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# LIGHT WATER REACTOR FUEL ANALYSIS CODE FEMAXI．IV（VER．2） <br> －Detalled structure and user＇s Mavual－ 

## November 1997

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Light Water Reactor Fuel Analysis Code<br>FEMAXI-IV(Ver.2)<br>-Detailed Structure and User's Manual-<br>Motoe Suzuki and Hiroaki Saitou*<br>Department of Reactor Safety Research Nuclear Safety Research Center Tokai Research Establishment Japan Atomic Energy Research Institute Tokai-mura, Naka-gun, Ibaraki-ken

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A light water reactor fuel behavior analysis code FEMAXI-IV(Ver.2) was developed as an improved version of FEMAXI-IV.

Development of FEMAXI-IV has been already finished in 1992, though a detailed structure and input manual of the code have not been open to users yet.

Here, the basic theories and structure, the models and numerical solutions applied to FEMAXI-IV(Ver.2), and the material properties adopted in the code are described in detail.

In FEMAXI-IV(Ver.2), programming bugs in previous FEMAXI-IV were eliminated, renewal of the pellet thermal conductivity was performed, and a model of thermal-stress restraint on FP gas release was incorporated.

For facilitation of effective and wide-ranging application of the code, methods of input/output of the code are also described in detail, and sample output is included.

[^0]*CRC Research Institute Inc.,

## 軽水炉燃料解析コード FEMAXI－IV（Ver．2）

一詳細構造とユーザーズマニュアルー

日本原子力研究所東海研究所安全性試験研究センター原子炬安全工学部鈴木 元衛•斉藤 裕明＊
（1997年10月8日受理）

軽水炉燃料のふるまい解析コードFEMAXI－IVの改良バージョンとしてFEMAXI－ IV（Ver．2）を開発した。FEMAXI－IVは，開発が1992年に既に終了しているが，その詳細構造及び入力マニュアルはユーザーに未公開であった。
本報告は，FEMAXI－IV（Ver．2）の基本理論と構造，モデルと数値解法，採用した物性値を詳述したものである。FEMAXI－IV（Ver．2）では，バグフィックスがされ，ベレット熱伝導率 の更新および熱応力による FP 放出抑制モデルの追加がされた。さらに，本コードの有効か つ広範な利用を可能とするため，入出力の種類と方法を詳しく説明し，具体的なサンプル出力を添えた。

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## 1. Introduction

Light water reactors are currently expected to serve as major facilities for nuclear power generation for quite a long period. Therefore it is important to ensure the reliability of fuel rods, and a fuel behavior analysis code is one of the indispensable tools.

Development of a fuel behavior analysis code FEMAXI-IV ${ }^{(1)}$, which is an extended version of FEMAXI-III ${ }^{(2)}$, has been already finished in 1992, though a detailed description of the code has not been open to users yet. FEMAXI-IV has been evaluated for its prediction performance using data from the Battelle High Burnup Experiment Program and Halden Project, etc ${ }^{(1) /(3)-(9)}$.

Thereafter, FEMAXI-IV(ver.2) was developed as an improved version of FEMAXI-IV.
Here, in addition to the explanation of improvements in FEMAXI-IV(ver.2), the present report describes the structure and methods that have been inherited to the ver. 2 as a basic frame from FEMAXI-IV.

### 1.1 Outline of the Code

FEMAXI-IV analyzes the thermal and mechanical behavior of a single fuel rod in the steady and transient states, while accident conditions are not within the scope of analysis of the code. The transient states include power ramp and load-following operation, etc.

In the present Ver. 2 of FEMAXI-IV, facilitation of use has been greatly enhanced by the following improvements and by this manual which describes details of the structure and input/output method.
(1) Bug elimination

Programming bugs have been eliminated throughout the code.

## (2) Pellet material properties

Thermal conductivity of $\mathrm{UO}_{2}$ pellet decreases with burnup. Therefore, we have adopted some representative empirical equations for the burnup dependence of pellet thermal conductivity. In addition, the empirical equations representing densification and swelling of
pellet have been modified, and the hot-press* model has been improved.
(* Shrinkage of a porous pellet caused by static pressure.)
(3) Model of thermal-stress restraint on FP gas release

Upon an increase in the power, thermal stress is generated inside the pellet. Recent findings have revealed that the FP gas release behavior is affected by this stress generation. A model of this phenomenon has been incorporated in the Ver.2.

## (4) Others

Additional input parameters and a function to simulate changes in the gas composition inside the fuel rod have been installed. In addition, the input data format has been improved.

Table 1.1 lists the phenomena analyzed by the code. Material properties adopted in the present code are obtained from as many literatures as available.

MOX fuels and $\mathrm{UO}_{2}$ fuels containing Gd can be analyzed by designating materials properties.

Table 1.1 Phenomena analyzed by FEMAXI-IV.

|  | Thermal process determining <br> temperature distribution | Process with mechanical <br> displacement |
| :---: | :---: | :---: |
| Pellet | Thermal conduction (depending <br> on flux distribution) <br> FP gas release (depending on <br> temperature and burnup level) | Thermal expansion, elasticity, <br> plasticity, creep, cracking, initial <br> relocation, densification, swelling <br> (solid FP, gas bubble), hot-press |
| Cladding | Thermal conduction <br> Thermal expansion, elasticity, <br> plasticity, creep, irradiation growth <br> in the axial direction |  |
| Fuel rod | Gap thermal conduction (mixed <br> gas, contact, radiation), cladding <br> surface heat transfer, gap gas flow | Mechanical interaction between pellet <br> and cladding, friction |

### 1.2 Basic structure

## (1) Whole structure

FEMAXI-IV consists of two parts: one for analyzing the temperature distribution, thermally induced deformation, and FP gas release etc. (hereafter called "thermal analysis part"), and the other for analyzing the mechanical behavior of the fuel rod (hereafter called

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```

"mechanical analysis part"). Figure 1.1 outlines the entire code structure.
In the thermal analysis part, calculation always covers an entire length of a fuel rod. Namely, the temperature distribution is calculated as a one-dimensional axisymmetrical problem in the radial direction, in which the change in gap width between pellet and cladding, FP gas release, gap gas flow in the axial direction, and their feedback effects on gap thermal conduction are analyzed. For analysis of the power distributions in the axial direction, a fuel rod is divided into a maximum of 12 axial segments, and iteration is performed until thermal feedback among these segments converges for the entire length of the rod.

In the mechanical analysis part, users can select either analysis of the entire length of a fuel rod, or analysis of one pellet length. In the former, the axisymmetrical finite element method (FEM) is applied to the entire length of the rod; in the latter, the axisymmetrical FEM is applied to half the pellet length, and mechanical interaction between pellet and cladding is analyzed.

In the mechanical analysis, the magnitude of pellet strain caused by thermal expansion, densification, swelling and relocation is calculated first, and a stiffness equation is formulated with consideration given to cracking, elasticity/plasticity and creep of pellet.

Then, stress and strain of pellet and cladding are calculated by solution of the stiffness equation with boundary conditions corresponding to the pellet-cladding contact mode. When pellet-cladding mechanical interaction occurs and states of pellet-cladding contact change, calculation is re-started with the new boundary conditions of contact from the time when the change occurs.

In the analysis of the entire length of a fuel rod, evaluation is possible for the axial force on a lower axial segment which is in contact with an upper segment. Also, the finite element method used is simplified to reduce the total number of degrees of freedom.

## (2) Method treating the inter-dependency between thermal analysis and mechanical analysis

As stated above, FEMAXI-IV consists of the thermal analysis part and mechanical analysis part. Since temperature and stress/strain and displacement distributions obtained from the two analysis parts physically depend on each other, strictly speaking, simultaneous
equations of thermal conduction and mechanical deformation should be solved.

For example, in order to obtain convergence in the calculation of the temperature distribution of a pellet in the thermal analysis part, it is necessary to introduce the mechanical analysis to predict gap width into the calculation of gap thermal conduction.

Accordingly, introduction of the mechanical analysis into the convergence calculation loop is required. Therefore, a model which can perform the gap width calculation within a short time is desired to facilitate the large number of iterations.

Meanwhile, it is almost impossible to perform detailed stress/strain and displacement analysis, which is the original objective of the mechanical analysis part, within a short time.

To avoid this contradiction, the mechanical analysis part of FEMAXI-IV is divided into two parts. One is a detailed mechanical analysis part which is used for an accurate prediction of stress/strain and displacement distribution, and the other is a simple mechanical analysis part which is developed to solve simultaneous equations of the relationship between temperature and stress/strain required in the thermal analysis part.

These two mechanical analysis parts use common material properties and empirical equations. Results of the analyses are not necessarily identical, but the overall tendencies are quite similar, and the absence of problems which might appear in estimation of temperature, stress/strain, and displacement distribution is confirmed.

The method of the simple mechanical analysis part is explained in section 2.1.3, Contactforce estimation model. The method of the detailed mechanical analysis part is explained in section 2.2, Mechanical Behavior over Entire Length of Fuel Rod (Analysis 1), and in section 2.3, Local Mechanical Behavior (Analysis II).

### 1.3 Features of numerical method and modelling

The main features of the code are as follows.

## (1) FEM element characteristics

Storage region and calculation time are reduced by introduction of rectangular 3-degrees-of-freedom elements into the FEM analysis in order to perform mechanical calculation for the
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entire length of the fuel rod.

## (2) Creep solution

Through use of an implicit procedure, the numerical solution stability for high creep rate is improved.

## (3) Matrix solution

The coefficient matrix of simultaneous equations of the FEM (stiffness equations) is a diagonal symmetrical matrix having a large number of zero elements, as shown in the figure below. Therefore, the skyline method has been adopted to solve the equations, and the memory method of nonzero elements in the matrix, as well as the calculation procedure, has been improved, in order to reduce the size of the storage region and calculation time.

In the skyline method, only the elements under the solid line in the figure below are stored. In the FP gas release model, the procedure has been improved so that the number of computing steps for the matrix becomes a minimum.

(4) Nonequilibrium residue

In order to avoid accumulation of non-equilibrium residue generated at each time step during solution of a nonlinear problem, equilibrium condition equations are formulated not in an incremental manner but in a form which maintains the total balance of loads and stresses.
(5) Contact problem

Three contact states are dealt with as the contact conditions between pellet and cladding: open gap state, clogged gap state and sliding state. In the FEM, contact conditions at each
node pair of pellet and cladding are determined, and the boundary conditions are set in accordance with the conditions.

## (6) Behavior of cracked pellet

Cracking of a pellet is modeled using a decreased stiffness approximation method, similar to the case for FEMAXI-III. In order to describe behavior of the cracked pellet which is relocated under PCI, recovery of the stiffness during compression is expressed as a function of the amount of relocation.

## (7) FP gas release model

An equivalent sphere model is adopted to simulate the FP gas release. This model allows prediction outside the range of experimental data, which cannot be obtained by an empirical model.
(8) Gap gas diffusion-flow model

Gap gas-diffusion flow is modeled, and effects of the released FP gas on gap thermal conductance are carefully evaluated.
(9) Nonsteady phenomena analysis

The fuel behavior in a nonsteady state can be analyzed by mechanistic treatment of a nonsteady heat transfer model, gap gas flow model and FP gas release model. Also, the accuracy of prediction is improved and calculation time is reduced through use of independent time-step controls in each model.
(10) Simplification of calculation

In the FP gas release model, when the same type of calculations are performed both in a low-temperature region and a high-temperature region, calculation results obtained for elements in one region are used for calculation in another region in order to avoid carrying out similar calculations twice. Also, physical properties and other values which are frequently referred to are stored in a data table, and use of special mathematical functions is avoided.

By means of the above-mentioned procedures, FEMAXI-IV can give highly accurate solutions within a shorter calculation time.


Fig. 1.1 Entire code structure of FEMAXI-IV

## 2. Analytical Theory and Functions

In this chapter, analytical theory and functions used in FEMAXI-IV are explained. The thermal analysis part is explained in section 2.1, the mechanical analysis part for the entire length of a fuel rod is explained in section 2.2 , and the local mechanical analysis part is explained in section 2.3. Materials properties are described in section 2.4.

### 2.1 Thermal Behavior

In the thermal analysis part, temperature distribution of a fuel rod is calculated with the boundary condition determined by coolant temperatures. The basic assumption and calculation procedure are as follows.
(1) The temperature and state of coolant at every axial segment at current time step are calculated from the inlet temperature, inlet pressure, flow velocity, and heat flux from a fuel rod, independently from the coolant state progress by the former time step. While, in a strict sense, this method can hold only when fuel rod and coolant are in a steady state relationship, FEMAXI-IV applies this method not only to the steady state, but also to such transient states as power ramp and load following operation, because these transients are substantially slow enough to be approximated with a steady state model.
(2) Specifically, coolant temperature at each axial segment is calculated from the coolant temperature at the lower adjacent segment and the coolant temperature rise which is given by the thermal power, i.e. heat flux, generated at the lower segment. This calculation begins with the inlet coolant temperature. Thus, the coolant temperature distribution in the axial direction is determined.
(3) Cladding surface temperature is calculated by the cladding surface heat transfer model using the coolant temperature as a starting point.
(4) The temperature distribution in the area between the center of the pellet and the cladding surface is calculated using a one-dimensional finite difference method in the radial direction, with the results of (3) as boundary conditions.
(5) Axial heat conduction of a fuel rod is neglected. Heat conduction caused by the axial power difference of the rod is substantially limited by such thermal resisitance as dish or gap in the pellet end surface, so that axial temperature gradient is much smaller in comparison with the radial gradient inside the pellet.

The above-mentioned methods will be explained in section 2.1.1. Such models determining temperature distribution in the radial direction, as a gap thermal conduction model, contact force model and FP gas release model, will be described in sections 2.1.2, 2.1.3, and 2.1.4, respectively.

### 2.1.1 Temperature distribution

(1) Fuel rod surface heat transfer model
(1)-1 Assumptions and methods

Enthalpy is used as a primary variable in the calculation of the coolant temperature distribution, taking into consideration the phase change of water. Calculation is performed in terms of either single-phase flow (subcooled water) or two-phase flow (nucleate boiling state). The basic assumptions and methods are:
(1) Regarding the increase in coolant enthalpy, a steady-state model is applied in accordance with the above assumption(1). Here, it is not required that inlet temperature and flow velocity be uniform throughout the analysis period, but they can be input as timedependent variables.
(2) State variables are calculated by interpolation from data obtained from the simplified steam table which is incorporated in the code.
(3) Pressure and mass flow rate are assumed to be constant in the axial direction. Slip between steam and water is assumed to be zero.

## (1)-2 Enthalpy of the coolant

In the system defined as shown in Fig. 2.1 based on the above assumptions, enthalpy of the coolant (water or steam) is sequentially obtained using the equation below, starting from the inlet.

$$
\begin{equation*}
h_{n+1}-h_{n}=\frac{2 \pi r \overline{\phi_{n}} l_{n}}{G S} \tag{2.1.1}
\end{equation*}
$$

Here,
$h_{n}$ : specific enthalpy of node $\mathrm{n}(\mathrm{J} / \mathrm{kg})$
$r$ : outer radius of fuel rod (m)
$l_{n}$ : length of axial segment $\mathrm{n}(\mathrm{m})$
$G:$ mass flow rate $(=\rho \mathrm{v}) \quad\left(\mathrm{kg} / \mathrm{m}^{2} \cdot \mathrm{~s}\right)$
$S$ : flow area (cross-sectional area of channel) $\left(\mathrm{m}^{2}\right)$
$\overline{\phi_{n}}$ : heat flux of axial segment $\mathrm{n}\left(\mathrm{J} / \mathrm{m}^{2} \cdot \mathrm{~s}\right)$.


Fig. 2.1 Model system.
A flowchart of the calculation is shown in Fig. 2.2, where 'representative entahlpy of each segment' is the average value of the two enthalpies at upper and lower nodes of one segment.


Fig. 2.2 Calculation flowchart.
(1)-3 Calculation of state quantities using the steam table

State quantities required in the calculation described in (1)-2 and in the heat transfer
calculation to be described in (1)-4 are specific enthalpy, specific volume, viscosity coefficient, heat transfer coefficient, and Prandtl number.

Regarding the coolant states in FEMAXI-IV, subcooled water and a two-phase region close to liquid phase are considered. The latter is indicated by hatched area of Fig.2.3

The calculation method is explained below, where $T$ is temperature, $P$ is pressure and $h$ is enthalpy.


Fig. 2.3 Relationship among status of coolant water.

## [1] Enthalpy and temperature

The enthalpy of the subcooled water depends weakly on pressure, but changes significantly with substantial change in pressure. Therefore, in the table showing $h(P, T)$ in subcooled regions, data are obtained for a large pressure interval of 30 atm, and used for interpolation as follows.
(1) Calculation of inlet enthalpy $h$ from $T$ and $P$

1) Determination of the state

First, saturation temperature $T_{s}$ is obtained by interpolation from data in a $T_{s}(P)$ diagram in terms of coolant pressure, and it is compared with water temperature $T$. Here, the $T_{s}(P)$ diagram is constructed for the pressure range of 1 bar to 180 bar.
2) Calculation of enthalpy
a. In the case of $T<T_{s}$ (subcooled water)

Using the $h(P, T)$ table ( $T: 20^{\circ} \mathrm{C}, P: 30 \mathrm{~atm}$ intervals), $h$ is obtained by interpolation from the first constant pressure datum which is higher than the coolant pressure at $T$ (interpolation is not performed in terms of pressure).

$$
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$$

b. In the case of $T=T_{s}$ (two-phase state, within an allowable range of $T_{s} \pm 0.1^{\circ} \mathrm{C}$ )

Even though this is a two-phase state, the enthalpy of the saturated water in the water phase is assumed to be $h=h_{f}$.
c. In the case of $T>T_{s}$ (overheated steam)

Overheated steam is not in the analysis range of FEMAXI-IV. When $T>T_{s}+0.1^{\circ} \mathrm{C}$, execution of the program is terminated.
(2) Calculation of $T$ from $P$ and $h$ (calculation of representative temperature of each segment)

After the enthalpy of each axial elevation is obtained using eq. (2.1.1), a representative enthalpy $h$ of axial segment $n$ is obtained as $h=\frac{1}{2}\left(h_{n}+h_{n+1}\right)$.

## 1) Determination of the state

Enthalpies of saturated water $h_{f}$ and saturated steam $h_{g}$ are obtained by interpolation from data in $h_{\mathcal{A}}(P)$ and $h_{g}(P)$ diagrams in terms of pressure, respectively. Here, $h_{\mathcal{A}}(P)$ and $h_{g}(P)$ diagrams have a pressure range of 1 to 180 bar.
2) Determination of $T$
a. In the case of $h \leqq h_{f}$

In the $h(P, T)$ table ( $T: 20^{\circ} \mathrm{C}, P: 30 \mathrm{~atm}$ intervals), $T$ is obtained by interpolation from the enthalpy datum for the $P_{l}$-row pressure which is the first value higher than $P$ (interpolation is not performed in terms of pressure).
b. In the case of $h_{f}<h<h_{g}$ (two-phase region)

Water-phase temperature is adopted and $T=T_{s}$ is assumed.

## [2] Other state variables

In FEMAXI-IV, density, viscosity coefficient, thermal conductivity and Prandtl number of water are used only in the Dittus-Boelter equation ${ }^{(10)}$. Since these quantities do not depend much on pressure, they are determined using data from the tables of $\rho_{S}(T), \mu_{S}(T), k_{S}$ (t) and $\operatorname{Pr}_{\mathrm{S}}(T)$ for saturated water. Data in these tables are obtained at $10^{\circ} \mathrm{C}$ intervals in terms of $T$.

Figures 2.4 through 2.10 show a $H_{S}(P)$ diagram, $T_{S}(P)$ diagram, and $h(P, T)$ diagram,
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and density, viscosity coefficient, thermal conductivity and Prandtl number of water, respectively. In these diagrams, data represented by open triangles $(\triangle)$ correspond to data in the table of material properties incorporated in FEMAXI-IV.


Fig. 2.4 $H_{5}(P)$ Diagram.


Fig. 2.5 $\quad T_{5}(P)$ Diagram.


Fig. $2.6 h(P, T)$ Diagram.


Fig. 2.7 Density of water.


Fig. 2.8 Viscosity coefficient of water.

$$
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$$



Fig. 2.9 Thermal conductivity of water.


Fig. 2.10 Prandtl number of water.
(1)-4 Cladding surface temperature (heat transfer model)

In FEMAXI-IV, the following equation is obtained from the heat transfer differential equation for the fuel (see item (3)).

$$
\begin{equation*}
\phi_{N}=A T_{N}+B \tag{2.1.2}
\end{equation*}
$$

Here,
$\phi_{N}$ : cladding surface heat flux ( $\mathrm{W} / \mathrm{m}^{2}$ )
$T_{N}$ : cladding surface temperature (K)
$N$ : mesh-point number of the cladding surface
$A, B$ : coefficients obtained from heat transfer differential equation.

Surface temperature $T_{N}$ can be obtained from eq. (2.1.2), the Dittus-Boelter equation ${ }^{(10)}$ regarding the cladding surface heat transfer coefficient (see item (1)-5) and the Jens-Lottes equation ${ }^{(11)}$ (see (1)-5). A method of obtaining $T_{N}$ for each state of the coolant is described below.
[1] Subcooled state 1 (cladding surface temperature $<$ saturation temperature)
In this case, the Dittus-Boelter equation shown as eq. (2.1.14) is used. When the coolant temperature is $T_{B}$, heat flux of the cladding surface is obtained as:

$$
\begin{equation*}
\phi_{N}=h_{W}\left(T_{N}-T_{B}\right) \tag{2.1.3}
\end{equation*}
$$

Here,
$\phi_{N}$ : cladding surface heat flux ( $\mathrm{W} / \mathrm{m}^{2}$ )
$h_{W}$ : heat transfer coefficient obtained by the Dittus-Boelter equation
$T_{N} \quad$ : cladding surface temperature (K)
$T_{B} \quad$ : coolant temperature (K).
$T_{N}$ is obtained by eliminating $\phi_{N}$ from eqs. (2.1.2) and (2.1.3).
[2] Subcooled state 2 (cladding surface temperature $>$ saturation temperature)
$T_{N}$ is obtained by simultaneously solving the heat transfer equation for subcooled water and the heat transfer equation for the two-phase state. Cladding surface heat flux $\phi_{N}$ can be obtained as the sum of the heat flux $\phi_{N 1}$ of the subcooled state heat transfer and $\phi_{N 2}$ of the two-phase state heat transfer,

$$
\begin{equation*}
\phi_{N}=\phi_{N 1}+\phi_{N 2} . \tag{2.1.4}
\end{equation*}
$$

Heat flux $\phi_{\mathrm{N} 1}$ of the subcooled state can be expressed as follows, using the heat transfer coefficient $h_{W 1}$ obtained from the Dittus-Boelter equation (eq. (2.1.14)).

$$
\begin{equation*}
\phi_{N 1}=h_{W 1}\left(T_{N}-T_{B}\right) \tag{2.1.5}
\end{equation*}
$$

Similarly, heat flux $\phi_{N 2}$ of the two-phase state can be expressed using the Jens-Lottes equation shown as eq. (2.1.15). Here, in eq. (2.1.15), heat transfer coefficient $h_{W 2}$ is given as a function of $\phi_{N 2}$. Accordingly, when eq. (2.1.15) is simply expressed as $h_{w_{2}}=\alpha^{*} \phi_{N 2}^{3 / 4}$,
the term $\phi_{N 2}$ can be expressed as

$$
\begin{align*}
\phi_{N 2} & =h_{W 2}\left(T_{N}-T_{s}\right) \\
& =\alpha^{*} \phi_{N 2}^{3 / 4}\left(T_{N}-T_{S}\right) . \tag{2.1.6}
\end{align*}
$$

Solving this equation in terms of $\phi$ using

$$
\begin{aligned}
& \phi_{N 2}^{1 / 4}=\alpha^{\cdot}\left(T_{N}-T_{S}\right) \\
& \phi_{N 2}=\alpha^{.4}\left(T_{N}-T_{S}\right)^{4},
\end{aligned}
$$

we obtain

$$
\begin{equation*}
\phi_{N 2}=\alpha\left(T_{N}-T_{S}\right)^{4}, \quad \alpha=\alpha^{*} \tag{2.1.7}
\end{equation*}
$$

By substituting eqs. (2.1.5) and (2.1.6) into eq. (2.1.4), the following equation for $T_{N}$ is obtained.

$$
\begin{equation*}
A T_{N}+B=h_{W 1}\left(T_{N}-T_{B}\right)+\alpha\left(T_{N}-T_{S}\right)^{4} \tag{2.1.8}
\end{equation*}
$$

In FEMAXI-IV, eq. (2.1.8) is converted to be solved by Newton's method.
Terms in eq. (2.1.8) are transpositioned as

$$
\left(A-h_{W 1}\right) T_{N}+B+h_{W 1} T_{B}=\alpha\left(T_{N}-T_{S}\right)^{4}
$$

Here, $\widetilde{T}=T_{N}-T_{S}, T_{N}=\widetilde{T}+T_{S}$, and the following equations hold.

$$
\begin{align*}
& \left(A-h_{W_{1}}\right)\left(\widetilde{T}+T_{S}\right)+B+h_{W 1} T_{B}=\alpha \widetilde{T}^{4}  \tag{2.1.9}\\
& \left(A-h_{W 1}\right) \widetilde{T}+\left(A-h_{W 1}\right) T_{S}+B+h_{W 1} T_{B}=\alpha \widetilde{T}^{4}
\end{align*}
$$

By setting

$$
\begin{equation*}
a=\left(A-h_{W 1}\right) / \alpha, \quad b=\left\{\left(A-h_{W 1}\right) T_{S}+B+h_{w 1} T_{B}\right\} / \alpha \tag{2.1.10}
\end{equation*}
$$

the equation for $\widetilde{T}$ holds as follows.

$$
\begin{equation*}
a \widetilde{T}+b=\widetilde{T}^{4} \tag{2.1.11}
\end{equation*}
$$

By solving this equation to obtain $\widetilde{T}$ using Newton's method and substituting the result into

$$
\begin{equation*}
T_{N}=\widetilde{T}+T_{S} \tag{2.1.12}
\end{equation*}
$$

$T_{N}$ is obtained.

## [3] Two-phase state

Since the coolant temperature is saturated in the two-phase state, using the heat transfer coefficient $h_{W}$ of the Jens-Lottes eq. (2.1.14), the following equation holds.

$$
\begin{equation*}
\phi_{N}=h_{W}\left(T_{N}-T_{S}\right) \tag{2.1.13}
\end{equation*}
$$

Here,
$\phi_{N}$ : cladding surface heat flux ( $\mathrm{W} / \mathrm{m}^{2}$ )
$h_{W}$ : heat transfer coefficient obtained from the Jens-Lottes equation (W/m $\left.{ }^{2} \cdot \mathrm{~K}\right)$
$T_{N}$ : cladding surface temperature (K)
$T_{S}:$ saturation temperature (K).
$T_{N}$ is obtained by eliminating $\phi_{N}$ from eqs. (2.1.2) and (2.1.13).
(1)-5 Cladding surface heat transfer coefficient

Dittus-Boelter equation ${ }^{(10)}$

$$
\begin{equation*}
h_{W}=0.023 \frac{k}{D_{e}}\left(\frac{D_{e} V \rho}{\mu}\right)^{0.2} \operatorname{Pr}^{0.4} \tag{2.1.14}
\end{equation*}
$$

$k \quad: \quad$ coolant water thermal conductivity $(\mathrm{W} / \mathrm{m} \cdot \mathrm{K})$
$D_{e} \quad$ : equivalent diameter (m)
$V$ : coolant water velocity ( $\mathrm{m} / \mathrm{s}$ )
$\rho:$ coolant water density $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$
$\mu \quad:$ coolant water viscosity $(\mathrm{kg} / \mathrm{m} \cdot \mathrm{s})$
$\operatorname{Pr}$ : Prandtl number
The equivalent diameter $D_{e}$ will be explained in section (1)-7.

## Jens-Lottes empirical equation ${ }^{(11)}$

$$
\begin{equation*}
h_{W^{\prime}}=0.1263 \cdot \exp \left(\frac{P_{W}}{6.201 \times 10^{6}}\right) \phi_{N}^{0.75} \tag{2.1.15}
\end{equation*}
$$

$h_{W^{\prime}}:$ surface heat transfer coefficient $\left(\mathrm{W} / \mathrm{cm}^{2} \cdot \mathrm{~K}\right)$
$P_{W}$ : coolant water pressure $\left(\mathrm{N} / \mathrm{m}^{2}\right)$
$\phi_{N}$ : cladding outer surface heat flux $\left(\mathrm{W} / \mathrm{cm}^{2}\right)$

Fitting parameter AKFAC
The cladding surface heat transfer coefficient is adjusted using the following equation. $h_{w}=h_{w} \times$ AKFAC
(1)-6 Flowchart of the heat transfer analysis:


Fig. 2.11 Flowchart of the heat transfer analysis

## (1)-7 Equivalent diameter and cross-sectional area of flow channel

Equivalent diameter and cross-sectional area of the coolant flow channel are the parameters required for obtaining cladding surface temperature. The equivalent diameter $D_{e}$ is the diameter of a virtual column when the shape of a coolant channel around the fuel rod is converted to a column. $\quad D_{e}$ is used in eq. (2.1.14) to determine the cladding surface heat transfer coefficient, and the cross-sectional area of the channel is used in eq. (2.1.1) to calculate the enthalpy of each axial node.

Usually these two parameters are directly set by input; in the case that one of them is not set or none of them is set, a method of converting one value to the other or of calculating both values using the pitch between fuel rods is incorporated in FEMAXI-IV. These methods are explained below.
[1] Equivalent diameter of the channel

1) When $D_{e}$ is specified by input data, the input value is used.
2) When $D_{e}$ is not input but the cross-sectional area of the channel is input, $D_{e}$ is obtained
using

$$
\begin{equation*}
D_{e}=\frac{4 S}{2 \pi \bar{r}}, \tag{2.1.16}
\end{equation*}
$$

where
$S:$ cross-sectional area of the channel,
$\bar{r} \quad:$ fuel rod outer radius.
3) When neither the equivalent diameter $D_{e}$ nor the cross-sectional area $S$ is input, these values are calculated using the pitch between fuel rods. Assuming channel (3) in Fig. 2.12, $S$ is given by

$$
\begin{equation*}
S=4 l^{2}-\pi \bar{r}^{2}, \tag{2.1.17}
\end{equation*}
$$

where $l$ is half of the pitch between fuel rods.
$D_{e}$ is calculated using eq. (2.1.16) after obtaining $S$.
[2] Cross-sectional area of the channel, $S$

1) When $S$ is specified by input data, the input value is used.
2) When $S$ is not input but $D_{e}$ is input, $S$ is obtained using the following equation.

$$
\begin{equation*}
S=\frac{2 \pi \bar{r} D_{t}}{4} \tag{2.1.18}
\end{equation*}
$$



Fig. 2.12 Channel model.
3) When neither $D_{e}$ nor $S$ is input, $S$ is calculated from eq. (2.1.17) using the pitch between fuel rods.

| Input values |
| :---: |
| Cross-sectional area of the channel, equivalent diameter |
| of the channel and pitch between fuel rods are input |
| as the following variables. |
| PITCH $\cdots$ Pitch between fuel rods (cm) |
| FAREA $\cdots$ Cross-sectional area of the channel $\left(\mathrm{cm}^{2}\right)$ |
| DE $\quad \cdots$ Equivalent diameter of the channel (cm) |

## (2) One-dimensional radial-direction temperature model

In the analysis of radial temperature gradient at each axial segment, one-dimensional radial-direction thermal conduction equations are used, while the thermal conduction in the axial direction is neglected. It is assumed that the thermal properties of the fuel at each mesh are dependent on temperature, and that the gap heat transfer coefficient and cladding surface temperature change at each axial segment. The radial mesh divisions are the same
as those used in the mechanical analysis I. (See section 2.2, Figs.2.29 and 2.31) Based on these assumptions, thermal conduction is described as follows.

$$
\begin{equation*}
\frac{\partial}{\partial t}\left[c_{v}(T, r) T(r, t)\right]=\nabla k(T, r) \cdot \nabla T(r, t)+q(r, t) \tag{2.1.19}
\end{equation*}
$$

Here,

$$
\begin{aligned}
T & : \text { temperature }(\mathrm{K}) \\
r & : \text { coordinate in the radial direction }(\mathrm{m}) \\
t & : \text { time }(\mathrm{s}) \\
C_{v} & : \text { volume specific heat }\left(\mathrm{J} / \mathrm{m}^{3}\right) \\
k & : \text { thermal conductivity }(\mathrm{W} / \mathrm{m} \cdot \mathrm{~K}) \\
q & : \text { heat generation per unit volume }\left(\mathrm{J} / \mathrm{m}^{3} \cdot \mathrm{~s}\right) .
\end{aligned}
$$



Fig. 2.13 Mesh model.

Volume integration is performed with eq. (2.1.19). Here, the volume to be integrated is the volume enclosed by the dotted lines in Fig. 2.13.

$$
\begin{equation*}
\iiint_{1} \frac{\partial}{\partial \partial} C_{v}(T, r) T(r, t) d V=\iiint_{V} \nabla k(T, r) \cdot \nabla T(r, t) d V+\iiint_{i^{\prime}} q(r, t) d V \tag{2.1.20}
\end{equation*}
$$

Since this is a one-dimensional problem, dimensions of the volume are set as 1 except for the radial direction. Eliminating the common factor $2 \pi$ and using the forward finite difference method for time differentiation, the first term of eq. (2.1.20) is expressed as

$$
\begin{align*}
& \iiint_{V} \frac{\partial}{\partial}\left[C_{v}(T, r) T(r, t)\right] d V \approx \iiint_{V} C_{v}(T, r) \frac{\partial T}{\partial t}(r, t) d V \\
& \approx \frac{\left(T_{n}^{m+1}-T_{n}^{m}\right)}{h_{p n}}\left[C_{v, p n} \frac{h_{p n}}{2}\left(r_{n}-\frac{h_{p n}}{4}\right)+C_{v, s n} \frac{h_{\mathrm{sn}}}{2}\left(r_{n}+\frac{h_{s n}}{4}\right)\right] \tag{2.1.21}
\end{align*}
$$

where $T_{n}{ }^{m}$ is the temperature at coordinate $r_{n}$ and time $t_{m}$, and $T_{n}{ }^{m+1}$ is the temperature at coordinate $r_{n}$ and time $t_{m+l}$. The second term of eq. (2.1.20) is expressed as

$$
\begin{align*}
& \iiint_{V} \nabla k(T, r) \cdot \nabla T(r, t) d V=\iint_{s} k(T, r) \nabla T(r, t) \cdot d \bar{S} \\
& \approx-\frac{k_{p n}\left(T_{n}^{m+1 / 2}-T_{n-1}^{m+1 / 2}\right)}{h_{p n}}\left(r_{n}-\frac{h_{p n}}{2}\right)+\frac{k_{s n}\left(T_{n+1}^{m+1 / 2}-T_{n}^{m+1 / 2}\right)}{h_{s n}}\left(r_{n}+\frac{h_{\mathrm{s} n}}{2}\right) . \tag{2.1.22}
\end{align*}
$$

Here, continuous conditions of the heat flux at the inner boundary are used for evaluation of the plane integration along the boundary surface.

The following terms are defined.

$$
\begin{gather*}
h_{p n}^{V}=\frac{h_{p n}}{2}\left(r_{n}-\frac{h_{p n}}{4}\right), \quad h_{s n}^{V}=\left(r_{n}+\frac{h_{s n}}{4}\right) \\
h_{p n}^{s}=\frac{1}{h_{p n}}\left(r_{n}-\frac{h_{p n}}{2}\right), \quad h_{s n}^{s}=\frac{1}{h_{s n}}\left(r_{n}+\frac{h_{s n}}{2}\right)  \tag{2.1.23}\\
D_{n}=C_{v, p n} h_{p n}^{V}+C_{v, s h} h_{s n}^{V}
\end{gather*}
$$

Then the heat generation term $q(r, t)$ of the third term in eq. (2.1.20) is separated with variables as

$$
q(r, t)=Q(r) P_{f} P(t)
$$

Here, $Q(r)$ is the relative power distribution in the radial direction, $P_{f}$ is the standard value of the heat generation density, and $P(t)$ is the relative change against time. Then the third term of eq. (2.1.20) is expressed as

$$
\begin{equation*}
\iiint_{V} q(r, t) d V \approx\left(Q_{p n} h_{p n}^{\prime}+Q_{s h} h_{s n}^{V}\right) P_{f} P\left(t_{m+1 / 2}\right) \tag{2.1.24}
\end{equation*}
$$

By adding the right sides of eqs.(2.1.21), (2.1.22) and (2.1.24) which are approximate expressions of the terms in eq.(2.1.20), eq.(2.1.20) is converted into the difference approximation equation for the $n$th mesh point as follows.

$$
\begin{align*}
\frac{\left(T_{m+1}-T_{n}^{n}\right) D_{n}}{\Delta t} & =-\left(T_{n}^{m+\frac{1}{2}}-T_{n-1}^{m+\frac{1}{2}}\right) k_{p n} h_{p n}^{\ulcorner }+\left(T_{n+1}^{m+\frac{1}{2}}-T_{n}^{m+\frac{1}{2}}\right) k_{s n} h_{s n}^{s}  \tag{2.1.25}\\
& +\left(Q_{p n} h_{p n}^{r}+Q_{s n} h_{s n}^{\prime}\right) P_{f} P\left(t_{n+\frac{1}{2}}\right)
\end{align*}
$$

Upon application of the Crank-Nicholson method to eq. (2.1.25), the following equation holds.

$$
\begin{align*}
\frac{\left(T_{n}^{m+1}-T_{n}^{m}\right) D_{n}}{\Delta t} & =\left(\frac{\left(T_{n}^{m+1}+T_{n}^{m}\right)}{2}-\frac{\left(T_{n-1}^{m+1}+T_{n-1}^{m}\right)}{2}\right) k_{p n} h_{p n}^{s} \\
& +\left(\frac{T_{n+1}^{m+1}+T_{n+1}^{m}}{2}-\frac{T_{n}^{m+1}+T_{n}^{m}}{2}\right) k_{v n} h_{v n}^{s}  \tag{2.1.26}\\
& +\left(Q_{\Gamma n} h_{r n}^{r}+Q_{v n} h_{s n}^{v}\right) P_{f} \frac{P\left(t_{m+1}\right)+P\left(t_{m}\right)}{2}
\end{align*}
$$

Here, $T^{m+1}$ and $T^{m}$ are obtained using the average temperature at mesh points $n-1$ and $n$, as well as the average temperature at mesh points $n$ and $n+1$.

Through modification of eq. (2.1.26), the differential equation at mesh point $n$ in the medium region is given as

$$
a_{n} T_{n-1}^{m+1}+b_{n} T_{n}^{m+1}+c_{n} T_{n+1}^{m+1}=d_{n}^{m},
$$

where

$$
\begin{align*}
& a_{n}=-\frac{k_{p n} h_{p n}^{s} \Delta t}{2}, \quad c_{n}=-\frac{k_{\mathrm{v}} h_{\mathrm{s} n}^{s} \Delta t}{2} \\
& b_{n}=D_{n}-a_{n}-c_{n} \\
& d_{n}^{m}=-a_{n} T_{n-1}^{m}+\left(D_{n}+a_{n}+c_{n}\right) T_{n}^{m}-c_{n} T_{n+1}^{m}  \tag{2.1.27}\\
& \quad+\Delta t\left(Q_{P n} h_{r n}^{r}+Q_{v n} h_{v n}^{r}\right) P_{t}\left\{\frac{P\left(t_{m+1}\right)+P\left(t_{m}\right)}{2}\right\} .
\end{align*}
$$

The gap region is shown in Fig. 2.14.


Fig. 2.14 Gap thermal conductance model.

For the gap region, the following equations hold by means of difference approximation, as in the case of eq. (2.1.25).

$$
\begin{align*}
\frac{\left(T_{n}^{m+1}-T_{n}^{m}\right) D_{n}^{\prime}}{\Delta t}= & -\left(T_{n}^{m+\frac{1}{2}}-T_{n-1}^{m+\frac{1}{2}}\right) k_{p n} h_{p n}^{s}+\left(T_{n+1}^{m+\frac{1}{2}}-T_{n}^{m+\frac{1}{2}}\right) h_{\mathrm{g}}  \tag{2.1.28}\\
& +Q_{p n} h_{P n}^{\Gamma} P_{f} P\left(t_{m+\frac{1}{2}}\right) \\
\frac{\left(T_{n+1}^{m+1}-T_{n+1}^{m}\right) D_{n+1}^{\prime \prime}}{\Delta t}= & -\left(T_{n+1}^{m+\frac{1}{2}}-T_{n}^{m+\frac{1}{2}}\right) h_{g}+\left(T_{n+2}^{m+\frac{1}{2}}-T_{n+1}^{m+\frac{1}{2}}\right) k_{s, n+1} h_{s, n+1}^{s}  \tag{2.1.29}\\
& +Q_{s, n+1} P_{f} P\left(t_{m+\frac{1}{2}}\right)
\end{align*}
$$

Here, $D_{n}^{\prime}=C_{v, p h} h_{p n}^{V}, D_{n+1}^{\prime \prime}=C_{v, s, n+1} h_{s, n+1}^{r}$, and $h_{g}$ is gap thermal conductance. The center region of the fuel rod is shown in Fig. 2.15, and the cladding surface region is shown in Fig. 2.16.


Fig. 2.15 Fuel rod center model.

For the center of the fuel rod, eq. (2.1.20) is transformed by the difference approximation as follows.

$$
\begin{equation*}
\frac{\left(T_{0}^{m+1}-T_{0}^{m}\right)}{\Delta t} C_{v, s 0}=\left(T_{1}^{m+\frac{1}{2}}-T_{0}^{m+\frac{1}{2}}\right) k_{s 0} h_{s 0}^{s}+Q_{s 0} h_{s 0}^{r} P_{f} P\left(t_{m+\frac{1}{2}}\right) \tag{2.1.30}
\end{equation*}
$$

The boundary equation for the cladding surface region is

$$
\begin{equation*}
\frac{\left(T_{n}^{m+1}-T_{n}^{m}\right)}{\Delta t} C_{v, p h} h_{p n}^{r}=-\left(T_{n}^{m+\frac{1}{2}}-T_{n-1}^{m+\frac{1}{2}}\right) k_{p n} h_{p n}^{s}-r_{n} \phi_{n}+Q_{p n} h_{p n}^{v} P_{f} P\left(t_{m+\frac{1}{2}}\right) . \tag{2.1.31}
\end{equation*}
$$

The difference approximation equation (2.1.31) is expressed as

$$
\begin{equation*}
a_{n} T_{n-1}^{m+1}+b_{n} T_{n}^{m+1}=d_{n} \tag{2.1.32}
\end{equation*}
$$

Then the coefficients $a_{n}, b_{n}$ and $d_{n}$ are given as

$$
\begin{align*}
a_{n}= & -\frac{k_{p n} h_{p n}^{s} \Delta t}{2}  \tag{2.1.33}\\
b_{n}= & C_{v, p n} h_{p n}^{V}-a_{n}  \tag{2.1.34}\\
d_{n}= & -a_{n} T_{n-1}^{m}+\left(C_{V, p n} h_{p n}^{V}-a_{n}\right) T_{n}^{m} \\
& -\Delta t r_{n}\left(\frac{\phi_{n}^{m+1}+\phi_{n}^{m}}{2}\right)+\Delta t Q_{p n} h_{p n}^{V} P_{f}\left\{\frac{P\left(t_{m+1}\right)+P\left(t_{m}\right)}{2}\right\}  \tag{2.1.35}\\
= & d_{n}^{\prime}+d_{n}^{\prime \prime} \phi_{n}^{m+1} .
\end{align*}
$$

Here, $\phi_{n}$ is the cladding surface heat flux.
Heat flux $\phi_{n}{ }^{m}$ at time $t_{m}$ in eq. (2.1.35) is given as follows in the steady-state calculation.

$$
\begin{equation*}
\phi_{n}{ }^{m}=q^{m} / 2 \pi r_{n} \tag{2.1.36}
\end{equation*}
$$

where

$$
q: \text { linear heat rate }(\mathrm{W} / \mathrm{m}) .
$$

This equation is used to avoid that difference errors generated by remeshing are accumulated in the calculated heat flux.
Now, unknown variables in eqs.(2.1.32) to (2.1.35) are $T_{n-1}^{m+1}, T_{n}^{m+1}$ and $\phi^{m+1}$.
Next, using coefficients expressed as $E$ and $F$, which are obtained using the forward elimination of the Gaussian elimination method starting from the first point to the $(n+1)$ th point, the following equation is derived.

$$
\begin{equation*}
T_{n-1}^{m+1}=-E_{n-1} T_{n}^{m+1}+F_{n-1} \tag{2.1.37}
\end{equation*}
$$

By substituting eqs.(2.1.33) to (2.1.35) and (2.1.37) into eq. (2.1.32), we obtain

$$
\begin{equation*}
A_{1} T_{n}^{m+1}+B_{1}=\phi^{m+1} \tag{2.1.38}
\end{equation*}
$$

where

$$
\begin{align*}
& A_{1}=\left(b_{n}-a_{n} E_{n-1}\right) / d_{n}^{\prime \prime}  \tag{2.1.39}\\
& B_{1}=\left(a_{n} F_{n-1}-d_{n}^{\prime}\right) / d_{n}^{\prime \prime} \tag{2.1.40}
\end{align*}
$$

Therefore, $A_{1}$ and $B_{1}$ are known values.

However, eq. (2.1.38) is equal to eq. (2.1.2), and $A$ and $B$ in eq. (2.1.2) are known values; thus $T_{n}^{m+1}$ is obtained as described in section (1)-4.

Therefore, using the backward substitution of the Gaussian elimination method, $T^{m+1}$ is sequentially obtained.

Two methods are available for designating the distribution function $Q(r)$. One is to designate it by input as a function of burnup, and the other is to use the Robertson formula (Halden experimental equation) ${ }^{(12)}$ which is incorporated in the code.

$$
\begin{equation*}
Q_{1}(R)=I_{0}(k \cdot R)+\frac{I_{1}\left(k \cdot R_{1}\right)}{K_{1}\left(k \cdot R_{1}\right)} \cdot K_{0}(k \cdot R) \tag{2.1.41}
\end{equation*}
$$

Here,

$$
\begin{array}{lll}
I & : & \text { first transformed Bessel function } \\
R_{\mathrm{I}} & : & \text { pellet center hole radius } \\
K & : & \text { second transformed Bessel function } \\
R & : & \text { radial coordinate in pellet } \\
k & : & \text { Inverse of the neutron diffusion distance }\left(\mathrm{cm}^{-1}\right) .
\end{array}
$$

Here, $\quad k$ is calculated using

$$
\begin{equation*}
k=0.328(E \cdot D)^{0.8}+0.54\left(\frac{0.5}{R_{p}}\right)^{0.82} \cdot(E \cdot D)^{0.19} \tag{2.1.42}
\end{equation*}
$$

where

$$
\begin{aligned}
E & :{ }^{235} \mathrm{U} \text { enrichment }(\%) \\
D & : \text { pellet theoretical density ratio }(-) \\
R_{p} & : \text { pellet diameter (cm). }
\end{aligned}
$$

The distribution function (2.1.41) can be approximated by the following function :

$$
\begin{equation*}
Q_{2}(r)=\frac{(b+2)\left(1-h^{2}\right)\left[(1-a) r^{b}+\left(a-h^{b}\right)\right]}{b\left(1-h^{2}\right)\left(a-h^{b}\right)+2\left(1-h^{b}\right)\left(1-a h^{2}\right)} \tag{2.1.43}
\end{equation*}
$$

where
$r$ : normalized pellet radius $(0 \leq r \leq 1)$
$a$ : heat generation density ratio of inner surface to outer surface of the pellet ( - )
$b:$ shape factor of the heat generation density function $Q(r)(-)$
$h:$ normalized inner radius of the pellet ( - ).

In the case of Halden reactor, the shape factor in eq. (2.1.43) can be set as $b=2$, since eq. (2.1.43) can be well approximated with a quadratic function. The heat generation density ratio $a$ is expressed as follows using eq. (2.1.41).

$$
\begin{equation*}
a=\frac{Q_{1}\left(R_{1}\right)}{Q_{1}\left(R_{p}\right)} \tag{2.1.44}
\end{equation*}
$$

Selection of option IFLX The heat generation density distribution is selected using IFLX as follows.
IFLX $>0$ : Designated by input as a function of burnup. The heat generation density distribution between the input burnup is obtained by interpolation in terms of burnup.
FLX $=0$ : Robertson formula is used.

### 2.1.2 Gap thermal conduction

Gap thermal conductance is represented by the following equation which is modified from the Ross and Stoute model. ${ }^{(13)}$

$$
\begin{equation*}
h=\frac{\lambda_{g a s}}{C\left(R_{e f f}+R_{2}\right)+\left(g_{1}+g_{2}\right)+\delta}+\frac{\lambda_{m} \cdot P_{c}}{0.5 \cdot R^{1 / 2} \cdot H}+h_{r} \tag{2.1.46}
\end{equation*}
$$

The first term on the right side of the equation is the gas conduction component, the second term is that due to solid contact, and the third term is that due to radiation.

Here,

$$
\begin{aligned}
& C= 2.77-2.55 \times 10^{-8} \cdot P_{c} \\
& \lambda_{m}= \frac{2 \lambda_{p}\left(T_{p o}\right) \cdot \lambda_{c}\left(T_{c i}\right)}{\lambda_{p}\left(T_{p o}\right)+\lambda_{c}\left(T_{c}\right)} \quad(\mathrm{W} / \mathrm{cm} \cdot \mathrm{~K}) \\
& h_{r}=\left[\frac{1}{\varepsilon_{p}}+\frac{1}{\varepsilon_{c}}-1\right]^{-1} \cdot \sigma \cdot \frac{T_{p o}^{4}-T_{c i}^{4}}{T_{p o}-T_{c i}} \\
& T_{p o}: \text { pellet outer surface temperature (K) } \\
& T_{c i}: \text { cladding inner surface temperature (K) } \\
& \lambda_{p}: \text { pellet thermal conductivity (W/cm } \cdot \mathrm{K}) \\
& \lambda_{c}: \text { cladding thermal conductivity (W/cm } \cdot \mathrm{K}) \\
& \lambda_{\text {gas }}: \text { thermal conductivity of the mixed gas (W/cm } \cdot \mathrm{K}) \\
& P_{c}: \text { contact pressure between pellet and cladding }(\mathrm{Pa}) \\
& R_{e f f}: \text { apparent surface roughness of the pellet (cm) } \\
& R_{2}: \text { cladding surface roughness (cm) } \\
& g_{1}+g_{2}: \text { temperature jump distance between solid phase and liquid phase (cm) } \\
& G A P: \text { radial gap width (cm) }
\end{aligned}
$$

$R: \sqrt{\frac{R_{e f f}{ }^{2}+R_{2}{ }^{2}}{2}}$
$H \quad: \quad$ cladding Mayer's hardness (Pa) $\left(H=2.8 \sigma_{Y}{ }^{(9)}\right)$
$\sigma_{Y} \quad$ : yield stress ( Pa )
$\sigma \quad: \quad$ Stefan-Boltzmann constant $\left(\mathrm{W} / \mathrm{cm} \cdot \mathrm{K}^{4}\right)\left(\sigma=5.67 \times 10^{-12}\right)$
$\varepsilon_{p} \quad: \quad$ pellet emissivity $(-), \quad \varepsilon_{c}$ : cladding black oxide emissivity $(-)$.

Fitting parameter $\mathrm{R}_{\text {eff, }}$ R2 The roughness $\mathrm{R}_{\text {eff }}$ and R 2 can be designated by the input parameters R1 and R2 $(\mu \mathrm{m})$, respectively. The default values are $1.0 \mu \mathrm{~m}$.

Equations for describing $\lambda_{\text {gas }}$ and $g_{1}+g_{2}$ are as follows.
(1) Thermal conductivity of mixed gas

This value can be represented as follows using the MATPRO-09 model. ${ }^{(14)}$

$$
\begin{equation*}
\lambda_{\mathrm{gas}}=\sum_{i=1}^{n}\left(\frac{\lambda_{i}}{1-\sum_{i=1}^{n} \phi_{i j} \frac{x_{j}}{x_{i}}}\right) \tag{2.1.47}
\end{equation*}
$$

Here, the equation

$$
\begin{equation*}
\phi_{l j}=\frac{\left[1+\binom{\lambda_{1}}{\lambda_{j}}^{\frac{1}{2}}\left(\frac{M_{i}}{M_{j}}\right)^{\frac{1}{4}}\right]^{2}}{2^{\frac{3}{2}}\left(1+\frac{M_{i}}{M_{j}}\right)^{\frac{1}{2}}}\left[1+\frac{2.41\left(M_{1}-M_{j}\right)\left(M_{1}-0.142 M_{j}\right)}{\left(M_{1}+M_{j}\right)^{2}}\right] \tag{2.1.48}
\end{equation*}
$$

holds, where

$$
\begin{array}{ll}
x_{1} & : \text { molar ratio of gas } i \\
\lambda_{i} & : \text { thermal conductivity of gas } i(\mathrm{~W} / \mathrm{cm} \cdot \mathrm{~K}) \\
M_{i} & : \text { molar mass of gas } i .
\end{array}
$$

The gases dealt with here are Helium, Nitrogen, Krypton and Xenon. Naturally, gas composition depends on FP gas release, which will be explained in section 2.1.4.

## (2) Temperature jump distance

The temperature jump distance is given by

$$
\begin{equation*}
g_{1}+g_{2}=\sum_{i=1}^{n}\left(g_{1}+g_{2}\right)_{j} \cdot \frac{10^{5}}{P_{g a s}} \tag{2.1.49}
\end{equation*}
$$

Here,

$$
\begin{aligned}
&\left(g_{1}+g_{2}\right): \quad \text { jump distance of gas } i \text { between solid phase and liquid phase } \\
&(\mathrm{cm}) \\
& P_{g a s}: \text { gas pressure }(\mathrm{Pa})
\end{aligned}
$$

According to the Ross and Stoute model, the values of $\left(\mathrm{g}_{1}+\mathrm{g}_{2}\right)$ for Helium, Nitrogen,

Krypton and Xenon are $10 \times 10^{-4}, 5 \times 10^{-4}, 1 \times 10^{-4}$ and $1 \times 10^{-4}(\mathrm{~cm})$, respectively.
Calculation of $P_{g a s}$ is explained later using eq. (2.1.217).

## Selection of option IGAPCN

Designation of IGAPCN allows selection of gap conduction models other than those described in section 2.1.2. (See section 2.4, Material Properties.)
IGAPCN $=0$ : Modified Ross and Stoute model, $=1:$ MATPRO-09 model,
$=2:$ Ross and Stoute model, $\quad=3$ : Modified Dean model.

### 2.1.3 Contact-force estimation model

[Simple mechanical model for thermal analysis]
To calculate the gap thermal conductance by eq.(2.1.46), the contact pressure between pellet and cladding $P_{c}$ must be obtained. For this purpose, FEMAXI-IV incorporates a contact-force estimation model which is independent of the analysis of the mechanical behavior of the entire fuel rod described in sections 2.2 and 2.3.

Features of this model are

- Creep is taken into consideration in the calculation of radial displacements of pellet and cladding.
- Calculation of the contact force utilizes a pellet stiffness recovery model.


## (1) Radial displacement of pellet

Radial displacement of pellet is given by the following equation, taking creep into consideration.

$$
\begin{equation*}
u_{f}=u^{r e l}+\sum_{i=1}^{10}\left(\varepsilon_{1}^{i n}+\varepsilon_{1}^{d c n}+\varepsilon_{1}^{s r}+\varepsilon_{i}^{u}+\varepsilon_{i}^{c}\right) \Delta r_{i} \tag{2.1.50}
\end{equation*}
$$

Here,
$u_{f}$ : radial displacement (cm)
$u_{r e l}:$ radial displacement due to relocation ( cm )
$\varepsilon_{1}^{\text {th }}:$ thermal strain of ring $i(-)$
$\varepsilon_{j}^{d e n}:$ densification of ring $i(-)$
$\varepsilon_{1}^{s 5}:$ solid FP (constrained) swelling of ring $i(-)$
$\varepsilon_{i}^{u}:$ gas FP (unconstrained) swelling of ring $i(-)$
$\varepsilon_{1}^{c} \quad: \quad$ creep strain of ring $i(-)$
$\Delta r_{i}$ : width of ring $i$, radial mesh (cm)
$i$ : ring number (total of 10 radial rings).
Among the above items, $\varepsilon_{1}^{\text {th }}, \varepsilon_{1}^{d e n}$ and $\varepsilon_{1}^{\text {ss }}$ are the strains which can be determined independent of the contact condition, while $\varepsilon_{i}^{u}$ and $\varepsilon_{i}^{c}$ are those that can be determined depending on the contact condition. It is assumed that pellet swelling by gas FP can be generated only under the unconstrained condition (i.e., contact force $=0$ ), and that compressive creep of pellet is induced under contact force.

## Fitting parameter XRELOC

 The initial relocation value of peller, $u^{\text {rel }}$ is designated by $u^{\text {rel }}=$ [initial radial gap width $] \times$ XRELOC. $\quad$ The default value of XRELOC is 0.2 .The following MATPRO-09 equation is used ${ }^{(14)}$ as the creep equation of pellet,

$$
\begin{equation*}
\dot{\bar{\varepsilon}}^{c}=\frac{\left(A_{1}+A_{2} F\right) \bar{\sigma} e^{-Q_{1} / R T}}{\left(A_{3}+f_{d}\right) G^{2}}+\frac{A_{4} \bar{\sigma}^{4.5} e^{-\left(Q_{2} / R T\right.}}{\left(A_{6}+f_{d}\right)}+A_{7} \bar{\sigma} F e^{-Q_{3} / R T} \tag{2.1.51}
\end{equation*}
$$

Here,

$$
\begin{aligned}
A_{1} & =9.728 \times 10^{6}, \quad Q_{1}=90,000 \\
A_{2} & =3.240 \times 10^{-12}, \quad Q_{2}=132,000 \\
A_{3} & =-87.7, \quad Q_{3}=5,200 \\
A_{4} & =1.376 \times 10^{-4}, \quad A_{6}=-90.5 \\
A_{7} & =9.24 \times 10^{-28} \\
\dot{\bar{\varepsilon}}^{c} & : \text { equivalent creep strain rate }\left(\mathrm{hr}^{-1}\right) \\
F & : \text { fission rate }\left(=10^{19} \text { fissions } / \mathrm{m}^{3} \cdot \mathrm{~s} \text { is designated by FEMAXI-IV }\right)
\end{aligned}
$$

$\bar{\sigma}$ : equivalent stress (psi)
$R \quad$ : gas constant ( $1.987 \mathrm{cal} / \mathrm{mol} \cdot \mathrm{K}$ )
$Q \quad: \quad$ activation energy (cal/mol)
$T$ : temperature (K)

## Fitting parameter TCRMX

The upper limit of the temperature used for the creep strain velocity is given by TCRMX. The default value of TCRMX is $1773.15(\mathrm{~K})$.
$f_{d}$ : theoretical density ratio (\%)
$G$ : grain diameter ( $\mu \mathrm{m}$ ).
However, when the pellet temperature exceeds the designated temperature TCRMX, the creep strain rate is calculated with TCRMX. Since the present model assumes the plane
stress condition and therefore the equivalent stress is $\sigma_{z}=0, \bar{\sigma}=P_{f c}$ holds when $\sigma_{r} \approx \sigma_{\theta}=-P_{f c}$ (contact force) is assumed.

In this condition, the creep strain rate components can be given as

$$
\left\{\begin{array}{l}
\dot{\varepsilon}_{r, 1}^{c}  \tag{2.1.52}\\
\dot{\varepsilon}_{z, i}^{c} \\
\dot{\varepsilon}_{\theta, i}^{c}
\end{array}\right\}=\dot{\bar{\varepsilon}}_{i}^{c} \frac{1}{2 \bar{\sigma}}\left\{\begin{array}{l}
2 \sigma_{r}-\sigma_{\theta} \\
-\sigma_{r}-\sigma_{\theta} \\
2 \sigma_{\theta}-\sigma_{r}
\end{array}\right\}=\dot{\bar{\varepsilon}}_{i}^{c}\left\{\begin{array}{c}
-\frac{1}{2} \\
1 \\
-\frac{1}{2}
\end{array}\right\}
$$

and the creep rate in the circumferential direction is

$$
\begin{equation*}
\dot{\varepsilon}_{\theta, i}^{c}=-\frac{1}{2} \dot{\varepsilon}_{i}^{c} . \tag{2.1.53}
\end{equation*}
$$

## (2) Radial displacement of cladding

In the calculation of the cladding radial displacement, the creep strain in addition to the elastic strain and thermal strain is considered. It is given by

$$
\begin{equation*}
u=\frac{r_{c t}}{E}\left[\frac{\left(P_{g a s}+P_{f t}\right)\left(r_{c i}^{2}+r_{c t}^{2}\right)-2 P_{w} r_{c o}^{2}}{r_{c o}^{2}-r_{c t}^{2}}+v P_{g a s}\right]+\left(\varepsilon^{t h}+\varepsilon^{c}\right) \frac{r_{c o}+r_{c \prime}}{2} . \tag{2.1.54}
\end{equation*}
$$

Here,

$$
\begin{aligned}
u & : \text { cladding radial displacement }(\mathrm{cm}) \\
E & : \text { Young's modulus of cladding }(\mathrm{Pa}) \\
r_{c i} & : \text { cladding inner diameter (cm) } \\
r_{c o} & : \text { cladding outer diameter (cm) } \\
P_{g a s} & : \text { internal pressure (Pa) } \\
P_{f c} & : \text { contact pressure between pellet and cladding (Pa) } \\
P_{w} & : \text { coolant water pressure (Pa) } \\
\nu & : \text { Poisson's ratio of cladding } \\
\varepsilon^{\text {( } h} & : \text { cladding thermal strain } \\
\varepsilon^{\varepsilon} & : \text { cladding creep strain. }
\end{aligned}
$$

Circumferential and axial components of cladding stress are given as follows using the thin cylindrical shell model:

$$
\begin{equation*}
\sigma_{\theta}=\frac{r_{c i}\left(P_{f c}+P_{g u s}\right)-r_{c o} P_{w}}{r_{c o}-r_{c i}} \tag{2.1.55}
\end{equation*}
$$

$$
\begin{align*}
& \text { JAERI-Data/Code 97-043 } \\
& \sigma_{z}=\frac{r_{c i}^{2}\left(P_{f c}+P_{g a s}\right)-r_{c o}^{2} P_{w}}{r_{c o}{ }^{2}-r_{c i}{ }^{2}} \tag{2.1.56}
\end{align*}
$$

However, $P_{f t}=0$ in the non-contact condition.
Here, since this model does not taken into account the shearing components, the equivalent stress is expressed as

$$
\begin{equation*}
\bar{\sigma}=\left[\frac{1}{2}\left\{\left(\sigma_{\theta}-\sigma_{z}\right)^{2}+\sigma_{\theta}^{2}+\sigma_{z}^{2}\right\}\right]^{\frac{1}{2}} . \tag{2.1.57}
\end{equation*}
$$

Using this $\bar{\sigma}$, the equivalent creep strain increment of cladding is expressed as

$$
\begin{equation*}
d \bar{\varepsilon}^{c}=f\left(\bar{\sigma}, T, \phi, \bar{\varepsilon}^{c}\right) \cdot d t \tag{2.1.58}
\end{equation*}
$$

Here, determination of the function $f$ requires a creep equation of cladding. This creep equation is selected from either MATPRO-09 equation ${ }^{(14)}$ or NENANSEN equation ${ }^{(15)}$. The concrete form of these equations are described in section 2.4.2.

The function $f=\dot{\bar{\varepsilon}}^{c}$ does not contain time explicitly. Therefore, time $t$ is eliminated from the formulation of $\dot{\bar{\varepsilon}}^{c}$ by transforming the creep equation :

1) MATPRO-09 equation has a form:

$$
\begin{equation*}
\dot{\varepsilon}=K \phi(\sigma+B \exp (C \sigma)) \exp (-10000 / R T) t^{-0.5} \tag{1}
\end{equation*}
$$

Integrating eq.(1) with t gives

$$
\begin{equation*}
\varepsilon=2 K \phi(\sigma+B \exp (C \sigma)) \exp (-10000 / R T) t^{0.5} \tag{2}
\end{equation*}
$$

Since eq.(2) is a primary creep equation which has non-unity power of $t$,

$$
\varepsilon_{H}=\varepsilon(\text { total creep strain })
$$

holds. Eliminating $t$ from the eqs.(1) and (2) gives

$$
\dot{\varepsilon}=2\{K \phi(\sigma+B \exp (C \sigma)) \exp (-10000 / R T)\}^{2} / \varepsilon
$$

Consequently,

$$
\begin{equation*}
f=\dot{\bar{\varepsilon}}^{c}=2\{K \phi(\sigma+B \exp (C \sigma)) \exp (-10000 / R T)\}^{2} / \bar{\varepsilon}^{c} \tag{2.1.59}
\end{equation*}
$$

holds, where
$\dot{\bar{\varepsilon}}^{c}$ : equivalent creep strain rate of cladding $\quad\left(s^{-1}\right)$
$\bar{\varepsilon}^{c}$ : equivalent creep strain of cladding

$$
\begin{aligned}
& C_{1}=5.129 \times 10^{-29}, \quad Q_{1}=10,000 \\
& C_{2}=7.252 \times 10^{2}, \quad Q_{2}=4.967 \times 10^{-8} \\
\phi: & \text { fast neutron flux }\left(\mathrm{n} / \mathrm{m}^{2} / \mathrm{s}\right) \\
\bar{\sigma}: & \text { equivalent stress }(\mathrm{Pa}) \\
T: & \text { temperature }(\mathrm{K}) \\
R: & \text { gas constant }(1.987 \mathrm{cal} / \mathrm{mol} \cdot \mathrm{~K}) .
\end{aligned}
$$

2) NENANSEN equation has the following form:

$$
\begin{equation*}
\text { creep strain rate: } \dot{\varepsilon}^{c}=\dot{\varepsilon}_{t h}^{c}+\dot{\varepsilon}_{i r r}^{c} \tag{2.1.60}
\end{equation*}
$$

$$
\begin{align*}
& \dot{\varepsilon}_{t h}^{c}=m K^{\frac{1}{m}} \varepsilon_{H}^{\left(1-\frac{1}{m}\right)}  \tag{2.1.61}\\
& \dot{\varepsilon}_{1 r r}^{c}=6.64 \times 10^{-25} \phi^{123} \sigma_{e q}^{134}, \tag{2.1.62}
\end{align*}
$$

so that it is not necessary to eliminate time $t$, and

$$
f=\dot{\bar{\epsilon}}^{c} \quad \text { holds. }
$$

The creep strain increments in the circumferential and axial directions are

$$
\begin{align*}
& d \varepsilon_{\theta}^{c}=\frac{1}{2 \bar{\sigma}}\left(2 \sigma_{\theta}-\sigma_{z}\right) \cdot d \bar{\varepsilon}^{c}  \tag{2.1.63}\\
& d \varepsilon_{z}^{c}=\frac{1}{2 \bar{\sigma}}\left(2 \sigma_{z}-\sigma_{\theta}\right) \cdot d \bar{\varepsilon}^{c} \tag{2.1.64}
\end{align*}
$$

Here, $\bar{\varepsilon}^{c}$ in eq. (2.1.58) is expressed as

$$
\bar{\varepsilon}^{c}=\bar{\varepsilon}_{n}^{c}+\theta \cdot d \bar{\varepsilon}^{c} \quad\left(\theta=\frac{1}{2}\right)
$$

and $\dot{\bar{\varepsilon}}^{c}$ is obtained by iteration of convergence calculation.
Also, with the time-step number designated as $m$ and the time-step number of the current step as $n+1, \varepsilon^{c}$ in eq. (2.1.54) is given by

$$
\begin{equation*}
\varepsilon^{c}=\varepsilon_{\theta, n+1}^{c}=\sum_{m=1}^{n+1} d \varepsilon_{\theta, m}^{c} \tag{2.1.65}
\end{equation*}
$$

(5) Pellet crack migration model

Crack shape in the pellet changes with burnup. This change is modeled as follows.

