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# Phenomenological aspects of no-scale inflation models

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**Abstract.** We discuss phenomenological aspects of inflationary models wiith a no-scale supergravity Kähler potential motivated by compactified string models, in which the inflaton may be identified either as a Kähler modulus or an untwisted matter field, focusing on models that make predictions for the scalar spectral index $n_s$ and the tensor-to-scalar ratio $r$ that are similar to the Starobinsky model. We discuss possible patterns of soft supersymmetry breaking, exhibiting examples of the pure no-scale type $m_0 = B_0 = A_0 = 0$, of the CMSSM type with universal $A_0$ and $m_0 \neq 0$ at a high scale, and of the mSUGRA type with $A_0 = B_0 + m_0$ boundary conditions at the high input scale. These may be combined with a non-trivial gauge kinetic function that generates gaugino masses $m_{1/2} \neq 0$, or one may have a pure gravity mediation scenario where trilinear terms and gaugino masses are generated through anomalies. We also discuss inflaton decays and reheating, showing possible decay channels for the inflaton when it is either an untwisted matter field or a Kähler modulus. Reheating is very efficient if a matter field inflaton is directly coupled to MSSM fields, and both candidates lead to sufficient reheating in the presence of a non-trivial gauge kinetic function.

**Keywords:** inflation, particle physics - cosmology connection, supersymmetry and cosmology

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## 1 Introduction

One of the biggest challenges for string theory is how to connect with particle and/or cosmological experiments. No-scale supergravity [1–4] is the natural framework to seek such connections, for many reasons. On the one hand, physics at scales hierarchically smaller than the Planck scale is expected to be protected by approximate supersymmetry, which should be local and combined with gravity in some supergravity theory. No-scale supergravity is the most appropriate form, since it emerges naturally as the effective low-energy theory derived from compactified string [5–7], and yields a positive semi-definite potential at the tree level, thus lending itself naturally to cosmology. Moreover, no-scale supergravity



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has recently emerged as a very effective framework for models of cosmological inflation, as discussed in [8–35], yielding models whose predictions can interpolate between those of the Starobinsky model [36] and chaotic inflation with a quadratic potential [37, 38].

This paper is concerned with two fundamental issues in such no-scale models of inflation, the incorporation of supersymmetry breaking and the identification of the inflaton field. Particle experiments hope to constrain the pattern of soft supersymmetry breaking, which is sensitive to the form of the effective supergravity theory, and the breaking of supersymmetry alters the form of the effective inflationary potential, in general. Scenarios for supersymmetry breaking within the minimal supersymmetric extension of the Standard Model (MSSM) that are frequently studied include the constrained MSSM (CMSSM) in which the soft supersymmetry-breaking scalar masses $m_0$, bilinear terms $B_0$, trilinear terms $A_0$ and gaugino masses $m_{1/2}$ are universal at some input scale [39–56]. An interesting special case is that found in minimal supergravity (mSUGRA), where $A_0 = B_0 + m_0$ [57–59]. On the other hand, no-scale supergravity naturally leads to the input conditions $m_0 = B_0 = A_0 = 0$ [1–4]. Generating $m_{1/2} \neq 0$ requires a non-trivial gauge kinetic function in the effective supergravity theory, as may be generated in the underlying string theory or through anomalies [60–64] as in the case of pure gravity mediation (PGM) [65–71]. As we discuss in this paper, CMSSM, mSUGRA, no-scale, and PGM boundary conditions may all be generated within the no-scale inflationary framework.

On the other hand, cosmological observations are providing ever tighter constraints on models of inflation, via measurements of the tilt in the spectral index of scalar perturbations, $n_s$, of the tensor-to-scalar perturbation ratio, $r$, and of non-Gaussian parameters such as $f_{\rm NL}$ [82, 83]. The measurements of $n_s$ and $r$, in particular, constrain the form of the inflationary potential and the number of e-folds, providing information about the form of the effective supergravity theory, the identification of the inflaton, and the couplings that control its decays. As we shall see, these decays, and hence the reheating temperature following inflation and the predicted values of $n_s$ and $r$ are sensitive not only to the identification of the inflaton field but also to the mechanism and magnitude of supersymmetry breaking.

The purpose of this paper is to study the interplay of these cosmological and particle constraints on the effective no-scale supergravity model of inflation with a Kähler potential motivated by string theory, showing how no-scale inflation may thereby serve as a bridge between string theory and LHC physics.

Section 2 of this paper contains a brief review of relevant aspects of the no-scale supergravity framework, and section 3 introduces no-scale scenarios for inflation. Possible patters of soft supersymmetry breaking within these scenarios are discussed in section 4, and inflaton decays and reheating are discussed in section 5. Finally, section 6 summarises our results and indicates possible directions for future work on no-scale inflation.

## 2 Review of the no-scale supergravity framework

As was shown in [5–7], generic string compactifications yield no-scale supergravity as the effective field-theoretical framework for sub-Planckian physics. In a large class of string compactifications, including orbifold examples [16], at the lowest-genus level the Kähler potential $K$ for the dilaton and untwisted moduli fields has the general form

$$K \;=\; -\ln(S+\bar{S}) - \sum_i \ln(T_i+\bar{T}_i) - \sum_j \ln(U_j+\bar{U}_j)\,, \tag{2.1}$$



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where $S$ is the dilaton, the first sum is over the $h_{1,1}$ untwisted Kähler moduli $T_i$, and the second sum is over the $h_{2,1}$ untwisted complex structure moduli $U_j$. We recall that the untwisted Kähler moduli parameterise the sizes of the compactification tori, and that the complex structure moduli parametrise their complex deformations. In general, both $h_{1,1} \geq 3$ and $h_{2,1}$ are model-dependent: here we assume the minimum value $h_{1,1} = 3$. We also assume that the dilaton $S$ and the complex structure moduli $U_j$ are fixed, as well as the relative sizes of the untwisted Kähler moduli, so that we may simplify

$$-\ln(S+\bar{S}) - \sum_i \ln(T_i+\bar{T}_i) - \sum_j \ln(U_j+\bar{U}_j) \;\rightarrow\; -3\ln(T+\bar{T})\,, \tag{2.2}$$

where we term $T$ the volume modulus. Untwisted matter fields $\phi_\alpha$ may then be included via the substitution

$$T+\bar{T} \;\rightarrow\; T+\bar{T} - \frac{1}{3}\sum_\alpha |\phi_\alpha|^2\,. \tag{2.3}$$

Finally, we include in the lowest-genus effective Kähler potential twisted matter fields $\varphi_a$ with generic modular weights $n_a$, arriving at

$$K \;=\; -3\ln\left(T+\bar{T} - \frac{1}{3}\sum_\alpha |\phi_\alpha|^2\right) + \sum_a \frac{|\varphi_a|^2}{(T+\bar{T})^{n_a}}\,, \tag{2.4}$$

which we use as the basis of our subsequent discussion.

Equation (2.4) is not the only possible starting-point for no-scale inflation and particle phenomenology, since it embodies several assumptions about the moduli of the string compactification and their stabilisation, but it is sufficiently general to have several relevant and interesting features such as accommodating Starobinsky-like inflation,[1] as we explore in the subsequent sections.

## 3 Scenarios for no-scale inflation

Supersymmetry offers a natural framework for constructing inflationary models [75–77] and, as the scales involved in these models approach the Planck scale, it is necessary to consider these models in the context of supergravity [78–81]. The simplest of such models in both simple [80] and no-scale supergravity [8] make a very definite prediction for the scalar tilt in the microwave background anisotropy, namely $n_s = 0.933$, which is now definitively excluded by Planck measurements [82, 83]. In contrast, the Starobinsky model of inflation based on a $R + R^2$ extension of gravity predicts $n_s = 0.965$ [84, 85], in excellent agreement with the Planck value $n_s = 0.9653 \pm 0.0048$.

It was shown that no-scale supergravity could lead to a consistent $R + R^2$ extension of gravity [86], and the Starobinsky model of inflation was derived recently from no-scale supergravity models [17, 19]. Phenomenologically viable models of inflation in no-scale supergravity generally require at least two chiral superfields. One of these fields is the volume modulus, $T$, and the other an untwisted matter field, $\phi$. In what follows, we will consider the phenomenological consequences of both possibilities when both untwisted and twisted matter fields are added to the theory. In this context, we discuss supersymmetry breaking in the next section, and scenarios for inflaton decays and reheating in the following section. As we shall see, these issues are connected in non-trivial ways.

[1] Our approach here is therefore complementary to constructions of explicit inflationary models in specific string scenarios such as those in [72–74], the second of which yields a value of $r$ a factor of 2 larger than Starobinsky inflation.



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### 3.1 No-scale inflationary models and the Starobinsky model

In this simplest no-scale supergravity, the two complex fields, denoted here by $(T, \phi)$, parametrise a $\mathrm{SU}(2,1)/\mathrm{SU}(2) \times \mathrm{U}(1)$ coset space, and the Kähler potential may be written in the form

$$K \;=\; -3\ln\left(T+\bar{T}-\frac{|\phi|^2}{3}\right). \tag{3.1}$$

We recall that, here and throughout the paper, we assume that the dilaton field $S$ has been fixed by some unspecified dynamics. The effective Lagrangian stemming from this Kähler potential has the form

$$\mathcal{L} \;=\; (T+\bar{T}-|\phi|^2/3)^{-1}(\partial_\mu T, \partial_\mu\phi)\begin{pmatrix} 3 & -\phi \\ -\bar{\phi} & T+\bar{T}\end{pmatrix}\begin{pmatrix}\partial^\mu\bar{T}\\ \partial^\mu\bar{\phi}\end{pmatrix} - \frac{\hat{V}}{(T+\bar{T}-|\phi|^2/3)^2}\,, \tag{3.2}$$

where

$$\hat{V} = |W^\phi|^2 + \frac{1}{3}(T+\bar{T})|W^T|^2 + \frac{1}{3}\left(W^T(\bar{\phi}\bar{W}_\phi - 3\bar{W}) + \text{h.c.}\right). \tag{3.3}$$

The kinetic terms and scalar potential are derived from

$$\mathcal{L}_{B,\text{kin}} = G^I_J D_\mu \Phi_I D^\mu \bar{\Phi}^J\,, \tag{3.4}$$

and

$$\mathcal{L}_{B,\text{pot}} = -e^G(G_I(G^{-1})^I_J G^J - 3)\,, \tag{3.5}$$

where the Kähler function $G$ is defined as

$$G = K + \ln|W|^2\,, \tag{3.6}$$

and first- (second-)order derivatives of $G$ with respect to generic fields [and their conjugates] $\Phi_I[\bar{\Phi}^J]$ are denoted by $G^I[G_J]$ $(G^I_J)$. In (3.6) we denote by $W(T,\phi)$ the superpotential, and $W^T \equiv \partial W/\partial T$, $W^\phi \equiv \partial W/\partial\phi$. Unless explicitly denoted, we will work in Planck units $M_P^2 = 1$, where $M_P^{-2} = 8\pi G_N$ refers to the normalized Planck mass. We note that the scalar kinetic term is invariant with respect to the action of the $\mathrm{SU}(2,1)$ group, but the scalar potential is in general not invariant. This implies that, for a given superpotential, the roles played by $T$ and $\phi$ are in general not interchangeable. In particular, depending on the form of $W$, either $T$ or $\phi$ may play the role of the inflaton, and we consider both possibilities in this paper.

For example, it was found in [17] that the $T$-independent Wess-Zumino superpotential

$$W = m\left(\frac{\phi^2}{2} - \frac{\phi^3}{3\sqrt{3}}\right) \tag{3.7}$$

leads to

$$V = 3m^2\,\mathrm{sech}^2\left(\frac{\chi-\bar{\chi}}{\sqrt{3}}\right)\left|\sinh\left(\chi/\sqrt{3}\right)\left(\cosh\left(\chi/\sqrt{3}\right) - \sinh\left(\chi/\sqrt{3}\right)\right)\right|^2\,, \tag{3.8}$$

where $\chi = \sqrt{3}\tanh^{-1}(\phi/\sqrt{3})$. In terms of the normalised real and imaginary parts of the inflaton, $\chi = (x+iy)/\sqrt{2}$, it takes the form

$$V = \frac{3}{2}m^2 e^{-\sqrt{2/3}x}\left[\cosh\left(\sqrt{2/3}\,x\right)\sec\left(\sqrt{2/3}\,y\right) - 1\right]\,, \tag{3.9}$$



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and for $y = 0$ it is identical to the Starobinsky inflationary potential

$$V = \frac{3}{4}m^2\left(1 - e^{-\sqrt{2/3}x}\right)^2 , \tag{3.10}$$

obtained from a higher derivative form of the gravitational action,

$$S = \frac{1}{2}\int d^4x\sqrt{-g}\left(R + \frac{R^2}{6m^2}\right) . \tag{3.11}$$

Note that at the minimum of the potential, the masses of both the real and imaginary parts of $\chi$ are equal to $m$. This identification between the no-scale Wess-Zumino model and $R^2$ gravity is possible if the modulus $T$ has a fixed vacuum expectation value $\langle T\rangle = 1/2$.[2] We also note here that $T$ must be stabilized, and we discuss the stabilization of $T$ later in section 4.1.1. This results in a hierarchically large mass for both the real and imaginary parts of $T$.

Conversely, with a superpotential of the form [86]:[3]

$$W = \sqrt{3}m\phi(T - 1/2), \tag{3.12}$$

the modulus $T$ plays the role of the inflaton field, with a Starobinsky potential along the canonically-normalized real direction, $T = \frac{1}{2}(e^{-\sqrt{2/3}t} + i\sqrt{2/3}\sigma)$, for $\phi$ fixed at zero.

Both forms (eqs. (3.7) and (3.12)) can be generalized by making use of SU(2,1) transformations, or by adding additional superpotential terms that do not affect the scalar potential along the inflationary trajectory [19]. We make use of one such generalization below, based on the addition of terms such as

$$\Delta W = \left[\frac{(T - 1/2)^n 2^{n-2}\phi}{(2T + 1)^{n-2}}\right] \tag{3.13}$$

that introduce new couplings between the inflaton ($\phi$ in this case) and the volume modulus.

### 3.2 Symmetric formulation

The $\mathrm{SU}(2,1)/\mathrm{SU}(2) \times \mathrm{U}(1)$ model can be rewritten equivalently in a more symmetric form with Kähler potential

$$K = -3\log\left(1 - \frac{|y_1|^2 + |y_2|^2}{3}\right) . \tag{3.14}$$

In this basis, the $\mathrm{SU}(2,1)$ transformations of the fields correspond to

$$y_1 \to \sqrt{3}\frac{A_{11}y_1 + A_{12}y_2 + \sqrt{3}A_{13}}{A_{31}y_1 + A_{32}y_2 + \sqrt{3}A_{33}} , \quad y_2 \to \sqrt{3}\frac{A_{21}y_1 + A_{22}y_2 + \sqrt{3}A_{23}}{A_{31}y_1 + A_{32}y_2 + \sqrt{3}A_{33}} , \tag{3.15}$$

with $A \in \mathrm{SU}(2,1)$. The complex fields $y_{1,2}$ are related to the fields $T, \phi$ by the relations

$$y_1 = \left(\frac{2\phi}{1 + 2T}\right) , \qquad y_2 = \sqrt{3}\left(\frac{1 - 2T}{1 + 2T}\right) , \tag{3.16}$$

[2] For a generic expectation value $\langle T\rangle = c$, the $R^2$ gravity model is obtained if one chooses a superpotential of the form $W = \tilde{m}\left(\phi^2/2 - \phi^3/(3\sqrt{6c})\right)$, where $\tilde{m} = (2c)^{1/2}m$. Thus the value of the expectation value for $T$ plays no role in our analysis. The choice $\langle T\rangle = 1/2$ is made out of convenience.

[3] It would be interesting to see whether this form could be derived in a suitable string framework.



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and their inverses

$$T = \frac{1}{2}\left(\frac{1 - y_2/\sqrt{3}}{1 + y_2/\sqrt{3}}\right), \qquad \phi = \left(\frac{y_1}{1 + y_2/\sqrt{3}}\right). \tag{3.17}$$

Simultaneously, the superpotential is transformed as

$$W(T, \phi) \rightarrow \widetilde{W}(y_1, y_2) = \left(1 + y_2/\sqrt{3}\right)^3 W\,. \tag{3.18}$$

Unsurprisingly, under the transformations (3.17), (3.18), inflationary potentials in the $(T, \phi)$ basis are mapped into inflationary potentials in the $y_{1,2}$ basis [19]. In particular, the Wess-Zumino superpotential (3.7) transforms to

$$\widetilde{W} = m\left[\frac{y_1^2}{2}\left(1 + \frac{y_2}{\sqrt{3}}\right) - \frac{y_1^3}{3\sqrt{3}}\right], \tag{3.19}$$

for which the Starobinsky potential is recovered along the canonically normalized $y_1$ direction for $y_2 = 0$. Analogously, the superpotential (3.12) transforms into

$$\widetilde{W} = m y_1 y_2 \left(1 + y_2/\sqrt{3}\right), \tag{3.20}$$

where now $y_2$ plays the role of the inflaton, with a Starobinsky potential along its real direction.

