EMSP Project 70070

Reactivity of Primary Soil Minerals and Secondary Precipitates beneath Leaking Hanford Waste Tanks

FINAL REPORT

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Principal Investigator:
Kathryn L. Nagy
University of Colorado
now at University of Illinois at Chicago
312-355-3276, klnagy@uic.edu

Project Team:
Barry R. Bickmore
University of Colorado
now at Brigham Young University

Sherry D. Samson
University of Colorado
now at University of Illinois at Chicago

R. Jeff Serne and Steven B. Yabusaki
Pacific Northwest National Laboratory
EXECUTIVE SUMMARY

Since the late 1950s, leaks from 67 single-shell tanks at the Hanford Site have released about 1 million curies to the underlying sediments. The radioactive material was contained in water-based solutions generally characterized as having high pH values (basic solutions), high nitrate and nitrite concentrations, and high aluminum concentrations. The solutions were also hot, in some cases at or near boiling, as well as complex and highly variable in composition reflecting solutions obtained from multiple methods of reprocessing spent nuclear fuel. In order to understand the observed and probable distribution of radionuclides in the ground at Hanford, major reactions that likely occurred between the leaked fluids and the sediment minerals were investigated in laboratory experiments simulating environmental conditions. Reactions involving the dissolution of quartz and biotite and the simultaneous formation of new minerals were quantified at controlled pH values and temperature. Results show that the dissolution of quartz and formation of new zeolite-like minerals could have altered the flow path of ground water and contaminant plumes and provided an uptake mechanism for positively-charged soluble radionuclides, such as cesium. The dissolution of biotite, a layered-iron-aluminum-silicate mineral, provided iron in a reduced form that could have reacted with negatively-charged soluble chromium, a toxic component of the wastes, to cause its reduction and precipitation as a new reduced-chromium mineral. The quantity of iron released in the experiments is sufficient to explain observations of reductions in dissolved chromium concentration in a plume beneath one Hanford tank. Fundamental data obtained in the project are the rates of the reactions at variable temperatures and pHs. Fundamental data were also obtained on aspects of the surface reactivity of clay or layered-silicate minerals, a small proportion of the total mass of the sediment minerals, but a large proportion of the number of sites where reactions can occur. Results were also finalized on a component of a previous project related to the Hanford waste tanks that had the goal of measuring the incorporation of rhenium, an analogue of radioactive technetium, in iron and aluminum-oxides minerals as they aged in tank sludges at higher temperatures. Small amounts of rhenium were occluded in the iron-rich solids and the amount increased with aging time. Results from the quartz and biotite experiments are in a form that can be used in models of fluid flow in the Hanford subsurface. Results from the rhenium experiments can be used to understand aspects of closing certain of the Hanford tanks.

PROJECT OBJECTIVES

Since the late 1950s, leaks from 67 single-shell tanks at the Hanford Site have released about 1 million curies to the underlying sediments. At issue is the distribution of contaminants beneath the tanks, and the processes that led to their current disposition and will control their future mobility. The high ionic strength, high pH, and high aluminum concentrations in the tank liquids can significantly alter the vadose zone sediments through dissolution of primary minerals and precipitation of secondary minerals. Dissolution and precipitation directly influence (1) the flow paths that control contaminant transport and (2) the reactivity of the solid matrix that controls contaminant mobility. The impact of these processes, however, depends on mineral reaction kinetics and the dynamic interaction of the reactions with the flow field and contaminant
sorption, neither of which are well known for this extreme chemical system. Data obtained will be directly useful to other EMSP projects addressing contaminant mobility in the vadose zone. We are addressing three specific issues:

1. Recognized factors that control the kinetics of dissolution and precipitation must be quantified for the unnatural system of tank solutions mixing with soils, including effects of high pH, high ionic strength (especially NaNO₃ solutions), temperature, and saturation state.
2. A clear understanding of the roles of nucleation mechanism, nucleation sites on soils minerals, and the role of reactive surface area in simultaneous dissolution and precipitation reactions are the key unknown components in comprehending this contaminated soil system.
3. Results obtained will help build a mechanistic understanding of how tank fluids migrate through the vadose zone. Local changes in porosity and permeability will dictate preferential flow paths which directly regulate the transport of later arriving chemical species. Changes in mineral surface area affect sorption site distribution. A comprehensive model is needed that integrates these feedback mechanisms with all the critically available data.

BACKGROUND

During the first three years of research funded by the Environmental Management Science Program, field observations on Hanford sediments and fluids beneath the S-SX tank farms have been useful in identifying a number of important reactions controlling the distribution of contaminants beneath the tanks (e.g., McKinley et al., 2001; Zachara et al., 2002; Zachara et al., 2004). In particular, radioactive cesium uptake on primary sediment minerals seems to occur largely on micas with a general uptake associated with amorphous-like secondary aluminosilicate precipitates. Also, results of column experiments on Hanford sediments suggest strongly that colloids may have been mobilized during contact with leaked tank fluids (Flury et al., 2002). These colloids consist of remobilized clay minerals and also new secondary zeolite-like precipitates that can take up cesium from solution (Chorover et al., 2003). Chromate immobilization is considered to occur via reduction of chromate (Cr(VI)) to insoluble chromium-oxyhydroxides (Cr(III)) by Fe(II) released during the dissolution of biotite grains (Zachara et al., 2004). The work supported under this EMSP project (70070) has evolved during the lifetime of the project in order to stay directed at investigating the fundamental nature and rates of reactions pertinent to the field observational data.

APPROACH AND METHODS

At the start of the project, there was no observational data on what actually happened to minerals and solutions beneath the Hanford tanks. Gamma-logging in well-bores drilled laterally to certain tanks showed the shapes of some cesium-containing contaminant plumes, for example, but no actual samples of sediment and solutions directly beneath the tanks had been collected. During the project period, data were obtained from a slant well-bore beneath the SX tank farm (e.g., McKinley et al., 2001; Zachara et al., 2002; Zachara et al., 2004). As these data were analyzed and released to the public, we redirected our experimental efforts to focus on
quantifying rates and reaction mechanisms that could explain the observations of these investigations with the overall goal of addressing geochemical and mineralogical controls on contaminant mobility in the Hanford subsurface.

Along the same lines, the work that was started under another EMSP project, but finished under this one, to simulate solid-contaminant interactions within the Hanford tank sludges was conducted without much knowledge at the time of specific sludge solids in the tanks. General compositional inventories were available for the entire Hanford site, but specific tank information was lacking. It had been generally thought that technetium-99 was dominantly portioned into the liquid phases in the tanks, and this is true for many specific tanks. Technetium-99 is one of the primary subsurface contaminants from the leaked tanks, for example. However, only recently has it been determined that there is at least one, if not some subset, of tanks that may have most of their technetium-99 somehow incorporated in iron-rich solid phases (K. Krupka, personal communication). The experimental results summarized in this report have proven useful towards understanding tank sludges where the ultimate goal is to complete tank closure. However, it is important to realize that at the time the experiments were conducted, the majority of the information available suggested that solid-phase incorporation of technetium was much less important than the solution-phase technetium.

The methods used in the experimental parts of the study were based on standard batch and stirred-reactor designs and full characterization of substrate solids and reacted solutions and solids. Probably one of the most challenging aspects of the research was developing approaches to work with high ionic strength solutions at high pH values. With time, the methodologies and approaches evolved to the use of solid-state electrodes for the measurement of pH with calibrations performed in solutions of known hydroxyl concentration. In all cases various plastics were used to contain the high pH solutions. When possible, Pitzer models developed largely by Andy Felmy at PNNL were used to model solution compositions.

Solids were characterized using various bulk and surface analytical techniques. This included using facilities and researchers (Field Emission Scanning Electron Microscopy and X-ray Diffraction) at the William R. Wiley Environmental Molecular Sciences Laboratory at Pacific Northwest National Laboratory.

Molecular modeling of mica reactivity was conducted in collaboration with Kevin Rosso of Pacific Northwest National Laboratory.

RESULTS OVERVIEW

The goal of the research was to obtain kinetic rate laws to describe the dissolution of primary minerals, as well as the precipitation of secondary phases, as they contact high pH, high ionic strength, high aluminum fluids. Results include data on the kinetics and thermodynamics of the precipitation of secondary nitrate-cancrinite during quartz dissolution (Bickmore et al., 2001); a study showing that the surface area of a clay can be obtained on picogram quantities of material using images obtained by atomic force microscopy (Bickmore et al., 2002), and a modeling approach to quantifying the thermodynamics of acid-base reactive sites on micas (Bickmore et al., 2003). The latter two manuscripts were not direct results of the specific kinetics experiments of this project, but are relevant to surface reactions occurring at Hanford with respect to cesium uptake by micas and clays (Zachara et al., 2002; Chorover et al., 2003). Data on the dissolution kinetics of biotite in Hanford tank simulants at 25 °C and on the
dissolution kinetics of quartz in Hanford tank simulants at 59-89 °C are in the process of being published as journal articles (Samson et al., in revision; Bickmore et al., in prep.). Finally, a results on measuring rhenium uptake in aging iron- and aluminum oxide minerals in tank simulants showed that a finite amount of rhenium was irreversibly sorbed in these materials and that the amount increased with aging time (Wakoff and Nagy, 2004).

Results on each of these topics are summarized below.

**Cancrinite Formation on Quartz** (Bickmore et al., 2001c): High pH, high NaNO₃ solutions with varying amounts of dissolved Al were reacted with quartz sand at 88.7 °C. After 2-10 days, nitrate-cancrinite, a feldspathoid mineral with a zeolite-like crystal structure, precipitated onto the quartz surfaces, cementing the grains together. Estimates of the K_{eq} for the precipitation reaction differ for solutions with 0.1 or 1.0 m OH⁻ (log K_{eq} = 30.4 ± 0.8 and 36.2 ± 0.6, respectively). The solubility difference is attributed to more perfect crystallinity (i.e., fewer stacking faults) in the higher-pH cancrinite structure. Precipitate crystallinity may be important for radionuclide mobility, because stacking faults in the cancrinite structure can reduce its zeolitic cation exchange properties. The evolution of Si concentration in the solutions was modeled by considering the dependence of quartz dissolution rate on Al(OH)₄⁻ activity, cancrinite precipitation, and the reduction of reactive surface area of quartz due to coverage by cancrinite.

**Clay Surface Area** (Bickmore et al., 2002): Rapid and accurate determination of the surface area of three kaolinite clay standards, taking into account the complex microtopography of the particles, was achieved using atomic force microscopy images and computerized image analysis. All surface areas were determined to within 3%. Edge surface area is 18.2 – 30.0% of the total surface area depending on the particular kaolinite standard. Specific surface areas agree to within 4% of published values determined by the BET method. The approach can be applied to clay and nanoparticle samples too small in quantity for BET analysis, since it requires ~11 orders of magnitude less material.

**Mica Edge Surface Reactivity** (Bickmore et al., 2003): The atomic structure of dioctahedral 2:1 phyllosilicate edge surfaces was calculated using pseudopotential planewave density functional theory. Bulk structures of pyrophyllite and ferripryrophyllite were optimized using periodic boundary conditions, after which crystal chemical methods were used to obtain initial terminations for ideal (110)- and (010)-type edge surfaces. The edge surfaces were protonated using various schemes to neutralize the surface charge, and total minimized energies were compared to identify which schemes are the most energetically favorable. The calculations show that significant surface relaxation should occur on the (110)-type faces, as well as in response to different protonation schemes on both surface types. This result is consistent with atomic force microscopy observations of phyllosilicate dissolution behavior. Bond-valence methods incorporating bond lengths from calculated structures can be used to predict intrinsic acidity constants for surface functional groups on (110)- and (010)-type edge surfaces. However, the occurrence of surface relaxation poses problems for applying current bond-valence methods. An alternative method is proposed that considers bond relaxation, and accounts for the energetics of various protonation schemes on phyllosilicate edges.
Quartz Dissolution Kinetics (Bickmore et al., 2001a,b; Bickmore et al., in prep.): The influence of Al(OH)$_4^-$ on the dissolution rate of quartz at pH 10-13 and 59-89 °C was determined using batch experiments. Al(OH)$_4^-$ at concentrations below gibbsite solubility depressed the dissolution rate by as much as 85%, and this effect was greater at lower pH and higher Al(OH)$_4^-$ concentration. For a given H$^+$ activity, the degree of rate depression due to the presence of Al(OH)$_4^-$ was invariant with temperature. That is, while dissolution rates did vary with temperature, the percent decrease in rate due to the presence of Al(OH)$_4^-$ was the same for a given H$^+$ activity and Al(OH)$_4^-$ concentration. These data, along with what is known about Al-Si interactions at high pH, are consistent with Al(OH)$_4^-$ and Na$^+$ coadsorbing on neutral silanol sites and passivating the surrounding quartz surface. The observed pH dependence, and lack of temperature dependence, of Al(OH)$_4^-$ sorption also supports the inference that the acid-base behavior of the surface silanol groups has only a small temperature dependence in this range. A Langmuir-type adsorption model was used to predict the degree of rate depression for a given in situ pH and Al(OH)$_4^-$ concentration. Attempts to incorporate the baseline rate data into models that assume a first order dependence of the rate on the fraction of deprotonated silanol sites were unsuccessful. However, the data are consistent with the hypothesis proposed in the literature that two mechanisms may be operative. Nucleophilic attack of water on siloxane bonds catalyzed by the presence of a deprotonated silanol group and OH$^-$ attack catalyzed by the presence of a neutral silanol group may operate in alkaline solutions. The second mechanism dominates at higher pH and temperature.

Biotite Dissolution Kinetics (Samson and Nagy, 2002a,b; Samson et al., in revision): Biotite dissolution under conditions of high pH and high Al and NaNO$_3$ concentrations was investigated using continuously stirred flow-through reactors at 22-25°C (Samson and Nagy, 2002). At the onset of each experiment, inlet solutions were pH 8 and free of nitrate and added Al. There were initial transients (i.e., initially rapid dissolution rates decaying to slower steady-state rates) and dissolution was non-stoichiometric with rapid preferential release of K followed by near-stoichiometric release of Si, Al, and Mg; release of Fe was much slower. Following a conditioning (aging) interval ranging from 96 to 500 hours, the pH 8 inlet solutions were replaced with solutions of higher pH (10-14), some including 0.055 M Al(NO$_3$)$_3$ and/or 2 M or 6 M NaNO$_3$. Each increase in the pH of the inlet solutions resulted in a second transient, i.e., a peak in the release rates decaying to new steady-state rates. The transients were pH-dependent; the amounts of Si, Al, Fe, and K released during the transient interval were greatest at pH 14, followed by pHs 13, 12, 11, and 10. Steady-state dissolution rates were at a minimum at pH 11-12 for Si, Al, Mg, and K, and at pH 10 for Fe, and increased in either direction in pH away from this minimum, but the total range in dissolution rates for Si and Al was only an order of magnitude (10$^{-12.0}$ to 10$^{-11.0}$ and 10$^{-11.9}$ to 10$^{-10.9}$, respectively, in units of moles biotite m$^{-2}$ s$^{-1}$). Normalized dissolution rates for K and Mg covered a range of approximately two orders of magnitude (10$^{-11.6}$ to 10$^{-9.8}$ and 10$^{-13.5}$ to 10$^{-11.0}$, respectively), while the range for Fe was nearly 3 orders of magnitude (10$^{-13.4}$ to 10$^{-10.6}$). The effects of Al and NaNO$_3$ on dissolution rate were highly variable and generally outweighed by the effect of pH. The most extensive solid-phase alterations, however, were consistently observed in solids reacted in sodium-enriched solutions.

Rhenium Uptake in Iron- and Aluminum Oxides (Wakoff and Nagy, 2004): This manuscript describes results of aging of iron and aluminum oxyhydroxides and concomitant uptake of perrhenate anion. The main result is that with aging in the iron system, the amount of perrhenate
incorporated irreversibly in the solids increases. No systematic effect as well as a smaller effect is observed in the aluminum system. Results imply that pertechnetate may be associated with iron-oxide phases in the tanks and may not have been partitioned completely into the tank solutions.

CONCLUSIONS

Experiments conducted to quantify rates of reactions between primary minerals in Hanford sediments and leaked waste tank simulants have provided information that should be useful for reactive-transport modeling of waste mobility in the Hanford subsurface.

PRODUCTS

Published and Submitted Manuscripts


Conference Abstracts


Bickmore B. R. and Nagy K. L., 2001a, Dissolution of quartz and precipitation of cancrinite in contact with Hanford tank simulants, Fall Meeting of the American Chemical Society.


**REFERENCES CITED**


APPENDIX OF PUBLICATIONS

All published journal papers are included in this appendix. Papers in revision or in preparation are not included and will be submitted at a later date as part of the annual reports for EMSP Project 86898, which is a continuation of EMSP Project 70070.

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Nitrate-Cancrinite Precipitation on Quartz Sand in Simulated Hanford Tank Solutions

BARRY R. BICKMORE,*†‡ KATHRYN L. NAGY,*‡ JAMES S. YOUNG,* and JOHN W. DREXLER*‡
Department of Geological Sciences, University of Colorado, Boulder, Colorado 80309-0399, and William R. Wiley Environmental Molecular Sciences Laboratory, Pacific Northwest National Laboratory, P.O. Box 999, Richland, Washington 99351

Caustic NaN03 solutions containing dissolved Al were reacted with quartz sand at 89 °C to simulate possible reactions between leaked nuclear waste and primary subsurface minerals at the U.S. Department of Energy's Hanford site in Washington. Nitrate-cancrinite began to precipitate onto the quartz after 2–10 days, cementing the grains together. Estimates of the equilibrium constant for the precipitation reaction differ for solutions with 0.1 or 1.0 m OH− (log Keq = 30.4 ± 0.8 and 36.2 ± 0.6, respectively). The difference in solubility may be attributable to more perfect crystallinity (i.e., fewer stacking faults) in the higher-pH cancrinite structure. This is supported by electron micrographs of crystal morphology and measured rates of Na volatilization under an electron beam. Precipitate crystallinity may affect radionuclide mobility, because stacking faults in the cancrinite structure can diminish its zeolite cation exchange properties. The precipitation rate near the onset of nucleation depends on the total Al and Si concentrations in solution. The evolution of experimental Si concentrations was modeled by considering the dependence of quartz dissolution rate on Al(OH)3 activity, cancrinite precipitation, and the reduction of reactive surface area of quartz due to coverage by cancrinite.

