diffraction, *Scr. Mater.* 58 (11) (2008) 994-997.

690 44 O. Muransky, L. Balogh, M. Tran, C. Hamelin, J.-S. Park, M.R. Daymond, On the measurement
691 of dislocations and dislocation substructures using EBSD and HRSD techniques, *Acta Mater.*
692 175 (2019) 297-313.

693 45 J.F. Nye, Some geometrical relations in dislocated crystals, *Acta Metall.* 1 (2) (1953) 153-162.

694 46 P.S. Karamched, A.J. Wilkinson, High resolution electron backscatter diffraction analysis of
695 thermally and mechanically induced strains near carbide inclusions in a superalloy, *Acta Mater.*
696 59 (1) (2011) 263-272.

697 47 R. Hielscher, C.B. Silbermann, E. Schmidl, J. Ihlemann, Denoising of crystal orientation maps,
698 *J. Appl. Crystallogr.* 52 (5) (2019) 984-996.

699 48 A. Piglione, T. Bellamy, J. Yu, J. Zhao, C. Xiao, F.P. Dunne, M.-S. Pham, Dislocation
700 arrangements and cyclic microplasticity surrounding stress concentration in a Ni-based single-
701 crystal superalloy, *Adv. Eng. Mater.* 26 (1) (2024) 2300602.

702 49 T. Yu, Y. Du, G. Fan, R. Xu, R. Barabash, N. Hansen, X. Huang, Y. Zhang, In-situ synchrotron
703 X-ray micro-diffraction investigation of ultra-low-strain deformation microstructure in
704 laminated Ti-Al composites, *Acta Mater.* 202 (2021) 149-158.

705 50 L. Zhang, L. Zhao, A. Roy, V. Silberschmidt, G. Mccolvin, Low-cycle fatigue of single crystal
706 nickel-based superalloy—mechanical testing and TEM characterisation, *Mater. Sci. Eng., A* 744
707 (2019) 538-547.

708 51 X. Chen, Q. Wang, Z. Cheng, M. Zhu, H. Zhou, P. Jiang, L. Zhou, Q. Xue, F. Yuan, J. Zhu, X.
709 Wu, E. Ma, Direct observation of chemical short-range order in a medium-entropy alloy, *Nature*
710 592 (7856) (2021) 712-716.

711 52 J.S. Cantó, S. Winwood, K. Rhodes, S. Biroasca, A study of low cycle fatigue life and its
712 correlation with microstructural parameters in IN713C nickel based superalloy, *Mater. Sci.*
713 *Eng., A* 718 (2018) 19-32.

714 53 K. Pang, H. Yuan, Fatigue life assessment of a porous casting nickel-based superalloy based on
715 fracture mechanics methodology, *Int. J. Fatigue* 136 (2020) 105575.

716 54 A.J. Allen, H.M. T., W.C. G., C. and Andreani, Neutron diffraction methods for the study of
717 residual stress fields, *Adv. Phys.* 34(4) (1985) 445-473.

718 55 P.E. Aba-Perea, T. Pirling, P.J. Withers, J. Kelleher, S. Kabra, M. Preuss, Determination of the
719 high temperature elastic properties and diffraction elastic constants of Ni-base superalloys,
720 *Mater. Des.* 89 (2016) 856-863.

721 56 J. Jiang, J. Yang, T. Zhang, J. Zou, Y. Wang, F. Dunne, T. Britton, Microstructurally sensitive
722 crack nucleation around inclusions in powder metallurgy nickel-based superalloys, *Acta Mater.*
723 117 (2016) 333-344.

724 57 V. Wan, J. Jiang, D. MacLachlan, F. Dunne, Microstructure-sensitive fatigue crack nucleation
725 in a polycrystalline Ni superalloy, *Int. J. Fatigue* 90 (2016) 181-190.

726 58 A.N. Stroh, A theory of the fracture of metals, *Adv. Phys.* 6 (24) (1957) 418-465.

727 59 J.C. Stinville, N. Vanderesse, F. Bridier, P. Bocher, T.M. Pollock, High resolution mapping of
728 strain localization near twin boundaries in a nickel-based superalloy, *Acta Mater.* 98 (2015) 29-
729 42.

730 60 A. Cervellon, S. Hémerly, P. Kürsteiner, B. Gault, P. Kontis, J. Cormier, Crack initiation
731 mechanisms during very high cycle fatigue of Ni-based single crystal superalloys at high
732 temperature, *Acta Mater.* 188 (2020) 131-144.

733 61 A. Cervellon, C.J. Torbet, T.M. Pollock, Crack initiation anisotropy of Ni-based SX superalloys
734 in the very high cycle fatigue regime, *Mater. Sci. Eng., A* 825 (2021) 141920.

735 62 S. Gustafson, W. Ludwig, P. Shade, D. Naragani, D. Pagan, P. Cook, C. Yildirim, C. Detlefs,
736 M.D. Sangid, Quantifying microscale drivers for fatigue failure via coupled synchrotron X-ray
737 characterization and simulations, *Nat. Commun.* 11 (1) (2020) 3189.

