

# Size and Stoichiometry Effects on the Reactivity of MoCy Nanoparticles Towards Ethylene

C. Jimenez-Orozco, J. A. Rodriguez

To be published in "Journal of Physical Chemistry C"

February 2021

Chemistry Department  
**Brookhaven National Laboratory**

**U.S. Department of Energy**  
USDOE Office of Science (SC), Basic Energy Sciences (BES) (SC-22)

Notice: This manuscript has been authored by employees of Brookhaven Science Associates, LLC under Contract No. DE-SC0012704 with the U.S. Department of Energy. The publisher by accepting the manuscript for publication acknowledges that the United States Government retains a non-exclusive, paid-up, irrevocable, world-wide license to publish or reproduce the published form of this manuscript, or allow others to do so, for United States Government purposes.

## **DISCLAIMER**

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or any third party's use or the results of such use of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof or its contractors or subcontractors. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

# Size and Stoichiometry Effects on the Reactivity of MoC<sub>y</sub> Nanoparticles Towards Ethylene

Carlos Jimenez-Orozco,<sup>\*a</sup> Marc Figueras,<sup>b</sup> Elizabeth Florez,<sup>a</sup> Francesc Viñes,<sup>b</sup> José A. Rodríguez,<sup>c</sup>  
Francesc Illas<sup>\*b</sup>

<sup>a</sup> *Universidad de Medellín, Facultad de Ciencias Básicas, Grupo de Materiales con Impacto (Mat&mpac), Carrera 87 No 30-65, Medellín, Colombia*

<sup>b</sup> *Universitat de Barcelona, Departament de Ciència de Materials i Química Física & Institut de Química Teòrica i Computacional (IQTCUB), c/ Martí i Franquès 1-11, 08028 Barcelona, Spain.*

<sup>c</sup> *Brookhaven National Laboratory, Chemistry Department, Upton, New York 11973, United States of America*

## Abstract

Molybdenum carbides are promising catalysts alternative to Pt-group metals for the hydrogenation of unsaturated hydrocarbons. Nanostructuring has been shown to be an efficient way to boost the catalytic activity of these materials with MoC<sub>y</sub> nanoparticles (NPs) exhibiting a good performance when encapsulated inside zeolites or dispersed on inert supports such as carbon or gold. Hereby, we focus on a systematic DFT study of the interaction of MoC<sub>y</sub> NPs with ethylene (C<sub>2</sub>H<sub>4</sub>), as a general and simple approach for examining binding and activation of C=C bonds. Models for 14 NPs, with a Mo/C ratio in the 0.67 to 2.00 range, have been built following a cascade procedure. Several chemical descriptors, including the adsorption energy, structural NPs distortion, C=C deformation, and C<sub>2</sub>H<sub>4</sub> attachment energy have been analyzed along with a meticulous geometric and electronic characterization of bare NPs and C<sub>2</sub>H<sub>4</sub> binding. The present results show that 1:1 stoichiometric Mo<sub>6</sub>C<sub>6</sub>, Mo<sub>12</sub>C<sub>12</sub>, and Mo<sub>24</sub>C<sub>24</sub>, and the non-stoichiometric Mo<sub>4</sub>C<sub>6</sub>, Mo<sub>8</sub>C<sub>12</sub> (MetCar), and Mo<sub>14</sub>C<sub>13</sub> (Nanocube) are excellent systems for the binding and activation of ethylene, exhibiting a much bigger reactivity than a bulk δ-MoC(001) surface with a similar Mo:C ratio. In addition, C<sub>2</sub>H<sub>4</sub> binding on the NPs with a Mo/C < 1.08 is advantageous since, apart from a rather large adsorption energy, implies low energy values for NPs deformation (from 0.00 to 0.31 eV), C=C distortion (from 0.30 to 0.52 eV), and C<sub>2</sub>H<sub>4</sub> attachment (from -2.12 to -2.58 eV). These theoretical results point to the ideal MoC<sub>y</sub> size and composition for C<sub>2</sub>H<sub>4</sub> binding, providing a background for further experimental studies aimed at the preparation of MoC<sub>y</sub> NPs as hydrogenation catalysts.

\* Corresponding authors: [cjimenez@udem.edu.co](mailto:cjimenez@udem.edu.co), [francesc.illas@ub.edu](mailto:francesc.illas@ub.edu)

## 1. Introduction

The use of catalysts is key for producing clean fuels and several commodities, particularly by means of hydrogenation reactions of C=C double bonds in olefins, where Pt, Pd, Ru, Rh, Os, and Ir—sometimes referred to as Pt-group elements—are so far the most used catalyst due to their good performance.<sup>1</sup> In practice, these metals are supported on oxides, zeolites, and activated carbon, and exhibit a high catalytic activity.<sup>2-11</sup> However, the scarcity of these metals in the Earth crust, together with their sensitivity to sulfur poisoning in the petrochemical industry, has motivated the search for alternative catalysts.<sup>2</sup>

Several studies have shown that transition metal carbides have excellent catalytic properties and appear as a good alternative to replace Pt-group based catalysts, especially on several hydrogenation reactions. Among them, molybdenum carbides are highlighted as promising materials, due to their remarkable interaction with hydrocarbons and with several successful applications in hydrogenation reactions.<sup>12-16</sup> Not surprisingly, several studies have been reported on the interaction of C<sub>2</sub>H<sub>4</sub> with molybdenum carbides surfaces, precisely to explore the capability of these materials as potential alternative catalysts to Pt-group metals.<sup>17-20</sup> The binding and hydrogenation of the ethynyl species on  $\delta$ -MoC(001) has also been considered,<sup>20</sup> since these species have been found to be responsible of poisoning in Pt-based catalysts. Interestingly, there is evidence that this material could avoid surface poisoning, in contrast to Pt and Pd extended surfaces.<sup>20</sup>

The good performance of molybdenum carbides in catalysis has triggered new research aimed at investigating their possible improvement by nanostructuring. Recently, Figueras *et al.*<sup>21</sup> presented experimental and theoretical evidence that MoC<sub>y</sub> nanoparticles supported on Au(111) can dissociate methane at room temperature. Additionally, this inverse catalyst system appears to be a good candidate for hydrogenation reactions as H<sub>2</sub> can easily dissociate and be stored on the supported nanoparticles<sup>22</sup> in a rather broad temperature range. Both, the activation of methane and the activity towards hydrogen suggest that these nanoparticles (NPs) could be useful for hydrogenation of olefins. In addition, MoC<sub>y</sub> NPs can be easily synthesized<sup>23</sup> thus overcoming the problems encountered when aiming at preparing MoC or Mo<sub>2</sub>C single crystal surfaces. Furthermore, it is known that MoC<sub>y</sub> NPs encapsulated inside zeolites or dispersed on supports such as carbon or oxides exhibit good catalytic properties.<sup>24-27</sup>

At the present time, very little is known about the intrinsic reactivity of MoC<sub>y</sub> NPs towards olefins or unsaturated hydrocarbons in general. The fact that the MoC<sub>y</sub> NPs are frequently dispersed on zeolites, oxides, metals and carbon-based supports raises the question about the possible influence of the substrate on their intrinsic chemical properties. To answer this question, we have carried out a computational study, based on density functional theory (DFT), aimed at examining the bonding and

activation of ethylene on a series of MoC<sub>y</sub> NPs with different shapes and Mo:C atomic ratios; ethylene can be taken as a model for larger olefins. Our results show that the MoC<sub>y</sub> NPs display a behavior which cannot be extrapolated from those seen for bulk  $\delta$ -MoC(001) and  $\beta$ -Mo<sub>2</sub>C(001) surfaces, with a substantial boost in chemical activity.

## 2. Nanoparticles Models and Computational Details

The interaction of ethylene (C<sub>2</sub>H<sub>4</sub>) with gas-phase MoC<sub>y</sub> NPs has been studied using a series of models of increasing size, considering also different stoichiometries, as shown in Figure 1. The NPs models contain up to 64 atoms where the Mo/C ratio varies from 0.67 to 2.00. Note that this comprises usual MoC and Mo<sub>2</sub>C stoichiometries, as well as C-rich NPs like the well-known Mo<sub>8</sub>C<sub>12</sub> MetCar. The initial stoichiometric structures of MoC<sub>y</sub> nanoparticles have been obtained from different sources. For instance, the Mo<sub>6</sub>C<sub>6</sub> and Mo<sub>12</sub>C<sub>12</sub> NPs have been gained by mimicking most stable gas-phase TiC NPs as previously reported.<sup>28</sup> These were acquired through data mining searches, global optimization using Interatomic Potentials (IP), and subsequent geometry optimization by DFT calculations. There, the authors reported a total of 21 low energy structures for each Ti<sub>6</sub>C<sub>6</sub> and Ti<sub>12</sub>C<sub>12</sub> stoichiometry. Here, these TiC NP structures have been used as templates, substituting Ti by Mo and fully re-optimizing the atomic structure using the methodology described below. Remarkably, the shape of most stable MoC<sub>y</sub> isomers of both sizes coincides with that of their TiC counterparts. This is not surprising as both TiC and the  $\delta$ -MoC polymorph exhibit the same rock-salt structure. This bottom-up approach revealed a quite fast convergence towards to cubic,  $\delta$ -MoC bulk-like shapes. Thus, a complementary top-down approach has been also considered creating cubic-like arrangements for Mo<sub>24</sub>C<sub>24</sub> and Mo<sub>32</sub>C<sub>32</sub> NPs, following a Wulff construction shape<sup>29</sup> and relying on the computed  $\delta$ -MoC surface energies.<sup>30,31</sup>

Moreover, non-stoichiometric NPs have been considered and built from different sources as well. First, the Mo<sub>8</sub>C<sub>12</sub> magic cluster, usually known as MetCar,<sup>32</sup> and the Mo<sub>14</sub>C<sub>13</sub> nanocube,<sup>33</sup> have been selected from the literature. Then, other small MoC<sub>y</sub> clusters have been considered through a cascade procedure, where for the two most stable isomers of Mo<sub>6</sub>C<sub>6</sub> and Mo<sub>12</sub>C<sub>12</sub> all inequivalent atoms have been sequentially removed generating different Mo<sub>x-1</sub>C<sub>x</sub> or Mo<sub>x</sub>C<sub>x-1</sub> structures. After optimizing the resulting structures, the cascade procedure is repeated to reach suitable structures for other Mo/C ratios. This methodology approximately scales as  $2 \cdot N^Z$  per removal, where N is the average number of inequivalent atoms per removal, Z states for the number of atoms that have been already removed, and the coefficient 2 is necessary as there are two different kinds of species. For instance, seven inequivalent C atoms exist for the most stable Mo<sub>12</sub>C<sub>12</sub> isomer. Thus, removing one atom leads to 7 structures and a second removal leads to 49 new structures that need to be considered for subsequent geometry optimization. In any case, the actual number of isomers to explore on each

batch depends on the new number of inequivalent atoms, yet the adoption of particularly symmetric shapes may reduce this number. Regardless of the previous, the  $2 \cdot N^Z$  expression should be taken as an upper bound. Clearly, a full cascade procedure becomes computational prohibitive for  $Z$  larger than two, especially for larger NPs such as  $\text{Mo}_{12}\text{C}_{12}$ . Thus, further  $Z$  steps have been explored only departing from the  $Z-1$  most stable isomer. This strategy is not entirely arbitrary, as systematically for the first round the most stable isomers are obtained from previous most stable ones.