Introduction

Between 0.6 and 1.4 million gallons of high level nuclear waste, containing 1–2 million curies of radiation (primarily from 137Cs), may have leaked into the sediments beneath the U.S. Department of Energy's (DOE) Hanford Site in southeast Washington since the late 1950s (1). To predict the fate of the released radionuclides, their thermodynamics and kinetics of reactions that could have occurred between leaked fluids and Hanford sediments must be known.

Leaked nuclear waste fluids are byproducts of Pu production and extraction procedures used from 1944 to 1968 at the Hanford Site. After irradiation of U fuel rods, various solvent extraction techniques were used to separate the Pu from U and other components of the spent fuel. A large amount of NaOH typically was added to acidified waste, which then was pumped into steel tanks. As a result, the stored waste was strongly basic (pH 12–14) and often included high concentrations of dissolved Al and NaNO3. Inventories of tank components are available from the Tank Waste Information Network System at http://twins.pnl.gov/8001/). Various compounds precipitated out of the waste liquid, resulting in stratification. Additionally, self-boiling and waste concentration procedures reduced liquid volumes, resulting in high Al, high pH (pH 6–14), high ionic strength, high-temperature supernatant in many tanks (1).

The leaked fluid has contacted sediments from the Hanford Formation (coarse-grained glacio-fluvial gravels and sands) and the Middle Ringgold Formation (braid-lacustrine gravel/sand/silt). Primary silicate minerals in these sediments comprise 80–98% of the mineral mass as sand-sized grains and include quartz, feldspar (both plagioclase and K-feldspar), mica (biotite and muscovite), and minor hornblende (2). It is likely that the caustic tank supernatants dissolved some primary minerals (3–6), releasing Si into solution. This could have caused precipitation of secondary minerals, especially aluminosilicate phases. Recent work showed that cancrinite, a zeolite-like mineral, precipitated after reacting Hanford sediments for 11.7 weeks at 60 °C and 90 °C in a complex tank simulant (7). However, only qualitative information was extracted from experiments with high-solution/solid ratios. After 2 weeks, some Cs was taken up in the reacted sediments, hypothetically in the cancrinite phase.

We report results from batch experiments with low solid/solution ratios in which high pH, high NaNO3 solutions with varying amounts of dissolved Al were reacted with quartz sand at 89 °C. After 2–10 days nitrate-cancrinite precipitated onto the quartz surfaces, cementing the grains together. The solubility and initial precipitation rates of nitrate-cancrinite are estimated. We infer that depending on solution conditions, nitrate-cancrinite precipitates may have different effects on the mobility of radionuclides in the Hanford subsurface.

Experimental Section

Materials. All solutions were prepared using reagent grade NaOH, NaNO3, and Al(NO3)3. Doubly deionized (dd) water was boiled while being purged with ultrapure Ar gas and then stored in a collapsible plastic container without headspace. Reagents were mixed in the purged water as Ar gas was again bubbled through the solution, after which the solution was immediately poured into reaction vessels, which were then sealed.

White quartz sand was purchased from Aldrich Chemicals. Although small amounts of mineral impurities could be seen in the sand with an optical microscope, they could not be detected via powder X-ray Diffraction (XRD). X-ray Fluorescence (XRF) analysis of the untreated sample indicated that it was 99.8% SiO2. The sand sample was magnetically separated to remove magnetic impurities. Then 300 g of sand was placed in a glass bottle with 490 mL of concentrated H2SO4 for 2 days to condition the surfaces. The treated sand was gently rinsed 5–10 times and placed in 2 L dd water at 75 °C for 3 days, changing the water daily. Finally, the sand was gently rinsed several times and oven-dried at 80 °C. Auger Electron Spectroscopy (AES) of untreated quartz surfaces with a Perkin-Elmer PHI 600 Scanning Auger Multiprobe revealed no impurities, except for adventitious C and trace Ca, perhaps from CaCO3. AES spectra of treated quartz surfaces showed no impurities other than adventitious C.

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Batch Chemical Experiments. Batch experiments (see Table 1, Supporting Information) were designed to measure both the kinetics of quartz dissolution and the conditions under which secondary aluminosilicates might precipitate. In each experiment, 1-3 g of treated quartz sand was placed in each of eight separate 60 mL HDPE plastic bottles, which were then filled with solution. Bottles were placed in an 89 °C constant temperature water bath for a time period of 1 hour and then removed. The water bath was periodically removed for analysis. The bottles were not shaken to avoid abrasion of the quartz surfaces. The pH of each sample was measured at a temperature as close to the in situ temperature as possible (see below). Twenty-five milliliter aliquots of the solution were collected, neutralized with acid (0.05 ml of 12.1 M HCl for Al analysis, 0.06 ml of 4.5 M H2SO4 for Si analysis) and then analyzed for Si (error ± 5%) and Al (error ± 7%) concentration using colorimetry (8, 9). Si concentration in the higher pH solutions was measured using Inductively Coupled Plasma Atomic Emission Spectroscopy (ICP-AES) (error ± 8%). Colorimetric analyses were performed with a Bausch & Lomb Spectronic 501 spectrophotometer, and ICP-AES was performed on a Fisons Instruments ARL 3410+. Reacted sand was dialyzed to a conductivity of < 3 μS and freeze-dried.

Most solutions contained 2 m NaNO3 with 0.0001, 0.001, 0.005, or 0.01 M Al(NO3)3. A free OH− concentration of 0.1 or 1.0 m (representing pH values of ~11.3 and ~12.4, respectively) was obtained by adding NaOH, taking into account the formation of Al(OH)2+. That is, if the desired free Al(OH)2+ concentration is designated x and the [Al(NO3)3] concentration is designated y, then the amount of NaOH added was equal to x + 4y. In addition, solutions with 0.005 m Al(NO3)3 and 0.1 m free OH− were made with 0.5, 1.0, 2.0, and 4.0 m NaNO3.

Analysis of Precipitates. Several reacted sand samples were analyzed by powder XRD. Field Emission Scanning Electron Microscopy (FESEM) and Energy Dispersive X-ray Spectroscopy (EDS), and electron microprobe analysis (EMPA) was used. A Leo 982 FESEM system with Oxford ISIS energy dispersive X-ray detector was used for Scanning Electron Microscopy and EDS analysis. Mineral composition was determined using a JEOL 8600 electron microprobe at 10 kV accelerating voltage, 18–20 nA copper current, and with a focused beam. Spectrometer crystals of TAP and LDE1 were used for quantification, and ZAF corrections were applied based on calculated k-ratios calculated from mineral standards (USNM 145966 Microcline for Si and Al, Amelia Albite for Na, and BN for N).

pH Measurement. After each sample bottle was removed from the bath, it was opened and partially immersed in a beaker of the hot bath water. The pH was measured using an Accumet AR-15 pH meter (Fisher) and Accumet solid state ion sensitive Field Effect Transistor (ISFET) electrode with automatic temperature compensation (Fisher) at a temperature as close as to the bath temperature as possible, usually above 70 °C. Measured pH was corrected to 89 °C using the temperature dependence of the dissociation constant of water. The pH was measured at high temperature to minimize the effect of CO2, which caused the temperature-corrected pH to drift downward as the solution cooled. The ISFET electrode was used to eliminate Na+ ion error, caused by Na+ ions migrating through the gel layer on a standard glass electrode (10, 11).

Solution pH values calculated using the Pitzer model described below differed from the temperature-corrected measured values by ~0.2 to 0.3 pH units. However, pH measurements of alkaline solutions are notoriously difficult; so it was assumed that the modeled values were more accurate. Values were measured only to confirm that the pH did not drift significantly during the experiments. Reasons for the discrepancy include the following. First, commercial pH 10.00 buffer (Fisher) and pH 13.00 buffers (Fisher) were used to calibrate the electrode at room temperature. Not only are such buffers prone to pH drift (10) but also the buffers do not bracket the experimental solution conditions. Second, temperature compensation for pH electrodes is often slow when the temperature sensor is imbedded within the electrode (as in this case), causing measurement errors (10). Third, large differences in ionic strength between the buffers and samples can lead to errors because of changes in activity coefficients, etc. (13).

Solution Model. The Geochemist’s Workbench 3.0 (GWB) (14) was used to model the precipitation of the reacting solutions. All equilibrium constants were used as given in the database for GWB except those for Al species, which were modified to be consistent with the data of Wesolowski (15) and that for the polysilicate species Si4(OH)42+ taken from Busey and Mesmer (16). In fact, a number of mononuclear silicate species are known to be present in solution (17), but Busey and Mesmer (16) assumed the existence of only one, using it to represent all polysilicate species. We have followed Busey and Mesmer (16) because they reported the only thermodynamic data for polysilicate equilibria above 25 °C. Although there was a small amount of carbonate contamination (0.4%) in the NaOH pellets used to make the solutions, CO32− was not considered in the solution model.

Interaction parameters for the Pitzer model were taken from the literature. The following ionic interactions were taken into account: Na+−OH−, Na+−NO3− (18), Na+−Al(OH)2+ (15), Na+−H2SiO4−, Na+−H2SiO32− (19), Na+−H2SiO4+ NO3−−H2SiO4− and OH−−H2SiO4− (20). No Pitzer parameters are available for Na+−Si(OH)42−, but the parameters for the Na+−HPO42− interaction were substituted (18) according to the suggestion of Wanner and Forest (21).

Sample solutions from which precipitation had occurred appeared to be in equilibrium with the solid precipitate because ion activity product approached constant values soon after the observed onset of precipitation. Equilibrium constants were calculated from the measured final concentrations of aqueous Si and Al and starting concentrations of NO3− and OH−, with respect to the following reaction:

\[ 8\text{Na}^+ + 6\text{Al}(\text{OH})_2^2+ + 6\text{H}_2\text{SiO}_4^2− + 2\text{NO}_3− \rightarrow \text{Na}_8\text{Si}_4\text{Al}_2\text{O}_10(\text{OH})_8 \cdot 4\text{H}_2\text{O} + 12\text{OH}^− + 8\text{H}_2\text{O} \]  

Therefore,

\[ K_{eq} = \frac{[\text{OH}^−]^4}{[\text{Na}^+]^8[\text{Al}(\text{OH})_2^2+]^6[\text{H}_2\text{SiO}_4^2−]^6[\text{NO}_3−]^2} \]  

where brackets indicate activities calculated via the Pitzer model described above. Barnes et al. (22) found that the anion present in the concinite structure does not strongly affect overall solubility; therefore, CO32− was not considered in the concinite formula.

The evolution of Si concentration in experiments with 1.0 m free OH−, 0.01 or 0.005 m Al(NO3)3, and 2.0 m NaNO3 was modeled using STELLA 2 (High Performance Systems), a computer program designed to numerically integrate systems of differential equations.

Results and Discussion

Precipitation from Supersaturated Solutions. When the alkaline solutions contacted the quartz, dissolution proceeded at a rate determined by the solution pH and Al(OH)2+ concentration (23). Dissolved silica increased until many solutions became supersaturated with respect to an aluminosilicate phase and precipitation occurred. At the onset of precipitation, the silica release rate changed abruptly, and Al(OH)2+ concentration simultaneously dropped (Figure 1).
The precipitate tended to cement the quartz grains together into clumps.

Precipitate Characterization. Precipitates that formed in both the 0.1 and 1.0 m OH⁻ solutions were identified by XRD as nitrate-cancrinite, which has an ideal formula of Na₅₋ₓAl₂₋ₓKₓ(OH)₄₋ₓ(NO₃)ₓ₋ₓ(H₂O)ₓ₋ₓ. Cancrinite, a feldspathoid, crystallizes in the space group P6₃ with a zeolitic-like structure. Its framework is formed of layers of six-membered rings of alternating SiO₄ and AlO₄ tetrahedra stacked along the c-axis in an AB-AB sequence (29). Large channels run through the structure and can contain Na⁺ or cations such as K⁺ and Ca²⁺ along with anions such as CO₃²⁻, OH⁻, and NO₃⁻ (24–27). Solid solution series are possible between endmember cationic compositions with different anions in the channels (e.g., ref 28). Smaller 11-hedral cages in the structure contain H₂O and cations such as Na⁺ (28). The ions in the channels appear to be exchangeable, as in zeolites, but stacking faults in the AB-AB sequence can block the channels, which counteracts the zeolitic cation exchange properties of the material (29).

SEM analysis revealed ball-shaped aggregates of precipitate crystals on the quartz surfaces. Precipitate growth proceeded in three main phases: initial nucleation on the quartz surface, growth and aggregation of crystals, and subsequent aggregate growth. The precipitate initially formed in pits or rough areas, rather than on smooth crystal faces of quartz overgrowths present on the sand grains (Figure 2a). The ball-shaped aggregates were able to nucleate on top of each other or grow together laterally (Figure 2b).

In the lower pH experiments, the precipitate nucleated as a film over a small area of the quartz surface (Figure 3), after which single plate-shaped crystals grew out of the film (Figure 4a). These crystals grew together to form small aggregates (Figure 4b) and eventually the ball-shaped aggregates. The identity of both films and crystalline aggregates was confirmed by EDS analysis. In the final stage, the aggregates consisted of plate-shaped crystals intergrown (twinned?) at so many angles that the combined form was nearly spherical (Figure 4c).

In the higher pH experiments the earliest observed precipitates were single aggregates of intergrown crystals, rather than films. Larger, platy, hexagonal crystals grew out of the initial precipitate and then together (Figure 5a). These aggregates were similar to those grown at lower pH, but individual crystals were more well-defined. These were then intergrown by euhedral hexagonal needle-shaped crystals soon after nucleation (Figure 5b). The needle-shaped crystals grew at different rates outward from their axial center, resulting in “cracks” at the edges of the crystals. Smaller needle-shaped crystals grew on the “crack” surfaces and were partially overgrown as the cracks filled in (Figure 5c). This process finally resulted in balls of radiating needle-shaped, euhedral crystals, exhibiting hexagonal prism and pyramid forms (Figure 5d).

Figure 2. (a) FESEM micrograph of nitrate-cancrinite precipitated on quartz sand from a 0.1 m OH⁻, 2.12 m Na⁺, 2.015 m NO₃⁻, and 0.005 m Al(II)OH₃⁻ solution after ~24 days of reaction. Flat surfaces on some clusters indicate they had grown against another quartz surface. (b) Balls of nitrate-cancrinite precipitate on quartz sand surfaces after ~13 days from a solution of 0.1 m OH⁻, 2.14 m Na⁺, 2.03 m NO₃⁻, and 0.01 m Al(II)OH₃⁻. Balls have grown together laterally and vertically.

Elemental maps obtained by EMPA of cross-sections of precipitate spheres grown at the lower pH show a uniform distribution of Si and Al but an enrichment of Na at the outer rims. The shape of the precipitates in cross-section appeared to be hexagonal, similar to the crystals in the aggregate. Elemental maps of crystal aggregates grown at the higher pH show Na-depletion in the central mass as compared to the euhedral crystals radiating outward from the edges (Figure 1c, Supporting Information). Thus, earlier intergrown masses in precipitates at both pHs have a different composition than single euhedral crystals. The observed zonation of Na⁺ is consistent with reported chemical formulas for synthesized nitrate-cancrinites, which can deviate from ideal composition with respect to the amount of Na⁺ and NO₃⁻ in the zeolitic-like channels (20).

Average microprobe analyses of lower and higher pH precipitates showed no significant compositional difference between the two and a large deficiency in Na (Table 2, Supporting Information). Some of this apparent deficiency may be real, due to the Na-poor intergrown masses. However, some is likely due to rapid volatilization of Na from the zeolitic-like channels, even though a 1 s collection time was used. Time-series analyses for Na exhibited an exponential decrease. It was not possible to extrapolate Na content to zero time, so it was necessary to choose a short, but arbitrarily determined, collection time. Measurements of Na content for 5 s indicated that the high pH precipitates lost Na at about twice the mean rate of the low pH precipitates, and a two-sample t-test assuming unequal variances showed the measurement populations to be statistically distinct at the 99.9% confidence level. Although NO₃⁻ residues in the cancrinite channels with Na⁺, N did not volatilize significantly...
during analysis. The compositions reported in Table 2, Supporting Information indicate an excess of N relative to the ideal formula, which can be attributed to inherent difficulties in microprobe analysis of N.

Nitrate-Cancrinite Solubility. Equilibrium constants (the inverse of the $K_{eq}$) calculated with eq 2 for 1.0 m OH$^-$ solutions are consistently higher than those calculated for 0.1 m OH$^-$ solutions, with the mean value of log $K_{eq}$ for the higher OH$^-$ concentration equal to 36.2 ± 0.6 and that for the lower OH$^-$ concentration equal to 30.4 ± 0.8 (95% confidence interval).

