

LA-UR-18-31035 (Accepted Manuscript)

## Emergent bound states and impurity pairs in chemically doped Shastry-Sutherland system

Shi, Zhenzhong; Steinhardt, William; Graf, David; Corboz, Phillippe; Weickert, Dagmar Franziska; Harrison, Neil; Jaime, Marcelo; Marjerrison, Casey; Dabkowska, Hanna A.; Mila, Frederic; Haravifard, Sara

Provided by the author(s) and the Los Alamos National Laboratory (2019-06-13).

**To be published in:** Nature Communications

**DOI to publisher's version:** 10.1038/s41467-019-10410-x

**Permalink to record:** <http://permalink.lanl.gov/object/view?what=info:lanl-repo/lareport/LA-UR-18-31035>

**Disclaimer:**

Los Alamos National Laboratory, an affirmative action/equal opportunity employer, is operated by Triad National Security, LLC for the National Nuclear Security Administration of U.S. Department of Energy under contract 89233218CNA00001. By approving this article, the publisher recognizes that the U.S. Government retains nonexclusive, royalty-free license to publish or reproduce the published form of this contribution, or to allow others to do so, for U.S. Government purposes. Los Alamos National Laboratory requests that the publisher identify this article as work performed under the auspices of the U.S. Department of Energy. Los Alamos National Laboratory strongly supports academic freedom and a researcher's right to publish; as an institution, however, the Laboratory does not endorse the viewpoint of a publication or guarantee its technical correctness.

ARTICLE

<https://doi.org/10.1038/s41467-019-10410-x>

OPEN

# Emergent bound states and impurity pairs in chemically doped Shastry-Sutherland system

Zhenzhong Shi<sup>1</sup>, William Steinhardt<sup>1</sup>, David Graf<sup>2</sup>, Philippe Corboz<sup>3</sup>, Franziska Weickert<sup>2</sup>, Neil Harrison<sup>4</sup>, Marcelo Jaime<sup>4</sup>, Casey Marjerrison<sup>1</sup>, Hanna A. Dabkowska<sup>5</sup>, Frédéric Mila<sup>6</sup> & Sara Haravifard<sup>1,7</sup>

Impurities often play a defining role in the ground states of frustrated quantum magnets. Studies of their effects are crucial in understanding of the phase diagram in these materials.  $\text{SrCu}_2(\text{BO}_3)_2$ , an experimental realization of the Shastry-Sutherland (SS) lattice, provides a unique model system for such studies using both experimental and numerical approaches. Here we report effects of impurities on the crystals of bound states, and doping-induced emergent ground states in Mg-doped  $\text{SrCu}_2(\text{BO}_3)_2$ , which remain stable in high magnetic fields. Using four complementary magnetometry techniques and theoretical simulations, a rich impurity-induced phenomenology at high fields is discovered. The results demonstrate a rare example in which even a small doping concentration interacts strongly with both triplets and bound states of triplets, and thus plays a significant role in the magnetization process even at high magnetic fields. Our findings provide insights into the study of impurity effects in geometrically frustrated quantum magnets.

<sup>1</sup>Department of Physics, Duke University, Durham, NC 27708, USA. <sup>2</sup>National High Magnetic Field Laboratory, Florida State University, Tallahassee, FL 32310, USA. <sup>3</sup>Institute for Theoretical Physics and Delta Institute for Theoretical Physics, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, The Netherlands. <sup>4</sup>National High Magnetic Field Laboratory, Los Alamos National Laboratory, Los Alamos, NM 87545, USA. <sup>5</sup>Brockhouse Institute for Material Research, McMaster University, Hamilton, Ontario L8S 4M1, Canada. <sup>6</sup>Institute of Physics, École Polytechnique Fédérale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland. <sup>7</sup>Department of Mechanical Engineering and Materials Science, Duke University, Durham, NC 27708, USA. Correspondence and requests for materials should be addressed to S.H. (email: [haravifard@phy.duke.edu](mailto:haravifard@phy.duke.edu))

**G**eometrical frustration in low-dimensional quantum spin systems underlies many of the exotic states of matter that are of great current interest in condensed matter physics<sup>1</sup>. One of the central topics in studying such systems is to understand the effects of impurities that are unavoidable in realistic materials<sup>2–5</sup> and sometimes intentionally introduced by chemical doping<sup>6</sup>. However, such studies are often hindered by the complex Hamiltonians in analytical and numerical studies, and difficulties in finding a suitable model system to make a direct comparison between theoretical calculations and experimental results. Here we show that  $\text{SrCu}_2(\text{BO}_3)_2$ , a realization of the exactly solvable SS model<sup>7,8</sup>, provides an important test ground for our understanding of the effects of impurities in frustrated quantum magnets.

The parent compound of  $\text{SrCu}_2(\text{BO}_3)_2$  consists of two-dimensional layers of  $\text{Cu}^{2+}(S=1/2)$  orthogonal dimers arranged on a square lattice (Fig. 1a inset), which form the *ab*-plane of its tetragonal unit cell. A spin gap  $\Delta \sim 3$  meV separates the  $S=0$  singlet ground state from an  $S=1$  triplet excited state. Without doping,  $\text{SrCu}_2(\text{BO}_3)_2$  has a ground state of a valence bond solid at low temperature and zero magnetic field. Studies on doped  $\text{SrCu}_2(\text{BO}_3)_2$  have been largely motivated by the prospect of resonating valence bond (RVB) superconductivity, when holes are doped into this material<sup>8–12</sup>, and the effects of the doping-introduced  $S=1/2$  spin singlet impurities on its ground state remain to be thoroughly explored.

To understand the ground state induced by the interplay among the non-magnetic spin singlets, the magnetic spin triplet excitations, and the doping-introduced  $S=1/2$  spin singlet

impurities at low energies, we have studied  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$ , in which the magnetic  $\text{Cu}^{2+}$  is substituted with non-magnetic isoelectronic  $\text{Mg}^{2+}$ , introducing minimal structure distortion because of their similar ionic radii. Previous inelastic neutron scattering and  $\mu\text{SR}$  experiments on  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$  ( $x=0.05$ ) have shown that some dimers are indeed broken, and in-gap states emerge<sup>13,14</sup>. It was suggested that the in-gap states might correspond to localized anisotropic spin polarons developed around the impurities<sup>13,15</sup>, or to the  $S=1/2$  states that consist of one spinon and one impurity<sup>16</sup>. However, a clear understanding for the effects of non-magnetic impurities in SS systems remains elusive. Here we demonstrate that critical insights are gained by studying the magnetization response of the Mg-doped  $\text{SrCu}_2(\text{BO}_3)_2$  in high magnetic fields.

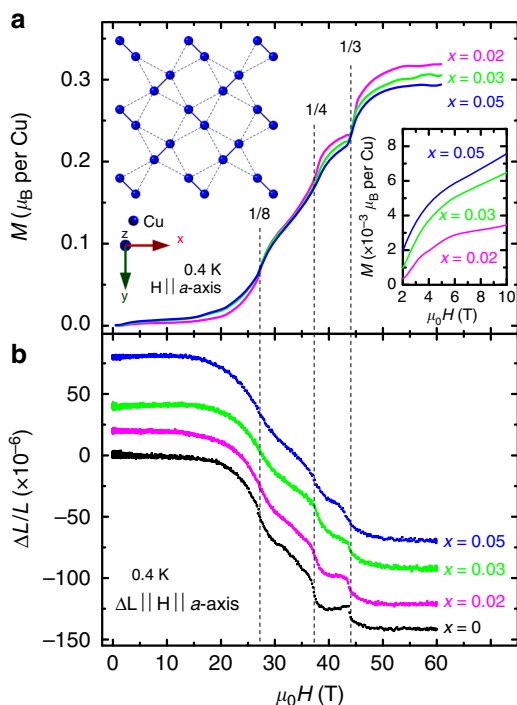
In the presence of magnetic field, frustration has been known to induce magnetization plateaus, occurring at fractional values of saturation magnetization  $M_{\text{sat}}$ , either due to a classical mechanism involving stabilization of some classical spin configurations, or due to a quantum mechanism which corresponds to symmetry-breaking phase transitions in an effective hard-core-boson model<sup>1</sup>. As one of the best examples of the latter case,  $\text{SrCu}_2(\text{BO}_3)_2$  exhibits a series of magnetization plateaus at magnetic fields above which the spin gap is closed by the Zeeman energy<sup>17–22</sup>. This has been understood as a result of the crystallization of  $S_z=2$  pinwheels of bound states of two triplets<sup>23</sup>, which are energetically more favorable than crystals of  $S_z=1$  triplets. This picture is well established in the undoped system. In the doped system, however, it is not clear how the added impurities would interact with the triplets and bound states of triplets, and hence alter their crystallization.