### 3.3 Incorporation of twisted matter

In [28, 29] we found a different realization of inflation within a no-scale setting, by considering a no-scale structure with a twisted matter field with a sum of modular weights $\sum_i n_a^i = 3$, described by the Kähler potential

$$K \;=\; -\sum_{i=1}^{3} \ln(T_i + \bar{T}^i) + \frac{|\varphi|^2}{\prod_{i=1}^{3}(T_i + \bar{T}^i)}\,. \tag{3.21}$$

In particular, when the ratios of the moduli are fixed at a high scale as in (2.3), the Kähler potential can be written in the form

$$K \;=\; -3\ln(T + \bar{T}) + \frac{|\varphi|^2}{(T + \bar{T})^3}\,. \tag{3.22}$$

Making the choice of superpotential[4]

$$W = \sqrt{3} m \varphi (T - 1/2)\,, \tag{3.23}$$

it was shown that at $\varphi = 0$ the effective potential for $T$ is sufficiently flat to allow inflation for any initial condition in the complex $T$ plane far away enough from the origin. Moreover, the standard Starobinsky potential is recovered along the (canonically-normalized) real direction, whereas the chaotic quadratic potential appears along the imaginary direction.[5]

[4] As commented in connection with (3.12), it would be interesting to see whether this form could be derived in any string framework.

[5] See [25, 26] for other attempts at quadratic chaotic inflation in a complexification of the Starobinsky model.



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### 3.4 Phenomenological issues

Our goal in this work is to embed the inflationary models with Kähler potentials (3.1), (3.22) in a more complete supergravity model, including matter fields and a source of supersymmetry breaking. As was pointed out in [28], the addition of a *supersymmetry-breaking* sector modifies in general the form of the inflationary potential, and it is of interest to determine to what extent the conclusions drawn in the pure $(T, \phi)$ or $(T, \varphi)$ scenarios still hold.[6] Furthermore, previous studies [87, 88] of *inflaton decays* in a no-scale set up have shown that, in the absence of a direct coupling of the inflaton to matter, or of a non-trivial gauge kinetic function, the decays of the inflaton are completely suppressed at tree level. It was assumed in [87] that the Kähler potential possessed an overall no-scale $\mathrm{SU}(N+1)/[\mathrm{SU}(N) \times \mathrm{U}(1)]$ symmetry, including $N$ matter fields, with the volume modulus $T$ playing the role of the supersymmetry-breaking field with flat tree-level potential. However, here we consider a generic no-scale model with the Kähler potential of the form (2.4), and we explore the phenomenological implications of this model for two different scenarios: one in which $T$ is the inflaton, and another in which one of the untwisted matter fields $\phi_\alpha$ is responsible for inflation. Matter fields may be either twisted or untwisted.

## 4 Patterns of supersymmetry breaking

In order to break supersymmetry, the superpotential must have a non-zero vacuum expectation value at the minimum of the scalar potential. We consider first scenarios in which the inflaton is identified with one of the untwisted matter fields $\phi_\alpha$, which we denote by $\phi_1$. In such a case we know that a $T$-independent superpotential like (3.7) leads to an inflationary potential. The volume modulus $T$ is free to play a role in supersymmetry breaking, and we discuss in this section various options for achieving this while obtaining Starobinsky-like inflation and zero vacuum energy.

### 4.1 Scenarios with a matter inflaton

#### 4.1.1 Supersymmetry breaking via the volume modulus

One possibility is to add a constant term to a superpotential that otherwise would have a vanishing vacuum expectation value (vev). For definiteness we consider a generic superpotential of the form

$$\begin{aligned} W = {} & W_{\rm inf}(T, \phi_1) + (T+c)^\beta W_2(\phi_i) + (T+c)^\alpha W_3(\phi_i) \\ & + (T+c)^\sigma W_2(\varphi_a) + (T+c)^\rho W_3(\varphi_a) + \mu \,, \end{aligned} \tag{4.1}$$

where $c$ is an arbitrary constant, and $W_{2,3}$ denote bilinear and trilinear terms with modular weights that are in general non-zero. If we assume vanishing $F$ terms for all the scalar fields: $\langle W^I \rangle = 0$, and vanishing vevs for all scalar fields except $T$, the inflationary minimum $\phi_1 = 0$ corresponds to a supersymmetry-breaking minimum with vanishing cosmological constant if the following constraints are satisfied,

$$\langle W^{TT} \rangle = \langle W^{T\phi_1} \rangle = 0 \,. \tag{4.2}$$

These are trivially fulfilled for the Wess-Zumino superpotential (3.7). When $\{\phi, \varphi\} = 0$, the effective potential for $T$ is completely flat at the tree level, so the volume modulus has an

[6] Throughout this paper, $\phi$ will refer to an untwisted field and $\varphi$ will refer to a twisted field.



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undetermined vev, and the gravitino mass

$$m_{3/2} = \frac{\mu}{(T+\bar{T})^{3/2}} \tag{4.3}$$

varies with the value of the volume modulus.

The induced soft terms can readily be calculated:[7] they are sector-dependent and sensitive to the vev of $T$, and are given by

$$\phi_\alpha : \quad m_0 = 0\,, \quad B_0 = -\beta m_{3/2}\frac{(T+c)^{\beta-1}}{(T+\bar{T})^{1/2}}\,, \quad A_0 = -\alpha m_{3/2}\frac{(T+c)^{\alpha-1}}{(T+\bar{T})^{1/2}}\,, \tag{4.4}$$

$$\varphi_a : \begin{cases} m_0 = m_{3/2}\dfrac{(1-n_a)^{1/2}}{(T+\bar{T})^{n_a/2}}\,, \\ B_0 = 2m_{3/2}\dfrac{(T+c)^{\sigma-1}}{(T+\bar{T})^{3/2}}\left[(1-n_a)(T+c) - \dfrac{\sigma}{2}(T+\bar{T})\right]\,, \\ A_0 = 3m_{3/2}\dfrac{(T+c)^{\rho-1}}{(T+\bar{T})^{3/2}}\left[(1-n_a)(T+c) - \dfrac{\rho}{3}(T+\bar{T})\right]\,, \end{cases} \tag{4.5}$$

One can immediately check that $G^I = 0$ for $I = \phi_\alpha, \varphi_a$, and that $G^T = -3/(T+\bar{T})$. Therefore, as expected, the Goldstino $\eta = \sum_l G^I \chi_I$ is the fermionic partner of the modulus $T$, namely the modulino $\chi_T$.

The previous results ignore the fact that one typically needs to fix the vacuum expectation value of the volume modulus $T$ during inflation. In the case of the Wess-Zumino model (3.7), the Starobinsky potential is obtained for $\langle T\rangle = c$. This vev may be fixed with the addition of strongly stabilizing terms in the Kähler potential of the form [19, 97]

$$K \;=\; -3\ln\left(T+\bar{T} + \frac{(T+\bar{T}-2c)^4 + d(T-\bar{T})^4}{\Lambda^2} - \frac{|\phi_1|^2}{3} + \cdots\right) + \cdots\,. \tag{4.6}$$

This modification of $K$ fixes $T$ during inflation and generates a mass term for it. If $\Lambda \ll 1$, this mass is hierarchically larger than the gravitino mass:

$$m_T^2 = 144c(d+1)\frac{m_{3/2}^2}{\Lambda^2}\,. \tag{4.7}$$

We note that stabilzation based on (4.6) does not upset the inflationary dynamics of the Starobinsky model. In contrast, it has been shown that other forms of stabilization (through the superpotential) do not allow for a successful realization of the Starobinsky model [98]. With the addition of the stabilizing terms, the induced soft parameters (4.4), (4.5) reduce to

$$\phi_i : \; m_0 = 0\,, \qquad B_0 = -\beta m_{3/2}\,, \qquad A_0 = -\alpha m_{3/2} \tag{4.8}$$

$$\varphi_a : \; m_0 = (1-n_a)^{1/2} m_{3/2}, \quad B_0 = 2\left(1-n_a-\frac{\sigma}{2}\right)m_{3/2}, \quad A_0 = 3\left(1-n_a-\frac{\rho}{3}\right)m_{3/2} \tag{4.9}$$

after rescaling the fields, $\phi_i' = (2c)^{-1/2}\phi_i$, $\varphi_a' = (2c)^{-n_a/2}\varphi_a$, where $\phi', \varphi'$ are canonically normalized, and upon rescaling:

$$\begin{aligned} &W_2(\phi_i) \to (2c)^{3/2-\beta} W_2(\phi_i')\,, \quad W_3(\phi_i) \to (2c)^{3/2-\alpha} W_3(\phi_i')\,, \\ &W_2(\varphi_a) \to (2c)^{3/2-\sigma} W_2(\varphi_a')\,, \quad W_3(\varphi_a) \to (2c)^{3/2-\rho} W_3(\varphi_a') \end{aligned} \tag{4.10}$$

[7] Related derivations of soft terms in string models with flux compactifications can be found in [94–96].



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with $m_{3/2} = (2c)^{-3/2}\mu$. The forms of the soft supersymmetry-breaking terms for the twisted matter fields suggest that modular weights with $n_a > 1$ in the Kähler potential are not consistent with this framework. A careful analysis reveals that in such cases the fields evolve towards a global anti-de-Sitter (AdS) minimum.

The forms of eqs. (4.8) and (4.9) open up various phenomenological possibilities, some of which we now enumerate.

- If all matter fields are of the untwisted type, we see that there are no supersymmetry-breaking contributions to scalar masses. If in addition, the modular weights $\alpha$ and $\beta$ vanish, then $A_0 = B_0 = 0$. and we recover the original *no-scale* boundary conditions [3, 4]. Models with radiative electroweak symmetry breaking [99–104] can be accommodated if these boundary conditions are fixed at scales above the GUT scale [22, 105, 106]. In addition, this yields a much more restrictive phenomenological parameter space than CMSSM-like models since the ratio of the Higgs vevs, $\tan\beta$, is determined by the Higgs minimization conditions and is no longer a free parameter [58, 59].

- However, if matter fields are of the twisted type, then other possibilities arise. For simplicity, let us take the kinetic modular weights to be 0. In this case, we have universal soft scalar masses as in *CMSSM*-like models, which are determined by the gravitino mass [57].

- On the other hand, when the superpotential weights are equal ($\rho = \sigma$), we obtain *mSUGRA*-like boundary conditions, with $A_0 = (3-\rho)m_{3/2}$ and $B_0 = (2-\rho)m_{3/2}$, i.e., $B_0 = A_0 - m_0$ [57–59]. These mSUGRA-like models also yield a much more restrictive phenomenological parameter space where, in the context of radiative electroweak symmetry breaking, the ratio of the Higgs vevs, $\tan\beta$, is again determined by the Higgs minimization conditions and no longer a free parameter.

- Had we chosen to work in the symmetric $(y_1, y_2)$ basis with no superpotential weights, we would find $\rho = \sigma = 3$, in which case $A_0 = 0$ and $B_0 = -m_{3/2}$. If, in addition, there are no tree-level sources for gaugino masses, the models would be equivalent to *pure gravity mediation* (PGM) with radiative electroweak symmetry breaking [68–71].

- Finally, we note that if the weights $n_a \neq 0$, we have a source for *non-universal scalar masses* in the twisted sector.

Further examples of no-scale, CMSSM and mSUGRA patterns of soft supersymmetry breaking are presented subsequently.

One possible generalization of the superpotential (4.1) is to incorporate a modular weight for $\mu$:

$$\mu \to \mu(T+c)^p \,. \tag{4.11}$$

It is not difficult to verify that the scalar potential is not minimized at $(T, \phi_1) = (c, 0)$ for generic $p \neq 0$. However, with the addition of the stabilizing term (4.6) one always has $\langle T \rangle \simeq c$ and a $p$-dependent inflationary potential of the form

$$\begin{aligned} V = 3m^2 \cosh^4\left(\frac{x}{\sqrt{6}}\right) \Bigg[ \tanh^4\left(\frac{x}{\sqrt{6}}\right) - 2\tanh^3\left(\frac{x}{\sqrt{6}}\right) \\ + \left(1 - \frac{p\tilde{\mu}}{3m}\right)\tanh^2\left(\frac{x}{\sqrt{6}}\right) + \left(\frac{p}{3} - 2\right)\frac{p\tilde{\mu}^2}{3m^2} \Bigg] \end{aligned} \tag{4.12}$$



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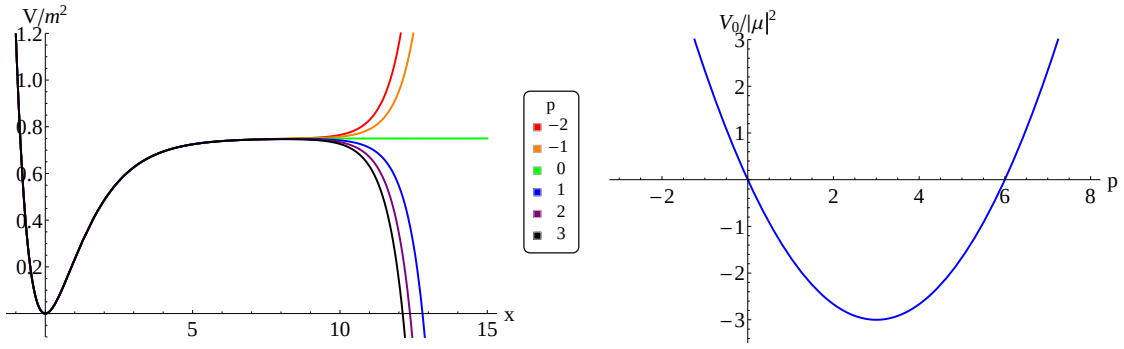


**Figure 1**. Projections of the effective inflationary potential for the model (3.7) with the stabilised Kähler potential (4.6) and the $T$-dependent superpotential $\Delta W = \mu(T + 1/2)^p$, for different values of $p$, and $c = 1/2$. Here $T$ is stabilized at $T = 1/2$ with $\Lambda^{-2} = 10$, and we use the nominal values $m = 10^{-5}$, $\mu = 10^{-13}$. Left: the potential along the canonically-normalized real direction, $x = \sqrt{6}\tanh^{-1}(\phi_1/\sqrt{3})$. Right: the cosmological constant as a function of $p$.

where

$$\tilde{\mu} = (2c)^{p-3/2}\mu, \tag{4.13}$$

and

$$x = \sqrt{6}\tanh^{-1}(\phi_1/\sqrt{6c}) \tag{4.14}$$

denotes the canonically-normalized real part of $\phi_1$. The left panel of figure 1 shows the shape of the potential for various values of $p$. As expected, for $p = 0$ one exactly recovers the Starobinsky potential. When we assume a ratio $\mu/m = 10^{-8}$ (corresponding to $\mu \sim 100\,\text{TeV}$) then for $x \lesssim 9$ (during the inflationary phase) the potentials are almost indistinguishable, yielding a maximum of $N_{\text{max}} \simeq 1160$ e-folds of inflation. For smaller $\mu$, the potential remains flat to higher $x$ and more e-folds of inflation are possible. However, the right panel of figure 1 shows that there is, in general, a non-vanishing cosmological constant at $x = 0$, where

$$V_0 = \frac{|\tilde{\mu}|^2}{3}p(p-6)\,. \tag{4.15}$$

Note that for $p > 0$, the potential is unbounded from below and for $p < 0$, we have a positive cosmological constant, so that $p = 0$ is the only possible solution in this case.

### 4.1.2 Supersymmetry breaking via the Polonyi mechanism

As another possible generalization of the above set of models, we can promote $\mu$ in (4.1) to have the form of the Polonyi superpotential [107], dependent on a singlet field $z$:

$$\mu \to \mu(z + \nu)\,, \tag{4.16}$$

which belongs to the twisted matter sector and has zero modular weight, assuming a strongly-stabilized Kähler potential [108–110]

$$K \supset z\bar{z} - \frac{(z\bar{z})^2}{\Lambda_z^2} \tag{4.17}$$

which might be due, e.g., to non-perturbative effects. In the standard scenario, the second term in (4.17) drives the field $z$ to a supersymmetry breaking minimum located at



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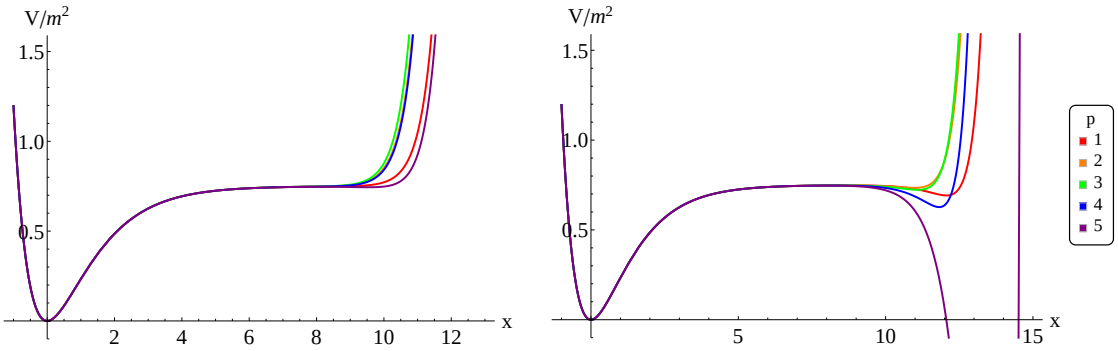


**Figure 2**. Projections of the effective inflationary potential for the model (3.7) with the Polonyi sector (4.17) with superpotential $\Delta W = \mu(z+\nu)(T+1/2)^p$ (4.18), for different values of $p$ and $c = 1/2$. Here $T = 1/2$, $z$ and $\nu$ are given by (4.19), and we use the nominal values $m = 10^{-5}$, $\mu = 10^{-13}$. Left: the potential along the canonically-normalized real direction, $x = \sqrt{6}\tanh^{-1}(\phi_1/\sqrt{3})$, for $\Lambda_z = 10^{-2}$. Right: idem. for $\Lambda_z = 4 \times 10^{-3}$.