Two-sample $t$-tests assuming unequal variances showed the two mean log $K_{eq}$ values to be statistically distinct at the 99.9% confidence level. Calculation of the log Ion Activity Product (IAP) for the solutions at the point when precipitation was estimated to have started yielded values of 34.9 ± 1.9 (log $Si = 1.3$) and 28.7 ± 1.3 (log $Si = 1.7$) for the higher and lower pH solutions, respectively (see Table 3, Supporting Information). Two-sample $t$-tests showed the log IAP values to be lower than the calculated log $K_{eq}$ values at the 90% confidence level.

Reactions for the difference in calculated $K_{eq}$ values include possible errors in the thermodynamic database resulting in incorrect speciation or actual differences in the two precipitates. For instance, a few workers (e.g., ref 29) reported third and fourth ionization constants for monomeric silica, which we did not include in our solution model. However, the discrepancy in calculated $K_{eq}$ values is only exacerbated if HSIO$_3$$^-$ or SiO$_2$$^-$ is the dominant silica species in these solutions, rather than H$_2$SiO$_4$$^-$.

On the other hand, if H$_2$SiO$_4$$^-$ is dominant, the calculated equilibrium constants for the solutions with different concentrations of free OH$^-$ are

![Figure 3](image3.png) FIGURE 3. FESEM micrograph and elemental maps of a quartz surface on which films of cancrite have precipitated in and around pits or depressions: (a) FESEM micrograph, (b) Al map with bright areas indicating high concentrations, and (c) Si map.

![Figure 4](image4.png) FIGURE 4. FESEM micrographs of nitrate-cancrinite precipitated from 0.1 m OH$^-$ solutions, showing various reaction stages: (a) a platy crystal grown outward from a precipitate film, (b) twinning of platy crystals creates an initial precipitate aggregate, and (c) a precipitate ball at a late reaction stage, exhibiting intergrown platy crystals, some with a crude hexagonal outline.

![Figure 5](image5.png) FIGURE 5. FESEM micrographs of nitrate-cancrinite precipitated from 1.0 m OH$^-$ solutions, showing various stages of the reaction: (a) Initially, tiny intergrown crystallitles cover part of the quartz surface, after which larger, hexagonal platelets grow from the initial precipitate and form twinned aggregates. (b) Just after initial precipitation, intergrown plates ("A") are overgrown by single hexagonal needle-shaped crystals ("B"). (c) Smaller needle-shaped crystals grow on "cracks" in the larger crystals and then are partially overgrown as precipitation proceeds. (d) Final products are balls of radiating euhedral, hexagonal, needle-shaped crystals.

Indistinguishable. Speciation of our solution compositions using the recent Pitzer model of Felmy et al. (30) showed that H$_2$SiO$_4$$^-$ is dominant at 25 °C. Deprotonation constants for the monomeric Si$^4+$ species shift to lower pH with increasing
temperature (16); therefore, we are reasonably certain that H$_2$SiO$_3$ dominates at 80°C, also.

NMR studies have shown that various aluminosilicate species exist in alkaline Al- and Si-bearing solutions (e.g., refs 31–38) but are probably metastable (48). However, Gout et al. (34) recently used Raman spectroscopy to show that in solutions similar to ours, a significant proportion of Si in solution is complexed with Al at 28°C. We did not find any applicable thermodynamic data for aluminosilicate species and therefore assumed that the activities of Al(OC$_2$H$_5$)$_4$ and H$_2$SiO$_3$ did not deviate significantly from their calculated values. However, this may be an incorrect assumption, and aluminosilicate speciation remains a pressing problem for zeolite synthesis studies, as well as for modeling high-pH nuclear waste solutions containing dissolved Si and Al. It should also be noted that aluminosilicate species are thought to be precursors to the formation of zeolites in industrial synthesis (39), and therefore may play a significant role in the precipitation process, even at low concentrations.

The most plausible explanation for the difference in apparent $K_m$ values appears to be actual differences in the precipitated phases. The relative enrichment of Na at the edges of the precipitate aggregates, where euhedral crystals dominate, suggests a compositional difference between the well-formed crystals and the aggregate masses. FESEM micrographs of the precipitates (Figures 4 and 5) clearly show differences in crystal form, and the higher pH precipitates appear to have a more well-formed crystal habit, suggesting a greater degree of crystallinity.

Microprobe analyses of Na support a difference in crystallinity, related to stacking fault density. The Na in the precipitate formed at higher pH volatilized more quickly than that in the lower pH precipitate. Given that stacking faults block zeolite channels in the calcite crystalline structure (20), a ready explanation for this volatilization phenomenon is apparent. The higher calculated $K_m$ at the higher pH (corresponding to a lower solubility product) is consistent with that expected for a more perfect crystalline structure.

Precipitation Kinetics. Estimates of initial calcite precipitation rates were obtained from the evolution of Al concentration in the experimental solutions. The precipitation rate did not correlate significantly with the Na$^+$, NO$_3^-$, or OH$^-$ concentrations or quartz surface area. However, the precipitation rate (mol calcite/s) did correlate with the total concentration of Al and Si at the onset of precipitation (Figure 2, Supporting Information; cf. Table 3, Supporting Information). Using the equation

$$\text{rate} = 1.03 \pm 0.05 \times 10^{-5} [\text{Al}]^{1.22 \pm 0.09} [\text{Si}]^{2.30 \pm 0.00}$$

most of the estimated rates were calculated to within ± 20% (Figure 2, Supporting Information; cf. Table 3, Supporting Information). (Rates are normalized to a 1 kg H$_2$O solution.) This formulation is consistent with the hypothesis that Na$^+$, NO$_3^-$, and OH$^-$ are in excess and therefore do not control precipitation rate. The rate may depend less strongly on [Si] because it is locally higher in concentration near the dissolving quartz surface.

The evolution of Si concentration in the experiment with 1.0 m OH$^-$, 3.04 m Na$^+$, 2.03 m NO$_3^-$, and 0.01 m Al(OC$_2$H$_5$)$_4$ was modeled, taking into account the dependence of quartz dissolution rate on Al(OC$_2$H$_5$)$_4$ concentration (Table 4, Supporting Information) (32), the stoichiometric precipitation of Si and Al in calcite, and the masking of reactive quartz surface area by the precipitated calcite. Image analysis of reacted sand grains indicated that the average surface coverage reached ~3%. Evolution of the calcite coverage was assumed to be inversely proportional to the evolution of Al(OC$_2$H$_5$)$_4$ concentration. This same model was also applied to an experiment with 1.0 m OH$^-$, 3.02 m Na$^+$, 2.015 m NO$_3^-$, 0.005 m Al(OC$_2$H$_5$)$_4$, and a final mean surface coverage of ~32%.

FIGURE 6. Si concentrations with time for experiments with 1.0 m OH$^-$, 3.04 m Na$^+$, 2.03 m NO$_3^-$, and 0.01 m Al(OC$_2$H$_5$)$_4$ (crosses), and 1.0 m OH$^-$, 3.02 m Na$^+$, 2.015 m NO$_3^-$, and 0.005 m Al(OC$_2$H$_5$)$_4$ (diamonds). Evolution of [Si] with time modeled with solid lines and without (dashed lines) reduced quartz dissolution rate due to increasing surface coverage by calcite.

Implications for Radionuclide Mobility in the Hanford Subsurface. Recently, it was reported that 137Cs was associated with frayed edges on micras at depths of 40–47 m in a well drilled through a contaminant plume between leaking tanks at the SX Tank Farm (36). If nitrate-calcite precipitates from interaction of leaked nuclear waste fluids with Hanford sediments closer to the undersides of the tanks, radionuclide mobility could have been affected in other ways. For example, precipitates could have cemented sand grains together, decreasing porosity and permeability and altering the flow pathway of subsequent leaked fluids. Synthesized calcite can contain Cs in H$_2$O cages, where it is not exchangeable (37, 38). The ability of the calcite phase to retard radionuclide migration may depend strongly on the prevalence of stacking defects, which decrease the zeolite exchange capacity. It has been shown here that the apparent stability of nitrate-calcite precipitates depends on the solution conditions. Further study of the kinetics and thermodynamics of nitrate-calcite precipitation is necessary to predict accurately both the magnitude and rate of its formation in the Hanford subsurface as well as its effects on radionuclide mobility. Such work is also important because calcite recently has been shown to be a secondary alteration product of CST (crystalline silicon tetrachloride) materials proposed for use as ion exchangers that would remove Cs$^+$ from high level waste streams at the DOE’s Savannah River Site (39).

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Supporting Information Available

Table 1 (solution conditions in precipitation experiments with time), Table 2 (microprobe analyses on nitrate-calcite
precipitates). Table 3 (solution conditions at the estimated onset of precipitation). Table 4 (quart dissolution rates). Figure 1 (microprobe elemental maps for a cross-section of a nitrate-calcine precipitate ball), and Figure 2 (calculated rate of nitrate-calcine precipitation vs measured rate at the onset of precipitation). This material is available free of charge via the Internet at http://pubs.acs.org.

Literature Cited


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Quantifying surface areas of clays by atomic force microscopy

BARRY R. BICKMORE,* KATHRYN L. NAGY, PAUL E. SANDLIN, AND TERRY S. CRATER

Department of Geological Sciences, University of Colorado at Boulder, Boulder, Colorado 80309-0399, U.S.A.

ABSTRACT

Rapid and accurate determination of the surface area of three kaolinite clay standards, taking into account the complex microtopography of the particles, was achieved using atomic force microscopy images and computerized image analysis. All surface areas were determined to within 3%. Edge surface area is 18.2–50.0% of the total surface area depending on the particular kaolinite standard. Specific surface areas agree to within 4% of published values determined by the BET method. The approach can be applied to clay and nanoparticle samples too small in quantity for BET analysis, since it requires ~11 orders of magnitude less material.

INTRODUCTION

One important application of atomic force microscopy (AFM) in mineralogy has been to quantify dimensions of distinct faces on finely divided crystallites or nanoparticles and relate these to chemical reactivity measured by other techniques such as sorption isotherms, reaction rate experiments, or EXAFS spectroscopy (e.g., Nagy 1994; Brady et al. 1996; Nagy et al. 1999; Sutterer et al. 1999; Schlegel et al. 1999; Manceau et al. 2000). Such measurements are significant when the type and abundance of surface functional groups on faces of a single grain vary widely. Phylllosilicate surfaces offer a prime example of this phenomenon because of the extreme anisotropy of their crystal structures, in which the dominant basal (001) surfaces are generally characterized by siloxane or hydroxyl groups that are charge-satisfied (except where isomorphous substitution has occurred), and particle edges are dominated by charge-unsatisfied broken bonds. Kaolinite is a common phylllosilicate clay mineral that is a component of many industrial products, can control porosity and permeability of sedimentary rocks, and can sorb contaminants and nutrients in soils. Uncertainty over the magnitude of the ratio of edge surface area (ESA) to total surface area (TSA) has in part led to significantly differing conclusions about the relative reactivity of kaolinite edge and basal surfaces (e.g., Zhou and Gunter 1992; Brady et al. 1996; Ma and Eggleton 1999).

AFM images should be routinely useful for vertical measurements at the angstrom-scale and lateral measurements at the nanoscale. However, many researchers have pointed out that tip-sample convolution can result in errors in quantifying crystallite dimensions (e.g., Blum 1994; Maurice 1996). Despite recognition of this imaging artifact, such corrections are rarely, if ever, applied. For example, Dias et al. (1997) calculated the surface area of approximately spherical MnZn ferrite particles using AFM to measure the “average diameter” (10–40 nm). The surface areas were 17–22% lower than those obtained by BET (Brunauer et al. 1938) and the difference was attributed to tip-sample convolution. Also, a rigorous approach for selecting the number of particles needed for accurate quantitative analysis of a bulk sample has not yet been determined.

We report a method of obtaining and processing AFM images that allows rapid accurate measurement of the edge (ESA), total (TSA), and specific surface (SSA) areas for three kaolinite standards. Tip/sample artifacts are quantitatively considered, and the number of particles necessary for statistically significant quantitative measurements is determined. Measuring the SSA of a clay or other powder sample based on AFM imaging of a small number of particles should prove valuable, especially in cases where small sample size precludes applying the BET method. For example, atmospheric dust, microbiological mineral products, or synthetic nanocrystals could be characterized in this way.

MATERIALS AND METHODS

Standards KGa-1, KGa-1b, and KGa-2 were obtained from the Source Clays Repository of the Clay Minerals Society. KGa-1 and KGa-1b are low-defect kaolinites from Washington County, Georgia, and KGa-2 is a high-defect kaolinite from Warren County, Georgia. Data on these clay standards can be found in van Olphen and Frijat (1979) and Costanzo and Guggenheim (2001).

The key to obtaining a statistically valid sampling of particles is to disperse the clay well on the substrate. Dispersion was achieved by mixing a drop of 0.2 M NaOH into 3 mL deionized water, and adding ~0.1–0.2 mg kaolinite. A substrate of freshly cleaved muscovite was attached to a steel sample disk and heated on a hotplate while dispersing the suspension ultrasonically for 2 minutes. A drop of suspension was placed onto the heated disk and flash-boiled immediately after ultrasonification. This procedure separated particles typically by several micrometers.

A Digital Instruments Multimode AFM was operated in tapping mode using etched silicon probes. Height images were used for dimensional analysis, while amplitude images were used to verify the sharpness and accuracy of the height images. Areas of 100–400 μm² were imaged randomly, and each particle in that area was imaged individually at higher resolution.
A few particles obviously tilted with respect to the substrate were excluded from subsequent analysis. Random variations in baseline height were removed from height images by applying a second-order "flattening" routine, with corrections based only on areas of exposed mica substrate. Six passes of a 5 x 5 median filter removed random noise without broadening edge features in the image, as occurs with lowpass (neighborhood averaging) filters (Russ 1990) (Fig. 1).

Edge-broadening due to tip-sample convolution can be significant when imaging relatively tall features like kaolinite particles, but can be minimized by using a relatively sharp tip such as an etched silicon probe. Another method for minimizing edge-broadening is to deconvolute the shape of the tip from the image. The program Deconvol 1.1 (Silicon-MDT) was used to reconstruct tip shape using the “blind reconstruction” algorithm of Villarrubia (1997). For each set of images taken with the same tip, tip shape was reconstructed from the image with the tallest features, which give the best approximation of tip shape, and then deconvoluted from the entire set of filtered images. The blind reconstruction method calculates an outer bound for the tip shape, and is preferable to methods employing a model tip. However, the reconstruction is sometimes inappropriately scaled for certain image features, causing unrealistic erosion of an image upon deconvolution. For instance, small hexagonal steps might be eroded to spikes if the radius of curvature of the reconstructed tip is large relative to the step height.

Deconvolution was applied successfully to KGa-1 and KGa-1b images, and tests on KGa-1b particles showed that ESA/ TSA and SSA changed by only ~3% overall. Ideally, deconvolution should have less of an effect for the KGa-2 standard because its average particle has a smaller height to width ratio; however, unreasonable erosion of these images resulted. Therefore, KGa-2 images were not corrected for tip shape. As long as a sharp tip is used, tip-sample convolution is not a critical issue for the measurements made on these particles.

Image analysis was performed using Image SXM (Barrett 1997). This environment allows the user to define a region of interest (ROI) of any shape and exclude unwanted features from calculations or operations performed on the ROI. Pascal-like macros can be created to perform pixel-by-pixel or line-by-line operations, and mathematical calculations (Barrett et al. 1998; Bickmore et al. 1999). We customized the computational analysis for particles with a platy habit, but algorithms specific to other morphologies could be programmed easily.

After selecting a ROI outlining a kaolinite particle, the basal surface area (BSA) was measured using macro code modified from that described in Bickmore et al. (1999). Briefly, the procedure employs a “chain code” algorithm and pixel counting (Russ 1990) to calculate the perimeter and area of horizontal slices of the particle at each gray level. The derivative of the perimeter vs. gray level (height) curve was used to distinguish sidewalls and terraces. The height for the BSA measurement was chosen just below the lowest terrace on the particle (Russ 1990; Bickmore et al. 1999), and BSA is defined as twice the measured horizontal area at that height.

To measure ESA, a baseline height was first defined using a gray level histogram of the image. Then, the particle's perim-

**Figure 1.** AFM height images that have been subjected to a shadowing routine to make topographical details apparent. (a) KGa-1 particle, maximum height = 218 nm. Lower left: convoluted image. Upper right: deconvoluted image. (b) KGa-1b particle, maximum height = 76 nm. (c) KGa-2 particles, maximum height = 145 nm.
eter at each gray level above the baseline was determined, and
multiplied by the height of one gray level. This effectively yields
ESA values for horizontal slices, which when summed, yield
the total ESA. TSA equals BSA plus ESA.

Particle volumes were determined using the defined baseline
height. The average pixel height relative to the baseline was
multiplied by the area of the ROI (Russ 1995). This method
implicitly assumes image noise is distributed symmetrically
about the true height values.

One limitation of AFM imaging is that the topography of
only a particle top can be measured; the bottom is assumed to
lie flat on the substrate. However, kaolinite surfaces often
exhibit complex microtopography, and it is reasonable to
imagine similar complexity for the hidden undersides. If so, the
algorithms could either overestimate or underestimate ESA,
and overestimate particle volume. Therefore, a correction was
applied to these calculations.

The ESA for the top half of the particle was measured by sum-
ming the ESA of “slices” one pixel in height; the volume of these
slices was also calculated and summed by multiplying the
horizontal area of the slices by the height of one gray level. Correction
of ESA and particle volume assumes the bottom half of each
particle is a mirror image of the top. While this is untrue for any
single particle, on average it is a reasonable approximation.