The total energy of the studied  $\text{MoC}_y$  models described in the previous subsection has been obtained through periodic Density Functional Theory (DFT) calculations using large enough supercells so that the interaction between the periodically repeated nanoparticles become negligible. Thus, the  $\text{MoC}_y$  nanoparticles have been placed inside a large cubic box, ensuring a minimum vacuum region of 10 Å in all directions and, obviously, considering the  $\Gamma$  point only. The calculations were carried out using the Vienna *Ab Initio* Simulation Package (VASP) code,<sup>34</sup> employing the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional,<sup>35</sup> as found to be especially well-suited in the description of Mo-based carbides.<sup>36</sup> In addition, the contribution of dispersion terms was accounted adding the Grimme D3 correction, *i.e.* PBE-D3,<sup>37</sup> especially adequate for the interaction of molecules with such molybdenum carbide systems.<sup>19,36,38,39</sup> The Kohn-Sham equations were solved by expanding the valence electron density in a plane-wave basis set with 415 eV cutoff whereas the effect of the inner electrons in the valence electron density has been taken into account by the Projected Augmented Wave (PAW) method<sup>40</sup> as implemented by Kresse and Joubert.<sup>41</sup> The convergence criteria were changes in total energies lower than  $10^{-5}$  eV and variations in interatomic forces lower than  $0.01 \text{ eV} \cdot \text{\AA}^{-1}$ . With this setup, total energies converge below the chemical accuracy of  $1 \text{ kcal} \cdot \text{mol}^{-1}$  —*i.e.*  $\sim 0.04 \text{ eV}$ .

Regarding the approach used to choose of the structures of the  $\text{MoC}_y$  NPs described above, one must acknowledge recent proposals in the literature aimed at exploring the landscape for several isomers.<sup>42-44</sup> These rely on geometry optimization and consideration of low-lying isomers, being able to scrutinize the role of possible higher energy isomers in a given reaction at a given temperature. These approaches can provide detailed information about the contribution of each isomer to the overall reactivity. Nevertheless, the importance of high energy isomers becomes relevant for subnanometer NPs only and, in general, becomes less and less important for larger NPs where the energy difference between structural isomers gradually increase with the NP size, see Table S1 of the SI. In addition, exploring the importance of different isomers for a set of nanoparticles becomes computationally too demanding and is, hence, beyond of the scope of the present work. Yet, the present approach, focusing on relatively low energy isomers, hopefully close to the global minima, allows one to extract meaningful information about the chemistry of these catalytically active  $\text{MoC}_y$

nanoparticles. Consequently, for each stoichiometry, the most stable cluster was selected to analyze the interaction with ethylene.

Once the optimum structure of the MoC<sub>y</sub> NPs has been obtained, the interaction of each of them with the C<sub>2</sub>H<sub>4</sub> molecule has been studied using the same computational setup. All conceivable binding sites and connectivities have been explicitly considered. The notation for the adsorption modes is as earlier reported.<sup>17,18,45</sup> Briefly,  $\pi$ -M relates to ethylene binding atop of a metal site; di- $\sigma$ -MM, di- $\sigma$ -CM, and di- $\sigma$ -CC correspond to the binding bridging metal-metal, carbon-metal, and carbon-carbon bond, respectively and; finally,  $\sigma$ -M,  $\mu$ -M stands for a situation in which one has one C atom of C<sub>2</sub>H<sub>4</sub> atop of a metal atom ( $\sigma$ -M) and one C<sub>2</sub>H<sub>4</sub> C atom located perpendicularly atop of a M-M bridge ( $\mu$ -M). For every NP, several initial adsorption geometries were evaluated to cover all binding possibilities, so that a complete scanning of the potential energy surface for C<sub>2</sub>H<sub>4</sub> binding in every NP can be assured. In total, the number of studied initial adsorption geometries was of *circa* 500. The final structures —bare nanoparticles and nanoparticles with adsorbed ethylene— were characterized as energy minima in the potential energy surface through pertinent vibrational analysis. The vibrational frequencies were gained within the harmonic approximation, accounting only the adsorbate vibrational frequencies, obtained through the building up and diagonalization of the Hessian matrix, constructed by finite differences of analytical gradients with atomic displacements of 0.03 Å.

The ethylene adsorption energy,  $E_{\text{ads}}$ , was calculated as

$$E_{\text{ads}} = E_{\text{C}_2\text{H}_4/\text{MoC}_y} - E_{\text{MoC}_y} - E_{\text{C}_2\text{H}_4} \quad (1),$$

where  $E_{\text{C}_2\text{H}_4/\text{MoC}_y}$  stands for the energy of the system with the C<sub>2</sub>H<sub>4</sub> adsorbed on the MoC<sub>y</sub> NP, the term  $E_{\text{MoC}_y}$  refers to the MoC<sub>y</sub> optimized energy, while  $E_{\text{C}_2\text{H}_4}$  represents the isolated ethylene molecular energy. The first and third terms in Eq. (1) include the ethylene related vibrational Zero-Point Energy (ZPE) contribution.

To investigate the bonding between ethylene and the MoC<sub>y</sub> nanoparticles, a Charge Density Difference (CDD) analysis,  $\Delta\rho$ , has been carried out, along with the Electron Localization Function (ELF). In the CDD  $\Delta\rho$  is defined as

$$\Delta\rho = \rho_{\text{C}_2\text{H}_4/\text{MoC}_y} - \rho_{\text{MoC}_y} - \rho_{\text{C}_2\text{H}_4} \quad (2),$$

where  $\rho_{\text{C}_2\text{H}_4/\text{MoC}_y}$  refers to the electron density of the ethylene adsorbed on the MoC<sub>y</sub> NP, and  $\rho_{\text{MoC}_y}$  and  $\rho_{\text{C}_2\text{H}_4}$  correspond the electron density of the nanoparticle and ethylene at the geometry they have in the adsorbed minimum. In addition, net charges on the adsorbed molecule are also obtained through the Atoms-in-Molecules topological analysis of Bader.<sup>46</sup>

### 3. Results and discussion

#### 3.1. Geometry and characterization of bare $\text{MoC}_y$ nanoparticles

In Figure 1, the arrangement of carbon and molybdenum atoms within the  $\text{MoC}_y$  NPs is found to be different for each Mo/C ratio, and even for the same Mo/C ratio the relaxed geometries can be completely different. Thus, being in the non-scalable regime of NPs sizes,<sup>29,47</sup> their performance towards the binding of adsorbates is expected to be significantly different between the explored NPs. The geometries for the most stable structures of each of the 14  $\text{MoC}_y$  NPs are the ones displayed in Figure 1. In order to separate stoichiometry from size effects, the  $\text{MoC}_y$  NPs analysis is split into stoichiometric and non-stoichiometric cases. The employed descriptors to unveil the properties of bare NPs are formation energies, computed taking the energy per atom in bulk Mo and graphite as atomic references, respectively —see Figure S1 and Table S2 of the SI— and the band gap, see Tables S2 and S3 of SI, which open the door towards the geometry and electronic properties characterization, respectively.

As far as stability is concerned, we first focus on the formation energy,  $E_{\text{form}}$ , as this quantity provides an estimate of the thermodynamic stability of a given NP, either stoichiometric or not. However, to have a meaningful comparison it is convenient to somehow normalize this quantity. For the stoichiometric NPs this can be done simply by considering  $E_{\text{form}}$  per MoC unit —*i.e.*  $E_{\text{form}}/\text{N}$ —. Here, a clear size effect is found where  $E_{\text{form}}$  linearly decreases as the size grows, see Table S2 and Figure S1 in SI. Interestingly, the band gap,  $E_{\text{gap}}$ , estimated in an approximate way from the Kohn-Sham orbital energies, exhibits a much less marked dependence with respect to the NP size and irrespective of whether these are stoichiometric or not; see Tables S2 and S3 in SI. For all NPs  $E_{\text{gap}}$  is close to 0.15 eV although with some oscillations of the energy levels that eventually lead to the valence and conduction band limits. In any case, from the calculated  $E_{\text{gap}}$  for these NPs, it is clear that they are still a bit far from metallic character predicted for the extended  $\delta$ -MoC (001) surface.<sup>31</sup> Test studies were carried out for  $\text{Mo}_6\text{C}_6$  and the MetCar, which are representative of stoichiometric and non-stoichiometric NPs, to calculate  $E_{\text{gap}}$  using the range-separated hybrid HSE06 functional. In both cases, the changes with respect to the PBE value are of 0.01 eV only.

Assuming that the frontier orbitals dominate the chemistry of these NPs, one would deduce that the binding of adsorbates on stoichiometric NPs in the range from  $\text{Mo}_6\text{C}_6$ , to  $\text{Mo}_{32}\text{C}_{32}$  will be quite similar. However, the adsorbate binding strength does also depend on other factors, including *i)* the adsorbate nature, *ii)* the electronic arrangement with respect the NP model, *iii)* the anchoring site, and even *iv)* the adsorbate molecular conformation.



### 3.2. $C_2H_4$ adsorbed on $MoC_y$ nanoparticles

Once all 14 stoichiometric  $MoC_y$  NPs were described, a thorough exploration sampling *ca.* 500 different initial  $C_2H_4$  adsorption geometries was performed, covering all conceivable binding possibilities, revealing 221 final topologically different structures. The subsequent analysis, however, focuses on most stable adsorption conformation for each NP, as summarized in Table 1, and shown in Figure 2. Note that, for each case, the second most stable adsorption conformations are located more than 0.1 eV higher in energy —see Table S5 in SI—, with the sole exception of the MetCar, with rotated conformers around the NP tetrahedron vertex axis. Indeed, in most of the explored NPs, the second isomer is less stable by at least 0.2 eV, a behavior observed in 62% of the NPs listed in Table S5. However, one must advert that in 38% of NPs the adsorption conformations for both first and second most stable adsorption modes should be thermally accessible at the high temperatures typical in catalytic experiments; particularly, for  $C_2H_4$  binding on  $Mo_5C_6$ ,  $Mo_{12}C_8$ ,  $Mo_{12}C_{10}$ ,  $Mo_8C_{12}$ , and  $Mo_{32}C_{32}$ . Therefore, future studies should carefully address the existence of low lying isomers and possibly include them whenever considering the reactivity of these systems. For NPs with a 1:1 atomic ratio, the  $E_{ads}$  values are sensibly stronger than on the  $\delta$ - $MoC(001)$  surface, but within the range of values found for C- and Mo-terminated surfaces of  $\beta$ - $Mo_2C(001)$  surfaces, as seen in Figure 3. The results in this figure indicate that the binding capabilities of the  $MoC_y$  NPs cannot be extrapolated from the behavior of the bulk  $\delta$ - $MoC(001)$  and  $\beta$ - $Mo_2C(001)$  surfaces.

For comparison purposes, the  $C_2H_4$  adsorption on extended  $\delta$ - $MoC(001)$  and C- and Mo-terminated  $\beta$ - $Mo_2C(001)$  surfaces, denoted as  $\beta$ - $Mo_2C(001)$ -C and  $\beta$ - $Mo_2C(001)$ -Mo, are included in Table 1.<sup>17-19</sup> The adsorption energies,  $E_{ads}$ , on the NPs are in the -1.54 to -2.88 eV range, comparable to the strong binding on polar  $\beta$ - $Mo_2C(001)$ -Mo surfaces, ranging -1.63 to -2.50 eV. On the other hand, the  $E_{ads}$  on polar  $\beta$ - $Mo_2C(001)$ -C —with  $E_{ads}$  from -1.29 to -1.49 eV— and on the  $\delta$ - $MoC(001)$  surfaces —with  $E_{ads}$  up to -1.03 eV— are clearly weaker than on the studied NPs. Thus, the  $C_2H_4$   $E_{ads}$  binding strength decays as  $\beta$ - $Mo_2C(001)$ -Mo  $\approx$  NPs  $>$   $\beta$ - $Mo_2C(001)$ -C  $>$   $\delta$ - $MoC(001)$ . Notice that for the latter, the most stable reconstructed surface has been used as reference.<sup>21</sup> Interestingly, the reported values for  $C_2H_4$  adsorption energy on a Pt(111) surface, -1.78 eV,<sup>45</sup> and on  $Pt_x$  ( $x = 7 - 10$ ) clusters, ranging from -1.4 to -1.7 eV,<sup>48,49</sup> are within the range found in this work for the  $MoC_y$  NPs. Notice that the adsorption energy on platinum clusters and the Pt(111) surface is very similar which is in agreement with their similar catalytic performance towards ethylene hydrogenation.<sup>50</sup> In other words, nanostructuring Pt could not be advantageous for this particular hydrogenation process. However, a different behavior exists when comparing ethylene adsorption on  $MoC_y$  NPs and on TMC surfaces, where the current work is the basis to further explore this possibility.