738 63 M. Arul Kumar, B. Clausen, L. Capolungo, R.J. McCabe, W. Liu, J.Z. Tischler, C.N. Tomé,
739 Deformation twinning and grain partitioning in a hexagonal close-packed magnesium alloy, *Nat.*
740 *Commun.* 9 (1) (2018) 4761.

741 64 T.L. Burnett, P.J. Withers, Completing the picture through correlative characterization, *Nat.*
742 *Mater.* 18 (10) (2019) 1041-1049.

743

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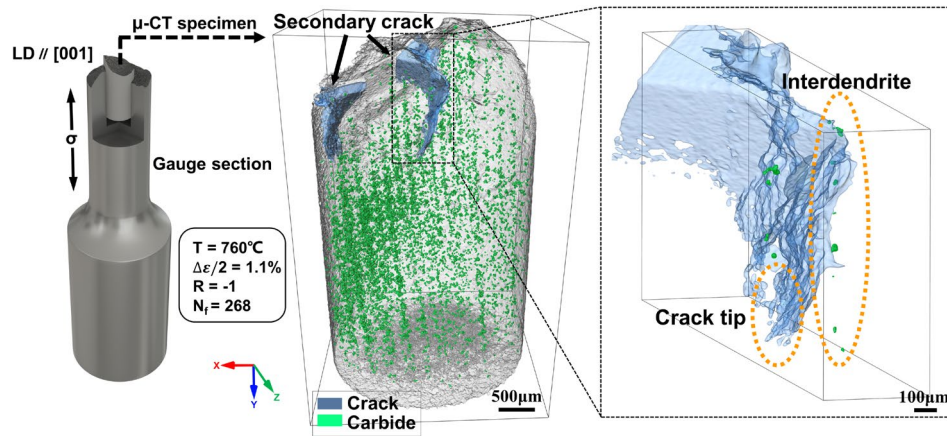
753 **Author contributions**

754 Y.-W., W.L., J.C. and Q.F. designed the research and advised on manuscript preparation. Z.Z., W.L. and
755 G. C. conducted mechanical, TEM and μ -CT experiments with assistance from C.S., J.Z. and S.L. Z.Z.,
756 Y.W., R.L. and Y.-W. analyzed the data and wrote the original draught with input from all co-authors. R.
757 L., S. L., and W.L. conducted synchrotron-based experiments. All co-authors discussed the results and
758 performed activities in writing, reviewing and editing the manuscript. Y.-W. supervised the project.

759 **Competing interests**

760 The authors declare no competing interests.

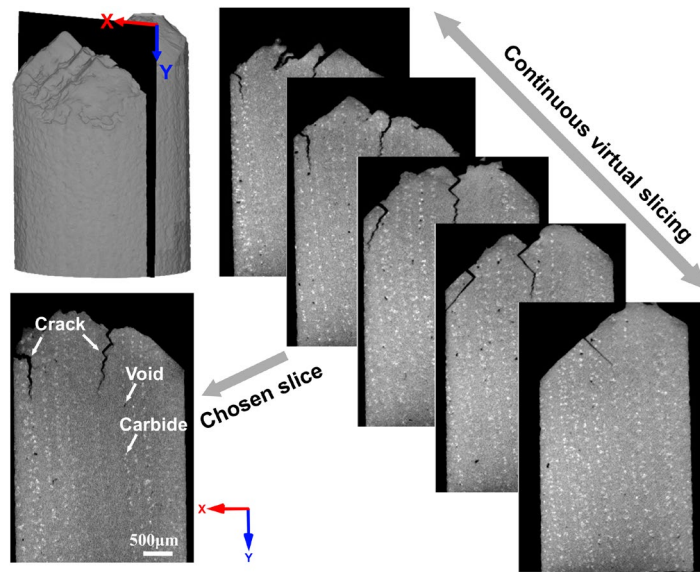
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763 **Fig. 1.** Post-mortem micro-computed tomography (μ -CT) captured the distribution of secondary cracks

764 and carbides within the miniature sample. The crack path is displayed on the right from a 3D perspective.



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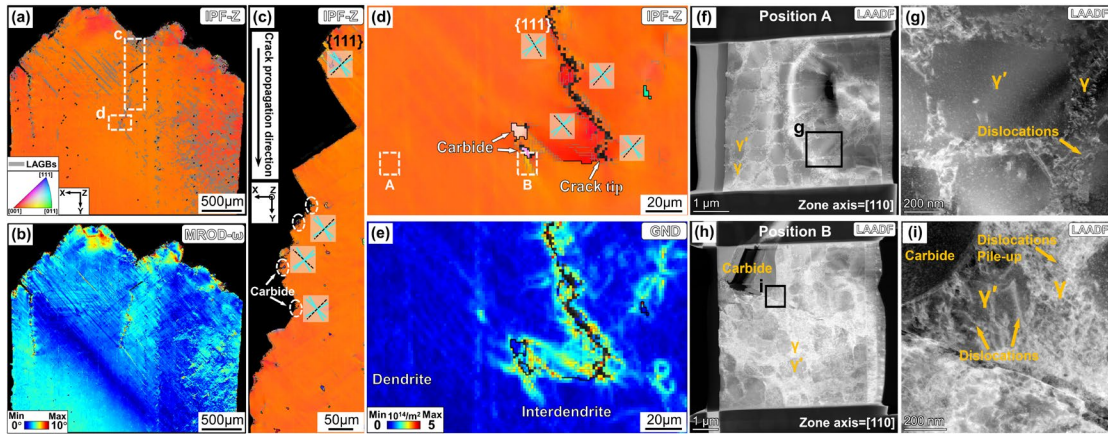
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Fig. 2. μ -CT slices parallel to the X-Y plane reveal a microcrack path aligned with chain-like intrinsic

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defects. The carbides and voids appear in a representative slice as white and black spots.