Particle volumes and the density of kaolinite (2.62 g/cm³)
were used along with calculated TSA values to calculate spe-
cific surface areas (SSA) for comparison with reported BET
SSA’s. To properly weight measured values for each particle,
running totals of ESA, TSA, and volume were recorded as
successive particles in a sample were measured. Cumulative ESA/
TSA ratios and SSA values were calculated using these sums.
Particles were imaged and analyzed until the cumulative values
settled into a range having ~5% relative variation. Mea-
surements of large particles had little effect on cumulative values.
Excluding the particle bottom correction, these meth-
ods were tested on “synthetic” images of shapes with known
gometry (Bickmore et al. 1999) and on images of kaolinite
particles with simple geometry. Measured values of ESA, TSA,
and particle volume consistently fell within ~5% of expected
values for synthetic images, and ~12% for images of kaolinite
particles. The larger discrepancy for the kaolinite particles shows
the importance of even a small amount of microtopography.

RESULTS AND DISCUSSION

Corrected ESA/TSA and SSA values indicate that the low-
defect kaolinite has an ESA/TSA ratio 1.5–1.6 times greater
than that of the high-defect kaolinite, although the high-defect
kaolinite has the greater SSA (Table 1). ESA/TSA ratios and
SSA values for individual particles (Fig. 2) show lognormal
distributions. KGa-1 and KGa-1b have similar distributions,
and KGa-2 has a distribution skewed toward lower ESA/TSA
and higher SSA. These observations are consistent with the
idea that high-defect kaolinite represents a material with a
higher density of nucleation and growth sites, and hence smaller
average particle size, whereas low-defect kaolinite likely grew
more slowly from fewer nucleation sites and resulted in a larger
average particle size. Slower growth rates are also compatible with
thicker particles in the c* direction for KGa-1, indicating that the
basal surfaces had more time to advance.

Applying the particle bottom correction led to SSA values
that agreed to within 4% with at least one published SSA value
determined by the BET method for each kaolinite (Table 2).
The error in the AFM measurements is estimated to be <5% (or
1/2 of the ~5% variability attained in the cumulative to-
tals), much less than the 10% error typically assigned to a BET
measurement. Therefore, the excellent agreement with pub-
lished BET SSAs validates use of the AFM analysis for this

![Figure 2: Frequency histograms for corrected (a) ESA/TSA ratios, and (b) SSA measurements of single kaolinite particles in all three samples.](image)

<p>| Table 1: Cumulative values of ESA/TSA and SSA with and without particle bottom correction |
|---------------------------------|------------------|------------------|------------------|------------------|------------------|</p>
<table>
<thead>
<tr>
<th>Sample</th>
<th>no. particles</th>
<th>Mass (g)</th>
<th>ESA/TSA% (corrected)</th>
<th>ESA/TSA% (uncorrected)</th>
<th>SSA (m²/g)</th>
<th>SSA (m²/g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>KGa-1</td>
<td>32</td>
<td>5.19 x 10^-12</td>
<td>33.1 ± 0.8</td>
<td>27.3 ± 0.7</td>
<td>6.0 ± 0.2</td>
<td>10.1 ± 0.3</td>
</tr>
<tr>
<td>KGa-1b</td>
<td>52</td>
<td>5.67 x 10^-12</td>
<td>38.3 ± 1.0</td>
<td>30.0 ± 0.8</td>
<td>4.7 ± 0.1</td>
<td>11.3 ± 0.3</td>
</tr>
<tr>
<td>KGa-2</td>
<td>77</td>
<td>2.35 x 10^-14</td>
<td>23.4 ± 0.6</td>
<td>18.2 ± 0.5</td>
<td>11.5 ± 0.3</td>
<td>24.1 ± 0.6</td>
</tr>
</tbody>
</table>

Note: A 2.5% error for ESA/TSA and SSA was assigned because cumulative ESA/TSA and SSA measurements settled within a 5% variability range.
measurement. We note also that only 32–77 particles were needed to obtain relatively invariant cumulative surface area values, with more particles needed for particle distributions skewed toward smaller sizes. Analyzed particles had cumulative masses (Table 1) of only a few picograms, whereas N2 BET analysis of these materials requires ~100 mg.

Several studies have been conducted to quantify EISA/TSA ratios of kaolinite particles from AFM images, often on the same samples examined here. Zbik and Smart (1996) measured 120 KGa-1 particles and determined an EISA/TSA ratio of >39%. This agrees well with our result, especially considering that it should correspond more closely to the value calculated without bottom correction (33.1 ± 1.7%). Brady et al. (1996) performed similar measurements of a small number of KGa-1 particles, and found EISA/TSA ratios ranging from 0.13–0.47. Suthheimer et al. (1999) and Zhou (1996) (two reports of the same study) performed less exact measurements of 170 KGa-1 and KGa-2 particles, defining an average diameter and average height for each particle and then calculating surface area values assuming a perfect hexagonal plate shape. They reported mean EISA/TSA values of 0.17 for KGa-1 and 0.18 for KGa-2. However, these ratios do not include contributions to the EISA from basal plane step edges, which they estimated would raise the ratio by 20–30%. Therefore, their estimate for KGa-2 is in good agreement with ours, but the estimate for KGa-1b disagrees substantially.

In all previous studies, mean, rather than cumulative, EISA/TSA ratios were calculated. Cumulative values correctly weight the contribution of each particle, whereas mean values weight all particles equally. Also, Zhou (1996) and Suthheimer et al. (1999) stated that they excluded many unimaged aggregated particles from their measurements, which might bias their particle size distributions. It is interesting to note that Zhou (1996) calculated mean SSA values for KGa-1b and KGa-2 that were within 4% of at least one BET measurement in Table 2. However, mean and median SSA values were higher by 20–68%, and no rigorous statistic argument was given for why the mean value should reproduce the BET SAs more accurately.

The excellent agreement between SSA values calculated from AFM images and the BET method indicates that the AFM technique should prove exceptionally useful for the characterization of clay or nanoparticle samples too small for BET analysis. The precise determination of edge vs. basal surface area of clays should lead to improved understanding of bulk powder reactivity in industrial and natural processes.

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**Ab Initio** Determination of
Edge Surface Structures for Dioctahedral 2:1 Phyllosilicates:
Implications for Acid-Base Reactivity

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Barry R. Bickmore¹, Kevin M. Rosso², Kathryn L. Nagy³, Randall T. Cygan⁴, and
Christopher J. Tadanier⁵

**Abstract**—The atomic structure of dioctahedral 2:1 phyllosilicate edge surfaces was calculated using pseudopotential planewave density functional theory. Bulk structures of pyrophyllite and ferripyrophyllite were optimized using periodic boundary conditions, after which crystal chemical methods were used to obtain initial terminations for ideal (110)- and (010)-type edge surfaces. The edge surfaces were protonated using various schemes to neutralize the surface charge, and total minimized energies were compared to identify which schemes are the most energetically favorable. The calculations show that significant surface relaxation should occur on the (110)-type faces, as well as in response to different protonation schemes on both surface types. This result is consistent with atomic force microscopy observations of phyllosilicate dissolution behavior. Bond-valence methods incorporating bond lengths from calculated structures can be used to predict intrinsic acidity constants for surface functional groups on (110)- and (010)-type edge surfaces. However, the occurrence of surface relaxation poses problems for applying current bond-valence methods. An alternative method is proposed that considers bond relaxation, and accounts for the energetics of various protonation schemes on phyllosilicate edges.

**Key Words**—Density functional theory, clay edge surfaces, MUSIC, dissolution kinetics, ab initio, pyrophyllite, surface structure

¹ Department of Geology, Brigham Young University, Provo, UT 84602-4606. E-mail: barry_bickmore@byu.edu
² Environmental Molecular Sciences Laboratory, Pacific Northwest National Laboratory, P.O. Box 999, MSIN K8-96, Richland, WA 99352.
³ Department of Earth and Environmental Sciences, University of Illinois at Chicago, Chicago, IL 60607-7059
⁴ Geochemistry Department, Sandia National Laboratories, Albuquerque, NM 87185-0750
⁵ Department of Geological Sciences and Charles E. Via Department of Civil and Environmental Engineering, Virginia Tech, Blacksburg, VA 24061.
Phyllosilicate surface chemistry is an important control on ion mobility and pH in natural waters, permeability reduction in reservoir rocks, groundwater flow through engineered barriers, and clay rheology. In addition, phyllosilicate clays have a number of industrial applications due to their distinctive surface chemical properties. Therefore, a detailed atomic-scale understanding of phyllosilicate surface chemistry is desirable. While the basal surfaces of phyllosilicates have been the subject of numerous studies, the reactivity of edge surfaces is less well known because edges are difficult to isolate experimentally, and more difficult to model atomistically.

Edge and basal surfaces of phyllosilicates vary greatly in reactivity due to the extreme anisotropy of phyllosilicate crystal structures. For example, edge surfaces exhibit pH-dependent surface charging behavior, whereas siloxane-terminated basal surfaces do not (White and Zelazny, 1988; Bleam, 1993; Bleam et al., 1993). Furthermore, acid dissolution of phyllosilicates proceeds almost exclusively at edge surfaces (Kaviratna and Pinnavaia, 1994; Turpault and Trotignon, 1994; Rufe and Hochella, 1999; Bosbach et al., 2000; Bickmore et al., 2001). These differences in acid-base reactivity arise because edge surfaces are terminated by valence unsaturated oxygen atoms, whereas oxygen atoms on siloxane-terminated basal surfaces are valence saturated. Underbonded oxygen atoms electrostatically attract protons, and participate in pH-dependent charging behavior or bond dissociation (Xiao and Lasaga, 1994; Ganor et al., 1995; Bickmore et al., 2001). Solution-chemical investigations of dissolution and pH-dependent charging cannot be interpreted on a molecular level without assuming some sort of surface structural model.

The most useful models of phyllosilicate edge surfaces take into account site type, distribution, and density. First attempts included schematic representations of surface site types (Schofield and Samson, 1953; Muljadi et al., 1966), but did not address site density or distribution. White and Zelazny (1988), Bleam (1993), Bleam et al. (1993), Brady et al. (1996), and Bickmore et al. (2001) used crystal chemical methods to predict site type, distribution, and density. The precise termination of each edge surface is determined by cutting the crystal structure parallel to the plane of interest in such a way as to break the weakest bonds and preserve stoichiometry (Bleam et al., 1993). The same results are achieved by terminating each surface at the edges of periodic bond chains, as defined by Hartman-Perdock periodic bond chain (PBC) theory (Hartman and Perdock, 1955a; 1955b; 1955c; White and Zelazny, 1988; Bickmore et al., 2001). Crystal chemical methods predict that only two types of edge surfaces should exist, (010) and (110) (Fig. 1) (White and Zelazny, 1988; Bickmore et al., 2001). (This assignment of Miller indices assumes a 1M polytype. The (110) face is not symmetrically equivalent to the(110) face in triclinic structures, but bond lengths and single-layer unit cell parameters are nearly identical for 1M and 1Tc pyrophyllite structures (Bleam et al., 1993), so the two faces are treated as equivalent here.) Edge surfaces are stabilized in the presence of water by chemisorption of water species (Bleam et al., 1993). However, crystal chemical rules cannot always be used to distinguish between different surface protonation schemes, and there are differences in this regard among the edge surface models mentioned above (Fig. 2). Another complication is surface relaxation (i.e. shifts in electron density, and hence bond lengths, with respect to the bulk structure), which Bleam et al. (1993) did not consider. White and Zelazny (1988) proposed a protonation scheme for the (110) surface based on relaxation patterns observed for related minerals (Fig. 2e), but this model remains hypothetical.
Molecular modeling methods can be used to calculate simultaneously the lowest-energy configuration of attached protons and surface structural relaxation. Yet few molecular modeling calculations are available for edge structures of phyllosilicates, and none at the ab initio level of theory to our knowledge (Bleam, 1993; Bleam et al., 1993). In this paper we report results of calculations using pseudopotential plane wave density functional theory (PPW-DFT) for neutral, protonated, edge-surface structures of dioctahedral 2:1 phyllosilicates. The calculations test and improve the models discussed above by treating edge structures at a more fundamental level than has been attempted before. Among other things, we specifically investigated the structural relaxation and energetic stability of proton configurations postulated by White and Zelazny (1988). Implications of these calculations were explored with respect to the pH-dependent charging behavior and acid dissolution of dioctahedral phyllosilicates.

**METHODS**

All structures and total energies were calculated using the PPW-DFT method as implemented in CASTEP (Payne et al., 1992). The generalized gradient approximation (GGA) and generalized gradient local spin approximation (GGS) were applied using the Perdew-Wang (Perdew and Wang, 1992) parameterization of the exchange-correlation functional, modified to work with planewave calculations (White and Bird, 1994). We used the CASTEP parameterization of ultrasoft pseudopotentials (Vanderbilt, 1990) without core corrections. Pseudopotentials were generated using the local density approximation (LDA/LSDA), meaning that the screening effect of the core electrons was modeled using LDA/LSDA, whereas the screening effect of the valence electrons was modeled using GGA/GGS. This approach has been validated previously (Garcia et al., 1992) and successfully applied to structure optimizations of 2:1 phyllosilicates (Rosso et al., 2001).

Pyrophyllite edge structure models with Al\textsuperscript{3+} or Fe\textsuperscript{3+} occupying the octahedral sites were generated from optimized bulk structures \( (Al,Fe)Si_2O_5(OH) \). The atomic coordinates and cell parameters of bulk 1\textit{Tc} pyrophyllite were optimized simultaneously without symmetry constraint (i.e., in the P1 space group). GGA was used for Al\textsubscript{2}Si\textsubscript{2}O\textsubscript{5} and GGS for Fe\textsubscript{2}Si\textsubscript{2}O\textsubscript{5}. For the latter, knowledge of the ordering of unpaired spins in ferripyrophyllite is incomplete, but anti-ferromagnetic coupling of high-spin Fe\textsuperscript{3+} within ideal dioctahedral layers has been observed (Coey, 1988). Thus, in our calculations, a net spin of zero was assigned to the unit cell so as to impose an anti-ferromagnetic spin distribution for each 2:1 layer. One k-point was used (gamma point), which gave satisfactory results for closely related mineral structures (Bridgeman et al., 1996; Chatterjee et al., 2000; Rosso et al., 2001). Optimization was performed using a cutoff energy of 300 eV and a conjugate gradient electronic minimizer using a density mixing scheme (Kresse and Furthmuller, 1996). Finite basis set error estimations using methods described in Payne et al. (1992) were < 0.1 eV/atom, indicating that the bulk structure calculations were converged with respect to basis set size. Although these computational conditions are chosen in part due to the need for computational efficiency for our large structures, similar conditions were found to provide accurate structures and energetics in a previous study on phyllosilicates (Rosso et al., 2001).

Edge structures were then excised from optimized bulk configurations. Because the PPW calculations in this study always have three-dimensional periodic boundary conditions, surfaces were constructed by building in a vacuum layer (Rosso, 2001). In our case, two mutually perpendicular vacuum layers were present for each edge model. Because we used only one 2:1
layer for the edge structure calculations, the first vacuum layer is oriented parallel to the basal plane. The other vacuum layer in each model separates the edge surfaces of interest. Thus, the edge models are best described as polymer-like, because they are structurally contiguous and are treated as infinitely periodic units along only one dimension. Edge terminations, generated by PBC theory, were identical to those described in White and Zelazny (1988) and other previous studies cited above. The vacuum layers separating the edge models between adjacent cells were always > 10 Å; and models were designed with an inversion center to ensure that interactions across the vacuum layers were negligible. The infinitely repeating chains were chosen to run along the [110] and [100] vectors, generating edge surfaces of the (110) and (010) types, respectively (Fig. 3). Protons were added to edge sites to correspond with neutral protonation schemes proposed by White and Zelazny (1988) and Bleam (1993), as well as one that has never before been suggested (see Fig. 2), while keeping the basal surfaces unchanged (vacuum terminated). The coordinates of all atoms in each of the protonated edge models were energy optimized using the same treatment as described for the bulk structures above, except with fixed lattice parameters, where the unit cell dimension along the edge vector was determined from the corresponding bulk optimization.

RESULTS AND DISCUSSION

Bulk Structures

Atomic positions and unit cell parameters derived from the bulk structure optimizations are reported in Table 1. Although these calculations were performed without symmetry constraints, the bulk structures converge to their proper space group symmetries (C1̅), as determined using a structural search tolerance of ~ 0.1 Å. The accuracy of the calculated structures can be evaluated further in two ways.

First, calculated unit cell parameters can be compared with experimental values for 1Tc pyrophyllite (Lee and Guggenheim, 1981) and a 2M ferripyrophyllite (Chukhrov et al., 1979) (Table 2). Unit cell parameters for the calculated structures are given in the C1̅ space group for direct comparison to the 1Tc pyrophyllite structure. However, only the calculated a and b cell dimensions are directly comparable to those measured for ferripyrophyllite (Chukhrov et al., 1979), which was a 2M polytype. Calculated ferripyrophyllite values agree well with those measured. Calculated unit cell parameters for pyrophyllite are close to measured values, except that the calculated c dimension is larger by 0.49 Å. Overestimated c-axis lengths may be due to the particular computational conditions applied. Our results for pyrophyllite and those from Teppen et al. (2002) were obtained using slightly different methods and produced slightly different c-axis dimensions. Their c-axis estimate is also overestimated, but is closer to the experimental value (larger by 0.16 Å). The overestimated lengths also could be related to the incomplete description of van der Waals attractive forces in DFT (Wu et al., 2001). Pyrophyllite layers are held together predominantly by van der Waals forces, and the c-axis dimension is sensitive to the description of interactions across the interlayer (Giese, 1975). However, the accuracy of the c-axis dimension becomes insignificant in the context of the edge surface calculations because the calculations are based on single isolated 2:1 layers making interlayer interactions irrelevant.