$z \simeq \Lambda_z^2/\sqrt{12}$, with the parameter $\nu \simeq 1/\sqrt{3}$ tuned to yield a vanishing cosmological constant [110, 111]. In the present case, with a no-scale inflationary sector where $\phi_1$ is identified as the inflaton, the same values of $z, \nu$ with $T = c$, $\phi_1 = 0$ minimize the scalar potential. However, this point in field space corresponds to a deSitter minimum with cosmological constant $V_0 \simeq |\tilde{\mu}|^2$.

This positive vacuum energy may be used to uplift a potential that would otherwise have an AdS minimum. In particular, in the case of (4.11) with $0 < p < 6$, the extremum at $x = 0$ can be uplifted if, instead of the superpotential (4.11), we assume

$$\mu \to \mu(z+\nu)(T+c)^p\,. \tag{4.18}$$

The scalar potential is minimized with a zero cosmological constant at $(T, \phi_1) = (c, 0)$ for

$$z \simeq -\frac{(p^2-6p+3)\Lambda_z^2}{4(3p(6-p))^{1/2}}\,, \qquad \nu \simeq \left(\frac{3}{p(6-p)}\right)^{1/2}\,, \tag{4.19}$$

assuming $\Lambda_z \ll 1$. For a small stabilizing parameter $\Lambda_z \ll \mu/m$, the superpotential (4.18) becomes virtually indistinguishable from (4.11). However, for the range of $p$ that we consider, the global minimum is not located at $x = 0$, but corresponds to an AdS minimum located at

$$x_{\rm AdS} \simeq -\frac{1}{2}\sqrt{\frac{3}{2}}\log\left[\frac{3(6-p)\mu^2}{64m^2p}\right]\,, \qquad V_{\rm AdS} \simeq -\frac{4m^3}{3\sqrt{3}\tilde{\mu}}\left(\frac{p}{6-p}\right)^{3/2}\,. \tag{4.20}$$

For larger, but still small values of $\Lambda_z$, there is still a minimum at large $x$, but it is no longer a global minimum. In order to avoid this minimum altogether, the stabilizing parameter $\Lambda_z$ must satisfy the constraint

$$\Lambda_z \gtrsim f(p)\left(\frac{\tilde{\mu}}{m}\right)^{0.3}\,, \tag{4.21}$$

where $f \sim 2$ for $0 < p \leq 4$, $f \simeq 4$ for $p = 5$. This constraint is illustrated in figure 2 for $\mu/m = 10^{-8}$.

The gravitino mass in this model is

$$m_{3/2} \;=\; \tilde{\mu}\left(\frac{3}{p(6-p)}\right)^{1/2}\,. \tag{4.22}$$



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Assuming a superpotential for the matter fields of the form (4.1), the induced soft parameters take the forms

$$\phi_i : \begin{cases} m_0 = \frac{1}{3}((6-p)p)^{1/2} m_{3/2}\,, \\ B_0 = -\frac{1}{3}(p - \beta(p-3)) m_{3/2}\,, \\ A_0 = \frac{1}{3}\alpha(p-3) m_{3/2}\,, \end{cases} \tag{4.23}$$

$$\varphi_a : \begin{cases} m_0 = \frac{1}{3}(9 - n_a(p-3)^2)^{1/2} m_{3/2}\,, \\ B_0 = \frac{1}{3}(6 + 2n_a(p-3) + p(\sigma-3) - 3\sigma) m_{3/2}\,, \\ A_0 = -\frac{1}{3}(3 - 3n_a - \rho)(p-3) m_{3/2}\,. \end{cases} \tag{4.24}$$

In this case, the untwisted matter sector has non-vanishing soft supersymmetry-breaking masses for any $0 < p < 6$, which are of universal CMSSM type. If $p = 3$, one has mSUGRA boundary conditions $m_0 = m_{3/2}, B_0 = -m_0$ and $A_0 = 0$ in both the untwisted and twisted sectors. Since the twisted-sector soft supersymmetry-breaking parameters are independent of the modular weights $n_a$ for $p = 3$, all values of the weights are allowed in this case. For $n_a = 0$ or for $p = 2, 4$ and modular weight $n_a = 9$, the soft supersymmetry-breaking scalar masses $m_0 = 0$ in the twisted sector.

It is natural to consider if an untwisted Polonyi sector can provide the necessary uplifting for the superpotential (4.11). It can be shown that this uplifting can be achieved, but at the cost of spoiling the inflationary potential. For example, using a superpotential of the form

$$\mu \to \mu \left( \frac{z}{\sqrt{3}} + \nu \right)^q (T + c)^p\,, \tag{4.25}$$

it is possible to show that the resulting potential is either unbounded from below or possesses an AdS minimum for large values of $x$, the canonically-normalized real component of $\phi_1$. The addition of strong stabilization terms for $z$ in the Kähler potential does not alleviate these problems.

### 4.1.3 Incorporating the Giudice-Masiero mechanism

The Giudice-Masiero (GM) mechanism [112] is a well-known extension of minimal supergravity in which a term proportional to $H_1 H_2$ is introduced into the Kähler potential, so as to avoid the explicit introduction of a term $\mu_H H_1 H_2$ in the superpotential with a coefficient $\mu_H$ with scale similar to that of electroweak symmetry breaking. In our no-scale framework, there are several ways to implement this mechanism, depending on the sector to which the Higgs superfields belong. If the Higgs belong to the twisted sector with modular weights $n_1, n_2$, then a generic GM term of the form

$$\Delta K = (T + \bar{T})^{-n_{12}} \left( c_H (T + c)^\gamma H_1 H_2 + \text{h.c.} \right) \tag{4.26}$$

induces the $\mu$-term and a soft $B$-term,

$$\begin{aligned} \Delta\mu_H &= (1 - \tilde{n}_{12}) c_H m_{3/2}\,, \\ \Delta B\mu &= \left[ (1 - \tilde{n}_{12})(2 - \tilde{\gamma} - \tilde{n}_1 - \tilde{n}_2 + \tilde{n}_{12}) + \frac{p}{3}\tilde{n}_{12} \right] c_H m_{3/2}^2\,, \end{aligned} \tag{4.27}$$



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where a tilde denotes a rescaling by a factor of $(3-p)/3$, e.g. $\tilde{\gamma} = \frac{3-p}{3}\gamma$, and where we have rescaled $c_H \to (2c)^{n_{12}-\gamma-(n_1+n_2)/2} c_H$. In the case of minimal (no) coupling to $T$, these reduce to $\Delta\mu_H = c_H m_{3/2}$, $\Delta B\mu = 2c_H m_{3/2}^2$. When the Higgs fields belong to the untwisted sector, a GM term such as (4.26) generates soft terms of the form

$$\Delta\mu_H = (1-\tilde{n}_{12}) c_H m_{3/2}\,, \qquad \Delta B\mu = [(1-\tilde{n}_{12})(\tilde{n}_{12}-\tilde{\gamma}+p/3)+p/3]\, c_H m_{3/2}^2. \tag{4.28}$$

Alternatively, one can consider scenarios in which the GM term resides inside the logarithm. One of the possibilities is

$$K = -3\ln\left[T+\bar{T} - \frac{1}{3}\left(|H_1|^2+|H_2|^2 + (T+\bar{T})^{-q}(c_H(T+c)^{\gamma} H_1 H_2 + \text{h.c.}) + \cdots\right)\right] \tag{4.29}$$

for which

$$\Delta\mu_H = (p/3-\tilde{q}) c_H m_{3/2}\,, \qquad \Delta B\mu = \left[-\tilde{q}(1+\tilde{q}-\tilde{\gamma}-p/3) + \frac{p}{3}(2-\tilde{\gamma})\right] c_H m_{3/2}^2, \tag{4.30}$$

with $c_H \to (2c)^{q-\gamma} c_H$.

### 4.1.4 Formulation in the symmetric basis

For completeness, let us relate the phenomenology in the basis (3.1), that we have used so far, to the phenomenology in the more symmetric basis (3.14). In addition to the transformations (3.16), (3.17), one must obtain the transformation rules for the matter fields $\{\phi, \varphi\}$. Denoting the matter fields belonging to the $(y_1, y_2)$ basis with a tilde ($\tilde{}$), we find the relations

$$\phi_i = \frac{\tilde{\phi}_i}{1+y_2/\sqrt{3}}\,, \qquad \varphi_a = \frac{\tilde{\varphi}_a}{(1+y_2/\sqrt{3})^{n_a}}\,, \tag{4.31}$$

and their inverses

$$\tilde{\phi}_i = \frac{2\phi_i}{1+2T}\,, \qquad \tilde{\varphi}_a = \frac{\varphi_a}{(T+1/2)^{n_a}}\,. \tag{4.32}$$

The Kähler potential (2.4) is then equivalent to

$$K = -3\ln\left[1-\frac{1}{3}\left(|y_1|^2+|y_2|^2+\sum_i |\tilde{\phi}_i|^2\right)\right] + \sum_a \frac{|\tilde{\varphi}_a|^2}{(1+|y_2|^2/3)^{n_a}}\,, \tag{4.33}$$

and the superpotential (4.1) is mapped into

$$\begin{aligned}\widetilde{W} = {} & \widetilde{W}_{\rm inf}(y_1,y_2) + \left(1+y_2/\sqrt{3}\right)^{1-\beta} W_2(\tilde{\phi}_i) + \left(1+y_2/\sqrt{3}\right)^{-\alpha} W_3(\tilde{\phi}_i) \\ & + \left(1+y_2/\sqrt{3}\right)^{3-2n_a-\sigma} W_2(\tilde{\varphi}_a) + \left(1+y_2/\sqrt{3}\right)^{3-3n_a-\rho} W_3(\tilde{\varphi}_a) + \mu\left(1+y_2/\sqrt{3}\right)^3\,,\end{aligned} \tag{4.34}$$

which leads to the same form of the soft supersymmetry breaking parameters given in (4.8), as expected. Analogous results hold for the generalizations of the parameter $\mu$ considered above, including the addition of a Polonyi sector, always recalling that upon changing basis one must substitute $\mu \to \mu(1+y_2/\sqrt{3})^3$.



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### 4.2 Scenarios in which the volume modulus $T$ is the inflaton

It is also possible to identify the volume modulus $T$ with the inflaton. As we discussed before, a superpotential such as (3.12), which couples $T$ with a matter field $\phi$ (identified for simplicity with $\phi_1$) leads to a Starobinsky-like inflationary potential. While the simple form for supersymmetry breaking by a constant in $W$ does not work in this case, we will see that the Polonyi mechanism and its generalizations will allow for successful phenomenological models. In the next subsubsection, we consider $\phi_1$ to be an untwisted field, and subsequently we will consider it to be a twisted field (labeled accordingly as $\varphi_1$).

#### 4.2.1 Inflation via coupling to untwisted matter fields

For definiteness, we assume that the scalar fields $\{\phi, \varphi\}$ have vanishing vevs, and we can consider the same superpotential (4.1) used in the previous subsection. However, the conditions for a supersymmetry breaking minimum with vanishing cosmological constant (4.2) are not satisfied by the example (3.12) for $T$ field inflation. In fact, none of the multiple examples discussed in [19] that yield inflationary potentials for $T$ satisfy these constraints.

For example, when the constant term to the superpotential (4.1) is used as the source of supersymmetry breaking with the inflationary superpotential given by (3.12), the minimum of the scalar potential is found at

$$T = \frac{1}{2} - \frac{\mu^2}{m^2}\,, \quad \phi_1 = \sqrt{3}\frac{\mu}{m}\,, \tag{4.35}$$

with cosmological constant $V_0 = -3\langle e^G\rangle = -3m^2\mu^2/(m^2 - 3\mu^2) < 0$.

This ADS vacuum must be lifted and we first attempt to use the a stabilized Polonyi sector as the source of supersymmetry breaking. With the Kähler potential (4.17) and superpotential (4.16). The supersymmetry breaking minimum is found at

$$T \simeq \frac{1}{2} + \frac{2}{3}\left(\frac{\mu}{m}\right)^2\,, \quad \phi_1 \simeq \frac{\mu}{m}\,, \quad z \simeq \frac{\Lambda_z^2}{\sqrt{12}}\,, \quad \nu \simeq \frac{1}{\sqrt{3}}\left(1 - \left(\frac{\mu}{m}\right)^2\right)\,, \tag{4.36}$$

for $\Lambda_z, \mu/m \ll 1$. In this case, the form of the inflationary potential is unmodified from the Starobinsky form, save for the horizontal shift of the position of the minimum given by $t_0 = -\sqrt{2/3}(\mu/m)^2$, where

$$T = \frac{1}{2}\left(e^{-\sqrt{\frac{2}{3}}t} + i\sqrt{\frac{2}{3}}\sigma\right)\,, \tag{4.37}$$

and $t$ denotes the canonically-normalized real part of $T$, which we associate with the inflaton. The supersymmetry breaking scale given by the gravitino mass is given by $m_{3/2} = \mu/\sqrt{3}$. The Goldstino in this case is identified with the fermionic partner of the Polonyi field, $\chi_z$, plus a small admixture of the fermion component of the $\phi_1$ superfield, $\chi_1$,

$$\eta \simeq \sqrt{3}\left(1 - \left(\frac{\mu}{m}\right)^2\right)\chi_z + 3\frac{\mu}{m}\chi_1\,. \tag{4.38}$$

When used with the superpotential (4.1) including matter we obtain the following universal soft parameters

$$m_0 = m_{3/2} \qquad B_0 = -m_{3/2} \qquad A_0 = 0\,, \tag{4.39}$$

which are of the mSUGRA type when the gaugino masses are of order $m_{3/2}$ and of the PGM type if gaugino masses are generated through anomalies. Unlike the case where $\phi_1$



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played the role of the inflaton (4.23), we find no dependence for the soft parameters on the modular weights in (4.1). This is because, in general, the weight-dependent parts of the induced soft parameters are generated by the presence of the term $\langle (K^{-1})^T_T D^T W \rangle W^T$ in the effective scalar potential for the matter fields. In the present case of $T$ inflation, $\langle D^T W \rangle = \langle K^T W + W^T \rangle \propto \langle G^T \rangle = 0$, and no contribution is generated. However, different phenomenological boundary conditions could arise in the presence of $z$-dependent weights for which $\langle G^z \rangle \neq 0$.

Supersymmetry can be broken by an untwisted Polonyi field that does not require stabilization in the Kähler potential if we choose

$$W_{\not{\text{susy}}} = \mu \left( \nu + \frac{z}{\sqrt{3}} \right)^3 . \tag{4.40}$$

For $\mu \ll m$, a solution to the system of equations $V = V_T = V_{\phi_1} = V_z = 0$ that preserves the Starobinsky potential along the real $T$ direction, except for a small shift in the position of the minimum to $t_0 = -\sqrt{6}(\mu/m)^2$, can be approximately found to second order in $\mu/m$, and is given by[8]

$$T \simeq \frac{1}{2} + \left( \frac{\mu}{m} \right)^2 , \quad \phi_1 \simeq \sqrt{3} \frac{\mu}{m} , \quad z \simeq -\sqrt{3} \left( \frac{\mu}{m} \right)^2 , \quad \nu \simeq 1 . \tag{4.41}$$

Supersymmetry is broken by the non-vanishing vev of the superpotential (4.40), with the gravitino mass given by $m_{3/2} = \mu$. It is straightforward to check that $G^I \neq 0$ for $I = T, \phi_{1,2}$ if $\mu \neq 0$. The Goldstino consists of $\chi_z$, with a small admixture of the modulino $\chi_T$, and $\chi_1$,

$$\eta \simeq \sqrt{3} \left( 1 - 3 \left( \frac{\mu}{m} \right)^2 \right) \chi_2 + 2\sqrt{3} \frac{\mu}{m} \chi_1 + 3 \left( \frac{\mu}{m} \right)^2 \chi_T . \tag{4.42}$$

The induced soft supersymmetry-breaking terms using (4.1) are given by

$$\phi_i : \quad m_0 = 0 , \qquad B_0 = -m_{3/2} , \qquad A_0 = 0 , \tag{4.43}$$

$$\varphi_a : \quad m_0 = m_{3/2} , \qquad B_0 = -m_{3/2} , \qquad A_0 = 0 . \tag{4.44}$$

In this case, the soft supersymmetry-breaking terms are universal in both sectors. Since the soft supersymmetry-breaking terms in the twisted sector are independent of the modular weights $n_a$, the latter are unconstrained in this case. In the untwisted sector we have a special case of a mSUGRA-like spectra with $m_0 = A_0 = 0$, which would impose universality above the GUT scale [113–116]. In the twisted sector, we recover mSUGRA- or PGM-like models with $m_0 = m_{3/2}$.

### 4.2.2 Inflation via coupling to twisted matter fields

The Starobinsky inflationary potential for the volume modulus $T$ can also be obtained by coupling $T$ with a matter field $\varphi$ with modular weight 3, belonging to the twisted matter sector. As we discussed before, a suitable superpotential has the form (3.23). As before, we consider (4.1) as the form of the couplings to matter. The conditions for vanishing gradients and cosmological constant for the scalar potential at this point are completely analogous to the constraints (4.2) after replacing $\phi_1 \to \varphi_1$ in $W_{\text{inf}}$. Once again, these conditions

[8] We have verified that for $\mu \ll m$, a minimum with $T \ll 1$, at which the supergravity approximation cannot be trusted, does not exist when we require a vanishing cosmological constant with a Starobinsky potential for $T$.