Analyzing the adsorptive landscape in Table 1, the most common binding mode is  $\pi$ -M, closely followed by  $\sigma$ -M,  $\mu$ -M, unfolding the main role played by Mo metal centers. The analogous

geometry sites for binding on surfaces<sup>17,18</sup> is shown in Figure 4. Metal sites involved in bridge di- $\sigma$ -CM are dominant on Mo<sub>10</sub>C<sub>12</sub> and Mo<sub>32</sub>C<sub>32</sub>, while bridge di- $\sigma$ -CC is only found for Mo<sub>5</sub>C<sub>6</sub> case. Indeed, C-interaction is only found for Mo/C ratio of 0.8, with the sole exception of the Mo<sub>32</sub>C<sub>32</sub> nanoparticle. The C<sub>2</sub>H<sub>4</sub> preference towards Mo seems to be ruled by its lower electronegativity compared to C.<sup>24</sup>

The strong C<sub>2</sub>H<sub>4</sub> adsorption on the NPs implies an elongation of the C=C double bond,  $d(\text{CC})$ , estimated to be 1.33 Å in gas phase. The  $d(\text{CC})$  thus elongates from 0.09 to 0.25 Å for the studied NPs, see values in Table 1 and Table S4, and the largest elongations are found for MoC<sub>y</sub> NPs involving C binding modes, such as in Mo<sub>5</sub>C<sub>6</sub>, Mo<sub>10</sub>C<sub>12</sub>, and Mo<sub>32</sub>C<sub>32</sub>, with elongations of 0.22 to 0.25 Å. The C<sub>2</sub>H<sub>4</sub> binding involving two Mo sites *via*  $\sigma$ -M,  $\mu$ -M mode display still moderate elongations of 0.15–0.18 Å, while  $\pi$ -M mode has a smaller, yet still noticeable lengthening of 0.09–0.10 Å. In this sense, the C<sub>2</sub>H<sub>4</sub> carbon-carbon bond length distortion decreases with the binding mode as di- $\sigma$ -CC, di- $\sigma$ -CM >  $\sigma$ -M,  $\mu$ -M >  $\pi$ -M. Notice in Table 1 that  $d(\text{CC})$  bond length elongations are linked to the adsorption mode, rather than to its strength.

### 3.3. Analysis of C<sub>2</sub>H<sub>4</sub> interaction with stoichiometric MoC<sub>y</sub> NPs

In this section we analyze the chemical nature of C<sub>2</sub>H<sub>4</sub> adsorption on stoichiometric MoC<sub>y</sub> NPs. At first sight, there is no clear trend for adsorption energy evolution with respect NP size, having ups and downs, as seen in Figure 5. This behavior could be explained because the interaction is a balance of energy contributions, including: *i*) the C<sub>2</sub>H<sub>4</sub> distortion energy when adsorbed,  $E_{dis}$ , as seen in the elongated  $d(\text{CC})$  values of Table 1; *ii*) the NP deformation energy,  $E_{def}$ , so as to better accommodate the C<sub>2</sub>H<sub>4</sub> moiety and the concomitant changes in the NP; and *iii*) the resulting attachment energy,  $E_{att}$ , as the binding energy of the distorted C<sub>2</sub>H<sub>4</sub> on the deformed MoC<sub>y</sub> NP, following a lock-and-key anchoring. The three different contributions are listed in Table S6 of the SI, revealing that the oscillations in the  $E_{ads}$  are also observed in the  $E_{att}$ , which is reminiscent of the fact that the studied NPs are in the non-scalable regime.<sup>29</sup> In any case, a slight trend is observed in Figure 5, as  $E_{ads}$  decreases as the NP size increases. Here the size is measured by  $N^{-1/3}$ ,  $N$  being the number of MoC units—see also Table S7 in SI—. Figure 5 also reports the effect of non-stoichiometry for Mo<sub>6</sub>C<sub>6</sub> and Mo<sub>12</sub>C<sub>12</sub>, where it clearly can be stated that the presence of Mo or C vacancies strengthen the adsorption.

Apart from the  $E_{ads}$  evolution, the size and attachment energy are useful descriptors to unveil the behavior of stoichiometric NPs as shown in Figure 6. Overall, an increase in size leads to a lowering of the  $E_{att}$ , with the sole outlier of Mo<sub>32</sub>C<sub>32</sub>, which has as a different signature displaying a di- $\sigma$ -CM C<sub>2</sub>H<sub>4</sub> mode, while others have a  $\pi$ -M mode. Indeed, the second most stable structure in Mo<sub>32</sub>C<sub>32</sub> is a  $\pi$ -M mode, shown in gray color in Figure 6, and nicely fitting to the trend, to the point

of being almost linear with a regression coefficient,  $R^2$ , of 0.96. Another distinct point for  $\text{Mo}_{32}\text{C}_{32}$  is that the  $E_{dis}$  relates to a decrease of charge for the adsorbed  $\text{C}_2\text{H}_4$  moiety, given the formation of a C–C covalent bond, see CDD and ELF plots in the Figure S2 of the SI.

Regarding Figure 5 again, one could argue that solely the  $\text{Mo}_{24}\text{C}_{24}$  NP is an outlier in the observed trend. This exception may obey to its particular atomic structure. Even if while comparing to  $\text{Mo}_{12}\text{C}_{12}$  both the adsorption mode and the  $d(\text{CC})$  elongations are similar, the  $\text{Mo}_{24}\text{C}_{24}$  NP is more symmetric, leading to a negligible NP distortion upon  $\text{C}_2\text{H}_4$  adsorption, see Figure 6. However, the charge transfer from the  $\text{MoC}_y$  NP to the  $\text{C}_2\text{H}_4$  molecule is quite large for  $\text{Mo}_{12}\text{C}_{12}$  and  $\text{Mo}_{24}\text{C}_{24}$  only;  $-0.30 e$  for both cases, while for  $\text{Mo}_6\text{C}_6$  and  $\text{Mo}_{32}\text{C}_{32}$  NPs the charge transfer from the adsorbate is below  $-0.15 e$ . Interestingly, the distortion energy is the same, 0.30 eV, for both  $\text{Mo}_{12}\text{C}_{12}$  and  $\text{Mo}_{24}\text{C}_{24}$  NPs. Overall, the maximum in  $E_{ads}$  relates to the minimum in  $E_{dis}$ . Therefore, the different  $\text{Mo}_{24}\text{C}_{24}$  behavior obeys to its strong stability, favoring a higher charge transfer towards  $\text{C}_2\text{H}_4$ , and requiring a lower energy for elongating the  $\text{C}_2\text{H}_4$  C=C bond. In fact, among all the 14 evaluated NPs, the distortion of  $\text{Mo}_{24}\text{C}_{24}$  NP is almost negligible. Furthermore, the use of another descriptor other than the adsorption energy could help to understand the trends from  $\text{Mo}_6\text{C}_6$  to  $\text{Mo}_{24}\text{C}_{24}$ . An increase in size leads to a drop in  $E_{att}$ , following a clear linear trend, although with  $R^2 = 0.90$  only, within the studied range, having a clearer behavior compared to the adsorption energy.

### 3.4. Analysis of $\text{C}_2\text{H}_4$ interaction with non-stoichiometric $\text{MoC}_y$ NPs

Several of the studied NPs are non-stoichiometric, with a Mo/C ratio in the range of 0.67–2.00. Even though the diversity in terms of geometries and Mo/C ratios, the systems with  $\text{Mo/C} < 1$ , see top of Figure 7, top, exhibit  $E_{ads}$  within the -1.78 to -1.98 eV range, *i.e.* in a narrow range of 0.20 eV. For the cases with  $\text{Mo/C} > 1$ , the binding energy variations are in the -1.76 to -2.88 eV range, *i.e.* in a broader range of 1.12 eV. Clearly, a large diversity is found for the latter cases. Aside from that, the decrease in the NPs size does not imply a clear trend in terms of the adsorption energy, and the only note of distinction are particular reconstructions as observed on the  $\text{Mo}_4\text{C}_6$  and  $\text{Mo}_5\text{C}_6$  NPs cases, see Figures S3 and S4 in the SI, forcing an  $sp^3$  hybridization of  $\text{C}_2\text{H}_4$  C atoms in the former, and the formation of C–C bonds in the latter. Notice that the catalyst reconstruction is an important issue that should be addressed, specially when in small NPs as recently reported by Sun *et al.*<sup>51</sup> Therefore, in further studies related to ethylene hydroconversion, the NPs reconstruction must be considered, particularly for the smallest ones.

For four Mo/C ratios —0.67, 0.83, 1.20, and 1.50—, there are particularly two different structures for each case, with different size; e.g.  $\text{Mo}_5\text{C}_6$  and  $\text{Mo}_{10}\text{C}_{12}$  for the case of  $\text{Mo/C} = 0.83$ . As generally seen in the top of Figure 3, the larger the size —in terms of C content—, the weaker the  $\text{C}_2\text{H}_4$  binding energy, where by doubling the size the  $E_{ads}$  weakens  $\sim 0.2$  eV, except for the  $\text{Mo/C} = 1.50$

ratio, where the drop is  $\sim 1$  eV. Thus, it seems that size effects get pronounced particularly at Mo/C ratio larger than 1.20. Even though the major change in  $E_{ads}$  corresponds to NPs with Mo/C=1.50 ratio,  $E_{def}$  values are merely 0.06 eV; quite small compared to the values for Mo/C=0.83 of 0.58 eV, see top of Figure 3. This difference seems to be linked to a different adsorption mode. For Mo/C=1.50, the  $C_2H_4$  binding mode is  $\pi$ -M, while for Mo/C=0.83 di- $\sigma$ -CC and di- $\sigma$ -CM modes. The  $C_2H_4$  interaction on 75% of the non-stoichiometric NPs has a distortion energy of  $\sim 0.2$  eV, in the range of ratio Mo/C = 0.67–2.00, with the sole exception of  $Mo_6C_4$ , that with a deformation energy of 0.07 eV could be negligible, implying an almost rigid NP structure upon  $C_2H_4$  adsorption.

Among the evaluated NPs,  $E_{dis}$  is above 1 eV for several cases, which may not be advantageous for further hydrogenation reactions as could imply the breaking of the C=C bond. However,  $E_{dis}$  is lower than 0.53 eV for the particular Mo/C ratios of 0.67, 1.00, and 1.08. It is worth to mention that  $E_{dis}$  and  $E_{att}$  follow a similar trend as a function of Mo/C ratio. Hence,  $E_{att}$  depends on  $E_{dis}$ , which is thus a better descriptor than the adsorption energy. Therefore, the NPs attachment energies should also follow *Le Sabatier's* principle, *i.e.* the  $C_2H_4$  binding should be not too strong, as ethylene could remain molecularly adsorbed or dissociated on the NP, nor too weak, as  $C_2H_4$  could not get hydrogenated. Moreover,  $C_2H_4$  should bind on the  $MoC_y$  NPs with moderate activated  $E_{dis}$  while having a low NP deformation,  $E_{def}$ . The NPs which comply with the previous criteria are  $Mo_4C_6$ ,  $Mo_8C_{12}$  (MetCar) and  $Mo_{14}C_{13}$  (Nanocube), together with stoichiometric  $Mo_6C_6$ ,  $Mo_{12}C_{12}$ , and  $Mo_{24}C_{24}$  systems.