Second, we suggest that the set of predicted bond lengths in each structure should show systematic correspondence with the bond valence model of Brown and Altermatt (1985). The
total Brown (1981) bond strength reaching each cation in the structure, computed using the relevant bond lengths predicted ab initio, should equal the cation’s formal charge. This evaluation method has at least one advantage—systematic deviations in the computed bond lengths can be identified for structures (such as that of pyrophyllite) comprised of asymmetrically distorted polyhedra. For example, it is not clear that simply tabulating and averaging all computed Al–O bond lengths for comparison with a “grand universal” mean observed Al–O distance would be sensitive to subtle computational errors. In fact, Brown’s (2002) “distortion theorem” states, “For any ion, lengthening some of its bonds and shortening others, keeping the bond valence sum the same, will always increase the average bond length.” Thus, comparing average Al–O bond length with some idealized value could lead to the conclusion that the computations overestimate bond lengths when, in fact, the opposite might be the case.

Brown and Altermatt (1985) fit the following bond valence expression to a large number of crystal structures in the Inorganic Crystal Structure Database:

\[ s = \exp\left(\frac{r_0 - r}{B}\right) \]  

where \( s \) is bond valence in valence units (v.u.), \( r \) is bond length, \( r_0 \) an arbitrary bond length fitted for each pair of atoms, and \( B \) is a fitted parameter usually equal to 0.37 Å. The summed strength of bonds reaching a cation should be equal to its formal charge. Based on our models, calculated total bond strengths reaching the Si atoms in pyrophyllite were 4.08-4.11 v.u. and 4.09 v.u. in ferripyrophyllite. Total bond strengths reaching Al atoms were 3.09-3.10 v.u. in pyrophyllite and total bond strengths reaching Fe atoms in ferripyrophyllite were 3.19-3.20 v.u. This means that the calculated bond lengths were, on average, ~0.01 Å too short for Si–O and Al–O bonds, and ~0.02 Å too short for Fe–O bonds. Estimated standard deviations for these bond lengths, reported by Brown and Altermatt (1985), range from 0.001 to 0.003 Å. Thus, the bond length underestimation is likely a real artifact of the PPW-DFT calculations. Nonetheless, the agreement between calculated and expected bond lengths is still quite good.

**Edge Structures**

Using the PPW-DFT optimizations, lowest energy configurations of protons were sought for each of the edge models, and the extent of surface relaxation was explored. For both (010)- and (110)-type faces, the protonation schemes suggested by White and Zelazny (1988) were clearly energetically favorable. Furthermore, the surface relaxation predicted for the (110)-type faces by White and Zelazny (1988) was qualitatively confirmed.

Edge structure calculations were based on models that were infinitely periodic in one direction. To avoid excessive computational costs, the models were designed to be no more than ~10 Å wide perpendicular to the edges. In cases where models are “thin,” it is important to verify that relaxation effects from the opposing surfaces do not penetrate the full width of the model. To test for such an effect, distortion of bond lengths in the relaxed structures was checked. Table 3 shows the range of distortion for each type of bond in the interior polyhedra of each edge structure (Fig. 2), with respect to the same bonds in unrelaxed structures. These bond shifts are relatively small, so we conclude that the edge structure models are of sufficient width to adequately mimic both the bulk and edge structural environments.

Our surface structure calculations did not include an overlying bulk water phase, which might affect the relative stabilities of surface proton configurations. However, we will show that the valences of O–H bonds in the surface hydroxyl groups in our calculations were similar to those of O–H bonds in bulk water. That is, the O–H bonds were about 0.8 v.u., leaving 0.2 v.u.
on the H to donate to H-bonds. Therefore, the vacuum-terminated surface structures probably would not be affected much by the addition of bulk water.

The structures of (010)-type faces were calculated with the protonation schemes shown in Fig. 2a-b, and their total energies compared. The (010)-type faces are terminated by silanol and aluminol or ferrinol groups, and the proton configuration to neutralize this surface typically has been assumed to be like that depicted in Fig. 2a. The proton configuration depicted in Fig. 2b also should be considered as a possibility, based on the results of this study which show that deprotonation of a silanol group occurs at a lower pH than deprotonation of one of the aluminols. However, when the starting structure in Fig. 2b was optimized, it was so energetically unfavorable that a proton on one of the aluminol (pyrophyllite)/ferrinol (ferripyrophyllite) groups “hopped” over to the adjacent deprotonated silanol group. This result is discussed further below.

(110)-type edge structures with starting proton configurations as shown in Fig. 2c-d were also optimized. The minimal edge unit of the vacuum-terminated (110)-type edge exposes four underbonded oxygen atoms for each 2:1 layer, consisting of two silanol groups, one Si–O–Al bridging oxygen, and one aluminol/ferrinol group. Each edge has a net charge of -4 that must be neutralized with protons. Adding one proton to each underbonded O atom at an edge is a commonly assumed scheme (Bleam, 1993) (Fig. 2c). Assuming that surface relaxation tends toward the neutralization of unsaturated valence on individual surface groups, White and Zelazny (1988) proposed an alternative protonation scheme that differs simply by doubly protonating the aluminol/ferrinol and leaving the bridging O atom unprotonated (Figs. 2d-e). Note that this difference requires only a small translocation of a proton from its optimized location on the bridging oxygen atom to the aluminol/ferrinol oxygen atom (a distance of ~ 2.2 Å). We optimized both configurations to assess their relative stabilities. Total energies of the two configurations indicate that White and Zelazny’s (1988) scheme is lower in energy by -0.44 eV for pyrophyllite and -0.25 eV for ferripyrophyllite per 2:1 edge. This indicates that the singly protonated aluminol/ferrinol groups have a higher proton affinity; i.e., they are more basic than the bare bridging O atom. Such a configuration appears to be partly stabilized by the participation of one of the Al–OH2/Fe–OH2 protons in hydrogen bonding to the bridging O atom. This result agrees in principle with the electrostatic calculations of Bleam et al. (1993) and the predictions of White and Zelazny (1988). The hydrogen-bonding interaction between the proton on the aluminol/ferrinol groups and the bridging O atom on the (110)-type surface is weak (0.026-0.032 v.u.). Thus, although it is probable that this interaction would be screened by intervening water molecules, we would not expect the screening to cause a reversal in the relative stabilities of the two protonation schemes. Therefore, it is concluded that the protonation scheme in Fig. 2c is less likely to be important than the scheme proposed by White and Zelazny (1988) (Figs. 2d-e).

White and Zelazny (1988) also predicted a certain amount of structural relaxation at the (110)-type surfaces, resulting in the configuration illustrated in Fig. 2e. Table 4 shows the total strength of bonds reaching the oxygen atoms of the surface functional groups on the (010)- and (110)-type surfaces shown in Figs. 2a and 2d-e, excluding O–H bonds. The values in Table 4 are corrected for the tendency of our calculations to underpredict bond lengths by subtracting the average overestimation of bond valence for each type of bond in our calculated bulk structures. That is, 0.017 v.u. was subtracted from the computed valence of Al–O bonds, 0.033 v.u. from that of Fe–O bonds, and 0.025 v.u. from Si–O bonds. The O–H bonds on the surface functional groups were computed to have bond strengths of 0.75-0.80 v.u., in good agreement with the assumption of Hiemstra et al. (1996) that surface hydroxyl bond strengths are close to O–H bond
strengths for bulk water (0.80 v.u.). White and Zelazny (1988) predicted that Si–O, Al–O, and Fe–O bond lengths reaching the bridging oxygens should contract significantly, and the Al–O and Fe–O bond lengths in the aluminol and ferrinol groups should expand significantly. Therefore, due to this relaxation of the edge structure, the total strength of bonds reaching the bridging oxygens on (110)-type surfaces was predicted to be 2.00 v.u., and the strength of the Al–O and Fe–O bonds in the aluminol and ferrinol groups was predicted to be 0.00 v.u. On the other hand, if no structural relaxation occurs (Bleam et al., 1993), the total strength of bonds reaching the bridging oxygens should be ~1.50 v.u., and the strength of the Al–O and Fe–O bonds in the aluminol/ferrinol groups would be ~0.50 v.u.

The PPW-DFT calculations confirm the structural relaxation predicted by White and Zelazny (1988), although the degree of relaxation is not so extreme as they envisaged. The Si–O, Al–O, and Fe–O bonds reaching the bridging oxygens do contract by 0.04-0.14 Å, and the Al–O and Fe–O bonds in the aluminol and ferrinol groups expand by 0.10-0.13 Å. The total corrected valence of bonds reaching the bridging oxygen is computed to be 1.861 v.u. for pyrophyllite and 1.757 v.u. for ferripyrophyllite. The Al–O bond strength in the aluminol (pyrophyllite) is 0.327 v.u., and the Fe–O bond strength on the ferrinol (ferripyrophyllite) is 0.316 v.u. Therefore, most of the structural relaxation predicted by White and Zelazny (1988) for the bonds reaching the bridging oxygens occurs, whereas predicted relaxation for the Al–O and Fe–O bonds in the aluminol/ferrinol groups is less.

The small relaxation of the aluminol/ferrinol groups on (110)-type surfaces takes on added meaning when compared to similar functional groups on the (010)-type surfaces. In the unrelaxed bulk structures, the Al–O bond on the (110)-type aluminol has a corrected bond valence of 0.431 v.u., and the Fe–O bond on the equivalent ferripyrophyllite site has a bond valence of 0.460 v.u.. Unrelaxed Al–O and Fe–O bonds on the (010)-type surfaces have bond strengths of 0.569 and 0.551-0.569 v.u., respectively. Table 4 shows that the Al–O and Fe–O bonds of singly-protonated (010)-type aluminol/ferrinol groups have bond strengths of 0.674 and 0.698 v.u., respectively. On the other hand, the Al–O and Fe–O bonds of doubly-protonated (010)-type aluminol/ferrinol groups have bond strengths of 0.290 and 0.332 v.u. These values are close to the bond strengths of doubly-protonated Al–O and Fe–O bonds in (110)-type aluminol/ferrinol groups—0.327 and 0.316 v.u., respectively. Since the Al–O and Fe–O bond valences for aluminol/ferrinol groups are different between unrelaxed (010)- and (110)-type surfaces, but nearly identical on relaxed surfaces when the protonation is the same, it can be argued that the valence of Al–O and Fe–O bonds in the aluminol/ferrinol groups is controlled largely by the degree of protonation.

Finally, the corrected bond valences of the Si–O bonds of the silanol groups on the surfaces studied ranged from 0.99-1.05 v.u. These values bracket the ideal bond strength of 1.00 for Si–O bonds in silica tetrahedra.

**Acidity of phyllosilicate edges**

In the past, treatments of phyllosilicate surface-charging behavior have employed various surface complexation models (e.g., constant capacitance, triple-layer, etc.) to rationalize potentiometric titration data (e.g., Brady et al., 1996; Kraepiel et al., 1998). However, most previous modeling has assumed the existence of two or three generic functional groups with integer charges, and the possibility of fractional charges has been ignored. Furthermore, with few exceptions (Chang and Sposito, 1994; Brady et al., 1996; Chang and Sposito, 1996) surface complexation models of clay minerals have not separated permanent structural charge located at
the siloxane basal surfaces from pH-dependent charge on the edge surfaces (Kraepiel et al., 1998). Neither have crystallographically distinct edge surfaces been treated separately.

In this section, we attempt to provide the basis for a more realistic treatment of phyllosilicate acid-base reactivity by using calculated surface structures to estimate acidity constants for specific functional groups. However, the current model (Hiemstra et al., 1996) designed for predicting site acidity may be oversimplified with respect to surface relaxation. Therefore, site acidities will be predicted using the model of Hiemstra et al. (1996), and also by combining ab initio surface structure calculations with a revised bond-valence approach.

The current model (MUSIC). Hiemstra and coworkers (e.g., Hiemstra et al., 1989; Hiemstra et al., 1996; Hiemstra et al., 1999) developed a multisite complexation (MUSIC) modeling approach capable of considering the contribution of specific sites on distinct crystalline surfaces. Site types are defined by crystallographic methods and intrinsic acidity constants are predicted based on the valence saturation of the oxo- and hydroxo- surface groups (Hiemstra et al., 1996). Valence saturation is calculated using the model of Brown and Altermatt (1985).

It should be possible to create MUSIC models for the acid-base behavior of euhedral clay samples using the information gained from the ab initio calculations reported here, including site coordination and bond lengths. Although we will not fit a MUSIC model to potentiometric titration data for phyllosilicates in this paper, the location, density, coordination, unsaturated valence, and predicted intrinsic acidity constants of reactive sites on dioctahedral phyllosilicate edge surfaces are calculated.

Hiemstra et al. (1996) predicted site acidities using a modified form of the following equation:

\[ pK_a = -A(\sum s_j + V) \]

where \( K_a \) is the intrinsic acidity constant, \( A \) equals 19.8, \( V \) is the valence of the surface oxygen (-2), and \( \sum s_j \) is the valence saturation of the surface oxygen, defined by:

\[ \sum s_j = \{ s_{Me} + m s_H + n(1-s_H) \} \]

Here \( s_{Me} \) is the valence of the Me–O bond, and \( s_H \) is the valence of the O–H bond to the surface oxygen if the base is a hydroxo- group. (This value was assumed by Hiemstra et al. (1996) to be 0.80 v.u., close to that for H–O bonds in bulk water.) Some of the surface oxygen valence is assumed to be neutralized by hydrogen bonds from surrounding water molecules. Oxygens have four empty orbitals with which to form Me–O, O–H, or hydrogen bonds, and \( n \) is the number free to form hydrogen bonds. However, for oxygens coordinated to one metal cation, it is usually assumed that one of the free orbitals is sterically hindered from hydrogen bonding at surfaces \( (m+n = 2 \) in equation 3), unless the surface structure is relatively open, in which case \( m+n = 3 \). One of the free orbitals may or may not be sterically hindered on surface oxygens coordinated by two metal cations. (For solution monomers, it is assumed that none of the orbitals are sterically hindered from bonding.)

Even though the bond valence method is an attempt to create physically realistic surface complexation models, it still requires several simplifying assumptions. For instance, Hiemstra et al. (1996) assumed the bond strength of H–O bonds on surface functional groups to be 0.80 v.u. Similarly, acidity constants for crystallographically distinct surface groups can sometimes be treated as equivalent, even though slight variations in bond valence exist. Also, surface reactions are written assuming Pauling bond valences for simplicity in charge bookkeeping (Hiemstra et al., 1996).
We calculated pKₐ values for reactions taking place on the various surface functional groups on (010)- and (110)-type surfaces using the MUSIC model (Table 5). Bulk bond lengths were used to calculate unsaturated valence.

Generally, the calculated pKₐ values are similar to those assigned to analogous functional groups on simple oxides. For instance, we calculate pKₐ values of 7.6–8.7 for silanol groups, and Hiemstra et al. (1996) assigned an average pKₐ of 7.9 for these groups on silica surfaces. Similarly, calculated pKₐ values for the loss of a proton from a doubly-protonated silanol group ranged from –4.3 to –3.1, whereas Hiemstra and coworkers used a value of –4.0. Aluminol groups were calculated to have pKₐ values of 8.5–10.6, whereas Hiemstra et al. (1999) assigned an average pKₐ of 9.9 for aluminols on gibbsite surfaces. The calculated pKₐ values for ferrinol groups (8.5–10.7) are somewhat higher than the value of 7.7 assigned to these groups on goethite surfaces (Hiemstra et al., 1996). However, this is easily explained by the highly distorted nature of Fe³⁺ octahedra in the 2:1 structure.

Problems with the current model. The above assignment of pKₐ values is somewhat unsatisfying for the following reasons. First, the bond-valence method of Hiemstra et al. (1996) explicitly assumes that no surface relaxation occurs, and therefore, bulk Me–O bond lengths can be used to calculate the unsaturated valence of surface oxygens. On the contrary, our calculations show that the Me–O bond lengths in the aluminol/ferrinol groups relax rather dramatically, the singly-protonated forms having shorter, and the doubly-protonated forms having longer, bond lengths than in the bulk structure. This difficulty is especially acute with respect to the estimation of pKₐ values for bridging oxygens on (110)-type faces. We have shown that the bonds to these oxygens relax considerably on neutral surfaces, so it is not apparent why bulk bond lengths should be adequate for predicting the acidity of these groups. Alternatively, we cannot simply substitute bond valences from calculated surface structures into Eq. 3 and expect to obtain realistic pKₐ values. For example, if the relaxed Al–O bond valence for singly-protonated aluminol groups on (010)-type surfaces were used (0.674 v.u.) in Eq. 3, the calculated pKₐ for the deprotonation of doubly-protonated aluminol groups would be 6.5, instead of 8.5–10.6.

Second, the treatment of solvation in this method is inconsistent. For instance, singly-coordinated surface oxygens are defined to have only two orbitals available for proton binding or H-bonding interactions \((m+n = 2)\) in Eq. 3 because of steric constraints, but in order to properly predict the acidity constants for silanol groups, it has to be assumed that three orbitals are available \((m+n = 3)\). Similarly, surface oxygens bound to two metal atoms can have either one or two orbitals available \((m+n = 1\) or 2\) for proton binding or H-bonding interactions (Hiemstra et al., 1996). Thus, the number of free oxygen orbitals is effectively another fitting parameter.

Third, the idea that acidity constants would be correlated with total unsaturated valence on surface oxygens of the base is also surprising. Since O–H bonds involve only one O orbital, it seems more likely that acidity would correlate with the unsaturated valence available in a single orbital of the basic form.