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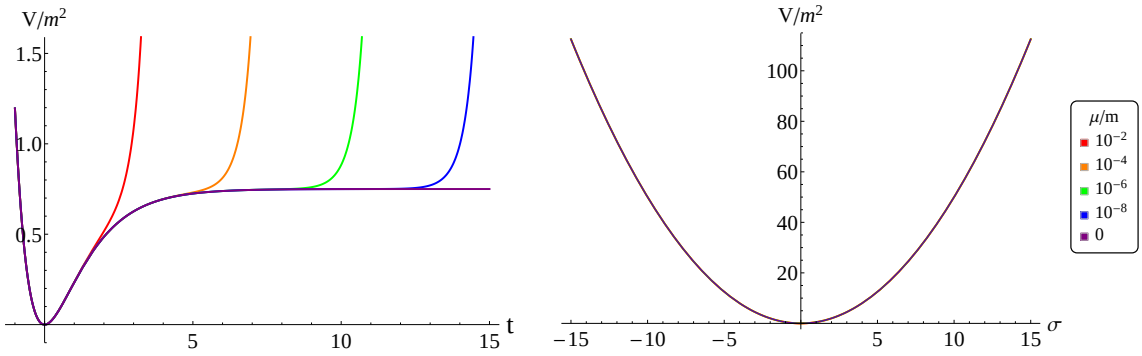


**Figure 3**. Projections of the effective inflationary potential for the model (3.23) with a Polonyi sector (4.16), for different values of the ratio $\mu/m$. The fields $\varphi_1$, $z$ are assumed to have their minimum values, computed numerically. Left: the potential along the canonically normalized real direction, $t = -\sqrt{\frac{3}{2}}\log(2\,\mathrm{Re}T)$. Right: the potential along the canonically normalized imaginary direction, $\sigma = \sqrt{6}\,\mathrm{Im}T$.

are not compatible with $T$ field inflation using (3.12) or its avatars. Our example using a constant term in (4.1) displaces the minimum of the potential to the approximate location given by (4.35) (with the replacement $\phi_1 \to \varphi_1$). It again corresponds to an AdS minimum, $V_0 \simeq -3\mu^2$. We note that the solution in this case is only approximate due to the presence of the factor $e^{|\varphi_1|^2/(T+\bar{T})^3}$ in the scalar potential.

Spontaneous supersymmetry breaking with a strongly stabilized Polonyi sector allows for a vanishing cosmological constant at the minimum given by

$$T \simeq \frac{1}{2} + \frac{2}{3}\left(\frac{\mu}{m}\right)^2\,, \quad \varphi_1 \simeq \frac{\mu}{m}\,, \quad z \simeq \frac{\Lambda_z^2}{\sqrt{12}}\,, \quad \nu \simeq \frac{1}{\sqrt{3}}\left(1 + \frac{1}{3}\left(\frac{\mu}{m}\right)^2\right)\,, \tag{4.45}$$

for $\Lambda_z, \mu/m \ll 1$. Unlike the $(T,\phi)$ scenario, this deformation is not limited to a shift in the position of the minimum; the behaviour of the potential at large values of the inflaton becomes dependent on the magnitude of $\mu$. In particular, along the real direction the potential receives the correction

$$\Delta V = \mu^2\left(e^{\sqrt{\frac{2}{3}}t} - 4e^{2\sqrt{\frac{2}{3}}t} + 3e^{\sqrt{6}t}\right)\,, \tag{4.46}$$

(see figure 3), and the gravitino mass is $m_{3/2} = \mu/\sqrt{3}$. The Goldstino is a mixture of the fermion components of the $T$, $\varphi_1$ and $z$ superfields,

$$\eta \simeq \sqrt{3}\left(1 - \frac{7}{3}\left(\frac{\mu}{m}\right)^2\right)\chi_z + 3\frac{\mu}{m}\tilde{\chi}_1 - 6\left(\frac{\mu}{m}\right)^2\chi_T. \tag{4.47}$$

In this case the couplings to matter generate universal soft supersymmetry breaking terms of the mSUGRA type, given by (4.39).

Finally, we can also consider an untwisted Polonyi sector field with the cubic superpotential (4.40). In complete analogy to the scenario contemplated in the previous section, the non-vanishing vev of this superpotential shifts the position of the minimum of the potential. For $\mu \ll m$, this minimum is located at

$$T \simeq \frac{1}{2} + \left(\frac{\mu}{m}\right)^2\,, \quad \varphi_1 \simeq \sqrt{3}\frac{\mu}{m}\,, \quad z \simeq \frac{\sqrt{3}}{2}\left(\frac{\mu}{m}\right)^2\,, \quad \nu = 1\,. \tag{4.48}$$



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The inflaton potential is again deformed by the addition of (4.40). Upon the addition of the Polonyi sector, the inflaton potential becomes dependent on $\mu$. To leading order in $\mu$, the potential correction along the real direction has the form

$$\Delta V \simeq 3\mu^2 \left( e^{\sqrt{\frac{2}{3}}t} - 3e^{2\sqrt{\frac{2}{3}}t} + 2e^{\sqrt{6}t} \right) . \tag{4.49}$$

Although different from the correction in (4.46), the form of the potential looks very similar to that shown in figure 3. As one can see, only for for very small $\mu/m$ can the potenital yield Starobinsky-like inflation at large field values.

In this case the gravitino mass given by $m_{3/2} = \mu$, and the Goldstino is

$$\eta \simeq \sqrt{3} \left( 1 - 3 \left( \frac{\mu}{m} \right)^2 \right) \chi_2 + 2\sqrt{3} \frac{\mu}{m} \tilde{\chi}_1 - \frac{33}{2} \left( \frac{\mu}{m} \right)^2 \chi_T . \tag{4.50}$$

The induced soft parameters can be readily evaluated, and correspond to the CMSSM and mSUGRA forms (4.43), (4.44) in the untwisted and twisted sectors, respectively.

## 5 Inflaton decays

Any complete model of cosmological inflation should include mechanisms for inflaton decay that yield successful reheating at the end of the inflationary epoch. In this section we consider inflaton decay in the model scenarios discussed in the previous section, emphasising differences in their corresponding predictions for the reheating temperature. These have important phenomenological impacts, e.g., the inferred number of e-folds during inflation, the resultant gravitino abundance and hence the possible scale of supersymmetry breaking, which may be used to discriminate between models.

### 5.1 Decay of the untwisted matter inflaton

We first calculate inflaton decays in the scenario where the untwisted matter field $\phi_1$ plays the role of the inflaton, assuming that all matter fields $\{\phi, \varphi\}$ have vanishing vevs at the end of inflation. This implies that

$$\langle W^i \rangle = \langle W^a \rangle = 0 , \quad \langle K^i \rangle = \langle K^a \rangle = 0 , \tag{5.1}$$

or, in terms of the Kähler function $G = K + \log |W|^2$,

$$G^i = G^a = 0. \tag{5.2}$$

The volume modulus $T$ must typically be stabilized in order to inflate successfully along the $\phi_1$ direction. As we have already seen, sufficient stabilization can be achieved by the addition of quartic terms in the Kähler potential as in (4.6). Thus, we assume now that $T$ has a non-vanishing vev, $\langle T \rangle = 1/2$, which implies $\langle G^T \rangle = p - 3$ for the supersymmetry breaking superpotentials (4.11), (4.18), and the simple scenario with breaking by a constant (4.1), for which $p \equiv 0$. In this case, all the matter scalar and fermion fluctuations about the global minimum are canonically normalized, whereas the canonically-normalised modulus fluctuation corresponds to $\delta T = \sqrt{3}(T - 1/2)$. For convenience, we define the ratio of the gravitino mass to the inflaton mass, $\Delta \equiv m_{3/2}/m$.



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For the present analysis we consider a generic superpotential of the form

$$W = W_{\rm inf}(T,\phi_1) + W_{\rm M}(T,\phi_i,\varphi_a;\mu)\,, \tag{5.3}$$

for which we assume that the constraints (4.2) are satisfied. Here $\mu$ denotes the mass parameter that determines the scale of supersymmetry breaking: $\langle W_{\rm M}\rangle = \mu$. A particular example corresponds to the superpotential (4.1) with $W_{\rm inf}(T,\phi_1)$ given by the Wess-Zumino superpotential (3.7). The decay rate of the inflaton is determined by its coupling to the moduli, matter and gauge fields. These couplings can be computed from a series expansion of the supergravity Lagrangian. For readability, in the following discussion we drop the subscript $M$ from the matter superpotential, except when otherwise stated.

### 5.1.1 Decays to matter scalars

The interactions between the inflaton $\phi_1$ and the rest of the matter sector are determined from the scalar kinetic and potential terms in the Lagrangian. The scalar kinetic term is given by (3.4). After substitution of the matter field and modulus vevs, the scalar kinetic term yields no interaction terms relevant for the kinematically-allowed decays up to four-body interactions. We therefore look at interactions stemming from the potential term in the Lagrangian. Recall that the gauge-independent part of the scalar potential is given in (3.5) and can be expanded to find the decay couplings. It is straightforward to calculate the scalar mass matrix, which takes the form

$$\bar\Phi^I(\mathcal{M}^2)^J_I\Phi_J = \begin{pmatrix}\bar\phi^1 & \bar\Phi^I\end{pmatrix}\begin{pmatrix} m^2 + m(W^{11}+\bar W_{11}) + W^{1K}\bar W_{K1} & mW^{1J} + W^{JK}\bar W_{K1} \\ m\bar W_{1I} + W^{1K}\bar W_{KI} & W^{JK}\bar W_{KI}\end{pmatrix}\begin{pmatrix}\phi_1\\ \Phi_J\end{pmatrix}, \tag{5.4}$$

where we denote $\Phi \equiv \{\delta T,\phi_i,\varphi_a\}$ and introduce the multiindex $I = \{\delta T, i, a\}$. Here we have segregated the inflaton explicitly from the rest of the matter and moduli fields, and we have associated the inflaton mass $m$ with the vev of $W^{11}_{\rm inf}$, as is true for the Wess-Zumino superpotential (3.7). It is immediately evident that, in the absence of a direct coupling between the inflaton and other fields in the matter superpotential, the field $\phi_1$ is the inflaton mass eigenstate.[9]

A direct coupling between $\phi_1$ and the rest of the matter sector may be allowed. For example, this field can be associated with a heavy singlet sneutrino [22, 117–123]. In such case, one can consider the addition of a Yukawa-like term

$$\Delta W = y_\nu H_u L \phi_1 \tag{5.5}$$

to the Standard Model superpotential, where $y_\nu$ denotes the Yukawa coupling. Such a coupling leads to a mass matrix characteristic of seesaw models,

$$\begin{pmatrix}\bar\phi^1 & \bar{\tilde\nu}\end{pmatrix}\begin{pmatrix} m^2+\tilde m^2 & -m\tilde m \\ -m\tilde m & \tilde m^2 + \kappa\mu^2\end{pmatrix}\begin{pmatrix}\phi_1\\ \tilde\nu\end{pmatrix}, \tag{5.6}$$

where $\tilde m \equiv y_\nu\langle H_u\rangle = y_\nu v\sin\beta$, and $\kappa = (1-n_\nu)$ for a twisted neutrino, $\kappa = 0$ for an untwisted neutrino. Therefore, even in the presence of direct couplings, we can consider $\phi_1$ to be the inflaton mass eigenstate, up to corrections of order $\mu/m, v/m \ll 1$.

[9] We have ignored subdominant $\mathcal{O}(\mu)$ contributions in the expression (5.4), which actually vanish for a $\phi_1$-independent matter superpotential.



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In order to determine the decay rate of the inflaton $\phi_1$, we must consider couplings beyond quadratic interactions. Expansion of the scalar potential yields

$$\begin{aligned}\mathcal{L}_{B,\text{pot}} = &\frac{2}{\sqrt{3}} m \bar{W}_{1J} \phi_1 \delta T \bar{\Phi}^J - \frac{1}{\sqrt{3}} B^1_J \phi_1 \delta T \bar{\Phi}^J - \frac{1}{3\sqrt{3}} W^{1TT}_{\text{inf}} \bar{W}_{TJ} \phi_1 \delta T \bar{\Phi}^J \\ &- \frac{c_{I\delta T}}{3} W^{1I} \bar{W}_{JT} \phi_1 \Phi_I \bar{\Phi}^J - W^{1IK} \bar{W}_{KJ} \phi_1 \Phi_I \bar{\Phi}^J - \frac{1}{6} m W^{1TT}_{\text{inf}} \phi_1 \delta \bar{T} \delta \bar{T} \\ &+ \frac{2}{\sqrt{3}} m \bar{W}_{1J} \phi_1 \delta \bar{T} \bar{\Phi}^J - \frac{1}{\sqrt{3}} B^1_J \phi_1 \delta \bar{T} \bar{\Phi}^J - \frac{1}{2} m \bar{W}_{1IJ} \phi_1 \bar{\Phi}^I \bar{\Phi}^J \\ &- \frac{1}{2} W^{1K} \bar{W}_{KIJ} \phi_1 \bar{\Phi}^I \bar{\Phi}^J - \frac{c_{IJ}}{6} W^{1T} \bar{W}_{IJ} \phi_1 \bar{\Phi}^I \bar{\Phi}^J + \text{h.c.} + \mathcal{O}(\mu) + \cdots\end{aligned} \tag{5.7}$$

where we have introduced the notation

$$B^{I_1 I_2 \ldots}_{J_1 J_2 \ldots} = \left[ (n_a - 3) W^{I_1 I_2 \ldots a} \bar{W}_{a J_1 J_2 \ldots} - 2 W^{I_1 I_2 \ldots k} \bar{W}_{k J_1 J_2 \ldots} \right] . \tag{5.8}$$

and

$$c_{IJ} = \begin{pmatrix} -1 & -3 & n_J - 2 \\ -3 & -5 & n_J - 4 \\ n_I - 2 & n_I - 4 & n_I + n_J - 3 \end{pmatrix} , \tag{5.9}$$

where the rows and columns correspond to submatrices following the notation $I = \{\delta T, i, a\}$. The expression (5.7) shows that all couplings to matter vanish in the absence of an explicit $\phi_1$ dependence in the matter superpotential, $W^{1 I_1 I_2 \cdots} = 0$. It can be verified that the same is true for all the $\mathcal{O}(\mu)$ terms that we have neglected in (5.7), as well for any couplings leading to three- and four-body decay of the inflaton. The only non-vanishing interaction in this limit correspond to those proportional to $W^{1TT}_{\text{inf}}$. This coupling vanishes identically for the Wess-Zumino superpotential (3.7). However, it is known that the superpotential (3.7) is not the unique superpotential that leads to Starobinsky inflation [19]. Consider, e.g., the addition of the term

$$\Delta W_{\text{inf}} = \zeta (T - 1/2)^2 \phi_1 , \tag{5.10}$$

which does not alter the shape of the potential for the inflaton Re $\phi_1$ for any value of $\zeta$. In the presence of this term, the mass matrix has the structure

$$m^2 |\phi_1|^2 + m_T^2 |\delta T|^2 + \frac{2\zeta}{3\sqrt{3}} (p - 3) m_{3/2} M_P (\phi_1 \delta T + \text{h.c.}) , \tag{5.11}$$

and the inflaton mass eigenstate corresponds to

$$\phi_1^M \simeq \phi_1 + (p - 3) \frac{2\zeta \Delta M_P}{3\sqrt{3} m} \delta \bar{T} . \tag{5.12}$$

In this case, the decay of the inflaton $\phi_1$ into the fluctuation of the modulus $T$ is possible, with rate

$$\Gamma(\phi_1 \to \delta T \, \delta T) = m \frac{|\zeta|^2}{72\pi} , \tag{5.13}$$

assuming that the modulus mass satisfies the hierarchy $m \gg m_T \gg m_{3/2}$ as in (4.7). As we see in the next subsubsection, this is the same rate as the decay into gravitinos. If these were the dominant decay rates, the Universe would become dominated by moduli and gravitinos, forcing their masses to exceed 10 TeV in order to obtain a reheating temperature above



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1 MeV, and hence suitable for nucleosynthesis. However, in this case, decays into neutralinos are liable to yield a relic neutralino density that is far too large. Thus we can not afford decays to moduli (and gravitinos) to be the dominant decay product.

Decay of the inflaton into matter becomes possible only if we allow a non-trivial dependence on $\phi_1$ for $W_M$. In particular, the superpotential (5.5) leads to a non-vanishing amplitude for which the dominant contribution corresponds to the seventh term in (5.7) if $W^{1IJ} \neq 0$, namely $-\frac{1}{2}m\bar{W}_{1IJ}\phi_1\bar{\Phi}^I\bar{\Phi}^J$. In the particular case of sneutrino inflation, this coupling would be $-my_\nu\bar{H}_u\bar{\tilde{L}}\phi_1$, and the decay width would be given by

$$\Gamma(\phi_1 \to H_u^0\tilde{\nu}, H_u^+\tilde{f}_L) = m\frac{|y_\nu|^2}{16\pi}\,, \tag{5.14}$$

where we have neglected the masses of the final-state particles. This decay rate would be fast if $|y_\nu| = \mathcal{O}(1)$ and, in order to avoid problems associated with gravitino production during reheating, we must set a bound on the Yukawa coupling associated with the inflaton [22]

$$y_\nu \lesssim 10^{-5} \tag{5.15}$$

with a corresponding constraint on the reheating temperature that we discuss below.