At the beginning-of-life, cracks develop in radial directions, and void spaces generated by cracking and relocation are present near the center of the pellet as shown in Fig. 2.17.

As the burnup progresses, these radial cracks gradually become circumferentially oriented, and as a result, circumferentially oriented cracks are formed as shown in Fig. 2.18 .


Fig. 2.17 Cracks in pellet at the beginning-of-life.


Fig. 2.18 Cracks at extended burnup

In FEMAXI-IV, it is assumed that this migration of cracks begins at a certain stage and is completed at another stage of burnup, and that the volumes of pellet, cladding, cracks and gaps change linearly with burnup during the migration process, as shown in Fig. 2.19.


Fig. 2.19 Change of crack volume with burnup.

Also, it is assumed that when the pellet and cladding make contact, the decrease in pellet volume due to contact force is accommodated only by the decrease in volume of the
circumferentially oriented cracks, and the contact force does not affect the volume of radial cracks near the pellet center. It follows that, in a burnup region before the beginning of crack migration, no apparent change in stiffness due to cracking of the pellet is assumed and the original Young's modulus is used. The contact force between pellet and cladding increases in proportion to the imaginary overlap width, $\delta_{f c}$, of the pellet and cladding.

In the burnup region after the beginning of crack migration, the apparent change in stiffness due to pellet cracking, which is in proportion to the amount of increase in the volume of circumferentially oriented cracks, should be dealt with. Namely, the model of varying Young's modulus of pellet is used.

When the burnup reaches the level at which migration is completed, the apparent change in stiffness due to pellet cracking becomes most moderate.

In FEMAXI-IV, burnup levels of beginning and completion of crack migration are designated by input parameters. The present model is applied only to the contact force prediction in the thermal analysis, and is similar but not identical to that used in the mechanical analysis, which will be described later.

> Fitting parameters BUMIN and BUMAX Burnup levels of beginning and copmletion of crack migration can be input as BUMIN and BUMAX, respectively. Default values of BUMIN and BUMAX are $0(\mathrm{Mwd} / \mathrm{t}-\mathrm{U})$. Namely, in the default condition, crack migration is already completed at the beginning-of-life.
(4) Recovery of stiffness of cracked pellet

Pellet cracks are described using a 'Stiffness Recovery model' in which the pellet Young's modulus is varied. The Young's modulus of the cracked pellet is represented by a linear function of the elastic strain as follows ${ }^{(2)}$.


Fig. 2.20 Young's modulus of the cracked pellet.
Assuming that the pellet radial displacement by relocation is $\delta_{\text {crk }}$ which is generated by circumferentially oriented cracks, the radial displacement of pellet which is caused when pellet is compressed by cladding in the radial direction is $\delta_{f}(>0)$, the model assumes that the pellet stiffness recovers to its original value when $\delta_{f}=2 \delta_{c r k}$. (See eq.(2.1.74))

As shown in Fig. 2.20, Young's modulus in the radial direction is given by the equations

$$
E_{f}= \begin{cases}0_{c} & \left(0 \leq \varepsilon_{f}\right)  \tag{2.1.66}\\ -\frac{E}{\varepsilon_{R}} \varepsilon_{f} & \left(-\varepsilon_{R}<\varepsilon_{f}<0\right) \\ E & \left(\varepsilon_{f} \leq-\varepsilon_{R}\right)\end{cases}
$$

Here,

$$
E_{f}: \text { apparent Young's modulus of pellet }
$$

$\varepsilon_{f}$ : radial compressive strain of pellet which is caused when pellet is compressed by contact force from cladding ( $\varepsilon_{f}<0$ )
$E$ : original Young's modulus of pellet $\varepsilon_{R}$ : pellet radial strain due to pushed-back portion of pellet displacement when stiffness of pellet is completely recovered Therefore,

$$
\begin{equation*}
\varepsilon_{f}=-\frac{\delta_{j}}{r_{p o}} \tag{2.1.67}
\end{equation*}
$$

holds, where

$$
r_{p o}: \text { pellet initial outer radius, }
$$

and pellet radial displacement is expressed as,

$$
\begin{equation*}
\delta_{c r k}=r_{p o} \varepsilon_{c r k} \tag{2.1.68}
\end{equation*}
$$

$\varepsilon_{R}(>0)$ is determined as follows:

$$
\begin{gathered}
-\varepsilon_{R}=(\text { lost portion of strain of circumferentially oriented crack }<0) \\
+(\text { elastic compressive strain }<0)
\end{gathered}
$$

namely,

$$
\begin{equation*}
-\varepsilon_{R}=\bar{\varepsilon}_{c r k}+\frac{\sigma_{k}}{E} \tag{2.1.69}
\end{equation*}
$$

holds, where

$$
\begin{gathered}
\bar{\varepsilon}_{\text {crk }}:=-\varepsilon_{\text {crk }}, \quad \text { lost portion of strain due to } \\
\\
\quad \text { circumferentially oriented crack, } \\
\sigma_{R}: \text { compressive stress imposed by cladding when } \\
\\
\text { stiffness of pellet completely recovered. }
\end{gathered}
$$

(See Fig.2.21.)
Here, as shown in section (3), $\bar{\varepsilon}_{\text {crk }}$, or the lost portion of strain due to circumferentially oriented crack is given as a function of burnup and relocation strain,

$$
\bar{\varepsilon}_{c r k}= \begin{cases}0 & \left(B u \leq B u_{\min }\right) \\ -\frac{B u-B u_{\min }}{B u_{\max }-B u_{\min }} & \varepsilon_{r e l} \\ \left.-B u_{\min }<B u<B u_{\max }\right) \\ -\varepsilon_{r e l} & \left(B u_{\max } \leq B u\right)\end{cases}
$$

where

$$
B u \text { : burnup, }
$$

$$
B u_{\min }: \text { burnup at the beginning of crack migration }
$$

$$
B u_{\max }: \text { burnup at the completion of crack migration }
$$

$$
\varepsilon_{r e l}: \text { relocation strain }=\text { XRELOC } \cdot \frac{\delta_{0}}{r_{p o}}
$$

$\delta_{0}$ :initial radial gap width.
As shown in eq.(2.1.66), $\varepsilon_{f}$ affects the determination of $E_{f}$ only within the range of $-\varepsilon_{R}<\varepsilon_{f}<0$. Therefore, using the relationship $\frac{d \sigma_{f}}{d \varepsilon_{f}}=E_{f}$,

$$
\begin{equation*}
\sigma_{f}=-\frac{E}{\varepsilon_{R}} \frac{\varepsilon_{f}^{2}}{2} \quad\left(-\varepsilon_{R}<\varepsilon_{f}<0\right) \tag{2.1.70}
\end{equation*}
$$



Fig.2.21 Relationship between stress and strain of cracked pellet
Solving eq.(2.1.70) for $\varepsilon_{f}<0$, the following equation is obtained.

$$
\begin{equation*}
\varepsilon_{f}=-\sqrt{\frac{2 \varepsilon_{R}\left(-\sigma_{t}\right)}{E}} \tag{2.1.71}
\end{equation*}
$$

Substituting eq.(2.1.71) into eq.(2.1.66) in the range of $-\varepsilon_{R}<\varepsilon_{f}<0$ and solving eq.(2.1.66) in terms of $E_{f}$,

$$
\begin{equation*}
E_{f}=\sqrt{\frac{2 E\left(-\sigma_{f}\right)}{\varepsilon_{R}}} \tag{2.1.72}
\end{equation*}
$$

holds.
When $\varepsilon_{f}=-\varepsilon_{R}, \sigma_{R}$ is obtained as follows substituting the relationship $E_{f}=E$ into eq.(2.1.70),

$$
\begin{equation*}
\sigma_{R}=-\frac{E \varepsilon_{R}}{2} \tag{2.1.73}
\end{equation*}
$$

Substituting eq.(2.1.73) into eq.(2.1.69),

$$
\begin{equation*}
\varepsilon_{R}=2 \varepsilon_{c r k} \tag{2.1.74}
\end{equation*}
$$

Substituting eqs.(2.1.67) and (2.1.73) into eq.(2.1.66), $\quad E_{f}$ is obtained as

$$
\begin{array}{ll}
E_{f}=\frac{E}{2 \varepsilon_{c r k}} \cdot \frac{\delta_{f}}{r_{p o}} & \left(-\varepsilon_{R}<\varepsilon_{f},\right.  \tag{2.1.75}\\
\text { i.e. , } \left.\delta_{f}<2 r_{p o} \varepsilon_{c r k}\right) \\
E_{f}=E & \left(\varepsilon_{f} \leq \varepsilon_{R},\right. \\
\text { i.e. , } \left.\delta_{f} \geq 2 r_{r o} \varepsilon_{c r k}\right)
\end{array}
$$

## (5) Gap width and contact force

Here, method to calculate pellet-cladding contact force $P_{f c}$ is explained on the basis of the imaginary overlap quantity $\delta_{f c}$ of pellet and cladding radial displacements and on the assumption of the stiffness recovery model described in section (4).

The contact force $P_{f c}$ is force that is generated across the contact surface to eliminate the imaginary overlap $\delta_{j c}$ by counter-pushing and balancing when pellet and cladding make a contact at the start of a time step.

The contact force $P_{f c}$ can be obtained as the force with which cladding pushes pellet and vise versa, if radial displacement of cladding in contact with pellet is known, from such quantities as inner and outer radii, thickness, and Young's modulus of cladding.

The gap width between pellet and cladding is expressedas

$$
\begin{equation*}
\delta=\delta_{o}+u_{c}-u_{f} \tag{2.1.76}
\end{equation*}
$$

where

$$
\begin{aligned}
& \delta: \text { radial gapwidth (m) } \\
& \delta_{o}: \text { initial gap width (m) } \\
& u_{c}: \text { radial displacement of cladding (m) } \\
& u_{f}: \text { radial displacement of pellet (m) }
\end{aligned}
$$

When $\delta$ is calculated to be negative at the start of a time step, it is judged that the pellet is in contact with the cladding and $P_{f c}$ is calculated. At this time of numerical calculation, the pellet and cladding have an imaginary overlap with each other by width

$$
\begin{equation*}
\delta_{f c}=-\delta=-\left(\delta_{o}+u_{c}-u_{f}\right)>0 \tag{2.1.77}
\end{equation*}
$$

Namely, $\delta_{f c}$ is known at the start of the time step.
It is assumed that, when $\delta_{f c}$ is positive, cladding pushes pellet and vice versa until $\delta_{f c}$ becomes 0 . In this situation, setting the pellet push-back displacement caused by cladding
pushing inward as $\delta_{f}$, and setting the cladding push-out displacement caused by pellet pushing outward as $\delta_{c}$,

$$
\begin{equation*}
\delta_{f c}=\delta_{j}+\delta_{c} \tag{2.1.78}
\end{equation*}
$$

holds.
At the pellet side, when $\varepsilon_{r}=\varepsilon_{\theta}$, using $\delta_{f}$, radial strain $\varepsilon_{r}$ and contact force $P_{f i}$ are

$$
\varepsilon_{r}=\varepsilon_{\theta}=\frac{\delta_{f}}{r_{c i}}
$$

and

$$
\begin{equation*}
P_{f i}=E_{f}\left(\frac{\delta_{j}}{r_{c i}}\right) \tag{2.1.79}
\end{equation*}
$$

Here,

$$
\begin{aligned}
E_{f} & : \text { pellet apparent (effective) Young's modulus } \\
r_{c}: & \text { cladding inner radius(=pellet outer radius }\left(r_{p o}\right) \text { in contact } \\
& \text { with cladding) }
\end{aligned}
$$

At the cladding side, since $\varepsilon_{\theta}=\delta_{c} / r_{c}$, holds, setting $E_{c}$ as cladding Young's modulus,

$$
\begin{gather*}
\sigma_{\theta}=E_{c} \varepsilon_{\theta}=E_{c} \frac{\delta_{c}}{r_{c t}}  \tag{2.1.80}\\
P_{f c}=\sigma_{r}=\sigma_{\theta} \frac{t}{r_{c i}}=E_{c} \frac{\delta_{c}}{r_{c i}} \cdot \frac{t}{r_{c i}}  \tag{2.1.81}\\
\quad\left(t=r_{c o}-r_{c t}: \text { cladding thickness }\right)
\end{gather*}
$$

Namely,

$$
\begin{equation*}
P_{f c}=E_{c} \frac{\delta_{c}\left(r_{c o}-r_{c i}\right)}{r_{c i}^{2}} \tag{2.1.82}
\end{equation*}
$$

holds.
Simultaneously solving eqs. (2.1.78)-(2.1.82) in terms of $\delta_{f}$ and $\delta_{c}$ and eliminating $P_{f c}$, we obtain

$$
\begin{align*}
& \delta_{f}=\frac{E_{c}\left(r_{c o}-r_{c i}\right)}{E_{c}\left(r_{c o}-r_{c i}\right)+E_{f} r_{c i}} \delta_{f c}  \tag{2.1.83}\\
& \delta_{c}=\frac{E_{f} r_{c i}}{E_{c}\left(r_{c o}-r_{c i}\right)+E_{f} r_{c i}} \delta_{f c} \tag{2.1.84}
\end{align*}
$$

However, eqs.(2.1.83) and (2.1.84) do not hold in a strict sense, since they are derived on
the basis of the balance of force and $\delta_{f c}$ contains 'displacement for the lost portion of strain due to circumferentially oriented crack'.

Here, pellet apparent Young's modulus $E_{f}$, i.e. one of the unknown variables, is expressed as follows from eqs.(2.1.66) and (2.1.75).
(1) When $\delta_{j}=0, \quad E_{j}=0$
(2) When $0<\delta_{j}<2 \delta_{c r k}, \quad E_{j}=\frac{\delta_{j}}{2 \delta_{c r k}} E$
(3) When $\delta_{f} \geq 2 \delta_{\text {crk }}, \quad E_{f}=E \quad$ (original property value)

Now, equations are defined taking 'the displacement due to circumferentially oriented crack' which is contained in $\delta_{f c}$ of eqs.(2.1.83) and (2.1.84) into consideration by using the above relationship.

When $\delta_{J} \geq 2 \delta_{\text {crk }}$, pellet loses entirely the radial displacement $\delta_{\text {crk }}$ due to circumferentially oriented crack and $E_{f}=E$ holds, eqs.(2.1.83) and (2.1.84) are rewritten as

$$
\begin{align*}
& \delta_{f}=\frac{E_{c}\left(r_{c o}-r_{c j}\right)}{E_{c}\left(r_{c o}-r_{c i}\right)+E r_{c \prime}}\left(\delta_{f c}-\delta_{c r k}\right)+\delta_{c r k}  \tag{2.1.86}\\
& \delta_{c}=\frac{E r_{c i}}{E_{c}\left(r_{c o}-r_{c i}\right)+E r_{c i}}\left(\delta_{f c}-\delta_{c r k}\right) \tag{2.1.87}
\end{align*}
$$

When $\delta_{f}=2 \delta_{c r k}, \delta_{f c}$ is calculated as follows.
Using the relationship $\delta_{f c}=\delta_{f}+\delta_{c}=2 \delta_{c r k}+\frac{E r_{c i}}{E_{c}\left(r_{c b}-r_{c i}\right)+E \quad r_{c i}}\left(\delta_{f c}-\delta_{c r k}\right)$,

$$
\begin{equation*}
\delta_{f c}=2 \delta_{c r k}+\frac{E r_{c i}}{E_{c}\left(r_{c o}-r_{c i}\right)} \delta_{c r k} \tag{2.1.88}
\end{equation*}
$$

holds.
Therefore, in the range of (3) in eq.(2.1.75), i.e., $\delta_{f c} \geq 2 \delta_{c r k}+\frac{E r_{c i}}{E_{c}\left(r_{c o}-r_{c i}\right)} \delta_{c r k}$, eq.(2.1.87) gives $\delta_{c}$.

Next, derivation of $\delta_{c}$ in the range of (2) in eq.(2.2.85), i.e., $o<\delta_{j c}<2 \delta_{c r k}+\frac{E r_{c i}}{E_{c}\left(r_{c t}-r_{c i}\right)} \delta_{c r k}$ is explained. In this range, in the same manner as eqs.(2.1.86) and (2.1.87), eqs.(2.1.83) and (2.1.84) are rewritten as

$$
\begin{equation*}
\delta_{f}=\frac{E_{c}\left(r_{c o}-r_{c i}\right)}{E_{c}\left(r_{c p}-r_{c l}\right)+E_{f} r_{c i}}\left(\delta_{f_{c}}-\widetilde{\delta}_{c r k}\right)+\widetilde{\delta}_{c r k} \tag{2.1.89}
\end{equation*}
$$

$$
\begin{equation*}
\delta_{\mathrm{c}}=\frac{E_{f} r_{c t}}{E_{c}\left(r_{c o}-r_{c i}\right)+E_{f} r_{c i}}\left(\delta_{f c}-\widetilde{\delta}_{c r k}\right) \tag{2.1.90}
\end{equation*}
$$

Here, $\widetilde{\delta}_{\text {crk }}$ is the lost relocation displacement.
$\widetilde{\delta}_{c r k}$ corresponds to the value which is obtained from $r_{p o}$ times the distance between the origin and intersection point of the tangential line of stress-strain curve with $\varepsilon_{f}$-axis shown in Fig.2.21.
$\widetilde{\delta}_{c r k}$ is calculated in the following method. Using the strain $\widetilde{\varepsilon}_{\text {crk }}$ due to circumferentially oriented crack,

$$
\begin{equation*}
\sigma_{f}=E_{f}\left(\varepsilon_{f}+\widetilde{\varepsilon}_{c r k}\right) \tag{2.1.91}
\end{equation*}
$$

holds, where $\quad \widetilde{\varepsilon}_{c r k}=\frac{\widetilde{\delta}_{c r k}}{r_{p u}}$.
Substituting eqs.(2.1.66) and (2.1.70) into this equation,
since

$$
\begin{gather*}
-\frac{E}{\varepsilon_{R}} \frac{\varepsilon_{f}^{2}}{2}=-\frac{E}{\varepsilon_{R}} \varepsilon_{f}\left(\varepsilon_{f}+\widetilde{\varepsilon}_{c r k}\right) \\
\widetilde{\varepsilon}_{c r k}=-\frac{\varepsilon_{f}}{2} \tag{2.1.92}
\end{gather*}
$$

is obtained. Multiplying the both sides of eq.(2.1.92) by $-r_{p o}$ gives

$$
\begin{equation*}
\widetilde{\delta}_{c r k}=\frac{\delta_{J}}{2} \tag{2.1.93}
\end{equation*}
$$

Substituting eqs.(2.1.85) and (2.1.93) into eq.(2.1.89), we obtain

$$
\delta_{f}=\frac{E_{c}\left(r_{c o}-r_{c i}\right)}{E_{\mathrm{c}}\left(r_{c o}-r_{c i}\right)+\frac{\delta_{f}}{2 \delta_{c r k}} E r_{c \mathrm{cs}}}\left(\delta_{f c}-\frac{\delta_{f}}{2}\right)+\frac{\delta_{f}}{2}
$$

Rearranging this equation in terms of $\delta_{f}$,

$$
E r_{c} \delta_{f}^{2}+4 \delta_{c r k} E_{c}\left(r_{c o}-r_{c i}\right) \delta_{f}-4 \delta_{c r k} E_{c}\left(r_{c o}-r_{c t}\right) \delta_{j c}=0
$$

is derived. Solving this in terms of $\delta_{J}(>0)$, we obtain

$$
\begin{equation*}
\delta_{j}=\frac{-2 \delta_{c r k} E_{c}\left(r_{c o}-r_{c i}\right)+\sqrt{4 \delta_{c r k}^{2} E_{c}^{2}\left(r_{c o}-r_{c i}\right)^{2}+4 \delta_{c r k} E E_{c} r_{c i}\left(r_{c o}-r_{c i}\right) \delta_{j c}}}{E r_{c i}} \tag{2.1.94}
\end{equation*}
$$

Substituting eq.(2.1.94) into eqs.(2.1.85) and (2.1.93), $E_{J}$ and $\bar{\delta}_{r e l}$ is obtained.
Rearranging in terms of $\delta_{c}$ using the above relationship,

$$
\delta_{c}=\left\{\begin{array}{cc}
\frac{E_{f} r_{c c}}{E_{c}\left(r_{c o}-r_{c i}\right)+E_{f} r_{c i}}\left(\delta_{f c}-\frac{\delta_{f}}{2}\right) & \left(0 \leq \delta_{f c}<2 \delta_{c r k}+\frac{E r_{c i}}{E_{c}\left(r_{c o}-r_{c i}\right)} \delta_{c r k}\right) \\
\frac{E r_{c c}}{E\left(r_{c o}-r_{c l}\right)+E r_{c i}}\left(\delta_{f c}-\delta_{c r k}\right) & \left(2 \delta_{c r k}+\frac{E r_{c i}}{E_{c}\left(r_{c o}-r_{c i}\right)} \delta_{c r k} \leq \delta_{f c}\right) \tag{2.1.95}
\end{array}\right.
$$

hold. $\delta_{f}$ is known from eq.(2.1.94), therefore the contact force can be determined by substituting $\delta_{c}$ which is determined by eq.(2.1.95) into eq.(2.1.82).

It is assumed that, after cladding yields, contact force does not exceeds the value obtained when cladding yields. Namely, when the equivalent stress of cladding exceeds the yield stress $\sigma_{y}$, the following equation is used instead of eq. (2.1.57).

$$
\bar{\sigma}=\sigma_{y}
$$

Here, the equation below is used to obtain $\sigma_{y}$ of the cladding in the case of recrystallized annealed materials. ${ }^{(2)}$

$$
\begin{equation*}
\sigma_{Y}=21.60-0.0213 \times T+\Delta{\sigma_{Y_{o}}{ }^{i r r}, ~}_{\text {, }} \tag{2.1.96}
\end{equation*}
$$

where

$$
\begin{aligned}
\sigma_{y} & : 0.2 \% \text { proof stress }\left(\mathrm{kg} / \mathrm{mm}^{2}\right) \\
T & : \text { temperature }\left({ }^{\circ} \mathrm{C}\right)
\end{aligned}
$$

In the cases of stress-relieved materials, the equation below is used. ${ }^{(2)}$

$$
\begin{equation*}
\sigma_{Y}=31.32-0.0213 \times T+\Delta \sigma_{Y O}{ }^{i r r} \tag{2.1.97}
\end{equation*}
$$

For the increase in yield stress $\Delta \sigma_{Y O}{ }^{i r r}$ due to irradiation hardening, the following equation is used. ${ }^{(2)}$

$$
\begin{equation*}
\Delta \sigma_{Y O}^{i r r}=33.4[1-\exp (-c \phi t)]^{\frac{1}{2}} \tag{2.1.98}
\end{equation*}
$$

Here,

$$
\begin{array}{ll}
c & : 2.92 \times 10^{-21} \exp \left(-1.6 \times 10^{-14} \phi\right) \\
\phi & : \text { fast neutron flux }\left(\mathrm{n} / \mathrm{cm}^{2} / \mathrm{s}\right) \\
c & : \text { time }(\mathrm{s}) .
\end{array}
$$

### 2.1.4 Generation and release of FP gas

In FEMAXI-IV, generation and release of FP gas are calculated with the pellet stack which is divided into a maximum of 12 axial segments, and each axial segment is divided into 10 concentric zones (ring element) in the radial direction. Either a mechanistic model or a temperature zone model is selected in the FP gas release analysis.

Selection of option IGASP
FP gas release model option
IGASP $=0$ : Mechanistic model, $=1$ : Temperature zoning model.

## (1) Generation rate

The FP gas generation rate in the axial segment $j$ and radial zone $i$ is represented by

$$
\begin{equation*}
P^{j j}=\frac{Y \cdot f^{y} \cdot q^{i}}{E_{f} \cdot N_{A}} \tag{2.1.99}
\end{equation*}
$$

Here,
$P^{i j}:$ FP gas generation rate per unit length in zone $i j(\mathrm{~mol} / \mathrm{cm} \cdot \mathrm{s})$

$$
f^{i j}=2 \pi \int_{-\frac{1}{2}}^{+\frac{1}{2}} \phi(r) r d r
$$

$\phi(r)$ : heat generation density distribution function in the radial direction, eq. (2.1.24)
$q^{j}:$ average heat generation density of axial segment $\mathrm{j}=\frac{P_{L H R}^{j}}{\pi\left(1-h^{2}\right)}$
$P_{L H R}^{j} \quad$ : linear heat rate of axial segment $\mathrm{j} \quad$ (W/cm)
$h$ : normalized radius of the center hole of pellet ( - )
$E_{f}:$ energy generated per one fission, $3.204 \times 10^{-11} \mathrm{~J}(=200 \mathrm{MeV})$
$Y:$ fission yield of FP gas $\left(K_{r}+K_{e}\right),=0.3$
$N_{A}:$ Avogadro's number, $6.02 \times 10^{23}$.
(2) FP gas release model (mechanistic model)
(2)-1 Assumptions of the release mechanism

The gas produced in $\mathrm{UO}_{2}$ grains is transported to grain boundaries through the two mechanisms described below, and that there it forms bubbles which accumulate there.

1) Gas atom diffusion within grains
2) Sweeping of gas atoms to grain boundaries by grain growth

When the amount of FP gas in the intergranular gas bubbles reaches a certain saturation value, a number of bubbles connect and a tunnel which leads to a free surface of pellet is formed. After the tunnel is formed, additional gas which has diffused from within grains to the grain boundaries enters the tunnel and is immediately released to the free surface. The gas accumulated at the grain boundaries also re-dissolves into the grains at a constant rate.

Analysis for the intragranular gas atoms includes trapping of the gas by the intragranular bubbles, or re-dissolution of the gas from the bubbles into the matrix.

## (2)-2 Diffusion accompanied by trapping

Figure 2.22 shows states of intragranular gas bubbles and intergranular gas bubbles in a pellet, and Fig. 2.23 shows an ideal model of crystal grains of a pellet.


Fig. 2.22 Schematics of intragranular and intergranular gas bubbles in a pellet.


Fig. 2.23 Ideal model of crystal grains of a pellet.
The grain shown in Fig. 2.23 is illustrated as if it were covered with a spherical shell blanket boundary. However, an actual grain boundary is a thin membrane layer separating adjacent crystal grains.

The relative amounts of gas dissolved in the matrix and present in intragranular bubbles depend on the equilibrium between trapping and re-dissolution. The gas dissolved in the matrix moves toward the grain boundary by concentration-gradient diffusion.

The gas diffusion rate in a spherical solid matrix with a radius of a is given by the following equation in which trapping and re-dissolution are taken into consideration ${ }^{(16)}$.

$$
\begin{equation*}
\frac{\partial c}{\partial t}=D\left(\frac{\partial^{2} c}{\partial r^{2}}+\frac{2}{r} \frac{\partial c}{\partial r}\right)-g c+b^{\prime} m+\beta \tag{2.1.100}
\end{equation*}
$$

Here,
$c$ : number of gas atoms dissolved per unit volume of solid matrix (atoms $/ \mathrm{cm}^{3}$ )
$D$ : diffusion coefficient of gas atoms $\left(\mathrm{cm}^{2} / \mathrm{s}\right)$
$g:$ rate of trapping of gas by intragranular bubbles $\left(\mathrm{s}^{-1}\right)$
$b^{\prime}$ : rate of re-dissolution of gas into solid phase $\left(s^{-1}\right)$
$m$ : number of gas atoms per unit bubble volume (atoms $/ \mathrm{cm}^{3}$ )
$\beta:$ generation rate of the gas per unit volume of pellet (atoms $/ \mathrm{cm}^{3} / \mathrm{s}$ ).
The gas equilibrium between trapping and re-dissolution is

$$
\begin{equation*}
\frac{\partial m}{\partial t}=g c-b^{\prime} m \tag{2.1.101}
\end{equation*}
$$

When the time-course change of $m$ can be neglected in the equilibrium state,
eq.(2.1.101) is simplified as

$$
\begin{equation*}
g c=b^{\prime} m \tag{2.1.102}
\end{equation*}
$$

Addition of eqs. (2.1.100) and (2.1.101) gives

$$
\begin{equation*}
\frac{\partial(c+m)}{\partial t}=D\left(\frac{\partial^{2} c}{\partial r^{2}}+\frac{2}{r} \frac{\partial c}{\partial r}\right)+\beta \tag{2.1.103}
\end{equation*}
$$

In the meantime, the following equation is obtained from eq. (2.1.102).

$$
\begin{equation*}
c+m=\frac{b^{\prime}+g}{b^{\prime}} c \tag{2.1.104}
\end{equation*}
$$

Substituting the above equation into eq. (2.1.103),

$$
\begin{equation*}
\frac{\partial(c+m)}{\partial t}=\frac{D b^{\prime}}{b^{\prime}+g}\left(\frac{\partial^{2}(c+m)}{\partial r^{2}}+\frac{2}{r} \frac{\partial(c+m)}{\partial r}\right)+\beta \tag{2.1.105}
\end{equation*}
$$

is obtained. Setting the sum of the number of gas atoms in the solid matrix and the number of those in the intra-granular bubbles as

$$
\begin{equation*}
\Psi=c+m \tag{2.1.106}
\end{equation*}
$$

the diffusion equation in the intra-granular spherical coordinate system, including trapping, is

$$
\begin{equation*}
\frac{\partial \Psi}{\partial t}=+D^{\prime}\left(\frac{\partial^{2} \Psi}{\partial r^{2}}+\frac{2}{r} \frac{\partial \Psi}{\partial r}\right)+\beta \tag{2.1.107}
\end{equation*}
$$

Here,

$$
\begin{equation*}
D^{\prime}=\frac{b^{\prime} D}{b^{\prime}+g} \tag{2.1.108}
\end{equation*}
$$

and $\Psi$ represents the apparent average number of gas atoms per unit intragranular volume regardless of the location of the gas (i.e., whether it is present in the matrix or in the intragranular bubbles). $D^{\prime}$ is the apparent diffusion cocfficient, which includes the trapping effect.

Next, to solve eq.(2.1.107), first $g$ and $b^{\prime}$ are obtained. Assuming that $N$ intragranular gas bubbles with an average radius of $\bar{R}$ are present per unit volume, $\bar{R}$ and $N$ are related as follows in an equilibrium state during irradiation ${ }^{(17)}$.

$$
\begin{align*}
& \text { JAERI-Data/Code 97-043 } \\
& N=1.52 \alpha / \pi \lambda\left(\bar{R}+Z_{o}\right)^{2} \tag{2.1.109}
\end{align*}
$$

Here,
$N$ : intragranular bubble density (bubbles $/ \mathrm{cm}^{3}$ )
$\bar{R} \quad$ : average radius of intragranular bubbles (cm)
$Z_{0} \quad: \quad$ affected zone (cm)
$\alpha$ : bubble generation rate (= 24 bubbles/fission fragment)
$\lambda:$ range $\left(6 \times 10^{-4} \mathrm{~cm}\right)$.

Fitting parameter APORE The affected zone of fission $Z_{0}$ is given as the input parameter APORE. The default value of APORE is $0.0(\mathrm{~cm})$.

The rate of trapping by intra-granular bubbles, $g$, is given by ${ }^{(18)}$

$$
\begin{equation*}
g=4 \pi D \bar{R} N \tag{2.1.110}
\end{equation*}
$$

$$
\begin{aligned}
\bar{R} & : \text { average intragranular bubble radius (cm) } \\
N & : \text { intragranular bubble density (bubbles } / \mathrm{cm}^{3} \text { ) }
\end{aligned}
$$

The rate of re-dissolution of the gas into the matrix is given by

$$
\begin{equation*}
b^{\prime}=3.03 F \pi \lambda\left(\bar{R}+Z_{0}\right)^{2} \tag{2.1.111}
\end{equation*}
$$

Here,
$F:$ fission rate (fissions $/ \mathrm{cm}^{3} / \mathrm{s}$ )
$\lambda:$ range $\left(=6 \times 10^{-4} \mathrm{~cm}\right)$
$Z_{0}$ : affected zone (cm).

## Fitting parameter BFCT

The rate of redissolution in the solid phase is controlled using BFCT.
$b^{\prime}=b^{\prime} \times$ BFCT $\quad$ (Default value: 1.0)
$\bar{R}$ is obtained using van der Waals' state equation, which is

$$
\begin{equation*}
\left(P_{0}+\frac{2 \gamma}{\bar{R}}\right)\left(V-m^{\cdot} B\right)=m^{\cdot} k T \tag{2.1.112}
\end{equation*}
$$

where
$\bar{R}:$ average intragranular bubble radius (cm)
$P_{0}:$ external force applied on intragranular bubbles (dyn/ $\mathrm{cm}^{2}$ )
$\gamma:$ surface tension ( $626 \mathrm{erg} / \mathrm{cm}^{2}$ )
$V$ : intragranular bubble volume $\left(=\frac{4}{3} \pi \bar{R}^{3} \mathrm{~cm}^{3}\right)$
$B:$ van der Waals' constant $\left(=8.5 \times 10^{-23} \mathrm{~cm}^{3} /\right.$ atom $)$

$$
\begin{aligned}
& m^{*}: \text { number of gas atoms per unit bubble volume (atoms/bubble) } \\
& k: \text { Boltzmann's constant }\left(=1.38 \times 10^{-16} \mathrm{erg} / \mathrm{K}\right) \\
& T: \\
& \text { temperature }(\mathrm{K}) .
\end{aligned}
$$

Since $\bar{R}$ is very small, less than $1 \mathrm{~nm}, 2 \gamma / \bar{R} \gg P_{0}$ holds and $P_{0}$ can be neglected. Setting $P_{0}=0$, eq. (2.1.112) is solved in terms of $m^{*}$ as

$$
\begin{equation*}
m^{*}=\frac{8 \pi \gamma \bar{R}}{3(2 \gamma B+k T \bar{R})} \tag{2.1.113}
\end{equation*}
$$

In the denominator of eq. (2.1.113), since $k T \bar{R}$ is smaller than $2 \gamma B$, when $k T \bar{R}$ is neglected,

$$
\begin{equation*}
m^{\prime}=\frac{4 \pi \gamma \bar{R}}{3 B} \tag{2.1.114}
\end{equation*}
$$

is obtained.
Meanwhile, from the equation describing the phase equilibrium between trapping and redissolution,

$$
\begin{equation*}
g c=b^{\prime} m \tag{2.1.102}
\end{equation*}
$$

is converted to the following equation of $m^{*}$ using $\quad m^{=} m^{*} N$ and $c=\Psi-m$.

$$
\begin{equation*}
\left(b^{\prime}+g\right) m^{*} N=g \Psi \tag{2.1.115}
\end{equation*}
$$

By substituting eqs.(2.1.110), (2.1.111) and (2.1.114) into eq.(2.1.115), the following equation is obtained.

$$
\begin{equation*}
\left(3.03 F \pi \lambda\left(\bar{R}+Z_{0}\right)^{2}+4 \pi D \bar{R} N\right) \frac{\bar{R}^{2}}{3 B}=D \Psi \tag{2.1.116}
\end{equation*}
$$

Then, by substituting eq. (2.1.109) and rearranging the equation, the following equation of $\bar{R}$ is obtained.

$$
\begin{equation*}
\frac{3.03 F \pi \lambda\left(\bar{R}+Z_{0}\right)^{2} \bar{R}^{2}}{3 B}+\frac{4 D \cdot 1.52 \alpha \bar{R}^{3}}{3 B \lambda\left(\bar{R}+Z_{0}\right)^{2}}-D \Psi=0 \tag{2.1.117}
\end{equation*}
$$

The diffusion coefficient $D$ is given by the following equation derived by Turnbull. ${ }^{(19)}$

$$
\begin{equation*}
D=7.6 \times 10^{-10} \exp \left(-7 \times 10^{4} / R T\right)+S^{2} j \nu V+2 \times 10^{-40} F \quad\left(\mathrm{~m}^{2} / \mathrm{s}\right) \tag{2.1.118}
\end{equation*}
$$

Here,
$R$ : gas constant $=1.987 \mathrm{cal} / \mathrm{mol} / \mathrm{K}$
$T$ : temperature (K)
$S:$ atomic jump distance $=\Omega^{\frac{2}{3}}$

## Fitting parameter FACD

The diffusion coefficient is controlled using FACD. $D=D \times$ FACD (Default value: 1.0 )
$\Omega:$ atomic volume $=4.09 \times 10^{-29}\left(\mathrm{~m}^{2} / \mathrm{s}\right)$

$$
\begin{aligned}
& j v=10^{13} \exp \left(-5.52 \times 10^{4} / R T\right) \\
& V=\frac{\left(\partial_{s} S^{2}+Z V_{o}\right)}{2 Z}\left[\left(1+\frac{4 K^{\prime} Z}{j v\left(\partial_{s} S^{2}+Z V_{o}\right)^{2}}\right)^{\frac{1}{2}}-1\right]
\end{aligned}
$$

$$
\partial_{s}: \text { sink strength }=10^{15} \quad\left(\mathrm{~m}^{-2}\right)
$$

$$
Z: \text { number of loss points=2 }
$$

$$
K^{\prime}: \text { loss ratio per atom }=10^{4}
$$

$$
V_{0}=\exp \left(-5.52 \times 10^{4} / R T\right)
$$

$$
F: \text { fission rate }=10^{19}\left(\text { fission } / \mathrm{m}^{3} / \mathrm{s}\right)
$$

Figure 2.24 shows the temperature dependence of the diffusion coefficient.


Fig. 2.24 Temperature dependence of the diffusion coefficient.

## (2)-3 Solution of partial differential equation

To solve the partial differential equation (2.1.107), the weighted residuals finite element method developed by Galerkin is used. Equation (2.1.107) can be rewritten as

$$
\begin{equation*}
\frac{\partial \Psi}{\partial}-D^{\prime} \nabla^{2} \Psi-\beta=0 \tag{2.1.119}
\end{equation*}
$$

where an approximation function of the function $\Psi(t, r)$ is set as follows.

$$
\Psi(t, r) \approx \hat{\Psi}(t, r)=\sum_{j} \Psi_{j}(t) \phi_{j}(r)
$$

Here, $\phi_{J}(r)$ is an arbitrary known function called the basic function, and $\Psi$, is an unknown coefficient, where the residuals are represented as

$$
R_{\Psi}(t, r)=\frac{\partial \hat{\Psi}}{\partial t}-D^{\prime} \nabla^{2} \hat{\Psi}-\beta
$$

The coefficient $\left\{\Psi_{j}\right\}$ which provides the minimum residuals is determined. The coefficient $\left\{\Psi_{j}\right\}$ can be determined by requiring a condition in which weighted integration becomes zero. When the basic function is selected as a weight function, this requirement can be satisfied by the equation

$$
\begin{equation*}
\int R_{\Psi}(t, r) \phi_{i} d v=0 \tag{2.1.120}
\end{equation*}
$$

To satisfy eq. (2.1.120) for an arbitrary weight function of $\phi_{j}, R_{\psi(t, r)}=0$ must be satisfied. Therefore, eq. (2.1.120) is equivalent to eq. (2.1.119). Integrating eq. (2.1.120),

$$
\begin{align*}
& \int\left(\frac{\partial \hat{\Psi}}{\partial t}-D^{\prime} \nabla^{2} \hat{\Psi}-\beta\right) \phi_{i} d v=0 \\
& \int\left(\frac{\partial \hat{\Psi}}{\partial t}-\beta\right) \phi_{i} d v-\int D^{\prime} \nabla^{2} \hat{\Psi} \phi_{i} d v=0 \tag{2.1.121}
\end{align*}
$$

are obtained. The second term of eq. (2.1.121) can also be expressed as

$$
\begin{aligned}
-\int_{i} D^{\prime} \nabla^{2} \hat{\Psi} \phi_{i} d v & =-D^{\prime}\left[\int \nabla \cdot\left(\phi_{i} \nabla \hat{\Psi}\right) d v-\int(\nabla \hat{\Psi}) \cdot\left(\nabla \phi_{i}\right) d v\right] \\
& =-D^{\prime} \int_{\varnothing \nabla} \phi_{i} \nabla \hat{\Psi} \cdot d \bar{s}+D^{\prime} \int(\nabla \hat{\Psi}) \cdot(\nabla \phi)_{i} d v
\end{aligned}
$$

Here, when a weight function which satisfies $\phi_{j}=0$ at the grain boundary $\partial$ is selected, the
surface integration term is eliminated and eq. (2.1.121) is expressed as

$$
\begin{equation*}
\left.\int\left(\frac{\partial \hat{\Psi}}{\partial t}-\beta\right) \phi_{i} d v+D^{\prime}\right\rfloor(\nabla \hat{\Psi}) \cdot\left(\nabla \phi_{i}\right) d v=0 \tag{2.1.122}
\end{equation*}
$$

When a pellet grain is divided into finite elements, eq. (2.1.122) is expressed for a certain element $V_{e}$ as

$$
\begin{equation*}
\sum_{j}\left(\dot{\Psi}_{j} E_{\mu}+D^{\prime} \Psi, A_{\mu}\right)-\beta H_{i}=0 \tag{2.1.123}
\end{equation*}
$$

where

$$
\begin{aligned}
E_{j i} & =\int_{i e} \phi_{j} \phi_{i} d v \\
A_{j i} & =\int_{i e} \frac{\partial \phi_{1}}{\partial} \frac{\partial \phi_{i}}{\partial r} d v \int_{v_{e}} \\
H_{i} & =\int_{e} \phi_{i} d v
\end{aligned}
$$

The following quadratic functions are adopted as basic functions $\phi_{j}$.

$$
\begin{align*}
& \phi_{1}(\xi)=-\frac{1}{2} \xi(1-\xi) \\
& \phi_{2}(\xi)=1-\xi^{2}  \tag{2.1.124}\\
& \phi_{3}(\xi)=\frac{1}{2}(1+\xi) \xi
\end{align*}
$$

Using these basic functions, $E_{j i}, A_{j i}$ and $H_{i}$ in eq.(2.1.123) are represented using $R_{k}$, i.e., coordinates of the midpoint of element $V e$, and $\Delta R$, i.e., half-width of the element, as follows.

$$
\begin{align*}
E_{j i} & =\int_{l_{e}} \phi_{j} \phi_{i} d v=4 \pi \int_{R_{k}-\Delta R}^{R_{k}+\Delta R} \phi_{j} \phi_{i} r^{2} d r \\
& =4 \pi \Delta R \int_{-1} \phi_{j} \phi_{i}\left(R_{k}+\Delta R \xi\right)^{2} d \xi \\
A_{j i}= & \int_{i i} \frac{\partial \phi_{i}}{\partial r} \frac{\partial \phi_{j}}{\partial r} d v=4 \pi \int_{R_{k}-\Delta R}^{R_{k}+\Delta R} \frac{\partial \phi_{i}}{\partial r} \frac{\partial \phi_{j}}{\partial} r^{2} d r \\
= & \frac{4 \pi}{\Delta R} \int_{-1} \frac{\partial \phi_{i}}{\partial \xi} \frac{\partial \phi_{j}}{\partial \xi}\left(R_{k}+\Delta R \xi\right)^{2} d \xi  \tag{2.1.125}\\
H_{i} & =\int_{v e} \phi_{i} d v=4 \pi \int_{R_{k}-\Delta R}^{R_{k}+\Delta R} \phi_{i} r^{2} d r=4 \pi \Delta R \int_{-1} \phi_{j}\left(R_{k}+\Delta R \xi\right)^{2} d \xi
\end{align*}
$$

Next, eq. (2.1.123) is represented by an implicit formula ( $Q$ is a constant).

$$
\begin{equation*}
\sum_{j}\left\{\frac{\Psi_{j}^{n+1}-\Psi_{j}^{n}}{\Delta t} E_{i j}+D^{*}\left((1-\theta) \Psi_{j}^{n}+\theta \Psi_{j}^{n+1}\right) A_{j i}\right\}-\beta^{*} H_{i}=0 \tag{2.1.126}
\end{equation*}
$$

Here,

$$
\begin{gathered}
D^{\prime}=(1-\theta) D^{\prime n}+\theta D^{\prime n+1} \\
\beta^{\prime}=(1-\theta) \beta^{n}+\theta \beta^{n+1} .
\end{gathered}
$$

Through rearrangement of the unknown and known values of eq. (2.1.126),

$$
\begin{equation*}
\sum_{j}\left(\frac{1}{\Delta t} E_{i j}+D^{*} \theta A_{j}\right) \Psi_{j}^{n+1}=\sum_{j}\left(\frac{1}{\Delta t} E_{i j}-D^{*}(1-\theta) A_{j \prime}\right) \Psi_{j}^{n}+\beta^{*} H_{i} \tag{2.1.127}
\end{equation*}
$$

is obtained. Therefore, the element matrix $W_{i j}$ and the element vector $Q_{i}$ are

$$
\begin{gather*}
W_{i j}=\frac{1}{\Delta k} E_{i j}+D^{*} \theta A_{j i}  \tag{2.1.128}\\
Q_{i}=\sum_{j}\left(\frac{1}{\Delta t} E_{i j}-D^{*}(1-\theta) A_{j i}\right) \Psi^{n}+\beta^{*} H_{i} \tag{2.1.129}
\end{gather*}
$$

Through superimposition of the equations for all elements and setting of the condition of $\Psi^{n+1}=0$ on the surface, $\left\{\Psi_{j}^{n+1}\right\}$ can be obtained by solving the simultaneous equations below.

$$
\begin{equation*}
\left[W_{i j}\right]\left\{\Psi_{j}^{n+1}\right\}=\left\{Q_{i}\right\} \tag{2.1.130}
\end{equation*}
$$

(2)-4 Sweeping of gas into grain boundary by grain growth, and re-dissolution of the gas from inter-granular gas bubbles into grains

During grain growth, the gas in grains is swept into the grain boundary. The rate of gas sweeping into the grain boundary is given as

$$
\begin{equation*}
f_{g}=\left(\frac{a^{n+1}}{a^{n}}\right)^{3}-1 \tag{2.1.131}
\end{equation*}
$$

Here,

$$
\begin{aligned}
a^{n+1} & : \text { grain size after grain growth }(\mathrm{cm}) \\
a^{n} & : \text { grain size before grain growth }(\mathrm{cm}) .
\end{aligned}
$$

## Fitting parameter FGG

The rate of gas sweepings is controlled with FGG as $f_{g}=f_{g} \times \mathrm{FGG}$.

Figure 2.25 shows a conceptual schematic of the grain growth. The gas present in the region with diagonal lines is released at the grain boundary during grain growth.


Fig. 2.25 Conceptual diagram of grain growth.
The grain growth model uses the following Itoh's equation as a representative one. ${ }^{(20)}$

$$
\begin{align*}
& \frac{d a}{d t}=K\left(\frac{1}{a}-\frac{1+N_{f} / N_{f}{ }^{\max }}{a_{m}}\right)(\mu \mathrm{m} / \mathrm{h})  \tag{2.1.132}\\
& K=5.24 \times 10^{7} \exp \left(-2.67 \times 10^{5} / R T\right)\left(\mu \mathrm{m}^{2} / \mathrm{h}\right)
\end{align*}
$$

$a$ : grain size at current time step ( $\mu \mathrm{m}$ )
$a_{m} \quad:$ maximum grain size $\left(=2.23 \times 10^{3} \exp (-7620 / T)\right)(\mu \mathrm{m})$
$R:$ gas constant $(=8.314 \mathrm{~J} / \mathrm{mol} / \mathrm{K})$
$N_{f} \quad$ : gas atom density at grain boundary (atoms $/ \mathrm{cm}^{2}$ )
$N_{f}^{\max }:$ saturation value of the gas atom density at grain boundary (atoms $/ \mathrm{cm}^{2}$ )

## Fitting parameters AG and GRWF

The grain growth rate can be controlled using AG and GRWF as follows.

1) Control of the gas atom density: $N_{f}=N_{f} \times \mathrm{AG}$ (Default value: $\mathrm{AG}=1.5$ )
2) Grain growth rate: $\frac{d a}{d t}=\frac{d a}{d t} \times$ GRWF (Default value: GRWF $=1.0$ )

Selection of option IGRAIN The option of the grain growth model can be selected using IGRAIN as follows. IGRAIN $=0$ : Itoh's model(default), $=1$ : Ainscough model, =2: MacEwan model, =3: Lyons model, =4: MATPRO-09 model.

$$
\text { JAERI-Data/Code } 97-043
$$

Each grain consists of a maximum of 5 elements. The outermost element is the boundary layer, which is a special element for consideration of re-dissolution. When grain growth occurs during time step from n to $\mathrm{n}+1$, elements (mesh) in the grains are re-meshed.


Fig. 2.26 Meshing of a pellet grain.

Setting the boundary layer width as $2 \Delta R$, coordinates $r$ at the node of the first and second elements are given as

$$
\begin{equation*}
r^{n+1}=\frac{a^{n+1}-2 \Delta R}{a^{n}-2 \Delta R} r^{n} \tag{2.1.133}
\end{equation*}
$$

where

$$
\begin{array}{ll}
r^{n+1} & : \text { coordinates at the node point after grain growth } \\
r^{n} & : \text { coordinates at the node point before grain growth. }
\end{array}
$$

Coordinates at the three node points in the outermost boundary layer are given as $a^{n+1}-2 \Delta R, a^{n+1}-\Delta R$ and $a^{n+1}$.

Model parameters NODEG and RREL
The number of elements in grains is designated by NODEG. The default value is 3 , and the maximum value is 5. The width of layers other than the outermost layer, namely the elements of NODEG-1, is designated by the ratio RREL. The default value is 5,1 , which means that the ratio of the width of the first to second layers is $5: 1$.

The FP gas concentration $\Psi$ at a given set of coordinates after re-meshing is given by

$$
\begin{array}{lr}
\Psi^{n+1,0}(r)=\Psi^{n}(r) & \left(0 \leqq r \leqq a^{n}\right)  \tag{2.1.134}\\
\Psi^{n+1,0}(r)=0 & \left(a^{n} \leqq r \leqq a^{n+1}\right),
\end{array}
$$

where

# $\Psi^{n+1,0}(r)$ : initial concentration distribution of FP gas after grain growth $\Psi(r):$ FP gas concentration distribution before grain growth. 

Namely, it is assumed that sweeping of the gas into the grain boundary due to grain growth occurs instantaneously. Therefore, the initial value of the FP gas atom density per unit area at the grain boundary during grain growth is set as $N_{f}^{n+1,0}$ in calculation of its change between time step $n$ and time step $(n+1)$, and the following equation holds.

$$
\begin{equation*}
\left(\frac{a^{n+1}}{a^{n}}\right)^{3}\left(\bar{\Psi}_{\text {totat }}^{n}+4 \pi a^{n^{2}} N_{t}^{n}\right)=\bar{\Psi}_{\text {total }}^{n}+4 \pi a^{n+1^{2}} N_{f}^{n+1,0} \tag{2.1.135}
\end{equation*}
$$

Here,

$$
\begin{aligned}
\bar{\Psi}_{t o n a l}^{n}: & \text { number of FP gas atoms in grain before grain growth (atoms) } \\
N_{t}^{n}: & \text { FP gas atom density per unit area at the grain boundary before grain } \\
& \text { growth (atoms } / \mathrm{cm}^{2} \text { ), and } N_{f}^{0}=0 .
\end{aligned}
$$

Equation (2.1.135) is solved in terms of $N_{t}^{n+1,0}$, and the equation

$$
\begin{equation*}
N_{f}^{n+1,0}=\frac{f_{g} \bar{\Psi}_{\text {totoll }}^{n}}{4 \pi a^{n+1^{2}}}+\frac{a^{n+1}}{a^{n}} N_{f}^{n} \tag{2.1.136}
\end{equation*}
$$

holds.
Thus, the initial value for determination of the FP gas concentrations of both intragrain and intergrain at time step $(n+1)$ is obtained. Using the initial value and eq. (2.1.134), the FP gas concentration at the time step $(n+1)$ during grain growth will be calculated.

## (2)-5 FP gas redissolution

In the model of FP gas atom re-dissolution from grain boundary into grains, since the grain boundary separates adjacent crystal grains, we assume that half of the FP gas per unit area of the grain boundary is re-dissolved. Namely,

$$
\begin{equation*}
\frac{b N_{f}}{2} \cdot(\mathrm{ADDF})\left(\mathrm{atoms} / \mathrm{cm}^{2} / \mathrm{s}\right) \tag{2.1.137}
\end{equation*}
$$

where

$$
b: \text { rate of re-dissolution }\left(10^{-6} / \mathrm{s}\right)
$$

> Model parameter RB
> RB is a parameter for controlling the thickness of the boundary layer where FP gas redissolves. The default value of RB is $2 \times 10^{-8}(\mathrm{~cm})$.

Re-dissolution means physical transfer of FP gas from the grain boundary into grains, which is virtually equivalent to an additional generation of FP gas in grains. Therefore, when the thickness of regions where FP gas re-dissolves is assumed to be equal to the boundary layer thickness ( $200 \AA$ ), the apparent rate of FP gas generation $\beta^{\prime}$ in the boundary layer is determined.

Fitting parameter ADDF
The amount of gas redissolved is controlled using ADDF. The default value of ADDF is 9.0 .

Therefore, $\beta^{\prime}$ is given by the following equation.

$$
\begin{equation*}
\beta^{\prime}=\frac{b}{2}\left\{(1-\theta) N_{j}^{n}+\theta N_{f}^{n+1}\right\} \frac{1}{2 \Delta R}(\cdot A D D F)\left(\text { atoms } / \mathrm{cm}^{3} / \cdot \mathrm{s}\right) \tag{2.1.138}
\end{equation*}
$$

Here,
$N_{f}^{n}$ : concentration of FP gas atoms in the grain boundary at time step $n$ (atoms $/ \mathrm{cm}^{2}$ )
$N_{f}^{n+1}$ : concentration of FP gas atoms in the grain boundary at time step $(n+1)$ (atoms $/ \mathrm{cm}^{2}$ )
$\theta$ : interpolation parameter between time steps in the implicit solution, where values of $N_{f}^{n}$ and $N_{f}^{n+1}$ do not depend on the occurrence of grain growth.

Accordingly, $\beta$ in eq. (2.1.96) for the boundary layer is expressed as

$$
\begin{equation*}
\widetilde{\beta}=\beta+\beta^{\prime} \tag{2.1.139}
\end{equation*}
$$

and $\widetilde{\beta}$ is defined as the FP gas generation rate.
$N_{f}^{n+1}$ is expressed as

$$
\begin{equation*}
N_{f}^{n+1}=\frac{a^{n+1}}{a^{n}} N_{f}^{n}+\frac{\left(1+f_{g}\right) \bar{\Psi}_{\text {total }}^{n}-\bar{\Psi}_{\text {tatal }}^{n+1}+\int_{V} \beta \Delta t d v}{4 \pi a^{n+1^{2}}} \tag{2.1.140}
\end{equation*}
$$

Here,
$\bar{\Psi}_{\text {oratal }}^{n+1}:$ number of FP gas atoms in grains at time step $n+1$ (atoms)
$\beta \Delta t v d$ : amount of FP gas generated excluding the amount of re-dissolved atoms during the time step increment (atoms), where $\int_{V} d v=\frac{4}{3} \pi a^{n+1^{2}}$ holds.
$\bar{\Psi}_{\text {total }}^{n+1}$ is expressed as follows when the number of elements comprising each grain is 3 .

$$
\begin{equation*}
\bar{\Psi}_{l o t a l}^{n+1}=\sum_{e=1}^{3} \int_{i} 4 \pi r^{2} \hat{\Psi}^{n+1}(r) d r, \tag{2.1.141}
\end{equation*}
$$

$$
\begin{aligned}
& \text { JAERI-Data/Code } 97-043 \\
& \hat{\Psi}^{n+1}(r)=\sum_{j=1}^{3} \Psi_{j}^{n+1} \phi_{j}(r)
\end{aligned}
$$

## (2)-6 Gas release due to connection of intergranular gas bubbles

With irradiation, intergranular bubble density increases and the bubbles expand and become connected. Then, a certain point of the connected bubbles comes into contact with a crack or a channel which leads to a free space inside the fuel rod, and the bubble becomes an open bubble, i.e. non-isolated bubble, releasing the gas it contains into the free space.

The current model assumes that when the number of gas atoms per unit area at the grain boundary exceeds $N_{f}^{\text {max }}$, bubbles are connected and a tunnel leading to a free space is formed. It is also assumed that once the gas concentration at the grain boundary reaches a certain value, additional gas atoms diffused from grains are immediately released into the free space. $\quad N_{f}^{\text {max }}$ is given by the following equation. ${ }^{(17)}$

$$
\begin{equation*}
N_{f}{ }^{\max }=\frac{4 r_{f} f_{f}(\vartheta)}{3 k T \sin ^{2} \vartheta} f_{h}\left\{\frac{2 \gamma}{r_{f}}+P_{e x x}\right\} \tag{2.1.142}
\end{equation*}
$$

Here,

$$
\begin{equation*}
f_{f}(\vartheta)=1-\frac{3}{2} \cos \vartheta+\frac{1}{2} \cos ^{3} \vartheta \tag{2.1.143}
\end{equation*}
$$

$N_{f}^{\text {max }}$ : saturation value of the number of gas atoms per unit area at the grain boundary (atoms $/ \mathrm{cm}^{2}$ )
$r_{f}$ : intergranular gas bubble radius $\left(=0.5 \times 10^{-4} \mathrm{~cm}\right)$
$f(\delta)$ : volume ratio of lenticular bubble to sphere bubble
$\vartheta$ : lenticular bubble angle $\left(=50^{\circ}\right)$
$k$ : Boltzmann's constant ( $=1.38 \times 10^{-16} \mathrm{erg} / \mathrm{K}$ )
$T$ : temperature (K),
$\gamma:$ surface tension ( $=626 \mathrm{erg} / \mathrm{cm}^{2}$ )
$f_{b}$ : covering ratio of lenticular bubbles over grain boundary $(=0.2)$ $P_{e x t}:$ external force (dyne $/ \mathrm{cm}^{2}$ )

The external pressure $P_{e x t}$ is obtained using a procedure described below, taking into account the plenum pressure, contact pressure between pellet and cladding, and pellet internal thermal stress.

To calculate the pellet thermal stress, the finite element method is generally applied to determine the strict values of temperature distribution inside the pellet, as in the case of the thermal analysis part. However, in the case of the current model, a simplified method in which approximate temperature distribution and thermal stresses are obtained by the use of an analytical solution is adopted. That is, using the restriction equation of Lame, the temperature distribution inside the pellet is set as follows.

$$
\begin{equation*}
T-T_{s}=\left(T_{c}-T_{s}\right)\left\{1-(r / R)^{2}\right\} \tag{2.1.144}
\end{equation*}
$$

Here,
$T$ : temperature at radius r
$T_{s}$ : pellet surface temperature
$T_{c}$ : pellet center temperature
$R$ : pellet outer radius
Then, the pellet internal thermal stress is expressed as

$$
\begin{align*}
& \sigma_{r}=\frac{E}{4(1-v)} a\left(T_{c}-T_{s}\right)\left\{\left(\frac{r}{R}\right)^{2}-1\right\}-P_{i}  \tag{2.1.145}\\
& \sigma_{\theta}=\frac{E}{4(1-v)} a\left(T_{c}-T_{s}\right)\left\{3\left(\frac{r}{R}\right)^{2}-2\right\}-P_{i}  \tag{2.1.146}\\
& \sigma_{z}=\frac{E}{4(1-v)} a\left(T_{c}-T_{s}\right)\left\{4\left(\frac{r}{R}\right)^{2}-1\right\}-P_{i}, \tag{2.1.147}
\end{align*}
$$

where

$$
\sigma_{r}, \sigma_{\theta}, \sigma_{z}: \text { stress in the } r, \theta \text { and } z \text { directions }
$$

$E \quad$ : Young's modulus of pellet
$v$ : Poisson's ratio of pellet
$a$ : thermal expansion coefficient of pellet
$P_{i} \quad$ : contact pressure between pellet and cladding
$P_{f}$ : pellet axial force.
Here, the contact pressure between pellet and cladding which was obtained in the thermal analysis is used as $P i$, and the pellet axial force is set to be equal to the contact pressure ( $P_{f}=P_{i}$ ), for convenience.

The average stress $\bar{\sigma}$ is set as

$$
\begin{equation*}
\bar{\sigma}=\frac{1}{3}\left(\sigma_{r}+\sigma_{\theta}+\sigma_{z}\right) \tag{2.1.148}
\end{equation*}
$$

The stress calculation method is described below.
First, a method to calculate stresses in the $n+l$ time step, $\sigma_{r, n+1}, \sigma_{\theta, n+1}$ and $\sigma_{z, n+1}$, from the stresses obtained in the $n$ time step, $\sigma_{r, n}, \sigma_{\theta, n}$ and $\sigma_{z, n}$, is considered. Here, stresses in the 0th time step (i.e. hot stand-by), $\sigma_{r, 0}, \sigma_{\theta, 0}$ and $\sigma_{z, 0}$, are assumed to equal the plenum gas pressure. Using eqs.(2.1.145), (2.1.146) and (2.1.147), the thermal stress increments between time steps are obtained as

$$
\begin{align*}
\Delta \sigma_{r, n+1}^{\text {ih }}= & \frac{E_{n+1}}{4(1-v)} a_{n+1}\left(T_{c, n+1}-T_{s, n+1}\right)\left\{\left(\frac{r}{R}\right)^{2}-1\right\}-P_{i, n+1} \\
& -\left\{\frac{E_{n}}{4(1-v)} a_{n}\left(T_{c, n}-T_{s, n}\right)\left\{\left(\frac{r}{R}\right)^{2}-1\right\}-P_{i, n}\right\}  \tag{2.1.149}\\
\Delta \sigma_{\theta, n+1}^{\text {th }}= & \frac{E_{n+1}}{4(1-v)} a_{n+1}\left(T_{c, n+1}-T_{s, n+1}\right)\left\{\left(3 \frac{r}{R}\right)^{2}-2\right\}-P_{i, n+1} \\
& -\left\{\frac{E_{n}}{4(1-v)} a_{n}\left(T_{c, n}-T_{s, n}\right)\left\{\left(3 \frac{r}{R}\right)^{2}-2\right\}-P_{i, n}\right\}  \tag{2.1.150}\\
\Delta \sigma_{z, n+1}^{\text {th }}= & \frac{E_{n+1}}{4(1-v)} a_{n+1}\left(T_{c, n+1}-T_{s, n+1}\right)\left\{4\left(\frac{r}{R}\right)^{2}-1\right\}-P_{i, n+1}  \tag{2.1.151}\\
& -\left\{\frac{E_{n}}{4(1-v)} a_{n}\left(T_{c, n}-T_{s, n}\right)\left\{4\left(\frac{r}{R}\right)^{2}-1\right\}-P_{i, n}\right\} .
\end{align*}
$$

The 0th approximation of the stresses in the $n+$ /time step is set as

$$
\begin{align*}
& \sigma_{r, n+1}^{0}=\sigma_{r, n}+\Delta \sigma_{r, n+1}^{i t}  \tag{2.1.152}\\
& \sigma_{\theta, n+1}^{0}=\sigma_{\theta, n}+\Delta \sigma_{\theta, n+1}^{i n}  \tag{2.1.153}\\
& \sigma_{z, n+1}^{0}=\sigma_{z, n}+\Delta \sigma_{z, n+1}^{t h} . \tag{2.1.154}
\end{align*}
$$

Substituting eqs.(2.1.152), (2.1.153) and (2.1.154) into eq. (2.1.148), the 0th approximation of the average stress $\bar{\sigma}_{n+1}^{0}$ is obtained as

$$
\begin{equation*}
\bar{\sigma}_{n+1}^{0}=\frac{1}{3}\left(\sigma_{r, n+1}^{0}+\sigma_{\theta, n+1}^{0}+\sigma_{z, n+1}^{0}\right) . \tag{2.1.155}
\end{equation*}
$$

Here, when $\bar{\sigma}_{n+1}^{0}$ is less than the plenum gas pressure $P_{g a r}$,

$$
\begin{equation*}
\bar{\sigma}_{n+1}^{0}=P_{\operatorname{gas}, n+1} \tag{2.1.156}
\end{equation*}
$$

holds. When $\bar{\sigma}_{n+1}^{0}$ is larger than the yielding stress $\sigma_{Y}$,

$$
\begin{equation*}
\bar{\sigma}_{n+1}^{0}=\sigma_{Y, n+1} \tag{2.1.157}
\end{equation*}
$$

is set.
Next, calculation of thermal stress alleviation by creep is carried out in an approximate manner, by setting the equivalent stress $\sigma_{e q}$ as

$$
\sigma_{e q}=\left|\bar{\sigma}_{n+1}^{0}\right| .
$$

The change of equivalent creep strain is assumed to be in proportion to the creep rate determined by a creep function $f$ (MATPRO-09 equation ${ }^{(14)}$ ), and $\eta$ is set as a proportion coefficient, the following holds:

$$
\begin{equation*}
\Delta \bar{\varepsilon}_{n+1}^{\mathrm{c}}=f\left(T, \sigma_{v q}, G, f_{d}, \dot{F}\right) \cdot \eta \cdot \Delta t \tag{2.1.158}
\end{equation*}
$$

where
$T$ : temperature
$\sigma_{e q}:$ equivalent stress
$G:$ grain size
$f_{d}$ : pellet theoretical density ratio
$\dot{F}$ : fission density
$\Delta t:$ time step width.
Here, $\eta=10^{-4}$ is adopted as an empirically obtained fitting parameter.
By substitution of the thus obtained $\Delta \bar{\varepsilon}_{n+1}^{c}$ into the equation

$$
\begin{equation*}
\bar{\sigma}_{n+1}^{1}=\bar{\sigma}_{n+1}^{0}+E \Delta \bar{\varepsilon}_{n+1}^{c}, \tag{2.1.159}
\end{equation*}
$$

the first approximation of the average stress $\bar{\sigma}_{n+1}^{1}$ is obtained. However, proportion coefficient between $\sigma$ and $\Delta \varepsilon$ in creep deformation is set as the pellet Young's modulus itself on the assumption that the coefficient depends linearly on the Young's modulus.