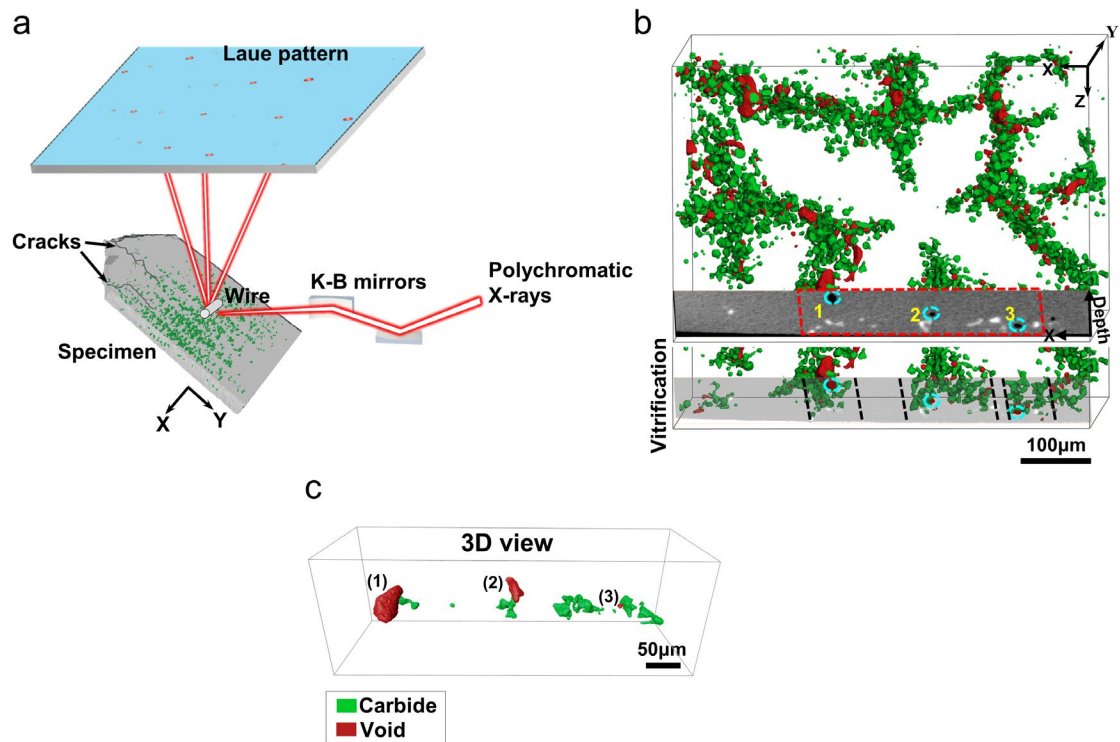
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770 **Fig. 3.** EBSD analysis of the selected slice. (a) IPF-Z map superimposed with LAGBs. (b) MROD- ω
 771 map of **a**. (c) A magnified view in **a** illustrates the short crack growth influenced by carbides, overlaid
 772 with {111} traces. (d) A magnified view of the crack tip region in **a** with arrows indicating the carbides
 773 to which the crack tip turned. (e) GND density map of **d**. LAADF STEM imaging discerns dislocation
 774 configurations in region A (f, g) and region B (h, i) (as indicated by white dashed rectangles in **d**).

775



776

777 **Fig. 4.** Spatially correlating 3D-μXRD and μ-CT to analyze crystallographic orientation and elastic strain

778 fields. (a) Schematic of 3D-μXRD setup. (b) The coverage of the 3D-μXRD scan inside the specimen