### 5.1.2 Decays to matter fermions

The decay of the inflaton $\phi_1$ to matter fermions is mediated by the interactions determined by the fermion kinetic term, the fermion mass matrix and the fermion-scalar interactions of the supergravity Lagrangian. The fermion kinetic term is given by

$$\mathcal{L}_{F,\text{kin}} = \frac{i}{2}G^I_J\bar{\chi}_{IL}\gamma^\mu D_\mu\chi^J_L + \text{h.c.}\,, \tag{5.16}$$

and yields no couplings relevant to two-, three- and four-body decays. One must then look for interactions stemming from the fermion mass matrix and the fermion-scalar interactions. Working in the unitary gauge, one finds no dependence on the modulino $\chi_T$, which becomes the longitudinal component of the gravitino,

$$\begin{aligned}\mathcal{L}_{F,\text{int}} = {} & \frac{i}{2}\bar{\chi}_{IL}\not{D}\Phi_J\chi^K_L(-G^{IJ}_K + \frac{1}{2}G^I_KG^J) \\ & + \frac{1}{2}e^{G/2}(-G^{IJ} - G^IG^J + G^{IJ}_K(G^{-1})^K_AG^A)\bar{\chi}_{IL}\chi_{JR} + \text{h.c.} \\ & + \text{four-fermion terms} \end{aligned} \tag{5.17}$$

$$\begin{aligned} = {} & -\frac{1}{2}W^{1IJ}\phi_1\bar{\chi}_{IL}\chi_{JR} + \frac{i}{4\mu}W^{1J}\Phi_J\bar{\chi}_{KL}\not{\partial}\phi_1\chi^K_L + \frac{i}{4\mu}W^{1J}\phi_1\bar{\chi}_{KL}\not{\partial}\Phi_J\chi^K_L \\ & + \frac{1}{4\mu}W^{1J}W^{IK}\phi_1\Phi_J\bar{\chi}_{IL}\chi_{KR} - \frac{1}{2}W^{1IJK}\phi_1\Phi_J\bar{\chi}_{IL}\chi_{KR} \\ & + \frac{\sqrt{3}}{2}W^{1JK}\phi_1(\text{Re}\,\delta T)\bar{\chi}_{JL}\chi_{KR} - \frac{1}{2}W^{1K}\phi_1\bar{\Phi}^J(\bar{\chi}_{KL}\chi_{JR} + \bar{\chi}_{JL}\chi_{KR}) + \cdots \end{aligned} \tag{5.18}$$

Similarly to the scalar case, all couplings to matter fermions vanish for a $\phi_1$-independent matter superpotential. The decay into a fermion and a higgsino is possible if we identify $\phi_1$ with a singlet neutrino, with superpotential (5.5). In this case, the rate is given by

$$\Gamma(\phi_1 \to \tilde{H}_u^0\nu,\, \tilde{H}_u^+ f_L) = m\frac{|y_\nu|^2}{16\pi}\,, \tag{5.19}$$

i.e., equal to the rate of decay into scalars.



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### 5.1.3 Decay to the gravitino and inflatino

We now explore the possibility of the decay of the inflaton $\phi_1$ to the gravitino. In the unitary gauge, this process is in general mediated by the interaction terms

$$\mathcal{L}_{3/2} = \frac{1}{8}\epsilon^{\mu\nu\rho\sigma}\bar{\psi}_\mu\gamma_\nu\psi_\rho G^I\partial_\sigma\Phi_I + \frac{i}{2}e^{G/2}\bar{\psi}_{\mu L}\sigma^{\mu\nu}\psi_{\nu R} + \text{h.c.}\,. \tag{5.20}$$

Since $\langle G^I\rangle = 0$ for all matter fields, and $\langle G^T\rangle = p-3$, the couplings vanish unless there is mixing between the inflaton $\phi_1$ and the volume modulus $T$. Such mixing is possible in the presence of a term such as (5.10), in which case the mass eigenstate is $\phi_1^M$, given by (5.12). In this case, the interaction is mediated by the Lagrangian

$$\mathcal{L}_{3/2} \simeq -\frac{\zeta m_{3/2}}{2m^2}\left[\frac{1}{2}\,\epsilon^{\mu\nu\rho\sigma}\bar{\psi}_\mu\gamma_\nu\psi_\rho\partial_\sigma\phi_1^M - im_{3/2}\phi_1^M\,\bar{\psi}_\mu\sigma^{\mu\nu}\psi_\nu\right]. \tag{5.21}$$

This results in the decay rate

$$\Gamma(\phi_1\to\psi_{3/2}\psi_{3/2}) \simeq m\frac{|\zeta|^2}{72\pi}. \tag{5.22}$$

The same result is found for the decay of $\phi_1$ to the canonically-normalized modulino $\chi_T$, the relevant coupling in this case being given by $\mathcal{L}\supset -\frac{1}{6}W_{\text{inf}}^{1TT}\phi_1\bar{\chi}_{\delta TL}\chi_{\delta TR}$.

The decays to a single gravitino and a matter fermion are mediated by the interaction terms

$$\mathcal{L}_{3/2,\chi} = \frac{i}{\sqrt{2}}e^{G/2}G^I\bar{\psi}_{\mu L}\gamma^\mu\chi_{IL} + \frac{1}{\sqrt{2}}G^I_J\bar{\psi}_{\mu L}\not{D}\bar{\Phi}^I\gamma^\mu\chi_{JR} + \text{h.c.} \tag{5.23}$$

$$= \frac{i}{\sqrt{2}}W^{1J}\phi_1\bar{\psi}_{\mu L}\gamma^\mu\chi_{jL} + \frac{i}{\sqrt{2}}m\phi_1\bar{\psi}_{\mu L}\gamma^\mu\chi_{1L} + \frac{1}{\sqrt{2}}\bar{\chi}_{1R}\gamma^\mu\not{\partial}\phi_1\psi_{\mu L} + \cdots. \tag{5.24}$$

The decay amplitude to a matter fermion different from the inflatino is zero, unless there is an explicit dependence on $\phi_1$ in the matter superpotential. Identifying the inflaton with a singlet neutrino, with a coupling given by (5.5), the decay to a left-handed neutrino and a single gravitino is allowed, but with a negligible width relative to the decays to the Higgs, fermions and their supersymmetric partners:

$$\Gamma(\phi_1\to\psi_{3/2}\,\nu) = v^2\sin^2\beta m\frac{|y_\nu|^2}{32\pi M_P^2} \sim 10^{-32}\,\Gamma(\phi_1\to\tilde{H}_u^0\nu,\,\tilde{H}_u^+ f_L)\,. \tag{5.25}$$

Equation (5.24) includes the interaction between the gravitino and the inflatino. The availability of this decay channel is strongly dependent on the mechanism of supersymmetry breaking. In the simplest scenario (4.1), the decay is not kinematically allowed, since there is no mass splitting at tree level for the untwisted matter field $\phi_1$. In the case when a splitting exists, such as (4.23), the decay will be suppressed [130, 131] due to the degeneracy $m - m_\chi \sim m_{3/2}$:

$$\Gamma(\phi_1\to\psi_{3/2}\,\chi_1) \sim \left(\frac{m_{3/2}}{m}\right)^2\frac{17m^3}{48\pi M_P^2}\,. \tag{5.26}$$

It can also be shown that all two-body decays involving one inflatino and one matter fermion $\chi_J$ are dependent on the coupling $W^{11J}$, which vanishes in the limit of no $\phi_1$ dependence in $W_M$, as well for a superpotential such as (5.5).



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We are led to conclude that, in the absence of a direct coupling between the inflaton and the rest of the matter (and gauge) sectors, there are no efficient decay channels for the inflaton, if it is identified with an untwisted matter field, as found in other studies of no-scale supergravity [87]. On the other hand, if the field $\phi_1$ is associated with a singlet neutrino, the decay rates (5.14) and (5.19) imply a reheating temperature

$$T_R = (5.6 \times 10^{14}\,\mathrm{GeV})|y_\nu| \left(\frac{g}{915/4}\right)^{-1/4} \left(\frac{m}{10^{-5} M_P}\right)^{1/2}, \tag{5.27}$$

assuming that the Yukawa coupling $y_\nu \lesssim \mathcal{O}(1)$ so that the decay of the inflaton occurs after the end of inflation, during the oscillation of the inflaton around the minimum of the potential. Here $g$ denotes the effective number of degrees of freedom, and $g = 915/4$ for the MSSM.

### 5.1.4 Decays to gauge bosons and gauginos

The decay of the inflaton $\phi_1$ into gauge fields and gauginos is possible in the presence of a non-trivial coupling between $\phi_1$ and the gauge degrees of freedom, as would be provided by a $\phi_1$-dependent gauge kinetic function $f_{\alpha\beta} = f(\phi_1)\delta_{\alpha\beta}$ [87, 132]. If supersymmetry is not broken by the inflaton, this term will not contribute to gaugino masses. These require a non-trivial dependence in the gauge kinetic function of fields involved in supersymmetry breaking. The relevant supergravity Lagrangian terms correspond to

$$\begin{aligned} \mathcal{L}_G = &-\frac{1}{4}(\mathrm{Re}\, f_{\alpha\beta}) F_{\alpha\,\mu\nu} F_\beta^{\mu\nu} + \frac{i}{4}(\mathrm{Im}\, f_{\alpha\beta}) F_{\alpha\,\mu\nu} \tilde{F}_\beta^{\mu\nu} \\ &+ \left(\frac{1}{4} e^{G/2} (\bar{f}_{\alpha\beta})_{,J} (G^{-1})^J_K G^K \bar{\lambda}_{\alpha L} \lambda_{\beta R} + \mathrm{h.c.}\right), \end{aligned} \tag{5.28}$$

where $\tilde{F}_\alpha^{\mu\nu} = \frac{1}{2}\epsilon^{\mu\nu\rho\sigma} F_{\alpha\,\rho\sigma}$. Neglecting contributions suppressed by the gaugino masses, the decay widths to canonically-normalized gauge boson pairs and gauginos can be evaluated in a straightforward way, resulting in [87]

$$\Gamma(\phi_1 \to gg) = \Gamma(\phi_1 \to \tilde{g}\tilde{g}) = \frac{3 d_{g,1}^2}{32\pi} \left(\frac{N_G}{12}\right) \frac{m^3}{M_P^2}, \tag{5.29}$$

where $N_G$ is the number of final states: $N_G = 12$ for the standard model, and $d_{g,1}$ is given by

$$d_{g,1} \equiv \langle \mathrm{Re}\, f \rangle^{-1} \left| \left\langle \frac{\partial f}{\partial \phi_1} \right\rangle \right|. \tag{5.30}$$

The equality of the rates to gauge bosons and gauginos requires that $W_{\phi_1\phi_1}$ is related to the inflaton mass rather than the supersymmetry-breaking scale. In the presence of a coupling such as (5.5), these rates are subdominant, being suppressed by $(m/M_P)^2$ relative to the widths into Higgs, leptons and their supersymmetric partners, cf, (5.14) and (5.19). On the other hand, if no such couplings are present, the decays to gauge bosons and gauginos are the dominant channels, and would yield a reheating temperature

$$T_R = (2 \times 10^{10}\ \mathrm{GeV})\, d_{g,1}\, g^{-1/4} \left(\frac{N_G}{12}\right)^{1/2} \left(\frac{m}{10^{-5} M_P}\right)^{3/2}. \tag{5.31}$$

In this case, the constraint on the thermal production of gravitinos is easily satisfied if $d_{g,1} \lesssim 10^{-1}$.



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The decay of $\phi_1$ to gauge bosons and gauginos can also be achieved through a coupling between $T$ and the gauge degrees of freedom. Indeed, a $T$-dependent gauge kinetic function $f_{\alpha\beta} = f(T)\delta_{\alpha\beta}$ is a generic feature of heterotic string effective field theories [16, 133–136]. A superpotential such as (5.10) produces a mixing between $\phi_1$ and $T$, allowing in this case decays of the $\phi_1$ mass eigenstate to gauge bosons, with a rate

$$\Gamma(\phi_1 \to gg) = (p-3)^2 \frac{d_{g,T}^2 |\zeta|^2}{216\pi} \left(\frac{N_G}{12}\right) \Delta^2 m \,, \tag{5.32}$$

where we define

$$d_{g,T} \equiv \langle \mathrm{Re}\, f \rangle^{-1} \left| \left\langle \frac{\partial f}{\partial T} \right\rangle \right| . \tag{5.33}$$

We see, however, that this rate is suppressed by a factor $(m_{3/2}/m)^2$ relative to the decay widths (5.13) and (5.22), and it can also be shown that the rate for decays to gauginos is further suppressed by an additional $(m_{3/2}/m)^2$ factor. Gaugino masses are generated in this case and are given by

$$m_{1/2} = \left| \frac{1}{2} e^{G/2} \frac{\bar{f}_{\alpha\beta,T}}{\mathrm{Re}\, f_{\alpha\beta}} (G^{-1})^T_T G^T \right| = \frac{d_{g,T}}{6} |p-3| m_{3/2} \tag{5.34}$$

There is an additional contribution if $f_{\alpha\beta}$ also depends also on the Polonyi field $z$.

### 5.2 Decays of a volume modulus inflaton

We will now consider the case where the inflaton is identified with the volume modulus $T$. We assume as before that all matter fields $\{\phi, \varphi\}$ have vanishing vevs at the end of inflation, which is equivalent to the conditions (5.1). For all scenarios explored in section 4.2, the volume modulus inflaton $T$ has a non-vanishing vev at the minimum of the potential, which is located at

$$\langle \mathrm{Re}\, T \rangle = \frac{1}{2} + \mathcal{O}(\mu^2/m^2) \,, \quad \langle \mathrm{Im}\, T \rangle = 0 \,, \tag{5.35}$$

where $\mu$ is the mass parameter that determines the scale of supersymmetry breaking: $\mu = \sqrt{3} m_{3/2}$ for an untwisted Polonyi modulus $z$ with superpotential (4.16), $\mu = m_{3/2}$ for breaking by an untwisted sector field with superpotential (4.40). At this minimum we have $\langle W^T \rangle / \langle W \rangle = 3 + \mathcal{O}(\mu^2/m^2)$, and $\langle K^T \rangle = -3 + \mathcal{O}(\mu^2/m^2)$. The decays of the inflaton are determined by its couplings to the moduli, matter and gauge fields, which can be computed from a series expansion of the supergravity Lagrangian. In this subsection, we denote $\Phi \equiv \{\phi, \varphi\}$ and use the multiindex $I = \{i, a\}$.

#### 5.2.1 Decays to matter scalars

The couplings of the inflaton $T$ to matter stem from the scalar kinetic term of the Lagrangian and the scalar potential. We first assume that no direct coupling between $T$ and the matter fields exists, except for the superpotential coupling to $\phi_1$ or $\varphi_1$ necessary to obtain the desired inflationary potential. The scalar kinetic term (3.4) may then be expanded to first order in $\delta T$, to yield

$$\mathcal{L}_{B,\mathrm{kin}} = \frac{1}{\sqrt{3}} \delta T \phi_i \partial_\mu \partial^\mu \bar{\phi}^i + \frac{n_a}{\sqrt{3}} \delta T \varphi_a \partial_\mu \partial^\mu \bar{\varphi}^a + \mathrm{h.c.} + \mathcal{O}\left(\Delta^2\right) + \cdots \tag{5.36}$$



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The gauge-independent part of the scalar potential (3.5) can also be expanded to reveal the interaction terms:

$$\begin{aligned}\mathcal{L}_{B,\text{pot}} = &-\frac{B^I_J}{\sqrt{3}}\delta T\Phi_I\bar{\Phi}^J - \frac{B^{IJ}_K}{2\sqrt{3}}\delta T\Phi_I\Phi_J\bar{\Phi}^K - \frac{B^I_{JK}}{2\sqrt{3}}\delta T\Phi_I\bar{\Phi}^J\bar{\Phi}^K - \frac{B^{IJK}_L}{6\sqrt{3}}\delta T\Phi_I\Phi_J\Phi_K\bar{\Phi}^L \\ &- \frac{B^I_{JKL}}{6\sqrt{3}}\delta T\Phi_I\bar{\Phi}^J\bar{\Phi}^K\bar{\Phi}^L - \frac{B^{IJ}_{KL}+C^{IJ}_{KL}}{4\sqrt{3}}\delta T\Phi_I\Phi_J\bar{\Phi}^K\bar{\Phi}^L + \text{h.c.} + \mathcal{O}(\Delta) + \cdots .\end{aligned} \tag{5.37}$$

Here the coefficients $B^{I_1 I_2\cdots}_{J_1 J_2\cdots}$ are as defined in (5.8), and the $C^{IJ}_{KL}$ are sector-dependent functions of the bilinear coupling constants of the superpotential given by

$$\begin{aligned}C^{IJ}_{KL} = &-\big(3+(n_I+n_J-3)(n_K+n_L-3)\big)W^{IJ}\bar{W}_{LK} \\ &+(n_I+n_M-3)\delta^I_L W^{JM}\bar{W}_{MK}.\end{aligned} \tag{5.38}$$

Note that this expression assumes $n_i = 1$ when $I$ represents an untwisted field (see below). We have ignored the couplings to $\phi_1$ (or $\varphi_1$), due to the fact that this field, when coupled to $T$, possesses a mass equal to the inflaton mass $m$, and therefore the decay of $T$ to $\phi_1$ ($\varphi_1$) is kinematically forbidden.