Thereafter, a convergence calculation regarding $\sigma_{n+1}$ is performed using the Newton-

Raphson method, on the assumption that $-\sigma_{Y, n+1} \leq \bar{\sigma}_{n+1} \leq-P_{\text {gar,n+1 }}$. The obtained $\bar{\sigma}_{n+1}$ is the thermal stress for grain boundary bubble gas. Therefore, $P_{e x t}=\bar{\sigma}_{n+1}$ holds. Namely, this stress acts on the bubbles as an external pressure $P_{\text {ext }}$ in eq.(2.1.142).

The stresses in the $n+1$ time step $\sigma_{r, n+1}, \sigma_{\theta, n+1}$ and $\sigma_{z, n+1}$ are obtained as

$$
\begin{align*}
& \sigma_{r, n+1}=\sigma_{r, n}+\Delta \sigma_{r, n+1}^{\prime t}+E \Delta \bar{\varepsilon}_{n+1}^{c} \\
& \sigma_{\theta, n+1}=\sigma_{\theta, n}+\Delta \sigma_{\theta, n+1}^{\text {th }}+E \Delta \bar{\varepsilon}_{n+1}^{c}  \tag{2.1.160}\\
& \sigma_{z, n+1}=\sigma_{z, n}+\Delta \sigma_{z, n+1}^{t h}+E \Delta \bar{\varepsilon}_{n+1}^{c} .
\end{align*}
$$

Here, $\sigma_{i, n+1}<0$, namely the stress is compressive.

## Selection of option IPEXT <br> Regarding the $P_{\text {ext }}$ evaluation method, a condition can

 be selected from among the following 8 conditions using IPEXT. The default value of IPEXT $=1$.$\mathrm{IPEXT}=0: P_{\text {ext }}=0, \quad$ IPEXT=I: $P_{\text {ext }}=$ plenum pressure, $\quad \mathrm{IPEXT}=2: P_{\text {exi }}=$ contact pressure between pellet and cladding, IPEXT $=3: P_{\text {exi }}=\max$ (plenum pressure, contact pressure), IPEXT=11: $P_{\text {ext }}=$ thermal stress (taking into account the plenum pressure), IPEXT $=12$ : $P_{\text {ext }}=$ thermal stress (taking into account the contact pressure between pellet and cladding),
IPEXT $=13$ : $P_{\text {exx }}=$ thermal stress (taking into account the plenum pressure and contact pressure),
IPEXT $=14$ : $P_{e x r}=$ average stress obtained by stress calculation in Detailed Mechanical Analysis (I). Here, when Detailed Mechanical Analysis (II) is used, the results will be the same as those in the case of IPEXT $=13$.

## Fitting parameters OPORO, FBSAT, ALHOT In the mechanistic model

 (IGASP=0), fraction of open gas bubbles of FP at grain boundary is designated by OPORO. The default value is 0.0 . FBSAT gives a multiplication factor for the saturation amount of gas at grain boundary. The default value is 1.0 .$\eta$ in eq.(2.1.158) can be designated by ALHOT. The default value is 0.0001 .

## (2)-7 Determination of time-step width

In the mechanistic FP gas release model, the calculation is performed with an original time-step width that is determined using apparent diffusion coefficient $D^{\prime}$ and node interval in the second layer $\Delta R_{2}$ as

$$
\begin{equation*}
\Delta t=\frac{\Delta R_{2}^{2}}{D^{\prime}} \times 0.05 \times \text { FMULT } . \tag{2.1.161}
\end{equation*}
$$

FMULT Fitting parameter for controlling time-step width. The default value is 1.0 .

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```


### 2.1.5 Gas diffusion and flow in the gap

(1) Assumptions and methods

Diffusion and flow calculation of gap gas is based on the following assumptions.
(1) Helium and Nitrogen (or Argon), as well as Xenon and Krypton are completely mixed instantaneously; therefore, behavior of Nitrogen (or Argon) is represented by that of Helium, and also behavior of Krypton is represented by that of Xenon. Thus, calculation is performed for a 2 -component mixed gas, i.e. mixture of Helium and Xenon.
(2) Counter-diffusion occurs with Helium and Xenon which pass through the gap.
(3) The counter-diffusion calculation is performed using an implicit solution based on Fick's first law. The diffusion is independent of flow caused by pressure difference in the fuel rod.
(4) Pressure inside the fuel rod is uniform during the diffusion calculation.
(5) Pressures at different parts inside the fuel rod are assumed to be equilibrated instantaneously. Therefore, gas flow between the axial segments induced by the pressure difference in the fuel rod also occurs instantaneously.

## (2) Equation for the gap region

The following is a list of symbols used.

$$
\begin{aligned}
& N \text { : gas molar number (mol) } \\
& n \text { : molar density }\left(\mathrm{mol} / \mathrm{cm}^{3}\right) \\
& D^{12} \text { : counter-diffusion constant }\left(\mathrm{m}^{2} / \mathrm{s}\right)\left(D^{12}=D^{21}\right) \\
& T \text { : temperature (K) } \\
& V \text { : volume }\left(\mathrm{m}^{3}\right) \\
& C \text { : molar fraction }\left(C_{1}=n_{1} /\left(n_{1}+n_{2}\right)\right)
\end{aligned}
$$

Subscripts are
$I:$ kind of gas ( $1=$ Xenon, $2=$ Helium ,
$j$ : axial segment $\left(j=P_{L}, 1,2,3, \cdots, N, P_{U}\right)\left(P_{L}:\right.$ lower plenum, $P_{U}$ : upper plenum $)$.
In particular, subscripts for molar density are
$n_{i j}$ : density of gas $i$ at axial segment $j$,
$n_{j}$ : density of all gases at axial segment $j$.

Figure 2.27 shows the present model of calculation.


Fig. 2.27 Gas diffusion and flow model.
The total amount of gas $i$ at axial segment $j$ is

$$
\begin{align*}
N_{i, j} & =n_{t, j} V_{j} \\
& =C_{t, j} n_{j} V_{j}=\frac{P}{R} C_{i, j} \frac{V_{j}}{T_{j}} . \tag{2.1.162}
\end{align*}
$$

Here, each segment has a channel cross-sectional area of $S_{j}$ and length of $2 l_{j}$; also, the boundary of segments $j$ and $j+1$ is indicated by *.

The amount of gas $1(\mathrm{Xe}) G_{1}(j \rightarrow j+1)$ flowing from segment $j$ to segment $j+1$ over the boundary * is obtained on the basis of Fick's law,

$$
\begin{equation*}
G_{1}\left(j \rightarrow^{*}\right)=S_{j} D_{j}^{12} \frac{n_{1, j}-n_{1,},}{l_{j}} . \tag{2.1.163}
\end{equation*}
$$

Similarly, the amount of gas $1(\mathrm{Xe})$ flowing into segment $j+1$ over * is represented as

$$
\begin{equation*}
G_{1}(* \rightarrow j+1)=S_{j+1} D_{j+1}^{12} \frac{n_{1 *}-n_{1, j+1}}{l_{j+1}} . \tag{2.1.164}
\end{equation*}
$$

From the continuous condition,

$$
G_{1}\left(j \rightarrow^{*}\right)=G_{1}(* \rightarrow j+1)
$$

holds and

$$
\begin{equation*}
S_{j} D_{j}^{12} \frac{n_{1, j}-n_{1,0}}{l_{j}}=S_{j+1} D_{j+1}^{12} \frac{n_{1}-n_{1, j+1}}{l_{j+1}} \tag{2.1.165}
\end{equation*}
$$

can be obtained. By solving this equation for $n_{1,0}$, we obtain

$$
\begin{equation*}
n_{1,}=\frac{S_{j} D_{j}^{12} l_{j+1} n_{1, j}+S_{j+1} D_{j+1}^{12} l_{j} n_{1, j+1}}{S_{j+1} D_{j+1}^{12} l_{j}+S_{j} D_{j}^{12} l_{j+1}} . \tag{2.1.166}
\end{equation*}
$$

Using eq. (2.1.163), we obtain the following equation.

$$
\begin{align*}
G_{1}(j \rightarrow j+1) & =G_{1}\left(j \rightarrow{ }^{*}\right) \\
& =\frac{S_{j} D_{j}^{12} S_{j+1} D_{j+1}^{12}}{S_{j+1} D_{j+1}^{12} l_{j}+S_{j} D_{j}^{12} l_{j+1}}\left(n_{1, j}-n_{1, j+1}\right) \tag{2.1.167}
\end{align*}
$$

Here, by setting

$$
\begin{equation*}
F_{j, j+1}=\frac{S_{j} D_{j}^{12} S_{j+1} D_{j+1}^{12}}{S_{j+1} D_{j+1}^{12} l_{j}-S_{j} D_{j}^{12} l_{j+1}} \tag{2.1.168}
\end{equation*}
$$

eq. (2.1.167) is expressed as

$$
\begin{equation*}
G_{1}(j \rightarrow j+1)=F_{j, j+1}\left(n_{1, j}-n_{1, j+1}\right) . \tag{2.1.169}
\end{equation*}
$$

Meanwhile, regarding gas $2(\mathrm{He})$,

$$
\begin{equation*}
G_{2}(j \rightarrow j+1)=F_{j, j+1}\left(n_{2, j}-n_{2, j+1}\right) \tag{2.1.170}
\end{equation*}
$$

is obtained.
Through addition of eqs.(2.1.169) and (2.1.170), the total amount of inflow mixed gas can be calculated as

$$
\begin{equation*}
G(j \rightarrow j+1)=F_{j, j+1}\left(n_{j}-n_{j+1}\right) . \tag{2.1.171}
\end{equation*}
$$

Here, the next equation

$$
n_{j}=n_{1, j}+n_{2, j}, n_{j+1}=n_{1, j+1}+n_{2, j+1}
$$

holds.
Since in general, the gap temperatures at segments $j$ and $j+1$ differ, the following equation holds in the equilibrium state.

$$
\begin{equation*}
n_{j} \neq n_{j+1} \tag{2.1.172}
\end{equation*}
$$

According to eq. (2.1.171), however, even if segments $j$ and $j+1$ are in equilibrium, imaginary flow from segment $j$ to $j+1$ is present in the numerical calculation.

This is because Fick's first law is applied to a field with a temperature gradient. To eliminate this flow, a second term representing the effect of temperature difference must be added to both eqs. (2.1.171) and (2.1.172).

The second term to be added to eq. (2.1.171) is

$$
\begin{equation*}
G(j \rightarrow j+1)=F_{J, j+1}\left\{\left(n_{j}-n_{j+1}\right)-\left(\bar{n}_{j}-\bar{n}_{j+1}\right)\right\}, \tag{2.1.173}
\end{equation*}
$$

where $\bar{n}_{j}$ and $\bar{n}_{j+1}$ are given by the ideal gas law as follows.

$$
\begin{equation*}
\bar{n}_{j}=\frac{P}{R} \frac{1}{T_{j}}, \bar{n}_{j+1}=\frac{P}{R} \frac{1}{T_{j+1}} \tag{2.1.174}
\end{equation*}
$$

The amount of flow of each component, namely eqs.(2.1.171) and (2.1.172), is given, respectively, as follows.

$$
\begin{align*}
& G_{1}(j \rightarrow j+1)=F_{j, j+1}\left\{\left(n_{1, j}-n_{1, j+1}\right)-\left(\bar{n}_{1, j}-\bar{n}_{1, j+1}\right)\right\}  \tag{2.1.175}\\
& G_{2}(j \rightarrow j+1)=F_{j, j+1}\left\{\left(n_{2, j}-n_{2, j+1}\right)-\left(\bar{n}_{2, j}-\bar{n}_{2 j+1}\right)\right\} \tag{2.1.176}
\end{align*}
$$

Here,

$$
\begin{gather*}
\bar{n}_{1, j}=\frac{P}{R} \frac{\bar{C}_{1}}{T_{j}}, \quad \bar{n}_{1, j+1}=\frac{P}{R} \frac{\bar{C}_{1}}{T_{j+1}}  \tag{2.1.177}\\
\bar{C}_{1}=\frac{N_{1, j}+N_{1, j+1}}{V_{j}+V_{j+1}}=\frac{n_{1, j} V_{j}+n_{1, j+1} V_{j+1}}{V_{j}+V_{j+1}}  \tag{2.1.178}\\
\bar{n}_{2, j}=\frac{P}{R} \frac{\bar{C}_{2}}{T_{j}}, \quad \bar{n}_{2, j+1}=\frac{P}{R} \frac{\bar{C}_{2}}{T_{j+1}}  \tag{2.1.179}\\
\bar{C}_{2}=\frac{N_{2, j}+N_{2, j+1}}{V_{j}+V_{j+1}}=\frac{n_{2, j} V_{j}+n_{2, j+1} V_{j+1}}{V_{j}+V_{j+1}}  \tag{2.1.180}\\
\bar{C}_{1}+\bar{C}_{2}=1 . \tag{2.1.181}
\end{gather*}
$$

## (3) Implicit solution of $\mathrm{He}-\mathrm{Xe}$ counter-diffusion model

The flux $J_{1, R}$ of gas $1(\mathrm{Xe})$ that diffuses through the boundary surface $R$ (boundary between segments $j-1$ and $j$ ) into segment $j$ is given by

$$
\begin{equation*}
J_{1, R}=F_{j-1, j}\left\{\left(n_{1, j-1}-n_{1, j}\right)-\left(\bar{n}_{1, j-1}-\bar{n}_{1, j}\right)\right\} . \tag{2.1.182}
\end{equation*}
$$

The flux $J_{1, s}$ of gas 1 (Xe) that diffuses through the boundary surface $S$ (boundary between segments $j$ and $j+1$ ) into segment $j+1$ is given by

$$
\begin{equation*}
J_{1, S}=F_{j+1,,}\left\{\left(n_{1, j}-n_{1, j+1}\right)-\left(\bar{n}_{1, j}-\bar{n}_{1, j+1}\right)\right\} . \tag{2.1.183}
\end{equation*}
$$

Then, the change in the amount of Xenon in segment $j$ is given by

$$
\begin{equation*}
V_{j} \frac{\partial n_{1, j}}{\partial t}=J_{1, R}-J_{1, S} \tag{2.1.184}
\end{equation*}
$$

Through differentiation of eq.(2.1.184) using eqs.(2.1.182) and (2.1.183) and the implicit method, the following equation is obtained. Here, $k$ denotes time-step number.

$$
\begin{align*}
\frac{n_{1, j}^{k+1}-n_{1, j}^{k}}{\Delta t}= & \frac{1}{V_{l}^{\theta 1}}\left\{F_{j-1, j}^{\theta_{1}}\left[\left(n_{1, j-1}^{\theta_{2}}-n_{1, j}^{\theta_{2}}\right)-\left(\bar{n}_{1, j-1}^{\theta_{1}}-\bar{n}_{1, j}^{\theta_{1}}\right)\right]\right.  \tag{2.1.185}\\
& \left.-F_{j-1, j}^{\theta_{1}},\left[\left(n_{1, j}^{\theta_{2}}-n_{1, j+1}^{\theta_{2}}\right)-\left(\bar{n}_{1, j}^{\theta_{1}}-\bar{n}_{1, j+1}^{\theta_{1}}\right)\right]\right\}
\end{align*}
$$

Here,
$\theta_{1}=$ interpolation with respect to temperature, volume, pressure and
equilibrium molar ratio,
$\theta_{2}=$ interpolation with respect to molarity.
$\theta_{1}$ and $\theta_{2}$ are the interpolation parameters in a converging loop in the axial direction and in the counter-diffusion calculation, respectively. $\theta_{1}$ changes in the converging loop in the axial direction, but remains constant in the counter-diffusion calculation.

Fitting parameters THG1 and THG2
$\theta_{1}$ and $\theta_{2}$ are designated by THG1 and THG2, respectively. Their default value is 1.0 .

Therefore, an interpolation equation for $\theta_{2}$,

$$
\begin{equation*}
n_{1, N}^{\theta 2}=\left(1-\theta_{2}\right) n_{1, j}^{k}+\theta_{2} n_{1, j}^{k+1} \tag{2.1.186}
\end{equation*}
$$

is substituted into eq. (2.1.185), and the following equation is obtained.

$$
\begin{align*}
& \frac{n_{1, j}^{k+1}-n_{1, j}^{k}}{\Delta t}=\frac{\theta_{2} F_{j-1, j}^{\theta_{1}}}{V_{j}^{\theta_{1}}} n_{1, j-1}^{k+1}-\frac{\theta_{2}\left\{F_{j, j+1}^{\theta_{1}}+F_{j-1, j}^{\theta_{1}}\right\}}{V_{j}^{\theta_{1}}} n_{1, j}^{k+1} \\
& \quad+\frac{\theta_{2} F_{j-1, j}^{\theta_{1}}}{V_{j}^{\theta_{1}}} n_{1, j+1}^{k+1}+\frac{1}{V_{j}^{\theta_{1}}}\left\{F _ { j - 1 , j } ^ { \theta _ { 1 } } \left[\left(1-\theta_{2}\right)\left(n_{1, j-1}^{k}-n_{1, j}^{k}\right)\right.\right.  \tag{2.1.187}\\
& \left.\left.\quad-\left(\bar{n}_{1, j-1}^{\theta_{1}}-\bar{n}_{1, j}^{\theta_{1}}\right)\right]-F_{j, j+1}^{\theta_{1}}\left[\left(1-\theta_{2}\right)\left(n_{1, j}^{k}-n_{1, j+1}^{k}\right)-\left(\bar{n}_{1, j}^{\theta_{1}}-\bar{n}_{1, j+1}^{\theta_{1}}\right)\right]\right\} .
\end{align*}
$$

Through rearrangement of eq. (2.1.187),

$$
\begin{equation*}
A_{j} n_{1, j-1}^{k+1}+B_{j} n_{1, j}^{k+1}+C_{j} \cdot n_{1, j+1}^{k+1}=D_{j} \tag{2.1.188}
\end{equation*}
$$

Here,

$$
\begin{equation*}
A_{j}=-\frac{\theta_{2} F_{j-1, i}^{\theta_{1}}}{V_{j}^{\theta_{1}}} \Delta t \tag{2.1.189}
\end{equation*}
$$

$$
\begin{gather*}
B_{j}=1+-\frac{\theta_{2}\left\{F_{j-1, i}^{\theta_{1}}+F_{j, j+1}^{\theta_{1}}\right\}}{V_{j}^{\theta_{1}}} \Delta t  \tag{2.1.190}\\
C_{j}=-\frac{\theta_{2} F_{j, j+1}^{\theta_{1}}}{V_{j}^{\theta_{1}}} \Delta t  \tag{2.1.191}\\
D_{j}=\frac{1}{V_{j}^{\theta_{1}}} F_{j, j-1}^{\theta_{1}}\left(1-\theta_{2}\right) \Delta t n_{1, j-1}^{k}+\left\{1-\frac{1}{V_{j}^{\theta_{1}}}\left(F_{j, j-1}^{\theta_{1}}+F_{j, j+1}^{\theta_{1}}\right)\left(1-\theta_{2}\right) \Delta t\right\} n_{1, j}^{k}  \tag{2.1.192}\\
+\frac{1}{V_{j}^{\theta_{1}}} F_{j, j+1}^{\theta_{1}}\left(1-\theta_{2}\right) \Delta t n_{1, j+1}^{k}+\frac{1}{V_{j}^{\theta_{1}}}\left\{F_{j, j+1}^{\theta_{1}}\left(\bar{n}_{1, j}^{\theta_{1}}-\bar{n}_{1, j+1}^{\theta_{1}}\right)-F_{j, j-1}^{\theta_{1}}\left(\bar{n}_{1, j-1}^{\theta_{1}}-\bar{n}_{1, j}^{\theta_{1}}\right)\right\} \Delta t .
\end{gather*}
$$

First, the upper and lower axial segments including plenum are considered.
Since there is no boundary surface $R$ for the first segment,

$$
\begin{align*}
V_{1} \frac{\partial n_{1,1}}{\partial t} & =-J_{1, S}  \tag{2.1.193}\\
& =-F_{1,2}\left[\left(n_{1,1}-n_{1,2}\right)-\left(\bar{n}_{1,1}-\bar{n}_{1,2}\right)\right]
\end{align*}
$$

holds; therefore, the following equation holds.

$$
\begin{align*}
\frac{n_{1,1}^{k+1}-n_{1,1}^{k}}{\Delta t}= & -\frac{\theta_{2} F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} n_{1,1}^{k+1}+\frac{\theta_{2} F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} n_{1,2}^{k+1}-\frac{\left(1-\theta_{2}\right) F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} n_{1,1}^{k}  \tag{2.1.194}\\
& +\frac{\left(1-\theta_{2}\right) F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} n_{1,2}^{k}+\frac{F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}}\left(\bar{n}_{1,1}^{\theta_{1}}-\bar{n}_{1,2}^{\theta_{1}}\right)
\end{align*}
$$

This equation is rearranged using

$$
\begin{align*}
& B_{1}=1+\frac{\theta_{2} F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} \Delta t, C_{1}=-\frac{\theta_{2} F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} \Delta t \\
& D_{1}=\left(1-\frac{\left(1-\theta_{2}\right) F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} \Delta t\right) n_{1,1}^{k}+\frac{\left(1-\theta_{2}\right) F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}} \Delta t n_{1,2}^{k}+\frac{F_{1,2}^{\theta_{1}}}{V_{1}^{\theta_{1}}}\left(\bar{n}_{1,1}^{\theta_{1}}-\bar{n}_{1,2}^{\theta_{1}}\right) \Delta t, \tag{2.1.195}
\end{align*}
$$

and we obtain

$$
\begin{equation*}
B_{1} \cdot n_{1,1}^{k+1}+C \cdot n_{1,2}^{k+1}=D_{1} . \tag{2.1.196}
\end{equation*}
$$

Similarly, there is no boundary surface $S$ for the uppermost segment $n$, and thus the following equation holds.

$$
\begin{align*}
& V_{n} \frac{\partial n_{1, n}}{\partial t}=-J_{1, R}  \tag{2.1.197}\\
& \quad=-F_{n-1, n}\left[\left(n_{1, n-1}-n_{1, n}\right)-\left(\bar{n}_{1, n-1}-\bar{n}_{1, n}\right)\right]
\end{align*}
$$

Therefore, by setting

$$
\begin{gather*}
\text { JAERI-Data/Code } 97-043 \\
A_{n}=-\frac{\theta_{2} F_{n-1, n}^{\theta_{1}}}{V_{n}^{\theta_{1}}} \Delta t, B_{n}=1+\frac{\theta_{2} F_{n-1, n}^{\theta_{1}}}{V_{n}^{\theta_{1}}} \Delta t \\
D_{n}=\frac{\left(1-\theta_{2}\right) F_{n-1, n}^{\theta_{1}}}{V_{n}^{\theta_{1}}} \Delta t n_{1, n-1}^{k}+\left(1-\frac{\left(1-\theta_{2}\right) F_{n-1, n}^{\theta_{1}}}{V_{n}^{\theta_{1}}} \Delta t\right) n_{1, n, n}^{k}-\frac{F_{n-1, n}^{\theta_{1}}}{V_{n}^{\theta_{1}}}\left(\bar{n}_{1, n-1}^{\theta_{1}}-\bar{n}_{1, n}^{\theta_{1}}\right) \Delta t,(2 \tag{2.1.198}
\end{gather*}
$$

we obtain

$$
\begin{equation*}
A_{n} \cdot n_{1, n-1}^{k+1}+B_{n} \cdot n_{1, n}^{k+1}=D_{n} . \tag{2.1.199}
\end{equation*}
$$

Combining the above, we obtain the following equation for the diffusion of gas 1 .

$$
\left[\begin{array}{lll}
B_{1} C_{1} & &  \tag{2.1.200}\\
A_{2} B_{2} C_{2} & & \\
A_{3} B_{3} C_{3} & & \\
& \cdot & \\
& \cdot & \\
& \cdot & \\
& & \\
& & A_{n-2} B_{n-2} C_{n-2} \\
& & A_{n-1} B_{n-1} C_{n-1} \\
& & A_{n} B_{n}
\end{array}\right]\left\{\begin{array}{c}
n_{1,1}^{k+1} \\
n_{1,2}^{k+1} \\
n_{1,3}^{k+1} \\
\cdot \\
\cdot \\
\cdot \\
\cdot \\
\\
\\
\end{array}\right.
$$

Gas concentration $n_{t, j}^{k+1}$ of each axial segment is obtained by solving eq. (2.1.200).
(4) Counter-diffusion constant

The gas counter-diffusion constant adopts Present's constant ${ }^{(21)}$.

$$
\begin{equation*}
D^{12}=\frac{3}{8}\left(\frac{\pi k T}{2 m^{*}}\right)^{\frac{1}{2}} \frac{1}{n \pi d_{12}^{2}} \tag{2.1.201}
\end{equation*}
$$

where

$$
\begin{aligned}
& m^{*}=\frac{m_{1} m_{2}}{m_{1}+m_{2}} \quad(m: \text { weight of one molecule }) \\
& d_{12}=\frac{1}{2}\left(d_{1}+d_{2}\right) \quad(d: \text { diameter of one molecule }) \\
& n=n_{1}+n_{2} \quad \text { (molar density) } \\
& k: \text { Boltzmann's constant } \\
& T: \text { temperature (K). }
\end{aligned}
$$

## (5) Pressure adjustment calculation

Setting the total gas molar number as $N_{j}$ for each axial segment at the end of time step,

$$
\begin{equation*}
N_{j}=\sum_{i} N_{i j}, \tag{2.1.202}
\end{equation*}
$$

holds, where $i$ represents kind of gas. For the entire volume of the fuel rod inner space, the gas molar number is given by

$$
\begin{equation*}
N=\sum_{i} N_{j} \tag{2.1.203}
\end{equation*}
$$



Fig. 2.28 Calculation of pressure adjustment (vertical axis: gas molar number).

Since

$$
\begin{equation*}
P=N \cdot R \cdot \frac{1}{\sum_{j}\left(\frac{V}{T}\right)_{j}} \tag{2.1.204}
\end{equation*}
$$

holds from the ideal gas law, the total molar number of gas $N_{j}^{\prime}$ in segment $j$ after the calculation of pressure adjustment is given by

$$
\begin{align*}
& \text { JAERI-Data/Code 97-043 } \\
& N_{j}^{\prime}=\frac{P}{R}\left(\frac{V}{T}\right)_{j} \tag{2.1.205}
\end{align*}
$$

The discrepancy between $N_{j}$ and $N_{j}$ 'is adjusted by balancing of the input and output flows between the upper and lower adjacent segments, beginning from the lowest part of pellet stack (see Fig. 2.28).

Namely, if the following are set, $N_{i-j}$ : molar number of mixed gas transported from segment $i$ to segment $j$ $f_{i j}:$ fraction of segment $i$ in segment $j$ before transport, the gas molar number $i$ for segment $j$ after transport is given by

$$
\begin{equation*}
N_{i j}^{\prime}=f_{i j}\left\{N_{j}-\sum_{k} N_{j \rightarrow k}\right\}+\sum_{l} f_{l l} N_{l \rightarrow j} . \tag{2.1.206}
\end{equation*}
$$

## (6) Method of space volume calculation

The void space volumes inside the fuel rod are classified into plenum volume, gap volume, pellet center hole volume and free gas volume inside the stack, as the reference temperature of each volume differs in the pressure calculation.

FEMAXI-IV assumes that no change occurs for both the pellet center hole volume and free gas volume inside the stack during irradiation.

The center hole volume is given using the initial inner radius of pellet $r_{p i}$ and the length $l_{z}^{j}$ of axial segment $j$ as

$$
\begin{equation*}
V_{h}^{j}=\pi r_{p l}^{2} l_{z}^{j} \tag{2.1.207}
\end{equation*}
$$

The free gas volume inside the stack includes dish volume, chamfer volume, pellet-to-pellet free space volume and void volume in cracks.

When the length of one pellet is set as $l_{p}$, dish volume per pellet as $V_{\text {dish }}$, chamfer volume as $V_{c h e m}$, pellet-to-pellet free space volume as $V_{p}$, and void volume in crack as $V_{c r a c k}$, the equations

$$
\begin{gather*}
V_{p}=\pi r_{p o}^{2} \Delta l / 2  \tag{2.1.208}\\
V_{\text {crack }}=2 \pi r_{p o} u^{r e l} l_{p} \tag{2.1.209}
\end{gather*}
$$

hold, where
$r_{p o}$ : outer radius of pellet
$\Delta l$ : pellet-to-pellet aperture width
$u^{\text {rel }}:$ radial displacement of pellet caused by relocation.
Parameter AY

The pellet-to-pellet aperture $\Delta l$ is defined as the distance between two edges of adjacent pellets as described by the right-side figure.

It specifies the tilting of pellets. It is designated by parameter AY. The default value is $20 \mu \mathrm{~m}$.


The free gas volume $V_{\mathrm{int}}^{j}$ in the stack in axial segment $j$ is given by

$$
\begin{equation*}
V_{\mathrm{int}}^{\prime}=\left(V_{d \mathrm{csh}}+V_{c h a m}+\pi r_{p o}^{2} \Delta l / 2+2 \pi r_{p o} u^{r e l} \cdot l_{p}\right) \frac{l_{z}^{j}}{l_{p}} . \tag{2.1.210}
\end{equation*}
$$

In contrast to the above, plenum volume and gas volume are assumed to change during irradiation. The plenum volume change is obtained from the change in axial segment length inside the stack. In segment $j$, setting the thermal expansion strain averaged by pellet volume as $\varepsilon_{t h}^{j}$, densification strain as $\varepsilon_{d e n}^{j}$, and solid swelling strain as $\varepsilon_{s s}^{j}$, the segment length $\tilde{l}_{z, p}^{j}$ including the changes by these strains is

$$
\begin{equation*}
\widetilde{l}_{z, p}^{j}=\left(1+\varepsilon_{t h}^{j}+\varepsilon_{d e n}^{j}+\varepsilon_{s s}^{j}\right) l_{z}^{j} \tag{2.1.211}
\end{equation*}
$$

In cladding, setting the thermal strain as $\Delta \varepsilon_{c, t h}^{\prime}$ and strain by irradiation growth as $\Delta \varepsilon_{c, i r r}^{\prime}$, the segment length $\widetilde{l}_{z, c}{ }^{j}$ is

$$
\begin{equation*}
\widetilde{l}_{z, C}^{j}=\left(1+\varepsilon_{c, t h}^{j}+\varepsilon_{c, i r r}^{j}\right) l_{z}^{j} . \tag{2.1.212}
\end{equation*}
$$

Similarly, when the plenum length $l_{z, p l}$ is set as

$$
\begin{equation*}
l_{z, p^{\prime}}=\left(1+\varepsilon_{c, t h}^{p l}+\varepsilon_{c, 1 r r}^{p l}\right) l_{z, p^{\prime}}, \tag{2.1.213}
\end{equation*}
$$

the change in plenum volume $\Delta V_{p l}$ is given by

$$
\begin{equation*}
\Delta V_{p l}=\pi r_{c 1}^{2}\left(\sum_{j=1}^{N A X I}\left(\tilde{l}_{z, c}^{j}-\tilde{l}_{z, p}^{j}\right)+\tilde{l}_{z, p l}-l_{z, p l}\right), \tag{2.1.214}
\end{equation*}
$$

where NAXI represents the number of axial segments, and $r_{c}$ the cladding inner radius.
Accordingly, when the initial plenum volume is set as $V_{p l}$, the plenum volume is

$$
\begin{equation*}
\tilde{V}_{p l}=V_{p l}+\Delta V_{p l} \tag{2.1.215}
\end{equation*}
$$

The gap volume of axial segment $j$ is given as follows, using the gap width $\delta$ obtained from eq. (2.1.95). Here, $\delta=0$ is assumed when numerically $\delta<0$.

$$
\begin{equation*}
\widetilde{V}_{g a p, j}=2 \pi r_{c i} \cdot \delta \cdot \tilde{l}_{Z, p}^{j} \tag{2.1.216}
\end{equation*}
$$

## (7) Gas pressure

It is assumed that the gas in the fuel rod behaves as an ideal gas and the pressure in the fuel rod is uniform. Then the gas pressure is calculated as

$$
\begin{equation*}
P_{g a s}=\frac{n_{T} \cdot R}{\frac{V_{p l^{\prime}}}{T_{p l}^{\prime}}+\sum_{j=1}^{M H}\left(\frac{V_{g a p}^{j}}{T_{g a p}^{J}}+\frac{V_{h}^{J}}{T_{p i}^{\prime}}+\frac{V_{i n t}^{j}}{T_{a v}^{\prime}}\right)}, \tag{2.1.217}
\end{equation*}
$$

where

$$
\begin{array}{rll}
P_{g a s} & : \text { gas pressure inside fuel rod }(\mathrm{Pa}) \\
n_{T} & : \text { total molar number of all gases }(\mathrm{mol}) \\
R & : \text { gas constant, } 8.314 \mathrm{~J} / \mathrm{K} \cdot \mathrm{~mol} \\
V_{p l} & : \text { plenum volume }\left(\mathrm{m}^{3}\right) \\
T_{p l} & : \text { plenum gas temperature }(\mathrm{K}) \\
T_{w} & : \text { coolant temperature }(\mathrm{K}) \\
V_{\text {gup }}^{j} & : \text { gap volume in axial segment } j\left(\mathrm{~m}^{3}\right) \\
V_{h}^{j} & : \text { pellet center hole volume in axial segment } j\left(\mathrm{~m}^{3}\right) \\
V_{\mathrm{mt}}^{j} & : \text { free gas volume in pellet stack }\left(\mathrm{m}^{3}\right) \\
T_{\text {gap }}^{j} & : \text { gap temperature in axial segment } j \quad(\mathrm{~K}) \\
& =0.5\left(T_{p s}^{j}+T_{c i}^{j}\right) \\
T_{p i}^{j} & : \text { pellet center temperature in axial segment } j(\mathrm{~K}) \\
T_{p i}^{j} & : \text { volumetric average temperature of pellet in axial segment } j \quad(\mathrm{~K}) .
\end{array}
$$

Here, the free gas volume $V_{\text {int }}^{j}$ includes dish volume, chamfer volume, pellet-to-pellet free
space volume, and volume between crack surfaces (= void volume in crack). $V_{\mathrm{int}}^{j}$ is already known by eq.(2.1.210)

```
Fitting parameter DTPL The plenum gas temperature \(T_{p l}\) is given as follows
    using coolant temperature \(T_{\text {cool }} . T_{p l}=T_{\text {cool }}+\mathrm{DTPL}\)
    The default value of DTPL is \(25(\mathrm{~K})\).
```


### 2.1.6 Time step control

The time-step width is automatically controlled in FEMAXI-IV. In the entire calculation, it is determined by the restriction $\Delta t_{1}$, while in the thermal analysis it is subdivided by $\Delta t_{2}$ in gas diffusion calculation. The restriction is explained as,
(1) $\Delta t_{1}$ is the minimum among the values determined by the following four conditions.

1) Changes in linear heat rate is within $10 \mathrm{~W} / \mathrm{cm}$ during one time-step.
2) Changes in burnup is within $500 \mathrm{MWd} / \mathrm{t}$ during one time-step.
3) Creep strain rate is limited so that creep strain increment does not exceed elastic strain.
4) time step width is within 1.5 times the former time step width.

The values for the conditions 1) and 2) are determined in subroutine PHIST to stabilize the solution. The condition 3) is a restriction to avoid divergence in creep calculation for all elements, and $\Delta t_{1}$ is determined by

$$
\begin{equation*}
\Delta t \leq \frac{\bar{\sigma}}{E \cdot \dot{\bar{\varepsilon}}^{c}} \cdot \mathrm{EFCOEF} \tag{2.1.218}
\end{equation*}
$$

where EFCOF is a tuning parameter.
The condition 4) restricts the expansion of $\Delta t_{1}$ within a factor of 1.5 when rod power increases at less than $10 \mathrm{~W} / \mathrm{cm} \cdot \mathrm{s}$ during one time step.

In the entire length mechanical analysis and local mechanical analysis, subdivision of $\Delta t_{1}$ is performed within these analyses in accordance with the change of pellet-cladding contact state. See sections 2.2.11 and 2.3.3.

However, in the thermal analysis, a time step width $\Delta t_{2}$ which is smaller than $\Delta t_{1}$ can be used in the following manner.
(2) $\Delta t_{2}$ is used for gas diffusion time-step width, which is the subdivision of $\Delta t_{1}$ and determined as the shortest time among the time required to reach the equilibrium state of gas flow in each axial segment and the time determined from the maximum amount of transport of gas between segments as well as from pressure adjustment conditions, with its upper limit value set as either 100 ms or $\Delta t_{1}$.

The time required to reach the equilibrium state in each axial segment is derived from eq. (2.1.184) as

$$
\begin{equation*}
\Delta t_{j}^{i}=\frac{\left(n_{1, j}-\bar{n}_{1, j}\right) V_{j}}{J_{1, R}-J_{1, S}} \tag{2.1.219}
\end{equation*}
$$

where the superscript $i$ represents axial segment number.
Next, the time determined from the maximum amount of transport of gas between segments is obtained as follows. Using the maximum molar number of the gas transported between segments $N_{\max }$ as standard, since $\left(J_{1, R}\right)_{j}=\left(J_{1, S}\right)_{j-1}$, we represent $\Delta t_{2}$ as follows using $\left(J_{1, R}\right)_{j}$.

$$
\begin{equation*}
\Delta t_{\jmath}^{2}=\frac{N_{\max }}{\left(J_{1, R}\right)} \tag{2.1.220}
\end{equation*}
$$

Then, the time determined from the pressure adjustment conditions in gas flow is obtained as follows. Due to the assumption of instantaneous equilibrium of pressure inside the fuel rod, numerical instability resulting from gas flow between segments may occur. To avoid this instability, we must impose a restriction on the amount of gas transport at each segment. Setting the gas transport rate in each segment as $\beta(\mathrm{mol} / \mathrm{s})$, the restriction is given by

$$
\begin{equation*}
\Delta t_{j}^{3}=\frac{N_{\max }}{\beta j} \tag{2.1.221}
\end{equation*}
$$

Thus, under the conditions

$$
\begin{align*}
& \Delta t_{21}=\min \left(\Delta t_{1}^{1}, \Delta t_{2}^{1}, \cdots, \Delta t_{n}^{1}\right) \cdot \eta_{2}  \tag{2.1.222}\\
& \Delta t_{22}=\min \left(\Delta t_{1}^{2}, \Delta t_{2}^{2}, \cdots, \Delta t_{n}^{2}\right)  \tag{2.1.223}\\
& \Delta t_{23}=\min \left(\Delta t_{1}^{3}, \Delta t_{2}^{3}, \cdots, \Delta t_{n}^{3}\right) \tag{2.1.224}
\end{align*}
$$

$\Delta t_{2}$ is given by

$$
\begin{equation*}
\Delta t_{2}=\min \left(\Delta t_{21}, \Delta t_{22}, \Delta t_{23}\right) \tag{2.1.225}
\end{equation*}
$$

$N_{\text {max }}$ in eqs. (2.1.220) and (2.1.221) and $\eta_{2}$ are the control parameters programmed in the code.

Fitting parameters AMLMX2, AMLX3, DTPR and FAC
$N_{\text {max }}$ in eq. (2.1.20) is set by AMLMX2, and the default value is $10^{-6}$ (mol).
$N_{\text {max }}$ in eq. (2.1.221) is set by AMLMX3, and the default value is $2 \times 10^{-6}(\mathrm{~mol})$. $\eta_{2}$ in eq. (2.1.222) is set by DTPR, and the default value is 0.01 .
Default value of tuning parameter EFCOEF is 1.0

### 2.2 Mechanical Behavior over Entire Length of Fuel Rod (Detailed Mechanical Analysis 1 [FEMROD] *)

(*) In Detailed Mechanical Analysis I, the analysis over the entire fuel rod is performed at the routine FEMROD. In Detailed Mechanical Analysis II described in Chapters 2 and 3, local analysis of the fuel rod deformation is performed at other routines. Anlayses I and II are exclusive with respect to each other; therefore, one of the two analyses is selected using the input parameter IFEMRD.

IFEMRD $=0$ : local analysis, $\quad$ IFEMRD $=1$ : analysis over entire length.

### 2.2.1 Finite element model

As shown in Fig. 2.29, the analysis model includes a 2-dimensional axisymmetrical system in which the entire length of the fuel rod is divided into axial segments, and each segment is further divided into concentric ring elements in the radial direction. In this system, the stress/strain analysis is performed using the finite element method with quadrangular elements with three degrees of freedom as shown in Fig. 2.30.


Fig. 2.29 Shape model.


Fig. 2.30 Quadrangular model element with three degrees of freedom.

Figure 2.31 shows the relationship between mesh division and degree of freedom of each node in an axial segment.


Fig. 2.31 Mesh division of the finite element method (for one segment).

As shown in Fig. 2.31, each node has only one degree of freedom, both in the axial and radial directions. On the assumption that the axial displacements of all the nodes $z_{1} \sim z_{10}$ for the pellet are identical, the degree of freedom of one element is used as a representative value,

$$
\begin{equation*}
z_{l}=z_{2}=z_{3}=\ldots \ldots=z_{l 0} \quad\left(=z_{p}\right) \tag{2.2.1}
\end{equation*}
$$

Here, we obtain various matrices of one element which are hereafter used in the basic equation of the FEM analysis. First, we obtain strain-displacement matrix [B]. Setting radial displacement $v$ and axial displacement as $\omega$, the displacement $(v, \omega)$ at an arbitrary point in the element $(r, z)$ shown in Fig. 2.30 is given by

$$
\begin{gather*}
v=\frac{r_{i+1}-r}{r_{i+1}-r_{i}} v_{i}+\frac{r-r_{i}}{r_{i+1}-r_{i}} v_{t+1}  \tag{2.2.2}\\
\omega=\frac{z}{z_{i}} \omega_{i} . \tag{2.2.3}
\end{gather*}
$$

The strain component in the axisymmetrical coordinate system is as follows.

$$
\{\varepsilon\}=\left\{\begin{array}{l}
\varepsilon_{r}  \tag{2.2.4}\\
\varepsilon_{\theta} \\
\varepsilon_{z}
\end{array}\right\}=\left\{\begin{array}{c}
\partial \nu / \partial r \\
v / r \\
\partial \omega / \partial z
\end{array}\right\} \equiv[B]\{u\}
$$

Using eqs. (2.2.2) and (2.2.3), the following equations hold.

$$
\begin{align*}
\frac{\partial}{\partial r} & =-\frac{1}{r_{i+1}-r_{i}} v_{i}+\frac{1}{r_{i+1}-r_{i}} v_{i+1} \\
\frac{v}{r} & =\frac{r_{i+1}-r}{r\left(r_{i+1}-r_{1}\right)} v_{i}+\frac{r-r_{i}}{r\left(r_{i+1}-r_{i}\right)} v_{i+1} \tag{2.2.5}
\end{align*}
$$

Setting $r$ as central-point coordinate of the element in the radial direction $\frac{r_{1}+r_{t+1}}{2}$, the following equations hold.

$$
\begin{align*}
& \begin{aligned}
\frac{v}{r} & =\frac{r_{i+1}-\frac{r_{1}+r_{t+1}}{2}}{\frac{r_{i}+r_{i+1}}{2}\left(r_{i+1}-r_{i}\right)} v_{i}+\frac{\frac{r_{1}+r_{i+1}}{2}-r_{i}}{\frac{r_{i}+r_{t+1}}{2}\left(r_{i+1}-r_{i}\right)} v_{i+1} \\
& =\frac{1}{r_{i}+r_{i+1}} v_{i}+\frac{1}{r_{i}+r_{i+1}} v_{l+1} \\
& \frac{\partial \omega}{\partial z}=\frac{1}{z_{i}} \omega_{i}
\end{aligned}, l \tag{2.2.6}
\end{align*}
$$

Substituting eqs. (2.2.5), (2.2.6) and (2.2.7) into eq. (2.2.4), we obtain

$$
\left\{\begin{array}{c}
\varepsilon_{r, i}  \tag{2.2.8}\\
\varepsilon_{\theta, i} \\
\varepsilon_{-, i}
\end{array}\right\}=\left[\begin{array}{ccc}
-\frac{1}{r_{i+1}-r_{i}} & \frac{1}{r_{i+1}-r_{i}} & 0 \\
\frac{1}{r_{i+1}+r_{i}} & \frac{1}{r_{i+1}+r_{i}} & 0 \\
0 & 0 & \frac{1}{z_{i}}
\end{array}\right]\left\{\begin{array}{l}
v_{i} \\
v_{t+1} \\
\omega_{i}
\end{array}\right\} .
$$

Accordingly, we obtain the components of matrix $[B]$ as follows.

$$
[B]=\left[\begin{array}{ccc}
-\frac{1}{r_{i+1}-r_{i}} & \frac{1}{r_{i+1}-r_{i}} & 0  \tag{2.2.9}\\
\frac{1}{r_{i+1}+r_{i}} & \frac{1}{r_{i+1}+r_{i}} & 0 \\
0 & 0 & \frac{1}{z_{i}}
\end{array}\right]
$$

The volume of each element $V_{i}$ is given as

$$
\begin{equation*}
V_{i}=\pi\left(r_{i+1}^{2}-r_{i}^{2}\right) z_{i} \tag{2.2.10}
\end{equation*}
$$

Next, we obtain strain-stress matrix [C]. The stress-strain relationship is

$$
\begin{equation*}
\{\Delta \sigma\}=[D]\left\{\Delta \varepsilon^{e}\right\} \tag{2.2.11}
\end{equation*}
$$

where $[D]$ is the stress-strain matrix that represents the stiffness of an element.
When matrix [ $C$ ] is defined as an inverse matrix of [ $D$ ], eq. (2.2.11) is expressed as

$$
\begin{equation*}
\left\{\Delta \varepsilon^{e}\right\}=[C]\{\Delta \sigma\} \tag{2.2.12}
\end{equation*}
$$

Accordingly, matrix $[C]$ is given by

$$
[C]=\frac{1}{E}\left[\begin{array}{ccc}
1 & -v & -v  \tag{2.2.13}\\
-v & 1 & -v \\
-v & -v & 1
\end{array}\right],
$$

where E is Young's modulus and $v$ is the Poisson ratio.
Here, solution of the basic equation of constitutive equations for stress-strain analysis is outlined. The external force and initial strain vector are set as $\{F\}$ and $\left\{\Delta \varepsilon_{0}\right\}$, respectively. When the calculation has proceeded to the $(n)$ th time step and calculation for the next $(n+1)$ th time step is performed, the equilibrium equation

$$
\begin{equation*}
\left\{F_{n+1}\right\}=\int[B]^{T}\left\{\sigma_{n+1}\right\} d V \tag{2.2.14}
\end{equation*}
$$

is given using the principle of virtual work.
Here,

$$
\begin{aligned}
& \left\{F_{n+1}\right\}: \text { external force vector at }(n+1) \text { th time step } \\
& \left\{\sigma_{n+1}\right\}: \text { stress vector at }(n+1) \text { th time step. }
\end{aligned}
$$

To distinguish between unknown and known values, we divide $\left\{\sigma_{n+1}\right\}$ into known stress $\left\{\sigma_{n}\right\}$ and unknown stress $\left\{\Delta \sigma_{n+1}\right\}$; then we obtain transformed equations of eq.(2.2.14) as

$$
\begin{align*}
& \left\{F_{n+1}\right\}=\int[B]^{T}\left\{\sigma_{n}\right\} d V+\int[B]^{T}\left\{\Delta \sigma_{n+1}\right\} d V  \tag{2.2.15}\\
& \int[B]^{T}\left\{\Delta \sigma_{n+1}\right\} d V=\left\{F_{n+1}\right\}-\int[B]^{T}\left\{\sigma_{n}\right\} d V \tag{2.2.16}
\end{align*}
$$

The right side of eq. (2.2.16) consists of known values and the left side consists of unknown values. Substituting eq. (2..2.11) into eq. (2.2.16), we obtain

$$
\begin{equation*}
\int[B]^{T}[D]\left\{\Delta \varepsilon_{n+1}^{e}\right\} d V=\left\{F_{n+1}\right\}-\int[B]^{T}\left\{\sigma_{n}\right\} d V \tag{2.2.17}
\end{equation*}
$$

Here, the following equation holds among elestic strain increment $\left\{\Delta \varepsilon_{n+1}^{e}\right\}$, total strain increment $\left\{\Delta \varepsilon_{n+1}\right\}$, and the known value initial strain increment $\left\{\Delta \varepsilon_{0, n+1}\right\}$.

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}\right\}=\left\{\Delta \varepsilon_{n+1}\right\}-\left\{\Delta \varepsilon_{0, n+1}\right\} \tag{2.2.18}
\end{equation*}
$$

Accordingly, substituting eq. (2.2.18) into eq. (2.2.17), we obtain

$$
\begin{equation*}
\int[B]^{T}[D]\left\{\Delta \varepsilon_{n+1}-\Delta \varepsilon_{0, n+1}\right\} d V=\left\{F_{n+1}\right\}-\int[B]^{T}\left\{\sigma_{n}\right\} d V \tag{2.2.19}
\end{equation*}
$$

Transposing the known value term $\int[B]^{T}[D]\left\{\Delta \varepsilon_{0, n+1}\right\} d V$ to the right-hand side,

$$
\begin{equation*}
\int[B]^{T}[D]\left\{\Delta \varepsilon_{n+1}\right\} d V=\left\{F_{n+1}\right\}+\int[B]^{T}[D]\left\{\Delta \varepsilon_{0, n+1}\right\} d V-\int[B]^{T}\left\{\sigma_{n}\right\} d V \tag{2.2.20}
\end{equation*}
$$

is obtained. Substituting eq. (2.2.4) into eq. (2.2.20), we obtain

$$
\begin{align*}
& \int[B]^{T}[D][B] d V\left\{\Delta u_{n+1}\right\} \\
& \quad=\left\{F_{n+1}\right\}+\int[B]^{T}[D]\left\{\Delta \varepsilon_{0, n+1}\right\} d V-\int[B]^{T}\left\{\sigma_{n}\right\} d V \tag{2.2.21}
\end{align*}
$$

and the unknown value $\left\{\Delta u_{n+1}\right\}$ can be calculated by integration.
Namely, expressing equation (2.2.21) in a descrete form with summation of M elements,

$$
\begin{align*}
& \sum_{i=1}^{M}\left[B_{i}\right]^{T}\left[D_{i}\right]\left[B_{i}\right] \Delta V_{i}\left\{\Delta u_{n+1}\right\} \\
& =\left\{F_{n+1}\right\}+\sum_{i=1}^{M}\left[B_{i}\right]^{T}\left[D_{i}\right]\left\{\Delta \varepsilon_{0, n+1}^{j}\right\} \Delta V_{i}-\sum_{i=1}^{M}\left[B_{i}\right]^{T}\left\{\sigma_{n}^{i}\right\} \Delta V_{i} \tag{2.2.22}
\end{align*}
$$

( $\Delta V_{i}$ represents the volume of the elelment $i$, and $M$ represents total number of elements),

The unknown displacement increment vector $\left\{\Delta u_{n+1}\right\}$ is expressed using known values.
The above is the basic calculation method. In actual calculations, a more complex solution is required due to the use of implicit solutions for creep and plasticity.

In the next section, modification of the basic equations when implicit solutions are used
will be described.

### 2.2.2 Basic equations

The equilibrium condition at time $t_{n+1}$ is expressed as follows using the principle of virtual work, similar to the case of eq. (2.2.14).

$$
\begin{equation*}
\int_{V}[B]^{T}\left\{\sigma_{n+1}\right\} d V-\left\{F_{n+1}\right\}=0 \tag{2.2.23}
\end{equation*}
$$

The equation representing the relationship between elastic strain increment and stress increment (=eq. (2.2.12)) $\square$ during time increment $\Delta t_{n+1}\left(=t_{n+1}-t_{n}\right)$ is expressed as follows, with consideration given to time dependence of [C].

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}\right\}=\left[C_{n+\theta}\right]\left\{\Delta \sigma_{n+1}\right\} \tag{2.2.24}
\end{equation*}
$$

Here,

$$
\begin{aligned}
& {\left[C_{n+\theta}\right]=(1-\theta)\left[C_{n}\right]+\theta\left[C_{n+1}\right] \quad\left(\theta=\frac{1}{2}\right)} \\
& \left\{\Delta \varepsilon_{n+1}^{e}\right\}: \text { elastic strain increment vector } \\
& {\left[C_{n+\theta}\right] \text { : strain-stress matrix }} \\
& \left\{\Delta \sigma_{n+1}\right\}: \text { stress increment vector }
\end{aligned}
$$

$\theta \quad: \quad$ parameter for the implicit solution.
The elastic strain increment vector is expressed as

$$
\begin{align*}
\left\{\Delta \varepsilon_{n+1}^{\mathrm{e}}\right\} & =\left\{\Delta \varepsilon_{n+1}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {th }}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {rel }}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {den }}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {we }}\right\}  \tag{2.2.25}\\
& -\left\{\Delta \varepsilon_{n+1}^{H P}\right\}-\left\{\Delta \varepsilon_{n+1}^{P}\right\}-\left\{\Delta \varepsilon_{n+1}^{c}\right\} .
\end{align*}
$$

Here,
$\left\{\Delta \varepsilon_{n+1}\right\}:$ total strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{\text {in }}\right\}$ : thermal strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{\text {rel }}\right\}$ : pellet relocation strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{c i k}\right\}$ : pellet crack strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{\text {den }}\right\}$ : pellet densification strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{s w}\right\}$ : pellet swelling strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{H P}\right\}:$ pellet hot-press strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{P}\right\}$ : plastic strain increment vector
$\left\{\Delta \varepsilon_{n+1}^{c}\right\}$ : creep strain increment vector.

Of these, strain increment vectors which do not depend on stress are collectively treated as an initial strain increment vector as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{o}\right\}=\left\{\Delta \varepsilon_{n+1}^{\text {in }}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {rel }}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {den }}\right\}-\left\{\Delta \varepsilon_{n+1}^{\text {sw }}\right\} \tag{2.2.26}
\end{equation*}
$$

where $\quad\left\{\Delta \varepsilon_{n+1}^{o}\right\}:$ initial strain increment vector.
Furthermore, when the pellet hot-press strain increment vector is integrated into the pellet plastic and creep strain increment vectors as described in detail in section 2.2.4, eq. (2.2.25) is expressed as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}\right\}=\left\{\Delta \varepsilon_{n+1}\right\}-\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left\{\Delta \varepsilon_{n+1}^{p}\right\}-\left\{\Delta \varepsilon_{n+1}^{c}\right\} . \tag{2.2.27}
\end{equation*}
$$

Here,
$\left\{\Delta \varepsilon_{n+1}^{P}\right\}$ : plastic strain increment vector including hot press strain
$\left\{\Delta \varepsilon_{n+1}^{c}\right\}$ : creep strain increment vector including hot press strain.
Meanwhile, the total strain is associated with nodal displacement as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}\right\}=[B]\left\{\Delta u_{n+1}\right\}, \tag{2.2.28}
\end{equation*}
$$

where $\left\{\Delta u_{n+1}\right\}$ represents nodal displacement increment vector.
Using eqs. (2.2.25) and (2.2.27), we rewrite the stress-strain relationship equation (2.2.24) as

$$
\begin{equation*}
\left[C_{n+\theta}\right]\left\{\Delta \sigma_{n+1}\right\}-[B]\left\{\Delta u_{n+1}\right\}+\left\{\Delta \varepsilon_{n+1}^{o}\right\}+\left\{\Delta \varepsilon_{n+1}^{p}\right\}+\left\{\Delta \varepsilon_{n+1}^{c}\right\}=0 \tag{2.2.29}
\end{equation*}
$$

In the calculation of the $(n+1)$ th time step, iteration of the stress calculation is required for obtaining strain increment vectors $\left\{\Delta \varepsilon_{n+1}^{c r k}\right\},\left\{\Delta \varepsilon_{n+1}^{P}\right\}$ and $\left\{\Delta \varepsilon_{n+1}^{c}\right\}$ in eq. (2.2.25), which depend on stress. The Newton-Raphson method is used for the iteration with counter $i$. When the $i$-th iteration is completed and the $(i+1)$ th iteration is being performed, eq. (2.2.29) is expressed as

$$
\begin{align*}
& {\left[C_{n+\theta}\right]\left\{d \sigma_{n+1}^{j+1}\right\}-[B]\left\{\Delta u_{n+1}^{i+1}\right\}} \\
& \quad+\left\{\Delta \varepsilon_{n+1}^{o}\right\}+\left\{\Delta \varepsilon_{n+1}^{P, i+1}\right\}+\left\{\Delta \varepsilon_{n+1}^{c, i+1}\right\}+\left[C_{n+\theta}\right]\left(\left\{\sigma_{n+\theta}^{j}\right\}-\left\{\sigma_{n}\right\}\right)=0 \tag{2.2.30}
\end{align*}
$$

where

$$
\left\{d \sigma_{n+1}^{i+1}\right\}=\left\{\sigma_{n+1}^{i+1}\right\}-\left\{\sigma_{n+1}^{i}\right\} .
$$

## Model parameter LMAX

The number of iterations in the Newton-Raphson method is given by LMAX. The default value of LMAX is 2 .

At this time, the equilibrium condition (2.2.23) is represented as

$$
\begin{equation*}
\int_{V}[B]^{T}\left\{\sigma_{n+1}^{i}\right\} d V+\int_{V}[B]^{T}\left\{d \sigma_{n+1}^{i+1}\right\} d V=\left\{F_{n+1}\right\} . \tag{2.2.31}
\end{equation*}
$$

In eqs. (2.2.30) and (2.2.31), $\left\{d \sigma_{n+1}^{i+1}\right\},\left\{\Delta \varepsilon_{n+1}^{c r k, i+1}\right\},\left\{\Delta \varepsilon_{n+1}^{P, i+1}\right\},\left\{\Delta \varepsilon_{n+1}^{c, i+1}\right\}$ and $\left\{\Delta u_{n+1}^{i+1}\right\}$ are the unknown values. Therefore, the number of unknown values exceeds the number of equations, i.e. two equations, eqs. (2.2.30) and (2.2.31), the solution cannot be obtained; thus it is necessary to reduce the number of unknown values to two.

Here, the unknown values $\left\{\Delta \varepsilon_{n+1}^{c r, i+1}\right\},\left\{\Delta \varepsilon_{n+1}^{p_{, i+1}}\right\},\left\{\Delta \varepsilon_{n+1}^{\left(, c_{1}+1\right.}\right\}$ which depend on $\left\{d \sigma_{n+1}^{i+1}\right\}$ can be eliminated by expression of them using $\left\{\Delta u_{n+1}^{i+1}\right\}$ and $\left\{d \sigma_{n+1}^{i+1}\right\}$. Actual methods will be introduced in the next section.

### 2.2.3 Pellet cracks

The behavior of a pellet with cracks was explained in section 2.1.3 (3)-(5). Here, the difference in the crack models between that in the mechanical analysis and that in the thermal analysis is described. The concept of the crack model in the mechanical analysis is explained using the schematic shown in Fig. 2.32. ${ }^{(2)}$


Fig. 2.32 Stiffness model of pellet with cracks.

When a pellet is in a tensile state in the $i$ direction (axial, circumferential or radial direction), it is assumed that cracks are generated on the surface perpendicular to the $i$ direction and the apparent Young's modulus in the $i$ direction decreases to approximately $1 / 100$ of the original material property value. (Since the Young's modulus occupies a diagonal position in the FEM matrix of the present detailed mechanical analysis, the value cannot be 0 , while in the thermal analysis model, this modulus is set as 0 in equations.)

When a pellet is in a compressive state, it is assumed that the elasticity of the pellet partly recovers when strain is generated by relocation. That is, in the initial state, i.e. burnup $=0$, power $=0$, and $\varepsilon_{i}-\varepsilon_{i}^{o}=0$, Young's modulus of the pellet $E_{i}$ is a small value represented by $E_{c}$. The pellet behavior change with increasing power is described as follows.
(1) When the pellet is not in contact with the cladding, thermal stress in the pellet is small due to the presence of cracks; accordingly, the pellet is thermally deformed in accordance with its natural thermal expansion coefficient and the gap is narrowed.
(2) When the pellet is in contact with the cladding, the compressive strain inside the pellet by the restraint of the cladding increases. Since the gap generated on the cracked surface of the pellet is compressed by relocation, the stiffness of the pellet increases. This process is approximated by linear changing of Young's modulus. Namely, the process modeled here is one in which a mechanical interaction between a cracked and relocated pellet and the cladding is gradually enhanced.
(3) Next, elasticity of a pellet completely recovers to that represented by the original elastic coefficient $=$ compression stiffness when pieces of the pellet are compressed by cladding so that they fill the gap generated by relocation. Here, the strong interaction between pellet and cladding is modeled.

> Fitting parameter ECRAC3 Young's modulus of a pellet with cracks is set by ECRAC3. The default value of ECRAC3 is $2 \times 10^{9}\left(\mathrm{~N} / \mathrm{m}^{2}\right)$, which is approximately $1 / 100$ of original Young's modulus of $\mathrm{UO}_{2}$.

## Model parameter IYNG (used only in the mechanical calculations)

The pellet stiffness model shown in Fig. 2.32 is for the case IYNG $=0$. The default value of IYNG is 1 . When IYNG $=1$, the region between $-\varepsilon^{\text {rel }}$ and 0 is described by a straight line. When $I Y N G=0$, this region is described by a concave quadratic function.

Next, based on the above-described model, a mechanical analysis is performed as follows.
Regarding the pellet cracks, a crack strain increment $\left\{\Delta \varepsilon_{n+1}^{c k}\right\}$ which is proportional to the change in $\{\Delta \sigma\}$ is given by transformation of the [C] matrix elements in eq. (2.2.29) from eq.
(2.2.13). The strain-stress matrix of the pellet $[\widetilde{C}]$ is represented as

$$
[\widetilde{C}]=\left[\begin{array}{ccc}
\frac{1}{E_{r}} & -\frac{v}{E} & -\frac{v}{E}  \tag{2.2.32}\\
-\frac{v}{E} & \frac{1}{E_{z}} & -\frac{v}{E} \\
-\frac{v}{E} & -\frac{v}{E} & \frac{1}{E_{\theta}}
\end{array}\right] \text {. }
$$

Here,
$E_{r}$ : Young's modulus in the radial direction ( Pa )
$E_{z}$ : Young's modulus in the axial direction ( Pa )
$E_{\theta}:$ Young's modulus in the circumferential direction $(\mathrm{Pa})$
$E$ : Young's modulus of pellet (material property) ( Pa )
$v$ : Poisson's ratio ( - ).
The apparent Young's modulus in each direction $E_{i}\left(E_{r}, E_{z}, E_{\theta}\right)$ is defined as follows.

$$
E_{i}=\left\{\begin{array}{lc}
E_{c} & , 0 \leqq \varepsilon_{i}-\varepsilon_{i}^{o}  \tag{2.2.33}\\
-\frac{\varepsilon_{i}-\varepsilon_{i}^{o}}{\varepsilon_{1}^{r e l}}\left(E-E_{c}\right)+E_{c} & ,-\varepsilon_{i}^{r e l}<\varepsilon_{i}-\varepsilon_{i}^{o}<0 \\
E & , \varepsilon_{1}-\varepsilon_{i}^{o} \leqq-\varepsilon_{i}^{r e l}
\end{array}\right.
$$

Here,

$$
\begin{aligned}
& \varepsilon_{i}: \text { strain in } i \text { direction } \\
& \varepsilon_{1}^{o}: \text { initial strain in } i \text { direction } \\
& \varepsilon_{i}^{r e l}: \text { initial relocation strain in } i \text { direction (input data) } \\
& E_{c}: \text { effective Young's modulus of pellet with cracks in a tensile state. }
\end{aligned}
$$

From eq. (2.2.24),

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}\right\}=\left[C_{n+\theta}\right]\left\{\Delta \sigma_{n+1}\right\}, \tag{2.2.34}
\end{equation*}
$$

and setting the sum of elastic strain increment and crack strain increment as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}+\Delta \varepsilon_{n+1}^{c r k+i+1}\right\}=\left[\widetilde{C}_{n+\theta}\right]\left\{\Delta \sigma_{n+1}^{i+1}\right\}, \tag{2.2.35}
\end{equation*}
$$

we obtain the crack strain increment vector using eqs. (2.2.34) and (2.2.35) as

$$
\begin{align*}
& \left\{\Delta \varepsilon_{n+1}^{c r k+1+1}\right\}=\left\{\left[\widetilde{C}_{n+\theta}\right]-\left[C_{n+\theta}\right]\right\}\left\{\Delta \sigma_{n+1}^{\prime+1}\right\} \\
& =\left(\left[\begin{array}{rrr}
\frac{1}{E_{r}} & -\frac{v}{E} & -\frac{v}{E} \\
-\frac{v}{E} & \frac{1}{E_{z}} & -\frac{v}{E} \\
-\frac{v}{E} & -\frac{v}{E} & \frac{1}{E_{\theta}}
\end{array}\right]-\left[\begin{array}{ccc}
\frac{1}{E} & -\frac{v}{E} & -\frac{v}{E} \\
-\frac{v}{E} & \frac{1}{E} & -\frac{v}{E} \\
-\frac{v}{E} & -\frac{v}{E} & \frac{1}{E}
\end{array}\right]\right)\left\{\begin{array}{l}
\Delta \sigma_{r, n+1}^{i+1} \\
\Delta \sigma_{z, n+1}^{i+1} \\
\Delta \sigma_{\theta, n+1}^{i+1}
\end{array}\right\} \\
& =\left\{\begin{array}{l}
\left(\frac{1}{E_{r}}-\frac{1}{E}\right) \Delta \sigma_{r, n+1}^{i} \\
\left(\frac{1}{E_{z}}-\frac{1}{E}\right) \Delta \sigma_{z, n+1}^{i} \\
\left(\frac{1}{E_{\theta}}-\frac{1}{E}\right) \Delta \sigma_{\theta, n+1}^{i}
\end{array}\right\}+\left\{\begin{array}{l}
\left(\frac{1}{E_{r}}-\frac{1}{E}\right) d \sigma_{r, n+1}^{i+1} \\
\left(\frac{1}{E_{z}}-\frac{1}{E}\right) d \sigma_{z, n+1}^{i+1} \\
\left(\frac{1}{E_{\theta}}-\frac{1}{E}\right) d \sigma_{\theta, n+1}^{i+1}
\end{array}\right\} . \tag{2.2.36}
\end{align*}
$$

Thus, the unknown value crack strain increment $\left\{\Delta \varepsilon_{n+1}^{c r k,+1}\right\}$ in eq. (2.2.30) can be eliminated.
Accordingly, eq. (2.2.30) can be transformed as follows. From the equation

$$
\begin{aligned}
& {\left[C_{n+\theta}^{i}\right]\left\{d \sigma_{n+1}^{i+1}\right\}-[B]\left\{\Delta u_{n+1}^{i+1}\right\}+\left\{\Delta \varepsilon_{n+1}^{0}\right\}} \\
& \quad+\left\{\left[\widetilde{C}_{n+\theta}^{i}\right]-\left[C_{n+\theta}^{i}\right]\right\}\left(\left\{\sigma_{n+1}^{\prime}\right\}+\left\{d \sigma_{n+1}^{\prime+1}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{p,+1}\right\}+\left\{\Delta \varepsilon_{n+1}^{(,+1+1}\right\}+\left[C_{n+\theta}^{i}\right]\left[\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)=0,
\end{aligned}
$$

we obtain
$\left[\widetilde{C}_{n+\theta}^{i}\right]\left\{d \sigma_{n+1}^{\prime+1}\right\}-[B]\left\{\Delta u_{n+1}^{l+1}\right\}+\left\{\Delta \varepsilon_{n+1}^{0}\right\}+\left\{\Delta \varepsilon_{n+1}^{P, l+1}\right\}+\left\{\Delta \varepsilon_{n+1}^{(,)+1}\right\}+\left[\widetilde{C}_{n+\theta}^{\prime}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)=0$.
Fitting parameters FRELOC and EPSRLZ (used only in the mechanical
Relocation strain $\varepsilon^{\text {ret }}$ in the radial direction is given by the value which is calculated from the initial radial gap width multiplied by RELOC and divided by the pellet radius.