Finally, application of the current bond-valence model predicts that silanol groups on (010)-type faces should be slightly more acidic than adjacent aluminol groups, but our calculations show that the protonation scheme in Fig. 2b is quite unstable.

An older model revised. It appears that bond relaxation may actually be a key to understanding surface acidity constants. Experimentation with different methods of predicting acidity constants for functional groups on our relaxed surfaces has led us to propose a revision of the bond-valence model first proposed by Brown (1981; 2002). This model is capable of
incorporating surface relaxation, does not require inconsistent treatment of solvation, and properly divides bonding power among orbitals. While full development of this model awaits more computational and experimental data, early results for the calculated phyllosilicate surface structures are promising.

Brown’s (1981) model is based on a correlation between the Lewis base strength of the base in an acid-base reaction and measured pKₐ values of solution monomers. The correlation equation is

\[ \text{pK}_a = 14.3 \ln(S_b/0.135) \]  (4)

where \( S_b \) is the base strength, which is the total unsaturated valence divided by the number of free possible bonds. Consider, for example, the following reaction.

\[ \text{HSO}_4^- \rightleftharpoons \text{SO}_4^{2-} + \text{H}^+ \]  (5)

The valence of sulfur (+6) is divided among four S–O bonds, so that each S–O bond has a valence of 1.5. This leaves a total unsaturated valence of 2 v.u. Since oxygen is 4-coordinated on average, we assume that there are four bonding “orbitals” per oxygen, one of which is taken up by an S–O bond. Since there are three remaining possible external bonds per oxygen, and 4 oxygens, we divide the total unsaturated valence by 12 to obtain a Lewis base strength of 0.17 (2 v.u./12 possible external bonds). Substituting this value into Eq. 4, we obtain a pKₐ of 3.0. This is fairly close to the value reported by Perrin (1982) of 1.99.

It is somewhat more complicated to calculate the Lewis base strength of a protonated oxyanion. Consider the following reaction.

\[ \text{H}_4\text{SiO}_4 \rightleftharpoons \text{H}_3\text{SiO}_4^- + \text{H}^+ \]  (5)

Assuming Si–O bonds of 1.00 v.u. and O–H bonds of 0.80 v.u., each of the oxygen atoms not connected to a hydrogen would have 1.00 v.u. of unsaturated valence. In the previous example, it was assumed that each oxygen atom could form four bonds, but Brown (2002) maintained that the protonated oxygen atoms only have enough unsaturated valence for one weak bond, so we assume that each of these is 3-coordinated, while the deprotonated oxygen is 4-coordinated. This leaves 6 possible external bonds among which to divide the unsaturated valence. Since there is 0.2 v.u. of unsaturated valence on each protonated oxygen, and 1.0 v.u. on the deprotonated oxygen, we divide the total 1.6 v.u. unsaturated valence between 6 possible external bonds to obtain a Lewis base strength of 0.27. Substituted into Eq. 4, this yields a pKₐ of 9.9, which exactly matches the experimentally determined value of 9.9 reported by Perrin (1982).

There are, however, potential problems with this method of calculating Lewis base strength. First, it is not clear why the unsaturated valence would be evenly distributed about the possible external bonds. Would not the base strength of possible bonds to the bare oxygen necessarily be greater than that of the possible bonds to protonated oxygens? Second, our calculations show that Me–O bond lengths tend to contract or expand in response to varying protonation of the oxygen. Therefore, it is not clear that all the Si–O bond valences in H₃SiO₄⁻ should be 1.00 v.u.

It is probable that similar base strengths can be estimated if bond relaxation is taken into account. For example, results from PPW-DFT optimizations of charged pyrophyllite and ferripyrophyllite edge surfaces (K.M. Rosso, unpublished results) produce Si–O bond valences of 1.1-1.3 v.u. for deprotonated silanol groups, whereas the calculations of neutral surface structures yield Si–O bond valences of around 1.00 for singly-protonated silanol groups. If we substitute 1.2 v.u. for the Si–O bond valence on the deprotonated oxygen, then divide the unsaturated valence of that specific oxygen between the three non-bonded orbitals, we obtain a Lewis base strength of 0.27 v.u. (0.8 v.u./3 possible bonds). This is exactly the same base
strength as calculated above, and can be used directly in Eq. 4 to predict a pKₐ of 9.7. Sefcik and Goddard (2001) recently used DFT methods to calculate silicate anion geometries. Calculated Si–O bond lengths for the deprotonated oxygen in gas and aqueous phases yielded bond strengths of 1.17 and 1.18 v.u., respectively. Following the procedure outlined above, these values yield respective base strength values of 0.28 and 0.27, and pKₐ values of 10.4 and 9.9.

Will this method of Lewis base strength and pKₐ estimation hold true for oxyanions in general? Structural calculations on oxyanions with well-defined acidities need to be carried out to test this hypothesis. However, at this point the method can be used with our calculated phyllosilicate surfaces to obtain reasonable pKₐ values (Table 6). Furthermore, the approach can explain aspects of our data that the model of Hiemstra et al. (1996) cannot.

Acid-base reactions on neutral surfaces are supplemented by those on charged surfaces containing fewer protons (K. Rosso, unpublished results) in Table 6. Comparison of pKₐs with those in Table 5 shows that the new method predicts values near those predicted using the method of Hiemstra et al. (1996). Exceptions include silanol groups on (110)-type surfaces and (110)-type bridging oxygens. (We note that calculated pKₐ values for the deprotonation of doubly-protonated silanol groups varied widely in the negative range. This is likely due to the sensitivity of Eq. 4 in this range, but even still several of the calculated values agree well with those in Table 5.)

The values of silanol pKₐs on (110)-type surfaces can be rationalized by observing that significant relaxation takes place on these faces, corresponding to shifts in bond valence. For example, since the Si atom bonded to the bridging oxygen shifts some of its bond valence to that oxygen, it cannot transfer as much valence to the adjacent silanol if that group is deprotonated. Therefore, the silanol becomes more basic.

If the relaxation of bonds between a metal cation and one functional group can affect the acidity of another functional group bonded to the same metal cation, this new method of pKₐ calculation may help explain our inability to optimize the surface structure in Fig. 2b. It is possible that doubly protonating both aluminols causes adjacent bonds in the structure to relax, with the net effect of making the silanol more basic. Thus, it would be energetically favorable for a proton to hop from one of the doubly-protonated aluminols to the silanol.

Implications of the proposed model. More calculations and experiments must be performed to test and refine this model of acidity constant prediction, but if the model premise is correct then there are profound implications for multsite complexation modeling.

First, the relaxation effects described above imply that one cannot simply assign a single pKₐ to each type of surface group. Acidity of one group may be strongly affected by the protonation state of adjacent groups. In retrospect, this conclusion should hardly be surprising, and we are not the first to put forward this idea (Stumm, 1992). Existing surface complexation models are not equipped to deal with shifting acidity constants, but detailed ab initio studies may correct this deficiency by providing information on the proportion of various site types that can be expected to exhibit a given pKₐ.

Second, our proposed model for pKₐ prediction treats the solvation of surface functional groups consistently. In fact, no differences in solvation are postulated, whether between surface functional groups with different coordination, or between functional groups on surfaces and solution monomers. This conclusion contradicts recent work postulating that differences in solvation behavior contribute significantly to differences in the acidity of surface functional groups and analogous groups on solution monomers. Sverjensky and Sahai (1996) and Sahai (2002) showed that points of zero charge for simple oxide surfaces can be correlated to equations
that take into account both average bond valence and average dielectric constant for the mineral structures. Although the correlation is completely empirical, the contribution of the dielectric constant was qualitatively related to Born solvation theory. We suggest that the correlation of the dielectric constant with surface acidity is due to the fact that the dielectric constant is a measure of the “polarizability” of the crystal structure, and might thus be related to the ability of bonds at the solid surface to relax. It may be differences in bond relaxation on surfaces and analogous solution monomers that control differences in acidity.

Acid dissolution of phyllosilicates

It is generally agreed that acid dissolution of phyllosilicates proceeds almost exclusively at edge surfaces, and recent *in situ* atomic force microscopy (AFM) observations of the process confirm this (Rufe and Hochella, 1999; Bosbach *et al.*, 2000; Bickmore *et al.*, 2001). However, different mechanisms of proton attack have been proposed. After fitting a surface complexation model to kaolinite, Wieland and Stumm (1992) noted that the dissolution rate could be modeled as a first-order function of the concentration of protonated aluminol sites at the edge faces. It was proposed that the rate-controlling activated complex in the dissolution reaction has a stoichiometry of 1 H to 1 Al, and protonated aluminol groups are precursors to the activated complex. On the other hand, results of *ab initio* cluster calculations (Xiao and Lasaga, 1994) showed that the key step in the dissolution of aluminosilicate groups should be proton attack at the bridging oxygen. Protons sorbed at neighboring locations did not significantly affect the dissolution reaction. Ganor *et al.* (1995) proposed that the rate-controlling dissolution step is the breaking of bonds to Si–O–Al bridging oxygen atoms. They also showed that kaolinite dissolution rates were approximately proportional to the total surface proton concentration, explaining this by hypothesizing equilibrium between the various types of surface sites. Zysset and Schindler (1996) showed that the dissolution rate of montmorillonite is proportional to the total surface proton concentration, including protons sorbed in charged interlayers. As did Ganor *et al.* (1995), they proposed equilibrium among all surface protons, but noted that they could not use their data to distinguish whether the rate-determining step in acid dissolution is hydrolysis of Si–O–Al or Al–O–Al bonds at edge surfaces.

Bickmore *et al.* (2001) attempted to settle this controversy by observing phyllosilicate dissolution with *in situ* AFM. Lath-shaped particles of nontronite (a dioctahedral smectite with mainly Fe³⁺ in the octahedral sites) and hectorite (a trioctahedral smectite with mainly Mg²⁺ in the octahedral sites) were fixed on a polyelectrolyte-coated mica surface (Bickmore *et al.*, 1999) and dissolved pH 2 HCl in the AFM fluid cell. The hectorite dissolution data were previously reported by Bosbach *et al.* (2000). It was observed that both minerals dissolved inward from the edges, but the reaction fronts on nontronite quickly became pinned at the pseudohexagonal face angles and then dissolution slowed to an imperceptible rate. In contrast, the hectorite reaction fronts showed no preferential orientation. Why were the pseudohexagonal nontronite faces so much more stable than the randomly oriented edges of nontronite and all the hectorite edges? Bickmore *et al.* (2001) used periodic bond chain theory to generate models of trioctahedral and dioctahedral edge faces. It was shown that if the surface relaxation proposed by White and Zelazny (1988) for the dioctahedral (110)-type surface occurs (Fig. 2e), all the stable faces have valence saturated bridging oxygen atoms, whereas the bridging oxygens on unstable faces are valence unsaturated. No scheme of bond relaxation could be conceptualized at the unstable faces that would neutralize the entire unsaturated valence of bridging oxygens. Underbonded bridging oxygens would electrostatically attract protons, and if the protons bonded to bridging oxygens, they would become overbonded, destabilizing the structure. If the predicted surface relaxation
does not occur (Fig. 2d), no such differences between stable and unstable faces could be detected. The acid dissolution behavior described seems to indicate that the rate-controlling step is the breaking of bonds to bridging oxygens at the edge surfaces. Furthermore, it seems to support White and Zelazny’s (1988) surface structure model, but the evidence is indirect and Bickmore et al. (2001) concluded that “molecular modeling calculations are needed to theoretically justify the predicted surface relaxation.”

As discussed above, the PPW-DFT calculations reported here confirm the structural relaxation predicted by White and Zelazny (1988), but the calculated relaxation is not so severe that the formal charge on the (110)-type bridging oxygens is fully neutralized. In fact, the bridging oxygens are predicted to be slightly underbonded, but less so than bridging oxygens on trioctahedral (110)-type surfaces (Bickmore et al., 2001). This conclusion is consistent with a modified form of the explanation of Bickmore et al. (2001) for hectorite and nontronite dissolution behavior. That is, the rate-determining step of the dissolution process is the breaking of bonds to bridging oxygens at the edge surfaces, and hence the most stable edge faces during acid dissolution are those with little or no unsaturated valence on the bridging oxygens.

CONCLUSIONS

The structure of ideal pyrophyllite and ferripyrophyllite neutral edge surfaces has been calculated ab initio using PPW-DFT methods. Results of the calculations favor the surface protonation scheme predicted by White and Zelazny (1988) and Bleam et al. (1993), and predict that much of the surface relaxation envisaged by White and Zelazny (1988) for (110)-type surfaces should occur. Relaxed surface structures were also used to predict intrinsic acidity constants for acid-base reactions involving the surface functional groups present on (110)- and (010)-type edge surfaces. It was demonstrated that surface relaxation must be taken into account in the prediction of surface acidity constants, and a revision of the bond-valence method for pK\textsubscript{a} prediction was proposed for this purpose. Collectively, these results are consistent with the atomic force microscopy observations of phyllosilicate dissolution behavior made by Bickmore et al. (2001).

ACKNOWLEDGMENTS

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REFERENCES


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<td>H</td>
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Table 1. Calculated unit cell parameters and atomic coordinates for the pyrophyllite and ferripyrophyllite 1Tc structures, assuming C1̅ symmetry.
Table 2. Experimentally determined unit cell parameters for pyrophyllite 1Tc and ferripyrophyllite 2M.

<table>
<thead>
<tr>
<th>Bond Length Shifts (Å)</th>
<th>(010)-type (See Fig. 2a)</th>
<th>(110)-type (See Fig. 2c)</th>
<th>(110)-type (See Fig. 2d-e)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bond Type</td>
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<td></td>
<td></td>
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<tr>
<td>Si–O</td>
<td>-0.030 to +0.011</td>
<td>-0.033 to +0.009</td>
<td>-0.037 to +0.016</td>
</tr>
<tr>
<td>Al–O</td>
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<td>-0.061 to +0.068</td>
<td>-0.046 to +0.053</td>
</tr>
<tr>
<td>Fe–O</td>
<td>-0.021 to +0.056</td>
<td>-0.015 to +0.061</td>
<td>-0.022 to +0.067</td>
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Table 3. Calculated bond length shifts for interior polyhedra in the pyrophyllite and ferripyrophyllite edge structures, relative to the same bond lengths in calculated bulk structures.
### Total Bond Strength (v.u.) Reaching Surface Oxygens, Excluding H–O Bonds (Pyrophyllite)

<table>
<thead>
<tr>
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<th>(010)-type</th>
<th>(110)-type</th>
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<tbody>
<tr>
<td>(See Fig. 2a)</td>
<td>(See Fig. 2d-e)</td>
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</tr>
<tr>
<td>&gt;Si–O</td>
<td>1.051</td>
<td>1.025</td>
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<tr>
<td>&gt;Al–OH</td>
<td>0.674</td>
<td>&gt;SiAl–O (bridging O) 1.861</td>
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<tr>
<td>&gt;Al–OH₂</td>
<td>0.290</td>
<td>&gt;Al–OH₂ 0.327</td>
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<tr>
<td>&gt;Si–O</td>
<td>1.002</td>
<td>&gt;Si–O 0.986</td>
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### Total Bond Strength (v.u.) Reaching Surface Oxygens, Excluding H–O Bonds (Ferripyrophyllite)

<table>
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<tbody>
<tr>
<td>(See Fig. 2a)</td>
<td>(See Fig. 2d-e)</td>
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<tr>
<td>&gt;Si–O</td>
<td>1.042</td>
<td>1.031</td>
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<tr>
<td>&gt;Fe–OH</td>
<td>0.698</td>
<td>&gt;SiFe–O (bridging O) 1.757</td>
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<tr>
<td>&gt;Fe–OH₂</td>
<td>0.332</td>
<td>&gt;Fe–OH₂ 0.316</td>
</tr>
<tr>
<td>&gt;Si–O</td>
<td>0.989</td>
<td>&gt;Si–O 0.991</td>
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**Table 4.** Total calculated Brown bond strength (v.u.) reaching the surface O atoms (excluding H–O bonds) on each type of edge structure studied.
### (010)-type Surface Reactions (Pyrophyllite)

<table>
<thead>
<tr>
<th>Site Type</th>
<th>Sites/unit cell face</th>
<th>Reactions</th>
<th>pK\textsubscript{a}</th>
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</thead>
<tbody>
<tr>
<td>&gt;Si-OH (silanol)</td>
<td>2</td>
<td>&gt;Si-OH = &gt;Si-O(^-) + H(^+)</td>
<td>8.3, 8.4(^*)</td>
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<tr>
<td></td>
<td></td>
<td>&gt;Si-OH(^+_2) = &gt;Si-OH + H(^+)</td>
<td>-3.6, -3.5</td>
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<tr>
<td>&gt;Al-OH(_2) (aluminol)</td>
<td>2</td>
<td>&gt;Al-OH(_2)(^{+1/2}) = &gt;Al-OH(^{-1/2}) + H(^+)</td>
<td>8.5</td>
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### (010)-type Surface Reactions (Ferripyrophyllite)

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<th>Site Type</th>
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<tr>
<td>&gt;Si-OH (silanol)</td>
<td>2</td>
<td>&gt;Si-OH = &gt;Si-O(^-) + H(^+)</td>
<td>8.1</td>
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<td>&gt;Si-OH(^+_2) = &gt;Si-OH + H(^+)</td>
<td>-3.8</td>
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<tr>
<td>&gt;Fe-OH(_2) (ferrinol)</td>
<td>2</td>
<td>&gt;Fe-OH(_2)(^{+1/2}) = &gt;Fe-OH(^{-1/2}) + H(^+)</td>
<td>8.5, 8.9</td>
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### (110)-type Surface Reactions (Pyrophyllite)

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<tbody>
<tr>
<td>&gt;Si-OH (silanol)</td>
<td>4</td>
<td>&gt;Si-OH = &gt;Si-O(^-) + H(^+)</td>
<td>8.7, 7.6</td>
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<tr>
<td></td>
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<td>&gt;Si-OH(^+_2) = &gt;Si-OH + H(^+)</td>
<td>-3.1, -4.3</td>
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<tr>
<td>&gt;SiAl-OH (bridging O)</td>
<td>2</td>
<td>&gt;SiAl-OH(^{+1/2}) = &gt;SiAl-O(^{-1/2}) + H(^+)</td>
<td>1.5 (5.5)(^#)</td>
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<tr>
<td>&gt;Al-OH(_2) (aluminol)</td>
<td>2</td>
<td>&gt;Al-OH(_2)(^{+1/2}) = &gt;Al-OH(^{-1/2}) + H(^+)</td>
<td>10.6</td>
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### (110)-type Surface Reactions (Ferripyrophyllite)

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<td>&gt;Si-OH (silanol)</td>
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<td>&gt;Si-OH(^+_2) = &gt;Si-OH + H(^+)</td>
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<td>&gt;SiFe-OH (bridging O)</td>
<td>2</td>
<td>&gt;SiFe-OH(^{+1/2}) = &gt;SiFe-O(^{-1/2}) + H(^+)</td>
<td>0.8 (4.8)</td>
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<td>&gt;Fe-OH(_2) (aluminol)</td>
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<td>&gt;Fe-OH(_2)(^{+1/2}) = &gt;Fe-OH(^{-1/2}) + H(^+)</td>
<td>10.7</td>
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</table>

\(^*\)Entries with a second pKa value after a comma indicate two different groups with identical topology, but different calculated pKa values.