At tree level, the equation of motion for the conjugate matter fields may be substituted in (5.36). To quadratic order, the tree-level contribution from the Kähler potential for untwisted matter fields has the same form as that of twisted matter fields with unit modular weight,

$$K \supset -3\log\left(T+\bar{T}-\sum_i\frac{|\phi_i|^2}{3}\right) = -3\log\left(T+\bar{T}\right)+\sum_i\frac{|\phi_i|^2}{T+\bar{T}}+\cdots \tag{5.39}$$

Therefore, at this level we can define $n_i \equiv 1$, where $i$ runs over all untwisted matter fields. The effective Lagrangian, including the contributions from (5.36) and (5.37), can then be written as

$$\begin{aligned}\mathcal{L}_{B,\text{eff}} = &-\frac{\delta T}{\sqrt{3}}(n_I+n_L-3)W^{IL}\bar{W}_{LJ}\Phi_I\bar{\Phi}^J \\ &-\frac{\delta T}{2\sqrt{3}}(n_I+n_L-3)W^{IL}\bar{W}_{LJK}\Phi_I\bar{\Phi}^J\bar{\Phi}^K \\ &-\frac{\delta T}{2\sqrt{3}}(n_I+n_J+n_L-3)W^{IJL}\bar{W}_{LK}\Phi_I\Phi_J\bar{\Phi}^K \\ &-\frac{\delta T}{\sqrt{3}}(n_J+n_L-3)W^{JL}\bar{W}_{LK}\Phi_I\Phi_J\bar{\Phi}^I\bar{\Phi}^K \\ &-\frac{\delta T}{6\sqrt{3}}(n_I+n_L-3)W^{IL}\bar{W}_{LJKM}\Phi_I\bar{\Phi}^J\bar{\Phi}^K\bar{\Phi}^M \\ &-\frac{\delta T}{4\sqrt{3}}(n_I+n_J+n_L-3)W^{IJL}\bar{W}_{LKM}\Phi_I\Phi_J\bar{\Phi}^K\bar{\Phi}^M \\ &-\frac{\delta T}{6\sqrt{3}}(n_I+n_J+n_K+n_L-3)W^{IJKL}\bar{W}_{LM}\Phi_I\Phi_J\Phi_K\bar{\Phi}^M \\ &-\frac{\delta T}{12\sqrt{3}}(n_I+n_J-3)\big(9+(n_I+n_J-1)(n_K+n_M-3)\big)W^{IJ}\bar{W}_{KM}\Phi_I\Phi_J\bar{\Phi}^K\bar{\Phi}^M \\ &+\cdots\end{aligned} \tag{5.40}$$



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Under the assumption that the masses of all scalar matter fields are hierarchically smaller than the inflaton mass, $m_I \ll m$, the two-body decay rate can be computed immediately:

$$\Gamma(T \to \Phi_I \bar{\Phi}^J) = (n_I + n_L - 3)^2 \frac{|W^{IL} \bar{W}_{LJ}|^2}{48\pi m M_P^2}\,, \tag{5.41}$$

where a sum over the repeated index $L$ is implied. This rate is dependent on the matter sector to which the decay products belong, and is weak-scale suppressed in the case of MSSM scalars. For example, the rate for decay to two Higgs bosons is

$$\Gamma(T \to H_{u,d} \bar{H}^{u,d}) = (2n_H - 3)^2 \frac{|\mu_H|^4}{24\pi m M_P^2}\,, \tag{5.42}$$

where $\mu_H$ denotes the MSSM bilinear Higgs coupling. These two-body rates lead to an extremely low reheating temperature: for an inflaton mass $m \sim 10^{-5} M_P$, and $\mu_H \sim 1\,\mathrm{TeV}$, $T_R \sim 10^{-1}\,\mathrm{eV}$. In the three-body case, the decay to light scalars is given by the widths

$$\Gamma(T \to \Phi_I \bar{\Phi}^J \bar{\Phi}^K) = (n_I + n_L - 3)^2 \frac{|W^{IL} \bar{W}_{LJK}|^2 m}{12(8\pi)^3 M_P^2}\,, \tag{5.43}$$

$$\Gamma(T \to \Phi_I \Phi_J \bar{\Phi}^K) = (n_I + n_J + n_L - 3)^2 \frac{|W^{IJL} \bar{W}_{LK}|^2 m}{12(8\pi)^3 M_P^2}\,. \tag{5.44}$$

In particular, the decay to the neutral $d$-type Higgs and the left and right stops has the rate

$$\Gamma(T \to \bar{H}_d^0 \bar{\tilde{t}}_R \tilde{t}_L,\, H_d^0 \tilde{t}_R \bar{\tilde{t}}_L) = \left((2n_H - 3)^2 + (2n_t + n_H - 3)^2\right) \frac{|\mu_H y_t|^2 m}{4(8\pi)^3 M_P^2}\,, \tag{5.45}$$

where $y_t$ denotes the top Yukawa coupling. The corresponding reheating temperature is also low, in the MeV range. The rates corresponding to four-body decays are the largest, despite the phase-space suppression. The decay width

$$\Gamma(T \to \Phi_I \Phi_J \bar{\Phi}^K \bar{\Phi}^M) = (n_I + n_J + n_L - 3)^2 \frac{|W^{IJL} \bar{W}_{LKM}|^2 m^3}{72(8\pi)^5 M_P^2}\,, \tag{5.46}$$

for which we have disregarded the bilinear couplings, implies the following decay rate to four stops

$$\Gamma(T \to \tilde{t}_R \tilde{t}_L \bar{\tilde{t}}_R \bar{\tilde{t}}_L) = (2n_t + n_H - 3)^2 \frac{|y_t|^4 m^3}{8(8\pi)^5 M_P^2} \tag{5.47}$$

which corresponds to

$$T_R = |2n_t + n_H - 3| (10^7\,\mathrm{GeV}) g^{-1/4} |y_t|^2 \left(\frac{m}{10^{-5} M_P}\right)^{3/2}\,. \tag{5.48}$$

Thus, as long as the matter fields do not reside in the untwisted sector (for which $n_i = 1$ and the rate vanishes), we obtain an adequate reheating temperature. The preceding rates may be modified if there are direct couplings between the modulus $T$ and the matter sector. A multiplicative coupling of the form

$$W \supset g(T) W_{\mathrm{M}}(\phi, \varphi) \tag{5.49}$$



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respects the form of the inflaton potential in the absence of linear terms in $W_M$. Assuming for simplicity that $g(1/2) = 1$, the addition of the factor $g(T)$ to the matter superpotential results in rates proportional to those obtained for constant $g(T)$, for a given sector. In particular, for the effective Lagrangian (5.40) it amounts to the substitution

$$(n_{I_1}+\cdots+n_L-3)W^{I_1 I_2 \ldots L}\bar{W}_{L J_1 J_2 \ldots} \longrightarrow \big(n_{I_1}+\cdots+n_L-3+g'(1/2)\big)W^{I_1 I_2 \ldots L}\bar{W}_{L J_1 J_2 \ldots}. \quad (5.50)$$

Therefore, the decay rates shown previously are enhanced by a factor of $|g'(1/2)|^2$, at most.

### 5.2.2 Decays to matter fermions

The direct decays of the volume modulus $T$ to fermions are determined by the couplings arising from the fermion kinetic term, the fermion mass matrix and the fermion-scalar interactions of the supergravity Lagrangian. The relevant couplings stemming from the fermion kinetic term (5.16) are shown in (5.51) below. Similarly to the scalar case, the interactions are diagonal with respect to matter field indices:

$$\mathcal{L}_{F,\text{kin}} = -\frac{i}{2\sqrt{3}}\delta T\,\bar{\chi}_{iL}\gamma^\mu\partial_\mu\chi^i_L - \frac{i\,n_a}{2\sqrt{3}}\delta T\,\bar{\chi}_{aL}\gamma^\mu\partial_\mu\chi^a_L + \text{h.c.} + \mathcal{O}(\Delta^2) + \cdots . \quad (5.51)$$

The interaction terms derived from the fermion mass matrix and the fermion-scalar interactions (5.17) correspond to

$$\begin{aligned}\mathcal{L}_{F,\text{int}} = {} & \frac{i}{2\sqrt{3}}\bar{\chi}_{iL}(\not{\partial}\delta T)\chi^i_L + \frac{i\,n_a}{2\sqrt{3}}\bar{\chi}_{aL}(\not{\partial}\delta T)\chi^a_L + \frac{\sqrt{3}}{2}\delta T\,W^{IJ}\bar{\chi}_{IL}\chi_{JR} \\ & + \frac{\sqrt{3}}{2}\delta T\,W^{IJK}\Phi_K\bar{\chi}_{IL}\chi_{JR} + \text{h.c.} + \mathcal{O}(\Delta^2) + \cdots . \end{aligned} \quad (5.52)$$

In analogy with the scalar case, at tree level the equation of motion for the fermion fields may be substituted in (5.51) and (5.52). Additionally, one must consider the fermion-dependent part of the equation of motion for the scalar fields in (5.36). Identifying $n_i = 1$ for all untwisted matter fields, the effective interaction Lagrangian for fermion decays can be written as

$$\mathcal{L}_{F,\text{eff}} = -\frac{\delta T}{2\sqrt{3}}(n_I + n_J - 3)W^{IJ}\bar{\chi}_{IL}\chi_{JR} - \frac{\delta T}{2\sqrt{3}}(n_I + n_J + n_K - 3)W^{IJK}\bar{\chi}_{IL}\chi_{JR}\Phi_K + \cdots . \quad (5.53)$$

Assuming negligible masses for all final states, $m_I \ll m$, the rates for two-body decays to matter fermions take the form

$$\Gamma(T \to \bar{\chi}_I\chi_J) = (n_I + n_J - 3)^2\frac{|W^{IJ}|^2 m}{192\pi M_P^2}. \quad (5.54)$$

which are (1/4) times the rate for three-body decays into scalars. The dominant rates are for three-body decays involving two fermions and one matter scalar are,

$$\Gamma(T \to \bar{\chi}_I\chi_J\Phi_K) = (n_I + n_J + n_K - 3)^2\frac{|W^{IJK}|^2 m^3}{36(8\pi)^3 M_P^2}. \quad (5.55)$$

which are non-vanishing in the MSSM so long the fields are twisted with weights $n_i \neq 1$. In particular, in the case of the top quark it implies the decay rate

$$\Gamma(T \to H_u^0 t_L\bar{t}_R,\, \tilde{t}_L\tilde{H}_u^0\bar{t}_R,\, \bar{\tilde{t}}_R t_L\tilde{H}_u^0) = (2n_t + n_H - 3)^2\frac{|y_t|^2 m^3}{12(8\pi)^3 M_P^2}. \quad (5.56)$$

which is somewhat larger than the four-scalar decay rate (5.47) because of the three-body phase-space factor.



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### 5.2.3 Decays to supersymmetry-breaking moduli and the gravitino

The volume modulus $T$ can also decay into the moduli responsible for the breaking of supersymmetry, with an amplitude that depends on the details of the inflationary and supersymmetry-breaking sectors. We consider first breaking by a hidden-sector untwisted matter field $z$, with the cubic superpotential (4.40). The direct decay is mediated by the effective Lagrangian

$$\mathcal{L}_z = -\frac{\delta T}{\sqrt{3}}(4+\gamma)\, m_{3/2}^2 z\bar{z} + \text{h.c.} + \mathcal{O}(\Delta^2) + \cdots , \tag{5.57}$$

where $\gamma$ is a constant that depends on the inflationary model: $\gamma = 8$ for the $(T, \phi_1)$ superpotential (3.12), and $\gamma = 6$ for the $(T, \varphi_1)$ superpotential (3.23). All terms shown explicitly in (5.57) are comparable and lead to the decay rate

$$\Gamma(T \to z\bar{z}) = \frac{(4+\gamma)^2 \Delta^4 m^3}{48\pi M_P^2} . \tag{5.58}$$

The coupling of $T$ to $z$ in the effective potential implies that, at the global supersymmetry breaking minimum, $\langle G^T \rangle \neq 0$. Therefore, the direct decay of $T$ to the gravitino is allowed. In the unitary gauge, this process is in general mediated by the Lagrangian (5.20). In the present case of supersymmetry breaking by $z$, the couplings are suppressed by the ratio of the gravitino mass to the inflaton mass, $\Delta$:

$$\mathcal{L}_{3/2,z} = -\frac{\sqrt{3}}{16}(82-13\gamma)\Delta^2 \left[\frac{1}{2}\,\epsilon^{\mu\nu\rho\sigma}\bar{\psi}_\mu \gamma_\nu \psi_\rho \partial_\sigma \delta T - i m_{3/2} \delta T\, \bar{\psi}_\mu \sigma^{\mu\nu} \psi_\nu\right] + \mathcal{O}(\Delta^4) + \cdots . \tag{5.59}$$

The decay rate can be readily evaluated to yield

$$\Gamma(T \to \psi_{3/2}\psi_{3/2}) \simeq (82-13\gamma)^2 \frac{\Delta^2 m^3}{768\pi M_P^2} . \tag{5.60}$$

The decay widths (5.58), (5.60) are suppressed by powers of the ratio of the gravitino mass to the inflaton mass, $\Delta$, relative to the three-body matter decays (5.56),

$$\frac{\Gamma(T \to z\bar{z})}{\Gamma(T \to H_u^0 t_L \bar{t}_R)} \sim 10^3 \Delta^4 , \qquad \frac{\Gamma(T \to \psi_{3/2}\psi_{3/2})}{\Gamma(T \to H_u^0 t_L \bar{t}_R)} \sim 10^3 \Delta^2 , \tag{5.61}$$

and hence are relatively unimportant for reheating.

One can also consider the scenario in which supersymmetry is broken by a strongly-stabilized Polonyi modulus in the twisted sector with superpotential (4.16). In this case, the couplings between the inflaton $T$ and the Polonyi field $z$ are given by

$$\mathcal{L}_z = -5\sqrt{3}\, m_{3/2}^2 \delta T z z - 4\sqrt{3}\, m_{3/2}^2 \delta T \bar{z}\bar{z} - 12\sqrt{3}\, \frac{m_{3/2}^2}{\Lambda_z^2}\, \delta T z\bar{z} + \text{h.c.} + \mathcal{O}(\Delta^4) + \cdots . \tag{5.62}$$

Since $\Lambda_z \ll 1$, the dominant decay channel corresponds to $z\bar{z}$, with a rate

$$\Gamma(T \to z\bar{z}) = \frac{27}{\pi} \frac{\Delta^4 M_P^2 m^3}{\Lambda_z^4} . \tag{5.63}$$



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The decay of $T$ to the gravitino in the Polonyi scenario is mediated by the following couplings:

$$\mathcal{L}_{3/2,z} = -\frac{3\sqrt{3}}{16}(4-3\bar{\gamma})\Lambda_z^{2\bar{\gamma}}\Delta^2\left[\frac{1}{2}\,\epsilon^{\mu\nu\rho\sigma}\bar{\psi}_\mu\gamma_\nu\psi_\rho\partial_\sigma\delta T + im_{3/2}\delta T\,\bar{\psi}_\mu\sigma^{\mu\nu}\psi_\nu\right] + \cdots\,, \tag{5.64}$$

where now $\bar{\gamma}=0$ for the $(T,\varphi_1)$ superpotential (3.23), and $\bar{\gamma}=1$ for the $(T,\phi_1)$ superpotential (3.12). In the latter case the amplitude is further suppressed by the factor $\Lambda_z^2$. The width is then given by

$$\Gamma(T\to\psi_{3/2}\psi_{3/2}) \simeq (4-3\bar{\gamma})^2\left(\frac{\Lambda_z}{M_P^2}\right)^{4\bar{\gamma}}\frac{3\Delta^2 m^3}{256\pi M_P^2}\,. \tag{5.65}$$

It is straightforward to verify that the decays of $T$ to the Polonyi modulus and to the gravitino in this scenario are negligible relative to the matter decay (5.56),

$$\frac{\Gamma(T\to z\bar{z})}{\Gamma(T\to H_u^0 t_L\bar{t}_R)} \sim 10^6\left(\frac{\Delta}{\Lambda_z/M_P}\right)^4, \qquad \frac{\Gamma(T\to\psi_{3/2}\psi_{3/2})}{\Gamma(T\to H_u^0 t_L\bar{t}_R)} \sim 10^3\Delta^2\left(\frac{\Lambda_z}{M_P^2}\right)^{4\bar{\gamma}}. \tag{5.66}$$

The decays to a single gravitino and a fermion belonging to a chiral multiplet are mediated by the interaction terms (5.23). It is straightforward to show that the amplitudes for the decays with a final-state matter fermion vanish up to $\mathcal{O}(\Delta^2)$. The only non-vanishing couplings with $T$ are those with the inflatino and the $\phi_1$ or $\varphi_1$-ino. The corresponding amplitudes are dependent on the supersymmetry-breaking mechanism. However, in all cases it can be shown that the decay rates to kinematically-allowed final-state mass eigenstates are suppressed by a factor of $\Delta^2$: $\Gamma\sim\Delta^2(m^3/M_P^2)$, due to the mass degeneracy $m-m_\chi\sim m_{3/2}$.

In the absence of a direct coupling of $T$ to the gauge degrees of freedom, i.e., $f^T_{\alpha\beta}=0$, where $f_{\alpha\beta}$ is the gauge kinetic function, the total decay rate of the inflaton is the sum of the rates previously shown. The largest width corresponds is that to two matter fermions plus a matter scalar, (5.56), which implies the reheating temperature

$$T_R = (10^8\ \text{GeV})\,|y_t(2n_t+n_H-6)|\left(\frac{g}{915/4}\right)^{-1/4}\left(\frac{m}{10^{-5}M_P}\right)^{3/2}. \tag{5.67}$$

### 5.2.4 Decays to gauge bosons and gauginos

The inflaton $T$ can decay to gauge fields and gauginos through a coupling in the gauge kinetic function $f_{\alpha\beta}(T)$, which, as was mentioned before, is a generic feature of heterotic string effective field theories [16, 133–136]. The supergravity Lagrangian terms containing the relevant interactions are given by (5.28), disregarding contributions suppressed by the gaugino masses. The decay width to the canonically-normalized gauge boson pairs is readily evaluated, resulting in

$$\Gamma(T\to gg) = \frac{d_{g,T}^2}{32\pi}\left(\frac{N_G}{12}\right)\frac{m^3}{M_P^2}\,, \tag{5.68}$$

where $N_G$ is the number of final states: $N_G=12$ for the Standard Model, and $d_{g,T}$ has been defined in (5.33). The corresponding reheating temperature is

$$T_R = (3\times10^9\ \text{GeV})\,d_{g,T}\left(\frac{N_G}{12}\right)^{1/2}\left(\frac{g}{915/4}\right)^{-1/4}\left(\frac{m}{10^{-5}M_P}\right)^{3/2}. \tag{5.69}$$

The coefficient $d_{g,T}$ might well be $\mathcal{O}(1)$, e.g., for a gauge kinetic function linear in $T$ with $\mathcal{O}(1)$ coefficients, in which case all other decay channels of the volume modulus $T$ would be



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overwhelmed by the decays to gauge bosons, and the reheating temperature would be large. The effective reheating temperature generated by decays into gauge bosons would exceed that due to decays into matter particles, (5.67), for any $d_{g,T} \gtrsim \mathcal{O}(1/30)$.