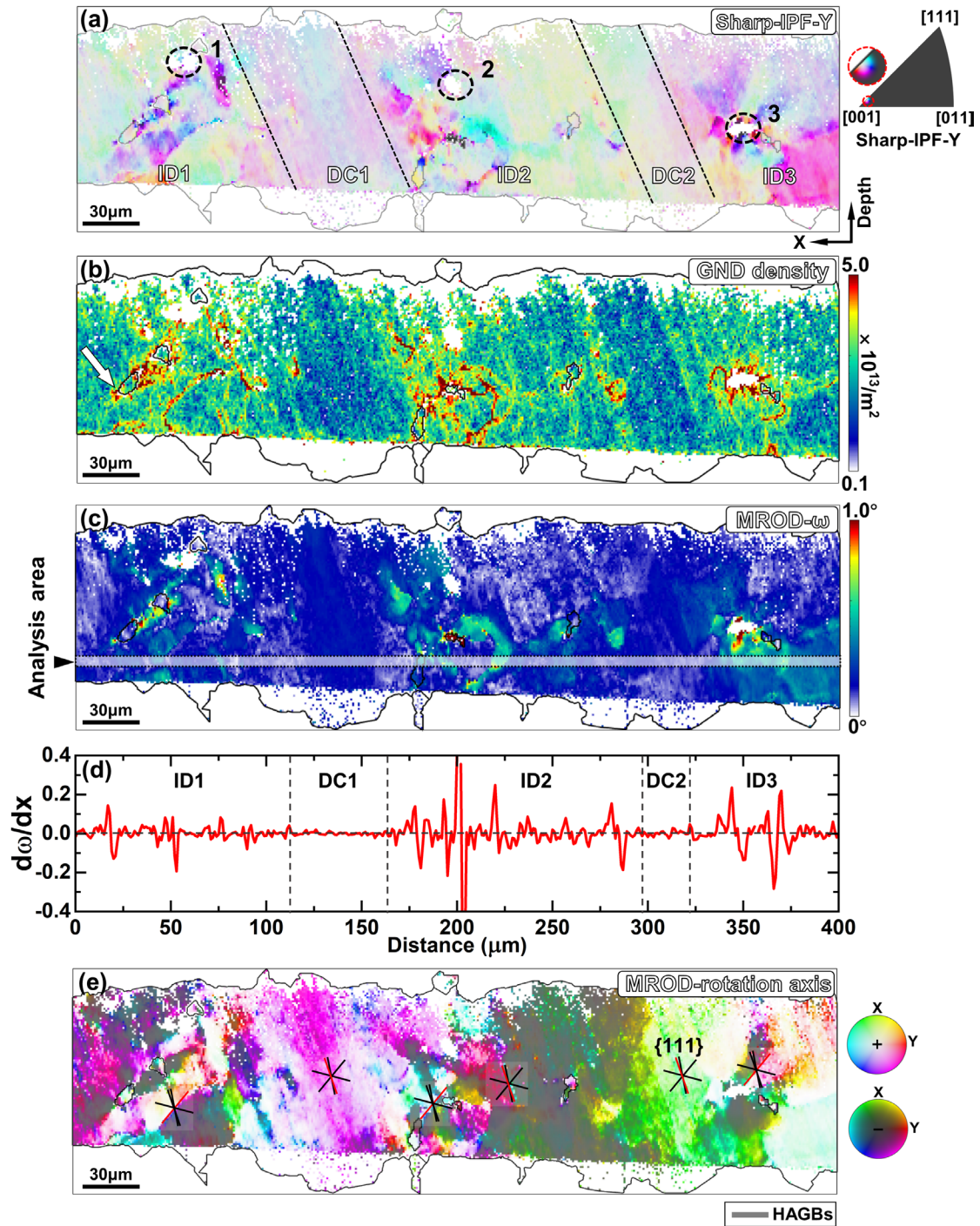
779 (depicted by the red dashed rectangle) includes three voids (outlined by blue dashed line) for registering

780 the μ-CT slice, with the lower semitransparent cross-section highlighting dendrites (DCs) and

781 interdendrites (IDs) subdivided by black dashed lines. (c) 3D morphology of intrinsic defects on the 3D-

782 μXRD cross-section.

783



784

785 **Fig. 5.** 3D- μ XRD crystallographic orientation fields. (a) IPF-Y within a $\sim 1^\circ$ range (Sharp-IPF-Y)

786 coloring map containing three registered voids, superimposed with HAGBs, DCs (DC1, DC2) and IDs

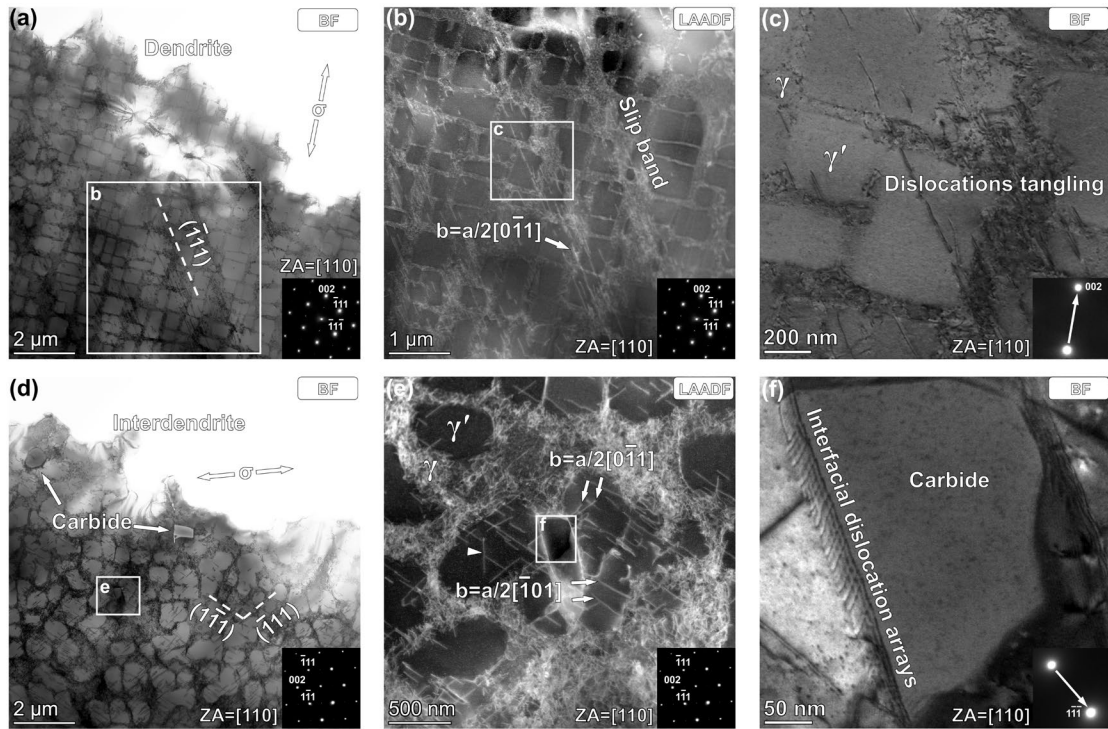
787 (ID1, ID2, ID3) are subdivided by black dashed lines. (b) GND density map. (c) MROD- ω map. (d)