Here, we report a comprehensive doping dependence study of the magnetometry in high magnetic fields, revealing a surprisingly rich impurity-induced phenomenology in these systems: doping-induced triplet states and emergent impurity pairs. It was found that the conventional magnetization measurements alone do not provide a full picture explaining the subtle changes associated with such a study. Therefore, we combined four complementary techniques: tunnel diode oscillator (TDO) and torque magnetometry, which measure magnetic susceptibility; magnetization measurements, which probe magnetization response directly; magnetostriction measurements, which detect lattice correlations to the magnetic order in very high magnetic fields. The results are in remarkable agreement with our numerical simulations using infinite projected entangled pair states (iPEPS), providing an accurate account of the various impurity-induced emergent states. Our results offer essential implications for the understanding of doped quantum spin systems.

## Results

**Magnetization plateaus.** The TDO and torque magnetometry experiments were conducted at the National High Magnetic Field Laboratory (NHMFL) dc field facility, while the magnetization and magnetostriction measurements were carried out at the NHMFL pulsed field facility. Single crystals of  $\text{SrCu}_2(\text{BO}_3)_2$  and  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$ , with  $x$  up to 0.05, were grown using the optical floating zone technique (see “Methods”). In the doped samples, the magnetic  $\text{Cu}^{2+}$  sites are replaced with non-magnetic isoelectronic  $\text{Mg}^{2+}$ , which effectively breaks the spin dimers into free  $S=1/2$  spins, without introducing structural distortions. The doping concentrations were confirmed by susceptibility measurements (see Supplementary Fig. 1).

We show in Fig. 1a the magnetization response for  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$  ( $x=0.02, 0.03$ , and  $0.05$ ) at  $0.4$  K with  $\mathbf{H} \parallel a$ -axis up to  $60$  T. At low fields, a notable finite magnetization, which



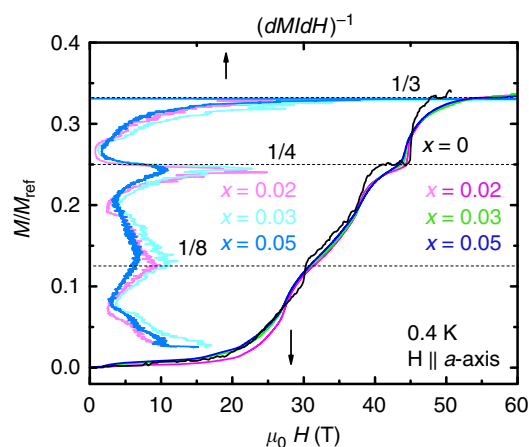
**Fig. 1** Magnetization plateaus in Mg-doped  $\text{SrCu}_2(\text{BO}_3)_2$ . **a** Magnetization ( $M$ ) vs. field ( $\mathbf{H} \parallel a$ -axis) for  $x=0.02$  (magenta),  $0.03$  (green), and  $0.05$  (blue), and **b** magnetostriction ( $\Delta L/L$ ) vs. field ( $\mathbf{H} \parallel a$ -axis) for  $x=0$  (black),  $0.02$  (magenta),  $0.03$  (green), and  $0.05$  (blue), at  $T=0.4$  K, conducted in a  $65$  T multi-shot magnet at the pulsed field facility of the national high magnetic field laboratory (NHMFL). Lower right inset:  $M(H)$  for the three dopings at low  $H$ , obtained from  $60$  T shots. Upper left inset: a schematic of the spin- $1/2$   $\text{Cu}^{2+}$  ions in the SS lattice, as realized in  $\text{SrCu}_2(\text{BO}_3)_2$ . Traces in (**b**) are shifted for clarity

increases with doping, is observed (see Fig. 1a lower right inset). For  $H$  smaller than  $6 \sim 8$  T,  $M(H)$  exhibits a Brillouin-like paramagnetic behavior for all three dopings, and the results are consistent with the field-induced alignment of free  $S=1/2$  impurity spins. However, a full saturation of magnetization is interrupted at  $H$  above  $6 \sim 8$  T, suggesting a more complicated picture than one solely explained by the impurity-induced free spins; as will be discussed later. The sharp onset of magnetization at  $H$  higher than  $\sim 18$  T is attributed to the increase in population of triplets, as spin gap closes with increasing field<sup>1</sup>. In doped  $\text{SrCu}_2(\text{BO}_3)_2$ , Fig. 1a clearly shows that the magnetization is suppressed with increasing doping, suggesting a suppressed density of triplets in the presence of impurities. Nevertheless, for all doping concentrations, magnetization plateaus similar to those in the undoped case are observed at the same onset fields, albeit with important differences as discussed below.

First, the plateaus in the doped systems can no longer be identified as fractions ( $1/8$ ,  $1/4$ ,  $1/3$ , ...) of the saturation magnetization  $M_{\text{sat}}$ , where all the magnetic  $\text{Cu}^{2+}$  moments are fully saturated. Therefore, for clarity, these plateaus are named as pseudo- $1/8$ , pseudo- $1/4$ , and pseudo- $1/3$  plateaus in the doped systems, to be differentiated from the  $1/8$ ,  $1/4$ , and  $1/3$  plateaus in the undoped case. Second, a term that is more general than  $M_{\text{sat}}$  can be defined: the reference magnetization  $M_{\text{ref}}$ . In the undoped system,  $M_{\text{ref}}$  is the same as  $M_{\text{sat}}$ , and the magnetization plateaus occur at fractions ( $1/8$ ,  $1/4$ ,  $1/3$ , ...) of  $M_{\text{sat}}$  ( $=M_{\text{ref}}$ ). In the doped system, however, the magnetization values of the pseudo- $1/n$  ( $n=2, 3, 8, \dots$ ) plateaus are found to be fractions ( $1/8$ ,  $1/4$ ,  $1/3$ , ...) of a doping-dependent magnetization value, which is different from the true saturation magnetization  $M_{\text{sat}}$  of these doped systems, as demonstrated later. This magnetization value is identified as  $M_{\text{ref}}$ . It can be extracted from the pseudo- $1/3$  plateaus for the doped system (or  $1/3$  plateau for the undoped case):  $M_{\text{ref}} = 3 \times M_{1/3}$ , where  $M_{1/3}$  refers to the magnetization at the pseudo- $1/3$  (or  $1/3$ ) plateau. We plot in Fig. 2 the normalized magnetization curves,  $M/M_{\text{ref}}$ , as function of field, for both the undoped and doped samples. Here, it is easy to verify that the pseudo- $1/8$  and pseudo- $1/4$  plateaus in the doped systems have magnetization values that are approximately  $1/8$  and  $1/4$  of  $M_{\text{ref}}$ , similar to the undoped case. Using this method,  $M_{\text{ref}}$  are found to be  $1.065$ ,  $0.952$ ,  $0.913$ , and  $0.881 \mu_B$  per Cu for the  $x=0$ ,  $0.02$ ,  $0.03$ , and  $0.05$  samples, respectively (see Figs. 1a and 2). Note that the  $x=0$  data is reproduced from ref. 24 (see Supplementary Note 1).

The observation that the values of  $M_{\text{ref}}$  decrease upon doping is rather interesting. One might expect that in the doped systems,  $M_{1/3}$  at the pseudo- $1/3$  plateau has contributions from both superstructures of bound states<sup>23</sup> (as in the undoped samples) and the free spins located on broken dimers with impurity sites (up to 2.5% with the highest doping  $x=0.05$ ), and therefore, the value of  $M_{\text{ref}}$  ( $3M_{1/3}$ ) would be slightly larger than the saturation magnetization, due to the overvaluation of the magnetization of the free spins. This is obviously not the case.