Aside from the previous considerations, the interaction of  $C_2H_4$  with the NP triggers a charge transfer from the NP to ethylene, see bottom of Figure 7. Such accumulated charge in the adsorbed  $C_2H_4$  increases with the Mo/C ratio, *i.e.* with an enrichment of Mo atoms in the system. Indeed, the amount of Mo in the NPs modulates their activity towards different elements in diverse chemical environments.<sup>24</sup> This behavior relates to the NP  $E_{def}$  and  $C_2H_4$   $E_{dis}$  energies, with an oscillating profile, pointing to a convergence towards the surface for bigger sizes, see Figure S5 of the SI. This rapidly oscillating behavior is typical of small NPs,<sup>29</sup> but increasing the number of Mo favors convergence, particularly from  $Mo_{12}C_6$  onwards.

Focusing on the largest non-stoichiometric NPs, *i.e.* the  $Mo_{12}C_x$ , the Mo enrichment over the stoichiometric point modulates the chemical activity of Mo atoms towards the carbons of  $C_2H_4$ , as seen by a major extent of charge transfer from the NP Mo atoms towards  $C_2H_4$ , see bottom of Figure 7. For the  $Mo_{12}C_x$  based NPs, the increase of the Mo/C ratio leads to a rise in the  $E_{ads}$ , see top of Figure S6 in the SI. In other words, the NP size decrease and the larger share of Mo atoms leads to an increase of the  $C_2H_4$  adsorption. The C=C bond in  $C_2H_4$  gets also activated in  $Mo_{12}C_x$  systems, but its extent is different only for the stoichiometric NP, being 0.09 Å, and similar for the rest of ratios, in the 0.15–0.17 Å range. This behavior is also related to the  $E_{dis}$ , which in turn relates to the

Bader charge on the adsorbate, see Figure S6 in the SI, showing that an increase in the Mo/C ratio favors a higher charge transfer from the NPs to C<sub>2</sub>H<sub>4</sub>.

above 1.08 are not advantageous for activating C<sub>2</sub>H<sub>4</sub>, even if key in hydrogenation processes. Increasing the Mo/C ratio up to 1.5 implies higher  $E_{def}$  and  $E_{dis}$  with concomitant lower  $E_{att}$  as in going from Mo<sub>12</sub>C<sub>6</sub> to Mo<sub>12</sub>C<sub>12</sub>. Therefore, the only desired ratios to bind ethylene are 1.00 and 1.08, *i.e.* having only a small content of C-deficiencies or, in other words, as close to stoichiometry as possible.

The results for the MetCar highlight another complex interplay between the Mo/C ratio and the chemical properties of a MoC<sub>y</sub> NP. In this C-rich system, there are 1.5 atoms of C per each Mo atom, but the special structure and electronic properties of the NP allow it to bind ethylene better than  $\delta$ -MoC(001) or  $\beta$ -Mo<sub>2</sub>C(001)-C surfaces. In the structure of the MetCar, Figures 1 and 2, multiple bonds exist between the carbon atoms and the system exhibits C<sub>2</sub> dimers. It has been argued that the presence of C<sub>2</sub> dimers leads to special chemical properties.<sup>52,53</sup> With the exception of Mo<sub>4</sub>C<sub>6</sub>, C<sub>2</sub> dimers are not present in the other MoC<sub>y</sub> NPs examined neither in the bulk  $\delta$ -MoC(001) nor in  $\beta$ -Mo<sub>2</sub>C(001) surfaces. Nevertheless, it is worth to mention that the C<sub>2</sub> dimers in Mo<sub>4</sub>C<sub>6</sub> and the MetCar have different nature. In Mo<sub>4</sub>C<sub>6</sub> these are formed upon interaction with ethylene as product of a significant structural rearrangement, see Figure S4 in SI, with a concomitant energy lowering of 0.6 eV. On the contrary, the isolated MetCar structure already contains C<sub>2</sub> dimers and, upon interaction with C<sub>2</sub>H<sub>4</sub>, the structure is not reconstructed. Therefore, the reactivity of the MetCar obeys not only to the presence of C<sub>2</sub> dimers, but also to its particular pyramidal-like geometry. Among the evaluated NPs, only Mo<sub>4</sub>C<sub>6</sub> and Mo<sub>5</sub>C<sub>6</sub> (the smallest ones) suffer changes in cluster geometry upon C<sub>2</sub>H<sub>4</sub> adsorption which is a typical behavior in small size clusters. In fact, this behavior was not seen in the larger NPs. Thus, in C-poor and C-rich MoC<sub>y</sub> NPs, there are phenomena which are not possible in a bulk surface and can lead to high reactivity towards ethylene.

### 3.5. Electronic structure organization

The electron density rearrangement between the MoC<sub>y</sub> NPs and the C<sub>2</sub>H<sub>4</sub> molecule is further illustrated by the Bader atoms-in-molecules analysis in Figure 6 —and also Figure S6 of the SI—. This is here complemented by CDD and ELF analyses. Four representative NPs were taken, since they embody different adsorption modes and Mo/C ratios, leading to descriptors differences as above explained. The chosen NPs are Mo<sub>12</sub>C<sub>6</sub> ( $\sigma$ -M,  $\mu$ -M), Mo<sub>12</sub>C<sub>12</sub> ( $\pi$ -M), Mo<sub>10</sub>C<sub>12</sub> (di- $\sigma$ -CM), and Mo<sub>5</sub>C<sub>6</sub> (di- $\sigma$ -CC), with Mo/C ratios of 2.00, 1.00, and 0.83 for two last cases, respectively.

The CDD and ELF plots for the adsorption on metal sites *via*  $\pi$ -M and  $\sigma$ -M,  $\mu$ -M modes are displayed in Figure 8. The binding *via*  $\sigma$ -M,  $\mu$ -M mode favors a high charge migration from the NP towards C<sub>2</sub>H<sub>4</sub>, as shown by the accumulation regions within the adsorbate, also observable in the *ELF*

plot. Indeed, this high electron density correlates with the Bader charge of  $-0.61 e$ . Overall, the largest adsorbate charges were seen for the  $\sigma$ -M,  $\mu$ -M binding mode. On the contrary, the adsorption *via*  $\pi$ -M mode has less electron density within the  $C_2H_4$ , in accordance with the smaller Bader charge of  $-0.30 e$ . Such a behavior may indicate that the  $C_2H_4$  adsorption on the  $MoC_y$  NPs has some ionic contribution to the bonding.

The aforementioned electron density migration occupies the  $C_2H_4$  Lowest Unoccupied Molecular Orbital (*LUMO*) antibonding orbitals, decreasing the bond order, and, consequently, elongating the C–C bond length. Indeed, the extent of the Bader charge relates to the  $d(CC)$  increase, as binding *via*  $\sigma$ -M,  $\mu$ -M mode is higher, ranging  $0.15 - 0.18 \text{ \AA}$ , compared to the binding *via*  $\pi$ -M mode, with increases of *ca.*  $0.10 \text{ \AA}$ . The largest  $d(CC)$  elongation is seen on  $MoC_y$ -  $C_{ethylene}$  sites, *i.e.* binding *via* di- $\sigma$ -CX —X = C or Mo. This is a direct consequence of the formation of new C-C covalent bond with the NP C atom, as clearly seen in the CDD and ELF plots of Figure S7 in the SI, even if one has to regard that coulombic interactions play a role. Notice that on  $Mo_5C_6$  not only  $d(CC)$  is elongated, but a  $sp^3$  hybridization emerges due to a molecular distortion. This explains the highest  $E_{dis}$  of  $3.68 \text{ eV}$ , among the evaluated NPs, see Table S6 of the SI.

The ethylene binding on the NPs and on the extended  $\delta$ - $MoC(001)$  surface *via*  $\pi$ -M mode has clear differences in terms of charges, see Figure S8 of the SI. In the  $\delta$ - $MoC(001)$  surface there is a continuous flux of electron density within the layers<sup>17</sup> a general behavior seen on other TMCs.<sup>45</sup> The electronic arrangement between Mo and C atoms is perturbed upon  $C_2H_4$  adsorption leading to an almost negligible  $d(CC)$  elongation of  $0.03 \text{ \AA}$ , with both ionic and covalent contributions. On the NPs the electron density is more affected, due to the stronger adsorption, higher Bader charge in  $C_2H_4$ , and a larger  $d(CC)$  elongation of  $0.09\text{--}0.25 \text{ \AA}$ .

## 4. Conclusions

The present systematic DFT study analyzed the ethylene binding on a series of  $MoC_y$  NPs, considering a broad Mo/C ratio range of  $0.67\text{--}2.00$ . Overall, 14 NPs have been explored with structures derived from a cascade procedure. The most stable structures were then used to analyze  $C_2H_4$  adsorption sampling *ca.* 500 adsorptive sites. The results show that a general classification can be established of the  $C_2H_4$  binding related to the C–C bond length elongation and the NP active site. Thus, Group I is for  $\pi$ -M mode adsorption, Group II is for  $\sigma$ -M,  $\mu$ -M mode and, finally, Group III involves NP C sites, *via* di- $\sigma$ -CX —X = Mo, C. Overall, the  $C_2H_4$  adsorption strongly affects the whole NP electron density, resulting in a stronger adsorption energy, higher negative charge on the

C<sub>2</sub>H<sub>4</sub> adsorbate, and a  $d(\text{CC})$  elongation of 0.09–0.25 Å, as compared to the respective behavior on an extended  $\delta$ -MoC(001) surface, revealing a complex mixture of ionic and covalent bond.

The reported analysis involved differentiating stoichiometric and non-stoichiometric NPs, a decomposition of the interaction in terms of C<sub>2</sub>H<sub>4</sub> distortion energy, NP deformation energy, and C<sub>2</sub>H<sub>4</sub> attachment energy in a lock-&-key fashion, considering cohesive energies, Mo/C ratios, and the explicit number of MoC units as possible interaction descriptors. Thus, the NPs with low distortion, deformation, and attachment energies are the non-stoichiometric Mo<sub>4</sub>C<sub>6</sub>, Mo<sub>8</sub>C<sub>12</sub> (MetCar), and Mo<sub>14</sub>C<sub>13</sub> (Nanocube), together with the stoichiometric Mo<sub>6</sub>C<sub>6</sub>, Mo<sub>12</sub>C<sub>12</sub>, and Mo<sub>24</sub>C<sub>24</sub> NPs. These are promising systems to further support on metal surfaces, in a closer approach to a practical catalyst. The best predicted performance for C<sub>2</sub>H<sub>4</sub> binding is for a Mo/C ratio below 1.08, as larger ratios are not advantageous for distorting C=C bond, which is key in the hydrogenation processes. The reasons rely on the above-mentioned descriptors analysis, accompanied by a geometric issue at high Mo/C ratios above 1.1, as an excess of Mo atoms leads to a lower coordination of Mo atoms, which is not advantageous since Mo binds C<sub>2</sub>H<sub>4</sub> just to compensate its under-coordination, instead of favoring the C<sub>2</sub>H<sub>4</sub> C–C lengthening, thus ultimately limiting its performance towards further hydrogenation reactions.

## Conflicts of interest

The authors declare no conflict of interest.