788 Derivative of MROD- ω along the X-direction in a bright white dashed rectangle (indicated by the black

789 arrow in c). (e) MROD- ω axes map superimposed with {111} slip traces. X, Y, Z, and depth denote the

790 transverse, loading, normal, and 45° incidence directions concerning the sample surface in the specimen

791 frame.



792

793 **Fig. 6.** Dislocation configurations near the 3D- μ XRD cross-section. (a) BF STEM imaging in the DC.

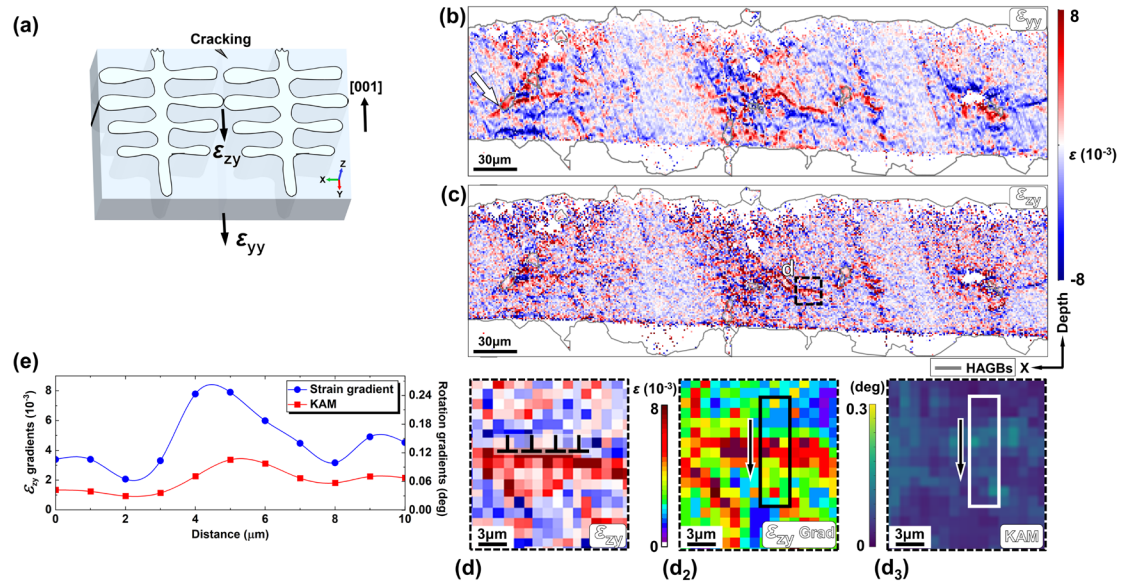
794 (b) LAADF STEM imaging of a magnified view in **a**. (c) BF STEM imaging of a magnified view in **b**.

795 (d) BF STEM imaging in ID. (e) LAADF STEM imaging of a magnified view in **d**. (f) BF STEM imaging

796 of a magnified view in **e**. Zone axis: [110] for **a-f**. g vector: [002] for **c** and $[\bar{1}\bar{1}\bar{1}]$ for **f**.

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800 **Fig. 7.** 3D- μ XRD elastic strain fields. (a) Schematic of elastic strain components in the sample frame.

801 (b) Normal elastic strain component ϵ_{yy} map. (c) Shear elastic strain component ϵ_{zy} map. (d) The

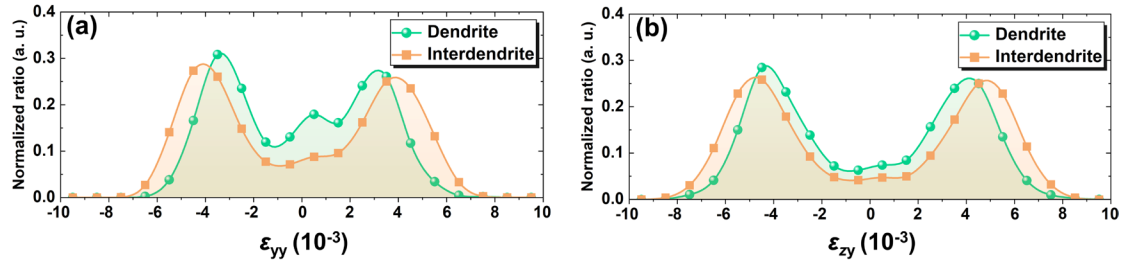
802 magnified view in **c** is superimposed with the dislocation pile-up configuration corresponding to the

803 tensile and compressive stress zones. (d₂) Shear elastic strain gradient (ϵ_{zy} Grad) map of **d**. (d₃) KAM

804 map of **d**. (e) Variations in ϵ_{zy} Grad and KAM across the elastic strain transition zone (indicated by black

805 and white rectangles in **d₂** and **d₃**), with arrows indicating increasing distance.