Moreover, as mentioned above,  $M_{\text{ref}}$  is also different from the true saturation magnetization  $M_{\text{sat}}$  in the doped systems. For example,  $M_{\text{sat}}$  for the  $x=0.05$  sample is expected to be 2.5% smaller than that in the undoped case, because of the loss of 2.5% of magnetic  $\text{Cu}^{2+}$  moments. However,  $M_{\text{ref}}$  for the same doping ( $0.881 \mu_B$  per Cu) is found to be  $\sim 17\%$  less than  $M_{\text{sat}}$  ( $=M_{\text{ref}}$ ) for the undoped sample ( $1.065 \mu_B$  per Cu). Therefore,  $M_{\text{ref}}$  must reflect an intrinsic change in the spin superstructures as a result of doping. Indeed, it is not surprising that doping with nonmagnetic static impurities would disrupt and soften the superstructure of the bound states underlying the magnetization plateaus: the formation of the  $1/3$  superstructure is perturbed in a certain neighborhood of the impurities, resulting in patches of



**Fig. 2** Magnetization normalized by the reference magnetization  $M_{\text{ref}}$ .  $M/M_{\text{ref}}$  vs.  $\mu_0 H$  (bottom axis) for  $x=0$  (black),  $0.02$  (magenta),  $0.03$  (green), and  $0.05$  (blue), with  $\mathbf{H} \parallel a$ -axis, at  $T=0.4$  K. Plateaus are indicated by peaks in the inverse susceptibility  $(dM/dH)^{-1}$  (top axis) for  $x=0.02$  (light magenta),  $0.03$  (light cyan), and  $0.05$  (light blue). Dashed lines guide the eye. The magnetization values at the  $1/3$  (pseudo- $1/n$ ) plateau are used to extract the reference saturation magnetization,  $M_{\text{ref}} = 1.065$ ,  $0.952$ ,  $0.913$ , and  $0.881 \mu_B$  per Cu for the  $x=0$ ,  $x=0.02$ ,  $x=0.03$ , and  $x=0.05$  samples, respectively. Here, the  $x=0$  trace (black) of  $M$  vs.  $\mu_0 H$  is reproduced from a  $\mathbf{H} \parallel c$ -axis trace (adapted with permission from, ref. 24, copyright American Physical Society 2005, also see Supplementary Note 1), rescaled to allow comparison with our  $\mathbf{H} \parallel a$ -axis data on the doped samples

superstructures rather than a perfect  $1/3$  superstructure with 2.5% of the sites removed. In this scenario,  $M_{\text{ref}}$  is the total magnetization of all the patches of superstructures and does not include the nonmagnetic spin singlets which lie in between. The fact that  $M/M_{\text{ref}}$  curves for the undoped<sup>24</sup> and doped samples overlap and show the same sequence for plateaus at  $1/8$  (pseudo- $1/8$ ),  $1/4$  (pseudo- $1/4$ ), and  $1/3$  (pseudo- $1/3$ ), as seen in Fig. 2, suggests that the undoped and doped systems share the same underlying superstructures<sup>23</sup> at these plateaus, enabled by some collaborative geometrical arrangement of the impurities and the triplets in the doped samples. The same onset fields of these (pseudo- $1/n$ ) plateaus also suggest the excitation energy (or effective chemical potential) of the superstructures of the bound states of triplets does not depend on doping. The smearing of the pseudo- $1/n$  plateaus with doping is consistent with the softening of the superstructures in the system. For instance, the volume of the superstructures in the undoped system is close to 100% of the total volume of the sample, and it is reduced to  $M_{\text{ref}}/M_{\text{sat}} \sim 85\%$  for the  $x=0.05$  sample. At the highest fields, however, all the moments are fully saturated, and the magnetization should eventually reach  $M_{\text{sat}}$ . It is interesting to speculate how this process takes place, and extremely high magnetic fields are required for such a study.

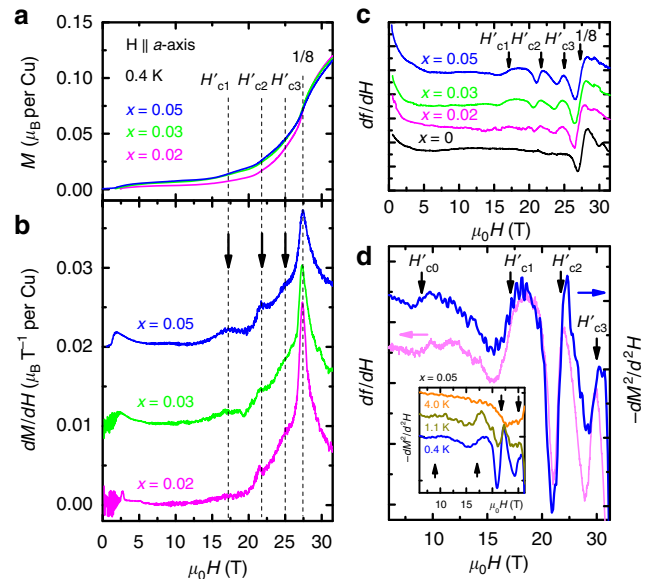
Complementary magnetostriction measurements (see “Methods”) performed for both the undoped and doped samples are plotted in Fig. 1b and Supplementary Fig. 2. These results reveal contraction along the  $a$ -axis, which closely corresponds to changes in magnetization and are consistent with previous results reported for the undoped system<sup>20,25</sup>. Furthermore, these results clearly show the (pseudo-)  $1/8$ , (pseudo-)  $1/4$ , and (pseudo-)  $1/3$  plateaus, for which the onset fields agree very well with those determined from the magnetization measurements. The increasingly softened pseudo- $1/n$  plateaus with doping also suggest that the overall lattice coupling is suppressed with the increased density of impurities.

**Emergent magnetization states at low  $H$ .** Our most important results are obtained from a close examination of the magnetization response for the doped samples in the field region below the pseudo-1/8 plateau, as presented in Figs. 3 and 4. In fact this region is of broad interest, though not well understood even in the undoped system. For example, other than the 1/9 plateau<sup>19,20</sup>, spin superstructures with even smaller fractions, i.e., larger unit cells, remain elusive. Theoretical considerations seem to suggest that they are energetically favorable only in very limited field ranges, if at all possible<sup>23</sup>. In a doped system, the phase diagram becomes even richer as the density of impurities increases.

We plot in Fig. 3a and b the magnetization curves as function of  $x$  for the low-field region. Indeed, the magnetization measurements clearly show three low-field anomalies, i.e., jumps in  $M(H)$  curves, as can be seen for all doped samples. For the  $x = 0.05$  sample, the onset fields of these anomalies are determined as  $H'_{C1} \sim 17.1$  T,  $H'_{C2} \sim 21.7$  T, and  $H'_{C3} \sim 25.0$  T (see Supplementary Figs. 3a and 4). For the  $x = 0.02$  and 0.03 samples, three anomalies are also identified at similar fields. Figure 3b shows the magnitudes of these anomalies, measured by  $dM/dH$ , are much smaller than that of the pseudo-1/8 plateau for all  $x$ . Their doping dependence, however, are exactly the opposite: the  $H'_{C1}$ ,  $H'_{C2}$ , and  $H'_{C3}$  anomalies are enhanced with higher doping concentration, while the pseudo-1/8 plateau is suppressed. This completely different behavior on doping suggests that these anomalies have origins that are different from the pseudo-1/ $n$  plateaus. The broad maxima at very low  $H \sim 1$  T – 2 T are attributed to field-aligned free  $S = 1/2$  impurity spins, associated with the onset of finite magnetization, as discussed above.

We plot in Fig. 3c and d the results for TDO magnetic susceptibility measurements (see Methods), where  $df/dH$  is proportional to  $dM^2/d^2H$ ; the corresponding comparison is clearly shown in Fig. 3d for the  $x = 0.05$  sample. The TDO measurements performed in a quieter magnet environment, i.e., a steady magnetic field instead of a pulsed field, show more clearly the emergence of the  $H'_{C1}$ ,  $H'_{C2}$ , and  $H'_{C3}$  anomalies with doping, and their absence in the undoped system (see Fig. 3c). This is consistent with the fact that these anomalies were never observed in the undoped system<sup>19,21,24</sup>. Strikingly, another broad anomaly at  $H'_{C0} \sim 9$  T, which is much weaker than its higher field counterparts, is only observed for the highest doping concentration  $x = 0.05$  sample. The confirmation of such a weak anomaly underlines the importance of adopting different techniques for measuring the same physical quantity when the signal is weak. These anomalies are found to be suppressed with increasing temperature (see Fig. 3d inset, Supplementary Figs. 5 and 6). In the  $x = 0.05$  samples, for example, they disappear at  $T \sim 2$  K, before the pseudo-1/ $n$  plateaus melt at  $\sim 3$  K–4 K (see Supplementary Figs. 2d and 5d). The different energy scales suggest that the underlying spin structures of these anomalies are different from the superstructures of bound states of triplets associated with the pseudo-1/ $n$  plateaus. This is confirmed by our simulation results as discussed below.