## Acknowledgments

The research carried out at the Universitat de Barcelona has been supported by the Spanish MICIUN RTI2018-095460-B-I00 and *María de Maeztu* MDM-2017-0767 grants, and, in part, by *Generalitat de Catalunya* 2017SGR13 grant and COST Action CA18234. C. J.-O. and E. F. acknowledge to *Universidad de Medellín* for financial support under the internal project 1143. F. I. acknowledges additional support from the 2015 ICREA Academia Award for Excellence in University Research. Part of this research used resources of the Center for Functional Nanomaterials, which is a U.S. DOE Office of Science Facility, and the Scientific Data and Computing Center, a component of the Computational Science Initiative, at Brookhaven National Laboratory under Contract No. DE-SC0012704.

## Supporting Information for Publication

The Supporting Information is available free of charge at DOI:

**Table S1.** Total energy difference between the lowest and second lowest structures per stoichiometry.

**Table S2.** Formation energies,  $E_{form}$ , for each stoichiometric NP per MoC unit and band gap related energies.

**Table S3.** Band gap energy,  $E_{gap}$ , for the non-stoichiometric MoC<sub>y</sub> NPs.

**Table S4.** Adsorption of C<sub>2</sub>H<sub>4</sub> on MoC<sub>y</sub> NPs.

**Table S5.** Two most stable C<sub>2</sub>H<sub>4</sub> adsorption energies and structures on every MoC<sub>y</sub> NP.

**Table S6.** Energy contributions to the C<sub>2</sub>H<sub>4</sub> adsorption energy on the different studied MoC<sub>y</sub> NPs.

**Table S7.** Cohesive energies for the studied stoichiometric MoC NPs.

**Figure S1.** Formation energies per MoC unit for each of the studied stoichiometric MoC NPs as a function of the MoC units.

**Figure S2.** CDD and ELF for the C<sub>2</sub>H<sub>4</sub> binding on Mo<sub>32</sub>C<sub>32</sub> NP.

**Figure S3.** Geometry changes in the Mo<sub>5</sub>C<sub>6</sub> NP upon C<sub>2</sub>H<sub>4</sub> adsorption.

**Figure S4** Geometry changes in the Mo<sub>4</sub>C<sub>6</sub> NP upon C<sub>2</sub>H<sub>4</sub> adsorption.

**Figure S5.** NP deformation energy and C<sub>2</sub>H<sub>4</sub> distortion energy on non-stoichiometric NPs sorted relative to the amount of Mo in the explored NPs.

**Figure S6.** Effect of Mo/C ratio of Mo<sub>12</sub>C<sub>x</sub> NPs in adsorption energy and size.

**Figure S7.** CDD and ELF for the C<sub>2</sub>H<sub>4</sub> binding through di-σ-CC on Mo<sub>5</sub>C<sub>6</sub> NP

**Geometry coordinates of bare NPs and C<sub>2</sub>H<sub>4</sub> adsorbed on them**



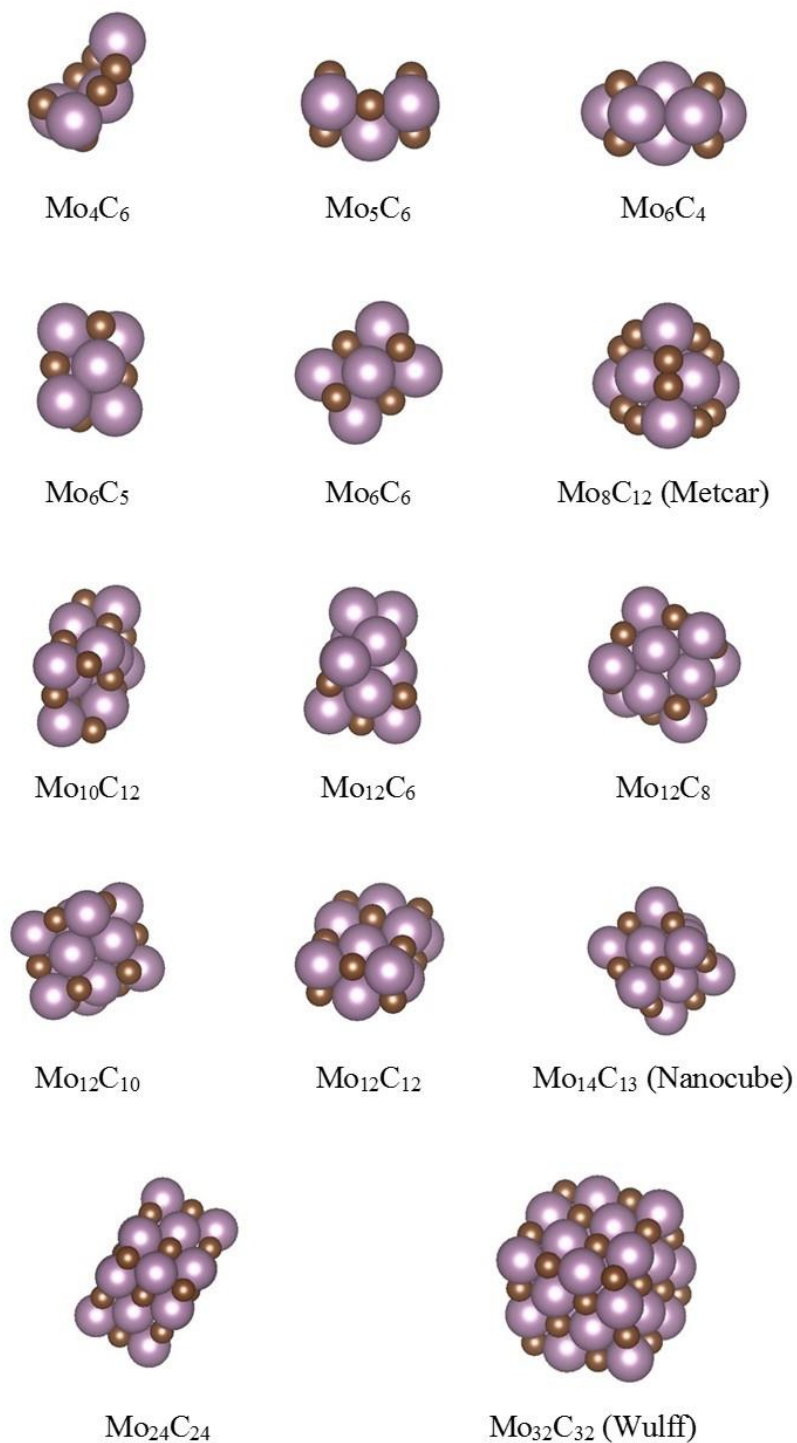
**Table 1.** Adsorption energy,  $E_{\text{ads}}$ , for the ethylene adsorption on the studied  $\text{MoC}_y$  nanoparticles, for the most-stable site, and evaluating the distortion (activation) by the  $\text{C}_2\text{H}_4$   $\text{C}=\text{C}$  bond length,  $d(\text{CC})$ . Energy values include the ZPE contribution. Reference data on most stable  $\delta$ - $\text{MoC}(001)$  and  $\beta$ - $\text{Mo}_2\text{C}(001)$  surfaces, either C- or Mo-terminated, as provided.

$\text{MoC}_y$	Site	$E_{\text{ads}} / \text{eV}$	$d(\text{CC}) / \text{\AA}$
Stoichiometric			
$\text{Mo}_6\text{C}_6$	$\pi$ -M	-1.76	1.43
$\text{Mo}_{12}\text{C}_{12}$	$\pi$ -M	-1.65	1.42
$\text{Mo}_{24}\text{C}_{24}$	$\pi$ -M	-1.84	1.42
$\text{Mo}_{32}\text{C}_{32}$	di- $\sigma$ -CM	-1.54	1.55
Non-stoichiometric			
$\text{Mo}_4\text{C}_6$	$\pi$ -M	-1.98	1.44
$\text{Mo}_5\text{C}_6$	di- $\sigma$ -CC	-1.97	1.56
$\text{Mo}_6\text{C}_4$	$\sigma$ -M, $\mu$ -M	-2.88	1.51
$\text{Mo}_6\text{C}_5$	$\sigma$ -M, $\mu$ -M	-1.99	1.51
$\text{Mo}_8\text{C}_{12}$	$\pi$ -M	-1.80	1.43
$\text{Mo}_{10}\text{C}_{12}$	di- $\sigma$ -CM	-1.78	1.58
$\text{Mo}_{12}\text{C}_6$	$\sigma$ -M, $\mu$ -M	-2.08	1.48
$\text{Mo}_{12}\text{C}_8$	$\sigma$ -M, $\mu$ -M	-1.86	1.49
$\text{Mo}_{12}\text{C}_{10}$	$\sigma$ -M, $\mu$ -M	-1.76	1.50
$\text{Mo}_{14}\text{C}_{13}$	$\pi$ -M	-1.85	1.44
Surfaces References			
$\delta$ - $\text{MoC}(001)^a$	$\pi$ -M	-0.44 <sup>c</sup>	1.36
$\beta$ - $\text{Mo}_2\text{C}(001)$ -C <sup>b</sup>	C-top, Mo-h <sub>1</sub>	-1.49	1.51
$\beta$ - $\text{Mo}_2\text{C}(001)$ -Mo <sup>b</sup>	Mo-top, C-h <sub>2</sub>	-2.50	1.48

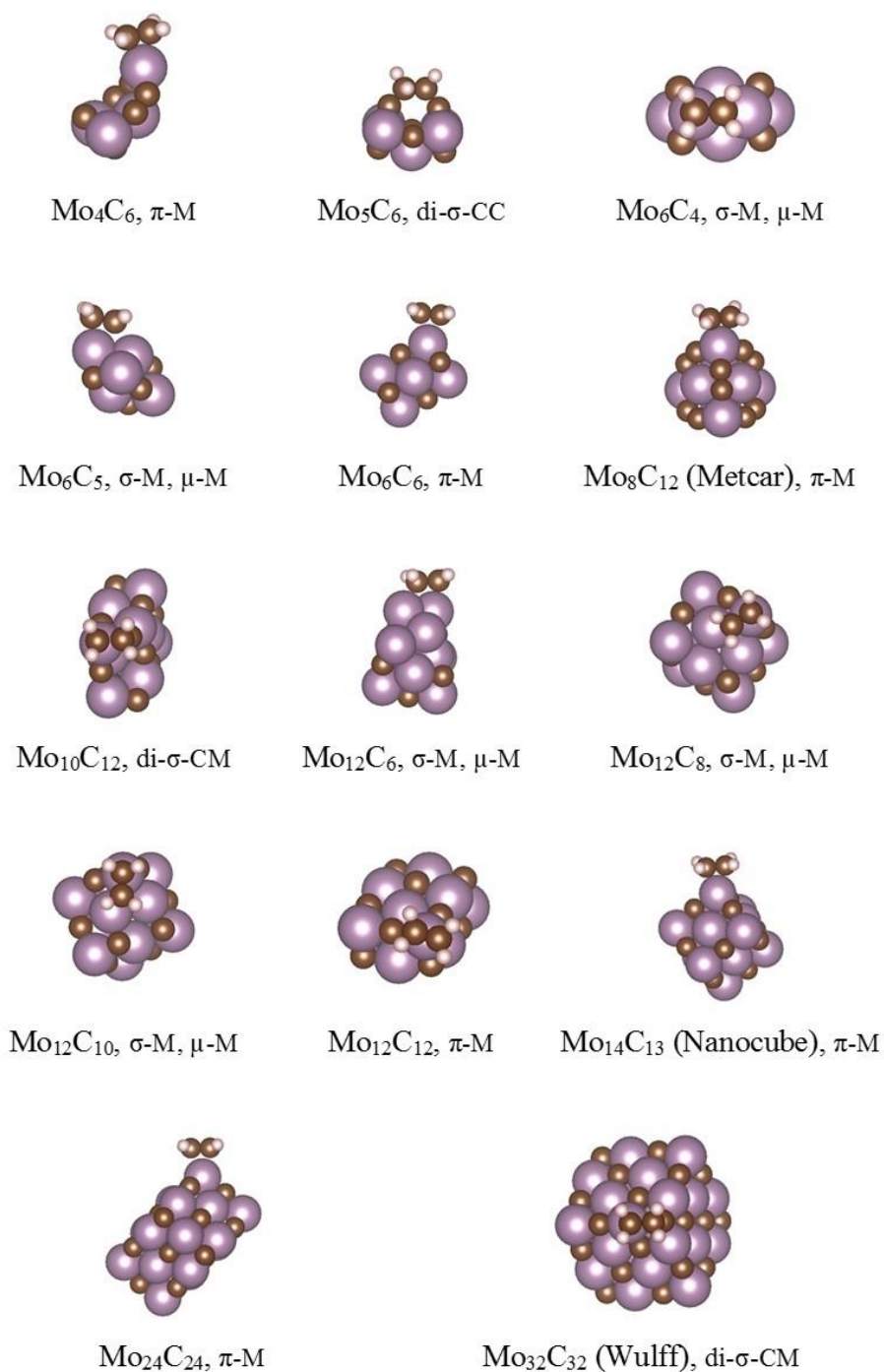
<sup>a</sup> Refs. <sup>17,19</sup>, <sup>b</sup> Ref. <sup>18</sup>, <sup>c</sup> reoptimized using present computational set-up.