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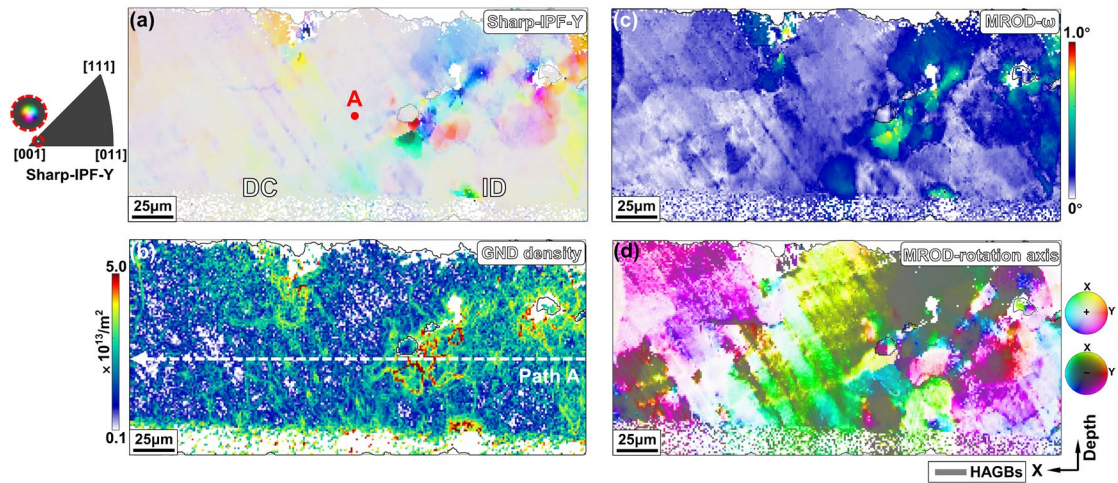


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Fig. 8. (a) Distribution of ε_{yy} in DCs and IDs. (b) Distribution of $\varepsilon_{z\gamma}$ in DCs and IDs.

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811 **Fig. 9.** 3D- μ XRD crystallographic orientation fields for samples interrupted at $\sim 40\%$ of LCF life. (a)

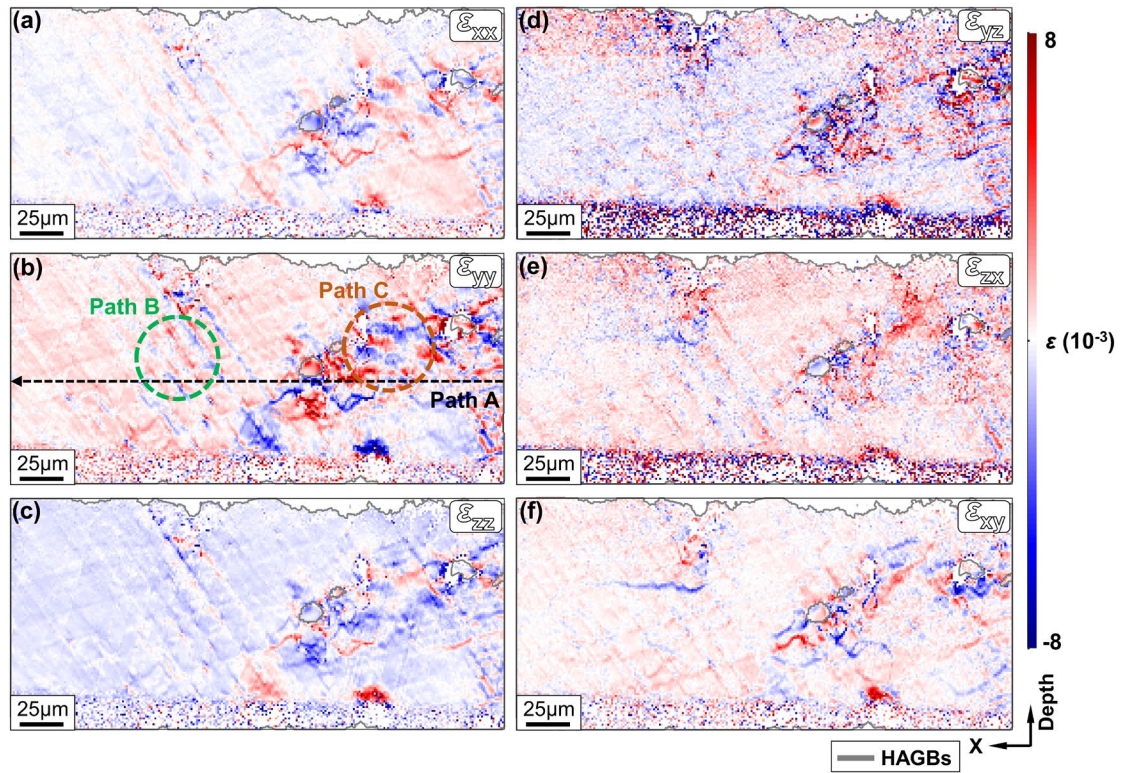
812 Sharp-IPF-Y coloring map, superimposed with HAGBs. DC and ID are subdivided by a black dashed