In the axial direction, relocation strain $\varepsilon^{\text {rel }}$ is directly set by EPSRLZ.
The default values of FRELOC and EPSRLZ are 0.5 and 0.003 , respectively.

Fitting parameters FACR and FACZ
$E_{i}=E$ holds when $\varepsilon_{i}-\varepsilon_{i}^{0}=-\varepsilon_{i}^{r e t}$; however, these values are adjusted using parameters FACR in the circumferential direction and FACZ in the axial direction as $\varepsilon_{i}-\varepsilon_{i}^{0}=-\varepsilon_{i}^{\text {rel }} \cdot \mathrm{FACR}$ and $\varepsilon_{i}-\varepsilon_{i}^{0}=-\varepsilon_{i}^{\text {rel }} \cdot \mathrm{FACZ}$, respectively. The default values of FACR and FACZ are both 1 .

### 2.2.4 Creep

The creep equation of cladding and pellet is generally represented as

$$
\begin{equation*}
\dot{\bar{\varepsilon}}^{c}=f\left(\bar{\sigma}, \bar{\varepsilon}^{H}, T, \phi, F\right) . \tag{2.2.38}
\end{equation*}
$$

Here,

$$
\begin{array}{ll}
\dot{\bar{\varepsilon}}^{c} & : \text { equivalent creep strain rate }(1 / \mathrm{s}) \\
\bar{\sigma} & : \text { equivalent stress }(\mathrm{Pa}) \\
\bar{\varepsilon}^{H} & : \text { creep hardening parameter (-) } \\
T & : \text { temperature }(\mathrm{K}) \\
\phi & : \text { fast neutron flux }\left(\mathrm{n} / \mathrm{m}^{2} \cdot \mathrm{~s}\right) \\
F & : \\
\text { fission rate }\left(\text { fission } / \mathrm{m}^{3} \cdot \mathrm{~s}\right) .
\end{array}
$$

If the creep hardening parameter $\bar{\varepsilon}^{H}$ is assumed to be equal to the equivalent creep strain $\bar{\varepsilon}^{c}$, the variation rate of the hardening parameter is represented as

$$
\begin{equation*}
\dot{\bar{\varepsilon}}^{H}=f\left(\bar{\sigma}, \bar{\varepsilon}^{H}, T, \phi, \dot{F}\right) . \tag{2.2.39}
\end{equation*}
$$

Equation (2.2.38) is an equation of creep under uniaxial stress. When this equation is generalized for a multi-axial stress state, the creep strain rate vector $\left\{\dot{\varepsilon}^{c}\right\}$ is expressed as a vector function of stress vector and creep hardening parameter. When this vector function is set as $\{\beta\},\left\{\dot{\varepsilon}^{c}\right\}$ is represented as

$$
\begin{equation*}
\left\{\dot{\varepsilon}^{c}\right\}=\left\{\beta\left(\{\sigma\}, \bar{\varepsilon}^{H}\right)\right\} . \tag{2.2.40}
\end{equation*}
$$

where $T, \phi$ and $F$ are omitted because they are known parameters.
When a calculation at time $t_{n}$ is finished and a calculation in the next time increment $\Delta t_{n+1}$ is being performed, the creep strain increment vector is represented as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{c}\right\}=\Delta t_{n+1}\left\{\dot{\varepsilon}_{n+\theta}^{c}\right\}=\left\{\beta\left\{\sigma_{n+\theta}\right\}, \bar{\varepsilon}_{n+\theta}^{H}\right\}, \tag{2.2.41}
\end{equation*}
$$

where

$$
\begin{gathered}
\left\{\sigma_{n+\theta}\right\}=(1-\theta)\left\{\sigma_{n}\right\}+\theta\left\{\sigma_{n+1}\right\} \\
\bar{\varepsilon}_{n+\theta}^{H}=(1-\theta) \bar{\varepsilon}_{n}^{H}+\theta \bar{\varepsilon}_{n+1}^{H} \\
\text { (here, } 0 \leqq \theta \leqq 1 \text { ). }
\end{gathered}
$$

When $\theta=0$ is assumed, the above equation represents a method to treat the creep rate which is determined by a state amount, which is a known value, at the starting point of an increment, i.e. the initial strain method. In this case, the calculation procedure is simple but the solution tends to be numerically unstable; therefore, it is known that the time increment width must be extremely small at high creep rate.

In contrast, when $\theta \neq 0$ is assumed, the calculation procedure becomes complex since the equation contains unknown values; however, as $\theta$ approaches 1 , the stability of the numerical solution improves; this method of setting $\theta \neq 0$ is called an implicit solution.

In FEMAXI-IV, $\theta=0$ is set to stress the importance of the stability.
Now, in a calculation performed from $t_{n}$ to $t_{n+l}$, when the $(i+1)$ th iteration by the NewtonRaphson method is being performed after completion of the (i)th iteration (see eqs. (2.2.30) and (2.2.31)), the creep rate vector can be expressed as follows.

The creep equation (2.2.40) is represented as follows, using a flow rule and eq. (2.2.38).
Since the function form of each principal direction component is identical,

$$
\begin{equation*}
\left\{\dot{\varepsilon}^{c}\right\}=\dot{\bar{\varepsilon}}^{c}\left\{\frac{d \bar{\sigma}}{d \sigma}\right\}=\frac{3 f}{2 \bar{\sigma}}\left\{\sigma^{\prime}\right\} \tag{2.2.42}
\end{equation*}
$$

Here, $\bar{\sigma}$ is an equipvalent stress which will be defined by eq. (2.2.54), given later.
Also, $\left\{\sigma^{\prime}\right\}$ is a deviation stress vector given by

$$
\left\{\sigma^{\prime}\right\}=\left\{\begin{array}{l}
\frac{2 \sigma_{r}-\sigma_{z}-\sigma_{\theta}}{3}+2 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right) \\
\frac{2 \sigma_{z}-\sigma_{\theta}-\sigma_{r}}{3}+2 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right) \\
\frac{2 \sigma_{\theta}-\sigma_{r}-\sigma_{z}}{3}+2 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right)
\end{array}\right\},
$$

which represents deviations of each principal stress component from averages.
Accordingly, the following equation holds.

$$
\begin{align*}
\left\{\dot{\varepsilon}_{n+\theta}^{\left.c^{, i+1}\right\}=}=\right. & \left\{\beta\left(\left\{\sigma_{n+\theta}^{i}\right\}+\theta\left\{d \sigma_{n+1}^{i+1}\right\}, \quad \bar{\varepsilon}_{n+\theta}^{H, i}+\theta d \bar{\varepsilon}_{n+1}^{H,+1}\right)\right\} \\
= & \frac{3 f\left(\bar{\sigma}\left(\left\{\sigma_{n+\theta}^{i}\right\}+\theta\left\{d \sigma_{n+1}^{i+1}\right\}\right), \quad \bar{\varepsilon}_{n+\theta}^{H, i}+\theta d \bar{\varepsilon}_{n+1}^{H, i+1}\right)}{2 \bar{\sigma}\left(\left\{\sigma_{n+\theta}^{i}\right\}+\theta\left\{d \sigma_{n+1}^{i+1}\right\}\right)}  \tag{2.2.43}\\
& \times\left\{\sigma^{\prime}\left(\left\{\sigma_{n+\theta}^{i}\right\}+\theta\left\{d \sigma_{n+1}^{i+1}\right\}\right)\right\}
\end{align*}
$$

Here, $\left\{d \sigma_{n+1}^{i+1}\right\}$ and $\left\{d \bar{\varepsilon}_{n+1}^{H i+1}\right\}$ are the amounts of correction made by iteration calculation.
Through first-order Taylor expansion, we approximate eq. (2.2.43) as follows.

$$
\begin{aligned}
\left\{\dot{\varepsilon}_{n+\theta}^{c,+1}\right\}= & \frac{3}{2 \bar{\sigma}_{n+\theta}^{i}} f_{n+\theta}^{\prime}\left\{\sigma_{n+\theta}^{\prime i}\right\}-\frac{3}{2\left(\bar{\sigma}_{n+\theta}^{i}\right)^{2}} f_{n+\theta}^{i}\left\{\sigma_{n+\theta}^{\prime i}\right\}\left[\frac{\partial \bar{\sigma}}{\partial \sigma}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+1}^{i+1}\right\} \\
& +\frac{3}{2 \bar{\sigma}_{n+\theta}^{i}} f_{n+\theta}^{i}\left[\frac{\partial \sigma^{\prime}}{\partial \sigma}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+1}^{i+1}\right\}+\frac{3}{2 \bar{\sigma}_{n+\theta}^{i}}\left\{\sigma_{n+\theta}^{\prime \prime}\right\}\left(\frac{\partial f}{\partial \bar{\sigma}}\right)_{n+\theta}^{i}\left[\frac{\partial \bar{\sigma}}{\partial \sigma}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+1}^{i+1}\right\} \\
& +\frac{3}{2 \bar{\sigma}_{n+\theta}^{i}}\left\{\sigma_{n+\theta}^{\prime i}\right\}\left(\frac{\partial f}{\bar{\varepsilon}^{H}}\right)_{n+\theta}^{i} \theta d \bar{\varepsilon}_{n+1}^{H,+1} \\
= & \left\{\dot{\varepsilon}_{n+\theta}^{c^{\prime},}\right\}+\frac{3}{2 \bar{\sigma}_{n+\theta}^{i}}\left(\left(\frac{\partial f}{\partial \bar{\sigma}}\right)_{n+\theta}^{i}-\frac{f_{n+\theta}^{i}}{\bar{\sigma}_{n+\theta}^{i}}\right)\left[\sigma^{\prime} \frac{\partial \bar{\sigma}}{\partial \sigma}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+\theta}^{i+1}\right\} \\
& +\frac{3 f_{n+\theta}^{i}}{2 \bar{\sigma}_{n+\theta}^{i}}\left[\frac{\partial \sigma^{\prime}}{\partial \sigma}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+1}^{i+1}\right\}+\frac{3}{2 \bar{\sigma}_{n+\theta}^{\prime}}\left\{\sigma_{n+\theta}^{\prime i}\right\}\left(\frac{\partial f}{\partial \bar{\varepsilon}^{H}}\right)_{n+\theta}^{\prime} \theta d \bar{\varepsilon}_{n+1}^{H,+1}
\end{aligned}
$$

The above equation is rearranged using the relationship $\left\{\frac{\partial \bar{\sigma}}{\partial \sigma}\right\}=\frac{3}{2 \bar{\sigma}}\left\{\sigma^{\prime}\right\}$ as

$$
\begin{align*}
\left\{\dot{\varepsilon}_{n+\theta}^{c^{\prime,+1}}\right\} & =\left\{\dot{\varepsilon}_{n+\theta}^{c^{i}}\right\} \\
& +\frac{9}{4\left(\bar{\sigma}_{n+\theta}^{i}\right)^{2}}\left(\left(\frac{\partial f}{\partial \bar{\sigma}}\right)_{n+\theta}^{i}-\frac{f_{n+\theta}^{i}}{\bar{\sigma}_{n+\theta}^{i}}\right)\left[\sigma_{i}^{\prime} \sigma_{j}^{\prime}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+1}^{i+1}\right\}  \tag{2.2.45}\\
& +\frac{3 f_{n+\theta}^{i}}{2 \bar{\sigma}_{n+\theta}^{i}}\left[\frac{\partial \sigma^{\prime}}{\partial \sigma}\right]_{n+\theta}^{i} \theta\left\{d \sigma_{n+1}^{i+1}\right\}+\frac{3}{2 \bar{\sigma}_{n+\theta}^{i}}\left\{\sigma_{n+\theta}^{\prime \prime}\right\}\left(\frac{\partial f}{\partial \bar{\varepsilon}^{H}}\right)_{n+\theta}^{i} \theta d \bar{\varepsilon}_{n+1}^{H,++1} .
\end{align*}
$$

Meanwhile, the creep hardening increment is represented as follows using eq. (2.2.39).

$$
\begin{aligned}
\Delta \bar{\varepsilon}_{n+\theta}^{H,++1} & =\Delta t_{n+1} f\left(\bar{\sigma}_{n+\theta}^{i+1}, \bar{\varepsilon}_{n+\theta}^{H,+1+}\right) \\
& =\Delta t_{n+1} f\left(\bar{\sigma}\left(\left\{\sigma_{n+\theta}^{\prime}\right\}+\theta\left\{d \sigma_{n+1}^{i+1}\right\}\right), \bar{\varepsilon}_{n+\theta}^{H, i}+\theta d \bar{\varepsilon}_{n+1}^{H,++1}\right)
\end{aligned}
$$

This equation is approximated by carrying out the first-order Taylor expansion as

$$
\begin{align*}
\Delta \bar{\varepsilon}_{n+\theta}^{H, i+1}= & \Delta \bar{\varepsilon}_{n+\theta}^{H, i}+d \bar{\varepsilon}_{n+1}^{i+1} \\
= & \Delta t_{n+1} f_{n+\theta}^{\prime}+\theta \Delta t_{n+1}\left(\frac{\partial f}{\partial \sigma}\right)_{n+\theta}^{i}\left\lfloor\frac{\partial \bar{\sigma}}{\partial \sigma}\right]_{n+\theta}^{i}\left\{d \sigma_{n+1}^{i+1}\right\}  \tag{2.2.46}\\
& +\theta \Delta t_{n+1}\left(\frac{\partial f}{\partial \varepsilon^{H}}\right)_{n+\theta}^{i} \quad d \bar{\varepsilon}_{n+1}^{H,+1}
\end{align*}
$$

Here, since $\Delta \bar{\varepsilon}_{n+\theta}^{H,+1}=\Delta t_{n+1} f_{n+\theta}^{i}, d \bar{\varepsilon}_{n+1}^{H, i+1}$ is expressed as

$$
\begin{equation*}
d \bar{\varepsilon}_{n+1}^{H,+1}=\frac{\theta \Delta t_{n+1}\left(\frac{\partial f}{\partial \bar{\sigma}}\right)_{n+\theta}^{\prime} \frac{\left|\frac{\partial \sigma}{\partial \sigma}\right|_{n+\theta}^{\prime}\left\{d \sigma_{n+1}^{\prime+1}\right\}}{1-\theta \Delta t_{n+1}\left(\frac{\partial f}{\partial \bar{\varepsilon}^{H}}\right)_{n+\theta}^{\prime}} . . . ~ . ~ . ~}{1} \tag{2.2.47}
\end{equation*}
$$

Substituting this equation into eq. (2.2.45) and rearranging, we obtain

$$
\begin{equation*}
\left\{\dot{\varepsilon}_{n+\theta}^{c, i+1}\right\}=\left\{\dot{\varepsilon}_{n+\theta}^{c, i}\right\}+F_{1} \theta\left[\sigma_{1}^{\prime} \sigma^{\prime}\right]_{n+\theta}^{i}\left\{d \sigma_{n+1}^{\prime+1}\right\}+F_{2} \theta\left[\frac{\partial \sigma^{\prime}}{\partial \sigma}\right]_{n+1}^{1}\left\{d \sigma_{n+1}^{\prime+1}\right\} \tag{2.2.48}
\end{equation*}
$$

where

$$
\begin{align*}
F_{1}=\frac{9}{4\left(\bar{\sigma}_{n+\theta}^{\prime}\right)^{2}} & \left.\left(\frac{\partial f}{\partial \bar{\sigma}}\right)_{n+\theta}^{\prime}-\frac{f_{n+\theta}^{i}}{\bar{\sigma}_{n+\theta}^{i}}+\frac{\left(\frac{\partial f}{\partial \bar{\varepsilon}^{H}}\right)_{n+\theta}^{\prime} \theta \Delta t_{n+1}\left(\frac{\partial f}{\partial \bar{\sigma}}\right)_{n+\theta}^{\prime}}{1-\theta \Delta t_{n+1}\left(\frac{\partial f}{\partial \bar{\varepsilon}^{H}}\right)_{n+\theta}^{\prime}}\right)  \tag{2.2.49}\\
F_{2} & =\frac{3 f_{n+\theta}^{\prime}}{2 \bar{\sigma}_{n+\theta}^{\prime}} . \tag{2.2.50}
\end{align*}
$$

The creep strain increment is given as

$$
\left.\left.\begin{array}{rl}
\left\{\Delta \varepsilon_{n+1}^{c, i+1}\right\} & =\Delta t_{n+1}\left\{\dot{\varepsilon}_{n+\theta}^{c, i+1}\right\}  \tag{2.2.51}\\
& =\left\{\Delta \varepsilon_{n+1}^{c,}\right\}+\left[C_{n+\theta}^{c,}\right]
\end{array}\right\} d \sigma_{n+1}^{\prime+1}\right\} . .
$$

where

$$
\left[C_{n+\theta}^{c, i}\right]=\theta \Delta t_{n+1}\left(F_{1}\left[\sigma_{,}^{\prime} \sigma_{j}\right]_{n+\theta}^{i}+F_{2}\left[\frac{\partial \sigma^{\prime i}}{\partial \sigma_{n+\theta}}\right]\right) .
$$

Thus, $\left\{\Delta \varepsilon_{n+1}^{c, i+1}\right\}$ in eq. (2.2.37) was eliminated. Substituting eq. (2.2.51) into eq. (2.2.37) and rearranging, we obtain

$$
\begin{align*}
\left\{d \sigma_{n+1}^{i+1}\right\} & =\left[\hat{D}_{n+\theta}^{\prime}\right]\left([B]\left\{\Delta u_{n+1}^{\prime+1}\right\}-\left[C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)\right.  \tag{2.2.52}\\
& \left.-\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left\{\Delta \varepsilon_{n+1}^{c_{i}^{i}}\right\}-\left\{\Delta \varepsilon_{n+1}^{P, i+1}\right\}\right)
\end{align*}
$$

where

$$
\left[\hat{D}_{n+1}^{i}\right]=\left(\left[C_{n+1}^{i}\right]+\left[C_{n+1}^{c, i}\right]\right)^{-1}
$$

$$
\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{u_{n+1}^{\prime}\right\}+\left\{d u_{n+1}^{i+1}\right\}-\left\{u_{n}\right\}
$$

and ${ }^{\wedge}$ means the apparent stiffness.

### 2.2.5 Plasticity

The yield condition of pellet and cladding is given by

$$
\begin{equation*}
h(\{\sigma\})=K\left(\bar{\varepsilon}^{P}, T\right) \tag{2.2.53}
\end{equation*}
$$

where

$$
\begin{array}{ll}
\bar{\varepsilon}^{P} & : \text { equivalent plastic strain } \\
T & : \text { temperature } \\
K & : \text { yield surface area } \\
h & : \text { yield function. }
\end{array}
$$

The yield function $h$ is given as follows, with consideration of the cladding anisotropy and the pellet compressibility (hot-press). However, the shear component is not taken into account in this model.

$$
\begin{align*}
h & =\frac{3}{2(F+G+H)}\left[\left\{\mathrm{H}\left(\sigma_{r}-\sigma_{\theta}\right)^{2}+\mathrm{F}\left(\sigma_{\theta}-\sigma_{z}\right)^{2}+\mathrm{G}\left(\sigma_{z}-\sigma_{r}\right)^{2}\right\}\right.  \tag{2.2.54}\\
& \left.+3 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right)^{2}\right]^{\frac{1}{2}} \equiv \bar{\sigma}
\end{align*}
$$

Here,
$\mathrm{H}, \mathrm{F}, \mathrm{G}:$ anisotropic coefficients $(\mathrm{H}=1, \mathrm{~F}=1$ and $\mathrm{G}=1$ are set for the pellet based on the assumption of isotropy of the pellet)
$\alpha \quad$ : pellet hot-press parameter ( $\alpha=0$ for cladding $)^{(22)}$.

Fitting parameters $\mathrm{HO}(2), \mathrm{FO}(2)$ and $\mathrm{GO}(2)$
Anisotropic coefficients of cladding $\mathrm{H}, \mathrm{F}$ and G are designated by $\mathrm{H} 0(2), \mathrm{F} 0(2)$ and $\mathrm{G} 0(2)$. The default values for these are 1.0 .

Fitting parameter IHOT When IHOT $=1$, pellet hot-press parameter $\alpha$ is defined
as a function of porosity $p$ as

$$
\alpha=\operatorname{BETAX} \frac{p}{1-D_{0}}
$$

Here, $\quad p$ : porosity inside a pellet
$D_{0}$ : initial theoretical density ratio
BETAX: initial value of hot-press parameter.

## Fitting parameter BETAX

Pellet hot-press parameter $\alpha$ is designated by BETAX. The default value is 0.002 .

The plastic strain increment vector from time $t_{n}$ to $t_{n+1}$ is represented by the flow rule as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{P}\right\}=\Delta \bar{\varepsilon}_{n+1}^{P}\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta} . \tag{2.2.55}
\end{equation*}
$$

During the $(i+1)$ th iteration that follows the (i)th iteration, the yield condition and flow rule are expressed as

$$
\begin{align*}
& h\left(\left\{\sigma_{n}\right\}+\left\{\Delta \sigma_{n+1}^{\prime+1}\right\}\right)=K\left(\bar{\varepsilon}_{n}^{P}+\Delta \bar{\varepsilon}_{n+1}^{P, t+1}, T_{n}+\Delta T_{n+1}\right)  \tag{2.2.56}\\
& \left\{\Delta \varepsilon_{n+1}^{P, i+1}\right\}=\Delta \bar{\varepsilon}_{n+1}^{P,+1}\left\{\frac{\partial}{\partial \sigma}\right\}_{n+\theta}^{\prime} . \tag{2.2.57}
\end{align*}
$$

Performing the first-order Taylor expansion for eq. (2.2.56) with respect to $\left\{\Delta \sigma_{n+1}^{i+1}\right\}$, $\Delta \bar{\varepsilon}_{n+1}^{P,+1}$ and $\Delta T_{n+1}$, we obtain the following approximation.
$h\left\{\sigma_{n}\right\}+\left\lfloor\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{\prime}\left\{\Delta \sigma_{n+1}^{i+1}\right\}=K\left(\bar{\varepsilon}_{n}^{P} T_{n}\right)+\left(\frac{\partial K}{\partial \bar{\varepsilon}^{P}}\right)_{n+\theta}^{\prime} \Delta \bar{\varepsilon}_{n+1}^{P, i+1}+\left(\frac{\partial K}{\partial T}\right)_{n+\theta} \Delta T_{n+1}$
By substituting

$$
\begin{equation*}
\left\{\Delta \sigma_{n+1}^{i+1}\right\}=\left\{\Delta \sigma_{n+1}^{\prime}\right\}+\left\{d \sigma_{n+1}^{i+1}\right\}-\left\{\sigma_{n}\right\} \tag{2.2.59}
\end{equation*}
$$

into eq. (2.2.58) and rearranging the equation, we obtain

$$
\begin{gather*}
\Delta \bar{\varepsilon}_{n+1}^{P, i+1}=\frac{1}{H_{n+\theta}^{\prime i}}\left(\left\lfloor\frac{\partial h}{\partial \sigma}\right\rfloor_{n+\theta}^{t}\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)+h\left(\left\{\sigma_{n}\right\}\right)-K\left(\bar{\varepsilon}_{n}^{P}, T_{n}\right)\right. \\
\left.-\left(\frac{\partial K}{\partial T}\right)_{n+\theta} \Delta T_{n+1}+\left\lfloor\frac{\partial}{\partial \sigma}\right\rfloor_{n+\theta}^{i}\left\{d \sigma_{n+1}^{i+1}\right\}\right), \tag{2.2.60}
\end{gather*}
$$

where

$$
\begin{equation*}
H_{n+\theta}^{\prime i}=\left(\frac{\partial K}{\partial \bar{\varepsilon}_{p}}\right)_{n+\theta}^{\prime} \tag{2.2.61}
\end{equation*}
$$

Substituting eq. (2.2.52) into eq. (2.2.60), we obtain

$$
\begin{align*}
H_{n+1}^{\prime i} & \Delta \bar{\varepsilon}_{n+1}^{P,+1}+\left(\frac{\partial K}{\partial T}\right)_{n+\theta} \Delta T_{n+1}-h\left(\left\{\sigma_{n}\right\}\right)+K\left(\bar{\varepsilon}_{n}^{P}, T_{n}\right) \\
= & {\left[\left.\frac{\partial \sigma}{\partial \sigma}\right|_{n+\theta} ^{\prime}\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)\right.}  \tag{2.2.62}\\
& +\left\lfloor\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right]\left([B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left[C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\Delta \bar{\varepsilon}_{n+1}^{P, i+1}\left[\frac{\partial h}{\partial \sigma}\right]_{n+\theta}^{i}\right) .
\end{align*}
$$

Rearranging eq. (2.2.54) with respect to $\Delta \bar{\varepsilon}_{n+1}^{P, i+1}$, we obtain

$$
\begin{gather*}
\Delta \bar{\varepsilon}_{n+1}^{P, i+1}=\frac{\left[\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{\prime}\right]\left[\left([B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left[C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right)\right.}{H_{n+\theta}^{\prime i}+\left[\left.\frac{\hbar}{\partial \sigma}\right|_{n+\theta} ^{i}\left[\hat{D}_{n+\theta}^{\prime}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{\prime}\right.} \\
+\frac{\left(\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)-\left(\frac{\partial K}{\partial T}\right)_{n+\theta} \Delta T_{n+1}-h\left(\left\{\sigma_{n}\right\}\right)+K\left(\bar{\varepsilon}_{n}^{P}, T_{n}\right)}{H_{n+\theta}^{\prime i}+\left[\frac{\hbar}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i}} \tag{2.2.63}
\end{gather*}
$$

Using eq. (2.2.57) and substituting the above equation into eq. (2.2.52), we obtain

$$
\begin{align*}
&\left\{d \sigma_{n+1}^{i+1}\right\}\left.\left.=\left[\hat{D}_{n+\theta}^{i}\right]\right\}[B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left[C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right) \\
&-\frac{\left.\left.\left[\hat{D}_{n+\theta}^{\prime}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i} \right\rvert\, \frac{\partial h}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{\prime}\right]}{H_{n+\theta}^{\prime \prime}+\left[\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i}} \\
&\left.\left.\times\left([B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left[C_{n+\theta}^{i}\right]\right]\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right)  \tag{2.2.64}\\
&- {\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\partial}{\partial \sigma}\right\}_{n+\theta}^{\prime}\left(\left\lfloor\frac{\partial h}{\partial \sigma}\right]_{n+\theta}^{i}\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)-\left(\frac{\partial K}{\partial T}\right)_{n+\theta} \Delta T_{n+1}-h\left(\left\{\sigma_{n}\right\}\right)+K\left(\bar{\varepsilon}_{n}^{P}, T_{n}\right)\right) } \\
& H_{n+\theta}^{\prime i}+\left\lfloor\frac{\partial h}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{\prime}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i}
\end{align*} .
$$

This equation is rearranged as follows.

$$
\begin{align*}
\left\{d \sigma_{n+1}^{i+1}\right\}= & {\left[\hat{D}_{n+\theta}^{p, j}\right]\left([B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left[C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right) }  \tag{2.2.65}\\
& +\left\{S_{n+\theta}^{i}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}
\end{align*}
$$

Here, the following equations hold.

$$
\begin{align*}
& {\left[\hat{D}_{n+\theta}^{P, i}\right]=\left[\hat{D}_{n+\theta}^{i}\right]-\frac{\left[\hat{D}_{n+\theta}^{i}\right]\left[\frac{\hbar}{\partial \sigma}\right]_{n+\theta}^{i}\left[\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right]}{H_{n+\theta}^{\prime i}+\left[\frac{\hbar h}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\hbar h}{\partial \sigma}\right\}_{n+\theta}^{i}}}  \tag{2.2.66}\\
& \left\{S_{n+\theta}^{i}\right\}=\frac{\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\hbar}{\partial \sigma}\right\}_{n+\theta}^{i}\left(\frac{\partial K}{\partial T}\right)_{n+\theta}}{H_{n+\theta}^{\prime i}+\left[\frac{\hbar}{\partial \sigma}\right\}_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right\}\left\{\frac{\partial}{\partial \sigma}\right\}_{n+\theta}^{i}} \tag{2.2.67}
\end{align*}
$$

$$
\begin{gather*}
\text { JAERI-Data/Code 97-043 } \\
\left\{Z_{1}\right\}=\frac{\left[\hat{D}_{n+\theta}^{\prime}\right]\left\{\frac{\partial}{\partial \sigma}\right\}_{n+\theta}^{i}\left[\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)}{H_{n+\theta}^{\prime i}+\left[\frac{\partial}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i}}  \tag{2.2.68}\\
\left\{Z_{21}\right\}=\frac{\left[\hat{D}_{n+\theta}^{i}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i}\left[\frac{\partial h}{\partial \sigma}\right]_{n+\theta}^{i}\left(h\left(\left\{\sigma_{n}\right\}\right)-K\left(\bar{\varepsilon}_{n}^{P}, T_{n}\right)\right)}{H_{n+\theta}^{\prime i}+\left[\frac{\partial h}{\partial \sigma}\right]_{n+\theta}^{i}\left[\hat{D}_{n+\theta}^{\prime}\right]\left\{\frac{\partial h}{\partial \sigma}\right\}_{n+\theta}^{i}} \tag{2.2.69}
\end{gather*}
$$

Thus, the unknown value $\left\{\Delta \varepsilon_{n+1}^{p, i+1}\right\}$ in eq. (2.2.30) was eliminated.
Accordingly, eq. (2.2.65) is a constitutive equation in which all the unknown values regarding pellet cracks, as well as creep and plasticity of pellet and cladding are eliminated.

In the above calculation, for the yield stress and creep rate of pellet and cladding, the same material properties values as those used in section 2.1 .3 (contact force evaluation model) are used.

### 2.2.6 Derivation of stiffness equation

The constitutive equation ( 2.2 .65 ) in which pellet cracks, creep and plasticity are expressed with known values is rewritten as

$$
\begin{align*}
\left\{d \sigma_{n+1}^{i+1}\right\}= & {\left[\hat{D}_{n+\theta}^{p, 1}\right]\left[[B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left[C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\left\{\Delta \varepsilon_{n+1}^{C_{1}^{\prime}}\right\}\right) }  \tag{2.2.65}\\
& +\left\{S_{n+\theta}^{i}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\} .
\end{align*}
$$

Substituting eq. (2.2.65) into the equilibrium condition equation (2.2.31) and rearranging the equation, we obtain the following stiffness equation.

$$
\begin{equation*}
\left[K_{n+\theta}^{i}\right]\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{i}\right\} \tag{2.2.70}
\end{equation*}
$$

For applying stiffness equation (2.2.70) to each element, each term of the equation is determined by integral with element volume, as shown in the following equations.

$$
\begin{equation*}
\left[K_{n+\theta}^{i}\right]=2 \pi \iint[B]^{T}\left[\hat{D}_{n+\theta}^{p_{i}, i}\right][B] \quad r d r d z \tag{2.2.71}
\end{equation*}
$$

$$
\begin{align*}
\left\{\Delta \hat{F}_{n+1}^{\prime}\right\} & \left.=2 \pi \iint[B]^{T}\left[\hat{D}_{n+\theta}^{p,}\right]\right\}\left\{C_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right) \\
& \left.+\left\{\Delta \varepsilon_{n+1}^{o}\right\}+\left\{\Delta \varepsilon_{n+1}^{c,}\right\}\right\} r d r d z  \tag{2.2.72}\\
& -2 \pi \iint[B]^{T}\left(\left\{S_{n+\theta}^{\prime}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) r d r d z \\
& +\left\{F_{n+1}\right\}-2 \pi \iint[B]^{T}\left(\sigma_{n+\theta}^{i}\right) \quad r d r d z
\end{align*}
$$

Here, the right-hand side of the stiffness equation of elements is expressed with $\left\{\Delta \hat{F}_{n+1}^{\prime}\right\}$ because this value represents the load increment vector, since the solution obtained from stiffness equation (2.2.70) is a displacement increment, $\left\{\Delta u_{n+1}^{i+1}\right\}$. The symbol $\wedge$ in $\Delta \hat{F}_{n+1}^{\prime}$ means that this term is a tentative value of $\Delta F_{n+1}$ during the iteration calculation.

Next, treatment method for spring elements in the upper and lower plenums will be explained. Regarding the spring elements in the upper and lower plenums, a degree of freedom is considered only in the axial direction, and only initial elastic strain (thermal strain) is allowed. Therefore, when

$$
\left\{\Delta \varepsilon_{n+1}^{p}\right\}=0, \quad\left\{\Delta \varepsilon_{n+\theta}^{c}\right\}=0
$$

are assumed in eq. (2.2.29), we obtain

$$
\begin{equation*}
\left[C_{n+\theta}\right]\left\{\Delta \sigma_{n+1}\right\}-[B]\left\{\Delta u_{n+1}\right\}+\left\{\Delta \varepsilon_{n+\theta}^{o}\right\}=0 . \tag{2.2.73}
\end{equation*}
$$

Equation (2.2.73) can also be expressed as

$$
\left[C_{n+\theta}\right]\left(\left\{\sigma_{n+1}\right\}+\left\{d \sigma_{n+\theta}^{i+1}\right\}-\left\{\sigma_{n}\right\}\right)-[B]\left\{\Delta u_{n+\theta}^{i+1}\right\}+\left\{\Delta \varepsilon_{n+\theta}^{o}\right\}=0 .
$$

Here, if we permute $\left[D_{n+\theta}\right]=\left[C_{n+\theta}\right]^{-1}$, the following equation holds.

$$
\begin{equation*}
\left\{d \sigma_{n+\theta}^{i+1}\right\}=\left[D_{n+\theta}\right]\left([B]\left\{\Delta u_{n+\theta}^{i+1}\right\}-\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left[C_{n+\theta}\right]\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right) \tag{2.2.74}
\end{equation*}
$$

Substituting this equation into eq. (2.2.31), we obtain

$$
\begin{align*}
& \left.\int_{v}[B]^{T}\left[D_{n+\theta}\right]\right]\left[[B]\left\{\Delta u_{n+1}^{i+1}\right\}-\left\{\Delta \varepsilon_{n+1}^{o}\right\}-\left[C_{n+\theta}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)\right) d V  \tag{2.2.75}\\
& +\int_{v}[B]^{T}\left\{\sigma_{n+1}^{i}\right\} d V=\left\{F_{n+1}\right\} .
\end{align*}
$$

Moving the unknown values to the left-hand side of this equation, we obtain

$$
\begin{align*}
& \int_{V}[B]^{T}\left[D_{n+\theta}\right][B]\left\{\Delta u_{n+1}^{i+1}\right\} d V \\
& =\left\{F_{n+1}\right\}+\int_{V}[B]^{T}\left[D_{n+\theta}\right]\left\{\Delta \varepsilon_{n+1}^{o}\right\} d V+\int_{V}[B]^{T}\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right) d V  \tag{2.2.76}\\
& \quad-\int_{V}[B]^{T}\left\{\sigma_{n+1}^{i}\right\} d V,
\end{align*}
$$

and the following equation holds.

$$
\begin{align*}
\int_{v}[B]^{T}\left[D_{n+\theta}\right][B]\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{F_{n+1}\right\} & +\int_{V}[B]^{T}\left[D_{n+\theta}\right]\left\{\Delta \varepsilon_{n+1}^{a}\right\} d V  \tag{2.2.77}\\
& -\int_{V}[B]^{T}\left\{\sigma_{n}\right\} d V
\end{align*}
$$

Equation (2.2.77) can be expressed as

$$
\begin{align*}
& {\left[K_{n+\theta}^{i}\right]\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{i}\right\}} \\
& {\left[K_{n+\theta}^{\prime}\right]=\left\{[B]^{T}\left[\hat{D}_{n+\theta}^{p, t}\right][B] d V\right.}  \tag{2.2.78}\\
& \left\{\Delta \hat{F}_{n+1}^{i}\right\}=\left\{F_{n+1}\right\}-\int[B]^{T}\left[D_{n+\theta}\right]\left\{\Delta \varepsilon_{n+1}^{0}\right\} d V-\int[B]^{T}\left\{\sigma_{n}\right\} d V
\end{align*}
$$

Therefore, eq.(2.2.78) is the constitutive equation in which the unknown variables are eliminated. This equation is expressed using vectors, but a degree of freedom is allowed only in the axial direction.

The external force is given as

$$
\begin{equation*}
F_{n+1}=\pi r_{c \prime}^{2} P_{k a r, n+1}-\pi r_{c o}^{2} P_{w a l e r, n+1} . \tag{2.2.79}
\end{equation*}
$$

Here,

$$
\begin{aligned}
r_{c o} & : \text { cladding outer radius }(\mathrm{m}) \\
r_{c i} & : \text { cladding inner radius }(\mathrm{m}) \\
P_{\text {water }, n+1} & : \text { coolant pressure in }(n+1) \text { th stage }(\mathrm{Pa}) \\
P_{\text {gas. } n+1} & : \text { plenum pressure in }(n+1) \text { th stage }(\mathrm{Pa}) .
\end{aligned}
$$

The third term on the right-hand side of eq. (2.2.77) is given by

$$
\begin{equation*}
\int[B]^{T}\left\{\sigma_{n}\right\} d V=k\left(v_{p l, n}-v_{u, n}\right), \tag{2.2.80}
\end{equation*}
$$

where

$$
\begin{array}{cll}
k & : & \text { spring constant }(\mathrm{N} / \mathrm{m}) \\
v_{p l, n}: & \text { upper part displacement of plenum in } n \text {th stage }(\mathrm{m}) \\
v_{u, n} & : & \text { upper part displacement of pellet (or cladding) in }(n) \text { th stage }(\mathrm{m}) .
\end{array}
$$

A similar calculation is applied to the lower plenum.
2.2.7 External force and contact force acting on pellet and cladding Forces acting on pellet and cladding are shown in Fig. 2.33.


Fig. 2.33 Forces acting on pellet and cladding.
Here,

$$
\begin{aligned}
F_{2} & : \text { contact force between pellet and cladding } \\
F_{3} & : \text { axial force } \\
F_{p c a} & : \text { plenum gas pressure } \\
F_{p c b} & : \text { coolant pressure. }
\end{aligned}
$$

The contact force between pellet and cladding is calculated independently of the calculation described in section 2.1.3.

Since gas is introduced inside the pellet by plenum gas pressure through the cracks, pellet compressive deformation caused by the plenum gas pressure are ignored in the calculation.

### 2.2.8 Boundary conditions

The boundary conditions are explained using the case of a three-layer pellet and two-layer cladding as an example, as shown in Fig. 2.34, and formulation for the total matrix is performed.


Fig. 2.34 Example of analysis model.

In Fig. 2.34, $u$ is the radial displacement, and $v$ is the axial displacement.
The stiffness equations for each element (2.2.70) and (2.2.72) and the stiffness equation (2.2.78) for upper and lower plenums are shown below.

$$
\begin{align*}
& {\left[K_{n+\theta}^{i}\right]\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{i}\right\} }  \tag{2.2.70}\\
&\left\{\Delta \hat{F}_{n+1}^{i}\right\}=\left.2 \pi \iint[B]^{T}\left[\hat{D}_{n+\theta}^{P, i}\right]\right]\left\{\left[\widetilde{C}_{n+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)\right. \\
&\left.+\left\{\Delta \varepsilon_{n+1}^{o}\right\}+\left\{\Delta \varepsilon_{n+1}^{c, \prime}\right\}\right\} r d r d z  \tag{2.2.72}\\
&-2 \pi \iint[B]^{T}\left(\left\{S_{n+\theta}^{i}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) r d r d z \\
&+\left\{F_{n+1}\right\}-2 \pi \iint[B]^{T}\left(\sigma_{n+1}^{i}\right) r d r d z \\
& {\left[K_{n+\theta}^{i}\right]\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{i}\right\} } \\
& {\left[K_{n+\theta}^{i}\right]=}\left\{[B]^{T}\left[\hat{D}_{n+\theta}^{p, i}\right][B] d V\right.  \tag{2.2.78}\\
&\left\{\Delta \hat{F}_{n+1}^{i}\right\}=\left\{F_{n+1}\right\}-\int[B]^{T}\left[D_{n+\theta}\right]\left\{\Delta \varepsilon_{n+1}^{0}\right\} d V-\int[B]^{T}\left\{\sigma_{n}\right\} d V
\end{align*}
$$

When the Newton-Raphson iteration is completed, these equations can be expressed as follows with omission of subscripts for iteration $i$.

$$
\begin{equation*}
\left[K_{n+\theta}\right]\left\{\Delta u_{n+1}\right\}=\left\{\Delta F_{n+1}\right\} \tag{2.2.81}
\end{equation*}
$$

Equation (2.2.81) can be expressed as follows for convenience in the following discussion.

$$
\begin{equation*}
\left[B_{e v}\right]\left\{\Delta u_{n+1}\right\}=\left\{F_{n+1}\right\}+\left\{B_{e l, n+1}\right\} \tag{2.2.82}
\end{equation*}
$$

Here,

$$
\begin{aligned}
& {\left[B_{e e}\right]=\left[K_{n+\theta}\right]} \\
& \left\{B_{e t, n+1}\right\}=\left\{\Delta F_{n+1}\right\}-\left\{F_{n+1}\right\} .
\end{aligned}
$$

Thus, the element matrices have been formulated; the formulation of the total matrix is explained next.

The total matrix for the segments is represented as follows, using the model shown in Fig. 2.34 as an example.

$$
\begin{aligned}
& {\left[\begin{array}{ccccccccc}
B_{11}^{1} & B_{12}^{1} & 0 & 0 & 0 & 0 & 0 & B_{13}^{1} & 0 \\
B_{21}^{1} & B_{22}^{1}+B_{11}^{2} & B_{12}^{1} & 0 & 0 & 0 & 0 & B_{23}^{1}+B_{13}^{2} & 0 \\
0 & B_{21}^{2} & B_{22}^{1}+B_{11}^{3} & B_{12}^{3} & 0 & 0 & 0 & B_{23}^{2}+B_{13}^{2} & 0 \\
0 & 0 & B_{21}^{3} & B_{22}^{3} & 0 & 0 & 0 & B_{23}^{3} & 0 \\
0 & 0 & 0 & 0 & B_{11}^{4} & B_{12}^{4} & 0 & 0 & B_{13}^{4} \\
0 & 0 & 0 & 0 & B_{21}^{4} & B_{22}^{4}+B_{12}^{5} & B_{12}^{5} & 0 & B_{23}^{4}+B_{13}^{5} \\
0 & 0 & 0 & 0 & 0 & B_{21}^{5} & B_{22}^{5} & 0 & B_{23}^{5} \\
B_{31}^{1} & B_{32}^{1}+B_{31}^{2} & B_{32}^{2}+B_{31}^{3} & B_{21}^{3} & 0 & 0 & 0 & B_{33}^{1}+B_{33}^{2}+B_{33}^{3} & 0 \\
0 & 0 & 0 & 0 & B_{31}^{4} & B_{32}^{4}+B_{31}^{5} & B_{32}^{5} & 0 & B_{33}^{4}+B_{33}^{5}
\end{array}\right]\left\{\begin{array}{l}
\Delta u_{1} \\
\Delta u_{2} \\
\Delta u_{3} \\
\Delta u_{4} \\
\Delta u_{5} \\
\Delta u_{6} \\
\Delta u_{2} \\
\Delta v_{1} \\
\Delta v_{2}
\end{array}\right\}}
\end{aligned}
$$

In this equation, the suffix number * of $B^{*}$ represents the number of elements in Fig. 2.34, and only $F_{p c a}$ and $F_{p c h}$ in Fig. 2.33 are considered as external force vectors $\left\{F_{n+1}\right\}$. Therefore, as a boundary condition for the total matrix of the segment, that corresponding to the contact state between pellet and cladding must be incorporated. Below, a case in which the pellet is in contact with the cladding is analyzed.

## (1) Clogged gap state case

In the case of a clogged gap state, the displacement of the outermost layer of the pellet $\Delta u_{4}$ and the displacement of the innermost layer of the cladding $\Delta u_{5}$ are positioned in the same place of the displacement vector matrix. Therefore, eq. (2.2.82) is given by

$F_{3}$ is obtained by solving eq. (2.2.84).
Then, eq. (2.3.83) is rearranged as follows and incorporated into the total matrix.

$l$ in eq. (2.2.85) is a segment number. Also, $B_{33}^{1+2+3}=B_{33}^{1}+B_{33}^{2}+B_{33}^{3}$ is used. This matrix is symmetric.

## (2) Sliding state case

In the case of sliding, the equation below is given in place of eq. (2.2.84).

where $\quad \mu$ : friction coefficient.
$F_{2}$ is obtained by solving eq. (2.2.86). Then, using

$$
\begin{equation*}
F_{3}=\mu F_{2}, \tag{2.2.87}
\end{equation*}
$$

we incorporate eq. (2.2.85) into the total matrix.
The friction coefficient $\mu$ must be corrected with respect to the different frictional areas, because $F_{2}$ is affected by the area of the pellet side $2 \pi r_{0} l_{z}$, and $F_{3}$ is affected by the area of the pellet cross section $\pi\left(r_{o}^{2}-r_{1}^{2}\right)$. Namely, the following conversion is performed.

$$
\begin{equation*}
\mu=\frac{r_{o}^{2}-r_{i}^{2}}{2 r_{o} l_{z}} \cdot \mu \tag{2.2.88}
\end{equation*}
$$

Here,
$r_{i}$ : pellet inner diameter
$r_{o}$ : pellet outer diameter
$l_{z}$ : length of the pellet in the axial direction
$\mu$ : friction coefficient (measured value)

## Fitting parameter AMU

Friction coefficient $\mu$ is designated by AMU. The default value of AMU is 0.4 .

## (3) Open gap state case

When gaps are open, no contact force is generated; therefore, contact forces in the radial and axial directions $F_{2}$ and $F_{3}$ in eq. (2.2.81) are set to be 0 and incorporated into the total matrix.

### 2.2.9 Creation of total matrix

When the number of axial segments of the pellet stack is assumed to be 3 , the total matrix regarding the pellet stack is given by


In order to avoid complexity in the later discussion, we express eq. (2.2.89) as follows through rearrangement of this equation, similar to the case of eqs. (2.2.81) and (2.2.82).

$$
\begin{equation*}
\left[B_{c e}^{T}\right]\{\Delta u\}=\{\Delta F\} . \tag{2.2.90}
\end{equation*}
$$

### 2.2.10 Boundary conditions for upper plenum and lower plenum

The presence of the upper and the lower plenums gives a boundary condition for the mechanical analysis. Described below are how this boundary condition is reflected in the total matrix.
(1) Upper plenum


Fig. 2.35 Boundary conditions for upper plenum

When plenum pressure is represented as $P_{\text {gas }}$, coolant pressure as $P_{\text {water }}$, inner radius of cladding as $N_{c a}$, and outer radius of cladding as $r_{c b}$, the external force $F_{p c z}$ on boundary plane (I) is given as

$$
\begin{equation*}
F_{p c z}=\pi r_{c a}^{2} P_{g a s}-\pi r_{c b}^{2} P_{\text {waler }} . \tag{2.2.91}
\end{equation*}
$$

$F_{p c z}$ on boundary plane (I) is equal to the sum of force $F_{1 z}$ given by the plenum spring and reaction force $F_{2 z}$ which is produced in the axial direction by the elasticity of the cladding surrounding the plenum. $\quad F_{p c z}$ is given by

$$
\begin{equation*}
F_{p c z}=-\left(F_{1 z}+F_{2 z}\right) . \tag{2.2.92}
\end{equation*}
$$

Here, with the plenum spring constant assigned as $k_{s}$ and the apparent spring constant of the cladding for the plenum part as $k_{c}, F_{1 z}$ and $F_{2 z}$ are given by

$$
\left.\begin{array}{l}
F_{1 z}=-k_{s}\left(v_{s z}-v_{1,3}^{u}\right)+k_{s} \alpha_{s} l_{s z}^{u}\left(T_{n+1}-T_{o}\right)  \tag{2.2.93}\\
F_{2 z}=-k_{c}\left(v_{s z}-v_{23}^{u}\right)+k_{s} \alpha_{c} l_{s z}^{u}\left(T_{n+1}-T_{o}\right)
\end{array}\right\},
$$

where
$v_{s z}$ : axial displacement at boundary plane (I)
$v_{1,3}^{u}$ : axial displacement of pellet at boundary plane (II)
$\nu_{2,3}^{u} \quad: \quad$ axial displacement of cladding at boundary plane (II)
$\alpha_{s}$ : thermal expansion coefficient of plenum spring
$\alpha_{c}$ : thermal expansion coefficient of cladding for the plenum part
$l_{\mathrm{s}}^{\prime \prime}$ : upper plenum length
$T_{n+1}$ : plenum temperature at current time step $((\mathrm{n}+1)$ th step $)$
$T_{0}$ : initial plenum temperature.

## Fitting parameters XKSU, XKSL, AKSU and AKSL

Spring constant of upper plenum XKSU, spring constant of lower plenum XKSL, thermal expansion coefficient of upper plenum spring AKSU, and thermal expansion coefficient of lower plenum spring AKSL are designated by input values.

Default values are: $\mathrm{XKSU}=1500(\mathrm{~N} / \mathrm{m}), \quad \mathrm{XKSL}=2500(\mathrm{~N} / \mathrm{m})$, and $\mathrm{AKSU}=\mathrm{AKSL}=1.5 \times 10^{-5}(1 / \mathrm{K})$.

Next, eq. (2.2.93) is rearranged to express the increments as follows.

$$
\left.\begin{array}{l}
\Delta F_{1 z}=-k_{s}\left(\Delta v_{s z}-\Delta v_{1,3}^{\prime \prime}\right)+k_{s} \alpha_{s} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right)  \tag{2.2.94}\\
\Delta F_{2 z}=-k_{c}\left(\Delta v_{s z}-\Delta v_{2,3}^{U \prime}\right)+k_{c} \alpha_{s} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right)
\end{array}\right\}
$$

Then eq. (2.2.94) is rewritten as

$$
\left.\begin{array}{l}
\left\{\begin{array}{r}
-\Delta F_{1 z} \\
\Delta F_{1 z}
\end{array}\right\}=\left\{\begin{array}{r}
-k_{s} \alpha_{s} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right) \\
k_{s} \alpha_{s} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right)
\end{array}\right\}+\left[\begin{array}{cc}
k_{s}-k_{s} \\
-k_{s} & k_{s}
\end{array}\right]\left\{\begin{array}{l}
\Delta v_{s z} \\
\Delta v_{1,3}^{U U}
\end{array}\right\}  \tag{2.2.95}\\
\left\{\begin{array}{r}
-\Delta F_{2 z} \\
\Delta F_{2 z}
\end{array}\right\}=\left\{\begin{array}{c}
-k_{c} \alpha_{c} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right) \\
k_{c} \alpha_{c} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right)
\end{array}\right\}+\left[\begin{array}{cc}
k_{c} & -k_{c} \\
-k_{c} & k_{c}
\end{array}\right]\left\{\begin{array}{l}
\Delta v_{s z} \\
\Delta v_{2,3}^{U}
\end{array}\right\}
\end{array}\right\} .
$$

Rearranging eq. (2.2.95), we obtain

$$
\left\{\begin{array}{l}
\Delta F_{r a z} \\
\Delta F_{1:} \\
\Delta F_{2 z}
\end{array}\right\}=\left\{\begin{array}{c}
-\Delta F_{1 z}-\Delta F_{2 z} \\
\Delta F_{1 z} \\
\Delta F_{2 z}
\end{array}\right\}=\left\{\begin{array}{c}
-\left(k_{s} \alpha_{s}+k_{c} \alpha_{c}\right) l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right) \\
k_{s} \alpha_{s} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right) \\
k_{c} \alpha_{c} l_{s z}^{\prime \prime}\left(T_{n+1}-T_{n}\right)
\end{array}\right\}+\left[\begin{array}{ccc}
k_{s} & +k_{c} & -k_{s} \\
& -k_{c} \\
-k_{s} & k_{s} & 0 \\
-k_{c} & k_{c} & k_{c}
\end{array}\right]\left\{\begin{array}{c}
\Delta v_{s z} \\
\Delta v_{1,3}^{v} \\
\Delta v_{2,3}^{\prime \prime}
\end{array}\right\}
$$

Equation (2.2.96) is substituted into eq. (2.2.90). Here, it is not necessary to consider $\Delta F_{1 z}$ and $\Delta F_{2, z}$, since these can be given as reaction forces from the lower segment when the total matrix is solved. Therefore, eq. (2.2.90) is the total matrix to be solved and can be expressed as

## (2) Lower plenum



Fig. 2.36 Boundary conditions for lower plenum.

When no lower plenum exists, boundary conditions are satisfied if the degree of freedom and rows and columns in the matrix which correspond to the lower plenum are omitted, because $\Delta v_{1,1}^{L}=\Delta v_{2.1}^{L}=0$ holds in eq. (2.2.89).

When a lower plenum exists, since $\Delta v_{1.1}^{L} \neq 0$, and $\Delta v_{2.1}^{L} \neq 0$,

$$
\left.\begin{array}{l}
\Delta F_{1 z}=-k_{s} v_{l, 1}^{L}+k_{s} \alpha_{s} l_{s z}^{L}\left(T_{n+1}-T_{n}\right)  \tag{2.2.98}\\
\Delta F_{2 z}=-k_{c} v_{2,1}^{L}+k_{c} \alpha_{c} l_{v z}^{L}\left(T_{n+1}-T_{n}\right)
\end{array}\right\} .
$$

Here,
$l_{s z}^{L}$ : lower plenum length.

When eq. (2.2.98) is expressed in incremental form, we obtain

$$
\left.\begin{array}{l}
\Delta F_{1 z}=-k_{s} \Delta v_{1,1}^{L}+k_{s} \alpha_{s} l_{s z}^{L}\left(T_{n+1}-T_{n}\right)  \tag{2.2.99}\\
\Delta F_{2 z}=-k_{c} \Delta v_{2,1}^{L}+k_{c} \alpha_{c} l_{s z}^{L}\left(T_{n+1}-T_{n}\right)
\end{array}\right\} .
$$

Substituting eq. (2.2.99) into eq. (2.2.97), we obtain

Here, $-\Delta F_{1 z}$ and $-\Delta F_{2, z}$ are given as reaction forces of segment 1 .
Equation (2.2.100) is the total matrix (symmetrical matrix) to be solved.

### 2.2.11 Judgment conditions of contact between pellet and cladding

As judgment conditions of contact between pellet and cladding, three states, namely open gap, clogged gap and sliding states, are considered. The transition among the three states is shown in Fig. 2.37 and Table 2.1


Fig. 2.37 Change in contact states. (Refer to Table 2.1 for numbers 1-6.)

Table 2.1 Changes and conditions of contact states.

| Number | State change | Condition of state change and treatment |
| :---: | :---: | :---: |
| (1) | $\begin{aligned} & \text { Open gap } \rightarrow \\ & \quad \text { Clogged gap } \end{aligned}$ | When gap width changes from positive to negative, time-step control is performed and a state is judged to be a clogged gap state when the condition $\left\|F_{3}\right\|<\mu\left\|F_{2}\right\|$ is satisfied. |
| (2) | $\begin{array}{r} \text { Clogged gap } \rightarrow \\ \text { Open gap } \end{array}$ | When contact force $F_{2}$ changes from negative to positive, a state is judged to be an open gap state. Time-step control is performed. |
| (3) | $\underset{\text { Clogged gap } \rightarrow}{\text { Sliding }}$ | When a contact state changes under the condition $\left\|F_{3}\right\| \geq \mu\left\|F_{2}\right\|$, it is judged to be a sliding state. Time-step control is not performed. |
| (4) | Sliding $\rightarrow$ Clogged gap | When a contact state changes under the condition $\left\|F_{3}\right\|<\mu\left\|F_{2}\right\|$, it is judged to be a clogged gap state. Time-step control is not performed. |
| (5) | Sliding $\rightarrow$ Open gap | Same as in case (2). |
| (6) | $\begin{array}{r} \text { Open gap } \overrightarrow{\text { Sliding }} \end{array}$ | When gap width changes from positive to negative, time-step control is performed, and when the condition $\left\|F_{3}\right\| \geq \mu\left\|F_{2}\right\|$ is satisfied, a state is judged to be a sliding state. |
| re, | $F_{2}$ : contact force between pellet and cladding in the radial direction <br> $F_{3}$ : contact force between pellet and cladding in the axial direction <br> $\mu$ : coefficient of friction between pellet and cladding. |  |

## (1) Judgment of clogged gap state/sliding state <br> (1) Clogged gap state condition

A state is judged to be a clogged gap state when the following conditions are satisfied: the displacement increment of the pellet is identical to that of the cladding and the axial force is smaller than the maximum static friction force determined from the contact force; namely,

$$
\left.\begin{array}{l}
\Delta v_{p}=\Delta v_{c}  \tag{2.2.101}\\
\left|F_{3}\right|<\mu\left|F_{2}\right|
\end{array}\right\}
$$

holds, where $\Delta v_{p}$ is the axial displacement increment of pellet, $\Delta v_{c}$ is the axial displacement increment of cladding, and $\mu$ is the friction coefficient corrected in terms of cross-sectional area, as described in section 2.2.8.

When a clogged gap state is assumed, $\Delta v_{p}=\Delta v_{c}$ is given as a boundary condition for judgment. Therefore, when $\left|F_{3}\right|<\mu\left|F_{2}\right|$ is not satisfied, the contact state is changed from the clogged gap state to the sliding state.
(2) Sliding state condition

In a sliding state, since the boundary condition
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$$
\begin{equation*}
\left|F_{3}\right|=\mu\left|F_{2}\right| \tag{2.2.102}
\end{equation*}
$$

is given, the equation below cannot be used as a contact-state judgment condition from a sliding state to a clogged gap state.

$$
F_{3}<\mu F_{2}
$$

Therefore, when a calculation shows a contradictory result in the direction of axial force and displacement increment even if an axial force exists, namely,
when $F_{3} \times F_{2}>0$ (since $\left.F_{2}<0, F_{3}<0\right), \Delta v_{p}<\Delta v_{c}$,
or
when $F_{3} \times F_{2}<0\left(\right.$ since $\left.F_{2}<0, F_{3}>0\right), \Delta v_{p}>\Delta v_{c}$, the contact state is changed from a sliding state to a clogged gap state.

Also, when

$$
F_{2} \times F_{3}=0
$$

the contact state is a clogged gap state. This is because $F_{2}<0$, and thus $F_{3}=0$.

## (2) Force acting on a boundary surface

As shown in Fig. 2.38, the force which acts on a boundary surface $S_{i, i+1}$ is given by

$$
\begin{align*}
S_{i, r+1}= & F_{3, v 1}+\left(F_{3,5}-F_{3, l \prime}\right)+\left(F_{3,4}-F_{3,5}\right) \\
& +\cdots+\left(F_{3, i}-F_{3,+1}\right)  \tag{2.2.103}\\
& =F_{3,,}
\end{align*}
$$

This force is not affected by forces from another segment, $F_{3, j}(j \neq i)$. Therefore, judgment of clogged gap/sliding states in all axial segments can be performed simultaneously according to the judgment conditions described above.

This fact indicates that the axial force which acts on a segment always balances the contact force between pellet and cladding in the axial direction (=friction force), and that the magnitude of this axial force determines whether a sliding or clogged gap state exists under the contact condition.