\(^#\)Entries outside the parentheses were calculated with \(m+n=2\) in eq. 3, and entries inside the parentheses were calculated with \(m+n=1\).

Table 5. Site types, number of sites per unit cell face, possible surface acid-base reactions, and intrinsic acidity constants for surface functional groups on pyrophyllite and ferripyrophyllite edge surfaces. The acidity constants are calculated using the method of Hiemstra et al. (1996)
### (010)-type Surface Reactions (Pyrophyllite)

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<td>&gt;Si-OH (silanol)</td>
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<td>&gt;Si-OH = &gt;Si-O⁻ + H⁺</td>
<td>7.6, 7.8</td>
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<tr>
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<td>&gt;Si-OH₂⁺ = &gt;Si-OH + H⁺</td>
<td>-8.5, -4.5</td>
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<tr>
<td>&gt;Al-OH₂ (aluminol)</td>
<td>2</td>
<td>&gt;Al-OH₂⁺¹/² = &gt;Al-OH⁺¹/² + H⁺</td>
<td>9.5</td>
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### (010)-type Surface Reactions (Ferripyrophyllite)

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<td>-7.7, -3.5</td>
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<tr>
<td>&gt;Fe-OH₂ (ferrinol)</td>
<td>2</td>
<td>&gt;Fe-OH₂⁺¹/² = &gt;Fe-OH⁺¹/² + H⁺</td>
<td>8.9</td>
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### (110)-type Surface Reactions (Pyrophyllite)

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<td>&gt;Si-OH₂⁺ = &gt;Si-OH + H⁺</td>
<td>-6.2, -3.3</td>
</tr>
<tr>
<td>&gt;SiAl-OH (bridging O)</td>
<td>2</td>
<td>&gt;SiAl-OH⁺¹/² = &gt;SiAl-O⁻¹/² + H⁺</td>
<td>-9.5</td>
</tr>
<tr>
<td>&gt;Al-OH₂ (aluminol)</td>
<td>2</td>
<td>&gt;Al-OH₂⁺¹/² = &gt;Al-OH⁺¹/² + H⁺</td>
<td>11.3</td>
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</tbody>
</table>

### (110)-type Surface Reactions (Ferripyrophyllite)

<table>
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<tr>
<th>Site Type</th>
<th>Sites/unit cell face</th>
<th>Reactions</th>
<th>pKₐ</th>
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</thead>
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<tr>
<td>&gt;Si-OH (silanol)</td>
<td>4</td>
<td>&gt;Si-OH = &gt;Si-O⁻ + H⁺</td>
<td>11.6</td>
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<tr>
<td></td>
<td></td>
<td>&gt;Si-OH₂⁺ = &gt;Si-OH + H⁺</td>
<td>-6.7, -3.7</td>
</tr>
<tr>
<td>&gt;SiFe-OH (bridging O)</td>
<td>2</td>
<td>&gt;SiFe-OH⁺¹/² = &gt;SiFe-O⁻¹/² + H⁺</td>
<td>-1.5</td>
</tr>
<tr>
<td>&gt;Fe-OH₂ (aluminol)</td>
<td>2</td>
<td>&gt;Fe-OH₂⁺¹/² = &gt;Fe-OH⁺¹/² + H⁺</td>
<td>12.5</td>
</tr>
</tbody>
</table>

Entries with a second pKₐ value after a comma indicate two different groups with identical topology, but different calculated pKₐ values.

### Table 6

Site types, number of sites per unit cell face, possible surface acid-base reactions, and intrinsic acidity constants for surface functional groups on pyrophyllite and ferripyrophyllite edge surfaces. The acidity constants are calculated using a method modified from that of Brown (1981). See text for discussion.
Figure Captions

**Figure 1.** Typical pseudo-hexagonal phyllosilicate morphology.

**Figure 2.** Proposed edge surface structures and protonation schemes resulting in an overall neutral charge. a) (010)-type edge structure. b) An alternate (010)-type edge structure that has not been suggested before. c) (110)-type edge structure proposed by Bleam (1993). d) (110)-type edge structure proposed by Bleam *et al.* (1993). e) (110)-type edge surface proposed by White and Zelazny (1988). Note that the protonation scheme is equivalent to that in c), but structural relaxation has resulted in an overall neutral charge for each functional group.

**Figure 3.** Ball and stick examples of the infinitely repeating chain structures used to calculate edge surface structures, in this case with Al in the octahedral sites. Equivalent models were used to calculate Fe$_2$Si$_2$O$_5$ edge structures. a) Chain running parallel to the [100] vector, generating a (010)-type edge surface. b) Chain running parallel to the [110] vector, generating a (110)-type surface.
Perrhenate Uptake by Iron and Aluminum Oxyhydroxides: An Analogue for Pertechnetate Incorporation in Hanford Waste Tank Sludges

BRADLEY WAKOFF AND KATHRYN L. NAGY
Department of Geological Sciences, University of Colorado, Boulder, Colorado 80309-0399

Perrhenate (ReO₄²⁻), a nonradioactive surrogate for pertechnetate (⁹⁹⁷⁷TcO₄⁻), was partitioned during precipitation and aging of iron and aluminum oxyhydroxide solids from aqueous simulants of high-level nuclear waste stored at Hanford, WA. Neutralization of acidic metal nitrate solutions (Al/Fe mole ratio 0.25 and 13.5:40 ppm Re) to a final pH > 13, followed by aging at 90 °C for up to 18 weeks, resulted in substantial amounts of reversibly sorbed Re (∼1–10 ppm). Irreversibly sorbed Re increased in the Fe-dominated system with aging, reaching a final value of ∼83 ppm after 168 h, in a mixture of hematite with minor goethite. Irreversibly sorbed Re in the Al-dominated system decreased with time to ∼30 ppm after 18 weeks in solids dominated by boehmite. Increasing the total amount of Re to 1000 ppm increased the extent of irreversible sorption. The presence of 100 ppm Si prevented transformation of and irreversible Re uptake by ferricydrate in Fe-dominated systems. In Al-dominated systems, 200 ppm Ni prevented hematite formation but did not affect perrhenate uptake. Results suggest that 5% of the ⁹⁹⁷⁷Tc inventory in the Hanford waste tanks may be associated with the sludges, and ∼0.5% incorporated into the solids under oxidizing conditions.

Introduction
Between 1944 and 1988, the U.S. Department of Energy's Hanford Site in southeastern Washington State produced special nuclear materials for the nuclear weapons program, and as a byproduct, large volumes of nitric acid-based liquid waste streams. The acidic waste streams initially were neutralized with NaOH to a pH above 10 for storage in low-carbon steel tanks and, over time, have been extensively reprocessed, leaving residuals of sludges, saltcake, and supernatant (1). These waste residuals are stored underground in 149 single-shell steel-lined concrete tanks and 28 newer double-shell tanks. Sixty-seven single-shell tanks definitely or possibly have leaked (2). The tank contents are treated as high-level waste (HLW) and are a complex mixture of distinct phases. Because of the large number of chemical separation processes used at Hanford and the mixing of wastes over time, the variability among tanks is great (3). Major solutes in the supernatants are Na⁺, Al(OH)₃⁺, OH⁻, NO₃⁻, and SO₄²⁻; the saltcakes are predominately NaNO₃, and the dominant solids in the sludges include aluminum and iron oxyhydroxides. U-fission products in the HLW include ¹²³Cs (t₁/₂ = 30 years), ¹³⁷Cs (t₁/₂ = 28 years), and ⁹⁵⁴Tc (t₁/₂ = 2.1 × 10⁷ years). It is generally considered that transuranic elements and their daughters are associated with the solids and ¹²³Cs and ⁹⁵⁴Tc are associated with the liquids. ⁹⁵⁴Tc is the major concern in long-term risk assessments because of its relatively long half-life and the chemical stability and solubility of the pertechnetate ion (TcO₄⁻) under aerobic conditions (3–8).

Approximately 32000 Ci of ⁹⁹⁷⁷Tc were produced in the Hanford reactor fuels and reprocessed using three different Pu-recovery processes (4). Some ⁹⁹⁷⁷Tc was co-extracted with uranium in the tributyl phosphate/kerosene-based (i.e., PUREX) separation processes (6, 7), and some was lost to the soil during intentional liquid waste discharges and in single-shell tank leaks (8). The pressurized Tc tank inventory is estimated to be 26000 Ci, distributed about equally between the single-shell and double-shell tanks.

There is considerable uncertainty about the current chemical speciation and distribution of ⁹⁹⁷⁷Tc in the tanks. Early on, ⁹⁹⁷⁷Tc remained in the liquids generated during reprocessing of tank wastes and was generally ignored until the 1960's when a few tens of kilograms were separated and recovered (8, 10). Large-scale recovery was not implemented, however, and most ⁹⁹⁷⁷Tc was left in ¹²³Cs-recovery waste streams that were comiled with other waste streams during complex dewatering processes and ultimately returned to the single-shell tanks. The reprocessing and redistribution of ⁹⁹⁷⁷Tc resulted in the occurrence of significant amounts of nonwater leachable forms of ⁹⁹⁷⁷Tc in some single-shell tanks (11). In addition, it has been shown that Tc exhibits a wide range of redox and solubility characteristics in the radiation fields and chemical mixtures that exist in some tanks (12, 13). Developing a better understanding of interactions between ⁹⁹⁷⁷Tc and tank waste solids is critical in developing strategies for tank waste retrieval and closure.

With respect to tank sludges, it is generally known that, upon neutralization of acidic solutions, Fe and Al form poorly ordered oxyhydroxides that age to more stable crystalline phases. The initial Fe precipitate is commonly two-line ferrilithite, which transforms to hematite and/or goethite. Early-formed amorphous Al phases or bayerite transforms to gibbsite and/or boehmite depending on temperature. There is a range of reported interactions of dissolved cations and anions with these oxides upon aging. For example, transition metals coprecipitated with ferrilithite or amorphous aluminum oxyhydroxides can be either incorporated into or reacted from the crystalline solids with aging (14–17). Oxanions (18–22) sorb strongly to iron oxides, can impede transformation reactions, and can be occluded in the solids.

Sorption of Tc or its chemical analogue Re (23) on oxides is minimal under oxidizing conditions (pH 7 (6–4–27)). Data on incorporation of Tc within solid oxides are less comprehensive, but indicative of conditions under which such uptake can occur. Trace amounts of Tc were incorporated into goethite and hematite upon aging of ferrilithite in 10⁻³ M Tc solutions at 60 °C for 44 h (28). Under reducing conditions and from bicarbonate solutions containing 10⁻³ M TcO₄⁻, 4% of the total inventory of Tc was taken up in hematite formed at 60 °C after 4 h, ostensibly as a Tc(IV)–bicarbonate complex (29). Tc and Re were incorporated in goethite formed by oxidizing mackinawite (FeS) that contained coprecipitated Tc(IV) or Re(IV). Tc remained as reduced domains of TcO₂.
but Re was thought to oxidize and diffuse to channels in the goethite structure (28). Both perhenate and pertechnetate were incorporated by Al-rich HLW simulants, but excluded by Fe-rich simulants, aged overnight at room temperature (27). Approximately 30% of 40 ppm added Re and 1 ppm added Tc were retained by the Al-rich sludges as determined by difference on the aqueous phase. However, long-term binding of perhenate and pertechnetate in the solids was not assessed in any of the above studies.

To understand Tc uptake in tank sludges, we investigated Re partitioning during oxyhydroxide precipitation and aging in simplified Fe–Al HLW simulants at 90°C, under oxidizing conditions. The influence of Si on Fe-dominated systems and Ni on Al-dominated systems was also investigated. Si and Ni are minor components in HLW sludges (1) and could affect aging kinetics and partitioning of Re through the formation of minor phases. Because of the importance of determining the long-term fate of 99Tc, we focused on quantifying and characterizing the extent of irreversible Re sorption in the synthetic sludge solids.

**Experimental Section**

**Sample Synthesis.** Sample synthesis mimicked HLW reprocessing procedures, and major component concentrations approximated those of reprocessing solutions (Table 1). Minor component (Si, Ni, and analogue Re) and Na concentrations approximated those of average HLW (Table 2). Minor component concentrations in sludge interstitial fluids vary greatly depending on the origin of the wastes and the presence of sludge solids that contain these components.

Two compositional systems characteristic of the range of Al/Fe mole ratios in the tanks were investigated: an Fe-dominated system (Al/Fe = 0.25) and an Al-dominated system (Al/Fe = 13.5). The Fe system was investigated with and without 100 ppm Si and the Al system with and without 200 ppm Ni. Each of these four systems was investigated with and without 40 ppm Re (equivalent to 21 ppm Tc on a per mole basis). Some experiments in the Fe system without Si or in the Al system without Ni contained 100 ppm Re (525 ppm equivalent Tc), much higher than equivalent Tc concentrations in HLW (~5–15 ppm). All chemicals were reagent grade except sources of Re (1000 ppm ammonium perchlorate solution, SPEX Certiprep) and sodium perenate salt (98% purity, Aldrich) and certain mineral acids. Si was added as sodium silicate, and all other components were added as nitrate salts.

Fe–Al–Na–NO₃ solutions with or without minor components (initial pH < 1) and open to the atmosphere were neutralized with 13 M NaOH to a final pH > 13 in 250 mL HDPE or 2 L PP bottles. The caustic suspensions were submerged and aged in a 50 ± 1°C water bath as either a series of 256 mL samples or a 1.5 or 2 L batch experiment from which 200–250 mL aliquots were drawn. Most experiments were conducted for 168 h, except for a single 18 week experiment in the Al system. Aged samples were withdrawn from the water bath and immediately centrifuged for 3–5 min at 1500 rpm. Supernatant was decanted, filtered (0.45 μm nylon), and analyzed for pH, Al, and Re where appropriate. Solids were centrifuged–washed twice with ~150 mL of deionized water, transferred to dialysis tubing (Spectrum Spectra/Por molecular porous membrane, MWCO 12–14000), and dialyzed with 1 or 2 L of deionized water daily for up to 10 days and to a final conductivity of <10 μS. Washed solids were freeze-dried. To assess the nature of Re retention, the dialysis step was omitted in some experiments.

For comparison to aged products in the Fe system experiments, pure goethite was synthesized (30) from a solution spiked with 40 ppm Re. Samples were aged (70°C, pH ≈ 13), dialyzed, and analyzed for Re. No attempt was made to assess Re uptake by other individual Fe or Al phases under the experimental aging conditions.

**Solution Analysis.** The final pH was measured at room temperature with an Orion glass combination electrode. The pH at 90°C and I = 0.1 M should be about 0.8 pH unit lower than that measured (31). Given the complex thermodynamics of multicomponent brines and the poor response of glass electrodes in concentrated Na solutions (22), however, it is not possible to infer accurately hydroxide concentrations at temperature from the measured pH.

Al was measured by UV–vis spectroscopy (33), which required dilution to the micromolar range in 0.1 M HCl. Fe was below the detection limit of the Ferrozine method (34; 7 × 10⁻⁷ M). Re was measured by ICP-AES (ABR model 3410+1) using standards prepared from the 10000 ppm standard in 1 M HCl (Fisher trace metal grade). To mitigate viscosity effects, samples were dialyzed 10 times in the same 1 M HCl.

**Solids Analysis.** Solids were identified by X-ray diffraction (XRD) on a Scintag powder diffractometer, scanning at 2θ = 1°/min using Cu Kα radiation and a graphite beam monochromator. Hematite/goethite mass ratios were quantified by comparing the integrated intensities of the hematite (110) and goethite (110) peaks (2θ = 35–36°) and 20–22°, respectively) scanned at 2θ = 0.2°/min to those of known mixtures of pure synthetic standards (35). Error in this analysis is probably minimal because the (110) and (111) peaks for goethite synthesized in the Al system were not shifted relative to peaks for pure Fe-goethite (36).