The coupling of these anomalies to the lattice is investigated using magnetostriction measurements. In both undoped and doped samples, the axial magnetostriction along  $a$ -axis deviates from zero at fields that gradually decrease from  $\sim 18$  T in  $x = 0$  to  $\sim 14$  T in the  $x = 0.05$  sample, as indicated by arrows in Fig. 4a. As can be seen in Fig. 4b, however, no anomalies are observed for any of the samples at fields below the pseudo-1/8 plateau. Though a lack of sufficient resolution cannot be completely ruled out, the absence of these anomalies in the magnetostriction data suggests their weak coupling to lattice. This is unlike the strong lattice coupling observed for magnetization plateaus corresponding to the crystallization of bound states of triplets, confirming their different origins. This interpretation is further strengthened by



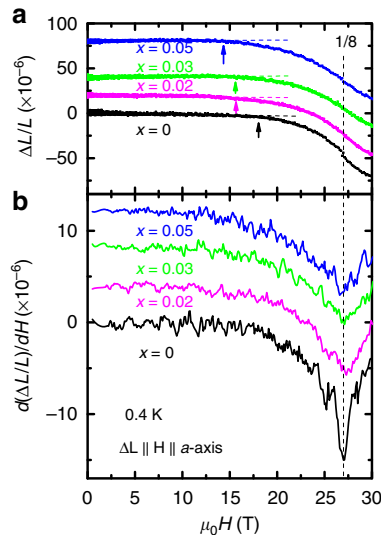
**Fig. 3** Emergence of magnetization anomalies below the 1/8 plateau. Field dependence of **a**,  $M$  and **b**,  $dM/dH$ , for three doping levels  $x = 0.02$  (magenta), 0.03 (green), and 0.05 (blue), with  $\mathbf{H} \parallel a$ -axis, at  $T = 0.4$  K. The feature corresponding to the pseudo-1/8 plateau is marked by a dashed line at  $\sim 27$  T.  $H'_{C1}$ ,  $H'_{C2}$ , and  $H'_{C3}$  and the corresponding dashed lines indicate three of the additional anomalies below the pseudo-1/8 plateau. For clarity, a shift of 0.01 (0.02)  $\mu_B T^{-1}$  per Cu is added to the  $x = 0.03$  (0.05) trace. **c** The first derivative of the frequency shift,  $df/dH$  ( $\propto dM^2/d^2H$ ), as a function of applied field for  $x = 0$  (black), 0.02 (magenta), 0.03 (green), and 0.05 (blue), measured by the tunnel diode oscillator technique (see “Methods”) at the dc field facility of NHMFL. Upon doping, three anomalies emerge at  $H'_{C1}$ ,  $H'_{C2}$ , and  $H'_{C3}$ , consistent with the magnetization measurements in **(b)**. **d** A zoomed-in plot of  $df/dH$  (light magenta, left axis) and  $-dM^2/d^2H$  (blue, right axis) vs.  $\mu_0 H$  for the  $x = 0.05$  sample, shows an additional broad anomaly at a lower field  $H'_{C0}$ . Inset:  $-dM^2/d^2H$  vs.  $\mu_0 H$  for a few selective temperatures. The arrows, from left to right, indicate  $H'_{C0}$ ,  $H'_{C1}$ ,  $H'_{C2}$ , and  $H'_{C3}$ , respectively. Traces in **(c)** and inset of **(d)** are shifted for clarity

the fact that the  $H'_{C1}$  and  $H'_{C0}$  anomalies appear at fields comparable with, or below, the gap closing fields at which bound states of triplets are absent and cannot play any role in their formation. Indeed, iPEPS numerical simulations clearly demonstrate that the observed anomalies all have impurity-induced origins, as we explain in the following sections.

**Infinite projected entangled pair states.** Our simulation results are obtained using iPEPS—a variational tensor network ansatz to represent a 2D ground state directly in the thermodynamic limit<sup>26–28</sup>. The ansatz consists of a unit cell of tensors which is periodically repeated on the infinite lattice, where in the present case we use one tensor per dimer<sup>23,29,30</sup>. The accuracy of the ansatz can be systematically controlled by the bond dimension  $D$  of the tensors.

The optimization of the variational parameters has been done using the simple update method which provides good estimates of ground state energies while being computationally affordable, even in the limit of very large unit cell sizes (up to  $12 \times 12$  dimers in the present work). For the computation of observables, a variant<sup>31,32</sup> of the corner-transfer matrix method<sup>33,34</sup> is used. To improve the efficiency, we exploit the  $U(1)$  symmetry of the model<sup>35,36</sup>. For an introduction to the method, see refs. 37,38 for example.





**Fig. 4** Absence of the magnetization anomalies in magnetostriction measurements. Field dependence of **a**, relative deformation  $\Delta L/L$  along the tetragonal axis, and **b**, its first derivative  $d(\Delta L/L)/dH$ , with  $\Delta \mathbf{L} \parallel \mathbf{H} \parallel a$ -axis, at  $T = 0.4$  K, for  $x = 0$  (black), 0.02 (magenta), 0.03 (green), and 0.05 (blue). The arrows in **a** point to the onsets of deviation from linear fits to the low-field regions for each doping (dashed lines). The vertical dashed line marks the (pseudo-)  $1/8$  plateau, identified as the local minima in  $d(\Delta L/L)/dH$  vs.  $\mu_0 H$ . Traces are shifted for clarity

**Model used for the Mg-doped  $\text{SrCu}_2(\text{BO}_3)_2$ .** A well-established effective model to describe the low-energy physics of  $\text{SrCu}_2(\text{BO}_3)_2$  is the SS model<sup>2</sup> given by the Hamiltonian

$$H = J \sum_{\langle i,j \rangle} S_i \cdot S_j + J' \sum_{\langle i,j \rangle} S_i \cdot S_j - h \sum_i S_i^z \quad (1)$$

where the bonds with coupling strength  $J$  build an array of orthogonal dimers and the bonds with coupling  $J'$  denote interdimer couplings, and  $h$  is the strength of the external magnetic field. In the present work we use  $J'/J = 0.63$  (with  $J \sim 51$  T) which was obtained from a fit to high magnetic field data<sup>30</sup>.

At zero external magnetic field, the ground state is given by a product of singlets on the dimers<sup>2</sup>. Early on, it was found that the SS model has almost localized triplet excitations<sup>39,40</sup> which has led to the viewpoint that the magnetization plateaus found in  $\text{SrCu}_2(\text{BO}_3)_2$  correspond to crystals of triplets<sup>39,41–51</sup>. However, it was predicted that  $S_z = 2$  excitations, which can be seen as a bound state of two triplets, are energetically lower in the dilute limit of excitations<sup>42</sup>. Based on iPEPS simulations, it was shown that these bound states are energetically favored even when they are localized, i.e., that the magnetization plateaus actually correspond to crystals of localized bound states rather than crystals of triplets<sup>23</sup>.