Fig. 2.38 Axial force acting on pellet.

```
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```

Therefore, unless strong PCMI (pellet-clad mechanical interaction) is generated, axial force does not become large, because axial force is significantly mitigated by sliding when PCMI is weak.

## (3) Time-step control

After the iteration calculation for assumption and judgment of clogged gap/sliding states described above is converged for all segments, if a contact state is changed (noncontact $\underset{\leftarrow}{\rightarrow}$ contact), time-step control is performed and a state is changed at the time described below.

- Non-contact $\rightarrow$ contact: the time point when gap width becomes zero.
- Contact $\rightarrow$ non-contact: the time point when contact pressure becomes zero.

In these cases, all time-dependent variables are corrected to the values at the time of state change, by means of linear interpolation in terms of time. Then, the time-step width $\Delta t_{1}$ (defined in Table 2.1) is changed, i.e., further divided, and the mechanical analysis calculations are performed under the new contact condition.

Namely, in the thermal analysis part, time step $\Delta t_{1}$ is divided using the method described in section 2.1.6, and in the mechanical analysis part, time step $\Delta t_{1}$ is divided by this time-step control. The time-step control is also applied in the local mechanical analysis.

Model parameter LCMAX
The maximum number of judgments on the state change within one time step is designated by LCMAX. The default value of LCMAX is 3 .

### 2.3 Local Mechanical Behavior [Detailed Mechanical Analysis II]

In local mechanical analysis, axis-symmetric FEM is applied to half a pellet length. We call this part an objective segment. Figures 2.39(a) and (b) show a mesh division of the present FEM model. As an element, a rectangular 8-node iso-parametric element is used, and displacement in the element is approximated by a quadratic function of displacement of nodes.

Figure 2.39(a) illustrates half a pellet length of the objective segment which is divided into coaxial ring elements to be analyzed in axi-symmetrical coordinate.



Fig.2.39(a) Local analysis model

Figure 2.39(b) shows in an
accurate manner the elements and nodes of the objective segment. A pellet is divided to 5 radial rings, while cladding is dealt with as one element. Half a pellet length is divided to the axial parts with lengths of 1:3:6 ratio. Each element has 8 nodes. Nodes of pellet and cladding across the gap form a nodecouple, which is explained later in section 2.3.3(2).


Fig.2.39 (b) Elements and node for half a pellet length

In this section, the strain component within an element is defined as

$$
\{\varepsilon\}=\left\{\begin{array}{l}
\varepsilon_{r}  \tag{2.3.1}\\
\varepsilon_{z} \\
\varepsilon_{\theta} \\
\gamma_{r z}
\end{array}\right\}=\left\{\begin{array}{c}
\frac{d u}{d r} \\
\frac{d v}{d z} \\
\frac{u}{r} \\
\left(\frac{\partial v}{\partial r}\right)+\left(\frac{\partial u}{\partial z}\right)
\end{array}\right\},
$$

where $\varepsilon_{r}, \varepsilon_{z}, \varepsilon_{\theta}$ and $\gamma_{r z}$ are strains in the radial, axial, circumferential and shearing ( $r$, $z$ ) directions, respectively. The shearing component was not considered in the previous section; however, since one of the objectives here is stress evaluation at a ridge part of a pellet under bending deformation, the shearing component is taken into account in this section.

### 2.3.1 Basic equations

The equilibrium condition at time $t_{n+1}$ is represented, based on the principle of virtual work, as

$$
\begin{equation*}
\int[B]^{T}\left\{\sigma_{n+1}\right\} d V-\left\{F_{n+1}\right\}=0 \tag{2.3.1}
\end{equation*}
$$

Here,

$$
\begin{array}{ll}
{[B]^{T}:} & \text { transposed matrix of a strain-displacement matrix }[B] \\
\left\{\sigma_{n+1}\right\}: & \text { stress vector at time } t_{n+1} \\
\left\{F_{n+1}\right\}: & \text { node point loading vector at time } t_{n+1} .
\end{array}
$$

The strain-displacement matrix $[B]$ is assumed to be determined from a dimension prior to deformation. $\quad[B]$ matrix is given by eq. (2.3.19), presented later.

The constitutive equation (stress-strain relationship equation) is given by

$$
\begin{equation*}
\left\{\sigma_{n+1}\right\}=[\bar{D}]\left\{\Delta \varepsilon_{n+1}^{e}\right\}, \tag{2.3.2}
\end{equation*}
$$

where
$\left\{\Delta \sigma_{n+1}\right\}:$ stress increment vector from time $t_{n}$ to $t_{n+1}$
$\left\{\Delta \varepsilon_{n+1}^{e}\right\}$ : elastic increment vector from time $t_{n}$ to $t_{n+1}$

$$
\left[D_{n+\theta}\right]=(1-\theta)\left[D_{n}\right]+\theta\left[D_{n+1}\right] \quad\left(\theta=\frac{1}{2}\right)
$$

$\left[D_{n}\right]:$ stress-strain matrix (stiffness) at time $t_{n}$.
If matrix [ $C$ ] is defined as an inverse matrix of this $D$ matrix, eq. (2.3.2) is transformed as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}\right\}=\left[C_{n+\theta}\right]\left\{\Delta \sigma_{n+1}\right\} . \tag{2.3.3}
\end{equation*}
$$

Matrix [C] in eq. (2.3.3) is given as

$$
[C]=\frac{1}{E}\left[\begin{array}{cccc}
1 & -v & -v & 0  \tag{2.3.4}\\
-v & 1 & -v & 0 \\
-v & -v & 1 & 0 \\
0 & 0 & 0 & 2(1+v)
\end{array}\right]
$$

where $E$ is Young's modulus and $v$ is Poisson's ratio.
The elastic strain increment vector can be expressed as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}^{e}\right\}=\left\{\Delta \varepsilon_{n+1}\right\}-\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left\{\Delta \varepsilon_{n+1}^{p}\right\}-\left\{\Delta \varepsilon_{n+1}^{c}\right\}, \tag{2.3.5}
\end{equation*}
$$

where

$$
\begin{array}{ll}
\left\{\Delta \varepsilon_{n+1}\right\} & : \text { total strain increment vector } \\
\left\{\Delta \varepsilon_{n+1}^{0}\right\} & : \text { initial strain increment vector } \\
\left\{\Delta \varepsilon_{n+1}^{p}\right\} & : \text { plastic strain increment vector } \\
\left\{\Delta \varepsilon_{n+1}^{c}\right\} & : \text { creep strain increment vector. }
\end{array}
$$

Strains by thermal expansion, densification, swelling and relocation are treated as initial strains. The strain-displacement relationship is expressed as

$$
\begin{equation*}
\left\{\Delta \varepsilon_{n+1}\right\}=[B]\left(\left\{u_{n+1}\right\}-\left\{u_{n}\right\}\right) \tag{2.3.6}
\end{equation*}
$$

where

$$
\left\{u_{n}\right\}: \text { node point displacement vector at time } t_{n+1}
$$

The following equation is obtained from eqs. (2.3.2) $\sim(2.3 .6$.).

$$
\begin{equation*}
\left[\bar{C}_{n+\theta}\right]\left[\left\{\sigma_{n+1}\right\}-\left\{\sigma_{n}\right\}\right)-[B]\left(\left\{u_{n+1}\right\}-\left\{u_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0}\right\}+\left\{\Delta \varepsilon_{n+1}^{r}\right\}+\left\{\Delta \varepsilon_{n+1}^{c}\right\}=0 \tag{2.3.7}
\end{equation*}
$$

Here,

$$
\left[\bar{C}_{n+\theta}\right]=\left(\left[C_{n+1}\right]+\left[C_{n}\right]\right) / 2:
$$

$$
\begin{aligned}
& \text { JAERI-Data/Code 97-043 } \\
& {\left[C_{n}\right]:\left[D_{n}\right]^{-1} .}
\end{aligned}
$$

Equations (2.3.1) and (2.3.7) are the basic equations for obtaining unknown values $\left\{\sigma_{n+1}\right\}$ and $\left\{u_{n+1}\right\}$.

Equation (2.3.7) can be solved by iteration using the Newton-Raphson method, since $\left\{\Delta \varepsilon_{n+1}^{p}\right\}$ and $\left\{\Delta \varepsilon_{n+1}^{c}\right\}$ are functions of unknown value $\left\{\sigma_{n+1}\right\}$ (refer to sections 2.2.4 and 2.2.5 for details). Pellet cracks, creep and plasticity are treated similarly to the case of entire length mechanical analysis.

At the ( $n+1$ )th stage (time-step) calculation, when the $i$ th iteration is completed and the $(i+1)$ th iteration is being performed, eq. (2.3.7) is expressed as

$$
\begin{equation*}
\left[\bar{C}_{n+\theta}\right]\left[\left\{\sigma_{n+1}^{i}\right\}+\left\{d \sigma_{n+1}^{i+1}\right\}-\left\{\sigma_{n}\right\}\right)-[B]\left(\left\{u_{n+1}^{i}\right\}+\left\{d u_{n+1}^{i+1}\right\}-\left\{u_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0}\right\}+\left\{\Delta \varepsilon_{n+1}^{f}\right\}+\left\{\Delta \varepsilon_{n+1}^{c}\right\}=0 \tag{2.3.8}
\end{equation*}
$$

Here,

$$
\begin{align*}
& \left\{d \sigma_{n+1}^{\prime+1}\right\}=\left\{\sigma_{n+1}^{\prime+1}\right\}-\left\{\sigma_{n+1}^{\prime}\right\}  \tag{2.3.9}\\
& \left\{d u_{n+1}^{\prime+1}\right\}=\left\{u_{n+1}^{\prime+1}\right\}-\left\{u_{n+1}^{\prime}\right\} .
\end{align*}
$$

The equilibrium condition of eq. (2.3.1) is given by substituting eq.(2.3.9) into eq.(2.3.1) as

$$
\begin{equation*}
\int[B]^{T}\left\{\sigma_{n+1}^{i}\right\} d V+\int[B]^{T}\left\{d \sigma_{n+1}^{\prime+1}\right\} d V=\left\{F_{n+1}\right\} \tag{2.3.11}
\end{equation*}
$$

### 2.3.2 Stiffness equation

The formulation method of the stiffness equation is the same for the local mechanical analysis and the mechanical analysis over the entire-length of the fuel rod. Therefore, by substituting eq. (2.2.60) which was obtained in the entire-length mechanical analysis part into the equilibrium condition equation (2.3.7), we obtain the equilibrium condition at the $(i+1)$ th iteration.

Note: Equation (2.2.65) is to be substituted into eq. (2.3.11). In formulation of eqs. (2.2.66) to (2.2.69) which should be incorporated in eq. (2.2.65), strain components are taken into account. Therefore, the yielding function $h$ ( $=$ equivalent stress $\bar{\sigma}$ ) shown by eq. (2.2.54) is modified as follows to be expressed in its original form.

$$
\begin{aligned}
h=\bar{\sigma}=\left[\frac { 3 } { 2 ( F + G + H ) } \left\{H\left(\sigma_{r}-\sigma_{z}\right)^{2}+F\left(\sigma_{z}-\sigma_{\theta}\right)^{2}\right.\right. & \left.+G\left(\sigma_{\theta}-\sigma_{r}\right)^{2}+2 N \tau_{r}^{2}\right\} \\
& \left.+3 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right)^{2}\right]^{\frac{1}{2}}
\end{aligned}
$$

That is,

$$
\begin{align*}
\int[B]^{T} & \left\{\sigma_{n+1}^{i}\right\} d V+\int[B]^{T}\left[\hat{D}_{n+\theta}^{P, i}\right][B]\left\{d u_{n+1}^{i+1}\right\} d V \\
& -\int[B]^{T}\left[\hat{D}_{n+\theta}^{P, i}\right]\left[\bar{C}_{i+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right) d V \\
& -\int[B]^{T}\left[\hat{D}_{n+\theta}^{P, i}\right]\left(\left\{\Delta \varepsilon_{n+1}^{0 i}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right) d V  \tag{2.3.12}\\
& +\int[B]^{T}\left(\left\{S_{n+1}^{i}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) d V=\left\{F_{n+1}\right\}
\end{align*}
$$

is obtained, where

$$
[\widetilde{C}]=\left[\begin{array}{rrrc}
\frac{1}{E_{r}} & -\frac{v}{E} & -\frac{1}{E} & 0  \tag{2.3.13}\\
-\frac{v}{E} & \frac{1}{E_{z}} & -\frac{v}{E} & 0 \\
-\frac{v}{E} & -\frac{v}{E} & \frac{1}{E_{\theta}} & 0 \\
0 & 0 & 0 & \frac{4(1+v)}{E_{r}+E_{z}}
\end{array}\right]
$$

Equation (2.3.13) is rearranged as follows.

$$
\begin{equation*}
\left[K_{n+\theta}^{i}\right]\left\{\Delta u_{n+1}^{i+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{\prime}\right\} \tag{2.3.14}
\end{equation*}
$$

This is the stiffness equation for elements.
Here,

$$
\begin{gather*}
{\left[K_{n+\theta}^{i}\right]=\int[B]^{T}\left[\hat{D}_{n+\theta}^{p, i}\right][B] d V}  \tag{2.3.15}\\
\left\{\Delta \hat{F}_{n+1}^{\prime}\right\}=\left\{F_{n+1}\right\}-\int[B]^{T}\left\{\sigma_{n+1}^{i}\right\} d V \\
\left.\left.-\int[B]^{T}\left[\hat{D}_{n+\theta}^{P, i}\right]\right\}\left[\bar{C}_{1+\theta}^{i}\right]\left(\left\{\sigma_{n+1}^{i}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0 i}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right\} d V  \tag{2.3.16}\\
\\
-\int[B]^{T}\left(\left\{S_{n+1}^{i}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) d V
\end{gather*}
$$

hold and represent stiffness matrix and loading vector, respectively.
Assuming axis-symmetry in deformation and performing the integration of $\theta$ coordinates in the circumferential direction in eqs. (2.3.15) and (2.3.16), we obtain

$$
\begin{equation*}
\left[K_{n+\theta}^{i}\right]=2 \pi \iint[B]^{T}\left[\hat{D}_{n+\theta}^{P, i}\right][B] r d r d z \tag{2.3.17}
\end{equation*}
$$

$$
\begin{align*}
& \left\{\Delta \hat{F}_{n+1}^{\prime}\right\}=\left\{F_{n+1}\right\}-2 \pi \iint[B]^{T}\left\{\sigma_{n+1}^{\prime}\right\} r d r d z \\
& \quad-2 \pi \iint[B]^{T}\left[\hat{D}_{n+\theta}^{p, i}\right]\left\{\left[\bar{C}_{i+\theta}^{\prime}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0,}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, i}\right\}\right\} r d r d z  \tag{2.3.18}\\
& \quad-2 \pi \iint[B]^{T}\left(\left\{S_{n+1}^{\prime}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) r d r d z
\end{align*}
$$

On the right-hand side of eq. (2.3.18), the first term is the non-equilibrium residue, the second term is an apparent load due to stress and initial strain, and the third term is a compensation term for yield stress change.

The stiffness equation for one element is shown below.
Displacement of an arbitrary point of an element in the axial and circumferential directions $\{u, v\}$ and displacement at 8 nodes $\left\{u^{1}, v^{1}, u^{2}, v^{2} \ldots, u^{8}, v^{8}\right\}$ are related as follows.

$$
\left\{\begin{array}{c}
u  \tag{2.3.19}\\
v
\end{array}\right\}=[N]\left\{\begin{array}{c}
u^{1} \\
v^{1} \\
u^{2} \\
v^{2} \\
\vdots \\
u^{8} \\
v^{8}
\end{array}\right\}
$$

Here, $[N]$ is called a form function, which is a matrix with the following shape.

$$
\begin{equation*}
[N]=\left[N_{1} I, N_{2} I, N_{3} I, \cdots, N_{8} I\right] \tag{2.3.20}
\end{equation*}
$$

Using a local coordinate system shown in Fig. 2.40 (given later), $N_{i}$ is expressed as

$$
\left.\begin{array}{l}
N_{1}=(1-\xi)(1-\eta)(-\xi-\eta-1) / 4  \tag{2.3.21}\\
N_{2}=(1+\xi)(1-\eta)(+\xi-\eta-1) / 4 \\
N_{3}=(1+\xi)(1-\eta)(+\xi-\eta-1) / 4 \\
N_{4}=(1-\xi)(1+\eta)(-\xi+\eta-1) / 4 \\
N_{5}=(1+\xi)(1-\xi)(1-\eta) / 2 \\
N_{6}=(1+\xi)(1+\eta)(1-\eta) / 2 \\
N_{7}=(1-\xi)(1+\eta)(1-\eta) / 2 \\
N_{8}=(1-\xi)(1+\eta)(1-\eta) / 2
\end{array}\right\} .
$$

Strain in the element of the axis-symmetrical problem is given by the following equation, which includes shearing components, different from the equation in the Detailed Mechanical Analysis I.

$$
\begin{gather*}
\text { JAERI-Data/Code } 97-043 \\
\{\varepsilon\}=\left\{\begin{array}{l}
\varepsilon_{r} \\
\varepsilon_{z} \\
\varepsilon_{\theta} \\
\varepsilon_{r=}
\end{array}\right\}=\left\{\begin{array}{c}
\partial V / \partial r \\
\partial W / \partial z \\
v / r \\
\partial V / \partial z+\partial W / \partial r
\end{array}\right\}=[B]\{u\} \tag{2.3.22}
\end{gather*}
$$

Therefore, matrix $[B]$ is given by

$$
\begin{equation*}
[B]=\left[\mathbf{B}_{1}, \mathbf{B}_{2}, \mathbf{B}_{3}, \cdots, \mathbf{B}_{8}\right] . \tag{2.3.23}
\end{equation*}
$$

Here, submatrix $\mathbf{B}_{i}$ is given by

$$
\mathbf{B}_{1}=\left(\begin{array}{cc}
\frac{\partial N_{i}}{\partial r} & 0  \tag{2.3.24}\\
0 & \frac{\partial N_{i}}{\partial z} \\
\frac{N_{i}}{r} & 0 \\
\frac{\partial N_{i}}{\partial z} & \frac{\partial N_{i}}{\partial r}
\end{array}\right)
$$

In eq. (2.3.21), $N_{i}$ is defined using a local coordinate system. For representation of matrix $[B]$ in eq. (2.3.22) in concrete form, the following coordinate transformation is performed.

The relationship between a local coordinate system and a cylindrical coordinate system $r, z$ is given by

$$
\left\{\begin{array}{l}
\frac{\partial N_{1}}{\partial \xi}  \tag{2.3.25}\\
\frac{\partial N_{i}}{\partial \eta}
\end{array}\right\}=\left\{\begin{array}{ll}
\frac{\partial r}{\partial \xi} & \frac{\partial z}{\partial \xi} \\
\frac{\partial r}{\partial \eta} & \frac{\partial z}{\partial \eta}
\end{array}\right)\left\{\begin{array}{c}
\frac{\partial N_{i}}{\partial r} \\
\frac{\partial N_{i}}{\partial z}
\end{array}\right\}=[\mathrm{J}]\left\{\begin{array}{c}
\frac{\partial N_{i}}{\partial r} \\
\frac{\partial N_{i}}{\partial z}
\end{array}\right\}
$$

or

$$
\left\{\begin{array}{c}
\frac{\partial N_{i}}{\partial r}  \tag{2.3.26}\\
\frac{\partial N_{i}}{\partial z}
\end{array}\right\}=[\mathbf{J}]^{-1}\left\{\begin{array}{c}
\frac{\partial N_{i}}{\partial \xi} \\
\frac{\partial N_{i}}{\partial \eta}
\end{array}\right\}
$$

Here, [J] is a Jacobian matrix. The location in an element $(r, z)$ is represented using a nodal coordinate system $\left(r_{i}, z_{i}, i=1 \sim 8\right)$ as

$$
\left.\begin{array}{l}
r=\sum_{i=1}^{8} N_{i} r_{i} \\
z=\sum_{i=1}^{8} N_{i} z_{i}
\end{array}\right\}
$$

Using this relationship, the Jacobian matrix [J] is expressed as

$$
[\mathrm{J}]=\left(\begin{array}{ll}
\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \xi} r_{i} & \sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \xi} z_{i}  \tag{2.3.27}\\
\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \eta} r_{1} & \sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \eta} z_{i}
\end{array}\right) .
$$

Therefore, $[\mathbf{J}]^{-1}$ is given by

$$
[\mathbf{J}]^{-1}=\frac{1}{\operatorname{det}[\mathbf{J}]}\left(\begin{array}{cc}
\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \eta} z_{i} & -\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \xi} z_{i}  \tag{2.3.28}\\
-\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \eta} r_{i} & \sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \xi} r_{i}
\end{array}\right) .
$$

Here,

$$
\begin{equation*}
\operatorname{det}[\mathbf{J}]=\left(\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \xi} r_{i}\right)\left(\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \eta} z_{i}\right)-\left(\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \eta} r_{i}\right)\left(\sum_{i=1}^{8} \frac{\partial N_{i}}{\partial \xi} z_{i}\right) . \tag{2.3.29}
\end{equation*}
$$

Components in eq. (2.3.24) are transformed into a local coordinate system using the above relationships, and we obtain

$$
\left.\begin{array}{l}
\frac{\partial N_{i}}{\partial r}=\frac{1}{\operatorname{det}[\mathbf{J}]}\left(\left(\sum_{j=1}^{8} \frac{\partial N_{j}}{\partial \eta} z_{j}\right) \frac{\partial N_{i}}{\partial \xi}-\left(\sum_{j=1}^{\mathrm{B}} \frac{\partial N_{j}}{\partial \xi} z_{j}\right) \frac{\partial N_{i}}{\partial \eta}\right) \\
\frac{\partial N_{i}}{\partial z}=\frac{1}{\operatorname{det}[\mathbf{J}]}\left(\left(\sum_{j=1}^{8} \frac{\partial N_{j}}{\partial \xi} r_{j}\right) \frac{\partial N_{i}}{\partial \eta}-\left(\sum_{j=1}^{8} \frac{\partial N_{j}}{\partial \eta} r_{j}\right) \frac{\partial N_{i}}{\partial \xi}\right)  \tag{2.3.30}\\
\frac{N_{i}}{r}=\frac{N_{i}}{\sum_{j=1}^{8} N_{i} r_{i}}
\end{array}\right\} .
$$

$d r d z$ is transformed by the equation

$$
\begin{equation*}
d r d z=\operatorname{det}[\mathbf{J}] d \xi d \eta \tag{2.3.31}
\end{equation*}
$$

Using the above transformation equation, we express eqs. (2.3.17) and (2.3.18) using a local coordinate system as follows.

$$
\begin{gather*}
{\left[K_{n+\theta}^{\prime}\right]=2 \pi \int_{1} \int_{1}[B]^{T}\left[\hat{D}_{n+\theta}^{P, t}\right][B]\left(\sum_{j=1}^{8} N_{1} r_{j}\right) \operatorname{det}[\mathbf{J}] d \xi d \eta}  \tag{2.3.32}\\
\left\{\Delta \hat{F}_{n+1}^{i}\right\}=\left\{F_{n+1}\right\}-2 \pi \int_{1} \int_{1}[B]^{T}\left\{\sigma_{n+1}^{\prime}\right\} d \xi d \eta \\
\left.\left.-2 \pi \int_{-1}^{1} \int_{-1}^{1}[B]^{T}\left[\hat{D}_{n+\theta}^{P, j}\right]\right\}\left[\bar{C}_{i+\theta}^{\prime}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0,}\right\}-\left\{\Delta \varepsilon_{n+1}^{c, 1}\right\}\right\} d \xi d \eta  \tag{2.3.33}\\
-2 \pi \int_{1} \int_{1}^{1}[B]^{T}\left(\left\{S_{n+1}^{\prime}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) d \xi d \eta
\end{gather*}
$$

In FEMAXI-IV, this integration is approximated by a Gaussian integration as

$$
\begin{equation*}
\int_{-1}^{1} \int_{1}^{1} f(\xi, \eta) d \xi d \eta=\sum_{i=1}^{n} \sum_{j=1}^{m} H_{1} H_{j} f\left(\xi_{1}, \eta_{j}\right) . \tag{2.3.34}
\end{equation*}
$$

In the case of rectangular 8-node elements, the number of integration points is known to be sufficient with $n=m=2$. In this case, since $H_{i}=H_{j}=1$, the following equation is used.

$$
\begin{equation*}
\mathcal{L}_{1} \int_{1} f(\xi, \eta) d \xi d \eta=\sum_{i=1}^{2} \sum_{j=1}^{2} f\left(\xi_{1}, \eta_{j}\right) \tag{2.3.35}
\end{equation*}
$$

Here,
$n$ : number of integration points in the $\xi$ direction
$m$ : number of integration points in the $\eta$ direction
$\xi_{I}$ : coordinates of integration point in the $\xi$ direction
$\eta_{j}$ : coordinates of integration point in the $\eta$ direction $H_{i}, H_{j}$ : weighted coefficients.


Fig. 2.40 Integration points for rectangular 8-node element.

The number of integration points is 4 , the coordinates of each point are $(a, a),(a,-a),(-a, a)$ and ( $-\mathrm{a},-\mathrm{a}$ ) as shown in Fig. 2.40, and $\mathrm{a}=0.5773502691^{*}$. (*Note: the Gauss's integral
formula for 2-point approximation $=\int_{-1}^{1} f(x) d x \cong(f(a)+f(-a))$
By calculation of the stress vector, strain vector and compensation term for each of the 4 integration points, the integral terms in eqs. (2.3.32) and (2.3.33) can be obtained.

### 2.3.3 Boundary conditions

(1) Geometric modeling and boundary conditions

The finite element model (geometric model) for mechanical analysis is applied to half the pellet length, as shown in Fig. 2.41. This model has a total of 8 boundaries: 4 on the pellet side $((1)-(4))$ and 4 on the cladding side $((5)-(8))$. Boundary conditions are determined from symmetry of deformation, coolant pressure, gas pressure and contact state.


Fig. 2.41 Boundaries of the geometric model
The loading vector in eq. (2.3.1) is expressed as the total load which acts on nodes located on the 8 boundaries, as follows.

$$
\begin{equation*}
\left\{F_{n+1}\right\}=\left\{F_{n+1}^{(1)}\right\}+\left\{F_{n+1}^{(2)}\right\}+\left\{F_{n+1}^{(3)}\right\}+\left\{F_{n+1}^{(4)}\right\}+\left\{F_{n+1}^{(5)}\right\}+\left\{F_{n+1}^{(6)}\right\}+\left\{F_{n+1}^{(7)}\right\}+\left\{F_{n+1}^{(8)}\right\} \tag{2.3.36}
\end{equation*}
$$

Here, $\left\{F_{n+1}^{(i)}\right\}$ is the vector of loading which acts on the node at boundary $(i)$.
Plane symmetry is assumed on boundaries (1) and (5), and nodes on these boundaries do not deform in the axial direction; that is,

$$
\begin{align*}
& \left\{\Delta v^{(1)}\right\}=0  \tag{2.3.37}\\
& \left\{\Delta v^{(5)}\right\}=0 \tag{2.3.38}
\end{align*}
$$

is assumed. Here, $\left\{\Delta v^{(1)}\right\}$ and $\left\{\Delta v^{(5)}\right\}$ are the deformation increment vectors of nodes on
boundaries (1) and (5), in the axial direction, respectively. The constraint force generated at boundary (1) due to the constraint condition of eq. (2.3.37) is $\left\{F_{n+1}^{(1)}\right\}$, and the constraint force generated at boundary (5) due to the condition of eq. (2.3.38) is $\left\{F_{n+1}^{(5)}\right\}$.

At boundary (2), in the case of a solid pellet, nodes located on the boundary are not displaced in the radial direction since axis-symmetry is assumed for deformation. That is,

$$
\begin{equation*}
\left\{\Delta u^{(2)}\right\}=0 \tag{2.3.39}
\end{equation*}
$$

is assumed. Here, $\left\{\Delta u^{(2)}\right\}$ is the radial displacement increment vector for the node located on boundary (2).

The constraint force generated at boundary (2) (rotationally symmetric axis) by the condition of eq. (2.3.39) is $\left\{F_{n+1}^{(2)}\right\}$. Here, in the case of a hollow pellet, $\left\{F_{n+1}^{(2)}\right\}=0$ holds since radial displacement is not restricted.

The surface force given by coolant pressure acts on boundary (7). $\left\{F_{n+1}^{(7)}\right\}$ represents the vector of equivalent node point loading due to this action.

At boundary (3), contact force exists due to the interaction (PCI) of boundaries (3) and (6). Gas pressure inside the fuel rod also acts on boundary (3); however, this is not taken into consideration since it is canceled by gas pressure present in a crack gap inside the pellet.
$\left\{F_{n+1}^{(3)}\right\}$ is a vector of contact force generated by the interaction of boundary (3) with the pellet (boundary (6)).

At boundary (6), actions of contact force produced by PCI and gas pressure are considered. $\left\{F_{n+1}^{(6)}\right\}$ represents the sum of the contact force vector and the vector of equivalent node point loading by gas pressure.

At boundary (8), the number of degrees of freedom in the axial direction of a node group on the boundary is set as I based on the assumption of symmetry of deformation.

$$
\begin{equation*}
\left\{\Delta \nu^{(8)}\right\}=\Delta \bar{v}^{(8)} \tag{2.3.40}
\end{equation*}
$$

Here, $\Delta \bar{v}^{(8)}$ is the axial displacement increment of nodes on boundary (8). At boundary (8), in addition to the restraint force generated from the condition of eq. (2.3.71), such loads as axial tensile load produced by the PCl in an upper region of a fuel rod, and axial loads given by gas pressure and coolant pressure are considered. The axial tensile load due to PCI in the upper region of the fuel rod which acts on boundary (8) is determined in an empirical manner.

This will be explained later.
At boundary (4), the above-described loads in the axial direction which is determined empirically acts as a compressive force. The contact force distribution which can be obtained by solving the pellet/pellet contact problem on the assumption of plane symmetry under this axial load is the load acting on the boundary.

As described above, the kinds of load which act on the 8 boundaries are of the following 6 types: reaction due to constraint of displacement, equivalent nodal force due to coolant pressure, equivalent nodal force due to gas pressure, pellet/cladding contact force, axial tensile load, and pellet/pellet contact force balanced with the axial tensile load.

For clarity of expression, these forces are represented by subscripts R, W, G, PC, AX, and PP, respectively, and eq. (2.3.36) is expressed as

$$
\begin{align*}
\left\{F_{n+1}\right\}= & \left\{F_{n+1}^{(1), R}\right\}+\left\{F_{n+1}^{(2), R}\right\}+\left\{F_{n+1}^{(3), P C}\right\}+\left\{F_{n+1}^{(4), P P}\right\}+\left\{F_{n+1}^{(5), R}\right\}+\left\{F_{n+1}^{(6), P C}\right\} \\
& +\left\{F_{n+1}^{(6), G}\right\}+\left\{F_{n+1}^{(7), W}\right\}+\left\{F_{n+1}^{(8), R}\right\}+\left\{F_{n+1}^{(8), A X}\right\}+\left\{F_{n+1}^{(8) W}\right\}+\left\{F_{n+1}^{(8), G}\right\} . \tag{2.3.41}
\end{align*}
$$

These forces are classified into three types according to the method of treatment of forces as

$$
\begin{equation*}
\left\{F_{n+1}\right\}=\left\{F_{n+1}^{\prime}\right\}+\left\{F_{n+1}^{\prime \prime}\right\}+\left\{F_{n+1}^{\prime \prime \prime}\right\}, \tag{2.3.42}
\end{equation*}
$$

where

$$
\begin{align*}
& \left\{F_{n+1}^{\prime}\right\}=\left\{F_{n+1}^{(6), G}\right\}+\left\{F_{n+1}^{(7), W}\right\}+\left\{F_{n+1}^{(8), W}\right\}+\left\{F_{n+1}^{(8), G}\right\}  \tag{2.3.43}\\
& \left\{F_{n+1}^{\prime \prime}\right\}=\left\{F_{n+1}^{(1), R}\right\}+\left\{F_{n+1}^{(2), R}\right\}+\left\{F_{n+1}^{(5), R}\right\}+\left\{F_{n+1}^{(8), R}\right\}  \tag{2.3.44}\\
& \left\{F_{n+1}^{\prime \prime \prime}\right\}=\left\{F_{n+1}^{(3), P C}\right\}+\left\{F_{n+1}^{(4), P P}\right\}+\left\{F_{n+1}^{(6), P C}\right\}+\left\{F_{n+1}^{(8), A X}\right\} . \tag{2.3.45}
\end{align*}
$$

$\left\{F_{n+1}^{\prime}\right\}$ is treated as those in which values are known at time $t_{n+1}$, and $\left\{F_{n+1}^{\prime \prime}\right\}$ is the constraint force due to the known boundary condition (designated displacement). $\left\{F_{n+1}^{\prime \prime \prime}\right\}$ is determined by boundary conditions which depend on unknown values; for obtaining $\left\{F_{n+1}^{\prime \prime \prime}\right\}$, the interaction between pellet andcladding, as well as pellet and pellet must be solved.

## (2) Interaction between pellet and cladding

The solution to obtain $\left\{F_{n+1}^{\prime \prime \prime}\right\}$ in eq. (2.3.45) is given below. When iteration of the

Newton-Raphson method is completed, eqs. (2.3.14), (2.3.15) and (2.3.16) are expressed as follows with omission of subscript $i$ for iteration. Here, ${ }^{\wedge}$ indicates that the value is a tentative one during the iteration calculation.

$$
\begin{gather*}
{\left[K_{n+\theta}\right]\left\{\Delta u_{n+1}\right\}=\left\{\Delta \hat{F}_{n+1}\right\}}  \tag{2.3.46}\\
{\left[K_{n+\theta}\right]=\int[B]^{T}\left[\hat{D}_{n+\theta}^{p}\right][B] d V}  \tag{2.3.47}\\
\left\{\Delta \hat{F}_{n+1}\right\}=\left\{F_{n+1}\right\}-\int[B]^{T}\left\{\sigma_{n+1}\right\} d V \\
-\int[B]^{T}\left[\hat{D}_{n+\theta}^{p}\right]\left\{\left[\bar{C}_{l+\theta}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left\{\Delta \varepsilon_{n+1}^{c}\right\}\right\} d V  \tag{2.3.48}\\
-\int[B]^{T}\left(\left\{S_{n+1}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) d V
\end{gather*}
$$

Here, with substitution of eq. (2.3.42) into the right-hand side of eq. (2.3.48), the load term can be given by

$$
\begin{align*}
\left\{\Delta \hat{F}_{n+1}\right\} & =\left\{F_{n+1}^{\prime}\right\}+\left\{F_{n+1}^{\prime \prime}\right\}+\left\{F_{n+1}^{\prime \prime \prime}\right\}-\int[B]^{T}\left\{\sigma_{n+1}\right\} d V \\
& \left.\left.-\int[B]^{T}\left[\hat{D}_{n+\theta}^{P}\right]\right]\left[\bar{C}_{1+\theta}\right]\left(\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left\{\Delta \varepsilon_{n+1}^{c}\right\}\right\} d V  \tag{2.3.49}\\
& -\int[B]^{r}\left(\left\{S_{n+1}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) d V \\
= & \left\{\Delta \hat{F}_{n+1}^{\prime}\right\}+\left\{F_{n+1}^{\prime \prime \prime}\right\},
\end{align*}
$$

where

$$
\begin{align*}
\left\{\Delta \hat{F}_{n+1}^{\prime}\right\} & =\left\{F_{n+1}^{\prime}\right\}+\left\{F_{n+1}^{\prime \prime}\right\}-\int[B]^{T}\left\{\sigma_{n+1}\right\} d V \\
& \left.\left.\left.-\int[B]^{T}\left[\hat{D}_{n+\theta}^{P}\right]\right\}\left[\bar{C}_{1+\theta}\right]\left[\left\{\sigma_{n+1}^{\prime}\right\}-\left\{\sigma_{n}\right\}\right)+\left\{\Delta \varepsilon_{n+1}^{0}\right\}-\left\{\Delta \varepsilon_{n+1}^{\mathrm{c}}\right\}\right\}\right\} d V  \tag{2.3.50}\\
& -\int[B]^{T}\left(\left\{S_{n+1}\right\} \Delta T_{n+1}-\left\{Z_{1}\right\}-\left\{Z_{2}\right\}\right) d V .
\end{align*}
$$

Here, $\left\{\Delta \hat{F}_{n+1}^{\prime}\right\}$ is the node point loading increment vector under the condition $\left\{F_{n+1}^{\prime \prime}\right\}$ (noncontact condition).

Substituting eq. (2.3.49) into eq. (2.3.46), we obtain

$$
\begin{equation*}
\left[K_{n+\theta}\right]\left\{\Delta u_{n+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{\prime}\right\}+\left\{F_{n+1}^{\prime \prime \prime}\right\} . \tag{2.3.51}
\end{equation*}
$$

As shown in Fig. 2.42, the two planes contacting each other are expressed by several contact node couples. As contact conditions, three states are considered: non-contact state, clogged gap state and sliding state.

In FEMAXI-IV, this pellet/cladding contact problem is solved in the following procedure.


Fig. 2.42 Pellet-cladding contact node couple.
(1) A contact state (either contact or non-contact) is assumed for each couple of nodes which are possibly in contact with each other. Initially, this assumption is made based on the results for the previous time step.
(2) The stiffness equation is solved using boundary conditions corresponding to the assumed contact state (contact or non-contact).
(3) Based on the solutions of nodal displacement and contact force obtained in (2), judgment is made on whether or not the assumption made in (1) for each node couple is correct. If one of the assumptions is contradictory to the solution obtained by calculation at one node couple, the procedure is returned to (1), the assumption is corrected for the node couple, and procedures (2) and (3) are performed again.
(4) Thus, the calculation procedures from (1) to (3)are repeated until no discrepancy is observed between the assumption and calculated results. When a change in state of non-contact or contact (clogged gap state or sliding state) occurs, interpolation is carried out for the calculated results into the time when the change in state occurred, the assumption is corrected after that time and the procedure is returned to (1) for continuous calculation.
When a pellet is not in contact with the cladding, $\left\{F_{n+1}^{(3), p^{\prime}}\right\}$ and $\left\{F_{n+1}^{(6), P C}\right\}$ in eq. (2.3.41) are zero. As described later, $\left\{F_{n+1}^{(4), P p}\right\}$ and $\left\{F_{n+1}^{(8), A X}\right\}$ are also set as zero, and accordingly $\left\{F_{n+1}^{\prime \prime \prime}\right\}=0$.

Therefore, from eq. (2.3.51) we obtain

$$
\begin{equation*}
\left[K_{n+\theta}\right]\left\{\Delta u_{n+1}\right\}=\left\{\Delta \hat{F}_{n+1}^{\prime}\right\} . \tag{2.3.52}
\end{equation*}
$$

When one contact node couple is in a sliding state and the remaining contact node couples
are in a non-contact state, then $\left\{F_{n+1}^{(3), P c}\right\}$ and $\left\{F_{n+1}^{(6), P c}\right\}$ are represented as

$$
\begin{gather*}
\left\{F_{n+1}^{(3) P C \cdot}\right\}=\left\{\begin{array}{c}
0 \\
\vdots \\
0 \\
U_{n+1} \\
V_{n+1} \\
0 \\
\vdots \\
0
\end{array}\right\}  \tag{2.3.53}\\
\left\{F_{n+1}^{(6), P \cdot}\right\}=\left\{\begin{array}{c}
0 \\
\vdots \\
0 \\
-U_{n+1} \\
-V_{n+1} \\
0 \\
\vdots \\
0
\end{array}\right\}, \tag{2.3.54}
\end{gather*}
$$

where

$$
\begin{equation*}
V_{n+1}= \pm \mu U_{n+1} \tag{2.3.55}
\end{equation*}
$$

$V_{n+1}$ : contact force in the radial direction at time step $t_{n-1}$
$U_{n+1}$ : contact force in the axial direction at time step $t_{n-1}$
$\mu$ : pellet/cladding friction coefficient.
Therefore, eq. (2.3.52) is represented as


Here,
$\Delta u_{p, n+1}:$ radial displacement increment of the node on the pellet side of a sliding-state contact node couple at time $t_{n+1}$
$\Delta v_{p, n+1}$ : axial displacement increment of the node on the pellet side of a sliding-state contact node couple at time $t_{n+1}$
$\Delta u_{c, n+1}:$ radial displacement increment of the node on the cladding side of a sliding-state contact node couple at time $t_{n+1}$
$\Delta v_{c, n+1}$ : axial displacement increment of the node on the cladding side of a sliding-state contact node couple at time $t_{n+1}$.

Equations expressing degrees of freedom of contact nodes $i, j, k$ and $l$ in the above equation are

$$
\begin{align*}
& K_{n+\theta}^{(i)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(1)}+U_{n+1}  \tag{2.3.57}\\
& K_{n+\theta}^{(j)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(j)} \pm \mu U_{n+1}  \tag{2.3.58}\\
& K_{n+\theta}^{(k)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(k)}-U_{n+1}  \tag{2.3.59}\\
& K_{n+\theta}^{(\prime)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(k)} \pm \mu U_{n+1} \tag{2.3.60}
\end{align*}
$$

Also,

$$
\begin{equation*}
-\Delta u_{p, n+1}+\Delta u_{c, n+1}=0 \tag{2.3.61}
\end{equation*}
$$

The stiffness equation when one contact node couple is in a clogged gap state and all the other couples are in a non-contact state is represented as


Here,
$\Delta u_{p, n+1}$ : radial displacement increment of the node on the pellet side of a clogged-gap-state contact node couple at time $t_{n+1}$
$\Delta v_{p, n+1}$ : axial displacement increment of the node on the pellet side of a clogged-gap-state contact node couple at time $t_{n+1}$
$\Delta u_{c, n+1}$ : radial displacement increment of the node on the cladding side of a clogged-gapstate contact node couple at time $t_{n+1}$
$\Delta v_{c, n+1}$ : axial displacement increment of the node on the cladding side of a clogged-gapstate
contact node couple at time $t_{n+1}$.
Stiffness equations expressing degrees of freedom of contact nodes $i, j, k$ and $l$ in the above equation are

$$
\begin{align*}
& K_{n+\theta}^{(i)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(1)}+U_{n+1}  \tag{2.3.63}\\
& K_{n+\theta}^{(\jmath)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(\jmath)}+V_{n+1}  \tag{2.3.64}\\
& K_{n+\theta}^{(k)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(k)}-U_{n+1}  \tag{2.3.65}\\
& K_{n+\theta}^{(1)}\left\{\Delta u_{n+1}\right\}=\Delta \hat{F}_{n+1}^{\prime(k)}-V_{n+1} . \tag{2.3.66}
\end{align*}
$$

Also,

$$
\begin{align*}
& -\Delta u_{p, n+1}+\Delta u_{c, n+1}=0  \tag{2.3.67}\\
& -\Delta v_{p, n+1}+\Delta v_{c, n+1}=0 \tag{2.3.68}
\end{align*}
$$

At judgment of the contact state and after this judgment, the following processes are carried out.
(1) In cases of a non-contact state at the previous time step Presence of overlap of displacement is checked for. Namely,

$$
\begin{equation*}
g_{n+1}=g_{n}-\Delta u_{p, n+1}+\Delta u_{c, n+1}, \tag{2.3.69}
\end{equation*}
$$

where

$$
g_{n+1}: \text { gap width at time step } t_{n+1}
$$

When $g_{n+1}>0$, eq. (2.3.69) is judged as being converged; when $g_{n+1} \leq 0$, the time step is returned to $t_{n+\alpha}$ using the equation

$$
\begin{equation*}
t_{n+\alpha}=\frac{t_{n+1}-t_{n}}{g_{n}-g_{n+1}} g_{n}+t_{n} \tag{2.3.70}
\end{equation*}
$$

Then, the calculation from time $t_{n+\alpha}$ to $t_{n+1}$ is performed again after changing of the contact
state to a clogged gap state.
(2) In cases of a clogged gap state at the previous time step

The state change is judged in terms of a contact force vector. Namely, when

$$
\begin{equation*}
U_{p, n+1}<0 \text { and }\left|V_{p, n+1}\right|<\mu\left|U_{p, n+1}\right| \tag{2.3.71}
\end{equation*}
$$

are satisfied, the contact state is judged as being converged;
when

$$
\begin{equation*}
U_{p, n+1}<0 \text { and }\left|V_{p, n+1}\right| \geq \mu\left|U_{p, n+1}\right| \tag{2.3.72}
\end{equation*}
$$

are satisfied, the assumed contact state is changed to a sliding state and the calculation is performed again. Also, when

$$
\begin{equation*}
U_{p, n+1} \geq 0 \tag{2.3.73}
\end{equation*}
$$

the contact state is changed from a clogged gap state to a non-contact state; therefore, the time step is returned to $t_{n+\alpha}$ using

$$
\begin{equation*}
t_{n+\alpha}=\frac{t_{n+1}-t_{n}}{U_{p, n}-U_{p, n+1}} U_{p, n}+t_{n}, \tag{2.3.74}
\end{equation*}
$$

and the calculation from time $t_{n+\alpha}$ to $t_{n+1}$ is performed again after changing of the contact state to a non-contact state.
(3) In cases of a sliding state at the previous time step

The state change is judged in terms of a contact force vector. Namely, when

$$
\begin{equation*}
U_{p, n+1}<0 \text { and }\left|V_{p, n+1}\right| \geq \mu\left|U_{p, n+1}\right| \tag{2.3.75}
\end{equation*}
$$

are satisfied, the contact state is judged as being converged. However, when

$$
\begin{equation*}
U_{p, n+1}<0 \text { and }\left|V_{p, n+1}\right|<\mu\left|U_{p, n+1}\right| \tag{2.3.76}
\end{equation*}
$$

hold, the contact state is changed to a clogged gap state.
Also, when

$$
\begin{equation*}
U_{p, n+1}<0 \text { and }\left|v_{p, n+1}^{*}\right| \leq\left|v_{c, n+1}^{*}\right| \tag{2.3.77}
\end{equation*}
$$

are satisfied, the assumed contact state is changed from a sliding state to a clogged gap state.

Here,
$v_{p, n+1}^{*} \quad: \quad$ axial displacement of a node on the pellet side after the start of contact
$v_{c, n+1}^{\prime} \quad:$ axial displacement of a node on the cladding side after the start of contact.
In contrast, when

$$
\begin{equation*}
U_{p, n+1} \geq 0 \tag{2.3.78}
\end{equation*}
$$

is satisfied, the contact state is judged as being changed from a sliding state to a non-contact state; the time step is returned to $t_{n+\alpha}$ using eq. (2.3.74) and the variable values are interpolated for the time step $t_{n+\alpha}$; then the calculation from time $t_{n+\alpha}$ to $t_{n+1}$ is performed again after changing of the contact state to a non-contact state.

In a system having several contact node couples as shown in Fig. 2.42, if we try to converge the contact state for each node couple independently, a large number of iterations are required for convergence of the entire system. Therefore, the following conditions are added in order to reduce the number of the iterations.
(1) For node couples in the contact state, all of the states are initially assumed to be clogged gap states.
(2) Among them, if some node couples satisfy the condition $\left|V_{p, n+1}\right| \geq \mu\left|U_{p, n+1}\right|$, the assumed contact state for such node couples and contact states of node couples located above them are changed to sliding states.
(3) At this time, directions of sliding are aligned. That is, friction force is exerted downward on the pellet surface, and upward on the inner surface of cladding. However, if all axial components of the contact force of the node couples which were judged to be in a sliding state when they were assumed to be in a clogged gap state are in the reverse directions, the direction of sliding should be reversed.

With the above method, convergence of the entire system can be achieved within less than 3 iterations in general cases.

## (3) Axial loads -Interaction between pellet/pellet-

When the gap width between a pellet and cladding which is located above the objective segment is less than a predetermined value, it is assumed that the pellet and cladding above the objective segment are in a clogged gap state, which restricts the axial displacement of the objective pellet; that is, locking is generated.

For modeling of the locking condition, among nodes which are distributed on the upper surface of the objective segment, a displacement increment of node $i$ with the maximum coordinate value in the axial direction is set to be equal to the displacement increment of the boundary surface of the pellet, i.e., boundary (8) shown in Fig. 2.41. By this setting, axial load is generated for the pellet and cladding. This condition is called a locking condition.

| Fitting parameter GAPLK | The radial gap width with which the locking condition is |
| :---: | :---: |
| given is adjusted by GAPLK. The default value of GAPLK is $3(\mu \mathrm{~m})$. |  |

The procedures for the judgment of contact condition between a pellet in the objective segment and a pellet located above it, as well as the process following the judgment are as follows.

When the axial coordinate of another node $j$ on the upper surface of the pellet in the objective segment exceeds that of node $i$, the axial displacement increment of node $j$ is also set to be equal to the axial displacement increment of the boundary surface (8), as in the case of the node $i$. That is, the locking condition is set on node $j$, also. At this time, the time is returned to the state change point $t_{n+\alpha}$ using the equation

$$
\begin{equation*}
t_{n+\alpha}=\frac{\bar{Z}_{i, n}-Z_{j, n}}{Z_{j, n+1}-Z_{j, n}-\left(\bar{Z}_{i, n+1}-\bar{Z}_{i, n}\right)}\left(t_{n+1}-t_{n}\right)+t_{n} . \tag{2.3.79}
\end{equation*}
$$

Here,
$\bar{Z}_{i, n}, \bar{Z}_{n+1}$ : axial coordinates of node $i$ in the locking condition at time $t_{n}$ and $t_{n+1}$ $Z_{j, n}, Z_{j, n+1}$ : axial coordinates of node $j$ at time $t_{n}$ and $t_{n+1}$.

From time $t_{n+\alpha}$ to $t_{n+1}$, the degree of freedom in the axial direction of node $j$ is set as the same degree of freedom in the axial direction of nodes $i$, which is also the same degree of freedom in the axial direction of the upper edge surface of the cladding (boundary (8)), namely the common degree of freedom; then the calculation is performed again.

By this method, the locking condition is generally realized by setting of a boundary condition in which axial displacement increments of a pellet-node group which supports the axial load on boundary (4) and those of a cladding-node group on boundary (8) are set to be equal. In this procedure, the number of degrees of freedom of the pellet-node group in the axial direction is assumed to be one, and those of the cladding-node group is also assumed to be one. That is, they are assumed to have common degrees of freedom. (see Fig. 2.41)

The contact force in the axial direction at an arbitrary time of an arbitrary node in the contact state is given by eq. (2.3.1). That is, in

$$
\begin{equation*}
\left\{F_{n+1}\right\}=\int[B]^{T}\left\{\sigma_{n+1}\right\} d V, \tag{2.3.1}
\end{equation*}
$$

since the only load which acts on boundary (4) is the contact force in the axial direction $\left\{F_{n+1}^{(4), P p}\right\}$,

$$
\begin{equation*}
\left\{F_{n+1}^{(4), p \varphi}\right\}=\left\{F_{n+1}\right\}=\int[B]^{T}\left\{\sigma_{n+1}\right\} d V \tag{2.3.80}
\end{equation*}
$$

holds.
The contact force in the axial direction of a node obtained from eq. (2.3.80) is represented by $V_{n+1}$. When $V_{n+1}<0$, the locking condition is maintained on this node. When $V_{n+1} \geq 0$, the locking condition is judged to be disengaged, and the time is returned to $t_{n+\alpha}$ using the equation

$$
\begin{equation*}
t_{n+\alpha}=\frac{V_{n}}{V_{n}-V_{n+1}}\left(t_{n+1}-t_{n}\right)+t_{n} \tag{2.3.81}
\end{equation*}
$$

From time $t_{n+\alpha}$ to $t_{n+1}$, the degree of freedom in the axial direction of this node is set to be different from the common degree of freedom.

Here, when the sign of $V$ is positive at all nodes on the edge surface of the pellet, the locking condition is disengaged.

A locking condition is set for the second time or later when a node on the edge surface of the pellet reaches the axial coordinates at the time when the previous locking condition was disengaged. Here, the load $\left\{F^{(8)}\right\}$ which acts on the upper edge surface of the cladding (boundary (8)) at the time of the locking condition setting is expressed as

$$
\begin{equation*}
\left\{F^{(8)}\right\}=\left\{F^{(8), R}\right\}+\left\{F^{(8), A X}\right\}+\left\{F^{(8), W}\right\}+\left\{F^{(8), G}\right\} \tag{2.3.82}
\end{equation*}
$$

where
$\left\{F^{(8)}\right\}$ : axial load which acts on boundary (8)
$\left\{F^{(8), R}\right\}$ : nodal force generated by setting of the number of degrees of freedom in the axial direction as 1 at boundary (8)
$\left\{F^{(8), A x}\right\}$ : axial tensile load due to the locking condition at boundary (8)
$\left\{F^{\left(8, W^{W}\right.}\right\}:$ axial load due to coolant pressure
$\left\{F^{(8), G}\right\} \quad: \quad$ axial load due to plenum gas pressure.

### 2.4 Material Properties

The following tables show the material properties and equations installed in the present FEMAXI-IV(Ver.2). An asterisk * in the right column indicates that reference source is unknown.

### 2.4.1 Material properties of pellet

(1) Pellet thermal conductivity

| $\mathrm{UO}_{2}$ thermal conductivity (1) MATPRO-Version 09 | Condition | Ref. |
| :---: | :---: | :---: |
| for a temperature range of $0-1,650^{\circ} \mathrm{C}$ : $K=\left\{\frac{1-\beta(1-D)}{1-0.05 \beta}\right\} \cdot\left\{\frac{40.4}{464+T}+1.216 \times 10^{-4} \exp \left(1.867 \times 10^{-3} T\right)\right\}$ <br> for a temperature range of $1,650-2,840^{\circ} \mathrm{C}$ $K=\left\{\frac{1-\beta(1-D)}{1-0.05 \beta}\right\} \cdot\left\{0.0191+1.216 \times 10^{-4} \exp \left(1.867 \times 10^{-3} T\right)\right\}$ <br> $K$ : thermal conductivity of $\mathrm{UO}_{2}$ pellet ( $\mathrm{W} / \mathrm{cm} \cdot \mathrm{K}$ ) <br> $D: \mathrm{UO}_{2}$ theoretical density ratio <br> $T$ : temperature $\left({ }^{\circ} \mathrm{C}\right)$ <br> $\beta$ : porosity coefficient: $\beta=2.58-0.58 \times 10^{-3} \mathrm{~T}$ | Default value: <br> IPTHCN=1 | 14 |
| $\mathrm{UO}_{2}$ thermal conductivity (2) Washington |  |  |
| $\begin{gathered} K=F \cdot\left\{\left(0.040+2.57 \times 10^{-4} \cdot T_{K}\right)^{-1}+72.6 \times 10^{-12} \cdot T_{K}^{3}\right\} \quad(W / \mathrm{mK}) \\ F=1.0-2.5 \cdot P \\ P: \text { porosity }=1.0-\left(\text { actual } \mathrm{UO}_{2} \text { density/theoretical density }\right) \\ T_{K}: \text { temperature }(\mathrm{K}) \end{gathered}$ | IPTHCN=2 | 23 |
| $\mathrm{UO}_{2}$ thermal conductivity (3) Hirai |  |  |
| $\begin{aligned} & K=K_{95 \% T D} \cdot(1-\beta p) /(1-0.05 \cdot \beta) \quad(W / m K) \\ & K_{95 \% T D}=\left(2.35 \times 10^{-2}+2.55 \times 10^{-4} \cdot T_{K}\right)^{-1}+3.57 \times 10^{-12} \cdot T_{K}{ }^{3} \\ & \left.\quad \beta=2.58-0.58 \times 10^{-3} T \rightarrow \text { Ref. } 14\right) \\ & P: \text { porosity } \\ & T_{K}: \text { temperature (K) } \end{aligned}$ | IPTHCN=3 | 24 |
| $\mathrm{UO}_{2}$ thermal conductivity (4) Halden |  |  |
| $\begin{aligned} & K=F\left\{\begin{array}{l} 0.1148+0.0035 \cdot B+\left(2.475 \times 10^{-4}-8 \times 10^{-7} \cdot B\right) T \\ \\ \\ \\ \\ F \end{array}\right)=(1-\beta p) /(1-0.052 \exp (0.00188 \cdot T) \\ & \beta=2.58-0.58 \times 10^{-3} T \rightarrow \text { Ref. }(14) \\ & P: \text { porosity } \\ & B: \text { burnup }\left(\mathrm{MWd} / \mathrm{kgUO}_{2}\right) \\ & T \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \\ & \hline \end{aligned}$ | IPTHCN=4 | 25 |


| $\mathrm{UO}_{2}$ thermal conductivity (5) Modified Hirai |  |  |
| :---: | :---: | :---: |
| $\begin{aligned} & K= K_{95 \% / T D} \cdot(1-\beta p) /(1-0.05 \cdot \beta) \quad(W / m K) \\ & K_{95 \% / D}=\left\{\left(2.35 \times 10^{-2}+4.8 \times 10^{-3} \cdot B\right)+\left(2.55 \times 10^{-4}-16.0 \times 10^{-7} \cdot B\right) \cdot T_{K}\right\}^{-1} \\ &+3.57 \times 10^{-12} \cdot T_{K}{ }^{3} \\ &\left.\beta=2.58-0.58 \times 10^{-3} T \rightarrow \text { Ref. } 14\right) \\ & P: \text { porosity } \\ & T_{K}: \text { temperature (K) } \\ & B: \text { burnup (MWd/kg-U) } \end{aligned}$ | IPTHCN=5 | 24 |
| $\mathrm{UO}_{2}$ thermal conductivity (6) Forsberg |  |  |
|  | IPTHCN=6 | 26 |
| $\mathrm{UO}_{2}$ thermal conductivity (7) Kjaer-Pedersen |  |  |
| $\begin{aligned} & K=93 /\left(0.0224 \cdot T_{K}+1.1+56 \cdot P+3 \cdot G(B)\right)+2.5 \cdot 10^{-14} \cdot T_{K}{ }^{4} \\ & B \leq 10 \quad G=(B / 10)^{2} \\ & B \geq 10 \quad G=((B-7.5) / 10)^{0.5} \\ & P: \text { porosity } \\ & T_{K}: \text { temperature }(\mathrm{K}) \\ & B: \text { burnup }(\mathrm{MWd} / \mathrm{kg}-\mathrm{U}) \end{aligned}$ | IPTHCN=7 | 27 |
| MOX pellet thermal conductivity Martin | Condition | Ref. |
| 1) In the case of $12 \% \leq \mathrm{PuO}_{2} \leq 30 \%$ $K=\left(0.037+3.33 y+2.37 \times 10^{-4} T_{K}\right)^{-1}+78.9 \times 10^{-12} T_{K}^{3}$ <br> 2) In the case of $0 \% \leqq \mathrm{PuO}_{2} \leqq 12 \%$ $K=(f)=K u(1-f / 0.12)+K(M o x) \times f / 0.12$ <br> Here, $\begin{aligned} & K: \text { thermal conductivity }(\mathrm{W} / \mathrm{m} \cdot \mathrm{~K}) \\ & T_{K}: \text { temperature }(\mathrm{K}) \\ & \mathrm{y}: \mathrm{MO}_{2-\mathrm{y}} \\ & K_{u}: \mathrm{UO}_{2} \text { thermal conductivity }(\mathrm{W} / \mathrm{m} \cdot \mathrm{~K}) \\ & K_{u}=\left[\left(0.035+2.25 \cdot 10^{-4} \cdot T_{K}\right)^{-1}+83.0 \cdot 10^{-12} \cdot T_{K}{ }^{3}\right] \cdot(1+z) \\ & \quad\left(z: U O_{2-z}, \quad 0 \leq z \leq 0.05\right) \end{aligned}$ | $\mathrm{MOX}=1$ | 28 |

When $\mathrm{MOX}=1$, the following values are designated by input.

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| PU | $\mathrm{PuO}_{2}$ weight ratio (converted to molar fraction by the code) | 0.0 |
| Y | Value of y for $\mathrm{MO}_{2 \cdot y}$ (this value is also used for z) | 0.0 |


| Thermal conductivity of pellet containing Gadolinium Fukushima | Condition | Ref. |
| :---: | :---: | :---: |
| $K=\frac{1}{a T+b}$ <br> Here, <br> $K$ : thermal conductivity ( $\mathrm{W} / \mathrm{m} \cdot \mathrm{K}$ ) <br> $T$ : temperature ( ${ }^{\circ} \mathrm{C}$ ) <br> $a, b:$ function of $\mathrm{Gd}_{2} \mathrm{O}_{3}$ concentration (see table below) <br> In order to interpolate $a, b$ for other $\mathrm{Gd}_{2} \mathrm{O}_{3}$ concentrations, two values of $a$ and $b$ in the above table whose $\mathrm{Gd}_{2} \mathrm{O}_{3}$ concentrations sandwich the current $\mathrm{Gd}_{2} \mathrm{O}_{3}$ concentration are substituted into $K=r A^{\text {(id }}$ to obtain $r$ and $A$, so that the two values of $K$ coincide. | $\mathrm{IGD}=1$ | 29 |

In the case of $\mathrm{IGD}=1$, the following value is input.

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| GD | $\mathrm{Gd}_{2} \mathrm{O}_{3}$ concentration (Weight fraction) | 0.0 |

(2) Pellet thermal expansion

Equations representing pellet thermal expansion are selected from among the following.

| $\mathrm{UO}_{2}$ thermal expansion (1) MATPRO-Version 09 | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} & \frac{\Delta L}{L}=-4.972 \times 10^{-4}+7.107 \times 10^{-6} \mathrm{~T}+2.581 \times 10^{-9} \mathrm{~T}^{2}+1.140 \times 10^{-43} \mathrm{~T}^{3} \\ & \frac{\Delta L}{L}: \text { linear thermal expansion } \\ & T: \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \end{aligned}$ | IPTHEX=0 <br> (default <br> value) IPTHEX=1 | 14 |
| $\mathrm{UO}_{2}$ thermal expansion (2) Burdick and Parker |  |  |
| $\frac{\Delta L}{L}=-3.0289 \times 10^{-4}+8.4217 \times 10^{-6} T+2.1481 \times 10^{-9} T^{2}$ <br> $T$ : temperature $\left({ }^{\circ} \mathrm{C}\right)$ <br> temperature range: $27-1260^{\circ} \mathrm{C}$ <br> $\Delta L / L$ : linear thermal expansion normalized by the length at $27^{\circ} \mathrm{C}$. | IPTHEX=2 | * |
| $\mathrm{UO}_{2}$ thermal expansion (3) Halden |  |  |
| $\begin{aligned} \frac{\Delta L}{L}= & 6.0 \times 10^{-6} \mathrm{~T}+2.0 \times 10^{-9} \mathrm{~T}^{2}+1.7 \times 10^{-12} \mathrm{~T}^{3} \\ & T: \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \\ & \text { temperature range: } 900-2,800^{\circ} \mathrm{C} \text { (melting point) } \end{aligned}$ | IPTHEX=3 | * |
| $\mathrm{UO}_{2}$ thermal expansion (4) Conway and Fincel |  |  |
| $\begin{aligned} \frac{\Delta L}{L}=- & .723 \times 10^{-4}+6.797 \times 10^{-6} \mathrm{~T}+2.896 \times 10^{-9} \mathrm{~T}^{2} \\ & T: \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \\ & \text { temperature range: } 1,000-2,250^{\circ} \mathrm{C} \end{aligned}$ | IPTHEX=4 | * |

(3) $\mathrm{UO}_{2}$ theoretical density

| $\mathrm{UO}_{2}$ density | MATPRO-Version 09 | Condition | Ref. |
| :---: | :---: | :--- | :--- |
| $\rho=10.96$, | $\rho: \mathrm{UO}_{2}$ theoretical density $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ | No restrictions | 14 |

(4) $\mathrm{UO}_{2}$ Young's modulus

| $\mathrm{UO}_{2}$ Young's modulus | MATPRO-Version 09 | Condition |
| :---: | :--- | :---: |
| $E=2.26 \times 10^{11}\left(1-\mathrm{l} .131 \times 10^{-4} \mathrm{~T}\right)[1-2.62(1-\mathrm{D})]$ |  |  |
| $\mathrm{E}:$ Young's modulus $(\mathrm{Pa})$ | No restrictions | 14 |
| $\mathrm{~T}:$ temperature $\left({ }^{\circ} \mathrm{C}\right)$ |  |  |
| $\mathrm{D}:$ theoretical density ratio |  |  |

(5) $\mathrm{UO}_{2}$ Poisson's ratio

| Poisson's ratio of $\mathrm{UO}_{2}$ | MATPRO-Version 09 | Condition | Ref. |
| :---: | :--- | :--- | :--- |
| $\nu=0.316$ |  | No restrictions | 14 |

(6) $\mathrm{UO}_{2}$ creep

| Creep of $\mathrm{UO}_{2}$ | MATPRO-Version 09 | Condition |
| :--- | :--- | :--- |
| $\varepsilon=\frac{\left(A_{1}+A_{2} \dot{F}\right) \sigma \exp \left(-Q_{1} / R T\right)}{\left(A_{3}+D\right) G^{2}}+\frac{A_{4} \sigma^{45} \exp \left(-Q_{2} / R T\right)}{\left(A_{5}+D\right)}+A_{6} \sigma \dot{F} \exp \left(-Q_{3} / R T\right)$ |  |  |
| $\varepsilon:$ steady-state creep rate $(1 / \mathrm{h})$ | No restrictions | 14 |
| $A_{1}=9.728 \times 10^{6}$ |  |  |
| $A_{2}=3.24 \times 10^{-12}$ |  |  |
| $A_{3}=-87.7$ |  |  |
| $A_{4}=1.376 \times 10^{-4}$ |  |  |
| $A_{5}=-905$ |  |  |
| $A_{6}=9.24 \times 10^{-28}$ |  |  |
| $Q_{1}=90,000(\mathrm{cal} / \mathrm{mol})$ |  |  |
| $Q_{2}=132,000(\mathrm{cal} / \mathrm{mol})$ |  |  |
| $Q_{3}=5,200(\mathrm{cal} / \mathrm{mol})$ |  |  |
| $F:$ fission rate $8.4 \times 10^{17} \sim 1.18 \times 10^{20}\left(\mathrm{fiss} . / \mathrm{m}^{3} \cdot \mathrm{sec}\right)$ |  |  |
| $\sigma:$ stress $1,000-16,000(\mathrm{psi})$ |  |  |
| $T:$ temperature $713-2,073(\mathrm{~K})$ |  |  |
| $D:$ density $92-98(\% \mathrm{TD})$ |  |  |
| $G:$ grain size $4-35(\mu \mathrm{~m})$ |  |  |
| $R:$ gas constant $1.987(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{K})$ |  |  |
| $\vdots$ |  |  |

The following fitting parameters can be used for the $\mathrm{UO}_{2}$ creep rate equation.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| FCRFAC | Magnification factor for the creep rate equation (deformation <br> model) | 10.0 |