On the other hand, the decays of $T$ to gauginos are subdominant. Our results differ from the treatment of [137], in that in our case the mass of the modulus $T$ is determined not by the bilinear coupling $W^{TT}$, which has a vanishing vev, but by the coupling $W^{T\phi_1}$ or $W^{T\varphi_1}$. This results in an amplitude for decay to gauginos that is suppressed by $\Delta$ relative to the amplitude for the decay to gauge bosons. Assuming for simplicity that $f(T)$ is a holomorphic function with real coefficients, the corresponding decay rate is

$$\Gamma(T \to \tilde{g}\tilde{g}) = \frac{d_g^2 \Delta^2}{16\pi} \left(\frac{N_G}{12}\right) \frac{m^3}{M_P^2} \,. \tag{5.70}$$

A similar suppression for the decay to gauginos was seen in [132].

## 6 Summary and prospects

We have considered in this paper various aspects of no-scale inflation, considering two main classes of models: those in which the inflaton is identified with an untwisted matter field $\phi$, and those in which the inflaton is identified with the compactification volume modulus $T$. We have focused on two important phenomenological issues: possible patterns of soft supersymmetry breaking, and inflaton decays and the related reheating temperature of the Universe subsequent to inflation. We have considered in section 4 various possible mechanisms for supersymmetry breaking, including via the volume moduli and the Polonyi mechanism. These mechanisms yield many possibilities for the soft supersymmetry-breaking parameters effective low-energy theory. In general, the patterns of soft supersymmetry breaking for the untwisted and twisted matter sectors are different. For example, no-scale, CMSSM or mSUGRA boundary conditions are natural possibilities in the untwisted sector, whereas in the twisted sector the soft supersymmetry-breaking parameters are not universal in general, since they depend on the modular weights of the fields. As usual, the gaugino masses would in general arise from a non-minimal gauge kinetic function or through loop effects via anomalies. Observation of supersymmetric particles at the LHC or elsewhere followed by studies of the pattern of supersymmetry breaking could give valuable insights into the form of no-scale inflationary model and the assignments of matter particles as well as the inflaton.

In section 5 we have considered inflaton decays in the same two classes of models, namely when the inflaton is the untwisted matter field $\phi$, and when the inflaton is the volume modulus field $T$. The reheating temperature could in principle be larger in the $\phi$ inflaton case, namely $\mathcal{O}(10^{15})$ GeV, if there is an $\mathcal{O}(1)$ trilinear superpotential coupling between $\phi$ and light matter fields, as might occur in a neutrino inflation scenario, see (5.14) and (5.19). A similar reheating temperature could in principle also be generated by decays into gravitino and modulino pairs, see (5.25). However, the gravitino problem imposes a non-trivial upper limit on the reheating temperature, and hence on the possible trilinear superpotential, moduli and gravitino couplings. On the other hand, the reheating temperature is naturally considerably smaller in the $T$ inflaton case, namely $\mathcal{O}(3 \times 10^8)$ GeV, with the dominant decays being into three-body matter final states, see (5.56), whereas decays into gravitinos are expected to be much smaller (5.66). We note, however, that in both scenarios decays into gauge bosons may also yield reheating temperatures as large as $10^{10}$ GeV, depending on the form of the gauge kinetic function, see eqs. (5.31) and (5.69). This provides a possible link between



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the supersymmetry-breaking mechanism for generating $m_{1/2} \neq 0$ and the thermal history of the Universe.

As commented in the Introduction, the values of the cosmic microwave background observables $n_s$ and $r$ are sensitive to the number of e-folds during inflation, $N^*$, which is in turn sensitive to the reheating temperature. Thus, there is in principle a connection between accelerator physics and inflationary cosmology via supersymmetry breaking, which may also cast light on the nature of string compactification. However, detailed exploration of this fascinating connection lies beyond the scope of this paper.

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## References

[1] E. Cremmer, S. Ferrara, C. Kounnas and D.V. Nanopoulos, *Naturally Vanishing Cosmological Constant in $N = 1$ Supergravity*, *Phys. Lett.* **B 133** (1983) 61 [INSPIRE].

[2] J.R. Ellis, A.B. Lahanas, D.V. Nanopoulos and K. Tamvakis, *No-Scale Supersymmetric Standard Model*, *Phys. Lett.* **B 134** (1984) 429 [INSPIRE].

[3] J.R. Ellis, C. Kounnas and D.V. Nanopoulos, *No Scale Supersymmetric Guts*, *Nucl. Phys.* **B 247** (1984) 373 [INSPIRE].

[4] A.B. Lahanas and D.V. Nanopoulos, *The Road to No Scale Supergravity*, *Phys. Rept.* **145** (1987) 1 [INSPIRE].

[5] E. Witten, *Dimensional Reduction of Superstring Models*, *Phys. Lett.* **B 155** (1985) 151 [INSPIRE].

[6] S.B. Giddings, S. Kachru and J. Polchinski, *Hierarchies from fluxes in string compactifications*, *Phys. Rev.* **D 66** (2002) 106006 [hep-th/0105097] [INSPIRE].

[7] V. Balasubramanian, P. Berglund, J.P. Conlon and F. Quevedo, *Systematics of moduli stabilisation in Calabi-Yau flux compactifications*, *JHEP* **03** (2005) 007 [hep-th/0502058] [INSPIRE].

[8] J.R. Ellis, K. Enqvist, D.V. Nanopoulos, K.A. Olive and M. Srednicki, *SU(N,1) Inflation*, *Phys. Lett.* **B 152** (1985) 175 [*Erratum ibid.* **156B** (1985) 452] [INSPIRE].

[9] K. Enqvist, D.V. Nanopoulos and M. Quirós, *Inflation From a Ripple on a Vanishing Potential*, *Phys. Lett.* **B 159** (1985) 249 [INSPIRE].

[10] A.S. Goncharov and A.D. Linde, *A simple realization of the inflationary universe scenario in* SU(1, 1) *supergravity*, *Class. Quant. Grav.* **1** (1984) L75 [INSPIRE].

[11] P. Binétruy and M.K. Gaillard, *Candidates for the Inflaton Field in Superstring Models*, *Phys. Rev.* **D 34** (1986) 3069 [INSPIRE].

[12] H. Murayama, H. Suzuki, T. Yanagida and J. Yokoyama, *Chaotic inflation and baryogenesis in supergravity*, *Phys. Rev.* **D 50** (1994) 2356 [hep-ph/9311326] [INSPIRE].



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[13] S.C. Davis and M. Postma, *SUGRA chaotic inflation and moduli stabilisation*, *JCAP* **03** (2008) 015 [arXiv:0801.4696] [INSPIRE].

[14] S. Antusch, M. Bastero-Gil, K. Dutta, S.F. King and P.M. Kostka, *Solving the eta-Problem in Hybrid Inflation with Heisenberg Symmetry and Stabilized Modulus*, *JCAP* **01** (2009) 040 [arXiv:0808.2425] [INSPIRE].

[15] S. Antusch, M. Bastero-Gil, K. Dutta, S.F. King and P.M. Kostka, *Chaotic Inflation in Supergravity with Heisenberg Symmetry*, *Phys. Lett.* **B 679** (2009) 428 [arXiv:0905.0905] [INSPIRE].

[16] S. Antusch, K. Dutta, J. Erdmenger and S. Halter, *Towards Matter Inflation in Heterotic String Theory*, *JHEP* **04** (2011) 065 [arXiv:1102.0093] [INSPIRE].

[17] J. Ellis, D.V. Nanopoulos and K.A. Olive, *No-Scale Supergravity Realization of the Starobinsky Model of Inflation*, *Phys. Rev. Lett.* **111** (2013) 111301 [arXiv:1305.1247] [INSPIRE].

[18] R. Kallosh and A. Linde, *Superconformal generalizations of the Starobinsky model*, *JCAP* **06** (2013) 028 [arXiv:1306.3214] [INSPIRE].

[19] J. Ellis, D.V. Nanopoulos and K.A. Olive, *Starobinsky-like Inflationary Models as Avatars of No-Scale Supergravity*, *JCAP* **10** (2013) 009 [arXiv:1307.3537] [INSPIRE].

[20] F. Farakos, A. Kehagias and A. Riotto, *On the Starobinsky Model of Inflation from Supergravity*, *Nucl. Phys.* **B 876** (2013) 187 [arXiv:1307.1137] [INSPIRE].

[21] W. Buchmüller, V. Domcke and C. Wieck, *No-scale D-term inflation with stabilized moduli*, *Phys. Lett.* **B 730** (2014) 155 [arXiv:1309.3122] [INSPIRE].

[22] J. Ellis, D.V. Nanopoulos and K.A. Olive, *A no-scale supergravity framework for sub-Planckian physics*, *Phys. Rev.* **D 89** (2014) 043502 [arXiv:1310.4770] [INSPIRE].

[23] C. Pallis, *Linking Starobinsky-Type Inflation in no-Scale Supergravity to MSSM*, *JCAP* **04** (2014) 024 [arXiv:1312.3623] [INSPIRE].

[24] C. Pallis, *Induced-Gravity Inflation in no-Scale Supergravity and Beyond*, *JCAP* **08** (2014) 057 [arXiv:1403.5486] [INSPIRE].

[25] S. Ferrara, A. Kehagias and A. Riotto, *The Imaginary Starobinsky Model*, *Fortsch. Phys.* **62** (2014) 573 [arXiv:1403.5531] [INSPIRE].

[26] S. Ferrara, A. Kehagias and A. Riotto, *The Imaginary Starobinsky Model and Higher Curvature Corrections*, *Fortsch. Phys.* **63** (2015) 2 [arXiv:1405.2353] [INSPIRE].

[27] J. Ellis, M.A.G. García, D.V. Nanopoulos and K.A. Olive, *Resurrecting Quadratic Inflation in No-Scale Supergravity in Light of BICEP2*, *JCAP* **05** (2014) 037 [arXiv:1403.7518] [INSPIRE].

[28] J. Ellis, M.A.G. García, D.V. Nanopoulos and K.A. Olive, *A No-Scale Inflationary Model to Fit Them All*, *JCAP* **08** (2014) 044 [arXiv:1405.0271] [INSPIRE].

[29] J. Ellis, M.A.G. García, D.V. Nanopoulos and K.A. Olive, *Two-Field Analysis of No-Scale Supergravity Inflation*, *JCAP* **01** (2015) 010 [arXiv:1409.8197] [INSPIRE].

[30] T. Li, Z. Li and D.V. Nanopoulos, *No-Scale Ripple Inflation Revisited*, *JCAP* **04** (2014) 018 [arXiv:1310.3331] [INSPIRE].

[31] T. Li, Z. Li and D.V. Nanopoulos, *Chaotic Inflation in No-Scale Supergravity with String Inspired Moduli Stabilization*, *Eur. Phys. J.* **C 75** (2015) 55 [arXiv:1405.0197] [INSPIRE].

[32] S. Renaux-Petel and K. Turzynski, *On reaching the adiabatic limit in multi-field inflation*, *JCAP* **06** (2015) 010 [arXiv:1405.6195] [INSPIRE].

[33] W. Buchmüller, E. Dudas, L. Heurtier and C. Wieck, *Large-Field Inflation and Supersymmetry Breaking*, *JHEP* **09** (2014) 053 [arXiv:1407.0253] [INSPIRE].

JCAP10(2015)003

[34] C. Kounnas, D. Lüst and N. Toumbas, *$R^2$ inflation from scale invariant supergravity and anomaly free superstrings with fluxes*, *Fortsch. Phys.* **63** (2015) 12 [arXiv:1409.7076] [INSPIRE].

[35] A.B. Lahanas and K. Tamvakis, *Inflation in no-scale supergravity*, *Phys. Rev.* **D 91** (2015) 085001 [arXiv:1501.06547] [INSPIRE].

[36] A.A. Starobinsky, *A New Type of Isotropic Cosmological Models Without Singularity*, *Phys. Lett.* **B 91** (1980) 99 [INSPIRE].

[37] A.D. Linde, *Recent Progress in the Inflationary Universe Scenario*, *Nucl. Phys.* **B 252** (1985) 153 [INSPIRE].

[38] M.S. Madsen and P. Coles, *Chaotic inflation*, *Nucl. Phys.* **B 298** (1988) 701 [INSPIRE].

[39] M. Drees and M.M. Nojiri, *The Neutralino relic density in minimal $N = 1$ supergravity*, *Phys. Rev.* **D 47** (1993) 376 [hep-ph/9207234] [INSPIRE].

[40] G.L. Kane, C.F. Kolda, L. Roszkowski and J.D. Wells, *Study of constrained minimal supersymmetry*, *Phys. Rev.* **D 49** (1994) 6173 [hep-ph/9312272] [INSPIRE].

[41] H. Baer and M. Brhlik, *Cosmological relic density from minimal supergravity with implications for collider physics*, *Phys. Rev.* **D 53** (1996) 597 [hep-ph/9508321] [INSPIRE].

[42] H. Baer and M. Brhlik, *Neutralino dark matter in minimal supergravity: Direct detection versus collider searches*, *Phys. Rev.* **D 57** (1998) 567 [hep-ph/9706509] [INSPIRE].

[43] J.R. Ellis, T. Falk, K.A. Olive and M. Schmitt, *Supersymmetric dark matter in the light of LEP-1.5*, *Phys. Lett.* **B 388** (1996) 97 [hep-ph/9607292] [INSPIRE].

[44] J.R. Ellis, T. Falk, K.A. Olive and M. Schmitt, *Constraints on neutralino dark matter from LEP-2 and cosmology*, *Phys. Lett.* **B 413** (1997) 355 [hep-ph/9705444] [INSPIRE].

[45] J.R. Ellis, T. Falk, G. Ganis, K.A. Olive and M. Schmitt, *Charginos and neutralinos in the light of radiative corrections: Sealing the fate of Higgsino dark matter*, *Phys. Rev.* **D 58** (1998) 095002 [hep-ph/9801445] [INSPIRE].

[46] V.D. Barger and C. Kao, *Relic density of neutralino dark matter in supergravity models*, *Phys. Rev.* **D 57** (1998) 3131 [hep-ph/9704403] [INSPIRE].

[47] J.R. Ellis, T. Falk, G. Ganis and K.A. Olive, *Supersymmetric dark matter in the light of LEP and the Tevatron collider*, *Phys. Rev.* **D 62** (2000) 075010 [hep-ph/0004169] [INSPIRE].

[48] H. Baer et al., *Yukawa unified supersymmetric* SO(10) *model: Cosmology, rare decays and collider searches*, *Phys. Rev.* **D 63** (2000) 015007 [hep-ph/0005027] [INSPIRE].

[49] J.R. Ellis, T. Falk, G. Ganis, K.A. Olive and M. Srednicki, *The CMSSM parameter space at large tan beta*, *Phys. Lett.* **B 510** (2001) 236 [hep-ph/0102098] [INSPIRE].

[50] V.D. Barger and C. Kao, *Implications of new CMB data for neutralino dark matter*, *Phys. Lett.* **B 518** (2001) 117 [hep-ph/0106189] [INSPIRE].

[51] L. Roszkowski, R. Ruiz de Austri and T. Nihei, *New cosmological and experimental constraints on the CMSSM*, *JHEP* **08** (2001) 024 [hep-ph/0106334] [INSPIRE].

[52] A. Djouadi, M. Drees and J.L. Kneur, *Constraints on the minimal supergravity model and prospects for SUSY particle production at future linear $e^+e^-$ colliders*, *JHEP* **08** (2001) 055 [hep-ph/0107316] [INSPIRE].

[53] U. Chattopadhyay, A. Corsetti and P. Nath, *Supersymmetric dark matter and Yukawa unification*, *Phys. Rev.* **D 66** (2002) 035003 [hep-ph/0201001] [INSPIRE].

[54] J.R. Ellis, K.A. Olive and Y. Santoso, *Constraining supersymmetry*, *New J. Phys.* **4** (2002) 32 [hep-ph/0202110] [INSPIRE].



JCAP10(2015)003

[55] H. Baer, C. Balázs, A. Belyaev, J.K. Mizukoshi, X. Tata and Y. Wang, *Updated constraints on the minimal supergravity model*, *JHEP* **07** (2002) 050 [hep-ph/0205325] [INSPIRE].

[56] R.L. Arnowitt and B. Dutta, *Dark matter, muon g-2 and other accelerator constraints*, hep-ph/0211417 [INSPIRE].

[57] R. Barbieri, S. Ferrara and C.A. Savoy, *Gauge Models with Spontaneously Broken Local Supersymmetry*, *Phys. Lett.* **B 119** (1982) 343 [INSPIRE].

[58] J.R. Ellis, K.A. Olive, Y. Santoso and V.C. Spanos, *Phenomenological constraints on patterns of supersymmetry breaking*, *Phys. Lett.* **B 573** (2003) 162 [hep-ph/0305212] [INSPIRE].

[59] J.R. Ellis, K.A. Olive, Y. Santoso and V.C. Spanos, *Very constrained minimal supersymmetric standard models*, *Phys. Rev.* **D 70** (2004) 055005 [hep-ph/0405110] [INSPIRE].