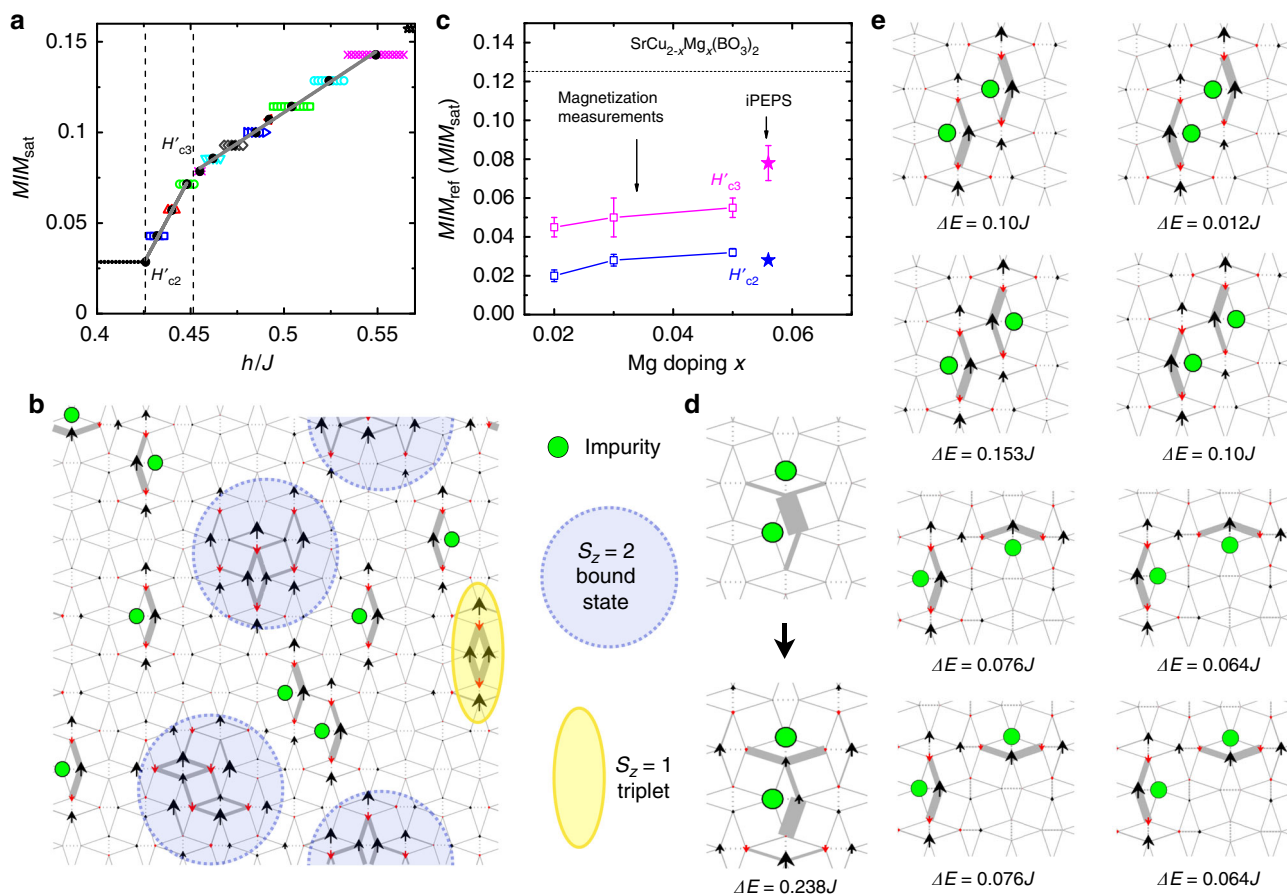
We model the Mg doping by introducing impurity sites where each impurity replaces one of the  $S = 1/2$  spins on a dimer with a non-magnetic site (i.e., with no coupling to the neighboring sites), leaving a free  $S = 1/2$  spin on the other site of the dimer. A single impurity in the lattice leads to a two-fold degenerate ground state, since it costs no energy to flip a single spin. Thus in the dilute limit of impurities we can expect that these free  $S = 1/2$  spins immediately align with an external magnetic field. The question is now how the presence of these impurities with attached  $S = 1/2$  spins affects the magnetization process, which we will investigate below using iPEPS simulations.

**iPEPS simulations results.** To understand the impurity effects in the doped samples, the first key question is whether the bound states of triplets are effectively attracted or repelled by an impurity site and its neighboring  $S = 1/2$  spin. To answer this question, we have performed simulations with a single impurity and one bound state in an  $8 \times 8$  unit cell using a bond dimension  $D = 10$ , and found that the latter is clearly repelled by the impurity (see Supplementary Fig. 7). Thus, based on this result we can expect that in a large system containing many impurities, bound states are first created far away from neighboring impurities as magnetic field increases.

Figure 5a shows the iPEPS magnetization curve ( $D = 6$ ) obtained using a  $12 \times 12$  unit cell of dimers with a random configuration of eight impurity sites, corresponding to a doping  $x = 0.056$ . For this system, a localized bound state first occurs at  $H_{C2} = (0.428 \pm 0.001)J$  ( $21.8 \pm 0.1$  T). In the infinite limit, since the system contains many locations in the lattice with similar energy costs to form a bound state, we may expect the non-smooth magnetization curve, exhibiting a jump at  $H_{C2}$ , compatible with the anomaly observed in experiments at  $H_{C2} \sim 21.7$  T (see Fig. 3). This value is essentially independent of the doping concentration, since a change of doping concentration only alters the density of such locations in the lattice, not the excitation energy. This is consistent with our experimental findings that the magnetization anomaly at  $H_{C2}$  becomes stronger with increasing doping concentration, while the value of  $H_{C2}$  is doping-independent. It is interesting to point out that  $H_{C2}$  is close to the energy scale necessary to create a localized bound state in systems without impurities,  $0.427J$ <sup>23</sup>. However, a localized bound state does not appear there, because its excitation energy ( $0.427J$ ) is higher than that of a delocalized bound state,  $0.41J$ <sup>23</sup>. Therefore, in undoped systems, bound states are delocalized in the dilute limit of excitations<sup>42</sup>, and a smooth increase of the magnetization, without a jump (anomaly) at  $H_{C2}$ , is expected.

Upon further increasing the magnetic field, the doped lattice gets occupied by more and more localized bound states. At a certain characteristic field  $H_{C3} = (0.452 \pm 0.004)J$  ( $23.1 \pm 0.2$  T) we observe the appearance of additional triplet excitations in the lattice, accompanied by a rapid change of slope in the magnetization curve. This can be understood from the fact that a bound state occupies more space than a triplet excitation, so that at locations with several nearby impurity sites it can become energetically favorable to place a triplet excitation rather than a bound state. Thus, this suggests that the anomaly observed at  $H_{C3} \sim 25$  T in experiments is due to a rapid change of slope in the magnetization curve accompanied with the appearance of additional triplet excitations, rather than a magnetization plateau. Because the doping does not affect the lowest possible triplet excitation energy,  $H_{C3}$  is also expected to be dependent only weakly on doping concentration. The probability to find such special locations in the lattice where it is preferable to put triplet excitations in the presence of impurities and bound states, however, increases with doping. Therefore, similar to our observation at  $H_{C2}$ , doping enhances the magnetization anomaly at  $H_{C3}$  but does not change the value of  $H_{C3}$ . An example spin configuration at  $H_{C3}$  is presented in Fig. 5b, containing three bound states and one triplet excitation. A good qualitative agreement between the simulation and experiments is demonstrated in Fig. 5c, which shows the doping dependence of the normalized magnetization  $M/M_{\text{ref}}$  at  $H_{C2}$  and  $H_{C3}$ , extracted from the magnetization measurements (see Fig. 3) for the  $x = 0.02, 0.03$ , and  $0.05$  samples and the iPEPS simulations of  $M/M_{\text{sat}}$  for  $x = 0.056$ .

Finally, we address the additional features at  $H_{C1} \sim 17.1$  T and  $H_{C0} \sim 9$  T observed in experiments. As explained above, in the



**Fig. 5** iPEPS simulation and magnetization measurements for the Mg-doped SS model. **a** iPEPS magnetization curve obtained using a  $12 \times 12$  unit cell with eight impurity sites. Black solid dots represent the centers of the plateaus. The full lines are linear fits to the black solid dots at high and low-field regions, respectively. Dashed lines indicate  $H'_{c2}$  and  $H'_{c3}$ . A clear slope change is identified at  $H'_{c3}$ . **b** Example spin configuration obtained in the total  $S_z = 11$  sector. The size of the spins scale with the magnitude of the local magnetic moment, where black (red) arrows point along (opposite to) the external magnetic field. The thickness of the gray bonds scales with the local bond energy (the thicker the lower the energy). **c** Mg-doping dependence of the normalized magnetization,  $M/M_{\text{ref}}$ , at  $H'_{c2}$  (magenta) and  $H'_{c3}$  (blue), obtained from experimental results on the  $x = 0.02, 0.03$ , and  $0.05$  samples, along with iPEPS simulation results for  $M/M_{\text{sat}}$  with an effective doping  $x = 0.056$ . Dashed line indicates the magnetization at the  $1/8$  plateau. The error bars of the magnetization measurements result from the uncertainty in determining magnetization values using the method shown in Supplementary Fig. 3. The iPEPS error bar takes into account the uncertainty of the location of  $H'_{c3}$  due to the finite unit cell size. **d** Special 2-impurity configuration in the  $S_z = 0$  (top) and  $S_z = 1$  (bottom) sectors, respectively, with an excitation energy  $\Delta E = 0.238J$ . **e** Special 2-impurity configurations obtained with iPEPS which lead to additional excitation levels below  $H'_{c1}$  - at an onset field  $H'_{c0}$ , as observed in the  $x = 0.05$  sample