| TCS | Cut-off value at the reference temperature in the creep <br> calculation (deformation model) (K) | 2073.15 |
| TCRMX | Cut-off value at the reference temperature in the creep <br> calculation (thermal model) $(\mathrm{K})$ | 1773.15 |

## (7) $\mathrm{UO}_{2}$ swelling

Shown below are the equations representing $\mathrm{UO}_{2}$ swelling. There are two types of $\mathrm{UO}_{2}$ swelling: solid FP swelling and gas-bubble swelling.

Using the options, one of the following two cases can be selected: a case in which the solid FP swelling and gas-bubble swelling are treated independently, and a case in which both types of swelling are given by a single material property equation.

| $\mathrm{UO}_{2}$ swelling (1) Chubb | Condition | Ref. |
| :---: | :---: | :---: |
| (gas-bubble swelling) $\begin{aligned} &\left(\frac{\Delta V}{V}\right)^{g T}=4.396 \times 10^{2} \exp \left(-\frac{1.645 \times 10^{4}}{T_{s}}\right) \\ & T_{s}=T-100 \\ &\left(\frac{\Delta V}{V}\right)^{g T}: \text { volume of gas-bubble swelling per } 10^{20} \text { fissions } / \mathrm{cm}^{3} \\ & T: \text { temperature (K) } \end{aligned}$ | IFSWEL=0 <br> (default <br> value) | 30 |
| $\mathrm{UO}_{2}$ swelling (la) FEMAXI-III |  |  |
| (Solid FP swelling) $\begin{aligned} & \left(\frac{\Delta V}{V}\right)^{s}=0.0025 \\ & \left(\frac{\Delta V}{V}\right)^{s r}: \text { volume of FP swelling per } 10^{20} \text { fissions } / \mathrm{cm}^{3} \end{aligned}$ |  | 2 |

In the case of ISWEL $=0$, the following fitting parameters can be used.

| Variable <br> name | Content | Default value |
| :---: | :--- | :--- |
| STFCP | Suppress generation of gas-bubble swelling average <br> contact pressure $(\mathrm{Pa})$ (used in the deformation model) | $-3 \times 10^{7}$ |
| SPCON | Suppress generation of gas-bubble swelling average <br> contact pressure $(\mathrm{Pa})$ (used in the thermal model) | $-10^{6}$ |


| $\mathrm{UO}_{2}$ swelling (2) Speight | Condition | Ref. |
| :---: | :---: | :---: |
| (Gas-bubble swelling) <br> Intragranular gas-bubble swelling $\begin{aligned} \left(\frac{\Delta V}{V}\right)^{g 1} & =\frac{4}{3} \pi a^{3} N \\ a & : \text { intragranular gas-bubble radius }(\mathrm{cm}) \\ N & : \text { number of gas bubbles per unit volume }\left(1 / \mathrm{cm}^{3}\right) \end{aligned}$ <br> Grain-boundary gas-bubble swelling | IFSWEL=1 | 16 |
| $\mathrm{UO}_{2}$ swelling (1a) FEMAXI-III |  |  |
| (Solid FP swelling) $\begin{aligned} & \left(\frac{\Delta V}{V}\right)^{\mathrm{s}}=0.0025 \\ & \left(\frac{\Delta V}{V}\right)^{k s 1}: \text { volumetric solid FP swelling per } 10^{20} \text { fissions } / \mathrm{cm}^{3} \end{aligned}$ |  | 2 |

In the case of IFSWEL=1, the following fitting parameters can be used.

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| FACP | The bubble radius at grain boundary $\bar{a}$ is obtained by the following equation. $P_{\text {in }}=\frac{m}{v} R T=\frac{2 r}{\bar{a}}+P_{o w t}$ <br> Here, $\quad P_{i n}$ : pressure at grain-boundary gas bubble <br> $m$ : gas molar number within 1 bubble <br> $v$ : gas-bubble volume $\left(=\pi h a^{3}\left(1+\frac{h^{2}}{3}\right)\right)$ <br> $R$ : gas constant <br> $T$ : temperature <br> $r$ : surface tension <br> $\bar{a} \quad$ : gas-bubble radius at grain boundary <br> $P_{\text {out }}$ : pressure outside grain-boundary gas bubble. <br> $P_{\text {out }}$ is given as $P_{o u t}=P_{g a s}+P_{f c} \cdot \mathrm{FACP}$ <br> Here, $\quad P_{g a s}:$ plenum pressure <br> $P_{f c}$ : pellet-cladding average contact pressure. <br> Therefore, FACP is a parameter for adjusting pressure external to the grain-boundary gas bubbles. (common to deformation and thermal models) | 1.0 |


|  | MATPRO-Version 09 | Condition | Ref. |
| :---: | :---: | :---: | :---: |
| Temperature at pellet center $\left({ }^{\circ} \mathrm{C}\right)$ | Swelling ratio $\left(\% / 10^{20}\right.$ fiss. $\left./ \mathrm{cm}^{3}\right)$ |  |  |
| $T \leq 1,400$ | 0.28 | IFSWEL=2 | 14 |
| $1,400 \leq T \leq 1,800$ | $0.28[1+0.00575(T-1,400)]$ |  |  |
| $1,800 \leq T \leq 2,200$ | $0.28[3.3-0.004(T-1,800)]$ |  |  |
| $2,200<T$ | 0.476 | Condition | Ref. |
| $\mathrm{UO}_{2}$ swelling $(4)$ | IFSWEL=3 | 44 |  |
| Volumetric swelling ratio: | Halden |  |  |
| $\left(\frac{\Delta V}{V}\right)=0.5 \% /\left(10 \mathrm{MWd} / \mathrm{kg} U O_{2}\right)$ |  |  |  |

(8) Hot pressing of $\mathrm{UO}_{2}$

The flow rule of the yield function is given as follows, including the ( $\mathrm{r}, \mathrm{z}$ ) plane shearing force term used in Section 2.3.

$$
\begin{align*}
& \bar{\sigma}=\left[\frac { 3 } { 2 ( F + G + H ) } \left\{H\left(\sigma_{r}-\sigma_{z}\right)^{2}\right.\right.\left.+F\left(\sigma_{z}-\sigma_{t \theta}\right)^{2}+G\left(\sigma_{\theta}-\sigma_{r}\right)^{2}\right\}  \tag{2.4.1}\\
&\left.+3 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right)^{2}+2 N \tau_{r z}^{2}\right]^{\frac{1}{2}} \\
&\left\{\Delta \varepsilon_{n+1}^{P}\right\}=\Delta \bar{\varepsilon}_{n+1}^{-P}\left\{\frac{\partial \bar{\sigma}}{\partial \sigma}\right\}_{n+\theta} \tag{2.4.2}
\end{align*}
$$

Here, $\alpha$ is the hot-press parameter of pellet.
When isotropy of pellet materials ( $H=F=G=1$ ) is assumed, the following equation holds from eq. (2.4.1).

$$
\begin{equation*}
\frac{\partial \bar{\sigma}}{\partial \sigma_{r}}=\frac{3}{2 \bar{\sigma}}\left\{\frac{2 \sigma_{r}-\sigma_{z}-\sigma_{\theta}}{3}+2 \alpha\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right)\right\} \tag{2.4.3}
\end{equation*}
$$

Therefore,

$$
\left\{\frac{\partial \sigma}{\partial \sigma}\right\}_{n+\theta}=\frac{1}{\bar{\sigma}_{n+\theta}}\left[\begin{array}{cccc}
1+3 \alpha & -0.5+3 \alpha & -0.5+3 \alpha & 0  \tag{2.4.4}\\
1-3 \alpha & -0.5+3 \alpha & 0 \\
& \text { Sym. } & 1+3 \alpha & 0 \\
& & & \frac{2}{3}
\end{array}\right]\left\{\sigma_{n+\theta}\right\}
$$

Substituting eq. (2.4.4) into eq. (2.4.2) and rearranging, we obtain

$$
\left\{\Delta \varepsilon_{n+\theta}^{P}\right\}=\frac{(1+3 \alpha) \Delta \bar{\varepsilon}_{n+1}^{P}}{\bar{\sigma}_{n+\theta}}\left[\begin{array}{rrrr}
1 & -v^{P} & -v^{P} & 0  \tag{2.4.5}\\
& 1 & -v^{P} & 0 \\
& & 1 & 0 \\
& \text { Sym. } & & \frac{2}{3}
\end{array}\right]\left\{\sigma_{n+\theta}\right\}
$$

Here, $\quad v^{p}=\frac{0.5-3 \alpha}{1+3 \alpha}$.

The volume strain increment $\Delta \varepsilon_{h, n+1}^{P}$ due to plasticity is given by

$$
\begin{align*}
\Delta \varepsilon_{h, n+1}^{P} & =\Delta \varepsilon_{n+1}^{P, r}+\Delta \varepsilon_{n+1}^{P, z}+\Delta \varepsilon_{n+1}^{P, \theta} \\
& =\frac{(1+3 \alpha) \Delta \bar{\varepsilon}_{n+1}^{P}}{\bar{\sigma}}\left(1-2 v^{P}\right)\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right)  \tag{2.4.6}\\
& =\frac{9 \alpha \Delta \bar{\varepsilon}_{n+1}^{P}}{\bar{\sigma}}\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right) .
\end{align*}
$$

Since eq. (2.4.6) is also applied in the case of pellet creep, the volume strain increment $\Delta \varepsilon_{h, n+1}^{c}$ by creep is given by

$$
\begin{equation*}
\Delta \varepsilon_{n, n+1}^{c}=\frac{9 \alpha \Delta \bar{\varepsilon}_{n+1}^{P}}{\bar{\sigma}}\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right) \tag{2.4.7}
\end{equation*}
$$

Accordingly, the change in pellet volume strain accompanied by plasticity and creep flow (=hot press), $\Delta \varepsilon_{h, n+1}$, is expressed as follows.

$$
\begin{align*}
\Delta \varepsilon_{n, n+1} & =\Delta \varepsilon_{h, n+1}^{P}+\Delta \varepsilon_{n, n+1}^{c} \\
& =\frac{9 \alpha}{\bar{\sigma}}\left(\Delta \bar{\varepsilon}_{n+1}^{p}+\Delta \bar{\varepsilon}_{n+1}^{c}\right)\left(\sigma_{r}+\sigma_{z}+\sigma_{\theta}\right) \tag{2.4.8}
\end{align*}
$$

Here, porosity $p_{n+1}$ at $(\mathrm{n}+1)$ time step is expresses as

$$
\begin{equation*}
p_{n+1}=p_{1}+\sum_{i=1}^{n+1} \Delta \varepsilon_{h, i}+\sum_{i=1}^{n+1} \Delta \varepsilon_{s w e l}+\sum_{i=1}^{n+1} \Delta \varepsilon_{d e n s} \tag{2.4.9}
\end{equation*}
$$

where $\quad p_{1}$ : initial porosity,
$\Delta \varepsilon_{\text {swel }}$ : swelling strain increment,
$\Delta \varepsilon_{d e n s}$ :densification strain increment.
Hot press of $\mathrm{UO}_{2}$ has the fitting parameter $\alpha$.

| Variable name | Content | Default value |
| :---: | :--- | :--- |
| BETAX <br> $=\alpha$, hot press <br> parameter of <br> $\mathrm{UO}_{2}$ | When IHOT $=0, \mathrm{BETAX}=\alpha$ is fixed at the initial <br> value. <br> When IHOT $=1, \alpha$ is determined as a function of <br> porosity as follows: <br> $\alpha=$ BETAX $\cdot \frac{p_{n+1}}{1-D_{0}}$ | 0.002 (initial value) |
| where $\quad$$p_{n+1}:$ porosity in pellet <br> $D_{0}:$ initial theoretical density ratio. |  |  |

(9) Densification of $\mathrm{UO}_{2}$

The following options can be selected for the equation representing $\mathrm{UO}_{2}$ densification.

| $\mathrm{UO}_{2}$ densification (1) $\quad$ FEMAXI-III | Condition | Ref. |
| :---: | :--- | :--- |
| $\frac{\Delta V}{V}=\frac{\Delta V^{\text {max }}}{V}\left(1-e^{-c \cdot B u}\right)$ |  |  |
| $\frac{\Delta V}{V} \quad:$ volume contraction due to densification | IDENSF=0 | 2 |
| (default value) |  |  |
| $\frac{\Delta V^{\text {max }}}{V}:$ maximum volume contraction due to |  |  |
| $\quad$densification <br> $:$ burnup $\left(\mathrm{MWd} / t-\mathrm{UO}_{2}\right)$ |  |  |

The following fitting parameters are used in the case of IDENSF $=0$.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| DMAX | Maximum volume contraction due to densification <br> $\frac{\Delta V^{\text {max }}}{V} \quad(\%)$ | 1.0 |
| SBU | Burnup of $90 \%$ completion of densification, <br> given by $C=\frac{2.3025}{S B U}, \quad\left(\mathrm{MWd} / \mathrm{t}-\mathrm{UO}_{2}\right)$, <br> where $\exp (-2.3025)=0.1$. | 2500.0 |


| $\mathrm{UO}_{2}$ densification (2) Rolstad | Condition | Ref. |
| :---: | :--- | :--- |
| The upper limit of the dimension change in the axial direction due to |  |  |
| densification is given by |  |  |
| $\frac{\Delta L}{L}=22.2 \times \frac{(100-T D)}{(T S-1180)}$ | IDENSF=1 | 31 |
| $T D:$ theoretical density ratio of $\mathrm{UO}_{2}(\% \mathrm{TD})$ |  |  |
| $T S:$ sintering temperature $\left({ }^{\circ} \mathrm{C}\right)$. |  |  |
| Burnup dependence: |  |  |
| $\frac{\Delta L}{L}=-3.0+0.93 e^{-B U}+2.07 e^{-35 B U}$ |  |  |
| $B U:$ burnup $(\mathrm{GWd} / \mathrm{t}-\mathrm{U})$ |  |  |

Here, the following fitting parameter is used for IDENSF.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| TDNSF | Sintering temperature (K) | 2000.0 |


| $\mathrm{UO}_{2}$ densification (3) NRC | Condition | Ref. |
| :---: | :---: | :---: |
| Density increment due to densification $\Delta \rho\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ : $\left[\begin{array}{ll} \Delta \rho=0 & \left(B U \leq B U_{1}\right) \\ \Delta \rho=m \log (B U)+b & \left(B U_{1}<B U<B U_{2}\right) \\ \Delta \rho=\Delta \rho_{\text {sn }} & \left(B U \geq B U_{2}\right) \end{array}\right.$ <br> $\Delta \rho_{\mathrm{s} n}$ : density increment $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ due to out-of-pile heat treatment $\left(1,700^{\circ} \mathrm{C} \times 24 \mathrm{~h}\right)$ <br> $B U$ : burnup ( $\mathrm{MWd} / \mathrm{t}$ ) <br> $B U_{l}, B U_{2}$ : constants for determining the burnup range; dependent on $\Delta \rho_{\mathrm{sn}}$ <br> $\mathrm{m}, b$ : constants for connecting the three equations for each burnup range | IDENSF=2 | 32 |

The following fitting parameter is used in the case of ISENSF=2.

| Variable name | Content | Default value |
| :--- | :--- | :---: |
| DMAX | Relative density increase (\%) due to out-of-pile heat <br> treatment $\left(1,700^{\circ} \mathrm{C} \times 24 \mathrm{~h}\right)$. | 1.0 |


| $\mathrm{UO}_{2}$ densification (4) Halden | Condition | ref. |
| :---: | :---: | :---: |
| Volumetric decrease by densification is: |  |  |
| $\frac{\Delta V}{V}=-\left[\begin{array}{c}0.01420(1-\exp (-6.7943 \cdot B U)) \\ +0.00793(1-\exp (-1.1434 \cdot B U))\end{array}\right] \cdot A D S T$ | IDENSF=4 | 44 |
| Here,$B U:$ Burnup $\left(\mathrm{MWd} / \mathrm{kgUO}_{2}\right)$ <br> $A D S T:$ adjusting factor $(=0.6)$ |  |  |


| $\mathrm{UO}_{2}$ densification (5) Marlowe | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} & \Delta \rho=\frac{M}{A} \ln \left(1+\frac{A D_{\text {irr }}^{0} \dot{F t}_{t r r}}{G_{0}{ }^{3}}\right) \\ & \Delta \rho: \text { amount of in-pile densification (\%TD) } \\ & M: \text { densification rate constant (\%TD-cm) } \\ & A: \text { grain growth rate constant }(\mathrm{cm}) \\ & D_{\text {irr }}^{0}: \text { irradiation diffusion constant }=1.27 \times 10^{-29}\left(\mathrm{~m}^{3} / \text { fiss. }\right) \\ & \dot{F} \quad\left.: \text { fission rate (fiss. } / \mathrm{cm}^{3} \cdot \mathrm{~s}\right) \\ & t_{\text {irr }}: \text { irradiation time }(\mathrm{s}) \\ & \dot{F}_{t r r}\left.: \text { burnup (fiss. } / \mathrm{cm}^{3}\right) \\ & G_{0}: \text { initial crystal grain size }(\mathrm{cm}) \end{aligned}$ <br> The constants $M$ and $A$ are calculated from the following equation using the results of the out-of-pile heat treatment test, in which a fuel produced in the same batch as the fuel for irradiation is used. $\begin{aligned} & A=\frac{G^{3}-G_{0}{ }^{3}}{D t}, \\ & M=\frac{A \Delta \rho_{t h}}{\ln \left(1+\frac{A D t}{G_{0}{ }^{3}}\right)} \\ & D=D_{0} \cdot \exp (-Q / R T) \\ & G \quad: \text { crystal grain size after heat treatment (cm) } \\ & t \quad: \text { heat treatment time (s) } \\ & \Delta \rho_{t h}: \\ & \begin{array}{l} \text { density change due to heat treatment }(\% \mathrm{TD}) \\ Q \quad: \text { thermal diffusion constant } \quad 2.32 \times 10^{-6}\left(\mathrm{~cm}^{2} / \mathrm{s}\right) \\ R \quad: 82,000 \text { cal } / \text { mol } \\ T \quad \end{array} \quad: \text { gas constant } \quad 1.987(\mathrm{cal} / \mathrm{mol}) \end{aligned}$ | IDENSF=3 | 33 |

The following fitting parameters are used in the case of 1DENSF=3.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| DMAX | degree of in-pile densification (\%TD) | 1.0 |
| GG | crystal grain size after heat treatment $(\mathrm{m})$ | $10^{-5}$ |
| GGO | initial crystal grain size $(\mathrm{m})$ | $8 \times 10^{-6}$ |
| SITIM | heat treatment time $(\mathrm{h})$ | 24.0 |

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## (10) Pellet relocation

The parts of a pellet that is cracked at start-up scatter in the radial direction and consequently the gap is narrowed. This phenomenon is called relocation. In FEMAXI-IV, the initial relocation is assumed to be proportional to the gap width at hot stand-by where burnup is 0 and linear heat rate is 0 , as

$$
\begin{equation*}
R E L=\alpha \cdot\left(r_{c i}^{c}-r_{p i}^{c}\right) \tag{2.4.10}
\end{equation*}
$$

where $r_{c i}^{c}$ and $r_{p i}^{c}$ are the cladding inner radius and pellet radius (cm) at hot stand-by, respectively. $\quad \alpha$ is an empirical parameter which is determined by comparison with experimental data, and is called a relocation parameter.

The fitting parameters for relocation are as follows.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| XRELOC | Relocation parameter $\alpha$ for the thermal model | 0.2 |
| FRELOC | Relocation parameter $\alpha$ for the mechanical model | 0.5 |
| EPSRLZ | Axial relocation strain for the mechanical model | 0.003 |

(11) $\mathrm{UO}_{2}$ plasticity

Equations representing yield stress and the strain hardening parameter (tangent stiffness) are selected from among the following.

| $\mathrm{UO}_{2}$ plasticity (1) Tachibana | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} & \sigma_{Y}= \begin{cases}66.9-0.0397 \cdot T+(520.0-0.386 \cdot T) \cdot \bar{\varepsilon}_{p} & \left(T \leq 1200^{\circ} \mathrm{C}\right) \\ 36.6-0.0144 \cdot T+(1395-0.06875 \cdot T) \cdot \bar{\varepsilon}_{p} & \left(T>1200^{\circ} \mathrm{C}\right)\end{cases} \\ & H^{\prime}= \begin{cases}520.0-0.386 \cdot T & \left(T \leq 1200{ }^{\circ} \mathrm{C}\right) \\ 139.5-0.06875 \cdot T & \left(T>1200^{\circ} \mathrm{C}\right)\end{cases} \\ & \sigma_{Y}: \text { yield stress }\left(\mathrm{kg} / \mathrm{mm}^{2}\right) \\ & H^{\prime}: \text { tangent stiffness }\left(\mathrm{kg} / \mathrm{mm}^{2}\right) \\ & T: \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \end{aligned}$ | IFY=1 <br> (default <br> value) | 34 |
| $\mathrm{UO}_{2}$ plasticity (2) Rodford |  |  |
| $\begin{aligned} & \sigma_{Y}=1176.1-1.688 \cdot T+8.179 \times 10^{-4} \cdot T^{2} \\ &-1.293 \times 10^{-7} \cdot T^{3} \\ & H^{\prime}=0.0: \text { tangential stiffness } \\ & \sigma_{Y}: \text { yield stress }(\mathrm{MPa}) \\ & T: \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \\ & \hline \end{aligned}$ | $\mathrm{IFY}=0$ | * |

(12) $\mathrm{UO}_{2}$ Specific heat

| $\mathrm{UO}_{2}$ specific heat | MATPRO-Version 09 | Condition | Ref. |
| :---: | ---: | :--- | :--- |
| $C_{P}=15.496\left[\frac{K_{1} \theta^{2} \exp (\theta / T)}{T_{2}[\exp (\theta / T)-1]^{2}}+2 K_{2} T+\frac{K_{3} E_{l}}{R T^{2}} \exp \left(-E_{D} / R T\right)\right]$ | no | 14 |  |
| $C_{P}: \mathrm{UO}_{2}$ specific heat $(\mathrm{J} / \mathrm{kg} \cdot \mathrm{K})$ | restrictions |  |  |
| $K_{l}=19.145(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{K})$ |  |  |  |
| $K_{2}=7.8473 \times 10^{-4}\left(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{K}^{2}\right)$ |  |  |  |
| $K_{3}=5.6437 \times 10^{6}(\mathrm{cal} / \mathrm{mol})$ |  |  |  |
| $\theta=535.285(\mathrm{~K}), \quad E_{D}=37,694.6(\mathrm{cal} / \mathrm{mol})$ |  |  |  |
| $T:$ temperature $(\mathrm{K}), \quad R=1.987(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{K})$ |  |  |  |

(13) $\mathrm{UO}_{2}$ grain growth

Equations representing $\mathrm{UO}_{2}$ grain growth are selected from among the following.

| $\mathrm{UO}_{2}$ grain growth Itoh (modified Ainscough) | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} & \frac{d D}{d t}=K\left(\frac{1}{D}-\frac{1+E \cdot N_{f} / N_{f}{ }^{\max }}{D_{m}}\right) \\ & D: \text { grain size at time } t(\mu \mathrm{~m}) \\ & K: \text { rate constant }\left(\mu \mathrm{m}^{2} / \mathrm{h}\right) \\ & K=5.24 \times 10^{7} \exp \left(-2.67 \times 10^{5} / R T\right) \\ & R=8.314(\mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K}), \quad T: \text { temperature (K) } \\ & D_{m}: \text { limit grain size }(\mu \mathrm{m}) \\ & D_{m}=2.23 \times 10^{3} \exp (-7620 / \mathrm{T}) \\ & E: \text { fitting parameter } \\ & \left.N_{f}: \mathrm{FP} \text { gas atom density at grain boundary (atoms } / \mathrm{cm}^{2}\right) \\ & N_{r}{ }^{\text {max }}: \text { saturated value of FP gas atom density at grain boundary } \\ & \text { (atoms } / \mathrm{cm}^{2} \text { ) } \end{aligned}$ | $\left\{\begin{array}{c} \text { IGRAIN }=0 \\ \text { (default } \\ \text { value }) \end{array}\right.$ | 20 |

The fitting parameters in the case of IGRAIN $=0$ are as follows.

| Variable name | Content | Default value |
| :--- | :---: | :--- |
| AG | Fitting parameter E | 1.0 |
| GRWF | The grain growth rate is multiplied by GRWF. | 1.5 |


| $\mathrm{UO}_{2}$ grain growth (2) Ainscough | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} & \frac{d D}{d t}=k\left(\frac{1}{D}-\frac{1+0.002 B}{D_{m}}\right) \\ & D: \text { grain size at time } t(\mu \mathrm{~m}) \\ & t: \text { time }(\mathrm{h}) \\ & k: \text { rate constant }\left(\mu_{\mathrm{m}}{ }^{2} / \mathrm{h}\right) \\ & k=5.24 \times 10^{\prime} \exp \left(-2.67 \times 10^{\circ} / R T\right) \\ & R=8.314(\mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K}) \\ & T: \text { temperature }(\mathrm{K}) \\ & \text { temperature range }: 1,300-1,500^{\circ} \mathrm{C} \\ & B: \text { burnup } \quad(\mathrm{MWd} / \mathrm{U}) \\ & \hline \end{aligned}$ | IGRAIN=1 | 35 |
| $\mathrm{UO}_{2}$ grain growth (3) MacEwan |  |  |
| $\begin{aligned} & D^{2}-D_{0}{ }^{2}=k_{0} 0^{08} \exp (-87,000 / R T) \\ & D: \text { grain size at time } t(\mu \mathrm{~m}) \\ & D_{0}: \text { initial grain size }(\mu \mathrm{m}) \\ & k_{0}: \text { constant of proportionality }\left(\mathrm{k}_{0}=3.9 \times 10^{10}\right) \\ & t \quad: \text { time }(\mathrm{h}) \\ & R: \text { gas constant } \quad 1.987 \quad(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{~K}) \\ & T: \text { temperature }(\mathrm{K}) \\ & \text { temperature range }: 1,555-2,440^{\circ} \mathrm{C} \end{aligned}$ | $\mathrm{IGRAIN}=2$ | 36 |
| $\mathrm{UO}_{2}$ grain growth (4) Lyons |  |  |
| $D^{3}-D_{0}^{3}=k_{0} e^{-Q / R T} \cdot t$ <br> $D$ : grain size at time $t(\mu \mathrm{~m})$ <br> $D_{0}$ : initial grain size ( $\mu \mathrm{m}$ ) <br> $k_{0}$ : rate constant ( $\mu \mathrm{m}^{3} / \mathrm{h}$ ) <br> $Q$ : activation energy required for grain growth (cal/mol) <br> $R=1.987$ ( $\mathrm{cal} / \mathrm{mol} \cdot \mathrm{K}$ ) <br> $T$ : temperature (K) <br> $t$ : time (h) <br> $K_{0}=\exp \left(5.096+2.476 \times 10^{-4} \cdot Q\right)$ <br> For the experimental data obtained by MacEwan, $Q=119,000(\mathrm{cal} / \mathrm{mol})$ | IGRAIN=3 | 37 |
| $\mathrm{UO}_{2}$ grain growth (5) MATPRO-Version 09 |  |  |
| $\begin{aligned} D^{4}-D_{0}{ }^{4}= & 6.18 \times 10^{13.3} e^{-92,400 / R T} \cdot t \\ D & : \text { grain size at time } \mathrm{t}(\mu \mathrm{~m}) \\ D_{0} & : \text { initial grain size }(\mu \mathrm{m}) \\ R & =1.987(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{~K}) \\ T & : \text { temperature }(\mathrm{K}) \\ t & : \text { time }(\mathrm{h}) \end{aligned}$ | IGRAIN=4 | 14 |

(14) FP gas release rate

The FP gas release rates and models are selected from among the following.

| FP gas release rate (1) mechanistic model |  |  |  | Condition | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Refer to section 2.I. 4 (2). <br> Fitting parameters are also explained in section 2.1.4 (2). |  |  |  | $\begin{gathered} \text { IGRASP }=0 \\ \text { (default } \\ \text { value) } \\ \hline \end{gathered}$ |  |
| FP gas release rate (2) temperature-dependent model |  |  |  |  |  |
| $\begin{array}{r} f= \\ =\frac{1}{V} \sum_{i} a_{i} V_{i} \\ V_{1}: \mathrm{UO}_{2} \text { pell } \\ \text { on the basi } \\ \text { length in e } \\ V=\sum_{i} V_{i} \\ a_{i}: \text { release ra } \\ \hline \text { Proposer } \\ \hline \text { R. C. Nelson } \\ \hline \text { Morishima } \\ \hline \text { W. B. Lewis } \\ \hline \text { G. Karsten } \end{array}$ |  | ction is concentrent <br> Data <br> Range <br> $>1,900^{\circ} \mathrm{C}$ <br> $1,650-1,900^{\circ} \mathrm{C}$ <br> $<1,650^{\circ} \mathrm{C}$ <br> $>1,900^{\circ} \mathrm{C}$ <br> $1,650-1,900^{\circ} \mathrm{C}$ <br> $<1,650^{\circ} \mathrm{C}$ <br> $>1,600^{\circ} \mathrm{C}$ <br> $1,300-1,600^{\circ} \mathrm{C}$ <br> $1,000-1,300^{\circ} \mathrm{C}$ <br> $<1,000^{\circ} \mathrm{C}$ <br> $>1,700^{\circ} \mathrm{C}$ <br> $1,300-1,700^{\circ} \mathrm{C}$ <br> $<1,300^{\circ} \mathrm{C}$ | divided into regions $V$, is volume per unit | IGASP=1 (common to all models) <br> (Nelson model) <br> IGAS $=1$ <br> (Morishima model) $\mathrm{IGAS}=2$ <br> (Lewis <br> model) <br> IGAS $=3$ <br> (Karsten <br> model) <br> $\mathrm{IGAS}=4$ | * |

(15) Pellet melting point

| Pellet melting point $\quad$ MATPRO-Version 11 | Condition | Ref. |
| :---: | :--- | :--- |
| $T_{m}=T_{u}-5.414 P+0.007468 P^{2}-0.0032 \mathrm{Bu}$ |  |  |
| $T_{m}:$ pellet melting point $\left({ }^{\circ} \mathrm{C}\right)$ | No | 38 |
| $T_{u}:$ melting point of unirradiated $\mathrm{UO}_{2}$ material $\left(=2,800^{\circ} \mathrm{C}\right)$ | restrictions |  |
| $P:$ molar fraction of $\mathrm{PuO}_{2}(\%)$ |  |  |
| $B u:$ burnup (MWd/t) |  |  |

### 2.4.2 Material properties of cladding

(1) Cladding thermal conductivity

| Zircaloy thermal conductivity MATPRO-Version 09 | Condition | Ref. |
| :---: | :--- | :--- |
| From room temp. to melting point <br> $k=7.51+2.09 \times 10^{-2} T-1.45 \times 10^{-5} T^{2}+7.67 \times 10^{-9} T^{3}$ <br> $k:$ thermal conductivity $(\mathrm{W} / \mathrm{m} \cdot \mathrm{K})$ <br> $T:$ temperature ( K ) | No | 14 |
| $\mathrm{ZrO}_{2}$ (oxide layer) thermal conductivity MATPRO-A | restrictions |  |
| $k=0.835+1.81 \times 10^{-4} \cdot T$ <br> $k: \mathrm{ZrO}_{2}$ thermal conductivity $(\mathrm{W} / \mathrm{m} \cdot \mathrm{K})$ | No <br> restrictions | 39 |

(2) Zircaloy thermal expansion

Regarding thermal expansion of zircaloy, only the axial expansion value is selected from among the following options.

| Zircaloy thermal expansion (1) MATPRO-Version 09 | Condition | Ref. |
| :---: | :---: | :---: |
| For $27-800^{\circ} \mathrm{C}$, <br> thermal expansion in the axial direction (Subcode CATHEX): $\Delta L / L_{0}=-2.506 \times 10^{-5}+4.441 \times 10^{-6} T$ <br> Therefore, thermal expansion coefficient is $\alpha=4.441 \times 10^{-6} .$ <br> thermal expansion in the radial direction (Subcode CDTHEX): $\Delta D / D_{0}=-2.373 \times 10^{-4}+6.721 \times 10^{-6} T$ <br> therefore, $\begin{aligned} \alpha=6.721 & \times 10^{-6} . \\ T & : \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \end{aligned}$ | $\begin{aligned} & \text { ICATHX=0 } \\ & \text { (default } \\ & \text { value) } \end{aligned}$ | 14 |
| Zircaloy thermal expansion (2) Scott |  |  |
| For $21-429^{\circ} \mathrm{C}$, thermal expansion in the axial direction $\begin{aligned} \Delta L / L_{o} & =42.53230+3.96753 T . \\ T & : \text { temperature }\left({ }^{\circ} \mathrm{C}\right) \end{aligned}$ | ICATHX=1 | 14 |

## (3) Young's modulus of cladding

| Young's modulus of Zircaloy | Fisher | Condition |
| :--- | :--- | :--- |
| $E=\left[9.900 \times 10^{5}-566.9 \times(T-273.15)\right] \times 9.8067 \times 10^{4}$ | Ref. |  |
| $E:$ Young's modulus (Pa) | restrictions | 40 |
| $T:$ temperature $(\mathrm{K})$ |  |  |

(4) Poisson's ratio of cladding

| Poisson's ratio of Zircaloy | Fisher | Condition | Ref. |
| :---: | :---: | :--- | :--- |
| $v=0.3303+8.376 \times 10^{-5}(T-273.15)$, | $T:$ temperature (K) | No restrictions | 40 |

(5) Creep of Zircaloy

| Zircaloy creep (1) MATPRO-Version 09 | Condition | Ref. |
| :---: | :---: | :---: |
| In-pile creep equation $\begin{aligned} \dot{\varepsilon}=K \phi( & \left.\sigma+B e^{c \sigma}\right) \exp (-10,000 / R T) t^{-\frac{1}{2}} \\ \dot{\varepsilon} & : \text { biaxial creep strain rate }(\mathrm{m} / \mathrm{m} \cdot \mathrm{~s}) \\ K & =5.129 \times 10^{-29}, \quad B=7.252 \times 10^{2} \\ C & =4.967 \times 10^{-8}, \quad R=1.987(\mathrm{cal} / \mathrm{mol} \cdot \mathrm{~K}) \\ T & : \text { temperature }(\mathrm{K}), \quad t: \text { time }(\mathrm{s}) \\ \phi & : \text { fast neutron flux }\left(\mathrm{n} / \mathrm{m}^{2} \cdot \mathrm{~s}\right) \mathrm{E}>1.0 \mathrm{MeV} \\ \sigma & : \text { circumferential stress }\left(\mathrm{N} / \mathrm{m}^{2}\right) \end{aligned}$ | CRPEQ=0 | 14 |
| Zircaloy creep (2) NENANSEN |  |  |
| In-pile creep equation for Zircaloy-4 : $\begin{equation*} \dot{\varepsilon}^{c}=\dot{\varepsilon}_{t h}^{c}+\dot{\varepsilon}_{i r r}^{c} \tag{1/hr} \end{equation*}$ <br> 1) thermal creep rate: setting thermal creep strain as $\varepsilon_{t h}^{c}=K \cdot t^{m}$, we have the creep rate as: $\dot{\varepsilon}_{t h}^{c}=m K^{\frac{1}{m}} \varepsilon_{H}^{\left(1-\frac{1}{m}\right)}$ <br> where <br> $\varepsilon_{H}\left(=\varepsilon_{t h}^{c}\right)=\sum_{k=1}^{n} \dot{\varepsilon}_{t h, k}^{c} \cdot \Delta t_{k}$ : thermal creep strain by the previous time step(n-1) $\begin{aligned} & K= \exp \left\{-13.3+\left(-0.416+8.22 \times 10^{-4} \mathrm{~T}\right) \sigma_{e q}+6.59 \times 10^{-3} \mathrm{~T}\right\} \\ & m=-1.07+\left(-0.00343+7.27 \times 10^{-5} \mathrm{~T}\right) \sigma_{e q}+1.95 \times 10^{-3} \mathrm{~T} \\ & \sigma_{e q} \text { :equivalent stress }\left(\mathrm{kgf} / \mathrm{mm}^{2}\right) \\ & \quad T \text { :temperature } \quad(\mathrm{K}) \end{aligned}$ <br> 2) irradiation creep rate : (ref. source is unknown) $\dot{\varepsilon}_{i r r}^{c}=6.64 \times 10^{-25} \phi^{123} \sigma_{e q}^{134}$ <br> $\phi$ :fast neutron flux ( $\mathrm{n} / \mathrm{cm}^{2} \mathrm{~s}$ ) | CRPEQ=1 | 15 |

The following fitting parameters are used for the zircaloy creep equation.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| CRFAC | For SR material, the creep strain rate is multiplied by <br> CRFAC. | 1.3 |
| IPUGH | PUGH $=0$ : inversion of Pugh is not taken into account <br> PUGH $=1$ : inversion of Pugh is taken into account | 0 |

Here, Pugh's method of cladding creep inversion caused by stress reversal is explained.
When the direction of stress is reversed during creep, the primary creep occurs again. Pugh proposed a simplified method to simulate this phenomenon ${ }^{(41)}$. An outline of Pugh's method is given as follows.

1) The creep hardening is represented by $\bar{\varepsilon}^{H}$, and

$$
\begin{equation*}
\left\{\dot{\varepsilon}_{c}\right\}=\left\{\frac{\partial \bar{\sigma}}{\partial \sigma}\right\} f\left(\bar{\sigma}, \bar{\varepsilon}^{H}, T\right) \tag{2.4.11}
\end{equation*}
$$

2) At the time of the first stress inversion, $\bar{\varepsilon}^{H}>\hat{\varepsilon}$ and

$$
\begin{equation*}
\hat{\varepsilon}=\varepsilon_{H}, \bar{\varepsilon}^{H}=0 \tag{2.4.12}
\end{equation*}
$$

is set.
3) At the time of the second or later inversions,
when $\bar{\varepsilon}^{H} \geq \hat{\varepsilon}$, then $\hat{\varepsilon}=\bar{\varepsilon}^{H}=0, \quad \bar{\varepsilon}^{H}=0$ is set, and when $\bar{\varepsilon}^{H}<\hat{\varepsilon}$, then $\bar{\varepsilon}^{H}=\hat{\varepsilon}-\bar{\varepsilon}^{H} \quad$ is set.

Figure 2.36 shows the above states.


Fig. 2.43 Inversion of creep strain due to stress inversion.
Here, the stress inversion is judged as follows. Since the equation for the creep is

$$
\begin{equation*}
\left\{\dot{\varepsilon}_{c}\right\}=\left\{\frac{\partial \bar{\sigma}}{\partial \sigma}\right\} f\left(\bar{\sigma}, \bar{\varepsilon}^{H}, T\right), f \geq 0 \tag{2.4.13}
\end{equation*}
$$

whether or not the sign of $\left\{\dot{\varepsilon}_{c}\right\}$ is reversed between the previous time step and the current time step is used for the judgment. In a multi-axial state, the judgment of sign reversal is performed using a scalar product of the component of $\left\{\dot{\varepsilon}_{c}\right\}$.
(6) Zircaloy plasticity

| Zircaloy strain-hardening curve $\quad$ FEMAXI $=$ III | Condition | Ref. |
| :---: | :--- | :--- |
| $\sigma=K \varepsilon^{n}$ |  |  |
| $\sigma:$ true stress $\left(\mathrm{kg} / \mathrm{mm}^{2}\right), \quad \varepsilon:$ true strain | No |  |
| $n:$ strain-hardening exponent | restrictions | 2 |
| $K=K_{0.2 \%}\left(\frac{\sigma_{y}}{E}+0.002\right)^{-n}$ |  |  |
| $K_{0.2 \%}=\sigma_{y}+33.44(1-\exp (-B \phi t))^{\frac{1}{2}} \quad\left(\mathrm{~kg} / \mathrm{mm}^{2}\right)$ |  |  |
| $B=2.92 \times 10^{-21} \exp \left(1-1.6 \times 10^{-14} \phi\right)$ |  |  |
| $\phi:$ fast neutron flux $\left(\mathrm{n}^{2} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$ | $\mathrm{E}>1 \mathrm{MeV}$ |  |
| $\sigma_{y}=$ yield stress $\left(\mathrm{kg} / \mathrm{mm}^{2}\right)$ |  |  |
| $=21.60-0.0213 \cdot \mathrm{~T}($ recrystallized material $)$ |  |  |
| $=31.32-0.0213 \cdot \mathrm{~T}$ (stress-relieved material) |  |  |
| $n=0.0504+0.0001435 \cdot \mathrm{~T}$ |  |  |
| $T:$ temperature $\left({ }^{\circ} \mathrm{C}\right)$ | $220 \leq T \leq 450^{\circ} \mathrm{C}$ |  |

The following parameter is used for the Zircaloy strain-hardening curve.

| Variable name | Content | Default value |
| :--- | :--- | :---: |
| ISTR | In the case of $\operatorname{ISTR} \neq 0, K=\sigma_{y}+33.44$ is set. | 0 |

(7) Zircaloy irradiation growth

The equation representing Zircaloy irradiation growth is selected from among the following.

| Zircaloy irradiation growth $(1)$ | MATPRO-Version 09 | Condition |
| :---: | :--- | :--- |
| $\frac{\Delta L}{L}=A[\exp (240.8 / T)][\phi t]^{1 / 2}\left[1-3 f_{Z}\right][1+2.0 C W]$ |  |  |
| $\frac{\Delta L}{L}:$ irradiation growth $(-)$ | ICAGRW=1 | 14 |
| $A=1.407 \times 10^{-16}\left(\mathrm{n} / \mathrm{m}^{2}\right)^{-1 / 2}$ |  |  |
| $T:$ temperature $(\mathrm{K})$ |  |  |
| $\phi t:$ fast neutron fluence $\left(\mathrm{n} / \mathrm{m}^{2}\right)(\mathrm{E}>1 \mathrm{MeV})$ |  |  |
| $f_{z}:$ factor in the axial direction |  |  |
| $C W:$ cold work |  |  |

The following parameters are used in the case of ICAGRW $=1$.

| Variable name | Content | Default value |
| :--- | :--- | :--- |
| CATEXF | Factor in the axial direction $f_{z}$ | 0.05 |
| COLDW | Cold work CW | 0.81 |


| Zircaloy irradiation growth (2) Manzel | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} \frac{\Delta L}{L_{0}}= & 0.1\left(\phi \cdot t / 10^{21}\right)^{n} \\ & \frac{\Delta L}{L_{0}}: \text { irradiation growth (\%) } \\ & \phi \cdot t: \text { fast neutron fluence }\left(\mathrm{n} / \mathrm{cm}^{2}\right) \\ & n \quad: \text { constant between } 0.65-0.67(0.66 \text { is used }) \end{aligned}$ | ICAGRW=2 | * |
| Zircaloy irradiation growth (3) Hanerz |  |  |
| $\begin{aligned} & \left(\frac{\Delta L}{L_{o}}\right) \perp c=6 \times 10^{-12}(\phi t)^{0.4} \\ & \left(\frac{\Delta L}{L_{o}}\right) \perp c: \text { growth of single crystal in the direction perpendicular to } \\ & \quad \text { the } \mathrm{C} \text { axis. }(-) \\ & \phi \cdot t: \text { fast neutron fluence }\left(\mathrm{n} / \mathrm{cm}^{2}\right) \end{aligned}$ | ICAGRW=3 | * |
| Zircaloy irradiation growth (4) Hesketh | Condition | Ref. |
| $\begin{aligned} & \frac{\Delta L}{L_{o}}= A \cdot \sqrt{\phi \cdot t} \\ & \frac{\Delta L}{L_{o}}: \text { irradiation growth }(-) \\ & \phi \cdot t: \text { fast neutron fluence }\left(\mathrm{n} / \mathrm{cm}^{2}\right) \\ & A \quad: \text { fitting constant }\left(=5 \times 10^{-14}\right) \end{aligned}$ | ICAGRW=4 | 42 |

(8) Zircaloy specific heat

| Zircaloy specific heat | MATPRO-Version 09 | Condition |
| :---: | :--- | :--- |
| $C p=245.11+0.15558 T-3.3414 \times 10^{-5} T^{2}$ |  |  |
| $C p:$ specific heat $(\mathrm{J} / \mathrm{kg} \cdot \mathrm{K})$ | No restrictions | 14 |
| $T:$ temperature $(\mathrm{K})(300-1090 \mathrm{~K})$ |  |  |

(9) Zircaloy density

| Zircaloy density | MATPRO-Version 09 | Condition |
| :---: | :--- | :---: |
| $\rho=6.55\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$ | Ref. |  |

(10) Zircaloy cladding corrosion

| Cladding corrosion rate $\quad$ EPRI | Condition | Ref. |
| :---: | :---: | :---: |
| Pre-transition corrosion rate $: d S / d t=\left(A / S^{2}\right) \exp \left(-Q_{1} / R T\right)$ |  |  |
| Post-transition corrosion rate $: d S / d t=C \exp \left(-Q_{2} / R T\right)$, |  |  |
| $C=C 0+U(M \phi)^{P}$ |  |  |
| Oxide layer thickness at transition : $D \exp \left(-Q_{3} / R T-E T\right)$ |  |  |
| $d S / d t:$ corrosion rate $(\mu \mathrm{m} /$ day $)$ |  |  |
| $S:$ oxide layer thickness $(\mu \mathrm{m})$ |  |  |
| $T:$ temperature at oxide-metal interface (K) |  |  |
| $\phi:$ fast neutron flux $\left(\mathrm{n} / \mathrm{cm}^{2} \mathrm{~s}\right)$ |  |  |
| $R:$ gas constant $(1.987 \mathrm{cal} / \mathrm{mol} \quad \mathrm{K})$ |  |  |
| $A=6.3 \times 10^{9}\left(\mu \mathrm{~m}^{3} / \mathrm{day}\right)$ | $Q_{1}=32289(\mathrm{cal} / \mathrm{mol})$ |  |
| $C_{0}=8.04 \times 10^{7}(\mu \mathrm{~m} / \mathrm{day})$ | $U=2.59 \times 10^{8}(\mu \mathrm{~m} / \mathrm{day})$ |  |
| $M=7.46 \times 10^{-15}\left(\mathrm{~cm}^{2} \mathrm{~s} / \mathrm{n}\right)$ | $\mathrm{P}=0.24$ |  |
| $Q_{2}=27354(\mathrm{cal} / \mathrm{mol})$ | $D=2.14 \times 10^{7}(\mu \mathrm{~m})$ |  |
| $Q_{3}=10763(\mathrm{cal} / \mathrm{mol})$ | $E=1.17 \times 10^{-2}\left(\mathrm{~K}^{-1}\right)$ |  |

### 2.4.3 Other material properties

(1) Gap thermal conduction

The gap conductance model is selected from among the following.

| Gap conductance (1) Ross and Stoute | Condition | Ref. |
| :---: | :---: | :---: |
| Refer to section 2.1.2. Here, thermal conductivities of helium, nitrogen, krypton and xenon are as follows:(MAPRO-Version 09) $\begin{aligned} & K_{H t}=3.366 \times 10^{-3} T^{0.668} \\ & K_{N_{2}}=2.091 \times 10^{-3} T^{0.846} \\ & K_{K_{r}}=4.726 \times 10^{-5} T^{0.923} \\ & K_{\text {Xe}}=3.366 \times 10^{-5} T^{0.872} \end{aligned}$ <br> K : thermal conductivity ( $\mathrm{W} / \mathrm{m} \cdot \mathrm{K}$ ) <br> T : temperature (K) | IGAPCN=0 <br> (default value) | 13 |
| Gap conductance (2) MATPRO-Version 09 |  |  |
|  | $\mathrm{IGAPCN}=1$ | 14 |


| $\begin{aligned} \text { when } x & >600 \mathrm{MWd} / \mathrm{t}-\mathrm{U}, \\ a_{1} & =100-98 F^{\prime} \\ a_{2} & =4-0.5 F^{\prime} \\ F^{\prime} & =1-\frac{1}{\left(\frac{x-600}{1000}\right)^{4}+1} \\ \text { when } x & \leq 600 \mathrm{MWd} / \mathrm{t}-\mathrm{U}, \\ a_{1} & =100 \\ a_{2} & =4 \end{aligned}$ |  |  |
| :---: | :---: | :---: |
| Gap conductance (3) Ross and Stoute |  |  |
| $\begin{aligned} & h_{g a p}=h_{g}+h_{s} \\ & h_{g a p}: \text { gap conductance }\left(\mathrm{W} / \mathrm{cm} \cdot{ }^{\circ} \mathrm{C}\right) \\ & h_{g}: \text { non-contact gap conductance }\left(\mathrm{W} / \mathrm{cm}^{2} \cdot{ }^{\circ} \mathrm{C}\right) \\ & h_{s}: \text { contact gap conductance }\left(\mathrm{W} / \mathrm{cm}^{2} \cdot{ }^{\circ} \mathrm{C}\right) \\ & h_{g}=\frac{K_{g}}{C\left(R_{1}+R_{2}\right)+\left(g_{1}+g_{2}\right)+\Delta r} \\ & K_{g}: \text { gap gas thermal conductivity }\left(\mathrm{W} / \mathrm{cm}^{2} \cdot{ }^{\circ} \mathrm{C}\right) \\ & \quad \mathrm{He}: 0.0021, \mathrm{Ar}: 0.00029, \quad \mathrm{Kr}: 0.0001 \end{aligned}$ <br> $C$ : constant for contact pressure $\begin{array}{ll} C=2.5 & \text { for } 100 \mathrm{kgf} / \mathrm{cm}^{2} \\ C=1.5 & \text { for } 500 \mathrm{kgf} / \mathrm{cm}^{2} \end{array}$ <br> $R_{1}$ and $R_{2}$ : surface roughness of pellet and cladding (cm) $g_{1}$ and $g_{2}$ : temperature jump distance ( cm ) <br> $\mathrm{He}: 10 \times 10^{-4}, \mathrm{Ar}: 5 \times 10^{-4}, \mathrm{Kr}: 1 \times 10^{-4}$ <br> $\mathrm{Xe}:<1 \times 10^{-4} \quad$ (value of $g_{1}+g_{2}$ ) <br> $\Delta r$ : hot gap width (cm) $h_{s}=\frac{K_{m} \cdot P}{a \cdot H}$ $\begin{aligned} K_{m} & =\frac{2 K_{1} \cdot K_{2}}{K_{1}+K_{2}} \\ P & =\frac{2 t \cdot Y_{s}}{I D} \\ a & =a_{0} \sqrt{R} \\ R & =\sqrt{\frac{1}{2}\left(R_{1}^{2}+R_{2}^{2}\right)} \end{aligned}$ <br> $K_{1}$ and $K_{2}$ : thermal conductivities of pellet and cladding <br> (W/cm • ${ }^{\circ} \mathrm{C}$ ) $\left.\begin{array}{l} K_{1}=0.038 \\ K_{2}=0.14 \end{array}\right\} K_{m}=0.05977$ | $\mathrm{IGAPCN}=2$ | 13 |



The following fitting parameter is used in the case of IGAPCN $=0$ or 2.

| Variable name | Contents | Default value |
| :---: | :---: | :---: |
| R1 | Pellet surface roughness $(\mu \mathrm{m})$ | 1.0 |

(2) Cladding surface heat transfer

| Cladding surface heat transfer (1) Jens-Lottes | Condition | Ref. |
| :---: | :---: | :---: |
| Used for the two-phase state. $\begin{aligned} & h_{W}= 0.1263 \cdot \exp \left(\frac{P_{W}}{6.201 \times 10^{6}}\right) q_{s}^{0.75} \\ & h_{W}: \text { surface heat transfer coefficient }\left(\mathrm{W} / \mathrm{cm}^{2} \cdot \mathrm{~K}\right) \\ & P_{W}: \text { coolant pressure }\left(\mathrm{N} / \mathrm{m}^{2}\right) \\ & q_{s}: \text { heat flux of cladding outer surface }\left(\mathrm{W} / \mathrm{cm}^{2}\right) \\ & \hline \end{aligned}$ | No restrictions | 11 |
| Cladding surface heat transfer (2) Dittus-Boelter |  |  |
| Used for the subcool state: $\begin{aligned} h_{W}= & 0.023 \frac{k}{D e}\left(\frac{D e V \rho}{\mu}\right)^{0.2} \cdot\left(p_{r}\right)^{0.4} \\ h_{W} & : \text { surface heat transfer coefficient }\left(\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right) \\ k & : \text { coolant thermal conductivity }\left(\mathrm{W} / \mathrm{m}^{2} \cdot \mathrm{~K}\right) \\ D e & : \text { equivalent diameter }(\mathrm{m}) \\ V & : \text { coolant velocity }(\mathrm{m} / \mathrm{s}) \\ \rho & : \text { coolant density }\left(\mathrm{kg} / \mathrm{m}^{3}\right) \\ \mu & : \text { coolant viscosity }(\mathrm{kg} / \mathrm{m} \cdot \mathrm{~s}) \\ p_{r} & : \text { Prandtl number } \end{aligned}$ | No restrictions | 10 |

The following fitting parameter is used for cladding surface heat transfer.

| Variable name | Content | Default value |
| :--- | :---: | :---: |
| AKFAC | Cladding surface heat transfer coefficient is multiplied by <br> AKFAC. | 1.0 |

(3) FP gas diffusion constant

| FP gas diffusion constant Turnbull | Condition | Ref. |
| :---: | :---: | :---: |
| $\begin{aligned} & D=7.6 \times 10^{-10} \exp \left(-7 \times 10^{4} / R T\right)+S^{2} j v V \div 2 \times 10^{-40} F\left(\mathrm{~m}^{2} / \mathrm{s}\right) \\ & R: \text { gas constant }=1.987(\mathrm{cal} / \mathrm{mol} / \mathrm{K}) \\ & T: \text { temperature }(\mathrm{K}) \\ & S: \text { atom jump distance }=\Omega^{\frac{2}{3}} \\ & \Omega: \text { atom volume }=4.09 \times 10^{-29}\left(\mathrm{~m}^{3}\right) \\ & j v=10^{13} \exp \left(-5.52 \times 10^{4} / R T\right) \\ & V=\frac{\left(\partial_{s} S^{2}+Z V_{o}\right)}{2 Z}\left[\left(1+\frac{4 K^{\prime} Z}{j v\left(\partial_{s} S^{2}+Z V_{o}\right)^{2}}\right)^{\frac{1}{2}}-1\right] \\ & \partial_{s}=10^{15}\left(\mathrm{~m}^{-2},\right. \text { sink intensity) } \\ & Z=2 \quad \text { (number of lost points) } \\ & K^{\prime}=10^{4} \text { (loss ratio per atom) } \\ & V_{0}=\exp \left(-5.52 \times 10^{4} / R T\right) \\ &\left.F=10^{19} \text { (fissions } / \mathrm{m}^{3} \cdot \mathrm{~s}, \text { fission rate }\right) \\ & \hline \end{aligned}$ | $\mathrm{IGASP}=0$ | 19 |

(4) $\mathrm{He}-\mathrm{Xe}$ gas counter diffusion constant

| He-Xe gas counter diffusion constant | Present | Condition |
| :---: | :--- | :--- |
| $D^{12}=\frac{3}{8}\left(\frac{\pi k T}{2 m^{*}}\right)^{\frac{1}{2}} \frac{1}{n \pi d_{12}^{2}}\left(\mathrm{~m}^{2} / \mathrm{s}\right)$ | Ref. |  |
| $m^{\prime}=\frac{m_{1} m_{2}}{m_{1}+m_{2}}(m$ : weight of 1 molecule $)$ | no |  |
| $d_{12}=\frac{1}{2}\left(d_{1}+d_{2}\right)(d:$ diameter of molecule $)$ |  |  |
| $=3.45 \times 10^{-10}(\mathrm{~m})$ |  |  |
| $n=n_{1}+n_{2}($ molecular density $)$ |  |  |
| $k:$ Boltzmann's constant $\left(=1.380 \times 10^{-16} \mathrm{erg} / \mathrm{K}\right)$ |  |  |
| $T:$ temperature $(\mathrm{K})$ |  |  |

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## Appendices

A1 Input Manual
A2 Input Manual for Plotter
A3 (1) Subroutine List
(2) Subroutine Tree

## A4 Sample Input/Output List

A1 Input Manual

| Card No. | SYMBOL (FORMAT) |  |
| :---: | :---: | :---: |
| 1 | MTITL(I), $\mathrm{I}=1,20$ | Free title |
| 2 | ¥INPUT $¥ \mathrm{END}$ | Free parameter |
|  | Calculation parameter is designated by "Name List". |  |
| 3 | NAX, IFEM1, IPLANT (3110) | Fuel rod specifications |
|  | NAX = number of axial segments ( $1 \leq$ NAX $\leq 12$ ) <br> IFEM = the objective segment number ( $1 \leq$ IFEMI $\leq$ NAX ) <br> IPLANT $=1 \cdots \cdots$ in the case of Halden reactor (BWR) <br> $=2 \cdots \cdots$ in the case of other BWR <br> $=3 \cdots \cdots$ in the case of PWR |  |
| 4 | MRASA, CDIN, CDOUT (110,2F10.0) | ladding specifications |
|  | $\begin{aligned} \text { MRASA } & =0 \cdots \cdots \text { RA material } \\ & =1 \cdots \cdots \text { SR material } \\ & =1 \\ \text { CDIN } & =\text { cladding inner diameter }(\mathrm{cm}) \\ \text { CDOUT } & =\text { cladding outer diameter }(\mathrm{cm}) \end{aligned}$ |  |
| 5 | The number of NAX required $(I=1, N A X)$ IDISH(I), ICHAM(I), PDIN(I), PDIA(I), PLENG(I), ENR(I), FDENI(1), DZ(I) (2110,6F10.0) | Pellet specifications |
|  | Number of radial ring elements of a pellet is fixed at 5 in local mechanical analysis, and at 10 in entire rod length mechanical analysis.```\(\operatorname{IDISH}(\mathrm{I})=0 \cdots \cdots\) pellet without dish \(=1 \cdots \cdots\) pellet with dish on only one side \(=2 \cdots \cdots\) pellet with one dish each side \(\operatorname{ICHAM}(\mathrm{I})=0 \cdots \cdots\) pellet without chamfer \(=1 \cdots \cdots\) pellet with chamfer \(\operatorname{PDIN}(\mathrm{I})=\) pellet center hole diameter \((\mathrm{cm})\) PDIA (I) \(=\) pellet diameter (cm) PLENG(I) = length of one pellet \((\mathrm{cm})\) ENR ( I\()=\mathrm{U}-235\) enrichment \((-)\) \(\operatorname{FDENI}(\mathrm{I})=\) pellet theoretical density ratio \((-)\) DZ (I) \(=\) axial segment length \((\mathrm{cm})\)``` |  |
| 6 | Input only when IDISH $=1$ or 2 | Dish specifications |
|  | DISH, DEPTH, DISHB (3F10.0) |  |
|  | DISH = dish diameter (cm) <br> DEPTH $=$ dish depth $(\mathrm{cm})$ <br> DISHB $=$ dish bottom diameter (cm) |  |
| 7 | Input only when ICHAM =1  <br> CHAMR,  <br> (2F10.0) CHAMZ | Chamfer specifications |
|  | CHAMR = chamfer width (cm) <br> CHAMZ $=$ chamfer depth (cm) |  |
| 8 | $\begin{aligned} & \text { PLENUM(2), GPIN, (GMIXO(I), I=1,4), } \\ & \text { PWEIT, PLENUM(1) }(8 \mathrm{~F} 10.0) \\ & \hline \end{aligned}$ | Plenum specifications |
|  | ```PLENUM(2) = upper plenum volume ( \(\mathrm{cm}^{3}\) ) GPIN \(\quad=\) initial gas pressure ( MPa ) GMIXO(I) \(=\) initial gas composition (-) \(\mathrm{i}=1 \cdots \mathrm{He}, \mathrm{i}=2 \cdots \mathrm{~N}_{2}, \mathrm{i}=3 \cdots \mathrm{Kr}, \mathrm{i}=4 \cdots \mathrm{Xe}\) PWEIT = pellet total weight (g) PLENUM \((1)=\) lower plenum volume \(\left(\mathrm{cm}^{3}\right)\)``` |  |


| Card No. | SYMBOL (FORMAT) |  |
| :---: | :---: | :---: |
| 9 | NHIST (I10) | History point number |
|  | Input NHIST > 1 <br> NIST sets consisting of cards 10 and 11 are input. |  |
| 10 | A $1, ~ B 1, ~ A 2, ~ A 5, ~ A 3, ~ A 4, ~ I T, ~ I P, ~ I S, ~ A 6 ~$ <br> $(6 \mathrm{~F} 10,315, ~ F 5.0) ~$ | History point data |
|  | ```\(\mathrm{Al}=\) time (Hour) \(\mathrm{BI}=\operatorname{burnup}\left(\mathrm{MWd} / \mathrm{tUO}_{2}\right) \quad(\mathrm{IBUNP}=0)\) \(\mathrm{MWd} / \mathrm{t} \mathrm{U} \quad(\mathrm{IBUNP}=1)\) \(\mathrm{GJ} / \mathrm{kgU} \quad(\mathrm{IBUNP}=2)\) A2 \(=\) linear heat rate \((\mathrm{W} / \mathrm{cm})\) \(\mathrm{A} 5=\) fast neutron flux \(\left(\mathrm{n} / \mathrm{cm}^{2}-\mathrm{s}\right)\) \(\mathrm{A} 3=\) coolant temperature \((\mathrm{K})\) \(\mathrm{A} 4=\) coolant pressure (MPa) IT \(=0\) : time (or burnup) represents the increment from the time step set at \(\mathrm{IT}=-100\) (when \(\mathrm{IT}=-100\) is not set, it represents the time (or burnup) elapsed from the initial time). \(=-100\) time increment from the previous time step (or burnup increment) \(=100\) cancellation of the \(\mathrm{IT}=-100\) setting (time or burnup represents the time (or burnup) that elapsed from the initial time). IP \(=0 \quad\) history point without output, \(=1\) history point with output IS \(=0 \quad\) no gas flow calculation: instantaneous mixing, \(=1\) gas flow calculation; gives \(\Delta t_{2}\) restriction (see 2.1.6) A6 \(=\) coolant velocity ( \(\mathrm{m} / \mathrm{s}\) ) ( \(\mathrm{ICLMAS}=0\) ), coolant mass flow rate ( \(\mathrm{kg}^{2} / \mathrm{cm}^{2} \mathrm{~s}\) ) (ICLMAS \(=1\) ). Here, either AI (time) or BI (burnup) is designated. If both are designated, B1 is neglected. Also, input of IS is not necessary, since it is automatically set in the program when IAUTO \(=1\).``` |  |
| 11 | $(\mathrm{RH}(\mathrm{I}, \mathrm{l}=1,12), 11$ | $\left\lvert\, \begin{aligned} & \text { Relative power profile in } \\ & \text { the axial direction }\end{aligned}\right.$ |
|  | $\mathrm{RH}(\mathrm{I})=$ relative power of axial segment $\mathrm{j}(-) \quad$ (number of data: NAX ) <br> II = number of history points at which similar relative power is input. <br> When II is designated as 2 or higher, card 11 is omitted for the input of later time step II-1. |  |
| 12 | $\mathrm{BU},(\mathrm{RRH}(\mathrm{I}, \mathrm{I}=\mathrm{l}, 10) \quad$ (F10.0, 10F5.0) | Relative power profile in the radial direction |
|  | Input only when IFLX $>0$BU $=$ burnup (unit is similar to that in card 10)RRH(I) $=$ relative power profile of concentric ring element I ( - )The input number is designated by IFLX in NAMELIST. |  |
| 13 | IEND (A4) | End-of-input card |
|  | Input "STOP". |  |

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Variables set by NAMELIST I

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| Input option |  |  |
| IBUNP | Designation of unit of burnup ( $\left.=0: \mathrm{MWd} / \mathrm{tUO}{ }_{2},=1: \mathrm{MWd} / \mathrm{UU},=2: \mathrm{GJ} / \mathrm{kgU}\right)$ | 0 |
| IDAY | Designation of unit of time ( $=0: \mathrm{hr},=1:$ day $)$ | 0 |
| IFLX | Number of power history points to designate the radial power profile ( $=0$ : Robertson model) | 0 |
| IRH | Interpolation option of axial power profile <br> ( $=0$ : the profile at omitted input points is the same as that in the previous stage, <br> $=1$ : linear interpolation in terms of burmup is performed for omitted input points) | 0 |
| PWCHG | Input heat generation rate is multiplied by ( $1+\mathrm{PWCHG}$ ). | 0.0 |
| FAIW | Fast neutron flux per unit $\left.W / \mathrm{cm}^{(\mathrm{n}} / \mathrm{cm}^{2}-\mathrm{s} / \mathrm{W} / \mathrm{cm}\right)$ <br> (Fast neutron flux data can be omitted if power history data is input) | 0.0 |
| BSBUNP | Initial burnup at the start of calculation ( $\mathrm{MWd} / \mathrm{tUO} 2)$ | 0.0 |
| ICLMAS | Coolant unit option: <br> $(=0$ : flow rate is input in velocity $(\mathrm{m} / \mathrm{s}), \quad=1$ : flow rate is input in mass flow rate $\left(\mathrm{kg} / \mathrm{cm}^{2} \mathrm{~s}\right)$ | 0 |
| Calculation option |  |  |
| IFEMRD | $\begin{aligned} \text { Calculation option } & (=0: \text { local mechanical analysis (II), } \\ & =1: \text { entire-length fuel rod mechanical analysis (I)) } \end{aligned}$ |  |
| INPCK | Input check option ( $=0$; normal calculation, $=1$ : input check only) | 0 |
| ICKI | Temperature calculation option (= $0:$ normal calculation, $=1:$ temperature calculation only) | 0 |
| ICHI | Elasticity calculation ( 0 : normal calculation, $=1$ : elasticity calculation only) | 0 |
| MPP | FP release calculation option $(=0$ : normal calculation, $=1$ : no calculation at points at which axial power profile does not change) | 0 |
| TLIM | Truncation control of CPU time (When the execution time reaches TLIM (s), the calculation is terminated.) | 20000.0 |
| Time step control |  |  |
| IAUTO | Automatic time step control option <br> IAUTO $=0$ : designation of IS input is effective for each input history point. <br> IAUTO $=1$ : 'IS=1' is automatically designated for all input history points. | 1 |
| DPXX | Power increment width per unit time step (W/cm) | 10.0 |
| DPBU | Burnup increment width per unit time step ( $\mathrm{MWd} / \mathrm{UUO}_{2}$ ) | 500 |
| IPH | When DPXX and DPBU control is performed at the objective segment (IFEM), $\mathrm{IPH}=0$; when it is at the segment with max. power, $\mathrm{IPH}=1$. | 0 |
| EFCOEF | Time step width determination factor due to creep $\Delta t=\frac{\bar{\sigma}}{E \cdot \dot{\dot{\varepsilon}}_{c}} \cdot \mathrm{EFCOEF}$ <br> where $\bar{\sigma}$ is equivalent stress, $E$ is Young's modulus and $\dot{\bar{\varepsilon}}_{c}$ is equivalent creep strain rate. | 1.0 |
| LCMAX | Maximum number of judgments of clogged or sliding state of the contact between pellet and cladding. | 3 |
| LMAX | Number of iterations in the Newton-Raphson method for deformation calculation | 2 |
| ITIMY | Time step control option for elasicity/plasticity judgment ( $=-1$ : without time step control, $=0$ : time step control is performed only upon the removal of load, $=1:$ with time step control) | -1 |

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Variables set by NAMELIST 2

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| Calculation condition |  |  |
| AY | Tilting of the pellet upper surface; in the case of dished pellet, $\mathrm{AY}=0$ ( cm ) | 0.002 |
| TROOM | Room temperature, or fuel rod initial temperature (K) | 291.15 |
| ITIME | Option to change the plenum gas pressure (input the history point number) | 3*0 |
| GASPRN | Plenum gas pressure at history point of ITIME (MPa) | 3*0.0 |
| PLENM | Plenum volume at history point of ITIME ( $\mathrm{cm}^{3}$ ) | 3*0.0 |
| GMIXN | Gas composition at history point of ITIME (-) (1:He, 2: $\left.\mathrm{N}_{2}, 3: \mathrm{Kr}, 4: \mathrm{Xe}\right)$ | 12*0.0 |
| GAPLK | Minimum gap width at which axial force is generated ( $\mu \mathrm{m}$ ) | 3.0 |
| XKSU | Upper plenum spring constant (N/m) | 1500.0 |
| ALSU | Upper plenum spring thermal expansion coefficient (1/K) | $1.5 \times 10^{-5}$ |
| XKSL | Lower plenum spring constant ( $\mathrm{N} / \mathrm{m}$ ) | 2500.0 |
| ALSL | Lower plenum spring thermal expansion coefficient (1/K) | $1.5 \times 10^{-5}$ |
| AMU | Friction coefficient between pellet and cladding | 0.4 |
| DE | Equivalent diameter of coolant channel (cm) | 0.0 |
| FAREA | Cross sectional area of coolant channel ( $\mathrm{cm}^{2}$ ) | 0.0 |
| PITCH | Pitch between fuel rods (cm) | I. 3 |
| Thermal conductivity option |  |  |
| IPTHCN | ```Option for equation of pellet thermal conductivity (=1:MATPRO-09, =2: Washington, =3: Hirai, =4: Halden, =5: Modified Hirai(EXBURN), =6: Forsberg, =7: Kjaer-Pedersen)``` | 0 |
| MOX | When MOX $=1$ is set, Martin's thermal conductivity equation for MOX fuel is used. | 0 |
| PU | $\mathrm{PuO}_{2}$ weight ratio (-) | 0.0 |
| Y | Value of y in $\mathrm{MO}_{2-y}$ | 0.0 |
| IGD | When IGD = 1 is set, Fukushima's thermal conductivity equation that includes the effect of gadolinia is used. | 0 |
| GD | $\mathrm{Gd}_{2} \mathrm{O}_{3}$ concentration (wt. frac.) | 0.0 |
| Thermal expansion option |  |  |
| IPTHEX | Option for equation representing material properties of pellet thermal expansion. $\begin{aligned} =0 \text { or } & =1: \text { MATPRO- } 09,=2: \text { Burdick, } \\ & =3: \text { Halden, } \quad=4: \text { Conway } \end{aligned}$ | 0 |
| ICATHX | Option for equation representing material properties of cladding thermal expansion. $=0:$ MATPRO-09, $=1:$ Scott | 0 |
| DTPL | Temperature difference between plenum and coolant temperature (K) | 25.0 |
| Creep option |  |  |
| FCRFAC | Magnification factor for pellet creep equation (deformation model) | 10.0 |
| TCS | Cut-off value of temperature in pellet creep calculation (deformation model) (K) | 2073.15 |
| TCRMX | Cut-off value of temperature in pellet creep calculation (thermal model) (K) | 1773.15 |
| CRFAC | Magnification factor for cladding creep rate (deformation model) | 1.0 (RA material) <br> 1.3 (SR material) |
| TCCRC | Magnification factor for cladding creep rate (thermal model) | 1.0 |
| FAIMAX | Upper limit value of fast neutron flux for calculation of cladding creep rate ( $\mathrm{n} / \mathrm{cm}^{2} \mathrm{~s}$ ) | $10^{14}$ |
| CRPEQ | Option for creep equation of cladding; $=0: M A T P R O-09, \quad=1$ : NENANSEN equation for Zircaloy-4. | 0 |

Variables set by NAMELIST 3

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| IPUGH | IPUGH $=1$ is set when Pugh's method is adopted in the cladding creep calculation | 0 |
| Pellet crack and relocation option |  |  |
| XRELOC | Relocation parameter (thermal model) | 0.2 |
| FRELOC | Relocation parameter (deformation model) | 0.5 |
| EPSRLZ | Relocation strain in the axial direction (deformation model) | 0.003 |
| FACR | When the gap is filled by the amount of relocation strain multiplied by FACR in the radial direction, stiffness of pellet is recovered (deformation model) | 1.0 |
| FACZ | When the gap is filled by the amount of relocation strain multiplied by FACR in the axial direction, stiffness of pellet is recovered (deformation model) | 1.0 |
| BUMIN | Burnup at which transfer of pellet relocation strain from the circumferential direction to the radial direction begins ( $\mathrm{MWd} / \mathrm{tU}$ ) (thermal model) | 0.0 |
| BUMAX | Burnup at which transfer of pellet relocation strain from the circumferential direction to the radial direction is completed (MWd/tU) (thermal model) | 0.0 |
| IURS | Option for pellet stiffness recovery model in thermal model. <br> IURS $=0: \varepsilon_{R}=$ relocation strain, <br> IURS $=1: \varepsilon_{R}=$ relocation strain + gas bubble swelling strain + creep strain | 0 |