[60] M. Dine and D. MacIntire, *Supersymmetry, naturalness and dynamical supersymmetry breaking*, *Phys. Rev.* **D 46** (1992) 2594 [hep-ph/9205227] [INSPIRE].

[61] L. Randall and R. Sundrum, *Out of this world supersymmetry breaking*, *Nucl. Phys.* **B 557** (1999) 79 [hep-th/9810155] [INSPIRE].

[62] G.F. Giudice, M.A. Luty, H. Murayama and R. Rattazzi, *Gaugino mass without singlets*, *JHEP* **12** (1998) 027 [hep-ph/9810442] [INSPIRE].

[63] J.A. Bagger, T. Moroi and E. Poppitz, *Anomaly mediation in supergravity theories*, *JHEP* **04** (2000) 009 [hep-th/9911029] [INSPIRE].

[64] P. Binetruy, M.K. Gaillard and B.D. Nelson, *One loop soft supersymmetry breaking terms in superstring effective theories*, *Nucl. Phys.* **B 604** (2001) 32 [hep-ph/0011081] [INSPIRE].

[65] M. Ibe, T. Moroi and T.T. Yanagida, *Possible Signals of Wino LSP at the Large Hadron Collider*, *Phys. Lett.* **B 644** (2007) 355 [hep-ph/0610277] [INSPIRE].

[66] M. Ibe and T.T. Yanagida, *The Lightest Higgs Boson Mass in Pure Gravity Mediation Model*, *Phys. Lett.* **B 709** (2012) 374 [arXiv:1112.2462] [INSPIRE].

[67] M. Ibe, S. Matsumoto and T.T. Yanagida, *Pure Gravity Mediation with* $m_{3/2} = 10-100$ *TeV*, *Phys. Rev.* **D 85** (2012) 095011 [arXiv:1202.2253] [INSPIRE].

[68] J.L. Evans, M. Ibe, K.A. Olive and T.T. Yanagida, *Universality in Pure Gravity Mediation*, *Eur. Phys. J.* **C 73** (2013) 2468 [arXiv:1302.5346] [INSPIRE].

[69] J.L. Evans, K.A. Olive, M. Ibe and T.T. Yanagida, *Non-Universalities in Pure Gravity Mediation*, *Eur. Phys. J.* **C 73** (2013) 2611 [arXiv:1305.7461] [INSPIRE].

[70] J.L. Evans, M. Ibe, K.A. Olive and T.T. Yanagida, *Light Higgsinos in Pure Gravity Mediation*, *Phys. Rev.* **D 91** (2015) 055008 [arXiv:1412.3403] [INSPIRE].

[71] J.L. Evans and K.A. Olive, *Universality in Pure Gravity Mediation with Vector Multiplets*, *Phys. Rev.* **D 90** (2014) 115020 [arXiv:1408.5102] [INSPIRE].

[72] J.P. Conlon and F. Quevedo, *Kähler moduli inflation*, *JHEP* **01** (2006) 146 [hep-th/0509012] [INSPIRE].

[73] M. Cicoli, C.P. Burgess and F. Quevedo, *Fibre Inflation: Observable Gravity Waves from IIB String Compactifications*, *JCAP* **03** (2009) 013 [arXiv:0808.0691] [INSPIRE].

[74] M. Cicoli, F.G. Pedro and G. Tasinato, *Poly-instanton Inflation*, *JCAP* **12** (2011) 022 [arXiv:1110.6182] [INSPIRE].

[75] J.R. Ellis, D.V. Nanopoulos, K.A. Olive and K. Tamvakis, *Cosmological Inflation Cries Out for Supersymmetry*, *Phys. Lett.* **B 118** (1982) 335 [INSPIRE].

[76] J.R. Ellis, D.V. Nanopoulos, K.A. Olive and K. Tamvakis, *Fluctuations in a Supersymmetric Inflationary Universe*, *Phys. Lett.* **B 120** (1983) 331 [INSPIRE].

JCAP10(2015)003

[77] J.R. Ellis, D.V. Nanopoulos, K.A. Olive and K. Tamvakis, *Primordial Supersymmetric Inflation*, *Nucl. Phys.* **B 221** (1983) 52 [INSPIRE].

[78] D.V. Nanopoulos, K.A. Olive, M. Srednicki and K. Tamvakis, *Primordial Inflation in Simple Supergravity*, *Phys. Lett.* **B 123** (1983) 41 [INSPIRE].

[79] D.V. Nanopoulos, K.A. Olive and M. Srednicki, *After Primordial Inflation*, *Phys. Lett.* **B 127** (1983) 30 [INSPIRE].

[80] R. Holman, P. Ramond and G.G. Ross, *Supersymmetric Inflationary Cosmology*, *Phys. Lett.* **B 137** (1984) 343 [INSPIRE].

[81] A.B. Goncharov and A.D. Linde, *Chaotic Inflation in Supergravity*, *Phys. Lett.* **B 139** (1984) 27 [INSPIRE].

[82] PLANCK collaboration, P.A.R. Ade et al., *Planck 2015 results. XIII. Cosmological parameters*, arXiv:1502.01589 [INSPIRE].

[83] PLANCK collaboration, P.A.R. Ade et al., *Planck 2015 results. XX. Constraints on inflation*, arXiv:1502.02114 [INSPIRE].

[84] V.F. Mukhanov and G.V. Chibisov, *Quantum Fluctuation and Nonsingular Universe* (in Russian), *JETP Lett.* **33** (1981) 532 [INSPIRE].

[85] A.A. Starobinsky, *The Perturbation Spectrum Evolving from a Nonsingular Initially De-Sitte r Cosmology and the Microwave Background Anisotropy*, *Sov. Astron. Lett.* **9** (1983) 302 [INSPIRE].

[86] S. Cecotti, *Higher derivative supergravity is equivalent to standard supergravity coupled to matter. 1.*, *Phys. Lett.* **B 190** (1987) 86 [INSPIRE].

[87] M. Endo, K. Kadota, K.A. Olive, F. Takahashi and T.T. Yanagida, *The Decay of the Inflaton in No-scale Supergravity*, *JCAP* **02** (2007) 018 [hep-ph/0612263] [INSPIRE].

[88] T. Terada, Y. Watanabe, Y. Yamada and J. Yokoyama, *Reheating processes after Starobinsky inflation in old-minimal supergravity*, *JHEP* **02** (2015) 105 [arXiv:1411.6746] [INSPIRE].

[89] M. Cicoli and A. Mazumdar, *Reheating for Closed String Inflation*, *JCAP* **09** (2010) 025 [arXiv:1005.5076] [INSPIRE].

[90] M. Cicoli, J.P. Conlon and F. Quevedo, *Dark radiation in LARGE volume models*, *Phys. Rev.* **D 87** (2013) 043520 [arXiv:1208.3562] [INSPIRE].

[91] T. Higaki and F. Takahashi, *Dark Radiation and Dark Matter in Large Volume Compactifications*, *JHEP* **11** (2012) 125 [arXiv:1208.3563] [INSPIRE].

[92] T. Higaki, K. Nakayama and F. Takahashi, *Moduli-Induced Axion Problem*, *JHEP* **07** (2013) 005 [arXiv:1304.7987] [INSPIRE].

[93] G. Kane, K. Sinha and S. Watson, *Cosmological Moduli and the Post-Inflationary Universe: A Critical Review*, *Int. J. Mod. Phys.* **D 24** (2015) 1530022 [arXiv:1502.07746] [INSPIRE].

[94] K. Choi, A. Falkowski, H.P. Nilles and M. Olechowski, *Soft supersymmetry breaking in KKLT flux compactification*, *Nucl. Phys.* **B 718** (2005) 113 [hep-th/0503216] [INSPIRE].

[95] O. Lebedev, H.P. Nilles and M. Ratz, *de Sitter vacua from matter superpotentials*, *Phys. Lett.* **B 636** (2006) 126 [hep-th/0603047] [INSPIRE].

[96] O. Lebedev, V. Lowen, Y. Mambrini, H.P. Nilles and M. Ratz, *Metastable Vacua in Flux Compactifications and Their Phenomenology*, *JHEP* **02** (2007) 063 [hep-ph/0612035] [INSPIRE].

[97] J.R. Ellis, C. Kounnas and D.V. Nanopoulos, *No Scale Supergravity Models with a Planck Mass Gravitino*, *Phys. Lett.* **B 143** (1984) 410 [INSPIRE].

JCAP10(2015)003

[98] E. Dudas and C. Wieck, *Moduli backreaction and supersymmetry breaking in string-inspired inflation models*, arXiv:1506.01253 [INSPIRE].

[99] L.E. Ibáñez and G.G. Ross, SU(2)-L × U(1) *Symmetry Breaking as a Radiative Effect of Supersymmetry Breaking in Guts*, *Phys. Lett.* **B 110** (1982) 215 [INSPIRE].

[100] K. Inoue, A. Kakuto, H. Komatsu and S. Takeshita, *Aspects of Grand Unified Models with Softly Broken Supersymmetry*, *Prog. Theor. Phys.* **68** (1982) 927 [*Erratum ibid.* **70** (1983) 330] [INSPIRE].

[101] L.E. Ibáñez, *Locally Supersymmetric* SU(5) *Grand Unification*, *Phys. Lett.* **B 118** (1982) 73 [INSPIRE].

[102] J.R. Ellis, D.V. Nanopoulos and K. Tamvakis, *Grand Unification in Simple Supergravity*, *Phys. Lett.* **B 121** (1983) 123 [INSPIRE].

[103] J.R. Ellis, J.S. Hagelin, D.V. Nanopoulos and K. Tamvakis, *Weak Symmetry Breaking by Radiative Corrections in Broken Supergravity*, *Phys. Lett.* **B 125** (1983) 275 [INSPIRE].

[104] L. Álvarez-Gaumé, J. Polchinski and M.B. Wise, *Minimal Low-Energy Supergravity*, *Nucl. Phys.* **B 221** (1983) 495 [INSPIRE].

[105] S. Profumo, *Neutralino relic density in supersymmetric GUTs with no scale boundary conditions above the unification scale*, *JHEP* **06** (2003) 052 [hep-ph/0306119] [INSPIRE].

[106] J. Ellis, A. Mustafayev and K.A. Olive, *Resurrecting No-Scale Supergravity Phenomenology*, *Eur. Phys. J.* **C 69** (2010) 219 [arXiv:1004.5399] [INSPIRE].

[107] J. Polonyi, *Generalization of the Massive Scalar Multiplet Coupling to the Supergravity*, Budapest preprint KFKI-1977-93 (1977).

[108] M. Dine, R. Kitano, A. Morisse and Y. Shirman, *Moduli decays and gravitinos*, *Phys. Rev.* **D 73** (2006) 123518 [hep-ph/0604140] [INSPIRE].

[109] R. Kitano, *Gravitational Gauge Mediation*, *Phys. Lett.* **B 641** (2006) 203 [hep-ph/0607090] [INSPIRE].

[110] J.L. Evans, M.A.G. Garcia and K.A. Olive, *The Moduli and Gravitino (non)-Problems in Models with Strongly Stabilized Moduli*, *JCAP* **03** (2014) 022 [arXiv:1311.0052] [INSPIRE].

[111] E. Dudas, A. Linde, Y. Mambrini, A. Mustafayev and K.A. Olive, *Strong moduli stabilization and phenomenology*, *Eur. Phys. J.* **C 73** (2013) 2268 [arXiv:1209.0499] [INSPIRE].

[112] G.F. Giudice and A. Masiero, *A Natural Solution to the mu Problem in Supergravity Theories*, *Phys. Lett.* **B 206** (1988) 480 [INSPIRE].

[113] L. Calibbi, Y. Mambrini and S.K. Vempati, *SUSY-GUTs, SUSY-seesaw and the neutralino dark matter*, *JHEP* **09** (2007) 081 [arXiv:0704.3518] [INSPIRE].

[114] L. Calibbi, A. Faccia, A. Masiero and S.K. Vempati, *Lepton flavour violation from SUSY-GUTs: Where do we stand for MEG, PRISM/PRIME and a super flavour factory*, *Phys. Rev.* **D 74** (2006) 116002 [hep-ph/0605139] [INSPIRE].

[115] E. Carquin, J. Ellis, M.E. Gomez, S. Lola and J. Rodriguez-Quintero, *Search for Tau Flavour Violation at the LHC*, *JHEP* **05** (2009) 026 [arXiv:0812.4243] [INSPIRE].

[116] J. Ellis, A. Mustafayev and K.A. Olive, *What if Supersymmetry Breaking Unifies beyond the GUT Scale?*, *Eur. Phys. J.* **C 69** (2010) 201 [arXiv:1003.3677] [INSPIRE].

[117] H. Murayama, H. Suzuki, T. Yanagida and J. Yokoyama, *Chaotic inflation and baryogenesis by right-handed sneutrinos*, *Phys. Rev. Lett.* **70** (1993) 1912 [INSPIRE].

[118] H. Murayama, H. Suzuki, T. Yanagida and J. Yokoyama, *Chaotic inflation and baryogenesis in supergravity*, *Phys. Rev.* **D 50** (1994) 2356 [hep-ph/9311326] [INSPIRE].

JCAP10(2015)003

[119] J.R. Ellis, M. Raidal and T. Yanagida, *Sneutrino inflation in the light of WMAP: Reheating, leptogenesis and flavor violating lepton decays*, *Phys. Lett.* **B 581** (2004) 9 [hep-ph/0303242] [INSPIRE].

[120] D. Croon, J. Ellis and N.E. Mavromatos, *Wess-Zumino Inflation in Light of Planck*, *Phys. Lett.* **B 724** (2013) 165 [arXiv:1303.6253] [INSPIRE].

[121] K. Nakayama, F. Takahashi and T.T. Yanagida, *Chaotic Inflation with Right-handed Sneutrinos after Planck*, *Phys. Lett.* **B 730** (2014) 24 [arXiv:1311.4253] [INSPIRE].

[122] J. Ellis, N.E. Mavromatos and D.J. Mulryne, *Exploring Two-Field Inflation in the Wess-Zumino Model*, *JCAP* **05** (2014) 012 [arXiv:1401.6078] [INSPIRE].

[123] J.L. Evans, T. Gherghetta and M. Peloso, *Affleck-Dine sneutrino inflation*, *Phys. Rev.* **D 92** (2015) 021303 [arXiv:1501.06560] [INSPIRE].

[124] M. Bolz, A. Brandenburg and W. Buchmüller, *Thermal production of gravitinos*, *Nucl. Phys.* **B 606** (2001) 518 [*Erratum ibid.* **B 790** (2008) 336] [hep-ph/0012052] [INSPIRE].

[125] R.H. Cyburt, J.R. Ellis, B.D. Fields and K.A. Olive, *Updated nucleosynthesis constraints on unstable relic particles*, *Phys. Rev.* **D 67** (2003) 103521 [astro-ph/0211258] [INSPIRE].

[126] F.D. Steffen, *Gravitino dark matter and cosmological constraints*, *JCAP* **09** (2006) 001 [hep-ph/0605306] [INSPIRE].

[127] M. Kawasaki, K. Kohri, T. Moroi and A. Yotsuyanagi, *Big-Bang Nucleosynthesis and Gravitino*, *Phys. Rev.* **D 78** (2008) 065011 [arXiv:0804.3745] [INSPIRE].

[128] R.H. Cyburt, J. Ellis, B.D. Fields, F. Luo, K.A. Olive and V.C. Spanos, *Nucleosynthesis Constraints on a Massive Gravitino in Neutralino Dark Matter Scenarios*, *JCAP* **10** (2009) 021 [arXiv:0907.5003] [INSPIRE].

[129] R.H. Cyburt, J. Ellis, B.D. Fields, F. Luo, K.A. Olive and V.C. Spanos, *Gravitino Decays and the Cosmological Lithium Problem in Light of the LHC Higgs and Supersymmetry Searches*, *JCAP* **05** (2013) 014 [arXiv:1303.0574] [INSPIRE].

[130] D.V. Nanopoulos, K.A. Olive and M. Srednicki, *After Primordial Inflation*, *Phys. Lett.* **B 127** (1983) 30 [INSPIRE].

[131] H.P. Nilles, K.A. Olive and M. Peloso, *The Inflatino problem in supergravity inflationary models*, *Phys. Lett.* **B 522** (2001) 304 [hep-ph/0107212] [INSPIRE].

[132] R. Kallosh, A. Linde, K.A. Olive and T. Rube, *Chaotic inflation and supersymmetry breaking*, *Phys. Rev.* **D 84** (2011) 083519 [arXiv:1106.6025] [INSPIRE].

[133] J.P. Derendinger, S. Ferrara, C. Kounnas and F. Zwirner, *On loop corrections to string effective field theories: Field dependent gauge couplings and $\sigma$-model anomalies*, *Nucl. Phys.* **B 372** (1992) 145 [INSPIRE].

[134] L.J. Dixon, V. Kaplunovsky and J. Louis, *Moduli dependence of string loop corrections to gauge coupling constants*, *Nucl. Phys.* **B 355** (1991) 649 [INSPIRE].

[135] D. Lüst and C. Muñoz, *Duality invariant gaugino condensation and one loop corrected Kähler potentials in string theory*, *Phys. Lett.* **B 279** (1992) 272 [hep-th/9201047] [INSPIRE].

[136] V. Kaplunovsky and J. Louis, *On Gauge couplings in string theory*, *Nucl. Phys.* **B 444** (1995) 191 [hep-th/9502077] [INSPIRE].

[137] S. Nakamura and M. Yamaguchi, *Gravitino production from heavy moduli decay and cosmological moduli problem revived*, *Phys. Lett.* **B 638** (2006) 389 [hep-ph/0602081] [INSPIRE].

JCAP10(2015)003