See complete table in Table S4, SI.

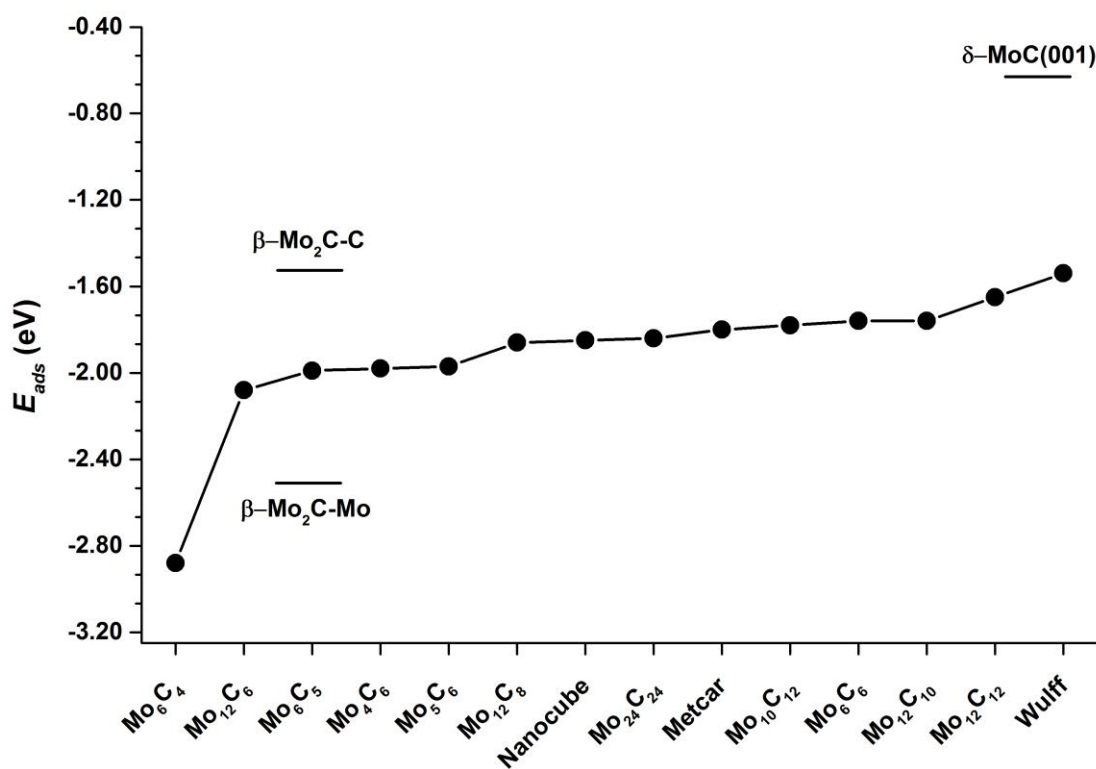
**Figure 1.** Geometry for the bare MoC<sub>y</sub> NPs The Mo and C atoms are represented by magenta and brown color, respectively.




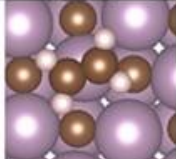
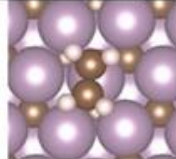

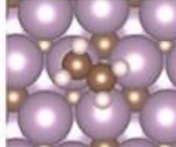

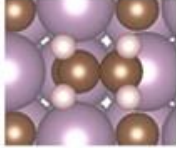
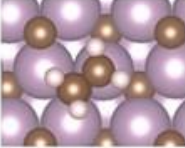

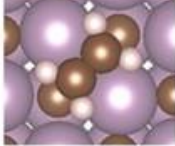
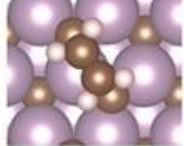
**Figure 2.** Most stable geometry of  $C_2H_4$  adsorbed on every NP. The Mo, C, and H atoms are represented by magenta, brown, and light gray, respectively. The binding mode is tagged along the structure.



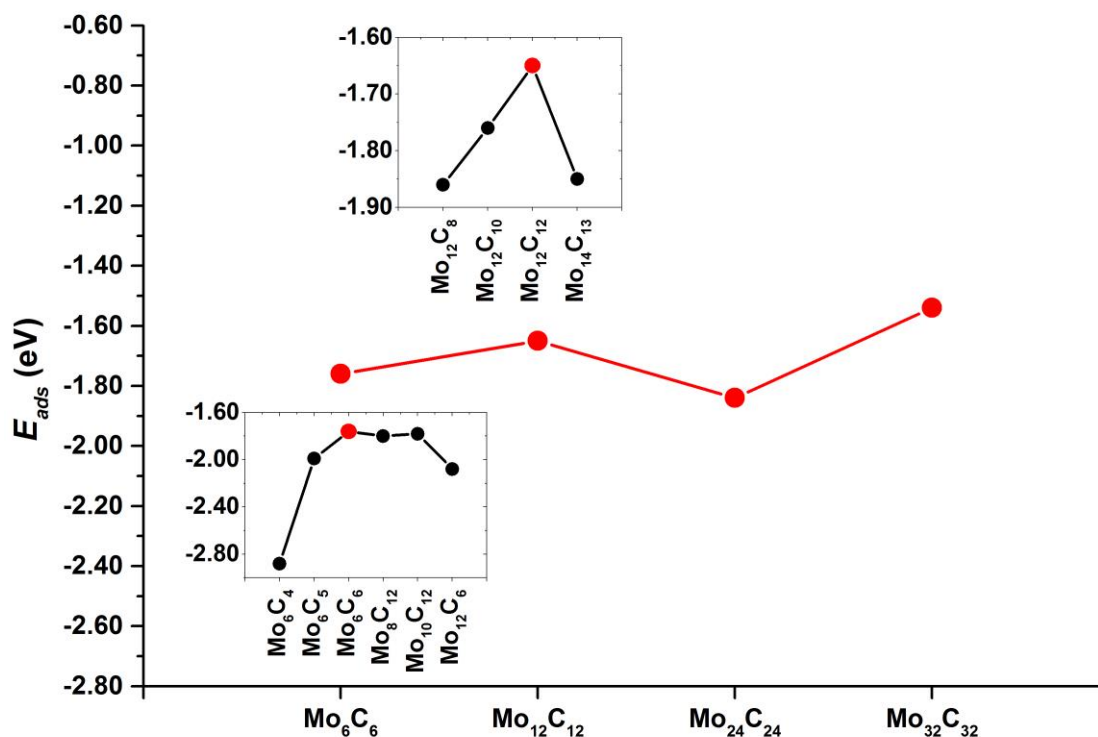
**Figure 3** Adsorption energies,  $E_{ads}$ , for the most stable  $C_2H_4$  structure adsorbed in every NP, sorted in terms of the energy strength. Extended surface values are shown as references.



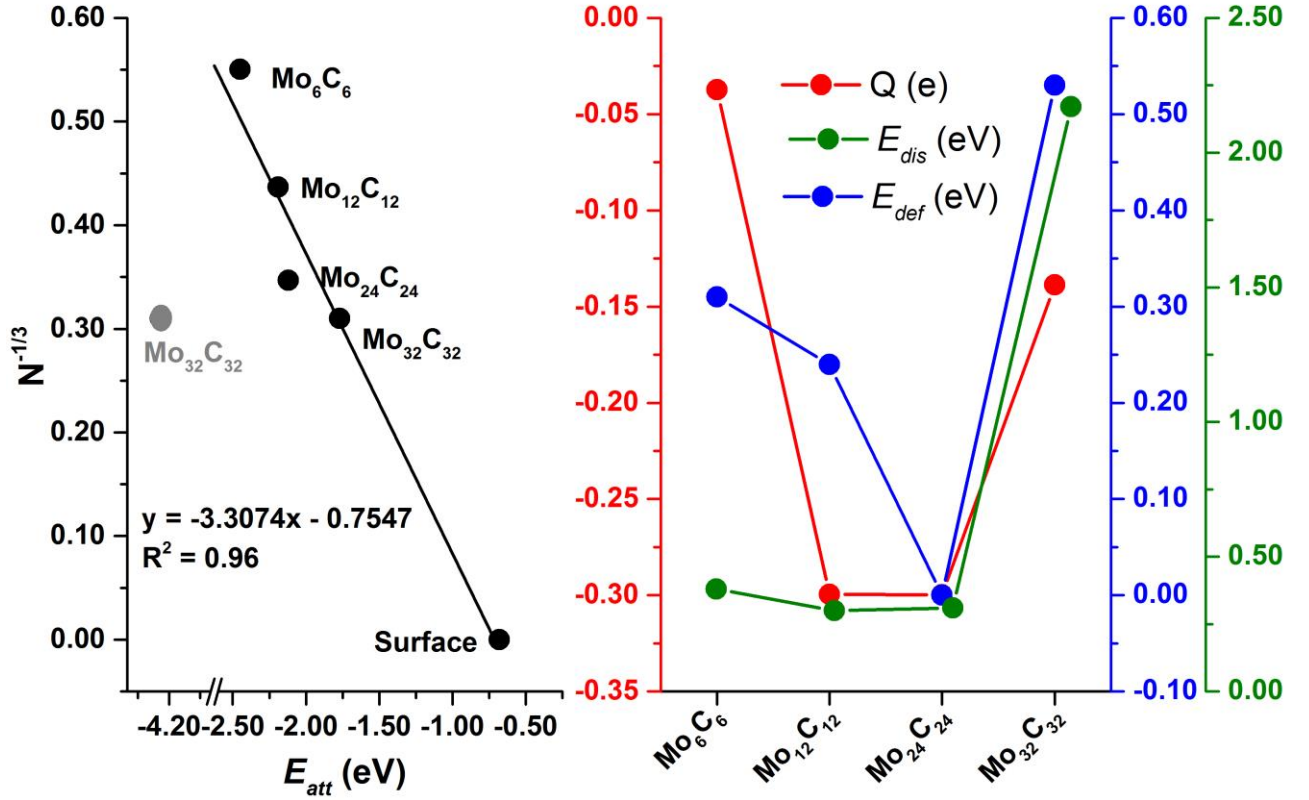
**Figure 4** Comparative geometry binding of C<sub>2</sub>H<sub>4</sub> on NPs and surfaces for the four adsorption modes found on NPs.