| IYNG | Pellet crack model option ( $=0$ : stiffness recovery follows a quadratic function, $=1$ : stiffness recovery follows a linear function) <br> (deformation model) | 1 |
| ECRAC3 | Pellet stiffness when completely cracked (Pa) (deformation model) | $2 \times 10^{9}$ |
| EFAC | Magnification factor for pellet Young's modulus | 1.0 |
| Pellet densification option |  |  |
| IDENSF | Option for equation of pellet densification $=0: \text { FEMAXI-III, }=1: \text { Rolstad, }=2: \text { NRC, }=3: \text { Marlowe, }=4: \text { Halden }$ | 0 |
| DMAX | (Used when IDENSF $=0,2$ or 3 ) <br> Maximum rate of volume shrinkage due to densification (\%) | 1.0 |
| SBU | (Used when IDENSF $=0$ ) <br> Burnup at which $90 \%$ of densification is completed ( $\mathrm{MWd} / \mathrm{tUO}_{2}$ ) | 2500 |
| TDNSF | (Used when IDENSF $=1$ or 3) Sintering temperature ( K ) | 2000 |
| GG | (Used when IDENSF = 3) Crystal grain size after heat treatment (m) | $10^{-5}$ |
| GG0 | (Used when IDENSF = 3) Initial crystal grain size (m) | $8 \times 10^{-6}$ |
| SITIM | (Used when IDENSF = 3) Heat treatment time (hr) | 24.0 |
| Pellet swelling option |  |  |
| IFSWEL | Option for equation of pellet swelling <br> $=0:$ Chubb, $=1:$ Speight, $=2:$ MATPRO-09, $=3:$ Halden | 0 |
| STFCP | (Used when IFSWEL $=0$ ) <br> Contact pressure at which gas bubble swelling does not occur ( Pa ) <br> (deformation model) | $-3 \times 10^{7}$ |
| SPCON | (Used when IFSWEL $=0$ ) <br> Contact pressure at which gas bubble swelling does not occur ( Pa ) (thermal model) | $-10^{6}$ |
| FACP | (Used when IFSWEL = 1) <br> Magnification factor for contact pressure in the external pressures on the bubble | 1.0 |
| BG | (Used when IFSWEL = 1) <br> Number of FP gas atoms per 1 bubble at garin boundary | $5 \times 10^{-8}$ |

Variables set by NAMELIST 4

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| Pellet hot press parameter option |  |  |
| BETAX | Pellet hot press parameter $\alpha$ | 0.002 |
| IHOT | $=0$ : hot press parameter $\alpha$ is fixed at BETAX value designated by input. $=1: \alpha$ changes as a function of porosity. | 1 |
| Plasticity model option |  |  |
| IFY | Pellet plasticity model option, $\quad=0$ : Rodford, $=1:$ Tachibana | 1 |
| ISTR | When ISTR $\neq 0, \quad K=$ magnitude of yield surface area of Zircaloy is set as $K=\sigma y+33.44\left(\mathrm{~kg} / \mathrm{mm}^{2}\right)$. | 0 |
| Irradiation growth option |  |  |
| ICAGRW | Cladding irradiation growth equation option: <br> $=0:$ not applied, $=1:$ MATPRO-09, $=2$ : Manzel <br> =3: Hannerz, $=4:$ Hesketh | 1 |
| CATEXF | (Used when ICAGRW $=1$ ) Factor in the axial direction $f_{Z}$ | 0.05 |
| COLDW | (Used when ICAGRW = 1) Cold work $C_{W}$ | 0.81 |
| FP gas release model option |  |  |
| IGASP | FP gas release rate model: <br> $=0$ : mechanistic model, $=1$ : temperature region model | 0 |
| IGAS | (Used when IGASP = 1) temperature region model option $=1:$ Nelson, $\quad=2:$ Morishima, $\quad=3$ : Lewis $=4$ : Karsten | 0 |
| APORE | (Used when IGASP $=0$ ) Initial radius of in-grain bubble ( cm ) | 0.0 |
| BFCT | (Used when IGASP $=0$ ) <br> Redissolution rate of in-grain bubbles into matrix is multiplied by BFCT | 1.0 |
| FACD | (Used when IGASP $=0$ ) <br> Effective diffusion coefficient in grain is multiplied by FACD. | 1.0 |
| ADDF | (Used when IGASP $=0$ ) <br> Redissolution rate of grain boundary bubbles into grain matrix is multiplied Jby ADDF. | 9.0 |
| FBSAT | (Used when IGASP $=0$ ) <br> Amount of gas saturation at grain boundary is multiplied by FPSAT. | 1.0 |
| PSAT | (Used when IGASP $=0$ ) <br> Limiting pressure acting on grain boundary bubbles ( Pa ) | $10^{8}$ |
| IPEXT | (Used when IGASP = 0) <br> Option for the external pressure Pext acting on grain boundary bubbles. <br> IPEXT $=0: P_{\text {ext }}=0$, IPEXT $=1: P_{\text {ex } 1}=$ plenum pressure, <br> IPEXT $=2$ : $P_{\text {exx }}=$ contact pressure between pellet and cladding, <br> IPEXT $=3: P_{\text {ext }}=\max$ (plenum pressure, contact pressure), <br> IPEXT $=11: P_{\text {ext }}=$ thermal stress (including the plenum pressure), <br> IPEXT $=$ 12: $P_{\text {exx }}=$ thermal stress (including the contact pressure between pellet and cladding), <br> IPEXT=13: $P_{\text {exx }}=$ thermal stress (including the plenum pressure and the contact pressure), <br> IPEXT $=14: P_{\text {err }}=$ average stress obtained by stress calculation in the entire length mechanical analysis. | 1 |
| OPORO | (Used when IGASP $=0$ ) ratio of open bubbles at grain boundary | 0.0 |
| ALHOT | (Used when IPEXT $=10,11,12$, and 13) Hot press parameter for the average stress acting on the grain boundary bubbles | 0.0001 |
| APEXT | (Used when IPEXT=14) Pext, average stress obtained in the Detailed Mechanical Analysis, is multiplied by APEXT . | 1.0 |
| FGG | (Used when IGASP $=0$ ) <br> Rate of grain growth sweeping of FP gas atom is multiplied by FGG. | 1.0 |

Variables set by NAMELIST 5

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| FP gas release model (Continued) |  |  |
| FRMIN | (Used when IGASP $=0$ ) <br> Minimum FP gas release rate (\%) | 0.5 |
| THEATF | (Used when IGASP $=0$ ) <br> Interpolation parameter used in in-grain diffusion equation $\theta$ | 1.0 |
| FMULT | (Used when IGASP $=0$ ) <br> Fitting factor of time step width for FP gas release model | 1.0 |
| NODEG | (Used when IGASP $=0$ ) <br> Number of in-grain meshes for FP gas release model (5 or less) | 3 |
| RREL | (Used when IGASP $=0$ ) <br> Dividing ratio of in-grain mesh for FP gas release model (to be set for each NODEG-1) | 10, 1 |
| RB | (Used when IGASP $=0$ ) Grain boundary layer thickness (mesh for re-dissolution) (cm) | $2 \times 10^{-6}$ |
| $\mathrm{UO}_{2}$ grain growth option |  |  |
| IGRAIN | Option for equation representing $\mathrm{UO}_{2}$ grain growth: $=0$ : Itoh (modified Ainscough) $\quad=1:$ Ainscough, $\quad=2$ : MacEwan, =3: Lyons, $=4:$ MATPRO-09 | 0 |
| GR | Initial pellet grain size ( $\mu \mathrm{m}$ ) | 10.0 |
| GRWF | (Used when IGRAIN $=0$ ) Grain growth rate is multiplied by GRWF | 1.5 |
| AG | (Used when IGRAIN $=0$ ) <br> Fitting parameter (grain growth suppression factor) | 1.0 |

Variables set by NAMELIST 6

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| Helium release option |  |  |
| NTVHE | Number of time points set by TVHE | 0 |
| $\begin{aligned} & \hline \text { TVHE } \\ & (13,50) \end{aligned}$ | TVHE $(1, n)$ : number of $n$th time points (hr) <br> TVHE $(i+1, n)$ : amount of He generated in axial segment $I$ at $n$th time point (mole) | 650*0. |
| Gas flow model option |  |  |
| IST | Gas flow option: <br> $=0$ : instantaneous complete mixing model <br> $=1$ : gas diffusion model in the axial direction | 1 |
| GMIN | Minimum gap width used in the gap gas flow model (cm) | 0.001 |
| THGI | Interpolation parameter for temperature, volume, etc., used in FP gas flow model in the axial direction $\theta_{1}$ | 1.0 |
| THG2 | Interpolation parameter used in diffusion calculation of FP gas flow model in the axial direction $\theta_{2}$ | 1.0 |
| AMLMX2 | Upper limit amount of gas transported between axial segments per unit time step $\qquad$ (mol) | $10^{-6}$ |
| AMLMX3 | Upper limit amount of FP gas released in each axial segment per unit time step <br> (mol) | $2 \times 10^{-6}$ |
| DTPR | Allowable ratio of amount of FP gas release to amount of plenum gas per unit time step | 0.01 |
| ETA | Control parameter (used for determination of time step width) | 0.05 |
| Cladding corrosion option |  |  |
| ICORRO | Cladding outer surface corrosion model option $=0:$ not applied, $=1:$ Halden | 0 |
| Gap conductance option |  |  |
| IGAPCN | Gap conductance model option <br> $=0$ : Modified Loss \& Stoute, $\quad=1:$ MATPRO-09, <br> $=2$ : Loss \& Stoute, $=3$ : modified Dean | 0 |
| R1 | (Used when IGAPCN $=0$ or 2) pellet surface roughness ( $\mu \mathrm{mm}$ ) | 1.0 |
| R2 | (Used when IGAPCN $=0$ or 2) cladding surface roughness ( $\mu \mathrm{m}$ ) | 1.0 |

Variables set by NAMELIST 7

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| Plotter output option |  |  |
|  | Output option ( $=0$ : no output, $=1$ : output) |  |
|  | Input data list | 1 |
|  | Fuel design data | 1 |
|  | Mesh coordinates data | 1 |
|  | List of parameters | 1 |
|  | History data | 1 |
|  | Results of thermal analysis of each time step | 1 |
|  | Results of mechanical analysis of each time step | 1 |
|  | Summary of thermal analysis results for each segment (thermal model) | 1 |
|  | Summary of mechanical analysis results for each segment (thermal model) | 1 |
|  | Summary of FP gas release calculation results for each segment (thermal model) | 1 |
|  | Summary of FP gas release calculation results for entire fuel rod (thermal model) | 1 |
|  | Summary of deformation behavior of pellet/cladding of each segment (mechanical model) | 1 |
|  | Summary of pellet stress and strain of each segment (mechanical model) | 1 |
|  | Summary of cladding stress and strain of each segment (mechanical model) | 1 |
|  | Summary of major results (final information) | , |
|  | Plotter output of thermal behavior of each segment (ON-LINE) (Unit 14) | 1 |
|  | Plotter output of FP gas behavior of each segment (ON-LINE) (Unit 14) | 1 |
|  | Plotter output of mechanical behavior (ON-LINE) (Unit 14) | 1 |
|  | Summary of entire-fuel-rod strain and corrosion of the objective segment | 0 |
|  | Not in use | 0 |
| IWNOD | Segment output option ( $=0$ : no output, $=1$ : output) | 12*0 |
|  | For IPRINT(8), IPRINT(9), IPRINT(10), IPRINT(16), IPRINT(17), output (including plotter output) is performed for segment I where IWNOD(I) = I, and output is not performed for segment I where IWNOD $(I)=0$. However, if all IWNOD is 0 , IWNOD (IFEM) $=1$ is set only at segment IFEM. |  |
| IWTHE | Thermal analysis output option ( $=0$ : no output, $=1$ : output), (Option when $\operatorname{IPRINT}(6)=1$ ) |  |
|  | Fuel temperature | 0 |
|  | Gap gas | 0 |
|  | Grain radius | 0 |
|  | In-grain gas bubble radius | 0 |
|  | In-grain gas bubble density | 0 |
|  | In-grain gas diffusion coefficient | 0 |
|  | In-grain gas effective diffusion coefficient | 0 |
|  | Number of gas atoms in grain | 0 |
|  | Number of gas atoms at grain boundary | 0 |
|  | Number of gas atoms released | 0 |
|  | Number of gas atoms in grain and at grain boundary | 0 |
|  | Number of gas atoms released, in grain, and at grain boundary | 0 |
|  | Number of gas atoms generated | 0 |
|  | FP gas release rate | 0 |
|  | Gas density at grain boundary | 0 |
|  | Saturated gas density at grain boundary | 0 |
|  | Average stress at grain boundary | 0 |
|  | Conditions for thermal calculation | 0 |
|  | Conventional output for thermal calculation | 0 |

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Variables set by NAMELIST

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| IWFEM | Output option for the Local Mechanical Analysis II (effective only when IFEMRD $=0$ ), ( $=0$ : no output, $=1$ : output) (option used when IPRINT(7) = 1) |  |
| (1) | Stress in the radial direction | 0 |
|  | Stress in the axial direction | 1 |
|  | Stress in the circumferential direction | 1 |
|  | Shear stress | 0 |
|  | Equivalent stress | 1 |
|  | Yield stress | 0 |
|  | Total strain in the radial direction | 0 |
|  | Total strain in the axial direction | 0 |
|  | Total strain in the circumferential direction | 0 |
|  | Total shear strain | 0 |
|  | Equivalent plastic strain | 1 |
|  | Creep strain in the radial direction | 0 |
|  | Creep strain in the axial direction | 0 |
|  | Creep strain in the circumferential direction |  |
|  | Shear creep strain | 0 |
|  | Equivalent creep strain | 0 |
|  | Elastic strain in the radial direction | 0 |
|  | Elastic strain in the axial direction | 0 |
|  | Elastic strain in the circumferential direction | 0 |
|  | Shear elastic strain | 0 |
|  | Thermal strain in the radial direction | 0 |
|  | Thermal strain in the axial direction | 0 |
|  | Densification strain | 0 |
|  | Swelling strain | 0 |
|  | Stiffness in the radial direction | 0 |
|  | Stiffness in the axial direction | 0 |
|  | Stiffness in the circumferential direction | 0 |
|  | Creep rate in the radial direction | 0 |
|  | Creep rate in the axial direction | 0 |
|  | Creep rate in the circumferential direction | 0 |
|  | Creep rate in the shear direction | 0 |
|  | Equivalent creep rate | 0 |
|  | Total strain rate in the radial direction | 0 |
|  | Total strain rate in the axial direction | 0 |
|  | Total strain rate in the circumferential direction | 0 |
|  | Total strain rate in the shear direction | 0 |
|  | Equivalent total strain rate | 0 |
|  | Strain energy | 0 |
|  | Temperature distribution in the radial direction | 1 |
|  | Mechanical interaction between pellet/cladding | 1 |
|  | Mechanical interaction between pellet/pellet | 1 |
|  | Displacement of node | 1 |
|  | Plot of "Pellet-Clad Mechanical Interaction" | 1 |
|  | Crack yielding map | 1 |
|  | Mechanical calculation conditions |  |

Variables set by NAMELIST 9

| Variable name | Content | Default value |
| :---: | :---: | :---: |
| IWROD | Output option for the Entire-Rod-Length Mechanical Analysis I (effective only when IFEMRD = 1), (= 0: no output, = I: output) (Option is used when IPRINT(7) =1) |  |
| (I) (2) (3) (4) (5) (6) (7) (8) $(9)$ $(10)$ $(11)$ $(12)$ $(13)$ $(14)$ $(15)$ $(16)$ $(17)$ $(18)$ | Stress in the radial direction <br> Stress in the axial direction <br> Stress in the circumferential direction <br> Equivalent stress <br> Yield stress <br> Creep strain in the radial direction <br> Creep strain in the axial direction <br> Creep strain in the circumferential direction <br> Creep hardening strain <br> Equivalent plastic strain <br> Swelling strain <br> Total strain in the radial direction <br> Total strain in the axial direction <br> Total strain in the circumferential direction <br> Thermal strain <br> Temperature of element <br> Pressure in the radial and axial directions <br> Displacement in the radial and axial directions | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| IPLT | Production of FEMAXI-IV plotter tape (mechanical model) (Unit 1) | 0 |
| IPLOPT | $=0$ : Output data at the time steps designated by input <br> $=1$ : Output data at all time steps calculated <br> $=-n$ : Output data at every $n$ time step <br> (Here, data are also output at the time steps designated by input) <Off-line plotter> | 0 |

## Input method for history data

Here, the method of production of history data (card numbers 10-11) of the input file is explained.

## Power history data

The following items must be input for the power history data: $\mathrm{Al}=$ time (hr), $\mathrm{Bl}=$ burnup, $\mathrm{A} 2=$ linear heat rate $(\mathrm{W} / \mathrm{cm}), \mathrm{A} 5=$ fast neutron flux $\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right), \mathrm{A} 3=$ coolant temperature $(\mathrm{K})$, $\mathrm{A} 4=$ coolant pressure $(\mathrm{MPa}), \mathrm{IT}=$ input generator, $\mathrm{IP}=$ output option, $\mathrm{IS}=$ temperature calculation option, A6 = coolant velocity (m/s). However, since B1 (burnup) is determined by input of A 1 (time) and vice versa, either Al or B 1 should be input. The unit of B 1 is designated by IBUNP of the NAMELIST: when $\operatorname{IBUNP}=0, \mathrm{~B} 1$ is $\mathrm{MWd} / \mathrm{t}-\mathrm{UO}_{2}$; when IBUNP $=1, \mathrm{Bl}$ is $\mathrm{MWd} / \mathrm{t}-\mathrm{U}$; and when $\mathrm{IBUNP}=2, \mathrm{Bl}$ is $\mathrm{GJ} / \mathrm{kg}-\mathrm{U}$.

Using IT (input generator), input by incremental form is possible. IT is selected from among 0,100 , and -100 ; when $\mathrm{IT}=0$ is set, Al (or Bl ) is recognized as a time increment from the previous history point (or burnup increment); when $\mathrm{IT}=100$, Al (or B1) is recognized as the time increment from the first history point (or burnup increment). IP is an output option; IP $\geq 1$ designates history points for detailed output, and IP $=0$ designates history points for simplified output only. IS is a switching flag between steady/unsteady status in temperature calculation; since this switching is automatically performed in the code, input of IP is usually unnecessary.
-FORMAT (6F 10.0, 215)

| F10.0 | F10.0 | F10.0 | F10.0 | F10.0 | F10.0 | I5 | I5 | I5 | F5.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A1 | B2 | A2 | A5 | A3 | A4 | IT | IP | IS | A6 |

## Relative power profile

Here, the input method for relative power profile is explained. RH is the relative power profile and designates the power ratio for A2 (linear heat rate, which was given by the history data) at the central position of an axial segment. Therefore, the number of RH data to be input is NAX (number of axial segments), whose maximum is 12 . When an identical power profile is input at history points, the input can be omitted using II (history point option).
-FORMAT (12F5.0, I5)

| 12 F 5.0 | 15 |
| :---: | :---: |
| $(\mathrm{RH}(\mathrm{I}), \mathrm{I}=1,12)$ | 1 II |

where NAX (number of segments) sets of data should be set for RH.

## Input method

For input of power history, the power-history-point number pairs of data (combination of power history data and relative power profile) must be input.

## Example of input (1)

An example of input for a case with one axial segment, where the power is increased to 500 W/cm during a period of 10 hr , is shown below. Here, the following values were used: fast neutron flux $=2.5 \times 10^{13}\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$ when $500 \mathrm{~W} / \mathrm{cm}$ is reached; coolant temperature $=513.15(\mathrm{~K})$;
coolant pressure $=3.4(\mathrm{MPa})$ and coolant velocity $=3.0(\mathrm{~m} / \mathrm{s})$.

| Example of input (1) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5... 0 | 5... 0 | 5. . . 0 | 5... 0 | 0. | 0. | 0 |
| 2 |  |  |  |  |  |  |
|  |  |  | 513. 15 | 3.4 | 1 | 3.0 |
| 1. 0 |  |  |  |  |  |  |
| 10.0 | 500.0 | 2. 5E13 |  |  | 1 |  |
| 5... 0 | 5. . . 0 | 5... 0 | 5... 0 | . 0 . | 0. | . 0 |

In the first line, NHIST $=2$ is shown; the number of history points is 2 .
In the second line, a hot stand-by state is set in the initial history data. Input for the hot stand-by state is not necessary since the following values are set: time ( Al ), $10^{-5}$ (hr); linear heat rate (A2), $10^{-3}(\mathrm{~W} / \mathrm{cm})$; fast neutron flux (A5), $2 \times 10^{1}\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$.

In the third line, $\mathrm{RH}(1)=1.0$ is set, since this case deals with a calculation of 1 axial segment for the input of relative power profile. The history point option is set as $\mathrm{II}=2$, which means that the same relative power profile is used for the two history points.

The fourth line shows input of $\mathrm{Al}=10(\mathrm{hr}), \mathrm{A} 2=500(\mathrm{~W} / \mathrm{cm})$ and $\mathrm{A} 5=2.5 \times 10^{13}\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$ for the history data of the second history point. Therefore, the time step is automatically divided, and at each division point, values of time-dependent variables are obtained by linear interpolation. Input of coolant temperature and coolant pressure is omitted; this means that the same values as those for the first history point are used; that is, $\mathrm{A} 3=513.14$ and $\mathrm{A} 4=3.4$ are input.

For the output option, IP = 1 is set in the second and third lines; therefore, detailed output is performed both in the hot stand-by state and when $500 \mathrm{~W} / \mathrm{cm}$ is reached.

## Example of output (2)

An example with 12 axial segments is shown in which base irradiation is first performed at $200 \mathrm{~W} / \mathrm{cm}$ up to $20 \mathrm{GWd} / \mathrm{t} \mathrm{UO}_{2}$. The power is decreased thereafter, and then increased to 250 $W / \mathrm{cm}$. After conditioning for 72 hr , the power is increased to $500 \mathrm{~W} / \mathrm{cm}$, maintained for 24 hr , and finally the power is decreased. Here, the power increase rate is $200 \mathrm{~W} / \mathrm{cm} \cdot \mathrm{hr}$ in every period.

The following values are set: fast neutron flux $=10^{14}\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$ when $500 \mathrm{~W} / \mathrm{cm}$ is reached; coolant temperature $=513.15(\mathrm{~K})$; coolant pressure $=3.4(\mathrm{MPa})$; and coolant velocity is
constant at $3.0(\mathrm{~m} / \mathrm{s})$. The relative power profile is given for base irradiation and for ramp irradiation. During the base irradiation, output of calculation results is performed at $5 \mathrm{GWd} / \mathrm{t}$ $\mathrm{UO}_{2}, 10 \mathrm{GWd} / \mathrm{t}-\mathrm{UO}_{2}, 15 \mathrm{GWd} / \mathrm{t}-\mathrm{UO}_{2}$ and at $20 \mathrm{GWd} / \mathrm{t}-\mathrm{UO}_{2}$; and during the ramp irradiation, the output of calculation is also performed at every $50 \mathrm{~W} / \mathrm{cm}$ power increment above $250 \mathrm{~W} / \mathrm{cm}$. When the power is maintained at $500 \mathrm{~W} / \mathrm{cm}$, the output of calculation is obtained after $1,3,6$, 12 and 24 hr .


The simplified output is obtained for the 21 history points shown above. Among these history points, IP $\geq 1$ is designated only at points where detailed output is required; here IP = 2 is input and detailed output information is obtained at history points after this designation. The unit of burnup should be $\mathrm{MWd} / \mathrm{t}-\mathrm{UO}_{2}$; therefore, $\operatorname{IBUNP}=0$.

The first line shows the number of history points, NHIST $=21$.
The second line shows the history data of the hot stand-by state.
Data in the third line show that the same relative power profile is used from the first history point to the 7th history point.

The fourth line shows the second history point data of $\mathrm{Al}=1(\mathrm{hr}), \mathrm{A} 2=200(\mathrm{~W} / \mathrm{cm})$ and A 5 $=4 \times 10^{13}\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$. Coolant temperature and pressure are the same as those in the hot standby state.

The 5th to 8th lines show input to extend burnup up to $20 \mathrm{GWd} / \mathrm{tUO}_{2}$ at $200(\mathrm{~W} / \mathrm{cm})$, and simplified output is obtained at $5 \mathrm{GWd} / \mathrm{tUO}_{2}$ and at $15 \mathrm{GWd} / \mathrm{UO}_{2}$. A2 (linear heat rate) and A5 (fast neutron flux) are obtained by interpolation. During this stage, A2 $=200(\mathrm{~W} / \mathrm{cm})$ and $\mathrm{A} 5=4 \times 10^{13}\left(\mathrm{n} / \mathrm{cm}^{2} \cdot \mathrm{~s}\right)$ are used.

The 9th line shows setting of IT $=-100$. This means that the power was decreased to $0.001(\mathrm{~W} / \mathrm{cm})$ within 1 hr from the burnup of $20 \mathrm{GWd} / \mathrm{tUO}_{2}$ shown in line 8.

The 10th line shows that the relative power profile was changed after the power levelled off at $0.001(\mathrm{~W} / \mathrm{cm})$ for 1 hr .

The 11th line shows that the relative power profile given in the 11th line is applied from the 8th history point up to the last (21st) history point. Here, since a power of 0 is not allowed, a value of around $10^{-3}(\mathrm{~W} / \mathrm{cm})$ must be set.

The 12th line shows that the power was increased to $250(\mathrm{~W} / \mathrm{cm})$ within 12.5 hr , and the 13th line shows that the power was maintained at $250(\mathrm{~W} / \mathrm{cm})$ for 72 hr .

The 14th to 18 th lines show that the power was increased by $50 \mathrm{~W} / \mathrm{cm}$ within 0.25 hr (200 $\mathrm{W} / \mathrm{cm} \cdot \mathrm{hr}$ ) after being maintained at $250(\mathrm{~W} / \mathrm{cm})$ for 72 hr . Namely, elapsed time at the previous history point where $\mathrm{IT}=-100$ was designated (shown in the 13 th line) is given by Al. Since the linear heat rate is given by the linear interpolation, setting of $\mathrm{A} 2=300,350,400$ and 450 in lines 14-17 gives the same results. Similarly, the fast neutron flux used here gives the same results by setting $\mathrm{A} 5=6 \times 10^{13}, 7 \times 10^{13}, 8 \times 10^{13}$ and $9 \times 10^{13}$.

The 19th-23rd lines show history data which were set to obtain simplified output when the power is maintained at $500(\mathrm{~W} / \mathrm{cm})$ and at $1,3,6$ and 12 hr from the starting time. The detailed output is obtained 24 hr after the starting time.

The 24th line shows that the power was decreased within a $2.5-\mathrm{hr}$ period starting from 24 hr from the starting time. Here, since the coolant temperature and pressure were set as constant, input for them at the second and later history points was omitted. Also, since linear heat rate and fast neutron flux are obtained by linear interpolation, input error occurs if no power is generated at the last history point. (Both values should not be zero.)

## A2 Input Manual for Plotter

| Card No. | SYMBOL | (FORMAT) |
| :---: | :--- | :--- |
| I | Comments |  |
| 2 | ISET | (*) $^{2}$ |

Input ISET-sets consisting of the following cards

| 3 | IRNUM, ITOPT, ISYM (*) Function setting |
| :---: | :---: |
|  | IRNUM: number of lines drawn in one figure (maximum of 5 lines) <br> ITOPT: designation of graph type <br> ITOPT $=0 \quad \mathrm{X}$ axis represents time, burnup or linear heat rate <br> ITOPT $=\mathrm{I} \quad \mathrm{X}$ axis represents coordinates in the radial or axial direction <br> ITOPT = 2 Construct a diagram for comparison of calculated values with measured values (in this case, maximum value of IRM becomes 4 since one line is used for the measured values) <br> ISYM: Center symbol option <br> $=0 \quad$ center symbol is not plotted <br> $=1$ center symbol is plotted |
| 4 | IXOPT, IXOPT2, IYOPT2, IYNUM, (IYOPT(I), I=I, IYNUM) (*) Axis setting |
|  | ```IXOPT: setting of the contents of \(X\) axis (set when ITOPT \(=0\) or 2 ) = 1: time \(=2\) : coordinates in the radial direction \((-) \quad\) (set when ITOPT \(=1\) ) \(=3\) : coordinates in the axial direction ( - ) = 4: burnup (at the objective segment) \(=5\) : linear heat rate (at the objective segment, \(\mathrm{W} / \mathrm{cm}\) ) = 6: bumup (average on all axial segments) =7: linear heat rate (average on all axial segments, W/cm)``` <br> IXOPT2: setting of units for time and burnup <br> Setting of units when X axis represents time (IXOPT $=1$ ) <br> IXOPT2 = 0: hour <br> IXOPT2 = $1:$ day <br> Setting of units when X axis represents burnup (IXOPT $=4$ or 6 ) <br> IXOPT2 $=0: \mathrm{MWd} / \mathrm{tUO}_{2}$ <br> IXOPT2 = $1: \mathrm{GWd}^{\mathrm{GW}} / \mathrm{tUO}_{2}$ <br> $\mathrm{IXOPT} 2=2: \mathrm{MWd} / \mathrm{t} \mathrm{U}$ <br> $\mathrm{IXOPT} 2=3: \mathrm{GWd} / \mathrm{tU}$ <br> IYOPT2; setting of units for time and burnup <br> Setting of units when Y axis represents time (IYOPT(I)=1 or 12) <br> IYOPT2 $=0 \quad \mathrm{MWd} / \mathrm{tUO}_{2}$ <br> $\mathrm{IYOPT} 2=\mathrm{I} \quad \mathrm{GWd} / \mathrm{tUO}_{2}$ <br> $\mathrm{IYOPT} 2=2 \quad \mathrm{MWd} / \mathrm{tU}$ <br> IYOPT2 $=3 \quad \mathrm{GWd} / \mathrm{tU}$ <br> IYNUM: number of $Y$ axes. When more than 2 physical properties are set for $Y$ axis (IYNUM $\geqq 2$ ), IYNUM = IRNUM must be set since one graph is drawn for one Y axis. <br> (IYOPT(I), I = 1, IYNUM): select contents of Y axis from Tables 1 to 3 and input the physical quantity number. |
| 5 | (IR(I), I = 1, IRNUM) ${ }^{*}$ ( ${ }^{\text {a }}$ Radial mesh number |
|  | (IR(I), I = I, IRNUM): radial mesh number is set for each figure. When setting is not necessary, input 1. |


| Card No. | SYMBOL (FORMAT) |  |
| :---: | :---: | :---: |
| 6 | (IZ(I), I= 1, IRNUM) (*) | Axial segment number |
|  | (IZ(I), $\quad \mathrm{I}=1, \mathrm{IRNUM}$ ) <br> Set the segment number in the axial direction for each figure. Input I when setting is not necessary. |  |
| 7 | (ITIM(I), $\mathrm{I}=1,2$ ) or (ITIM(I), $\mathrm{I}=\mathrm{I}, \mathrm{RNUM}$ ) (*) | Time step number |
|  | (When ITOPT $=0$ or 2 , input (ITIM(I), $\mathrm{I}=\mathrm{I}, 2)$ )ITIM $(\mathrm{I})=$ set a time step number for starting point of the figureITIM $(2)=$ set a time step number for end point of the figure(When ITOPT $=1$, input (ITIM (I), $\mathrm{I}=1$, RNUM $)$ )set a time step number for each figure |  |
| 8 | X0, XM, XNUM, IXN, IFLAG(6) (*) | Setting of X -axis scale |
|  | This card is a DUMMY when IXOPT $=2$ or 3 . <br> X 0 : minimum value of X -axis scale <br> XM: maximum value of X -axis scale <br> XNUM: increment of X-axis scale <br> IXN: number of digits after decimal point on X axis (example) $\begin{aligned} & \text { IXN }=-1 \text { for } 10 \\ & \text { IXN }=1 \text { for } 10.0 \\ & \text { IXN }=2 \text { for } 10.00 \end{aligned}$ <br> IFLAG(6): setting of $X$-axis scale <br> $=3$ : automatic scaling is applied to X axis <br> $\neq 3$ : X axis is drawn with designated scaling by input |  |
| 9 |  |  |
|  | $\mathrm{Y} 0(\mathrm{I}):$ minimum value of Y -axis scale <br> YM(I): maximum value of Y-axis scale <br> YNUM(I): increment of Y -axis scale <br> IYN(I): number of digits after decimal point on Y axis (input in the same manner as for IX <br> JFLAG(I): option for Y -axis scale <br> $=0$ : scale is expressed with real numbers (decimal nu <br> $=1$ : scale is expressed with floating format <br> $=2$ : logarithmic scaling is used for Y axis <br> $=3$ : automatic scaling is applied to Y axis <br> When $\operatorname{IFLAG}(\mathrm{I})=3, \mathrm{Y} 0 \sim \mathrm{IYN}$ are DUMMY, since autor | N) <br> mber expression) <br> natic scaling is selected. |

(Note 1) When ITOPT $=2$, measured values are input from unit 2. Therefore, data row for ( $\mathrm{X}, \mathrm{Y}$ ) must be prepared in unit 2 .
(Note 2) Data specified by asterisk (*) are input with free format.

Table (1): Physical Quantities of Y axis (1) ${ }^{\left({ }^{* *}\right)}$ :designated by IYOPT2

| Group | No. | Item | Unit |
| :---: | :---: | :---: | :---: |
| A <br> Data regarding time and burnup | 1 | Rod average burnup | (**) |
|  | 2 | FP gas release rate | (\%) |
|  | 3 | Rod internal pressure | (MPa) |
|  | 4 | Plenum volume | (cc) |
|  | 5 | Pellet elongation (when IFEMRD $=1$, pellet elongation at the ojective segment designated by IFEM) | (\%) |
|  | 6 | Entire rod elongation (in the case of IFEMRD=1) | $\begin{gathered} (\%) \\ (\mu \mathrm{m}) \end{gathered}$ |
|  | 7 | Maximum change of cladding outer radius | (W/cm) |
|  | 8 | Average linear heat rate in the axial direction | $\left(\mathrm{g} / \mathrm{cm}^{2}\right)$ |
|  | 10 | Average iodine concentration |  |
|  | 10 | Maximum iodine concentration | (g/cm) |
|  | 67 | Average change in cladding outer radius |  |

Table (2): Physical Quantities of Y axis (2) (**):designated by IYOPT2

| Group | No | Item | Unit |
| :---: | :---: | :---: | :---: |
| BData <br> regarding <br> time, burnup <br> and <br> axial <br> coordinate | 11 | Linear heat rate (thermal analysis=TA) | (Wd ${ }^{\text {d }}$ |
|  | 12 | Burnup (TA) | ( $\mathrm{MWd} / \mathrm{tUO}_{2}$ ) |
|  | 13 | Diametral gap width (mechanical analysis; when IFEMRD $=0$, gap at each axial segment, and when IFEMRD=1, gap at each node couple is output sequentially) | ( mm ) |
|  | 14 | PCMI pressure (radial direction) | (MPa) |
|  | 15 | FP gas release rate (TA) | (\%) |
|  | 16 | Frictional force between pellet and cladding in the axial direction (mechanical analysis) | (MPa) |
|  | 17 | Pellet elongation | (\%) |
|  | 18 | Cladding elongation (Items 17 and 18 are output from mechanical analysis. <br> When IFEMRD $=0$, elongation at each axial segment is obtained; when IFEMRD $=1$, the same values in the axial direction are output) | (\%) |
|  | 19 | Gap conductance (TA) | ( $\mathrm{W} / \mathrm{cm}^{2} \mathrm{C}$ ) |
|  | 20 | Coolant temperature (TA) | $\left({ }^{\circ} \mathrm{C}\right)$ |
|  | 21 | Cladding inner surface temperature (TA) | $\left({ }^{\circ} \mathrm{C}\right)$ |
|  | 22 | Cladding outer surface temperature (TA) | $\left({ }^{\circ} \mathrm{C}\right)$ |
|  | 23 | Pellet center temperature (TA) | $\left({ }^{\circ} \mathrm{C}\right)$ |
|  | 24 | Pellet outer surface temperature (TA) | $\left({ }^{\circ} \mathrm{C}\right)$ |
|  | 25 | Cladding outer radius change(the same as 13) | ( m ) |
|  | 26 | Composition of $\mathrm{Xe}+\mathrm{Kr}$ (TA) | (\%) |
|  | 68 | Pellet density (TA) | (T•D) |

Table (3): $\quad$ Physical Quantities of Y axis (3)


## [Comment on the C-group of Physical Quantities in Plotter Figure]

In the following explanation, thermal analysis is identical irrespective of IFEMRD value designated by input. Also, FP gas release rate (No.47) is an exception of the explanation, because it is always output at each axial segment.

## (1) Physical quantities No. $27 \sim 46$ for pellet

(1) In the case of IFEMRD $=0$, or local mechanical analysis, stress, strain, and temperature are evaluated at points indicated by $\times$ marks, which are the Gauss's integral points. See Fig.2.39(b). Displacement is evaluated at node point.

(2) In the case of IFEMRD $=1$, or entire length mechanical analysis, stress, strain, and temperature are evaluated at points indicated by $\times$ marks, which are the Gauss's integral points. See Fig.2.29.

| [10 radial divisions] |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{lk}=1$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 8 (No. of Axial |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 7 segments |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 6§12) |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 5 |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 4 |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 3 |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | 2 |
| $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\times$ | $\mathrm{IZ}=1$ |

Center line of Pellet

## (1) Physical quantities No. $48 \sim 66$ for cladding

Stress, strain, and temperature are evaluated at points indicated by $\times$ marks, or the Gauss's integral points.
(1) In the case of IFEMRD $=0$, or local mechanical analysis:

See Fig.2.39(b). Displacement is evaluated at node.

(2) In the case of IFEMRD $=1$, or entire length mechanical analysis, stress, strain, and temperature are evaluated at points indicated by $\times$ marks, which are the Gauss's integral points. See Fig.2.29.


## A3 (1) Subroutine List

Table A1 lists the FEMAXI-IV subroutines which are classified in terms of their analytical functions. The abbreviations in the table are as follows:

P: Program controlling routines, plotter routines, and other auxiliary function subroutines which are not included in the analytical models.
T : Subroutines used in the thermal analysis models.
M1: Subroutines used in the entire rod length mechanical analysis model.
M2: Subroutines used in the local mechanical analysis model.
Table A1 FEMAXI-IV Subroutine and functions

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| AAZERO | Zero setting of common areas | $\bigcirc$ |  |  |  |
| ADBU | Calc. of burnup increment from time history increment | $\bigcirc$ |  |  |  |
| ADRESS | Calc. of address in matrix |  |  | $\bigcirc$ |  |
| ADTM | Calc. of time history increment from burnup increment | $\bigcirc$ |  |  |  |
| ADVANC | Updating of grain size and FP gas atom density in FP release model |  | $\bigcirc$ |  |  |
| AXIVAL | Y-axis setting for ON-LINE plotter | $\bigcirc$ |  |  |  |
| BBL | Calc. of in-grain bubble radius |  | $\bigcirc$ |  |  |
| BBLDEN | Calc. of in-grain bubble density |  | $\bigcirc$ |  |  |
| BDMAT | Formation of $[\mathrm{B}]^{\mathrm{T}}[\mathrm{D}]$ matrix |  |  |  | $\bigcirc$ |
| blockdata | Block data list | $\bigcirc$ |  |  |  |
| BMAT | Formation of [B] matrix |  |  |  | $\bigcirc$ |
| BOUNDF | Calc. of nodal force on the upper surface of pellet in the axial direction |  |  |  | $\bigcirc$ |
| BURNUP | Calc. of burnup | $\bigcirc$ |  |  |  |
| CAGROW | Calc. of irradiation growth strain of cladding in the axial direction |  |  | $\bigcirc$ | $\bigcirc$ |
| CANDM | FP release model routine |  | $\bigcirc$ |  |  |
| CATHEX | difection of thermal expansion of cladding in the axial |  |  | $\bigcirc$ | $\bigcirc$ |
| CCREEP | Calc. of cladding creep strain |  | $\bigcirc$ |  |  |
| CDTHEX | difection of thermal expansion of cladding in the radial |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| CELMOD | Calc. of cladding Young's modulus |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| CFRFZ | Calc. of cladding axial force |  |  |  | $\bigcirc$ |
| CHCAP | Calc. of cladding volumetric specific heat |  | $\bigcirc$ |  |  |
| CHSOFT | Calc. of stress-differential term of cladding yield function |  |  | $\bigcirc$ | $\bigcirc$ |
| CLBDF | Calc. of contact force on the upper surface of pellet |  |  |  | $\bigcirc$ |
| CLEAR | Zero setting of real number areas | $\bigcirc$ |  |  |  |

Table A1 (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CMAT | Calc. of effective Young's moduli of pellet and cladding, and Poisson's ratio |  |  |  | $\bigcirc$ |
| CMATl | Formation of pellet [C] matrix |  |  | $\bigcirc$ |  |
| CMAT2 | Formation of cladding [C] matrix |  |  | $\bigcirc$ |  |
| CNSTR | Setting of displacement increment |  |  | $\bigcirc$ |  |
| COLECT | Calc. of total stiffness matrix and loading vector |  |  |  | $\bigcirc$ |
| COORDI | Setting of shape coordinates for FEM in the local mechanical analysis |  |  |  | $\bigcirc$ |
| CPOIR | Calc. of Poisson's ratio of cladding |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| CPUGH | Control routine of PUGH's reversal method |  |  |  | $\bigcirc$ |
| CRACK | Setting of pellet crack status |  |  |  | $\bigcirc$ |
| CREEP1 | Formation of [ $\left.\mathrm{C}^{c}\right]$ matrix and creep strain vector $\left\{\Delta \varepsilon^{c}\right\}$ |  |  |  | $\bigcirc$ |
| CREEP2 | Formation of creep strain increment $\left\{\Delta \varepsilon^{c}\right\}$ of cladding |  |  |  | $\bigcirc$ |
| CRPEP2 | Formation of cladding creep strain rate $1 / \varepsilon^{c}$ (MATPRO-9) |  |  |  | $\bigcirc$ |
| CRPEP3 | Formation of cladding creep strain rate $1 / \varepsilon^{c}$ (NENANSEN) |  |  |  | $\bigcirc$ |
| CRPEQ2 | Formation of $\frac{1}{\varepsilon^{c}}(=f), \frac{\partial f}{\partial \sigma}, \frac{\partial f}{\partial \bar{\varepsilon}^{H}}$ in cladding creep (MATPRO-9) |  |  |  | $\bigcirc$ |
| CRPEQ3 | Formation of $\frac{1}{\varepsilon^{c}}(=f), \frac{\partial f}{\partial \sigma}, \frac{\partial f}{\partial \varepsilon^{H}}$ in cladding creep (NENANSEN) |  |  |  | $\bigcirc$ |
| CRPHD2 | Formation of $\frac{1}{\varepsilon^{H}}(=g), \frac{\partial g}{\partial \bar{\sigma}}, \frac{\partial g}{\partial \bar{\varepsilon}^{c}}$ in cladding creep (MATPRO-9) |  |  |  | $\bigcirc$ |
| CRPHD3 | Formation of $\frac{1}{\varepsilon^{H}}(=g), \frac{\partial g}{\partial \sigma}, \frac{\partial g}{\partial \bar{\varepsilon}^{c}}$ in cladding creep (NENANSEN) |  |  |  | $\bigcirc$ |
| CRPM11 | Formation of [ $\left.\mathrm{C}^{\mathrm{c}}\right]$ matrix and pellet creep vector $\left\{\Delta \varepsilon^{\mathrm{c}}\right\}$ |  |  |  | $\bigcirc$ |
| CRPM12 | Formation of creep strain increment $\left\{\Delta \varepsilon^{c}\right\}$ of pellet |  |  |  | $\bigcirc$ |
| CTHCON | Calc. of cladding thermal conductivity |  | $\bigcirc$ |  |  |
| CTSOFT | Calc. of temperature differential term in cladding yield function |  |  | O | $\bigcirc$ |
| CUBIC | Calc. of largest real number solution of cubic equation (bubble radius) |  | $\bigcirc$ |  |  |
| CYIE | Calc. of Zircaloy yield stress ( $0.2 \%$ proof stress) |  |  | $\bigcirc$ | $\bigcirc$ |
| CYIE2 | Calc. of Zircaloy yield stress (size of yiels surface at $\bar{\varepsilon}^{p}$ ) |  |  | $\bigcirc$ | $\bigcirc$ |
| CYLD | Calc. of Zircaloy yield stress ( $0.2 \%$ proof stress) |  | $\bigcirc$ |  |  |

Table A1 (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DELTAN | FEM mesh element data in the local mechanical analysis |  |  |  | $\bigcirc$ |
| DENSF | Pellet densification model |  | $\bigcirc$ |  | $\bigcirc$ |
| DEVSIG | Deviation stress |  |  |  | $\bigcirc$ |
| DFCLAD | Formation of loading vector of cladding |  |  | $\bigcirc$ |  |
| DFPLT | Formation of loading vector of pellet |  |  | $\bigcirc$ |  |
| DFX | Determines the size of cladding yield surface |  |  | $\bigcirc$ | $\bigcirc$ |
| DIFC | Diffusion coefficient of FP atom in pellet grains |  | $\bigcirc$ |  |  |
| DIFCON | Xe-He mutual diffusion coefficient |  | $\bigcirc$ |  |  |
| DOT | Routine for Pugh's reversal method in cladding creep |  |  | $\bigcirc$ | $\bigcirc$ |
| DPMAT | Formation of [ $D^{P}$ ] matrix |  |  |  | $\bigcirc$ |
| DPST | Calc. of $\Delta \bar{\varepsilon}^{p}$ |  |  |  | $\bigcirc$ |
| ELMLP1 | Control of formation of element stiffness matrix and loading vector |  |  |  | $\bigcirc$ |
| ELMLP2 | Control of calculation of stress-strain of elements |  |  |  | $\bigcirc$ |
| EQIEPS | Calc. of equivalent strain |  |  |  | $\bigcirc$ |
| EQISIG | Calc. of equivalent stress |  |  |  | $\bigcirc$ |
| EQSCAL | Convergence calculation of size of yield surface at $\bar{\varepsilon}^{p}$ |  |  | $\bigcirc$ | $\bigcirc$ |
| ESMAT | Formation of element stiffness matrix |  |  |  | $\bigcirc$ |
| FCREEP | Calc. of pellet creep strain (MATPRO-09) |  | $\bigcirc$ |  |  |
| FDIST | Calc. of flux depression in pellet in the radial direction |  | $\bigcirc$ |  |  |
| FDISTF | Calc. of flux depression in pellet in the radial direction |  | $\bigcirc$ |  |  |
| FELMOD | Calc. of pellet Young's modulus |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| FEMAX4 | Control of entire program | $\bigcirc$ |  |  |  |
| FEMRDI | Connecting routine of thermal analysis and rod entire length mechanical analysis length mechanical analysis |  |  | $\bigcirc$ |  |
| FFG | Calc. of sweeping ratio of FP atoms by grain growth |  | $\bigcirc$ |  |  |
| FGPRO | Calc. of FP gas generation |  | $\bigcirc$ |  |  |
| FGRELN | Calc. of FP gas release rate at each element of pellet |  | $\bigcirc$ |  |  |

Table A1 (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| FHSOFT | Calc. of stress-differential term of pellet yield function $\sigma_{y}$ |  |  |  | $\bigcirc$ |
| FISGAS | Reference table to determine FP gas release rate at each temperature range |  | $\bigcirc$ |  |  |
| FISRAT | Calc. of nuclear fission density | $\bigcirc$ |  |  |  |
| FLMCON | Calc. of cladding surface heat transfer coefficient by Jens-Lottes equation |  | $\bigcirc$ |  |  |
| FLOAD | Calc. of element loading vector |  |  |  | $\bigcirc$ |
| FLXDEP | Calc. of flux depression in pellet in the radial direction |  | $\bigcirc$ |  |  |
| FORCE | Calc. of total external force vector |  |  |  | $\bigcirc$ |
| FPOIR | Poisson's ratio of pellet |  |  | $\bigcirc$ | $\bigcirc$ |
| FPRES2 | Calc. of effective width of surface nodes |  |  |  | $\bigcirc$ |
| FTSOFT | Calc. of temperature-differential term of pellet yield function $\sigma_{Y}$ |  |  |  | $\bigcirc$ |
| FX | Routine to determine the size of cladding yield surface |  |  | $\bigcirc$ | $\bigcirc$ |
| FYIE | Pellet yield stress (0.2\% proof stress) |  |  | $\bigcirc$ | $\bigcirc$ |
| GAPCON | Calc. of gap conductance |  | $\bigcirc$ |  |  |
| GAPELN | Contact judgment of pellet/clad and pellet/pellet |  |  |  | $\bigcirc$ |
| GAPMOD | Convergence calculation of gap conductance |  | $\bigcirc$ |  |  |
| GAPS | Calc. of gap width |  |  | $\bigcirc$ |  |
| GAULP1 | Formation of stiffness matrix and loading vectors at gauss point in element |  |  |  | $\bigcirc$ |
| GAULP2 | Calc. of stress-strain at gauss point in element |  |  |  | $\bigcirc$ |
| GDTHCN | Thermal conductivity of Gadolinia |  | $\bigcirc$ |  |  |
| GPSSET | Setting of boundary conditions |  |  |  | $\bigcirc$ |
| GRAIN | Calc. of pellet grain growth |  | $\bigcirc$ |  |  |
| GRAPH1 | Control routine for ON-LINE plotter (thermal analysis) | $\bigcirc$ |  |  |  |
| GRAPH2 | Control routine for ON-LINE plotter (FP gas release analysis) | $\bigcirc$ |  |  |  |
| GRAPH3 | Control routine for ON-LINE plotter (stress-strain analysis) | $\bigcirc$ |  |  |  |
| GRID | Setting of grid point for ON-LINE plotter | $\bigcirc$ |  |  |  |

Table Al (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| GTHCON | Thermal conductivity of gases |  | $\bigcirc$ |  |  |
| HEAD2 | Title of the rod entire length mechanical analysis | $\bigcirc$ |  |  |  |
| HEADER | Title of the local mechanical analysis | $\bigcirc$ |  |  |  |
| HEATG | Thermal conductivity of Zirconia |  | $\bigcirc$ |  |  |
| HOTVOL | Auxiliary routine to calculate plenum volume |  | $\bigcirc$ |  |  |
| HTX | Cladding surface heat transfer coefficient by Jens-Lottes eq. |  | $\bigcirc$ |  |  |
| ICLEAR | Zero setting of integer areas | $\bigcirc$ |  |  |  |
| INIGAS | Calc. of plenum pressure and volume at hot stand-by |  | $\bigcirc$ |  |  |
| INIMAT | Calc. of [C] matrix |  |  |  | $\bigcirc$ |
| INISTR | Calc. of initial strain |  |  |  | $\bigcirc$ |
| INPGER | Generator of historical input data | $\bigcirc$ |  |  |  |
| INPHIS | Input routine of power history | $\bigcirc$ |  |  |  |
| INPIMG | Print-out of input data image | $\bigcirc$ |  |  |  |
| INPR | Radial meshing in the local mechanical analysis |  |  |  | $\bigcirc$ |
| INPUT1 | Input routine for thermal analysis | $\bigcirc$ |  |  |  |
| INPZ | Axial meshing in the local mechanical analysis |  |  |  | $\bigcirc$ |
| INTG | Calc. of the coefficient matrices [A] and [E] for FP gas release |  | $\bigcirc$ |  |  |
| INTGH | Calc. of the coefficient matrix [H] for FP gas release |  | $\bigcirc$ |  |  |
| INTGX | Volumetric integral of residual FP in pellet grains |  | $\bigcirc$ |  |  |
| INTPLT | Routine of quadratic interpolation | $\bigcirc$ |  |  |  |
| INV3 | Inverse matrix of $3 \times 3$ symmetrical matrix |  |  | $\bigcirc$ |  |
| INVERS | Inverse matrix of $4 \times 4$ symmetrical matrix |  |  |  | $\bigcirc$ |
| JACK2 | Jacobian of quadratic elements |  |  |  | $\bigcirc$ |
| LENGT | Calc. of character length for ON-LINE plotter | $\bigcirc$ |  |  |  |
| LINER | Pattern of lines in plotter output figure | $\bigcirc$ |  |  |  |
| LINSET | Setting of node array at outer surface in the local mechanical analysis |  |  |  | $\bigcirc$ |

Table Al (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| LOCALI | Storage and extract of information at gauss point |  |  |  | $\bigcirc$ |
| LSYM | Printing of symbols for ON-LINE plotter | $\bigcirc$ |  |  |  |
| MAIN | Main routine | $\bigcirc$ |  |  |  |
| MATDAT | Setting of materials properties for heat conduction calc. |  | $\bigcirc$ |  |  |
| MDEPS0 | Calc. of initial strain in rod entire length analysis |  |  | $\bigcirc$ |  |
| MDSIG | Calc. of stress in the rod entire length analysis |  |  | $\bigcirc$ |  |
| MODIFY | Setting of contact boundary conditions in local mechanical analysis |  |  |  | $\bigcirc$ |
| MODSET | Calc. of total matrix area in local mechanical analysis |  |  |  | $\bigcirc$ |
| MOVE | Storage of total matrix (entire length analysis) |  |  | $\bigcirc$ |  |
| MTDF | Formation of total loading vector (entire length analysis) |  |  | $\bigcirc$ |  |
| NCOUPL | Initial setting of contact pair in local mechanical analysis |  |  |  | $\bigcirc$ |
| ONPLOT | Control routine for ON-LINE plotter | $\bigcirc$ |  |  |  |
| OPTSO2 | Solution of asymmetrical matrix |  |  | $\bigcirc$ | $\bigcirc$ |
| OPTSOL | Solution of symmetrical matrix |  |  | $\bigcirc$ |  |
| OURELM | Output of stress and strain at element gauss point |  |  |  | $\bigcirc$ |
| OUREM | Auxiliary routine for OURELM |  |  |  | $\bigcirc$ |
| OUTND | Auxiliary routine for output of nodal displacement |  |  |  | $\bigcirc$ |
| OUTND | Output of nodal displacement |  |  |  | $\bigcirc$ |
| OUTP | Output of time-dependent variables in the entire length analysis |  |  | $\bigcirc$ |  |
| OUTP1 | Output of time-dependent variables in the local mechanical analysis |  |  |  | $\bigcirc$ |
| OUTPT0 | Final summary output 0 |  |  | $\bigcirc$ |  |
| OUTPT1 | Final summary output 1 |  | $\bigcirc$ | $\bigcirc$ |  |
| OUTPT2 | Final summary output 2 |  | $\bigcirc$ | $\bigcirc$ |  |
| P2 | Shape function of quadratic element |  |  |  | $\bigcirc$ |
| PAPLOT | Map of crack and yield of pellet |  |  |  | $\bigcirc$ |
| PDENS | Densification strain of pellet |  | $\bigcirc$ | $\bigcirc$ |  |

Table Al (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PFRFZ | Calc. of pellet axial force |  |  | $\bigcirc$ |  |
| PHCAP | Specific volumetric heat of pellet |  | $\bigcirc$ |  |  |
| PHIST | Time step control | $\bigcirc$ |  |  |  |
| PJUMP | Initial relocation |  | $\bigcirc$ |  | $\bigcirc$ |
| PLOTLN | Mapping of gap contact state |  |  |  | $\bigcirc$ |
| POWDIS | Calc. of power distribution |  | $\bigcirc$ |  |  |
| PPLOT | Auxiliary routine for PLOTLN |  |  |  | $\bigcirc$ |
| PRHIS2 | Output routine for power history | $\bigcirc$ |  |  |  |
| PRINT0 | Output of input data of thermal calculation |  | $\bigcirc$ |  |  |
| PRINT1 | Output of time-dependent variables in thermal analysis |  | $\bigcirc$ |  |  |
| PRINT2 | Output of time-dependent variables in gap gas state |  | $\bigcirc$ |  |  |
| PRINT3 | Output of time-dependent temperature distribution |  | $\bigcirc$ |  |  |
| PRINT5 | Detailed output of time-dependent variables in thermal analysis |  | $\bigcirc$ |  |  |
| PRIOPT | Option output in local mechanical analysis | $\bigcirc$ |  |  |  |
| PROPT2 | Option output for entire length analysis | $\bigcirc$ |  |  |  |
| PROBD1 | Setting of pellet axial force condition |  |  |  | $\bigcirc$ |
| PROBDF | Judgment of pellet/pellet contact state |  |  |  | $\bigcirc$ |
| PROBTY | Judgment of yield/unloading state |  |  |  | $\bigcirc$ |
| PROFIL | Address calculation by profile method |  |  |  | $\bigcirc$ |
| PSWEL | Pellet swelling strain |  |  |  | $\bigcirc$ |
| PSWELT | Pellet swelling strain by solid FP atoms |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| PTHCON | $\mathrm{UO}_{2}$ pellet thermal conductivity |  | $\bigcirc$ |  |  |
| PTHEX | Pellet thermal expansion |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| PUGH | Calc. of cladding creep by PUGH's reversal method |  |  |  | $\bigcirc$ |
| PUTHCN | MOX pellet thermal conductivity |  | 0 |  |  |

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Table Al (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PX2 | $\frac{\partial N}{\partial \xi}$ of quadratic element of FEM |  |  |  | $\bigcirc$ |
| PY2 | $\frac{\partial N}{\partial \eta}$ of quadratic element of FEM |  |  |  | $\bigcirc$ |
| RDGASI | Setting of time step width for gas transfer calculation in the axial direction |  | $\bigcirc$ |  |  |
| RDGAS2 | Diffusion and flow transfer of gas in the axial direction |  | $\bigcirc$ |  |  |
| RDTEMP | Control of entire thermal analysis |  | $\bigcirc$ |  |  |
| REDSTR | Re-distribution of FP density after grain growth of pellet |  | $\bigcirc$ |  |  |
| REPLG | Updating of stress and strain at gauss point |  |  |  | $\bigcirc$ |
| REPLN | Updating of displacement and nodal force at each node point |  |  |  | $\bigcirc$ |
| SBES0 | 0-th Bessel function |  | $\bigcirc$ |  |  |
| SBES1 | Primary Bessel function |  | $\bigcirc$ |  |  |
| SECOND | Calculation time (s) |  |  | $\bigcirc$ |  |
| SETPL1 | Mapping of cracked, elastic and plastic regions |  |  |  | $\bigcirc$ |
| SETPL2 | Mapping of cracked, elastic and plastic regions |  |  |  | $\bigcirc$ |
| SETPL3 | Mapping of cracked, elastic and plastic regions |  |  |  | $\bigcirc$ |
| SETPLT | Mapping of cracked, elastic and plastic regions |  |  |  | $\bigcirc$ |
| SETR | Re-meshing of pellet grains after grain growth |  | $\bigcirc$ |  |  |
| SETR0 | Initial setting of in-grain coordinate of pellet |  | $\bigcirc$ |  |  |
| SHAPE2 | Quadratic shape function |  |  |  | $\bigcirc$ |
| SOLVE | Solver for FP gas release calculation of 3 elements |  | $\bigcirc$ |  |  |
| SOLVE2 | Solver for FP gas release calculation |  | $\bigcirc$ |  |  |
| SOLVF2 | Setting of sliding state between pellet and cladding |  |  | $\bigcirc$ |  |
| SOLVF3 | Setting of clogged state between pellet and cladding |  |  | $\bigcirc$ |  |

Table Al (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| SSMAT | Formation of total matrix for each segment |  |  | $\bigcirc$ |  |
| STRESS | Stress strain calculation |  |  |  | $\bigcirc$ |
| SUFCN | Control of cladding surface heat transfer coefficient |  | $\bigcirc$ |  |  |
| SWELL | Pellet swelling model related to FP gas release model |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| TEMP1D | One dimensional heat conduction calculation |  | $\bigcirc$ |  |  |
| TERP | Calc. routine for ON-LINE PLOTTER plotter |  | $\bigcirc$ |  |  |
| THERFD | Calc. of gap closure by FP gas swelling of pellet |  | $\bigcirc$ |  |  |
| THGAPN | Deformation calculation in thermal analysis |  | $\bigcirc$ |  |  |
| TIC | Auxiliary routine for ON-LINE plotter | $\bigcirc$ |  |  |  |
| TIMEB | Time step control by pellet/pellet contact in the axial direction |  |  |  | $\bigcirc$ |
| TIMEG | Time step control by pellet/clad contact in the radial direction |  |  |  | $\bigcirc$ |
| TIMER | Main routine for time step control |  |  |  | $\bigcirc$ |
| TIMEY | Time step control by plasticity/unloading |  |  |  | $\bigcirc$ |
| TMELT | Calc. of pellet melting point |  | $\bigcirc$ |  |  |
| TMSTP | Determination of time step in entire length analysis |  |  | $\bigcirc$ |  |
| TYPE1 | ON-LINE plotter type 1 | $\bigcirc$ |  |  |  |
| TYPE2 | ON-LINE plotter type 2 | $\bigcirc$ |  |  |  |
| URSWEL | Chubb'sBMI model of pellet swelling strain |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| USMESH | Meshing for heat conduction calculation |  | $\bigcirc$ |  |  |
| USTEMP | Main routine for heat conduction calculation |  | $\bigcirc$ |  |  |
| VLUMES | Calc. of plenum volume |  | $\bigcirc$ |  |  |
| XBDMAT | $[B]^{\top}[D]$ matrix |  |  | $\bigcirc$ |  |
| XBMAT | [B] matrix |  |  | $\bigcirc$ |  |
| XCPEP2 | Calc. of cladding creep strain rate $\dot{\bar{\varepsilon}}^{\theta}$ |  |  | $\bigcirc$ |  |

Table Al (continued)

| Name | Function | P | T | M1 | M2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| XCPEQ2 | Calc. of $\dot{\bar{\varepsilon}}^{c}(=f)$ and $\frac{\partial f}{\partial \bar{\sigma}}, \frac{\partial f}{\partial \varepsilon^{c}}$ in cladding creep |  |  | $\bigcirc$ |  |
| XCPHD2 | Calc. of $\dot{\bar{\varepsilon}}^{H}(=g)$ and $\frac{\partial g}{\partial \sigma}, \frac{\partial g}{\partial \varepsilon^{H}}$ in cladding creep |  |  | $\bigcirc$ |  |
| XCPM11 | Formation of $\left[C^{C}\right]$ matrix and $\left\{\Delta \varepsilon^{c}\right\}$ vector in pellet creep |  |  | $\bigcirc$ |  |
| XCPM12 | Formation of strain increment $\left\{\Delta \varepsilon^{c}\right\}$ of pellet creep |  |  | $\bigcirc$ |  |
| XCREP1 | Formation of $\left[\mathrm{C}^{c}\right]$ matrix and $\left\{\Delta \varepsilon^{\top}\right\}$ vector in cladding creep |  |  | $\bigcirc$ |  |
| XCREP2 | Formation of strain increment $\left\{\Delta \varepsilon^{c}\right\}$ of cladding |  |  | $\bigcirc$ |  |
| XDPMAT | [ $D^{\text {' }}$ ] matrix |  |  | $\bigcirc$ |  |
| XDPST | Calc. of equivalent plastic strain increment |  |  | $\bigcirc$ |  |
| XDVSIG | Deviation stress |  |  | $\bigcirc$ |  |
| XELML1 | Formation of element matrix and loading vector |  |  | $\bigcirc$ |  |
| XELML2 | Calc. of stress and strain in element |  |  | $\bigcirc$ |  |
| XEQEPS | Equivalent strain |  |  | $\bigcirc$ |  |
| XEQSIG | Equivalent stress |  |  | $\bigcirc$ |  |
| XESMAT | Element stiffness matrix |  |  | $\bigcirc$ |  |
| XFHSFT | Stress-differential term in pellet yield function |  |  | $\bigcirc$ |  |
| XFLOAD | Element loading vector |  |  | $\bigcirc$ |  |
| XFTSFT | Temperature-differential term of pellet yield function |  |  | $\bigcirc$ |  |
| XIODD | Calc. of iodine concentration |  |  | $\bigcirc$ |  |
| XPCM | Main routine for the entire length analysis |  |  | $\bigcirc$ |  |
| XPJUMP | Initial relocation |  |  | $\bigcirc$ |  |
| XPRBTY | Judgment of plasticity/unloading |  |  | $\bigcirc$ |  |
| XPSWEL | Pellet swelling strain |  |  | $\bigcirc$ |  |
| XPUGH | Pugh's reversal method for cladding creep |  |  | $\bigcirc$ |  |

A3-(2) Subroutine Tree











ZORITA-1 GROUP A < ZOOIP > MOMINM
P. I. R. fuel rod
-Imput data
(1) Pellet specifications -