813 line. (b) GND density map. (c) MROD- ω map. (d) MROD- ω axes map. X, Y, Z, and depth denote the

814 transverse, loading, normal, and 45° incidence directions concerning the sample surface in the specimen

815 frame.

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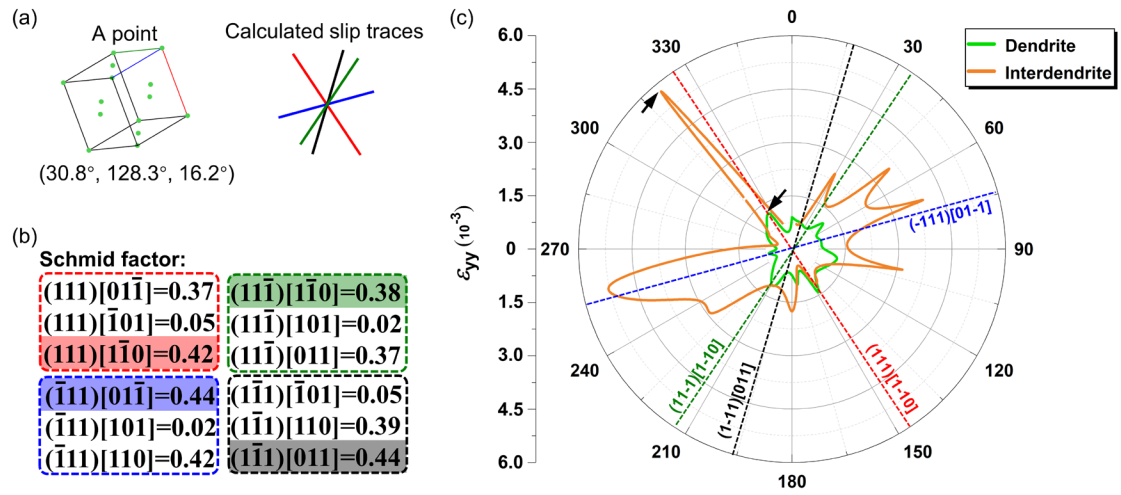


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818 **Fig. 10.** 3D- μ XRD elastic strain component maps for samples interrupted at $\sim 40\%$ of LCF life. (a) ϵ_{xx} .

819 (b) ϵ_{yy} . (c) ϵ_{zz} . (d) ϵ_{yz} . (e) ϵ_{zx} . (f) ϵ_{xy} .

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Fig. 11. Quantitative comparison of fatigue damage modes between DCs and IDs. (a) Slip traces

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calculated from the crystallographic orientation (Euler angles) at Point A in Fig. 9a. (b) Comparison of

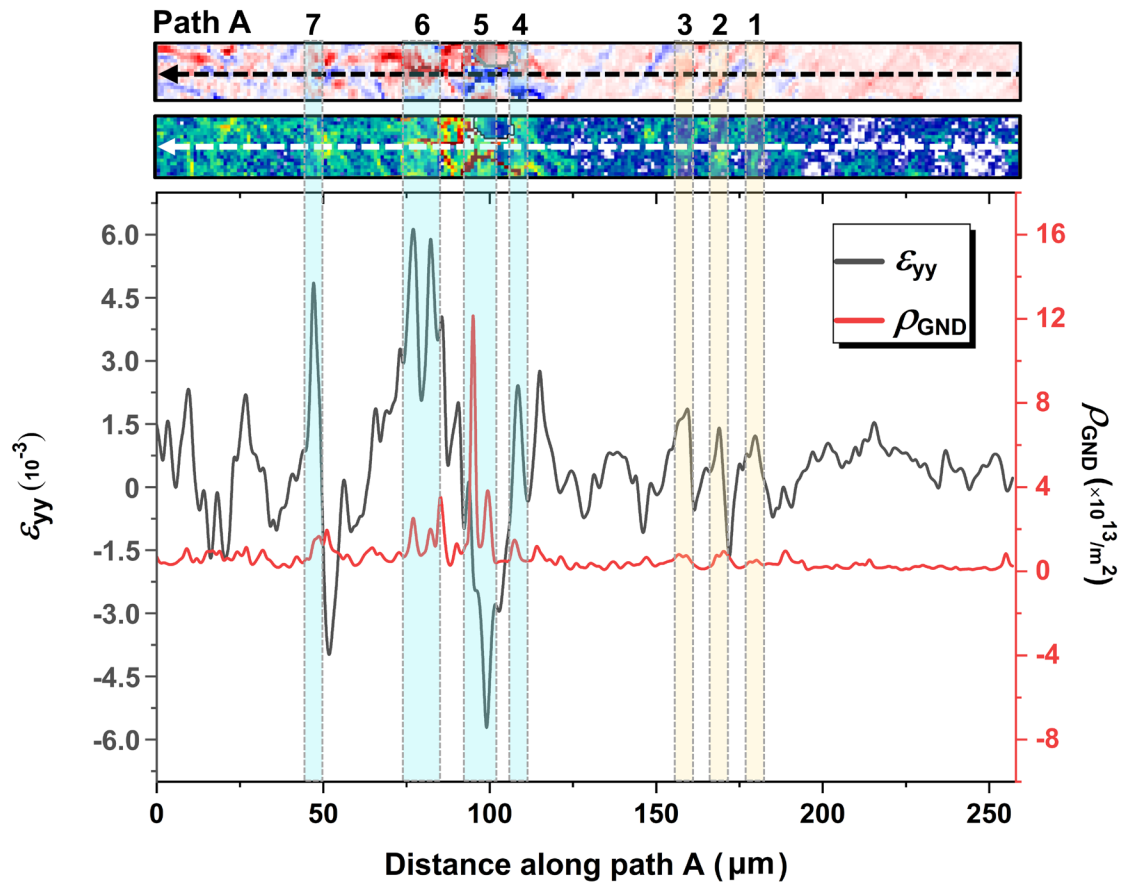
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the Schmid factors for different slip systems at Point A. (c) Comparison of the distributions of ϵ_{yy}