Adsorption mode	MoC <sub>y</sub> NP	δ-MoC(001)	β-Mo <sub>2</sub> C(001)-C	β-Mo <sub>2</sub> C(001)-Mo
π-M			N.A.	
σ-M, μ-M		N.A.	N.A.	
di-σ-CM				N.A.
di-σ-CC				N.A.

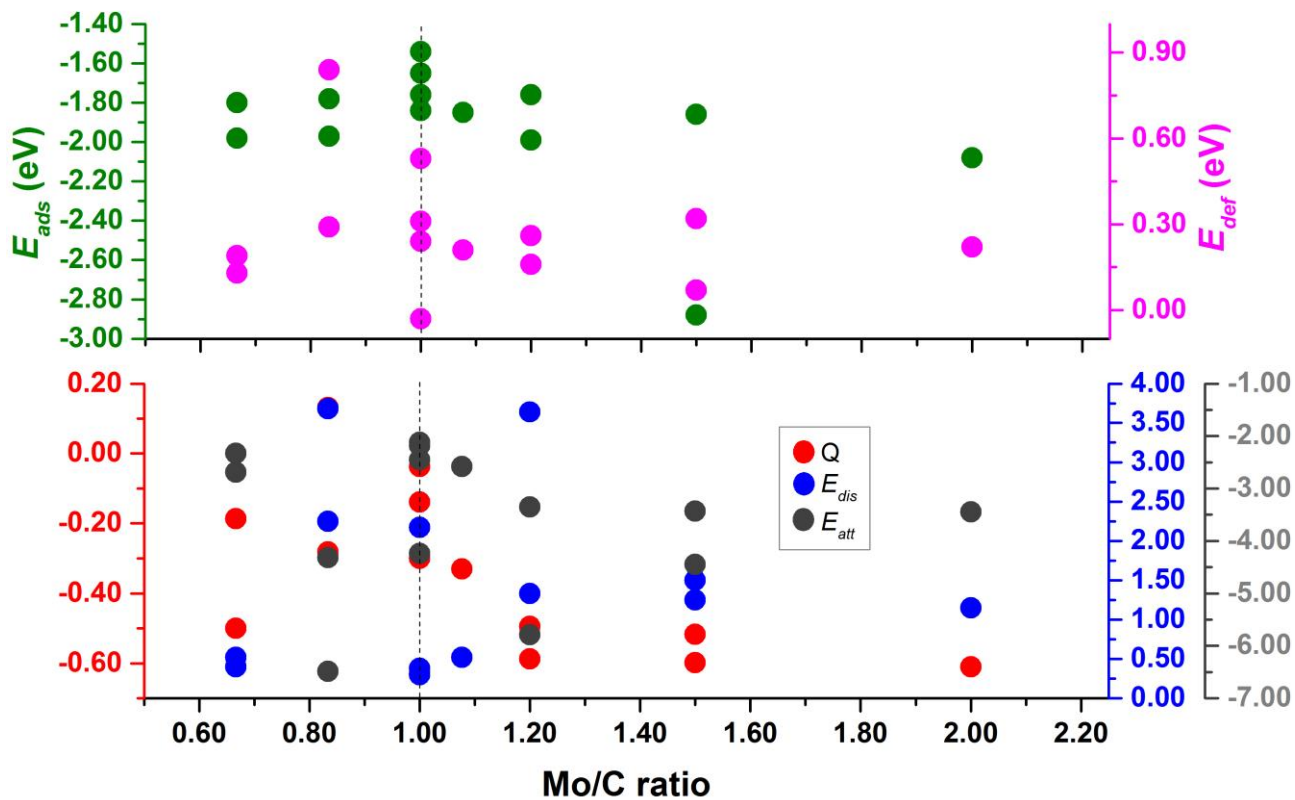
**Figure 5.** C<sub>2</sub>H<sub>4</sub> adsorption on stoichiometric NPs (red points), while values on related non-stoichiometric NPs (black points) are shown in insets.



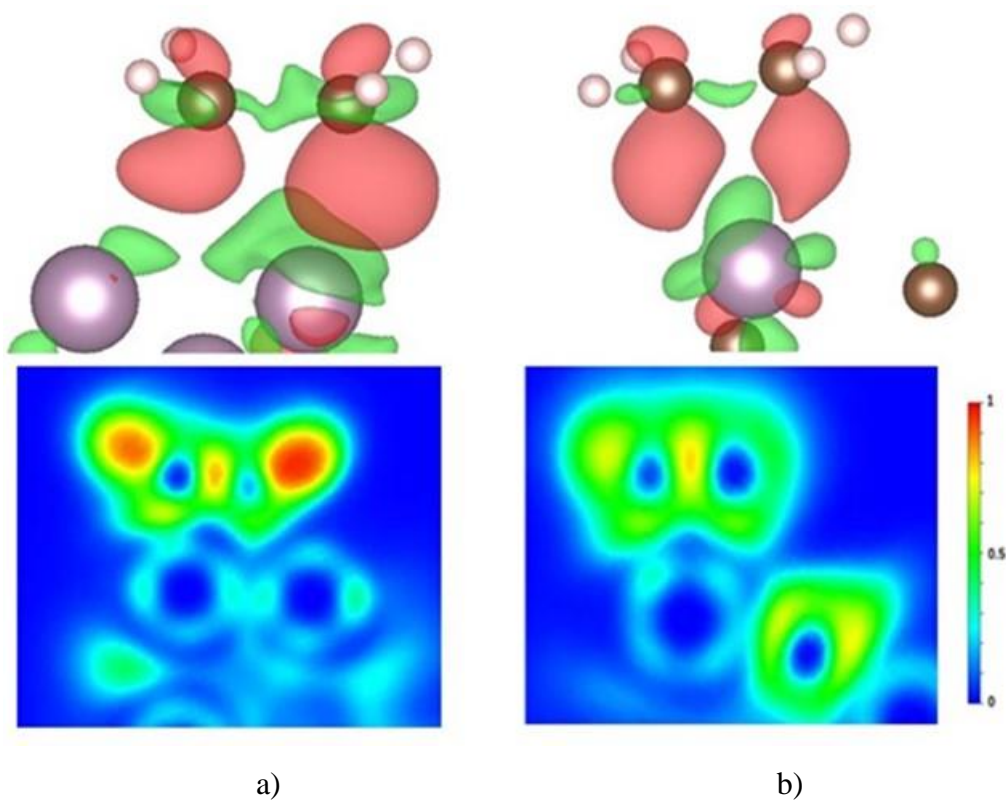
**Figure 6.** Left panel: Evolution with respect size, measured as  $N^{-1/3}$ , of the attachment energy,  $E_{att}$ . The second most stable structure for  $\text{Mo}_{32}\text{C}_{32}$  is shown in gray. Right panel: Bader charge,  $Q$ ,  $\text{C}_2\text{H}_4$  distortion energy,  $E_{dis}$ , and NP deformation energy,  $E_{def}$ .



**Figure 7.** Effect of Mo/C ratio in non-stoichiometric NPs on the adsorption energy,  $E_{ads}$ , and NP deformation energy,  $E_{def}$  (upper panel). Adsorbed  $C_2H_4$  Bader charge (in  $e$ ),  $C_2H_4$  distortion energy  $E_{dis}$ , and ethylene attachment energy,  $E_{att}$  (lower panel), both in eV.



**Figure. 8.** CDD plot (top) and ELF (bottom) for binding *via* a)  $\sigma$ -M,  $\mu$ -M ( $\text{Mo}_{12}\text{C}_6$ ),  $E_{\text{ads}} = -2.08$  eV; b)  $\pi$ -M mode ( $\text{Mo}_{12}\text{C}_{12}$ ),  $E_{\text{ads}} = -1.65$  eV. For the CDD, red and green colors represent the regions where the charge ( $0.05 e/\text{\AA}^3$ ) was lost and earned, respectively, after ethylene adsorption. The Mo, C, and H atoms are represented by magenta, brown and light gray color, respectively. In the ELF, blue, green, and red colors represent low (0), intermediate (0.5), and high (1) likelihood of finding electron pair, respectively.





## References

---

- (1) Wilson, J. N.; Otvos, J. W.; Stevenson, D. P.; Wagner, C. D. Hydrogenation of Olefins over Metals. *Ind. Eng. Chem.* **1953**, *45*, 1480–1487.
- (2) Dhandapani, B.; St. Clair, T.; Oyama, S. T. Simultaneous Hydrodesulfurization, Hydrodeoxygenation, and Hydrogenation with Molybdenum carbide *Appl. Catal. A: Gen.* **1998**, *168*, 219–228.
- (3) Bus, E.; Ramaker, D. E.; van Bokhoven, J. A. Structure of Ethene Adsorption Sites on Supported Metal Catalysts from in Situ XANES Analysis. *J. Am. Chem. Soc.* **2007**, *129*, 8094–8102.
- (4) Binder, A.; Seipenbusch, M.; Muhler, M.; Kasper, G. Kinetics and Particle Size Effects in Ethene Hydrogenation Over Supported Palladium Catalysts at Atmospheric Pressure. *J. Catal.*, **2009**, *268*, 150–155.
- (5) Tsung, C.; Kuhn, J. N.; Huang, W.; Aliaga, C.; Hung, L.; Somorjai, G. A.; Yang, P. Sub-10 nm Platinum Nanocrystals with Size and Shape Control: Catalytic Study for Ethylene and Pyrrole Hydrogenation. *J. Am. Chem. Soc.* **2009**, *131*, 5816–5822.
- (6) Aboul-Gheit, A. K.; Aboul-Fotouh, S. M.; Aboul-Gheit, N. A. K. Hydroconversion of Cyclohexene Using Catalysts Containing Pt, Pd, Ir, and Re Supported on H-ZSM-5 Zeolite. *Appl. Catal. A: Gen.* **2005**, *283*, 157–164.
- (7) Sapi, A.; Thompson, C.; Wang, H.; Michalak, W. D.; Ralston, W. T.; Alayoglu, S.; Somorjai, G. A. Recovery of Pt Surfaces for Ethylene Hydrogenation-Based Active Site Determination. *Catal. Lett.* **2014**, *144*, 1151–1158.
- (8) Rioux, R. M.; Komor, R.; Song, H.; Hoefelmeyer, J. D.; Grass, M.; Niesz, K.; Yang, P.; Somorjai, G. A. Kinetics and Mechanism of Ethylene Hydrogenation Poisoned by CO on Silica-supported Monodisperse Pt Nanoparticles. *J. Catal.* **2008**, *254*, 1–11.
- (9) Cunha, D. S.; Cruz, G. M. Hydrogenation of Benzene and Toluene Over Ir Particles Supported on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>. *Appl. Catal. A: Gen.* **2002**, *236*, 55–66.
- (10) Guil, J. M.; Masiá, A. P.; Paniago, A. R.; Menayo, J. M. T. Energetics of H<sub>2</sub> and O<sub>2</sub> Adsorption on Ir/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> and Ir/SiO<sub>2</sub> Catalysts. Dependence on Support and on Metal Particle Size. *Thermochimica Acta* **1998**, *312*, 115–124.
- (11) Piegsa, A.; Korth, W.; Demir, F.; Jess, A. Hydrogenation and Ring Opening of Aromatic and Naphthenic Hydrocarbons Over Noble Metal (Ir, Pt, Rh)/Al<sub>2</sub>O<sub>3</sub> Catalysts. *Catal. Lett.* **2012**, *142*, 531–540.
- (12) Levy, R. B.; Boudart, M. Platinum-Like Behavior of Tungsten Carbide in Surface Catalysis. *Science* **1973**, *181*, 547–549.