```
Fuel design data
    (Output in the case of IPRINT(2)=1)
```


## (1) Pellet

Inner diameter, outer diameter, shape, U235, enrichment, density ratio, height, axial segment length
A single asterisk is used to mark the
objective segment
In the case of dish pellet or chamfer pellet, form, pellet total weight, grain size, final density due to densification, and completion burn-up are output
(2) Others

Cladding material, inner diameter, outer diameter, ratio of thermal relocation, upper and lower plenum volumes, initial gas pressure, plasticity, pellet/cladding surface roughness, room temperature





```
Parameter list
(Output in the case of IPRNNT(4)=1)
```




```
Numu2 MAXIMM TRANSFER mOM NmOER IN EACH SEGMENT
\(\begin{array}{ll}\mathrm{HOL} & \begin{array}{l}1.000 \mathrm{E}-06 \\ \mathrm{~mol} \\ 2\end{array} \\ 2.000 \mathrm{E}=06\end{array}\)
```



``` DTPR RATIO OF VOL OF FP GAS RELEASE TO THAT OF PEEMM GAS AT EACH TIIE STEP eia control paraieter (used in deierainimg tiá siep midit)
0.050
```


(3) OPTION FOR OUIPUT OF THERMAL CNLCLATION

IWTHE
THERMAL INFORMAIION OUTPUT OPIION ( $=0 ;$ OFF,$=1$ :OW)
=1: TEMPERATU
$=2$ : GAP GAS
$=2$ :GAP GAS
$=3$ GRAIN RADIUS
$=4$ :INT
=4: INT RMBBLE RADIUS
5: INT. BLBERE DENSIT
=5: INT. BUBERLE DENSIT
=6: DIFFUSION COEF
$=6$ idIFFUSION COEF COE
$=7$ :EFFECT DIF.
=a:GRAIN ATOMS
=9: BOUNOARY ATOMS
=10:RLEASEO ATOUS
$=10:$ RELEASEO ATOMS
$=11: G R$ +BOU ATOUS

=13 PROOUCED ATOUS
$=14$ FISSION GAS
$=14$ : FISSION GAS RELEAS
$=15:$ BOUHOAMY DENSITY
16: BOUND. SAT. DENSITY
=17 BOHOATY PDESS

=19: THERMAL INFORMAIION
$=19$ : THERMAL GENERL OUTPUT
(4) OPIION FOR OUTPUT OF LOCN FEU CNLCULAIION
$\begin{aligned} & =1 \text { RADIAL SIRESS } \\ & =2: \text { AXIAL SIRESSES }\end{aligned}$
$=3$ CIRCIMFERENTIAL STRESSES
$\begin{aligned} & \text { 4: SHEAR STRESSES } \\ & =5 \text { :EOUIVALENT STRESSES }\end{aligned}$
$\begin{aligned} & =\text { S:EGUIVALENT SIRESSES } \\ & =\text { G:YIELD SIRESSES }\end{aligned}$
$=$ I; RhDINL Total. Strains
$\begin{aligned} & =8: A X I A L \text { TOTAL STRAINS } \\ & =9: G I R C M F E R E N T I M L \text { TTIAL STRAINS }\end{aligned}$
$\begin{aligned} & =10: \text { SHEAR IOINL STRAINS } \\ & =11 \text { EOUIVNLENT PPASTIC STRAIMS }\end{aligned}$
$\begin{aligned} & =11 \text { EONDNLENT PLASIIC S } \\ & =12 ; \text { RNIN CREEP SIRAINS }\end{aligned}$
$\begin{aligned} & =13 \text { : AXIAL CREEP STRAINS } \\ & =14: C \text { IRCIWFERENTIAL CREEP STRAINS }\end{aligned}$
$\begin{aligned} & \text { =14:CIRC CRFRENT IAL CREEP STRAI } \\ & =15 \text { SHEAR EREEP STRAINS }\end{aligned}$
$\begin{aligned} & \text { =15: SHEAR CREEP STRAINS } \\ & =16 \text { EOUVIVALENT CREEP STRAINS }\end{aligned}$
=17:RAOINL ELASIIC STRAINS
$\begin{aligned} & \text { 19:AXIAL ELASTIC STRAINS } \\ & =19 \text { CIRCUMFRENTIN ELSTIC STRAIH }\end{aligned}$
$\begin{aligned} & =20 \text { SHEAR ELASTIC STRAIMS } \\ & =21: \text { RADINL THERUN STRAS }\end{aligned}$
$\begin{aligned} & =22: \text { AXIAL THERMNL STRAINS } \\ & =23: S T R A I N S\end{aligned}$
$\begin{aligned} & \text { =23:STRAINS BY DENSIFIGATI } \\ & =24 \text { : STRAINS BY SWFILIMG }\end{aligned}$
$\begin{aligned} & \text { =27: } \\ & \text { =2: RAOINL CREEP STRAINS RAIE }\end{aligned}$
$=29: A \times 1$ AL CRREEP STRAINS RATE
$\begin{aligned} & =29: \text { AXIAL CPEEEP STRAINS RAE } \\ & \text { = } 30 \text { :CIRCWI CREEP STRIINS RATE }\end{aligned}$
$\begin{aligned} & \text { =31: SHEAR CREEP STRIINS RATE } \\ & =32 \text { : EOUI CREEP STRAINS RATE }\end{aligned}$
$\begin{aligned} & \text { =32:EOUN CREEP STRANS } \\ & =33 \text { RNDIN STRAIMS RAIE } \\ & =34\end{aligned}$
$\begin{aligned} & \text { =34: } \operatorname{AXINL} \text { STRAINS RATE } \\ & =35: G I R C L W F R E N T I N L ~ S T R A I M S ~ R A I E ~\end{aligned}$
$\begin{aligned} & \text { =35: CIRCMFERENTIAL STR } \\ & \text { =36; SHEAR STRAINS RATE }\end{aligned}$
=37: EQUIVALENT STRAIMS RA
$\begin{aligned} & \text { =33:EEOUIVALENT STRAIMS ENERO } \\ & \text { = }=39 \text { ITAS }\end{aligned}$
$\begin{aligned} & \text { =39:RMOINL DISTRIBUTION ENER TEMP. } \\ & =10: \text { PGIEL } \\ & \text { = }\end{aligned}$
$\begin{aligned} & =40 \text { :PELLEI/GLADDIMO INTERAGIION } \\ & =41 \text {; PELLET/PELETTE INTERAGTION }\end{aligned}$
$=42$ DISPLACE
$=43$; PCAI PLOT



## (5) OPTION FOR OUTPUT OF HOLE ROD FEN CNLCULATION

IWROD ECHANICAL IMFORMAIION OUIPUT CONTROL TABLE $(=0 ;$ OFF $=1:$ OWI $=1:$ RRDIAL STRESS
$=2: G I R C A M$ STRESS
$=2:$ GIRCN STM STRESS
$=3 ; A 1 N$ St
$=4$ :EQUI. STRESS
1:EQUL, STRESS
$=$ 5:YELO STRESS
= G;RADIN CREEP STRAIM
$=7$
$=7$ i:GIRNM. CREEP SIRAIM
$=8:$ AXINL CREEP STRAIM

$=9$ :ECUI. HWRO STRAIM
$=10:$ EUI PLS. STRAI
$=11$ STIELIMG STRAIM
$=10: E O U I$ MLAS STRAM
$=11 ;$ SIELIMG STM
$=12$ :RADINL TOTAL STRAIM $=12:$ RADIN TOTAL STRAIM
$=13: G I R G M$ TOTA STRAIN =13:CIRGMM TOTAL STRAI
$=14$ :NKINL TOTAL STRAIN $=14$ :AXINL TOTM STRAIM
$=15:$ THERML STRAIM

=17:PRESSURE
=19:MOOE DISPLACEMENT
(6) OPTION FOR GETTIMG PLOTTER TAPE

-1
-5

## **** history oata (1)

| $\begin{aligned} & \text { STAGE } \\ & \text { (WOISI) } \end{aligned}$ | $\begin{gathered} \text { IIME } \\ (H: \mathbf{H}) \end{gathered}$ | ( $100 /$ TH02 $)$ | $\begin{aligned} & \text { BURNUP } \\ & \text { (mo/Tu) } \end{aligned}$ | ( $0 \mathrm{~J} / \mathrm{KOU}$ ) | L. H. R. (W/CN) | $\begin{aligned} & \text { COOLNTT } \\ & \text { IEWP. } \\ & \text { (DEG. K) } \end{aligned}$ | COOLMT PRESS. (MPA) | COOLNTT (II/5) | FASI MEWTRON FLUX $(\mathbf{N} / \mathrm{CM} 2$. | $\begin{aligned} & \text { HISTRY } \\ & \text { OPIIOW } \\ & \text { (O=OFF) } \end{aligned}$ | $\begin{aligned} & \text { PRIRT } \\ & \text { OPIION } \\ & (I=O W) \end{aligned}$ | $\begin{aligned} & \text { SS/US } \\ & \text { OPIION } \\ & (1=O N) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0: 0: 0 | 0.0 | 0.0 | 0.00 | 0.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 0 | 0 | 0 |
| 2 | 5: 0:0 | 3. 9 | 4.4 | 0. 38 | 260. | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 0 | 0 | 0 |
| 3 | 2917:28:45 | 4407.2 | 5000.0 | 431.47 | 260.0 | 555. 15 | 13. 79 | 6.5 | 5. $3000+13$ | 0 | 0 | 0 |
| 4 | 5632:27:30 | 8814.5 | 10000.0 | 852.94 | 260.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 0 | 0 | 0 |
| 5 | 8447:26:15 | 13221.7 | 15000.0 | 1294.40 | 260.0 | 555.15 | 13. 79 | 6. 5 | 5. $3000+13$ | 0 | 0 | 0 |
| 6 | 11262:25: 0 | 17628.9 | 20000.0 | 1725. 67 | $260 . a$ | 555.15 | 13.79 | A. 5 | 5. $3000+13$ | 0 | 0 | 0 |
| 7 | 14077:23:45 | 22036.1 | 25000.0 | 2157.34 | 250.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 0 | 0 | 0 |
| 8 | 17230:10:22 | 26972. 2 | 306000 | 2640.59 | 260.0 | 555. 15 | 13. 79 | 6. 5 | 5. $3000+13$ | 0 | 0 |  |
| 9 | 17235:10:22 | 26980.7 | 30609.a | 2641.41 | 304.0 | 555. 15 | 13. 79 | 6.5 | 5. $3000+13$ | -100 | 0 | 0 |
| 10 | 18396: 9:27 | 29087.7 | 33000.0 | 2947, 69 | 304.0 | 555.15 | 13. 79 | 0.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 11 | 19830:41:11 | 31732.0 | 36000.0 | 3106.57 | 304.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 12 | 21275:12:55 | 34376.4 | 39000.0 | 3365. 45 | 304.0 | 555. 15 | 13. 79 | 6. 5 | 5. $3000+13$ | 100 | 0 | 0 |
| 13 | 22960:29:56 | 37461.4 | 42500.0 | 3687. 48 | 304.0 | 555. 15 | 13. 79 | 6.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 14 | 22985:29:58 | 37470.1 | 42509.8 | 3668. 32 | 269.0 | 555. 15 | 13.78 | 8.5 | 5. $3000+13$ | -100 | 0 | 0 |
| 15 | 24320:34:21 | 39685.1 | 45000.0 | 3883. 21 | 269.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 16 | 25953: 3: 4 | 42309.4 | 48000.0 | 4142.09 | 269.a | 555. 15 | 13.79 | 0.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 17 | 27585:31:47 | 44953.7 | 51000.0 | 4400.97 | 289.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 18 | 29218: 0:30 | 47598.1 | 54000.0 | 4659.85 | 269. | 555. 15 | 13. 79 | 6.5 | 5. $3000+13$ | 100 | 0 | 0 |
| 19 | 31122:34:0 | 50683. 1 | 57500.0 | 4961. 88 | 269.0 | 555. 15 | 13.79 | 6.5 | 5. $3000+13$ | 100 | 1 | 0 |
| 20 | 31127:34: 0 | 50691. 2 | 57509.2 | 4962.67 | 269.0 | 555.15 | 13. 79 | 6.5 | 5. $3000+13$ | -100 | 0 | 0 |
| 21 | 31132:34: 0 | 50695. 3 | 57513.8 | 4963.07 | 0.0 | 291. 15 | 0.10 | 6. 5 | 1. 0000009 | -100 | 2 | 0 |

[^1] option
**** HISTORY DATA (2) ****

| $\underset{\text { (WTACE }}{\substack{\text { STI }}}$ | $\stackrel{\mathbf{H} \boldsymbol{H} \mathbf{M E}}{(\mathbf{M}: \mathrm{s})}$ | $\begin{gathered} \text { L.H/R } \\ (\mathbf{W} / \mathrm{Cm}) \end{gathered}$ | (1) | ( 2) | ( 3 ) | (4) | $\underset{(5)}{\substack{x \\(5)}}$ | $\underset{(6)}{\operatorname{MODE}}$ |  | actor $\text { ( } 8 \text { ) }$ | (9) | (10) | (11) | (12) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0: 0: 0 | 0.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 2 | 5: 0:0 | 260.00 | 0.800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 |  | 0 | 0 | 0 |
| 3 | 2817:28:45 | 260.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 4 | 5632:27:30 | 260.00 | 0. 800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 5 | 8447:26:15 | 260.00 | 0.800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1. 000 | 0. 500 | 0 | 0 | 0 | 0 |
| 0 | 11262:25: 0 | 260.00 | 0.800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1. 000 | 0. 500 | 0 | 0 |  | 0 |
| 1 | 14077:23:45 | 280.00 | 0.800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1. 000 | 0. 500 |  | 0 | 0 | 0 |
| 8 | 17230:10:22 | 260.00 | 0. 800 | 1.050 | 1. 140 | 1. 200 | 1.160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 9 | 17235:10:22 | 30400 | 0.800 | 1.050 | 1. 140 | 1. 200 | 1.160 | 1. 150 | 1. 000 | 0. 500 | 0 | 0 | 0 | 0 |
| 10 | 18386: 9:27 | 304.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1. 000 | 0. 500 | 0 | 0 | 0 | 0 |
| 11 | 19830:41:11 | 304.00 | 0. 800 | 1.050 | 1. 140 | 1. 200 | 1. 180 | 1. 150 | 1. 000 | 0. 500 | 0 | - | 0 | 0 |
| 12 | 21275:12:55 | 304.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 13 | 22960:29:58 | 304.00 | 0. 800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | 1.150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 14 | 22985:29:56 | 269.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1.160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 15 | 24320:34:21 | 269.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | I. 150 | 1.000 | 0. 500 | - | 0 | 0 | 0 |
| 16 | 25953: 3: 4 | 289.00 | 0. 800 | 1.050 | 1.140 | 1. 200 | 1.180 | 1. 150 | 1.000 | 0. 500 | - | 0 | - | 0 |
| 17 | 27505:31:47 | 289.00 | 0. 800 | 1.050 | 1. 140 | 1.200 | 1. 180 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 18 | 29218: 0:30 | 269.00 | 0.800 | 1.050 | 1. 140 | 1. 200 | 1. 180 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 19 | 31122:34: 0 | 269.00 | 0. 800 | 1.050 | 1. 140 | 1. 200 | 1. 160 | f. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 20 | 31127:34: 0 | 26900 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| 21 | 31132:34: 0 | 0.00 | 0. 800 | 1. 050 | 1. 140 | 1. 200 | 1. 160 | 1. 150 | 1.000 | 0. 500 | 0 | 0 | 0 | 0 |
| FEE | nulysis is | applied at | SEGwent | Of mun | ater 4 |  |  |  |  |  |  |  |  |  |

History of relative power profile in the axial cirection




## fission ans resul

| 10.00500 | 2000095 | 3 | 0.01906 | 40.03857 | 50.02909 | 6 | 0.03113 | 70.00618 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |



Thermal analysis results at each time step (Output in the case of IPRINT(6)=1)

Time-step number, time
coolant temperature, coolant pressure
Linear heat rate, burnup, gap conductance (total gas, solid, radiation), temperature (pellet center pellet surface, cladding inner surface, cladding outer surface), radial gap size, contact pressure

Pellet inner/outer power density ratio, factor for power profile, burnup, pellet displacement (thermal expansion, swelling, densification, relocation, total), cladding displacement (thermal expansion, elasticity, creep, total)

Cladding surface temperature, oxide film growth rate, oxide film thickness

Initial gas molar number,
FP gas release rate of each axial segment, average FP gas release rate of the rod, fuel rod inner pressure, fuel rod space volume (gap, plenum), total gas molar number, iodine concentration (average, maximum), produced gas, released gas, gas molar number inside the fuel rod

|  | RNO 14 1 $\stackrel{\operatorname{se}}{8}$ | temeratu <br> 1436 |  |  |  | $\begin{aligned} 10 \ldots \\ \cdots \end{aligned}$ |  |  |  | 501.22 <br> 608. 39 <br> 585. 27 <br> 548. 10 <br> 514.38 513.58 |  | Temperature distribution in the radial direction of the objective segment <br> Hereafter, items designated by IWTHE(i) are output |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | temperature distribution in the flel (deg. c) |  |  |  |  | IITHE= | 1 |  |  |  |
|  |  |  |  |  | $\begin{array}{r} 655.91 \\ 825.60 \\ 1083.59 \\ 1041.68 \\ 1056.74 \\ 980.13 \\ 891.48 \\ 783.18 \end{array}$ |  | 608.24 <br>  ${ }^{892} .12$ 838. 81 768. 85 697.60 $\rightarrow$ |  | 541.28 647.19 <br> 719.52 <br> 695. 26 <br> 652.30 <br> 606.17 581.10 |  |  | Temperature distribution in the pellet |
|  | 1 | gap as | INFORM位 |  |  |  |  | IITHE | $1$ |  |  | Gas composition |
| $\begin{aligned} & 1 \\ & N \\ & N \\ & 0 \end{aligned}$ | SEO <br> 8 <br> 7 <br> 7 <br> 5 <br> 4 <br> 3 <br> 3 <br> 2 | HE. 96.4. 96.0 95.4 95.1 95.0 95.0 95.1 95.2 95.3 | M2 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 | KR 0.5 0.5 0.5 0.6 0.6 0.6 0.6 0.6 0.6 | XE 3.1 3.5 4.0 4.2 4.3 4.2 4.2 4.1 |  |  |  |  |  |  |  |
|  | 1 | reolus | gran (1m |  |  |  |  | ITTHE $=3$ | -1 |  |  | Pellet grain size |
|  | se <br> 8 <br>  <br> 8 <br> 5 <br> 4 <br> 3 <br> 3 <br> 2 <br> 1 |  |  | 5.00 5.00 5.00 5.01 5.01 5.09 5.00 5.00 5.00 |  |  |  | 5.00 5.00 5.00 5.00 5.00 5000 5.00 5.00 5.00 | 5. 00 S. 5.0 5.0 5.00 5.00 5.00 5.00 5.00 |  |  |  |
|  | 1 | Ruolus | F Intregre | ne ans aub | $E$ ( Mmasta |  |  | ITHTH= | $1$ |  |  | Radius of intragranular gas bubble |
|  | $\stackrel{2}{1}$ |  |  |  |  |  |  | 3.32 4.38 4.308 4.60 4.62 4.67 4.58 4.4 4.48 4.00 | 3.32 4.368 4.308 4.82 4.82 4.67 4.58 4.4 4.00 | 3.32 4.36 4.360 4.60 4.82 4.67 4.59 4.4 4.4 4.00 |  |  |



| paseapar suote ses da jo arqumn |  |  |  |
| :---: | :---: | :---: | :---: |





D_DISPLACEMENT OF MOOES (MICROW) IWEEN 42

Time-step number, time, linear heat rate, fast neutron flux, fission rate, burnup, coolant temperature, coolant pressure
Hereafter, items designated by IWFEM (i) are output
Temperature distribution in the radial direction

Pellet/cladding contact status

Contact state, radial and axial components of the contact stress increment, radial and axial components of the contact stress, radial gap

## Pellet/pellet contact states

Contact states, stress increment in the axial direction, axial stress, axial displacement, contact boundary, distance to the contact boundary

[^2]
$\qquad$
axin stresses in the fuel ano the cladoimo ( $1(1 / 2 * * 2)$

IWFEW 2 1

| S10 (2) |  |  |  |  |  |  |  |  |  | 0 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -0. 5 | -0. 1 | -0. 4 | -0. 2 | -0. 5 | -0. 2 | -0.7 | -2.9 | -3. 8 | -3. 1 | 1 | -20.0 | -18. 9 |
| -1. 0 | $-1.8$ | -0. 8 | -1.7 | -0. 9 | -2. 2 | -1.8 | -1.7 | -2. 2 | -1.6 |  | -18.2 | -21.4 |
| -2.7 | -1.7 | -2. 5 | -1.6 | -2. 5 | $-1.7$ | -2. 2 | -2.3 | -1.8 | -1.9 | 1 | -16.0 | -21.1 |
| -2.1 | -2.9 | -2. 6 | -2.8 | -2.5 | -2. 6 | -2.4 | -2.4 | -2.2 | -2.3 |  | -18.3 | -18.2 |
| -3. 1 | -3. 1 | -2.9 | -3.0 | -2. 8 | -2.8 | -2.8 | -2.5 | -2.5 | -2.0 |  | -16.6 | -16.8 |
| -3. 3 | -3. 2 | . 2 | -3.0 | -3.0 | -3.0 | -2.9 | -2.8 | -2.5 | -2.3 |  | -16.3 | -15. 8 | an | -3.3 | -3.1 | -2.9 | -3.0 | -2.8 | -2.8 | -2.8 | -2.5 | -2.5 | -2.0 | -16.6 | -16.8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -3.2 | -3.2 | -3.0 | -3.0 | -3.0 | -2.9 | -2.8 | -2.5 | -2.3 | 1 | -16.3 | -15.8 |


| S10(1) |  |  |  |  |  |  |  |  |  | cap |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -1. 1 | -0. 9 | -1.3 | -1.2 | -1.7 | -1.6 | -2. 2 | -3. 5 | -4.0 | -4. 2 | 1 | -31.6 | -34. 6 |
| -2. 2 | -3.1 | -2. 2 | -3. 2 | -2.3 | -3. 3 | -2. 8 | -2.5 | -3.1 | -3.2 | 1 | -32.1 | -36. 1 |
| -3. 5 | -2. 6 | -3, 5 | -2.7 | -3. 6 | -2. 6 | ${ }^{-3.1}$ | $-3.3$ | -3. 0 | ${ }^{-3.9}$ | 1 | -31.8 | -36. 9 |
| -3. 3 | -3. 5 | -3.4 | -3. 5 | -3.4 | -3. 5 | -3. 2 | -3. 4 | -3. 3 | -4.0 | 1 | -31.7 | -35. B |
| -3.6 | -3.8 | -3. 5 | -3.7 | -3. 5 | -3. 5 | -3.6 | -3.4 | -3.6 | -3.7 | 1 | -31.3 | -34. 3 |
| -3. 7 | -3. 7 | -3. 7 | -3. 7 | -3. 7 | -3. 6 | -3. 6 | -3. 5 | -3. 5 | -3. 9 |  |  |  |



Stress in the circumferential direction


-872-


## Summary of thermal analysis of the objective segment <br> (Output in the case of $\operatorname{IPRINT}(8)=1$ )

Time-step number, time, linear heat rate, burnup, temperature (pellet center, pellet surface, inner surface and outer surface of cladding), gap conductance (total, gas, solid), radial gap width, contact pressure, amount of gas produced, FP gas release ratio, iodine concentration, computation time

Summary of thermal analysis and
mechanical information for the objective
segment
(Output in the case of (IPRNTT(9)=1)
Time-step number, time, linear heat rate, burnup

Pellet:
thermal expansion, creep, densification, swelling, relocation, total amount of radial displacement

## Pellet-cladding:

radial gap width, contact pressure

## Cladding:

thermal expansion, elastic deformation, creep, total amount of radial displacement

| POWER |  | HISTORY I |  |  |  | FUEL CENTER |  |  |  |  | 1 | IFUEL-CLAD |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { STEP } \\ & \text { No. } \end{aligned}$ | HILE |  |  | FLEA CENTER TEWP. (DEO. C) | cpaln radius (MIC) | BUBELE RADIUS <br> (ancst) |  | DIFFUS. COEFF. (100-18 | DIFFUS COEFF /EFFECI CW2/S) | gas <br> DENS AT BOMD. (10013 | SATURA DENS. AI/CH2) | LOCAL FGR AT CENTER (*) | FISSON ans relase |  | KE+KR percemt in gap ( $\times$ ) |
| 1 | 0.0 | 0.0 | 0.0 | 282.0 | 5.00 | 0.00 | 19.35 | 0.2 | 0. 20 | 0.0 | 567.7 | 0. 50 | 0.50 | 1.31 | 0.00 |
| 33 | 5.0 | 312.0 | 4.7 | 1231.7 | 5. 00 | 0.06 | 19. 12 | 0.2 | 0. 20 | 0.0 | 430.2 | 0. 50 | 0.50 | 0.67 | 0.00 |
| 45 | 29175 5632 | 312.0 | 5288.7 | 1249.6 | 5. 50 | 5.45 6.46 | 8.11 | ¢. ${ }^{\text {c }}$ - | 5. 18 | 138.5 | 2282 | - 0.50 | 0.50 | 0.71 | 0. 19 |
| 67 | 8447.4 | 312.0 | 15868.0 | 1208.7 | 5. 40 | 6. 55 | 7.07 | 3.6 | 3. 14 | 235.0 | 235.0 | 17.24 | 1.01 | 0. 64 | 0. 52 |
|  | 11262.4 | 312.0 | 21154.7 | 1178.6 | 5. 40 | 6. 55 | 7.07 | 2.2 | 2.07 | 24.4 | 241.5 | 19.84 | 1. 14 | 0.60 | 0.83 |
| 89 | 14077.4 | 3120 | 26443.4 | 1147.2 | 5. 40 | 6. 55 | 7.07 | 1.4 | 1.32 | 248.5 | 248.8 | 19. 21 | 1.09 | 0.55 | 0. 72 |
| 101 | 17230.2 | ${ }^{312} 0$ | 32366.7 | 1114.5 | 5.40 | 6. 55 | 7.07 | 0.9 | 0.84 | 256.5 | 256. ${ }^{\text {a }}$ | 16.65 | 0. 99 | 0.50 | 0.86 |
| 107 | 17235. 2 | ${ }^{364}{ }^{\text {a }}$ | 32376. 9 | 1269. 2 | 5. 40 | 11. 30 | 4.26 | 8.8 | 7.19 | 232.8 | ${ }^{232.8}$ | 17. 92 | 1. 03 | 0.48 | 1.37 |
| 114 | 18386.2 | 364.8 | 34905. 2 | 1261.6 | 5. 40 | 11.35 | 4.24 | 7.8 | 6.57 | 236.3 | 236.3 | 34. 53 | 2.63 | 0.49 | 7.58 |
| 121 | 19830.7 | 304.8 | 38078. 1 | 1258.1 | 5.40 | 11.35 | 4.24 | 7.4 | 6. 28 | 239.4 | 239.4 | 41.00 | 3. 31 | 0. 50 | 7.15 |
| 128 | 21275. 2 | 364. 8 | 41251.7 | 1268.2 | 5.40 | 11.35 | 4.24 | 8. 5 | 7.11 | 238.3 | 238.3 | 46. 52 | 3. ${ }^{96}$ | 0.50 | 7.40 |
| 136 | 22960.5 | 364. 8 | 44953.7 | 1282.5 | 5. 40 | 11. 35 | 4.24 | 10.5 | 8.41 | 237.9 | 237.9 | 52. 84 | 4.72 | 0.50 | 9. 50 |
| 141 | 22965.5 | 322.8 | 44964.1 | 1129.0 | 5. 40 | 11.35 | 4. 24 | 1.1 | 1.03 | 231.6 | 262.6 | 52.63 | 4.72 | 0.53 | 8. 23 |
| 148 | 24320. 6 | 322. 8 | 47598.1 | 1130.6 | 5. 40 | 11.35 | 4.24 | 1.1 | 1. 06 | 170.6 | 262.7 | 49.74 | 4. 49 | 0.53 | 4. 94 |
| 155 | 25953.1 | 322.8 | 50771.3 | 1137. ${ }^{118}$ | 5. 40 | 11. 35 | 4. 24 | 1.2 | 1.17 | 217.7 | 262.0 | 46.67 | 4.24 | 0.53 | 4.03 |
| 162 | 27585.5 | 322. ${ }^{\text {a }}$ | 53944.5 | 1146. 9 | 5. 40 | 11. 35 | 4.24 | 1.4 | 1. 34 | 281.0 | 261.0 | 44.39 | 4.02 | 0.53 | 3. 83 |
| 169 | 29218.0 | 322.8 | 57117.7 | 1157.6 | 5. 40 | 11. 35 | 4. 24 | 1.6 | 1.56 | 259.9 | 259.9 | 44.17 | 3. 88 | 0. 52 | 4.07 |
| 177 | ${ }^{31122.6}$ | 322.8 | 60119.7 | 1172.1 | 5. 40 | 11. 35 | 4. 24 | 2.0 | 1.93 | 258.6 | ${ }^{258.6}$ | 45.07 | 3. 86 | 0. 52 | 5. 00 |
|  | 31127.6 | 322. 8 | 60829.5 | 1172.6 | 5. 40 | 11. 35 | 4.24 | 2.0 | 1.94 | 258.5 | 258.5 | 45.07 | 3. 86 | 0.52 | 5.00 |
| 211 | 31132.6 | 0.0 | 60834.3 | 18.0 | 5. 40 | 11.35 | 4. 24 | 0.2 | 0.20 | 244.9 | 755.8 | 45.07 | 3. 86 | 0.90 | 4.27 |

Summary of thermal analysis and FP gas information for the objective segment
(Output in the case of $\operatorname{IPRINT}(10)=1$ )

Time-step number, time, linear heat rate, burnup

Pellet center:
temperature, grain size, bubble radius, bubble density, diffusion coefficient, effective diffusion coefficient, FP gas density at grain boundary, FP gas density limit, FP gas release ratio

The objective segment:
FP gas release ratio, gas molar number in gap, percentage of $\mathrm{Xe}+\mathrm{Kr}_{\mathrm{r}}$ in gap gas

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline \multicolumn{2}{|l|}{POMER} \& \multicolumn{3}{|l|}{HISTORY} \& \& \multicolumn{4}{|r|}{FUEL ROD} \& \& \& \& \& \& \\
\hline \[
\begin{aligned}
\& \text { STEP } \\
\& \text { NO. }
\end{aligned}
\] \& (IME \& \[
\begin{aligned}
\& \text { LINEAR } \\
\& \text { HEAT } \\
\& \text { RATE } \\
\& \text { (W/GI) }
\end{aligned}
\] \&  \& \[
\begin{aligned}
\& \text { RNUP } \\
\& \text { (10020 } \\
\& \text { FISS/CC) }
\end{aligned}
\] \& \[
\begin{aligned}
\& \text { PROOUCE } \\
\& (X E+K R)
\end{aligned}
\] \& \[
\begin{gathered}
\text { MELLONT } \\
\begin{array}{c}
\text { PEEASE } \\
\text { (KEKE) } \\
(100-3
\end{array}
\end{gathered}
\] \& \begin{tabular}{l}
of gas PLEMH \\
3 MO.E)
\end{tabular} \& Qap \& total in FUEL ROO \& FRACT
If
(x) \& an of

N2

$(\times)$ \& $\underset{\substack{\text { KR } \\(4)}}{ }$ \& $$
\begin{aligned}
& \text { XE } \\
& (\mathbf{x})
\end{aligned}
$$ \& FISSIO GAS release ( ${ }^{(1)}$ \& INWER GAS PRESSURE (MPA) <br>

\hline 1 \& 0.0 \& 0.0 \& 0.0 \& 0. 0 \& 0.00 \& 0.00 \& 44.11 \& 10.47 \& 54. 57 \& 10000 \& 0.00 \& 0.00 \& 0.00 \& 0. 50 \& 8. 58 <br>
\hline 33 \& 5.0 \& 312.0 \& 4.7 \& 0.00 \& 0.01 \& 0.00 \& 48. 34 \& 6. 23 \& 54.57 \& 100.00 \& 0.00 \& 0.00 \& 0.00 \& 0.50 \& 7.67 <br>
\hline 45 \& 2817.5 \& 312.0 \& 5288. 7 \& 1.47 \& 8. 89 \& 0.04 \& 49. 09 \& 6. 52 \& 54.62 \& 99. 92 \& 0.00 \& 0.01 \& 0.07 \& 0. 50 \& 7.48 <br>
\hline 56 \& 5632.5 \& 312.0 \& 10577. 3 \& 2. 93 \& 17. 76 \& 0.09 \& 48.21 \& 6. 46 \& 54.67 \& 99. 83 \& 0.00 \& 0.02 \& 0.15 \& 0. 53 \& 7.46 <br>
\hline 67 \& 8447.4 \& 312.0 \& 15886.0 \& 4. 40 \& 26. 64 \& 0.16 \& 48. 49 \& 6.25 \& 54. 73 \& 99.71 \& 0.00 \& 0.04 \& 0.26 \& 0.61 \& 7.50 <br>
\hline 78 \& 11282.4 \& 312.0 \& 21154.7 \& 5. 87 \& 35. 52 \& 0. 23 \& 48. 82 \& 5. 98 \& 54.80 \& 99. 58 \& 0.00 \& 0.05 \& 0.36 \& 0.65 \& 7.57 <br>
\hline 89 \& 14077.4 \& 312.0 \& 26443. 4 \& 7.34 \& 44. 40 \& 0.28 \& 49. 17 \& 5. 69 \& 54. 85 \& 99.49 \& 0.00 \& 0.07 \& 0.45 \& 0.63 \& 7.64 <br>
\hline 101 \& 17230.2 \& 312.0 \& 32366. 7 \& 8. 98 \& 54. 35 \& 0.33 \& 49. 58 \& 5. 33 \& 54.90 \& 99.40 \& 0.00 \& 0.09 \& 0. 53 \& 0.61 \& 7. 73 <br>
\hline 107 \& 17235. 2 \& ${ }^{364.8}$ \& 32376. 9 \& a. 98 \& 54. 37 \& 0.34 \& ${ }^{50} 500$ \& 4.91 \& 54.91 \& 99. 38 \& 0.00 \& 0.08 \& 0.54 \& 0. 62 \& 7.91 <br>
\hline 114 \& 18386. 2 \& 364. 8 \& 34905. 2 \& 9.89 \& 58. 81 \& 0.85 \& 50. 58 \& 4. 84 \& 55. 42 \& 98. 47 \& 0.00 \& 0.20 \& 1.33 \& 1. 44 \& 7.91 <br>
\hline 121 \& 19830.7 \& 384. 8 \& 38078.4 \& 10.50 \& 03. 94 \& 1.15 \& 50.91 \& 4.82 \& 55.72 \& 97. 94 \& 0.00 \& 0.27 \& 1.79 \& 1.80 \& 7.98 <br>
\hline 128 \& 21275. 2 \& 364. 8 \& 41251.7 \& 11. 44 \& 69. 27 \& 1. 43 \& 51.19 \& 4. 82 \& 56. 00 \& 97. 44 \& 0.00 \& 0.33 \& 2. 23 \& 2. 07 \& 8.04 <br>
\hline 1138 \& 22950.5
22965.5 \& 364.8 \& 44953.7 \& 12.47
12.47 \& 75. 49
75.50 \& 1.81 \& 51.56
51.33 \& 4. 82
5
5 \& 56.38
56.38 \& 96.79
98.79 \& 0.00
0.00 \& 0. 42 \& 2. 79 \& 2. 2.40 \& 8.12
8.07 <br>
\hline 148 \& 24320.6 \& 322.8 \& 47598.1 \& 13. 21 \& 79.93 \& 1. 83 \& 51. 35 \& 5. 06 \& 56.40 \& 96. 75 \& 0.00 \& 0.42 \& 2.92 \& 2. 29 \& 8. 09 <br>
\hline 155 \& 25953.1 \& 322. ${ }^{\text {8 }}$ \& 50771.3 \& 14.09 \& 85. 25 \& 1.86 \& 51.39 \& 5.04 \& 56.43 \& 98.71 \& 0.00 \& 0.43 \& 2.86 \& 2. 18 \& 8.11 <br>
\hline 162 \& 27585.5 \& 322.8 \& 53944.5 \& 14.97 \& 90. 58 \& 1.88 \& 51.44 \& 5.02 \& 56.45 \& 96.66 \& $0 . \infty$ \& 0.43 \& 2. 90 \& 2.08 \& 8. 14 <br>
\hline 169 \& 29218.0 \& 322. 8 \& 57117.7 \& 15. 85 \& 95. 91 \& 1.93 \& 51.52 \& 4.98 \& 56. 50 \& 96. 59 \& 0. 00 \& 0.44 \& 2. 97 \& 2. 01 \& 8.18 <br>
\hline 177 \& 31122.6 \& 322. 8 \& 60819.7 \& 16.87 \& 102. 13 \& 2. 05 \& 51. 68 \& 4.94 \& 56. 62 \& 96. 39 \& 0. 00 \& 0.47 \& 3. 14 \& 2. 00 \& 8.23 <br>
\hline 178 \& 31127.6 \& 322.8 \& 60829. 5 \& 16. 89 \& 102. 14 \& 2.05 \& 51. 69 \& 4. 93 \& 56.62 \& 96. 39 \& 0.00 \& 0.47 \& 3. 14 \& 2.00 \& 8. 23 <br>
\hline 211 \& 31132.6 \& 0.0 \& 60834.3 \& 16. 88 \& 102.15 \& 2.05 \& 48.74 \& 7. 88 \& 56.62 \& 96. 39 \& 0.00 \& 0.47 \& 3.14 \& 2.00 \& 3. 84 <br>
\hline
\end{tabular}

Summary of thermal analysis and FP gas information for whole fuel rod (Output in the case of IPRINT(11)=1)

Time-step number, time, linear heat rate, burnup

Whole fuel rod:
amount of FP gas produced, amount of FP gas released, gas molar number in the plenum, gas molar number in the gap, total gas molar number, gas composition, FP gas release rate, inner pressure of the fuel rod

| POMER |  | HISTORY |  | TOP Of flel |  |  |  | 1 fuel - | CLAD AT TOP 1 |  | 1 |  | I dinmetral ridge |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\overline{\text { STEP }}$ | THE | LIMEAR HEAT RATE ( ${ }^{(1 / C M}$ ) | $\begin{aligned} & \text { suravep } \\ & \text { (MmD/ } \\ & \text { (1402) } \end{aligned}$ | AXIAL DIPS CENTER (M\|G) | $A X I A L$ DIPS SURFACE ( $\mathrm{M} \mid \mathrm{C}$ ) | RADIAL OIPS INNER ( $\left.{ }_{(1)} 16\right)$ | RADIAL DIPS OUTER ( $\mathrm{Cl} / \mathrm{C}$ ) | $\begin{aligned} & \text { RNDIN } \\ & \text { GAP AT } \\ & \text { TOP } \\ & \text { (MIC) } \end{aligned}$ | contac PRESS AXIAL ( (IPA) | $\begin{aligned} & \text { CONTACT } \\ & \text { PRESS. } \\ & \text { RAOIAL } \\ & (\mathbb{P N A}) \end{aligned}$ | $A X \mid A 1$ 01SP AT TOP (U\|C) | rabial DISP OUT/TOP (-IC) |  | RIDGE HEIGHT (MAX) ( 1 IC) | $\begin{aligned} & \text { RIDGE } \\ & \text { HEIGHT } \\ & \text { (IOP MID } \\ & (M \mid C) \end{aligned}$ |
| 1 | 0.0 | 0.0 | 0.0 | 0.00 | 0. 0 | 0.0 | 0.00 | 39.74 | 0.0 | a. 00 | a. 0 | 0.00 | 0.00 | 0. 0 | 0.00 |
| ${ }^{3} 3$ | 5.0 | 3120 | 4.7 | 67. 69 | 4327 | 0.00 | 78.17 | 2. 27 | 0.00 | 0. 00 | 2.33 | 3. 63 | 3.63 | 0.00 | $0 . \infty$ |
| 45 | 2817.5 | 312.0 | 5288.7 | 48. 87 | 11. 91 | 0.00 | 47. 00 | 6. 42 | 0.00 | 0.00 | 13. 31 | $-17.03$ | -17.03 -28 | 0.00 | 0. 0 |
| ${ }_{6}^{56}$ | 5632.5 8447 | 312.0 312.0 | 10571.3 15866.0 | 51.47 56.02 | 9. ${ }^{\text {9. }} 131$ | $0 . \infty$ 0.00 | 47.73 <br> 43.65 | 0.71 0.00 | 0.00 1.52 | 0.00 <br> 3.80 <br> 80 | 17.77 | -26.68 | -28.68 -33.72 | 0.00 2.36 | 0. 1. 1 |
| 78 | 11282.4 | 312.0 | 21154.7 | 65. 40 | 17.60 | 0.00 | 43.57 | 0.00 | 3.11 | 7. 78 | 24.15 | -31.74 | -33. 59 | 4.21 | 1.85 |
| 9 | 14077.4 | 312.0 | 26443.4 | 81.79 | 21. 87 | 0.00 | 46. 59 | 0.00 | 3. 83 | 9. 58 | 26.55 | -28.89 | -31. 09 | 4.81 | 2. 20 |
| 101 | 17230.2 | 312.0 | 32366.7 | 105.73 | 26. 74 | 0.00 | 51.79 | 0.00 | 4.99 | 12. 48 | 29.50 | -24.04 | -26. 28 | 6. 03 | 2. 24 |
| 107 | 17235.2 | ${ }^{364.8}$ | 32376.9 | 114.95 | 28.70 | 0.00 | 59. 22 | 0.00 | 5. 37 | 23. 53 | 31.46 | -17.10 | -21.50 | 7. 83 | 4.40 |
| 114 | 18388.2 | 364. 8 | 34905. 2 | 141.34 | 28. 27 | 0.00 | 58.81 | 0.00 | 5. 30 | 14.94 | 31.03 | -17.57 | -19.99 | 7.90 | 2. 42 |
| 121 | 19830.7 | 364. ${ }^{-8}$ | 38078.4 | 159.48 | 29. 23 | 0.00 | 58.19 | 0.00 | 4.69 | 11.72 | 31.94 | -18. 18 | -20. 33 | 8. 23 | 2.16 |
| 128 | 21275. 2 | 364. 8 | 41251.7 | 175.60 | 30.16 | 0.00 | 57.57 | 0.00 | 3. 95 | 9. 88 | 32.81 | -18. 72 | -20.77 | 8. 46 | 2.05 |
| 136 | 22960.5 | 364. 8 | 44953.7 | 192.72 | 31. 15 | 0.00 | 56. 63 | 0.00 | 3.24 | 8. 11 | 33.75 | -19.58 | -21. 53 | 8.57 | 1.97 |
| 141 | 22965. 5 | 322.8 | 44964.1 | 185. 57 | 30.42 | 0.00 | 52. 54 | 0.00 | 1. 10 | 2.76 | 32.90 | -23.43 | -24. 95 | 7. 89 | 1. 52 |
| 148 | 24320.6 | 322. | 47598. 1 | 185. 55 | 31.51 | 0.00 | 50.44 | 0.00 | 0. 70 | 1.79 | 33. 95 | -25. 32 | -26. 44 | 7.56 | 1.12 |
| 155 | 25953.1 | 322. 8 | 5071. 3 | 187.52 | 32. 59 | 0.00 |  | 0.00 | 0.31 | 2.15 | 35.04 | -26. 49 | -27. 59 | 7.63 |  |
| 162 | 27585.5 | 322.8 | 53944.5 | 191.09 | 33. 70 | 0.00 | 48.18 | 0.00 | 0. 86 | 2. 76 | 36. 14 | -27. 26 | $-28.43$ | 7.80 | 1. 16 |
| 169 | 29218.0 | 322. ${ }^{\text {322 }}$ | 57117.7 | 195. 42 | 34.78 | 0.00 | 47. 50 | 0.00 | 1.15 | 3. 29 | 37. 23 | -27. 83 | -29.01 | 9. 01 | 1. 19 |
| 177 | ${ }^{31122.6}$ | 322. ${ }^{\text {328 }}$ | 60819 | 201.28 | 36. 04 | 0.00 | 46. 93 | 0.00 | 1.34 | 3. 83 | 38.48 | -28.28 | -29.49 | 8. 29 | 1. 20 |
| 178 | 31127.6 | 322. 8 | 60829.5 | 201.33 | 36. 05 | 0.00 | 46. 97 | 0.00 | 1.36 | 3. 87 | 38. 49 | -28. 24 | -29. 45 | 8. 29 | 1.21 |
| 211 | 31132.6 | 0.0 | 60834. 3 | 145.21 | 6.00 | 0.00 | -3. 23 | 16. 76 | 0.00 | 0.00 | 27. 88 | -48. 05 | -49.13 | 7.93 | 1.09 |


| POUER |  | HISTORYI |  |  |  |  | TOP | ANO | INNER OF |  | FUEL |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { SIEP } \\ & \text { NO. } \end{aligned}$ | TIWE | LIMEAR HEAT RATE ( $\mathbf{M} / \mathbf{C M}$ ) | $\begin{aligned} & \text { eurwip } \\ & \text { (Wyo/ } \\ & \text { Tu02) } \end{aligned}$ | circam TOTA STRAIN (0.01×) | AXIAL TOTAL SIRAIN (0 01\%) | RADIAL TOTAL strain (0.01\%) | CIRCIM CREEP STRAIN (0.01\%) | AXIAL GREEP STRAIN (0.014) | RADIAC CREEP STRAIM ( 0.01 x ) | EQUIVA. CREEP Stralm (0.01\%) | equiva. PLASTIC (0. 01 N ) | CIRCUM STRESS (MPA) | AXIAL STRESS (MPA) | RADIAL STRESS ( (19ค) | eoulva. STRESS (MPA) |
| 1 | 0.0 | 0.0 | 0.0 | 104. | 7. | 104. | 0. | 0. | 0. | 0. | 0. | 0.0 | 0.0 | 0.0 | 0.0 |
| 33 | 50 | 312.0 | 4.7 | 226. | 176. | 225. | 0. | 0 | 0. | 0. | 0. | 3. 0 | -0. 4 | 2.8 | 3.4 |
| 45 | 2817.5 | 312.0 | 5288.7 | 204. | 117. | 201. | 19. | -35. | 16. | 35. | 0. | -0.1 | -0. 4 | -0. 1 | 0.3 |
| 56 67 | 5632 8447 | 312.0 3120 | 10577.3 15866.0 | 211. 213. | 107. 115. | 208. 210 | 24. 23. | -45. | ${ }_{21}^{19}$ | 43. | 0. | -0.0 | -0. 2 | -0.0 | 0.2 |
| 67 | 0447.4 | 312.0 | 15966.0 | 213. | 115. | 210. | 23. | -43. | 19. | 43. | 0. | -0. 5 | -0. 2 | -0. 5 |  |
| 78 | 11262.4 | 312.0 | 21154.7 | 212. | 132. | 209. | 17. | -32. | 13. | 32. | 0. | -1.3 | -0.5 | -1.3 | 0. ${ }^{\text {a }}$ |
| 101 | 17230.2 | 312.0 | 26443.4 32368.7 | 210. 210. | 153. 180. | 206. | O. | -17. | -4. | 17. | 0. | -1.8 -2.4 | -0. 0 | -1.8 | 1. 6 |
| 107 | 17235.2 | 364. ${ }^{\text {a }}$ | 32376.9 | 228. | 199. | 224. | 0. | 1. | -4. | 7. | 0. | -7.1 | -3.9 | $-7.4$ | 3. 8 |
| 114 | 18386. 2 | 364. 8 | 34905.2 | 232. | 202. | 226. | -2. | 1. | -8. | 18. | 0. | -2.0 | -1. 8 | -2. 0 | 0.5 |
| 121 | 19830.7 | ${ }^{364} 8.8$ | 38078.4 | 230. | 210. | 222. | -5. | 7. | -12. | 23. | 0. | $-1.7$ | -1. 4 | $-1.7$ | 0.5 |
| 128 | 21275.2 | 384, 8 | 41251.7 | 228. | 218. | 220. | -9. | 13 | -17. | 30. | 0 | -1.4 | -1. 2 | -1.4 | 0.4 |
| 136 | 22960.5 | 364. ${ }^{3}$ | 44953.7 | 227. | 225. | 218 | -12. | 18. | -22. | 36. | 0. | -1.1 | -1.0 | -1.1 | 0.3 |
| 141 | 22965.5 | 322. 8 | 44964.1 | 216. | 205. | 207. | -12. | 18. | -22. | 36. | 0. | 1.4 | -0. 1 | 1.5 | 1.6 |
| 148 | 24320. 6 | 322. B | 47598.1 | 211. | 203. | 202. | -11. | 15. | -20. | 34. | 0. | 0.0 | -0.1 | 0.0 | 0.1 |
| 155 | 25953.1 | 322. 8 | 50771.3 | 208. | 207. | 198. | -12. | 18. | -22. | 36. | 0. | -1.1 | -0. 2 | -1.1 | 0.9 |
| 162 | 27585.5 | 322. ${ }^{\text {a }}$ | 53944. 5 | 200. | 214. | 196. | $-16$. | 24. | -25. | 40. | 0 | -1.1 | -0.4 | $-1.1$ | 0.8 |
| 169 | 29218.0 | 322.8 | 57117.7 | 204. | 220. | 195. | -18. | 29. | -28. | 44. | 0. | -1. 1 | -0. 4 | -1.1 | 0.7 |
| 177 | 31122.6 31127.6 | 322. 322. | 60819.7 60829.5 | 203. | 228. | 194. 194. | -21. | 35. | -31. | 49. | 0. | -1.1 -1.1 | -0.5 | -1.1 -1.1 | 0.6 0.6 |
| 211 | 31132.6 | 0.0 | 60834. 3 | 122. | 114 | 113. | -21. | 35. | -31. | 49. | 0. | 6.9 | 0.8 | 7.0 | 6.2 |

## Summary of mechanical analysis and pellet stress/strain information for the objective segment <br> (Output in the case of IPRINT(13)=1)

Time-step number, time, linear heat rate, burnup

## Pellet center:

total strain in the circumferential, axial and radial directions;
creep strain in the circumferential, axial and radial directions;
equivalent creep strain; equivalent plastic
and radial directions;
equivalent stress

| 0 E |  | HISTOAY |  |  |  |  | 10 P | A AD | INNE | ER OF | CLA | DDING |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { STEP } \\ & \text { Mo. } \end{aligned}$ | IIME | $\begin{aligned} & \text { LIMEAR } \\ & \text { HEATAT } \\ & \text { RATE } \\ & \text { W/CNM) } \end{aligned}$ | $\begin{aligned} & \text { Burap } \\ & \text { (wooz) } \end{aligned}$ | CIRCUM TOTA STRAIN (0.01\%) | AXIAL TOTAL STRAIN (0.01x) | RADINL TOTA STRAIN (0.01×) | circim CREEP strain (0.01*) | $A X I A L$ CREEP STRAIN (0.01\%) | RADIN CREEP STRAIM (0.01) | EOUIVA CREEP STRAIN (0.01×) | ENJIVA. PLASTIC STAAIM (0.01\%) | CIRCAM STRESS <br> ( | $A X I N L$ STRESS ( $\mathrm{mapA}_{\mathrm{M}}$ ) | RNDINL STRESS <br>  | EOUIVA. STRESS ( 4 PA) |
| 1 | 00 | 0.0 | 00 | 11.3 | 11.1 | 20.8 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | -71. 3 | -33. 2 | -8. 3 | 54.9 |
| ${ }^{13}$ | 5.0 | 312.0 |  | 14.9 | 14.1 | 25.5 | -0.9 | 0.1 | 0.8 | 1.0 | 0.0 | -69. 5 | -34. 2 | -9.4 | 52.3 |
| 45 | 2817.5 583 | 3120 | 5288.7 | -8.1 | 28.2 | 45.4 | -25. 5 | 3. 5 | 21.9 | 26.9 | 0.0 | -58. 9 | -27.4 | -8.8 | 43. 8 |
| 56 68 | 5632.5 8447 | 312.0 312.0 | 10577.3 15866.0 | -18.9 -24.9 | 33.4 | 54.4 60.4 | -36.3 -4.2 | 5.3 6.0 | 31.0 37.2 | 38.5 46.2 | 0.0 0.0 | -58.3 -53.0 | -26.8 -30.6 | -8.8 -10.5 | 437.4 |
| 78 | 11292.4 | 312.0 | 21154.7 | -25. 4 | 40.5 | 81.9 | -46. 1 | 5.9 | 40.2 | 49.8 | 0.0 | -34. 1 | -27.0 | -13. 8 | 18.5 |
| 89 | 14077.4 | 312.0 | 26443.4 | -22. 1 | 42.5 | 60.5 | -46. 2 | 5.7 | 40.5 | 50.1 | 0.0 | $-9.0$ | -21.0 | -15. 5 | 10.6 |
| 101 | 17230.2 | 312.0 | 32366.7 | -17. 3 | 44.6 | 57.5 | -43. 9 | 4.7 | 39.2 | 52.4 | 0.0 | 14.4 | -9.5 | -18.0 | 29.2 |
| 1107 | 17235. 2 | 364. 8 | 32376. 9 | -10.0 | 46.0 | 53. 5 | $-43.8$ | 4.7 | 39.2 | 52.5 | 0.0 | 71.3 | 15.6 | -25. 2 | 84.1 |
| 114 | 18383. 2 | 364.8 | 34905.2 | $-10.6$ | 45. 2 | 53.5 | $-38.6$ | 3.7 | 34.9 | 58.1 | 0.0 | 19.7 | -7. 4 | -19.7 | 35.1 |
| 121 | 19830.7 | 364.8 | 38078.4 | $-11.2$ | 46.2 | 53. 9 | $-37.3$ | 3.4 | 34.0 | 59.4 | 0.0 | 3.4 | -11.0 | -17.5 | 18. 6 |
| 128 | 21275.2 | 364. 8 | 41251.7 | $-11.9$ | 47.2 | 54.6 | -37.0 | 3. 2 | 33.7 | 59.7 | 0.0 | -6.4 | -14.1 | -16. 2 | 9. 2 |
| 136 | 22960.5 | 364. 8 | 44953.7 | -12.8 | 48.3 | 55.6 | -36.9 | 3. 2 | 33.7 | 59.8 | 0.0 | -16. 6 | -17.7 | -15. 0 | 3.1 |
| 141 | 22985.5 24320.6 | 322. ${ }_{\text {322 }}^{8}$ | 44964.1 47598.1 | -16.9 -18.9 | 47.9 49.4 | 57.2 59.0 | -36.9 -38.9 | 3.2 | 33.7 35 | 59.8 62.0 | 0.0 0.0 | -44.8 -4.9 | -27.1 -24.0 | -11.5 -10.8 | 29.9 29.8 |
| 155 | 25953.1 | 322. 8 | 50771.3 | -20.3 | 50.8 | 60.7 | -40.9 | 3.7 | 37.2 | 64.2 | 0.0 | -40. 8 | -23.1 | $-11.0$ | 26.0 |
| 162 | 27585.5 | 322.8 | 539445 | -21.2 | 52.1 | 61.9 | -42.4 | 3.9 | 39.8 | 65.9 | 0.0 | -37. 2 | -21. 9 | -11.3 | 22.5 |
| 169 | 29218.0 | 322. 8 | 57117.7 | -21.9 | 53.3 | 83.0 | -43. 7 | 4.0 | 39.7 | 67.2 | 0.0 | -34.4 | -20.9 | $-11.7$ | 19.8 |
| 177 | 31122.6 31127 | 322. 8 | 60819.7 | -22.5 | 54.7 | 64.1 | -44.9 | 4.2 | 40.7 | 68. 5 | 0.0 | $-31.8$ | $-200$ | $-12.0$ | 17.2 |
| 178 | 31127.8 | 322.8 | 60829.5 | -22. 5 | 54.8 | 64.1 | -44. 9 | 4.2 | 40.7 | 68.5 | 0.0 | -31. 6 | -19.9 | -12.0 | 17.0 |
| 211 | 31132.6 | 0.0 | 60834.3 | -40. 2 | 41.1 | 37.0 | -44. 9 | 4.2 | 40.7 | 68.5 | 0.0 | 40.4 | 25.1 | -2. 5 | 37.6 |

Summary of results of mechanical analysis and cladding stress/strain information for individual segment
(Output in the case of $\operatorname{IPRINT}(14)=1$ )

Time-step number, time, linear heat rate, burnup

Ridge inner surface of cladding: total strain in the circumferential, axial and radial directions; creep strain in the circumferential, axial and radial directions; equivalent creep strain; equivalent plastic and radial directions; equivalent stress
$=\mathrm{TITL}$ ZORITA-1 GROLP A 〈 ZOOIP > NOWIMAL
fimle ingormation


Summary of final results of major items (Output in the case of $\operatorname{PPRINT}(15)=1$ )

## Title, segment number

Total number of time steps, irradiation time, maximum linear heat rate, initial gap width, maximum burnup, maximum temperature, iodine concentration, creep down (average) at a designated time step, creep down (maximum) at a designated time step, displacement at ridge of cladding after irradiation, displacement at center of cladding after irradiation, ridge height of cladding after irradiation

Total number of time steps, maximum displacement at ridge of cladding, maximum displacement at center of cladding, ridge height at the time of maximum displacement of cladding, maximum equivalent stress at ridge of cladding, maximum axial stress at ridge of cladding, maximum circumferential stress at ridge of cladding, maximum equivalent stress of cladding, maximum axial stress of claddings, maximum circumferential stress of cladding, average diametral gap width at a designated time step, ridge gap width at a designated time step (diameter), linear heat rate at starting time of contact.

国際単位系（SI）と換算表

| E | 名 妳 | 記 号 |
| :---: | :---: | :---: |
| 長 さ | ＊－トル | m |
| 質 畐 | キログラム | kg |
| 時 間 | 杪 | s |
| 電 流 | アンベア | A |
| 照力学榅度 | ヶルビン | K |
| 物 質 畳 | も ル | mol |
| 光 度 | カンデラ | cd |
| 平面角 | ラシアアン | rad |
| 立体 角 | ステラジアン | sr |

表き 固有の名标を6つSI租立単位

| 而 | 名 妳 | 記号 | 他のSI 単位 によろ表晛 |
| :---: | :---: | :---: | :---: |
| 周 波 数 | へ ッ | Hz | $\mathbf{s}^{-1}$ |
| 力 | 二ュートン | N | $\mathrm{m} \cdot \mathrm{kg} / \mathrm{s}^{\text { }}$ |
| 压力，心力 | ハスカル | Pa | $\mathrm{N} / \mathrm{m}^{2}$ |
| エォルギー，仩事，就棗 | $シ ュ ー ル$ | J | $\mathrm{N} \cdot \mathrm{m}$ |
| 工集．放射束 | $7 \quad$ 「 | W | J／s |
| 䂗気且，雷荷 | クーロン | C | A．s |
| 需位，萓压，起電力 | ボルト | V | W／A |
| 解 電 容 量 | 73 フ | F | $\mathrm{C} / \mathrm{V}$ |
| 電気抵抗 | 才－ム | $\Omega$ | V／A |
|  | シーネンス | S | A／V |
| 砤 束 | ウェーバ | Wb | V．s |
| 磁 束 密 度 | テ ス ラ | T | $\mathrm{Wb} / \mathrm{m}^{2}$ |
| インダクタンス | へンリー | H | Wb／A |
| セルジ | セルシウス度 | ${ }^{\circ} \mathrm{C}$ |  |
| 光 束 | ルーメン | 1 m | cd．sr |
| 照 度 | ル ク ス | lx | $\mathrm{lm} / \mathrm{m}^{2}$ |
| 放 射 能 | べクレル | Bq | $\mathrm{s}^{-1}$ |
| 吸 収 線 旦 | グレイ | Gy | $\mathrm{J} / \mathrm{kg}$ |
| 線 量 当 量 | シーベルト | Sv | $\mathrm{J} / \mathrm{kg}$ |

表2 SIと併用される単位

| 名 栋 | 記 号 |
| :---: | :---: |
| 分，時，目 | min，$h, d$ |
| 度，分，杪 |  |
| リットル | 1，L |
| $ト$ ト | t |
| 雷子ボト | eV |
| 原子啠量単位 | u |

$1 \mathrm{eV}=1.60218 \times 10^{-1 \cdot} \mathrm{~J}$
$1 \mathrm{u}=1.66054 \times 10^{-27} \mathrm{~kg}$

$1 \dot{A}=0.1 \mathrm{~nm}=10^{-19} \mathrm{~m}$
$1 \mathrm{~b}=100 \mathrm{fm}^{2}=10^{-24} \mathrm{~m}^{2}$
$1 \mathrm{bar}=0.1 \mathrm{MPa}=10^{5} \mathrm{~Pa}$
$1 \mathrm{GaI}=1 \mathrm{~cm} / \mathrm{s}^{2}=10^{-2} \mathrm{~m} / \mathrm{s}^{2}$
$1 \mathrm{Ci}=3.7 \times 10^{10} \mathrm{~Bq}$
$1 \mathrm{R}=2.58 \times 10^{-4} \mathrm{C} / \mathrm{kg}$
$1 \mathrm{rad}=1 \mathrm{cGy}=10^{-2} \mathrm{~Gy}$
$1 \mathrm{rem}=1 \mathrm{cSv}=10^{-2} \mathrm{~Sv}$

誛5 S1㢺䫝語

| 倍数 | 接頭語 | 記 号 |
| :---: | :---: | :---: |
| $10^{18}$ | エ 7 | E |
| $10^{15}$ | －夕 | P |
| $10^{12}$ | $\overline{\boldsymbol{j}}$ | T |
| $10^{\prime}$ | ＊カ | G |
| $10^{6}$ | 入 ガ | M |
| $10^{\prime}$ | キ | k |
| $10^{2}$ | へクト | h |
| $10^{\prime}$ |  | de |
| $10^{-1}$ | $テ ゙ シ$ | d |
| $10^{-2}$ | センチ | c |
| $10^{-3}$ | ミ リ | m |
| $10^{-6}$ | マイクロ | $\mu$ |
| $10^{-9}$ | ＋ | n |
| $10^{-12}$ | $ヒ ゙ コ$ | P |
| $10^{-15}$ | フェムト | 1 |
| $10^{-14}$ | $7 \quad 1$ | a |

（注）
1．表1－5は「国際単位系」第5饭，国際度量衡局1985年刊行による。ただし，1 eV および 1 u の値はCODATAの1986年推笑値によった。
2．表4には海里，ノット，アール，ヘクタ ールも含まれているが団常の単位なのでて てでは省略した。
3．barは，JISでは流体の圧力を表わす場台に限り表2のカテゴリーに分䫫されてい る。
 U「血任の単位」 mmHg を表2のカテゴリ ーに入れている。

| 力 | $\mathrm{N}\left(=10^{\text {s }} \mathrm{dyn}\right)$ | kgf | lb |
| :---: | :---: | :---: | :---: |
|  | 1 | 0.101972 | 0.224809 |
|  | 9.80665 | 1 | 2.20462 |
|  | 4.44822 | 0.453592 | 1 |
| 轳 度 $1 \mathrm{~Pa} \cdot \mathrm{~s}\left(\mathrm{~N} \cdot \mathrm{~s} / \mathrm{m}^{2}\right)=10 \mathrm{P}($ ボアズ）$(\mathrm{g} /(\mathrm{cm} \cdot \mathrm{s})$ ） |  |  |  |
| 動粘度 $1 \mathrm{~m}^{2} / \mathrm{s}=10^{4} \mathrm{St}$（ストークス）$\left(\mathrm{cm}^{2} / \mathrm{s}\right)$ |  |  |  |


| 圧 | $\mathrm{MPa}(=10 \mathrm{bar})$ | $\mathrm{kgf} / \mathrm{cm}^{2}$ | atm | $\mathrm{mmHg}(\mathrm{Torr})$ | $\mathrm{lbr} / \mathrm{in}^{2}(\mathrm{psi})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 力 | 10.1972 | 9.86923 | $7.50062 \times 10^{3}$ | 145.038 |  |
|  | 1 | 0.967841 | 735.559 | 14.2233 |  |
|  | 1.03323 | 1 | 760 | 14.6959 |  |
|  | $1.35951 \times 10^{-3}$ | $1.31579 \times 10^{-3}$ | 1 | $1.93368 \times 10^{-2}$ |  |
|  | $7.03070 \times 10^{-2}$ | $6.80460 \times 10^{-2}$ | 51.7149 | 1 |  |


| $\underline{1}$ | $\mathbf{J}\left(=10^{\prime} \mathrm{erg}\right)$ | kgf．m | kW $\cdot \mathrm{h}$ | cal（計量法） | Btu | ［t－Ibf | eV | $1 \mathrm{cal}=4.18605 \mathrm{~J}$（計量法） |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ， | 1 | 0.101972 | $2.77778 \times 10^{-7}$ | 0.238889 | $9.47813 \times 10^{-4}$ | 0.737562 | $6.24150 \times 10^{18}$ | $=4.184 \mathrm{~J}$（焦化学） |
| 1 | 9.80665 | 1 | $2.72407 \times 10^{-6}$ | 2.34270 | $9.29487 \times 10^{-3}$ | 7.23301 | $6.12082 \times 10^{19}$ | $=4.1855 \mathrm{~J}\left(15^{\circ} \mathrm{C}\right)$ |
| 仕 | $3.6 \times 10^{6}$ | $3.67098 \times 10^{5}$ | 1 | $8.59999 \times 10^{5}$ | 3412.13 | $2.65522 \times 10^{\text {c }}$ | $2.24694 \times 10^{75}$ | $=4.1868 \mathrm{~J}$（国際烝気表） |
| － | 4． 18605 | 0.426858 | $1.16279 \times 10^{-6}$ | 1 | $3.96759 \times 10^{-3}$ | 3.08747 | $2.61272 \times 10^{19}$ | 仕事事 1 PS（仏馬力） |
| 星 | 1055.06 | 107.586 | $2.93072 \times 10^{-4}$ | 252.042 | 1 | 778.172 | $6.58515 \times 10^{21}$ | $=75 \mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s}$ |
|  | 1.35582 | 0.138255 | $3.76616 \times 10^{-7}$ | 0.323890 | $1.28506 \times 10^{-3}$ | 1 | $8.46233 \times 10^{18}$ | $=735.499 \mathrm{~W}$ |
|  | $1.60218 \times 10^{-19}$ | $1.63377 \times 10^{-20}$ | $4.45050 \times 10^{-26}$ | $3.82743 \times 10^{-70}$ | $1.51857 \times 10^{-32}$ | $1.18171 \times 10^{-19}$ | 1 |  |


| 放 | Bq | Ci |
| :---: | :---: | :---: |
| 射 | 1 | $2.70270 \times 10^{-11}$ |
| 能 | $3.7 \times 10^{10}$ | 1 |


| $\begin{aligned} & \text { 吸 } \\ & \text { 收 } \\ & \text { 縓 } \end{aligned}$ | Gy | rad |
| :---: | :---: | :---: |
|  | 1 | 100 |
|  | 0.01 | 1 |


| 照射線蕰 | $\mathrm{C} / \mathrm{kg}$ | R |
| :---: | :---: | :---: |
|  | 1 | 3876 |
|  | $2.58 \times 10^{-4}$ | 1 |


| 絔 | Sv | rem |
| :---: | :---: | :---: |
| 当 | 1 | 100 |
| 異 | 0.01 | 1 |


[^0]:    Keywords: LWR, Fuel, FEM, Pellet, Cladding, PCMI, Cladding, PCMI, FP Gas Release

[^1]:    History data
    (Output in the case of $\operatorname{IPRINT}(5)=1$ )

    Time-step number, time, burnup, linear heat rate, coolant temperature, coolant pressure, coolant velocity, fast neutron flux, input option, print option, steady/unsteady manual

[^2]:    Displacement of node in the radial and