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(considering only tensile components) along Paths B and C in Fig. 10b, overlaid with slip traces.

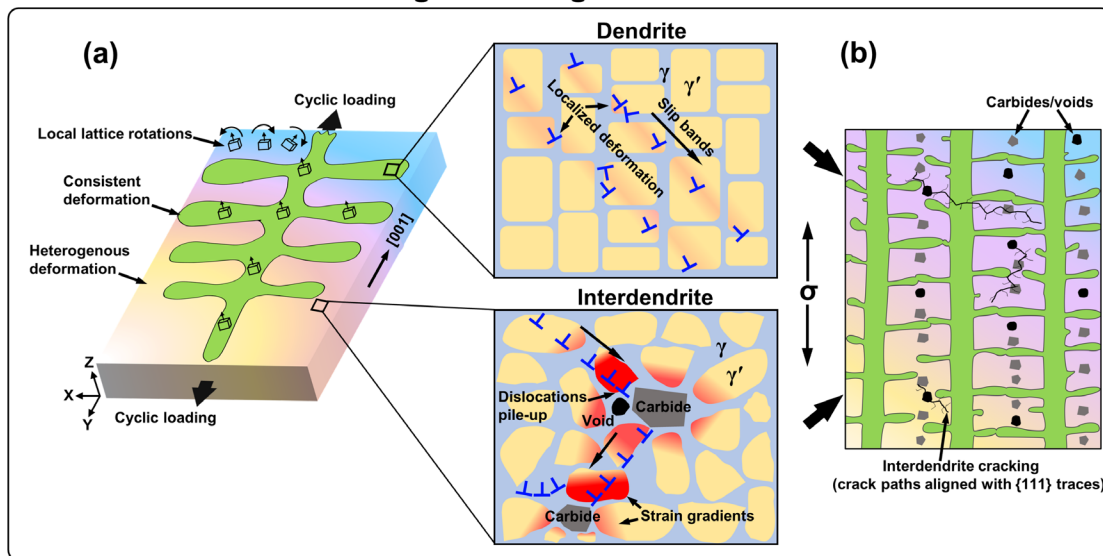
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828 **Fig. 12.** Quantitative comparison of ε_{yy} and GND density along Path A in Figs. 9b and 10b.

Fatigue damage mechanism



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830 **Fig. 13.** Schematic of the heterogeneous fatigue damage mechanism. (a) DCs represented by a
 831 homogeneous color indicating consistent orientation showcase a unidirectionally aligned dislocation
 832 configuration with a relatively mild banded elastic strain field. IDs characterized by varied colors
 833 suggesting fluctuating orientation reveal dislocation pile-ups from various slip systems and sharp elastic
 834 strain gradients around intrinsic defects. (b) Chain-like intrinsic defects within IDs can result in extensive
 835 fatigue cracking aligned with $\{111\}$ slip traces.

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Table 1. Chemical compositions of the Ni-SX superalloy DD413 (wt.%).

C	Cr	Co	W	Mo	Al	Ti	Ta	Ni
0.05~0.1	11.5~12.5	8.5~9.5	3.5~4.5	1.5~2.5	3.0~4.0	3.5~4.5	4.5~5.5	Bal.

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Table 2. Crystallographic parameters of the matrix and carbides.

Phase	Space group	lattice parameter/nm
MC carbide	Fm-3m	0.4340
γ	Fm-3m	0.3664
γ'	Pm-3m	0.3580

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Table 3. Detailed explanations of the main abbreviations in the text.

Acronyms	Interpretations
DC	Dendrite core region
ID	Interdendritic region
MROD- ω	Grain reference orientation deviation angle
GND	Geometrically necessary dislocation
KAM	Kernel average misorientation

844