- (13) Ardakani, S. J.; Liu, X.; Smith, K. J. Hydrogenation and Ring Opening of Naphthalene on Bulk and Supported Mo<sub>2</sub>C Catalysts. *Appl. Catal. A: Gen.* **2007**, *324*, 9–19.
- (14) Hwu, H. H.; Chen, J. G. Surface Chemistry of Transition Metal Carbides. *Chem. Rev.* **2005**, *105*, 185–212.
- (15) Posada-Pérez, S.; Viñes, F.; Ramirez, P. J.; Vidal, A. B.; Rodriguez, J. A.; Illas, F. The Bending Machine: CO<sub>2</sub> Activation and Hydrogenation on  $\delta$ -MoC(001) and  $\beta$ -Mo<sub>2</sub>C(001) Surfaces. *Phys. Chem. Chem. Phys.* **2014**, *16*, 14912–14921.
- (16) Rocha, A. S.; Rocha, A. B.; Teixeira, V. Benzene Adsorption on Mo<sub>2</sub>C: A Theoretical and Experimental Study. *Appl. Catal. A: Gen.* **2010**, *379*, 54–60.
- (17) Jimenez-Orozco, C.; Florez, E.; Moreno, A.; Liu, P.; Rodriguez, J. A. Systematic Theoretical Study of Ethylene Adsorption on  $\delta$ -MoC(001), TiC(001), and ZrC(001) Surfaces. *J. Phys. Chem. C* **2016**, *120*, 13531–13540.
- (18) Jimenez-Orozco, C.; Florez, E.; Moreno, A.; Liu, P.; Rodriguez, J. A. Acetylene and Ethylene Adsorption on a  $\beta$ -Mo<sub>2</sub>C(100) Surface: A Periodic DFT Study on the Role of C- and Mo-Terminations for Bonding and Hydrogenation Reactions. *J. Phys. Chem. C* **2017**, *121*, 19786–19795.
- (19) Jimenez-Orozco, C.; Flórez, E.; Viñes, F.; Rodriguez, J. A.; Illas, F. Critical Hydrogen Coverage Effect on the Hydrogenation of Ethylene Catalyzed by  $\delta$ -MoC(001): An *Ab Initio* Thermodynamic and Kinetic Study. *ACS Catal.* **2020**, *10*, 6213–6222.
- (20) Jimenez-Orozco, C.; Flórez, E.; Moreno, A.; Rodriguez, J. A. Platinum vs. Transition Metal Carbide Surfaces as Catalysts for Olefin and Alkyne Conversion: Binding and Hydrogenation of Ethylidyne. *J. Phys.: Conf. Ser.* **2019**, *1247*, 012003.
- (21) Figueras, M.; Jurado, A.; Morales-Garcia, Á.; Viñes, F.; Illas, F. Bulk (in)stability as a Possible Source of Surface Reconstruction. *Phys. Chem. Chem. Phys.* **2020**, *22*, 19249–19253.
- (22) Figueras, M.; Gutiérrez, R. A.; Viñes, F.; Ramírez, P. J.; Rodriguez, J. A.; Illas, F. Supported Molybdenum Carbide Nanoparticles as Hot Hydrogen Reservoirs for Catalytic Applications. *J. Phys. Chem. Lett.* **2020**, *11*, 8437–8441.
- (23) Horn, J. M.; Song, Z.; Potapenko, D. V.; Hrbek, J.; White, M. G. Characterization of Molybdenum Carbide Nanoparticles Formed on Au(111) Using Reactive-Layer Assisted Deposition. *J. Phys. Chem. B* **2005**, *109*, 44.
- (24) Gao, J.; Zheng, Y.; Fitzgerald, G. B.; de Joannis, J.; Tang, Y.; Wachs, I. E.; Podkolzin, S. G. Structure of Mo<sub>2</sub>C<sub>x</sub> and Mo<sub>4</sub>C<sub>x</sub> Molybdenum Carbide Nanoparticles and Their Anchoring Sites on ZSM-5 Zeolites. *J. Phys. Chem. C*, **2014**, *118*, 4670–4679.
- (25) N. Vo, Dai-Viet; Adesina, A. A. Fischer–Tropsch synthesis over alumina-supported molybdenum carbide catalyst. *Applied Catalysis A: General*, **2011**, *399*, 221–232.

- (26) Shou, Heng; Davis, R. J. Multi-product steady-state isotopic transient kinetic analysis of CO hydrogenation over supported molybdenum carbide. *Journal of Catalysis*, **2013**, *306*, 91–99.
- (27) Baddour, F. G.; Roberts, E. J.; To, A. T.; Wang, L.; Habas, S. E.; Ruddy, D. A.; Bedford, N. M.; Wright, Joshua; Nash, C. P.; Schaidle, J. A.; Brutchey, R. L.; Malmstadt, N. An Exceptionally Mild and Scalable Solution-Phase Synthesis of Molybdenum Carbide Nanoparticles for Thermocatalytic CO<sub>2</sub> Hydrogenation. *J. Am. Chem. Soc.*, **2020**, *142*, 1010–1019.
- (28) Lamiel, O.; Bromley, S. T.; Illas, F. Low-energy Nanoscale Clusters of (TiC)<sub>n</sub> n = 6, 12: A Structural and Energetic Comparison with MgO. *Theor. Chem. Acc.* **2013**, *132*, 1312.
- (29) Viñes, F.; Gomes, J. R. B.; Illas, F. Understanding the Reactivity of Metallic Nanoparticles: Beyond the Extended Surface Model for Catalysis. *Chem. Soc. Rev.* **2014**, *43*, 4922–4939.
- (30) Quesne, M.; Roldán, A.; De Leeuw, N. H.; Catlow, C. R. A. Bulk and surface properties of metal carbides: implications for catalysis. *Chem. Soc. Rev.* **2018**, *20*, 6905–6916.
- (31) Viñes, F.; Sousa, C.; Liu, P.; Rodriguez, J. A.; Illas, F. A systematic Density Functional Theory Study of the Electronic Structure of Bulk and (001) Surface of Transition-metals Carbides *J. Chem. Phys.* **2005**, *122*, 174709.
- (32) Guo, B. C.; Kerns, K. P.; Castleman Jr., A. W. Ti<sub>8</sub>C<sup>12+</sup>-Metallo-Carbohedrenes: A New Class of Molecular Clusters? *Science* **1992**, *255*, 1411.
- (33) Pilgrim, J. S.; Duncan, M. A. Beyond Metallo-carbohedrenes: Growth and Decomposition of Metal-carbon Nanocrystals. *J. Am. Chem. Soc.* **1993**, *115*, 9724–9727.
- (34) Kresse, G.; Furthmüller, J. Efficient Iterative Schemes for *ab initio* Total-energy Calculations Using a Plane-wave Basis Set. *Phys. Rev. B* **1996**, *54*, 11169–11186.
- (35) Perdew, J. P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868.
- (36) Politi, J. R. D. S.; Viñes, F.; Rodriguez, J. A.; Illas, F. Atomic and Electronic Structure of Molybdenum Carbide Phases: Bulk and Low Miller-index Surfaces. *Phys. Chem. Chem. Phys.* **2013**, *15*, 12617–12625.
- (37) Grimme, S.; Antony, J.; Ehrlich, S.; Krieg, H. A consistent and accurate *ab initio* parametrization of density functional dispersion correction (DFT-D) for the 94 elements H-Pu. *J. Chem. Phys.* **2010**, *132*, 154104.
- (38) Kunkel, C.; Viñes, F.; Illas, F. Transition Metal Carbides as Novel Materials for CO<sub>2</sub> Capture, Storage, and Activation. *Energy Environ. Sci.* **2016**, *9*, 141–144.
- (39) Liu, X.; Kunkel, C.; Ramírez de la Piscina, P.; Homs, N.; Viñes, F.; Illas, F. Effective and Highly Selective CO Generation from CO<sub>2</sub> Using a Polycrystalline  $\alpha$ -Mo<sub>2</sub>C Catalyst. *ACS Catal.* **2017**, *7*, 4323–4335.

- (40) Blöchl, P. E. Projector Augmented-wave Method. *Phys. Rev. B* **1994**, *50*, 17953–17979.
- (41) Kresse, G.; Joubert, D. From ultrasoft pseudopotentials to the projector augmented-wave method. *Phys. Rev. B* **1999**, *59*, 1758–1775
- (42) Ha, M.; Baxter, E. T.; Cass, A.; Anderson, S. L.; Alexandrova, A. N. Boron Switch for Selectivity of Catalytic Dehydrogenation on Size-Selected Pt Clusters on Al<sub>2</sub>O<sub>3</sub>. *J. Am. Chem. Soc.* **2017**, *139*, 11568–11575.
- (43) Gorey, T. J.; Zandkarimi, B.; Li, G.; Baxter, E. T.; Alexandrova, A. N.; Anderson, S. L. Coking-Resistant Sub-Nano Dehydrogenation Catalysts: Pt<sub>n</sub>Sn<sub>x</sub>/SiO<sub>2</sub> (n = 4, 7). *ACS Catal.* **2020**, *10*, 4543–4558.
- (44) Li, G.; Zandkarimi, B.; Cass, A.; Gorey, T. J.; Allen, B. J.; Alexandrova, A. N.; Anderson, S. L. Sn-modification of Pt<sub>7</sub>/alumina model catalysts: Suppression of carbon deposition and enhanced thermal stability. *J. Chem. Phys.* **2020**, *152*, 024702.
- (45) Jimenez-Orozco, C.; Flórez, E.; Montoya, A.; Rodriguez, J. A. Binding and Activation of Ethylene on Tungsten Carbide and Platinum Surfaces. *Phys. Chem. Chem. Phys.* **2019**, *21*, 17332–17342.
- (46) Bader, R. Atoms in Molecules: A Quantum Theory; Oxford University Press: New York, **1990**
- (47) Bromley, S.; Moreira, I. P. R.; Neyman, K. M.; Illas, F. Approaching Nanoscale Oxides: Models and Theoretical Methods. *Chem. Soc. Rev.* **2009**, *38*, 2657–2670.
- (48) Shen, J.; Hill, J. M.; Watwe, R. M.; Spiewak, B. E.; Dumesic, J. A. Microcalorimetric, Infrared Spectroscopic, and DFT Studies of Ethylene Adsorption on Pt/SiO<sub>2</sub> and Pt-Sn/SiO<sub>2</sub> Catalysts. *J. Phys. Chem. B.* **1999**, *103*, 3923–3934.
- (49) Watwe, R. M.; Spiewak, B. E.; Cortright, R. D.; Dumesic, J. A. Density Functional Theory (DFT) Studies of C<sub>1</sub> and C<sub>2</sub> Hydrocarbons Species on Pt Clusters. *J. Catal.* **1998**, *180*, 184–193.
- (50) Crampton, A. S.; Rötzer, M. D.; Schweinberger, F. F.; Yoon B.; Landman, U.; Heiz, U.; Controlling Ethylene Hydrogenation Reactivity on Pt<sub>13</sub> Clusters by Varying the Stoichiometry of the Amorphous Silica Support. *Angew. Chem. Int. Ed.* **2016**, *55*, 8953–8957.
- (51) Sun, G.; Fuller III, J. T.; Alexandrova, A. N.; Sautet, P. Global Activity Search Uncovers Reaction Induced Concomitant Catalyst Restructuring for Alkane Dissociation on Model Pt Catalysts. *ACS Catal.* **2021**, *11*, 1877–1885.
- (52) Liu, P.; Rodriguez, J. A.; Muckerman, J. T. The Ti<sub>8</sub>C<sub>12</sub> Metcar: A New Model Catalyst for Hydrodesulfurization. *J. Phys. Chem. B*, **2004**, *108*, 18796 – 18798.
- (53) Liu, P.; Rodriguez, J. A. Effects of carbon on the stability and chemical performance of transition metal carbides: A density functional study. *J. Chem. Phys.*, **2004**, *120*, 5414.

## Graphic for TOC