dilute limit of impurities we expect all the attached  $S = 1/2$  moments to be aligned already at a small magnetic field. However, at larger doping there is an increasing probability of having two neighboring impurities, as shown in Fig. 5d. In this configuration, the  $S = 1/2$  spins attached to the impurities can no longer be regarded as free, but they prefer to couple to a singlet. As a consequence, the two  $S = 1/2$  spins do not immediately align with a small external field, but only do so beyond a certain critical field. From computing the excitation energy in a  $8 \times 8$  cell we find a critical field  $H'_{c1} = 0.238J$  ( $\sim 12.1$  T), i.e. well below  $H'_{c2}$ . This value corresponds to the excitation energy in the limit of an isolated pair of neighboring impurities. Here, the weak dependence of  $H'_{c1}$  on doping can be understood from the fact that changing the impurity concentration affects the probabilities of finding an (almost isolated) 2-impurity configuration, whereas its excitation energy remains unchanged—except at extremely high doping concentrations, which is beyond the scope of our current study. Therefore, the magnetization anomaly at  $H'_{c1}$  also becomes more prominent with increasing doping. In the presence of additional nearby impurities (e.g., a third impurity with an

attached aligned spin in the vicinity of the impurity pair) the excitation energy will be higher, leading to a collaborative arrangement of impurities and additional energy excitation levels in between  $H'_{c1}$  and  $H'_{c2}$ . As shown in Fig. 5e, there exist also other two-impurity configurations at lower excitation energies, which is consistent with the experimental observation of the broad maximum at an onset field  $H'_{c0} \sim 9$  T. These further distant impurities have a smaller gap  $\Delta E$ , with  $\Delta E \rightarrow 0$  in the limit of large separations. The excitation energies are influenced also by additional impurities nearby. We note that the state at  $H'_{c0}$  is less prominent than the one at  $H'_{c1} = 0.238J$ , since the probability of these configurations to appear is smaller: e.g., the probability for the state with  $\Delta E = 0.153J$  is only half of that at  $H'_{c1}$ .

## Discussion

One of the most prominent properties of  $\text{SrCu}_2(\text{BO}_3)_2$  is the sequence of magnetization plateaus noticeably at  $1/8$ ,  $1/4$ , and  $1/3$  of the saturation magnetization, which have been shown to correspond to various superstructures that break the translational

symmetry of the lattice. It is remarkable that the high-field magnetization curve exhibits even more features in the presence of impurities. Impurities create local defects that are usually saturated by a small field. Our findings, however, portray a very different picture. Here, even a small concentration of impurity plays an important role in the magnetization process at very high magnetic fields. It highlights a nontrivial interplay between impurities, triplets, and bound states of triplets.

At high magnetic fields, the presence of impurities is found to disrupt the formation of superstructure of bound states of triplets and break it into small patches. In the  $x = 0.05$  sample, these patches of superstructures account for  $\sim 85\%$  of the total  $\text{Cu}^{2+}$  moments, as shown earlier. This significant softening of the superstructures is the reason for the smearing of the pseudo- $1/n$  plateaus in the doped sample. It is expected that the pseudo- $1/n$  plateaus would eventually be totally suppressed as the superstructures are further disrupted with increasing doping. Indeed, the fate of symmetry-breaking phases in the presence of impurities is itself of great current interest<sup>52</sup>. For the crystals of bound states formed at the magnetization plateaus of  $\text{SrCu}_2(\text{BO}_3)_2$ <sup>22,23</sup>, the non-magnetic impurities generically break the symmetries of their order parameters and play the role of random field disorder<sup>52</sup>. Therefore, it is interesting to speculate if there exists impurity-induced Bragg glass phase analogous to that in a type II superconductor<sup>53</sup>. It is also intriguing for future studies to search for other novel phases such as Bose glass, which has been found near Bose-Einstein condensate phase in another doped quantum magnet<sup>54</sup>.

At fields lower than the pseudo- $1/8$  plateau, the emergence of the  $H_{C2}$  and  $H_{C3}$  anomalies upon doping is also a striking and unexpected result. In the undoped system, the energy cost for creating localized bound states is higher than that for the delocalized ones. Therefore, localized bound states are absent, and the bound states are delocalized in the dilute limit, leading to smoothly increasing magnetization curve (i.e., no anomaly at  $H_{C2}$ ). In the doped system, however, the bound states cannot delocalize anymore due to the presence of the impurities. At  $H_{C2}$  all the locations which are sufficiently far away from the impurities (and which have a similar energy cost to form a bound state) will be populated by a bound state, leading to a small jump in the magnetization (i.e., an anomaly) at  $H_{C2}$ . The  $H_{C3}$  anomaly is also absent in the undoped case, where bound states form a superfluid in the dilute limit and regular crystals at higher density, i.e., localized triplets do not occur. Therefore, only in the presence of impurities, the  $H_{C2}$  and  $H_{C3}$  anomalies are realized. It is interesting to speculate how these states evolve, and if more exotic states with some special configurations of impurities and triplets would appear at higher doping.

The observation of the various 2-impurity configurations (impurity pairs) that survive up to  $H_{C0}$  and  $H_{C1}$  is another significant result. It is found that the excitation energies for these impurity pairs are doping independent, at least in the doping range of our study, but the probability of finding them increases with doping. Our results demonstrate a rich and interesting geometrical arrangement of impurities in the doped  $\text{SrCu}_2(\text{BO}_3)_2$ . Moreover, these spin-singlet impurity pairs are fairly stable (binding energy  $\gtrsim g\mu_B H_{C0} \sim 1$  meV), and it is interesting to speculate the formation of Cooper pairs if holes (or electrons) can be associated with the impurities without too much energy cost. Note that the impurity pairs that we observe are strongly localized, suggesting that Cooper pairs, if present, might also be strongly localized. It is interesting to note that in cuprates as well as the doped  $\text{SrCu}_2(\text{BO}_3)_2$  studied in ref. 11, the impurities reside in between the copper-oxide planes, while in  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$ ,  $\text{Mg}^{2+}$  replaces  $\text{Cu}^{2+}$  in the  $\text{CuO}_4$  plane. Further studies are

required to explore the difference between the impurity configurations in the two cases.

In summary, our results present the Mg-doped  $\text{SrCu}_2(\text{BO}_3)_2$  as a model system for studying the effects of non-magnetic impurities in a frustrated quantum magnet, where results from theoretical simulation and multiple experimental methods can be directly compared. We have provided a clear description of the magnetization process for a Shastry-Sutherland system in the presence of impurities, which has a profound effect on the formation of the crystals of bound states of triplets. The results also reveal a rich impurity-induced phenomenology at fields below the magnetization plateaus, suggesting that even for samples with a Mg-doping as low as  $1\% \sim 2.5\%$ , a single-impurity description such as that discussed in refs. 15,16 is not enough to capture the essential physics, and interactions between the impurities and triplets must be considered. Further studies are desired to better understand the impurity-induced emergent states, to search for other possible novel phases (Bragg glass, Bose glass) at high fields, and to pursue the grand prize of RVB superconductivity.

## Methods

**Sample synthesis and characterization.** High quality single crystal samples of both  $\text{SrCu}_2(\text{BO}_3)_2$  and  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$  ( $x = 0.02, 0.03$ , and  $0.05$ ) were grown by the optical floating zone technique using self-flux, at a growth rate of  $0.2 \text{ mm h}^{-1}$  in an  $\text{O}_2$  atmosphere<sup>55</sup>. The  $x = 0.02$  and  $0.03$  samples were successfully grown and were characterized by X-ray powder diffraction. The free  $S = 1/2$  impurities, i.e., the Mg-doping concentrations, for the  $x = 0.02$  and  $0.03$  samples were also characterized with measurements of the dc susceptibility as a function of temperature, using a commercial Quantum Design MPMS (see Supplementary Fig. 1).