XRD data were used to estimate the rate of ferricydrate transformation, which follows first-order kinetics (37):

\[
\frac{d[\text{hem}]}{dt} = k_{\text{hem}}[\text{hl}](1-e^{-kt})
\]

where [hl] is the amount of ferricydrate present at time t, [hem] is the initial amount of ferricydrate, and k is a rate constant with units of inverse time. Equation 1 suggests that the rate of hematite (or analogously goethite) appearance is first order in ferricydrate:

\[
\frac{d[\text{hem}]}{dt} = k_{\text{hem}}[\text{hl}](1-e^{-kt})
\]

This can be integrated to give

\[
[\text{hem}] = [\text{hem}]_0 + \frac{k_{\text{hem}}[\text{hl}]}{k} (1 - e^{-kt})
\]

The proportion of a phase at time t relative to its final amount was quantified by normalizing the peak intensity of a sample to the final peak intensity for that experiment. This quantity
was multiplied by the mass fraction of the phase in the final sample to yield the mass fraction at time t. Model parameters $k_0, k_{0n}, k_F$, $k_{0m}$, and $g_L$ were regressed from the data (38). The only parameter with independent physical significance is $k_0$, because the exact stoichiometry of the ferrhydrite was unknown and the transformation kinetics involved an induction time.

Re in the solids was analyzed by ICP-MS (Varian Ultracem 700). Because digested oxide solutions were highly concentrated and difficult to analyze by ICP-MS, Re was first purified and concentrated with a modified anion exchange technique (38).

A 2 mL sample of exchange resin (Dowex Marathon A anion exchange resin, 30–40 mesh, chloride form) was added to a 10 mL PP syringe used as an exchange column. Only Fisher trace metal grade acids were used during the Re extraction procedure. Solid samples were digested in HCl (0.1 g of Fe solids in ~10 g of 6 M HCl, ~0.1 g of AI solids in ~30 g of 12 M HCl), usually in a 50 °C oven overnight. Since Fe(III) poisons the resin, 15 mL of 10% hydroxylamine hydrochloride solution (Aldrich) was added to form Fe(II). The Fe(II) solution was diluted with deionized water to a final acid concentration of 0.5 M.

The resin was washed prior to use with 10 mL of 12 M HNO₃ (initially at ~80 °C), 10 mL of 8 M HNO₃ (at room temperature), 20 mL of deionized water, 10 mL of 6 M HCl, and 20 mL of 0.5 M HCl. Samples were then loaded onto the columns. Rhenium sorbed to the resin was removed with 50 mL of 8 M HNO₃. The pale green eluate contained some Fe, likely from residual solution in the column. However, this Fe did not significantly influence the results. To concentrate Re, the solution was evaporated to either a soluble red solid or a small volume of dense, viscous liquid (~0.1 mL) which was taken up in ~4.5 mL of 0.01 M HNO₃. ICP-MS analyses were performed using standards prepared in the same matrix.

The procedure was tested by preparing a 0.6 wt % Fe solution from FeCl₃ in 6 M HCl. Aliquots of this solution were spiked with 5 and 10 ppb Re and treated as described above. Reproducibility and accuracy were within 10%.

Results and Discussion

Solid-Phase Transformations in Fe Systems. Initially two-line ferrhydrite precipitated in all experiments; however, the mineralogy of the aged solids depended on the system composition. Without Si, ferrhydrite transformed into hematite with minor goethite. In contrast, the presence of 100 ppm Si prevented ferrhydrite transformation over the 168 h of the experiments, consistent with previous work (22).

In the Si-absent system, 40 ppm Re delayed slightly the first appearances of both hematite and goethite (Figure 1), and enhanced the formation of hematite relative to that of goethite. However, ferrhydrite transformation was not substantially different with or without Re as indicated by the similar $k_0$ values. Aqueous AI remained constant in all experiments at ~90,014 m⁻².

Preferential formation of hematite from ferrhydrite at high pH has been shown to occur in the presence of Al, NO₃, and low concentrations of Si (22, 40). The slight delay in recrystallization in the presence of 40 ppm Re may be due to impedance of ferrhydrite transformation caused by Re sorption onto solid surfaces. Strongly sorbed oxianions such as arsenate and silicate both impede ferrhydrite transformation (18, 37), possibly by enhancing grain adhesion during aggregation at near-neutral pH. Perborate may have a similar, but weaker, effect. Enhanced aggregation of ferrhydrite particles also may inhibit the transformation to goethite, which is thought to occur dominantly by a dissolution/precipitation or "via solution" mechanism (42). In contrast to the transformation to hematite, which is described as a solid-state transformation or short-range dissolution/precipitation mechanism (42).

Re Uptake in Fe Systems. In the experiments with 40 ppm Re, aqueous Re remained constant at ~38 ppm in the presence and absence of Si (Figure 2a). However, the Re content of the solids varied with the extent of washing, extent of aging, and Si concentration. Two types of sorbed Re were distinguished. Re removed during dialysis is termed “irreversibly sorbed”, and that retained by the solids after dialysis is termed “irreversibly sorbed”. Re in the dialyzed Si-absent solids increased with time, reaching a final concentration of ~83 ppb. In contrast, Re in the dialyzed Si-present solids was constant at ~3 ppb, effectively the detection limit of the method (Figure 2b). Because the amounts of irreversibly sorbed Re were small, another set of Si-free experiments was performed in which total Re was increased from 40 to 1000 ppm. Increasing total Re by a factor of 25 resulted in a factor of 14 increase in Re in dialyzed solids (~1170 ppb) at 168 h (Figure 2c). However, at 4 h the Re contents of dialyzed solids in both Re-bearing Si-free systems were low (~21 ppb), suggesting that a similar irreversible uptake mechanism operated at short times that was independent of total Re.

Variation in the Re content of dialyzed Si-absent solids after 45 h (Figure 2b) is outside the 10% error of the Re analysis.

<table>
<thead>
<tr>
<th>Table 2. Experimental and Actual HLW Compositions</th>
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</thead>
<tbody>
<tr>
<td>[Na] (mol/L)</td>
</tr>
<tr>
<td>---------------</td>
</tr>
<tr>
<td>tank liquid*</td>
</tr>
<tr>
<td>Fe system</td>
</tr>
<tr>
<td>A1 system</td>
</tr>
</tbody>
</table>

*Compositions are the mean of all appropriate analyses in ref 1. Numbers in parentheses represent 1 standard deviation. *Not applicable.
and may result from mineralogical heterogeneity. After 120 h the mass fraction of hematite for all samples was fairly constant with an average standard deviation of 8%. Assuming that all Re is in hematite and comparing this error with that of the Re analysis yields a total error of only 13%, less than the 33% observed variation. In addition, samples were from two replicate experiments, in which transformation rates may not have been exactly reproduced. Transformation rates depend on the nature of the initial ferrhydrite, which contains hematite with a variety of structures resembling Fe-deficient hydroxylated hematite in pure Fe systems (45). In the absence of Al, Al-bearing ferrhydrite (44) and hydroxylated hematite also occur (45). These materials may retain variable amounts of Re at the grain scale and thus variable final Re contents of the crystalline phases. There may also have been inconsistency in the composition measured at the end of dilaysis, which did not reflect the same degree of Re removal from the solids. Residual centrifuged wash water, with a pH between 10 and 11, could have affected the leaching rate of Re from the solids through charge-dependent desorption and/or dissolution or dispersion of fine-grained particles.

Results from undialyzed experiments contained more Re than dialyzed solids as expected, but the trend with aging was opposite that observed after dialysis. After 4 h, undialyzed solids contained 2.9 ppm Re. This amount decreased to 0.8 ppm after 24 h, and more gradually to 0.6 ppm at 168 h (Figure 2c).

Samples ranged from 2.9 to 0.51 ppm, and 200 ppb is 3% of these amounts. Therefore, the trend of decreasing Re content of undialyzed solids with aging is upheld even if the solids were contaminated by residual supernatant.

**Mechanisms of Re Incorporation in Fe Solids.** Reversibility typically describes ion adsorption resulting from electrostatic attraction (outer-sphere sorption) or stereochemical similarity and electron affinity (inner-sphere sorption). Such sorption on iron oxihydroxides is pH-dependent. Reversibility, or uptake, in aging iron oxides may occur by three processes: adsorption within interlayer porosity, solid solution, and surface precipitation (14). The last two can be discarded for the experiments of (48) study. First, although the ionic radii of Fe(II) and Fe(III) are sufficiently close (0.64 and 0.53 Å, respectively), crystallographic substitution of Re for Fe is unlikely because Re(III) has over twice the positive charge of Fe(III). This implies that a solid structure would need an excessive number of vacancies to compensate for the excess positive charge. Second, Re must be reduced to the VI or lower oxidation state before precipitating (23). At pH 12, this requires a solution Eh below about −0.5 V conditions not met in these experiments. Therefore, entrapment of perhenate within interlayer porosity or crystal defects during the phase transformation is likely the primary process resulting in Re uptake in the solids.

In discussing this process, recall that initially the solutions were acidic and at room temperature. After the pH was raised to above 13, the temperature was increased to 90 °C. At the beginning of aging at 90 °C, the only phase observed by XRD was two-line ferrhydrite, indicating that it formed from Fe-dominated polymers as the pH passed through the solubility minimum for Fe phases at room temperature. The net charge on these species was positive until the point of zero charge was reached (pH = 7.5), above which the net surface charge became negative. Aggregation of ferrhydrite near neutrality was likely aided by the presence of nitrate (49) and perhaps perhenate, which can compete successfully for surface sites with nitrate (27).

The mechanism(s) of ferrhydrite formation and subsequent transformation can explain the observed Re uptake and retention. In the absence of Si and presence of 40 ppm total Re, the Re in ferrhydrite after 4 h was about 21 ppm, whereas undialyzed ferrhydrite contained 2700 ppm (corrected for estimated supernatant contamination), indicating that 99% of the Re was reversibly sorbed. Upon transformation, total Re sorbed to the solids dropped to 350 ppm (also corrected), while the amount of reversibly sorbed Re increased to 83 ppm. Therefore, reversibly sorbed Re (total sorbed minus irreversibly sorbed) decreased to 270 ppm at 168 h.

This decrease in reversibly sorbed Re can be explained by surface area effects, temperature-dependent sorption, and/or sorption strength. Hematite and goethite have lower specific surface areas than ferrhydrite (typically 20–25 m²/g for hematite and goethite, but up to 200 m²/g for ferrhydrite, 37). Assuming an equal surface density of Re on all phases, a lower surface area for the aged phases could account for the observed 90% decrease in reversibly sorbed Re. However, the rate of desorption does not correspond to the rate of recrystallization. At 24 h, 78% of the total Re had desorbed, but only 30% of the ferrhydrite had transformed. This may be related to the temperature dependence of surface complexation equilibrium constants that describe inner-sphere sorption of perhenate. Oxanions (i.e., silicate, arsenate, and molybdate) are known to sorb by inner-sphere sorption mechanisms at and slightly above the ferrhydrite ped (40). Perhenate probably behaves similarly although its sorption may be relatively weak, like that of sulfate (49). Weak sorption is supported by the observation that transformation was delayed for only a few hours in the presence of 40 ppm.
perhenate in contrast to a minimum of 168 h in the presence of 100 ppm Si. A decrease in the weak sorption as a result of increased temperature could explain the faster desorption than transformation rate upon aging.

Particle aggregation likely retained Re in the ferronhydrate at room temperature. At 90 °C, the transformation to hematite or goethite could have trapped Re in the crystalline products, the amount depending on the distribution of structures within, and composition of, the initial ferronhydrate as well as the rates of transformation and desorption. Both synthetic and natural ferronhydrtes contain nanoscale domains of hematite (43, 47, 48) which aggregate or grow to form larger hematite crystals over time (49). The occurrence of microstructural defects such as grain boundaries in the growing hematite provides sites in which incompatible components could reside, a process known as grain boundary segregation (49). It has been proposed previously that multidomain goethite crystals may also reversibly sorb oxanions such as silicate along domain boundaries (25).

Pure synthetic goethite contained 135 ppb irreversibly sorbed Re. In the presence of 40 ppm Re, the amount of goethite in the Si-free experiments approached 20% of the solids. Using the amount of Re retained in the pure goethite, approximately 25–30 ppb irreversibly sorbed Re could be in the sludge goethite, indicating that 50% or more of the irreversibly sorbed Re is in the hematite.

Solid-Phase Transformation in Al Systems. The solid evolution of the Al system followed the general trend toward more stable phases: bayerite → gibbsite → boehmite (50, 51). However, transformation kinetics varied greatly and did not correlate well with system composition (38). The mineralogy of aluminum oxyhydroxide precipitates is sensitive to solution saturation state and neutralization rate (52). The neutralization rate in the experiments was not strictly controlled (NaOH was added slowly but manually), and thick slurry formed as the pH increased through the Al solubility minimum: it was not possible to stir the slurry and keep a homogeneous base concentration. Nonetheless, bayerite disappeared after no more than ~24 h, gibbsite persisted for up to 42 days, but in some experiments disappeared after only 3 days, and boehmite first appeared after ~24 h, increasing in amount with time.

Qualitative XRD detected a small amount of hematite in the Ni-absent system, but not goethite. XRD also could not detect a Ni-Al layered double hydroxide (LDH) phase previously observed in complex synthetic sludges (S. Krumhansl, personal communication), a hypothesized sink for perhenate. Ni inhibited the formation of hematite, in amounts observable by routine XRD (~5 wt %), for up to 168 h. The inhibition of goethite formation is not surprising given the high concentrations of Al in the experimental system (39).

Re Uptake in Al Systems. In the 40 ppm Re experiments with and without Ni higher initial amounts of irreversibly sorbed Re were observed after 4 h of aging than in the Fe-dominated system (~40 ppb vs 40 ppb) (Figure 3a). However, Re decreased rapidly; after 24 h the Re content of the Al solids was only slightly above background. After 168 h in the system with Ni and 18 weeks in the system without Ni, irreversibly sorbed Re in the solids rose to about 30 ppb. This moderate increase in Re content does not correlate with the timing of hematite appearance and is probably not related to formation of an LDH phase since this phase could not have formed in the Ni-absent system. Increasing total Re to 1000 ppm in the Ni-free system increased the amount sorbed irreversibly, although again less (132 ppb) was retained after 168 h of aging (Figure 3b) compared to the amount retained in the Fe system (1179 ppb), and the amount declined with time (from 220 to 132 ppb between 4 and 168 h).

In the absence of Ni, reversibly sorbed Re in the 40 ppm experiment was as much as 10 times higher than in the Si-free Fe system, but did not follow the same decreasing trend with time (Figure 3b). Dissolved Al increased over the first few days in both Al systems (with and without Ni) containing 40 ppm Re (Figure 3c). The increase in Al signals the dissolution of metastable Al phases that formed before the temperature was raised to 90 °C. Such phases could include microcrystalline gibbsite or solids composed of various polyoxometalate cations (53, 54) that can form during the initial neutralization of acidic Al solutions at room temperature. Dissolution of metastable phases occurred faster in the absence of Ni, and caused initially trapped Re to be released to solution and excluded from recrystallizing stable solids at 90 °C. The greater amount of reversibly sorbed Re in the Al-dominant system agrees qualitatively with the results of ref 27; however, they observed no reversible uptake of Re in Fe-dominant systems, in contrast to our results showing both reversible and irreversible uptake in Fe phases. Differences in competitive sorption among minor components in the sludges of the two studies might explain this difference in reversible Re uptake in Fe-dominated systems.

Because of the variable mineralogy, it is difficult to draw firm conclusions about Re uptake in the Al-dominated systems. Re was clearly incorporated in the solids during neutralization and precipitation, but the mechanisms affecting the extent of long-term Re retention remain unclear.

Implications for the Hanford Tanks. Research investigations (12, 13) have demonstrated likely mechanisms for γ-radiation reduction of TRU in the presence of certain organic compounds known to exist in Hanford waste tanks that contain residual or degradation products of chelating agents used in isotope recovery processes. In the absence of such compounds, which consume oxidizing free radicals produced.
in the radiolysis of water, pertechnetate was found to be chemically stable. Although it is generally assumed that TcO$_2$(s) would be the most likely candidate for incorporation of Tc into tank waste solid phases, structural information about Tc-containing tank solids remains elusive. However, results of this investigation, using perhydro as a surrogate for pertechnetate, suggest a second mechanism by which Tc could have been incorporated into Hanford tank waste solids, particularly during the extensive waste solidification programs that were conducted over several decades (4).

The experimental data indicate that on average, up to about 5% of the total $^{99m}$Tc inventory may reside in sludge solids under fully oxidizing conditions. Furthermore, up to 14% of the solids-inventory $^{99m}$Tc may be irreversibly sorbed in iron and aluminum oxide phases, with a greater amount seques tered in crystalline iron oxides. The amount of irreversible sequestration in crystalline iron oxides might be less in tanks with high Si concentrations, but predicting such a relationship may be complicated by the formation of various Si-containing phases and the timing of Si addition to the waste streams. Goethite, hematite, and X-ray amorphous iron oxides (presumably ferrihydrite) have been identified in some of the ferrihydrite and goethite-rich part of tank solids (55). Acid-leaching of C-106 and AY-102 tank sludges (50) showed that between 50% and 97% of the Fe residue consisted of hematite, even though these sludges contained significant amounts of total Si (identified in solid form as cancrinite or amorphous aluminum silicates). The solid-phase sequestration mechanism for Tc indicated in this study may apply to aged precipitated solids of other compositions as well. Current strategies for separating $^{99m}$Tc from remaining tanks, such as anion exchange and diathyle cation leaching, are designed to extract weakly sorbed and aqueous $^{99m}$Tc and may not reclaim all $^{99m}$Tc from the sludge.

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