**Magnetization measurements.** Magnetization measurements were conducted on samples with approximate dimensions of  $\sim 3.0 \times 0.5 \times 0.5 \text{ mm}^3$  ( $a \times b \times c$ ) using a sample-extraction magnetometer in a 25 ms, 65 T pulsed magnet at the pulsed field facility of the National High Magnetic Field Laboratory in Los Alamos, NM<sup>24</sup>. The sample was placed inside a plastic capsule, which is inserted into or extracted from a pair of coaxial counterwound coils. The background signal was also determined for each temperature and subtracted from the data. Data was obtained for  $\mathbf{H} \parallel a$ -axis down to 0.4 K, and calibrated with absolute values measured in a SQUID magnetometer from Quantum Design.

**Tunnel diode oscillator.** The TDO measurements<sup>56</sup> were carried out on cylinder-shaped crystals with approximate dimensions of  $\sim 2 \text{ mm}$  in length and  $\sim 1 \text{ mm}$  in diameter, at the dc field facility of the National High Magnetic Field Laboratory in Tallahassee, FL. A tunnel diode, operating in its negative resistance region, was used to provide power that maintains the resonance of a LC-circuit, at a frequency range between 10 and 50 MHz. The sample was placed inside a detection coil, with the  $a$ -axis of the sample aligned with the coil axis, forming the inductive component of the LC circuit. Changes in sample magnetization induce a change in the inductance, which is detected as a shift in the resonance frequency. The ability to measure the resonance frequency to a very high precision ensures the highly sensitive measurements in changes of magnetic moments  $\sim 10^{-12}$  e.m.u.<sup>57</sup>.

**Torque magnetometry.** Torque magnetometry measurements were conducted to probe the susceptibility anisotropy of samples with approximate dimensions of  $\sim 0.2 \times 0.2 \times 0.2 \text{ mm}^3$  ( $a \times b \times c$ ) in static magnetic field<sup>22</sup>. Samples were attached with silicone grease to the commercial piezoresistive atomic force microscopy (AFM) cantilevers (Seiko PRC400)<sup>58</sup>, which form a Wheatstone bridge configuration with two additional adjustable resistors. Changes of sample magnetization with field induced torque on the cantilever, and are detected as a voltage across the bridge.

**Magnetostriction measurements.** An optical fiber, equipped with a 1-mm-long fiber Bragg grating (FBG), was attached to single crystal samples with approximate dimensions of  $\sim 3.0 \times 0.5 \times 0.5 \text{ mm}^3$  ( $a \times b \times c$ ) along their  $a$ -axes, using cyanoacrylate. The samples were held in place solely by the fiber, and were orientated such that the applied field is parallel with the  $a$ -axes of the samples. The FBG is illuminated by a broadband light (1525–1565 nm) source, and reflects a narrow band of light ( $\approx 1550 \text{ nm}$ )<sup>59</sup>. The length variation  $\Delta L/L$  along  $a$ -axis axial configuration is detected by monitoring the shift of the reflected light by the FBG<sup>20</sup>.

## Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.



Received: 14 November 2018 Accepted: 9 May 2019

Published online: 04 June 2019

## References

- Lacroix, C., Mendels, P. & Mila, F. *Introduction to Frustrated Magnetism* (Springer, 2011).
- Dommange, S., Mambrini, M., Normand, B. & Mila, F. Static impurities in the  $S=1/2$  kagome lattice: dimer freezing and mutual repulsion. *Phys. Rev. B* **68**, 224416 (2003).
- Fukuhara, T. et al. Quantum dynamics of a mobile spin impurity. *Nat. Phys.* **9**, 235–241 (2013).
- Liu, L., Shao, H., Lin, Y.-C., Guo, W. & Sandvik, A. W. Random-singlet phase in disordered two-dimensional quantum magnets. *Phys. Rev. X* **8**, 041040 (2018).
- Kimchi, I., Sheckelton, J. P., McQueen, T. M. & Lee, P. A. Scaling and data collapse from local moments in frustrated disordered quantum spin systems. *Nat. Commun.* **9**, 4367 (2018).
- Xu, G. et al. Holes in a quantum spin liquid. *Science* **289**, 419–422 (2000).
- Shastry, B. S. & Sutherland, B. Exact ground state of a quantum mechanical antiferromagnet. *Phys. B+C* **108**, 1069–1070 (1981).
- Shastry, B. S. & Kumar, B.  $\text{SrCu}_2(\text{BO}_3)_2$ : A unique Mott Hubbard insulator. *Prog. Theor. Phys. Suppl.* **145**, 1–16 (2002).
- Chung, C.-H. & Kim, Y. B. Competing orders and superconductivity in the doped Mott insulator on the Shastry-Sutherland lattice. *Phys. Rev. Lett.* **93**, 207004 (2004).
- Liu, J., Trivedi, N., Lee, Y., Harmon, B. N. & Schmalian, J. Quantum phases in a doped Mott insulator on the Shastry-Sutherland lattice. *Phys. Rev. Lett.* **99**, 227003 (2007).
- Liu, G. T. et al. Doping effects on the two-dimensional spin dimer compound  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. B* **71**, 014441 (2005).
- Liu, G. T. et al. In-plane substitution effect on the magnetic properties of the two-dimensional spin-gap system  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. B* **73**, 014414 (2006).
- Haravifard, S. et al. In-gap spin excitations and finite triplet lifetimes in the dilute singlet ground state system  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$ . *Phys. Rev. Lett.* **97**, 247206 (2006).
- Aczel, A. A. et al. Impurity-induced singlet breaking in  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. B* **76**, 214427 (2007).
- El Shawish, S. & Bonča, J. Spin-polaron excitations in a doped Shastry-Sutherland model. *Phys. Rev. B* **74**, 174420 (2006).
- Capponi, S., Poilblanc, D. & Mila, F. Theory of the Raman spectra of the Shastry-Sutherland antiferromagnet  $\text{SrCu}_2(\text{BO}_3)_2$  doped with nonmagnetic impurities. *Phys. Rev. B* **80**, 094407 (2009).
- Kageyama, H. et al. Exact dimer ground state and quantized magnetization plateaus in the two-dimensional spin system  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. Lett.* **82**, 3168–3171 (1999).
- Kodama, K. et al. Magnetic superstructure in the two-dimensional quantum antiferromagnet  $\text{SrCu}_2(\text{BO}_3)_2$ . *Science* **298**, 395–399 (2002).
- Sebastian, S. E. et al. Fractalization drives crystalline states in a frustrated spin system. *Proc. Natl Acad. Sci. USA* **105**, 20157–20160 (2008).
- Jaime, M. et al. Magnetostriiction and magnetic texture to 100.75 Tesla in frustrated  $\text{SrCu}_2(\text{BO}_3)_2$ . *Proc. Natl Acad. Sci. USA* **109**, 12404–12407 (2012).
- Takigawa, M. et al. Incomplete Devil's staircase in the magnetization curve of  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. Lett.* **110**, 067210 (2013).
- Haravifard, S. et al. Crystallization of spin superlattices with pressure and field in the layered magnet  $\text{SrCu}_2(\text{BO}_3)_2$ . *Nat. Commun.* **7**, 11956 (2016).
- Corboz, P. & Mila, F. Crystals of bound states in the magnetization plateaus of the Shastry-Sutherland model. *Phys. Rev. Lett.* **112**, 147203 (2014).
- Jorge, G. A. et al. Crystal symmetry and high-magnetic-field specific heat of  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. B* **71**, 092403 (2005).
- Radtke, G., Saül, A., Dabkowska, H. A., Salamon, M. B. & Jaime, M. Magnetic nanopantograph in the  $\text{SrCu}_2(\text{BO}_3)_2$  Shastry-Sutherland lattice. *Proc. Natl Acad. Sci. USA* **112**, 1971–1976 (2015).
- Verstraete, F. & Cirac, J. I. Renormalization algorithms for quantum-many body systems in two and higher dimensions. Preprint at <https://arxiv.org/abs/cond-mat/0407066> (2004).
- Jordan, J., Orús, R., Vidal, G., Verstraete, F. & Cirac, J. I. Classical simulation of infinite-size quantum lattice systems in two spatial dimensions. *Phys. Rev. Lett.* **101**, 250602 (2008).
- Nishio, Y., Maeshima, N., Gendiar, A. & Nishino, T. Tensor product variational formulation for quantum systems. Preprint at <https://arxiv.org/abs/cond-mat/0401115> (2004).
- Corboz, P. & Mila, F. Tensor network study of the Shastry-Sutherland model in zero magnetic field. *Phys. Rev. B* **87**, 115144 (2013).
- Matsuda, Y. H. et al. Magnetization of  $\text{SrCu}_2(\text{BO}_3)_2$  in ultrahigh magnetic fields up to 118 T. *Phys. Rev. Lett.* **111**, 137204 (2013).
- Corboz, P., White, S. R., Vidal, G. & Troyer, M. Stripes in the two-dimensional  $t$ - $J$  model with infinite projected entangled-pair states. *Phys. Rev. B* **84**, 041108 (R) (2011).
- Corboz, P., Rice, T. M. & Troyer, M. Competing states in the  $t$ - $J$  model: Uniform d-Wave state versus stripe state. *Phys. Rev. Lett.* **113**, 046402 (2014).
- Nishino, T. & Okunishi, K. Corner transfer matrix renormalization group method. *J. Phys. Soc. Jpn.* **65**, 891–894 (1996).
- Orús, R. & Vidal, G. Simulation of two-dimensional quantum systems on an infinite lattice revisited: corner transfer matrix for tensor contraction. *Phys. Rev. B* **80**, 094403 (2009).
- Singh, S., Pfeifer, R. N. C. & Vidal, G. Tensor network states and algorithms in the presence of a global  $U(1)$  symmetry. *Phys. Rev. B* **83**, 115125 (2011).
- Bauer, B., Corboz, P., Orús, R. & Troyer, M. Implementing global Abelian symmetries in projected entangled-pair state algorithms. *Phys. Rev. B* **83**, 125106 (2011).
- Corboz, P., Orús, R., Bauer, B. & Vidal, G. Simulation of strongly correlated fermions in two spatial dimensions with fermionic projected entangled-pair states. *Phys. Rev. B* **81**, 165104 (2010).
- Phien, H. N., Bengua, J. A., Tuan, H. D., Corboz, P. & Orús, R. Infinite projected entangled pair states algorithm improved: Fast full update and gauge fixing. *Phys. Rev. B* **92**, 035142 (2015).
- Miyahara, S. & Ueda, K. Exact dimer ground state of the two dimensional Heisenberg spin system  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. Lett.* **82**, 3701–3704 (1999).
- Kageyama, H. et al. Direct evidence for the localized single-triplet excitations and the dispersive multitriplet excitations in  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. Lett.* **84**, 5876–5879 (2000).
- Momoi, T. & Totsuka, K. Magnetization plateaus as insulator-superfluid transitions in quantum spin systems. *Phys. Rev. B* **61**, 3231–3234 (2000).
- Momoi, T. & Totsuka, K. Magnetization plateaus of the Shastry-Sutherland model for  $\text{SrCu}_2(\text{BO}_3)_2$ : spin-density wave, supersolid, and bound states. *Phys. Rev. B* **62**, 15067–15078 (2000).
- Fukumoto, Y. & Oguchi, A. Magnetization process in the Shastry-Sutherland system  $\text{SrCu}_2(\text{BO}_3)_2$ : results of third-order dimer expansion. *J. Phys. Soc. Jpn.* **69**, 1286–1289 (2000).
- Fukumoto, Y. Magnetization plateaus in the Shastry-Sutherland model for  $\text{SrCu}_2(\text{BO}_3)_2$ : Results of fourth-order perturbation expansion with a low-density approximation. *J. Phys. Soc. Jpn.* **70**, 1397–1403 (2001).
- Miyahara, S. & Ueda, K. Theory of the orthogonal dimer Heisenberg spin model for  $\text{SrCu}_2(\text{BO}_3)_2$ . *J. Phys. Condens. Matter* **15**, R327–R366 (2003).
- Miyahara, S., Becca, F. & Mila, F. Theory of spin-density profile and lattice distortion in the magnetization plateaus of  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. B* **68**, 024401 (2003).
- Dorier, J., Schmidt, K. P. & Mila, F. Theory of magnetization plateaus in the Shastry-Sutherland model. *Phys. Rev. Lett.* **101**, 250402 (2008).
- Abendschein, A. & Capponi, S. Effective theory of magnetization plateaus in the Shastry-Sutherland lattice. *Phys. Rev. Lett.* **101**, 227201 (2008).
- Takigawa, M., Waki, T., Horvatic, M. & Berthier, C. Novel ordered phases in the orthogonal dimer spin system  $\text{SrCu}_2(\text{BO}_3)_2$ . *J. Phys. Soc. Jpn.* **79**, 011005 (2010).
- Nemec, M., Foltin, G. R. & Schmidt, K. P. Microscopic mechanism for the  $\frac{1}{8}$  magnetization plateau in  $\text{SrCu}_2(\text{BO}_3)_2$ . *Phys. Rev. B* **86**, 174425 (2012).
- Lou, J., Suzuki, T., Harada, K. & Kawashima, N. *Study of the Shastry Sutherland model using multi-scale entanglement renormalization ansatz*. Preprint at <https://arxiv.org/abs/1212.1999> (2012).
- Vojta, T. Disorder in quantum many-body systems. *Annu. Rev. Condens. Matter Phys.* **10**, 233–252 (2019).
- Klein, T. et al. A Bragg glass phase in the vortex lattice of a type II superconductor. *Nature* **413**, 404–406 (2001).
- Yu, R. et al. Bose glass and Mott glass of quasiparticles in a doped quantum magnet. *Nature* **489**, 379–384 (2012).
- Dabkowska, H. A. et al. Crystal growth and magnetic behaviour of pure and doped  $\text{SrCu}_2(\text{BO}_3)_2$ . *J. Cryst. Growth* **306**, 123–128 (2007).
- Clover, R. B. & Wolf, W. P. Magnetic susceptibility measurements with a tunnel diode oscillator. *Rev. Sci. Instrum.* **41**, 617–621 (1970).
- Van, C. T. Degriif, Tunnel diode oscillator for 0.001 ppm measurements at low temperatures. *Rev. Sci. Instrum.* **46**, 599–607 (1975).
- Ohmichi, E. & Osada, T. Torque magnetometry in pulsed magnetic fields with use of a commercial microcantilever. *Rev. Sci. Instrum.* **73**, 3022 (2002).
- Jaime, M. et al. Fiber Bragg Grating Dilatometry in Extreme Magnetic Field and Cryogenic Conditions. *Sensors* **17**, 2572 (2017).

## Acknowledgements

We are grateful to V. Zapf for help in acquiring the PPMS/MPMS data. We thank T. F. Rosenbaum, D. M. Silevitch, C. D. Batista and B. D. Gaulin for helpful discussions. A portion of this work was performed at the National High Magnetic Field Laboratory,

which is supported by the National Science Foundation Cooperative Agreement No. DMR-1157490 and DMR-1644779, the State of Florida and the U.S. Department of Energy. We acknowledge the use of the Analytical Instrumentation Facility (AIF) at North Carolina State University, which is supported by the State of North Carolina and the National Science Foundation (award number ECCS-1542015). Z.S., W.S., C.M., and S.H. acknowledge support provided by funding from the Powe Junior Faculty Enhancement Award, and William M. Fairbank Chair in Physics at Duke University. P.C. and F.M. acknowledge the support provided by Swiss National Science Foundation and the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement No. 677061). N.H. and M.J. acknowledge support of the DOE BES program Science of 100 Tesla.

### Author contributions

Research conceived and supervised by S.H.; Single-crystal  $\text{SrCu}_{2-x}\text{Mg}_x(\text{BO}_3)_2$  samples grown by C.M., H.A.D., and S.H.; High-field measurements performed by Z.S., W.S., D.G., F.W., N.H., M.J., and S.H., and analyzed by Z.S., W.S. and S.H.; iPEPS calculations performed by P.C. and F.M.; Manuscript written by Z.S., P.C., and S.H.; all authors commented on the manuscript.

### Additional information

**Supplementary Information** accompanies this paper at <https://doi.org/10.1038/s41467-019-10410-x>.

**Competing interests:** The authors declare no competing interests.

**Reprints and permission** information is available online at <http://npg.nature.com/reprintsandpermissions/>

**Journal peer review information:** *Nature Communications* thanks Muhammad Shahbaz Anwar and the other, anonymous, reviewer(s) for their contribution to the peer review of this work. Peer reviewer reports are available.

**Publisher's note:** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.



**Open Access** This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit <http://creativecommons.org/licenses/by/4.0/>.

© The Author(s) 2019